

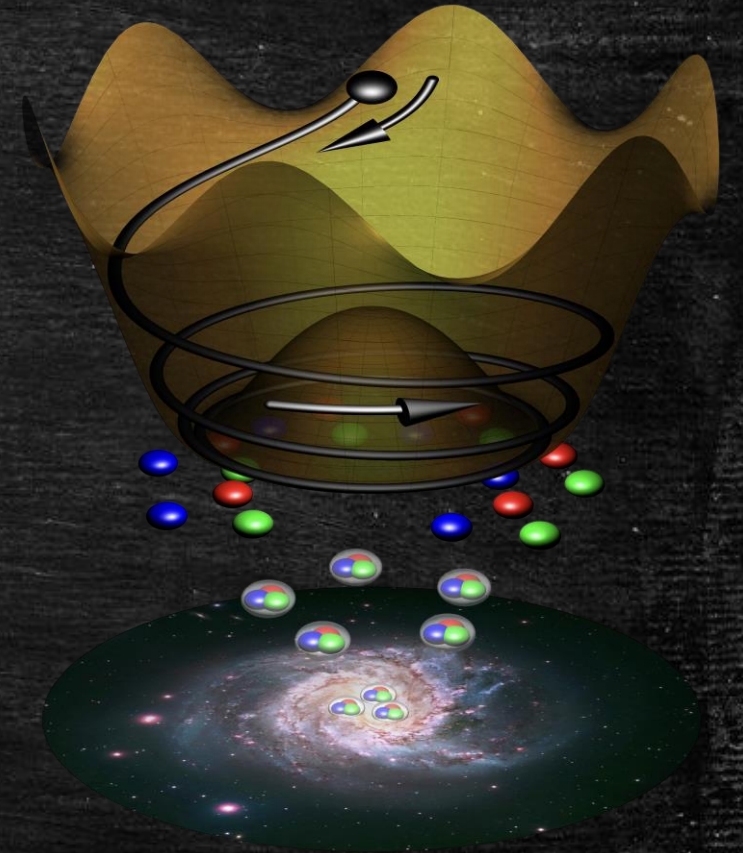
# Cosmological Implications of Axion Rotations

The Early Universe: A Window to New Physics  
University of Florida

October 22<sup>nd</sup>, 2023

Raymond Co

Indiana University





# Today



**Nobel Prize in Physics 1937**

for their experimental discovery of the diffraction of electrons by crystals

Clinton Joseph Davisson

born on

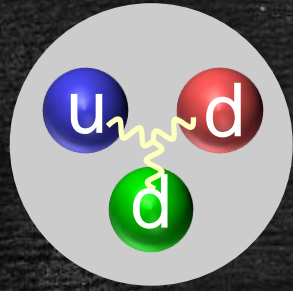
**October 22<sup>nd</sup> 1881**

Bloomington, IL, USA



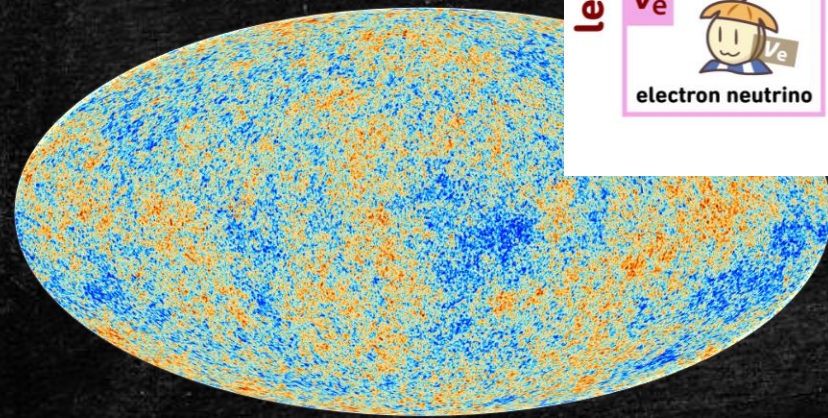
# Outline of the Talk

strong CP problem



neutron

	matter (fermions)			gauge bosons	
quarks	u up quark	c charm quark	t top quark	$\gamma$ photon	electro-magnetic
	d down quark	s strange quark	b bottom quark	g gluon	strong
	e electron	$\mu$ muon	$\tau$ tau	Z, W $^{\pm}$ weak bosons	weak
leptons	$\nu_e$ electron neutrino	$\nu_{\mu}$ muon neutrino	$\nu_{\tau}$ tau neutrino	H higgs boson	Higgs bosons



Source: Planck

 +  
axion?

matter-antimatter  
asymmetry

dark matter



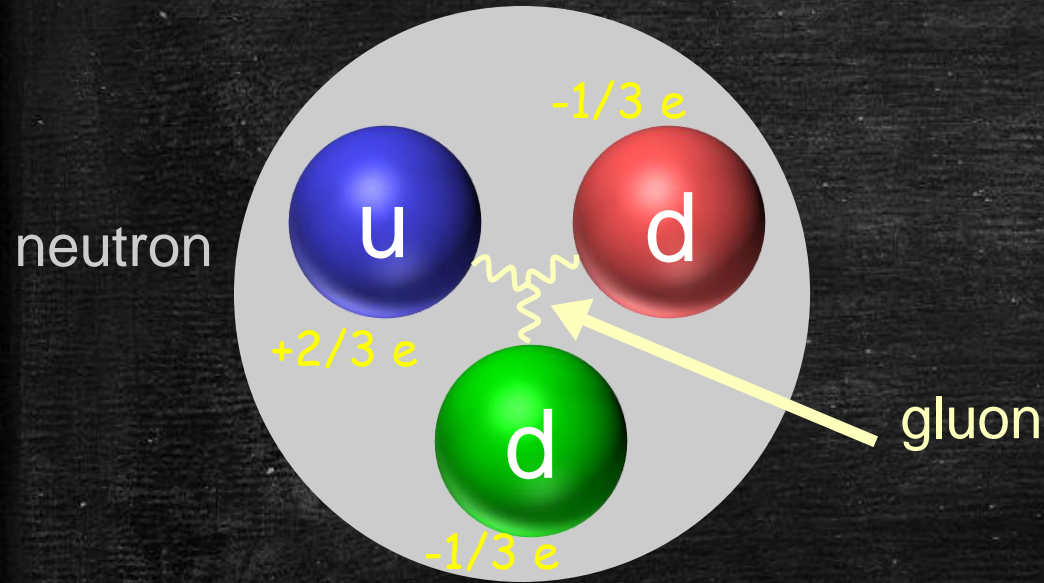
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# Review of the QCD Axion

# Strong CP Problem

“Charge-Parity” symmetry



Quantum field theory:

$$\mathcal{L} \supset \bar{\theta} \frac{\alpha_s}{8\pi} G_b^{\mu\nu} \tilde{G}_{b\mu\nu}$$

gluon

$$|d_n| \simeq 2.4 \times 10^{-16} \bar{\theta} e \cdot \text{cm}$$

Crewther, Di Vecchia, Veneziano, Witten 1979, Pospelov, Ritz 2000

Experiments:

$$|d_n| \lesssim 1.8 \times 10^{-26} e \cdot \text{cm}$$

PRL 97, 131801 2006, PRL 124, 081803 2020

Strong CP problem:

$$\bar{\theta} \lesssim 10^{-10}$$

Why exceedingly small?



# Strong CP Problem solution



Peccei

Quinn

2017  Quanta magazine

$$\mathcal{L} \supset \bar{\theta} \frac{\alpha_s}{8\pi} G_b^{\mu\nu} \tilde{G}_{b\mu\nu}$$

Peccei, Quinn 1977  
Weinberg 1978  
Wilczek 1978

QCD axion

Promoted to a dynamical field:

$$\mathcal{L} \supset \left( \bar{\theta} + \frac{a}{f_a} \right) \frac{\alpha_s}{8\pi} G_b^{\mu\nu} \tilde{G}_{b\mu\nu}$$

decay constant

QCD effects automatically generate an axion potential  $V(a) = m_a^2 f_a^2 \left[ 1 - \cos \left( \bar{\theta} + \frac{a}{f_a} \right) \right]$

This potential dynamically drives the axion to a field value that cancels  $\bar{\theta}$ . Problem solved!



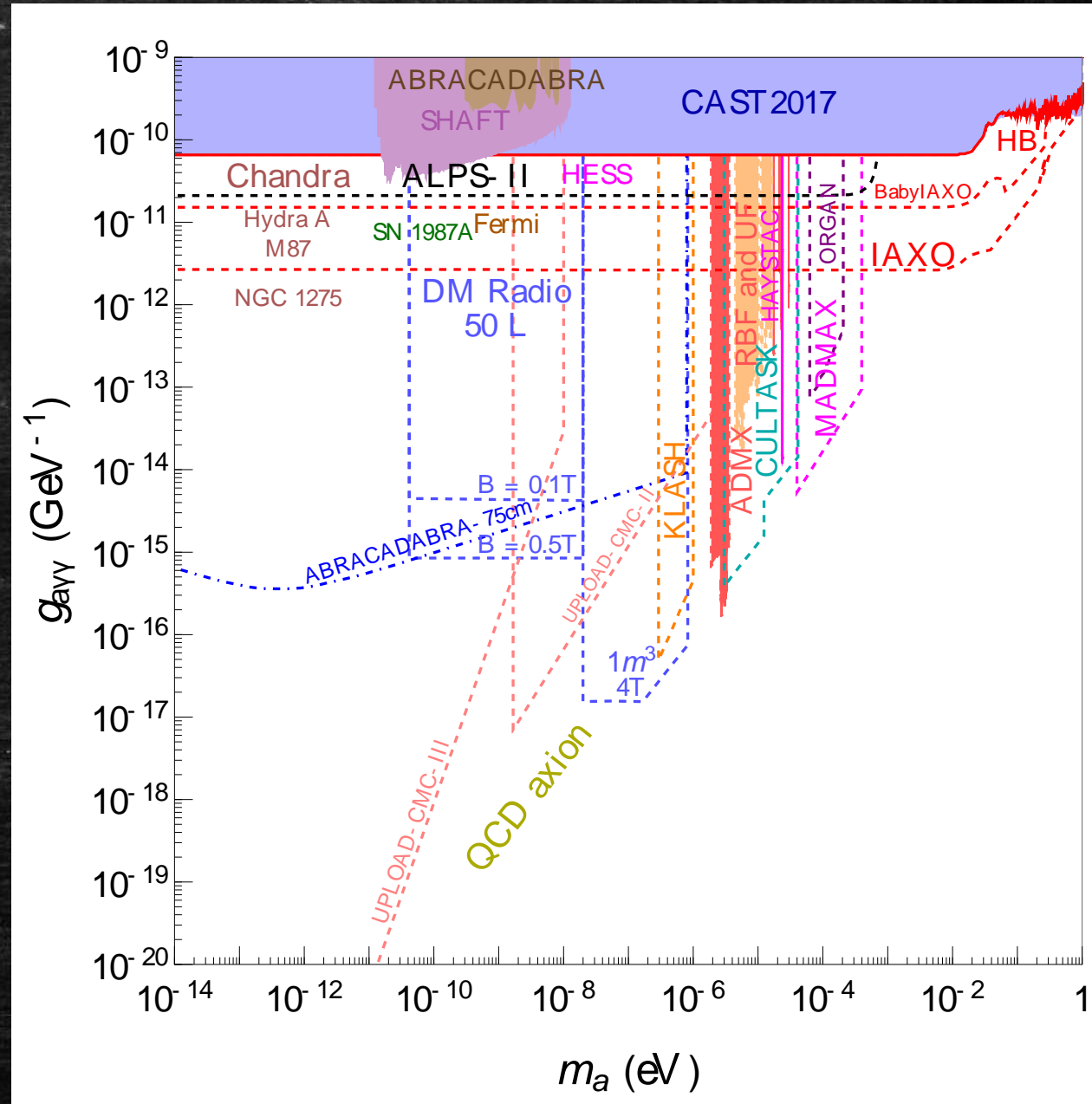
# Status of Axion Dark Matter

# Experimental Searches

## Experimental progress

shaded regions: excluded

broken lines: future sensitivities





# Axion Dark Matter Abundance

damped simple harmonic oscillator

Equation of motion: 
$$\left(\partial_t^2 + 3H\partial_t + m_a^2\right) a = 0$$

Hubble "friction"  
(from cosmic expansion)



# Axion Dark Matter Abundance

damped simple harmonic oscillator

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$$\left(\partial_t^2 + 3H\partial_t + m_a^2\right) a = 0$$

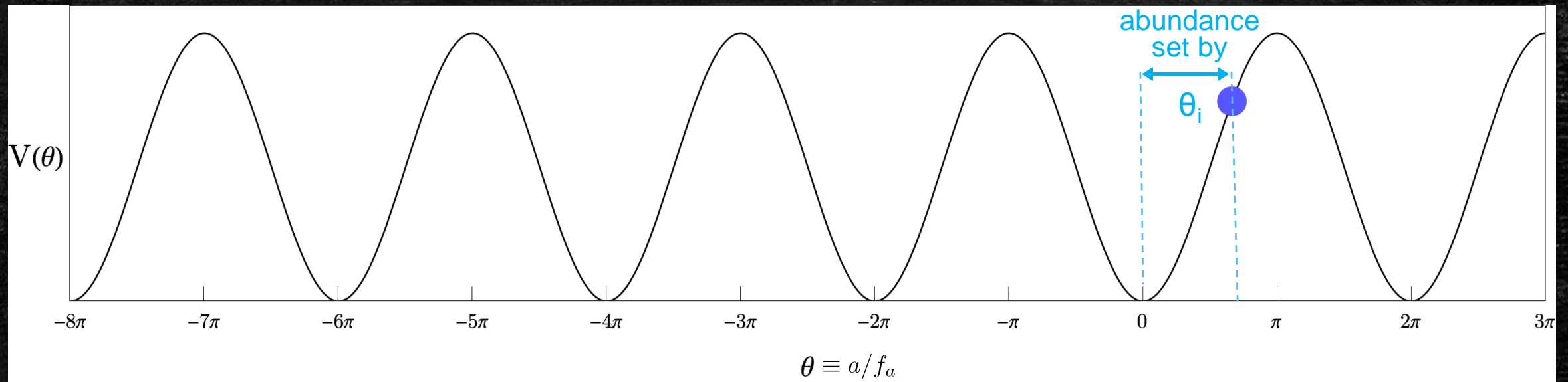
Hubble "friction"  
(from cosmic expansion)

## Misalignment Mechanism

Preskill, Wise, Wilczek 1983  
Abbott, Sikivie 1983  
Dine, Fischler 1983

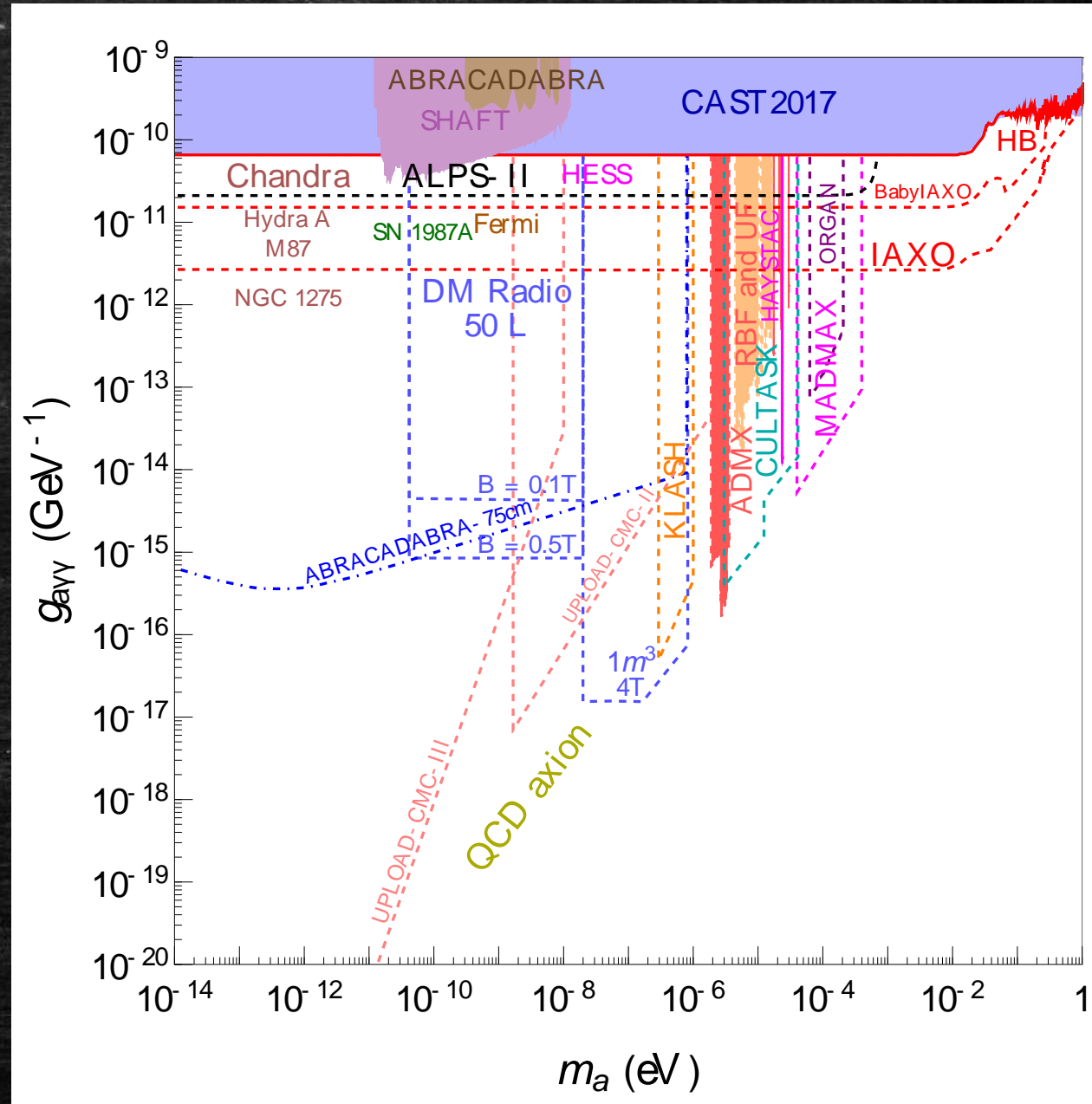
oscillations start when

$$H \lesssim m_a$$





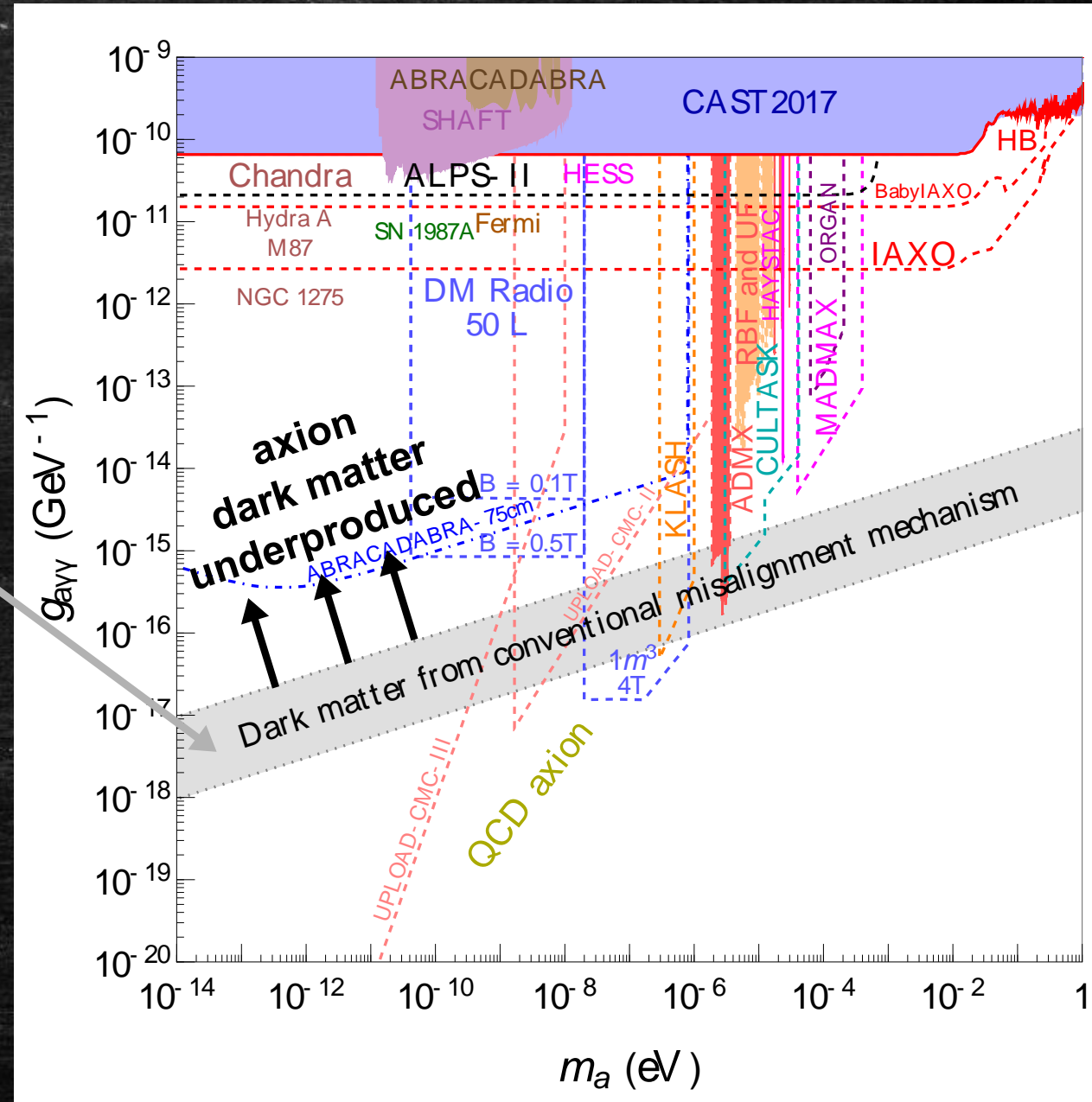
# Axion Dark Matter Abundance





# Axion Dark Matter Abundance

We assume  $\theta_i = \mathcal{O}(1)$  here.

