

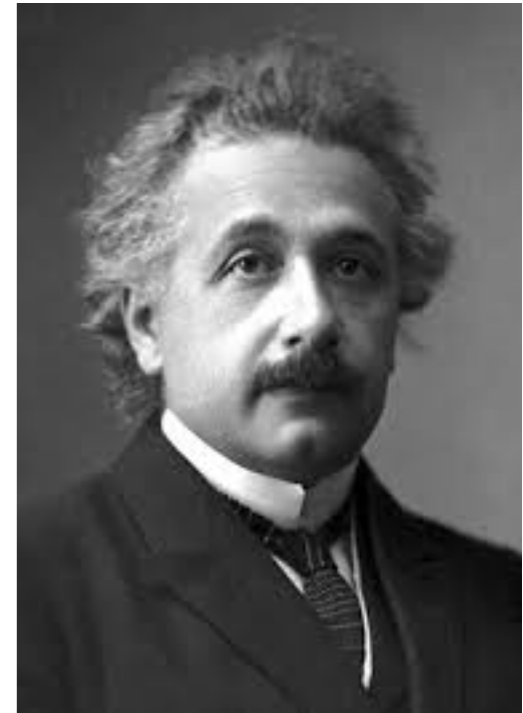
Higgs(ino) physics in the era of future accelerators



Howard Baer
University of Oklahoma

Corfu future accelerators,
April 2023

twin pillars of guidance:
naturalness & simplicity



“The appearance of fine-tuning in a scientific theory is like a cry of distress from nature, complaining that something needs to be better explained”

S. Weinberg

“Everything should be made as simple as possible, but not simpler”

A. Einstein

The Standard Model of Particle Physics

- ★ gauge symmetry: $SU(3)_C \times SU(2)_L \times U(1)_Y \Rightarrow g_{\mu A}, W_{\mu i}, B_{\mu}$
- ★ matter content: 3 generations quarks and leptons

$$\begin{pmatrix} u \\ d \end{pmatrix}_L, u_R, d_R; \begin{pmatrix} \nu \\ e \end{pmatrix}_L, e_R \quad (1)$$

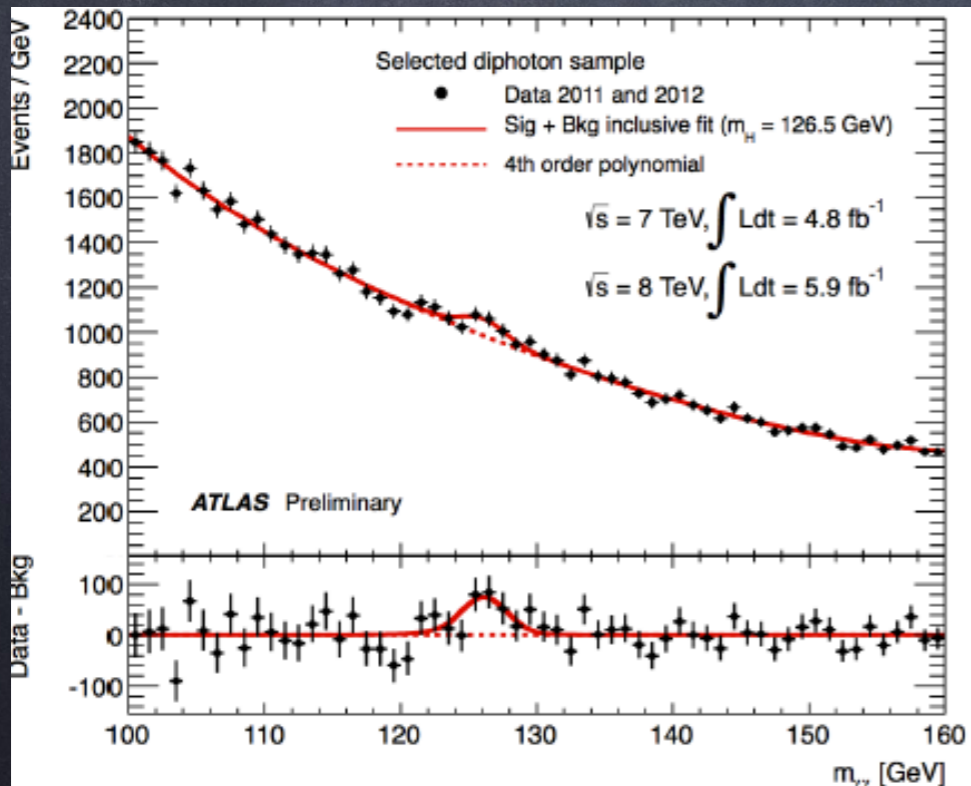
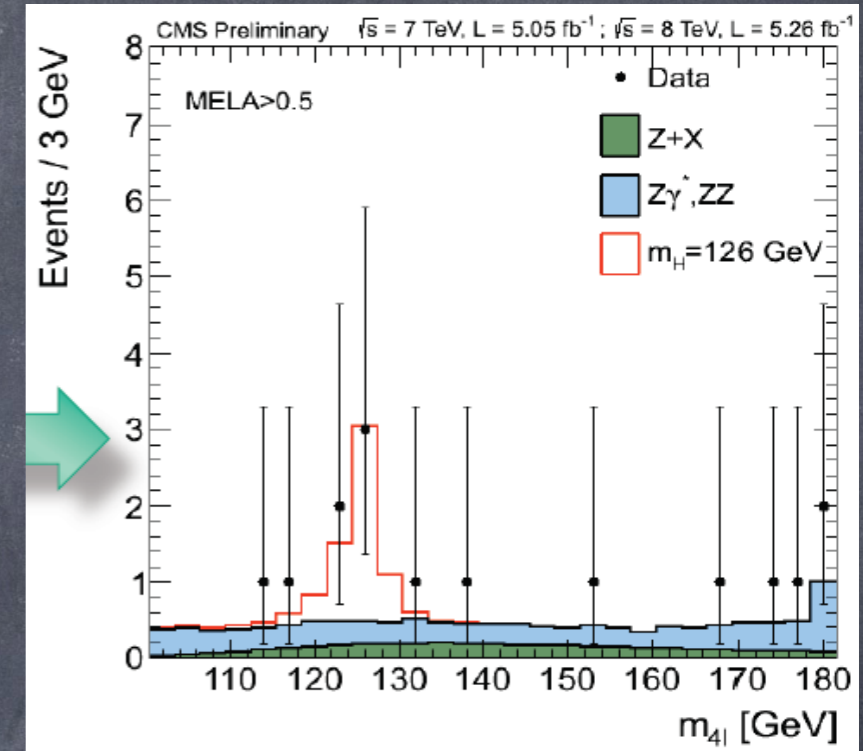
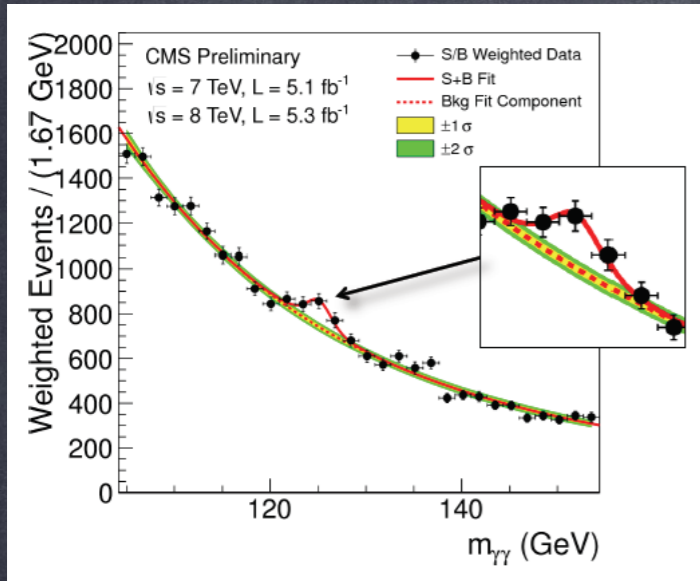
- ★ Higgs sector \Rightarrow spontaneous electroweak symmetry breaking:

$$\phi = \begin{pmatrix} \phi^+ \\ \phi_0 \end{pmatrix} \quad (2)$$

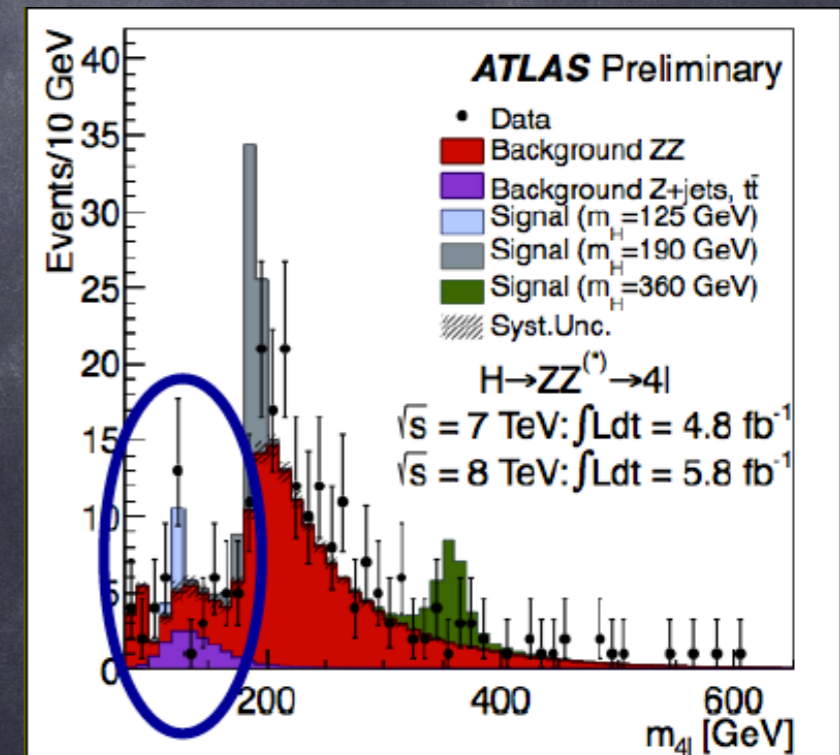
- ★ \Rightarrow massive W^{\pm}, Z^0 , massless γ , massive quarks and leptons; Higgs scalar H
- ★ $\mathcal{L} = \mathcal{L}_{gauge} + \mathcal{L}_{matter} + \mathcal{L}_{Yuk.} + \mathcal{L}_{Higgs}$: 19 parameters
- ★ good-to-excellent description of (almost) *all* accelerator data!

LHC Higgs discovery: July 4, 2012!

$$m_h \sim 125 \text{ GeV}$$

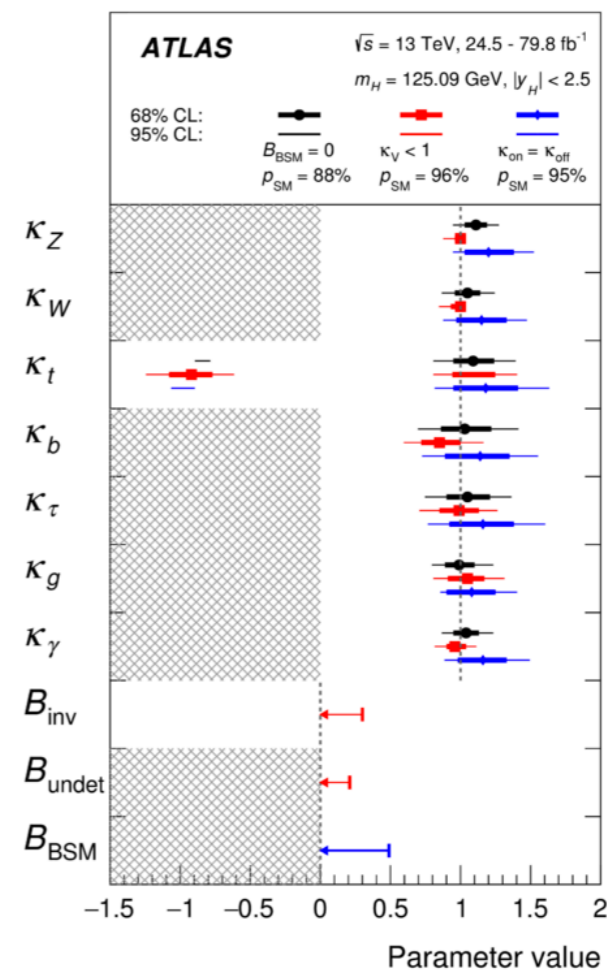
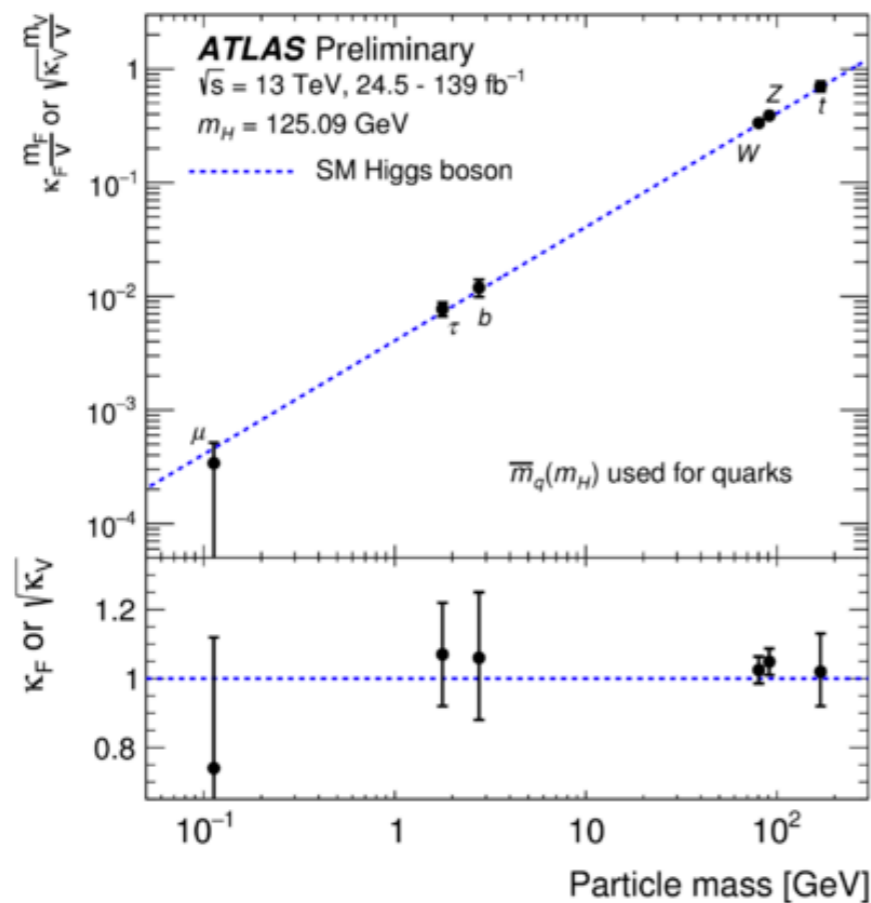
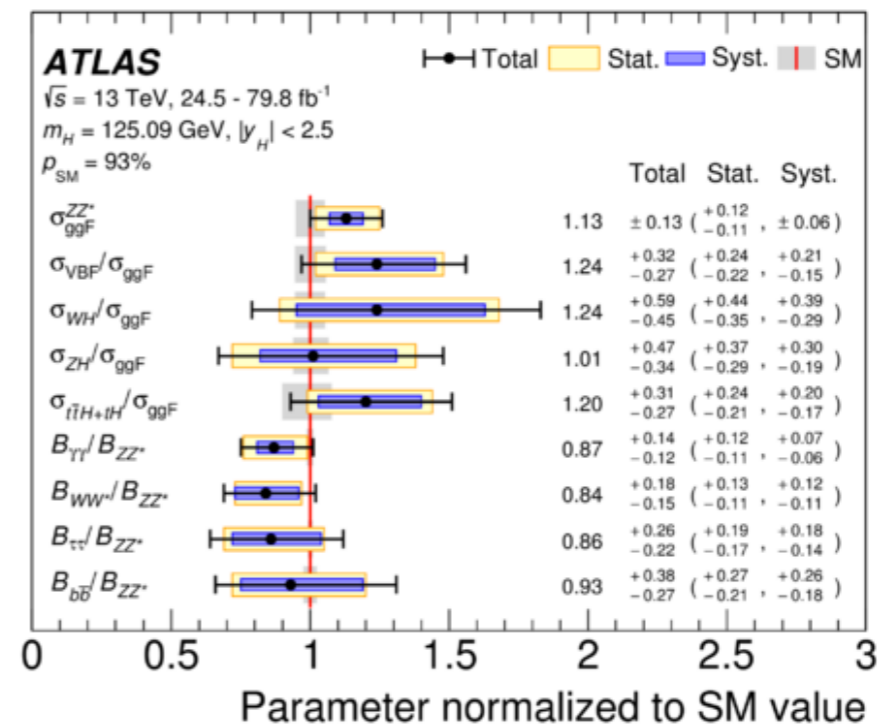
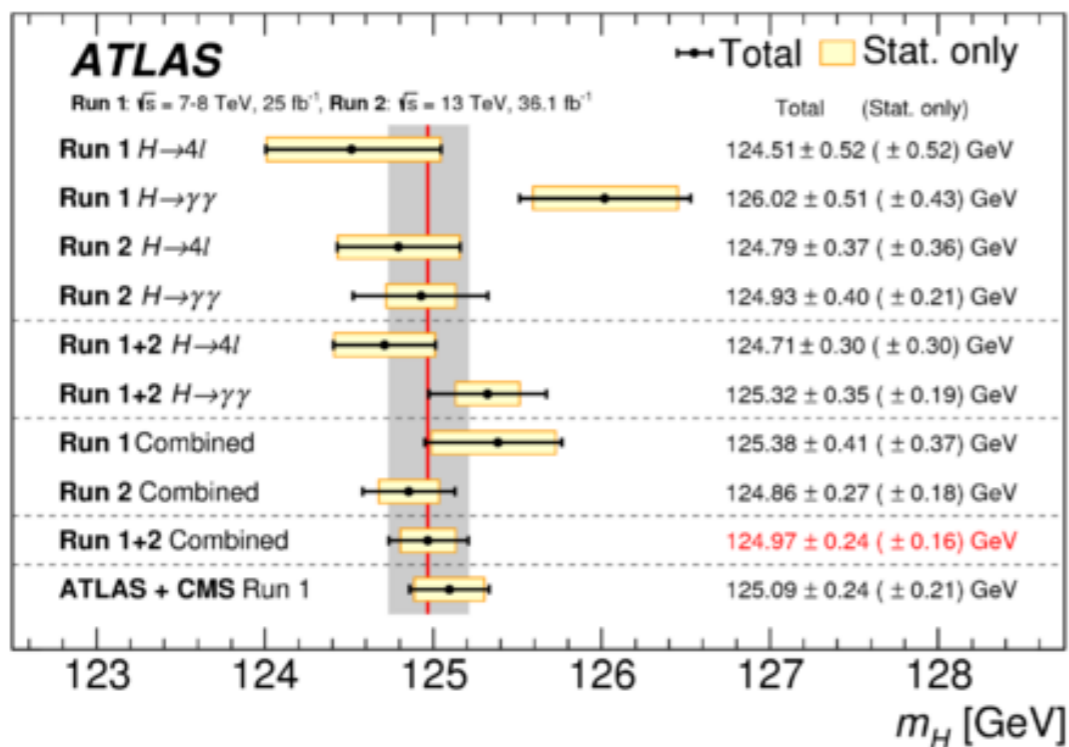


2013 Nobel



Excess of events also reported from CDF/D0

Higgs properties: $m(h)=125.1$ GeV and very SM-like!



- What to make of this?
- What happened to SUSY? (was expected)
- Is there a 'naturalness' crisis?
- What does it imply for future collider facilities?

Standard Model is regarded as an
“effective field theory” valid at energy scales $< \sim 1$ TeV

- Higgs mass instability
- strong CP problem
- cosmological constant
- inclusion of gravity
- origin of generations
- dark matter
- dark energy
- baryogenesis

expect new physics:
but what form?
and at what mass scale?

The top three SM finetuning problems:

and most plausible solutions to date

- Hierarchy problem: how can weak scale be so much smaller than GUT/Planck scale? **SUSY**
- Strong CP problem (QCD): why is QCD theta parameter so small $\lesssim 10^{-10}$ **axion**
- Cosmological constant: $\rho_{vac} \sim (0.003 \text{ eV})^4 \ll m_P^4$

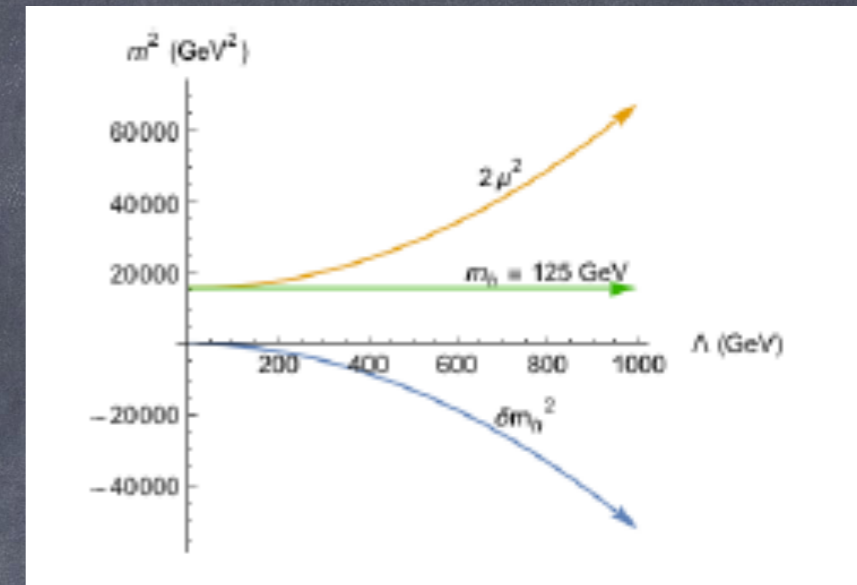
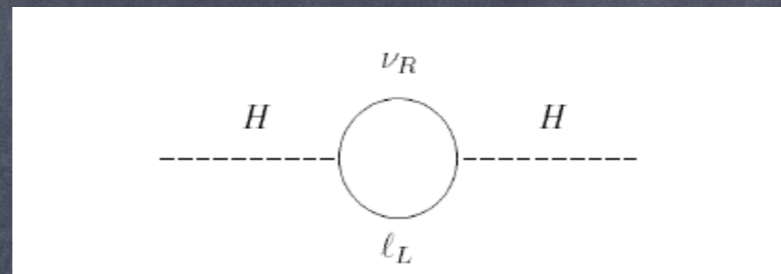
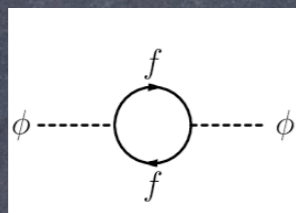
anthropic vacua selection from multiverse/string vacua

Hierarchy of scales problem in the SM

Biggest conundrum of SM: why is Higgs mass so small?

1. There is a lowest order mass term

2. Quantum corrections diverge quadratically with energy scale of new physics



$$m_{H_{SM}}^2 = 2\mu^2 + \delta m_{H_{SM}}^2$$

$$\delta m_{H_{SM}}^2 \simeq \frac{3}{4\pi^2} \left(-\lambda_t^2 + \frac{g^2}{4} + \frac{g^2}{8 \cos^2 \theta_W} + \lambda \right) \Lambda^2$$

3. To avoid the pathology of fine-tuning, SM must be valid only to $\Lambda \sim 1$ TeV

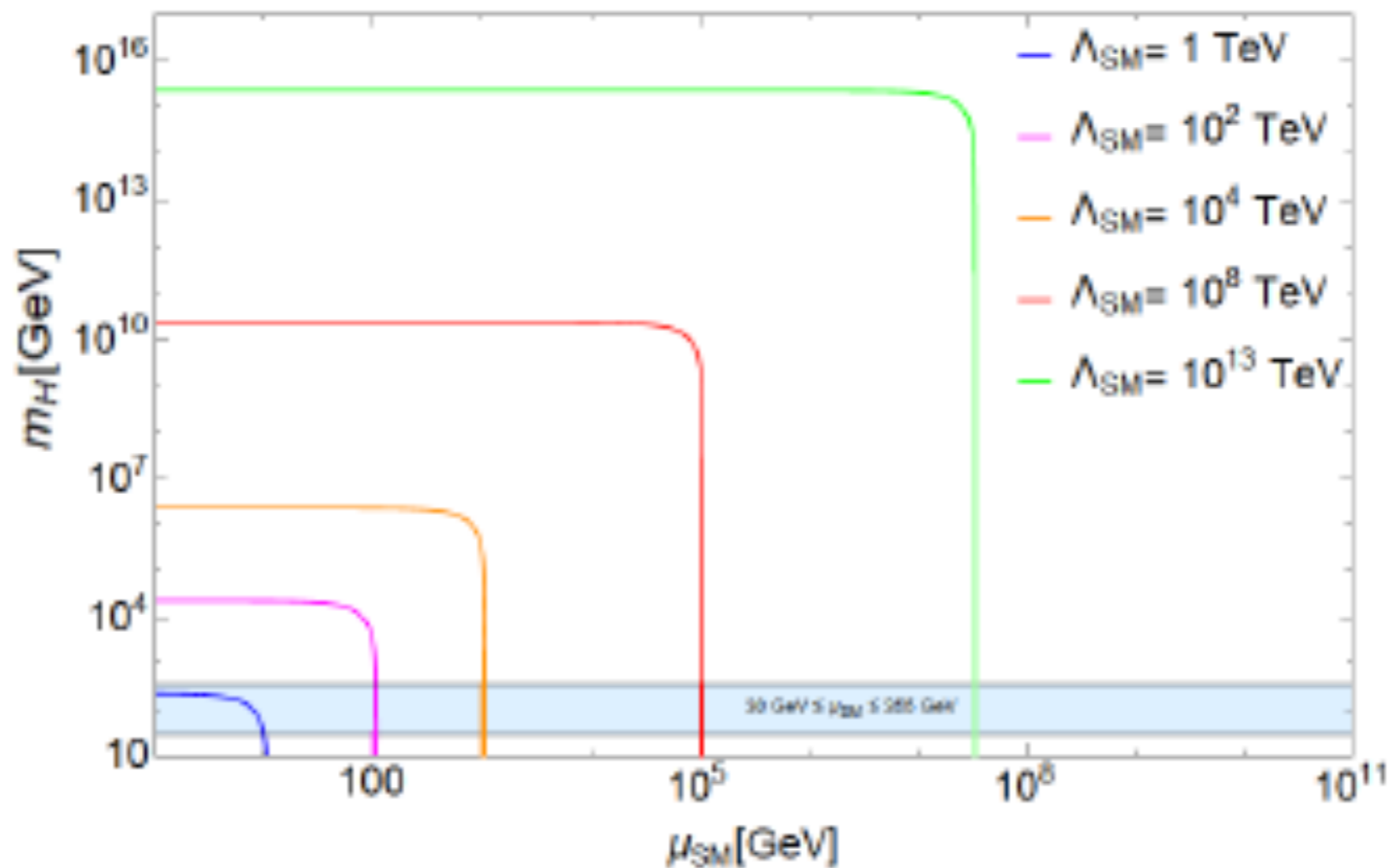
4. Need theory which is free of quadratic divergences to extend e.g. to GUT/Planck scale

another vantage point: SM is logically possible
but **highly implausible** finetuning is needed!

$$V = -\mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2$$

$$m_h^2 \simeq 2\mu^2 + \delta m_h^2$$

$$\delta m_h^2 \simeq \frac{3}{4\pi^2} \left(-\lambda_t^2 + \frac{g^2}{4} + \frac{g^2}{8 \cos^2 \theta_W} + \lambda \right) \Lambda^2$$



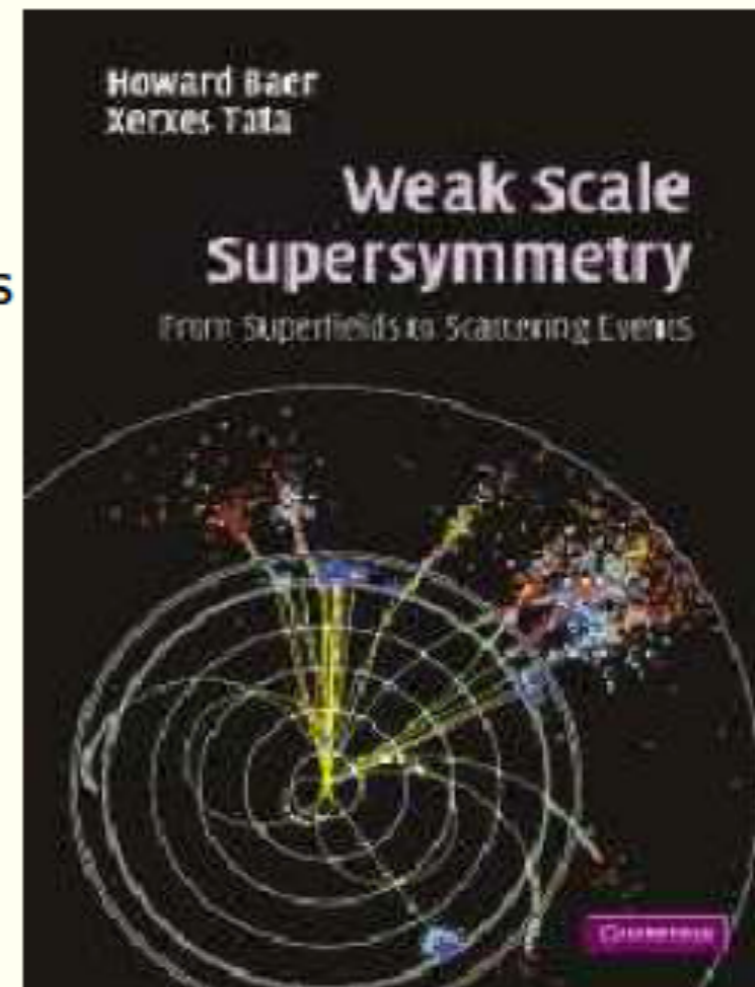
SUSY provides a clean/elegant solution to hierarchy problem

Weak Scale Supersymmetry

HB and X. Tata

Spring, 2006; Cambridge University Press

- ★ Part 1: superfields/Lagrangians
 - 4-component spinor notation for exp'ts
 - master Lagrangian for SUSY gauge theories
- ★ Part 2: models/implications
 - MSSM, SUGRA, GMSB, AMSB, ...
- ★ Part 3: SUSY at colliders
 - production/decay/event generation
 - collider signatures
 - R -parity violation



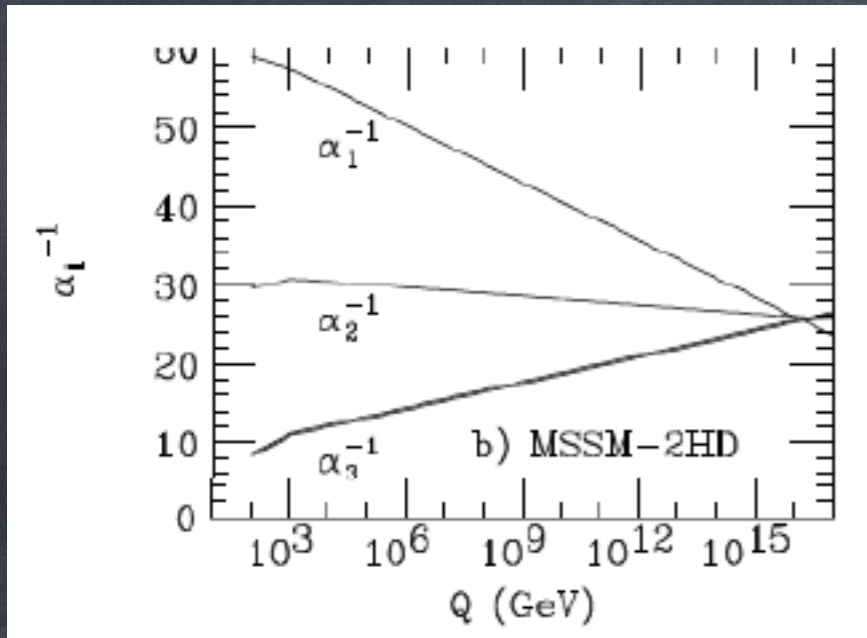
Minimal Supersymmetric Standard Model (MSSM)

- ★ Adopt gauge symmetry of Standard Model: $SU(3)_C \times SU(2)_L \times U(1)_Y$
 - gauge boson plus spin $\frac{1}{2}$ gaugino \in gauge superfield
- ★ SM fermions \in chiral scalar superfields: \Rightarrow scalar partner for each SM fermion helicity state
 - electron $\Leftrightarrow \tilde{e}_L$ and \tilde{e}_R
- ★ *two* Higgs doublets to cancel triangle anomalies: H_u and H_d
- ★ add all admissible soft SUSY breaking terms
- ★ resultant Lagrangian has 124 parameters!
- ★ Lagrangian yields mass eigenstates, mixings, Feynman rules for scattering and decay processes
- ★ predictive model!

Physical states of MSSM:

- ★ usual SM gauge bosons, quarks and leptons
- ★ gluino: \tilde{g}
- ★ bino, wino, neutral higgsinos \Rightarrow neutralinos: $\tilde{Z}_1, \tilde{Z}_2, \tilde{Z}_3, \tilde{Z}_4$
- ★ charged wino, higgsino \Rightarrow charginos: $\tilde{W}_1^\pm, \tilde{W}_2^\pm$
- ★ squarks: $\tilde{u}_L, \tilde{u}_R, \tilde{d}_L, \tilde{d}_R, \dots, \tilde{t}_1, \tilde{t}_2$
- ★ sleptons: $\tilde{e}_L, \tilde{e}_R, \tilde{\nu}_e, \dots, \tilde{\tau}_1, \tilde{\tau}_2, \tilde{\nu}_\tau$
- ★ Higgs sector enlarged: h, H, A, H^\pm
- ★ a plethora of new states to be found at LHC/ILC?!

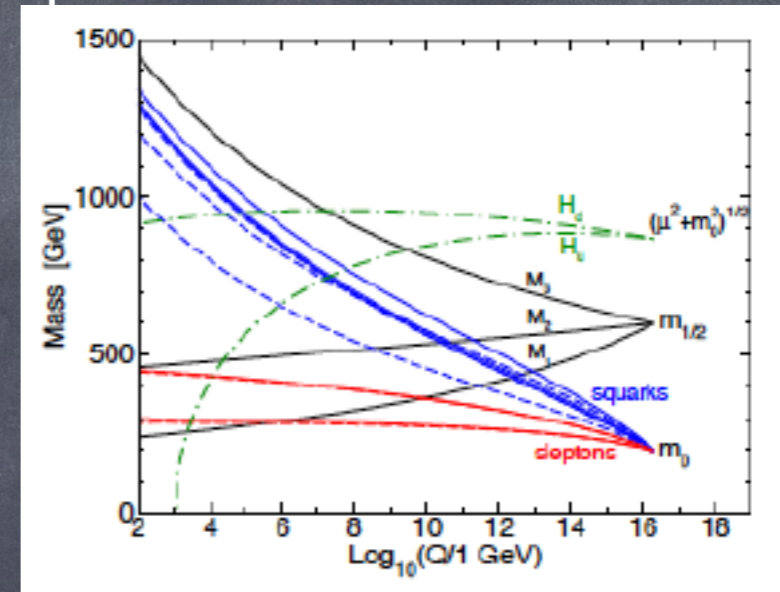
The MSSM is supported by virtual quantum effects!



