

The Cosmological Constant is probably zero

Tony Padilla

Based on work with Francisco Pedro and Yang Liu [2303.17723](#) [hep-th]



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Take Home Message

In the Bousso-Polchinski set up, we can select the current vacuum on probabilistic grounds, provided we make some assumptions on the underlying parameters.
Anthropics is not required.

This idea extends to a wide class of 4D EFTs containing families of four-form fields and dual scalars



The Cosmological Constant Problem

In standard QFT, vacuum energy density scales like M_{UV}^4

In GR, vacuum energy gravitates like a cosmological constant

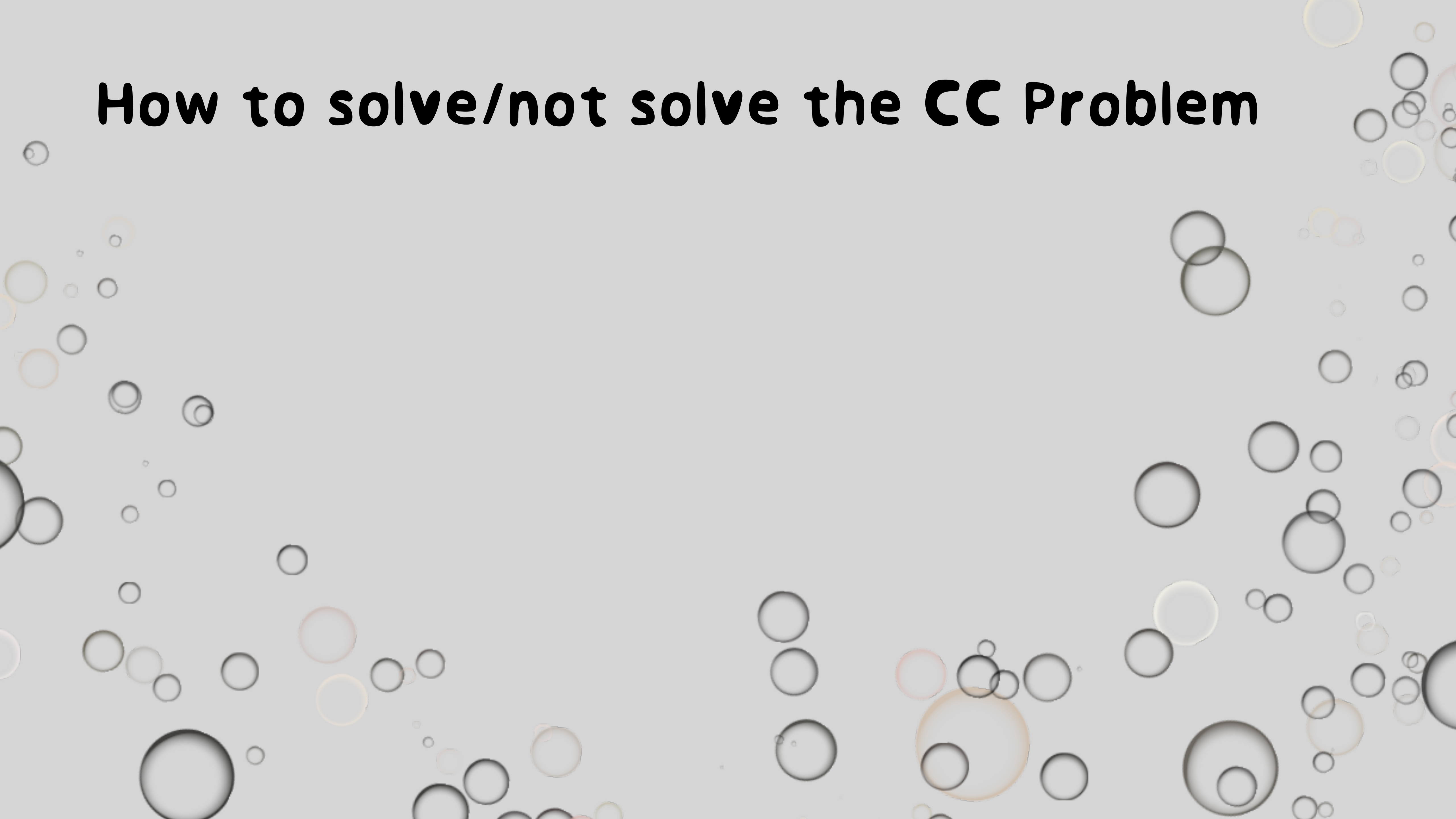
Observed cosmological constant is many orders of magnitude less than the natural value

$$\Lambda_{\text{obs}} \sim M_{pl}^2 H_0^2 \sim (\text{meV})^4 \ll M_{UV}^4$$

the universe would not even reach to the moon!



