

Minimal matter supergravity and asymmetric orbifold



Yuta Hamada 하마다 유타 (KEK)

Based on the work in progress

w/ Zihni Kaan Baykara, Houri-Christina Tarazi, Cumrun Vafa (Harvard)

2023/07/03 String Phenomenology 2023

Supergravity without universal hypermultiplet

~~Minimal matter supergravity~~

and asymmetric orbifold



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We want to identify theories in the
Landscape and the Swampland.

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This seems to be understood for minimal supersymmetric $d > 6$ theories.

10d, 16 SUSY

For $d > 6$, the minimal number of SUSY is 16.

The anomaly-free gauge groups are

$SO(32)$, $E_8 \times E_8$, $E_8 \times U(1)^{248}$, $U(1)^{496}$ [e.g. Green-Schwarz-Witten].

$SO(32)$ and $E_8 \times E_8$ are in the **Landscape** (Heterotic/Type I).

while $E_8 \times U(1)^{248}$ and $U(1)^{496}$ are in the **Swampland**.

However, the anomaly can not be cancelled in a supersymmetric way

for $E_8 \times U(1)^{248}$ and $U(1)^{496}$ [Adams-DeWolfe-Taylor '10].

Also ruled out by 1-brane argument [Kim-Shiu-Vafa '19].

9d, 8d, 7d

All vacua can be understood geometrically (with frozen singularities) in terms of M/F-theory. [..., de Boer+ '01, ... , Font+ '20, Font+ '21, Fraiman+ '21, Cvetič+ '22, Parra De Freitas '22, Montero+ '22]

9d \rightarrow IIA on S^1/\mathbb{Z}_2

8d \rightarrow F-theory on elliptic K3.

7d \rightarrow M-theory on K3.

Swampland argument based on brane probe suggests this is indeed all the vacua [YH, Vafa '21, Bedroya, YH, Montero, Vafa '21] (Note: for 7d, classification of 3d SCFT is assumed)

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Let's go to $d \leq 6$ theories.

Talk Plan

1. $d = 6$ supergravity and the Swampland
2. $d = 5$ supergravity and the Swampland

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6d Supergravity

6d gravity theories with minimal supersymmetry (8 SUSY).

Multiplets are

- Gravity multiplet $(g_{\mu\nu}, \psi_\mu, B_{\mu\nu}^-)$.

- Tensor multiplet $(B_{\mu\nu}^+, \phi, \psi)$.

- Vector multiplet (A_μ, λ) .

- Hyper multiplet (ϕ, ψ) .

Moduli



Anomaly Cancellation

Anomaly cancellation conditions: Gauge group $G_1 \times \cdots \times G_k$.

The anomaly polynomial for 6d theory is 8-form.

$\text{Tr}(R^4)$ and $\text{Tr}(F^4)$ cancels w/o **Green-Schwarz-Sagnotti** mechanism.

$$H - V = 273 - 29T, \quad \leftarrow \text{Tr}(R^4)$$

$$0 = \sum_R n_R^i B_R^i - B_{\text{adj}}^i, \quad \leftarrow \text{Tr}(F^4) \quad \text{with } \text{tr}_R(F^4) = B_R \text{tr}_F(F^4) + C_R [\text{tr}_F(F^2)]^2,$$

n_R^i : #(hyper in rep. R of G_i).

There are other conditions for GSS mechanism to work.

The cancellation of perturbative anomaly implies the absence of the global anomaly [Lee, Tachikawa '20; Davighi, Lohitsiri '20].

Bottom-up

The number of consistent (at the level of EFT) 6d SUGRA is finite for $T < 9$

[Kumar, Morrison, Taylor '10].

The infinite series appear for $T \geq 9$.

The Swampland bounds using brane probe [Kim-Shiu-Vafa '19; Tarazi-Vafa '21] explains the finiteness.

We try to do explicit enumeration using ideas from **graph theory** [YH, Loges, WIP].

Talk by **Gregory Loges** on **Tuesday**.
Session1-B.



Top-down

A large class of 6d $\mathcal{N} = (1,0)$ vacua is obtained from F-theory compactified on the elliptic Calabi-Yau threefold.

Q: Given an experience at higher dimensions, is this all vacua (with possibly frozen singularities?)

F-theory vacua

The number of **neutral** hypermultiplets:

$$H^0 = h^{2,1}(X) + 1$$

Universal hypermultiplet

The number of **tensor** hypermultiplets:

$$T = h^{1,1}(B) - 1$$

The **rank** of gauge group is

$$r(T) = h^{1,1}(X) - h^{1,1}(B) - 1.$$

If these are all consistent vacua, we have the Swampland condition:

All consistent 6d SUGRA must contain **at least one neutral hyper**.

Otherwise it is in the Swampland.

