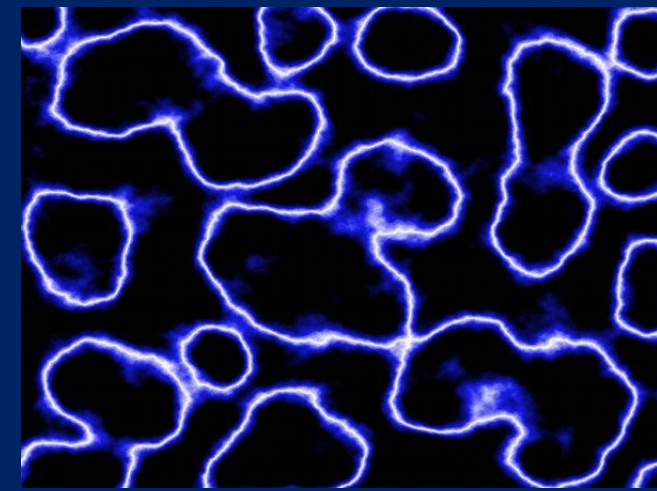


Progress in constructing KKLT de Sitter vacua

시작이 반이다

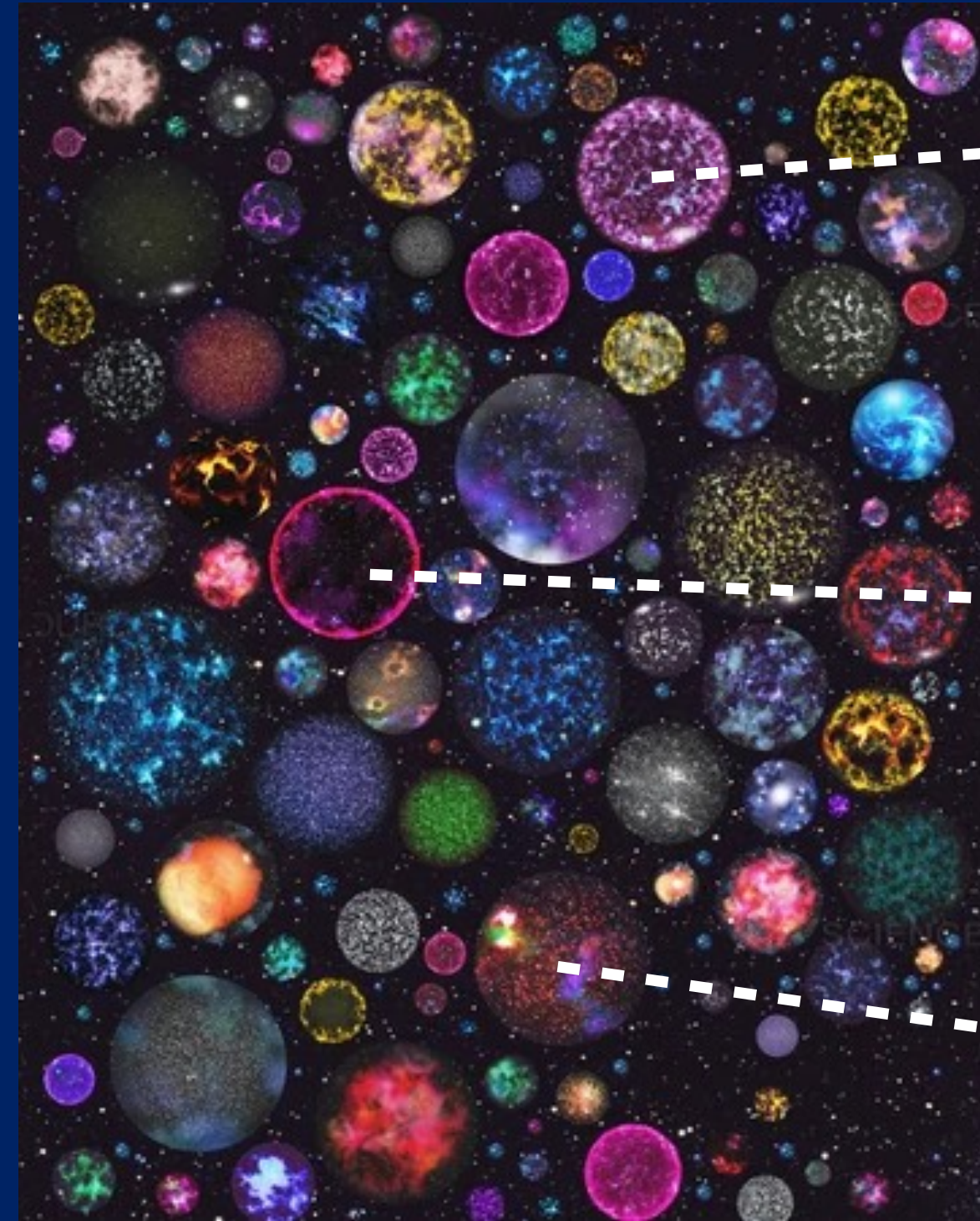
Based on work in progress with N. Gendler, L. McAllister, J. Moritz, R. Nally



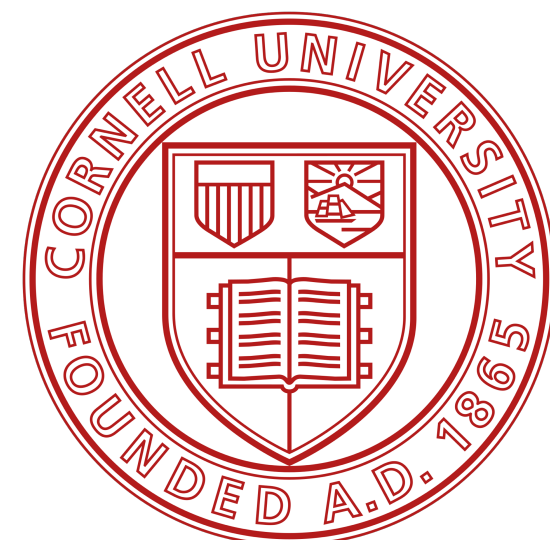
String Theory



Compactification



String Landscape



Andreas Schachner

String Phenomenology Conference 2023
Institute for Basic Science, Daejeon, South Korea
July 6, 2023

Email: as3475@cornell.edu

Collaboration

Cornell University



Naomi Gendler
(now at Harvard)



Liam McAllister

MIT



Manki Kim
(applying this year)

LMU Munich



Sven Krippendorf



Julian Ebelt
(Master)



