

Massive Spin-2 particles and the swampland

Joan Quirant



Ben-Gurion University
of the Negev



Based on 2307.xxxx with S. Kundu and E. Palti

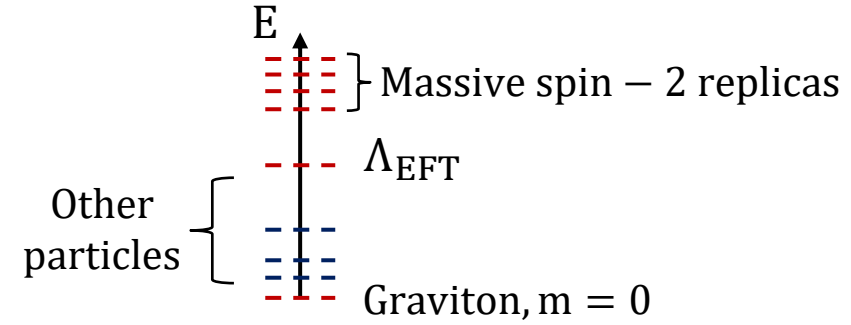
String Phenomenology 2023

Motivation

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- Massive spin-2 particles appear in (string) compactifications

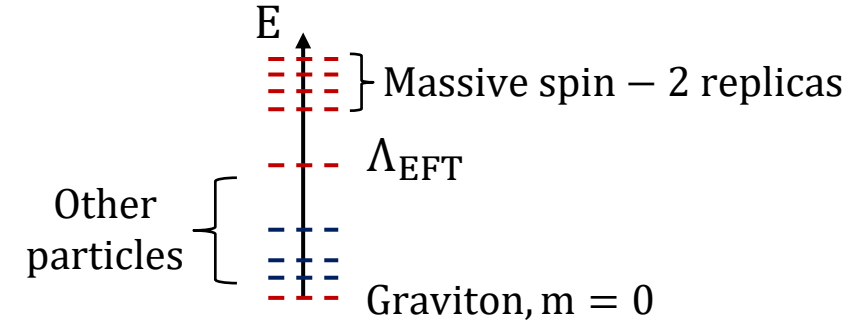
- KK copies of the graviton
- Ignore their effects at low energies
- Top-down approach



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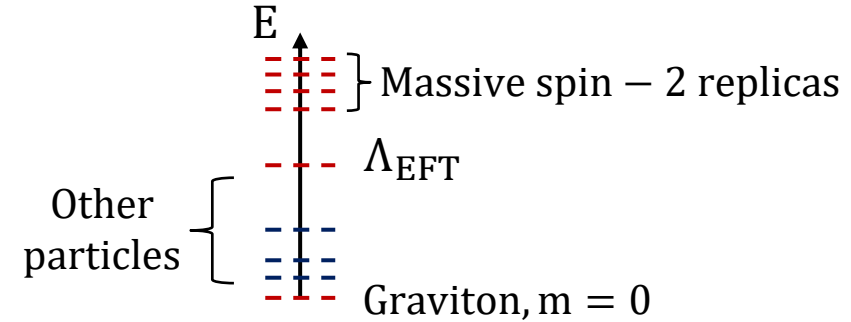


- But... from a bottom-up perspective

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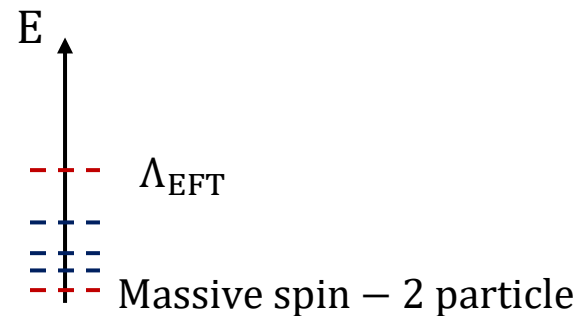
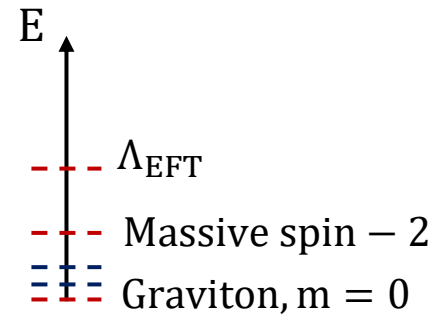
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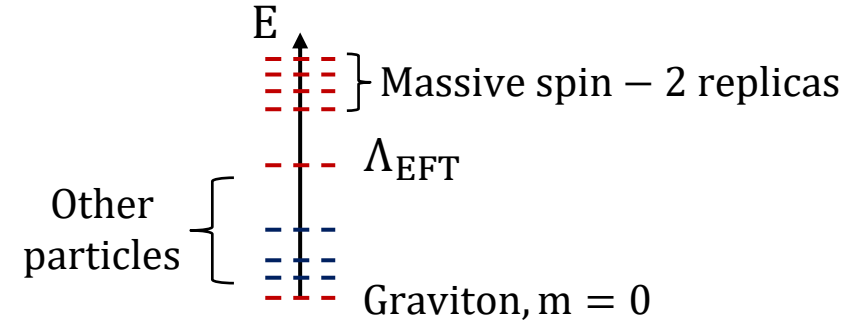
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- Single massive spin-2 particle