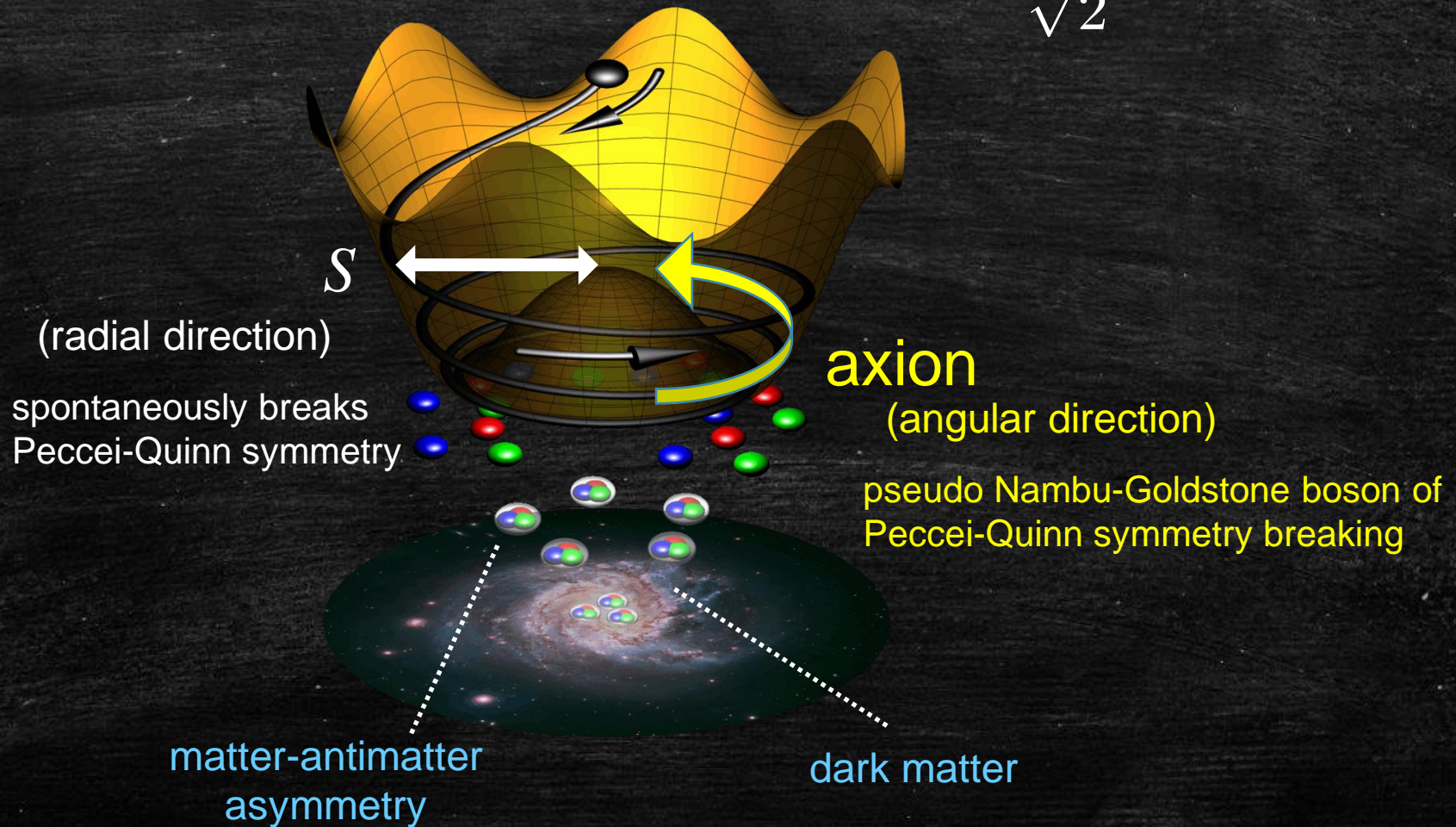




# Axion Rotation

$$\mathcal{L} \supset \frac{\alpha_s}{8\pi} \frac{a}{f_a} G_b^{\mu\nu} \tilde{G}_{b\mu\nu}$$

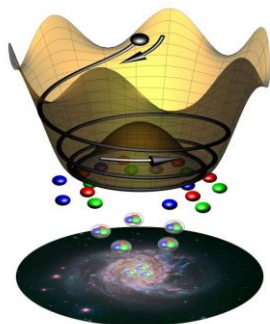
$$P = \frac{S + f_a}{\sqrt{2}} e^{i \frac{a}{f_a}}$$





## Paper sheds light on infant universe and origin of matter

10 March 2020



the School of Natural Sciences at the Institute for Advanced Study, and Raymond T. Co of the University of Michigan, have presented a compelling case in which the quantum chromodynamics (QCD) axion, first theorized in 1977, provides several important answers to these questions.

"We revealed that the rotation of the QCD axion can account for the excess of matter found in the universe," stated Harigaya. "We named this mechanism axiogenesis."

Infinitesimally light, the QCD axion—at least one billion times lighter than a proton—is nearly ghost-like. Millions of these particles pass through ordinary matter every second without notice. However, the subatomic level interaction of the QCD axion can still leave detectable signals in experiments with unprecedented sensitivities. While the QCD axion has never been directly detected, this study provides added fuel for experimentalists to hunt down the elusive particle.

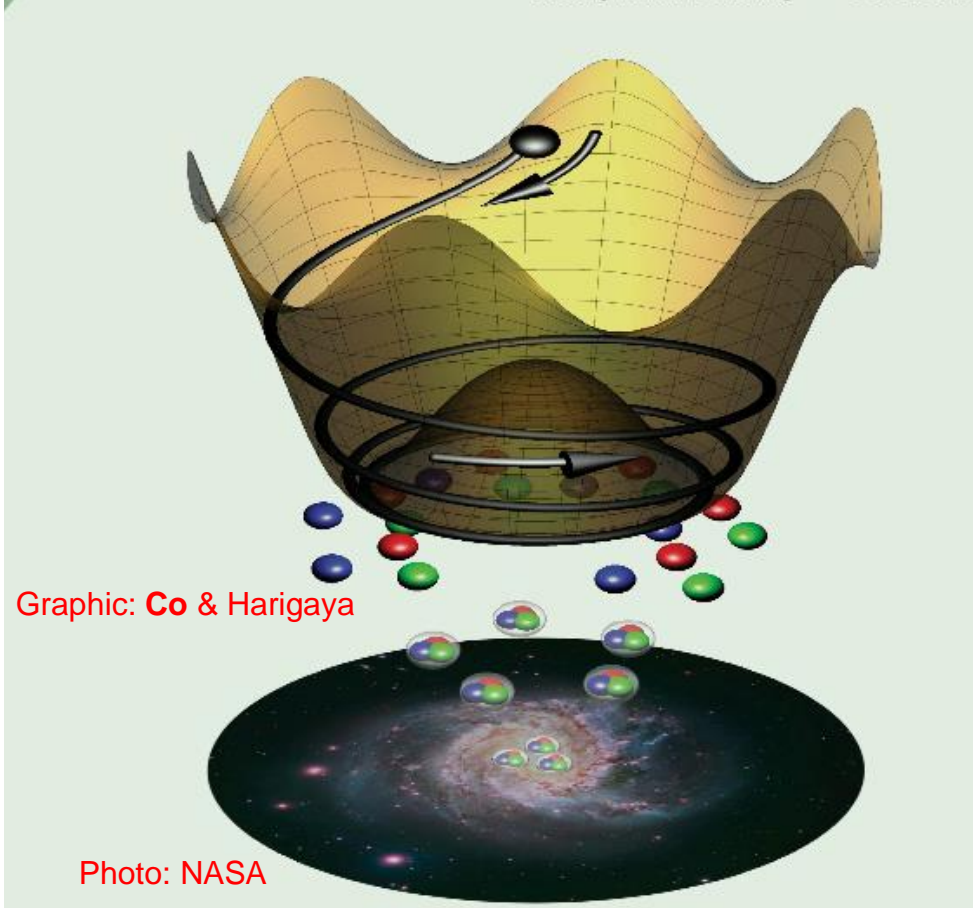
"The versatility of the QCD axion in solving the mysteries of fundamental physics is truly amazing," stated Co. "We are thrilled about the unexplored theoretical possibilities that this new aspect of the QCD axion can bring. More importantly, experiments may soon tell us whether the mysteries of nature truly hint towards the QCD axion."

Harigaya and Co have reasoned that the QCD axion is capable of filling three missing pieces of the physics jigsaw puzzle simultaneously. First, the QCD axion was originally proposed to explain the so-called strong CP problem—why the strong force, which binds protons and neutrons together, unexpectedly preserves a symmetry called the Charge Parity (CP) symmetry. The CP symmetry is inferred from the observation that a neutron does not react with an electric field despite its charged constituents. Second, the QCD axion was found to

A new study, conducted to better understand the origin of the universe, has provided insight into some of the most enduring questions in fundamental physics: How can the Standard Model of particle physics be extended to explain the cosmological excess of matter over antimatter? What is dark matter? And what is the theoretical origin of an unexpected but observed symmetry in the force that binds protons and neutrons together?

In the paper "Axiogenesis," scheduled to be published in *Physical Review Letters* on March 17, 2020, researchers Keisuke Harigaya, Member in

Articles published week ending 20 MARCH 2020



Graphic: Co & Harigaya

Photo: NASA

Quanta magazine | Physics Mathematics Bio

ABSTRACTS BLOG

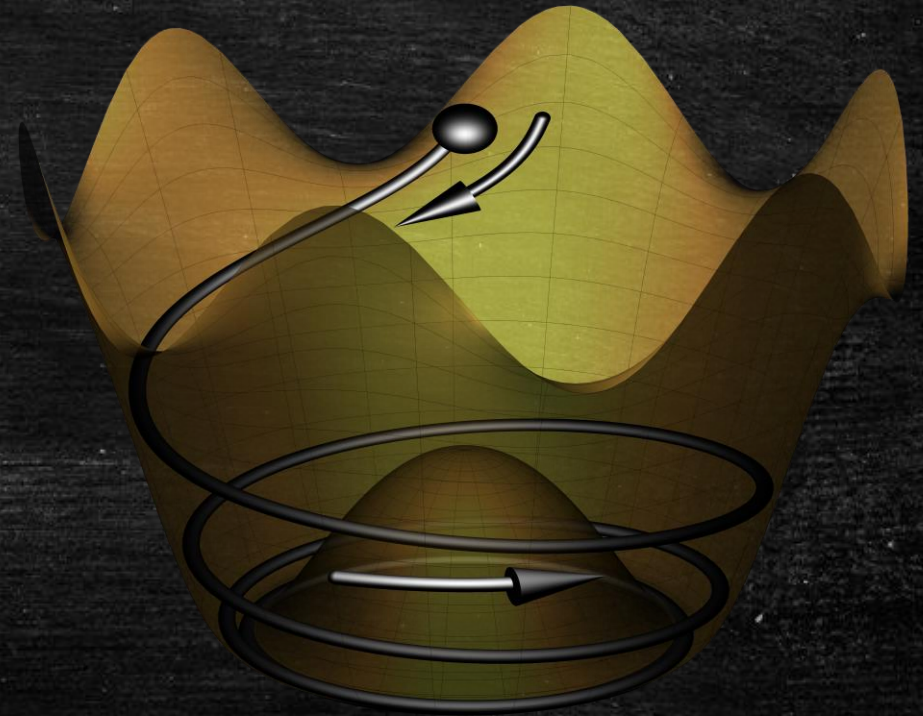
## Axions Would Solve Another Major Problem in Physics

In a new paper, physicists argue that hypothetical particles called axions could explain why the universe isn't empty.



# Why Rotation?

$$P = \frac{S + f_a}{\sqrt{2}} e^{i \frac{a}{f_a}}$$



Dynamics analogous to that in Affleck-Dine baryogenesis

I. Affleck and M. Dine 1991

PRL 92, 011301 (2004) T. Chiba, F. Takahashi, M. Yamaguchi  
PRL 124, 111602 (2020) RC and K. Harigaya



# Why Rotation?

Wiggles :

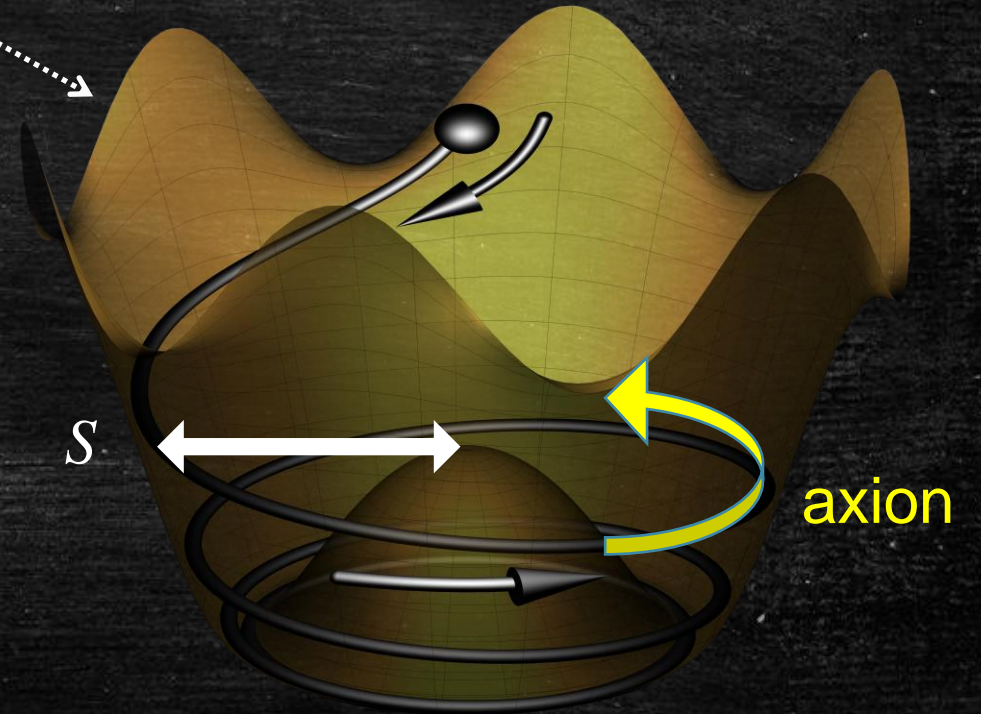
$$V(P) \sim \frac{P^n}{M^{n-4}} e^{i\varphi} + \text{h.c.} \sim \frac{|P|^n}{M^{n-4}} \cos\left(n \frac{a}{f_a} + \varphi\right)$$

$$P = \frac{S + f_a}{\sqrt{2}} e^{i \frac{a}{f_a}}$$

Explicit PQ breaking

expected from quantum gravity  
or PQ as an accidental symmetry

S. Giddings et al. 1988  
S. Coleman 1988  
G. Gilbert 1988



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# Why Rotation?

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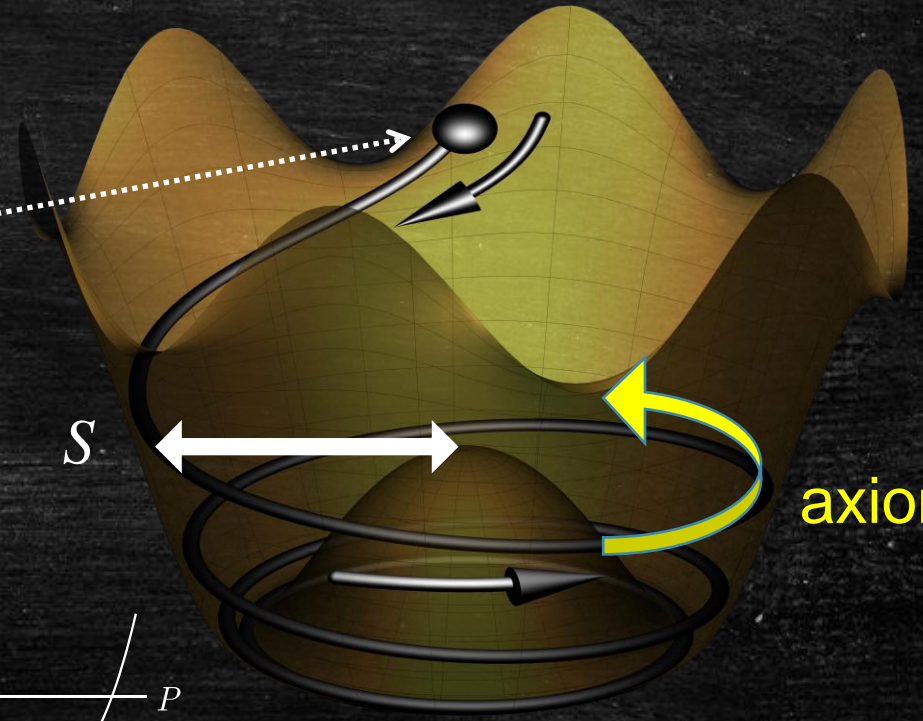
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Explicit PQ breaking

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S. Coleman 1988  
G. Gilbert 1988



Large field value :

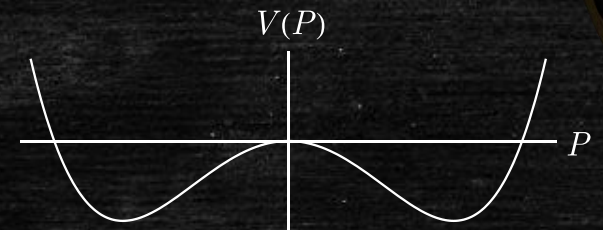
Flat potential

For example, as an initial condition or  
set dynamically by inflationary dynamics

$$V(|P|) \sim -H_I^2 |P|^2 + \frac{|P|^d}{M^{d-4}}$$

Hubble-induced mass

M. Dine, L. Randall, and S. D. Thomas 1991



Dynamics analogous to that in Affleck-Dine baryogenesis

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# Asymmetry of PQ Charge

Noether charge associated with the shift symmetry

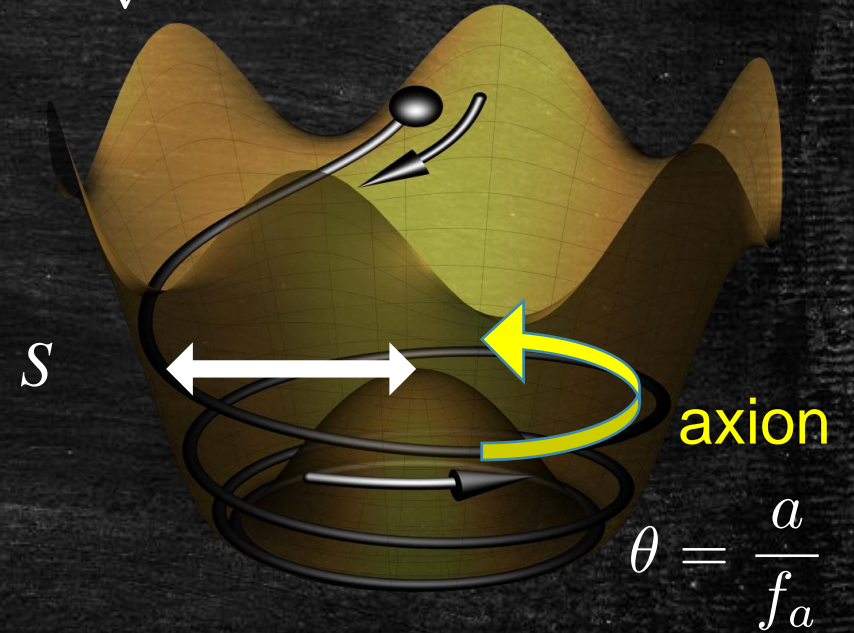
$$n_\theta = S^2 \dot{\theta}$$

this is nothing but  
"angular momentum"  $r^2 \omega$

$$P = \frac{S + f_a}{\sqrt{2}} e^{i \frac{a}{f_a}}$$

PQ asymmetry  
PQ charge density = Rotation of PQ field

This is conserved soon after the initial kick.