How to solve/not solve the CC Problem



How to solve/not solve the CC Problem

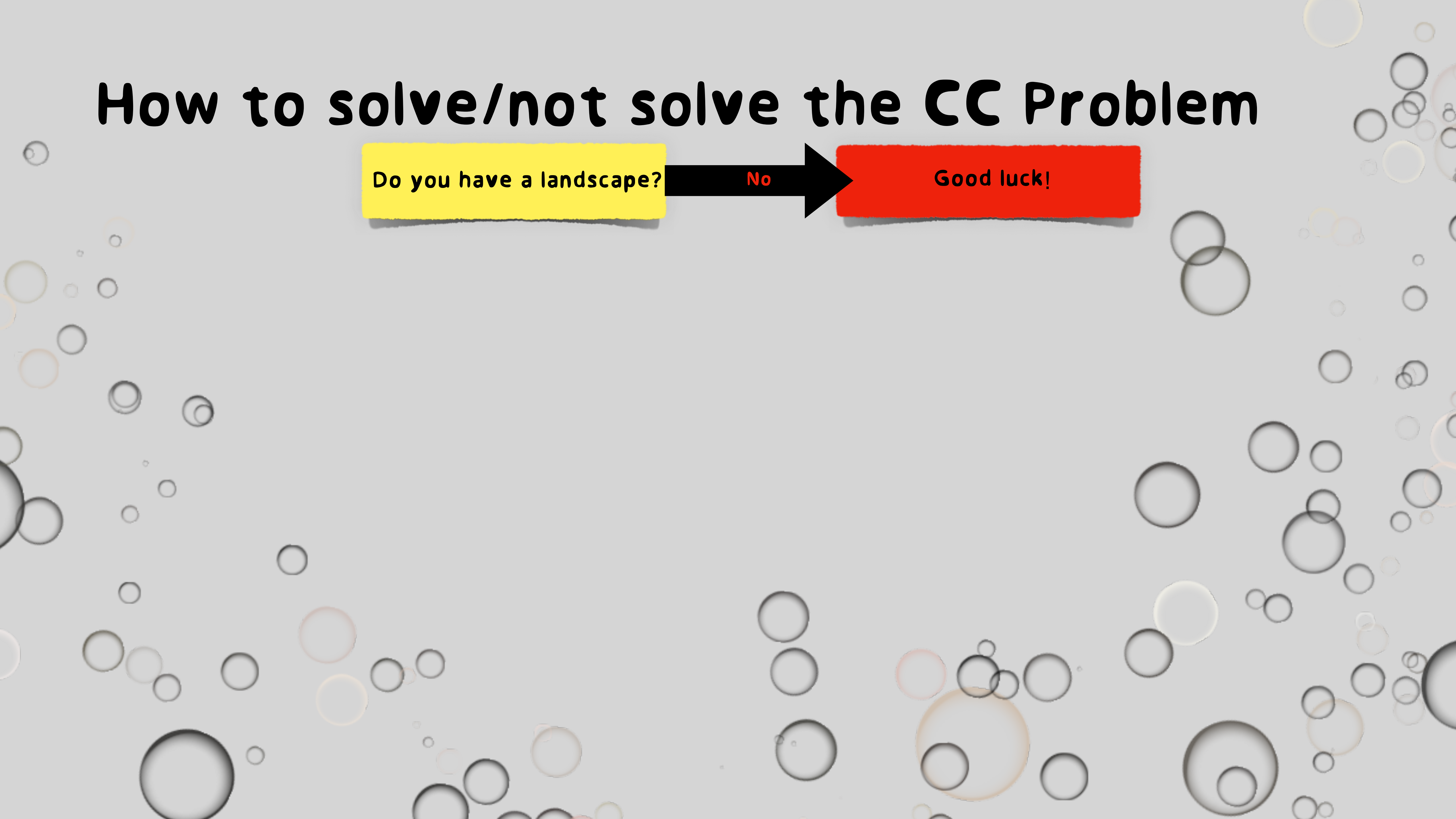
Do you have a landscape?

How to solve/not solve the CC Problem

Do you have a landscape?

No

Good luck!



How to solve/not solve the CC Problem

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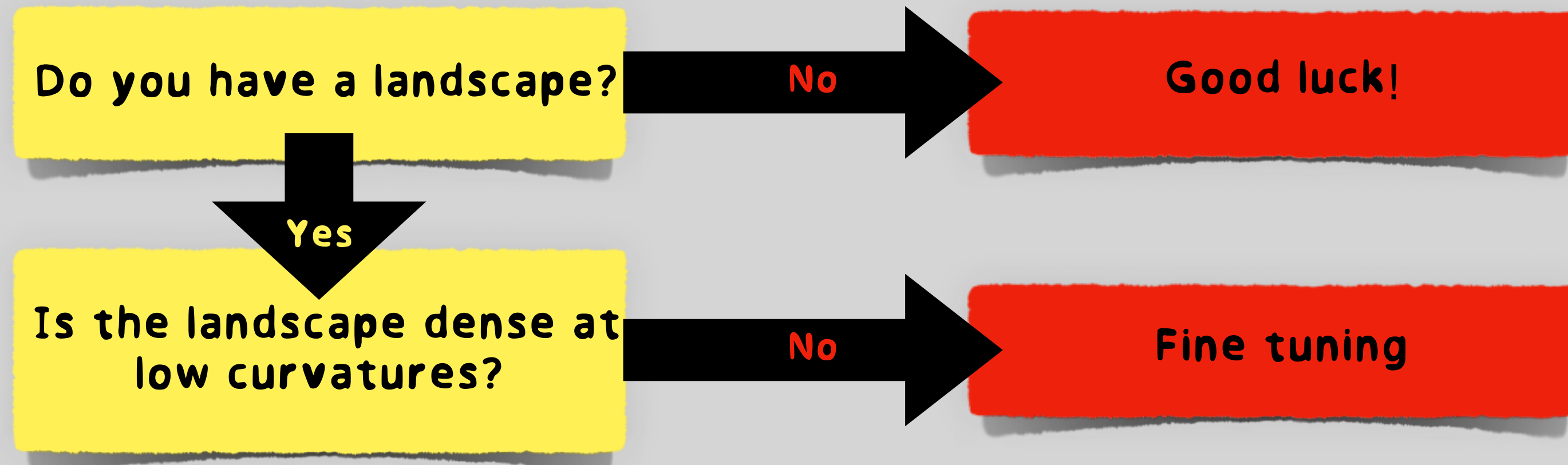
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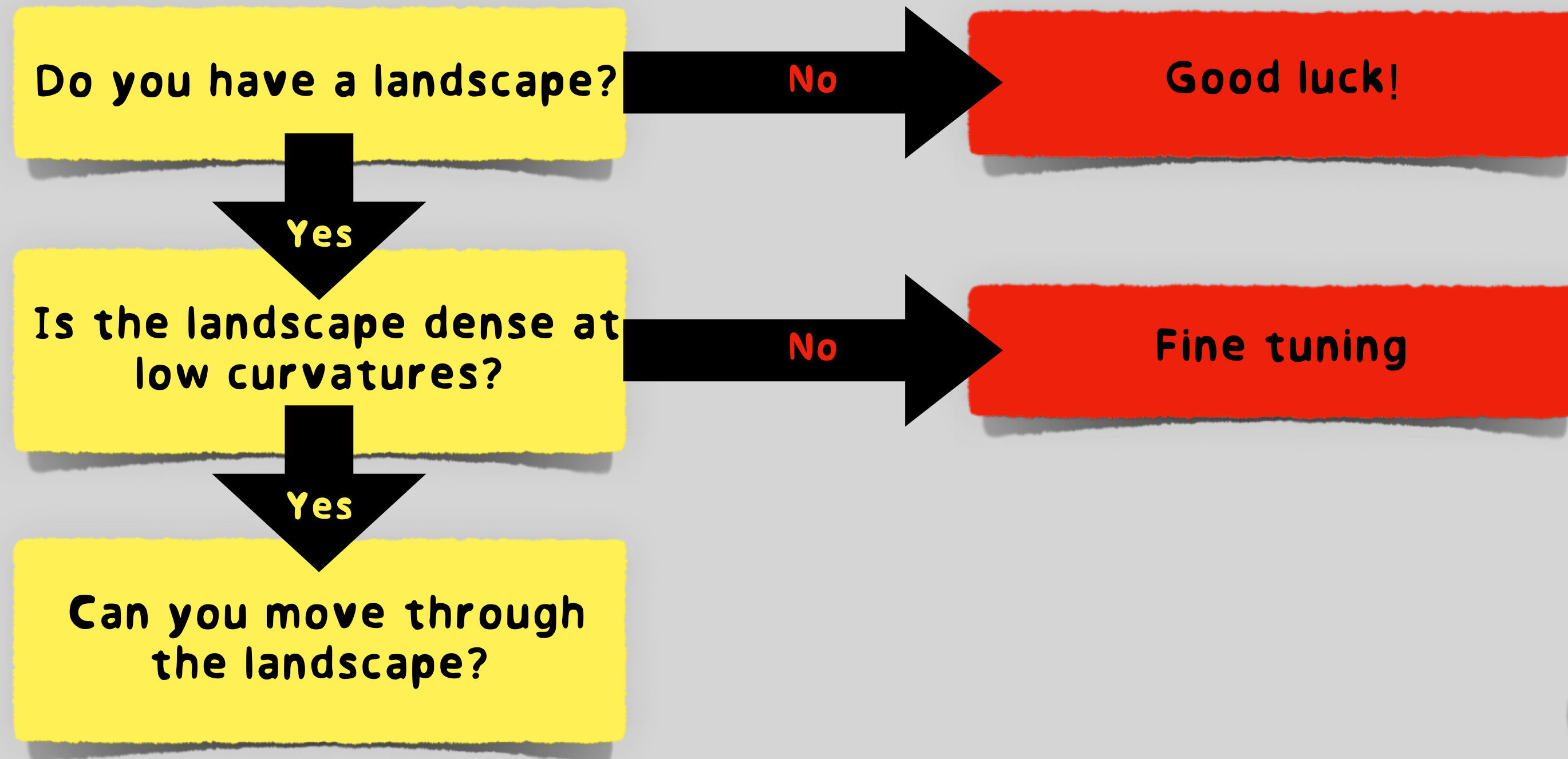
Yes