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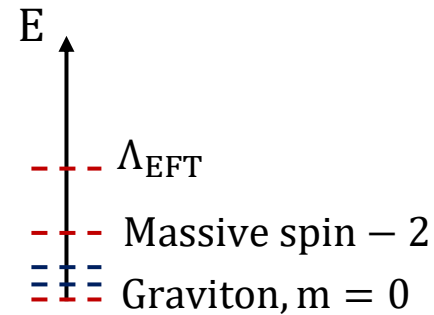
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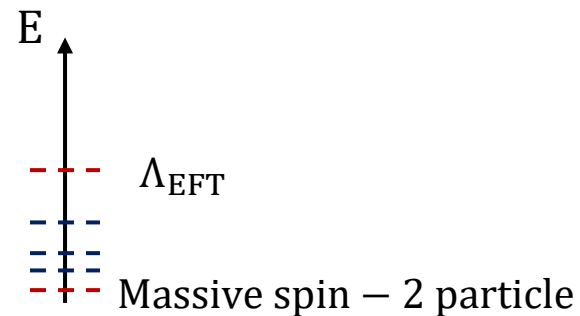


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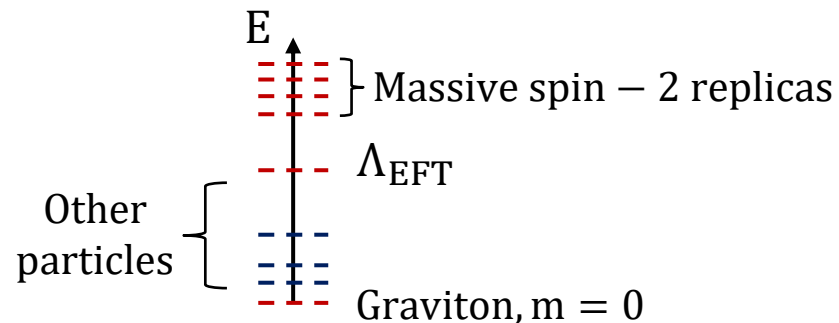
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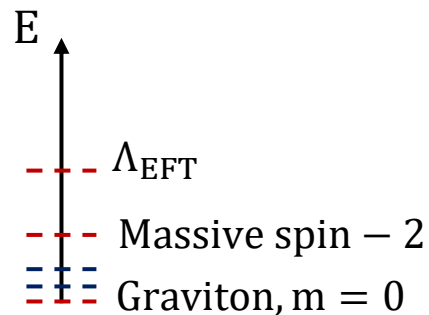
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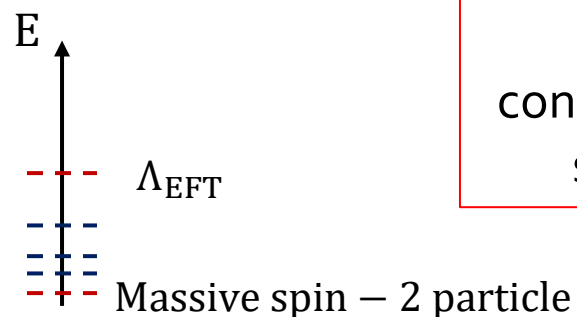


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(Swampland) constraints for massive spin-2 particles?



Contents

0) Motivation



We will only consider
 $d = 4$ in this talk

1) The Classical Regge Growth Conjecture (CRG)

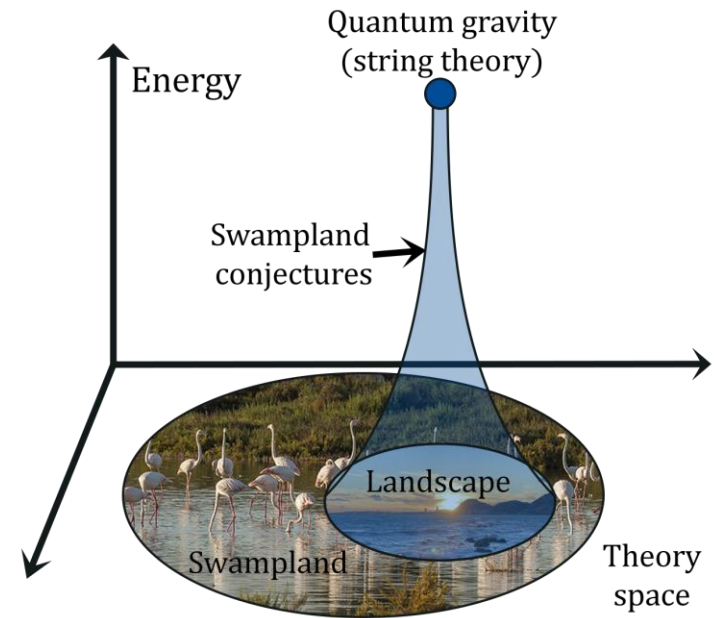
2) Vertices (three-point amplitudes and contact terms)

3) Results

4) Conclusions and outlook

Classical Regge Growth Conjecture

- We are all familiar with the **swampland program**
 - Properties **EFT** must satisfy to be **compatible** with **quantum gravity**.



