

# $J/\psi$ hadroproduction from color reconnection

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We want to check whether inclusion of Color Reconnection effects may explain  $J/\psi$  hadroproduction data

Talk based on recent results [arxiv:2303.13128]

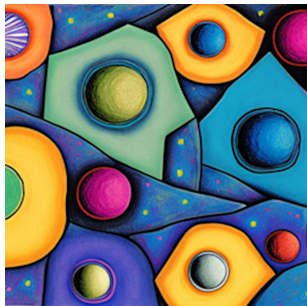
1 Part I (by LM):

- WHAT?
- WHY?

2 Part II: Piotr Kotko:

- HOW?
- THE RESULTS

*“color reconnection effects in making mesons from charm quarks”*



by AI: [hotpot.ai/s/art-generator](https://hotpot.ai/s/art-generator)

# Motivation: puzzles and questions in heavy vector quarkonia hadroproduction

As motivation we consider classical processes  $pp \rightarrow J/\psi + X$  and  $p\bar{p} \rightarrow J/\psi + X$  and double  $J/\psi$  production  $pp \rightarrow J/\psi J/\psi + X$

## Challenge for theory: puzzles and questions

- 1 Spectacular failure of the most natural QCD description with Color Singlet Model  
→ widely accepted solution with Color Octet Model
- 2 Problems of Color Octet Model with double  $J/\psi$  hadroproduction — theory underestimates the cross section by factor of about 3
- 3 Does hard factorization hold in fragmentation into  $J/\psi$ ?
- 4 What is the origin of strong correlations of  $J/\psi$  rates with charged particle multiplicity?

# What are we dealing with?

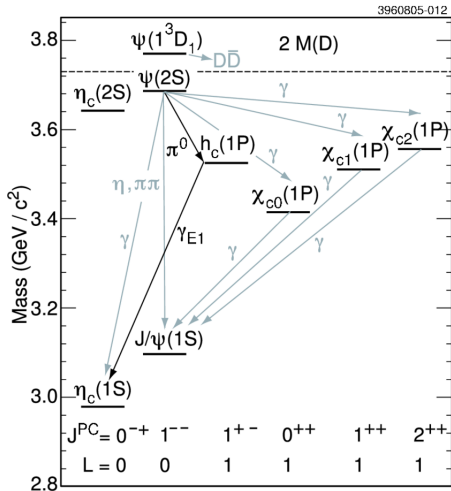
$\Upsilon / \psi$ : a  $c\bar{c}$  state

Mass = 3.097 GeV

Charmonium system mass range:

$\sim 2.98$  GeV —  $3.74$  GeV

Typical  $\Delta M \sim 0.5$  GeV



[Fig.: CLEO. Phys.Rev.D 72 (2005) 092004]

# Motivation of this study: puzzles and questions in $J/\psi$ hadroproduction

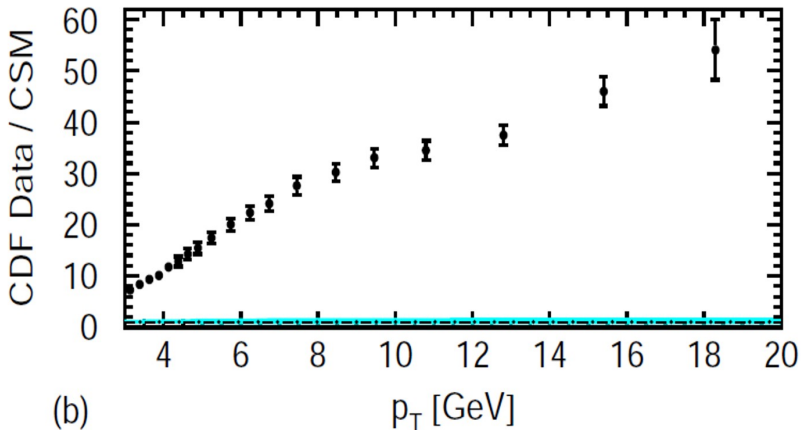
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## Challenge for theory: puzzles and questions

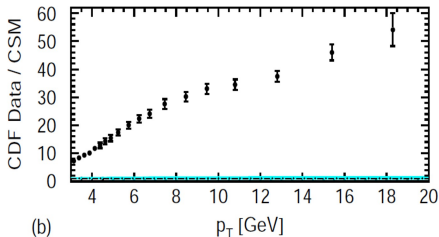
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# Puzzle 1: Why does the color singlet mechanism fail?

