# Flavour Physics (of quarks) <br> Part 1: Flavour in the SM 

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## Overview

Lecture 1: Flavour in the SM (Today)

- Flavour in the SM
- Quark Model History
- The CKM matrix

Lecture 2: Mixing and $C P$ violation

- Neutral Meson Mixing (no CPV)
- $B$-meson production and experiments
- $C P$ violation

Lecture 3: Measuring the CKM parameters

- Measuring CKM elements and phases
- Global CKM fits
- $C P T$ and $T$-reversal
- Dipole moments

Lecture 4: Flavour Changing Neutral Currents

- Effective Theories
- New Physics in $B$ mixing
- New Physics in rare $b \rightarrow s$ processes
- Lepton Flavour Violation


## Reading Material

- I have provided a short document containing an overview of the course and a reading list which can be found on the indico event page https://indico.cern.ch/event/1130558
- I've also put a copy of it on my warwick page (along with these slides) https://warwick.ac.uk/fac/sci/physics/staff/academic/kenzie
- Most of the material for these slides comes from one of the sources on that reading list

> Many thanks to Tom Blake, Tim Gershon, Alex Lenz, Niels Tuning, Mitesh Patel, Monika Blanke and Gino Isidori for inspiration, ideas and outright plagiarism

## Please interupt if you have a question! <br> I will be quizzing you as we go along!

## What is flavour physics?

## Flavour (particle physics)

From Wikipedia, the free encyclopedia
(Redirected from Flavour physics)

WikipediA The Free Encyclopedia

In particle physics, flavour or flavor refers to the species of an elementary particle. The Standard Model counts six flavours of quarks and six flavours of leptons. They are conventionally parameterized with flavour quantum numbers that are assigned to all subatomic particles. They also can be described by some of family symmetries proposed for the quark-lepton generations.
"The term flavor was first used in particle physics in the context of the quark model of hadrons. It was coined in 1971 by Murray Gell-Mann and his student at the time, Harald Fritzsch, at a BaskinRobbins ice-cream store in Pasadena. Just as ice cream has both color and flavor so do quarks."

RMP 81 (2009) 1887

## Flavour in particle physics

Flavour quantum numbers

- Isospin: I or $I_{3}$
- Charm: C
- Strangeness: $S$
- Topness: $T$
- Bottomness: $B^{\prime}$

Related quantum numbers

- Baryon number: $B$
- Lepton number: $L$
- Weak isospin: $\mathbf{T}$ or $T_{3}$
- Electric charge: $Q$
- X-charge: $X$


## Combinations

- Hypercharge: $Y$
- $Y=\left(B+S+C+B^{\prime}+T\right)$
- $Y=2\left(Q-l_{3}\right)$
- Weak hypercharge: $Y_{W}$
- $Y_{W}=2\left(Q-T_{3}\right)$
- $X+2 Y_{W}=5(B-L)$


## Flavour mixing

- CKM matrix
- PMNS matrix
- Flavour complementarity
"Heavy flavour physics" predominantly involves study of weak decays of heavy quarks


## Why bother with flavour physics?

- The SM is beautiful but incomplete - there are fundamental new particles somewhere


## High energy frontier

## Direct observation



Require $E>m c^{2}$ for direct production

## Precision frontier

## Indirect effects



New particles arise in loop processes

- Most direct particle discoveries have been preceded by indirect evidence first!
- Think charm, bottom and top quarks, even the Higgs
- If we don't see New Physics directly at the LHC, indirect evidence can guide us where to look (or what to build) next


## Standard Model Particles

Standard Model of Elementary Particles


## Standard Model Particles

- Spin-0 particle: Masses of the weak gauge bosons (and fermions) are generated via the Higgs mechanism which gives rise to new scalars. In the simplest realisation this is a single neutral particle, the Higgs boson
- Spin-1/2 particles: Matter consists of fermions: \{quarks, leptons\}, in three generations


## Quarks:

## Leptons:

$$
\binom{u}{d}\binom{c}{s}\binom{t}{b}
$$

$$
\binom{\nu_{e}}{e}\binom{\nu_{\mu}}{\mu}\binom{\nu_{\tau}}{\tau}
$$

Quarks: feel strong, weak and EM (up-type $q=+2 / 3$, down-type $q=-1 / 3$ ). Leptons do not feel strong, $e, \mu$ and $\tau$ EM and weak, $\nu$ only weak

- Spin-1 particles: carry the fundamental interactions via gauge bosons:
- Electromagnetic interaction: photon $\gamma$
- Weak interaction: weak gauge bosons $W^{+}, W^{-}, Z^{0}$
- Strong interaction: gluons $g_{1}, \ldots, g_{8}$

> Nearly all ordinary matter is first generation only

## Parameters of the Standard Model

- 3 gauge couplings
- 2 Higgs parameters


## Flavour Parameters

- 6 quark masses
- 3 quark mixing angles +1 phase [CKM matrix]
- $3(+3)$ lepton masses
- (3 lepton mixing angles +1 phase) [PMNS matrix]

$$
()=\text { with Dirac neutrino masses }
$$

These lectures cover the flavour physics of quarks and I will not discuss neutrinos (much)

## Aspects of flavour physics

- Families / generations
- 3 pairs of quarks
- 3 pairs of leptons
- Why? Do we know this for sure?
- Clear (and not so clear) hierarchies
- $m(t)>m(c)>m(u)$
- $m(b)>m(s)>m(d)$
- $m(\tau)>m(\mu)>m(e)$
- $m\left(\nu_{\tau}\right)>m\left(\nu_{\mu}\right)>m\left(\nu_{e}\right)$ ?
- Mixing and couplings
- Hierarchy in (quark/lepton) mixings?
- Universality
- (no) flavour changing neutral current (FCNC)
- Symmetry (violation)
- $P / C / C P /$ T violation
- Baryon asymmetry of the universe
- Lepton flavour violation / universality?
- Unification


## What's with neutrinos?

- Parity violation / chirality
- Neutrinos are only left-handed
- Anti-neutrinos are only right-handed
- BUT NOT massless!
- What happened to right-handed neutrinos?
- New Physics?
- Probe of Grand Unification?

See Steve Boyd's lectures for more.