Is the landscape dense at low curvatures?

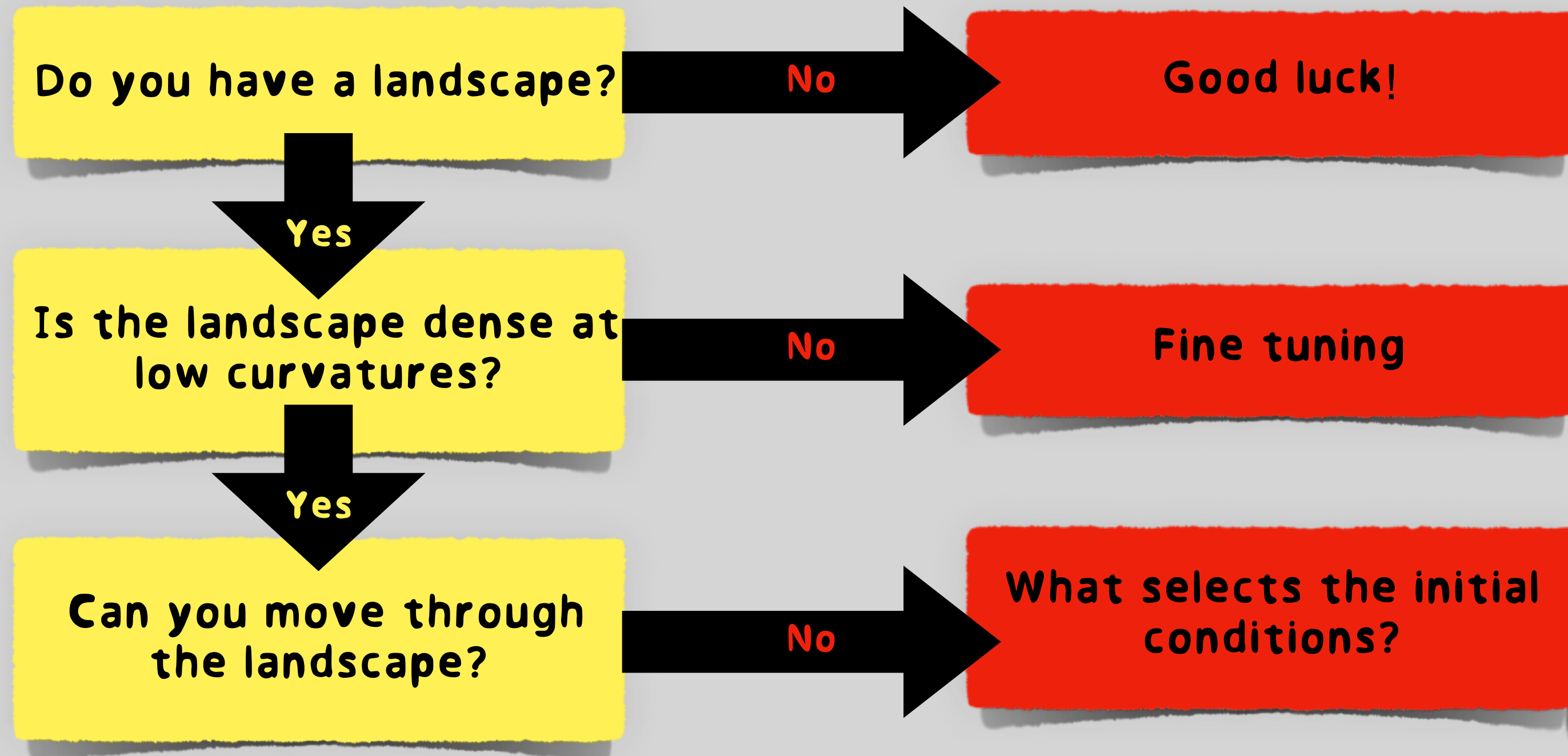
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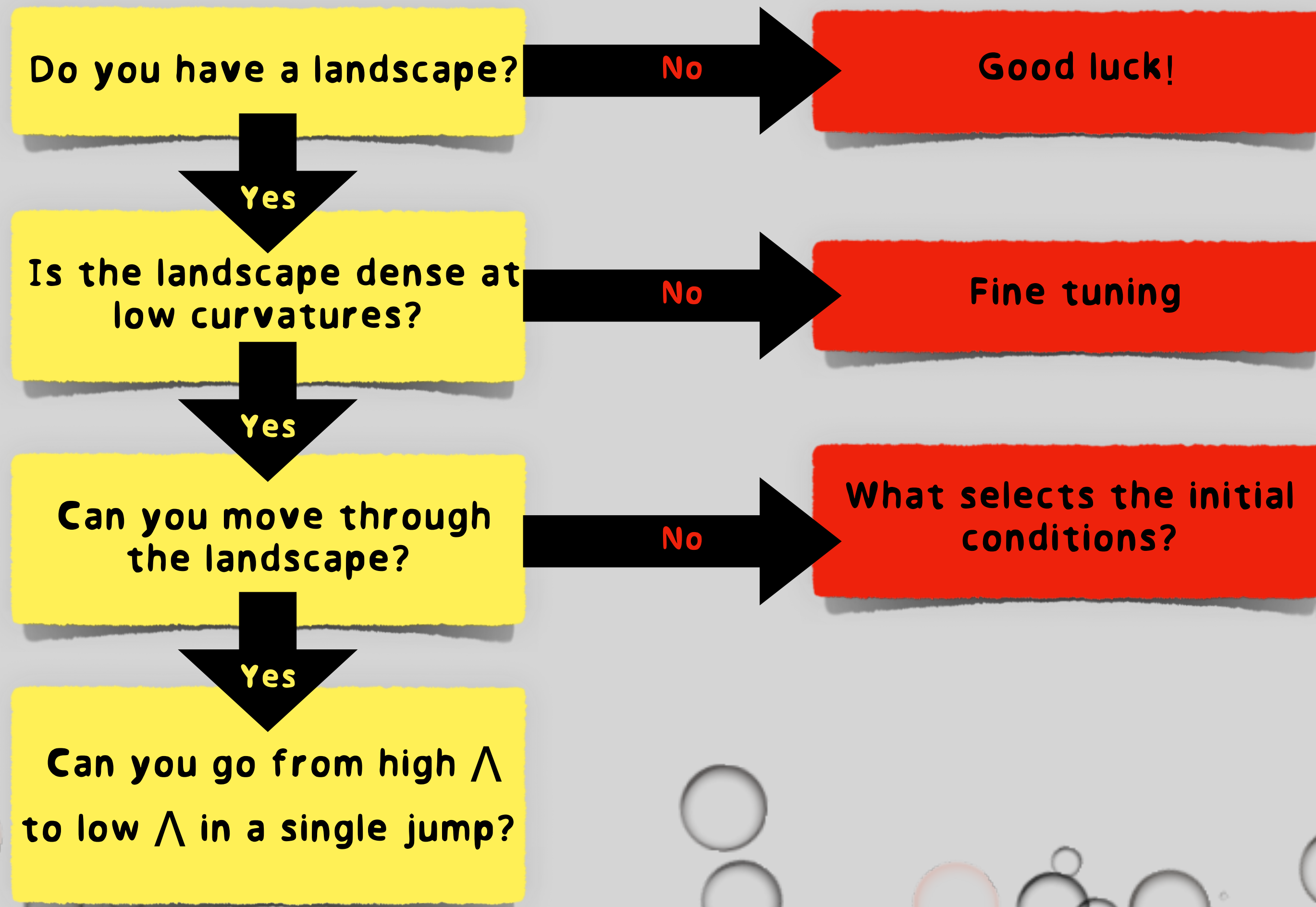