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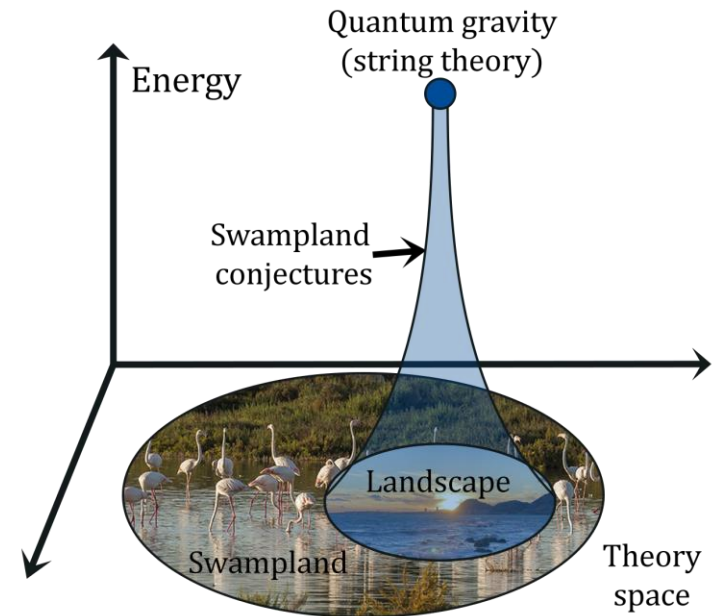
➤ Properties **EFT** must satisfy to be **compatible** with **quantum gravity**.

- **Spin-2 conjecture** Klaewer, Lüst, Palti '18

➤ **WGC** to the **helicity-1** mode of the massive spin-2 ($w_{\mu\nu}$) with mass m :

$$w_{\mu\nu} \text{ and } g_{\mu\nu}: \Lambda_{\text{EFT}} \sim \frac{mM_p}{M_w}$$

$$\text{Only } w_{\mu\nu}: \Lambda_{\text{EFT}} \sim m$$



Classical Regge Growth Conjecture

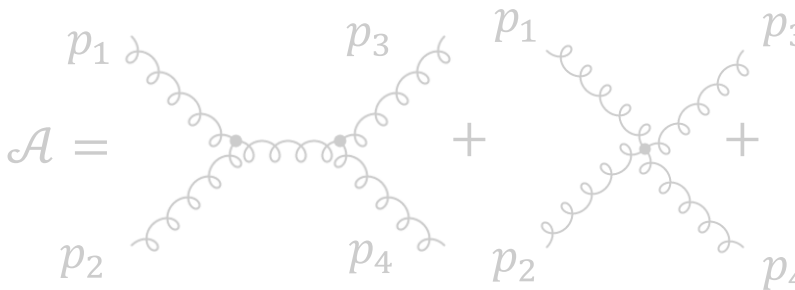
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- Formulated in Chowdhury, Gadde, Gopakka, Halder, Janagal, Minwalla '19
- Technically not a swampland conjecture but same spirit. It states

The S-matrix of a consistent **classical** theory cannot grow faster than s^2 at fixed (and physical) t

- **Classical**: non analyticities can only be simple poles. **Tree-level** scattering

Any $2 \rightarrow 2$:



exchange of other particles \rightarrow

$$\lim_{s \rightarrow \infty} \frac{\mathcal{A}}{s^3} \rightarrow 0$$
$$\begin{aligned} s &= -(p_1 + p_2)^2 > 0, \\ t &= -(p_1 - p_3)^2 > 0, \\ u &= -(p_1 - p_4)^2 < 0, \\ s + t + u &= 4m^2 \end{aligned}$$

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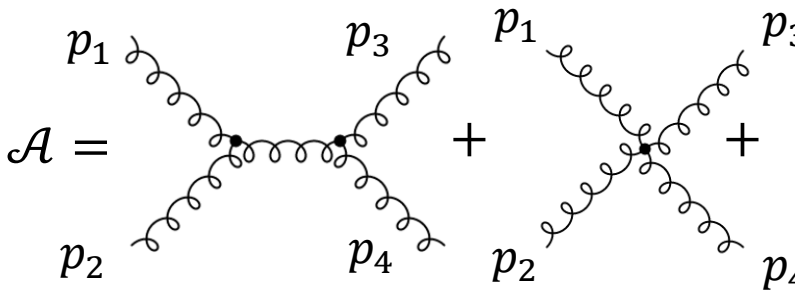
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Camanho, Edelstein, Maldacena, Zhiboedov '14
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 - ❖ Take AdS/CFT \rightarrow Theory on the bulk having a CFT dual \rightarrow Flat limit \rightarrow If $S \sim s^n$, $n > 2 \rightarrow$ The CFT violates the **chaos bound** proposed in Maldacena, Shenker, Stanford '15 .
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- Apply the **CRG** to theories containing a massive spin-2 particle $w_{\mu\nu}$ 😊
 - Construct a theory where the scattering of $2 \rightarrow 2$ (identical) **massive spin-2** particle goes like $\mathcal{A} \sim s^n$, $n \leq 2$?
 - Include all possibilities: **exchange** of a **massive** and **massless spin-2** particle, a **spin-1** particle and a **scalar** particle