$$\theta = \frac{a}{f_a}$$



# Asymmetry of PQ Charge

Noether charge associated with the shift symmetry

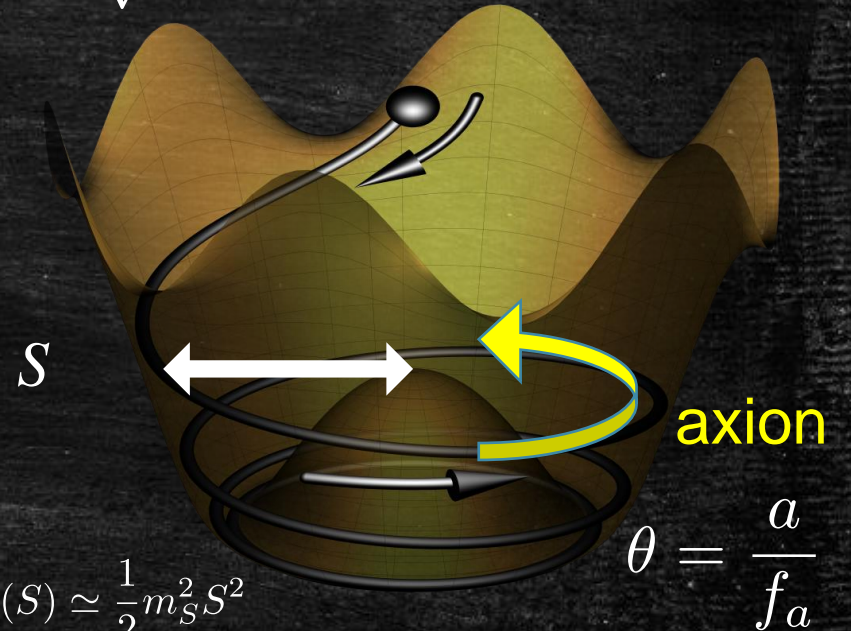
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PQ asymmetry  
PQ charge density = Rotation of PQ field

This is conserved soon after the initial kick.



What determines  $\dot{\theta}$ ? Centripetal force!

$$F_c = m a_c$$

$$V'(S) = S \dot{\theta}^2$$

$$m_S^2 S = S \dot{\theta}^2$$

$$V(S) \simeq \frac{1}{2} m_S^2 S^2$$

from supersymmetry

$$\theta = \frac{a}{f_a}$$

$\dot{\theta} = m_S$  which is in turn set by supersymmetry scale.



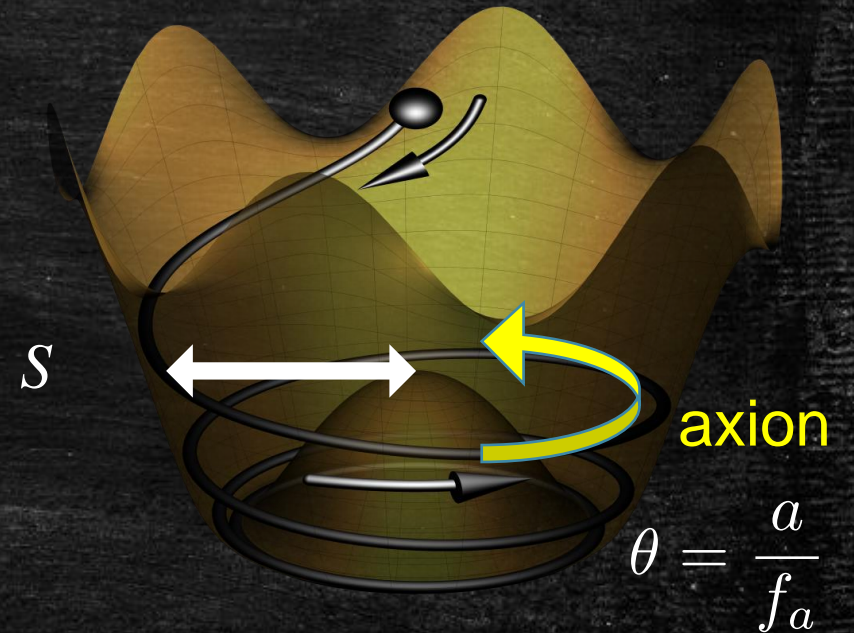
# PQ Charge Evolution

Charge conservation:

$$n_\theta = S^2 \dot{\theta} \propto \frac{R^{-3}}{S}$$

scale factor of the universe

dilution due to cosmic expansion





# PQ Charge Evolution

Charge conservation:

$$n_\theta = S^2 \dot{\theta} \propto \frac{R^{-3}}{\text{scale factor of the universe}}$$

Large field ( $S \gg f_a$ ):

$$S^2 \propto R^{-3}$$

for quadratic potential  
 $V(S) \simeq \frac{1}{2} m_S^2 S^2$

$$\dot{\theta} = \text{constant}$$

$$\rho_\theta = \dot{\theta}^2 S^2 \propto R^{-3}$$

matter

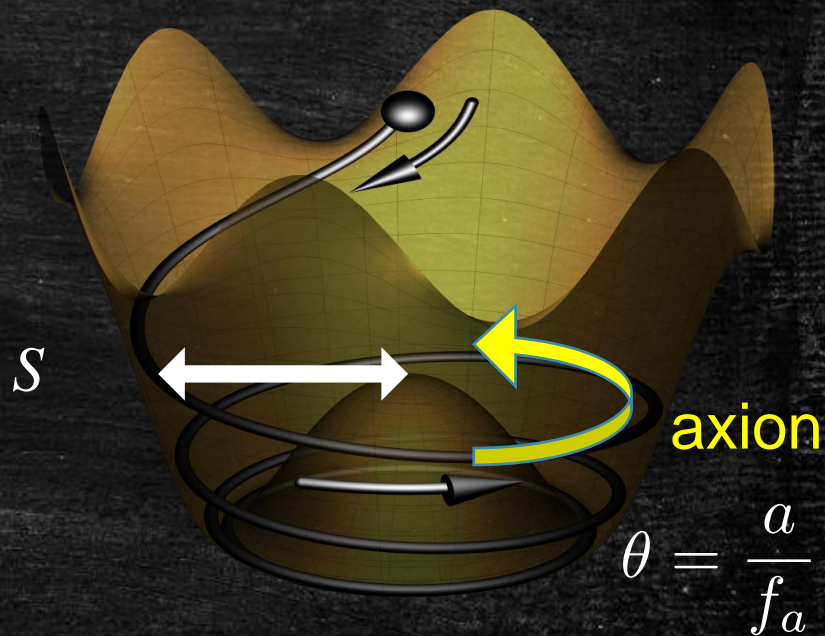
At the minimum:

$$S^2 = f_a^2$$

$$\dot{\theta} \propto R^{-3}$$

$$\rho_\theta = \dot{\theta}^2 f_a^2 \propto R^{-6}$$

kination





# Asymmetries in Thermal Equilibrium

The free energy is minimized at equilibrium.

fermion asymmetry

$$n_\psi \equiv n_{+\mu} - n_{-\mu} \sim \mu T^2$$

Change of the free energy

$$\Delta F_{\text{th}} \sim \Delta\rho - T\Delta s \sim \frac{n_\psi^2}{T^2}$$

$$\Delta F_{\text{rot}} \sim -\dot{\theta} n_\psi$$

$$\Delta F_{\text{tot}} \text{ is minimized when } n_\psi \sim \underline{\underline{\dot{\theta} T^2}} \ll \dot{\theta} S^2 = n_{\text{PQ}}$$

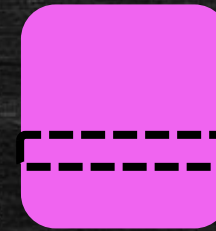
Most of the PQ charge remains in the rotation!

thermal bath

$$n_{\text{th}} \simeq T^3$$

rotation

$$n_{\text{PQ}} = \dot{\theta} S^2$$



$$n_\psi \simeq \dot{\theta} T^2$$

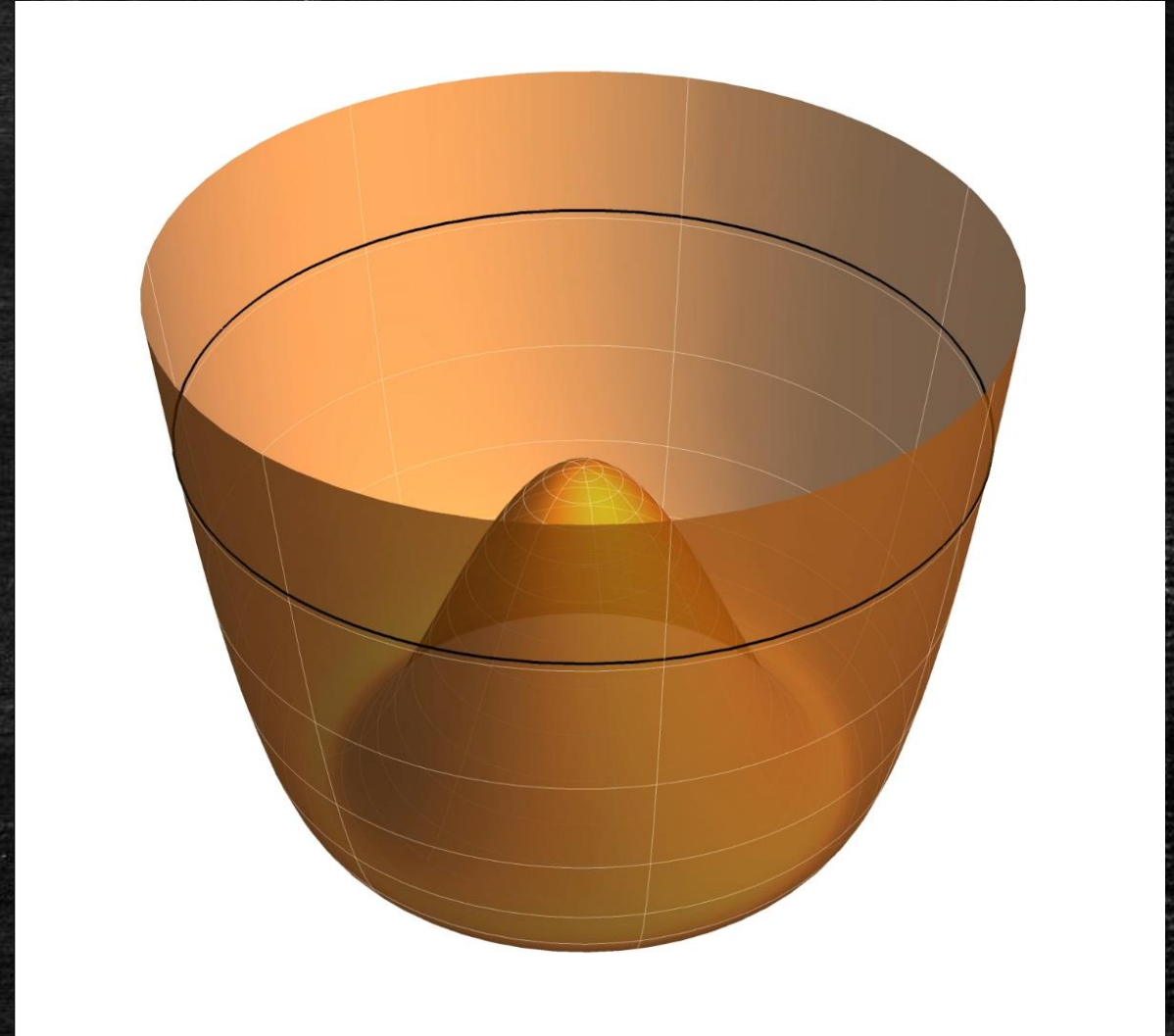
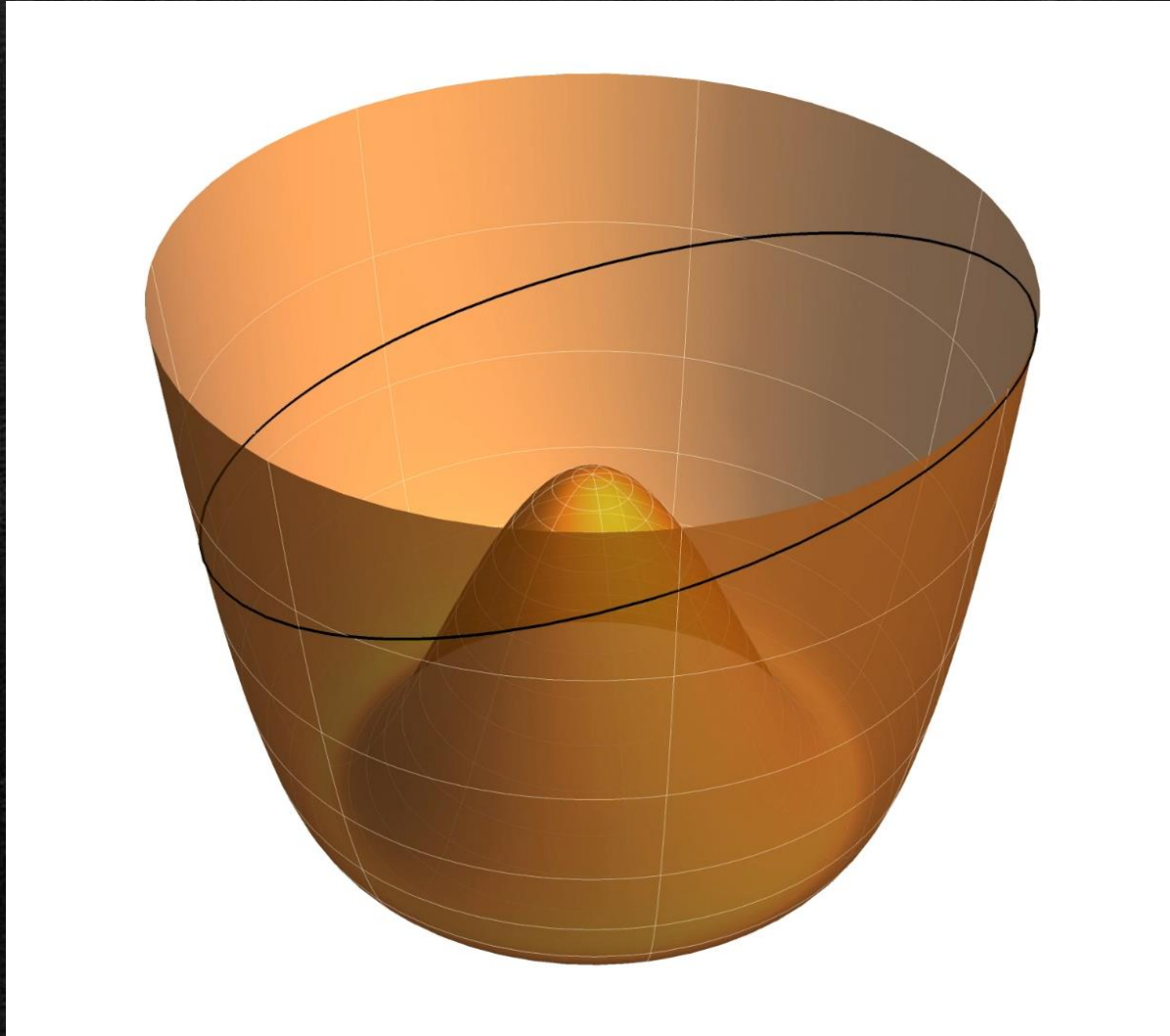


# Asymmetries in Thermal Equilibrium

Thermalization

$$n_{\text{PQ}} = S^2 \dot{\theta}$$

Redshift



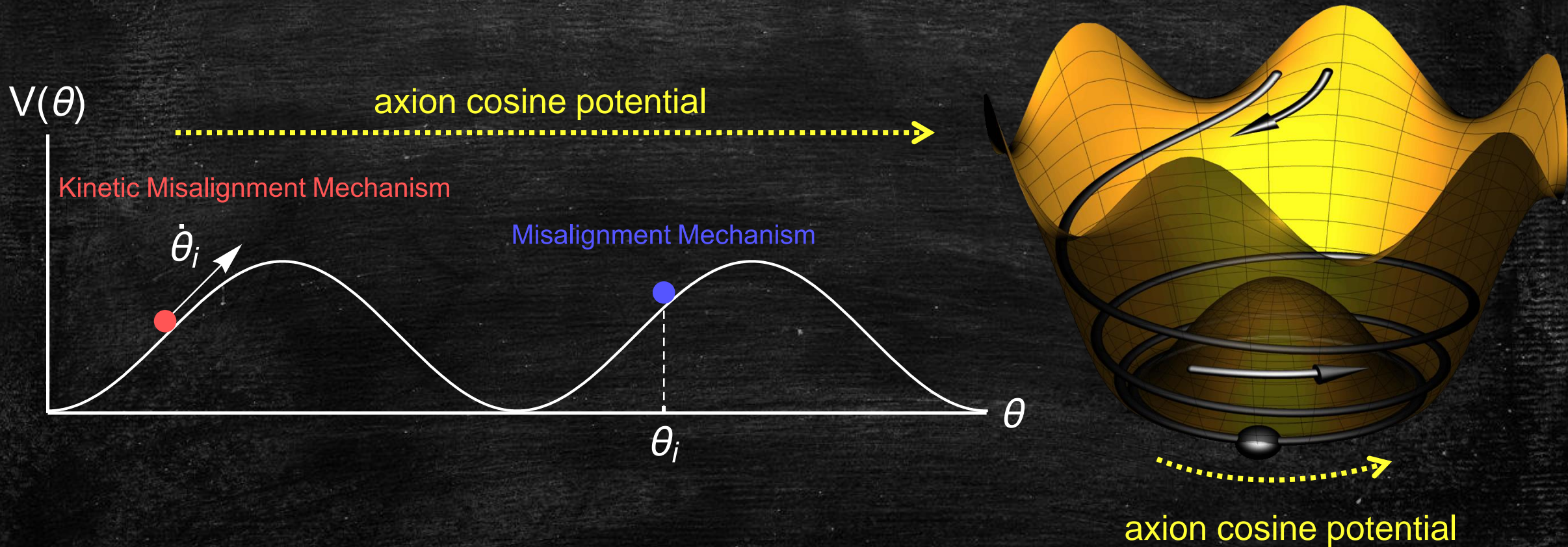


# Axion Dark Matter



# Kinetic Misalignment Mechanism

a novel scenario where the axion field has a nonzero initial velocity, e.g., from axion rotations.