Jakob Moritz



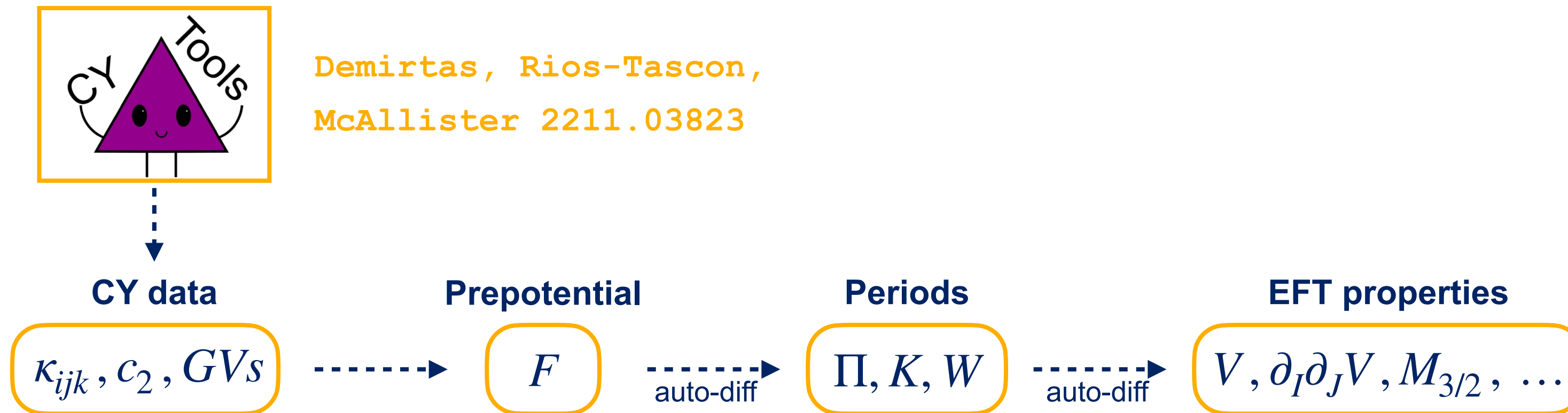
Richard Nally
(applying this year)



Abhishek Dubey
(Master)

JAXVacua - A framework for string vacua

Objective: Numerical framework to determine and evaluate EFT (e.g. scalar potential, Hessian etc.) with only minimal input by using auto-differentiation



Based on work with:

- A. Dubey, S. Krippendorf [2306.06160](#)
- J. Ebelt, S. Krippendorf (to appear next week)
- S. Krippendorf (to appear next week)

See talk of Sven Krippendorf.

LMU Munich



Sven Krippendorf



Julian Ebelt
(Master)



Abhishek Dubey
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KKLT proposal: de Sitter vacua in Type IIB String Theory

Kachru, Kallosh, Linde, Trivedi [hep-th/0301240](#)

Claim 1:

Well-controlled SUSY AdS₄ exist in Type IIB flux compactifications with

$$\langle W_{flux} \rangle \ll 1$$

and non-perturbative D-brane instantons.

Achieved explicitly in [Demirtas et al. \[2107.09064, 2107.09065\]](#)

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For such a SUSY AdS₄, provided one finds

- warped deformed conifold [[Klebanov, Strassler hep-th/0007191](#)]
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Do there exist geometries that realise this idea?

Yes, we found explicit configurations that satisfy all requirements for KKLT de Sitter vacua **in the leading approximation.**

Important work in progress is checking effects of further corrections like:

- perturbative corrections to Kähler potential, beyond BBHL [[hep-th/0204254](#)], and
- α' corrections to anti-D3-brane action [[Hebecker, 2x \(Schreyer, Venken\) 2208.02826, 2212.07437](#)].

[Gendler, McAllister, Moritz, Nally, Schachner 230X.XXXX](#)

KKLT SUSY AdS_4 vacua **with conifolds**

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[Gukov et al. hep-th/9906070]

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We work at **large complex structure** using mirror symmetry to compute W_{flux} .

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Stabilise τ

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$$|W_0| = |\langle W_{inst} \rangle| \ll 1 \quad z_{cf} \approx \frac{1}{2\pi} \exp\left(-\frac{2\pi K}{n_{cf} g_s M}\right)$$

[Demirtas et al. 2009.03312, Álvarez-García et al. 2009.03325]

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[Witten hep-th/9604030]

$$W_{np}(\tau, z^a, T_A) = \sum_A \mathcal{A}_A(\tau, z^a) e^{-2\pi T_A / c_A}$$

verified condition of
[Witten hep-th/9610234]

$$\mathcal{A}_A(\tau, z^a) = \text{const.}$$

Special thanks to Manki Kim for explaining the computation to us!

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We solve $D_A W = 0$ for the Kähler moduli such that

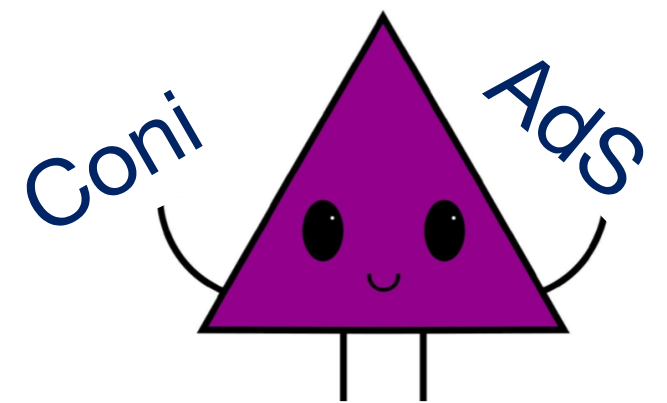
$$T_A \approx \frac{c_A}{2\pi} \log(|W_0|^{-1})$$

This leads to SUSY AdS_4 vacua with

$$g_s \sim \frac{2\pi}{\log(|W_0|^{-1})} \ll 1$$

(see talk L. McAllister string pheno 2022 for details)

[Demirtas et al. 2107.09064, 2107.09065]

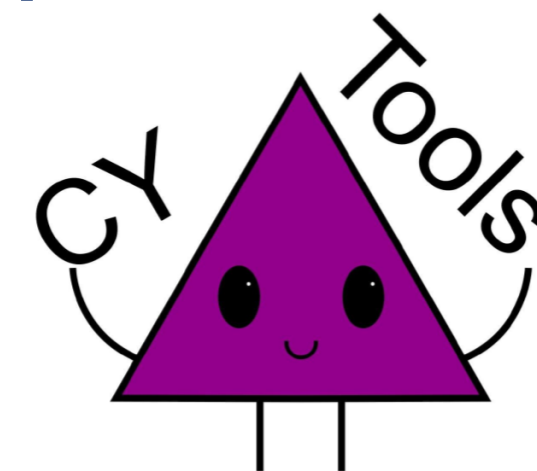


Initial scan for vacua

We search for

- CY_3 from 4D reflexive polytopes with $3 \leq h^{1,2} \leq 8$ [Kreuzer, Skarke hep-th/0002240]
- orientifolds with $h_+^{1,2} = 0$ from \mathbb{Z}_2 -involutions $x \rightarrow -x$ following [Moritz 2305.06363]
- conifold points by shrinking toric flop curves
- flux vacua with $|W_0| \ll 1$ together with stabilisation near conifold loci
- $\geq h^{1,1}$ rigid divisors supporting D-instantons and having constant Pfaffian [Jefferson, Kim 2211.00210]