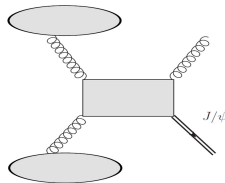
The old surprise: the QCD Color Singlet Model vs Tevatron (CDF) data [1992]



# Puzzle 1: Why does the color singlet mechanism fail?



- Heavy vector quarkonia: the main issue is the **COLOR** treatment
- $J/\psi$  a  $C$ -odd color singlet — in pQCD one needs at least three gluons to make it (for  $C$ -even, e.g.  $\chi_c$  — two gluons)
- Color Singlet Model: gluon emission:  $gg \rightarrow J/\psi + g$  — the leading twist partonic channel but too little  $p_T$  given

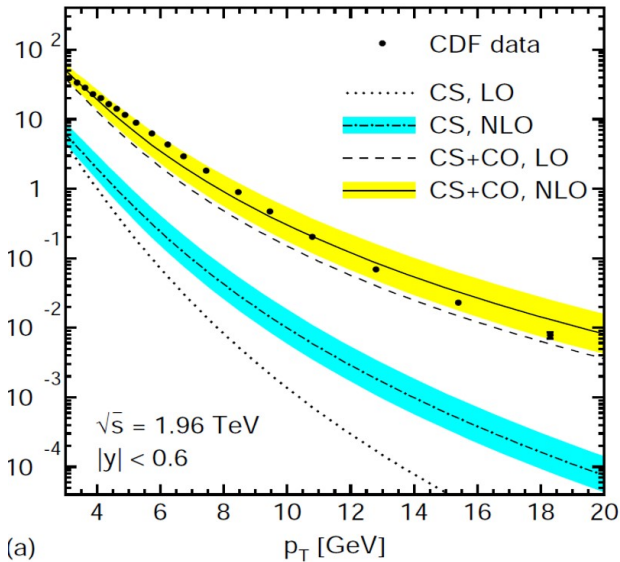


# Puzzle 1: A way out – the Color Octet Model

- Observation: at the Tevatron the ratio of  $J/\psi$  and jet cross sections was found to be roughly constant as function of  $p_T$ . Implies: the hardest possible  $p_T$  dependence  $d\sigma/dp_T \sim 1/p_T^5$
- Cho and Leibovitch [1995] (also Braaten, Yuan [1993]) gave the key idea of the COM:  
**non-zero amplitudes of gluon fragmentation into  $J/\psi$**
- Formulation in terms of transition amplitudes of  $c\bar{c}$  states in color **8** representation with various  $L$  and  $S$  into the meson, with the order of magnitude inspired by NRQCD
- The Color Octet Model assumes pQCD production mechanism of partonic  $c\bar{c}$  states followed by **universal — i.e. environment independent**, fragmentation coefficients
- Currently calculated at the NLO. With several free parameters very good description of the data. High  $p_T$  part: driven by  
 $gg \rightarrow \underbrace{g(-p_T) + g(p_T)}_{\sim \text{dijets}} \rightarrow g + (c\bar{c})(p_T) \rightarrow g + J/\psi(p_T)$



# Puzzle 1: A way out – the Color Octet Model



[M. Butenschoen, B.Kniehl, Phys.Rev.Lett. 106 (2011) 022003]

# Puzzle 2: Double $J/\psi$ hadroproduction

Double Parton  
Scattering

$$\sigma_{AB}^{(\text{DPS})} = s_{AB} \frac{\sigma_A^{(1)} \sigma_B^{(1)}}{\sigma_{\text{eff}}}$$

$s_{AB} = 1$  for  $A \neq B$

$s_{AB} = 1/2$  for  $A = B$

Typically measured:

$$\sigma_{\text{eff}} \simeq 15 - 20 \text{ mb}$$

**Smaller**  $\sigma_{\text{eff}}$

**→ larger DPS**

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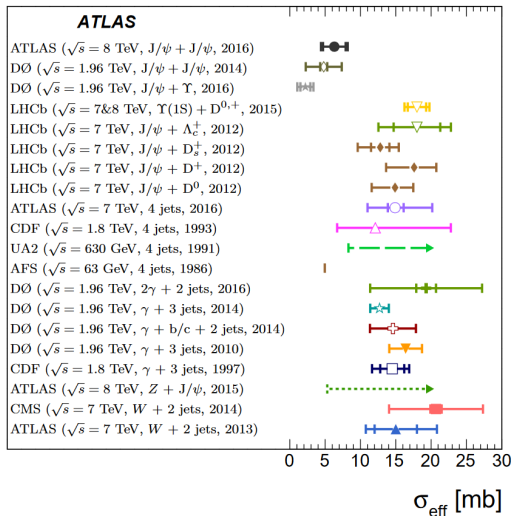
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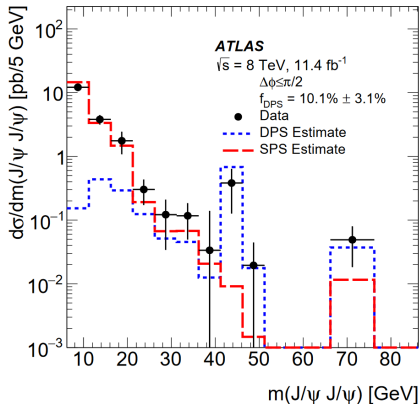
→ larger DPS

Experiment (energy, final state, year)



[ATLAS, 1612.02950]

# Puzzle 2: Double $J/\psi$ hadroproduction at ATLAS



- Two  $J/\psi$ -s can be created from in Single Parton (pair) Scattering (SPS) or in DPS
- At larger invariant masses of the pairs SPS dies out (COM included)
- Large DPS necessary there

$$\sigma_{\text{eff}} \simeq 5 \text{ mb}$$

Double heavy vector quarkonium production requires about 3 times stronger DPS effects than other processes!

## Puzzle 2: Implications

What does imply the strong enhancement of double  $J/\psi$  hadroproduction?

- 1 Possibility 1: initial state.

The partonic mechanisms for individual parton-parton to  $J/\psi$  subprocesses factorize, but initial parton configurations are particularly strongly correlated in quarkonia pair production

**Problem:** why should quarkonia pair production should have such a strong effect on parton correlations, while other hard processes do not show it?

- 2 Possibility 2: production mechanism.

Partonic configurations are typical, but strong correlations in the production mechanisms of the two quarkonia. Such correlations could be introduced by multiple interactions in pQCD, but this would correspond to higher twist effects.

**Alternative:** factorization breaking at the leading twist

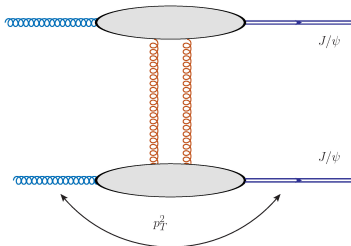
# Can perturbative multiple scattering solve the problem?

We need a mechanism that generates large distance rapidity correlations

Natural candidate:

$gg \rightarrow J/\psi J/\psi$  via entangled  
 $g + 2g \rightarrow J/\psi$  subprocesses

Problem: Large momentum flows through the mesons: additional power suppression



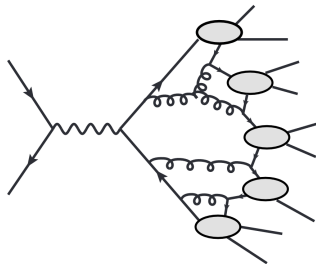
Explicit calculations: by A. Szczurek, A. Cisek and W. Schäfer [1710.11450] and our in-house calculations show that this mechanism is by far too weak

# Question 3: Does hard factorization hold in $g \rightarrow J/\psi$ fragmentation?

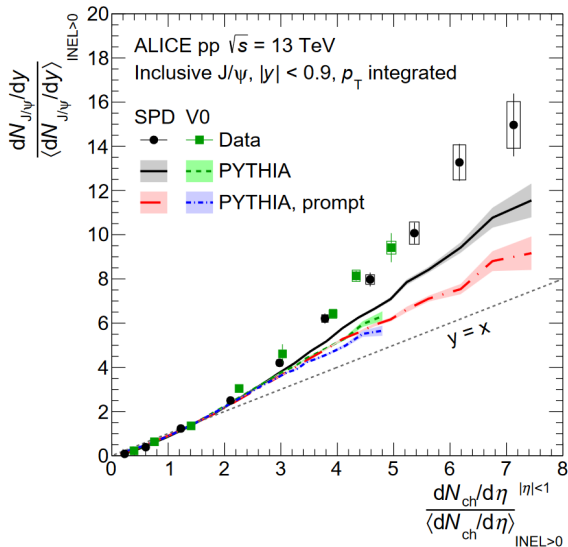
Answer by John Collins, 1610.09994: it is not guaranteed that hard factorization works in fragmentation.