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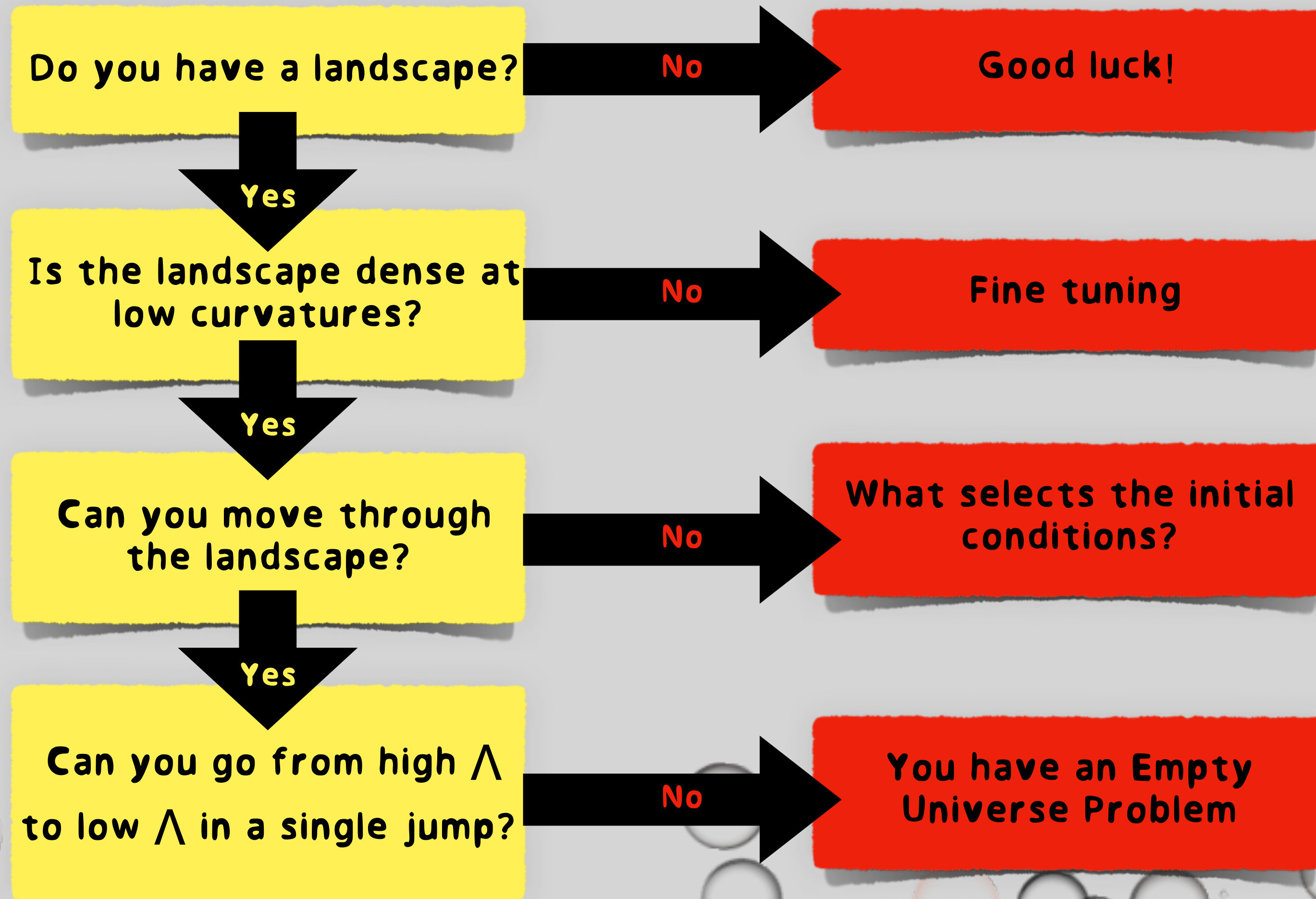
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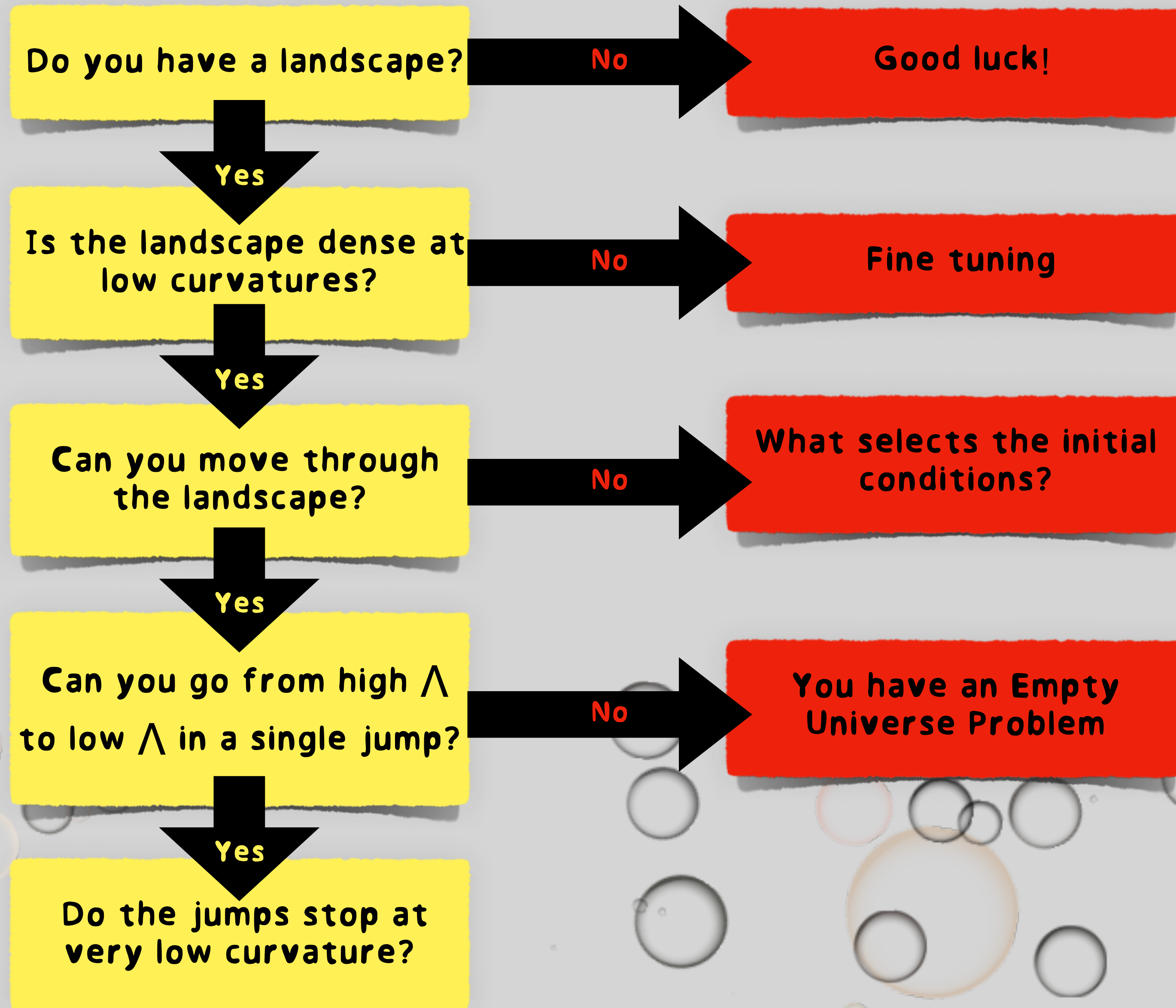