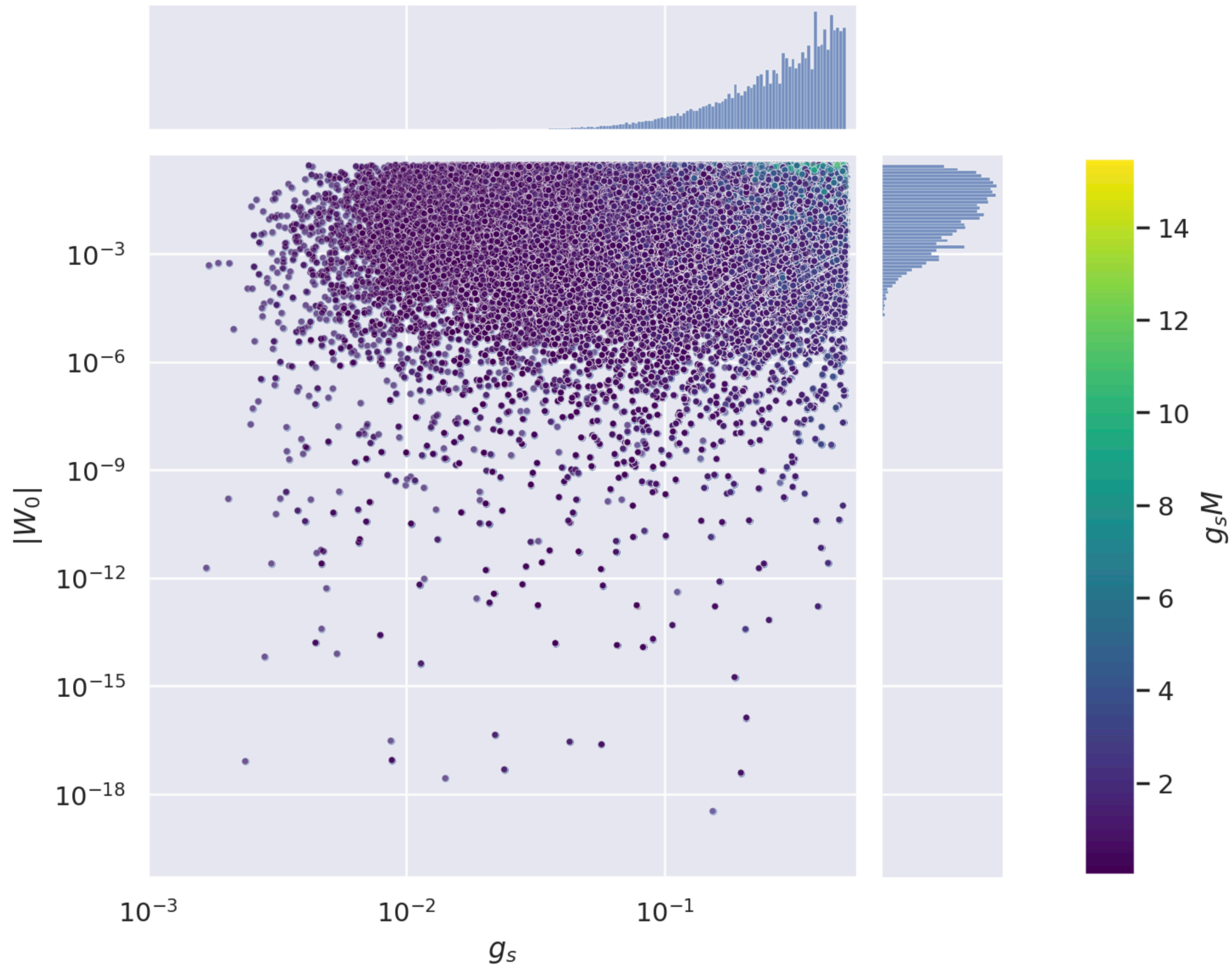
Computations performed with



<http://cy.tools>

Demirtas, Rios-Tascon, McAllister 2211.03823

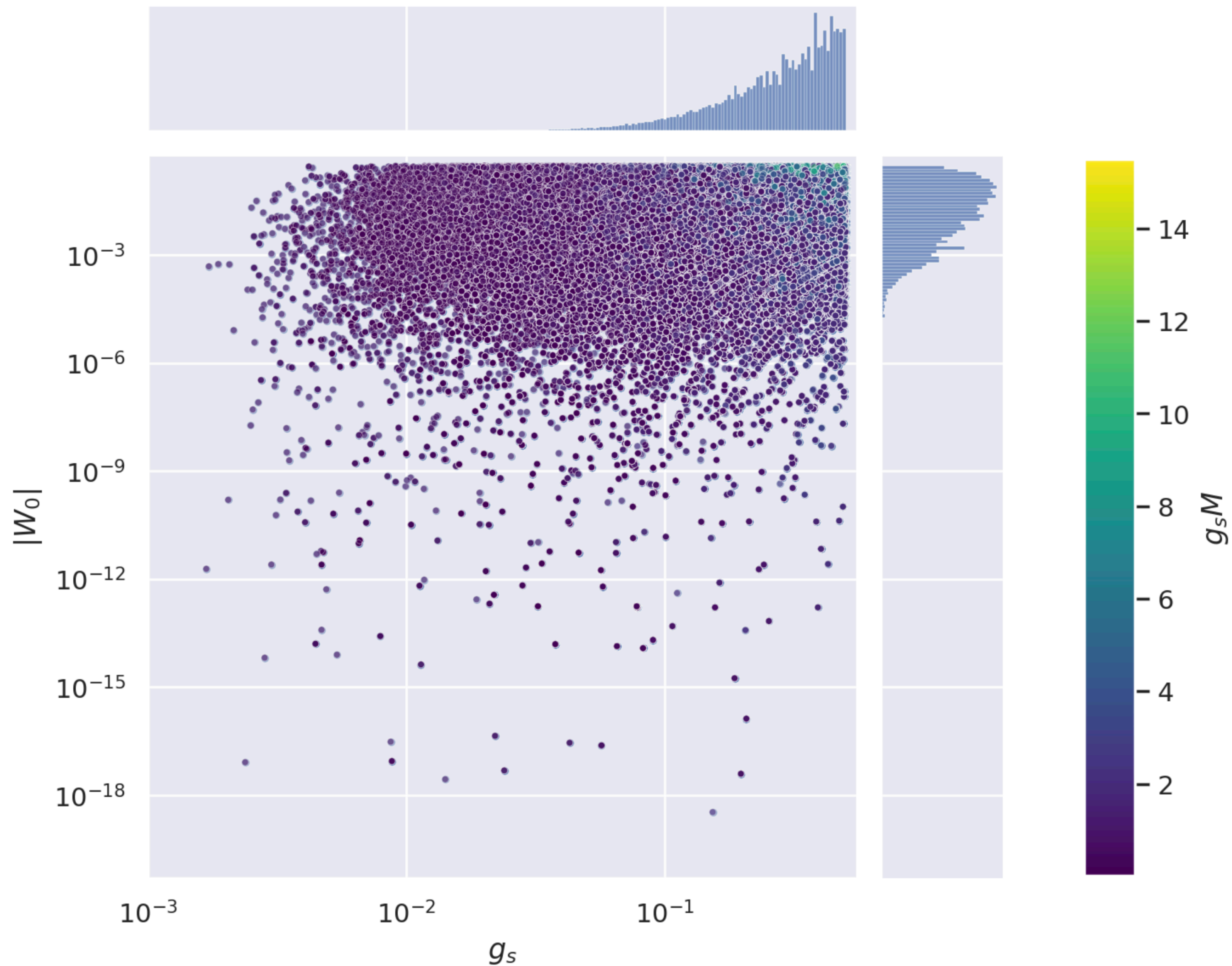
KKLT SUSY AdS_4 vacua with conifolds



From a scan over 36 polytopes and 300 CY geometries, we obtained 4,831,234 vacua with

- $g_s < 0.5$
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In what follows, I will impose more and more cuts on this dataset to eventually satisfy all of the requirements in Claim 2 of KKLT!

Claim 2 checklist:

- warped throat
- anti-D3 branes
- suitable parameter regime

KKLT SUSY AdS_4 vacua with warped throats