The reason: hadronization effects that fill rapidity ranges between hard partons, and that are of non-perturbative origin (comment: e.g. the Schwinger pair creation effect)

Argument: “Let  $\Delta y$  be total available rapidity range, about  $\ln(Q^2/m^2)$ , and let  $\delta y$  be typical cluster separation, i.e.,  $\Delta y/\#\text{clusters}$ . Experimentally  $\delta y$  is typically small, a unit of rapidity or so. Now suppose we were able apply soft-to-collinear approximations. Errors would now be a power of  $\exp(-\delta y)$ , not  $m/Q$ , while the order of the relevant graphs increases with  $\ln Q$ .”



# Puzzle 4: What is the reason of strong correlations of $J/\psi$ production with multiplicity? [ALICE 2005.11123]





# Possible solution: Color Reconnection

- Question: what happens between the partonic and hadronic phase?
- Color is not locally preserved in this transitions: colored partons get to white hadrons
- For quarks: they pick antiquarks from the vacuum to make color singlets — this is related to color string breaking in the Lund string picture
- Hadronization occurs at distances of  $\sim 1$  fm. In the presence of color fields the short distance parton color ordering may not survive
- These reasons and data analysis  $\rightarrow$  multi-purpose event simulators like PYTHIA and HERWIG include possibility of changing large  $N_c$  color ordering between the partonic phase and hadronization: the Color Reconnection (CR) mechanism

# Possible solution: Color Reconnection — why interesting?

Key features of Color Reconnection in the Lund approach:

- Changes color configuration, while preserving the color strings connected to large  $N_c$  limit of QCD
- Allows to transform partonic color octets to singlets  
e.g.  $(c\bar{c})^8 \rightarrow (c\bar{c})^1$  (*like in Color Octet Model*)
- The effect of color reconnection depends on color flow in the whole event  $\rightarrow$  long range correlations in color flow  
(*unlike in Color Octet Model*)
- Simple combinatorics implies that probability of reconnection is higher for events with more partons (*unlike in COM*)  
higher multiplicity  $\rightarrow$  more reconnections  $\rightarrow$  more  $(c\bar{c})^1$

Edin, Ingelman and Rathsman (1997) showed that Color Reconnection effects in certain realization may lead to a good description of quarkonia production and hard diffractive processes

## PART II



# GENERIC MC EVENT

initial state shower (ISR)

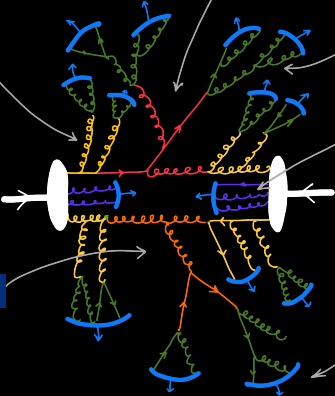
hard process

final state shower (FSR)

beam remnants

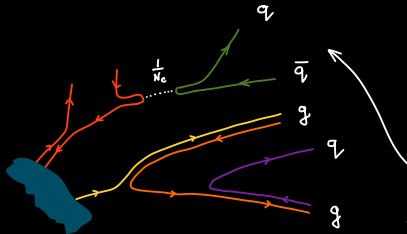
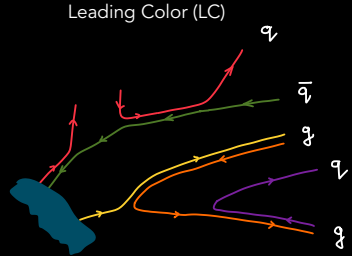
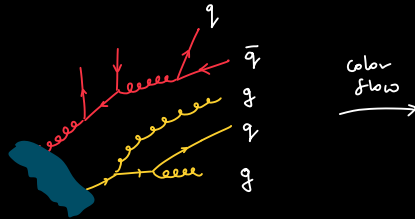
multi parton interactions (MPI)

hadronization



# COLOR RECONNECTIONS

## Color management in a MC event



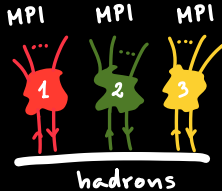
Each line has a "color tag"  $i$  or "anti-color tag"  $\bar{i}$ .  
In Pythia  $i, \bar{j} = 101, 102, 103, 104, \dots$   
Partons are characterized by a pair of tags  $\{i, \bar{j}\}$ .