## Checkpoint Reached

## 2. Flavour in the SM

## Flavour in the SM

## A brief theoretical interlude which we will flesh out with some history afterwards

- Particle physics can be described to excellent precision by a relatively straightforward and very beautiful theory:

$$
\begin{align*}
\mathcal{L}_{\mathrm{SM}}= & \mathcal{L}_{\text {Gauge }}\left(A_{a}, \psi_{i}\right) \\
& +\mathcal{L}_{\text {Higgs }}\left(\Phi, A_{a}, \psi_{i}\right)  \tag{1}\\
= & -\frac{1}{4} F_{\mu \nu} F^{\mu \nu}+i \bar{\psi} \not D \psi \\
& +\left|D_{\mu} \Phi\right|^{2}-V(\Phi)+\bar{\psi}_{i} Y_{i j} \Phi \psi_{j}+\text { h.c. } \tag{2}
\end{align*}
$$

Gauge terms: describe the gauge fields, $A_{a}$, and their interactions with the massless fermions, $\psi_{i}$
Higgs terms: describe the Higgs field, $\Phi$, and its interactions with the gauge fields and the fermion fields


## Flavour in the SM

- The Gauge part of the Lagrangian is well verified


## SM gauge terms

$$
\mathcal{L}_{\text {Gauge }}=\sum_{j}^{\text {fermions }} i \bar{\psi}_{j} \not D \psi_{j}-\sum_{a}^{\text {forces }} \frac{1}{4} F_{\mu \nu}^{a} F^{\mu \nu, a}
$$

- Parity is seen to be violated in weak interactions [1, 2]
- So we arrange the fermion fields as left-handed doublets and right-handed singlets

$$
\begin{aligned}
\psi= & Q_{L}, U_{R}, D_{R} \text { quarks } \\
& L_{L}, L_{R} \text { leptons }
\end{aligned}
$$

with

Quarks:

$$
Q_{L}=\binom{u_{L}}{d_{L}},\binom{c_{L}}{s_{L}},\binom{t_{L}}{b_{L}}
$$

$$
U_{R}=u_{R}, c_{R}, t_{R}
$$

$$
D_{R}=d_{R}, s_{R}, b_{R}
$$

Leptons:
and $\quad L_{L}=\binom{e_{L}}{\nu_{e L}},\binom{\mu_{L}}{\nu_{\mu L}},\binom{\tau_{L}}{\nu_{\tau L}}$

$$
L_{R}=e_{R}, \mu_{R}, \tau_{R}
$$

## Quark Gauge Couplings

- Without the Higgs we have flavour universal gauge couplings equal for all three generations (huge degeneracy)


## SM quark gauge couplings

$$
\mathcal{L}_{\text {quarks }}=\sum_{j}^{\text {quarks }} i \bar{\psi}_{j} \not D \psi_{j}=\sum_{j}^{3} \underbrace{i \bar{Q}_{L}^{j} \not D_{Q} Q_{L}^{j}}_{\begin{array}{c}
\text { left-handed } \\
\text { doublets }
\end{array}}+\underbrace{i \bar{U}_{R}^{j} \not D_{U} U_{R}^{j}+i \bar{D}_{R}^{j} \not D_{D} D_{R}^{j}}_{\begin{array}{c}
\text { right-handed } \\
\text { singlets }
\end{array}}
$$

leptons have been omitted for simplicity

- Writing out the covariant derivatives we see the chiral nature of the weak force

$$
\begin{array}{rlr}
D_{Q, \mu} & =\partial_{\mu}+i g_{s} \lambda_{\alpha} G_{\mu}^{\alpha}+i g \sigma_{i} W_{\mu}^{i} & +i Y_{Q} g^{\prime} B_{\mu} \\
D_{U, \mu} & =\partial_{\mu}+i g_{s} \lambda_{\alpha} G_{\mu}^{\alpha} & \\
D_{D, \mu} & =\partial_{\mu}+i Y_{U} g^{\prime} B_{\mu} \lambda_{\alpha} G_{\mu}^{\alpha} & \\
\text { strong } & \text { weak } & \mathrm{EM}
\end{array}
$$

and hypercharge $Y_{Q}=1 / 6, Y_{U}=2 / 3, Y_{D}=-1 / 3$

## Yukawa couplings

- In order to realise fermion masses we introduce "Yukawa couplings"
- This is rather ad-hoc. It is necessary to understand the data but is not stable with respect to quantum corrections (the Hierarchy problem).
- By doing this we introduce flavour non-universality via the Yukawa couplings, $Y_{A}$, between the Higgs and the quarks

$$
\begin{aligned}
& \text { SM quark Yukawa (mass) terms } \\
& \mathcal{L}_{\text {Yukawa }}=\sum_{i, j}^{\text {quarks }} \bar{\psi}_{i} Y_{i j} \Phi \psi_{j}+\text { h.c. }=\sum_{i, j}^{3}\left(-\bar{Q}_{L}^{i} Y_{U}^{i j} \Phi^{c} U_{R}^{j}-\bar{Q}_{L}^{i} Y_{D}^{i j} \Phi D_{R}^{j}+\text { h.c. }\right)
\end{aligned}
$$

leptons have been omitted for simplicity
$\Phi^{c}$ gives up-quark masses but is not independent of $\Phi$ in the SM

- Replace $H$ by its vacuum expectation value, $\langle H\rangle=(0, \nu)^{T}$, and we obtain the quark mass terms

$$
\begin{equation*}
\sum_{i, j}^{3}\left(-\bar{u}_{L}^{i} m_{U}^{i j} u_{R}^{j}-\bar{d}_{L}^{i} m_{D}^{i j} d_{R}^{j}\right) \tag{4}
\end{equation*}
$$

with the quark mass matrices given by $m_{A}=\nu Y_{A}$ with $A=(U, D, L)$

## Diagonalising the mass matrices

- Quark mass matrices, $m_{U}, m_{D}, m_{L}$, are $3 \times 3$ complex matrices in "flavour space" with a priori arbitary values.
- We can diagonalise them via a field redefintion

$$
\begin{equation*}
u_{L}=\hat{U}_{L} u_{L}^{m}, \quad u_{R}=\hat{U}_{R} u_{R}^{m}, \quad d_{L}=\hat{D}_{L} d_{L}^{m}, \quad d_{R}=\hat{D}_{R} d_{R}^{m} \tag{5}
\end{equation*}
$$

- such that in the mass eigenstate basis the matrices are diagonal

$$
\begin{equation*}
m_{U}^{\text {diag }}=\hat{U}_{L}^{\dagger} m_{U} \hat{U}_{R}, \quad m_{D}^{\text {diag }}=\hat{D}_{L}^{\dagger} m_{D} \hat{D}_{R} \tag{6}
\end{equation*}
$$

- The right-handed $S U(2)$ singlet is invariant but recall the left-handed $S U(2)$ doublet gives rise to terms like

$$
\begin{equation*}
\frac{g}{\sqrt{2}} \bar{u}_{L}^{i} \gamma_{\mu} W^{\mu} d_{L}^{i} \tag{7}
\end{equation*}
$$

- In the mass basis this then becomes

$$
\begin{equation*}
\frac{g}{\sqrt{2}} \bar{u}_{L}^{i} \underbrace{\hat{U}_{L}^{\dagger i j} \hat{D}_{L}^{j k}}_{\hat{V}_{\mathrm{CKM}}} \gamma_{\mu} W^{\mu} d_{L}^{k} \tag{8}
\end{equation*}
$$