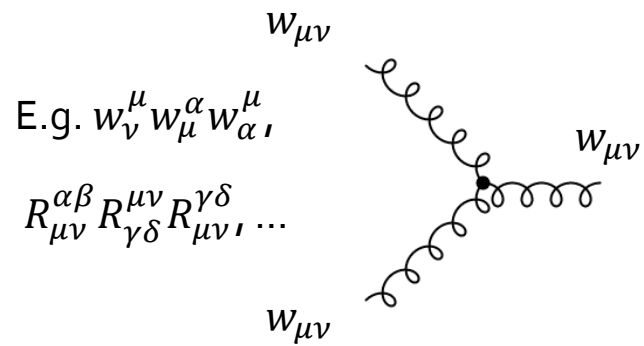
Amplitudes

- **Model** (lagrangian) **independent** approach: construct directly the tree-level amplitudes. How?

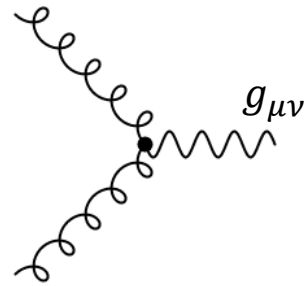
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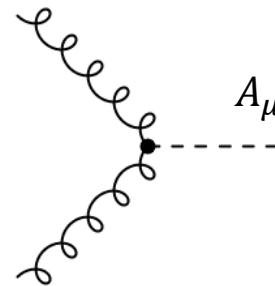
1. Find all possible on-shell **cubic vertices**. Following Costa, Penedones, Poland, Rychkov '11



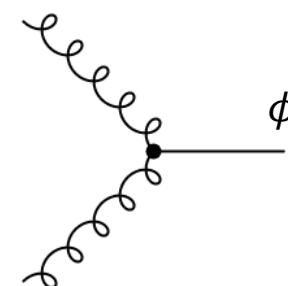
Massless spin-2



Massive spin-1



Scalar

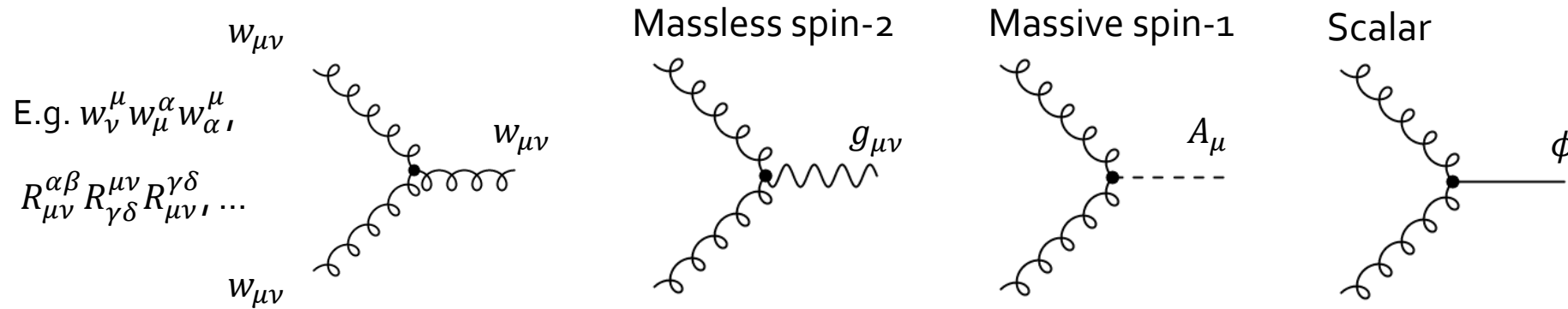


Already appeared in the literature, e.g., Bonifacio, Hinterbichler '18

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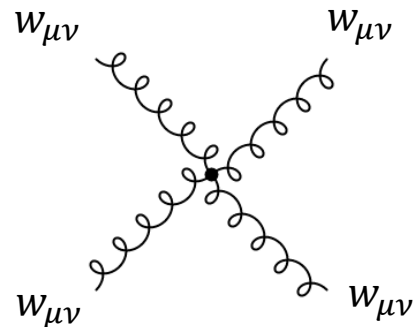
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2. Find all possible Lorentz-invariant **quartic vertices** (finite number of derivatives). Using Bonifacio, Hinterbichler, Rose '19



E.g. $w_\nu^\mu w_\mu^\alpha w_\alpha^\beta w_\beta^\nu, \partial^\lambda w_\nu^\mu \partial_\lambda w_\mu^\alpha w_\alpha^\beta w_\beta^\nu, \dots$