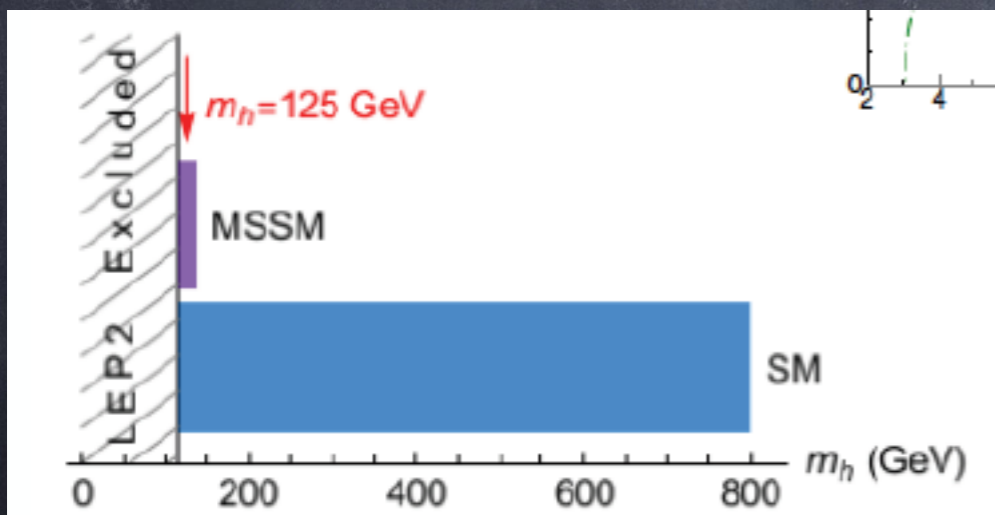
Unification of gauge couplings

$$m(t) \sim 150-200 \text{ GeV}$$

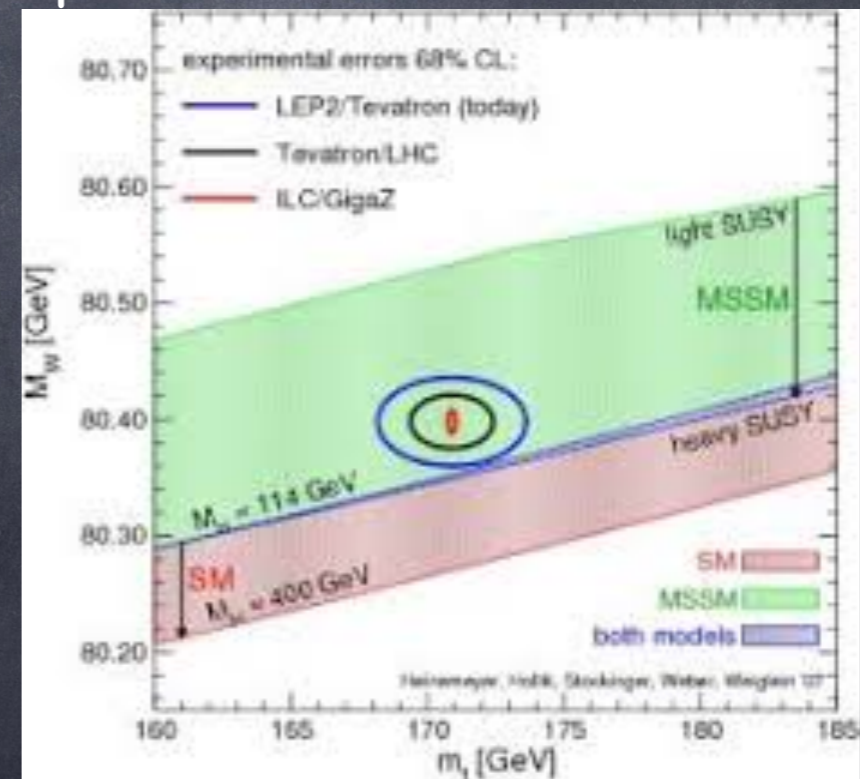
required for radiative EWSB



$m(h)$ just right



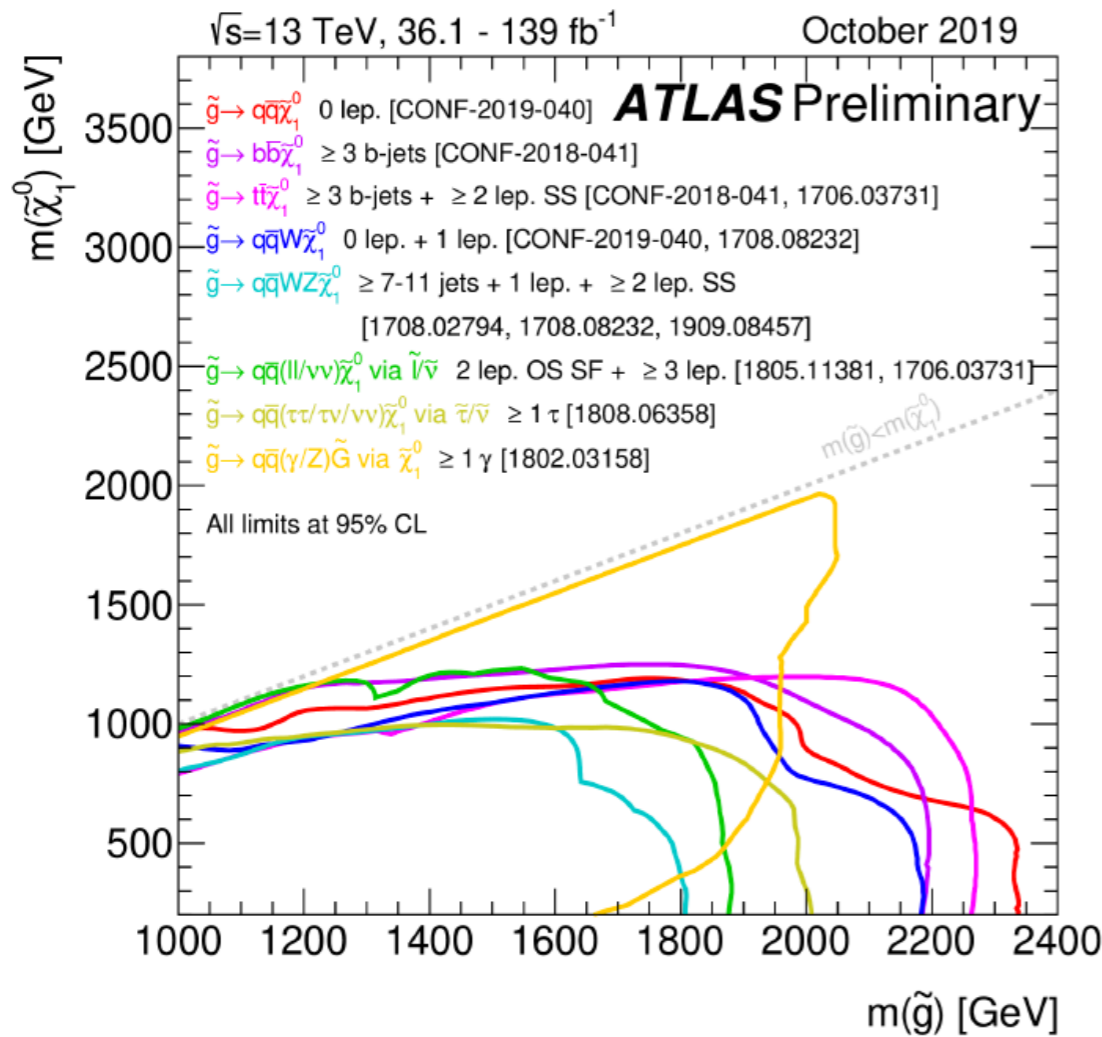
precision electroweak fits



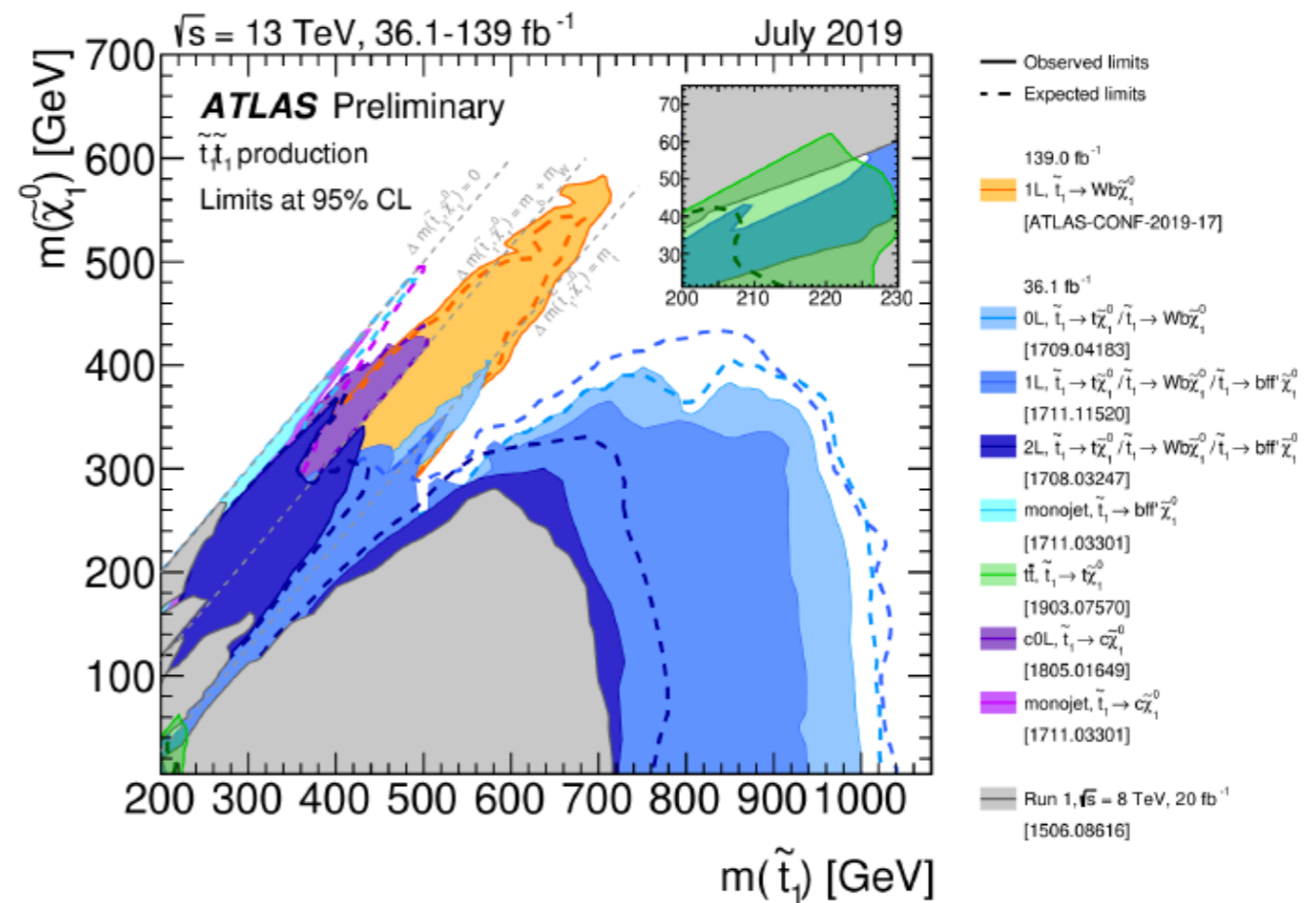
Radiative corrections have proven to be a reliable guide to new physics

But where are the sparticles?

none seen so far at LHC

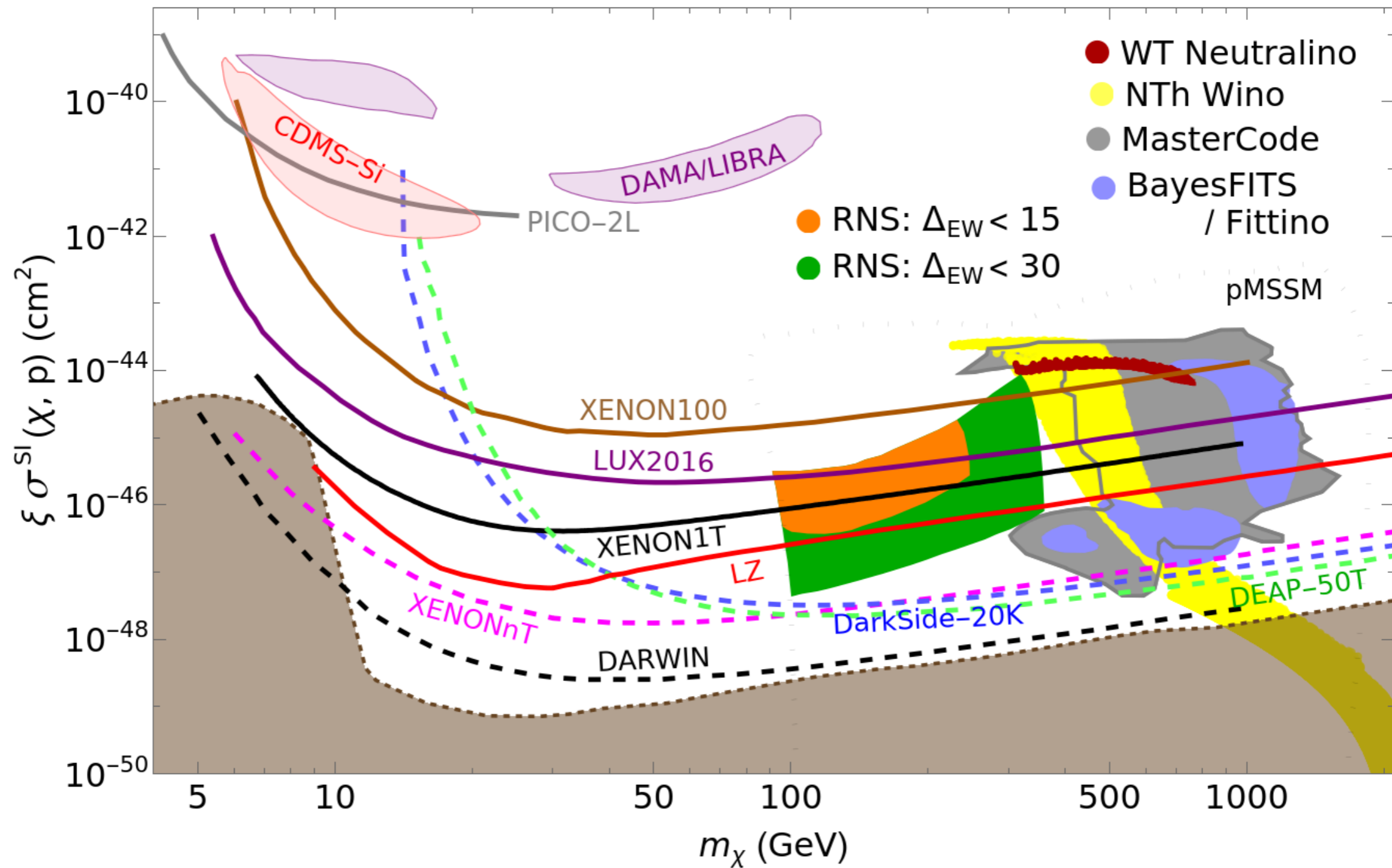


$$m_{\tilde{g}} > 2.25 \text{ TeV}$$



$$m_{\tilde{t}_1} > 1.1 \text{ TeV}$$

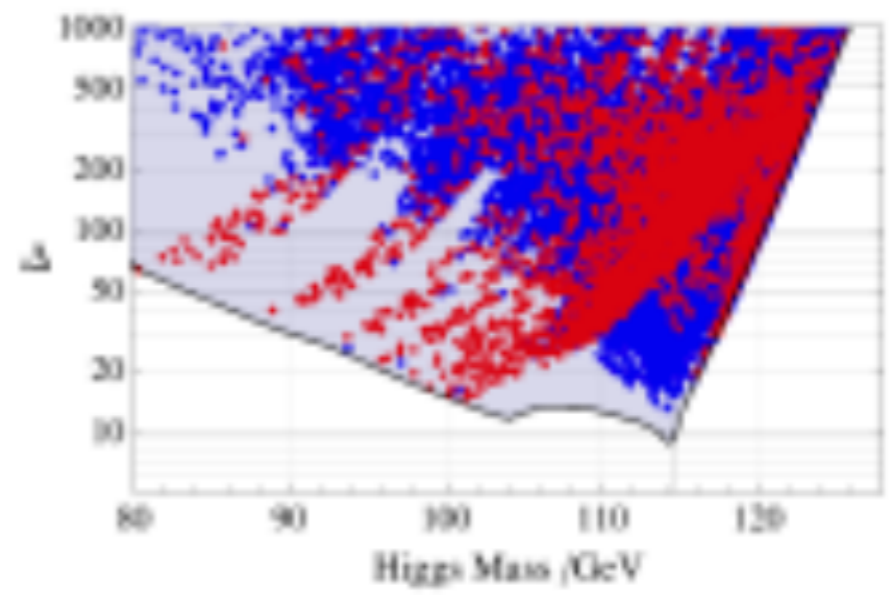
Where are the WIMPs?



latest DD bounds from LZ2022: still no signal

These bounds appear in sharp conflict with EW “naturalness”

	mass
gluino	400 GeV
uR	400 GeV
eR	350 GeV
chargino	100 GeV
neutralino	50 GeV



Cassel, Ghilencea, Ross, 2009

$\Delta \rightarrow 1000$
 as $m_h \rightarrow 125$ GeV
 0.1% tuning!?

Barbieri-Giudice 10% bounds, 1987

“...settling the ultimate fate of naturalness is perhaps the most profound theoretical question of our time”



Arkani-Hamed et al.,
arXiv:1511.06495

“Given the magnitude of the stakes involved,
it is vital to get a clear verdict
on naturalness from experiment”

This should be matched by theoretical scrutiny
of what we mean by naturalness

SUSY provides a 't Hooft natural solution
to the Big Hierarchy problem (BHP):
as $m(\text{soft}) \rightarrow 0$, model becomes super- and EW- symmetric

But the present concern is: **Little Hierarchy problem (LHP):**

how is $m(\text{weak}) \sim m(W, Z, h) \ll m(\text{soft})$?

Introduce notion of **practical naturalness:**

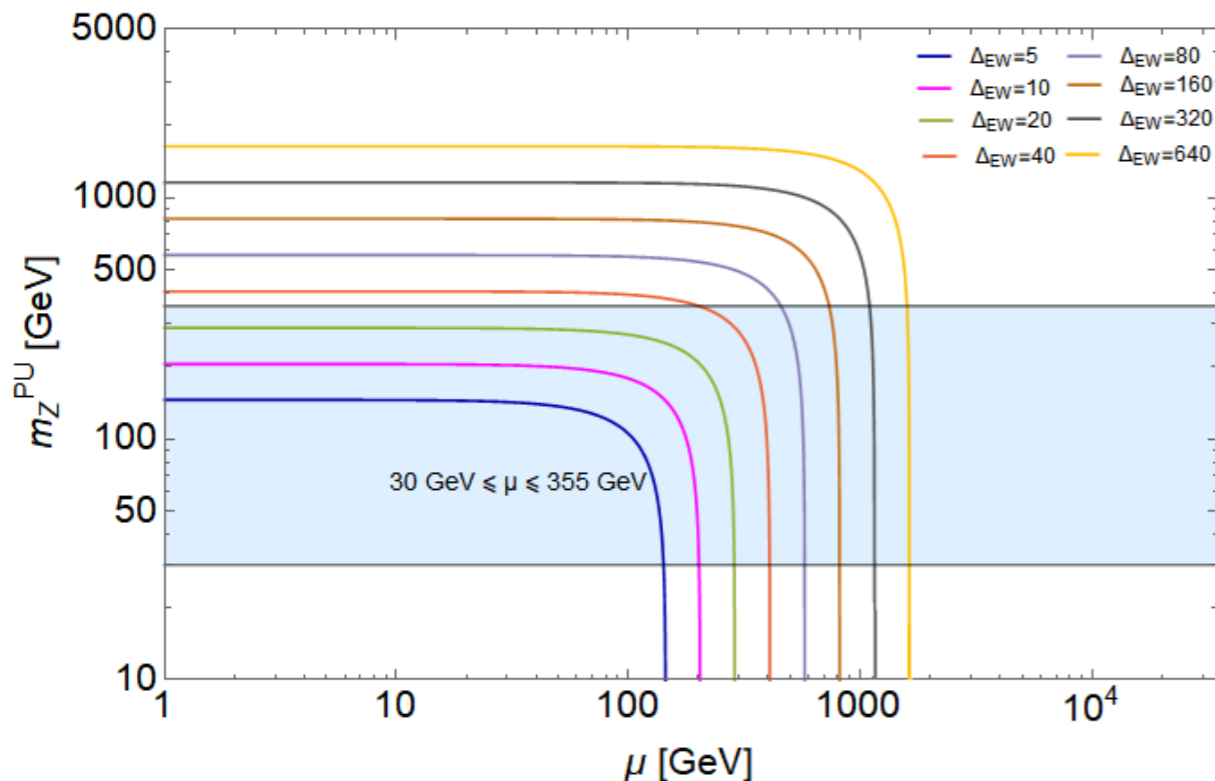
HB, Barger, Savoy: [arXiv:1509.02929](https://arxiv.org/abs/1509.02929)

An observable \mathcal{O} is *natural* if all contributions to \mathcal{O} are $< \sim \mathcal{O}$

- *e.g.* if $\mathcal{O} = a + b - c$, and if $a \gg \mathcal{O}$, then some *independent* contribution such as b would have to be fine-tuned to large opposite-sign value such as to maintain \mathcal{O} at its measured value.
- Such a fine-tuning is regarded as unnatural and implausible, and indicative of some missing element in the theory (see Weinberg, Title page).
- A pit-fall occurs if $\mathcal{O} = a + b - b + c$ where $b \rightarrow \text{large}$, *i.e.* contributions are *dependent*: **combine dependent terms before evaluating fine-tuning!**

Next: simple electroweak fine-tuning in SUSY:
 minimize Higgs potential in MSSM to relate
 magnitude of weak scale $m(Z)$ to SUSY Lagrangian;
 dial value of μ so that Z mass comes out right:
 everybody does it but it is hidden inside spectra codes
 (Isajet, SuSpect, SoftSUSY, Spheno, SSARD)

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \simeq -m_{H_u}^2 - \Sigma_u^u - \mu^2$$



SUSY breaking
 Higgs mass
 >40 loop corrections
 finetuning required
 natural solution

SUSY preserving
 mu parameter

#1: Simplest SUSY measure: Δ_{EW}

No large uncorrelated cancellations in $m(Z)$ or $m(h)$;
what you see is what you get!

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \sim -m_{H_u}^2 - \Sigma_u^u - \mu^2$$

$$\Delta_{EW} \equiv \max_i |C_i| / (m_Z^2/2) \quad \text{with} \quad C_{H_u} = -m_{H_u}^2 \tan^2 \beta / (\tan^2 \beta - 1) \quad \text{etc.}$$

simple, direct, unambiguous interpretation:

- $|\mu| \sim m_Z \sim 100 - 200 \text{ GeV}$
- $m_{H_u}^2$ should be driven to small negative values such that $-m_{H_u}^2 \sim 100 - 200 \text{ GeV}$ at the weak scale and
- that the radiative corrections are not too large: $\Sigma_u^u \lesssim 100 - 200 \text{ GeV}$

CETUP*-12/002, FTPI-MINN-12/22, UMN-TH-3109/12, UH-511-1195-12

Radiative natural SUSY with a 125 GeV Higgs boson

Howard Baer,¹ Vernon Barger, Peisi Huang,² Azar Mustafayev,³ and Xerxes Tata⁴

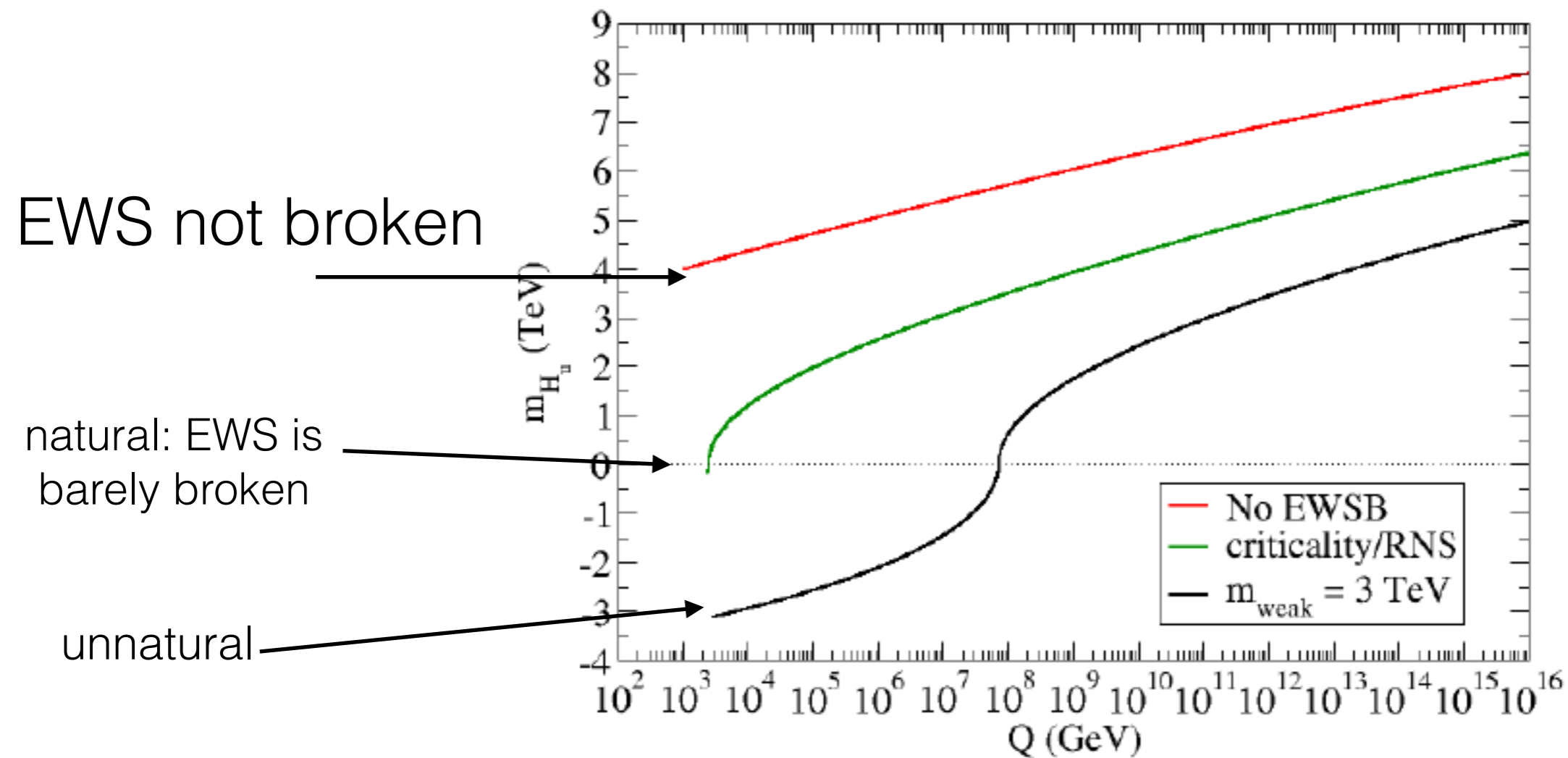
¹Dept. of Physics and Astronomy, University of Oklahoma, Norman, OK, 73019, USA

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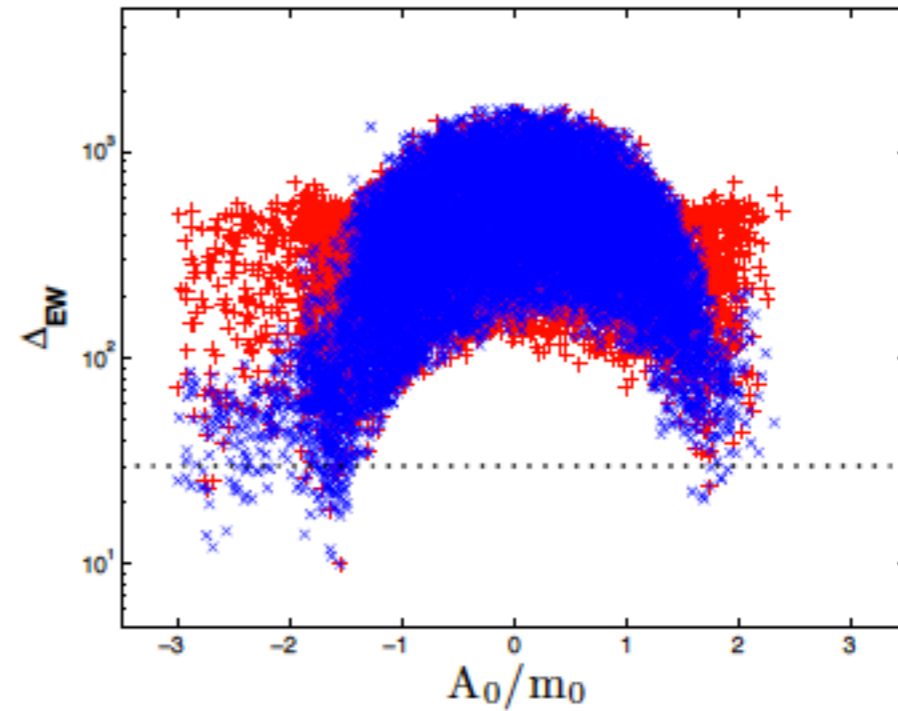
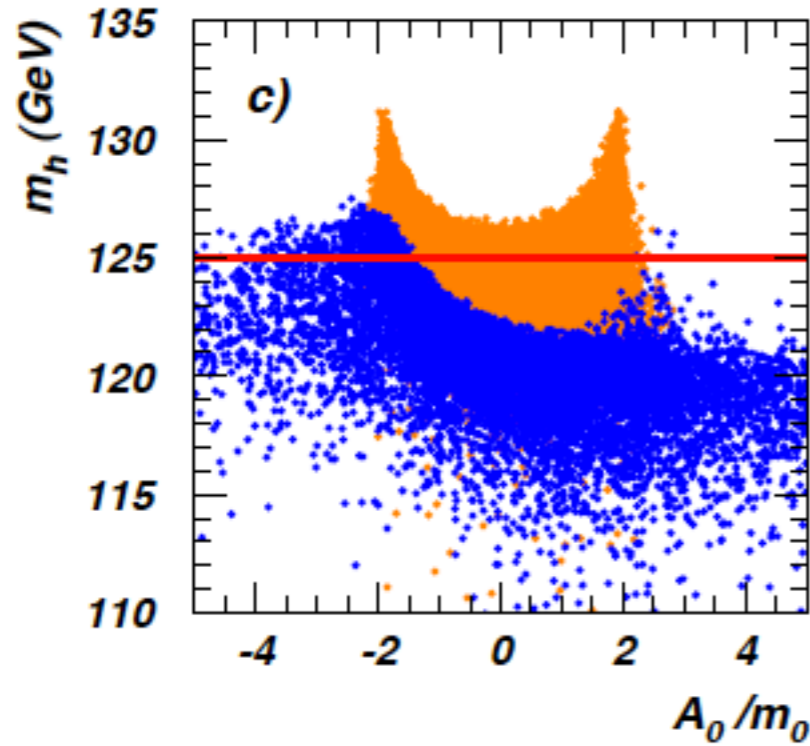
PRL109 (2012) 161802

radiative corrections drive $m_{H_u}^2$ from unnatural GUT scale values to naturalness at weak scale:
radiatively-driven naturalness



Evolution of the soft SUSY breaking mass squared term $sign(m_{H_u}^2)\sqrt{|m_{H_u}^2|}$ vs. Q

Large value of A_t reduces $\Sigma_u^u(\tilde{t}_{1,2})$ contributions to Δ_{EW} while uplifting m_h to ~ 125 GeV

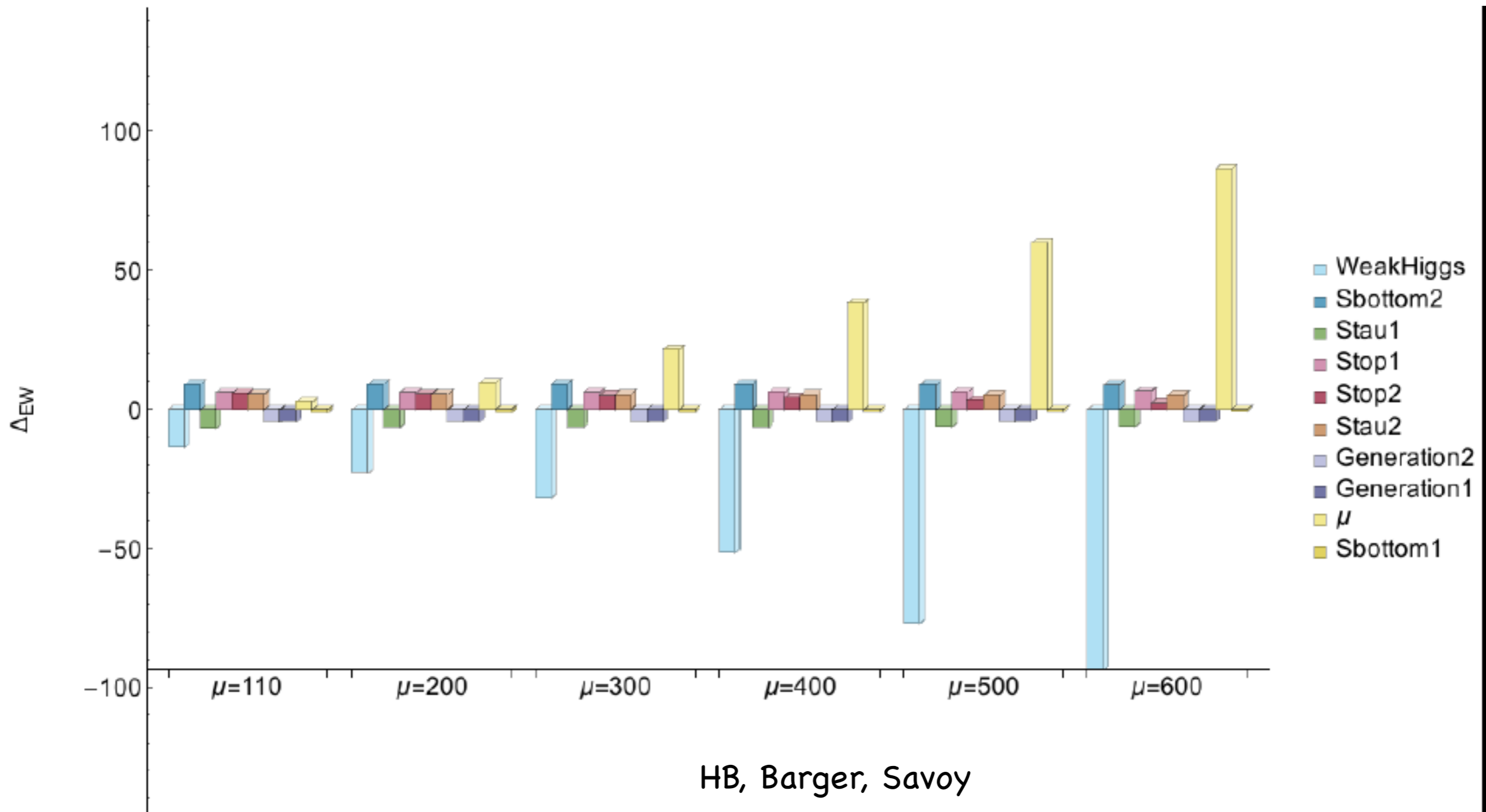


$$\Sigma_u^u(\tilde{t}_{1,2}) = \frac{3}{16\pi^2} F(m_{\tilde{t}_{1,2}}^2) \left[f_t^2 - g_Z^2 \mp \frac{f_t^2 A_t^2 - 8g_Z^2 (\frac{1}{4} - \frac{2}{3}x_W) \Delta_t}{m_{\tilde{t}_2}^2 - m_{\tilde{t}_1}^2} \right]$$

$$\Delta_t = (m_{\tilde{t}_L}^2 - m_{\tilde{t}_R}^2)/2 + M_Z^2 \cos 2\beta (\frac{1}{4} - \frac{2}{3}x_W)$$

$$F(m^2) = m^2 \left(\log \frac{m^2}{Q^2} - 1 \right) \quad Q^2 = m_{\tilde{t}_1} m_{\tilde{t}_2}$$

How much is too much fine-tuning?



Visually, large fine-tuning has already developed by $\mu \sim 350$ or $\Delta_{EW} \sim 30$

bounds from naturalness (3%)	BG/DG	Delta_EW
mu	350 GeV	350 GeV
gluino	400-600 GeV	6 TeV
t1	450 GeV	3 TeV
sq/sl	550-700 GeV	10-30 TeV

h(125) and LHC limits are perfectly compatible with 3-10% naturalness: **no crisis!**

other measures of finetuning

- **log derivative measure**: used arbitrary soft terms as free parameters in EFT which are necessarily correlated in more UV complete theory $\Delta = \max_i |(p_i/m_Z^2) \partial m_Z^2 / \partial p_i|$

- **high scale measure**: oversimplified higgs soft mass RGE thus deleting dependent terms that cancel against large logs $m_h^2 \sim \mu^2 + m_{H_u}^2(\Lambda) + \delta m_{H_u}^2$ with $\Delta \sim \delta m_{H_u}^2 / m_h^2$

can overestimate finetuning by up to 3 orders of magnitude!