This combination, $\hat{V}_{\mathrm{CKM}}=\hat{U}_{L}^{\dagger i j} \hat{D}_{L}^{j k}$, is the physical CKM matrix and generates flavour violating charged current interactions. It is complex and unitary, $V V^{\dagger}=\mathbb{1}$

## The Standard Model before/after symmetry breaking

## The Standard Model of Particle Physics

Spin 0
(Higgs Boson)


Spin 1/2
(Fermions)


Spin 1
(Gauge Bosons)



Unbroken Symmetry Broken Symmetry



Image source: Wikipedia - Mathematical formulation of the Standard Model

## Flavour in the SM

- CKM matrix transforms the mass eigenstate basis to the flavour eigenstate basis
- and brings with it a rich variety of observable phenomena

$$
\text { mass eigenstates } \neq \text { weak eigenstates }
$$

$$
\left(\begin{array}{c}
d^{\prime}  \tag{9}\\
s^{\prime} \\
b^{\prime}
\end{array}\right)=\left(\begin{array}{ccc}
V_{u d} & V_{u s} & V_{u b} \\
V_{c d} & V_{c s} & V_{c b} \\
V_{t d} & V_{t s} & V_{t b}
\end{array}\right)\left(\begin{array}{l}
d \\
s \\
b
\end{array}\right)
$$

- The up-type quark to down-type quark transition probability is proportional to the squared magnitude of the CKM matrix elements, $\left|V_{i j}\right|^{2}$


Weak coupling

$$
\propto \frac{g}{2 \sqrt{2}} \gamma_{\mu}\left(1-\gamma_{5}\right) V_{i j}
$$

## Lepton and baryon number conservation

- The gauge part of the SM Lagrangian is invariant under $\mathrm{U}(3)$ symmetries of the left-handed doublets and right-handed singlets if the fermions are massless

$$
\mathcal{L}_{\text {Gauge }}=\sum_{j} i \bar{\psi}_{j} \not D \psi_{j}-\sum_{a} \frac{1}{4} F_{\mu \nu}^{a} F^{\mu \nu, a}
$$

- These $U(3)$ symmetries are broken by the Yukawa terms.
- The only remaining symmetries correspond to lepton number and baryon number conservation
- These are "accidental" symmetries, coming from the particle content, rather than being explicitly imposed

We will return to the CKM matrix and CKM metrology later!

## Why is flavour important?

- Most of the free parameters in the SM are related to the flavour sector
- The flavour sector provides the only source of $C P$-violation in the SM
- Flavour changing neutral current processes can probe mass scales well beyond those directly accessible at the LHC
- If there are new particles at the TeV -scale, why don't they manifest themselves in FCNC processes (called the flavour problem)?


## Puzzles in flavour

- Why are there so many parameters and why do they have the values they do?
- Why do we have a flavour structure with 3 generations
- As we will see shortly, we know that we need $\geq 3$ generations to get $C P$-violation. Are there more generations to discover? If not why exactly 3?
- Why do the quarks have a flavour structure that exhibits both smallness and hierarchy?
- Why is the neutrino sector so different (neither small nor hierarchical)?


## Mass and flavour hierarchy?

- Large hierarchy in scale between the masses of the fermions
- Equivalent to having a large hierarchy in the Yukawa couplings
- Why / how is this hierarchy so large and why is $y_{t} \sim 1$ ?

CKM matrix for the quark sector



PMNS matrix for the neutrino sector


## Checkpoint Reached

3. Quark Model History

## Isospin

-What's the difference between a proton $(p)$ and a neutron $\left(n^{0}\right)$ ?

- They have similar masses
- They have a similar strong coupling
- Just have a different charge
- In 1932 Heisenberg proposed that ( $p, n^{0}$ ) are members of an isospin doublet [3]
- Can be treated as the same particle with different isospin projections

$$
p:\left(I, I_{z}\right)=(1 / 2,+1 / 2), \quad n:\left(I, I_{z}\right)=(1 / 2,-1 / 2)
$$

- The pions can be arranged as an isospin triplet

$$
\pi^{+}:\left(I, I_{z}\right)=(1,+1), \quad \pi^{0}:\left(I, I_{z}\right)=(1,0), \quad \pi^{-}:\left(I, I_{z}\right)=(1,-1)
$$

- Isospin is conserved in strong interactions
- Isospin is violated in weak interactions
- We now know this is not the correct model (it's not an exact symmetry) but it's still a very useful concept
- It works because $m_{u} \sim m_{d}<\Lambda_{\mathrm{QCD}}$ and can be used to predict interaction rates:

$$
\sigma\left(p+p \rightarrow d+\pi^{+}\right): \sigma\left(p+n \rightarrow d+\pi^{0}\right)=2: 1
$$

HOMEWORK $\rightarrow$ can you explain this 2:1 ratio?

## Strangeness (the kaon observation)

- In 1947 Rochester and Butler [4] observed two new particles with mass $\sim 500 \mathrm{MeV}$ and long lifetimes
- Neutral particle (no track) $\rightarrow$ two charged pions
- Charged particle (track) $\rightarrow$ charged pion + something
- Long lifetimes, $O\left(10^{-10} s\right)$, so dubbed "strange"

$$
K_{\mathrm{S}}^{0} \rightarrow \pi^{+} \pi^{-}
$$

$$
K^{+} \rightarrow \mu^{+} \nu_{\mu}
$$



## The Quark Model

- Many new particles (a "zoo") discovered in the 50s and 60s
- Gell-Mann, Nakano and Nishijima (1953-1956) [5, 6] suggest conservation of "strangeness"
- Gell-Mann and Ne'eman (1961) [7, 8] introduced the quark "model" ( $u, d, s$ ) which could elegantly categorise them (the "eight-fold way" - flavour $\operatorname{SU}(3)$ symmetry) ${ }^{[i]}$
- Gell-Mann and Pais [9, 10]
- Strangeness conserved in strong interactions (production)
- Strangeness violated in weak interactions (decay)
${ }^{[1]}$ The famous "Eight-fold way" was never even published $\rightarrow$ publish your work!


## The Quark Model

- Can only make colour neutral objects
- Quark anti-quark mesons ( $q \bar{q}$ ) or three quark baryons ( $q q q$ ). Nearly all known states fall into one of these two categories
- Can also build colour neutral states containing more quarks (e.g. 4 or 5 quark states). Only quite recently confirmed (and still not entirely understood).



## The Quark Model

## Gell-Mann knew about tetraquarks and pentquarks $[11,12]$

A SCHEMATIC MODEL OF BARYONS AND MESONS *<br>M. GELL-MANN<br>Califomia Instilute of Technology. Pasadena, California

Received 4 January 1964

If we assume that the strong interactions of baryons and mesons are correctly described in terms of the broken "eightfold way" 1-3), we are tempted to look for some fundamental explanation of the situation. A highly promised approach is the pureiy dynamical 'bootstrap' model for all the strongly interacting particles within which one may try to derive isotopic spin and strangeness conservation and broken eightold symmetry from self-consistency alone 4). Of course, with only strong interactions, the orientation of the asymmetry in the unitary space cannot be specified; one hopes that in some way the selection of specific components of the Fspin by electromagnetism and the weak interactions determines the choice of isotopic spin and hypercharge directions.

