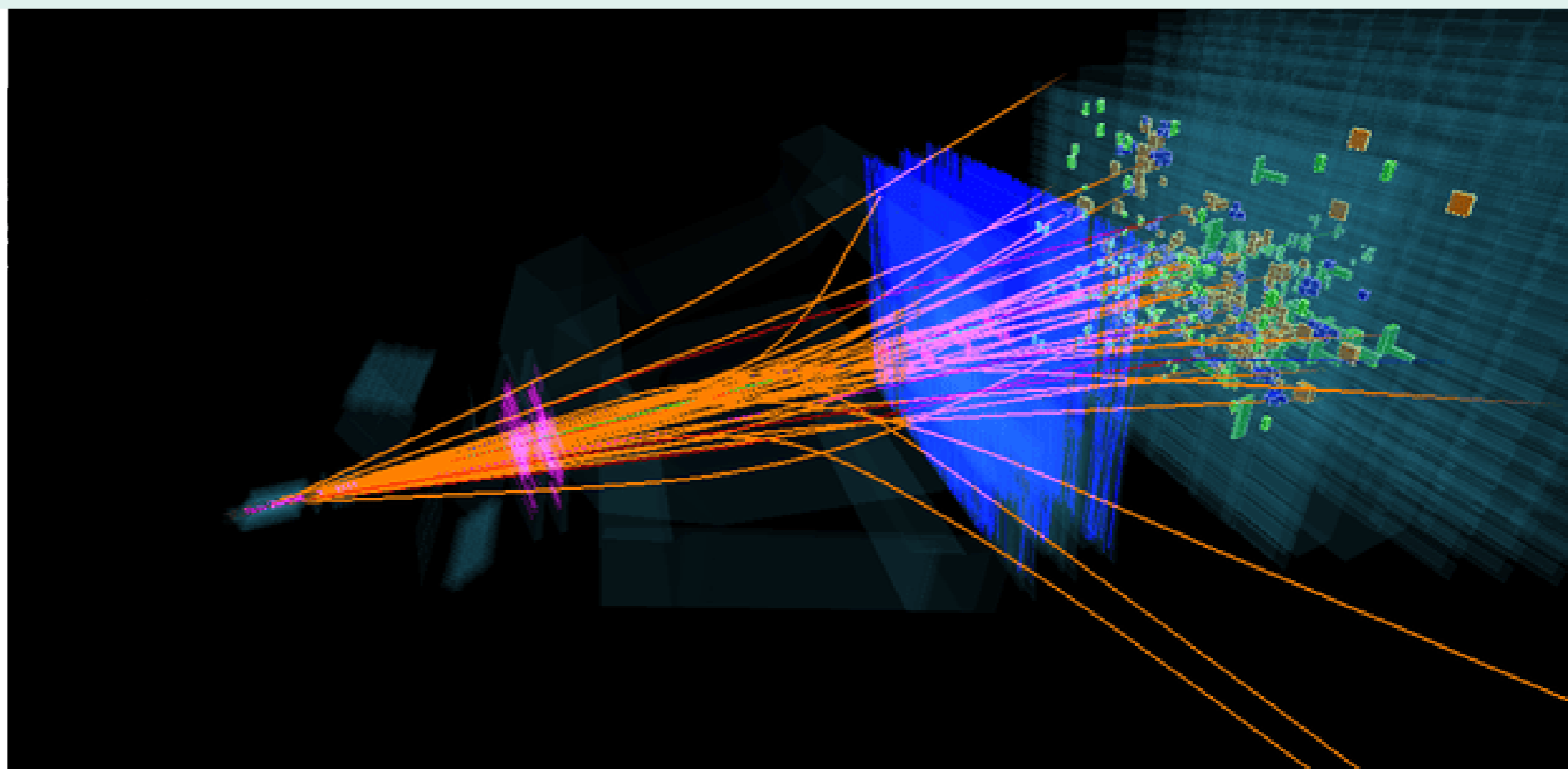
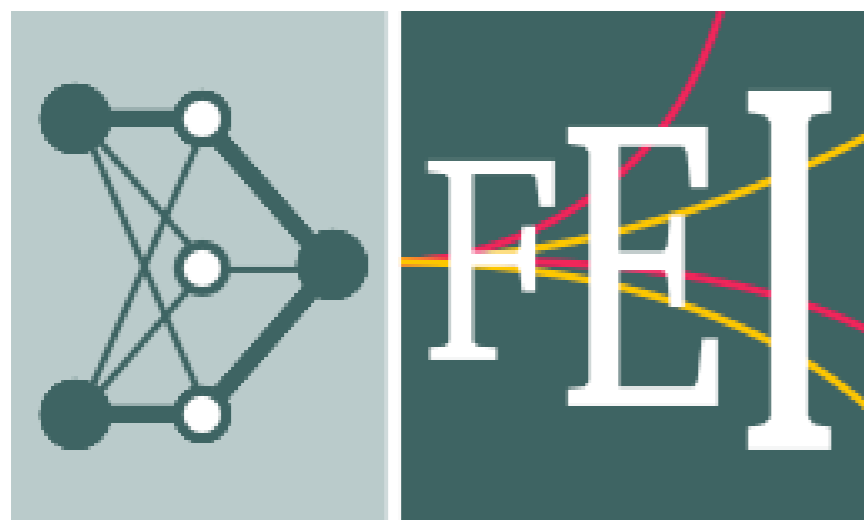


GNN for Deep Full Event Interpretation and hierarchical reconstruction of heavy-hadron decays in proton-proton collisions



Julián García Pardiñas^{1,2}, Marta Calvi¹, **Jonas Eschle**³, Andrea Mauri^{4,5}
Simone Meloni¹, Martina Mozzanica¹, Nicola Serra³

1 University and INFN Milano-Bicocca (Italy)

2 CERN (Switzerland)

3 University of Zürich, Switzerland

4 Imperial College London (UK)

5 NIKHEF (The Netherlands)

Outlook

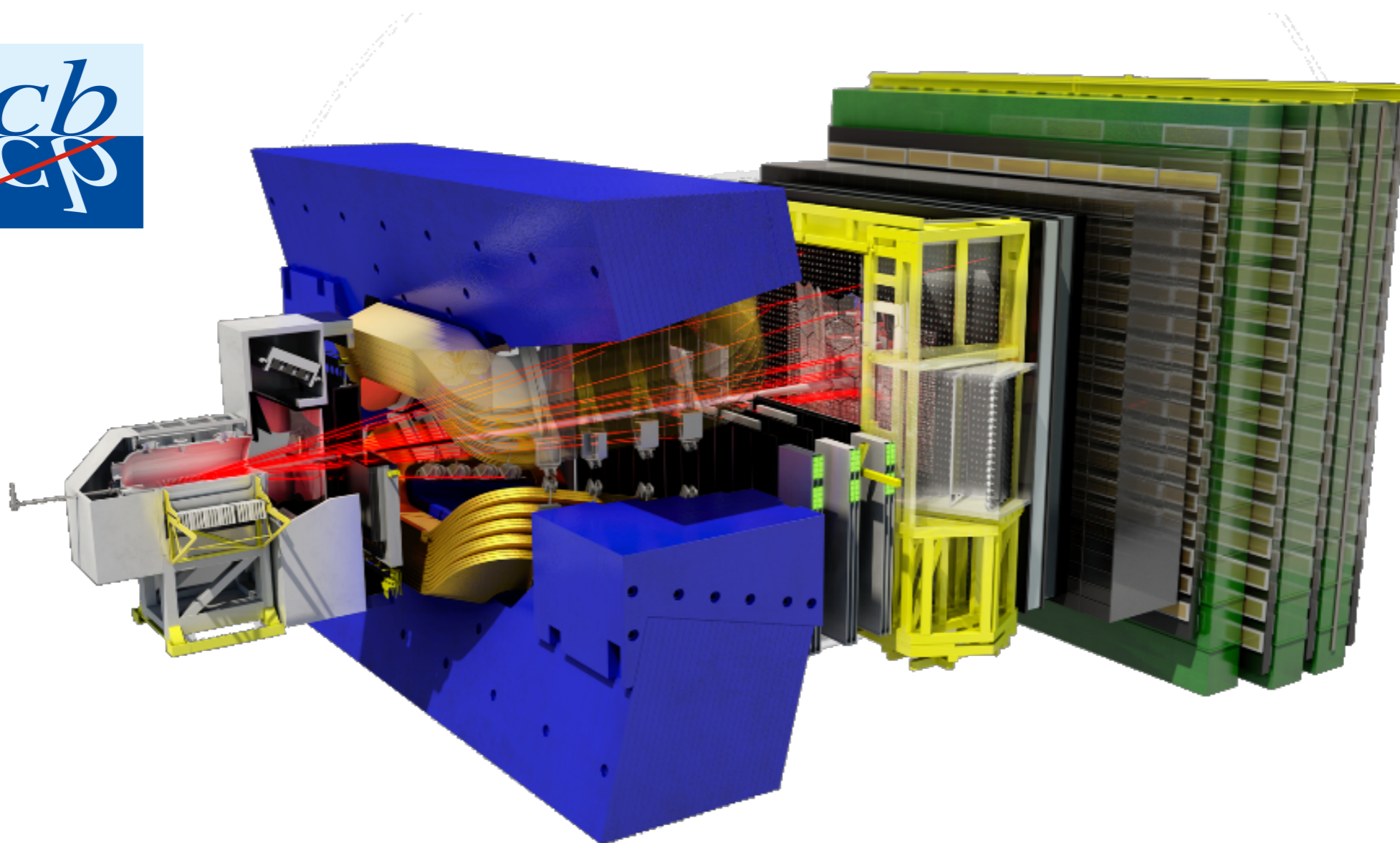
**Performance
(preliminary)**

The algorithm

Motivation

The LHCb detector

Single-arm forward spectrometer, studying the decays of beauty and charm hadrons.
Very broad physics program. → To be maintained and expanded in future LHC runs.



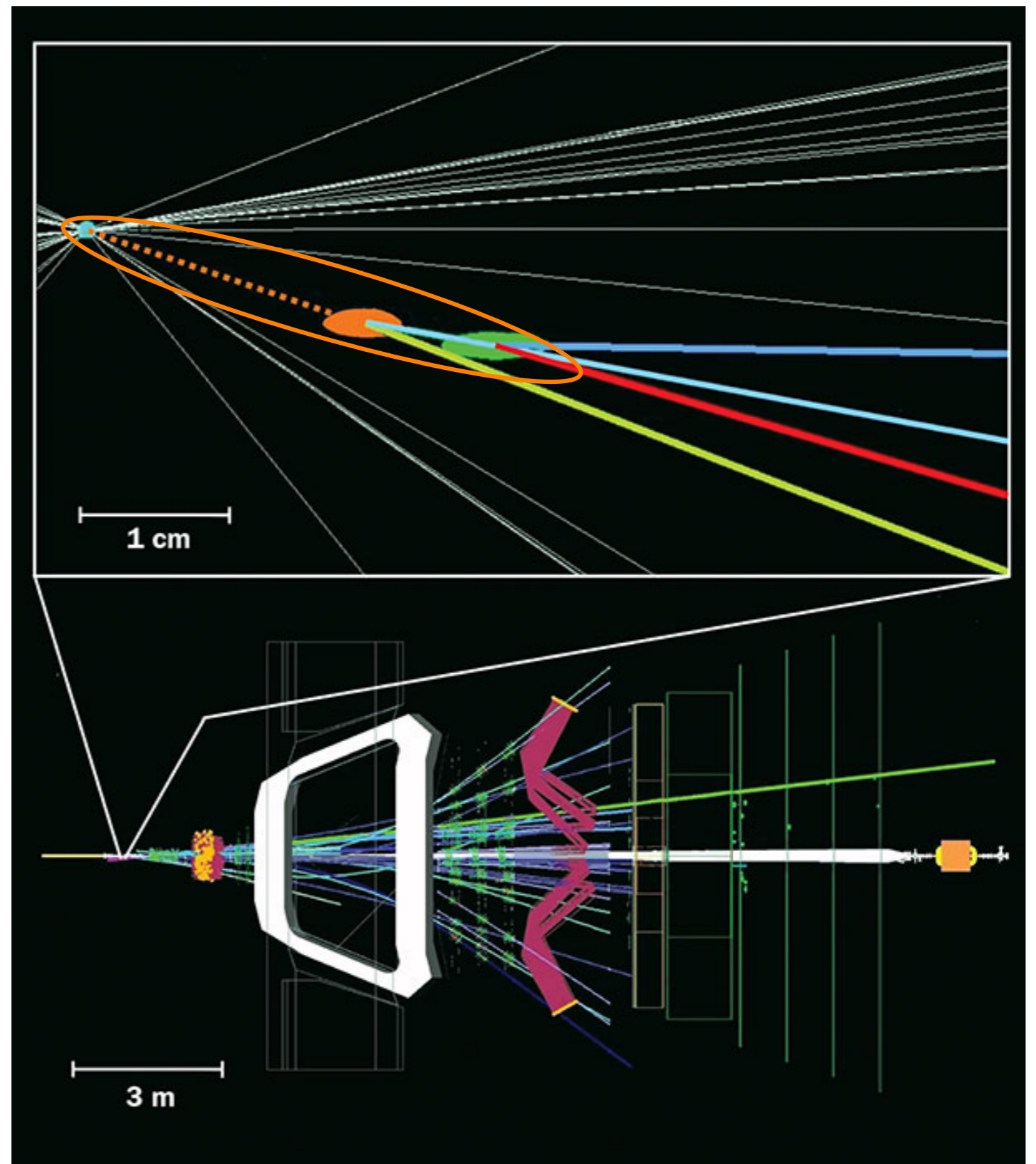
Excellent vertexing capabilities, momentum resolution and PID performance.

Event information and size

Current trigger

OR between decay modes

Store whole event*



Event information and size

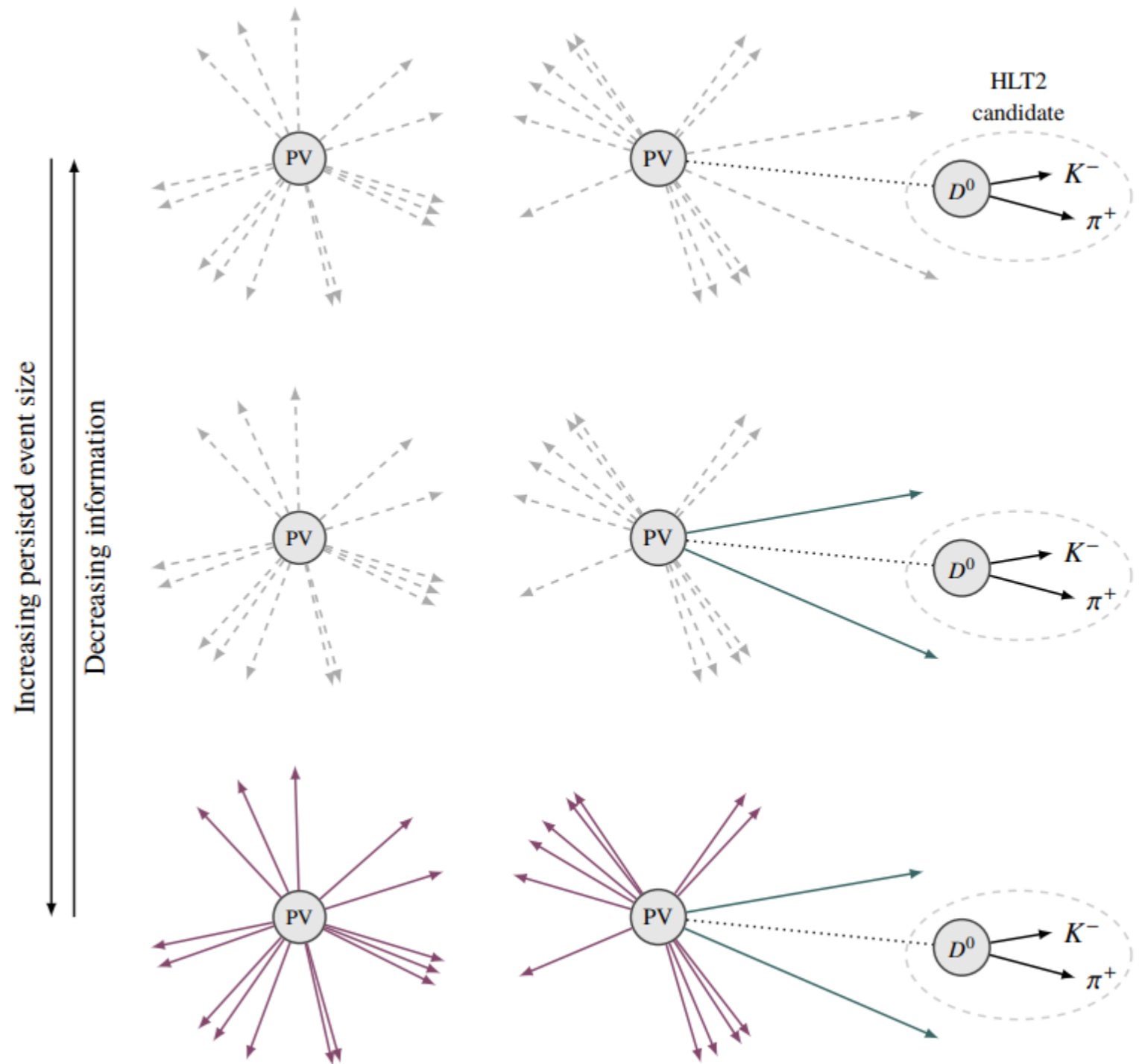
Current trigger

OR between decay modes

Store whole event

→ Store only PV + Tracks?

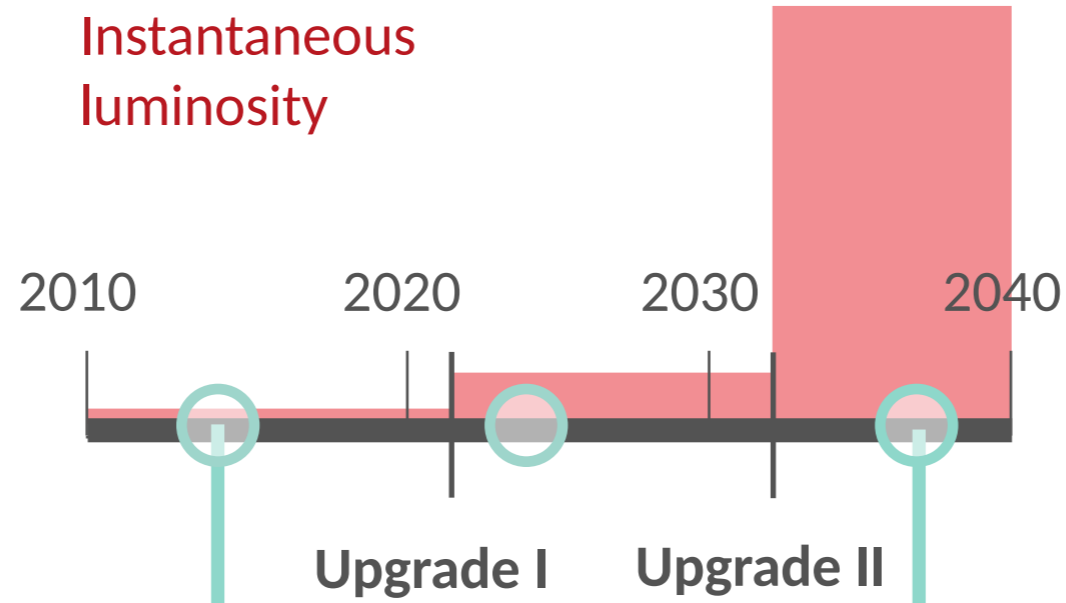
Full event
VS
disk space



Evolution in the LHCb trigger

<< 1 signal
~ 50 tracks

Which events are interesting?
↓
Trigger strategy:
signal based.