Stabilisation near conifold point in moduli space leads to warped throat [[GKP hep-th/0105097](#)] with warp factor at the tip

$$e^{4A_{IR}} \approx e^{-8\pi K/3n_{cf}g_s M} \sim |z_{cf}|^{\frac{4}{3}} \quad M, K \text{ fluxes threading the } S^3 \text{ at the tip}$$

For $e^{4A_{IR}} \ll 1$, we obtain long warped throats that for $g_s M \gg 1$ is well approximated by the KS solution [[hep-th/0007191](#)]

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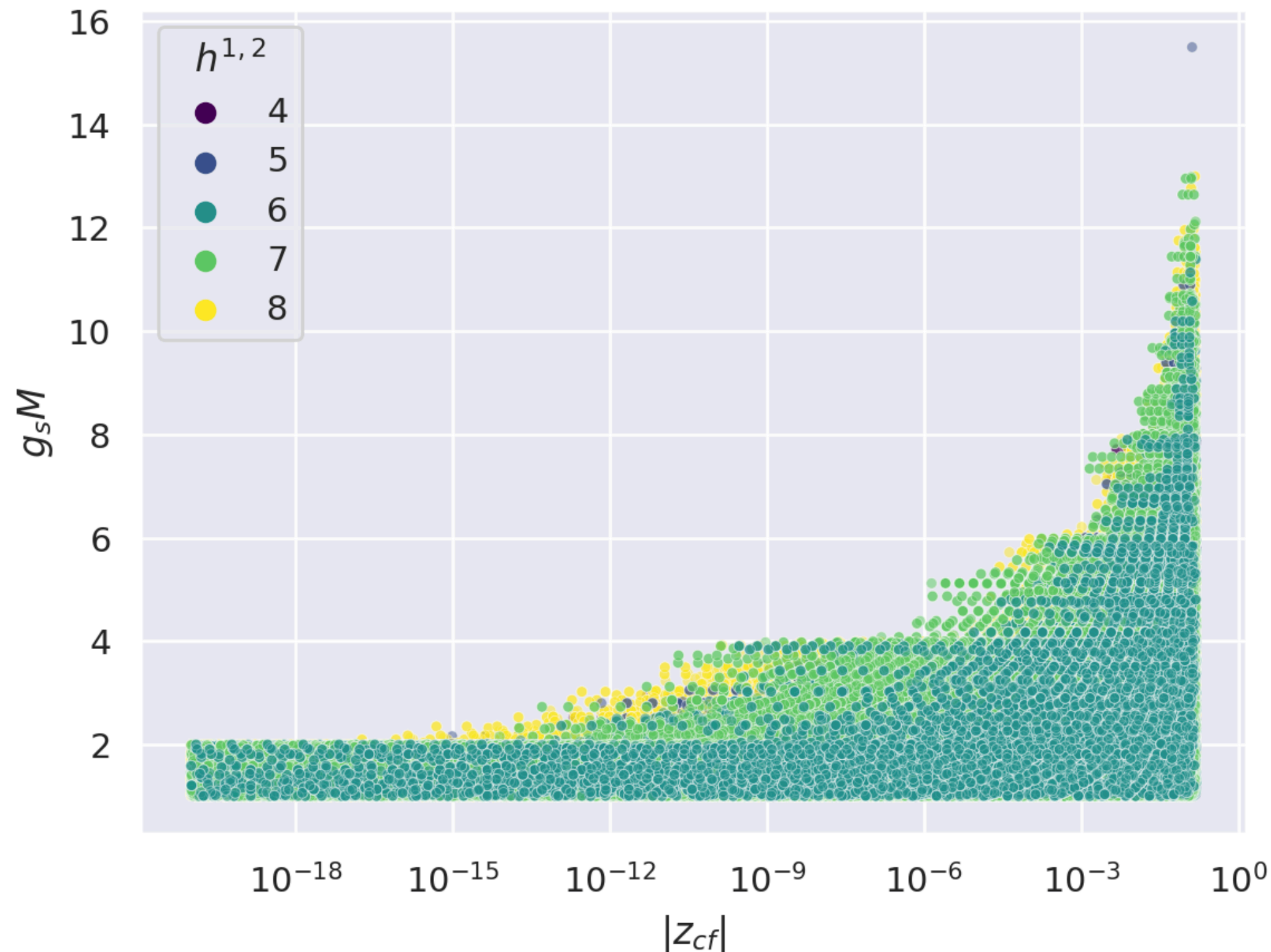
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We find 3,801,168 vacua satisfying

- $g_s < 0.5$
- $|W_0| < 0.3$
- $g_s M > 1$

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Are there flux configurations that allow **anti-D3 branes**?