(For details, see paper below or backup slides)

PHYSICAL REVIEW D 88, 095013 (2013)

How conventional measures overestimate electroweak fine-tuning in supersymmetric theory

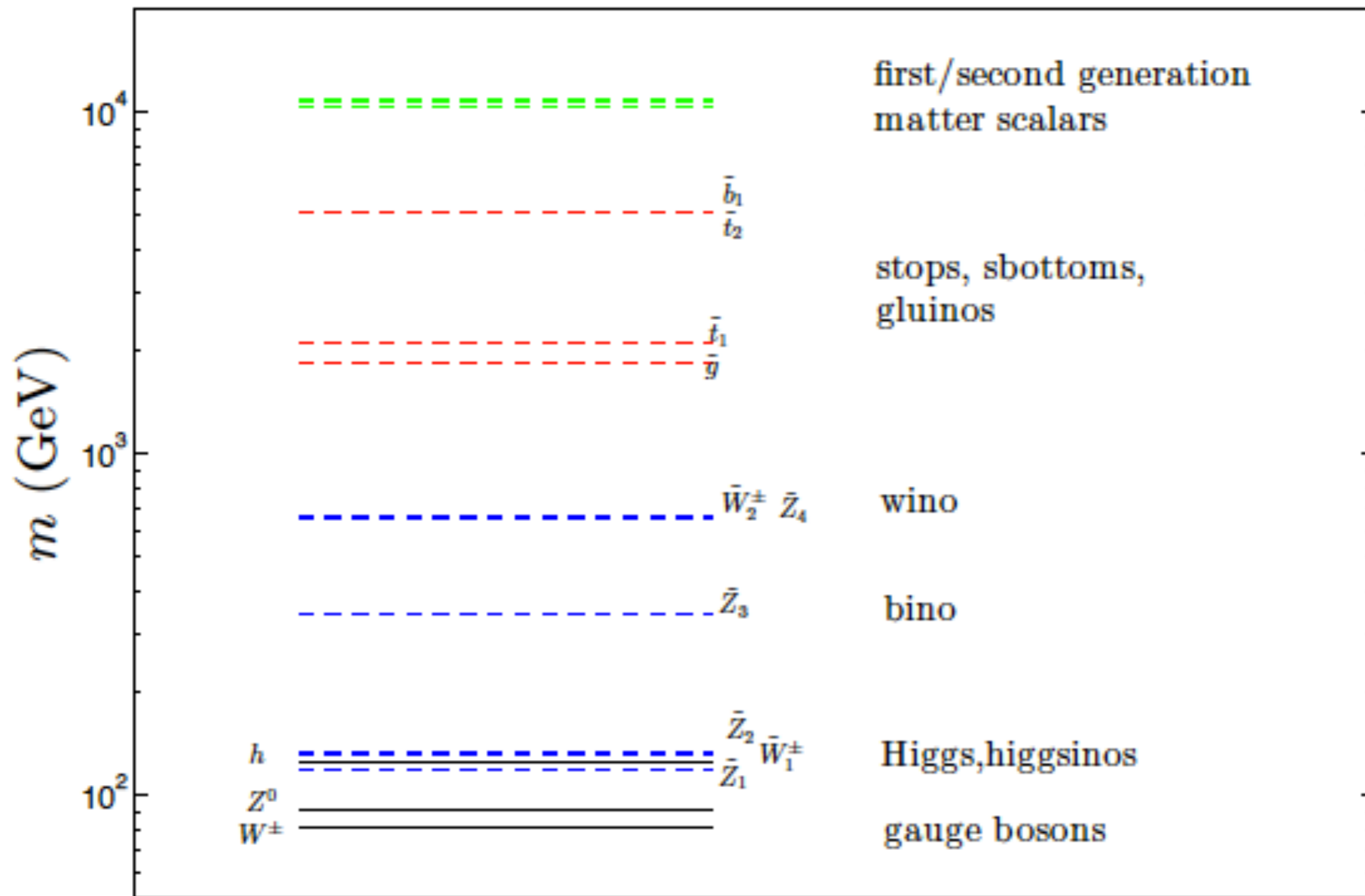
Howard Baer,^{1,*} Vernon Barger,^{2,†} and Dan Mickelson^{1,‡}

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(Received 17 September 2013; published 18 November 2013)

Typical spectrum for low Δ_{EW} models



There is a Little Hierarchy, but it is **no problem**

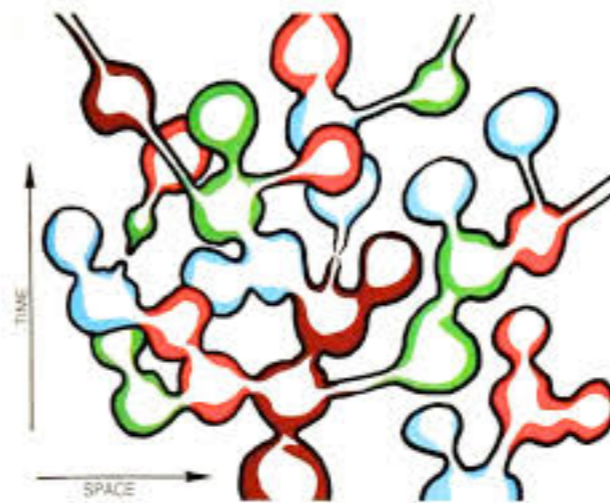
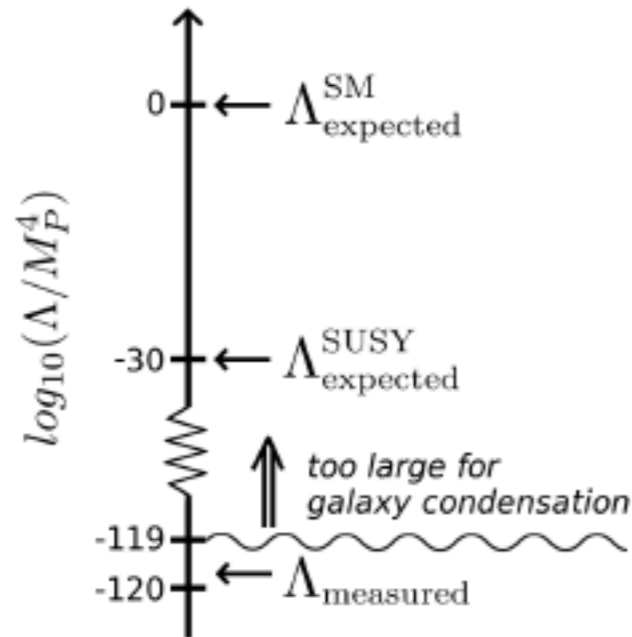
$$\mu \ll m_{3/2}$$

higgsinos likely the lightest superparticles!

Takeway lesson:
policy decisions for future accelerators
should not be based on
faulty naturalness estimates!

String theory after 2001: the string landscape

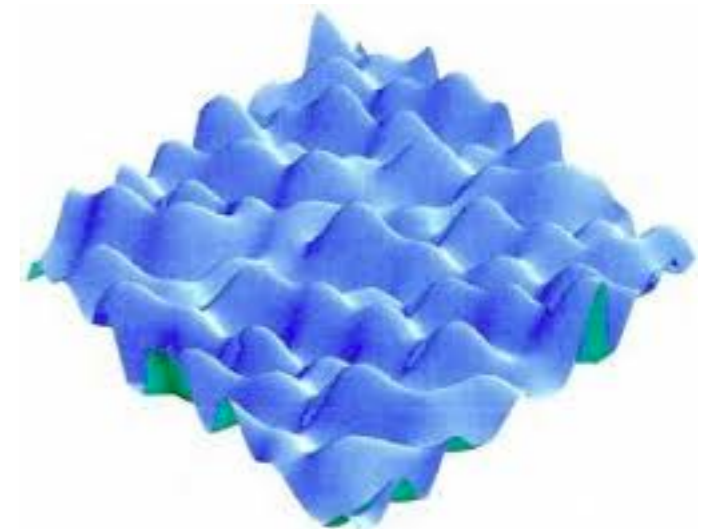
It is sometimes invoked that maybe we should abandon naturalness: after all, isn't the cosmological constant (CC) fine-tuned?



eternally inflating
multiverse

In the landscape with 10^{500} vacua with different CCs, then the tiny value of the CC may not be surprising since larger values would lead to runaway **pocket universes** where galaxies wouldn't condense—anthropics: no observers in such universes (Weinberg)

The CC is as natural as possible subject to the condition that it leads to galaxy condensation



Bousso & Polchinski;
Susskind; Douglas

For some recent review material, see M. Douglas,
The String Theory Landscape, 2018, Universe 5 (2019) 7, 176

Apply similar reasoning to origin of weak scale
(which arises from SUSY breaking in SUSY models):

Statistical analysis of SUSY breaking scale in IIB theory:

M. Douglas, hep-th/0405279

start with 10^{500} string vacua states

- string theory landscape contains vast ensemble of $N=1$, $d=4$ SUGRA EFTs at high scales
- the EFTs contain the SM as weak scale EFT
- the EFTs contain visible sector +potentially large hidden sector
- visible sector contains MSSM plus extra gauge singlets (e.g. a PQ sector, RN neutrinos,...)
- SUGRA is broken spontaneously in hidden sector via superHiggs mechanism via either F- or D- terms or in general a combination

In fertile patch of vacua with MSSM as weak scale effective theory
but with no preferred SUSY breaking scale...

$$dP/d\mathcal{O} \sim f_{prior} \cdot f_{selection}$$

What is $f(\text{prior})$ for SUSY breaking scale?

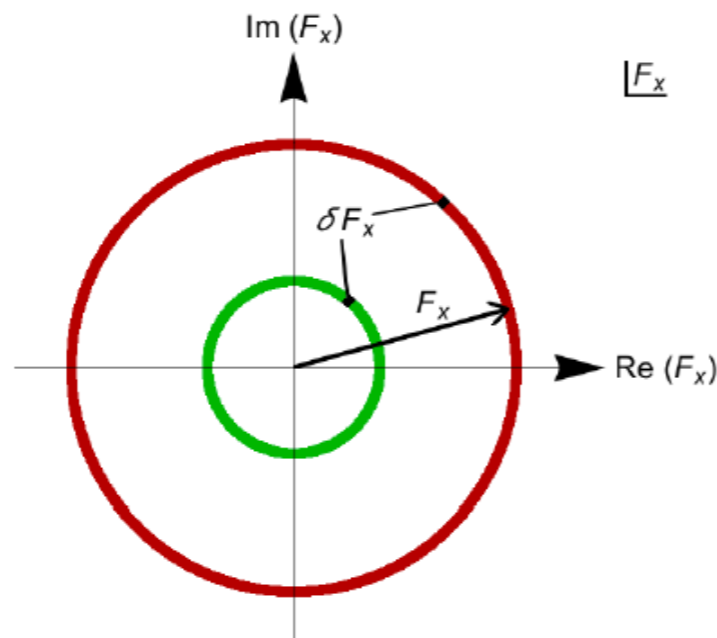
In string theory, usually multiple (~ 10) hidden sectors
containing a variety of F- and D- breaking fields

For comparable $\langle F_i \rangle$ and $\langle D_j \rangle$ values, then expect

$$f_{prior} \sim m_{soft}^{2n_F + n_D - 1}$$

Douglas ansatz
arXiv:0405279

Under single F-term
SUSY breaking,
expect **linearly increasing
statistical selection
of soft terms**



For uniform values of SUSY breaking fields,
expect landscape to prefer
high scale of SUSY breaking!

Figure 1: Annuli of the complex F_X plane giving rise to linearly increasing selection of soft SUSY breaking terms.

What about **f(selection)**?

Originally, people adopted $f_{EWFT} \sim m_{weak}^2/m_{soft}^2$

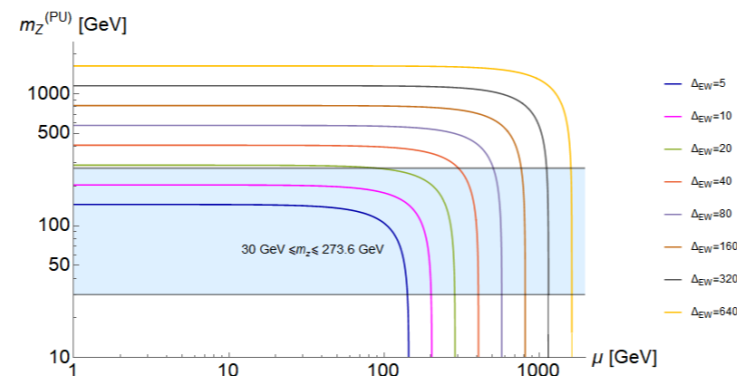
to penalize soft terms straying too far from weak scale

This doesn't work for variety of cases

- Too big soft terms can lead to CCB minima: must veto such vacua
- Bigger $m(H_u)^2$ leads to more natural value at weak scale
- Bigger $A(t)$ trilinear suppresses t_1, t_2 contribution to weak scale

$$\frac{(m_Z^{PU})^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2$$

Adopt μ value so no longer available for tuning; then $m_Z(PU) \approx 91.2$ GeV



Then for statistically selected soft terms, **m(weak) is output**, not input

Must veto too large $m(weak)$ values: nuclear physics screw up: no complex atoms
(Agrawal, Barr, Donoghue, Seckel, 1998)

Factor four deviation of weak scale from measured value $\Rightarrow \Delta_{EW} < 30$

Agrawal, Barr, Donoghue, Seckel result (1998):

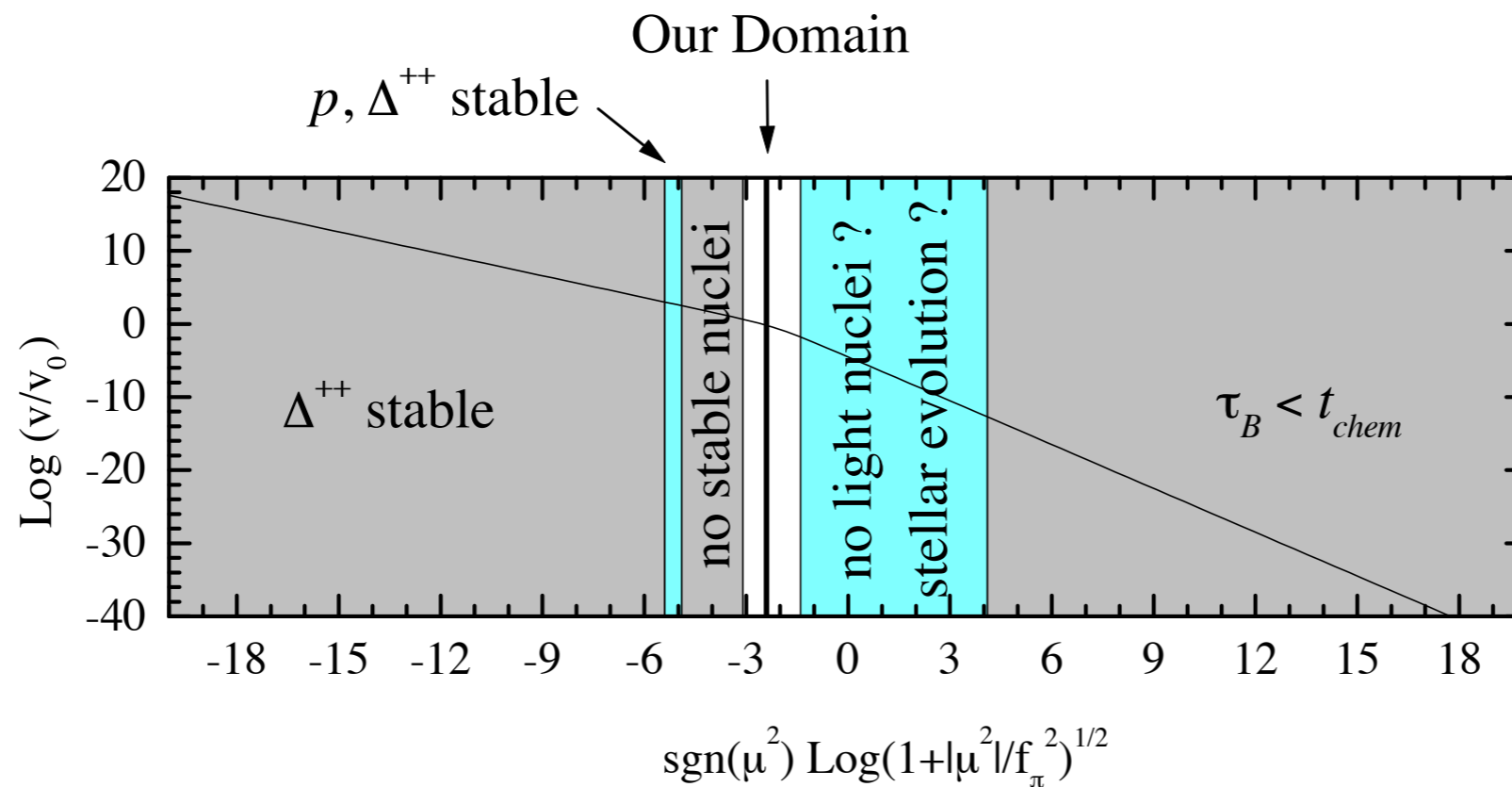
pocket-universe value of weak scale

cannot deviate by more than

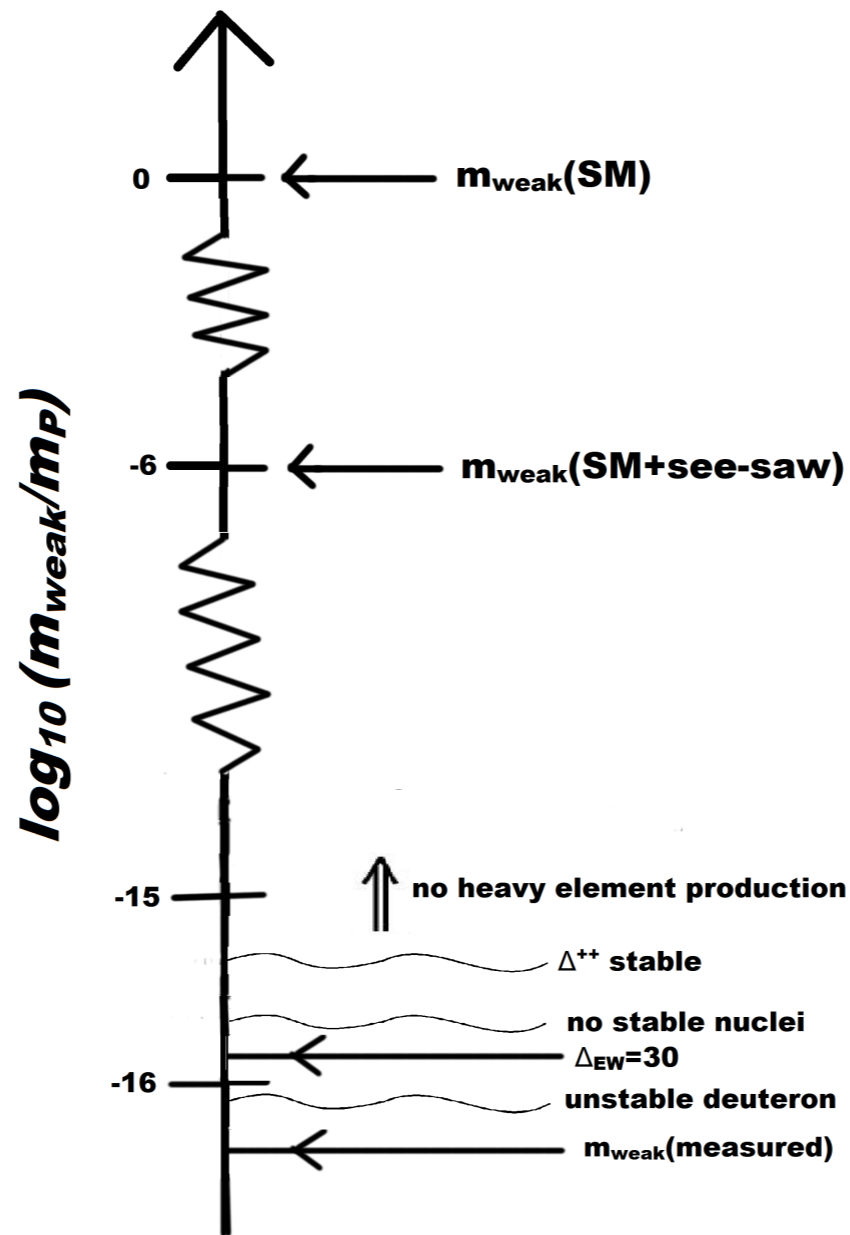
factor 2-5 from its measured value

lest disasters occur in nuclear physics: no nuclei, no atoms

(violates atomic principle)

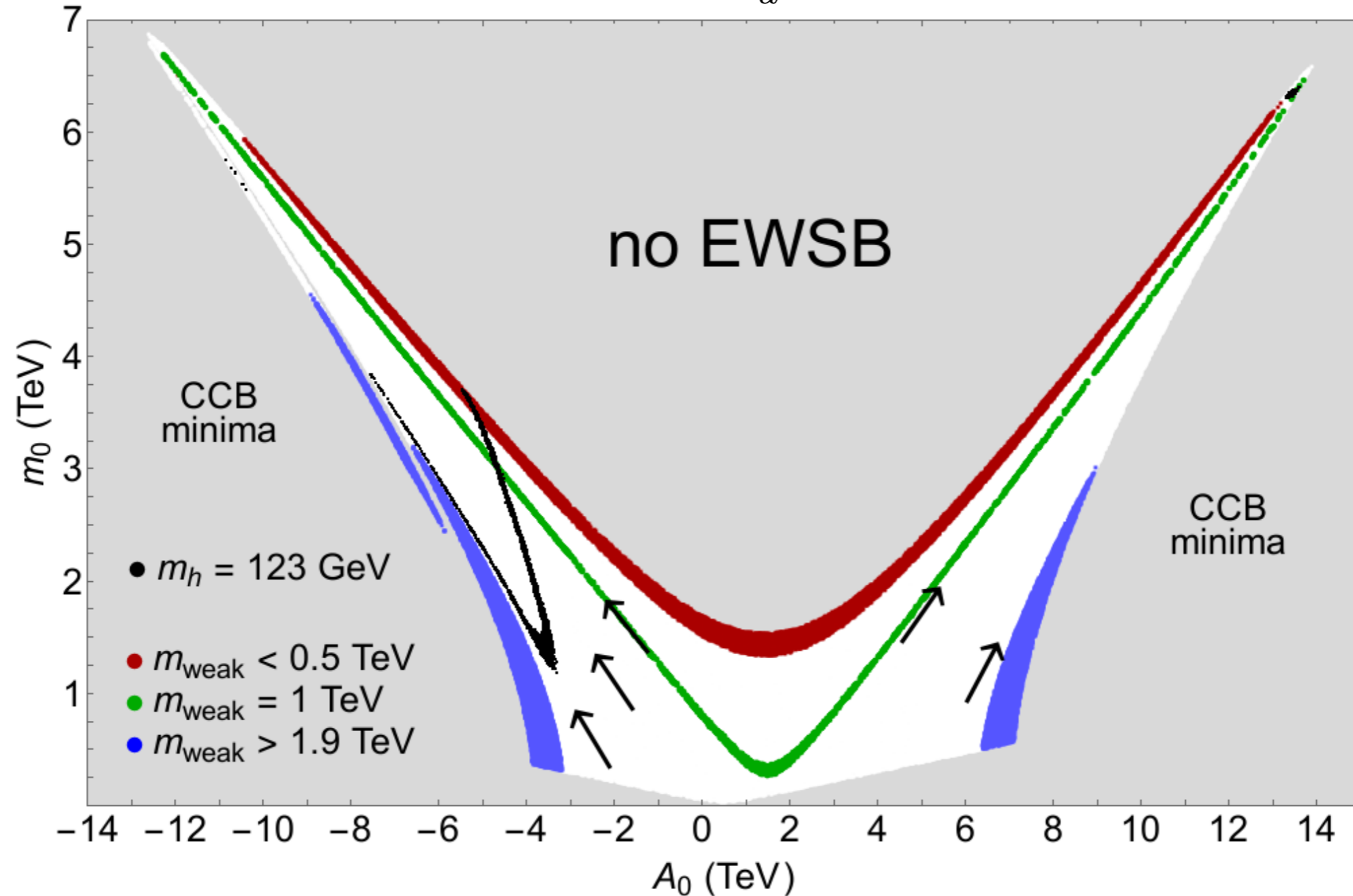


$m(\text{weak})$ must lie within ABDS window to have atoms/chemistry



Veto pocket universes with CCB minima or minima leading to weak scale a (conservative) factor four greater than our value $m(W,Z,h) \sim 100 \text{ GeV}$

$$m_{H_u} = 1.3m_0$$



statistical draw to large soft terms balanced by anthropic draw toward red ($m(\text{weak}) \sim 100$ GeV): then $m(\text{Higgs}) \sim 125$ GeV and natural SUSY spectrum!

Recent work: place on more quantitative footing:
scan soft SUSY breaking parameters in NUHM3 model
as $m(\text{soft})^n$ along with $f(\text{EWFT})$ penalty

We scan according to m_{soft}^n over:

- $m_0(1, 2) : 0.1 - 40 \text{ TeV},$

- $m_0(3) : 0.1 - 20 \text{ TeV},$

- $m_{1/2} : 0.5 - 10 \text{ TeV},$

- $A_0 : 0 - -60 \text{ TeV},$

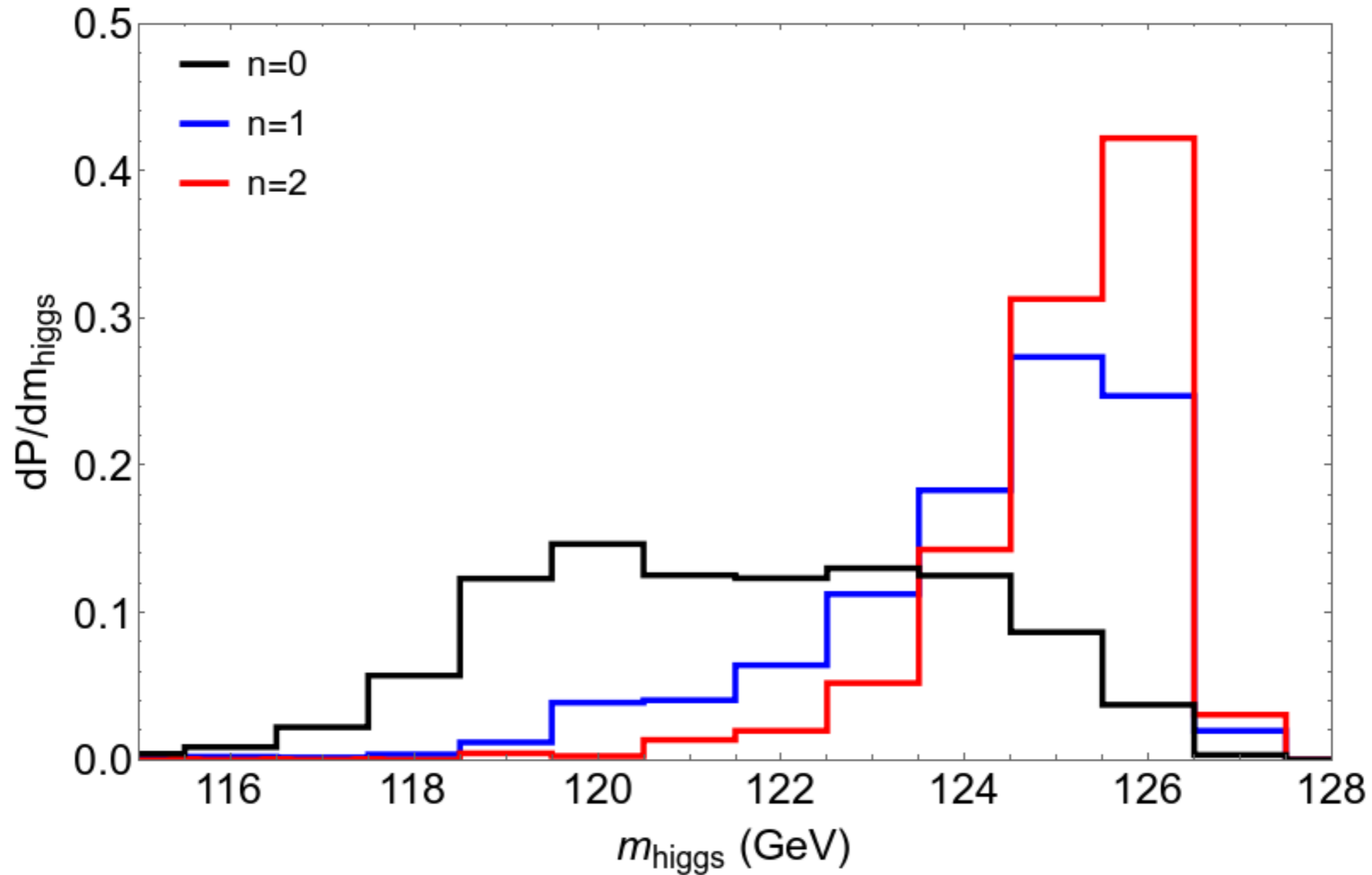
- $m_A : 0.3 - 10 \text{ TeV},$

$\tan \beta : 3 - 60 \quad (\text{flat})$

$\mu = 150 \text{ GeV (fixed)}$

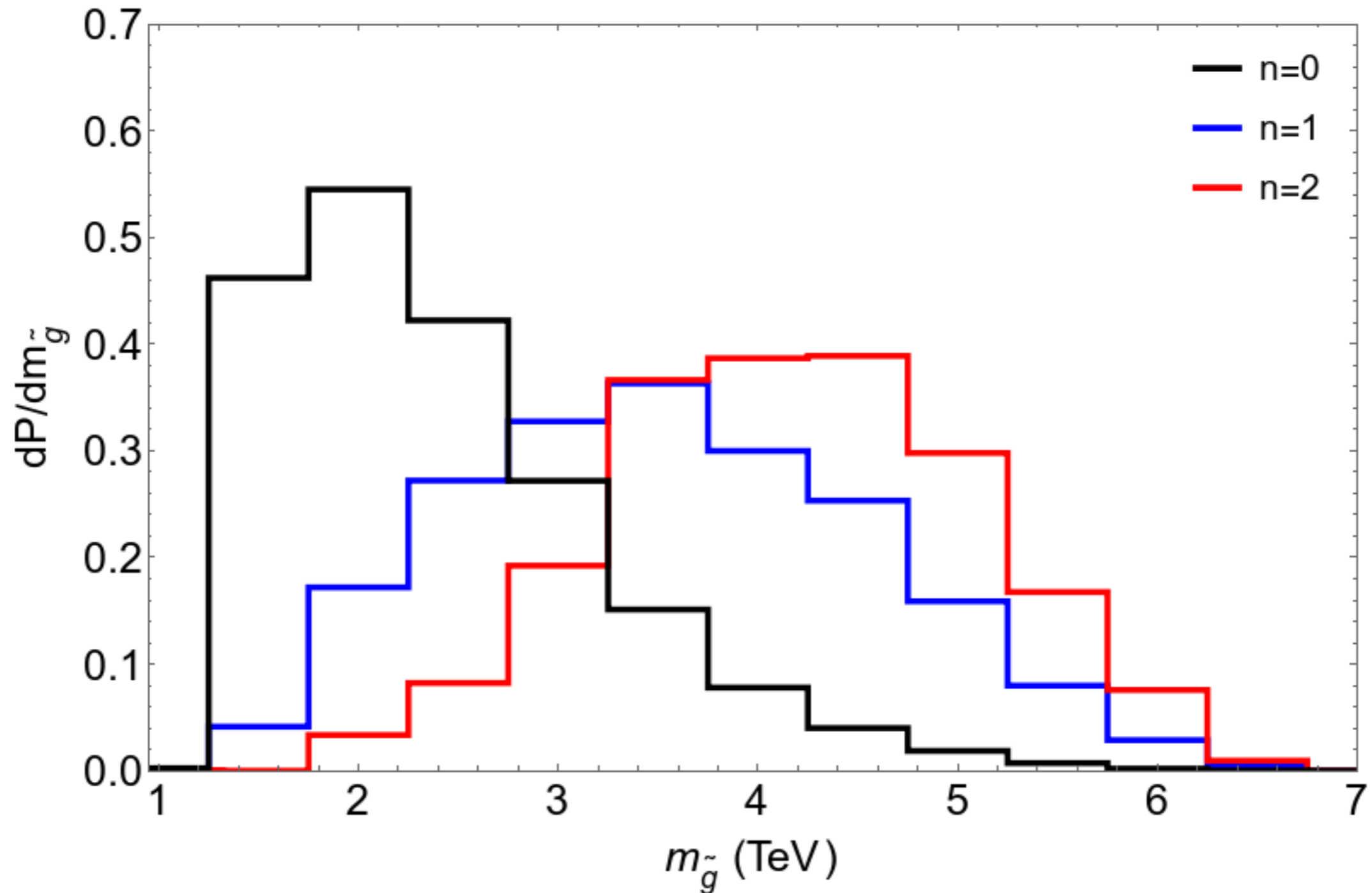
Making the picture more quantitative:

$$dN_{vac}[m_{hidden}^2, m_{weak}, \Lambda] = f_{SUSY}(m_{hidden}^2) \cdot f_{EWFT} \cdot f_{cc} dm_{hidden}^2$$



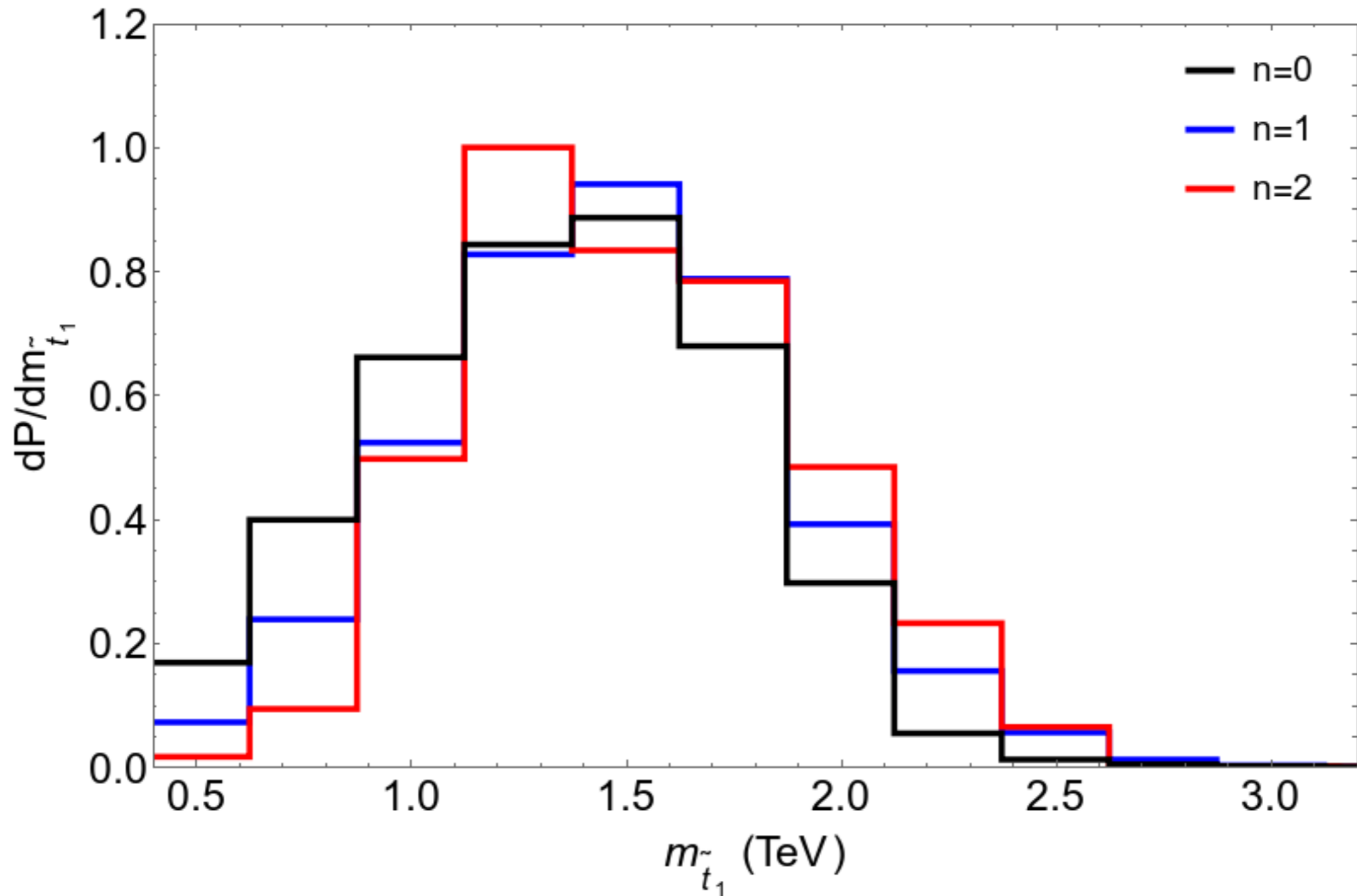
$m(h) \sim 125$ most favored for $n \geq 1$

What is corresponding distribution for gluino mass?



