# Hairy Black Holes by Spontaneous Symmetry Breaking<sup>1 2</sup>

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#### "String Phenomenology 2023"

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<sup>&</sup>lt;sup>1</sup>2205.00907, Phys.Rev.D 106 (2022) 8, 084024 <sup>2</sup>2305.19814

#### Test general relativity

#### **Detection of gravitational waves**

- The direct detection of gravitational waves from the merger of binary black holes was a major breakthrough in physics in recent decades.
- One of the important missions of LIGO or gravitational waves is to test general relativity
- general relativity alone struggles to explain the presence of dark matter, dark energy, and inflationary expansion.
- To improve general relativity, many alternative theories of gravity have been proposed.

Let us consider EsGB theory

$$S = \int d^4x \sqrt{-g} \left[ \frac{R}{2\kappa^2} - \frac{1}{2} \nabla_\alpha \varphi \nabla^\alpha \varphi + f(\varphi) \mathcal{G} \right], \tag{1}$$

$$\mathcal{G} = R_{\mu\nu\rho\sigma}R^{\mu\nu\rho\sigma} - 4R_{\mu\nu}R^{\mu\nu} + R^2 \tag{2}$$

<sup>&</sup>lt;sup>3</sup>G. Antoniou, A. Bakopoulos, and P. Kanti, Phys. Rev. Lett., vol. 120, no. 13, p. 131102, 2018.

<sup>&</sup>lt;sup>4</sup>B.-H. Lee, W. Lee, and D. Ro, Phys. Rev. D, vol. 99, no. 2, p. 024002, 2019.

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- evasion of no-hair theorem<sup>3 4 5</sup>

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- ullet yields  $2^{nd}$  order differential equation (topological in 4-d): Hondenski theory
- evasion of no-hair theorem<sup>3 4 5</sup>

If  $f(\varphi_{\infty})=0$  or  $\varphi_1=0$ , the no-hair theorem is evaded

when 
$$f(\varphi) > 0$$

If  $f(\varphi_\infty) \neq 0$  and  $\varphi_1 \neq 0$ , the no-hair theorem fails. Solutions might exist

when 
$$f(\varphi) > 0$$
 and  $f(\varphi) < 0$ 

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#### Hairy Black Holes for in EsGB

Our metric ansatz

$$ds^2 = -A(r)dt^2 + \frac{1}{B(r)}dr^2 + r^2d\Omega_2,$$

Boundary conditions

Near horizon : 
$$A(r) \sim A_h \epsilon$$
,  $B(r) \sim B_h \epsilon$ ,  $\varphi(r) \sim \varphi_h + \varphi_{h,1} \epsilon$   
Near infinity :  $A(r) \sim 1$ ,  $B(r) \sim 1$ ,  $\varphi(r) \sim \varphi_{\infty}$ 

where

$$\varphi'(r_h) = \varphi_{h,1} = -\frac{r_h}{4\dot{f}_h} \left( 1 \mp \sqrt{1 - \frac{96}{r_h^4} \dot{f}_h^2} \right), \qquad B_h = \frac{2}{r_h} \left( 1 \pm \sqrt{1 - \frac{96}{r_h^4} \dot{f}_h^2} \right)^{-1}$$

• To avoid  $\varphi''(r_h)$  being divergent the inside of the root should not be zero, namely

$$\dot{f}_h^2 < \frac{r_h^4}{96}$$
.



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#### Hairy Black Holes for $f = \alpha e^{\gamma \varphi}$ in EsGB

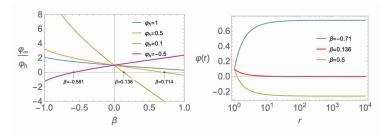


FIG. 2. For  $f = \alpha e^{\gamma \varphi}$  (left)  $\varphi_{\infty}/\varphi_h$  vs  $\beta$  and (right)  $\varphi(r)$  for different values of  $\beta$  fixing  $\varphi_h = 0.1$ 

# Hairy Black Holes for $f = \alpha \varphi^2$ in EsGB

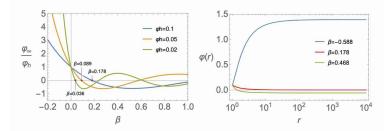


FIG. 4. For  $f = \alpha \varphi^2$ , (left)  $\varphi_{\infty}/\varphi_h$  vs  $\beta$  and (right)  $\varphi(r)$  for different values of  $\beta$  fixing  $\varphi_h = 0.1$ 

# Formation of Hairy Black Holes<sup>6 7 8</sup>

"How hairy black holes acquire their hair from non-hairy ones?"