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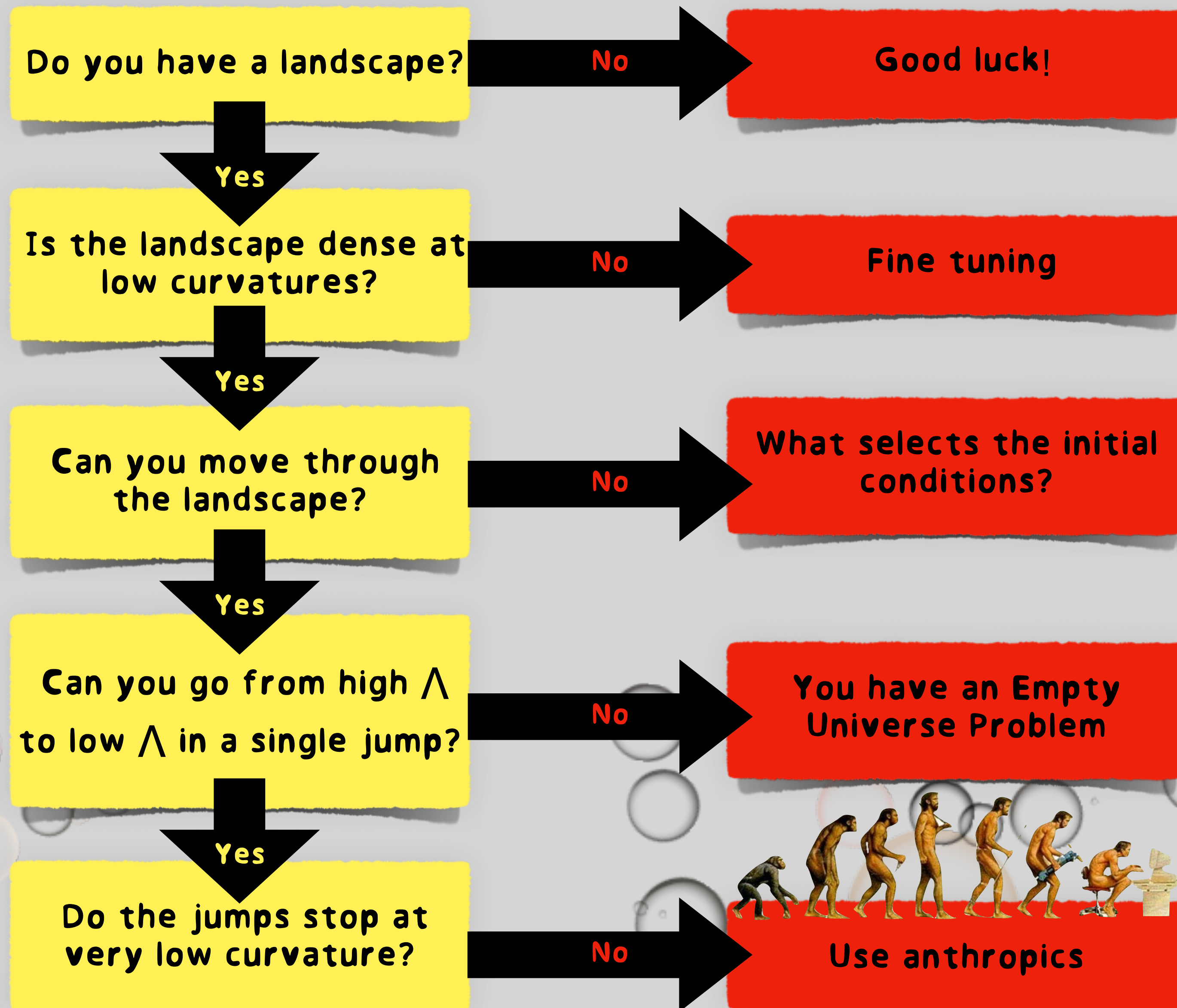
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What if the answer to this