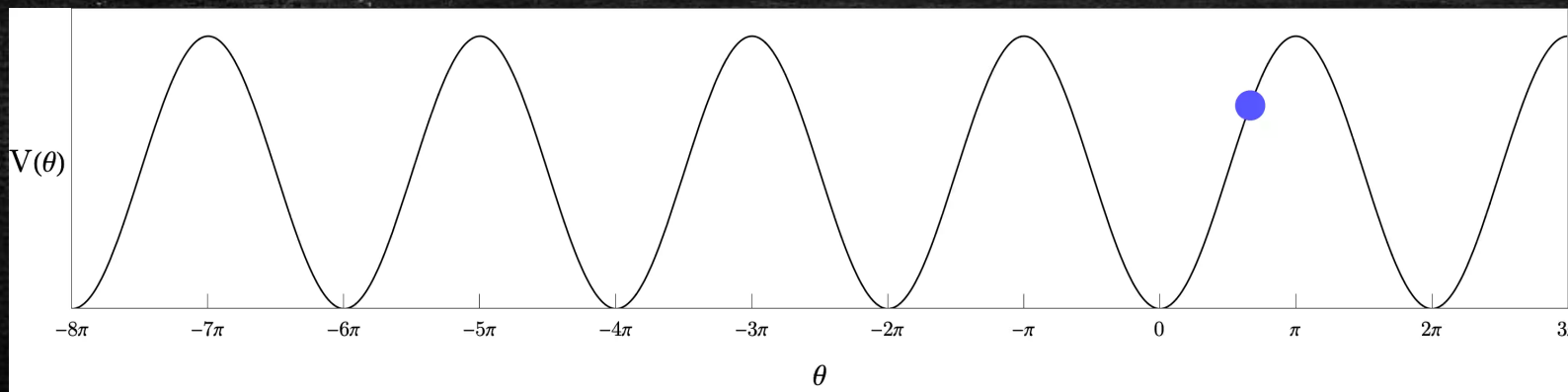




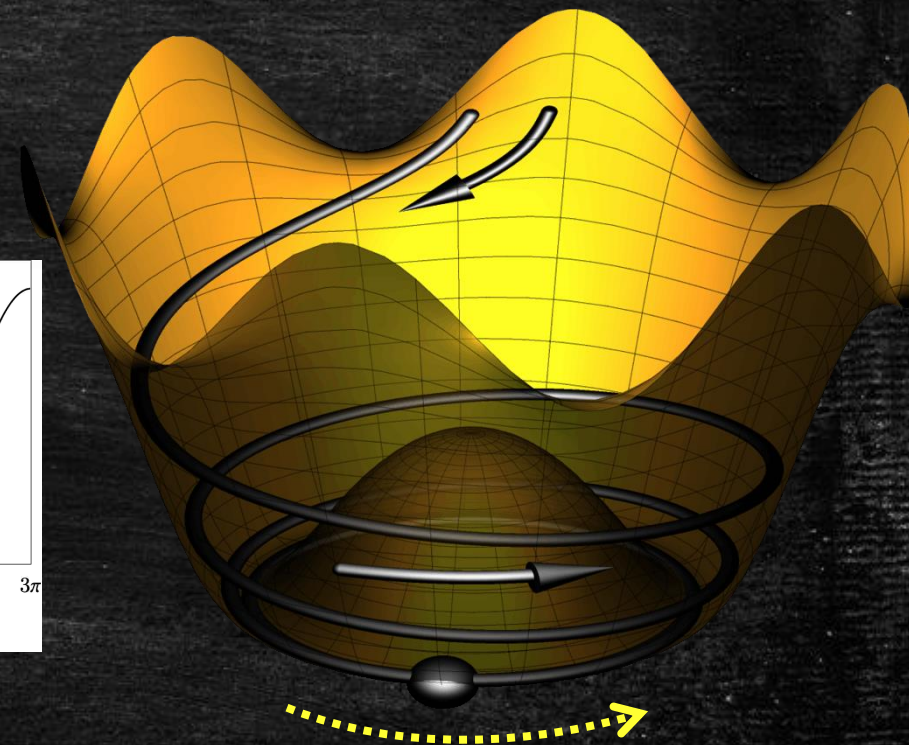
# Kinetic Misalignment Mechanism

a novel scenario where the axion field has a nonzero initial velocity, e.g., from axion rotations.

axion cosine potential



kinetic energy > potential energy  
enhancing axion abundance

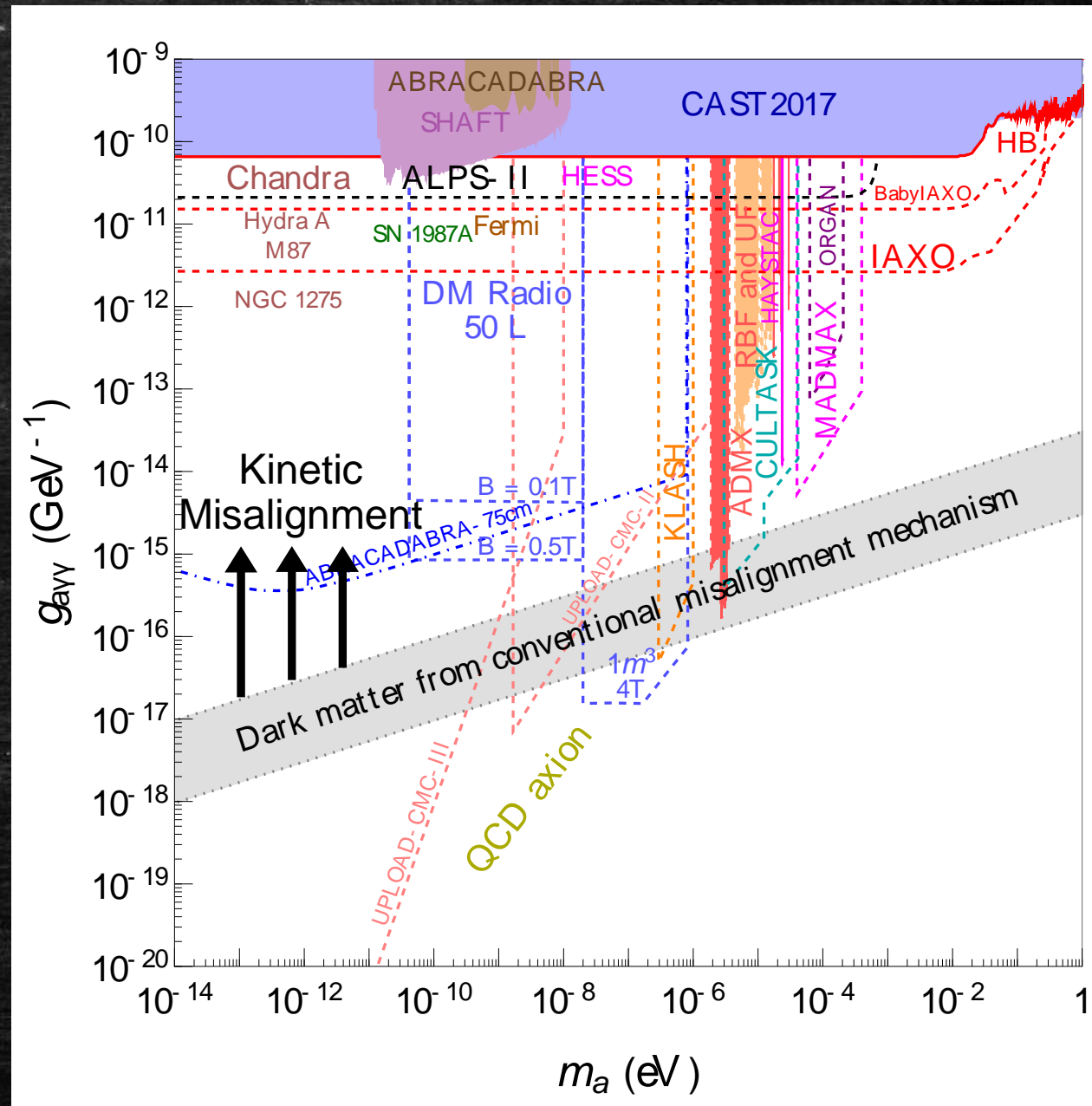


axion cosine potential



# Kinetic Misalignment Mechanism

giving a strong motivation for axion dark matter experiment





# Kinetic Misalignment Mechanism

Kinetic Misalignment\*

charge yield

$$Y_\theta = \frac{n_\theta}{s}$$

$$\frac{\rho_a}{s} \simeq m_a Y_\theta$$

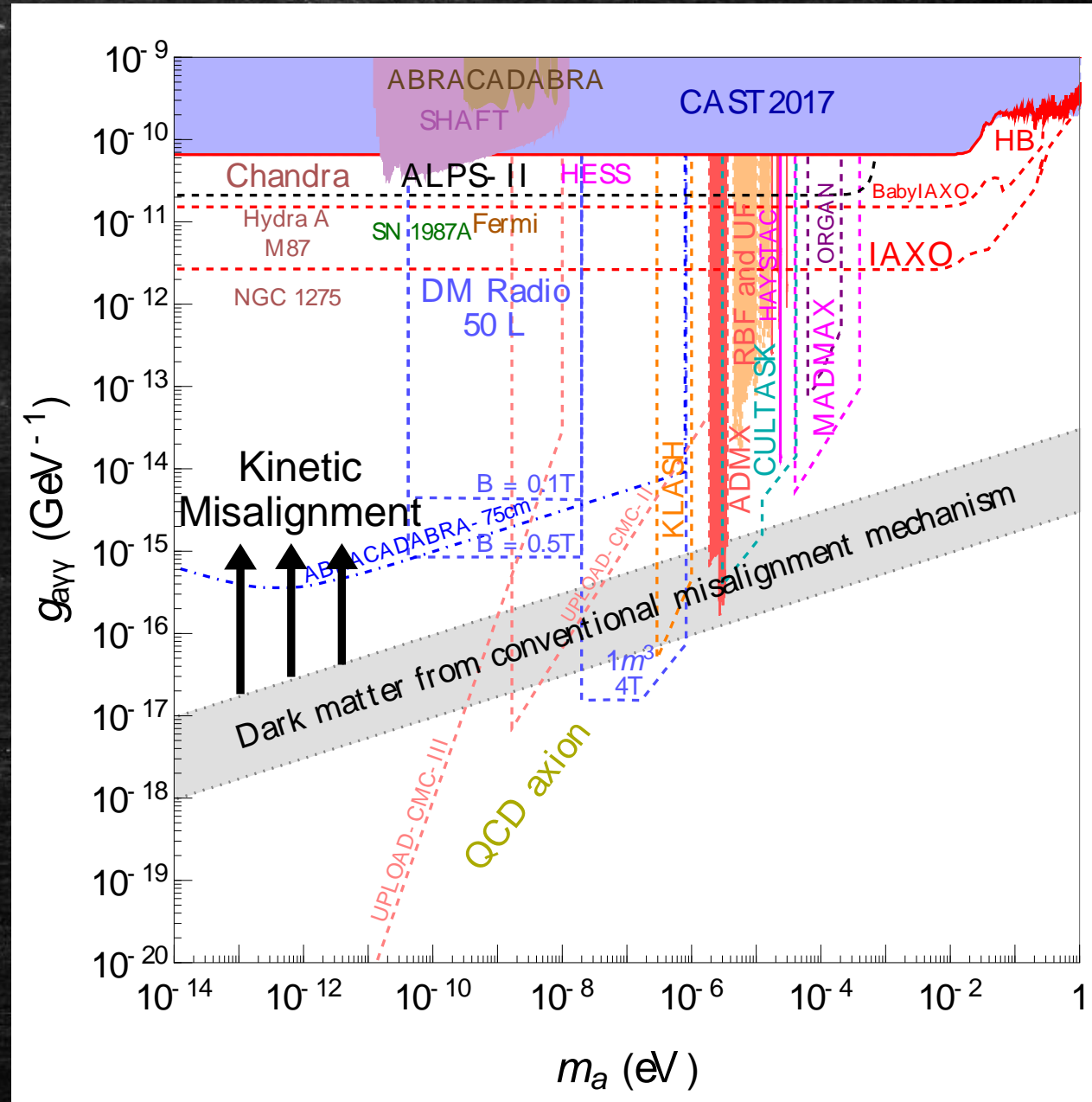
abundance

Observed dark matter abundance

$$\frac{\rho_{\text{DM}}}{s} \simeq 0.44 \text{ eV} \quad (\text{Planck 2018})$$

Thus, dark matter relates

$$m_a \overset{\text{DM}}{\longleftrightarrow} Y_\theta$$





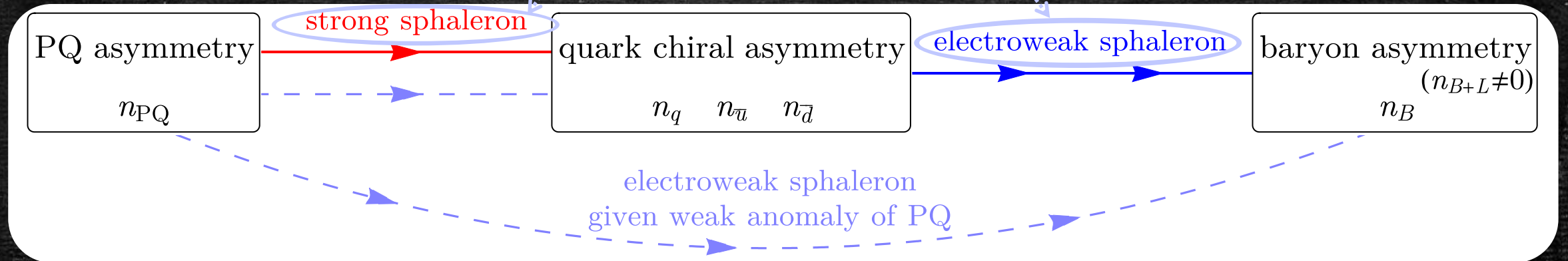
# Baryon Asymmetry



# Axiogenesis

Baryogenesis is automatic, thanks to Standard Model processes  
(production of baryon asymmetry)

matter-antimatter asymmetry



$$Y_B \equiv \frac{n_B}{s} = c_B Y_\theta \left( \frac{T_{EW}}{f_a} \right)^2$$

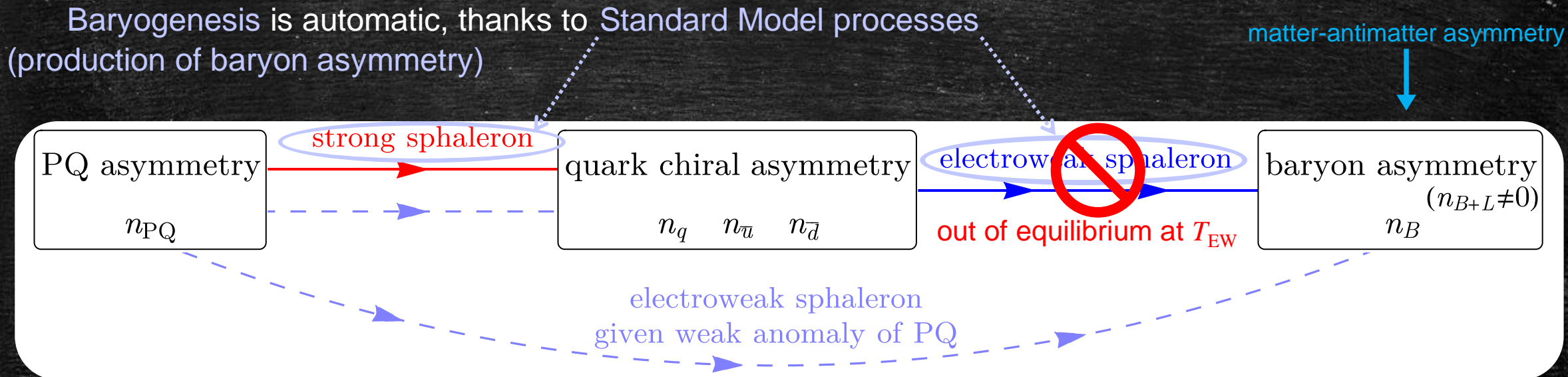
produced by axion rotations

$$Y_B^{\text{obs}} \simeq 8.7 \times 10^{-11}$$

experimentally measured value  
(Planck 2018)



# Axiogenesis



$$Y_B \equiv \frac{n_B}{s} = c_B Y_\theta \left( \frac{T_{\text{EW}}}{f_a} \right)^2 \quad Y_B^{\text{obs}} \simeq 8.7 \times 10^{-11}$$

Namely, the baryon asymmetry relates

$$\left( \frac{T_{\text{EW}}}{f_a} \right)^2 \xleftrightarrow{Y_B} Y_\theta$$

experimentally measured value (Planck 2018)



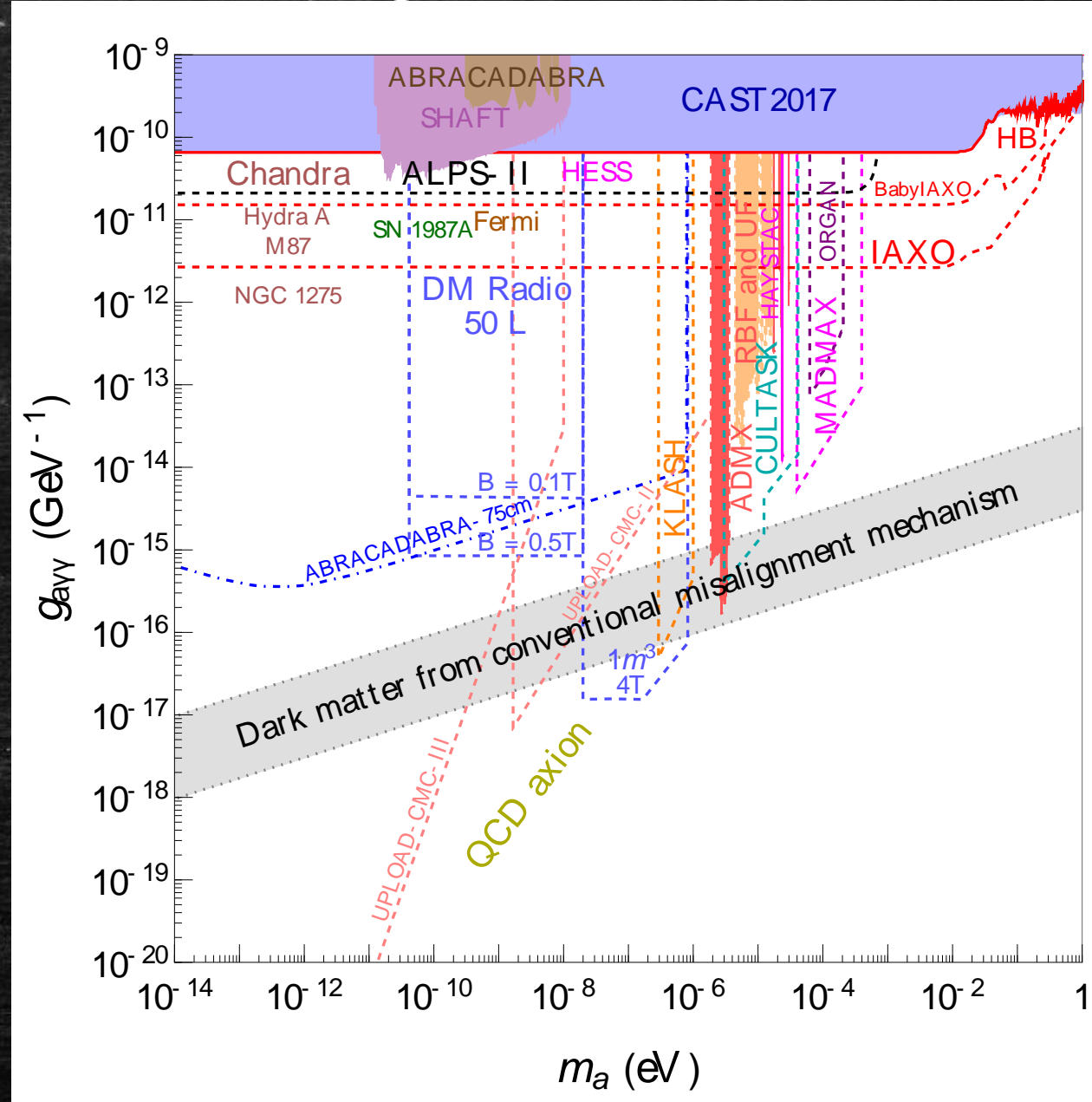
# Axion/ALP Cogenesis



# Kinetic Misalignment + Axiogenesis

Prediction:

$$m_a \xleftrightarrow{\text{DM}} Y_\theta \xleftrightarrow{Y_B} \left( \frac{T_{\text{EW}}}{f_a} \right)^2$$





# Kinetic Misalignment + Axiogenesis

Prediction:

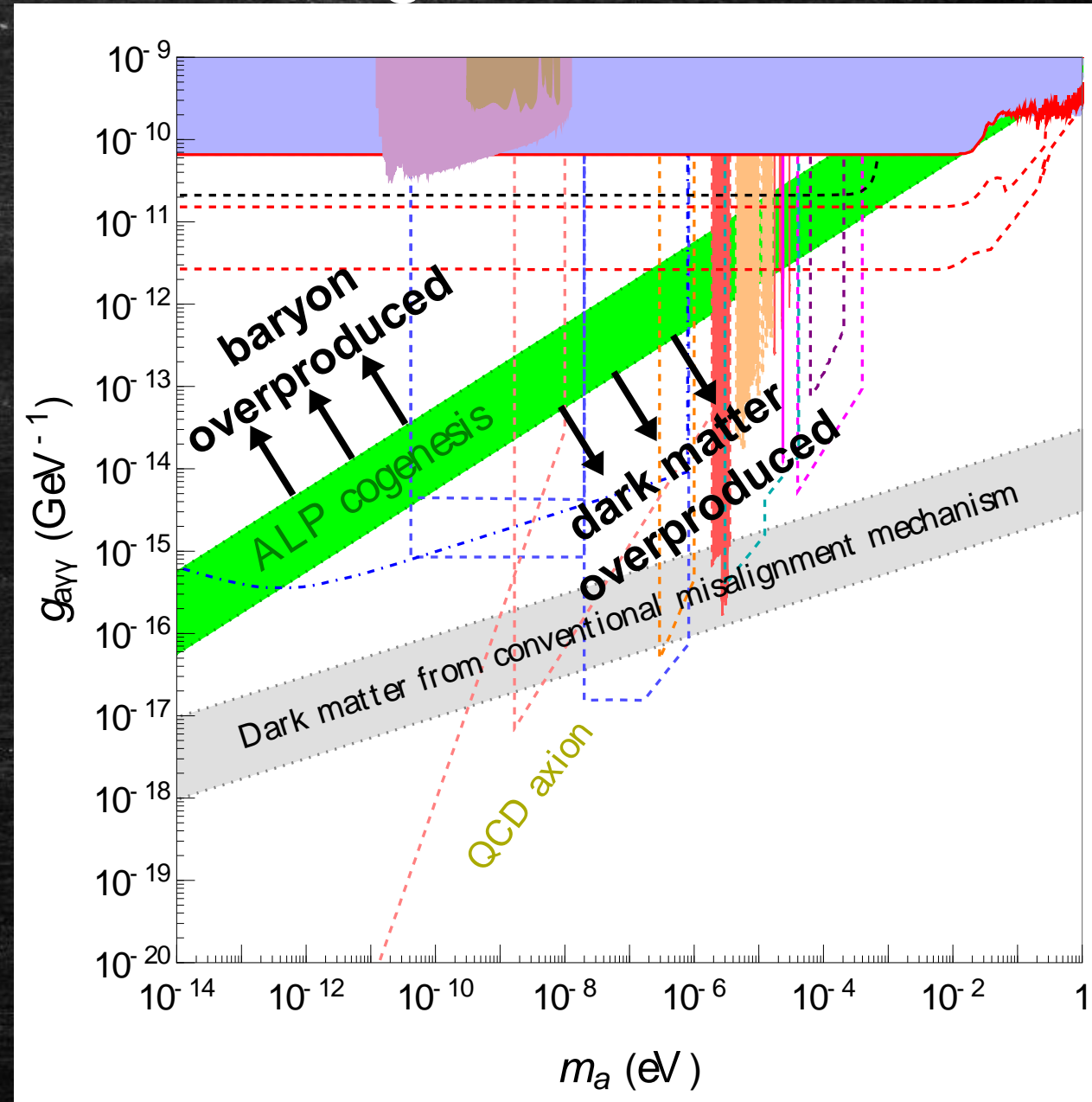
$$m_a \xleftrightarrow{\text{DM}} Y_\theta \xleftrightarrow{Y_B} \left( \frac{T_{\text{EW}}}{f_a} \right)^2$$

ALPogenesis :

ALP = axion-like particle  
(no gluon coupling)  
cogenesis

= production of both dark matter  
& matter-antimatter asymmetry

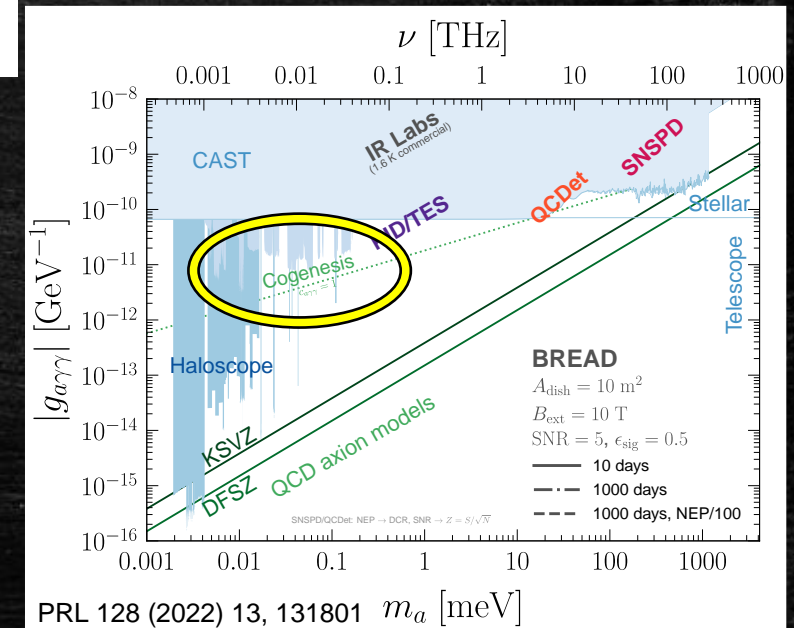
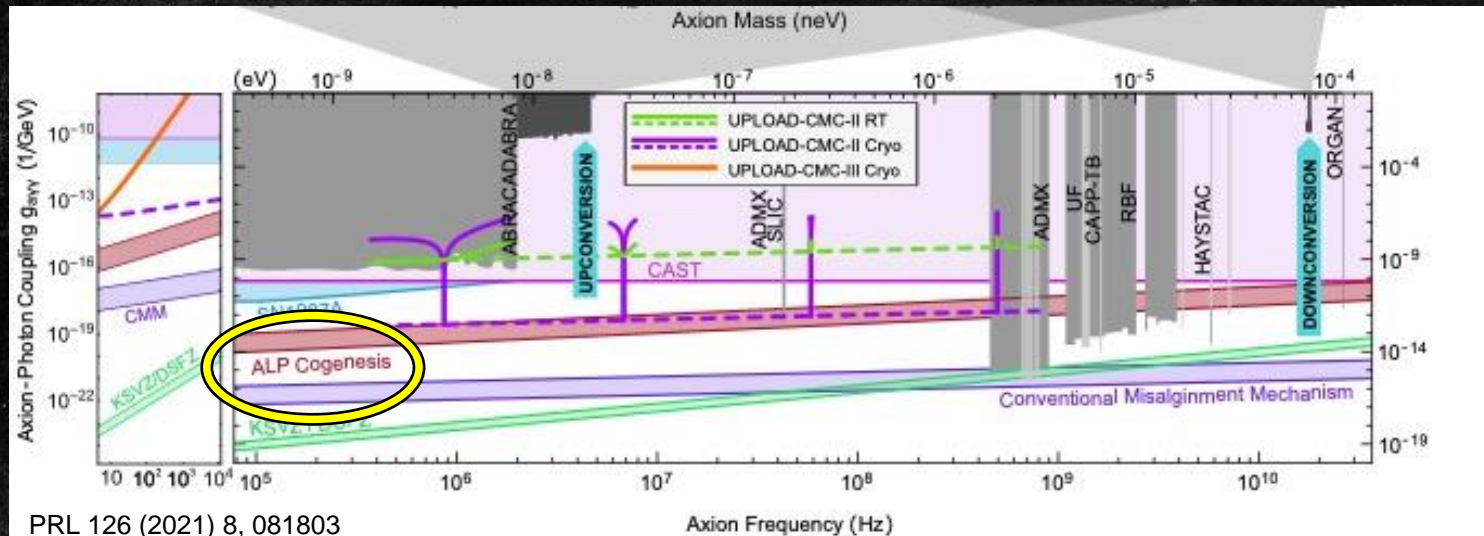
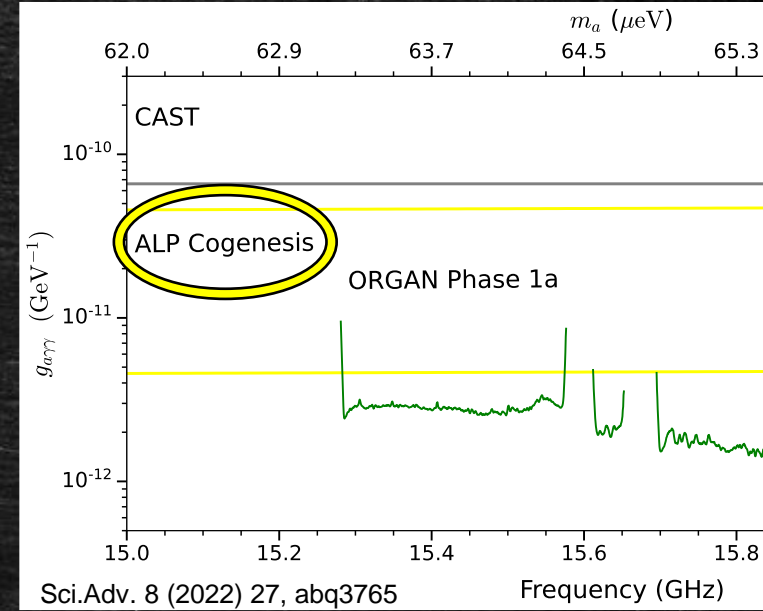
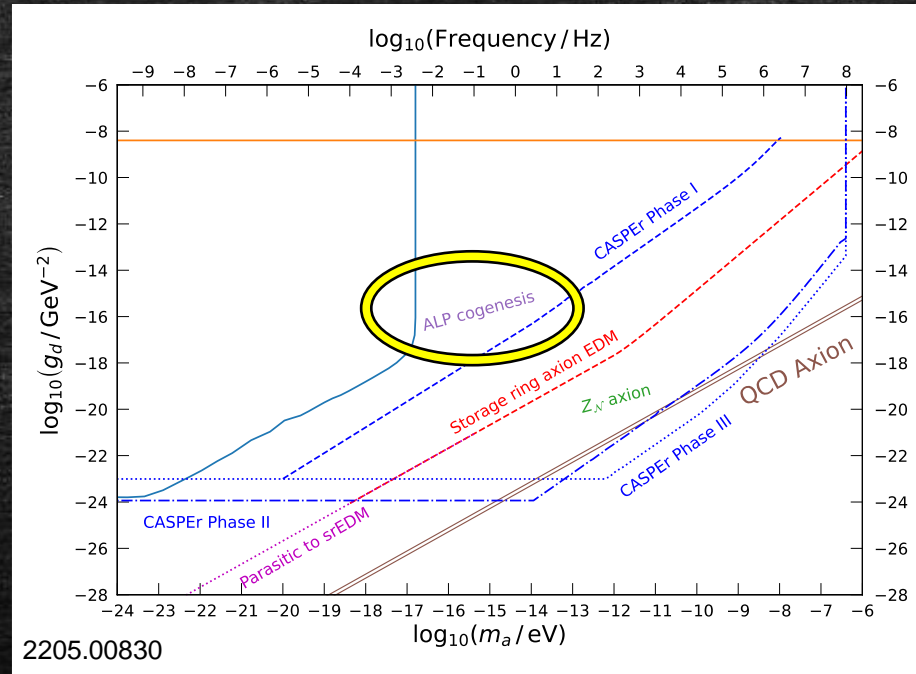
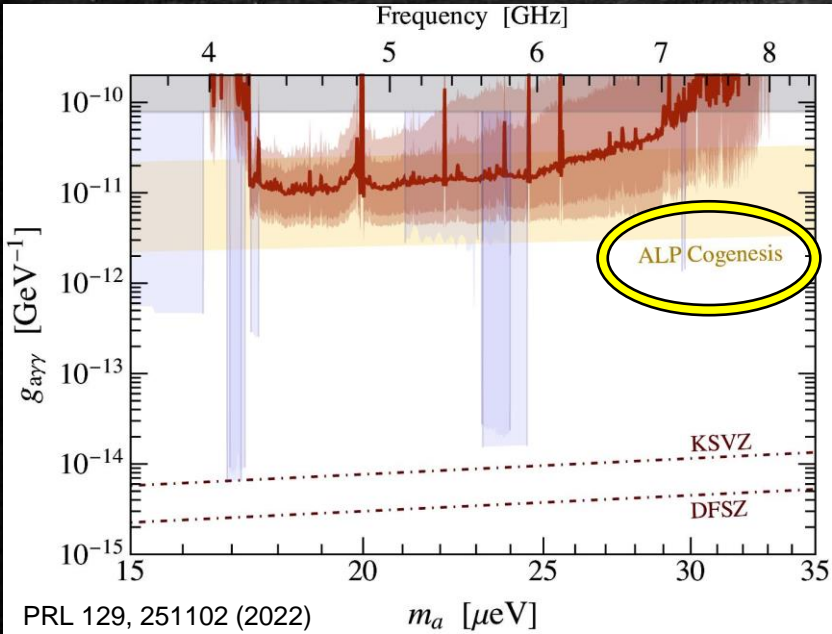
We assume  $T_{\text{EW}} = 130 \text{ GeV}$ .





# ALP Cogenesis

Experimental probes are happening!





# Kinetic Misalignment + Axiogenesis

Prediction:

$$m_a \xleftrightarrow{\text{DM}} Y_\theta \xleftrightarrow{Y_B} \left( \frac{T_{\text{EW}}}{f_a} \right)^2$$

ALPogenesis :

ALP = axion-like particle  
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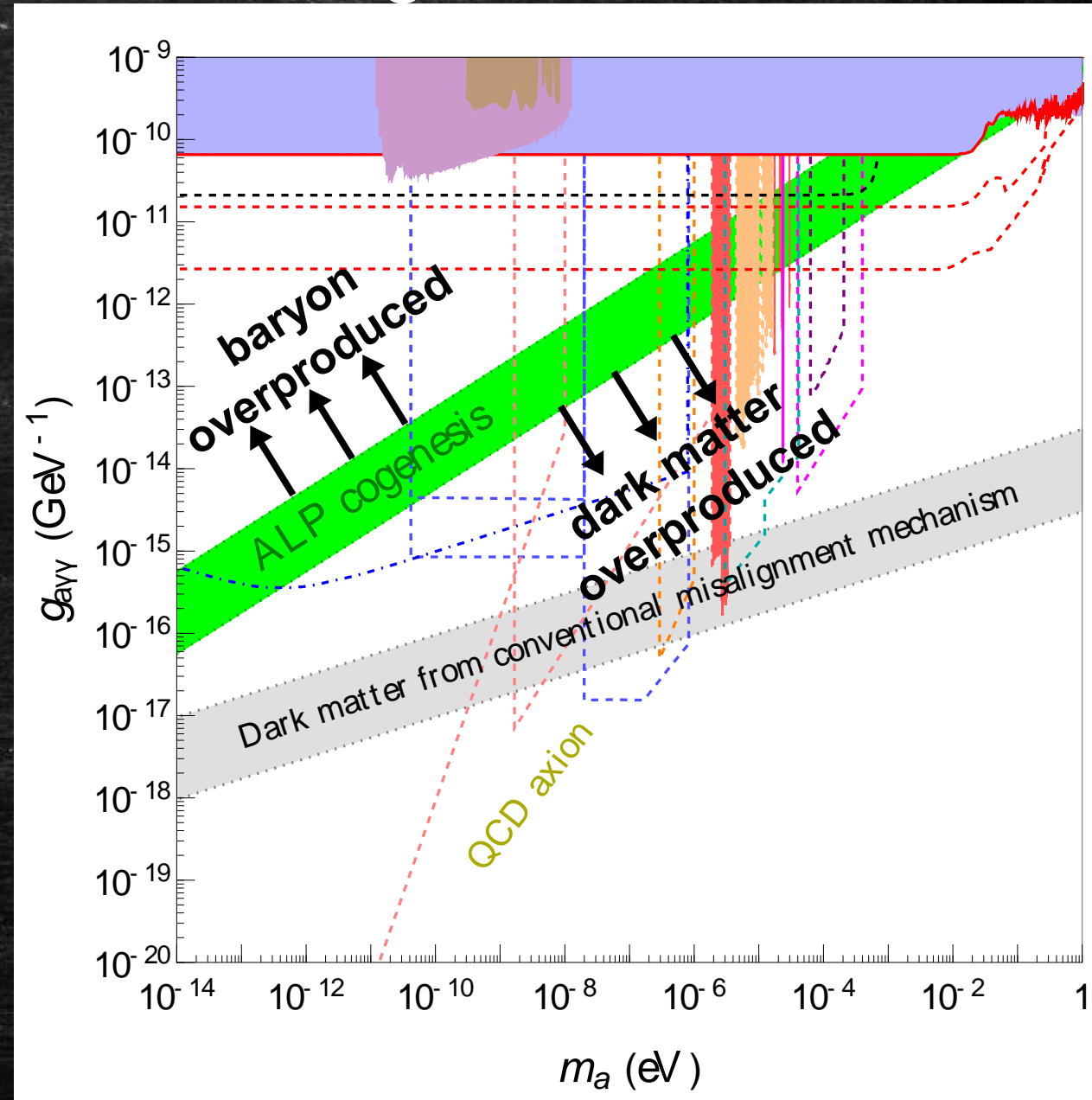
= production of both dark matter  
& matter-antimatter asymmetry

We assume  $T_{\text{EW}} = 130 \text{ GeV}$ .

QCD axion cogenesis?

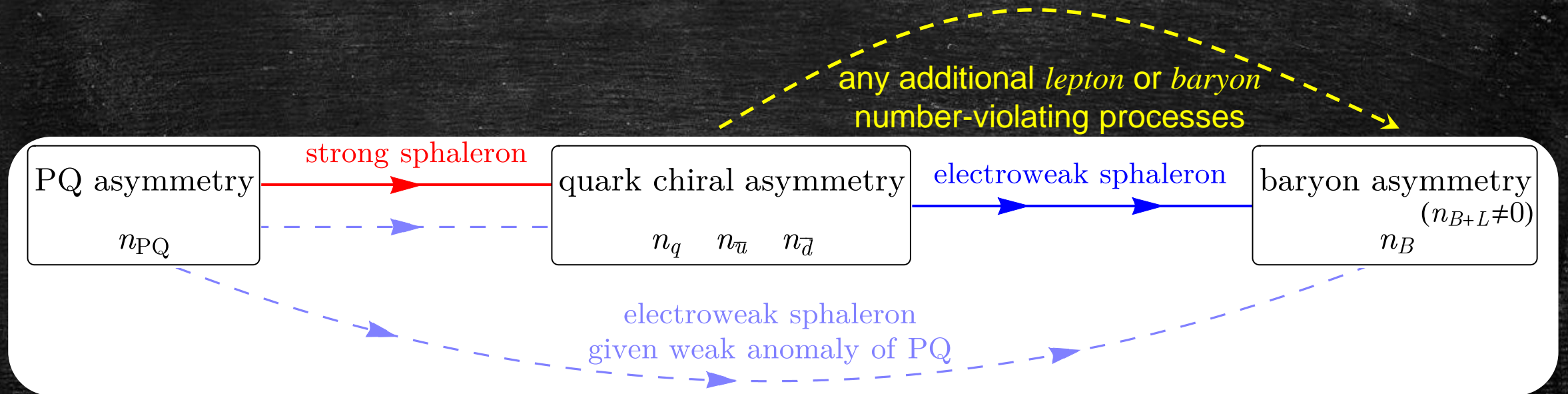
Can the QCD axion be compatible  
with cogenesis from axion rotations?

Yes. This is a great opportunity to bring  
other open questions into the picture!