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<sup>&</sup>lt;sup>6</sup>H. O. Silva, J. Sakstein, L. Gualtieri, T. P. Sotiriou, and E. Berti, "Spontaneous scalarization of black holes and compact stars from a gauss-bonnet coupling," Phys. Rev. Lett., vol. 120, p. 131104. Mar 2018.

<sup>&</sup>lt;sup>7</sup>Blázquez-Salcedo, D. D. Doneva, J. Kunz, and S. S. Yazadjiev, "Radial perturbations of the scalarized Einstein-Gauss-Bonnet black holes," Phys. Rev. D, vol. 98, no. 8, p. 084011, 2018.

<sup>&</sup>lt;sup>8</sup>Boris Latosh, Miok Park, 2305.19814

## Spontaneous Symmetry Breaking (SSB)

"The underlying theory has a symmetry while the underlying vacuum state does not share the same symmetry with the theory."

• Global symmetry :  $\varphi(r) \to \varphi(r) e^{i\chi}$  for global U(1)

$$\mathcal{L} = \nabla^{\mu} \varphi^* \nabla_{\mu} \varphi - V(\varphi), \qquad V(\varphi) = -\mu^2 \varphi^* \varphi + \lambda (\varphi^* \varphi)^2$$

• Gauge symmetry :  $\varphi(r) \to \varphi(r) e^{i\chi(r)}$  for local U(1)

$$\mathcal{L} = D^{\mu} \varphi^* D_{\mu} \varphi - V(\varphi) - \frac{1}{4} F^2, \qquad V(\varphi) = -\mu^2 \varphi^* \varphi + \lambda (\varphi^* \varphi)^2$$

: Ginzburg-Landau theory, superconductivity

 Higgs mechanism in standard model: responsible for giving mass to elementary particles in standard model.

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"Scalar fields are about to grow from non-hairy black holes. Finally the non-hairy evolves to hairy black holes."

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- physical fields are the excitation above the vacuum
- $\bullet \ \ "V = -f(\varphi)\mathcal{G}"$  as an "interacting potential" :
  - effective near the black hole horizon
  - not effective at infinity  $(V \to 0 \text{ as } r \to \infty, \text{ since } \mathcal{G} \to 0 \text{ as } r \to \infty)$

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- ullet scalar hair is about to form from the non-hairy ones :  $arphi_h$  is small ( $|arphi_h|<rac{3}{10}$ )

#### EsGB theory with global U(1): $\alpha < 0$

The following Lagrangian respects the global U(1) symmetry :  $\varphi(r) \to e^{i\chi} \varphi(r)$ 

$$S = \int d^4x \sqrt{-g} \left[ \frac{1}{2\kappa^2} R - \nabla_\alpha \varphi^* \nabla^\alpha \varphi + f(\varphi) \mathcal{G} \right], \tag{3}$$

$$\mathcal{L}_{\varphi} = -\nabla_{\alpha} \varphi^* \nabla^{\alpha} \varphi + f(\varphi) \mathcal{G} = T - V, \qquad V = -f(\varphi) \mathcal{G}, \tag{4}$$

$$f(\varphi) = \alpha \, \varphi^*(r)\varphi(r) - \lambda \left(\varphi^*(r)\varphi(r)\right)^2, \qquad (\lambda > 0)$$
(5)

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In the presence of symmetry, the conserved current is defined as

$$\partial_{\alpha}J^{\alpha} = 0, \qquad J_{\alpha} = i g \left( \varphi^* \partial_{\alpha} \varphi - \varphi \partial_{\alpha} \varphi^* \right).$$