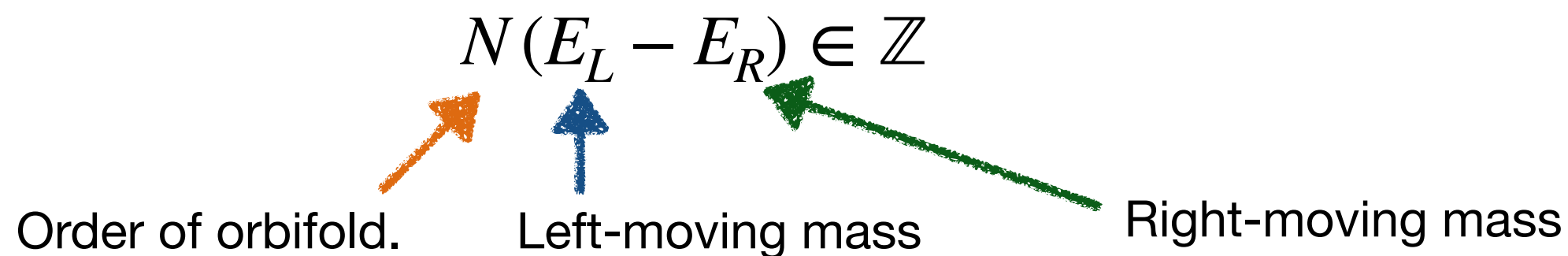
Asymmetric Orbifold

The left-mover and right-mover live in different spaces.

→ Non-geometric.

Modular invariance is key to constructing consistent models.

The level-matching condition is

$$N(E_L - E_R) \in \mathbb{Z}$$


The diagram shows the equation $N(E_L - E_R) \in \mathbb{Z}$ with three arrows pointing to its parts: an orange arrow points to N , a blue arrow points to E_L , and a green arrow points to E_R . Below the equation, the text "Order of orbifold." is aligned with the orange arrow, "Left-moving mass" is aligned with the blue arrow, and "Right-moving mass" is aligned with the green arrow.

Order of orbifold. Left-moving mass Right-moving mass


Imposing the level-matching condition for the twisted sector provides non-trivial constraints.

$E_8 \times E_8$ Heterotic on T^4/\mathbb{Z}_2

Heterotic string on T^4 . The special point in the Narain moduli space, the Lie algebra lattice is realized as a momentum lattice:


$$\Gamma^{20,4} = 2\Gamma^{8,0}(E_8) + \Gamma^{4,4}(D_4).$$

$$\Gamma^{4,4}(D_4) = \{(p_L, p_R) \mid p_L \in \Lambda_W(D_4), p_R \in \Lambda_W(D_4), p_L - p_R \in \Lambda_R(D_4)\}.$$



$$(n_1, \dots, n_4), \text{ or}$$

$$\left(n_1 + \frac{1}{2}, \dots, n_4 + \frac{1}{2}\right).$$



$$(n_1, \dots, n_4),$$

$$\sum n_i \in 2\mathbb{Z}$$

\mathbb{Z}_2 twist: $p_L \rightarrow p_L, \quad p_R \rightarrow -p_R$.

Shift vector in $E_8 \times E_8$: $V_L = \frac{1}{2}(1, 1, 0, 0, 0, 0, 0, 0; 1, 1, 0, 0, 0, 0, 0, 0)$.

Spectrum

From $E_8 \times E_8$ heterotic asymmetric orbifold on T^4/\mathbb{Z}_2 , we obtain the spectrum

$$G + T + 300V + 544H.$$

The gauge group is

$$E_7 \times SU(2) \times E_7 \times SU(2) \times SO(8).$$

All hypers are charged:

$$2(\mathbf{56}, \mathbf{2}, \mathbf{1}, \mathbf{1}, \mathbf{1}) + 2(\mathbf{1}, \mathbf{1}, \mathbf{56}, \mathbf{2}, \mathbf{1}) + (\mathbf{1}, \mathbf{2}, \mathbf{1}, \mathbf{2}, \mathbf{8}_V) + (\mathbf{1}, \mathbf{2}, \mathbf{1}, \mathbf{2}, \mathbf{8}_S) \\ + (\mathbf{1}, \mathbf{2}, \mathbf{1}, \mathbf{2}, \mathbf{8}_C).$$

No neutral hypers.

Anomaly Cancellation

The anomaly polynomial for 6d theory is 8-form.

$\text{Tr}(R^4)$ and $\text{Tr}(F^4)$ cancels w/o Green-Schwarz-Sagnotti mechanism.

$$\text{Tr}(R^4): H - V = 273 - 29T.$$

$$\text{Tr}(F^4): \sum_R n_R^i B_R^i - B_{\text{Adj}}^i = 0. \quad \text{with } \text{tr}_R(F^4) = B_R \text{tr}_F(F^4) + C_R [\text{tr}_F(F^2)]^2.$$

The heterotic asymmetric orbifold T^4/\mathbb{Z}_2 satisfies the anomaly-free conditions.