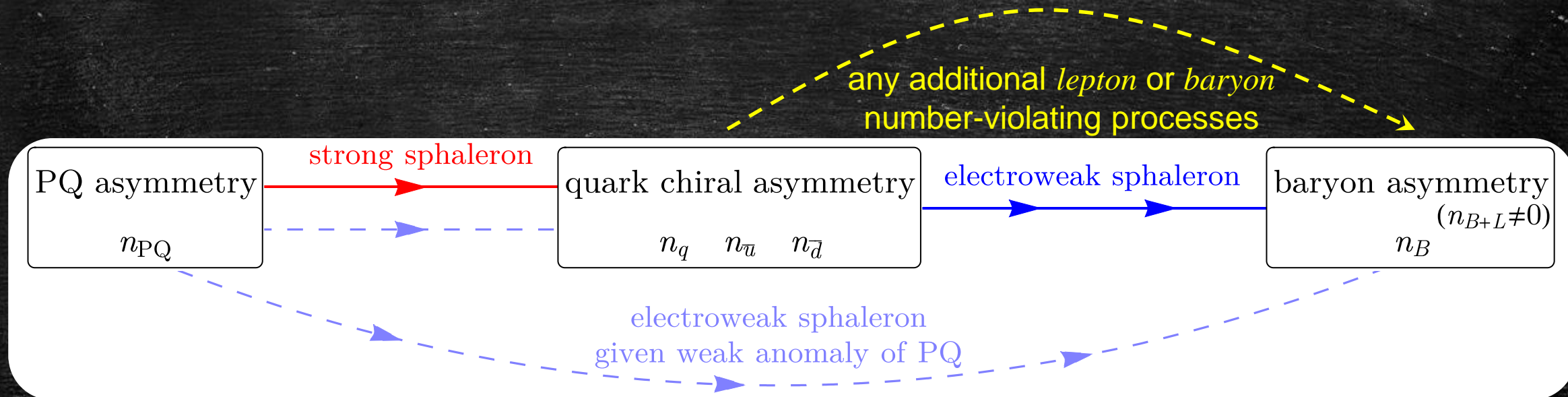


# Extensions of Axiogenesis





# Extensions of Axiogenesis



## Lepto-Axiogenesis

$$\mathcal{L} \supset \frac{m_\nu}{2v_{EW}^2} \ell \ell H^\dagger H^\dagger$$

e.g., from the seesaw mechanism,  
or the Zee-Babu model

This Weinberg operator gives Majorana neutrino masses,  
breaks lepton number, and thus affects the charge transfer.

## other extensions

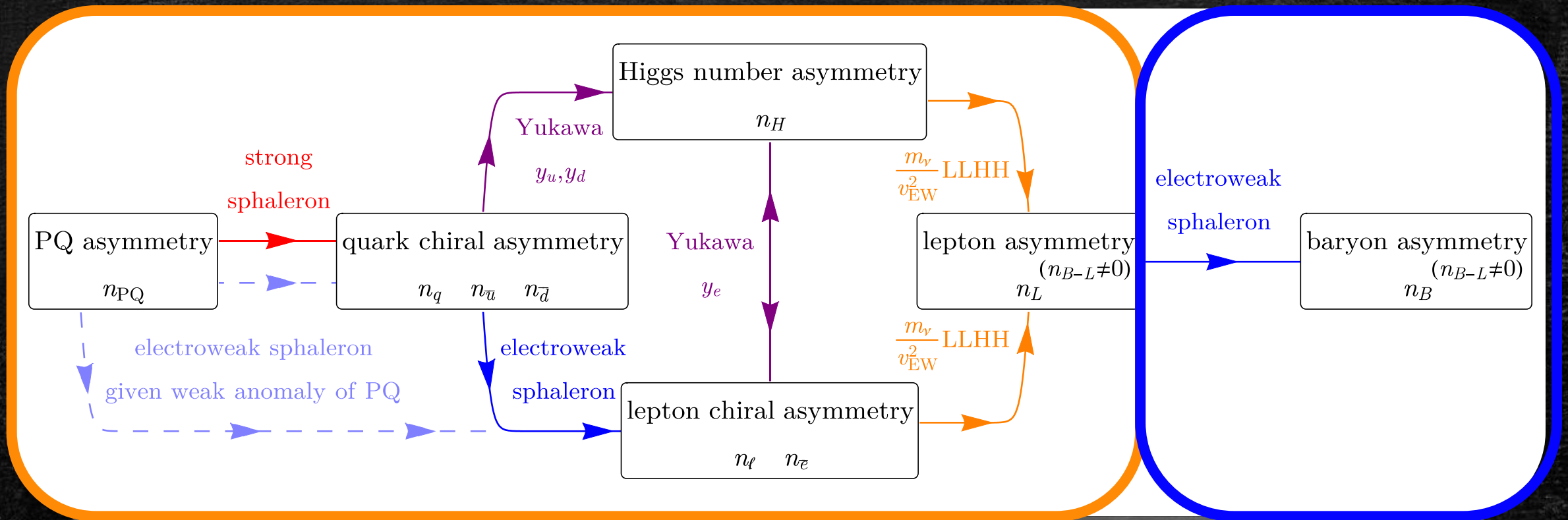
- ✓ **RC** *et al.* 1910.02080
- ✓ Harigaya *et al.* 2107.09679
- ✓ Chakraborty *et al.* 2108.04293
- ✓ Kawamura *et al.* 2109.08605
- ✓ **RC** *et al.* 2110.05487
- ✓ **RC** *et al.* 2206.00678
- ✓ Barnes, **RC** *et al.* 2208.07878
- ✓ **RC** *et al.* 2211.12517



# Lepto-Axiogenesis

Producing L at high temperatures

Converting to B at  $T_{EW}$









# Baryogenesis from Decaying Magnetic Helicity in Axiogenesis

tachyonic instability

M. S. Turner and L. M. Widrow  
PRD 37 (1997) 2743

axion-photon coupling

chiral plasma instability

M. Joyce, M. E. Shaposhnikov  
PRL 79 (1997)

decaying magnetic helicity

K. Kamada and A. J. Long  
PRD 94 no. 6, (2016)

chiral magnetic field

$h$

PQ asymmetry

$n_{\text{PQ}}$

strong sphaleron

quark chiral asymmetry

$n_q$   $n_{\bar{u}}$   $n_{\bar{d}}$

electroweak sphaleron

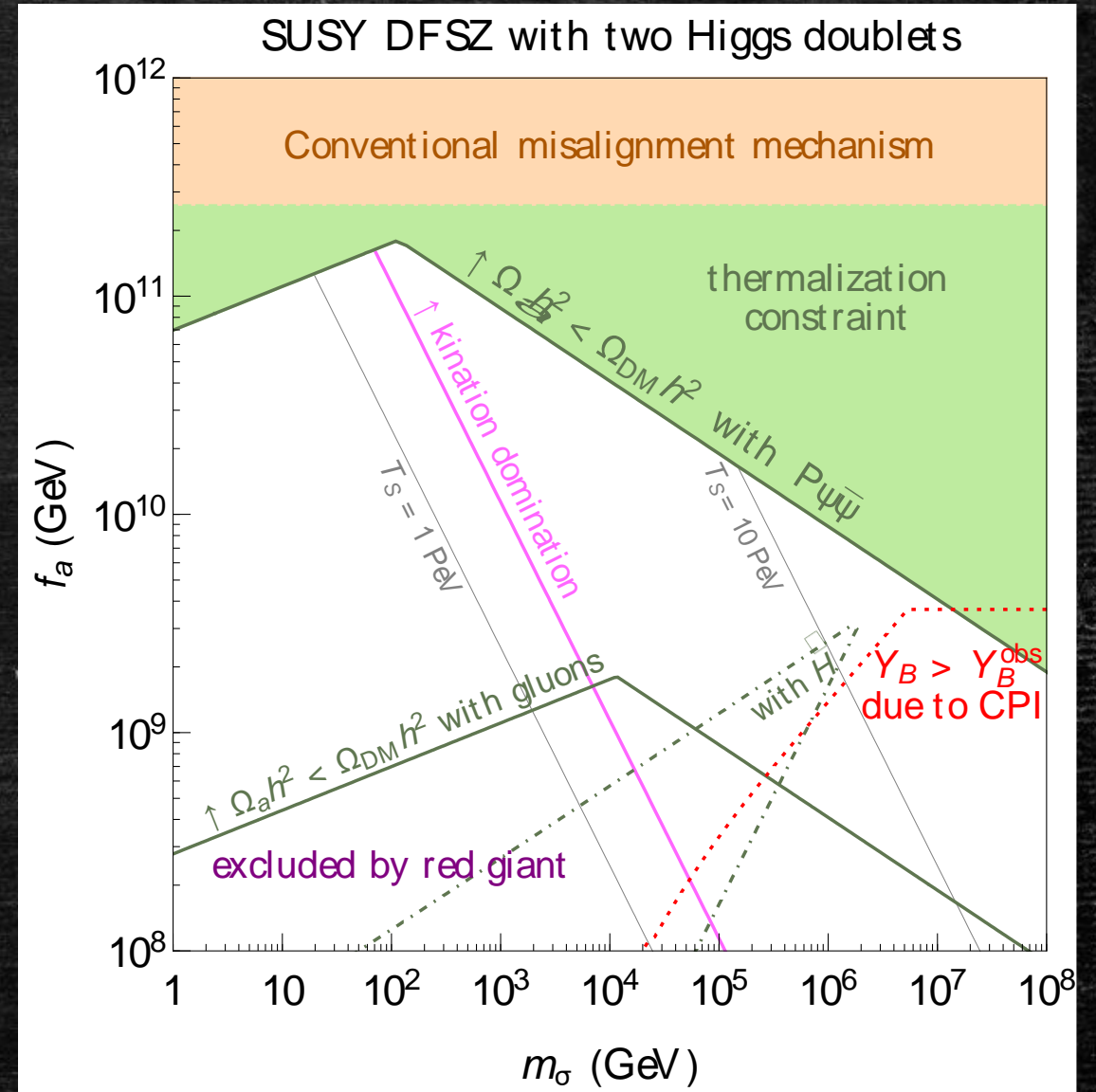
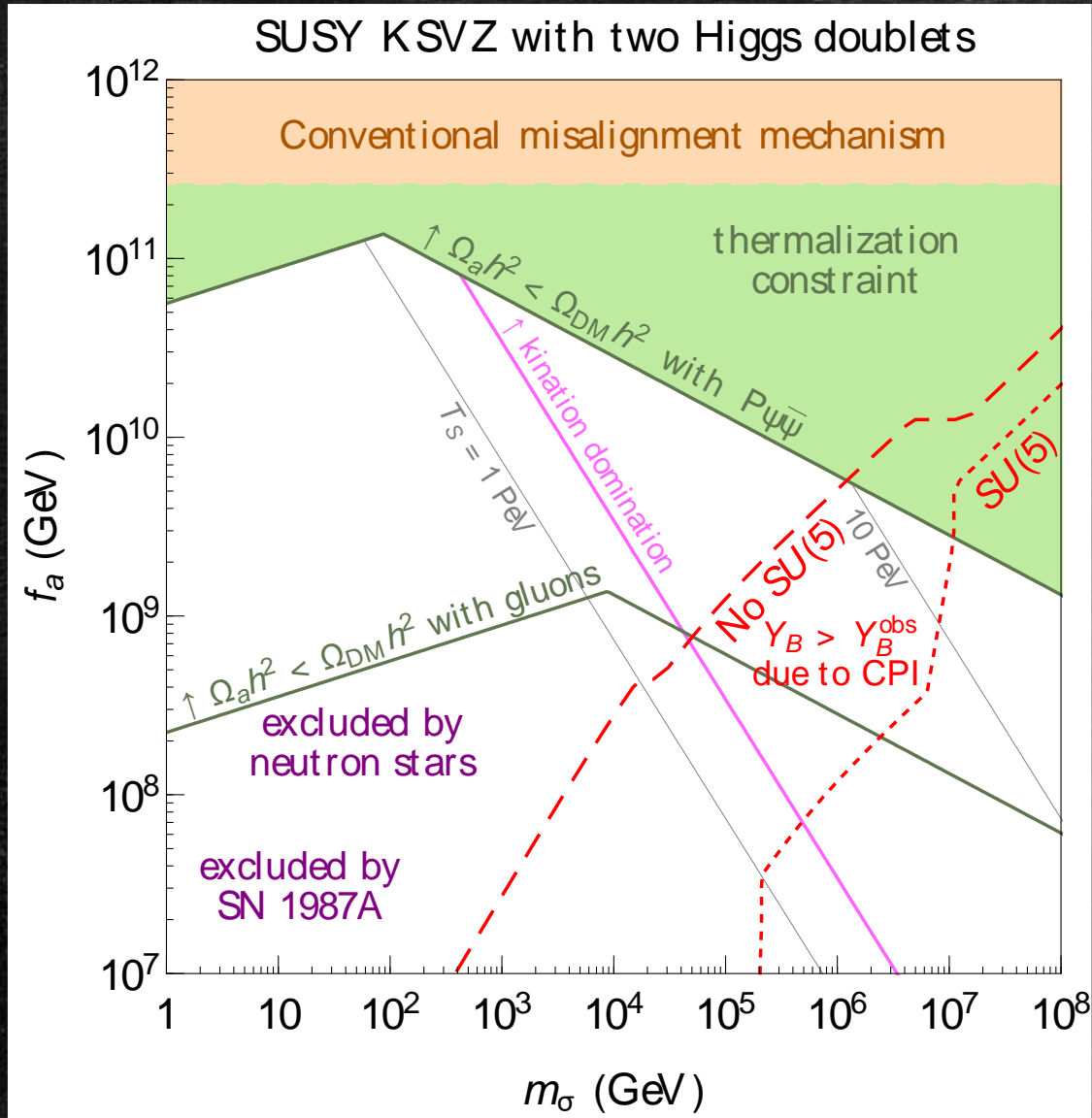
baryon asymmetry

$(n_{B+L} \neq 0)$   
 $n_B$

electroweak sphaleron  
given weak anomaly of PQ



# Baryogenesis from Decaying Magnetic Helicity in Axiogenesis



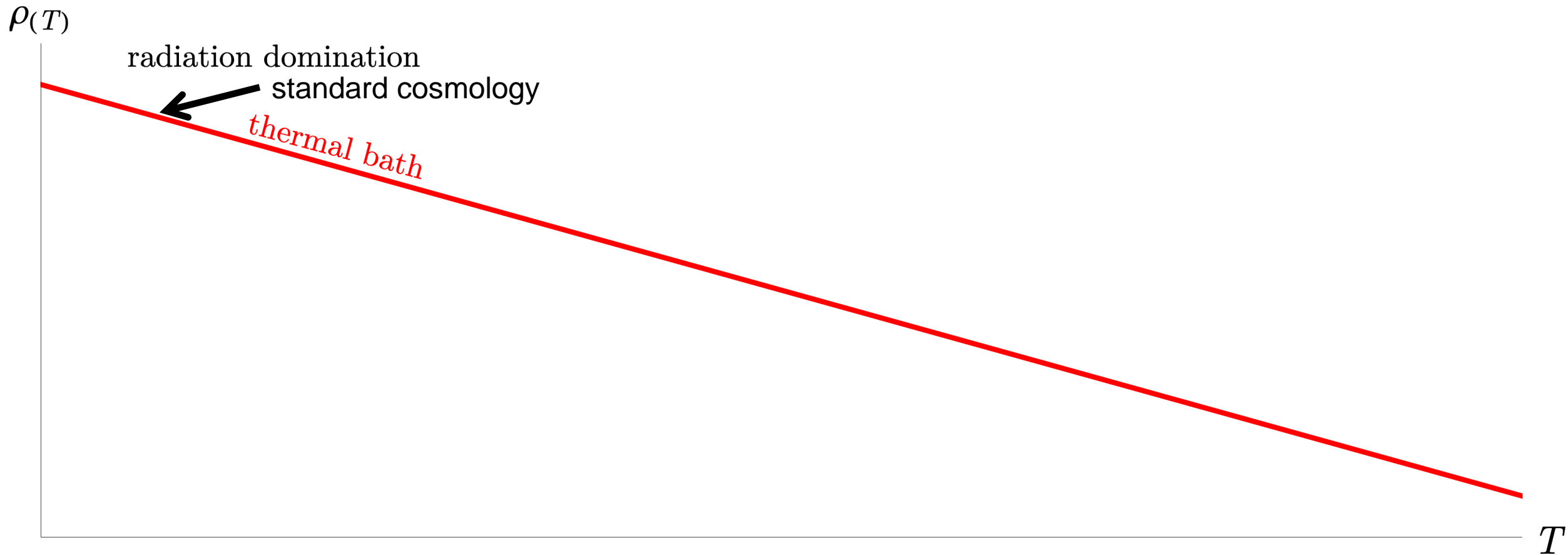


# Gravitational Wave Signatures



# Evolution of Energy Densities

The **energy content** determines the universe's **expansion rate**.

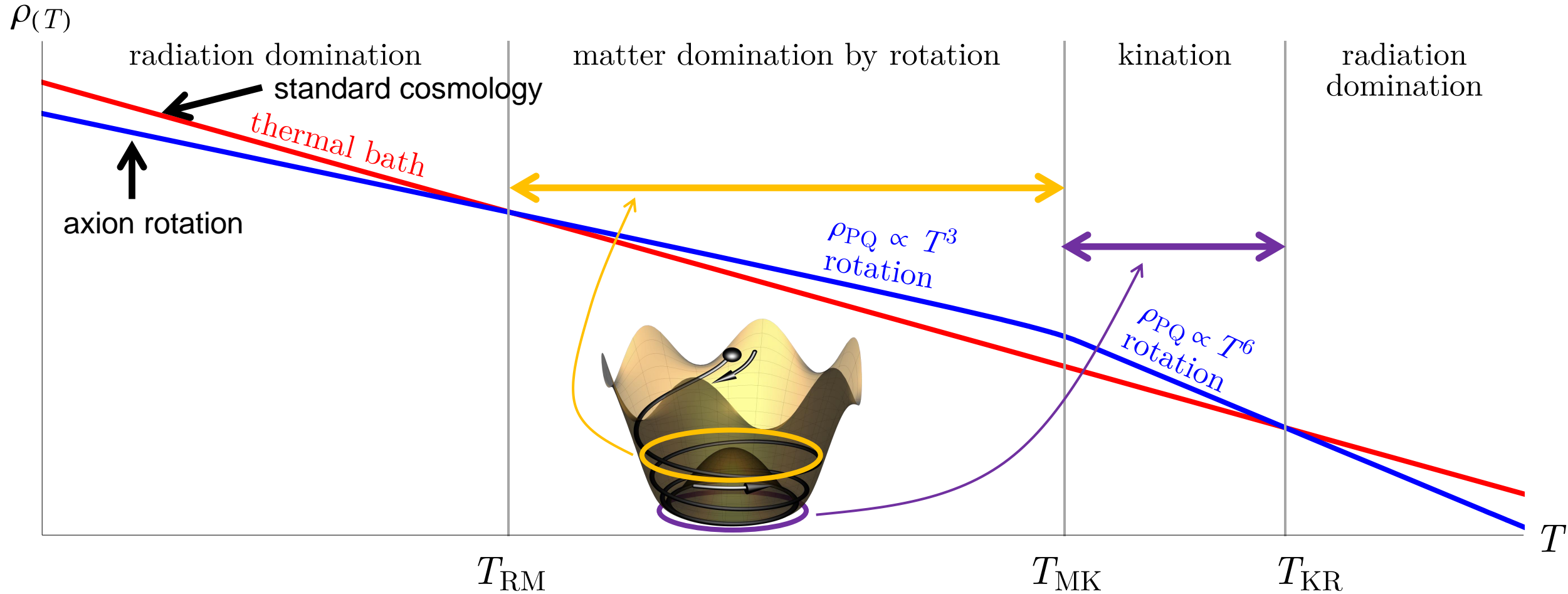


Over time, the universe cools and temperature drops.