~ 5 signals
~ 1000 tracks

Which parts of the event are interesting?

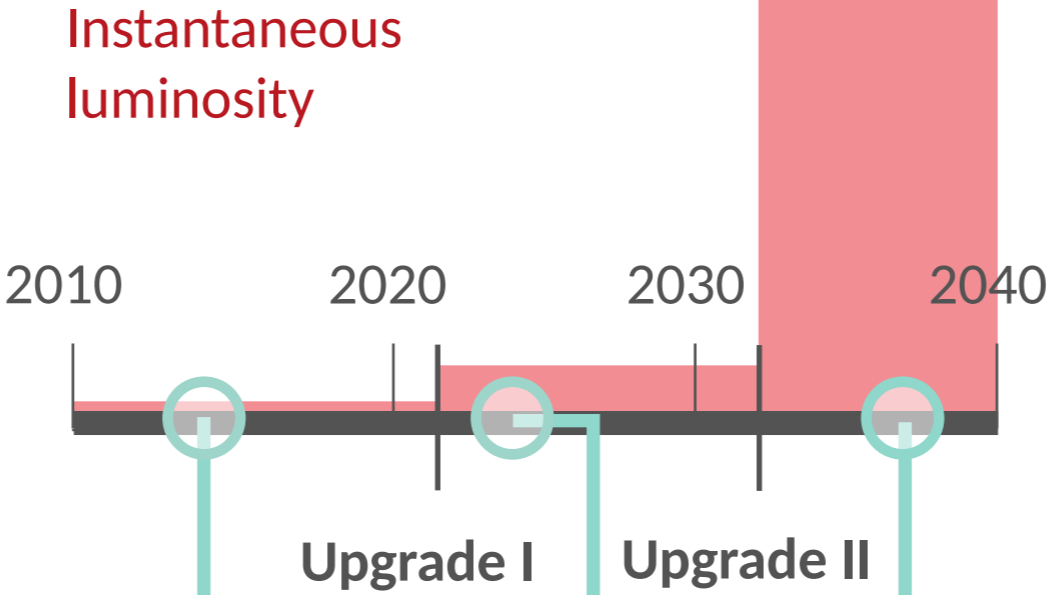
New era for LHCb!

[\[LHCb-PUB-2014-027\]](#)

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New era for LHCb!

[\[LHCb-PUB-2014-027\]](#)

~ 0.5 signals
~ 140 tracks

Fully software trigger, CPU + GPU [\[JINST 14 \(2019\) 04, P04006\]](#).
→ Online alignment and calibration, offline-quality online reconstruction.

Key developments that enable more ambitious trigger strategies.

Evolution in the LHCb trigger

Reconstruction difficulty $\sim n^2$

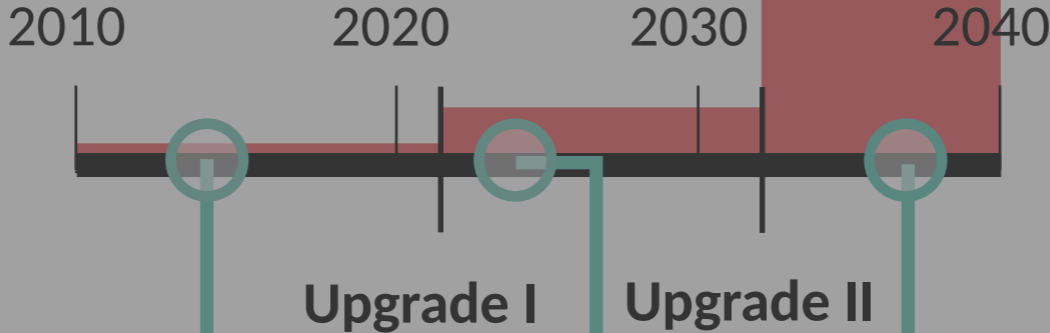
track & decay

- Hits & tracks combinatorics
- Pile-up

interesting.



Trigger strategy:
signal based.



~ 5 signals
~ 1000 tracks

Which parts of the event are interesting?

New era for LHCb!

[\[LHCb-PUB-2014-027\]](#)

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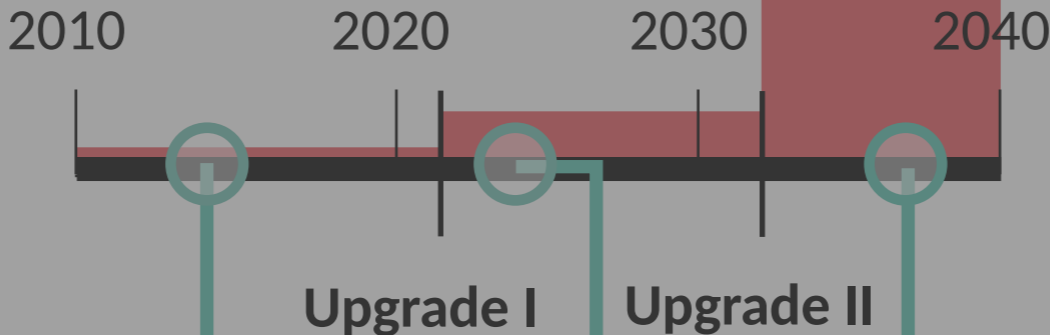
track & decay

- Hits & tracks combinatorics
- Pile-up

Storage space $\sim n^2$

- Event size $\sim n$
- Trigger rate $\sim n$
(more signal events on avg.)

Trigger strategy:
signal based.



**New era
for LHCb!**

[LHCb-PUB-2014-027]

~ 0.5 signals
~ 140 tracks

Fully software trigger, CPU + GPU [JINST 14 (2019) 04, P04006].

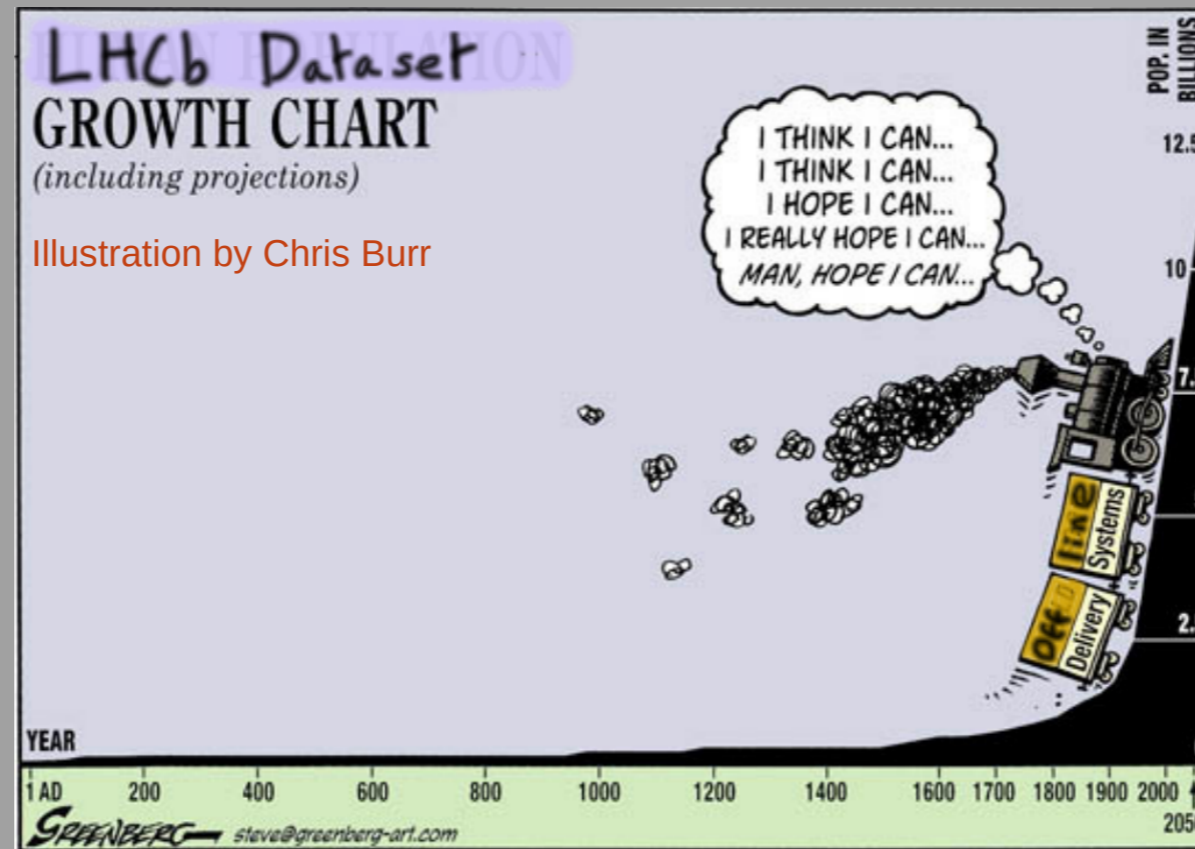
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New era for LHCb!

[\[LHCb-PUB-2014-027\]](#)

Upgrade I

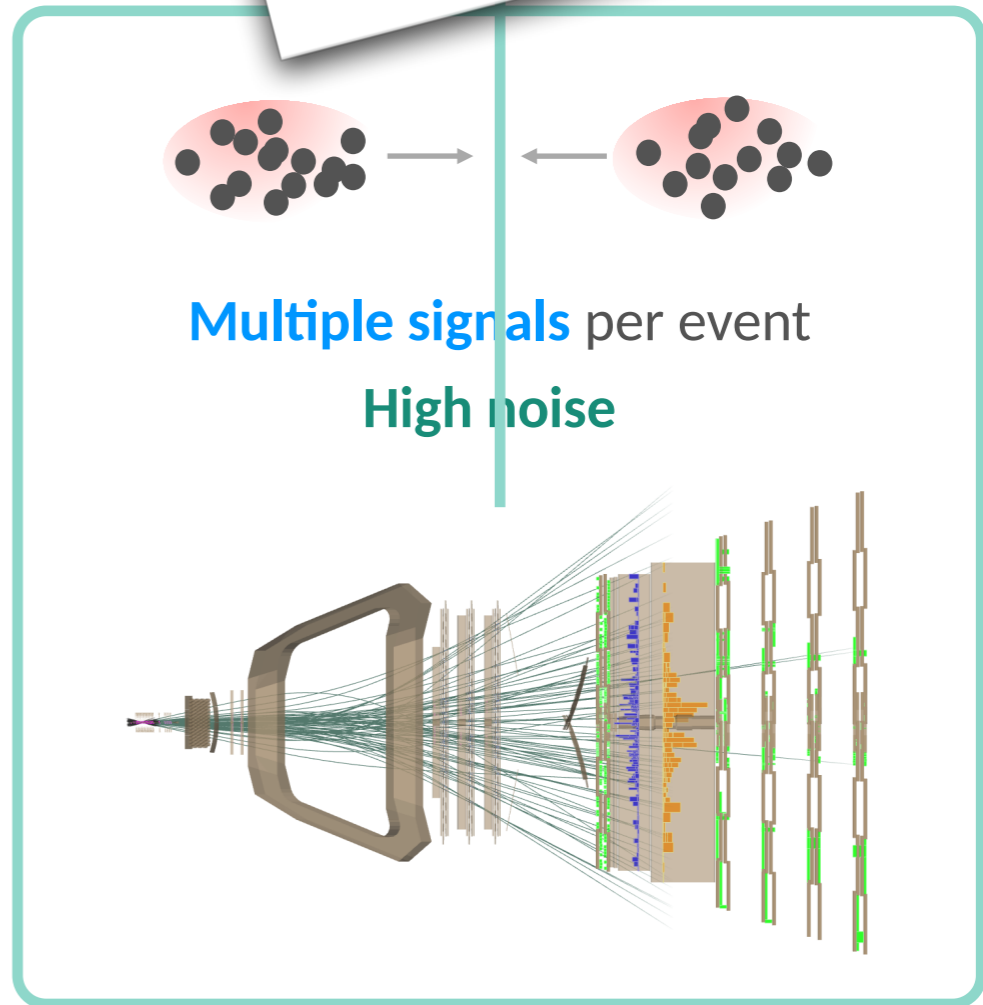
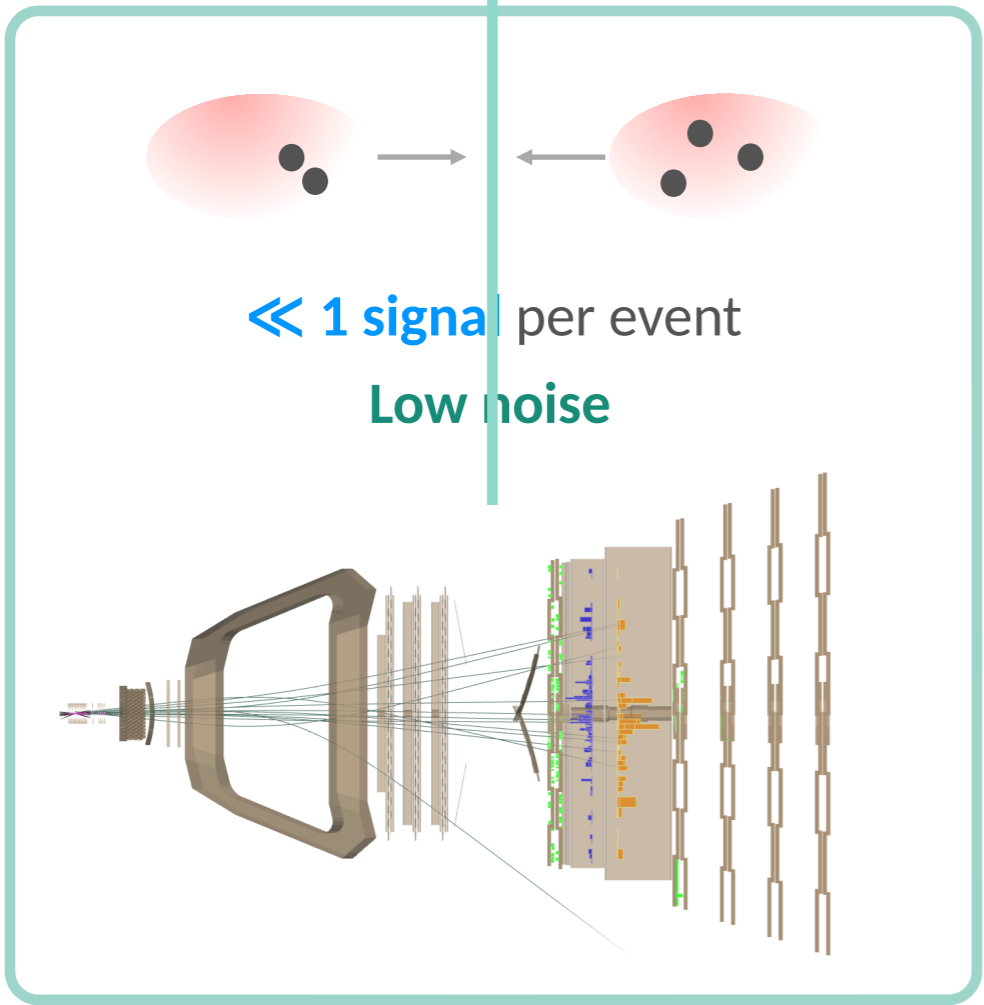
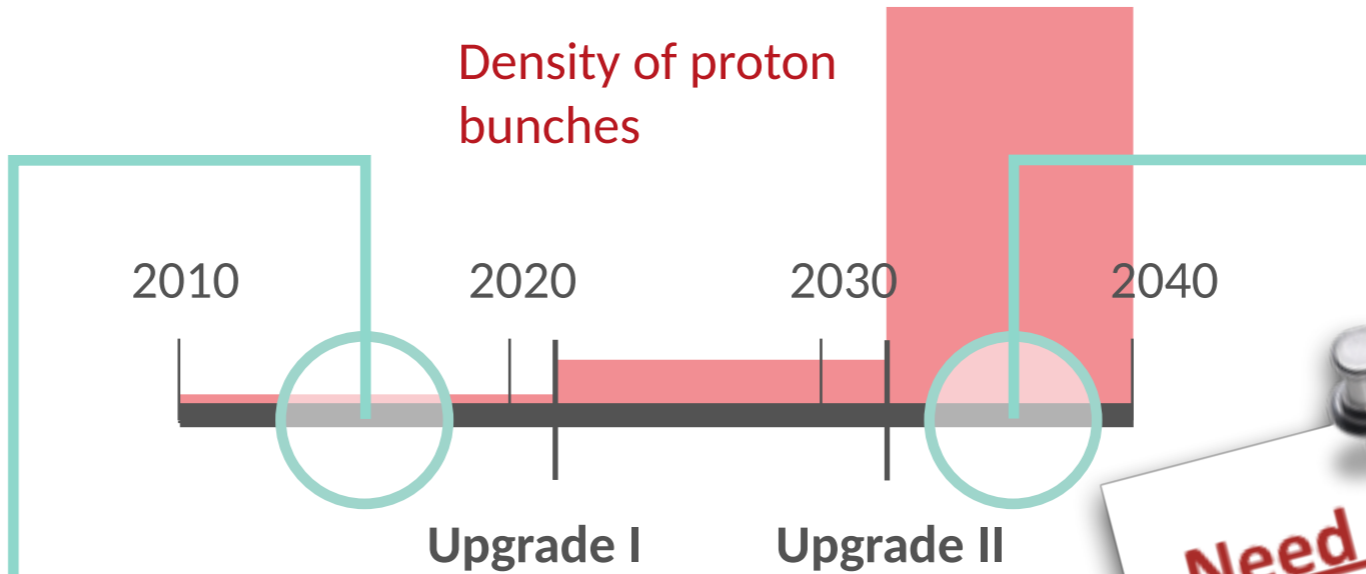
Upgrade II

~ 0.5 signals
~ 140 tracks

Fully software trigger, CPU + GPU [\[JINST 14 \(2019\) 04, P04006\]](#).
→ Online alignment and calibration,
offline-quality online reconstruction.

Key developments that enable more ambitious trigger strategies.