Even if we consider the scattering amplitudes of strongly interacting particles on the mass shell only and treat the matrix elements of the weak, electromagnetic, and gravitational interactions by means
ber $n_{\mathrm{t}}$ - $n_{\mathrm{t}}^{\mathrm{T}}$ would be zero for all known baryons and mesons. The most interesting example of such a model is one in which the triplet has spin $\frac{1}{2}$ and $z=-1$, so that the four particles $\mathrm{d}^{-}, \mathrm{s}^{-}, u^{0}$ and $\mathrm{b}^{0}$ exhibit a parallel with the leptons.

A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon $b$ if we assign to the triplet the following properties: $\operatorname{spin} \frac{1}{2}, z=-\frac{1}{3}$, and baryon number $\frac{1}{3}$. We then refer to the members $\mathrm{u}^{\frac{2}{3}}, \mathrm{~d}^{-\frac{1}{3}}$, and $\mathrm{s}^{-\frac{1^{2}}{3}}$ of the triplet as "quarks" ${ }^{6}$ ) $q$ and the members of the anti-triplet as anti-quarks $\bar{q}$. Baryons can now be constructed from quarks by using the combinations ( $q q q$ ), ( $q q q q q$ ), etc., while mesons are made out of $(q \bar{q})$, ( $q q \bar{q} \bar{q}$ ), etc. It is assuming that the lowes baryon configuration (qqq) gives just the representations 1,8 , and 10 that have been observed, whils the lowest meson configuration ( $q \bar{q}$ ) similarly give: just 1 and 8.

## The Quark Model

SU(2) flavour mixing

- Four possible combinations from two quarks ( $u$ and $d$ )

$$
u \bar{u}, d \bar{d}, u \bar{d}, \bar{u} d
$$

- Under $\mathrm{SU}(2)$ symmetry the $\pi$ and $\eta$ states are members of an isospin triplet and singlet respectively

$$
\pi^{0}=\frac{1}{\sqrt{2}}(u \bar{u}-d \bar{d}), \quad \eta=\frac{1}{\sqrt{2}}(u \bar{u}+d \bar{d})
$$

SU(3) flavour mixing

- Introducing the strange quark (under SU(3) symmetry) we now have an octuplet and a singlet

$$
\pi^{0}=\frac{1}{\sqrt{2}}(u \bar{u}-d \bar{d}), \quad \eta_{1}=\frac{1}{\sqrt{3}}(u \bar{u}+d \bar{d}+s \bar{s}), \quad \eta_{8}=\frac{1}{\sqrt{6}}(u \bar{u}+d \bar{d}-2 s \bar{s})
$$

- The physical states involve a further mixing

$$
\eta=\eta_{1} \cos \theta+\eta_{8} \sin \theta, \quad \eta^{\prime}=-\eta_{1} \sin \theta+\eta_{8} \cos \theta
$$

## The Quark Model

- Can elegantly categorise states by isospin (up/downess) and strangeness
- Also get the excited states which can be categorised in the same way

Spin-0 Mesons


Spin-1/2 Baryons


Homework

- What is the quark content of these states?
- Do you know the spin-1 (spin-3/2) states?


## The Cabibbo Angle

- Compare rates of:

$$
\begin{array}{lll}
s \rightarrow u: & K^{+} \rightarrow \mu^{+} \nu_{\mu} & \left(\Lambda^{0} \rightarrow p \pi^{-}, \Sigma^{+} \rightarrow n e^{+} \nu_{e}\right) \\
d \rightarrow u: & \pi^{+} \rightarrow \mu^{+} \nu_{\mu} & \left(n \rightarrow p e^{+} \nu_{e}\right)
\end{array}
$$

- Apparent that $s \rightarrow u$ transitions are suppressed by a factor $\sim 20$
- Cabibbo (1963) [13] suggested that "down-type" is some ad-mixture of $d$ and $s$
- The first suggestion of quark mixing
- Physical state is an admixture of flavour states

$$
\begin{equation*}
\binom{u}{d^{\prime}}=\binom{u}{d \cos \left(\theta_{C}\right)+s \sin \left(\theta_{C}\right)} \tag{10}
\end{equation*}
$$

- The mixing angle is determined experimentally to be $\sin \left(\theta_{C}\right)=0.22$.


## GIM mechanism

- Cabibbo's solution opened up a new experimental problem
- $K^{+} \rightarrow \mu^{+} \nu_{\mu}$ had been seen but not $K_{\mathrm{L}}^{0} \rightarrow \mu^{+} \mu^{-}$
$-\mathcal{B}\left(K_{\mathrm{L}}^{0} \rightarrow \mu^{+} \mu^{-}\right) \approx 7 \times 10^{-9}$
- $\mathcal{B}\left(K_{\mathrm{L}}^{0} \rightarrow e^{+} e^{-}\right) \approx 1 \times 10^{-11}$
- $K^{+} \rightarrow \pi^{0} \mu^{+} \nu_{\mu}$ had been seen but not $K_{\mathrm{L}}^{0} \rightarrow \pi^{0} \mu^{+} \mu^{-}$

$$
-\mathcal{B}\left(K_{\mathrm{L}}^{0} \rightarrow \pi^{0} \mu^{+} \mu^{-}\right) \approx 1 \times 10^{-10}
$$

- If the doublet of the weak interaction is the one Cabibbo suggested, Eq. (10), then one can have neutral currents

$$
\begin{equation*}
J_{\mu}^{0}=\bar{d}^{\prime} \gamma_{\mu}\left(1-\gamma_{5}\right) d^{\prime} \tag{11}
\end{equation*}
$$

which introduces tree level FCNCs (which we don't see)

- Glashow, Iliopoulos and Maiani (1970) provided a solution by adding a second doublet

$$
\begin{equation*}
\binom{c}{s^{\prime}}=\binom{c}{-d \sin \left(\theta_{C}\right)+s \cos \left(\theta_{C}\right)} \tag{12}
\end{equation*}
$$

- This exactly cancels the term above, Eq. (11)
- Thus FCNC contributions are suppressed via loops


## GIM suppression

- Consider the $s \rightarrow d$ transition required for $K_{\mathrm{L}}^{0} \rightarrow \mu^{+} \mu^{-}$
- Given that $m_{u}, m_{c} \ll m_{W}$

$$
\begin{aligned}
\mathcal{A} & \approx V_{u s} V_{u d}^{*}+V_{c s} V_{c d}^{*} \\
& =\sin \left(\theta_{C}\right) \cos \left(\theta_{C}\right)-\cos \left(\theta_{C}\right) \sin \left(\theta_{C}\right) \\
& =0
\end{aligned}
$$