# Evolution of Energy Densities

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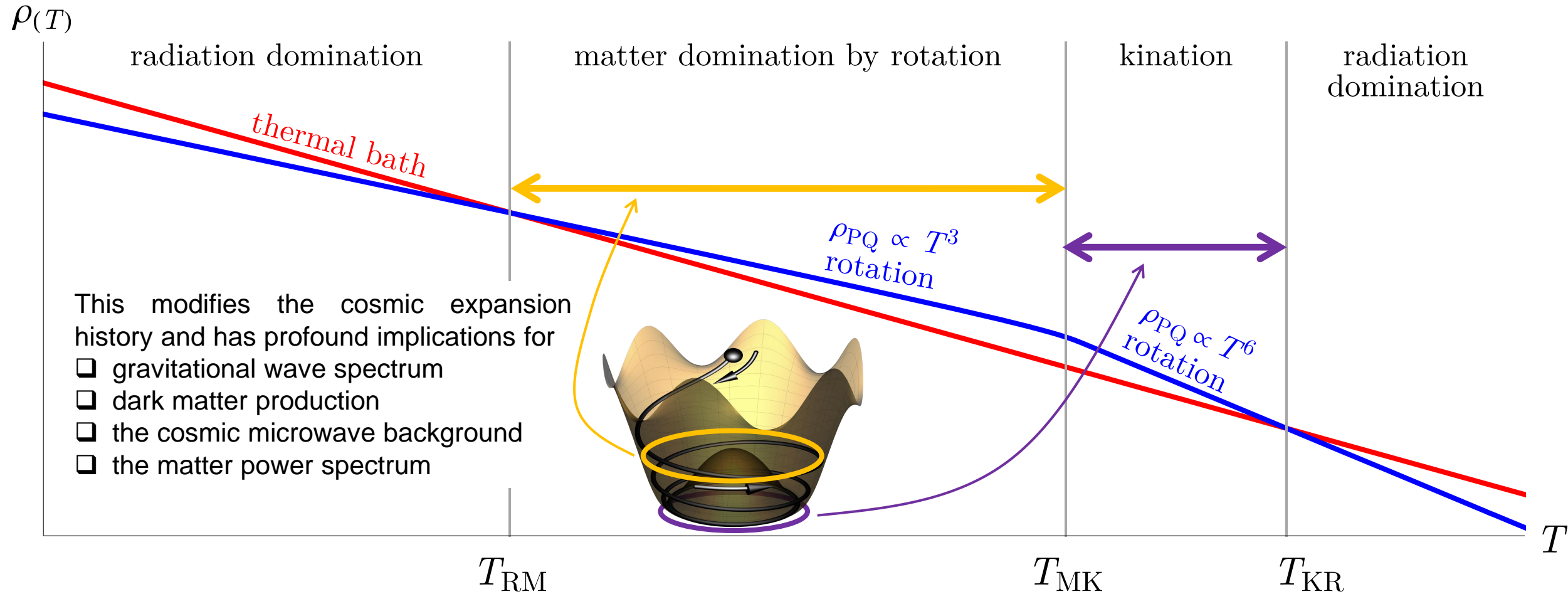


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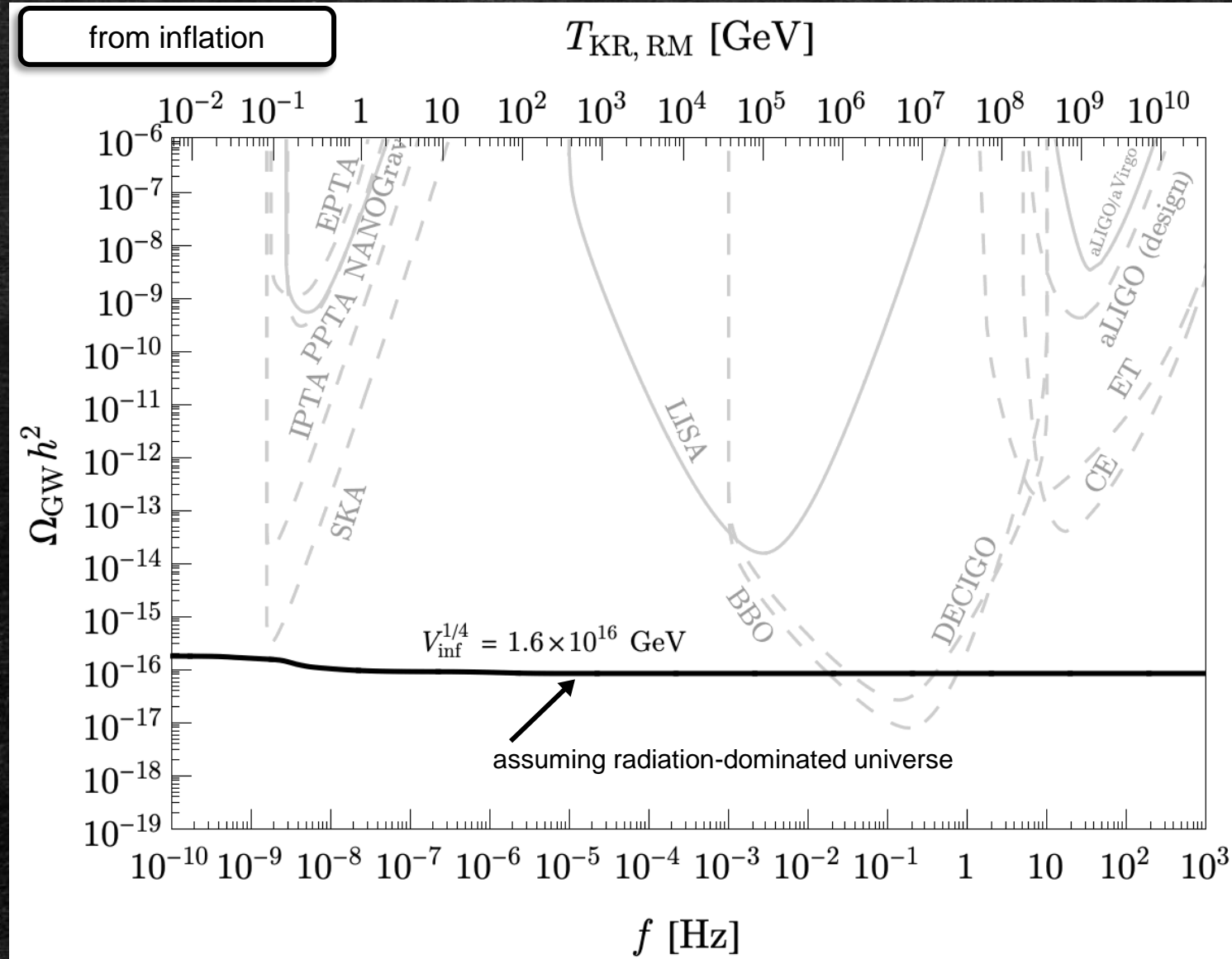
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# Smoking Gun: Triangular Peak in Gravitational Wave Spectra

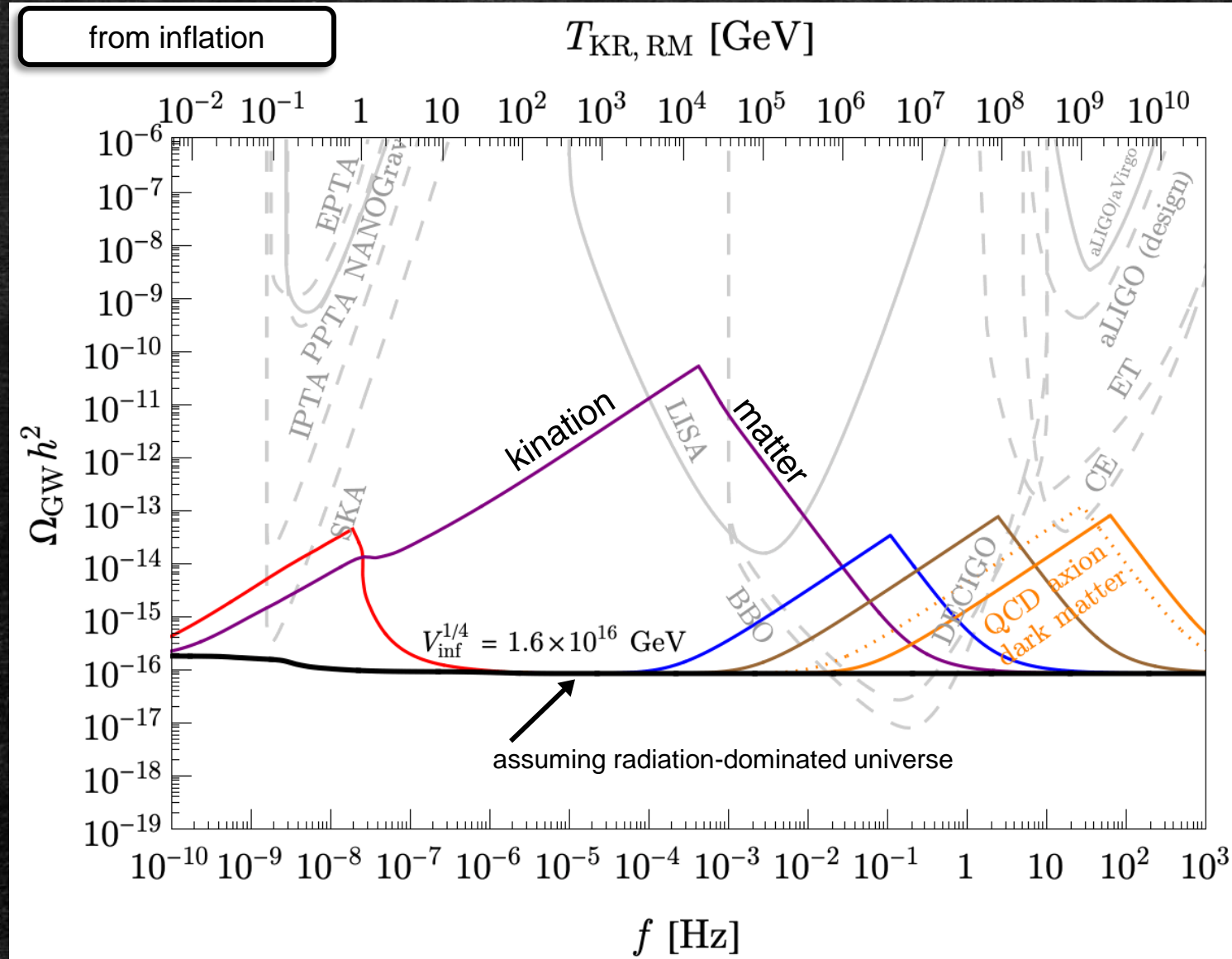


2108.09299 [JHEP 09 \(2022\) 116](#) [RC](#), D. Dunsky, N. Fernandez, A. Ghalsasi, L. Hall, K. Harigaya, J. Shelton

2108.10328, 2111.01150 Y. Gouttenoire, G. Servant, P. Simakachorn



# Smoking Gun: Triangular Peak in Gravitational Wave Spectra

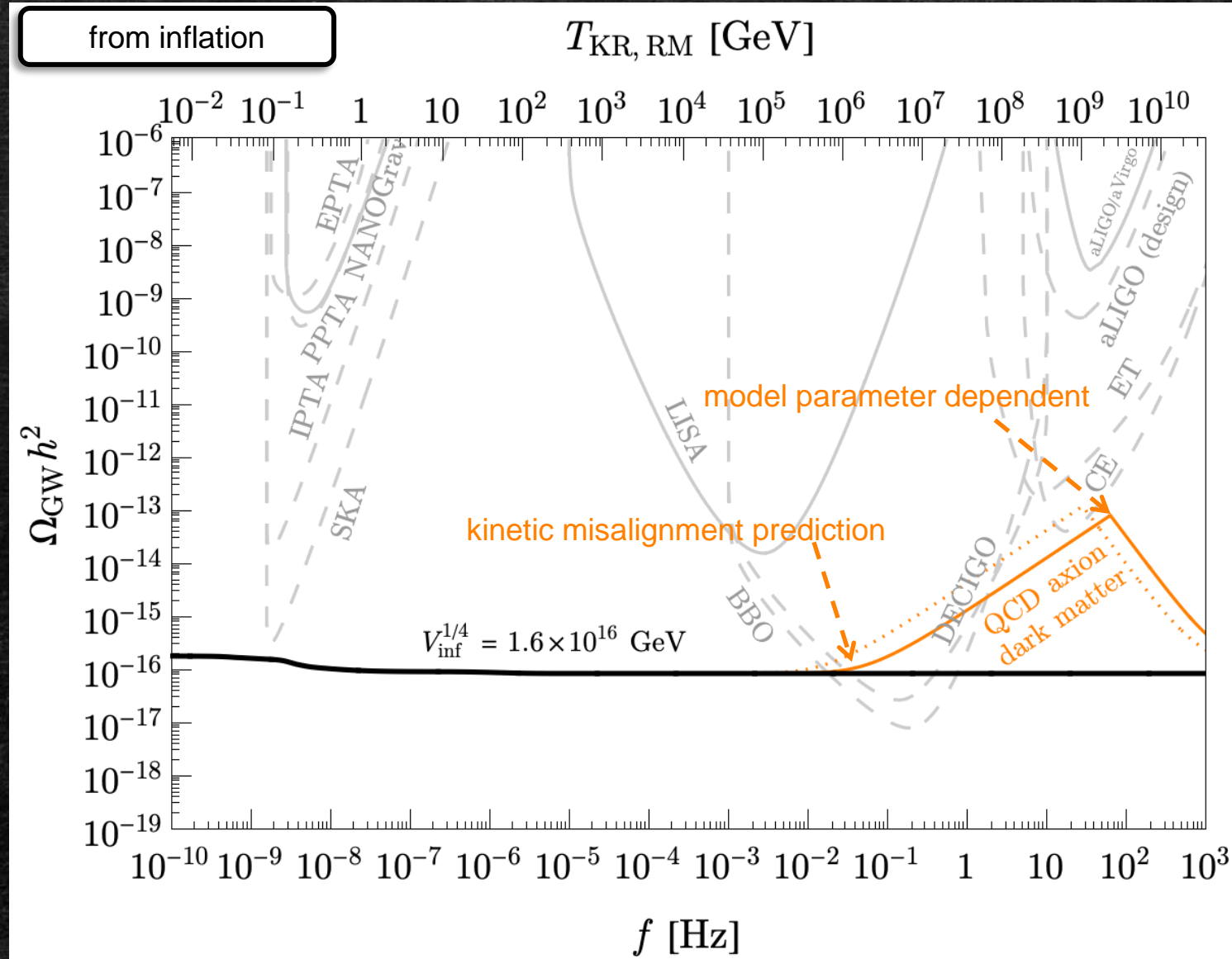


2108.09299 [JHEP 09 \(2022\) 116](#) [RC](#), D. Dunsy, N. Fernandez, A. Ghalsasi, L. Hall, K. Harigaya, J. Shelton

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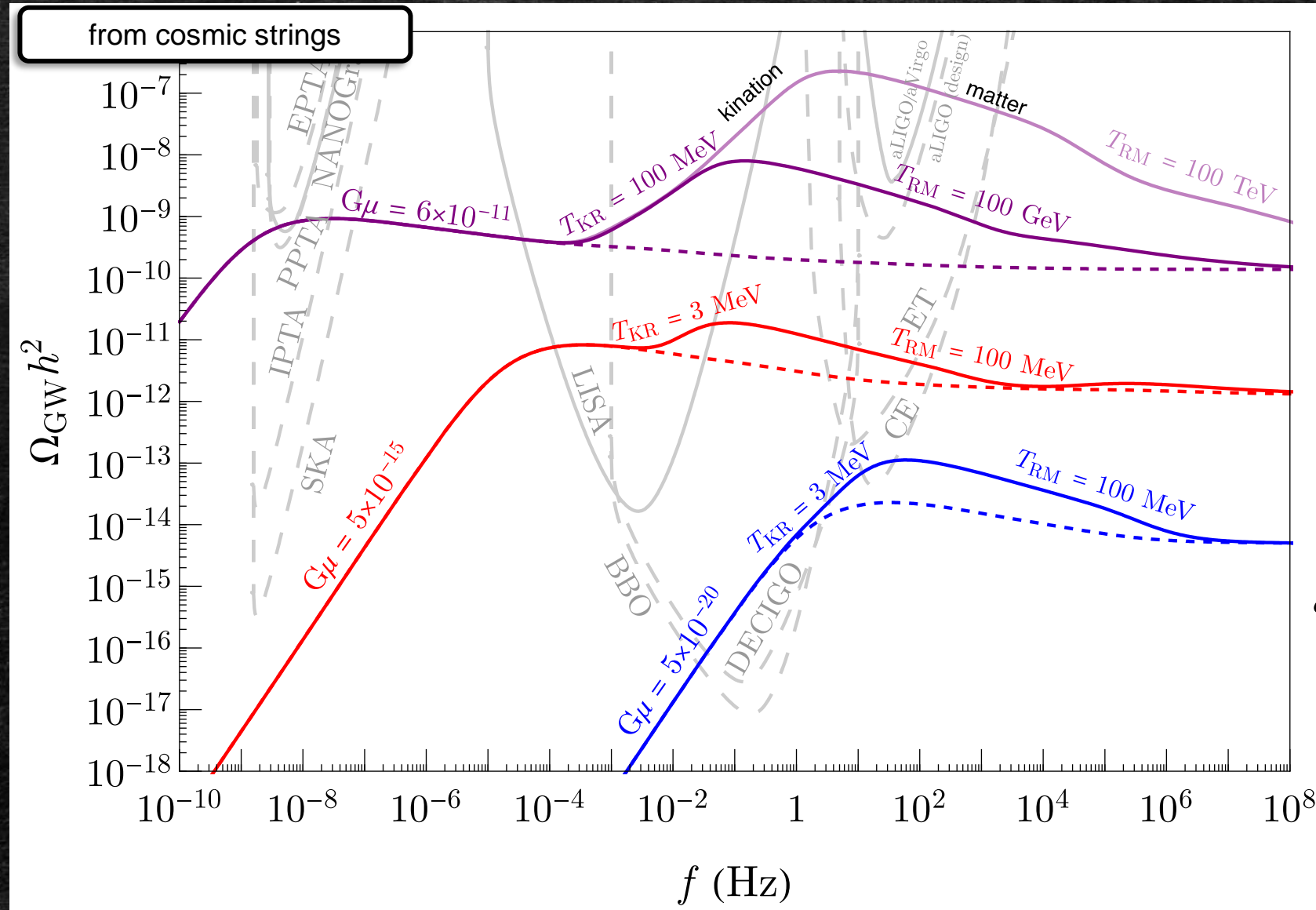


2108.09299 [JHEP 09 \(2022\) 116](#) [RC](#), D. Dunsky, N. Fernandez, A. Ghalsasi, L. Hall, K. Harigaya, J. Shelton