Amplitudes

3. Compute the Amplitude $A_{\text{total}}(s, t) = A_{\text{interchange}} + A_{\text{contact}}$ for all polarisations.

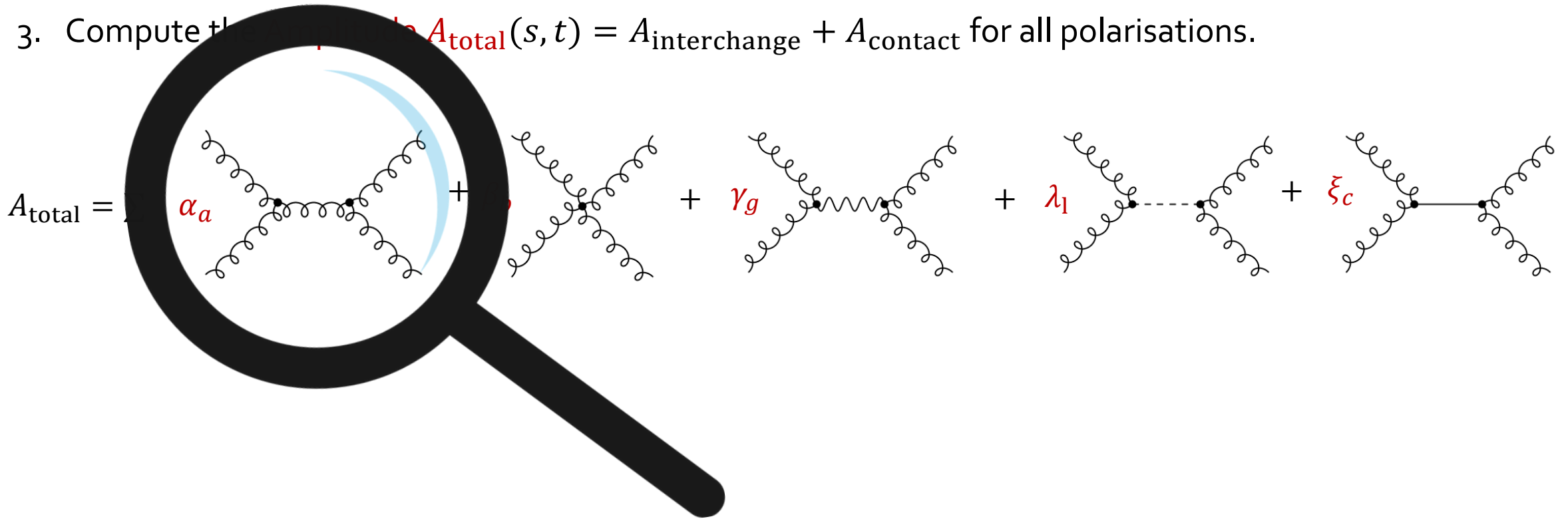
$$A_{\text{total}} = \sum \alpha_a \text{ (diagram 1)} + \beta_b \text{ (diagram 2)} + \gamma_g \text{ (diagram 3)} + \lambda_l \text{ (diagram 4)} + \xi_c \text{ (diagram 5)}$$

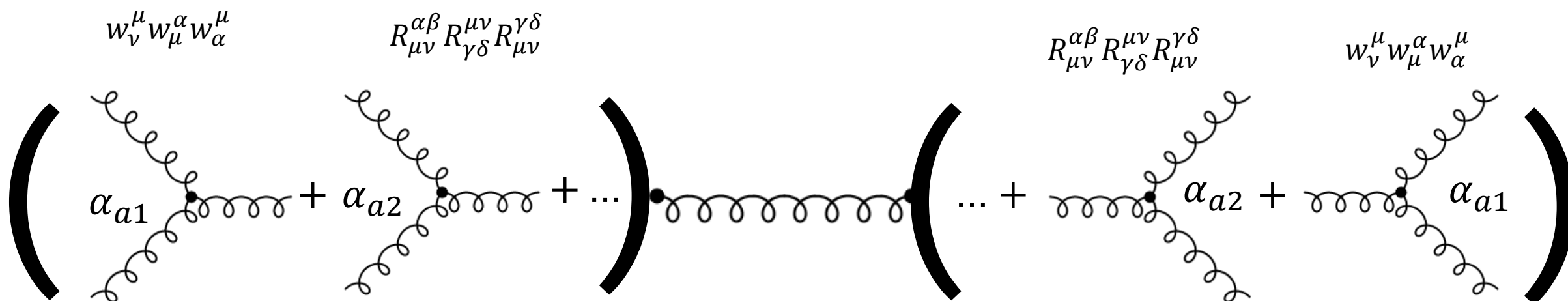
The equation shows the total amplitude A_{total} as a sum of five terms, each represented by a Feynman diagram and a coefficient:

- α_a : s-channel exchange of a wavy line.
- β_b : t-channel exchange of a wavy line.
- γ_g : u-channel exchange of a wavy line.
- λ_l : contact interaction via a dashed line.
- ξ_c : contact interaction via a solid line.