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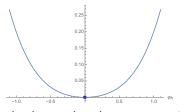
The flux for a timelike hypersurface near the horizon is given by

$$\int_{\Sigma} J_{\alpha} n^{\alpha} \sqrt{-h} \, d^{3}y = \int_{\Sigma} \left[ g(\varphi_{2} \partial_{r} \varphi_{1} - \varphi_{1} \partial_{r} \varphi_{2}) \right] \left[ \sqrt{A(r)B(r)} \, r^{2} \sin \theta \, d\theta \, d\phi \, dt \right] = 0$$

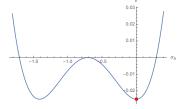
where

$$\varphi(r) = \frac{1}{\sqrt{2}} \left( \varphi_1(r) + i \, \varphi_2(r) \right)$$

"When  $\alpha < 0$ , vacuum is symmetric under global U(1)"



"When  $\alpha>0$ , vacuum is changed and not symmetric under global U(1)"



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#### EsGB theory with global U(1): $\alpha > 0$

When  $\alpha > 0$ : V forms degenerate vacuums and the stable minima are described by

$$\langle \varphi \rangle = v e^{i\beta}, \qquad v = \sqrt{\frac{\alpha}{2\lambda}}$$
 (6)

We expand a field around a ground state v by reparameterizing it as follows

$$\varphi(r) = \left(v + \frac{\sigma(r)}{\sqrt{2}}\right)e^{i\theta(r)}.\tag{7}$$

the new Lagrangian is written as

$$\mathcal{L}_{\varphi} = -\frac{1}{2} \nabla_{\alpha} \sigma(r) \nabla^{\alpha} \sigma(r) - \left( v + \frac{\sigma(r)}{\sqrt{2}} \right)^{2} \nabla_{\alpha} \theta(r) \nabla^{\alpha} \theta(r) + f(\sigma) \mathcal{G}$$
 (8)

where

$$f(\sigma) = -\alpha \, \sigma(r)^2 - \sqrt{\alpha \, \lambda} \, \sigma(r)^3 - \frac{\lambda}{4} \, \sigma(r)^4. \tag{9}$$

Field  $\theta(r)$  is decoupled from the system, and the solution for  $\theta'(r)$  reads

$$\theta'(r) = \frac{c_2}{4r^2\sqrt{A(r)B(r)}} \left(v + \frac{\sigma(r)}{\sqrt{2}}\right)^{-2}$$

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$$\int_{\Sigma} J_{\alpha} n^{\alpha} \sqrt{-h} \, d^{3}y = \int_{\Sigma} \left[ -2g \left( v + \frac{\sigma(r)}{\sqrt{2}} \right)^{2} \theta'(r) \right] \left[ \sqrt{A(r)B(r)} \, r^{2} \sin \theta d\theta d\phi dt \right] = -8\pi g c_{2}$$

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"The hairy black holes in this theory can only possess trivial Goldstone bosons hair."

#### symmetric and symmetry-broken phase

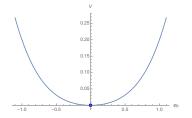


Figure: symmetric (left) and symmetry-broken phase (right)



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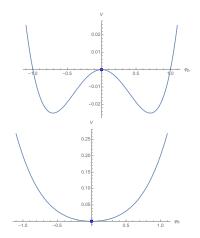


Figure: symmetric (left) and symmetry-broken phase (right)



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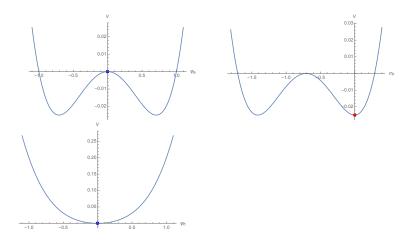


Figure: symmetric (left) and symmetry-broken phase (right)



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#### scalar field perturbation in EsGB: instability