Fighting the scaling



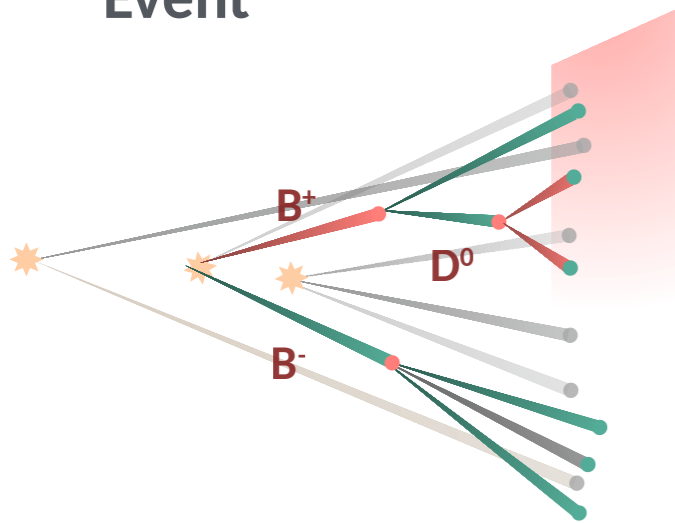
Facing the new era with machine learning

Novel approach
proposed

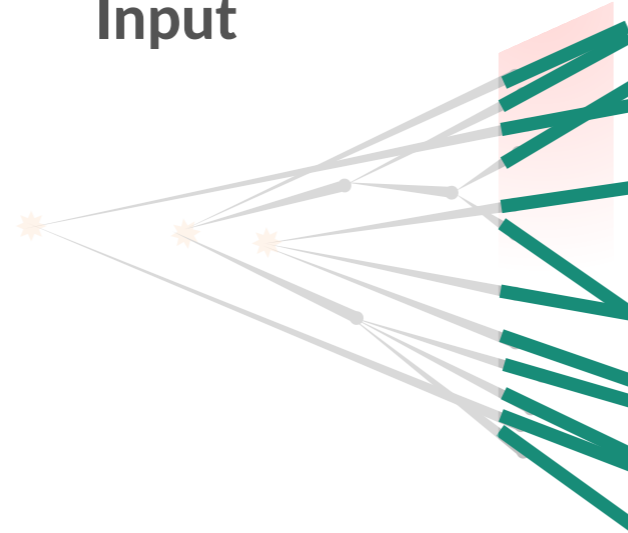


DFEI:
Deep-learning based
Full Event Interpretation

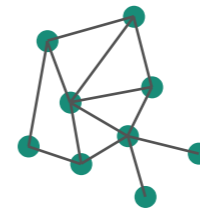
Event



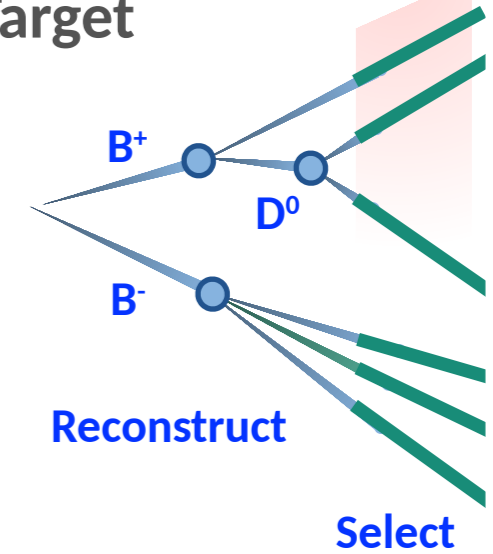
Input



Graph
neural
network



Target



“Maximally efficient” trigger.

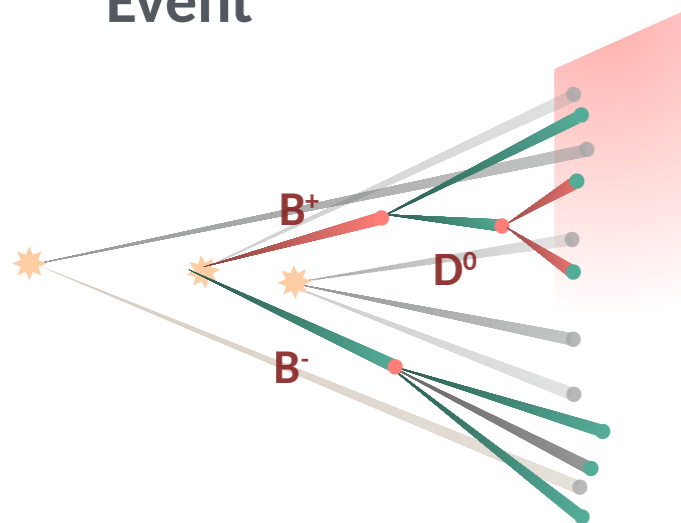
Facing the new era with machine learning

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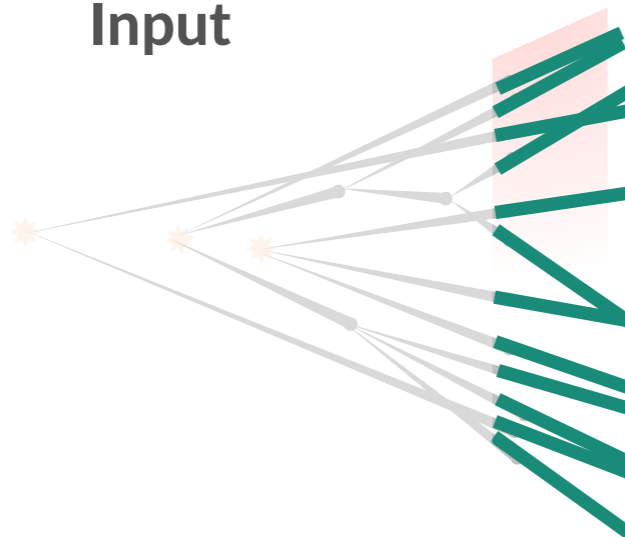


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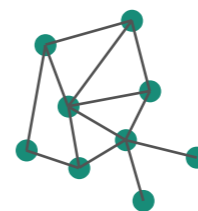
Event



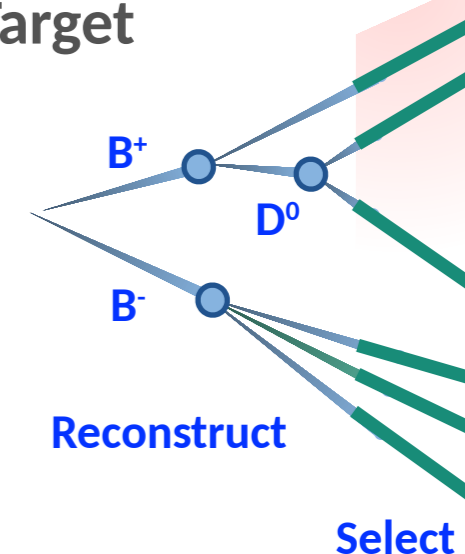
Input



Graph
neural
network



Target



“Maximally efficient” trigger.

Similar developments in other experiments



Full Event Interpretation algorithm at an e+e- collider
[[Comput.Softw.Big Sci. 3 \(2019\) 1 6](#)], [BELLE2-MTHESIS-2020-006](#)].



GNNs for trigger purposes
[see e.g. [Eur.Phys.J.C 81 \(2021\) 5, 381](#), [Frontiers in Big Data 3 \(2021\) 44](#)].

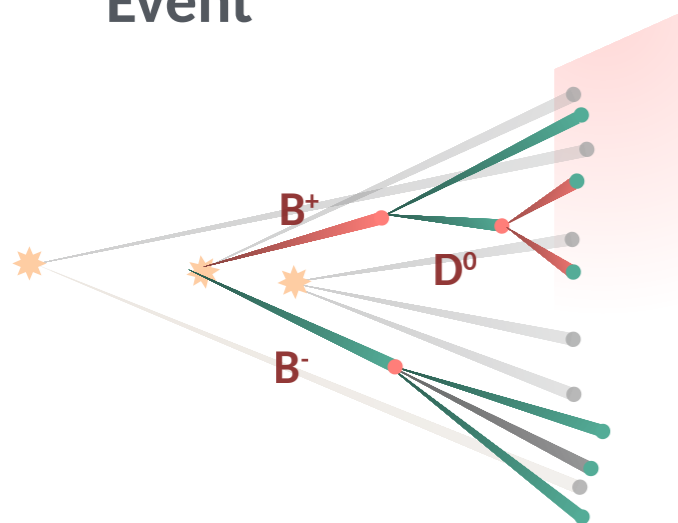
Facing the new era with machine learning

Novel approach proposed



DFEI:
Deep-learning based
Full Event Interpretation

Event



Input

Graph neural

Target

B⁺

Belle II case

Only B⁰/B[±] hadrons.
e⁺e⁻ environment.
Hermetic detector.

LHCb case

All b,c-hadron species.
pp environment.
Non-hermetic detector.

Similar developments in other experiments



Full Event Interpretation algorithm at an e⁺e⁻ collider
[[Comput.Softw.Big Sci. 3 \(2019\) 1 6](#)], [BELLE2-MTHESIS-2020-006](#)].



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[see e.g. [Eur.Phys.J.C 81 \(2021\) 5, 381](#), [Frontiers in Big Data 3 \(2021\) 44](#)].

Outlook

**Performance
(preliminary)**

The algorithm

**First prototype of DFEI for LHCb,
focused on b-hadron decays and
charged stable particles.**

Motivation

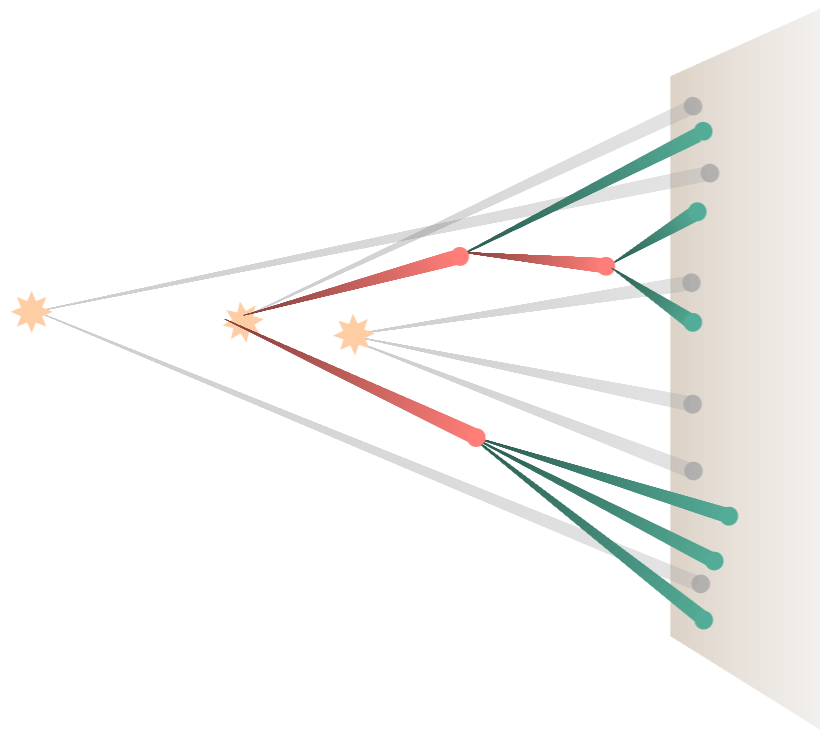
Decays and graph structures

Decay

Global (n vars): event information
nTracks, ...

Nodes (m_{event} vars): track variables
momentum, (PID), ...

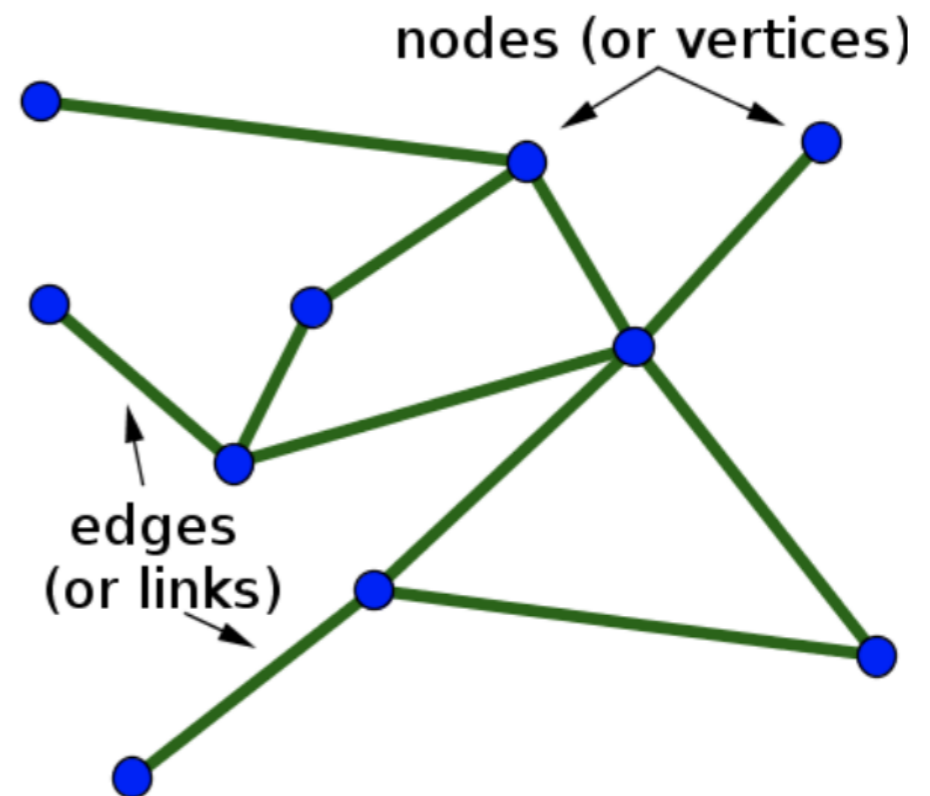
Edges (m_{event}^2): track *relations*
angle, DOCA, ...



Graph structures

Representation of objects
with relations

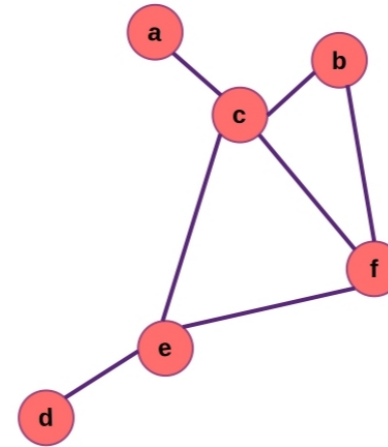
Arbitrary, sparse/dense relations



Graph Neural Networks

Mathematically expression

Adjacency matrix defines graph completely

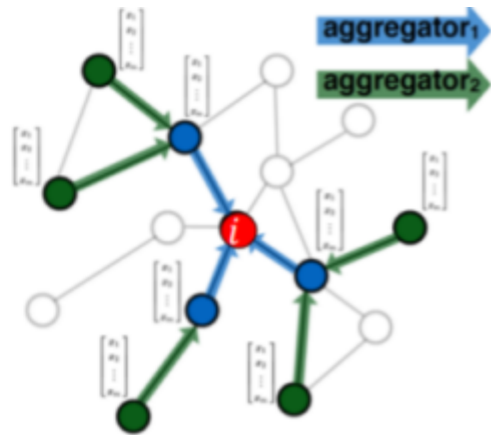


	a	b	c	d	e	f
a	0	0	0	0	0	0
b	0	0	1	0	0	1
c	1	1	0	0	1	1
d	0	0	0	0	1	0
e	0	0	1	1	0	1
f	0	1	1	0	1	0

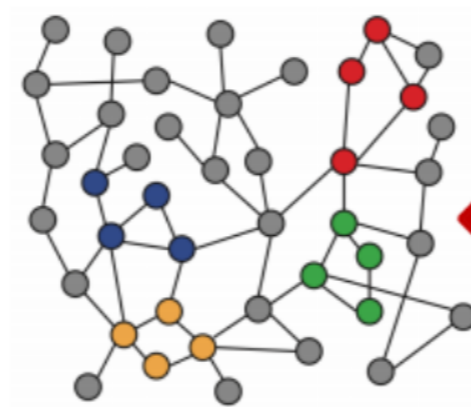
Comparison of data structure

Images/text special case of graph

GNN: "generalized" CNN

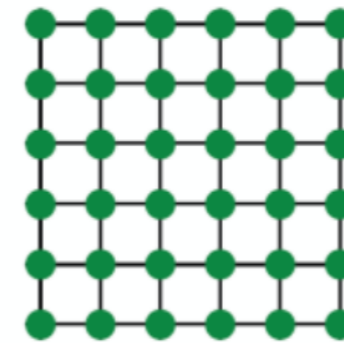


Propagate and transform information



Networks

VS.



Images

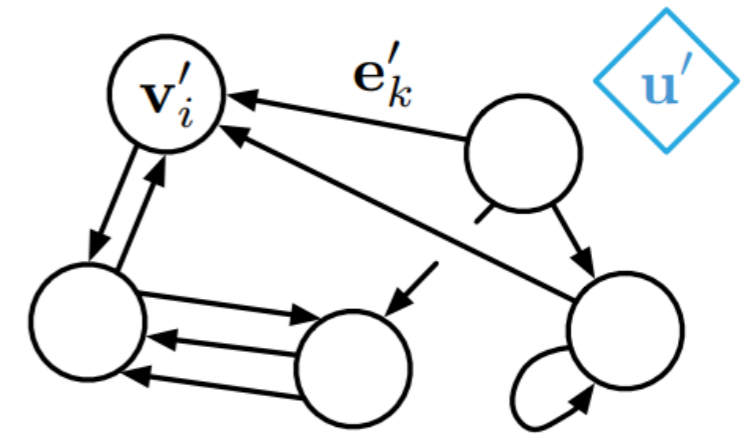
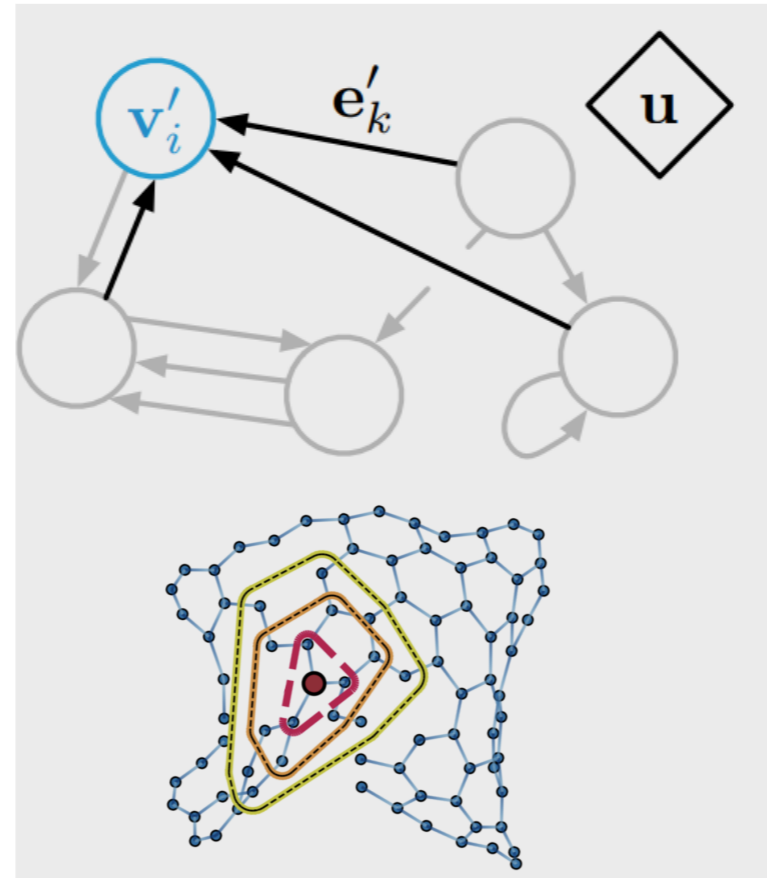
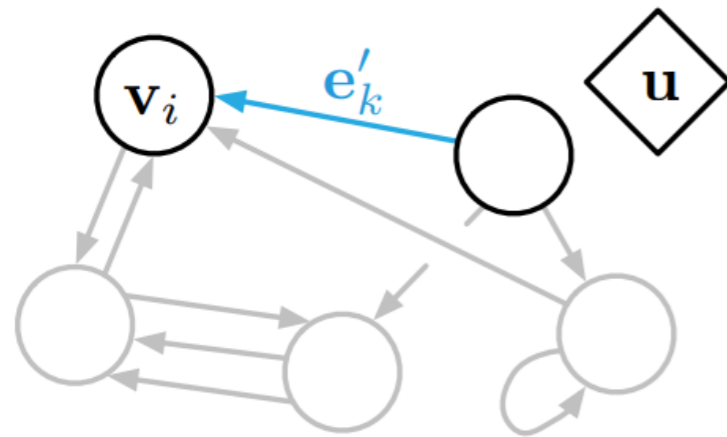