Amplitudes

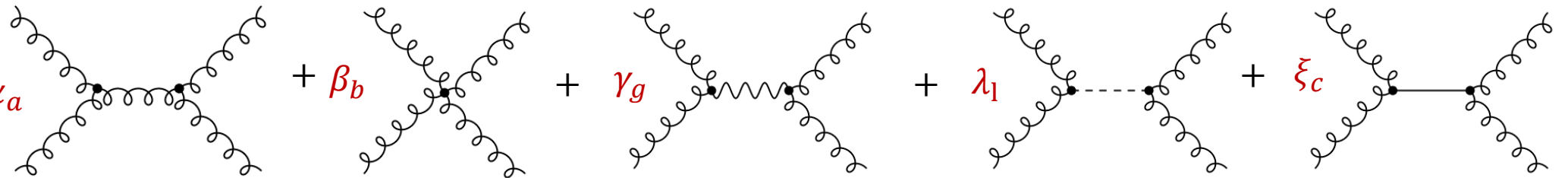
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4. Take $\{s \rightarrow \infty, t \text{ fixed}\}$ and expand $A_{\text{total}}(s, t) = A_0 s^0 + A_1 s^1 + A_2 s^2 + A_3 s^3 + A_4 s^4 + \dots$

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5. Impose $A_i = 0, i \geq 3$. Solution for $\{\alpha, \beta, \gamma, \lambda, \xi\} \neq 0$?

Vertices

Only parity even interactions

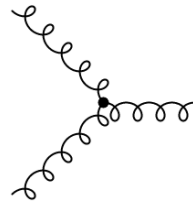


- Briefly...

- Massive-2 – massive 2 – massive 2 vertices:

1 renormalizable operator ($w_\nu^\mu w_\alpha^\nu w_\mu^\alpha$)

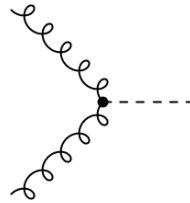
4 non-renormalizable operators



- Massive-2 – massive 2 – massive 1 vertices:

1 renormalizable operator

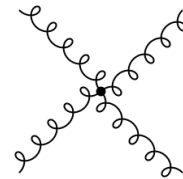
1 non-renormalizable operators



- Contact terms

1 renormalizable operator ($w_\nu^\mu w_\alpha^\nu w_\beta^\alpha w_\mu^\beta$)

Many non-renormalizable operators (consider any finite number of derivatives)

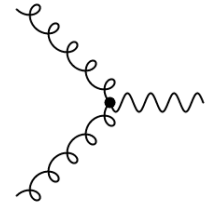


Only a small number contributes at a given s^n

- Massive-2 – massive 2 – graviton vertices:

3 renormalizable operator (e.g. $w^{\mu\nu} w^{\alpha\beta} R_{\mu\alpha\nu\beta}$)

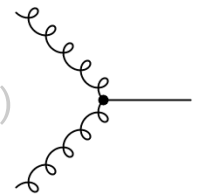
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- Massive-2 – massive 2 - scalar:

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2 non-renormalizable operators



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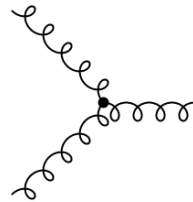


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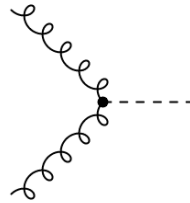
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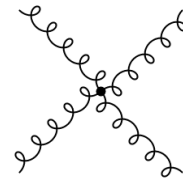
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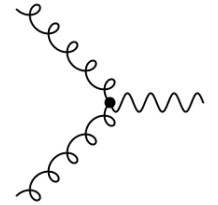
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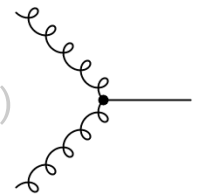
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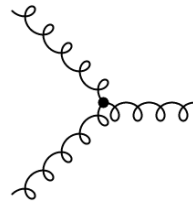


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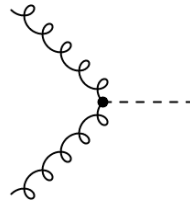
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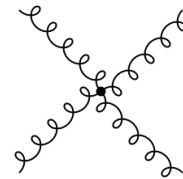
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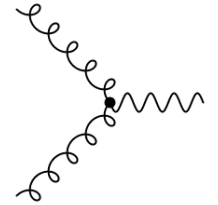


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3 renormalizable operator (e.g. $w^{\mu\nu} w^{\alpha\beta} R_{\mu\alpha\nu\beta}$)

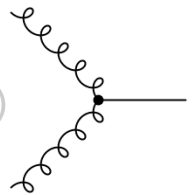
3 non-renormalizable operators



- Massive-2 – massive 2 - scalar:

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2 non-renormalizable operators



Vertices

Only parity even interactions

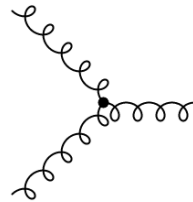


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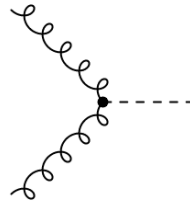
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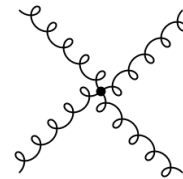
1 renormalizable operator

1 non-renormalizable operators



- Contact terms

1 renormalizable operator ($w_\nu^\mu w_\alpha^\nu w_\beta^\alpha w_\mu^\beta$)



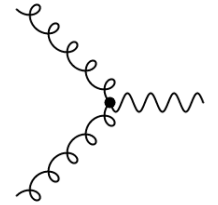
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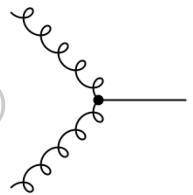
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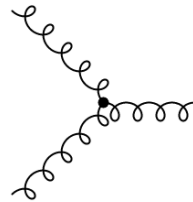


