

# QCD and top phenomena at future colliders

Stefan Kluth

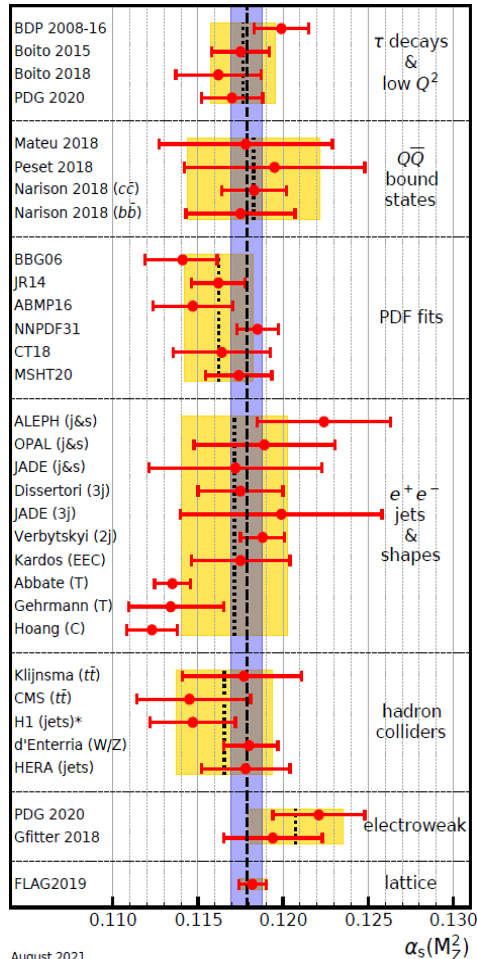
MPI für Physik, München

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25.04.23

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- 3 Z and W decays
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- 5 Jets and event shapes
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# 1 Introduction



**FCC-ee**

**FCC-ee**

**FCC-eh**  
**LHeC**

**FCC-ee**

**FCC-hh**

**FCC-ee**

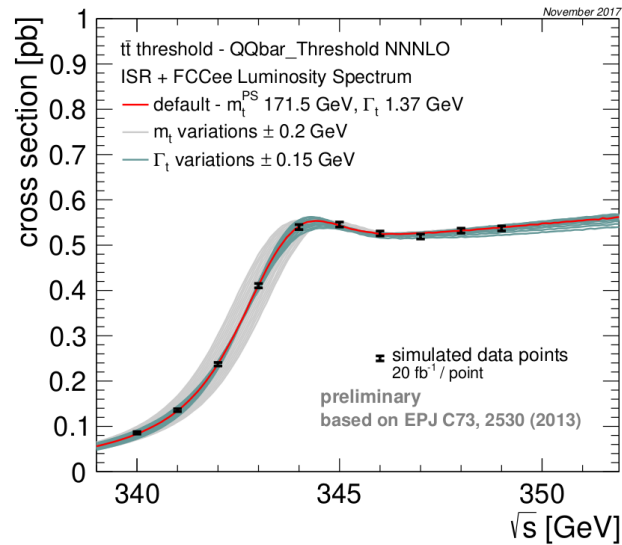
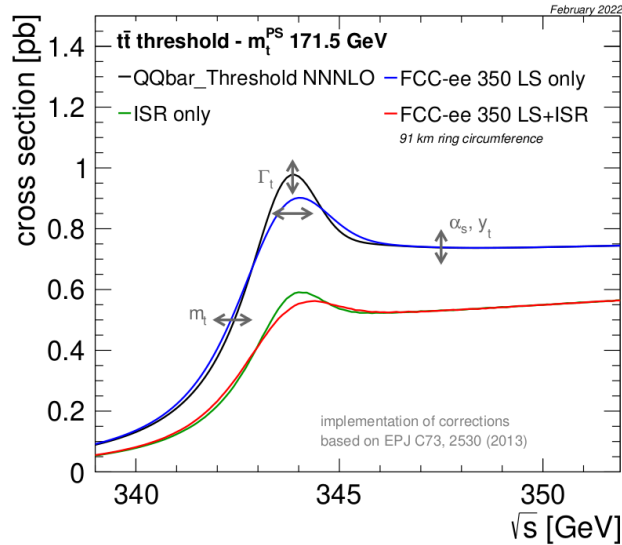
Summary from “ $\alpha_s$  (2022) – Precision measurements of the QCD coupling” at ECT\* (Trento) 31.01.-04.02.2022