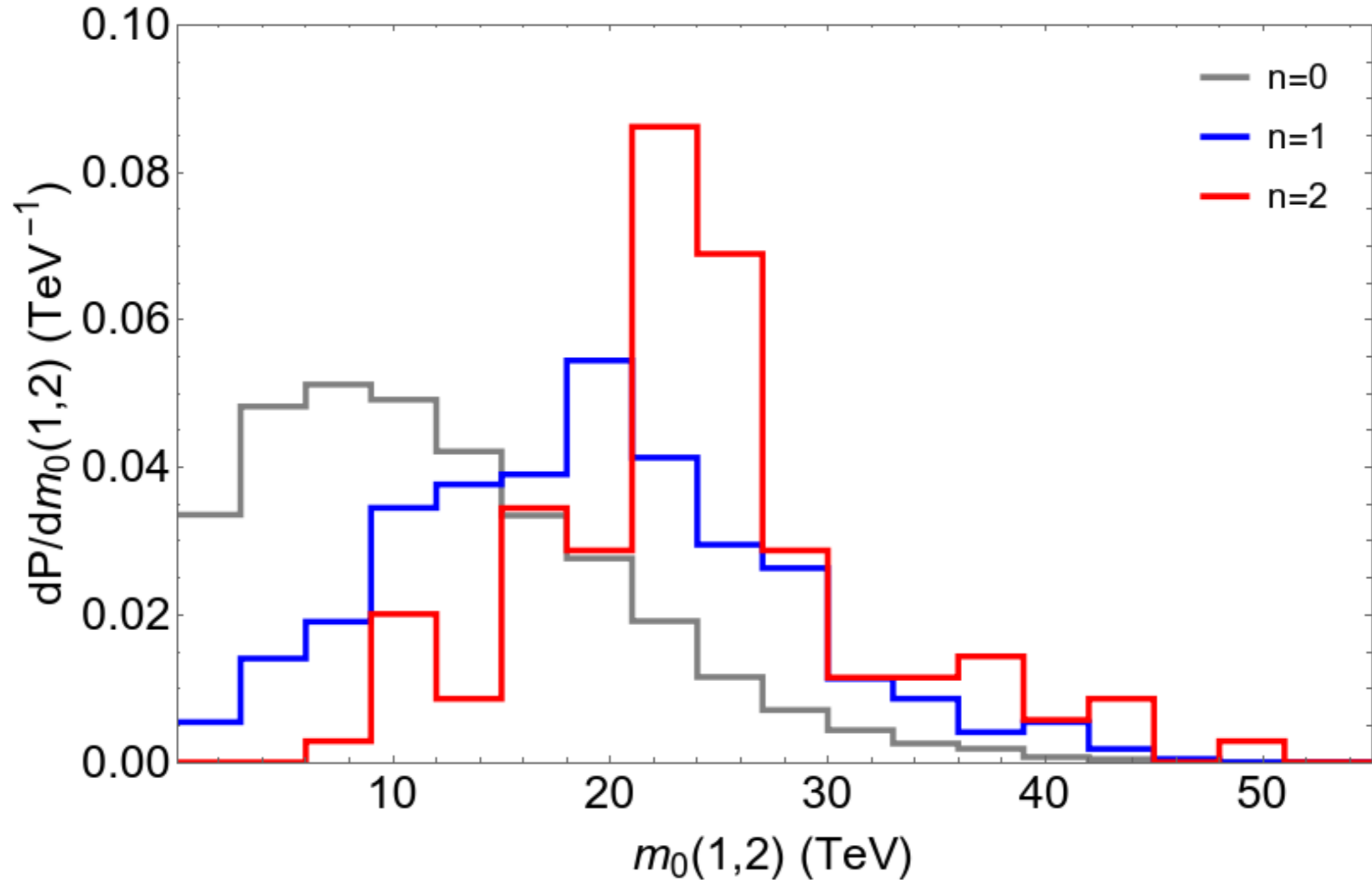
gluino typically beyond LHC 14 reach
(need higher energy hadron collider)

and top-squark mass $m(t_1)$?

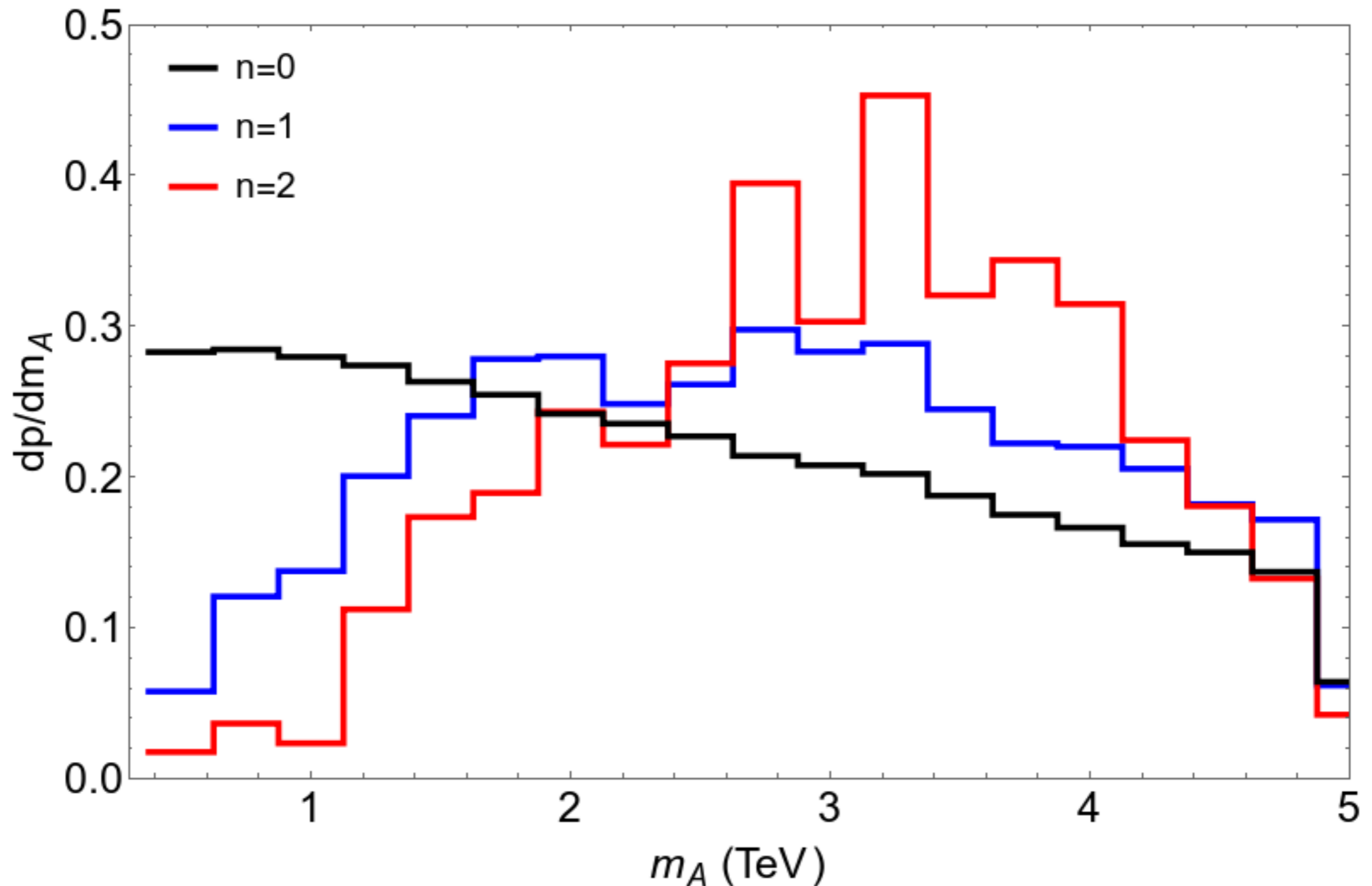


$m(t_1)$ typically beyond present LHC reach

first/second generation sfermions pulled to 10–40 TeV:
decoupling sol'n to SUSY flavor/CP problems



Landscape=> h boson has $m \sim 125$ GeV and very SM-like;
heavy Higgs bosons A, H, H^{\pm} : multi-TeV scale



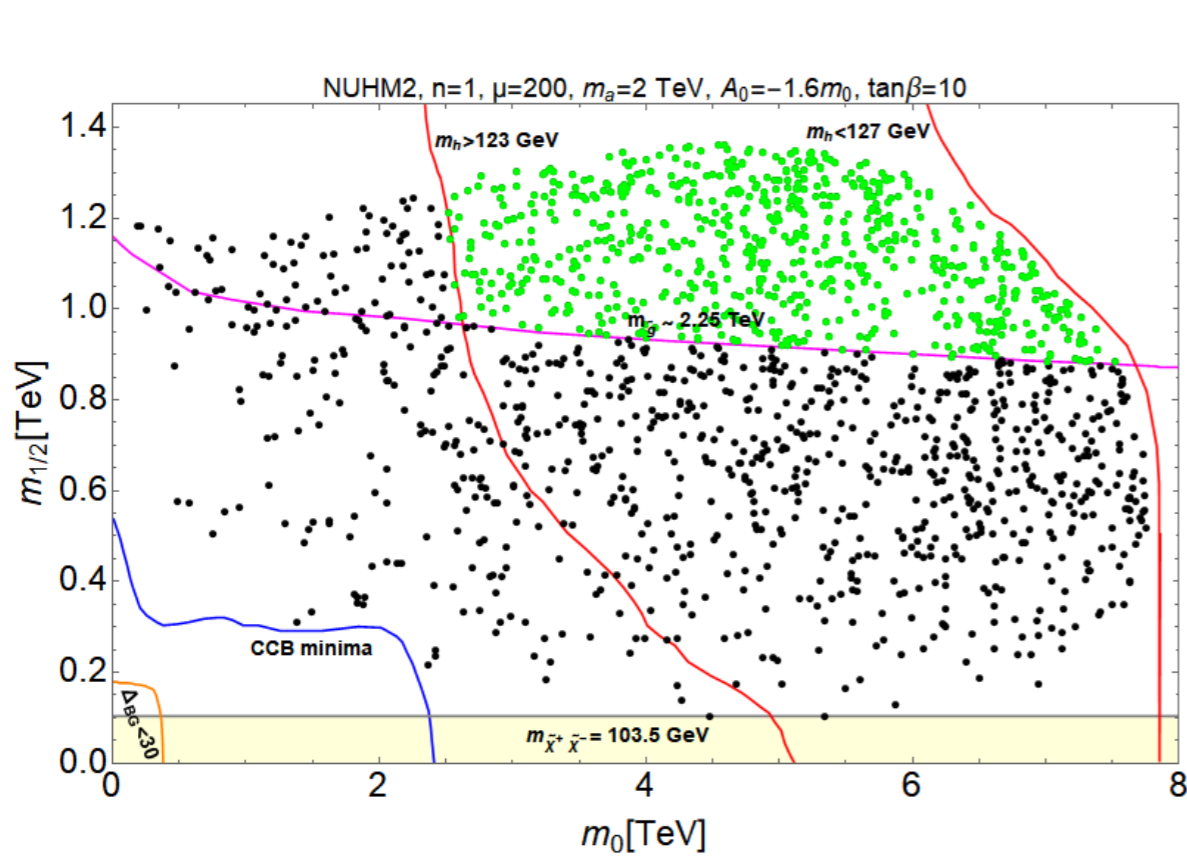
Stringy naturalness: higher density of points are more stringy natural!

conventional natural: favor low m_0 , m_h

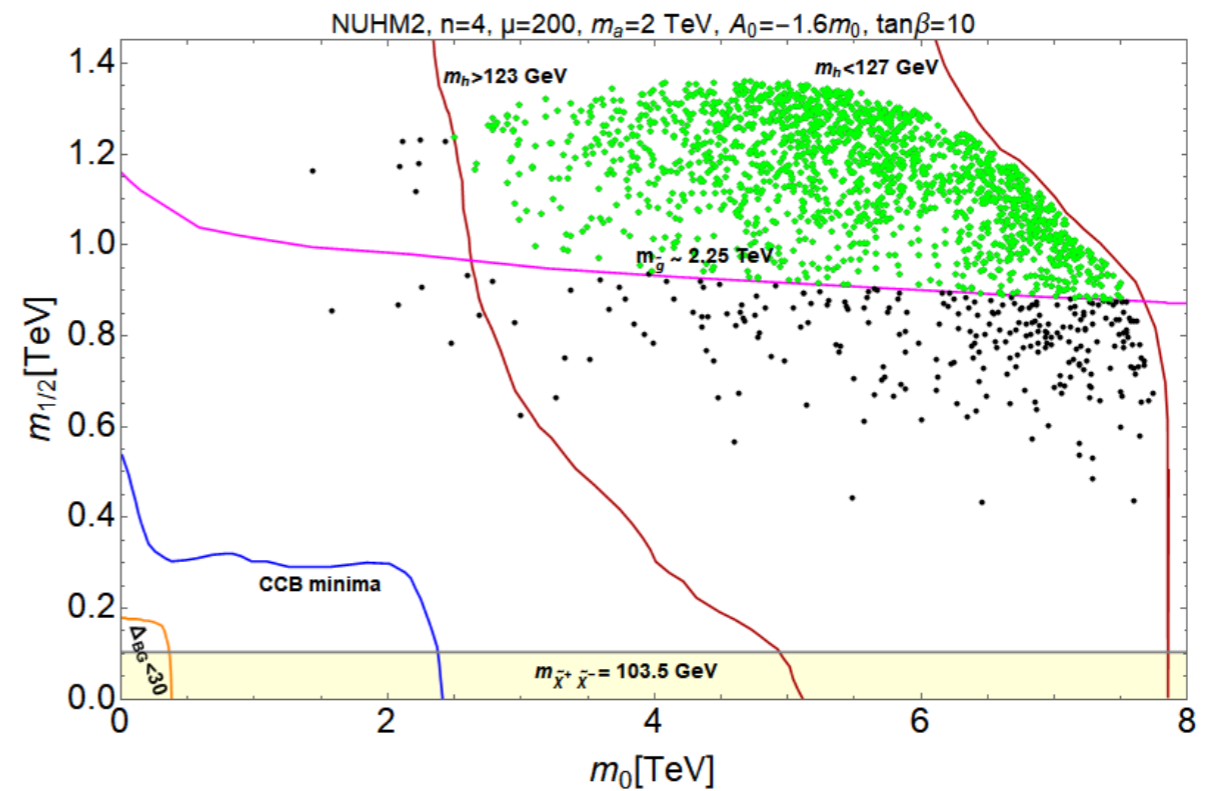
stringy naturalness: favor high m_0 , m_h so long as $m(\text{weak}) \sim 100 \text{ GeV}$

HB, Barger, Salam, arXiv:1906.07741

Living dangerously: Arkani-Hamed, Dimopoulos, Kachru, hep-ph/0501082



$$m(\text{soft})^1$$

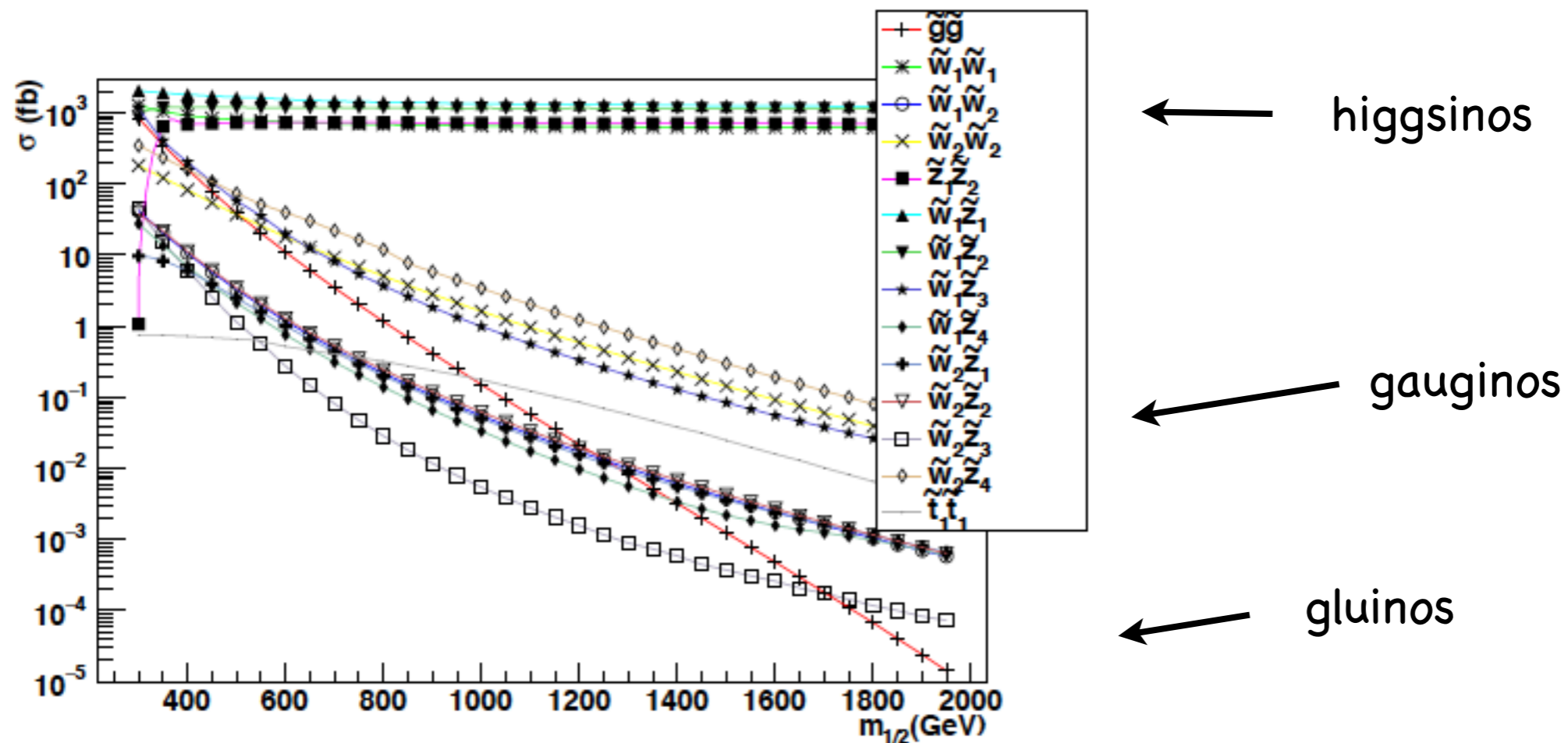


$$m(\text{soft})^4$$

Under stringy naturalness, a 3 TeV gluino is more natural than a 300 GeV gluino!

Prospects for discovering Higgs and higgsinos at LHC and ILC

Sparticle prod'n along RNS model-line at LHC14:



higgsino pair production dominant—but only soft visible energy release from higgsino decays

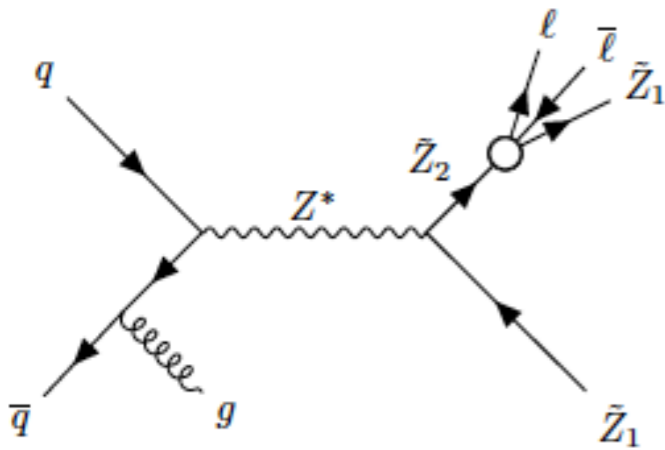
largest visible cross section: **wino pairs**

gluino pairs sharply dropping

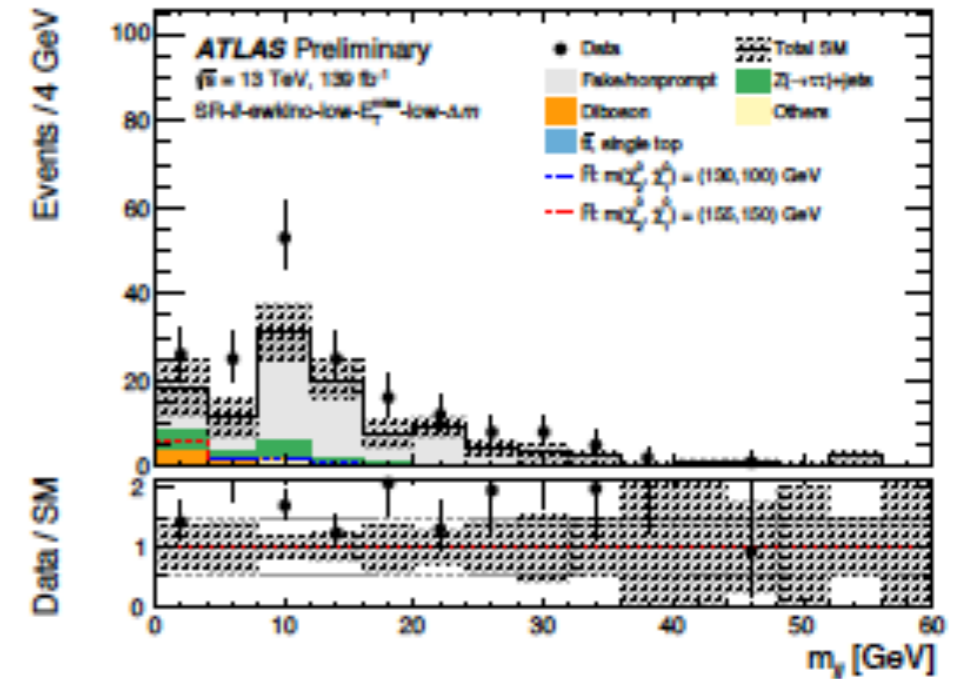
HL-LHC best bet: higgsino pair production

Natural SUSY: only higgsinos need lie close to weak scale

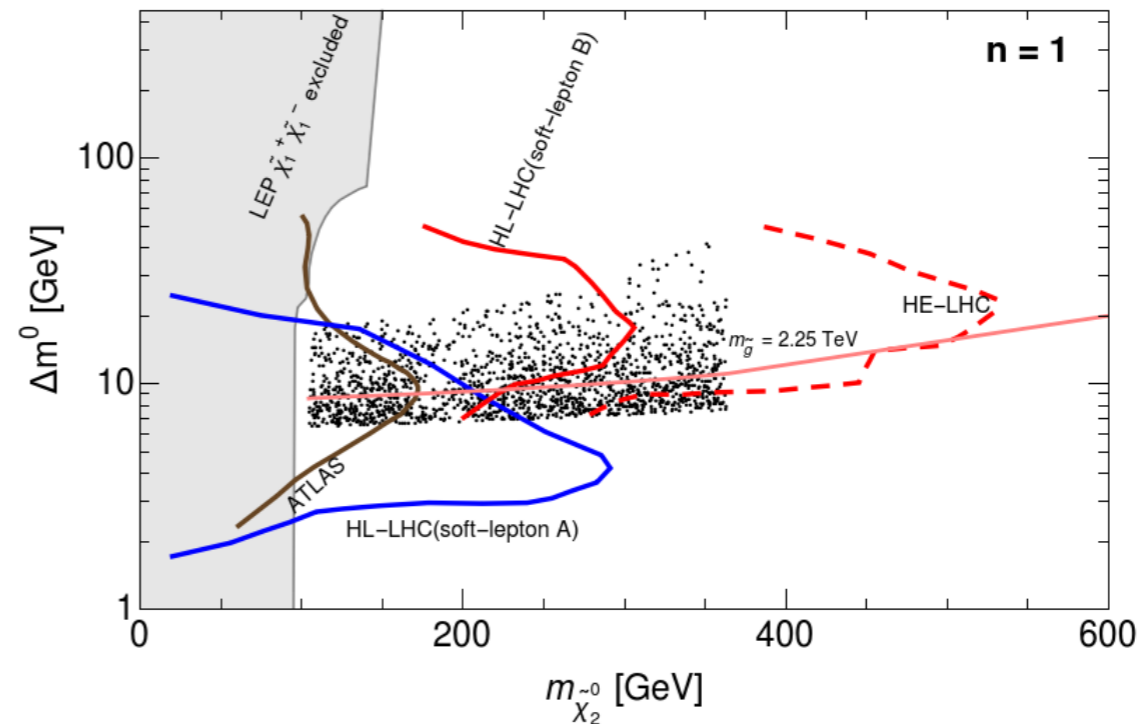
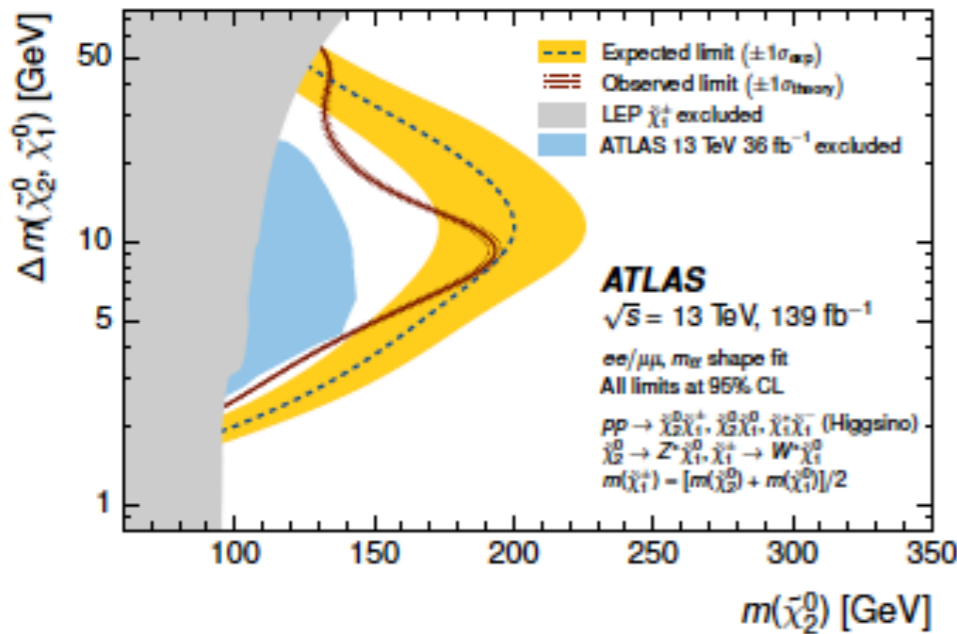
Soft dilepton+jet+MET signature from higgsino pair production



- HB, Barger, Huang, 1107.5581;
- Z. Han, Kribs, Martin, Menon, 1401.1235;
- HB, Mustafayev, Tata; 1409.7058;
- C. Han, Kim, Munir, Park, 1502.03734;
- HB, Barger, Savoy, Tata, 1604.07438;
- HB, Barger, Salam, Sengupta, Tata, 2007.09252;
- HB, Barger, Sengupta, Tata, 2109.14030

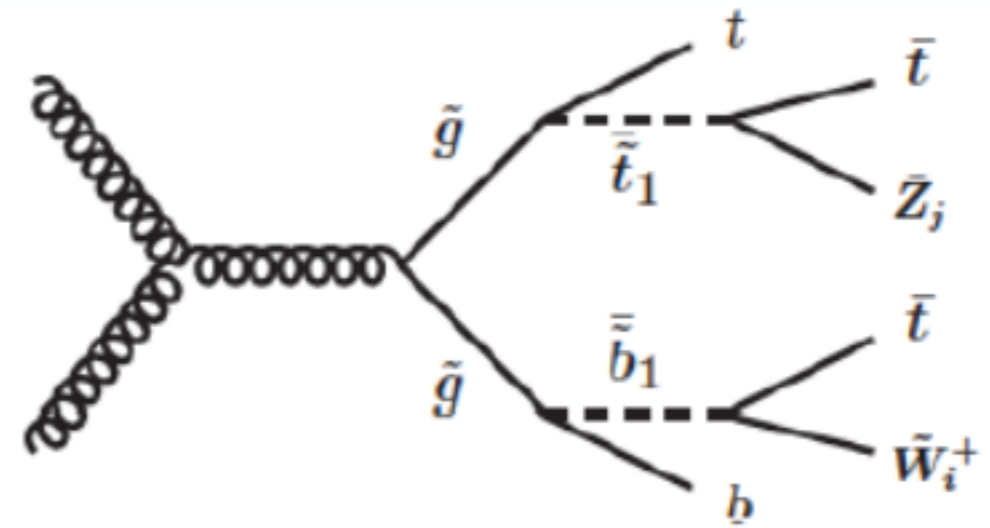


GMM', $m_{3/2} = 20$ TeV, $m_A = 2$ TeV, $\tan \beta = 10$, $c_m = c_{m3}$

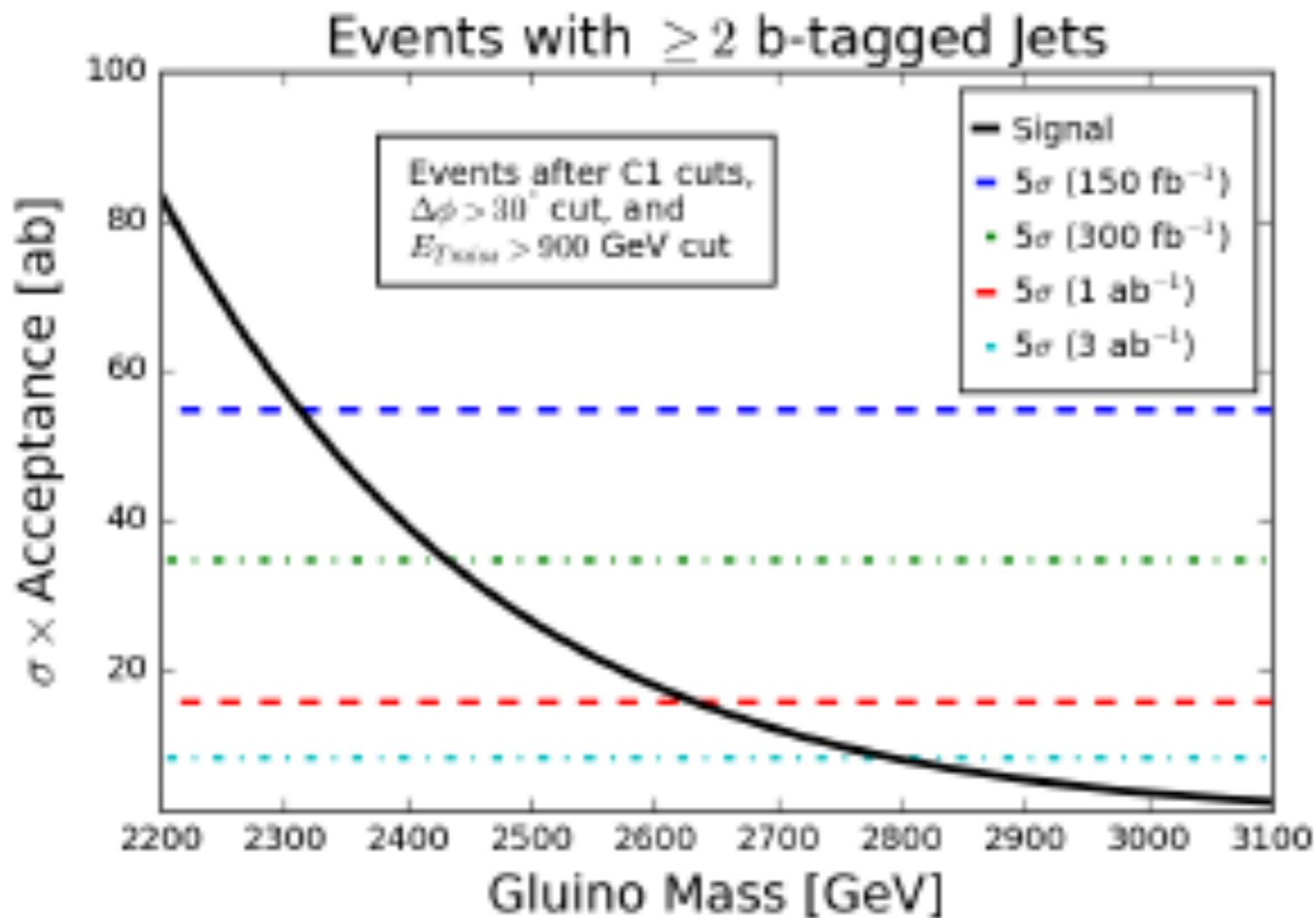


It appears that HL-LHC can see much of natural SUSY p-space; signal in this channel should **emerge slowly** as more integrated luminosity accrues

gluino pair cascade decay signatures



LHC14

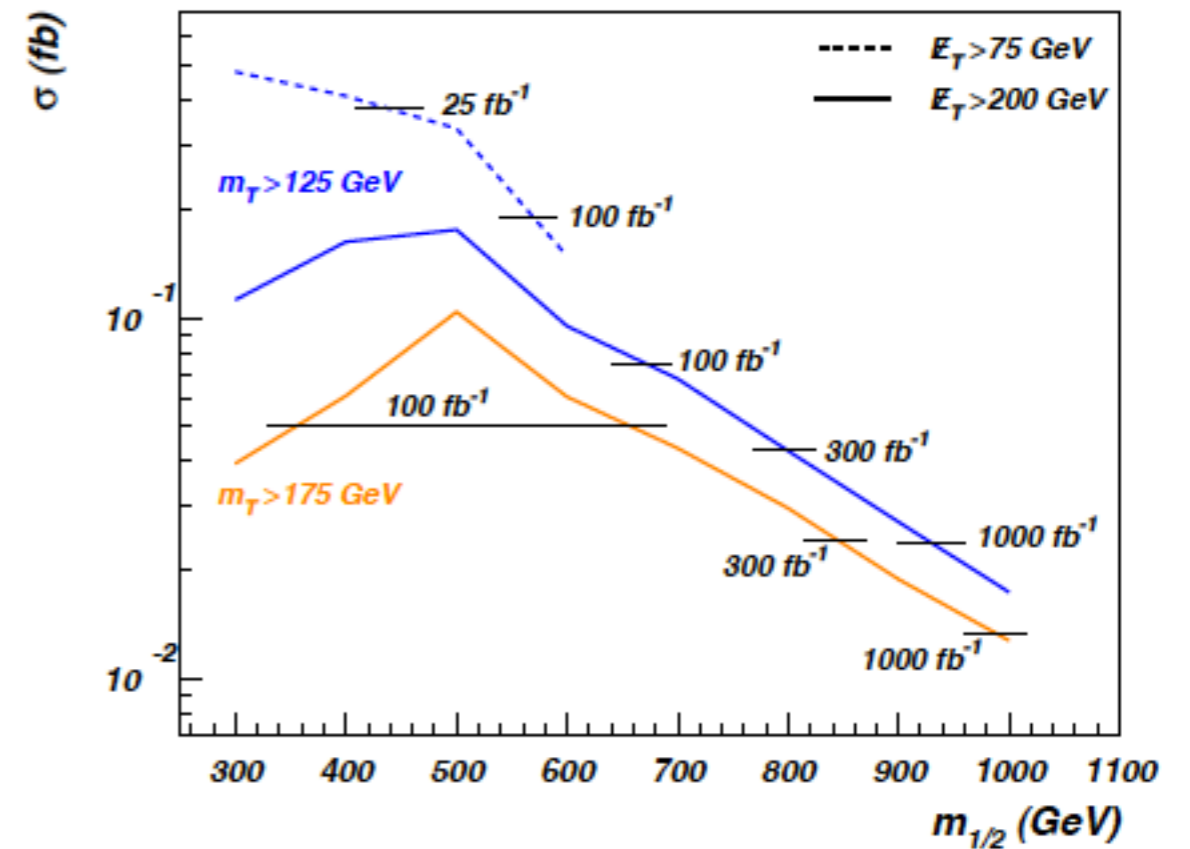
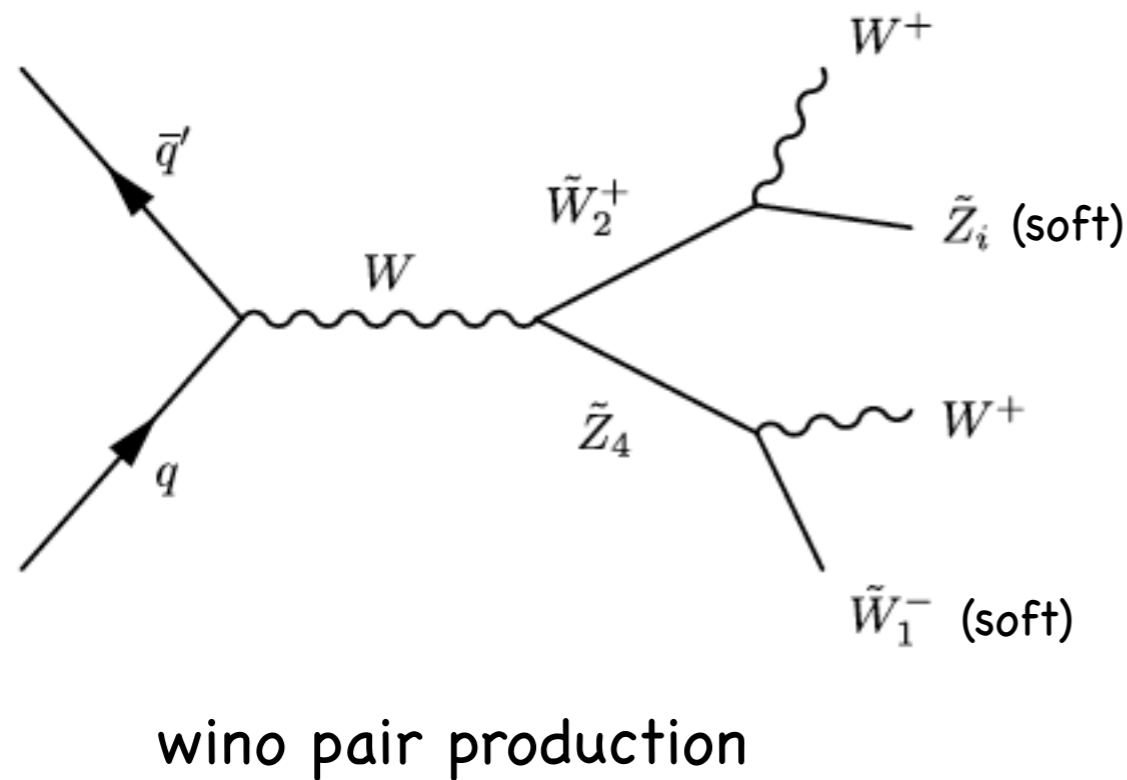


HB, Barger, Gainer, Huang, Savoy, Sengupta, Tata

HL-LHC to probe $m(\text{gl}) \sim 2.8 \text{ TeV}$

FCC-hh(100) to probe $m(\text{gl}) \sim 10 \text{ TeV}$

Distinctive new same-sign diboson (SSdB)
signature from SUSY models with light higgsinos!