Claim 2 checklist:

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Towards KKLT dS_4 vacua from a single anti-D3 brane

We consider flux choices allowing to add a single anti-D3 brane $N_{flux} = Q_{D3} + 1$.
There are roughly 1 % $\sim 10^4$ vacua of this type.

Related LVS construction
[Crino et al. 2010.15903]

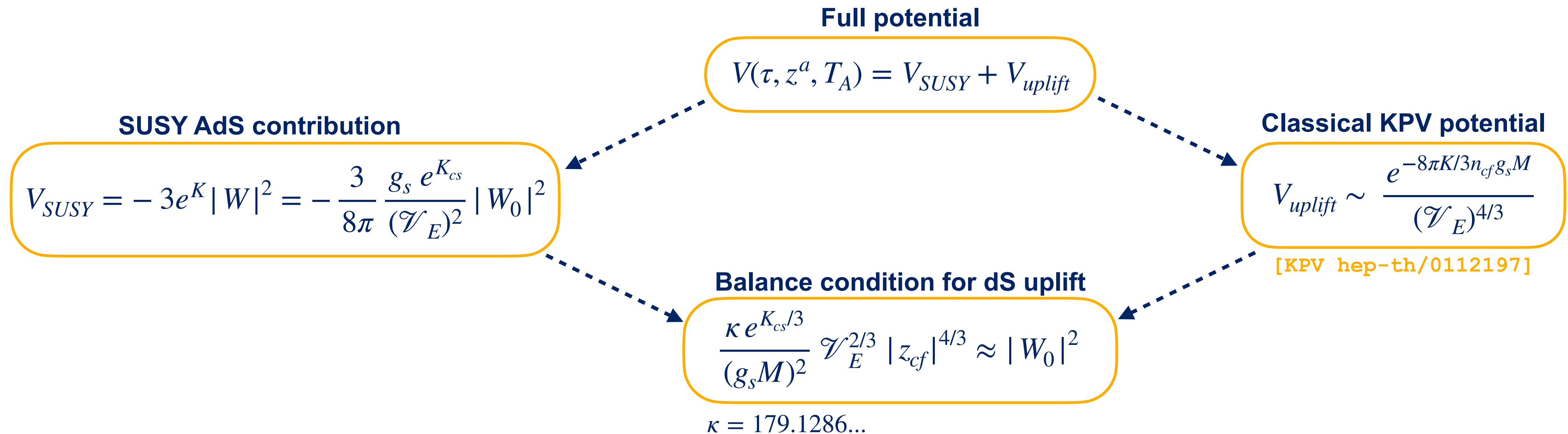
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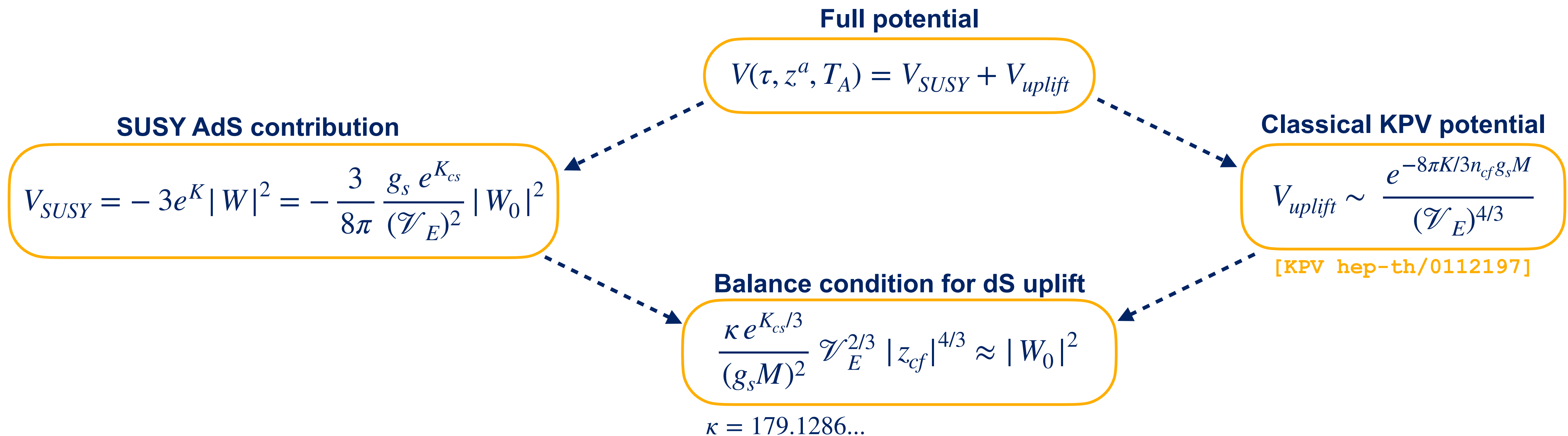
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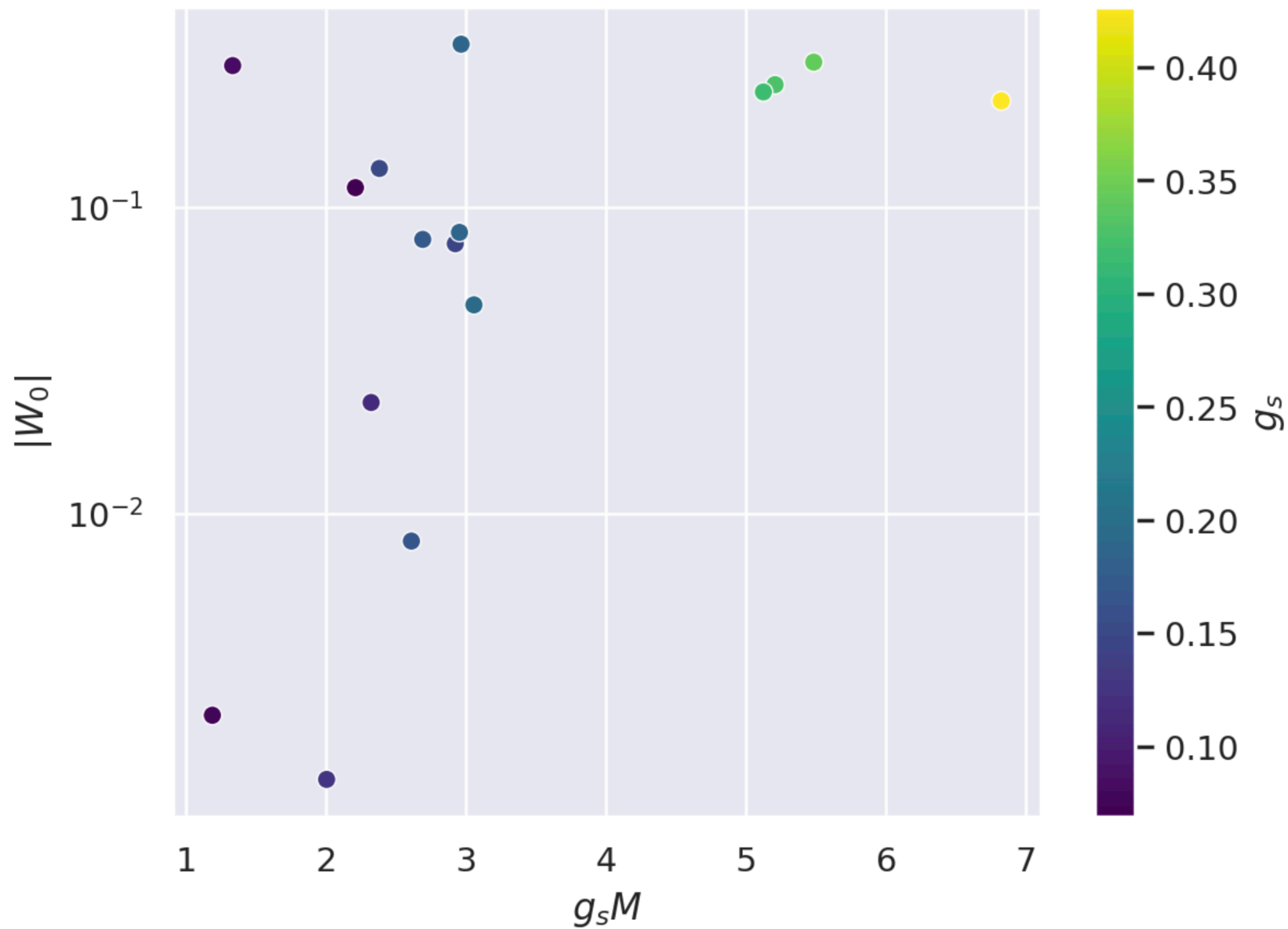
Conditions on control:

- $M \gtrsim 12$: meta-stability of the throat configuration against brane-flux annihilation [KPV hep-th/0112197]
- $g_s M > 1$: small curvature at bottom of throat [Klebanov, Strassler hep-th/0007191]
- $z_{cf} \ll 1$: long throat
- $g_s < 0.5$ and $W_0 < 0.3$: perturbative control and Kähler moduli stabilisation

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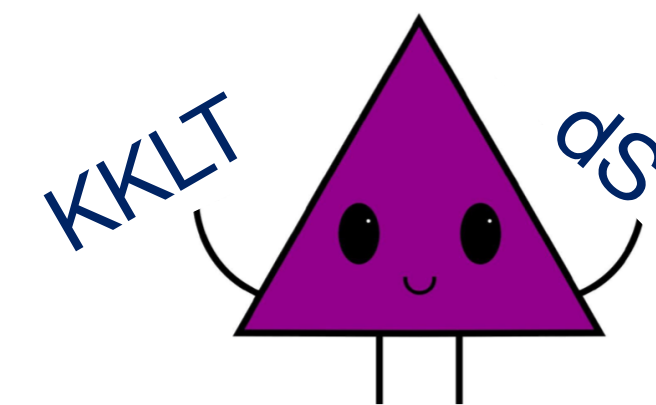
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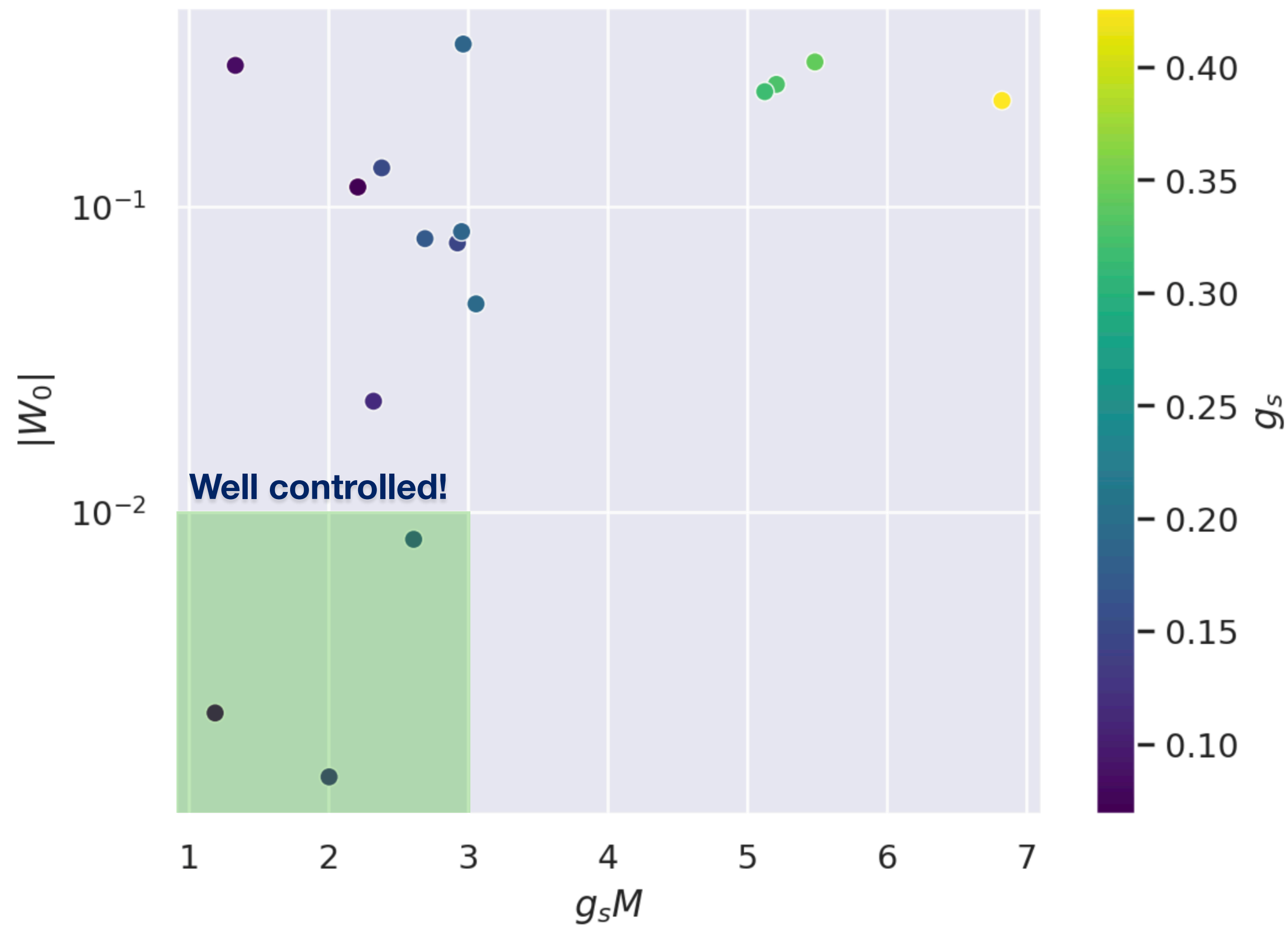