The linearized equation then becomes

$$\left(\nabla_{\alpha}\nabla^{\alpha} + f_{\varphi^*\varphi}\mathcal{G}\right)\delta\varphi(r) = 0, \qquad m_{\text{eff}}^2 = -f_{\varphi^*\varphi}\mathcal{G}$$

$$\delta\varphi(t, r, \theta, \phi) = \sum_{l,m} \frac{\Phi(r)Y_{lm}(\theta, \phi)}{r} e^{-i\omega t}$$

the perturbation equation is written as

$$\Phi''(r_*) - (V_{\text{eff}} - \omega^2)\Phi(r_*) = 0, \qquad dr_* = \frac{1}{\sqrt{AB}}dr,$$

$$V_{\text{eff}}(r) = \frac{l(l+1)A}{r^2} + \frac{1}{2r} \left( A'B + AB' \right) - f_{\varphi^*\varphi} A \mathcal{G},$$

The system becomes unstable if the following condition is met

$$\int\limits_{r_h}^{\infty} dr \frac{1}{\sqrt{AB}} V_{\text{eff}}(r) < 0.$$



#### Instability for Schwarzschild black hole

$$ds^{2} = -A(r)dt^{2} + \frac{1}{B(r)}dr^{2} + r^{2}(d\theta^{2} + \sin^{2}(\theta)d\phi^{2}), \qquad A = B = 1 - \frac{2M}{r}$$
 (10)

Instability check yields

$$\alpha > \frac{5}{6} (2l(l+1) + 1)M^2 = \alpha_{Sch.}$$
 (11)

When  $M=\frac{1}{2}$  and l=0,

$$\alpha_{\rm Sch.} = \frac{5}{24} \approx 0.2083$$
 (12)

"Schwarzschild black holes are unstable if  $\alpha > \alpha_{\rm Sch.}$ "

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#### Phase space

#### The regularity condition yields

$$1 - 96(\dot{f}_h)^2 > 0$$

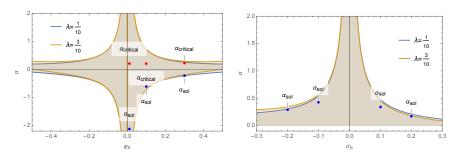


Figure: Phase space for symmetric phase (left) and symmetry-broken phase (right)

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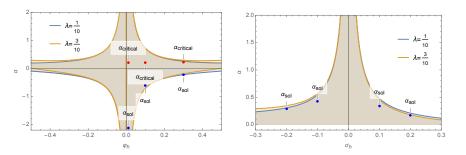
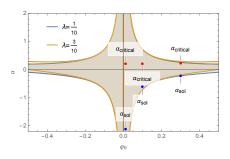


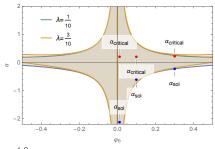
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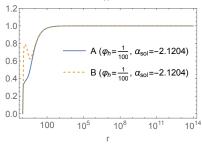
"  $\alpha_{\rm critical} \approx \alpha_{\rm Sch.}$ "

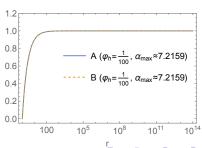
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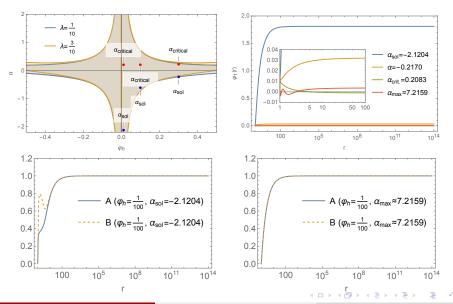
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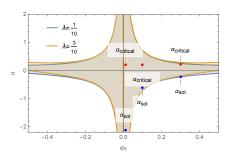