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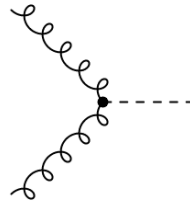
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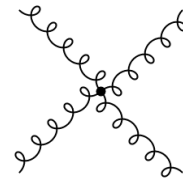
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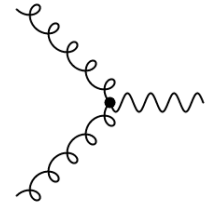
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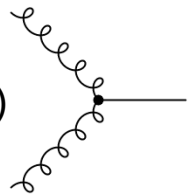
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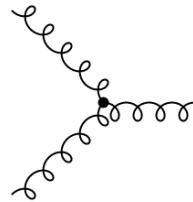


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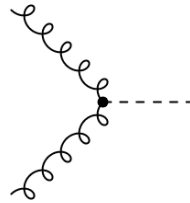
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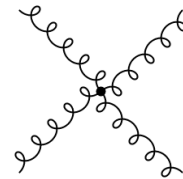
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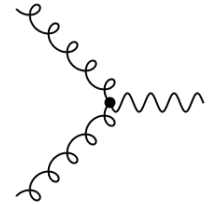
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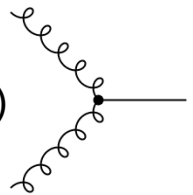
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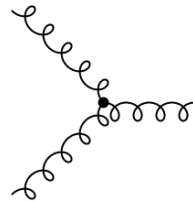


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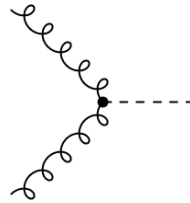
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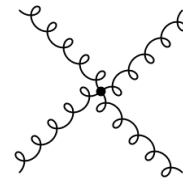
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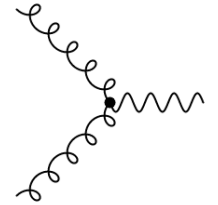


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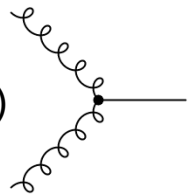
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 6 renormalizable operators
10+ many non-renormalizable operators

How to deal with the *many*? Algorithm developed in Bonifacio, Hinterbichle '18; Bonifacio, Hinterbichle Rose' 19

Results

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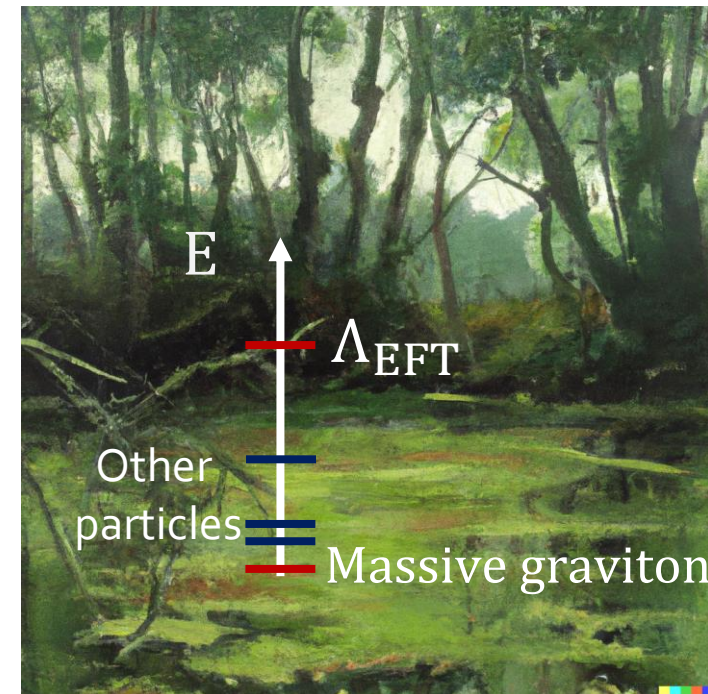
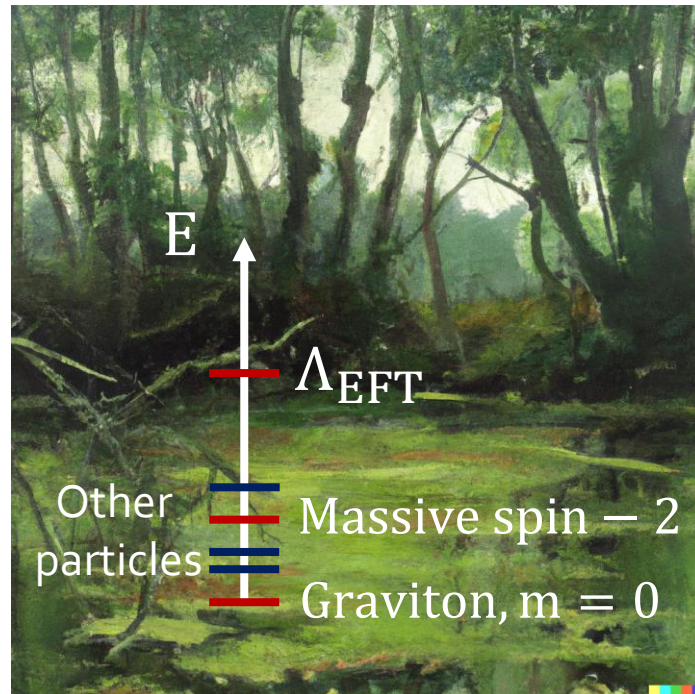
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Conclusions and outlook