Text

GNN training

e' v' u' updated (by DNN) e , v , u

BLUE updated by **BLACK** not utilizing **GREY**



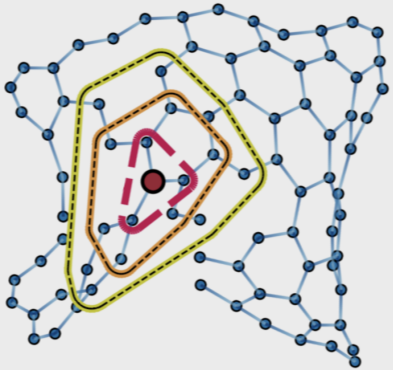
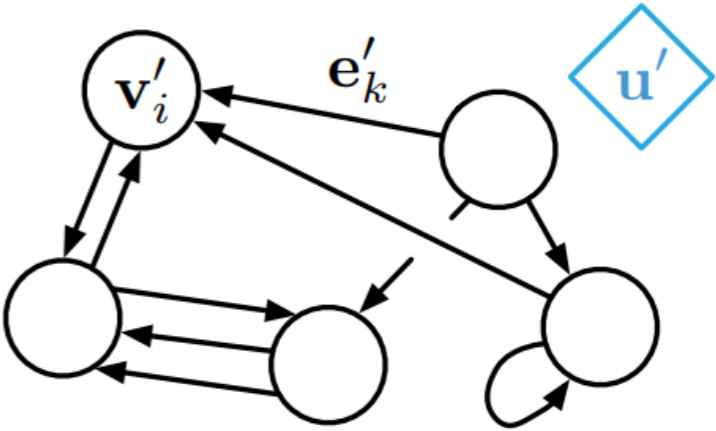
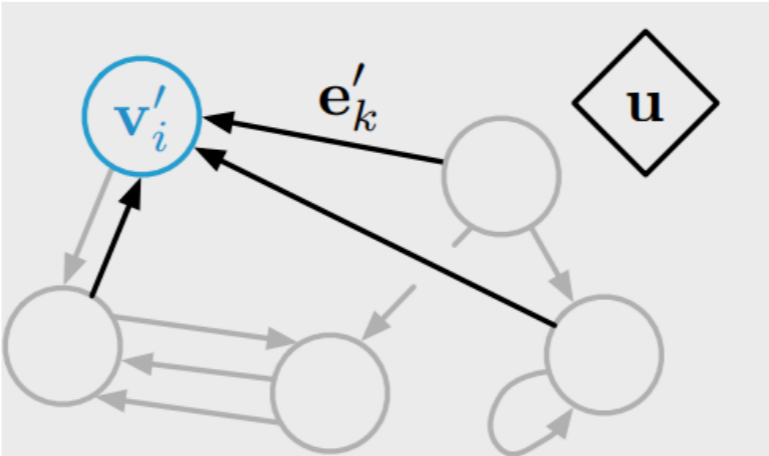
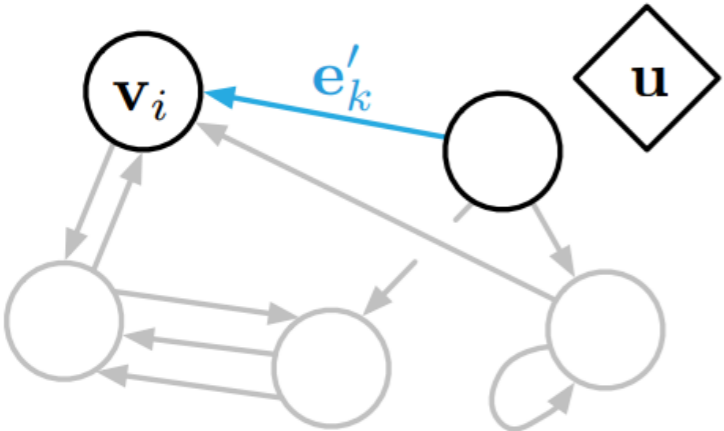
Node Aggregation

Aggregating information from neighbors

GNN training

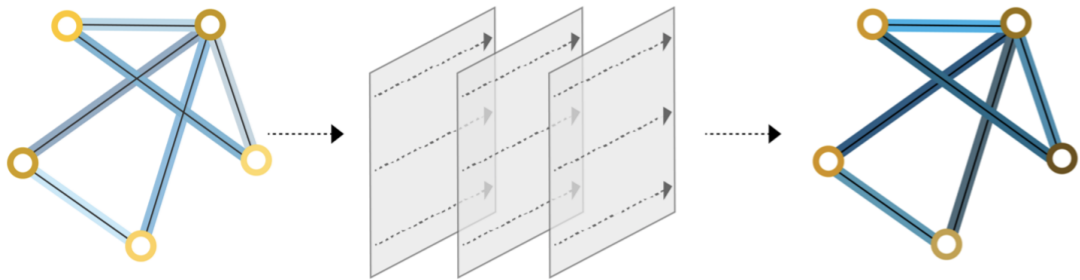
e' v' u' updated (by DNN) e, v, u

BLUE updated by **BLACK** not utilizing **GREY**



Node Aggregation

Aggregating information from neighbors



Transformation of graph

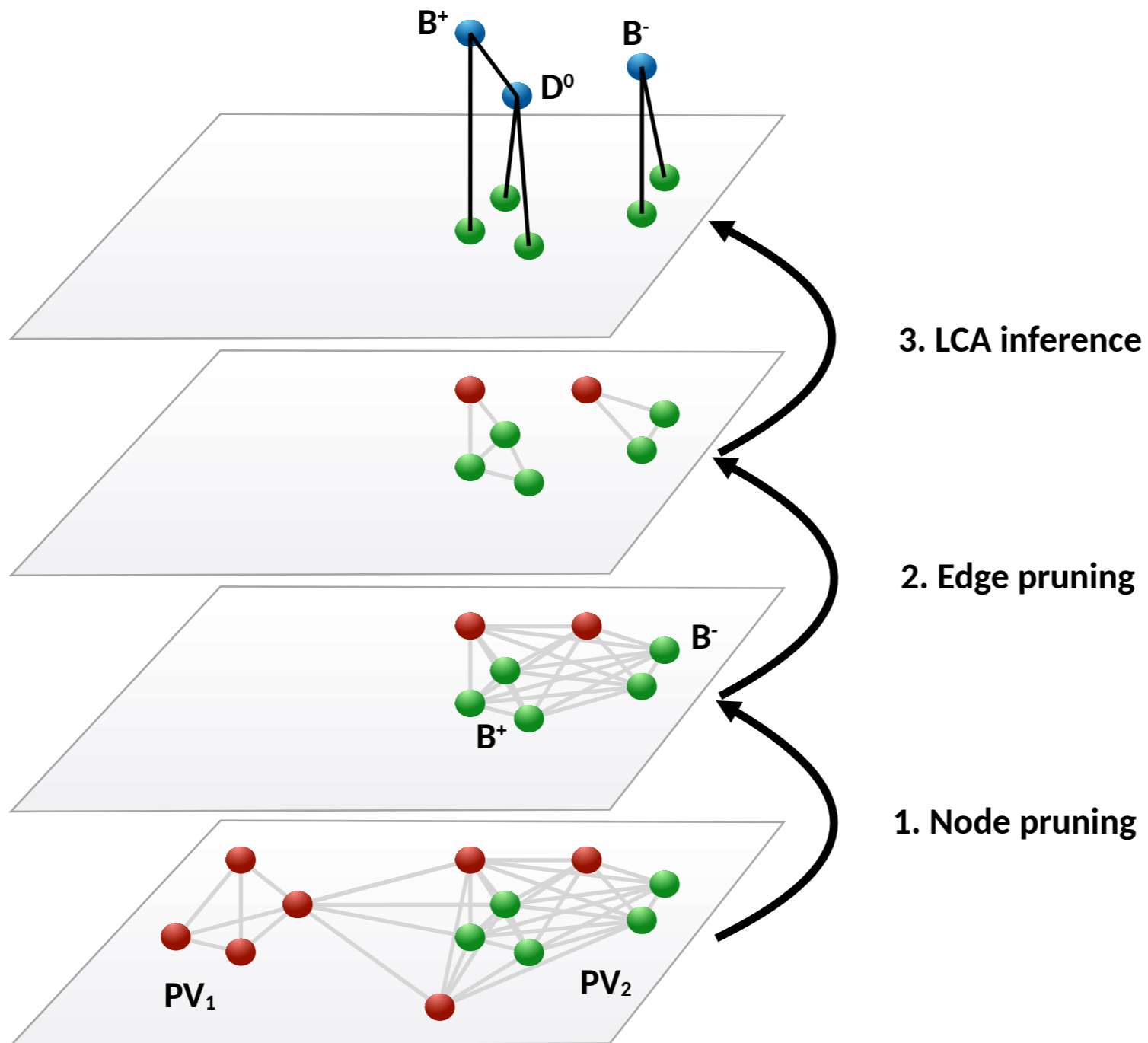
Input graph (X), return graph (y)

Output graph

Node/edge/global features

Different interpretations depending on application

DFEI Overview



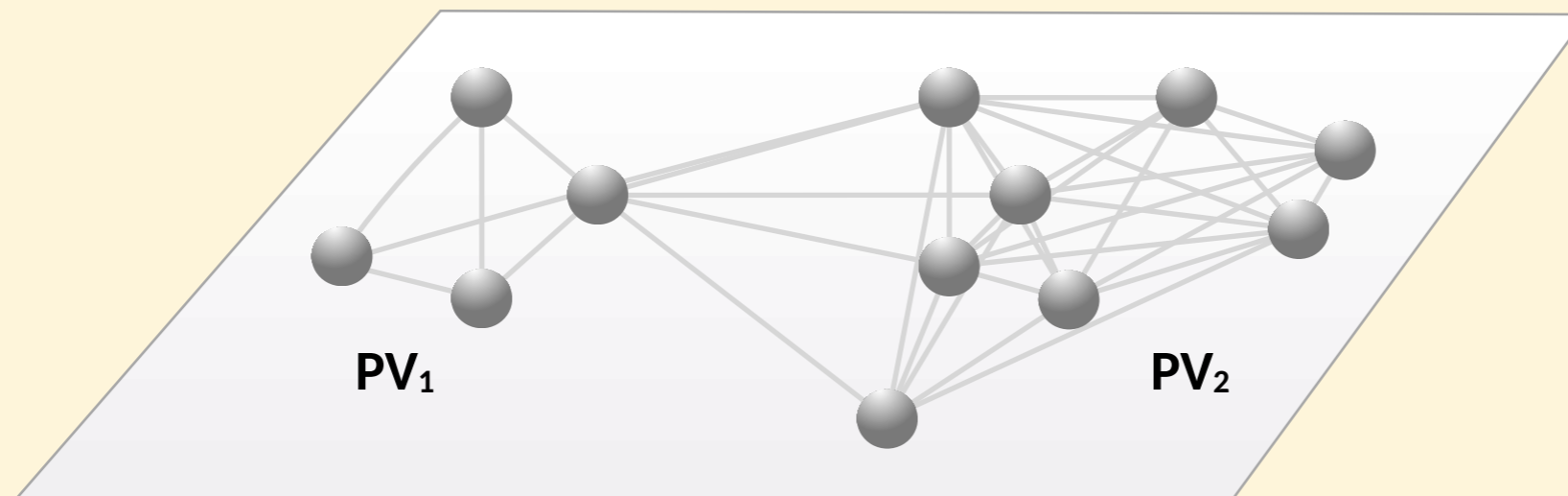
Input graph construction

Nodes: all the charged particles in the event.

→ On average **~140**.

Edges: connect particles which are topologically close (see backup for details).

→ On average **~10 000**.



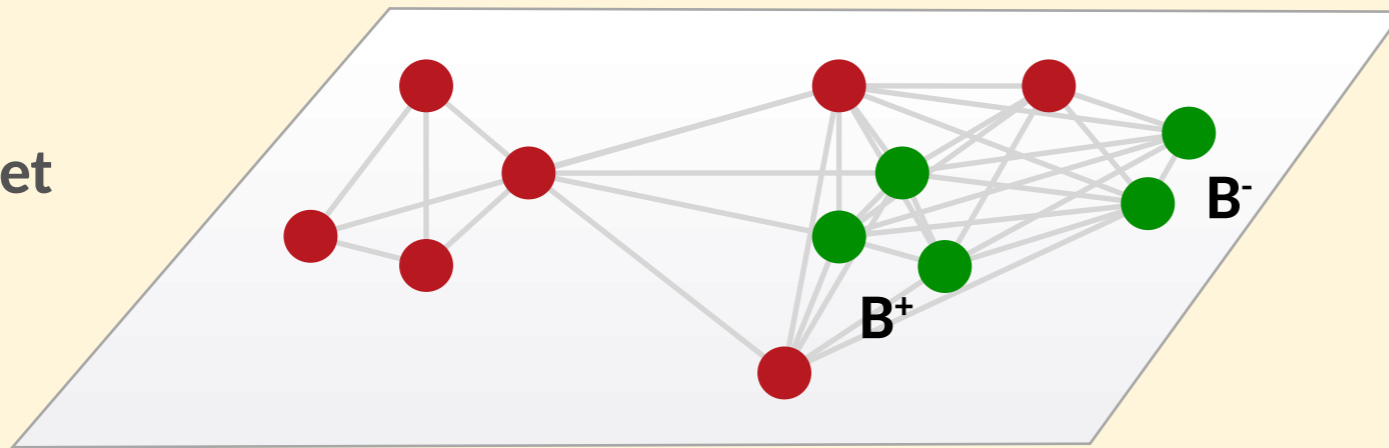
PV_1, PV_2 : different proton-proton primary vertices.

1st module: node pruning

Signal nodes: particles from a b-hadron (any of them)

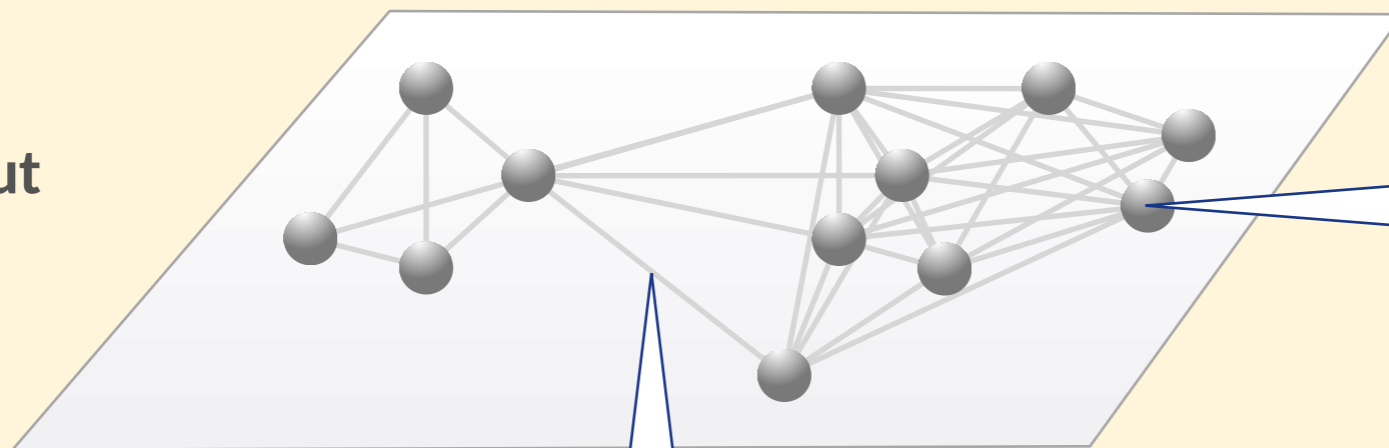
Background nodes: particles from the rest of the event

Target



pT: transverse momentum
ETA: pseudorapidity
PV: associated primary vertex
IP: impact parameter with respect to the PV
q: charge

Input



pT, ETA, IP, q

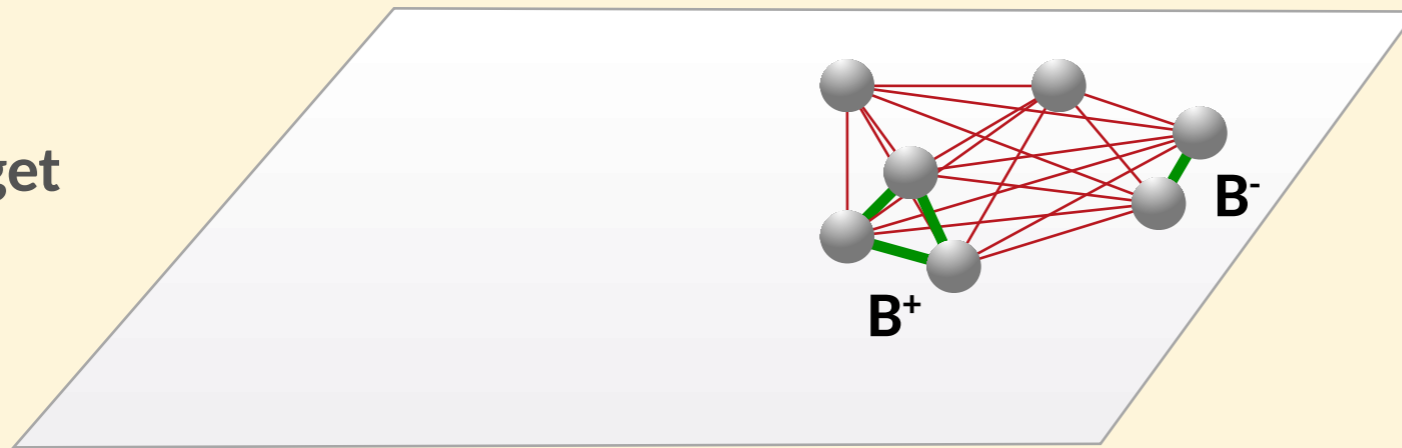
Opening angle, distance (between origins) along the beam axis, "transverse distance" (see backup), from same PV (boolean)