Requires switching the color tags for final state particles.

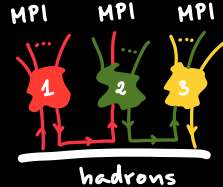
Non-Leading Color

# COLOR RECONNECTIONS

## Color ambiguities



color reconnection

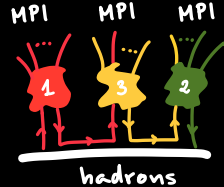


But why not to reconnect  $1 \leftrightarrow 3 \leftrightarrow 2$  ?

Uncorrelated MPIs give too much color charge extracted from the colliding hadrons



too large hadronic activities at forward rapidities...

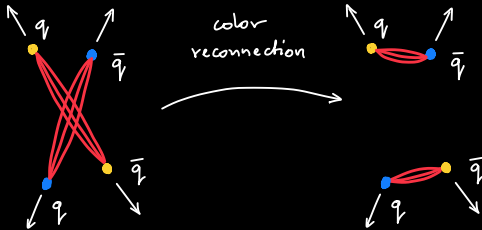


[J. Christiansen, P. Skands, 2015]

# COLOR RECONNECTIONS

## QCD-based Pythia CR model

- possible color topologies are SU(3) QCD-driven
- detailed modeling of the beam remnants
- reconnections are such, that the color topology for which the "string length" is minimized, are passed on to hadronization



[based on J. Christiansen  
talk at MPI@LHC 2014]

# $J/\psi$ PRODUCTION IN PYTHIA

## Algorithm

- we **do not** use COM or other models available in Pythia for charmonium production
- we take default Pythia 8.3, no tuning, with MPI and showers turned on
- the hadronization is turned off
- we scan through the event record to look for  $c\bar{c}$  quarks
- if present, we look for  $c\bar{c}$  pairs with matching color and anti-color tags
  - these are  $J/\psi$  candidates
- we apply the invariant mass cut:  $3.0 \text{ GeV} \leq M \leq M_{\text{max}}$ 
  - the color singlets satisfying this cut are treated as  $J/\psi$
- $M_{\text{max}}$  is our free parameter; we fix  $M_{\text{max}} \approx 3.3 \text{ GeV}$  to have best description of data
- we compute  $p_T$  spectra in central rapidity window  $|y| \leq 2.4$
- we test color reconnection on/off



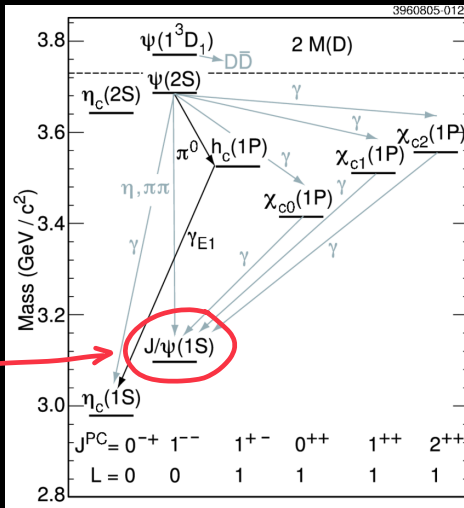
# J/ψ PRODUCTION IN PYTHIA

## Charmonium system

Our final invariant mass cut on the singlet system

$$3.0 \text{ GeV} \leq M \leq 3.3 \text{ GeV}$$

lies within reasonable range

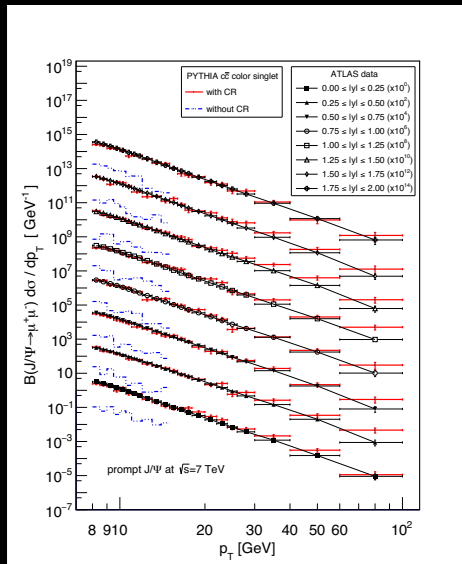


[taken from CLEO, Phys. Rev.D 72 (2005) 092004]