- Indeed $2 \times 2$ unitarity implies that

$$
V_{u s} V_{u d}^{*}+V_{c s} V_{c d}^{*}=0
$$

- Predicts the existence of the charm quark:
- Kaon mixing

- Low branching fractions for FCNC decays


## Observation of the $J / \psi$

- Experimental evidence for the charm quark came in 1974
- Discovery of charmonium $(J)$ at Brookhaven in $p \mathrm{Be} \rightarrow \mathrm{e}^{+} \mathrm{e}^{-} \mathrm{X}$ [14]
- Discovery of charmonium $(\psi)$ at SLAC in $e^{+} e^{-} \rightarrow$ (hadrons), $\mathrm{e}^{+} \mathrm{e}^{-}, \mu^{+} \mu^{-}$[15]



FIG. 2. Mass spectrum showing the existence of $J$. sults from two spectrometer settings are plotted swing that the peak is independent of spectrometer rents. The rum at reduced current was taken two nths later than the normal run.

## Charmed Quarks

- We now have a quark model with 4 flavours and one mixing angle

$$
\binom{d^{\prime}}{s^{\prime}}=\left(\begin{array}{rr}
\cos \theta_{C} & -\sin \theta_{C} \\
\sin \theta_{C} & \cos \theta_{C}
\end{array}\right)\binom{d}{s}
$$

- Our quark mixing matrix is a $2 \times 2$ rotation matrix with a single mixing angle (the Cabibbo angle)
- We will now see why the discovery of $C P$ violation requires a third generation of quarks


## Charmed Multiplets

Mesons

Spin-0


Spin-1


## Charmed Multiplets

## Baryons

Spin-1/2


Spin-3/2


## Parity violation

- Two decays were found for charged strange mesons
- $\theta \rightarrow \pi^{+} \pi^{0}$
- $\tau \rightarrow \pi^{+} \pi^{-} \pi^{+}$
- The $\theta-\tau$ puzzle
- Masses and lifetimes of $\theta$ and $\tau$ are the same
- But $2 \pi$ and $3 \pi$ final states have the opposite parity
- The resolution is that $\theta$ and $\tau$ are the same particle, $K^{+}$, and parity is violated in the decay [1]


## $C$ and $P$

- Prior to 1956 it was thought that the laws of physics were invariant under parity, $P$, (i.e. a mirrored reflection)
- Shown to be violated in $\beta$ decays of Co-60 by Wu [2] (following an idea by Lee and Yang [1])
- Now known that parity, $P$, is maximally violated in weak decays
- There are no right-handed neutrinos
- Charge, $C$, is also maximally violated in weak decays
- There is no left-handed anti-neutrino
- The product $C P$ is conserved (Landau 1957 [16]) and distinguishes absolutely between matter and antimatter
- The product CPT is conserved in any Lorentz
 invariant gauge field theory


## Neutral Kaon Mixing

HOMEWORK: draw the mixing diagrams for $K^{0} \rightarrow \bar{K}^{0}$ in a 4 quark model

- Ignoring $C P$-violation, in the neutral kaon system the two physical (mass/lifetime) states are admixtures of the strangeness (flavour) states

$$
\begin{equation*}
\left|K_{1}\right\rangle=\frac{\left|K^{0}\right\rangle-\left|\bar{K}^{0}\right\rangle}{\sqrt{2}} \quad \text { and } \quad\left|\mathrm{K}_{2}\right\rangle=\frac{\left|\mathrm{K}^{0}\right\rangle+\left|\overline{\mathrm{K}}^{0}\right\rangle}{\sqrt{2}} \tag{13}
\end{equation*}
$$

under parity, $P$, and charge conjugation, $C$, the flavour states transform as

$$
\begin{equation*}
\mathcal{P}\left|K^{0}\right\rangle=-\left|K^{0}\right\rangle, \quad \mathcal{C}\left|K^{0}\right\rangle=\left|\bar{K}^{0}\right\rangle \quad \text { and } \quad \mathcal{C} \mathcal{P}\left|K^{0}\right\rangle=-\left|\bar{K}^{0}\right\rangle \tag{14}
\end{equation*}
$$

- For the physical states

$$
\begin{equation*}
\mathcal{P}\left|K_{1,2}\right\rangle=-\left|K_{1,2}\right\rangle, \quad \mathcal{C}\left|K_{1,2}\right\rangle=\mp\left|K_{1,2}\right\rangle \quad \text { and } \quad \mathcal{C P}\left|K_{1,2}\right\rangle= \pm\left|K_{1,2}\right\rangle \tag{15}
\end{equation*}
$$

i.e. they are eigenstates of $P, C$ and $C P$ as well.

- What does this tell us about their decays?
- $\pi^{+} \pi^{-} \quad$ has $P=+1, C=+1, C P=+1$ - shorter lived $K_{1}=K_{\mathrm{S}}^{0}$
- $\pi^{+} \pi^{-} \pi^{0}$ has $P=-1, C=+1, C P=-1$ - longer lived $K_{2}=K_{\mathrm{L}}^{0}$
- If $C P$ is preserved $K_{\mathrm{L}}^{0}$ decay to two pions should be forbidden


## $C P$-violation

- In 1964 Christenson, Cronin, Fitch and Turlay observed $2 \pi$ decays of the $K_{2}\left(K_{\mathrm{L}}^{0}\right)$ meson (this is a beautiful experiment) [17]

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## CKM mechanism

- In 1973 Kobayashi and Maskawa [18] introduce the CKM mechanism to explain $C P$-violation (this paper is rather impenetrable)
- As we will see this requires a third generation of quark and so they predict the existence of $b$ and $t$ quarks


## CP Violation in the Renormalizable Theory of Weak Interaction

Makoto Kobayashi, Toshihide Maskawa (Kyoto U.)<br>Feb 1973-6 pages<br>Prog.Theor.Phys. 49 (1973) 652-657<br>Also in *Lichtenberg, D. B. (Ed.), Rosen, S. P. (Ed.): Developments In The Quark Theory Of Hadrons, Vol. 1*, 218-223.<br>DOI: 10.1143/PTP.49.652<br>KUNS-242