2nd module: edge pruning

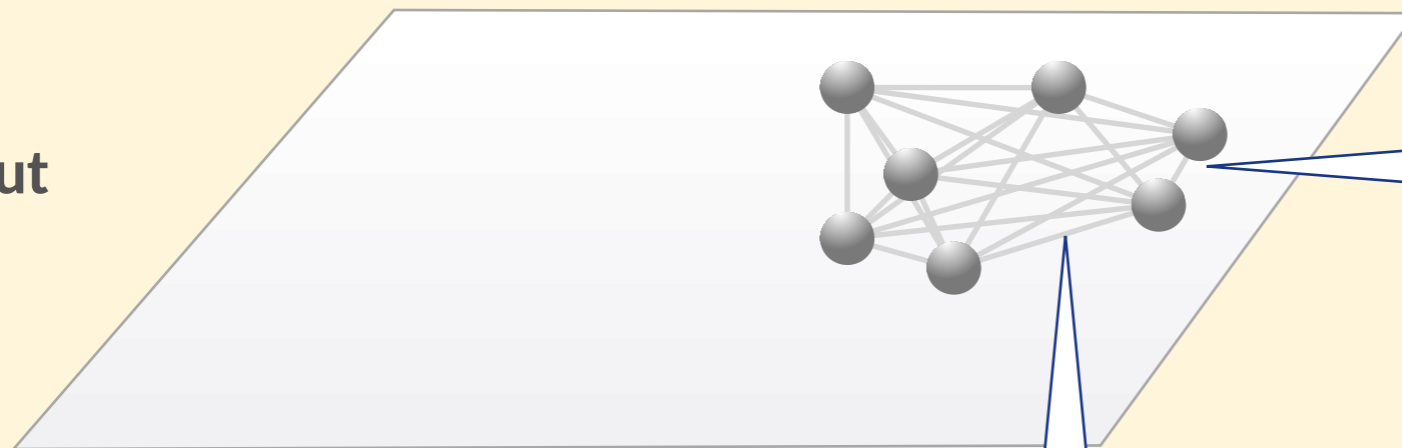
Signal edges: pairs of particles with the same b-hadron ancestor

Background edges: any other pair of particles

Target



Input



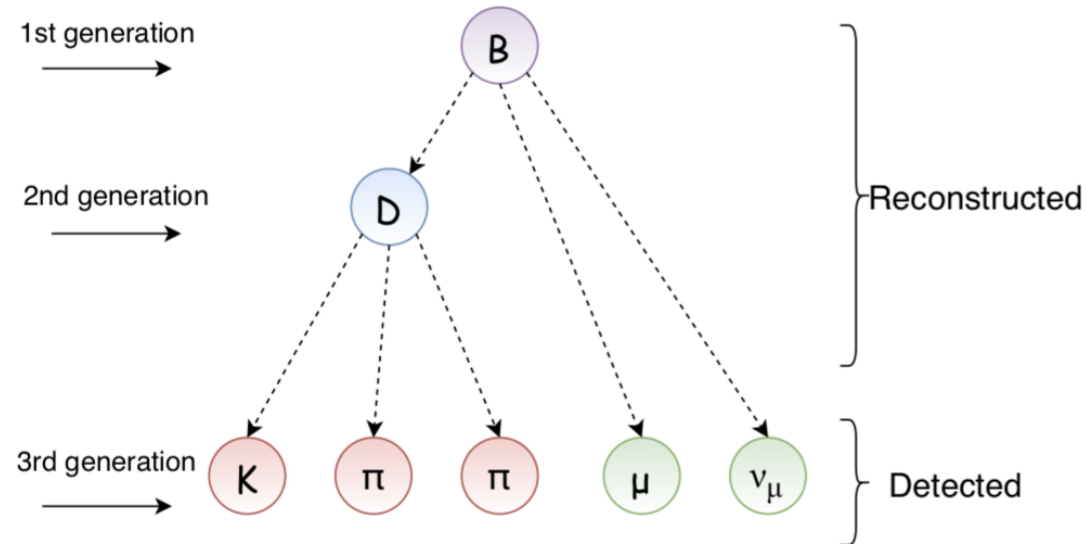
Same as before

Same as before

3rd module: Lowest Common Ancestor (LCA) inference

From [\[BELLE2-MTHESIS-2020-006\]](#):

(see also [\[James Kahn et al 2022 Mach. Learn.: Sci. Technol. 3 035012\]](#))



Adjacency Matrix

	B	D	K	π	π	μ	νμ
B	0	1	0	0	0	1	1
D	1	0	1	1	1	0	0
K	0	1	0	0	0	0	0
π	0	1	0	0	0	0	0
π	0	1	0	0	0	0	0
μ	1	0	0	0	0	0	0
νμ	1	0	0	0	0	0	0

LCA Matrix

	K	π	π	μ	νμ
K	0	1	1	2	2
π	1	0	1	2	2
π	1	1	0	2	2
μ	2	2	2	0	2
νμ	2	2	2	2	0

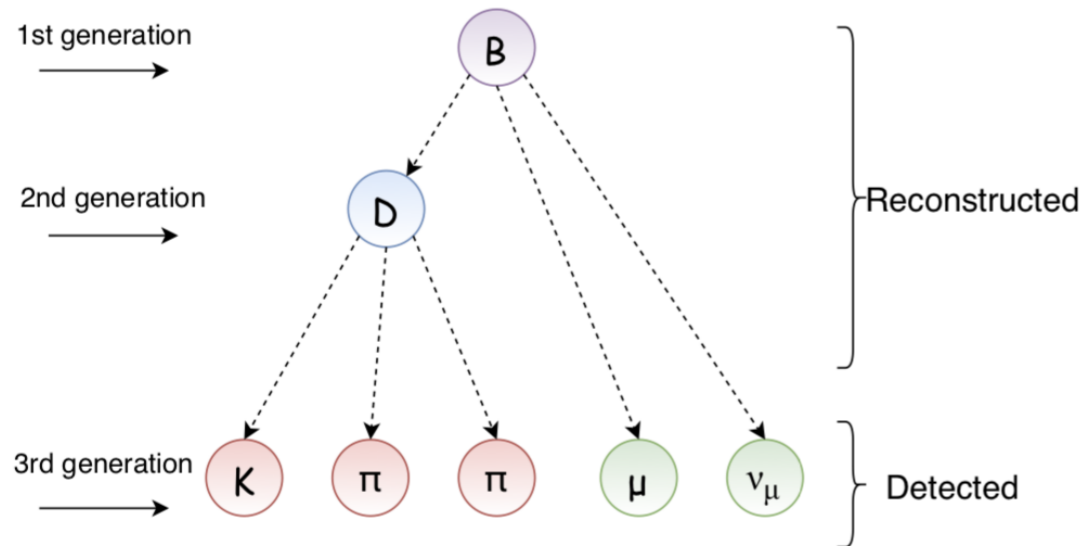


Problem reduced to **multi-class classification on edges.**

3rd module: Lowest Common Ancestor (LCA) inference

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π	0	1	0	0	0	0	0
μ	1	0	0	0	0	0	0
ν_μ	1	0	0	0	0	0	0

LCA Matrix

	K	π	π	μ	ν_μ
K	0	1	1	2	2
π	1	0	1	2	2
π	1	1	0	2	2
μ	2	2	2	0	2
ν_μ	2	2	2	2	0

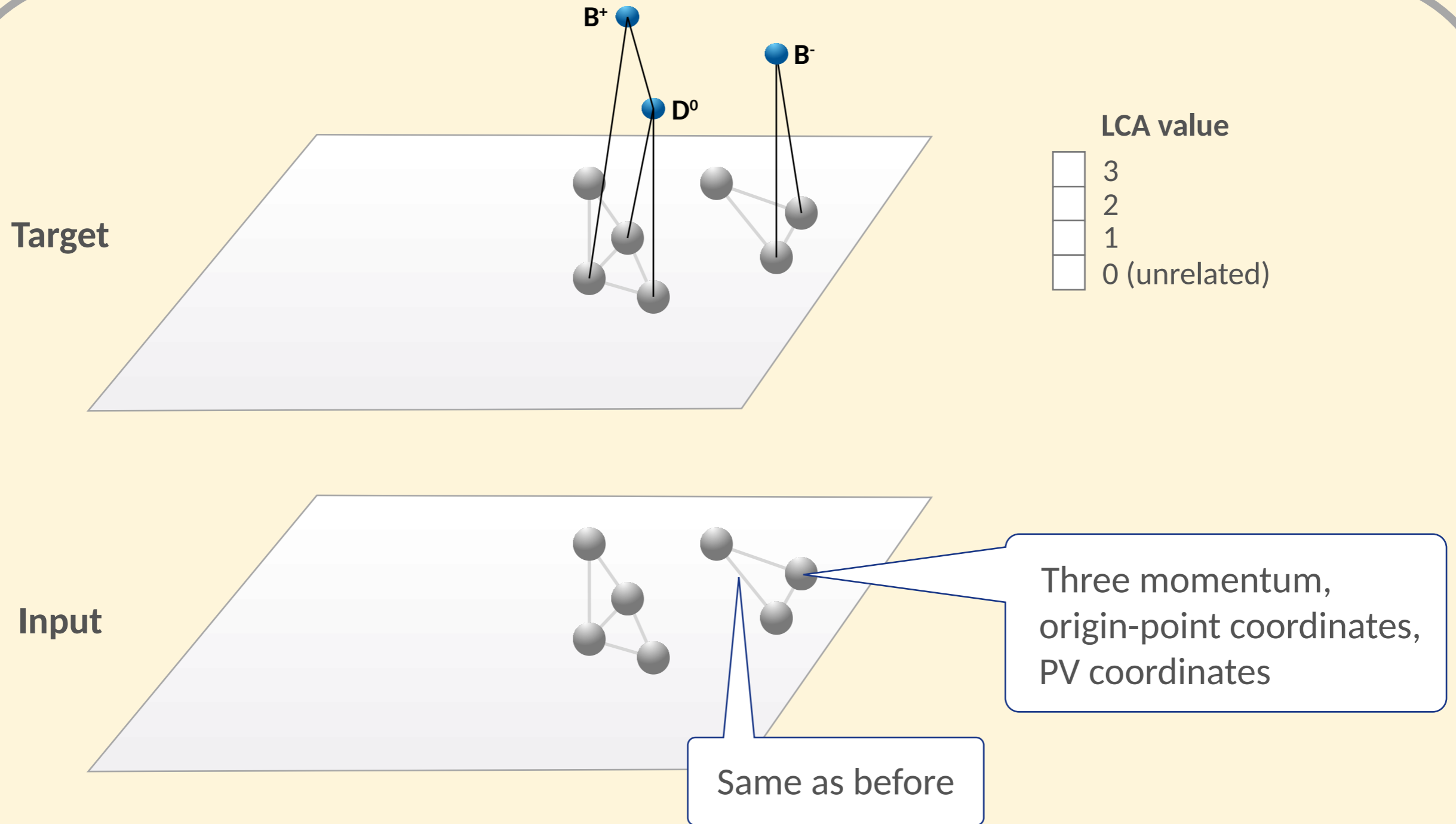


Problem reduced to **multi-class classification on edges.**

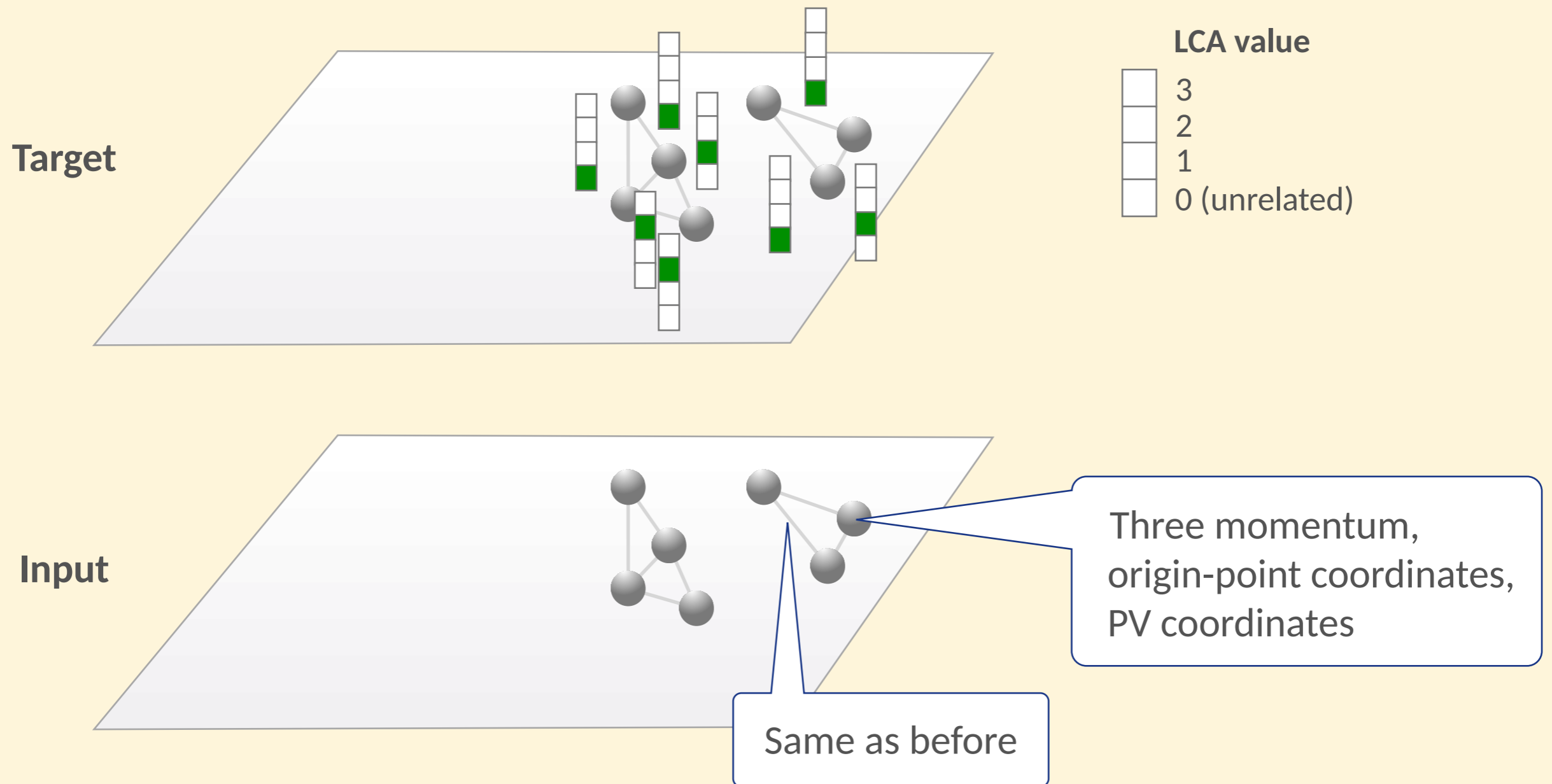
For the prototype, use as target a **simplified version of the decay chain, based on the reconstructible vertices.**

- Very-short-lived resonances merged with the previous ancestor.
- Resonances with less than two charged descendants merged with the previous ancestor.

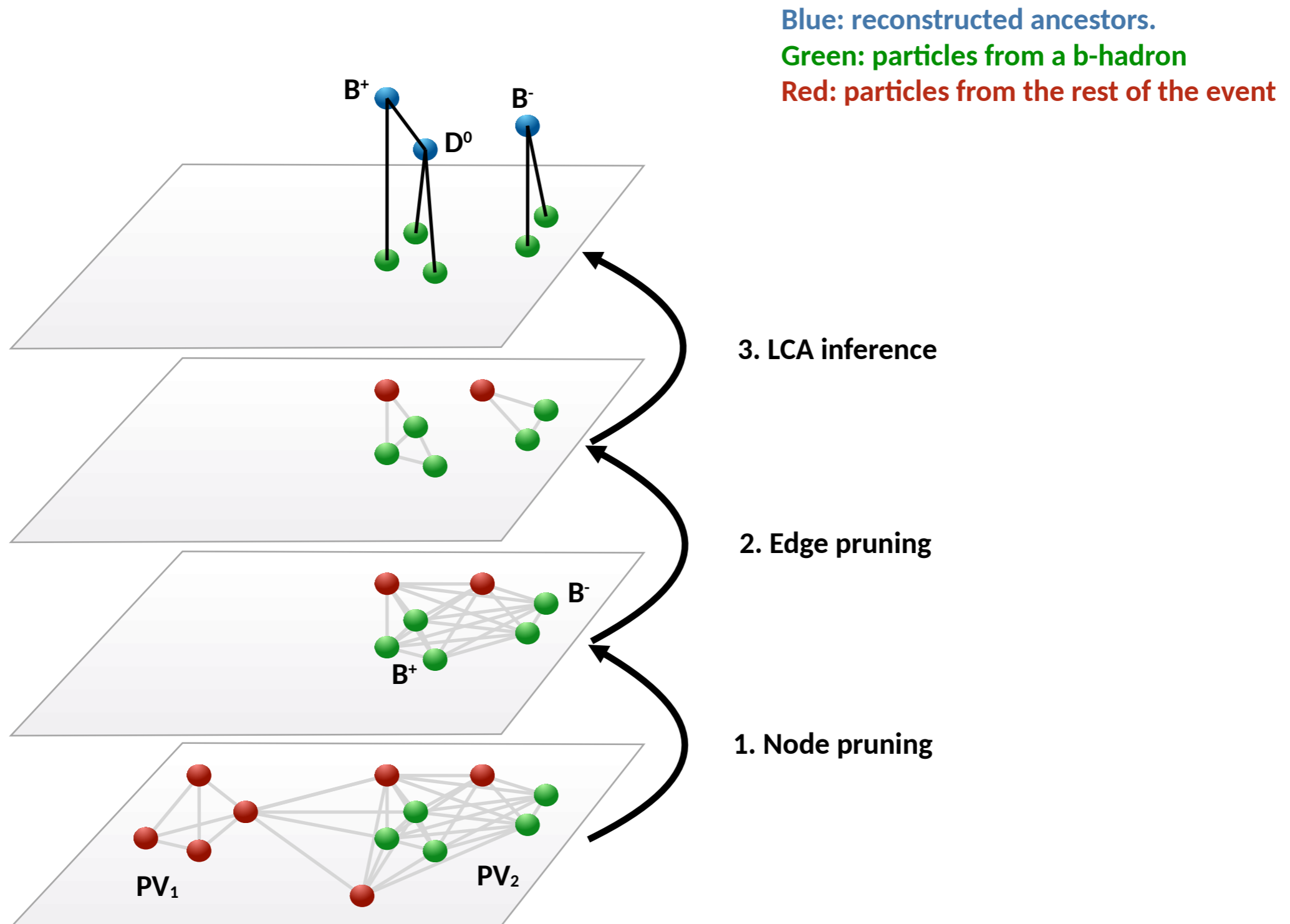
3rd module: Lowest Common Ancestor (LCA) inference