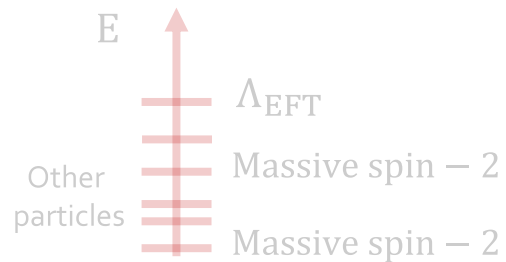
Take home



- **CRG** conjecture ($A \sim s^n, n \leq 2$): **EFT** containing a **single massive spin-2** and no higher spin particles would be in the **swampland**.

➤ Only considered parity even interactions, $d = 4$. Include parity odd terms? $d \neq 4$?

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➤ Related work: Bonifacio, Hinterbichler '20. Dimensional reducing GR on a closed internal manifold + unitarity. Mass of the spin-2 KK replicas: $\frac{m_{k+1}}{m_k} \leq 4$

- **Prove** the **CRG** conjecture. Have a **more direct evidence** in support of it. Apply it to **other contexts**.

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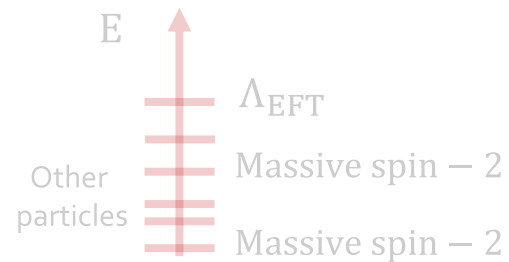
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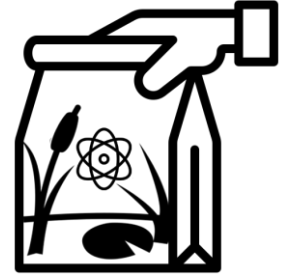
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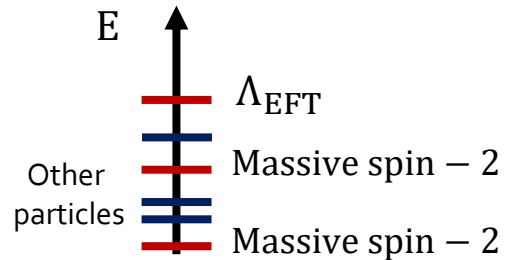
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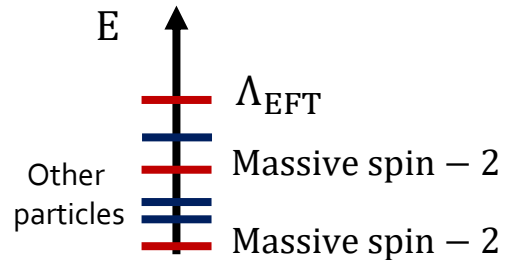
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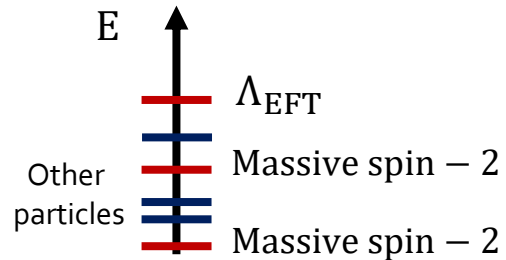
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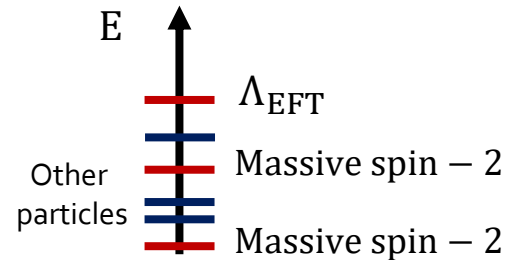
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Thank you for your attention! 😊

Renormalizable operators

- In principle, it seems natural to consider only renormalizable vertices. Example:

Normalisable: $\alpha \cdot w_\nu^\mu w_\alpha^\nu w_\beta^\alpha w_\mu^\beta \rightarrow \alpha s^m t^n$

Non-renormalisable: $\frac{\beta}{\Lambda^2} \cdot \partial^\xi w_\nu^\mu \partial_\xi w_\alpha^\nu w_\beta^\alpha w_\mu^\beta \rightarrow \frac{\beta}{\Lambda^2} s^m t^n$

Naturalness: $\alpha \gg \frac{\beta}{\Lambda^2}$ they cannot compensate

- We are being more general and assuming that it could happen $\alpha \sim \frac{\beta}{\Lambda^2}$