$h^{1,2}$	$h^{1,1}$	g_s	W_0	M	$g_s M$	$g_s M^2$	$ z_{cf} $	\mathcal{V}_E	$Q/\mathcal{V}_E^{2/3}$
5	205	0.069	0.116	32	2.21	70.74	$7.61 \cdot 10^{-6}$	46464	0.080
7	219	0.146	0.076	20	2.92	58.48	$3.43 \cdot 10^{-6}$	32803	0.101
7	219	0.168	0.079	16	2.69	43.07	$4.36 \cdot 10^{-6}$	20613	0.138
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7	219	0.185	0.083	16	2.95	47.26	$3.83 \cdot 10^{-6}$	9009	0.240
8	198	0.125	0.001	16	2.00	32.08	$1.00 \cdot 10^{-8}$	10453	0.222
8	198	0.163	0.008	16	2.61	41.77	$1.60 \cdot 10^{-7}$	9266	0.240
8	198	0.191	0.048	16	3.06	48.92	$3.28 \cdot 10^{-6}$	75155	0.077
8	198	0.325	0.251	16	5.21	83.33	$2.09 \cdot 10^{-4}$	13751	0.185
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We find 16 dS_4 vacua satisfying the aforementioned conditions!

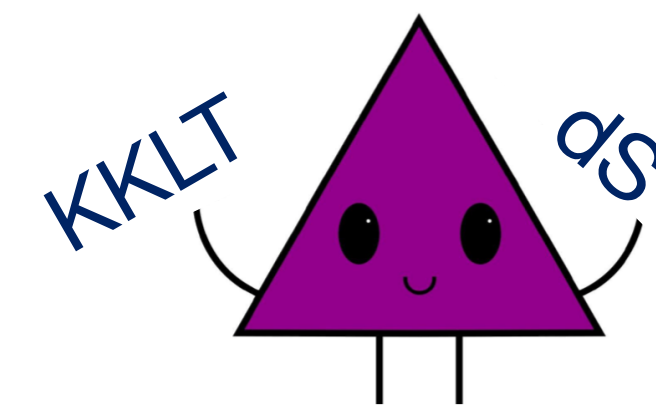


Towards KKLT dS_4 vacua from a single anti-D3 brane

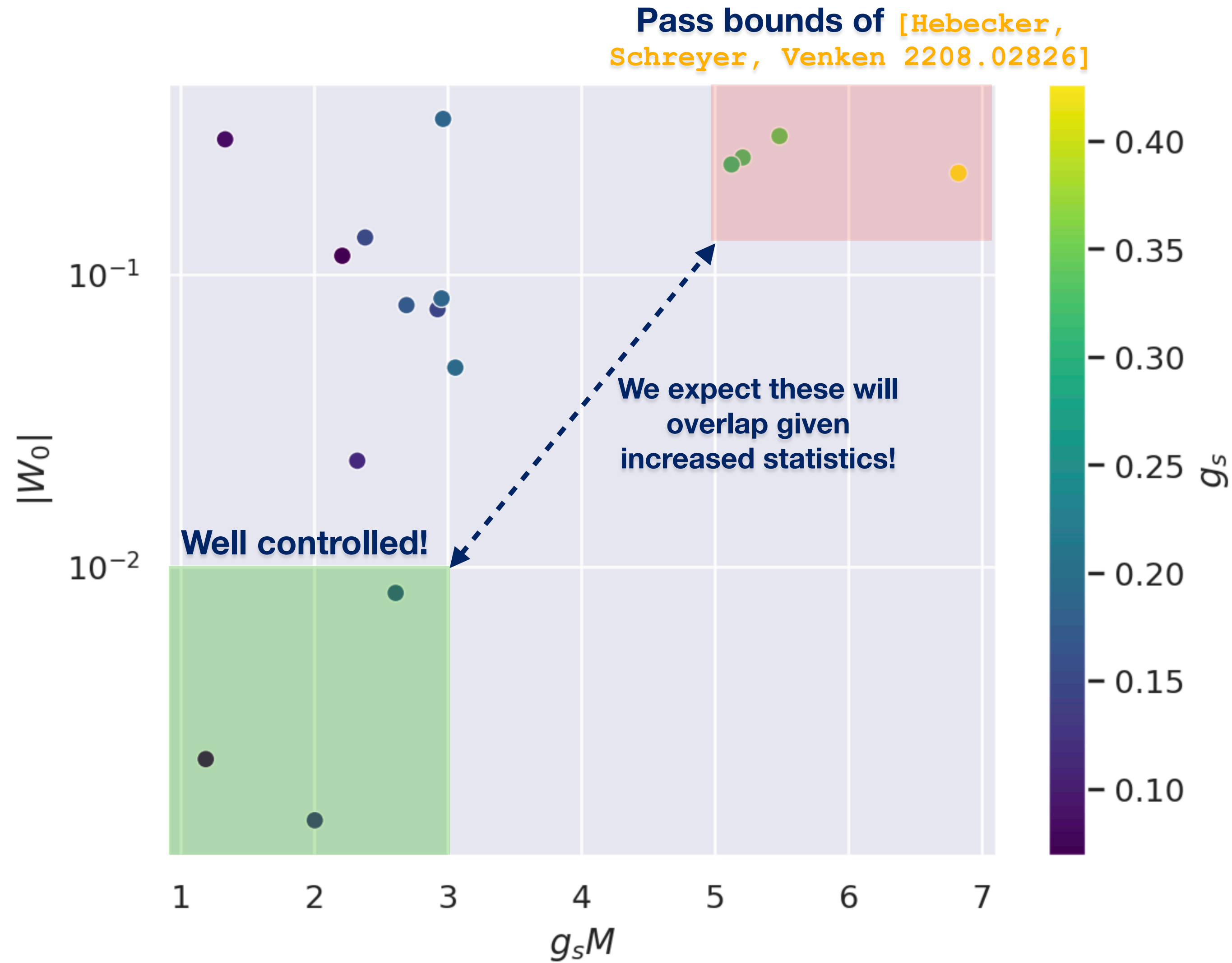


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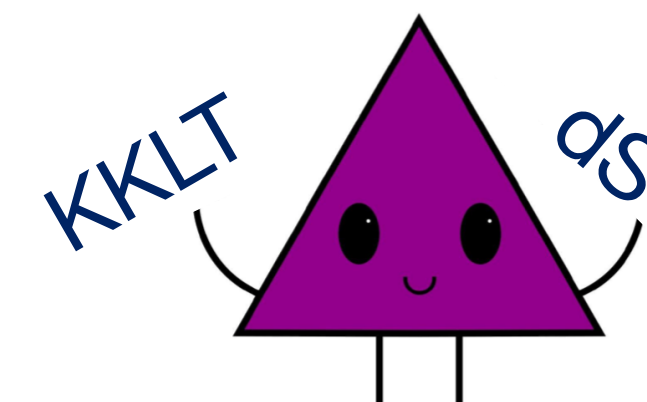