Do the jumps stop at
very low curvature?

is yes?

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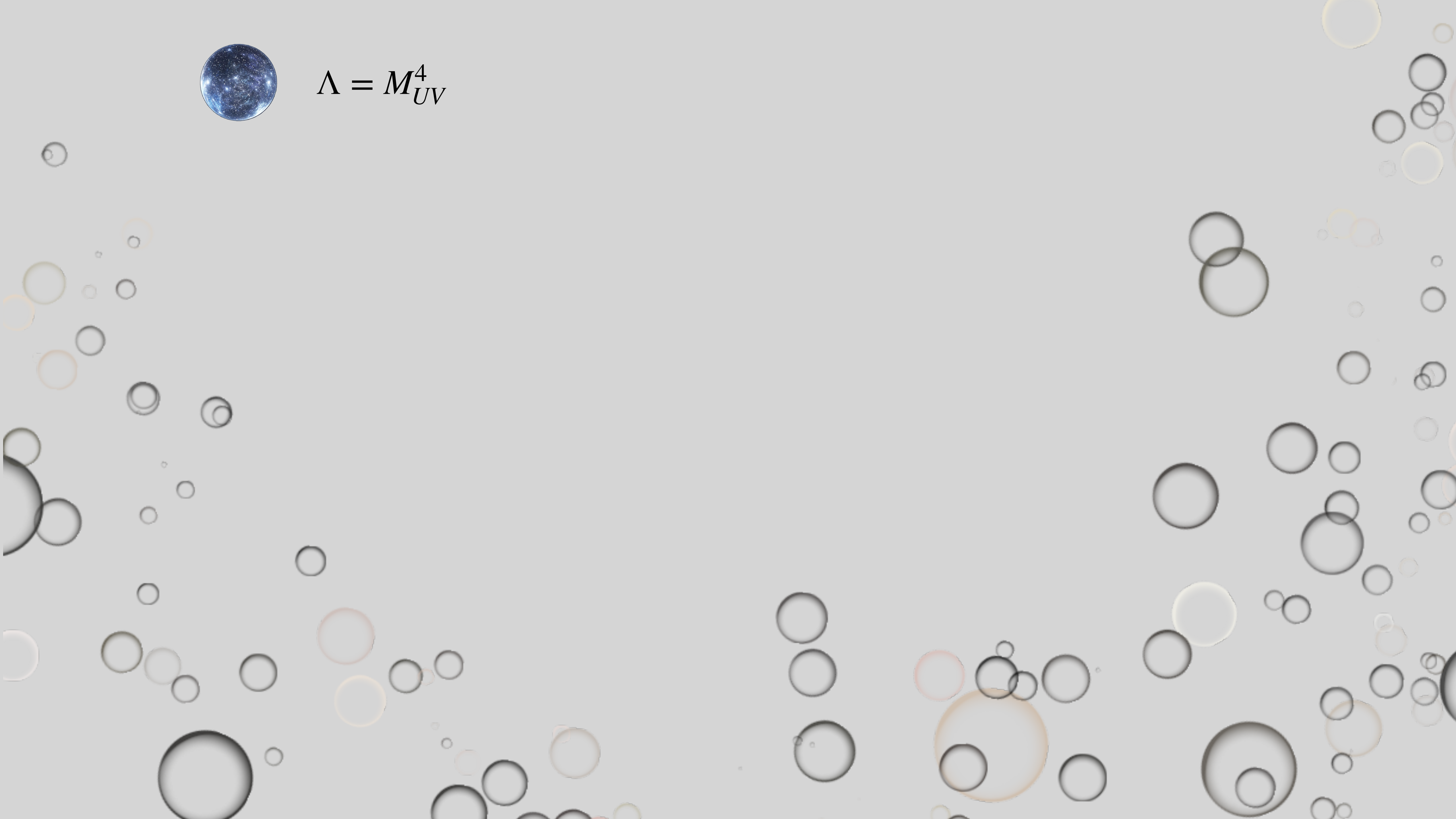
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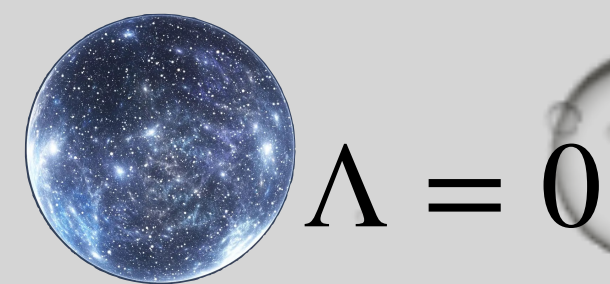