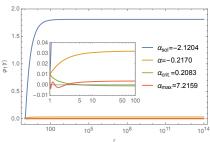


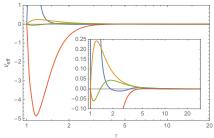


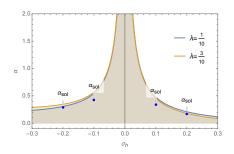


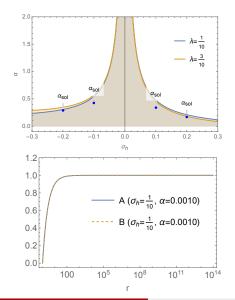


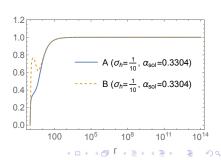


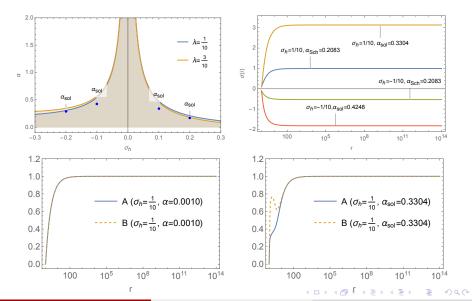


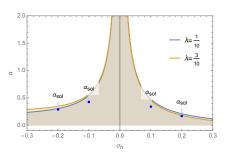


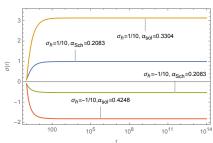


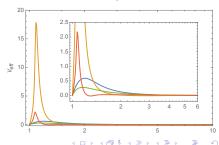












# SSB in EsGB theory with local U(1)

This action is invariant under local U(1) symmetry :  $\varphi \to \varphi \, e^{i\chi(r)}$ 

$$S = \int d^4x \sqrt{-g} \left[ \frac{1}{2\kappa^2} R - \frac{1}{4} F^2 - D_\alpha \varphi^* D^\alpha \varphi + f(\varphi^*, \varphi) \mathcal{G} \right], \tag{13}$$

where F = dP and  $D_{\alpha} = \nabla_{\alpha} - iqP_{\alpha}$ .

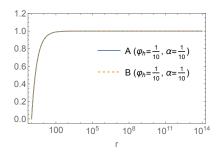
When q = 0,

$$\begin{split} A(r) &\sim 1 + \frac{A_1}{r} + \frac{P_1^2}{4\,r^2} - \frac{A_1\varphi_1^2}{12\,r^3} + \cdots \\ B(r) &\sim 1 + \frac{A_1}{r} + \frac{P_1^2 + 2\,\varphi_1^2}{4\,r^2} - \frac{A_1\varphi_1^2}{4\,r^3} + \cdots \\ P(r) &\sim P_\infty + \frac{P_1}{r} - \frac{P_1\,\varphi_1^2}{12\,r^3} + \cdots \\ \varphi(r) &\sim \varphi_\infty + \frac{\varphi_1}{r} - \frac{A_1\,\varphi_1}{2\,r^2} - \frac{\varphi_1\left(-4\,A_1^2 + P_1^2 + \varphi_1^2\right)}{12\,r^3} + \cdots \end{split}$$

- When  $q \neq 0$ , the asymptotic expansions of the gauge field and scalar fields yield  $P_{\infty} = P_1 = 0$  or  $\varphi_{\infty} = \varphi_1 = 0$ .
- ullet This may imply that either the gauge field or the scalar field falls off faster than  $1/r^n$  at infinity, or that there are no electrically-charged scalar hairy black hole

### Hairy Black Holes in EsGB theory with local U(1)

#### Numerical solutions for q=0 case



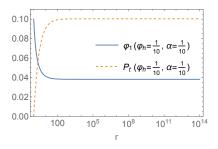


Figure: Hairy black hole solutions when q = 0

\* We were not able to find hairy black hole solutions with charged scalar hairs ( $q \neq 0$ ).



ullet We considered the Einstein-Scalar-Gauss-Bonnet (ESGB) theory with U(1) symmetry and showed that SSB can lead to the formation or evolution of hairy black holes from non-hairy ones.



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- Goldstone bosons are decoupled from other equations and only trivial solutions are accepted.
- Thus, we expect that the Schwarzschild black holes in the unstable range of  $\alpha$  ( $\alpha > \alpha_{\rm Sch.}$ ) would evolve into the hairy black holes in the symmetry-broken phase.
- Spontaneous symmetry breaking associated with local U(1) cannot be realized in this theory.

















Thank you!