[^0]
## CKM mechanism

- Kobayashi, Maskawa paper intially went largely unnoticed (be patient with your papers), it now was has $>10 \mathrm{~K}$ citations
- They were the first to write down what we now know as the CKM martix, although they had a mistake

$$
\begin{aligned}
\left.\begin{array}{lll}
\cos \theta_{1} & -\sin \theta_{1} \cos \theta_{3} & -\sin \theta_{1} \sin \theta_{3} \\
\sin \theta_{1} \cos \theta_{2} & \cos \theta_{1} \cos \theta_{2} \cos \theta_{3}-\sin \theta_{2} \sin \theta_{3} e^{i 8} & \cos \theta_{1} \cos \theta_{2} \sin \theta_{3}+\sin \theta_{2} \cos \theta_{8} e^{i 8} \\
\sin \theta_{1} \sin \theta_{2} & \cos \theta_{1} \sin \theta_{2} \cos \theta_{3}+\cos \theta_{2} \sin \theta_{3} e^{i \delta} & \cos \theta_{1} \sin \theta_{2} \sin \theta_{3}-\cos \theta_{2} \sin \theta_{3} e^{i \delta}
\end{array}\right) \xrightarrow[\theta_{3}=\delta=0]{\theta_{1}=\theta_{2}=0}\left(\begin{array}{lll}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 0
\end{array}\right) \\
\rightarrow \text { Whoops! }
\end{aligned}
$$

- It didn't really start getting noticed until it was picked up by Pakvasa and Sugawara [19]
- They fixed that mistake but introduced a new one!

$$
\left(\begin{array}{ccc}
\cos \theta_{1} & -\sin \theta_{1} \cos \theta_{3} & -\sin \theta_{1} \sin \theta_{3} \\
\sin \theta_{1} \cos \theta_{2} & \cos \theta_{1} \cos \theta_{2} \cos \theta_{3}-\sin \theta_{2} \sin \theta_{3} e^{i \sigma} & \cos \theta_{1} \cos \theta_{2} \sin \theta_{3}+\sin \theta_{2} \cos \theta_{3} e^{i \delta} \\
\sin \theta_{1} \sin \theta_{2} & \cos \theta_{1} \sin \theta_{2} \cos \theta_{3}+\cos \theta_{2} \sin \theta_{3} e^{i 6} & \cos \theta_{1} \sin \theta_{2} \sin \theta_{3}-\cos \theta_{2} \cos \theta_{3} e^{i 6}
\end{array}\right) \xrightarrow[\theta_{3}=\delta=0]{\theta_{1}=\theta_{2}=0}\left(\begin{array}{ccc}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & -1
\end{array}\right)
$$

## CKM mechanism

- Eventually (1984) Chau and Keung wrote it down without mistakes [20]
- This has been the PDG version since 1988
- We will now study this parameterisation and see another one which exploits the small size of $\lambda=\sin \theta_{C}$ as an expansion parameter

$$
\begin{aligned}
& 3^{\text {rd }} \text { rotate } \quad 2^{\text {nd }} \text { rotate around } s^{\prime} \\
& 1^{\text {st }} \text { rotate } \\
& \left(\begin{array}{ccc}
\text { around } d^{\prime \prime} \\
1 & 0 & 0 \\
0 & c_{y} & s_{y} \\
0 & -s_{y} & c_{y}
\end{array}\right)\left(\begin{array}{ccc}
c_{z} & 0 & s_{z} e^{-i \phi} \\
0 & 1 & 0 \\
-s_{z} e^{i \phi} & 0 & c_{z}
\end{array}\right)\left(\begin{array}{ccc}
c_{x} & s_{x} & 0 \\
-s_{x} & c_{x} & 0 \\
0 & 0 & 1
\end{array}\right)=\left(\begin{array}{ccc}
c_{x} c_{z} & s_{x} c_{z} & s_{z} e^{-i \phi} \\
-s_{x} c_{y}-c_{x} s_{y} s_{z} e^{i \phi} & c_{x} c_{y}-s_{x} s_{y} s_{z} e^{i \phi} & s_{y} c_{z} \\
s_{x} s_{y}-c_{x} c_{y} s_{z} e^{i \phi} & -c_{x} s_{y}-s_{x} c_{y} s_{z} e^{i \phi} & c_{y} c_{z}
\end{array}\right) \xrightarrow[\theta_{3}=\theta_{2}=0]{\longrightarrow}\left(\begin{array}{ccc}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{array}\right)
\end{aligned}
$$

- But first let's quickly see the top and bottom discoveries for completeness


## Discovery of bottomonium

- Kobayashi and Maskawa's matrix and mechanism for $C P$ violation predicted the existence of a third generation
- The $\Upsilon(b \bar{b})$ resonance was discovered at Fermilab in 1977 [21]
- The top wasn't discovered until 1995 at the CDF and D0 experiments [22,23]
$\Upsilon$ discovery at E288


Top discovery at CDF


We now have a full model of all three generations including mixing and CPV, so next lecture we will see what phenomenology this produces

## Checkpoint Reached

## 4. The CKM Matrix

## Parameters of the CKM matrix

- $3 \times 3$ complex matrix
- 18 parameters
- Unitary
- 9 parameters (3 mixing angles, 6 complex phases)
- Quark fields absorb 5 of these (unobservable) phases
- Left with:
- 3 mixing angles $\left(\theta_{12}, \theta_{23}, \theta_{13}\right)$
- one complex phase ( $\delta$ ) which gives rise to $C P$-violation in the SM


## The CKM Matrix

$$
V_{\mathrm{CKM}}=\left(\begin{array}{ccc}
V_{u d} & V_{u s} & V_{u b} \\
V_{c d} & V_{c s} & V_{c b} \\
V_{t d} & V_{t s} & V_{t b}
\end{array}\right)
$$

- A highly predictive theory


## Parameters of the CKM matrix

- Absorbing quark phases can be done because under a quark phase transformation

$$
\begin{equation*}
u_{L}^{i} \rightarrow e^{i \phi_{u}^{i}} u_{L}^{i}, \quad d_{L}^{i} \rightarrow e^{i \phi_{d}^{i}} d_{L}^{i} \tag{16}
\end{equation*}
$$

and a simultaneous rephasing of the CKM matrix $\left(V_{j k} \rightarrow e^{i\left(\phi_{j}-\phi_{k}\right)} V_{j k}\right)$

$$
V_{\mathrm{CKM}} \rightarrow\left(\begin{array}{ccc}
e^{i \phi_{u}} & &  \tag{17}\\
& e^{i \phi_{c}} & \\
& & e^{i \phi_{t}}
\end{array}\right)\left(\begin{array}{ccc}
V_{u d} & V_{u s} & V_{u b} \\
V_{c d} & V_{c s} & V_{c b} \\
V_{t d} & V_{t s} & V_{t b}
\end{array}\right)\left(\begin{array}{ccc}
e^{i \phi_{d}} & & \\
& e^{i \phi_{s}} & \\
& & e^{i \phi_{b}}
\end{array}\right)
$$

the charged current $J^{\mu}=\bar{u}_{L i} V_{i j} \gamma^{\mu} d_{L j}$ is left invariant