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The Bousso-Polchinski set up

$$S = \int_{\text{bulk}} d^4x \sqrt{|g|} \frac{M_{pl}^2}{2} R + \sum_i \int_{\text{bulk}} -\frac{1}{2} F_i \wedge \star F_i - q_i \int_{\text{membrane}} A_i - \tau_i \int_{\text{membrane}} d^3\xi \sqrt{|\gamma|}$$

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membrane
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Four forms are quantised in units of membrane charge

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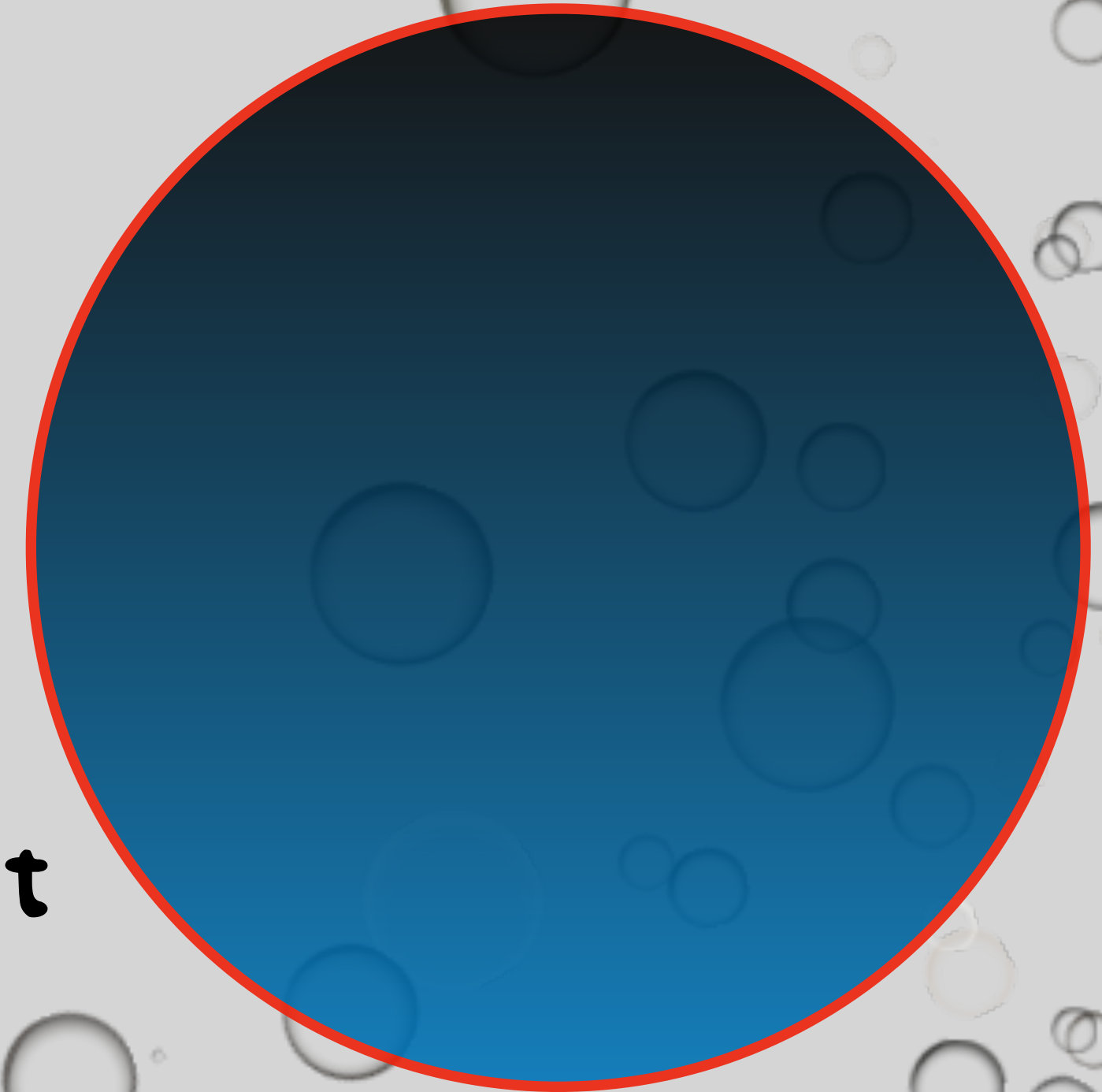
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The Bousso-Polchinski set up

Do you have a landscape?