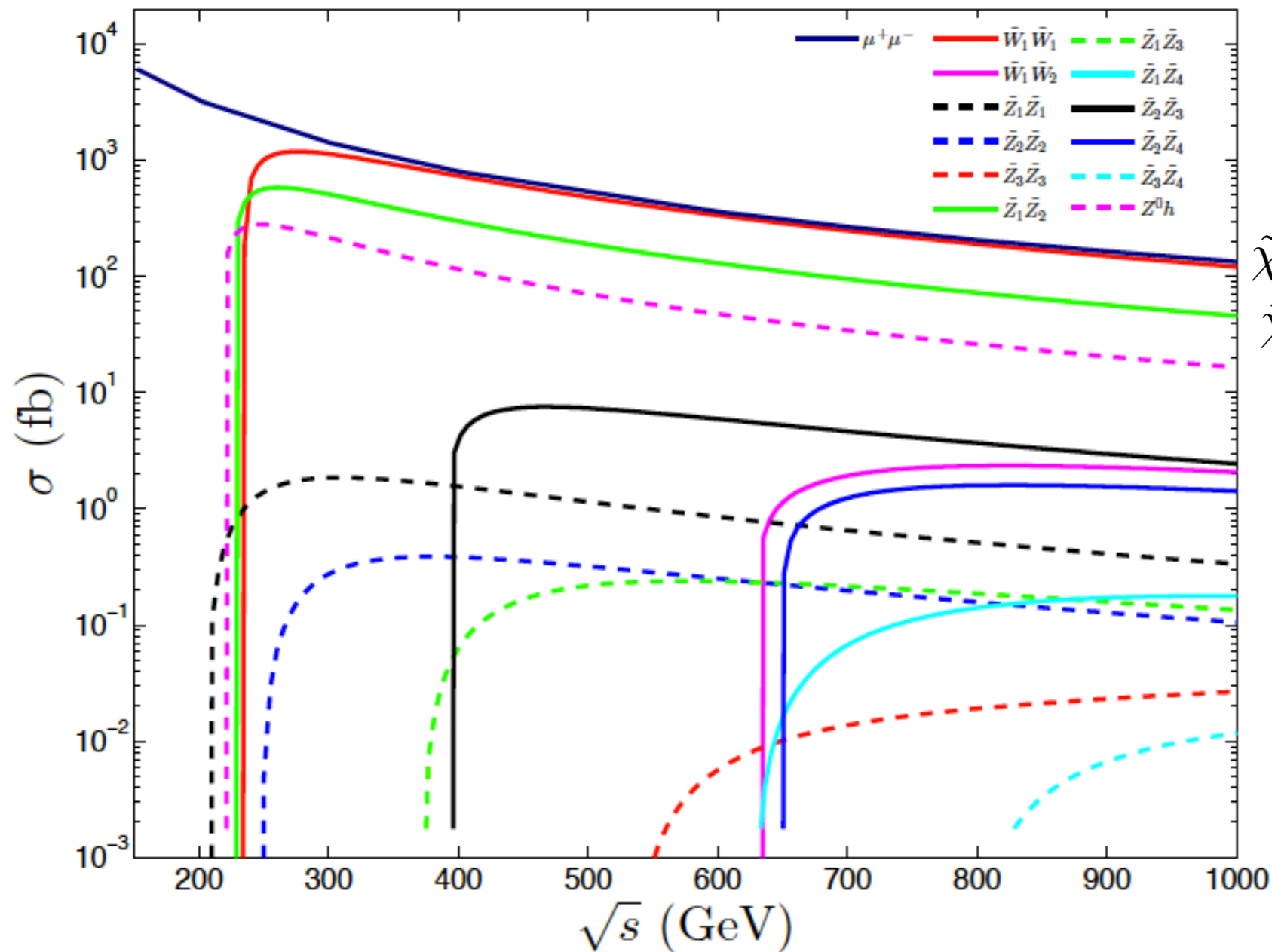


This channel offers added reach of LHC14 for natSUSY; it is also indicative of wino-pair prod'n followed by decay to higgsinos

Smoking gun signature: light higgsinos at ILC:

ILC is Higgs/higgsino factory!

ILC1: $m_0 = 7025$ GeV, $m_{1/2} = 568.3$ GeV, $A_0 = -11426.6$ GeV, $\tan\beta = 10$, $\mu = 115$ GeV, $m_A = 1000$ GeV



$$\sigma(\text{higgsino}) \gg \sigma(Zh)$$

$\tilde{\chi}_1^+ \tilde{\chi}_1^-$
 $\tilde{\chi}_1^0 \tilde{\chi}_2^0$

3-15 GeV higgsino mass
gaps no problem
in clean ILC environment

HB, Barger, Mickelson, Mustafayev, Tata
arXiv:1404.7510

$$e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow (\ell\nu_\ell \tilde{\chi}_1^0) + (q\bar{q}' \tilde{\chi}_1^0)$$

measure $m(jj) < m_{\tilde{\chi}_1^\pm} - m_{\tilde{\chi}_1^0}$ and $E(jj)$

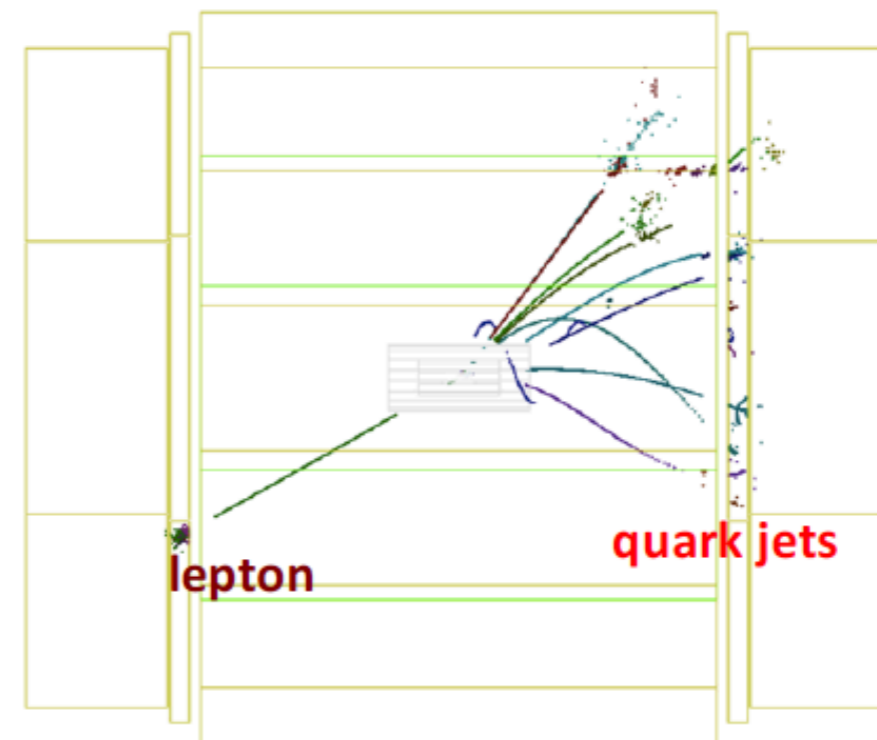
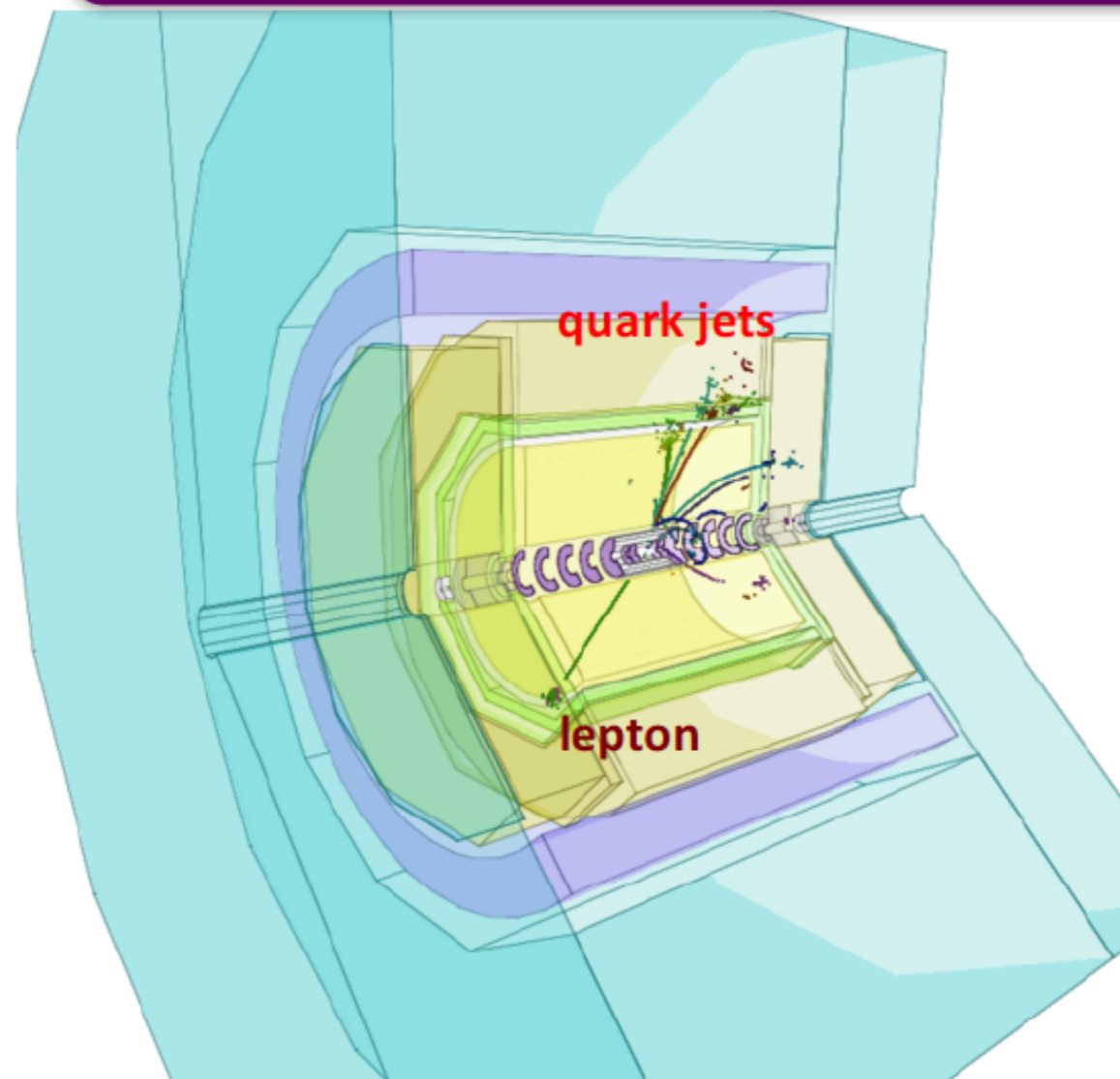
soft visible particles since small higgsino mass gaps

How do these signals look in the detector? (2)

$\sqrt{s} = 500 \text{ GeV}$

Chargino pair production with semileptonic decay

$$e^+e^- \rightarrow \tilde{\chi}_1^+ \tilde{\chi}_1^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 qq' \ell \nu$$



$$e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 + (\ell^+ \ell^- \tilde{\chi}_1^0)$$

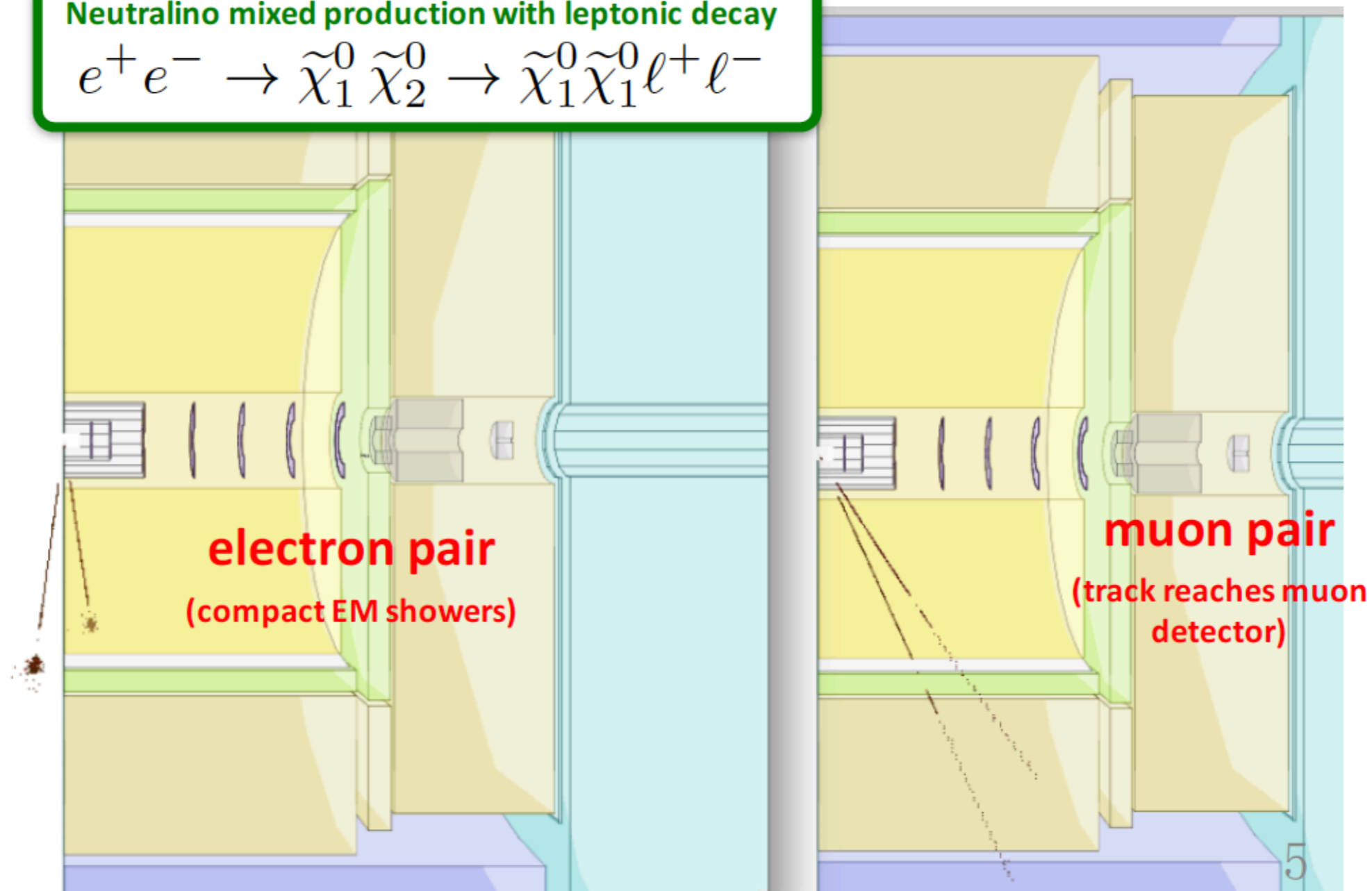
measure $m(\ell^+ \ell^-) < m_{\tilde{\chi}_2^0} - m_{\tilde{\chi}_1^0}$ and $E(\ell^+ \ell^-)$

How do these signals look in the detector? (1)

$\sqrt{s} = 500 \text{ GeV}$

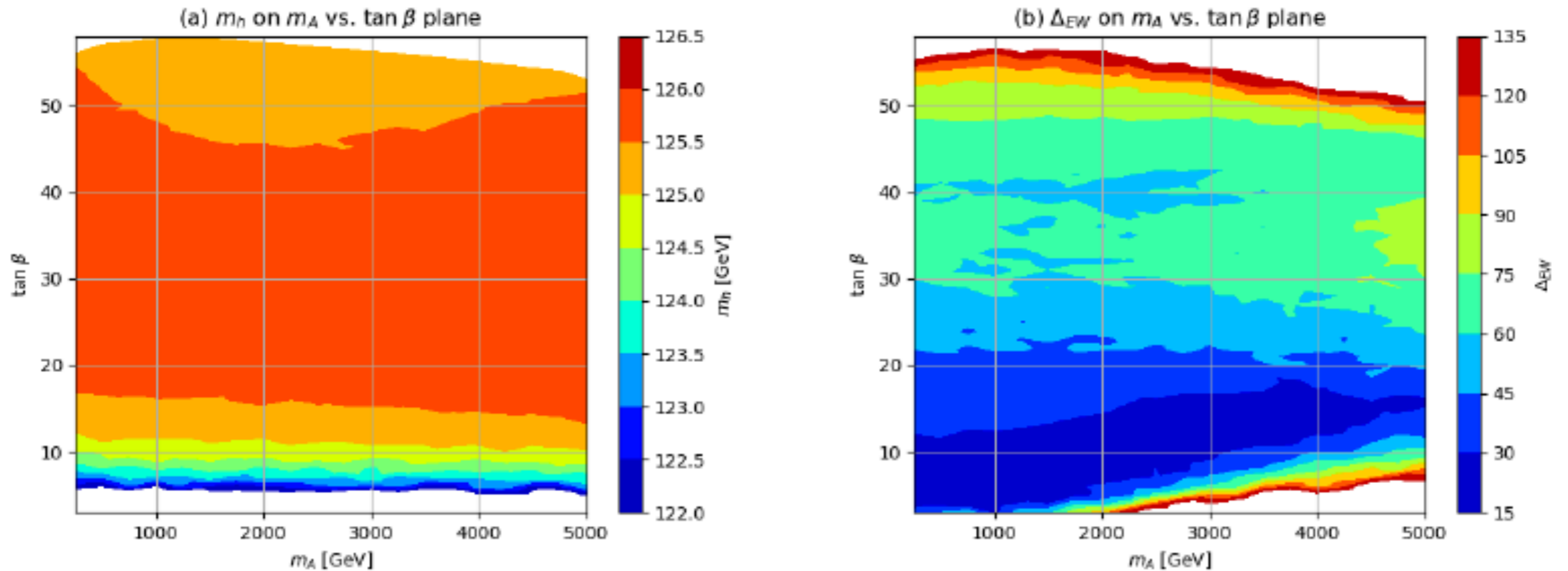
Neutralino mixed production with leptonic decay

$$e^+e^- \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \ell^+ \ell^-$$



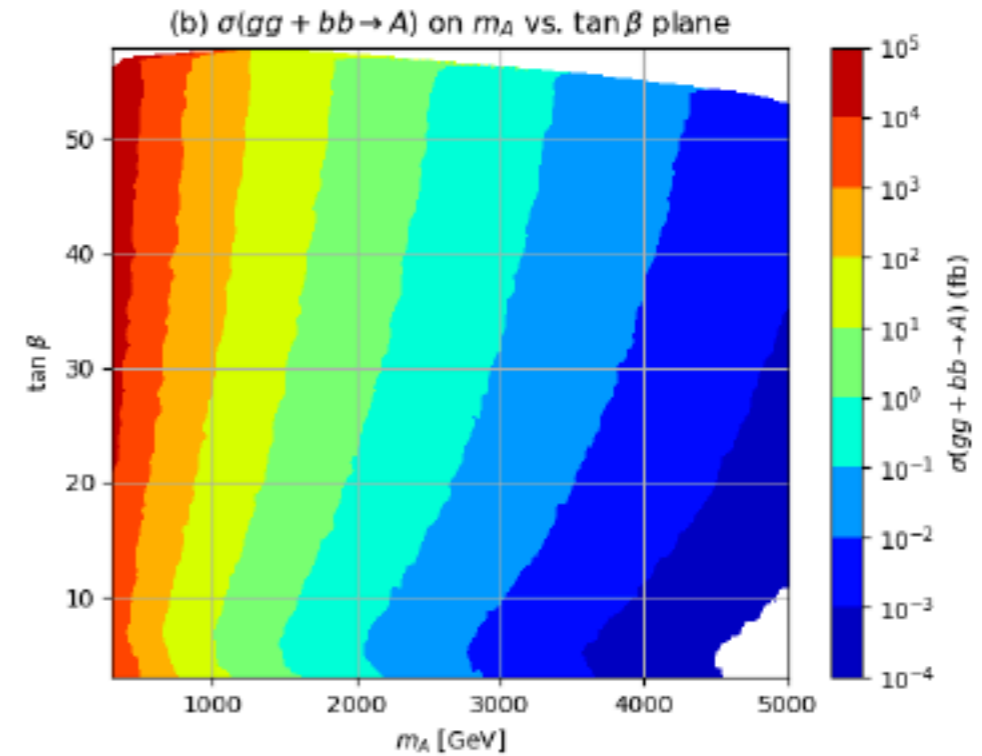
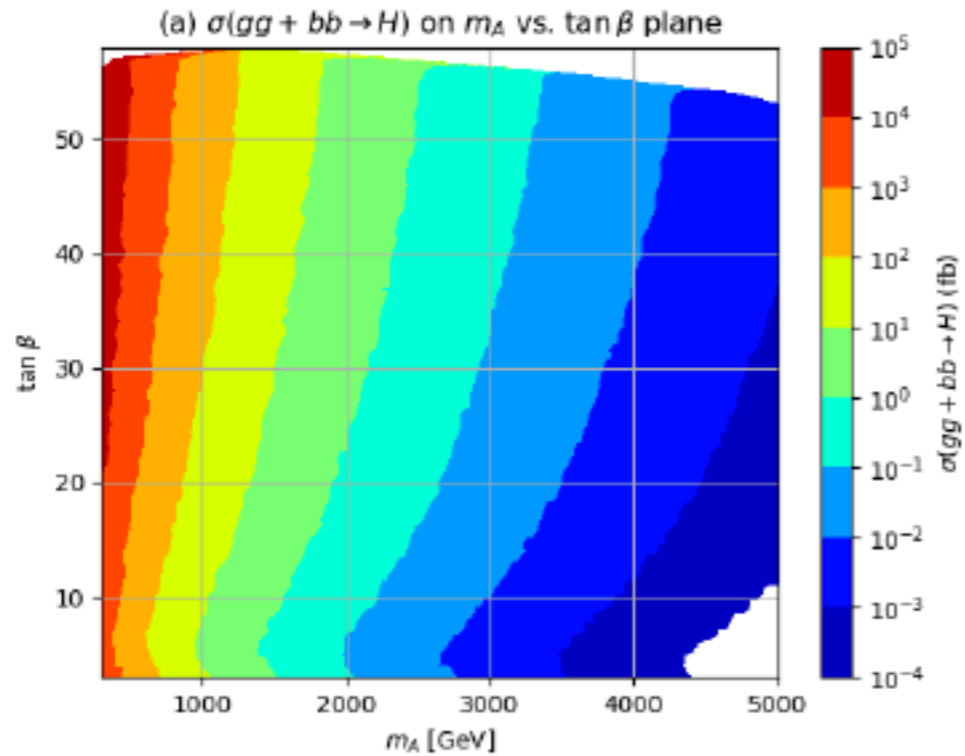
Prospects for heavy SUSY Higgs bosons at HL-LHC

traditional results in m_A vs. $\tan\beta$ plane

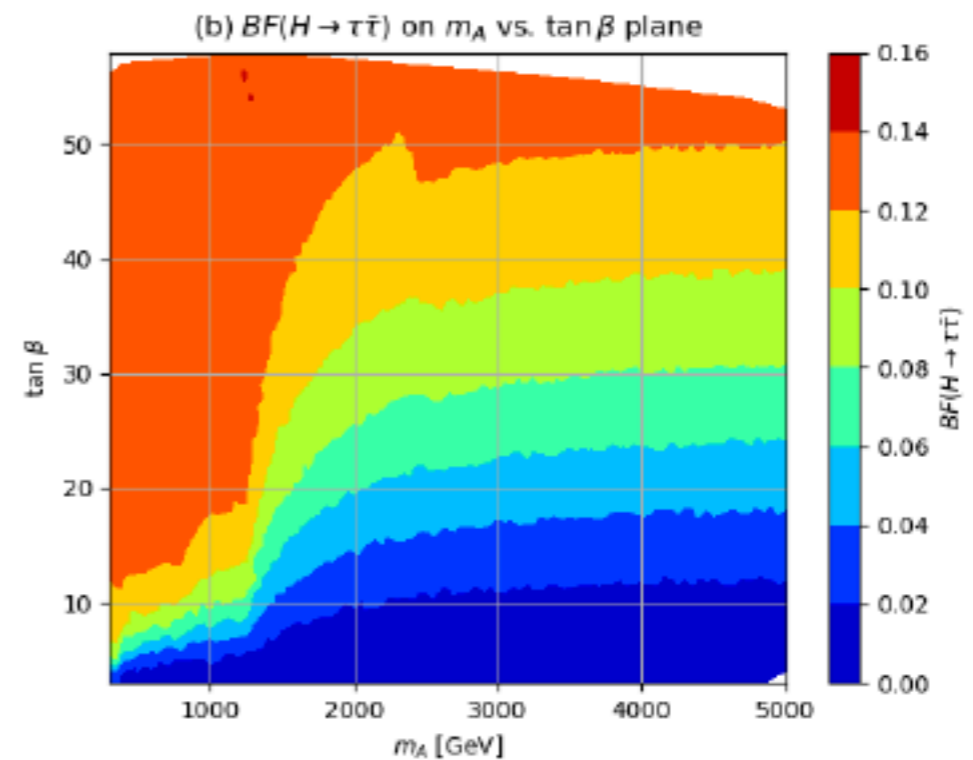
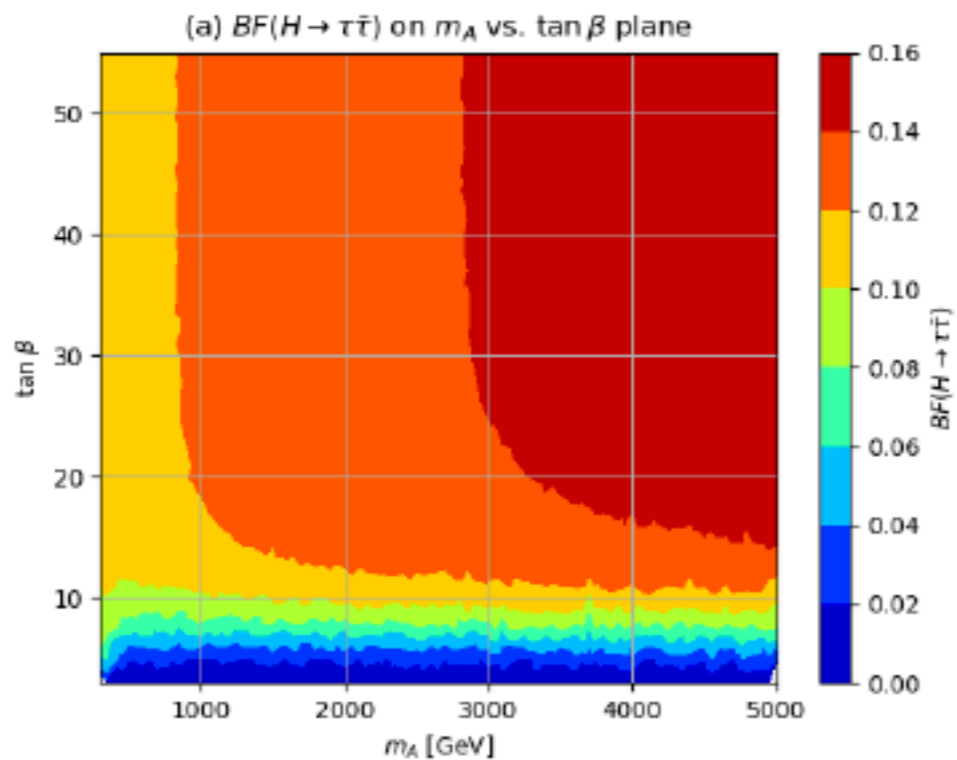


In EW natural SUSY, it is
easy to get $m_h \sim 125$ GeV (large $-A_0$)
and low $\Delta_{EW} < \sim 30$

Direct s-channel production of A, H:



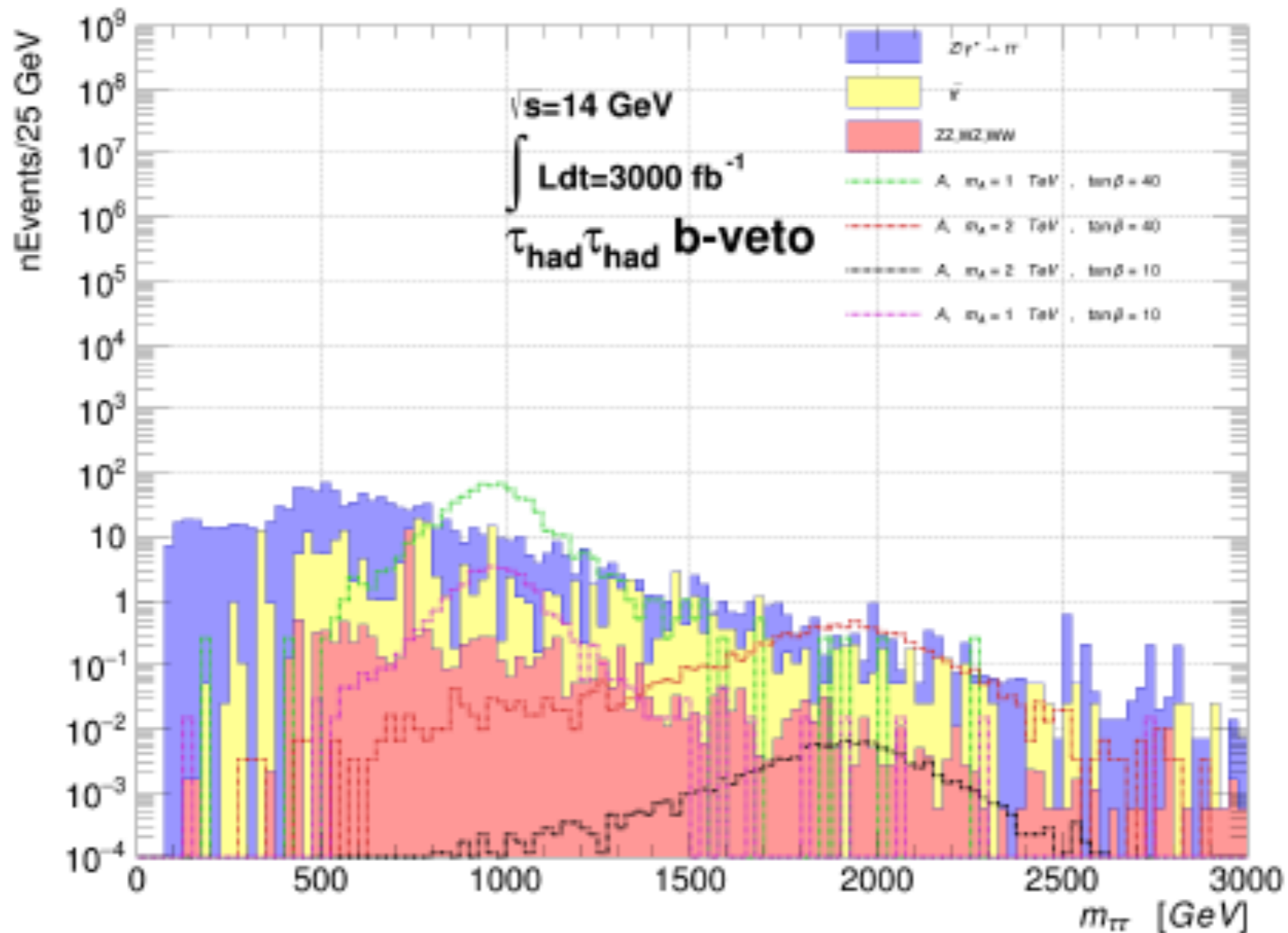
best decay channel: ditau



unnatural SUSY

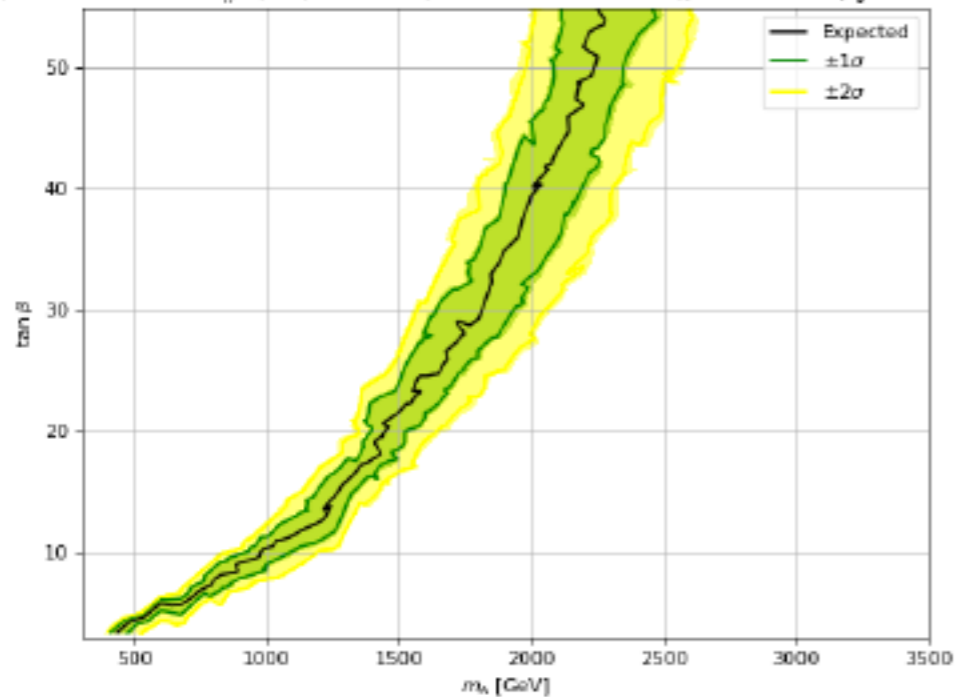
natural SUSY

Best signature: $H, A \rightarrow \tau\tau$ with $\nu\tau$ aligned with $\tau\tau$:
 can reconstruct ditau mass!