- So all additional quark phases are rephased to be relative to just one


## Degrees of freedom in an $N$ generation CKM matrix

| Number of generations | $\mathbf{2}$ | $\mathbf{3}$ | $N$ |
| :--- | ---: | ---: | :--- |
| Number of real parameters | 4 | 9 | $N^{2}$ |
| Number of imaginary parameters | 4 | 9 | $N^{2}$ |
| Number of constraints $\left(V V^{\dagger}=\mathbb{1}\right)$ | -4 | -9 | $-N^{2}$ |
| Number of relative quark phases | -3 | -5 | $-(2 N-1)$ |
| Total degrees of freedom | 1 | 4 | $(N-1)^{2}$ |
| Number of Euler angles | 1 | 3 | $N(N-1) / 2$ |
| Number of $C P$ phases | 0 | 1 | $(N-1)(N-2) / 2$ |

## CKM parameterisations

- The standard form is to express the CKM matrix in terms of three rotation matrices and one $C P$-violating phase ( $\delta$ ) [20]

$$
\begin{align*}
V_{\mathrm{CKM}} & =\underbrace{\left(\begin{array}{ccc}
1 & 0 & 0 \\
0 & c_{23} & s_{23} \\
0 & -s_{23} & c_{23}
\end{array}\right)}_{\text {2nd and 3rd gen. mixing }} \underbrace{\left(\begin{array}{ccc}
c_{13} & 0 & s_{13} e^{-i \delta} \\
0 & 1 & 0 \\
-s_{13} e^{+i \delta} & 0 & c_{13}
\end{array}\right)}_{\text {1st and 3rd gen. mixing }+\mathrm{CPV} \text { phase }} \underbrace{\left(\begin{array}{ccc}
c_{12} & s_{12} & 0 \\
-s_{12} & c_{12} & 0 \\
0 & 0 & 1
\end{array}\right)}_{\text {1st and 2nd gen. mixing }}  \tag{18}\\
& =\left(\begin{array}{ccc}
\left(\begin{array}{ccc}
\left(c_{12} c_{13}\right. & s_{12} c_{13} & s_{13} e^{-i \delta} \\
-s_{12} c_{23}-c_{12} s_{23} s_{13} e^{i \delta} & c_{12} c_{23}-s_{12} s_{23} s_{13} e^{i \delta} & s_{23} c_{13} \\
s_{12} s_{23}-c_{12} c_{23} s_{13} e^{-i \delta} & -c_{13} s_{23}-s_{12} c_{23} s_{13} e^{i \delta} & c_{23} c_{13}
\end{array}\right)
\end{array}\right. \tag{19}
\end{align*}
$$

where

$$
c_{i j}=\cos \left(\theta_{i j}\right) \quad \text { and } \quad s_{i j}=\sin \left(\theta_{i j}\right)
$$

## CKM parameterisations

- Emprically $s_{12} \sim 0.2, s_{23} \sim 0.04, s_{13} \sim 0.004$, i.e. $s_{13} \ll s_{23} \ll s_{12}$
- CKM matrix exhibits a very clear hierarchy
- The so-called Wolfenstein parameterisation [24] exploits this
- Expand in powers of $\lambda=\sin \left(\theta_{12}\right)$
- Use four real parameters which are all $\sim O(1),(A, \lambda, \rho, \eta)$ where

$$
\lambda=s_{12}, A \lambda^{2}=s_{23}, A \lambda^{3}(\rho+i \eta)=s_{13} e^{i \delta}
$$

## The CKM Wolfenstein parameterisation

$$
V_{\mathrm{CKM}}=\left(\begin{array}{ccc}
1-\lambda^{2} / 2 & \lambda & A \lambda^{3}(\rho-i \eta) \\
-\lambda & 1-\lambda^{2} / 2 & A \lambda^{2} \\
A \lambda^{3}(1-\rho-i \eta) & -A \lambda^{2} & 1
\end{array}\right)+\mathcal{O}\left(\lambda^{4}\right)
$$

- The CKM matrix is almost diagonal
- Provides strong constraints on NP models in the flavour sector
- Have seen already that quark masses also exhibit a clear hierarchy
- The flavour hierarchy problem
- Where does this structure come from?


## CKM Unitarity Constraints

- The unitary nature of the CKM matrix provides several constraints, $V V^{\dagger}=\mathbb{1}$
- The ones for off-diagonal elements consist of three complex numbers summing to 0
- Hence why these are often represented as triangles in the real / imaginary plane (see next slide)
Constraints along diagonal


## Constraints off-diagonal

$$
\begin{aligned}
& \left|V_{u d}\right|^{2}+\left|V_{u s}\right|^{2}+\left|V_{u b}\right|^{2}=1 \\
& \left|V_{c d}\right|^{2}+\left|V_{c s}\right|^{2}+\left|V_{c b}\right|^{2}=1 \\
& \left|V_{t d}\right|^{2}+\left|V_{t s}\right|^{2}+\left|V_{t b}\right|^{2}=1
\end{aligned}
$$

$$
V_{u d} V_{u s}^{*}+V_{c d} V_{c s}^{*}+V_{t d} V_{t s}^{*}=0
$$

$$
V_{u d} V_{u b}^{*}+V_{c d} V_{c b}^{*}+V_{t d} V_{t b}^{*}=0
$$

$$
V_{u s} V_{u b}^{*}+V_{c s} V_{c b}^{*}+V_{t s} V_{t b}^{*}=0
$$

$$
\left|V_{u d}\right|^{2}+\left|V_{c d}\right|^{2}+\left|V_{t d}\right|^{2}=1
$$

$$
\left|V_{u s}\right|^{2}+\left|V_{c s}\right|^{2}+\left|V_{t s}\right|^{2}=1
$$

$$
\left|V_{u b}\right|^{2}+\left|V_{c b}\right|^{2}+\left|V_{t b}\right|^{2}=1
$$

$$
\begin{aligned}
& V_{u d} V_{c d}^{*}+V_{u s} V_{c s}^{*}+V_{u b} V_{c b}^{*}=0 \\
& V_{u d} V_{t d}^{*}+V_{u s} V_{t s}^{*}+V_{u b} V_{t b}^{*}=0 \\
& V_{c d} V_{t d}^{*}+V_{c s} V_{t s}^{*}+V_{c b} V_{t b}^{*}=0
\end{aligned}
$$

## CKM Unitarity Triangles and the Jarlskog Invariant

- The off-diagonal constraints can be represented as triangles in the complex plane

$$
\begin{gathered}
V_{u d} V_{u s}^{*}+V_{c d} V_{c s}^{*}+V_{t d} V_{t s}^{*}=0 \\
\lambda+\lambda+\lambda^{5} \\
V_{u d} V_{u b}^{*}+V_{c d} V_{c b}^{*}+V_{t d} V_{t b}^{*}=0 \\
\lambda^{3}+\lambda^{3}+\lambda^{3} \\
V_{u s} V_{u b}^{*}+V_{c s} V_{c b}^{*}+V_{t s} V_{t b}^{*}=0 \\
\lambda^{4}+\lambda^{2}+\lambda^{2}
\end{gathered}
$$