Type IIB on T^4/\mathbb{Z}_2

Take IIB on T^4 . The special point in the Narain moduli space, the Lie algebra lattice is realized:

$$\Gamma^{4,4}(D_4) = \{(p_L, p_R) \mid p_L \in \Lambda_W(D_4), p_R \in \Lambda_W(D_4), p_L - p_R \in \Lambda_R(D_4)\}.$$

\mathbb{Z}_2 twist: Left $p_L \rightarrow -p_L$, Right $(-1)^{F_R}$.

The spectrum is

$$G + 9T + 12V + 24H.$$

All vectors are $U(1)$ gauge bosons, and charges of hyper are

$$\left(\underline{\pm 1, 0, 0, 0}, 0^8\right) + \left(\pm \frac{1}{2}, \pm \frac{1}{2}, \pm \frac{1}{2}, \pm \frac{1}{2}, 0^8\right) + \left(\underline{\pm \frac{1}{2}, \mp \frac{1}{2}, \mp \frac{1}{2}, \mp \frac{1}{2}}, 0^8\right) + \left(\underline{-\frac{1}{2}, -\frac{1}{2}, \frac{1}{2}, \frac{1}{2}}, 0^8\right).$$

6d $\mathcal{N} = (1,0)$ supergravity theories
without neutral hypermultiplets
are in the **Landscape**.

Moduli space

We have seen two models without neutral hypermultiplets.
Are these models disconnected to F-theory vacua?

Not necessary. The models can be Higgsed.

Heterotic T^4/\mathbb{Z}_2 orbifold $\xrightarrow{\text{Higgsing}}$ $G + T + 244H$.

All hypers are neutral. Maybe dual to F-theory on elliptically fibered \mathbb{F}_n
($n = 0, 1, 2$).

Moduli space in IIB model

$$\text{IIB } T^4/\mathbb{Z}_2 \text{ orbifold} \xrightarrow{\text{Higgsing}} G + 9T + 8V + 20H.$$

All hypers are neutral. The same can be obtained by F-theory on

$$\frac{T^2 \times T^2 \times T^2}{\mathbb{Z}_2 \times \mathbb{Z}'_2}$$

\mathbb{Z}_2 : $(-1, -1, 1)$ twist. Half shift on the third torus.

\mathbb{Z}'_2 : $(1, -1, -1)$ twist. No shift.

This suggests the following picture:

In the context of F-theory compactification when the base volume becomes stringy size, all hypers (including **volume modulus of base**) are charged.

Talk Plan

1. $d = 6$ supergravity and the Swampland
2. $d = 5$ supergravity and the Swampland

S^1 compactification

S^1 compactifications of 6d models.

6d

gravity multiplet

tensor multiplet

vector multiplet

hypermultiplet

S^1
→

S^1
→

S^1
→

S^1
→

5d

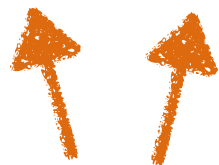
gravity multiplet + vector multiplet

vector multiplet

vector multiplet

hypermultiplet

5d SUSY multiplets are
gravity, vector, hyper.



contains scalar field.

5d hyper-free models

Let us compactify 6d models w/o neutral hypermultiplets.

S^1
 \rightarrow 5d theory without neutral hypers.

5d vector multiplet has a real scalar ϕ .

The VEV $\langle \phi \rangle$ is mass of charged hypers.

By turning on $\langle \phi \rangle \neq 0$, all hypers become massive. We obtain 5d theory without hypers [Gkountoumis+ '23].

This is again **non-geometric**. M-theory on CY_3 has at least one universal hyper.


Open question


- As pointed out in [Gkountoumis+ '23], all no-hyper models have even rank.

Is this a Swampland condition, or just a lamppost of orbifold construction here?

Anomaly may **not** be helpful to explain evenness.

If there is **one hyper**, then both rank and even rank theories appear.

[Candelas+ '16] provides CY_3 with $h^{1,1} = 13, h^{2,1} = 0$  $H = 1, V = 12$.

and with $h^{1,1} = 2, h^{2,1} = 0$  $H = 1, V = 3$.

- The maximal rank is 22. Similar to the rank bound in 16Q model, $(\text{rank}) \leq 26 - d$

[Kim-Tarazi-Vafa '19].

Any argument for maximal rank?

Summary&Future direction

- We investigate $d \leq 6$ non-geometric compactifications.
- Non-geometric compactifications provide models without universal hypermultiplets.
- These models seem to follow some patterns. Can we explain it using the Swampland principles?