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We find 16 dS_4 vacua satisfying the aforementioned conditions!



Control issues and further challenges

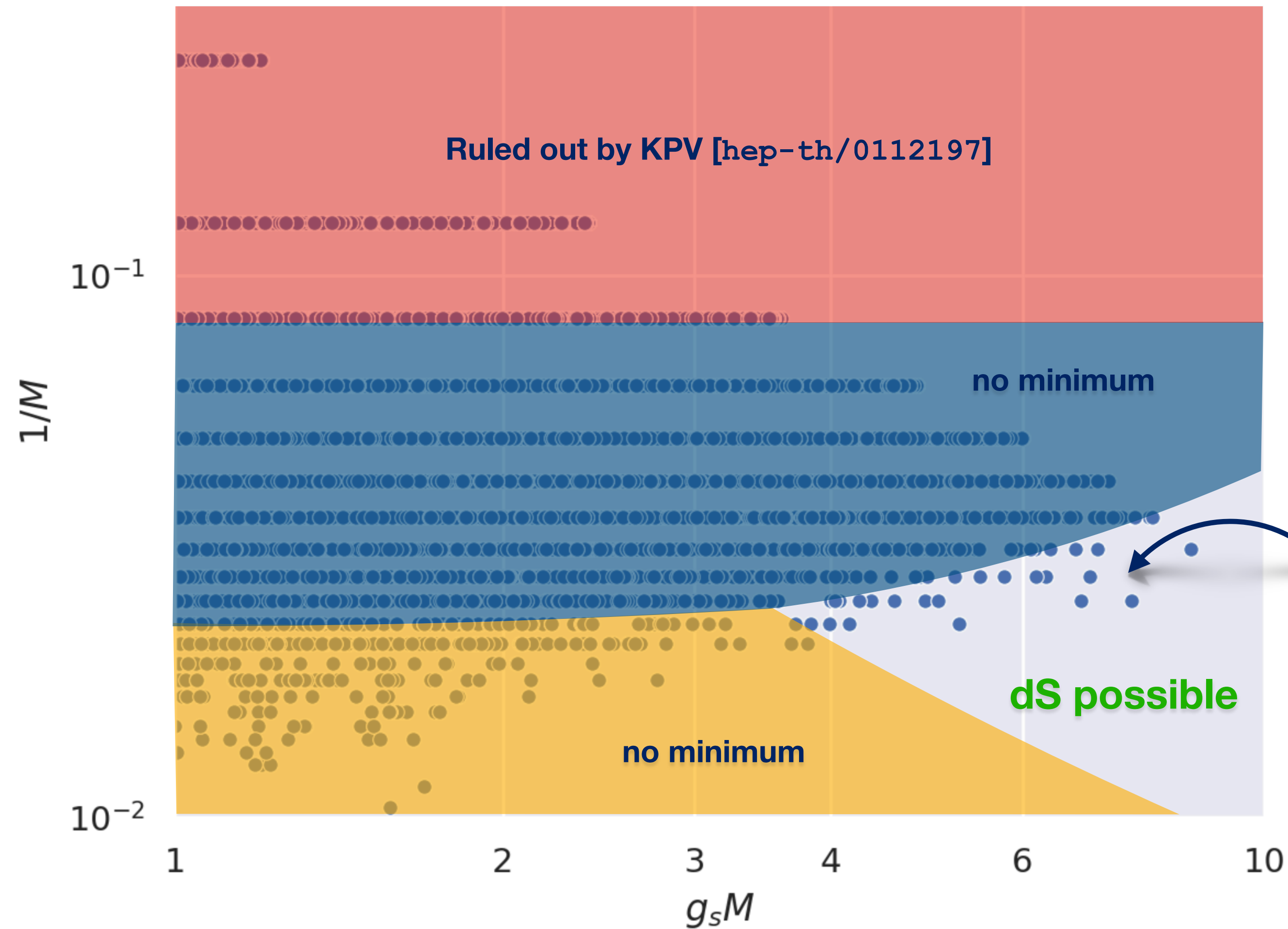
So far, we have been working in the **leading approximation**.

More work is required to understand the role of

- loop corrections to the Kähler potential, see [Kim 2301.03602, 2302.12117, 2305.08263] for recent progress
- the singular bulk problem [Gao, Hebecker, Junghans 2009.03914], but note that it is already rather well-controlled in our examples, cf. [Demirtas et al. 2107.09064] and also [Carta, Moritz 2101.05281]
- α' corrections to KPV such as computed by [Hebecker, 2x(Schreyer, Venken) 2208.02826, 2212.07437]

Coming back to the full dataset...

Contours from flux dependent α' corrections to the KPV potential as obtained by [Schreyer, Venken 2212.07437]



Surviving solutions have $N_{flux} \leq Q_{D3}$ requiring additional D3-branes which is potentially interesting for realising inflation (work in progress)

Conclusions

We have exhibited explicit examples of CY orientifold flux compactifications with

- **small W_0**
- **small g_s**
- **all moduli explicitly stabilised**
- **including a single anti-D3-brane in an explicit KS throat**

for which the KPV computation of the anti-brane energy predicts uplift to a KKLT de Sitter vacuum.

We think this is tremendously exciting, but we are not declaring the job done:

- We are still working to find examples in which the KS throat has large enough $g_s M$ so that upon including (the known) corrections to the KPV computation, one remains in de Sitter.
- This appears to us to be a matter of statistics, and will take more compute time.

An aerial photograph showing a dense green forest in the foreground, with a cityscape and mountains in the background under a cloudy sky. The text '매우 감사합니다' is centered over the forest.

매우 감사합니다

Contours from curvature corrections to the KPV potential as obtained by [Hebecker, Schreyer, Venken 2208.02826]