- All the triangles have the equivalent area (known as the Jarlskog invariant), $J / 2$
- $J$ is a phase convention independent measure of $C P$-violation in the quark sector

$$
\begin{equation*}
|J|=\operatorname{Im}\left(V_{i j} V_{k l} V_{k j}^{*} V_{i l}^{*}\right) \text { for } i \neq k \text { and } j \neq k \tag{21}
\end{equation*}
$$

- In the standard notation

$$
\begin{equation*}
J=c_{12} c_{13}^{2} c_{23} s_{12} s_{23} s_{13} \sin (\delta) \tag{22}
\end{equation*}
$$

- The small size of the Euler angles means $J$ (and $C P$-violation) is small in the SM


## A clue to our existence: The matter-antimatter asymmetry

- From CMB measurements by WMAP and Plank

$$
\begin{equation*}
\frac{n_{B}-n_{\bar{B}}}{n_{\gamma}} \approx 6 \times 10^{-10} \tag{23}
\end{equation*}
$$

- In the early hot universe we expect annihilation (upon expansion and cooling) to give

$$
\begin{equation*}
n_{B} \approx n_{\bar{B}} \approx n_{\gamma} \tag{24}
\end{equation*}
$$

- The matter-antimatter imbalance is certainly small but far too large to be explained by electroweak baryogenesis.
- But $C P$-violation in the quark sector is too small because of the size of the mixing angles and the large hierarchy of quark masses.
Sakharov (1967) conditions [25] ${ }^{[i i]}$ :
- required for a matter dominated universe from a symmetric initial state

1. Baryon number violation
2. $C$ and $C P$ violation
3. Interactions out of thermal equilibrium
${ }^{[i i]}$ Took 10 years for Sakharov's paper [25] to get cited, it now has $>4000$ - be patient with your papers

## Generating a Baryon Asymmetry

- If we start with equal amounts of matter ( $M$ ) and antimatter $(\bar{M})$
- And assume there are only two possible decay modes:
- $M \rightarrow A$ (baryon number $N_{A}$ ) with probability $p$
- $M \rightarrow B$ (baryon number $\quad N_{B}$ ) with probability $(1-p)$
- $\bar{M} \rightarrow \bar{A}$ (baryon number $-N_{A}$ ) with probability $\bar{p}$
- $\bar{M} \rightarrow \bar{B}$ (baryon number $-N_{B}$ ) with probability $1-\bar{p}$
- Generated baryon asymmetry:

$$
\begin{align*}
\Delta N_{\mathrm{tot}} & =N_{A} p+N_{B}(1-p)-N_{A} \bar{p}-N_{B}(1-\bar{p})  \tag{25}\\
& =(p-\bar{p})\left(N_{A}-N_{B}\right) \tag{26}
\end{align*}
$$

- To have $\Delta N_{\text {tot }} \neq 0$ requires both $p \neq \bar{p}$ and $N_{A} \neq N_{B}$
- i.e. need baryon number violation and $C P$ violation
- Even then, the system needs to be out of thermal equilibrium otherwise

$$
\begin{equation*}
\Gamma(A \rightarrow B+C)=\Gamma(B+C \rightarrow A) \tag{27}
\end{equation*}
$$

and the asymmetry is destroyed as soon as it's created
Would be a great time to talk about phase transitions in the early universe - I don't have time but see Alex Lenz's lecture notes for a good summary

## Jarlskog Invariant and BAU

- We can estimate the size of the BAU from $C P$-violation in the quark sector using the Jarlskog invariant

$$
\begin{equation*}
\frac{n_{B}-n_{\bar{B}}}{n_{\gamma}} \approx \frac{n_{B}}{n_{\gamma}} \sim \frac{J \times P_{u} \times P_{d}}{M^{12}} \tag{28}
\end{equation*}
$$

where

$$
\begin{align*}
J & =\cos \left(\theta_{12}\right) \cos \left(\theta_{23}\right) \cos ^{2}\left(\theta_{13}\right) \sin \left(\theta_{12}\right) \sin \left(\theta_{23}\right) \sin \left(\theta_{13}\right) \sin (\delta)  \tag{29}\\
P_{u} & =\left(m_{t}^{2}-m_{c}^{2}\right)\left(m_{c}^{2}-m_{u}^{2}\right)\left(m_{t}^{2}-m_{u}^{2}\right)  \tag{30}\\
P_{d} & =\left(m_{b}^{2}-m_{s}^{2}\right)\left(m_{s}^{2}-m_{d}^{2}\right)\left(m_{b}^{2}-m_{d}^{2}\right)  \tag{31}\\
M & =\text { mass scale } \tag{32}
\end{align*}
$$

- Take the mass scale as the electroweak scale - $O(100 \mathrm{GeV})$
- Generates an asymmetry of $O\left(10^{-17}\right) \ll$ than the cosmological observation of $O\left(10^{-10}\right)$
Thus $C P$-violation in the quark sector cannot explain the observed matter-antimatter asymmetry of the universe


## Where is the rest of the $C P$-violation?

- SM insufficient to describe the BAU
- A large asymmetry requires
- New sources of $C P$ violation
- At higher energy scales
- Where might this be?
- Quark sectors
- Discrepancies with CKM predictions
- Lepton sector
- $C P$ violation in the neutrino sector
- New Physics
- New forces, extra dimensions, lepto-quarks, $Z^{\prime}, W^{\prime \pm}$
- Many flavour observables are sensitive to generic additions to the SM (we discuss this more in Lecture 4)


## Prospects for Flavour Physics

- Historically provide evidence before the energy frontier
- GIM mechanism before discovery of charm
- CKM mechanism before discovery of bottom and top
- Neutral currents before the Z
- Electroweak precision before the Higgs
- Very sensitive to loop processes
- Massive virtual particles
- SM contributions heavily suppressed (or not allowed)
- Flavour changing neutral currents
- Penguin decays (CPV from interference between tree and loop)
- Lepton flavour universality


## Checkpoint Reached

## 5. Recap

## Recap



## Recap

In this lecture we have covered

- What is (and what is not) flavour physics
- Flavour in the SM
- The Quark Model in the SM
- Isospin
- Strangeness
- Cabibbo Mixing
- The GIM mechanism
- $P$ and $C P$ violation
- The CKM matrix
- CKM parameterisations and hierarchy
- Unitarity triangles
- The Jarlskog invariant and the Matter-antimatter asymmetry


## End of Lecture 1

## End of Lecture 1

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[^0]:    Abstract (Oxford Journals)
    In a framework of the renormalizable theory of weak interaction, problems of CPviolation are studied. It is concluded that no realistic models of CP-violation exist in the quartet scheme without introducing any other new fields. Some possible models of CP-violation are also discussed.