3rd module: Lowest Common Ancestor (LCA) inference



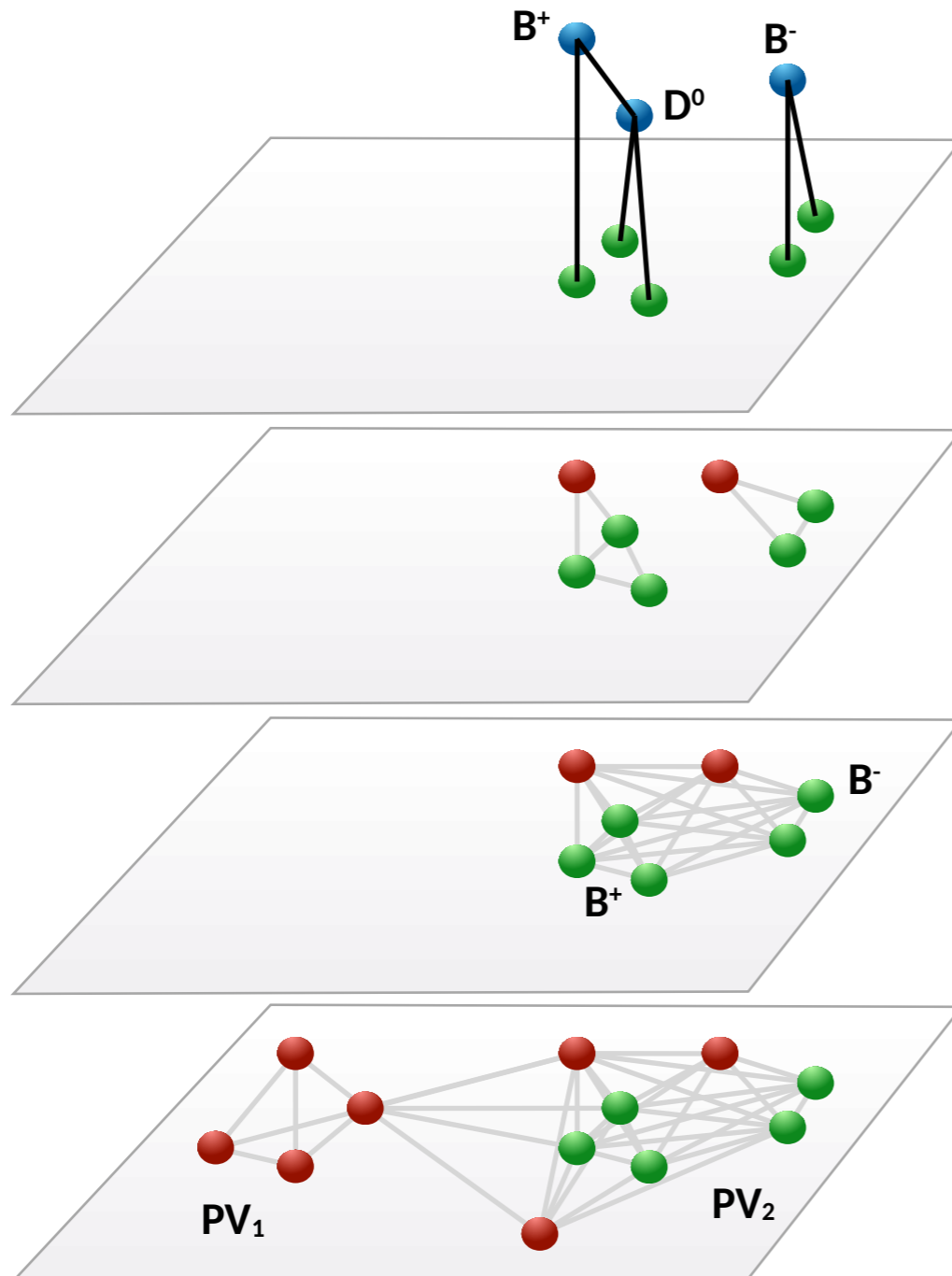
Overview and training



Training

Dataset:

- PYTHIA-based simulation, Run 3-like conditions, approximated emulation of LHCb reconstruction.
- Events required to contain at least one b-hadron (inclusive decay).



PYTHIA configuration

- Proton-proton collisions at 13 TeV
- Avg. number of collisions per event: 7.6

Emulated "Reconstruction"

using public Run 3 expectations

- Within LHCb acceptance
- Origin point of the tracks
- Three-momentum of the tracks.
- Position of the primary vertices.

Dataset published

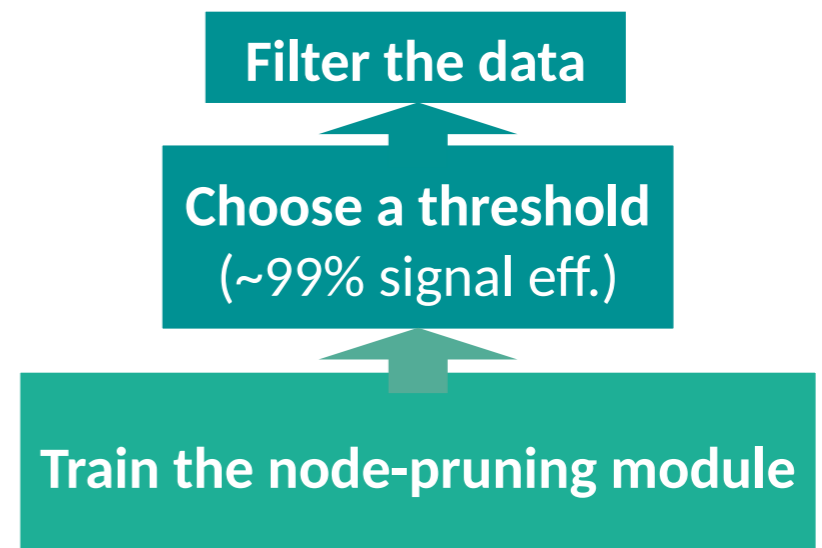
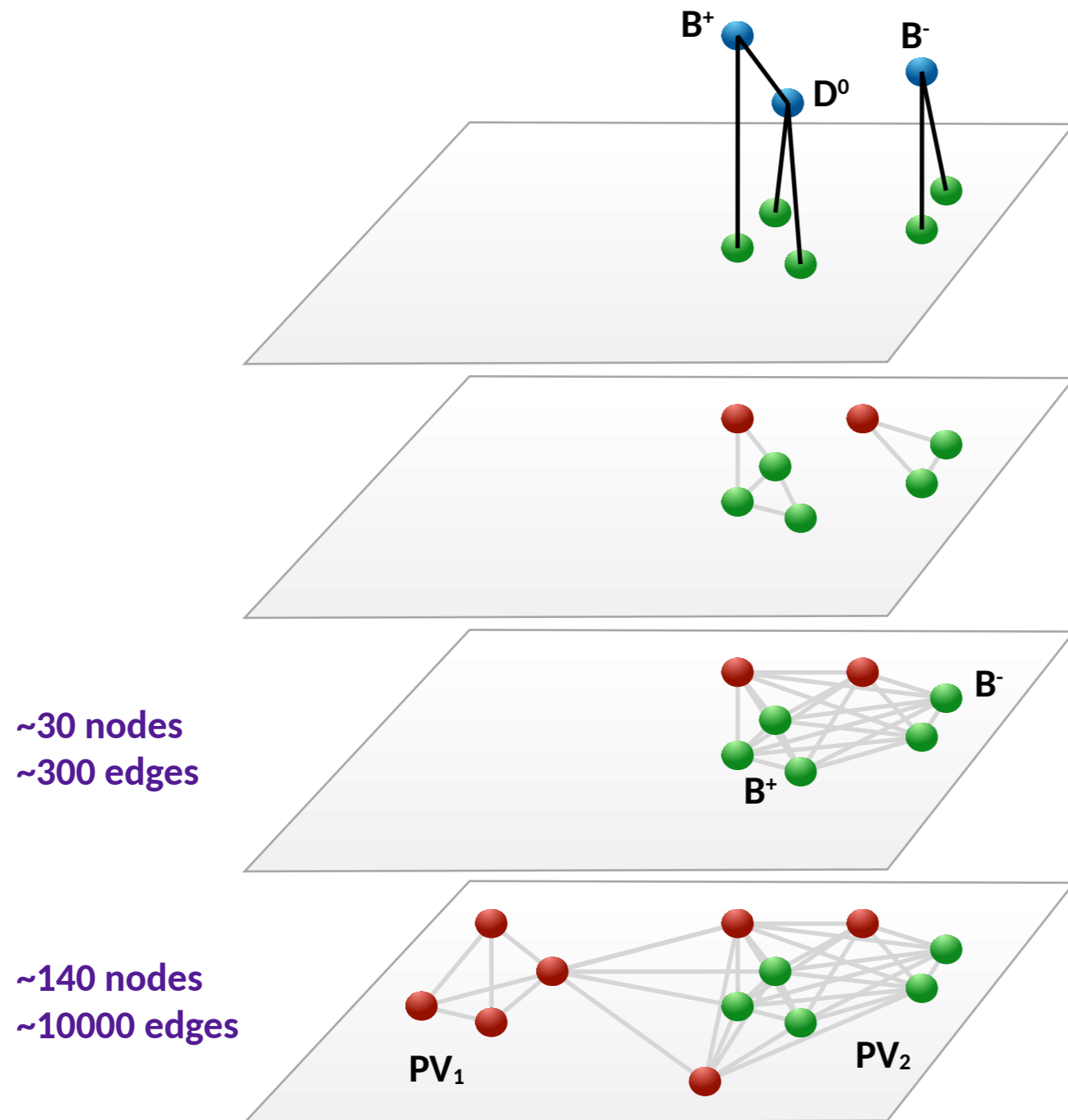
for benchmarking & comparison

[10.5281/zenodo.7799169](https://zenodo.org/doi/10.5281/zenodo.7799169)

Training

Dataset:

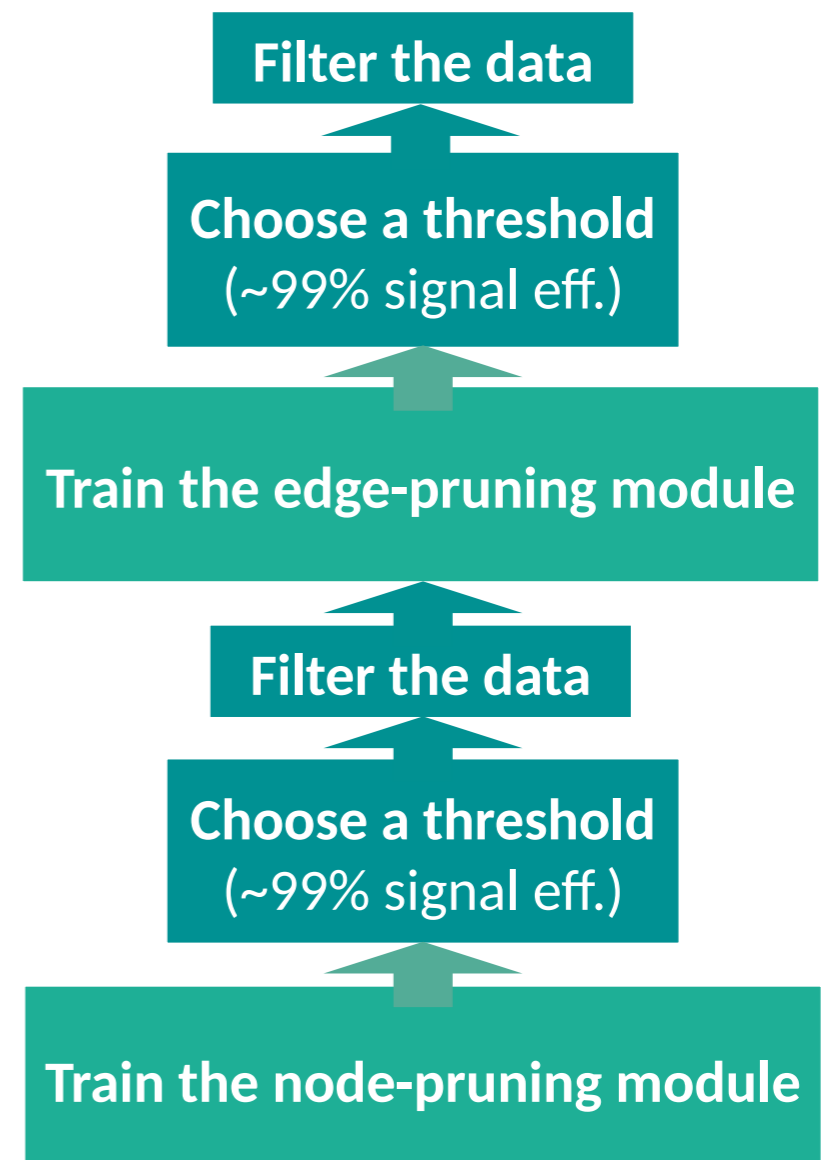
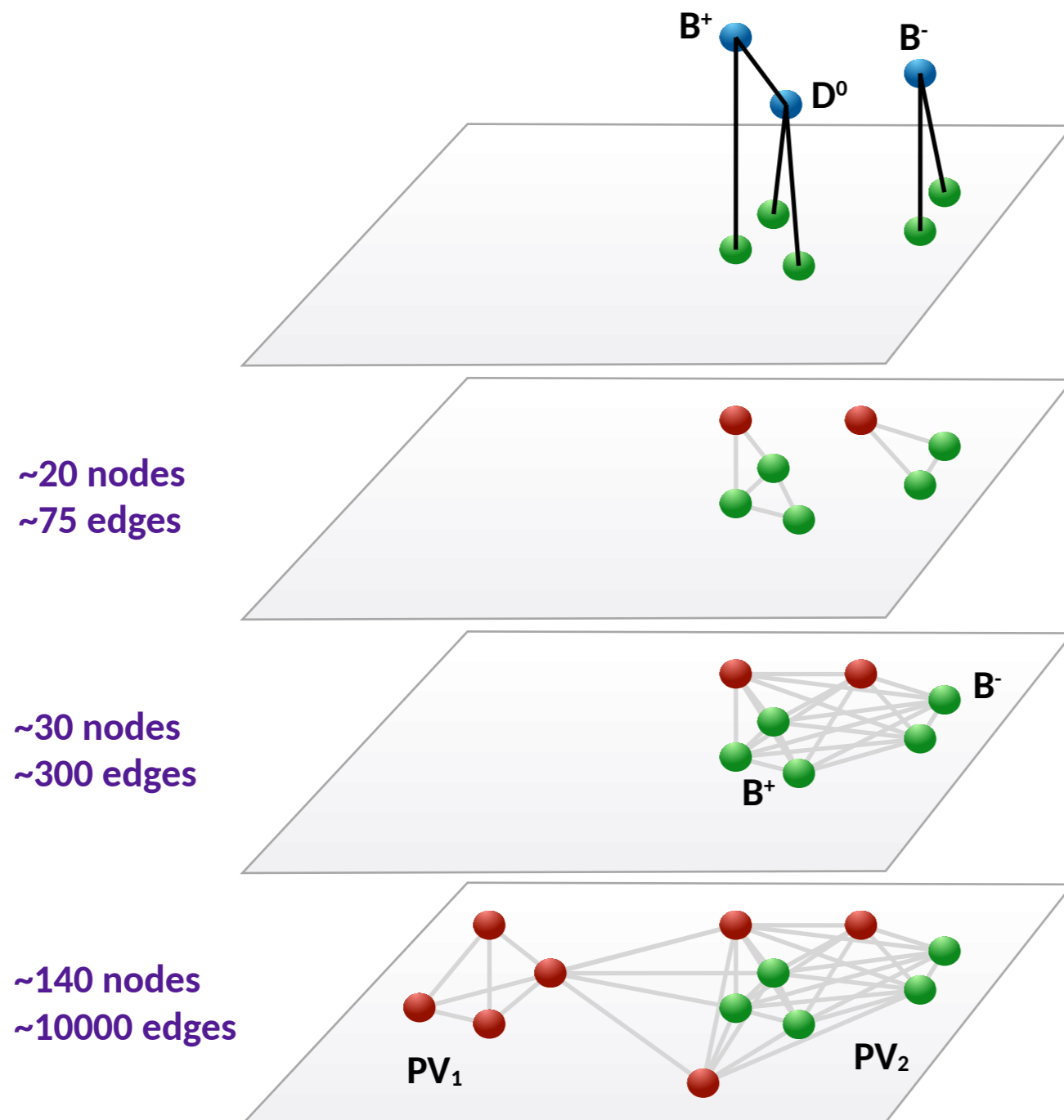
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Training

Dataset:

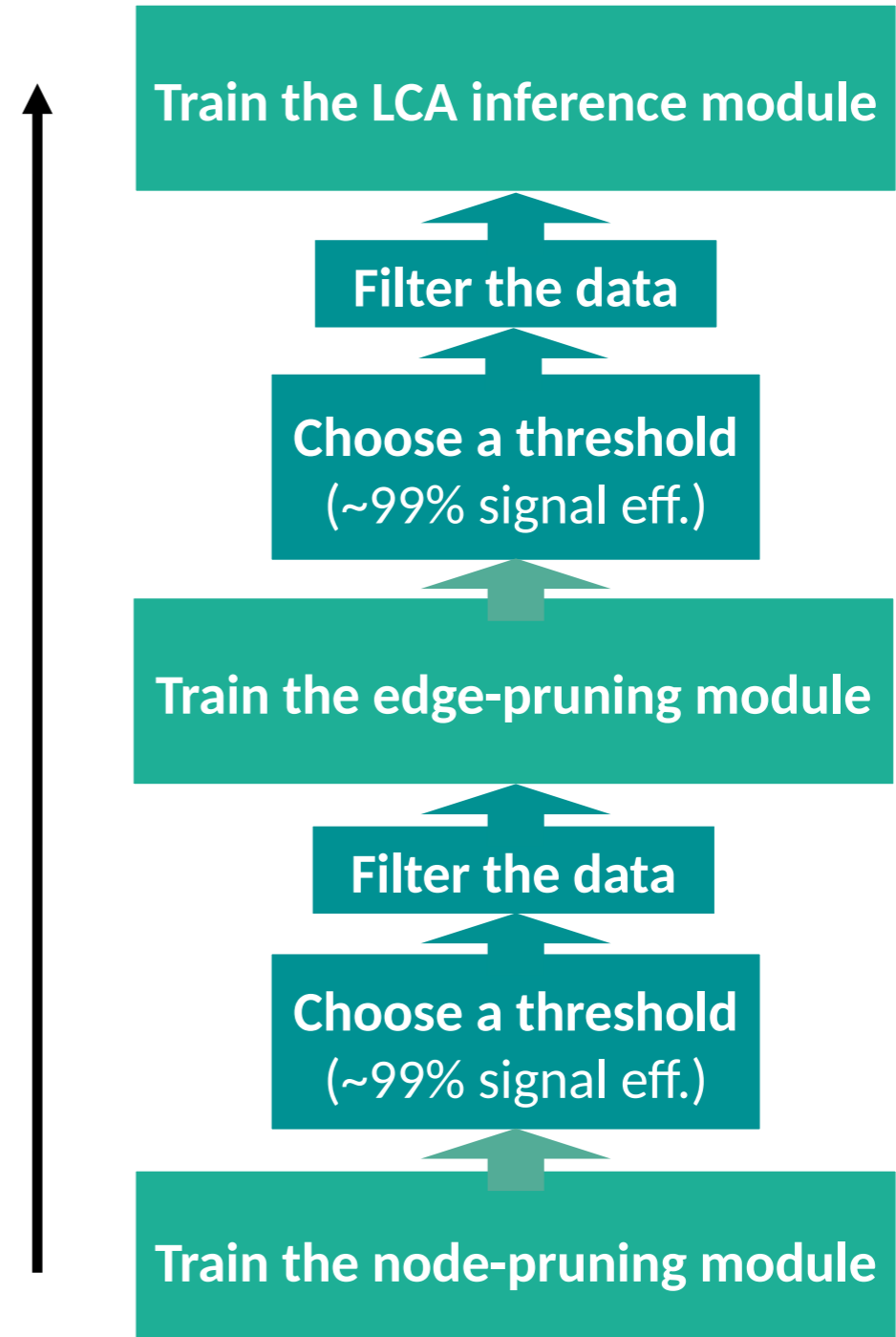
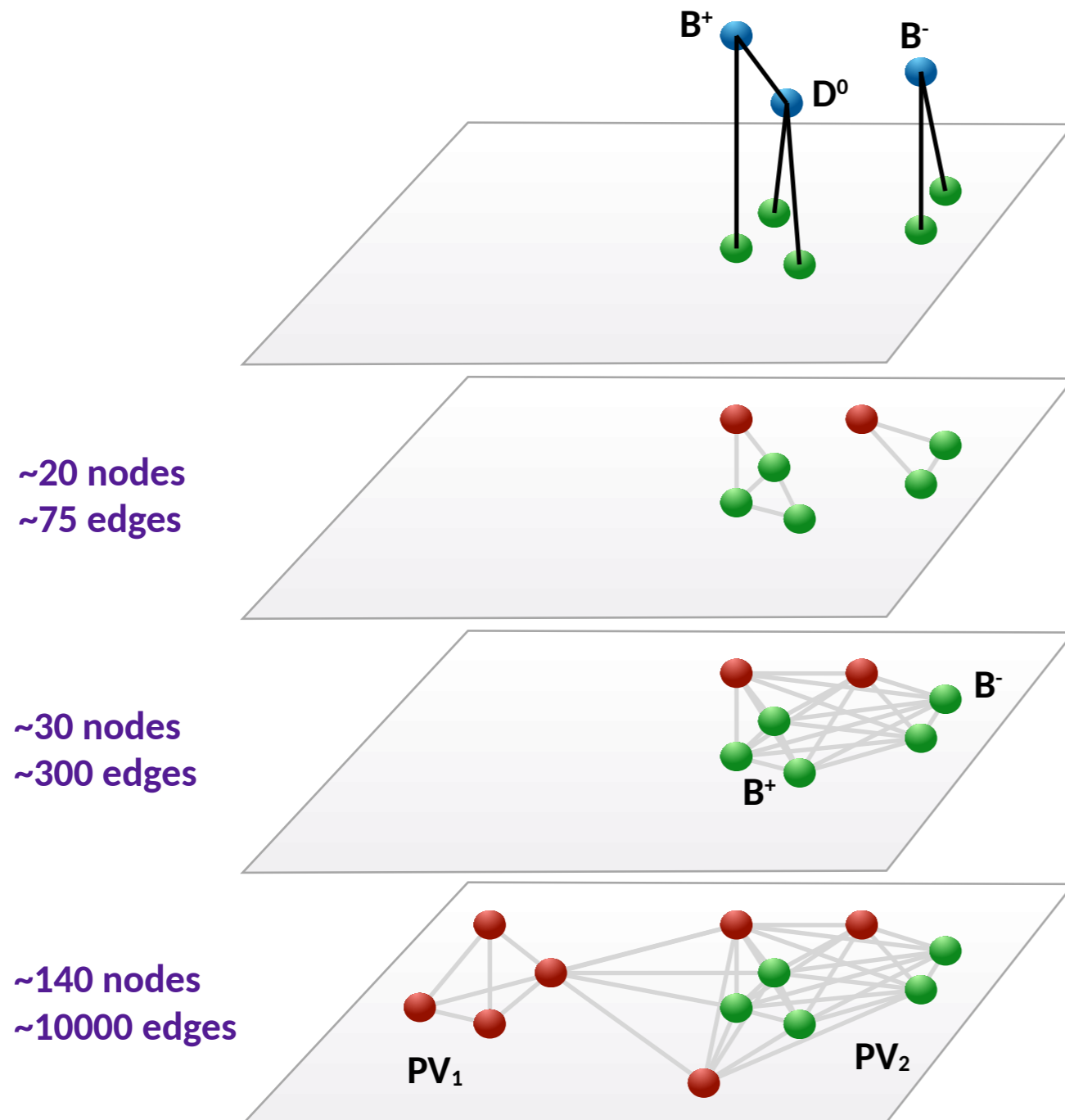
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Training

Dataset:

- PYTHIA-based simulation, Run 3-like conditions, approximated emulation of LHCb reconstruction.
- Events required to contain at least one b-hadron (inclusive decay).



Outlook

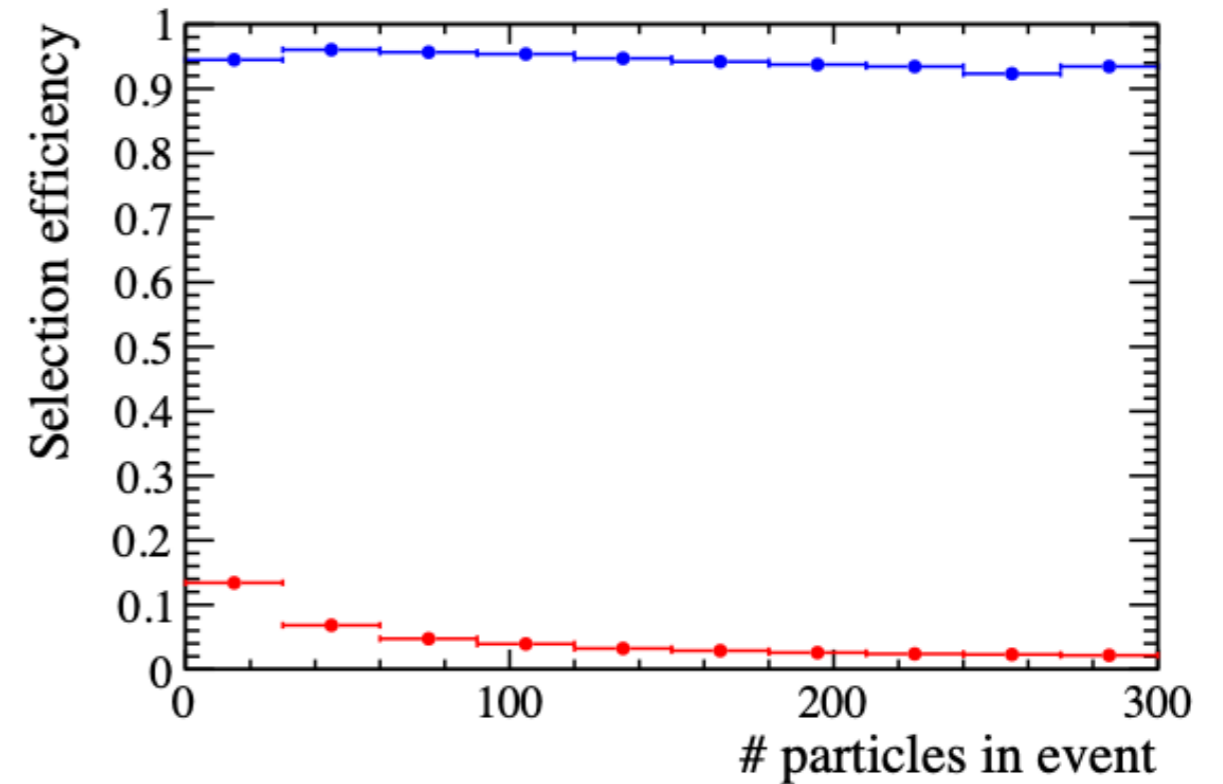
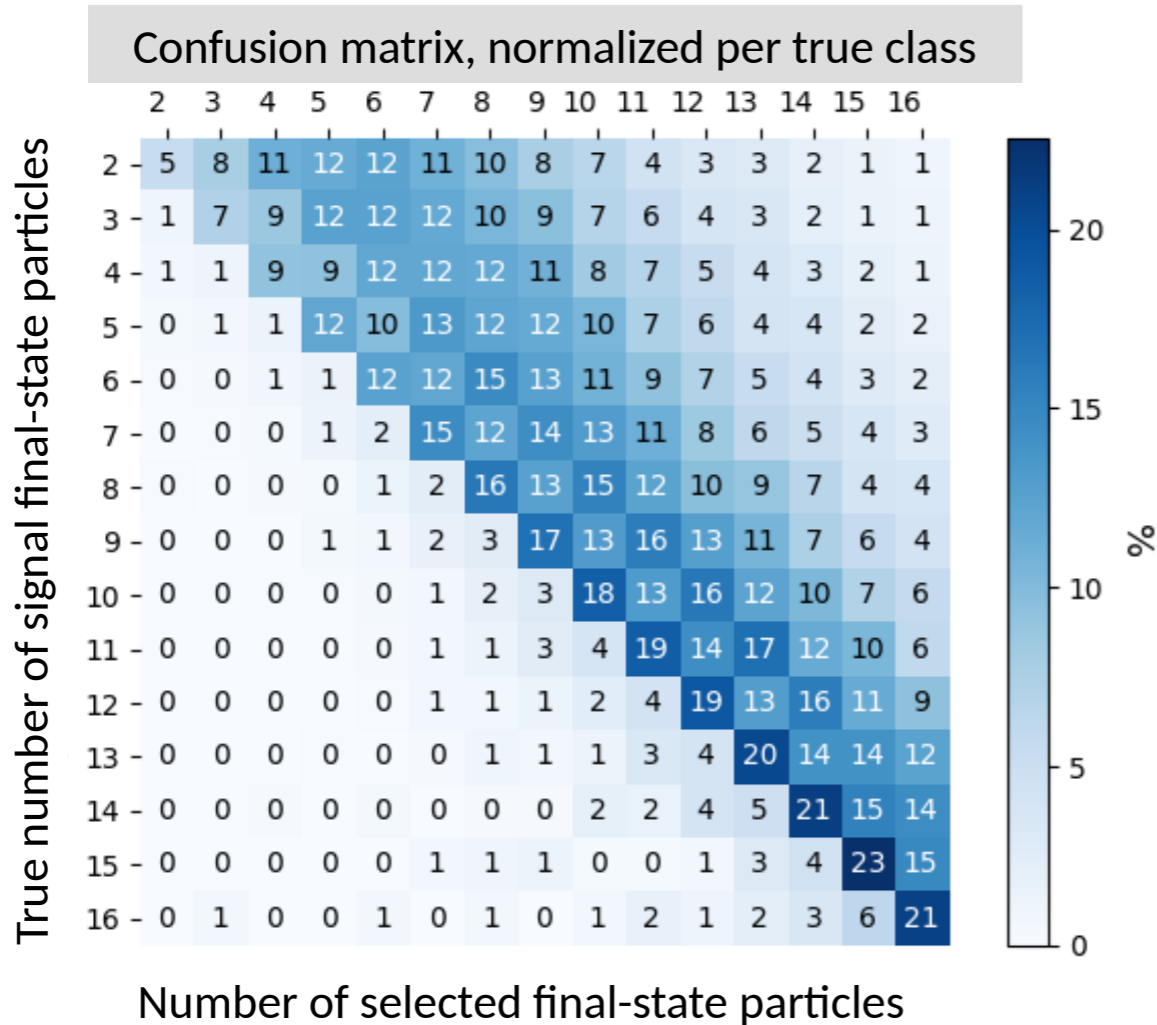
Performance

**Run3-like
conditions**

The algorithm

Motivation

Performance: final-state particle filtering



Consistent performance with different number of signals

“single-b-hadron-signal” approach performance **comparable** to the envisaged nominal LHCb strategy for Run 3 [\[JINST 14 \(2019\) 04, P04006\]](#)

LHCb: 90% sig eff, 90% bkg rej. power
DFEI: 94% sig eff, 96% bkg rej. power

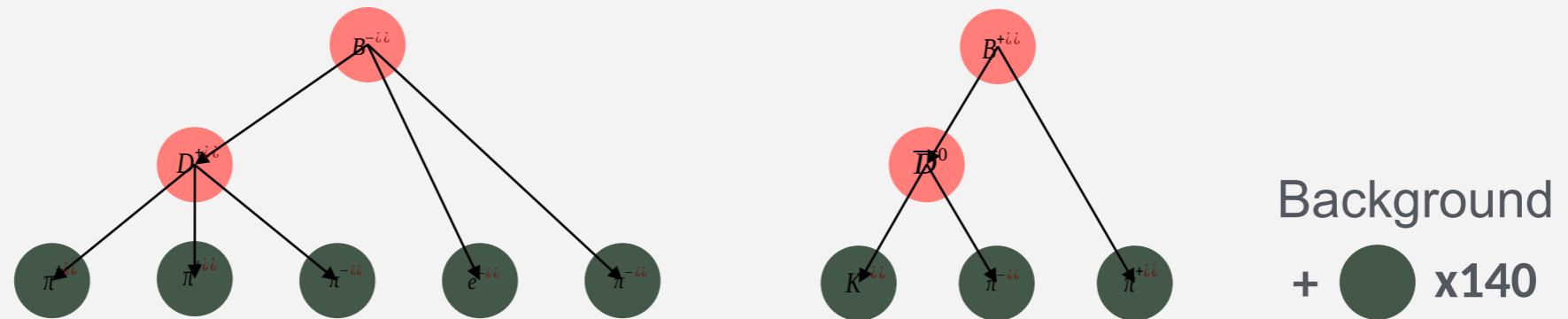
DFEI selects all of them simultaneously

DFEI capability #1
 Powerful event size (~ x14) reduction in a multi-signal environment.

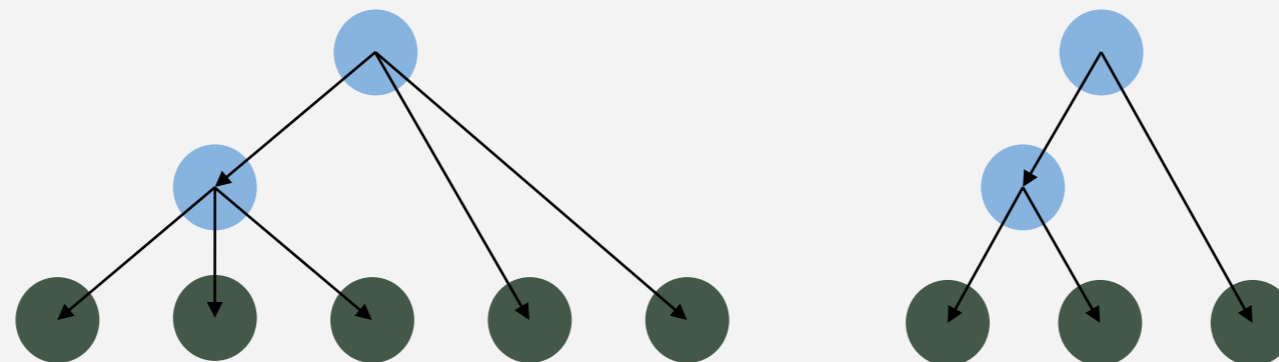
Performance: perfect event reconstruction (PER)

Real example of a perfectly reconstructed simulation event.

Simulated event



DFEI output



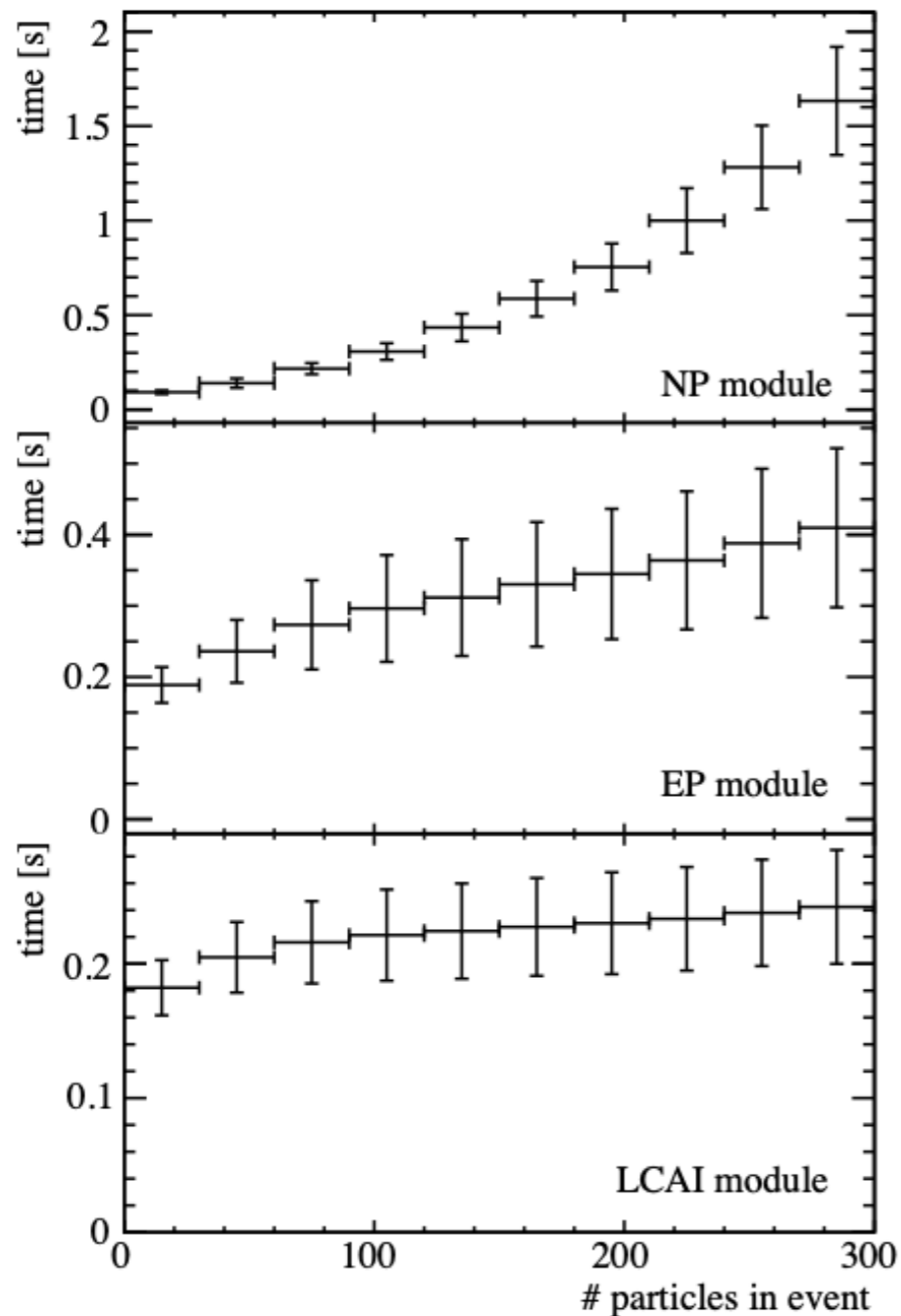
- PER efficiency similar to tag-side efficiency for Belle (II)
- Can be easily extended for more target variables!

DFEI capability #2
Automatised and inclusive
reconstruction of decay chains.