# $J/\psi$ PRODUCTION IN PYTHIA

## Results for ATLAS kinematics

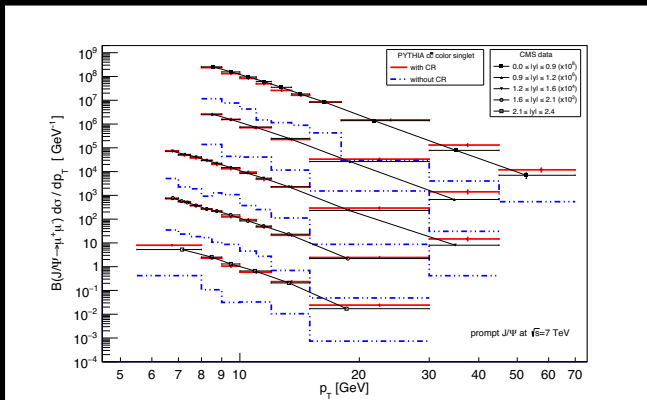
- comparison with ATLAS data [ATLAS, Eur.Phys.J C (2016) 283]
- **good description of data for most rapidity bins, provided the CR is on (red histograms)**
- without CR  $J/\psi$  production rate is dramatically insufficient to describe the data
- some deviations at large  $p_T$ , but also large statistical MC errors
- challenging computation; we used the PLGrid facility and Prometheus supercomputer to create sufficient statistics



# J/ψ PRODUCTION IN PYTHIA

## Results for CMS kinematics

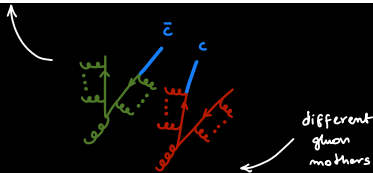
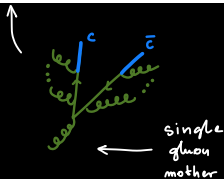
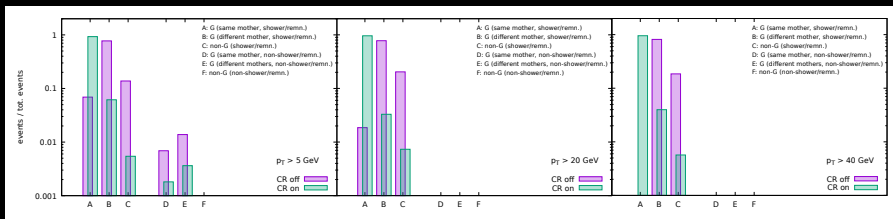
- comparison with CMS data [CMS, JHEP (2012) 011]
- similar conclusions



# J/ $\psi$ PRODUCTION IN PYTHIA

## Origin of $c\bar{c}$ singlets in Pythia

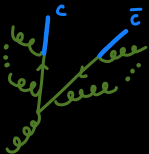
- we analyze event records with low invariant mass  $c\bar{c}$  singlets
- we extract information on mother partons and its production mechanism
- each plot is normalized by the total number of events, independently for CR on and CR off



# $J/\psi$ PRODUCTION IN PYTHIA

## Interpretation

- in the Leading Color (large  $N_c$ ) no perturbative mechanism can contribute to class A ("single gluon mother")



the color  
bags can  
never  
repeat



- the very few events in class A with **CR off** are due to color reshuffling in the MPI and beam remnant; it dies out with  $p_T$
- dominant mechanism when **CR is off** is via "different gluon mothers", but this has small probability due to less likely phase space overlap
- when **CR is on**, class A mechanism dominates; narrow angle quark pair is favored by the smallness of the string length and tend to be color-reconnected to become the singlet

# Conclusions and outlook

- 1 The model of  $J/\psi$  hadroproduction by Color Reconnection works in a simple and natural way. Both the magnitude of cross section and  $p_T$  dependence are well described
- 2 No need for any special tuning of PYTHIA, only one parameter added to describe  $J/\psi$  formation — the cut on  $c\bar{c}$  invariant mass — found to be in the expected range
- 3 Without Color Reconnection the production rates are found to be by far too small
- 4 The key importance of gluon fragmentation, including the gluons from the shower
- 5 Color Reconnection correlates fragmentation in different regions of an event. Factorization breaking?
- 6 Outlook: interesting to test this model with data on  $J/\psi$  pair production and on  $J/\psi$  correlations with multiplicity. Also to constrain Color Reconnection.

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Thanks!