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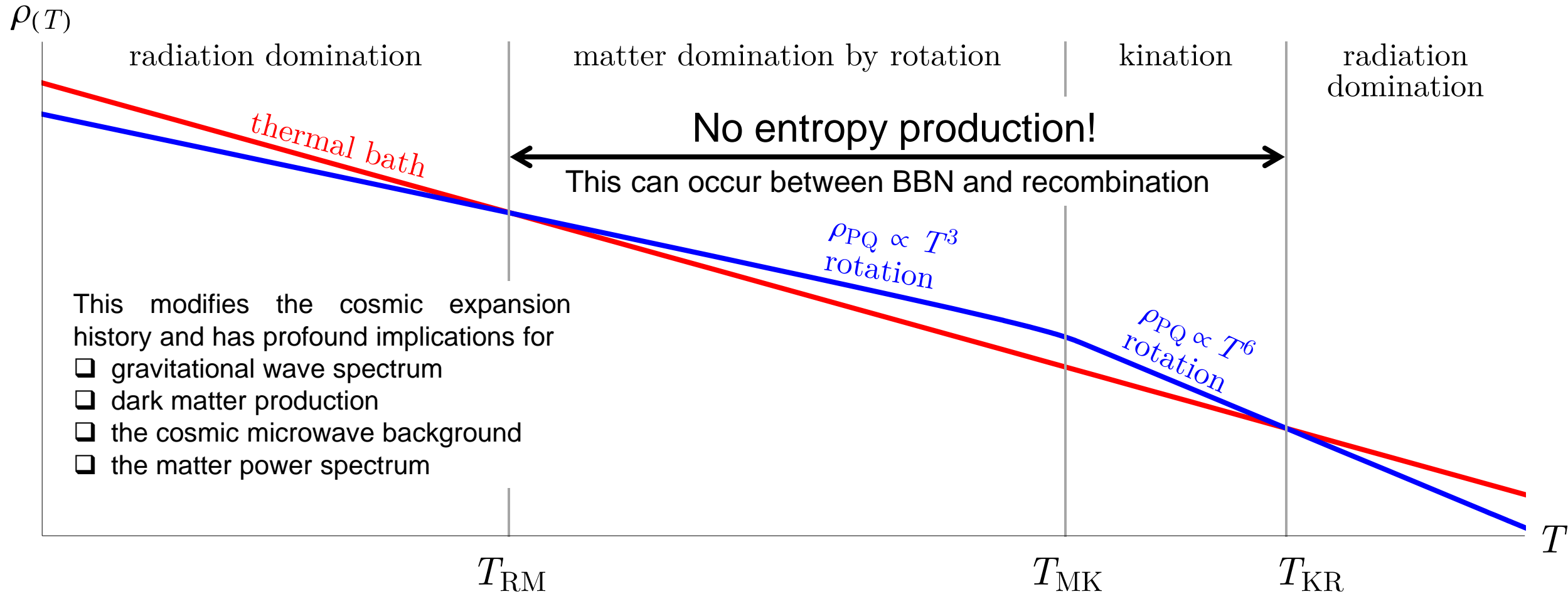
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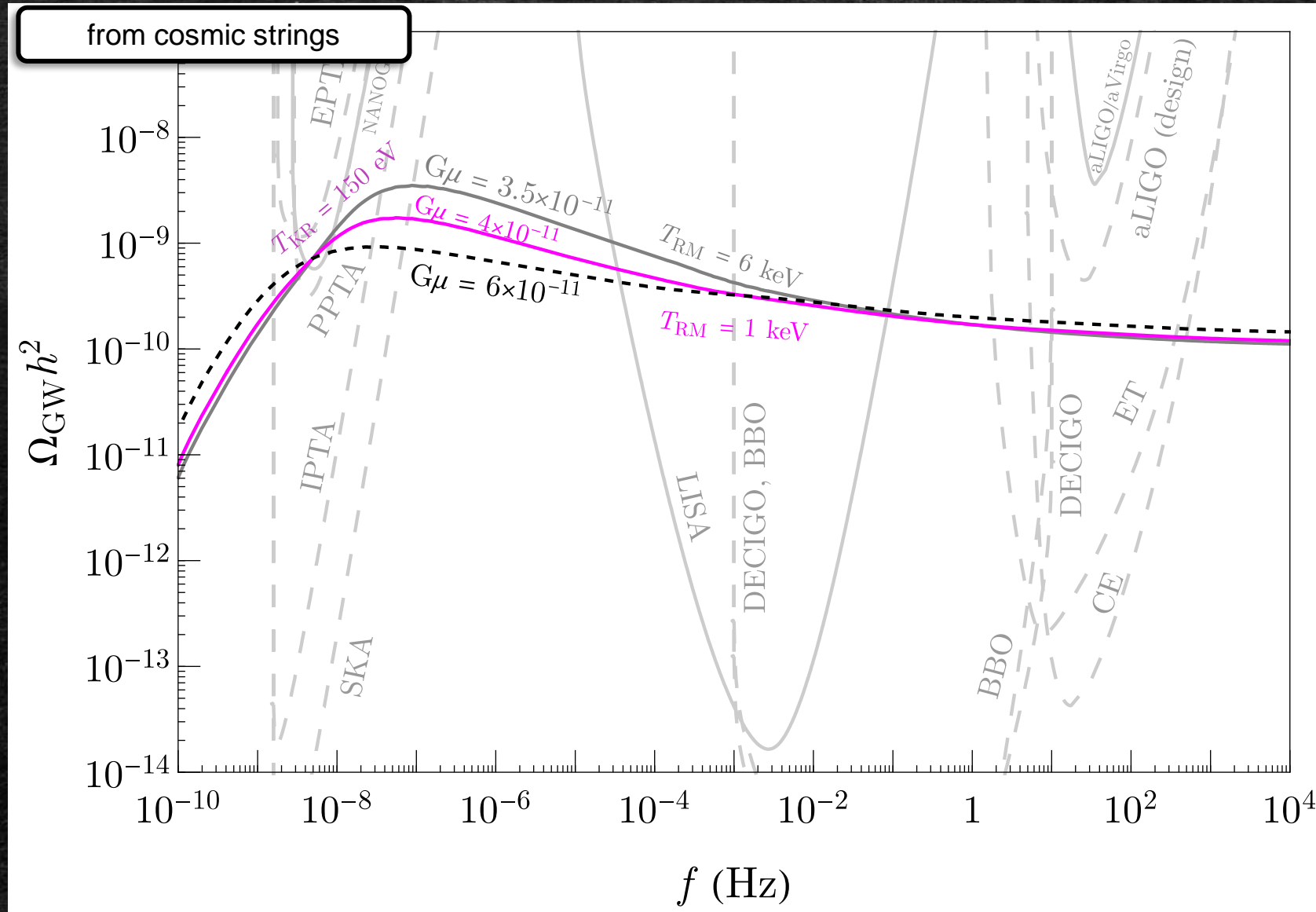
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2108.09299 [JHEP 09 \(2022\) 116](#) [RC](#), D. Dunsky, N. Fernandez, A. Ghalsasi, L. Hall, K. Harigaya, J. Shelton

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# Probing PQ-breaking Potential

Piecewise approximation

$$\rho_\theta \propto \begin{cases} R^{-3} & \text{for } S \gg f_a \text{ i.e. } T \gg T_{\text{MK}} \\ R^{-6} & \text{for } S \simeq f_a \text{ i.e. } T \ll T_{\text{MK}} \end{cases}$$

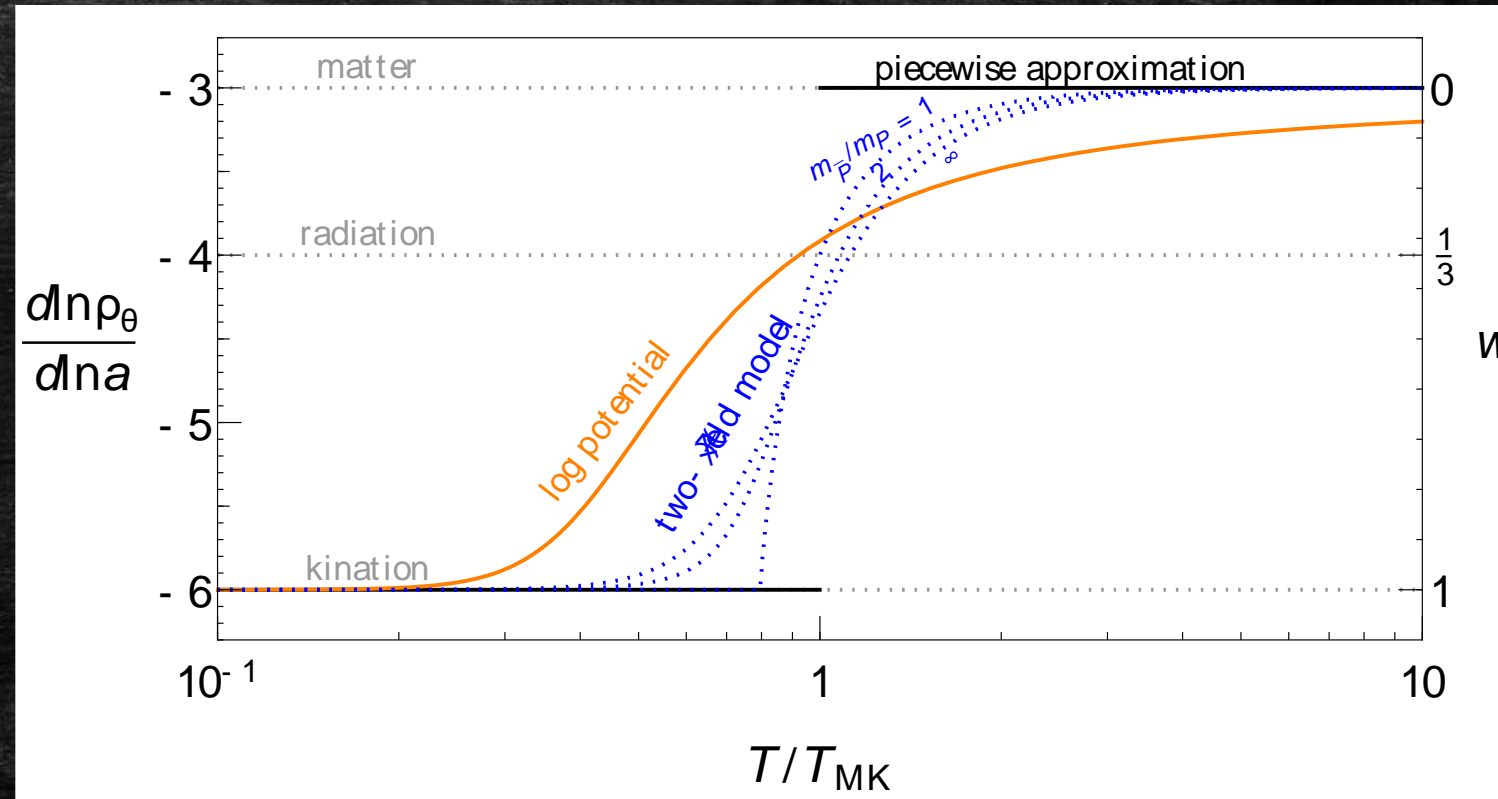
log potential

$$V(P) = m_S^2 |P|^2 \left( \ln \frac{2|P|^2}{f_a^2} - 1 \right)$$

Two-field model

$$W = X(P\bar{P} - v_P^2)$$

$$V_{\text{soft}} = m_P^2 |P|^2 + m_{\bar{P}}^2 |\bar{P}|^2$$

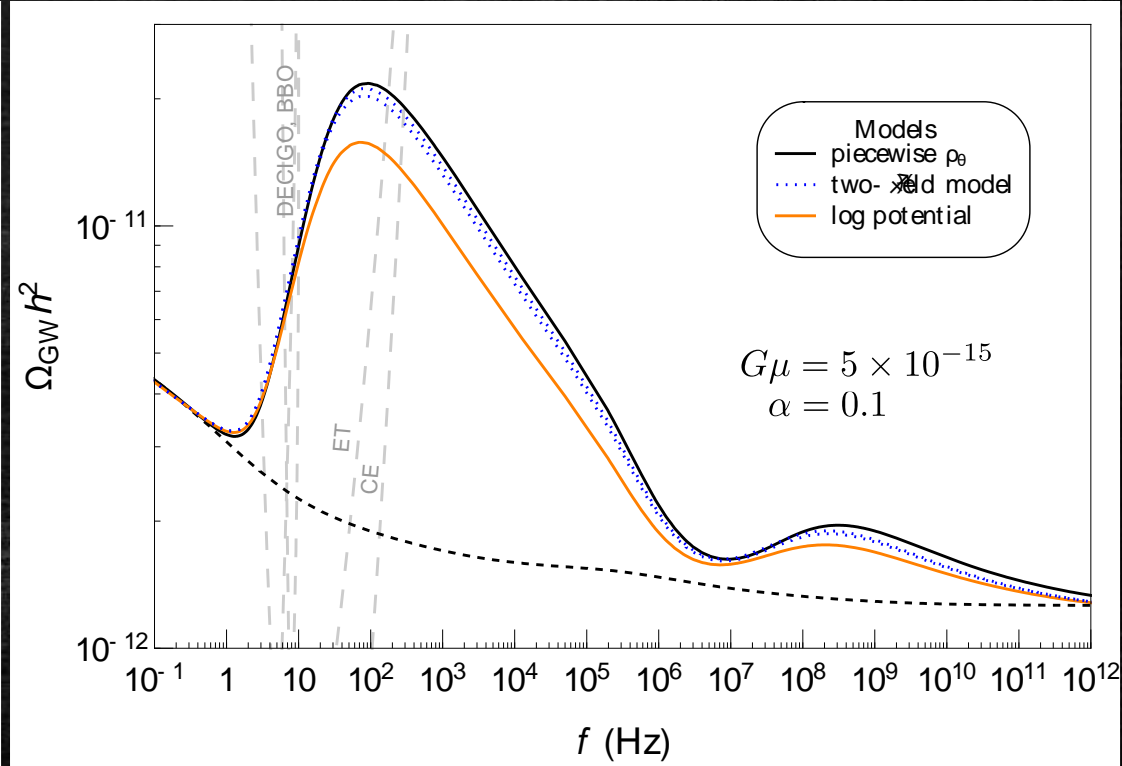
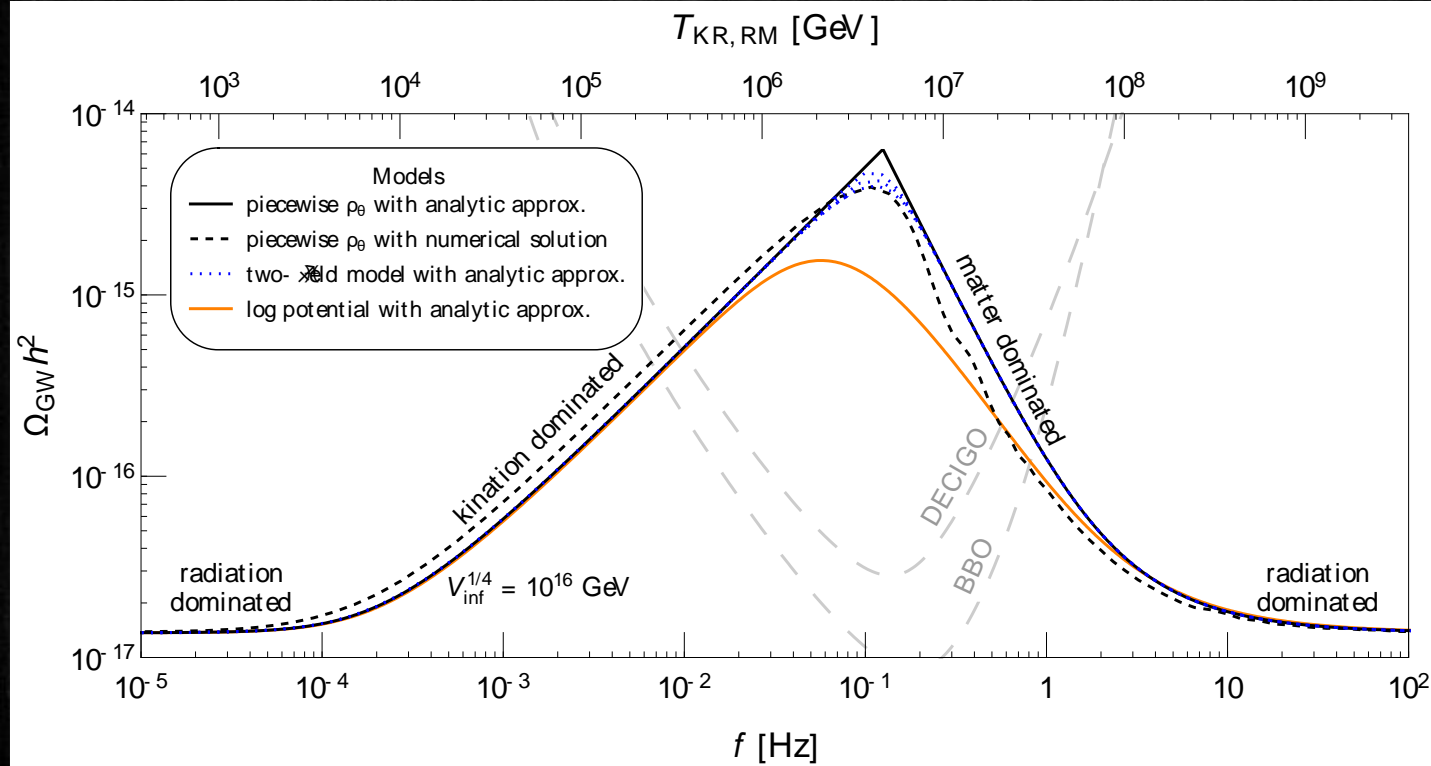




# Probing PQ-breaking Potential

from inflation

from cosmic strings



# Axion Rotations

## Axion Kination

- ✓ **RC et al.** 2108.09299
- ✓ Gouttenoire *et al.* 2108.10328
- ✓ Gouttenoire *et al.* 2111.01150

## Dark Matter

- ✓ **RC et al.** 1910.14152
- ✓ Chang *et al.* 1911.11885
- ✓ **RC et al.** 2004.00629
- ✓ Di Luzio *et al.* 2102.01082
- ✓ Rusov *et al.* 2109.01833
- ✓ Barman *et al.* 2111.03677
- ✓ Eröncel *et al.* 2206.14259
- ✓ Eröncel *et al.* 2207.10111
- ✓ Oikonomou 2208.05544
- ✓ Kozów *et al.* 2212.03518

## Baryogenesis

- ✓ **RC et al.** 1910.02080
- ✓ **RC et al.** 2006.04809
- ✓ Domcke *et al.* 2006.03148
- ✓ **RC et al.** 2006.05687
- ✓ Harigaya *et al.* 2107.09679
- ✓ Chakraborty *et al.* 2108.04293
- ✓ Kawamura *et al.* 2109.08605
- ✓ **RC et al.** 2110.05487
- ✓ **RC et al.** 2206.00678
- ✓ Barnes, **RC et al.** 2208.07878
- ✓ **RC et al.** 2211.12517
- ✓ Berbig 2307.14121

## Gravitational Waves

- ✓ **RC et al.** 2104.02077
- ✓ Madge *et al.* 2111.12730
- ✓ Harigaya *et al.* 2305.14242

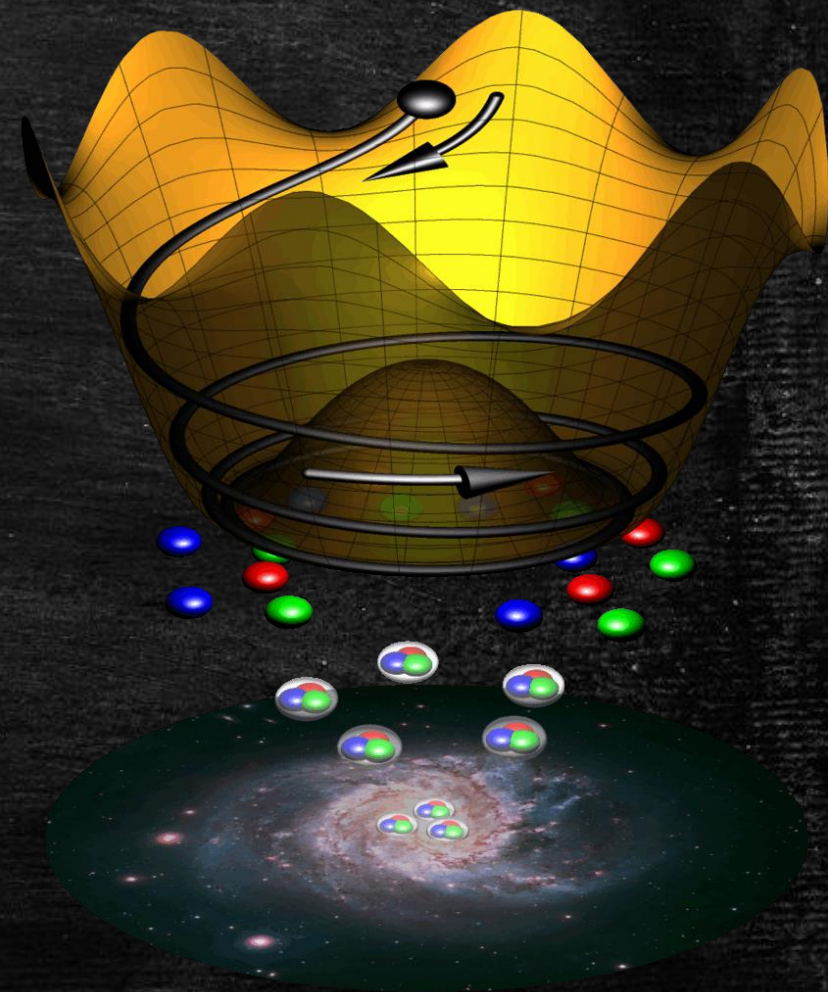
## Cosmic Perturbations

- ✓ **RC et al.** 2202.01785



# Conclusions

- ✓ **New axion dynamics** allows the QCD axion to simultaneously explain
  - ✓ Strong CP problem
  - ✓ dark matter abundance
  - ✓ baryon asymmetry
- ✓ This paradigm predicts **exciting phenomenology**
  - ✓ specific axion mass-coupling relations
  - ✓ axion kination: unique gravitational wave spectra
- ✓ Other possible signatures include
  - ✓ gravitational lensing of axion mini-clusters
  - ✓ enhanced matter power spectrum
  - ✓ warm axion dark matter
  - ✓ Majorana neutrinos
- ✓ New model building opportunities
  - ✓ **other open questions** across disciplines





Thank you for your attention  
on a **Sunday** morning