Timing studies

Scaling

current implementation



Implementation

Currently Python & TensorFlow
flexible for experimenting

TMVA SOFIE implementation (WIP)
Fast Inference System

Possible speed improvements

Simplification of layers, especially first
Approximate convolutions etc.

Hardware accelerators such as FPGA, GPU,...
WIP for GNNs in general

Outlook

Performance

The algorithm

Motivation

Summary

Increased particle multiplicities for LHCb Upgrades I and II bring **big challenges**, both for trigger and offline analysis

Paradigm change in trigger:

“which events?” → “which parts of the event?”

Deep-learning based Full Event Interpretation

Online application:

- Safely discard rest of event, minimal loss for analyses
- Hierarchical reconstruction of heavy-hadron decay chains

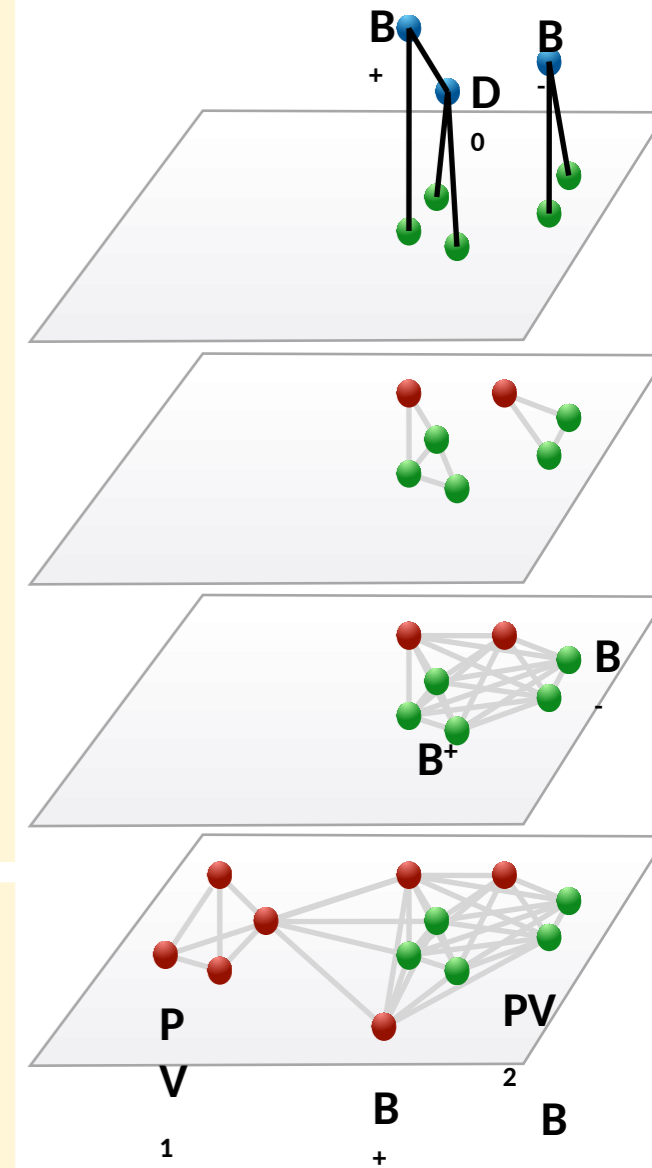
Offline application:

- Tool for powerful background classification & suppression

First prototype of the DFEI algorithm based on GNN

focused on b -hadron decays and charged stable particles

Very promising performance in realistic conditions!



Next steps

Algorithmic optimization and architectural choices

- Accuracy and useful information (separation, signal channels, ...)
- Expansion in functionality (neutrals, PID, ...)

Extensive performance studies, crucial for calibration

- In simulation
- In real data

Integration in LHCb trigger

- Export into ROOTs TMVA SOFIE, finishing GNN implementation
- Study usage of hardware accelerators for Upgrade II (FPGA, GPU, ...)

Backup slides

Signal-based trigger vs Full Event Interpretation (FEI)

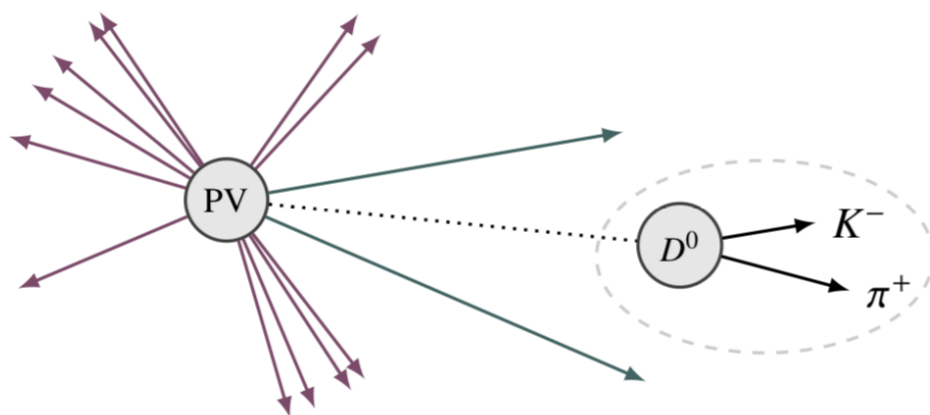
Signal based

The current LHCb trigger is an **OR between many decay-mode selection lines.**

Since Run2, to reduce the event size, some lines **store only parts of the event which are related** to the specific signal.

[\[JINST 14 \(2019\) 04, P04006\]](#)

E.g.: store the signal + the tracks in the same primary vertex (PV).



FEI

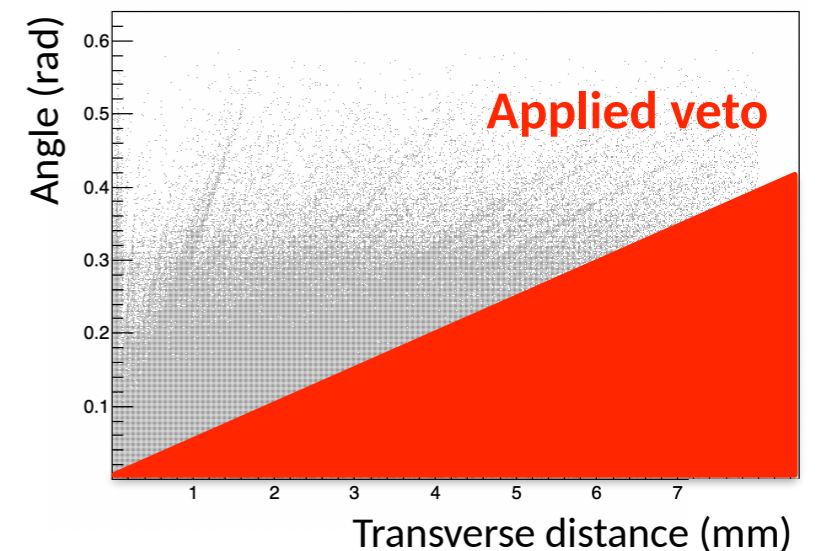
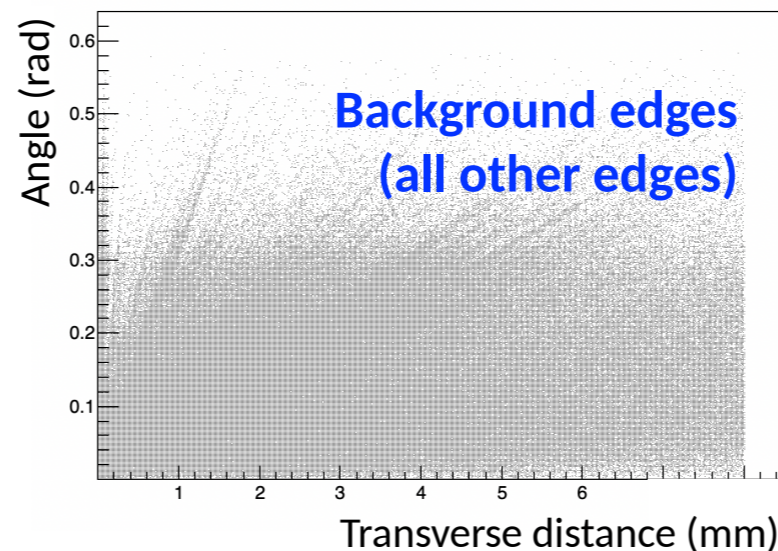
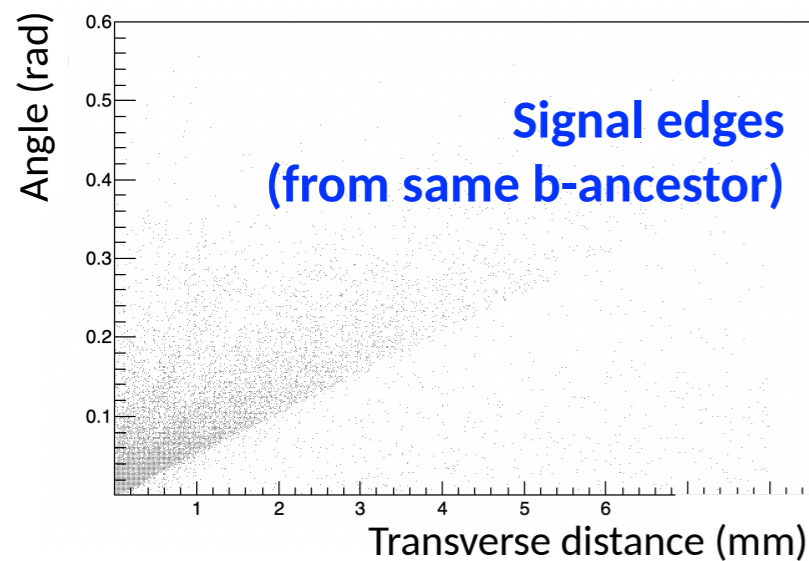
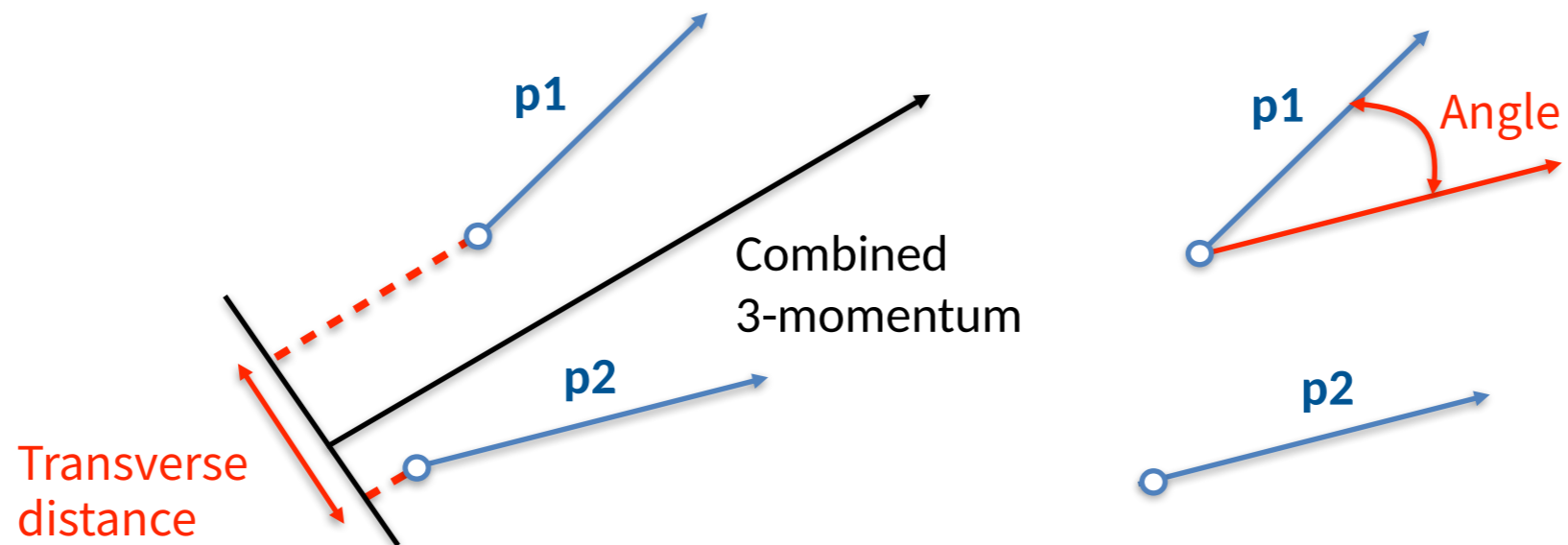
New proposal: try to **reconstruct the b- and c- hadron decay chains in the event**, in a hierarchical-clustering manner (cluster → unstable particle), **and discard the rest.**

Advantages:

- **Exploit extra correlations** between objects in the event.
- **Bandwidth oriented**: focus on storing as much “useful” information as possible.
 - Case of several signals per event as an integral part of the approach.
 - Establishment of a basis for an expanded functionality of the trigger: inclusive selections, study of anomalous events ...

Cut-based edge pruning

Define two adequate topological variables for each edge (pair of particles)



This veto reduces on average 60% of the total number of edges in the graph. It also reduces connections between signal tracks, but it only leaves ~2% of the signal tracks fully disconnected.

Training dataset: emulating Run3 conditions

Particle collision&decay

The training and performance studies are currently done using **PYTHIA**, with the following configuration:

- Proton-proton collisions at 13 TeV.
- Average number of collisions per event: 7.6.
- Selecting **events with at least one b-hadron produced (inclusive decay)**.

“Detection and reconstruction”

We require all the tracks and the b-hadrons to be **inside the LHCb geometrical acceptance**.

In addition, we **emulate the reconstruction of the following quantities**, using publicly available expectations for the LHCb performance in Run3 (see backup):

- **Origin point of the tracks** (first measurement in the Vertex Locator).
- **Three-momentum of the tracks**.
- **Position of the primary vertices**.

Example of decay-tree simplification used in the prototype

Original chain of ancestors:

$$\pi^+ \leftarrow \rho(770)^0 \leftarrow \varphi(1020) \leftarrow D^+ \leftarrow B^0 \leftarrow B^{*0}$$



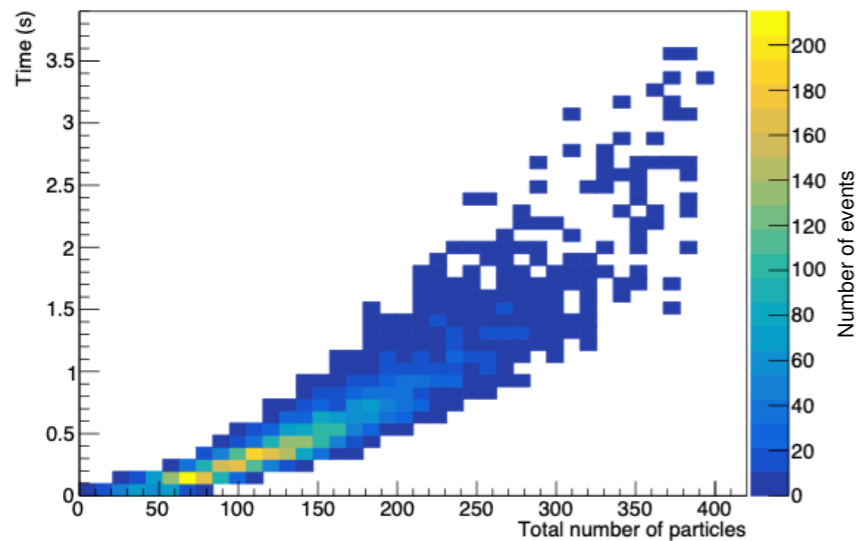
Simplified chain of ancestors (based on reconstructible vertices):

$$\pi^+ \leftarrow D^+ \leftarrow B^0$$

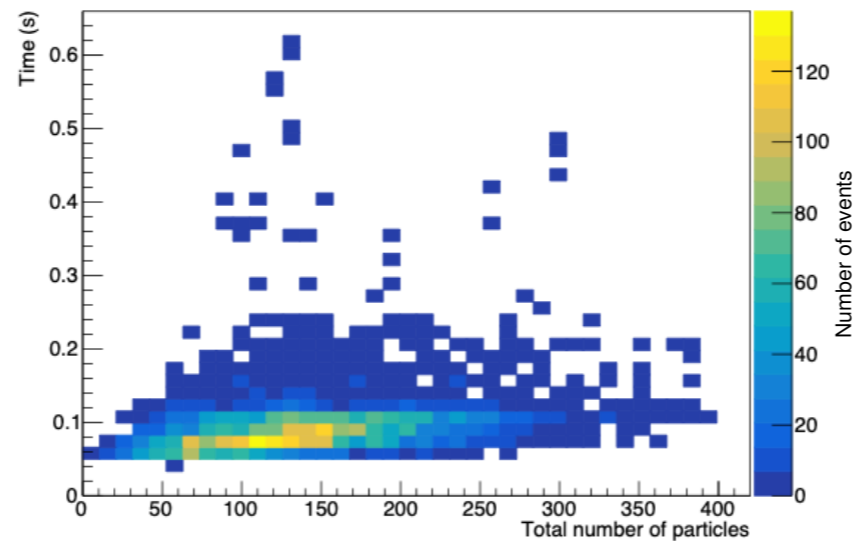
Performance: timing

Simplistic study (no parallelisation, no hardware accelerators*, algorithm to be further optimised), to understand which are the slowest parts of the algorithm and how they scale with the total number of particles per event.

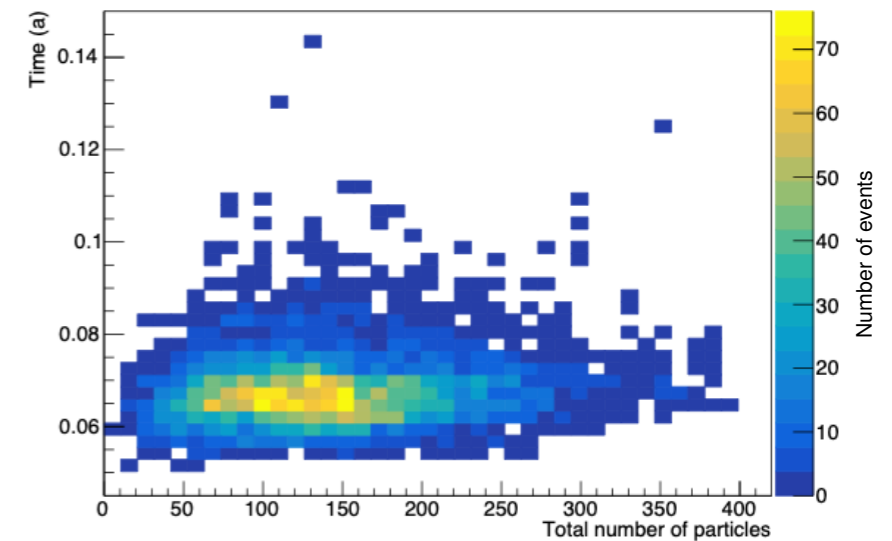
Node pruning



Edge pruning



LCA reconstruction



The slowest part is the node pruning, which also has the strongest dependency on the number of particles. → Many possible ways of optimisation.

The processing time of the subsequent algorithms is quite stable regarding changes in event complexity.

(*) Study done on a darwin-x86_64 architecture with a 2.8 GHz Intel Core i7 processor.