FCC-ee impact on most categories  
Expect  $3 \cdot 10^{12}$  hadronic Z decays  $\Rightarrow$   
 $6 \cdot 10^{11}$   $Z \rightarrow b\bar{b}$ ,  $10^{11}$   $\tau$  pairs, ...  
 $5 \cdot 10^8$  W decays,  $10^6$   $t\bar{t}$  on threshold

FCC-hh, FCC-eh (LHeC)

# 2 Top quark properties in $e^+e^-$

Threshold scan:  $\sim 10^6$   $t\bar{t}$  events, ultimate measurement of  $m_t$  and  $\Gamma_t$



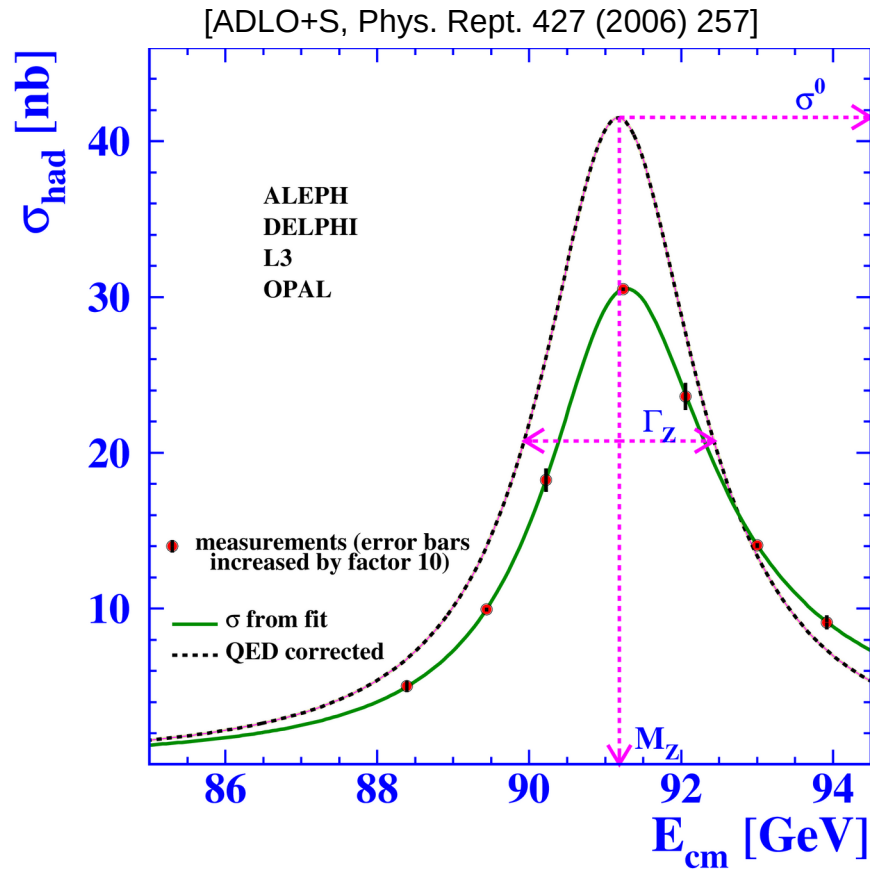
[FCC coll., Eur. Phys. J. C79 (2019) 474, arxiv: 2209.11267]

$$m_t = ( 171.5 \pm 0.017_{\text{stat}} \pm 0.007_{\text{cms}} \pm 0.005_{\alpha_S} \pm 0.040_{\text{theo}} ) \text{ GeV}$$

$$\Gamma_t = ( 1.37 \pm 0.045_{\text{stat}} \pm 0.003_{\text{cms}} \pm 0.005_{\alpha_S} \pm 0.040_{\text{theo}} ) \text{ GeV}$$

$\Delta\alpha_s(m_Z) \approx 0.0002$  needed, unambiguous theo. definition of  $m_t$

# 3 Z and W decays in $e^+e^-$



SM prediction:  $R_I^{Z,W} = \Gamma_{\text{had}}^{Z,W} / \Gamma_{\text{lep}}^{Z,W} = R_{EW} ( 1 + \sum a_i (\alpha_s(Q)/\pi)^i + \delta_{EW} + \delta_{\text{mix}} + \delta_{\text{np}} )$