Yes

Is the landscape dense at low curvatures?

Yes

Can you move through the landscape?

Yes

Can you go from high Λ to low Λ in a single jump?

Yes

Do the jumps stop at very low curvature?

Four-forms $F_{\mu\nu\alpha\beta} = 4\partial_{[\mu}A_{\nu\alpha\beta]}$

Bousso & Polchinski use $O(100)$ four-forms

Membrane nucleation

Near Planckian membrane charge

Let's compute the membrane nucleation rate....

The Bousso-Polchinski set up

Membrane nucleation rate $\Gamma \propto e^{-B}$ where the bounce B has a potential pole as the parent vacuum approaches Minkowski

Specifically, as parent approaches Minkowski

$$B \sim \frac{6M_{pl}^4 \Omega_3}{\Lambda_{\text{parent}}} (1 - S) + \frac{8M_{pl}^6 \Omega_3}{T^2 X (X - 1)^2} [(X - 1)^2 (1 - S) + 2S]$$

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$$S = \text{sgn}(X - 1)$$

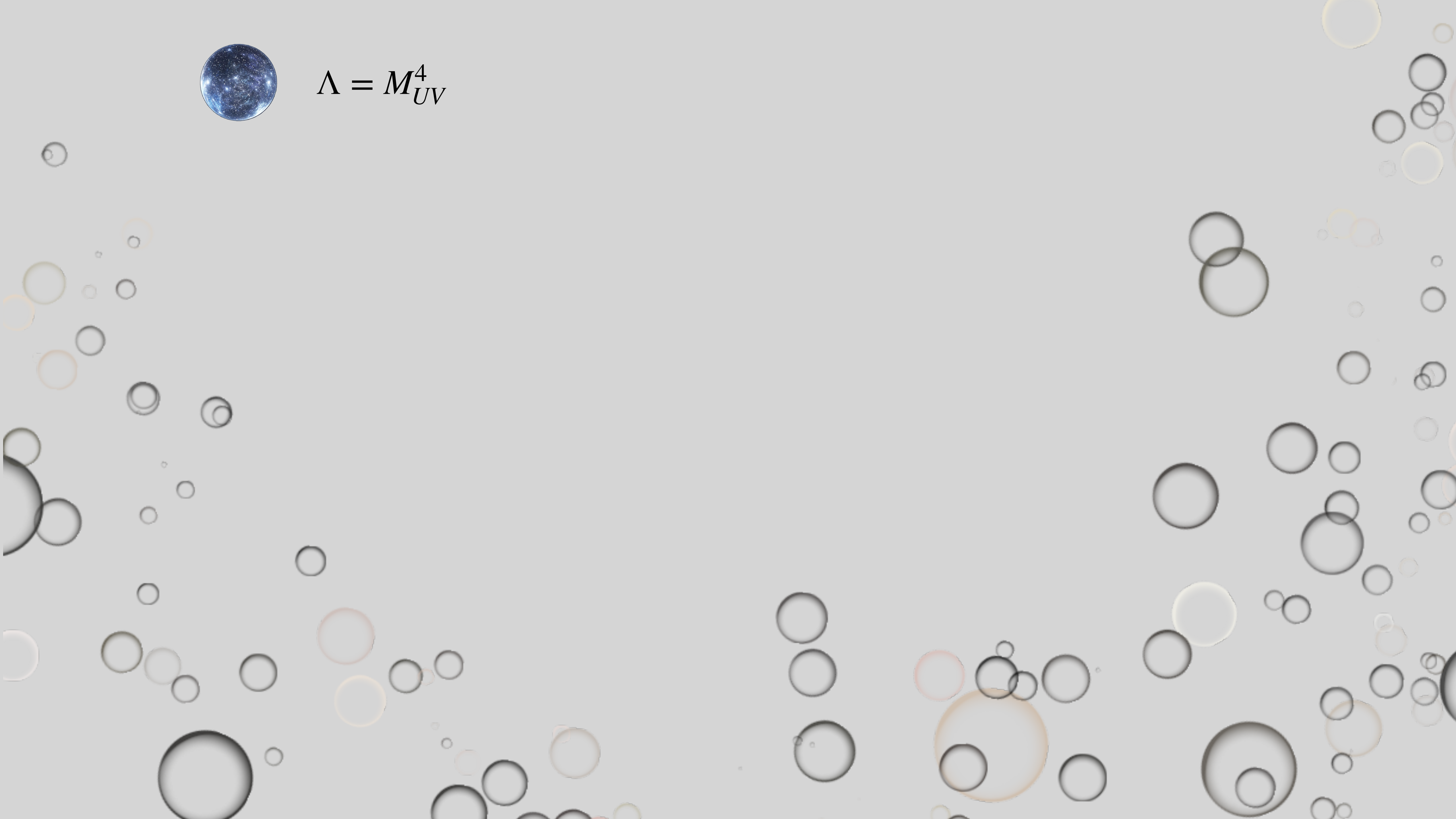
The Bousso-Polchinski set up

Specifically, as parent approaches Minkowski,

$$B \sim \frac{12M_{pl}^4 \Omega_3}{\Lambda_{\text{parent}}} \quad \text{if } X \lesssim \frac{2M_{pl}^2 q}{3T^2} \sqrt{8|V_{\text{QFT}}|} < 1$$



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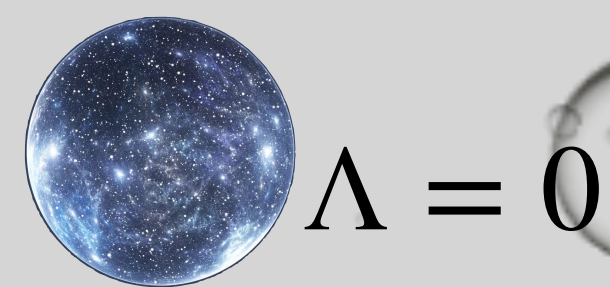


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There is a pole in the bounce as parent vacuum approaches Minkowski

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In the Bousso-Polchinski set up, we can select the current vacuum on probabilistic grounds, provided we make some assumptions on the underlying parameters.
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