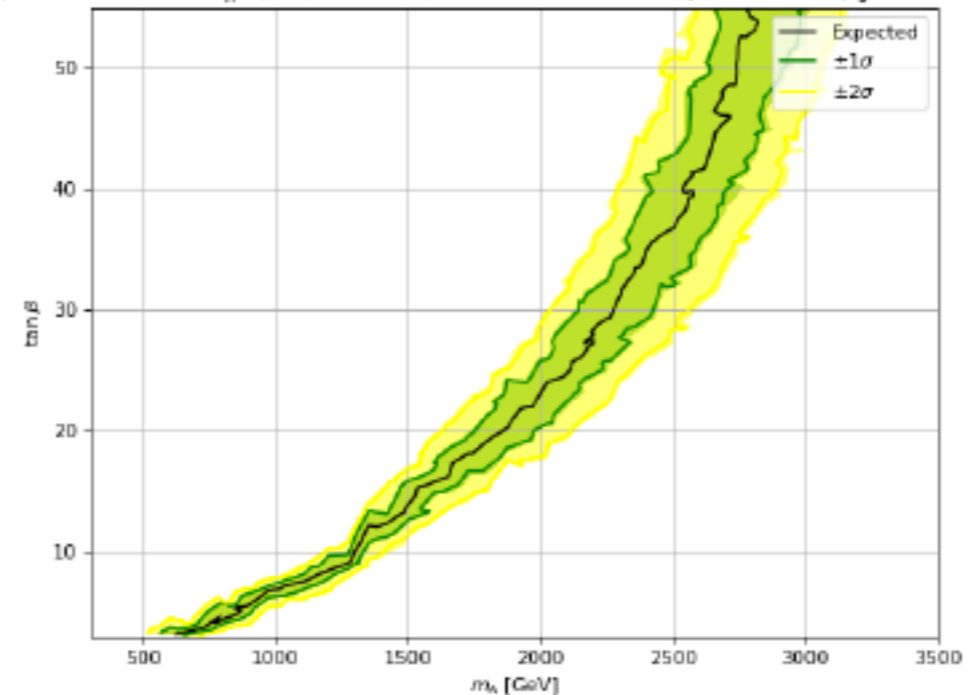


2-sigma exclusion contours for H, A-> ditau in natural SUSY at LHC14 with 300 (3000) fb⁻¹

(b) Exclusion Plane $m_h^{125}(\text{nat})$ scenario (BtB & non-BtB events), $\sqrt{s} = 14$ TeV, $\int Ldt = 300 \text{ fb}^{-1}$



(b) Exclusion Plane $m_h^{125}(\text{nat})$ scenario (BtB & non-BtB events), $\sqrt{s} = 14$ TeV, $\int Ldt = 3000 \text{ fb}^{-1}$



HB, Barger, Tata, Zhang, arXiv:2209.00063

HL-LHC **exclusion** reaches to $m_A \sim 1.3$ TeV for $\tan\beta = 10$

$m_A \sim 2.5$ TeV for $\tan\beta = 40$

$H, A \rightarrow$ SUSY offers new discovery channels!

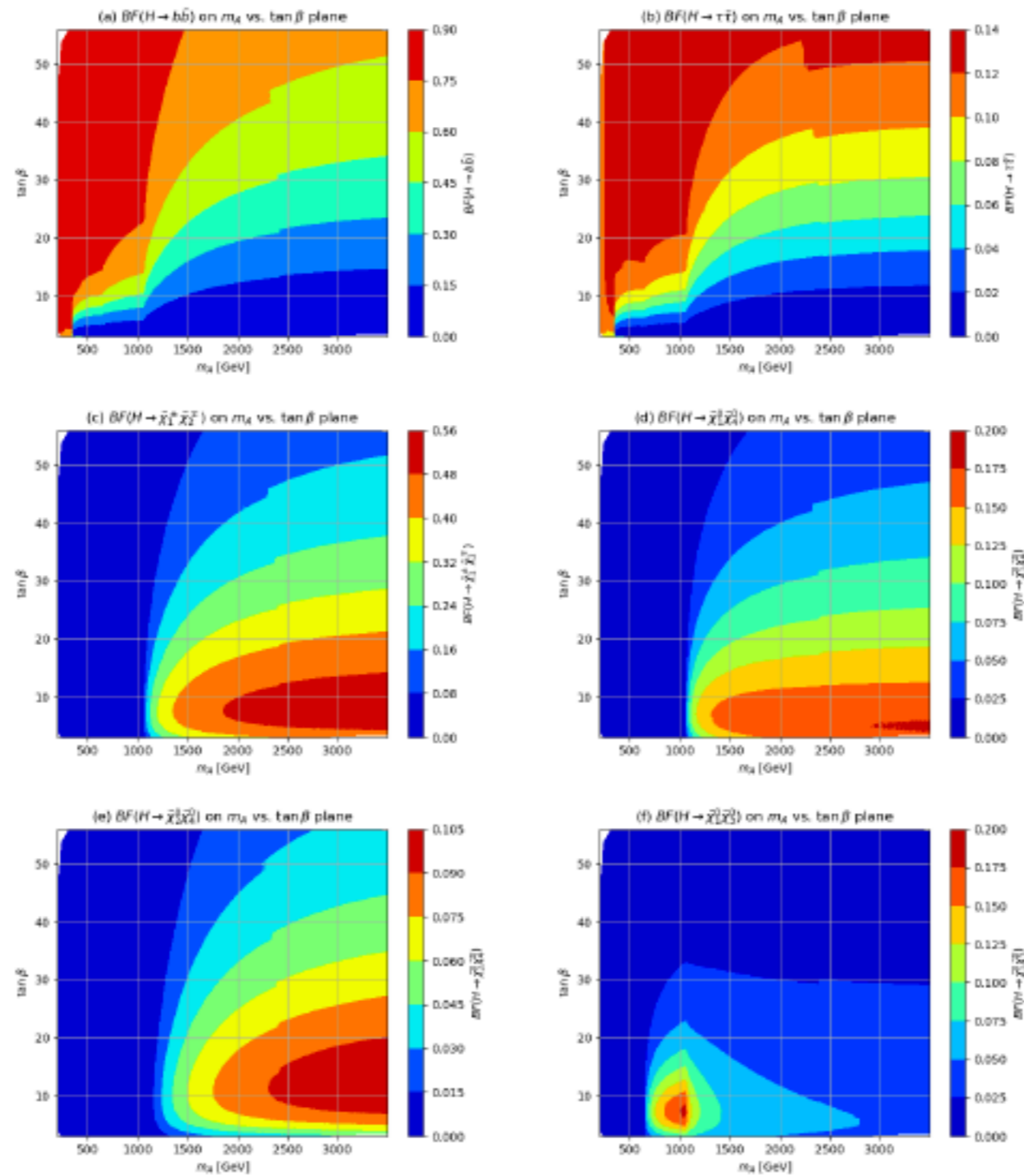


Figure 2: Branching fractions for H to a) $b\bar{b}$, b) $\tau\bar{\tau}$, c) $\tilde{\chi}_1^\pm \tilde{\chi}_2^\mp$, d) $\tilde{\chi}_1^0 \tilde{\chi}_2^0$, e) $\tilde{\chi}_2^0 \tilde{\chi}_4^0$ and f) $\tilde{\chi}_1^0 \tilde{\chi}_3^0$ from Isajet 7.88 [36].

H,A → SUSY → (W,Z,h)+MET

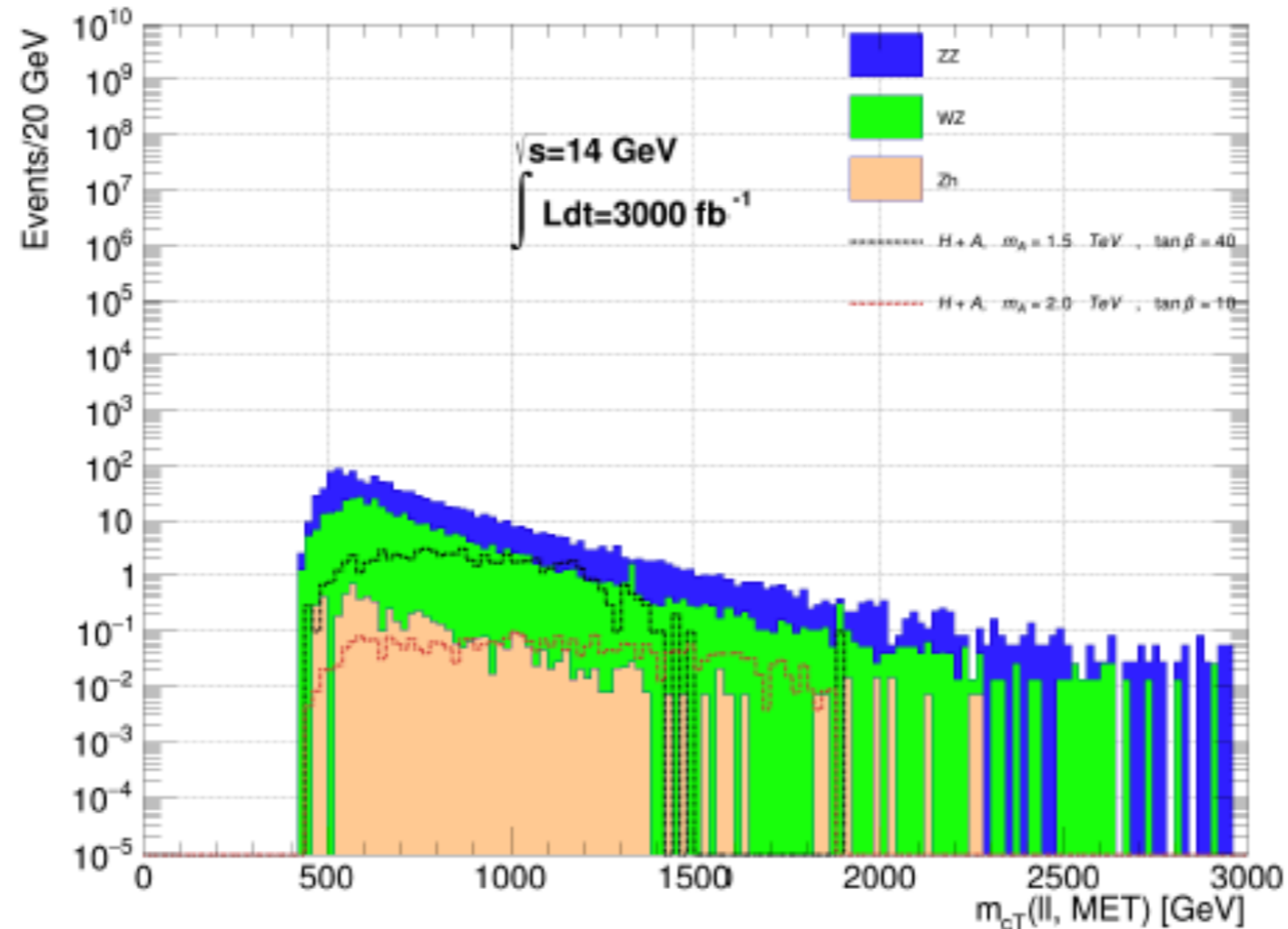
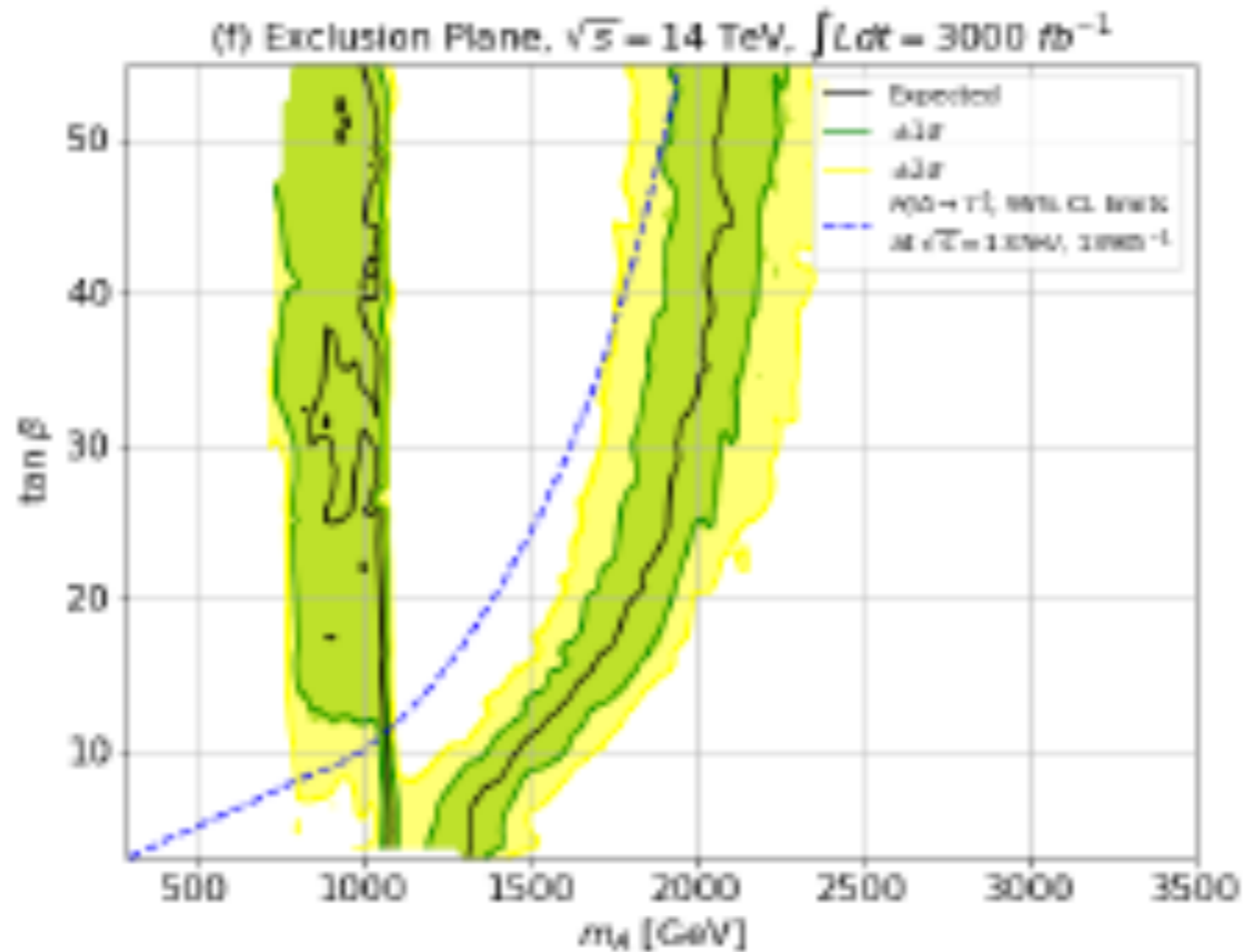


Figure 5: Distribution in $m_{cT}(\ell\bar{\ell}, E_T)$ for $pp \rightarrow H, A \rightarrow Z + E_T$ with $Z \rightarrow \ell^+ \ell^-$ decay events at $\sqrt{s} = 14$ TeV. We show two signal distributions (dashed) along with dominant SM backgrounds (not stacked).

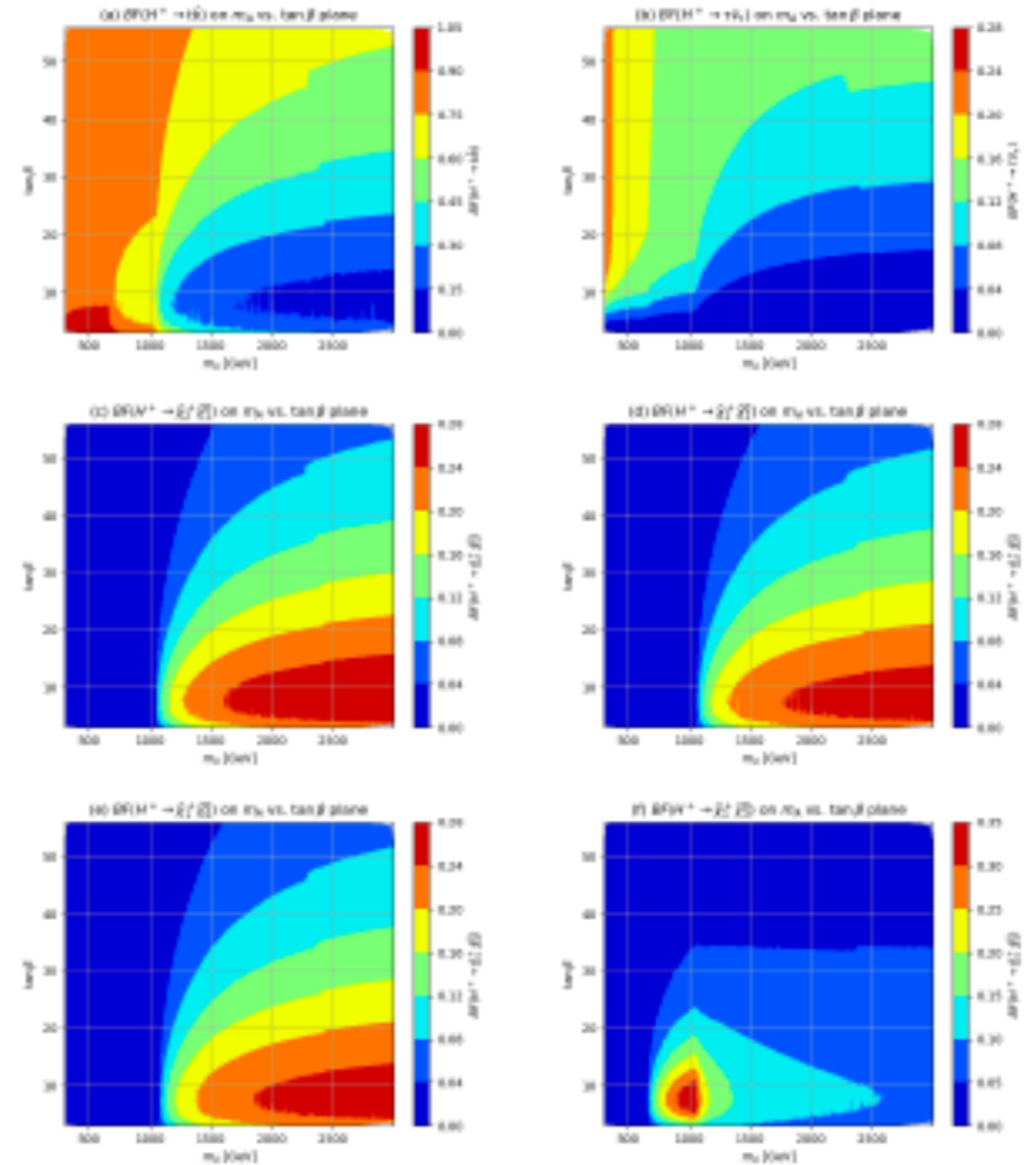
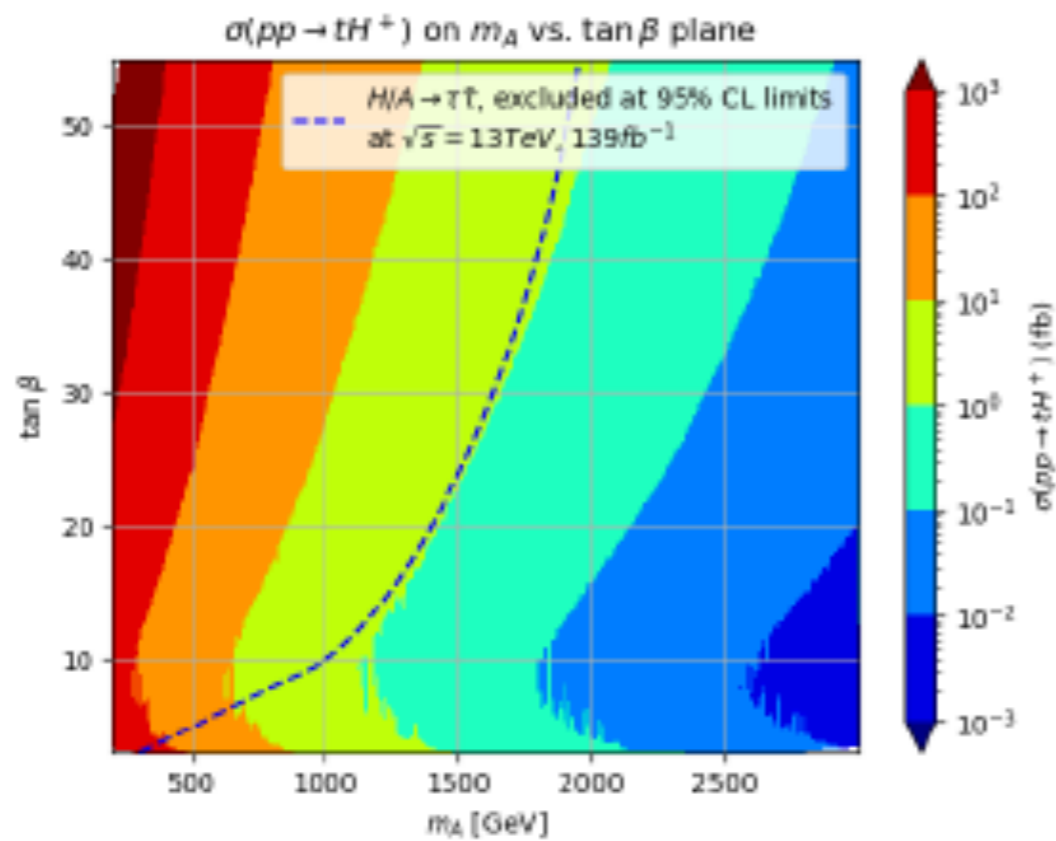
look for buildup of excess mT at very high energies!

HL-LHC exclusion plane for combined 6 H,A->nat SUSY channels

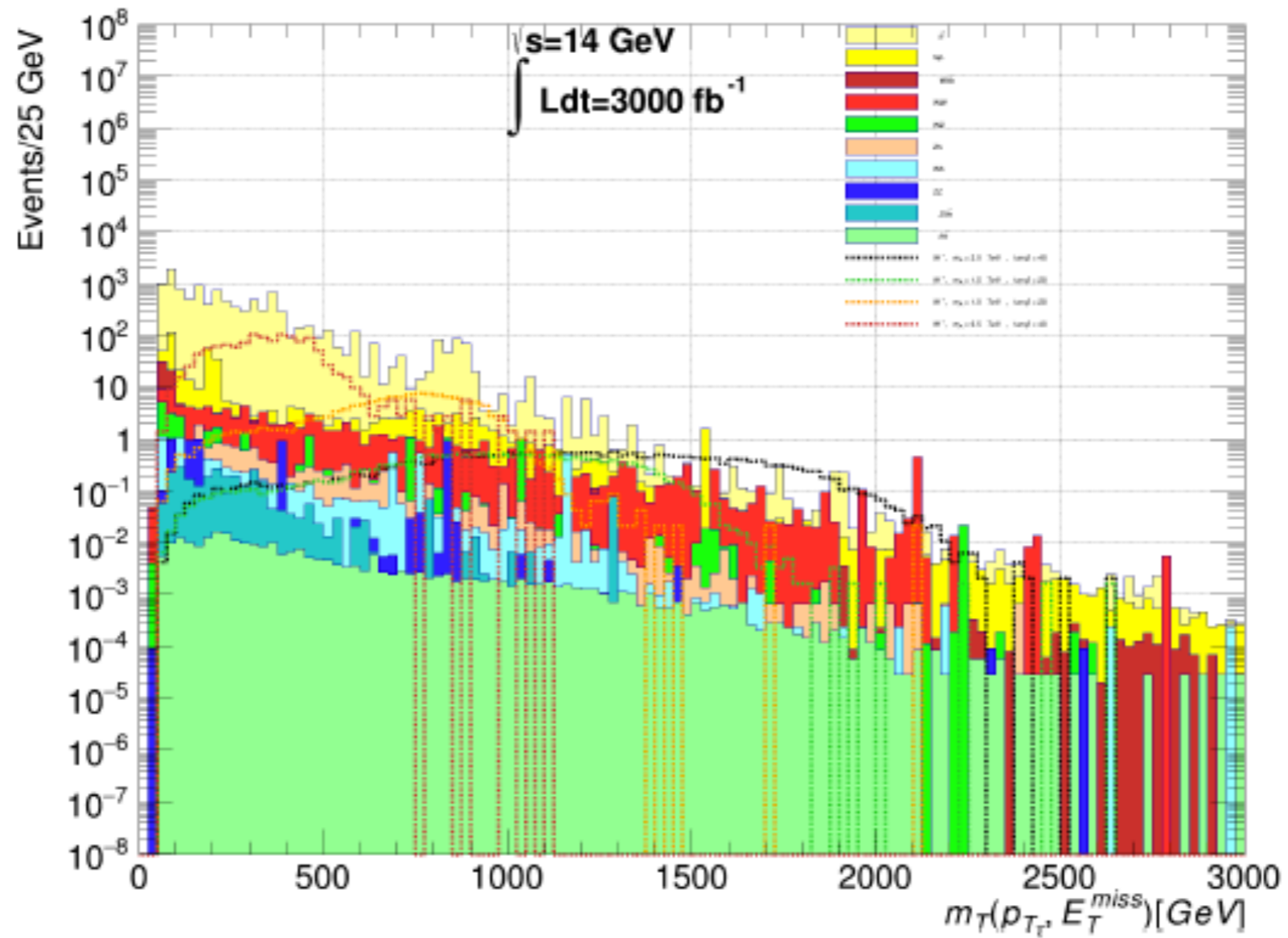


some new p-space opens up

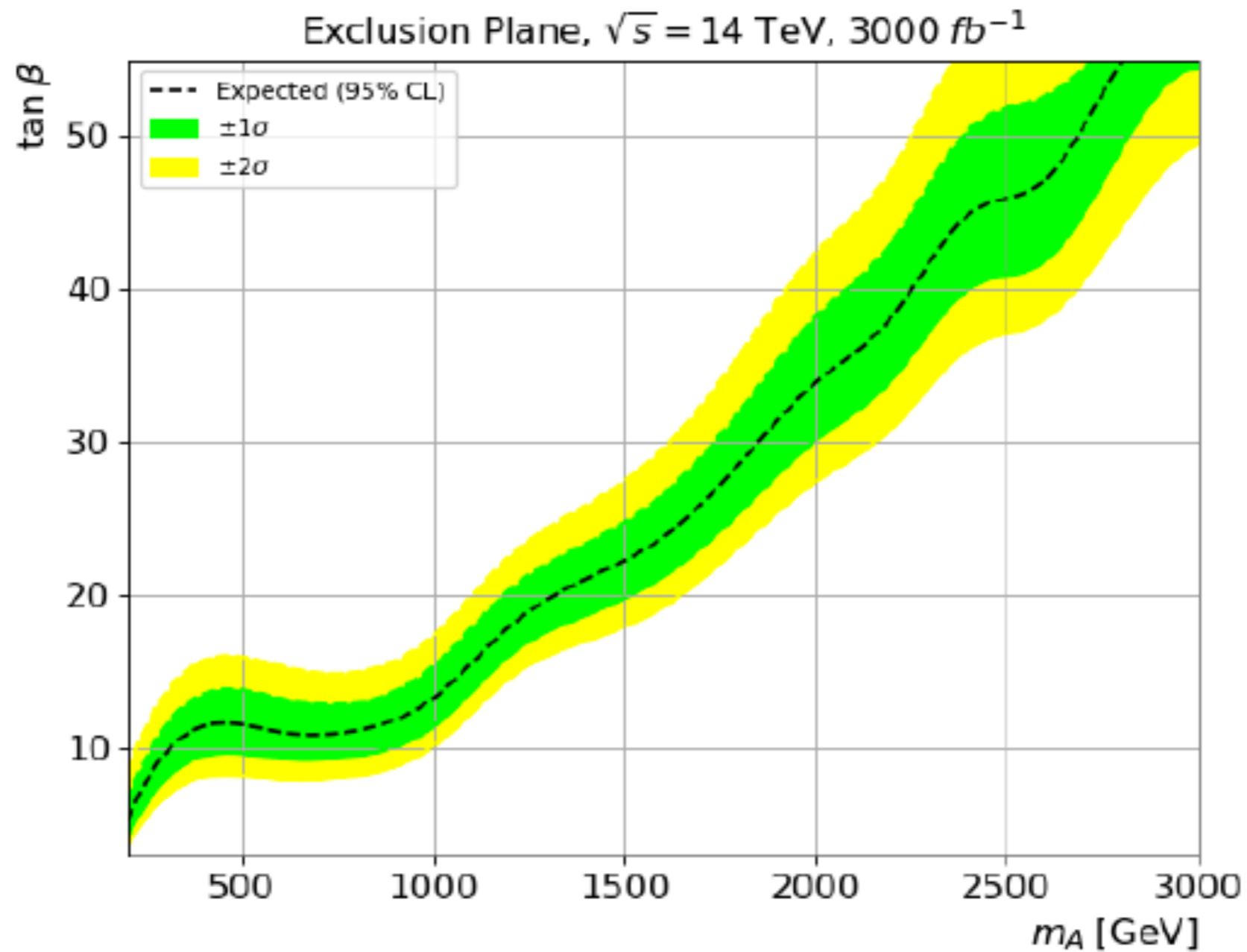
See $pp \rightarrow tH^+$ at HL-LHC?



$H^+ \rightarrow \tau + \nu_\tau$ channel seems best



HL-LHC exclusion plot for $pp \rightarrow t\hat{H}^{\pm} \rightarrow t+(\tau+\nu)$



HB, Barger, Tata, Zhang, in progress

more exotic heavy Higgs signatures await FCChh!

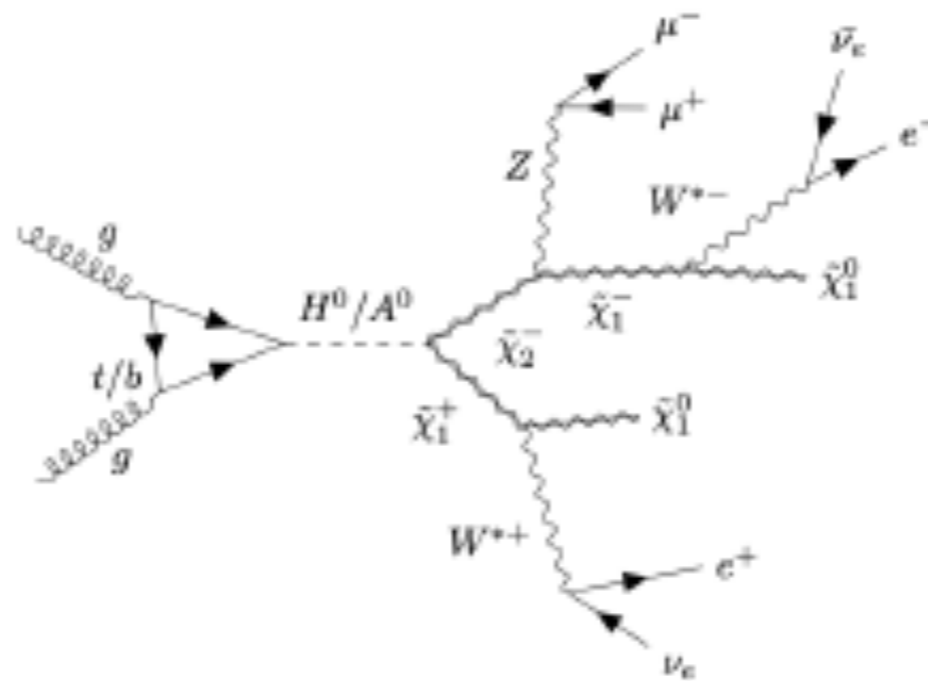


FIG. 1: Feynman diagram for $gg \rightarrow H, A(\rightarrow \tilde{\chi}_2^\pm \tilde{\chi}_1^\mp \rightarrow 4\ell + \cancel{E}_T) + X$ production; there is a similar diagram for H, A production via $b\bar{b}$ fusion.

$pp \rightarrow A, H \rightarrow \text{SUSY} \rightarrow 4\ell + \text{MET};$

HB, Barger, Jain, Kao, Sengupta, Tata, arXiv:2112.02232

For further reading:

- The string theory landscape, Bousso & Polchinski, Sci. Am. 291 (2004) 60–69
- Midi-review: Status of weak scale supersymmetry after LHC Run 2 and ton-scale noble liquid WIMP searches, HB, Barger, Salam, Sengupta, Sinha, arXiv: 2002.03013

Conclusions:

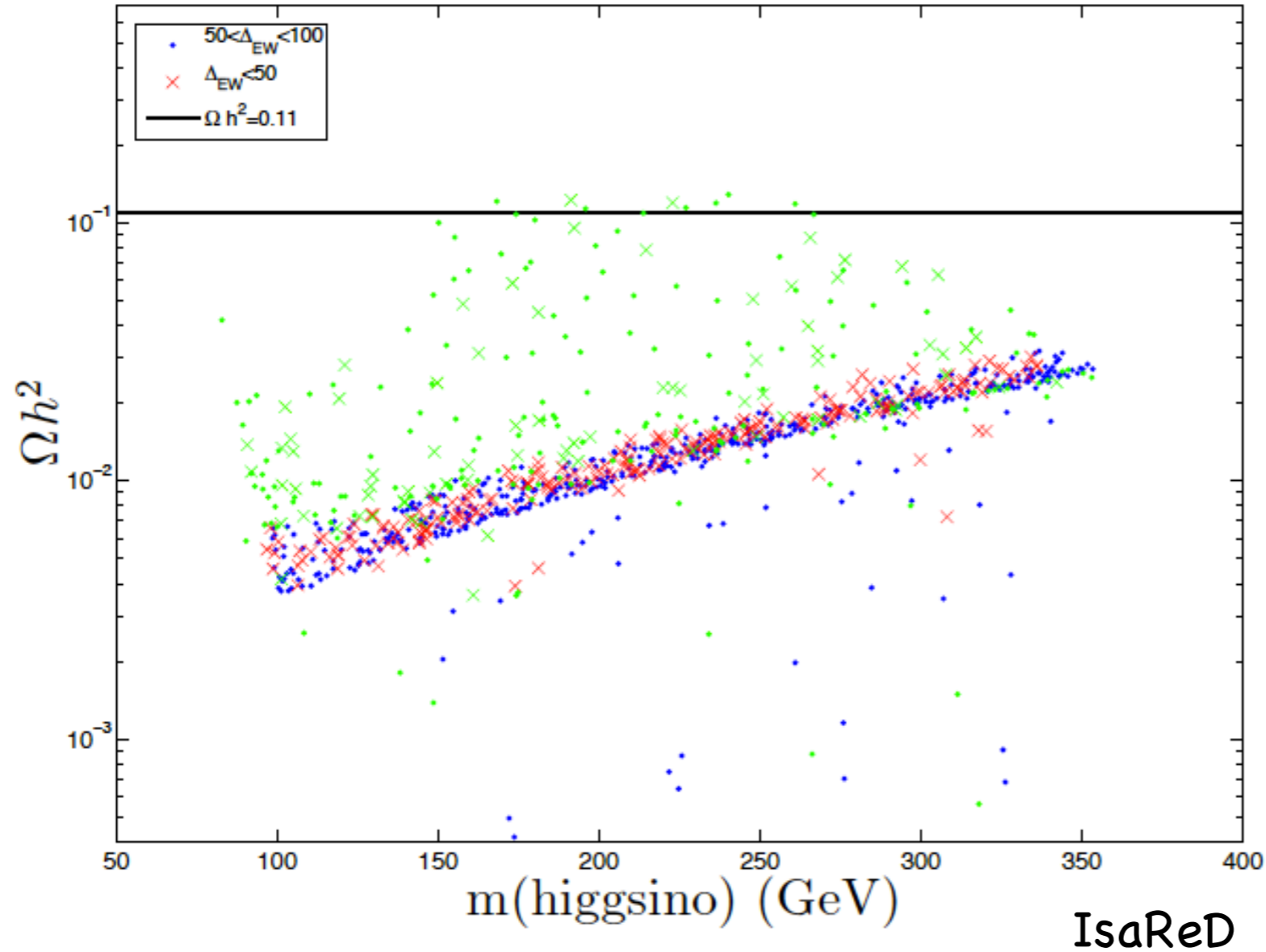
- Time to set aside old/flawed measures of naturalness:
- Plenty of natural parameter space under model independent measure DEW
- $\mu \sim 100\text{--}350$ GeV: **light higgsinos!**
- other sparticle contributions to $m(\text{weak})$ are loop suppressed- masses can be TeV-
>multi-TeV
- stringy naturalness: **what the string landscape prefers**
- draw to large soft terms provided $m(\text{weak}) \sim (2\text{--}5) * 100$ GeV
- predicts LHC sees $m_h \sim 125$ GeV but as yet no sign of sparticles
- under stringy naturalness, a 3 TeV gluino more natural than 300 GeV gluino
- landscape \rightarrow non-universal 1st/2nd gen. scalars at 20-40 TeV: natural but gives quasi-degeneracy/decoupling sol'n to SUSY flavor, CP and CMP
- most promising: LHC \rightarrow light higgsinos via soft dilepton+jet+MET channel
- see heavy Higgs H, A, H^\pm up to $\sim 1\text{--}3$ TeV at HL-LHC (depending on $\tan\beta$)
- ILC: for $\sqrt{s} > 2m(\text{higgsino})$, expect light higgsinos
- dark matter: a mix of axions+higgsino-like WIMPs (typically mainly axions)

More slides:

DM, baryogenesis, aspects of naturalness

Dark matter from SUSY
with radiatively-driven naturalness

Mainly higgsino-like WIMPs thermally underproduce DM



green: excluded;
red/blue: allowed

HB, Barger, Mickelson

Factor of 10-15 too low

But so far we have addressed only **Part 1**
of fine-tuning problem:

In QCD sector, the term $\frac{\bar{\theta}}{32\pi^2} F_{A\mu\nu} \tilde{F}_A^{\mu\nu}$ must occur

But neutron EDM says it is not there: strong CP problem

(frequently ignored by SUSY types)

Best solution after 35 years:

PQWW/KSVZ/DFSZ **invisible axion**

In SUSY, axion accompanied by axino and saxion

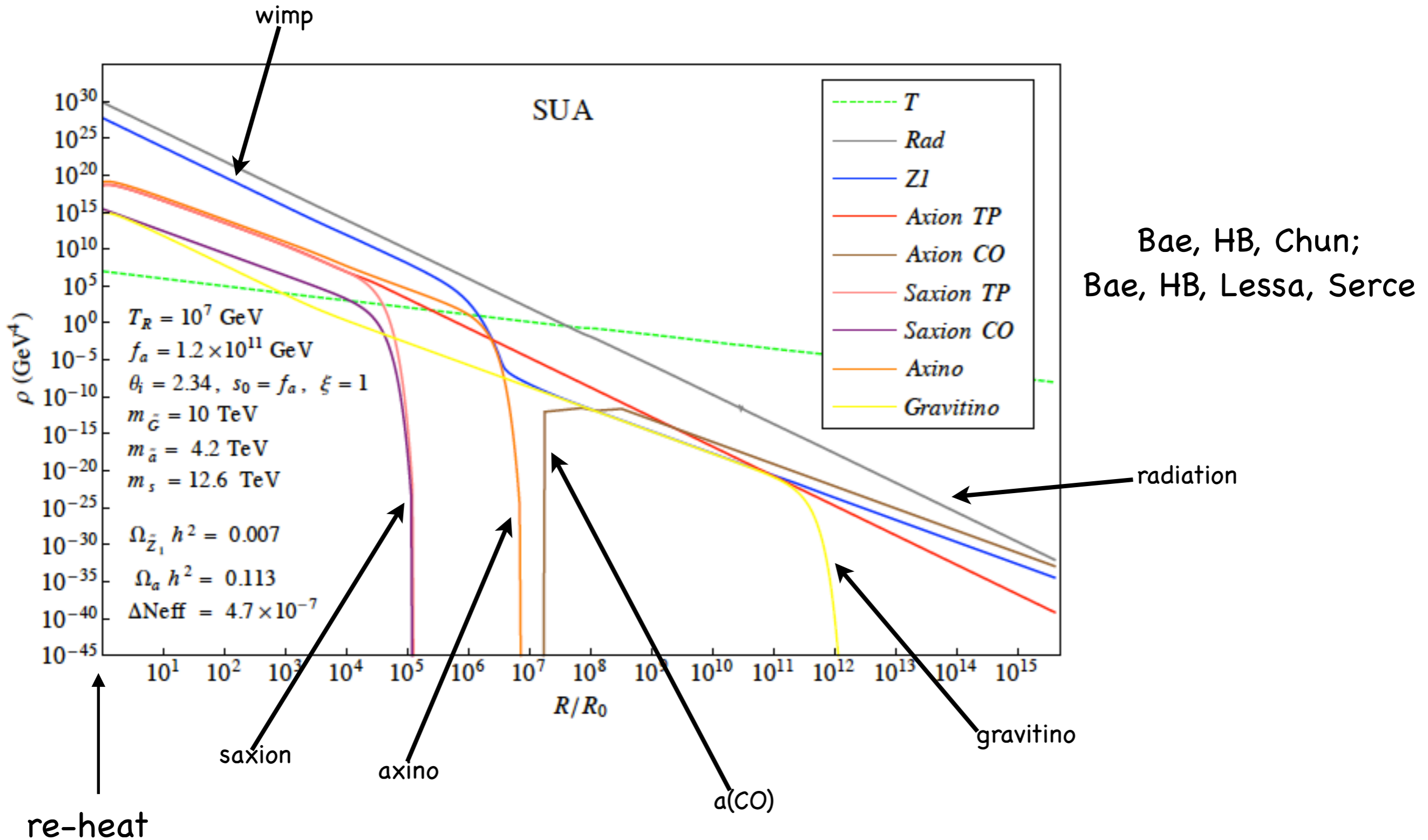
Changes DM calculus:

expect mixed WIMP/axion DM (**2 particles**)

mixed axion-neutralino production in early universe

- neutralinos: thermally produced (TP) or NTP via \tilde{a} , s or \tilde{G} decays
 - re-annihilation at $T_D^{s,\tilde{a}}$
- axions: TP, NTP via $s \rightarrow aa$, bose coherent motion (BCM)
- saxions: TP or via BCM
 - $s \rightarrow gg$: entropy dilution
 - $s \rightarrow SUSY$: augment neutralinos
 - $s \rightarrow aa$: dark radiation ($\Delta N_{eff} < 1.6$)
- axinos: TP
 - $\tilde{a} \rightarrow SUSY$ augments neutralinos
- gravitinos: TP, decay to SUSY

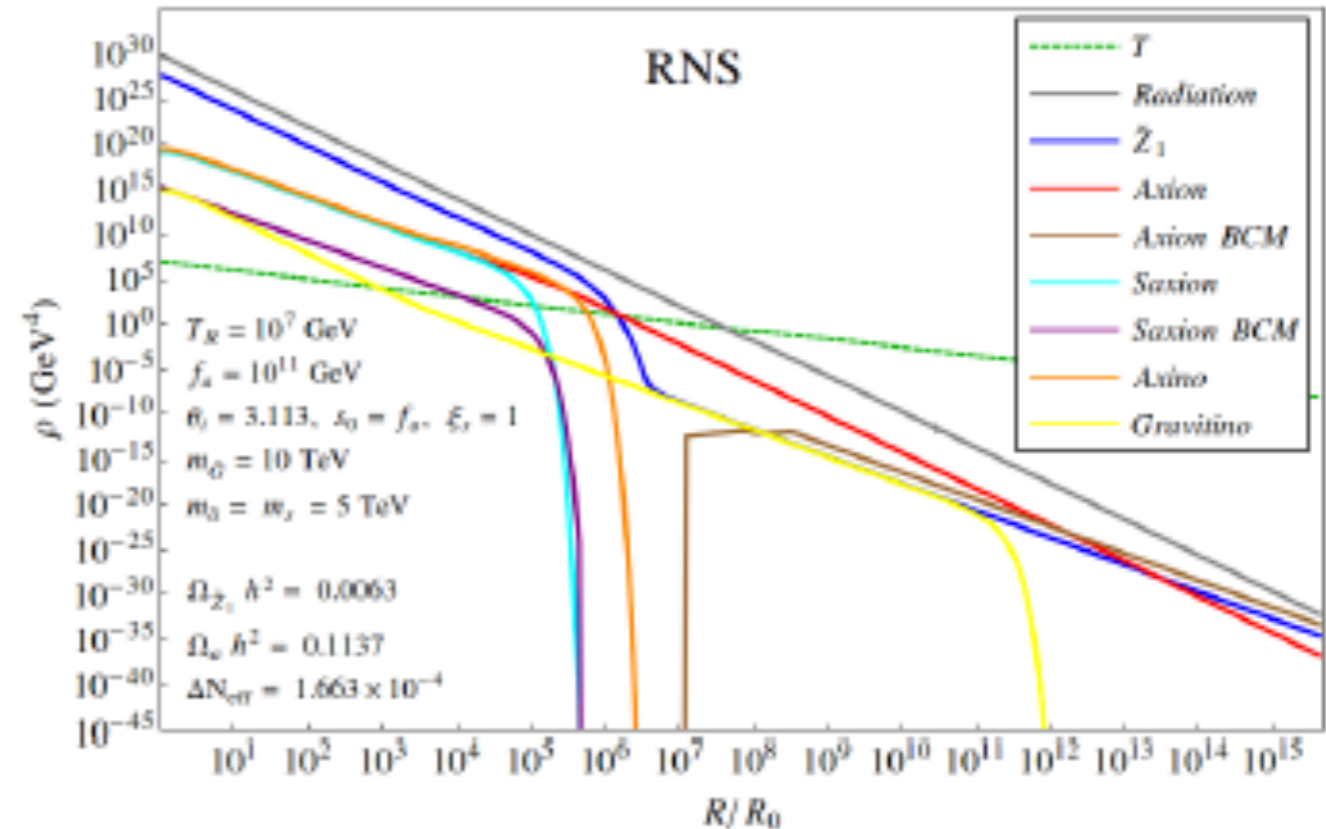
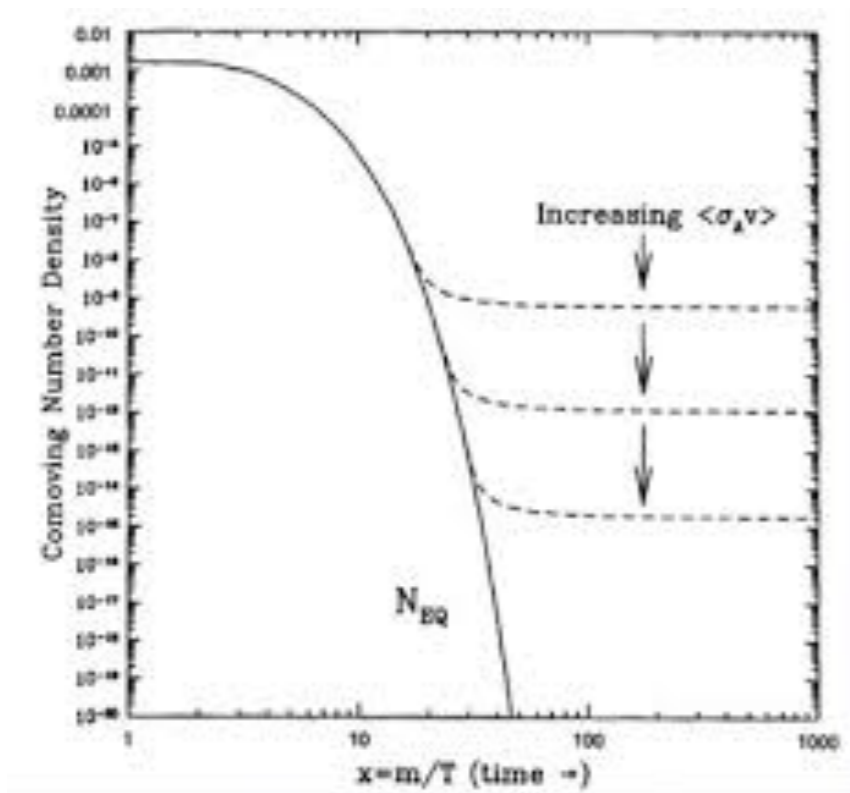
DM production in SUSY DFSZ: solve eight coupled Boltzmann equations



usual picture

=>

mixed axion/WIMP



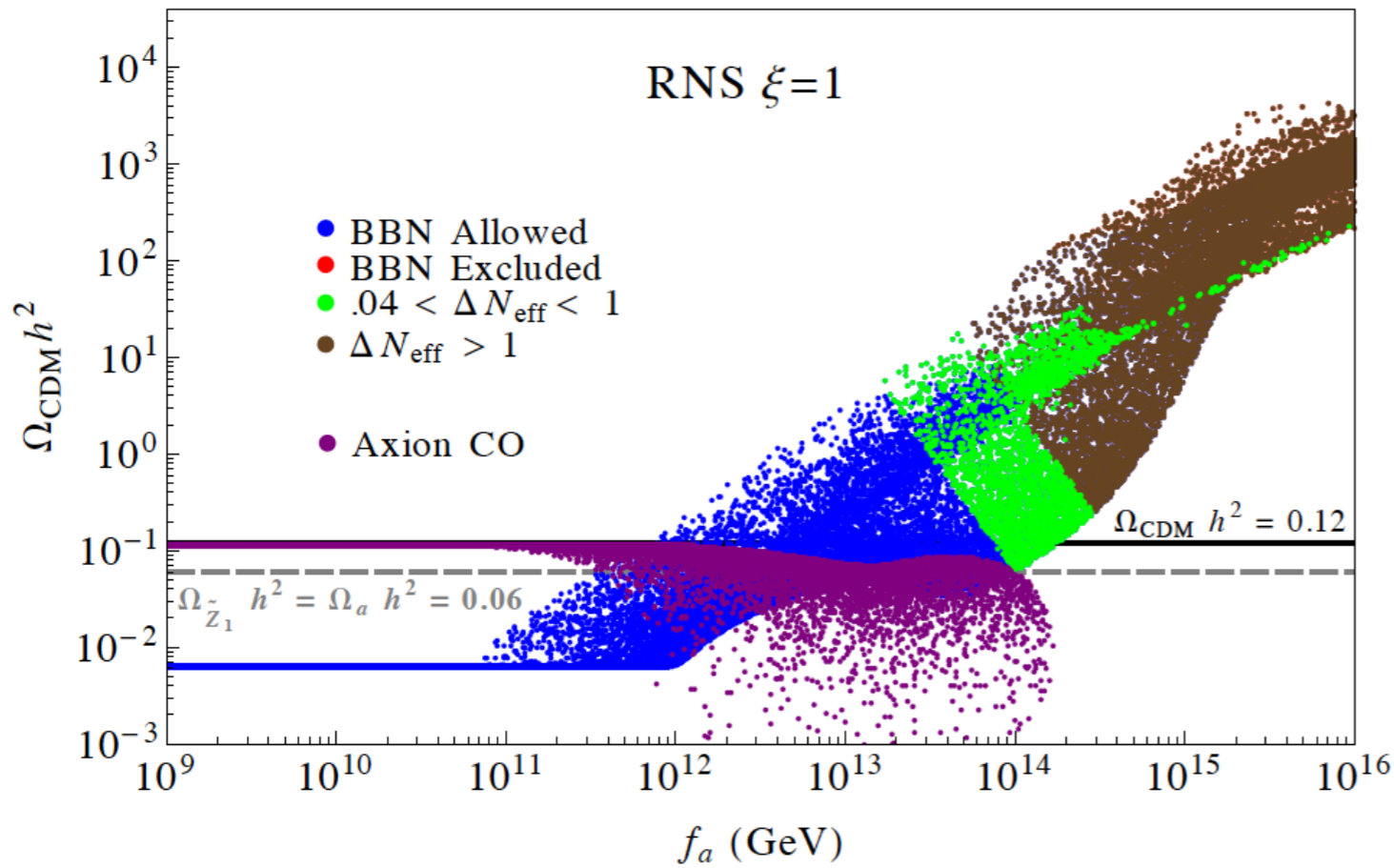
KJ Bae, HB, Lessa, Serce

much of parameter space is axion-dominated
with 10-15% WIMPs



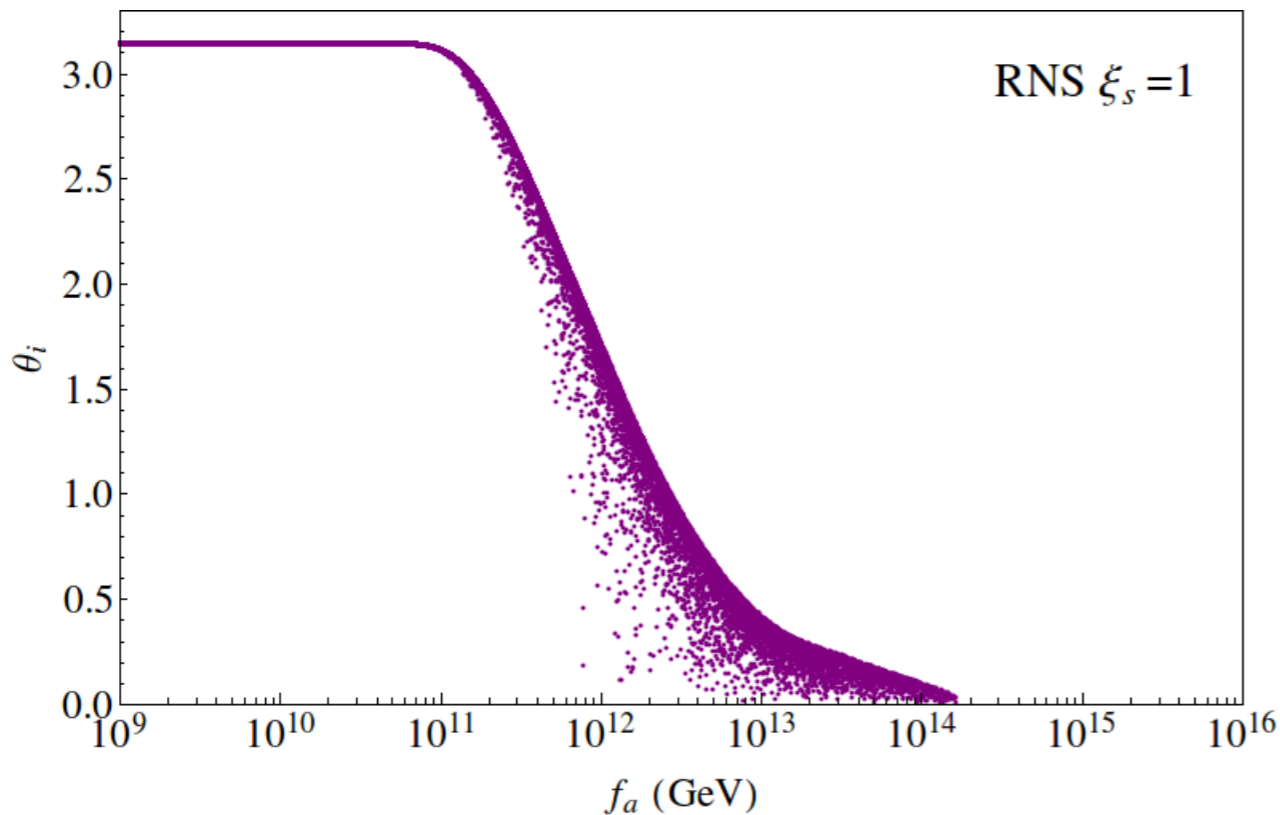
\Rightarrow





higgsino abundance

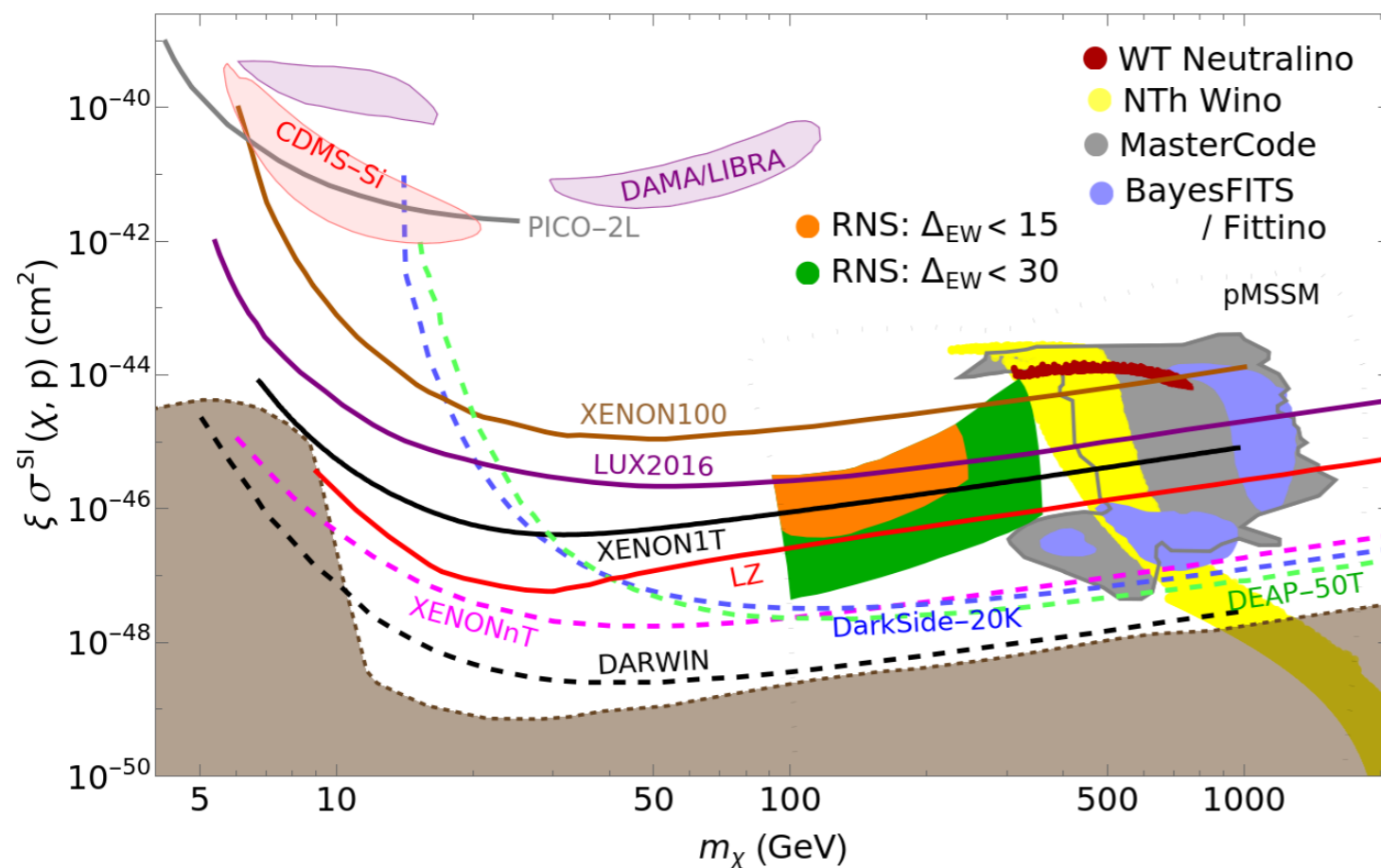
axion abundance



mainly axion CDM
 for $f_a < \sim 10^{12}$ GeV;
 for higher f_a , then get
 increasing wimp
 abundance

Direct higgsino detection rescaled

for minimal local abundance $\xi \equiv \Omega_{\chi}^{TP} h^2 / 0.12$



Bae, HB, Barger, Savoy, Serce

$$\mathcal{L} \ni -X_{11}^h \bar{\tilde{Z}}_1 \tilde{Z}_1 h$$

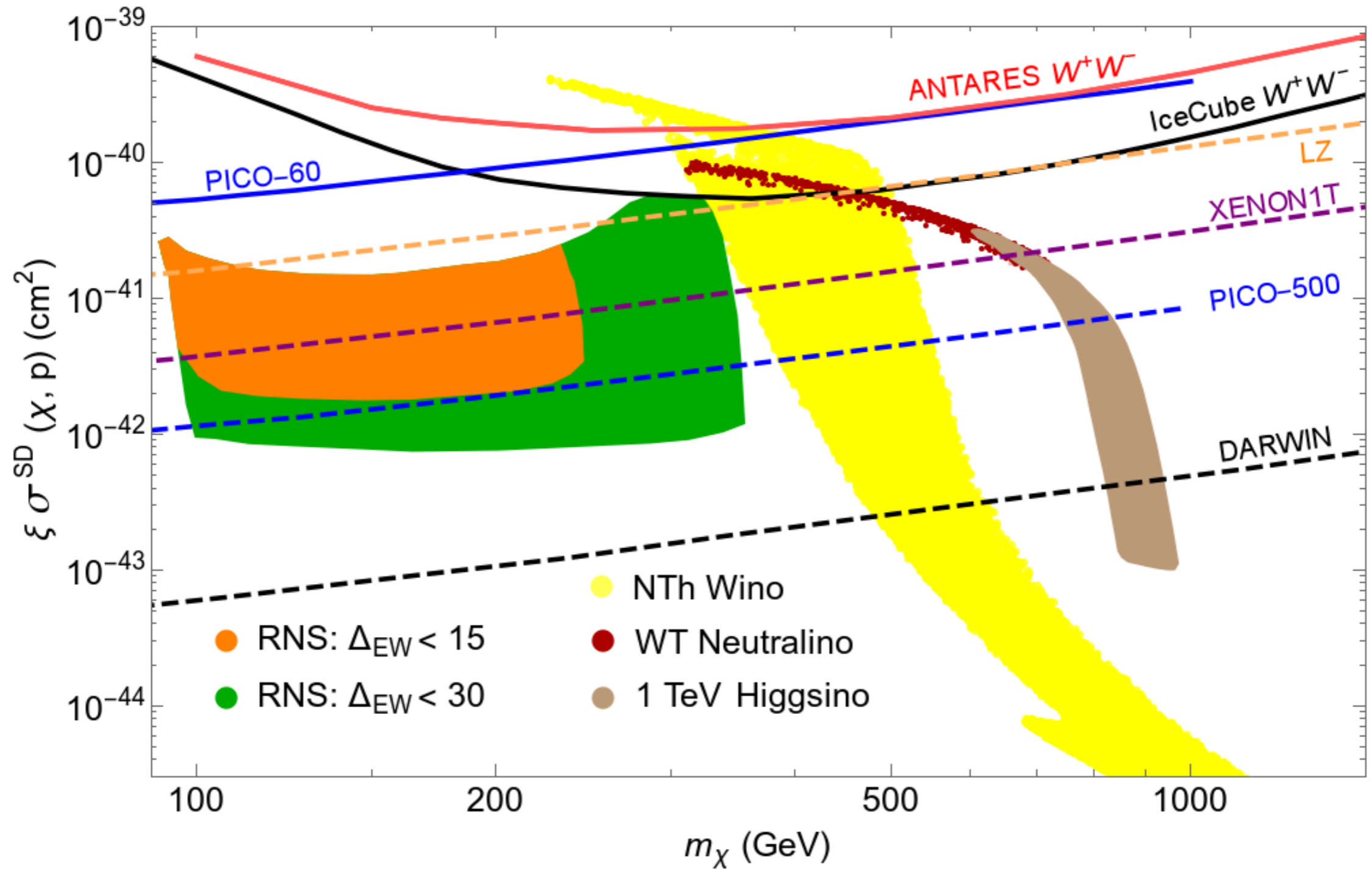
$$X_{11}^h = -\frac{1}{2} (v_2^{(1)} \sin \alpha - v_1^{(1)} \cos \alpha) (g v_3^{(1)} - g' v_4^{(1)})$$

includes latest
LZ2022 results!

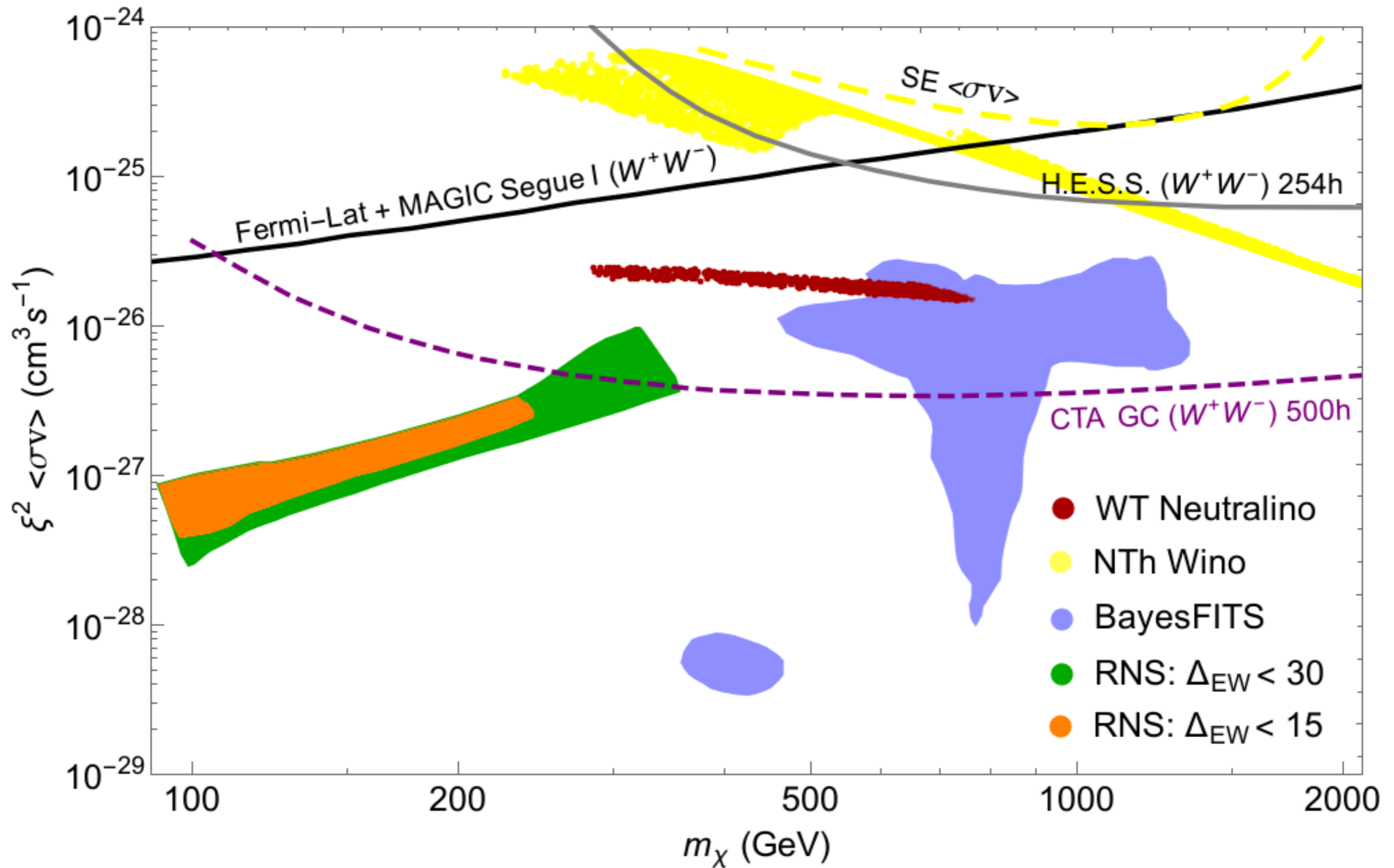
natural SUSY

Can test completely with ton scale detector
or equivalent (subject to minor caveats)

Prospects for SD WIMP searches:



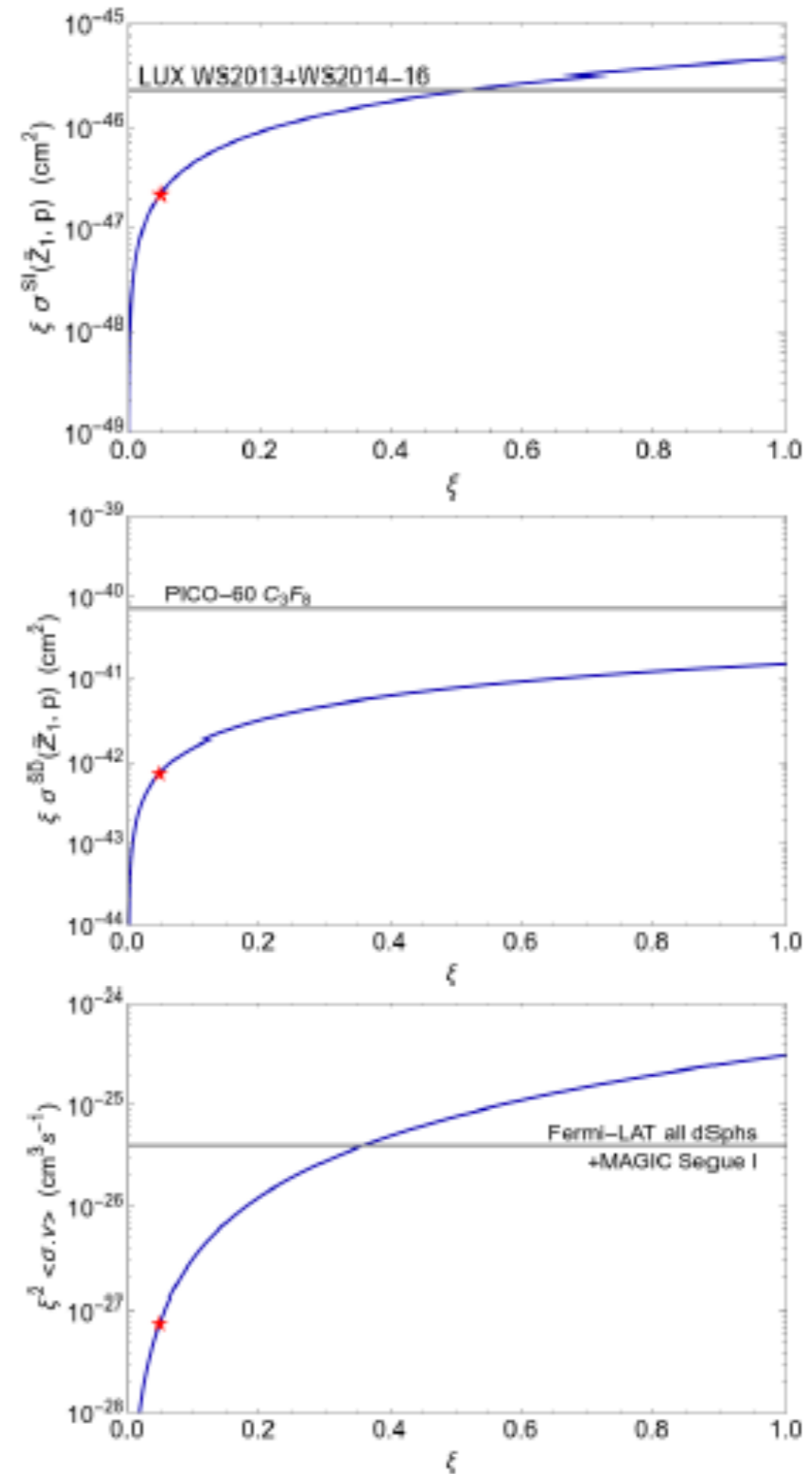
Prospects for IDD WIMP searches:

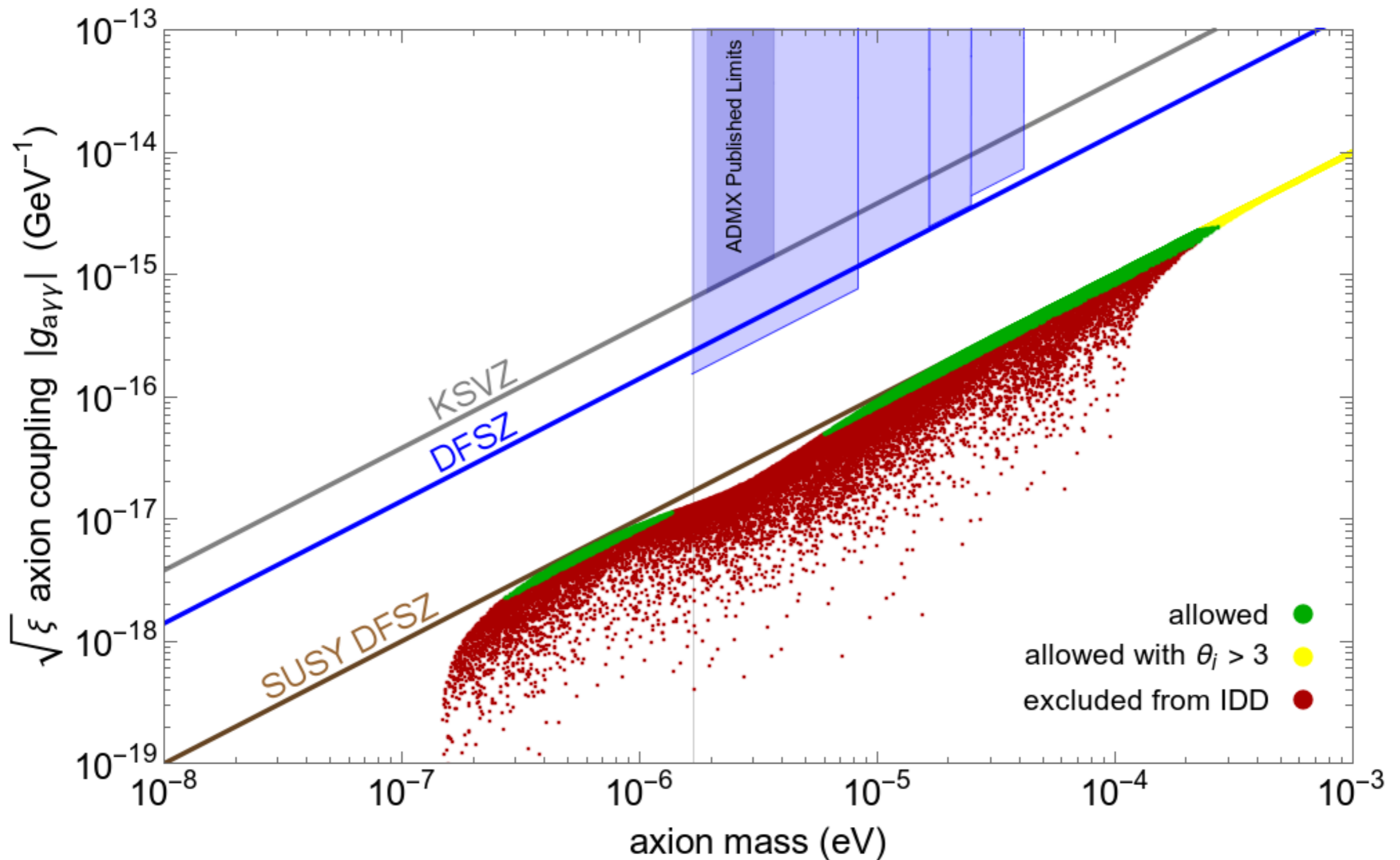


suppressed by square of diminished WIMP abundance

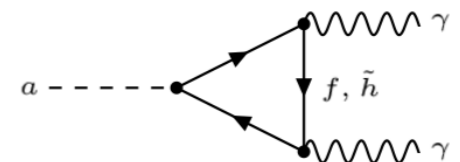
ξ

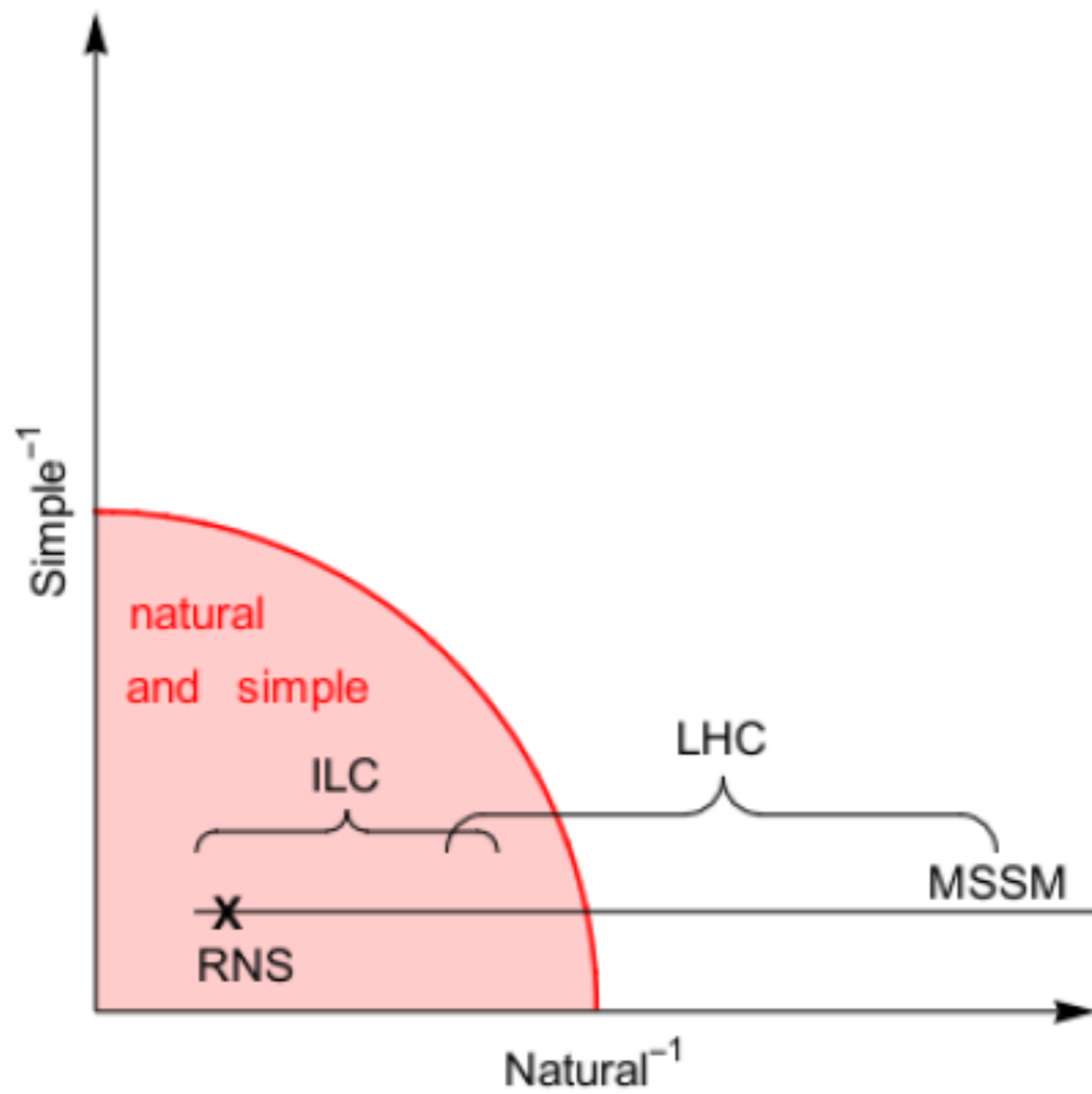
As ξ increases due to non-thermal WIMP production from saxion/axino decay, then axion parameter space becomes constrained by WIMP searches





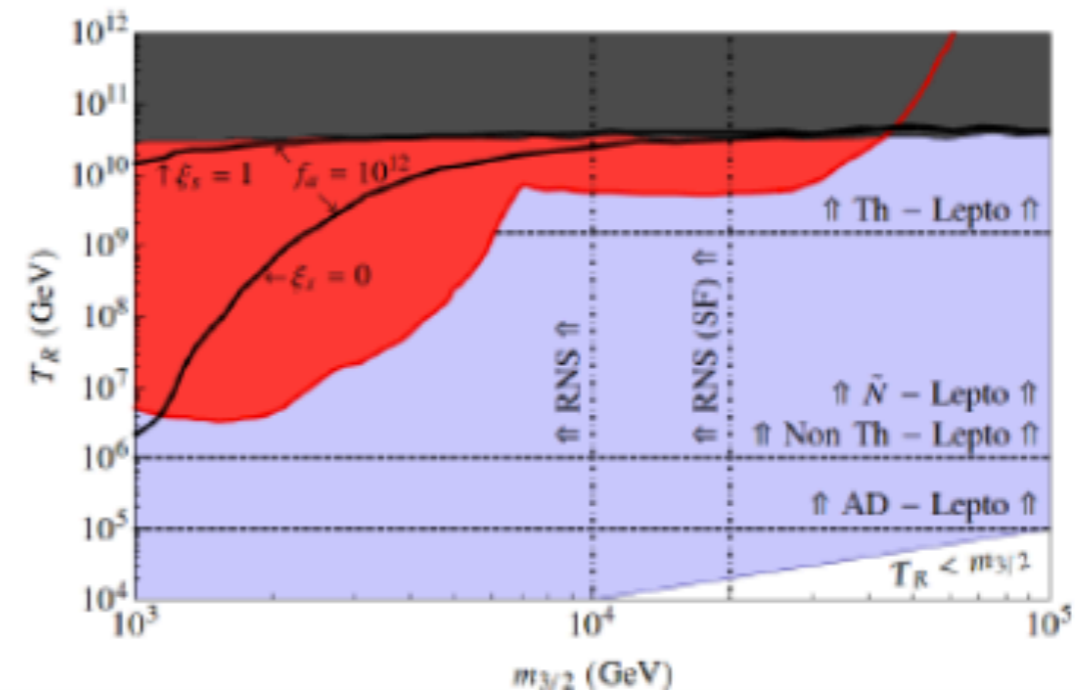
SUSY DFSZ axion: large range in $m(a)$ but coupling reduced
 may need to probe broader and deeper!





Baryogenesis scenarios for radiative natural SUSY

- thermal leptogenesis
- non-thermal (inflaton decay)
- oscillating sneutrino
- Affleck-Dine (AD)



gravitino problem plus
axino/saxion problem:
still plenty room

$$f_a = 10^{11}, 10^{12} \text{ GeV}$$

Bae, HB, Serce, Zhang, arXiv:1510.00724

#2: Higgs mass or large-log fine-tuning

 Δ_{HS}

It is tempting to pick out one-by-one quantum fluctuations **but** must combine log divergences before taking any limit

$$m_h^2 \simeq \mu^2 + m_{H_u}^2 + \delta m_{H_u}^2|_{rad}$$

$$\frac{dm_{H_u}^2}{dt} = \frac{1}{8\pi^2} \left(-\frac{3}{5}g_1^2 M_1^2 - 3g_2^2 M_2^2 + \frac{3}{10}g_1^2 S + 3f_t^2 X_t \right) \quad X_t = m_{Q_3}^2 + m_{U_3}^2 + m_{H_u}^2 + A_t^2$$

neglect gauge pieces, S, mHu and running;
then we can integrate from m(SUSY) to Lambda

$$\delta m_{H_u}^2 \sim -\frac{3f_t^2}{8\pi^2} (m_{Q_3}^2 + m_{U_3}^2 + A_t^2) \ln(\Lambda/m_{SUSY})$$

$$\Delta_{HS} \sim \delta m_h^2 / (m_h^2/2) < 10$$

$$m_{\tilde{t}_{1,2}, \tilde{b}_1} < 500 \text{ GeV}$$

$$m_{\tilde{g}} < 1.5 \text{ TeV}$$

old natural SUSY

then

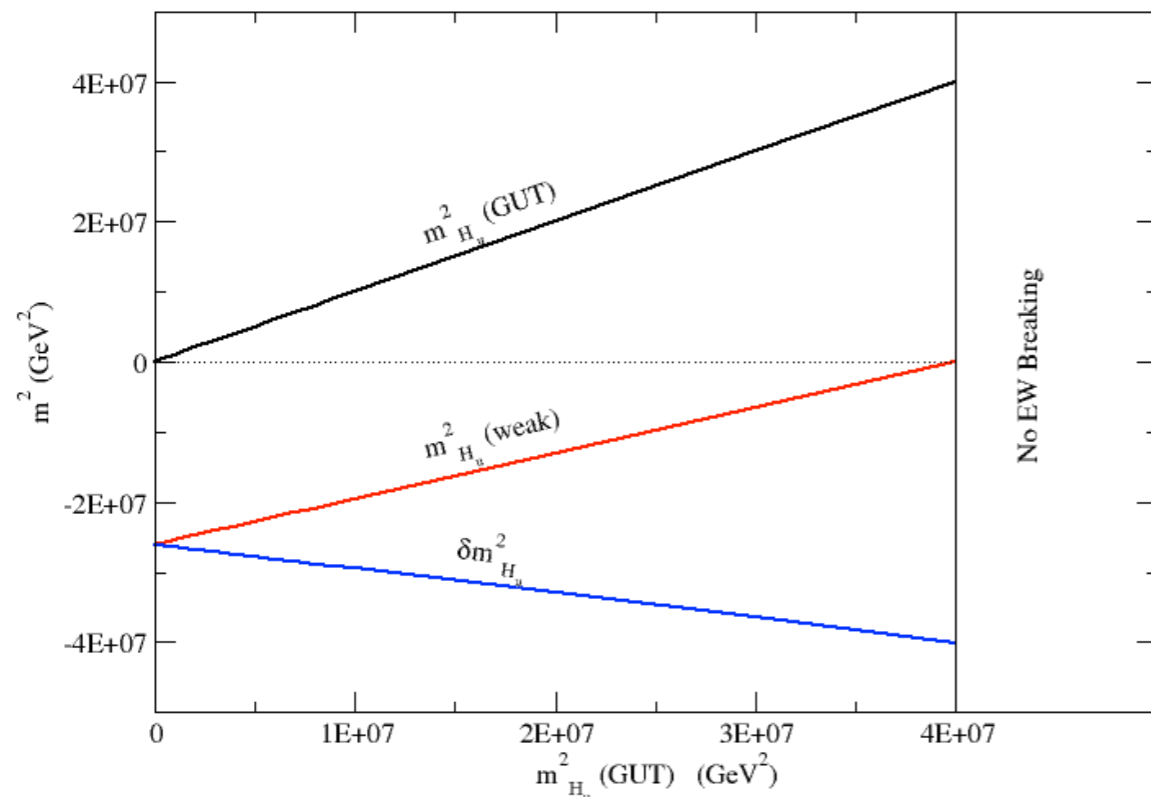
A_t can't be too big

What's wrong with this argument?

In zeal for simplicity, have made several simplifications: most **egregious** is that one sets $m(H_u)^2=0$ at beginning to simplify

$m_{H_u}^2(\Lambda)$ and $\delta m_{H_u}^2$ are *not* independent!

violates prime directive!



The larger $m_{H_u}^2(\Lambda)$ becomes, then the larger becomes the cancelling correction!

HB, Barger, Savoy

To fix: combine dependent terms:

$$m_h^2 \simeq \mu^2 + (m_{H_u}^2(\Lambda) + \delta m_{H_u}^2) \text{ where now both } \mu^2 \text{ and } (m_{H_u}^2(\Lambda) + \delta m_{H_u}^2) \text{ are } \sim m_Z^2$$

After re-grouping: $\Delta_{HS} \simeq \Delta_{EW}$

Instead of: the radiative correction $\delta m_{H_u}^2 \sim m_Z^2$
we now have: the radiatively-corrected $m_{H_u}^2 \sim m_Z^2$

Recommendation: put this horse out to pasture

$$\delta m_{H_u}^2 \sim -\frac{3f_t^2}{8\pi^2} (m_{Q_3}^2 + m_{U_3}^2 + A_t^2) \ln(\Lambda/m_{SUSY})$$

R.I.P.

sub-TeV 3rd generation squarks **not** required for naturalness

#3. What about EENZ/BG measure?

$$\Delta_{BG} = \max_i \left| \frac{\partial \log m_Z^2}{\partial \log p_i} \right| = \max_i \left| \frac{p_i}{m_Z^2} \frac{\partial m_Z^2}{\partial p_i} \right|$$

p_i are the theory parameters

applied to pMSSM, then $\Delta_{BG} \simeq \Delta_{EW}$

apply to high (e.g. GUT) scale parameters

$$\begin{aligned} m_Z^2 \simeq & -2.18\mu^2 + 3.84M_3^2 + 0.32M_3M_2 + 0.047M_1M_3 - 0.42M_2^2 \\ & + 0.011M_2M_1 - 0.012M_1^2 - 0.65M_3A_t - 0.15M_2A_t \\ & - 0.025M_1A_t + 0.22A_t^2 + 0.004M_3A_b \\ & - 1.27m_{H_u}^2 - 0.053m_{H_d}^2 \\ & + 0.73m_{Q_3}^2 + 0.57m_{U_3}^2 + 0.049m_{D_3}^2 - 0.052m_{L_3}^2 + 0.053m_{E_3}^2 \\ & + 0.051m_{Q_2}^2 - 0.11m_{U_2}^2 + 0.051m_{D_2}^2 - 0.052m_{L_2}^2 + 0.053m_{E_2}^2 \\ & + 0.051m_{Q_1}^2 - 0.11m_{U_1}^2 + 0.051m_{D_1}^2 - 0.052m_{L_1}^2 + 0.053m_{E_1}^2, \end{aligned}$$

applied to most parameters,

Δ_{BG} large, looks fine-tuned for e.g. $m_{\tilde{t}_1} \sim 1$ TeV

$$\Delta_{BG}(Q_3) \simeq 0.73 \frac{1000^2}{91.2^2} \sim 100$$

#3. What about EENZ/BG measure?

$$\Delta_{BG} = \max_i \left| \frac{\partial \log m_Z^2}{\partial \log p_i} \right| = \max_i \left| \frac{p_i}{m_Z^2} \frac{\partial m_Z^2}{\partial p_i} \right|$$

applied to pMSSM, then $\Delta_{BG} \simeq \Delta_{EW}$

What if we apply to high (e.g. GUT) scale parameters ?

$$\begin{aligned} m_Z^2 \simeq & -2.18\mu^2 + 3.84M_3^2 + 0.32M_3M_2 + 0.047M_1M_3 - 0.42M_2^2 \\ & + 0.011M_2M_1 - 0.012M_1^2 - 0.65M_3A_t - 0.15M_2A_t \\ & - 0.025M_1A_t + 0.22A_t^2 + 0.004M_3A_b \\ & - 1.27m_{H_u}^2 - 0.053m_{H_d}^2 \\ & \hline & + 0.73m_{Q_3}^2 + 0.57m_{U_3}^2 + 0.049m_{D_3}^2 - 0.052m_{L_3}^2 + 0.053m_{E_3}^2 \\ & \hline & + 0.051m_{Q_2}^2 - 0.11m_{U_2}^2 + 0.051m_{D_2}^2 - 0.052m_{L_2}^2 + 0.053m_{E_2}^2 \\ & \hline & + 0.051m_{Q_1}^2 - 0.11m_{U_1}^2 + 0.051m_{D_1}^2 - 0.052m_{L_1}^2 + 0.053m_{E_1}^2, \end{aligned}$$

For correlated scalar masses $\equiv m_0$,
scalar contribution collapses:

what looks fine-tuned isn't: *focus point SUSY*
multi-TeV scalars are *natural*

Feng, Matchev, Moroi

Even with FP, still
fine-tuned on $m(\text{gluino})$:(

But wait! in more complete models,
soft terms **not independent**

violates prime directive!

e.g. in SUGRA, for well-specified hidden sector,
each soft term calculated as multiple of $m_{3/2}$;
soft terms must be combined!

e.g. dilaton-dominated SUSY breaking: $m_0^2 = m_{3/2}^2$ with $m_{1/2} = -A_0 = \sqrt{3}m_{3/2}$

in general:

$$\begin{aligned} m_{H_u}^2 &= a_{H_u} \cdot m_{3/2}^2, \\ m_{Q_3}^2 &= a_{Q_3} \cdot m_{3/2}^2, \\ A_t &= a_{A_t} \cdot m_{3/2}, \\ M_i &= a_i \cdot m_{3/2}, \\ &\dots \end{aligned}$$

since μ hardly runs, then

$$\begin{aligned} m_Z^2 &\simeq -2\mu^2 + a \cdot m_{3/2}^2 \\ &\simeq -2\mu^2 - 2m_{H_u}^2 (weak) \end{aligned}$$

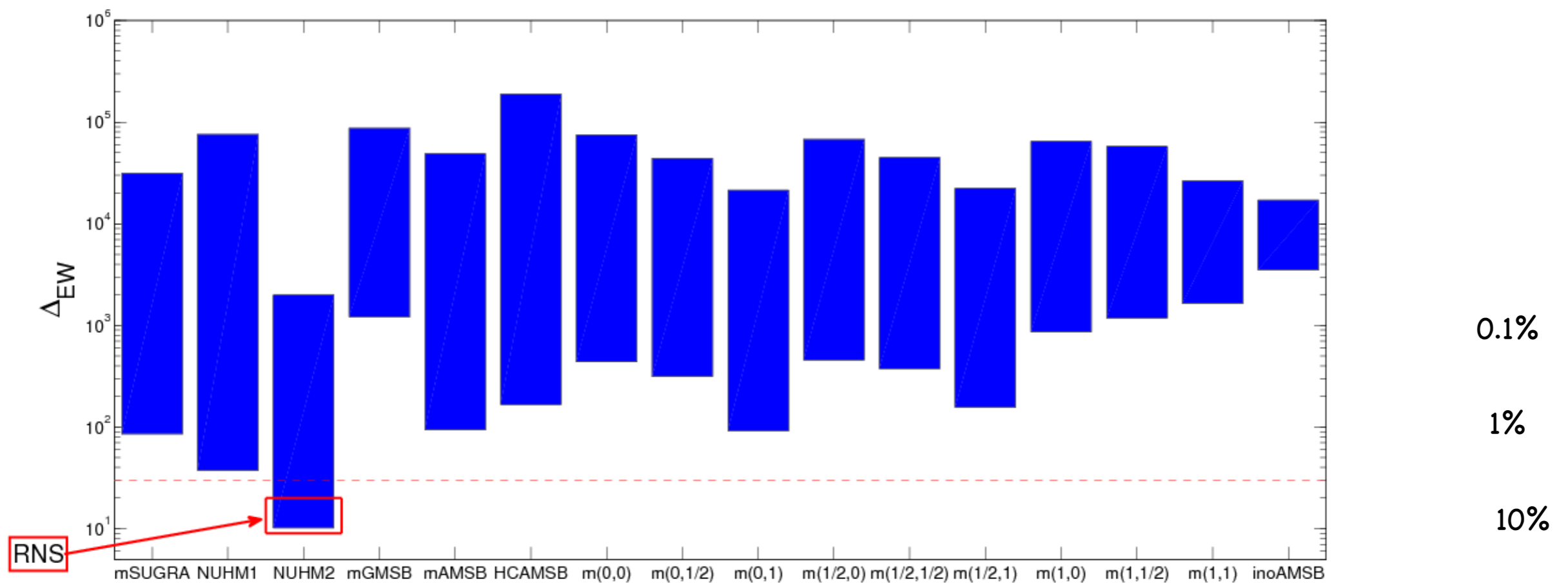
$$m_{H_u}^2 (weak) \sim -(100 - 200)^2 \text{ GeV}^2 \sim -a \cdot m_{3/2}^2/2$$

using μ^2 and $m_{3/2}^2$ as fundamental,
then $\Delta_{BG} \simeq \Delta_{EW}$ even using high scale parameters!

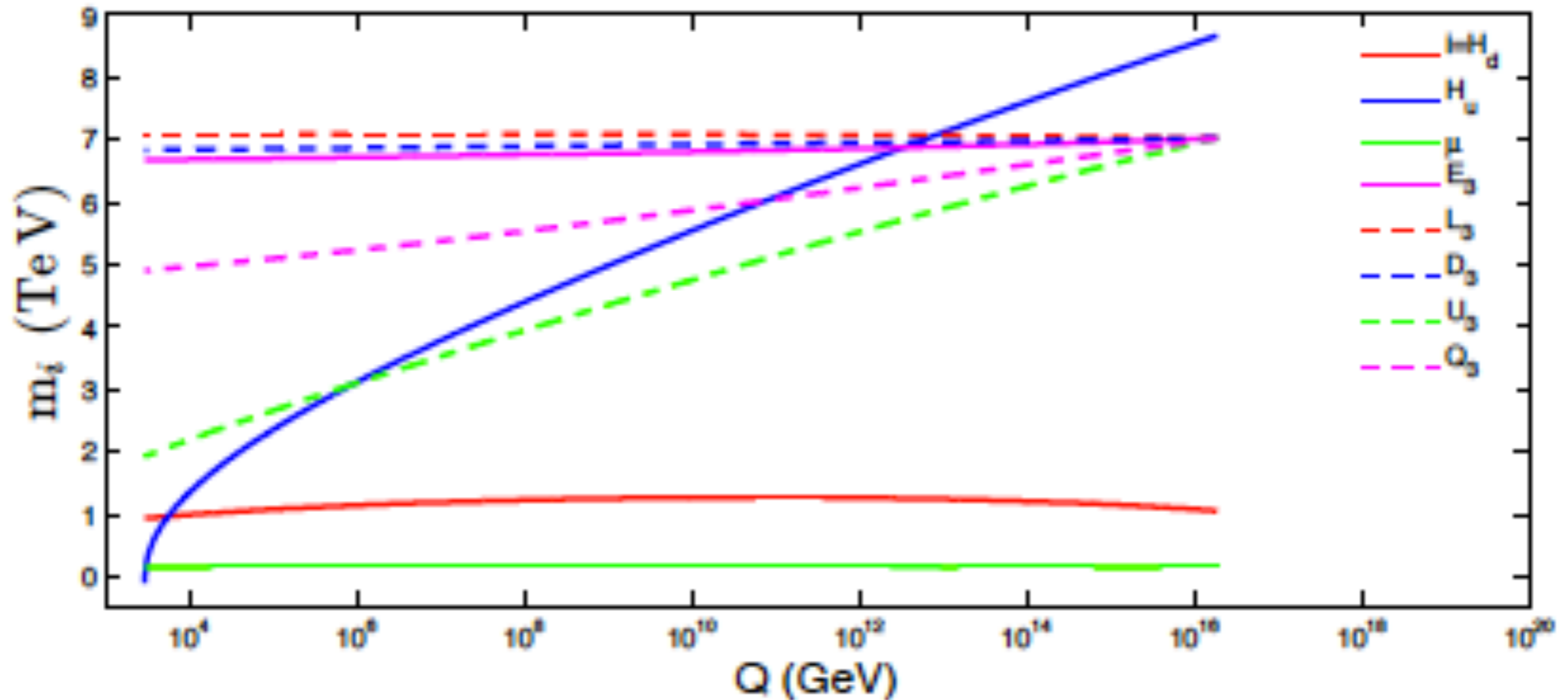
Δ_{EW} is highly selective:
 most constrained models are ruled out
 except NUHM2 and its generalizations:

J. Ellis, K. Olive and Y. Santoso, *Phys. Lett. B* 539 (2002) 107; J. Ellis, T. Falk, K. Olive and Y. Santoso, *Nucl. Phys. B* 652 (2003) 259; H. Baer, A. Mustafayev, S. Profumo, A. Belyaev and X. Tata, *J. High Energy Phys.* 0507 (2005) 065.

scan over p-space with $m(h)=125.5\pm 2.5$ GeV:



Applied properly, all three measures agree:
 naturalness is unambiguous and highly predictive!



Radiatively-driven natural SUSY, or RNS:

(typically need $m_{H_u} \sim 25\text{-}50\%$ higher than m_0)

H. Baer, V. Barger, P. Huang, A. Mustafayev and X. Tata, *Phys. Rev. Lett.* **109** (2012) 161802.

H. Baer, V. Barger, P. Huang, D. Mickelson, A. Mustafayev and X. Tata, *Phys. Rev. D* **87** (2013) 115028 [arXiv:1212.2655 [hep-ph]].

Axion cosmology

★ Axion field eq'n of motion: $\theta = a(x)/f_a$

$$- \ddot{\theta} + 3H(T)\dot{\theta} + \frac{1}{f_a^2} \frac{\partial V(\theta)}{\partial \theta} = 0$$

$$- V(\theta) = m_a^2(T) f_a^2 (1 - \cos \theta)$$

– Solution for T large, $m_a(T) \sim 0$:

$$\theta = \text{const.}$$

– $m_a(T)$ turn-on ~ 1 GeV

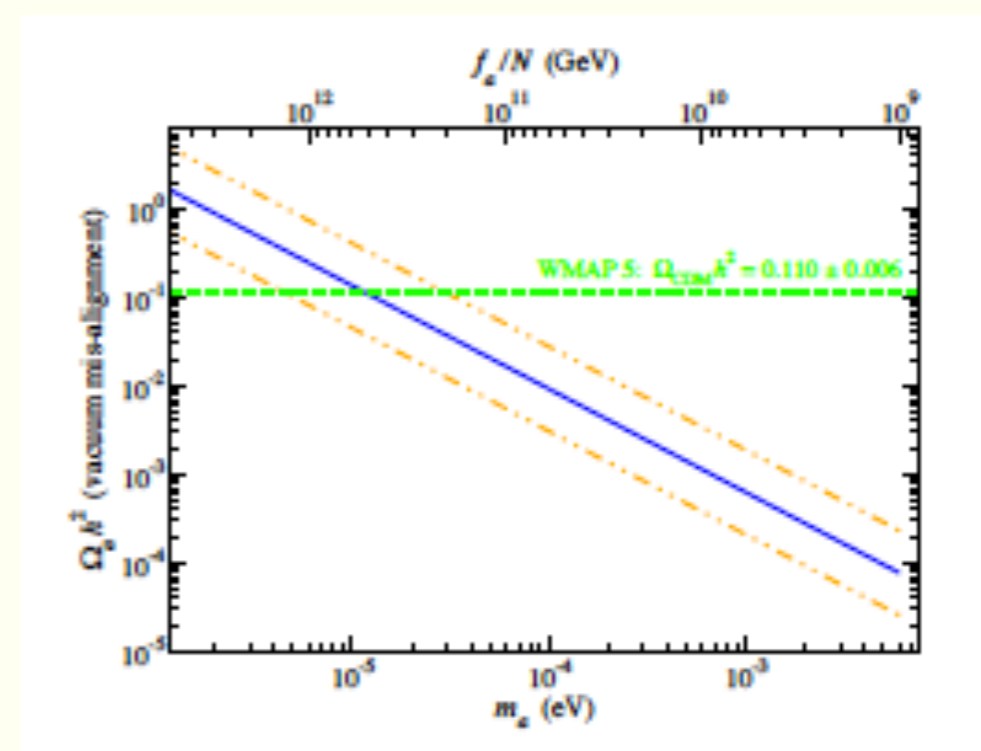
★ $a(x)$ oscillates,

creates axions with $\vec{p} \sim 0$:

production via vacuum mis-alignment

$$\star \Omega_a h^2 \sim \frac{1}{2} \left[\frac{6 \times 10^{-6} \text{ eV}}{m_a} \right]^{7/6} \theta_i^2 h^2$$

★ astro bound: stellar cooling $\Rightarrow f_a \gtrsim 10^9 \text{ GeV}$



Why might $\mu \ll m(\text{soft})$?

SUSY μ problem: μ term is SUSY, not SUSY breaking:
expect $\mu \sim M(\text{Pl})$ but phenomenology requires $\mu \sim m(\text{Z})$

- NMSSM: $\mu \sim m(\text{soft})$; but beware singlets!
- Giudice–Masiero: μ forbidden by some symmetry: generate via Higgs coupling to hidden sector: $\mu \sim m(\text{soft})$
- **Kim–Nilles**: invoke SUSY version of DFSZ axion solution to strong CP:

KN: PQ symmetry forbids μ term,
but then it is generated via PQ breaking

$$\mu \sim \lambda_\mu f_a^2 / m_P$$

Little Hierarchy due to mismatch between
PQ breaking and SUSY breaking scales?

$$m(\text{soft}) \sim m_{3/2} \sim m_{\text{hidden}}^2 / m_P$$

$$f_a < m_{\text{hidden}} \Rightarrow \\ \mu \ll m(\text{soft})$$

Higgs mass $m(h) \sim \mu$
tells us where to look for axion!

$$m_a \sim 6.2 \mu\text{eV} \left(\frac{10^{12} \text{ GeV}}{f_a} \right)$$

Gravity safe, electroweak natural axionic solution to strong CP and SUSY μ problems

HB, Barger, Sengupta, arXiv:1810.03713

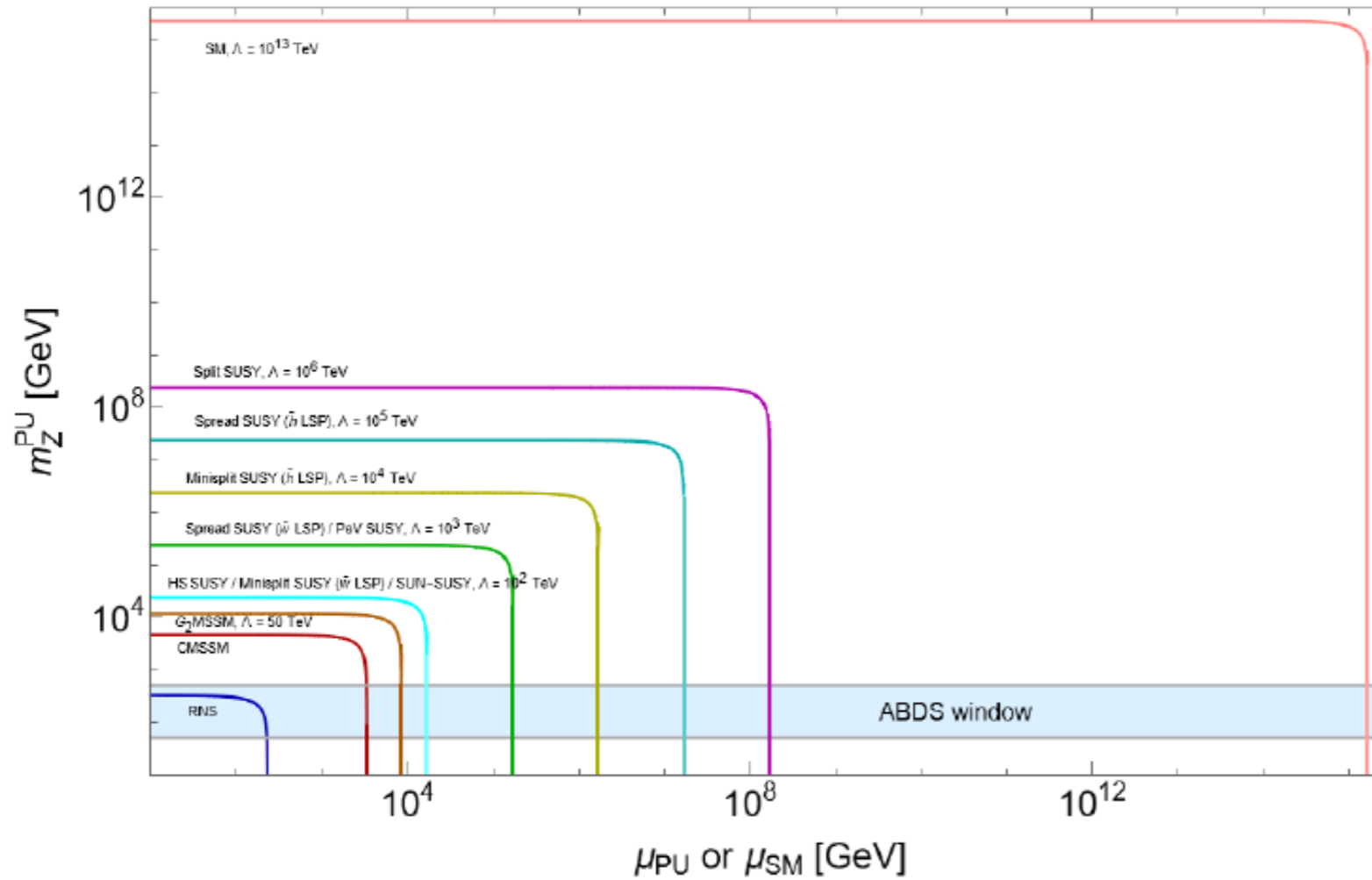
1. Global symmetries fundamentally incompatible with gravity completion
2. Expect global symmetry to emerge as accidental (approximate) symmetry from some more fundamental gravity-safe (e.g. gauge or R-) symmetry
3. Krauss-Wilczek: gauge symmetry with charge N object condensing leaves charge e fields with Z_N discrete gauge symmetry
4. Babu et al.: Z_{22} symmetry works but charge 22 object in swampland?
5. **Better choice: discrete R-symmetries which arise from compactification of extra dimensions in string theory**

A model which works: $Z(24)$ R symmetry (see also Lee et al.)

$$W \ni f_u Q H_u U^c + f_d Q H_d D^c + f_\ell L H_d E^c + f_\nu L H_u N^c + M_N N^c N^c / 2 + \lambda_\mu X^2 H_u H_d / m_P + f X^3 Y / m_P + \lambda_3 X^p Y^q / m_P^{p+q-3}$$

- Lowest dimension PQ breaking operator contributing to scalar PQ potential $\sim 1/m_P^8$: enough suppression so that PQ is gravity-safe
- Also forbids/suppresses RPV/p-decay operators
- $\mu \sim \lambda_\mu f_a^2 / m_P$

Are finetuned or natural models preferred by landscape?



It is sometimes claimed that the landscape provides an alternative to naturalness; we find, all things being equal, this is not so: finetuned models have a tiny p-space for sampling on the landscape compared to natural models

model	$\tilde{m}(1, 2)$	$\tilde{m}(3)$	gauginos	higgsinos	m_h	P_μ
SM	-	-	-	-	-	$7 \cdot 10^{-27}$
CMSSM ($\Delta_{EW} = 2641$)	~ 1	~ 1	~ 1	~ 1	0.1 – 0.13	$5 \cdot 10^{-3}$
PeV SUSY	$\sim 10^3$	$\sim 10^3$	~ 1	$1 - 10^3$	0.125 – 0.155	$5 \cdot 10^{-6}$
Split SUSY	$\sim 10^6$	$\sim 10^6$	~ 1	~ 1	0.13 – 0.155	$7 \cdot 10^{-12}$
HS-SUSY	$\gtrsim 10^2$	$\gtrsim 10^2$	$\gtrsim 10^2$	$\gtrsim 10^2$	0.125 – 0.16	$6 \cdot 10^{-4}$
Spread (\tilde{h} LSP)	10^5	10^5	10^2	~ 1	0.125 – 0.15	$9 \cdot 10^{-10}$
Spread (\tilde{w} LSP)	10^3	10^3	~ 1	$\sim 10^2$	0.125 – 0.14	$5 \cdot 10^{-6}$
Mini-Split (\tilde{h} LSP)	$\sim 10^4$	$\sim 10^4$	$\sim 10^2$	~ 1	0.125 – 0.14	$8 \cdot 10^{-8}$
Mini-Split (\tilde{w} LSP)	$\sim 10^2$	$\sim 10^2$	~ 1	$\sim 10^2$	0.11 – 0.13	$4 \cdot 10^{-4}$
SUN-SUSY	$\sim 10^2$	$\sim 10^2$	~ 1	$\sim 10^2$	0.125	$4 \cdot 10^{-4}$
G ₂ MSSM	30 – 100	30 – 100	~ 1	~ 1	0.11 – 0.13	$2 \cdot 10^{-3}$
RNS/landscape	5 – 40	0.5 – 3	~ 1	0.1 – 0.35	0.123 – 0.126	1.4

Table 1: A survey of some unnatural and natural SUSY models along with general expectations for sparticle and Higgs mass spectra in TeV units. We also show relative probability measure P_μ for the model to emerge from the landscape. For RNS, we take $\mu_{min} = 10$ GeV.

HB, Barger,
Martinez, Salam