N3LO QCD, 2-loop EW corrections

$\Gamma_{\text{had}}, \Gamma_{\text{lep}}, \dots$  (EWPO) mod.ind. fits

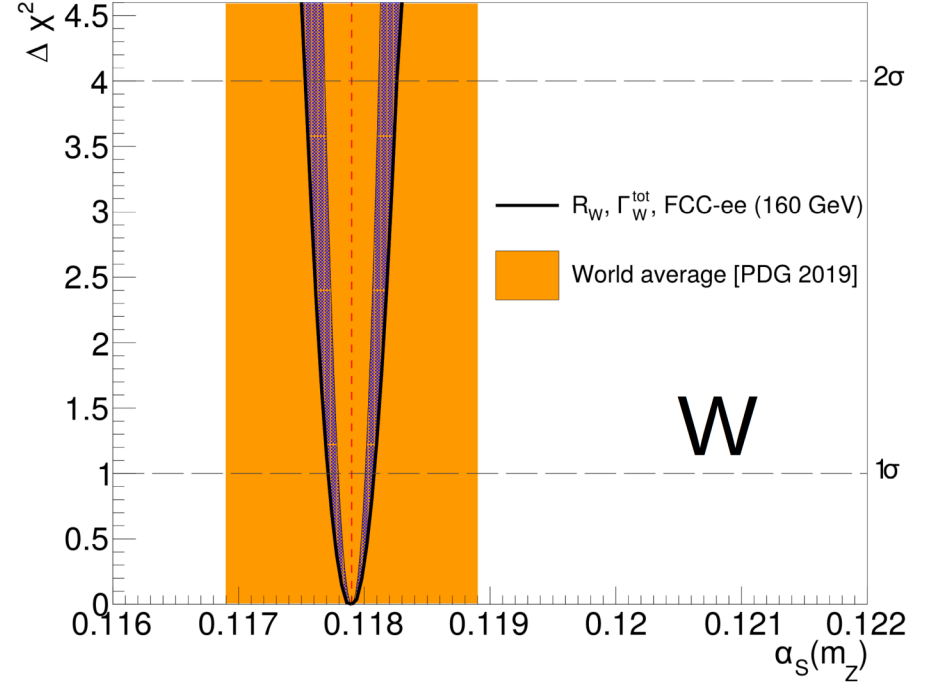
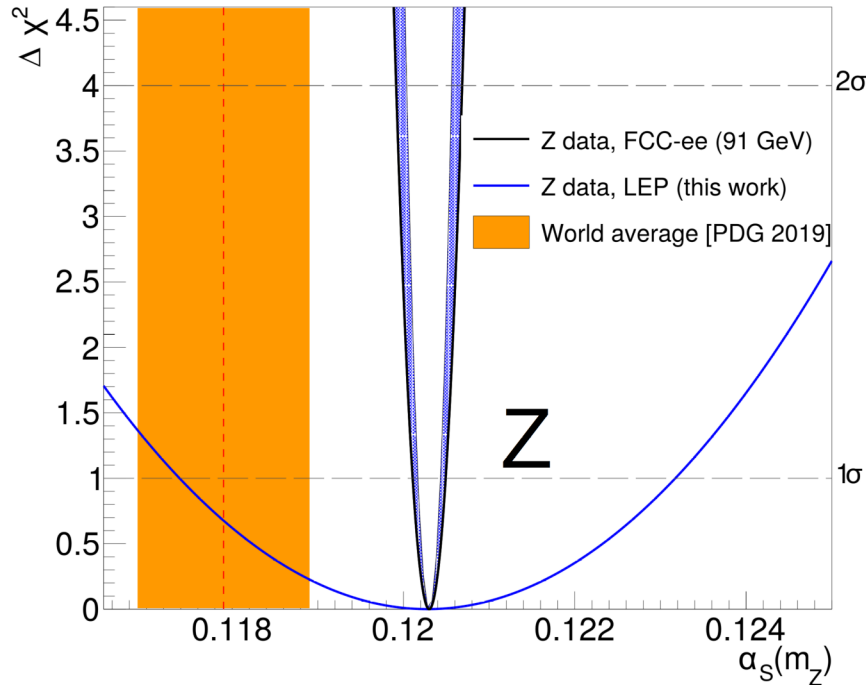
LEP:

Z:  $\alpha_s(m_Z) = 0.120 \pm 0.003_{\text{exp}} \pm 0.001_{\text{theo}}$

W:  $\alpha_s(m_Z) = 0.107 \pm 0.035_{\text{exp}} \pm 0.002_{\text{theo}}$

[D. d'Enterria, in arxiv: 2203.08271]

# 3 Z and W decays



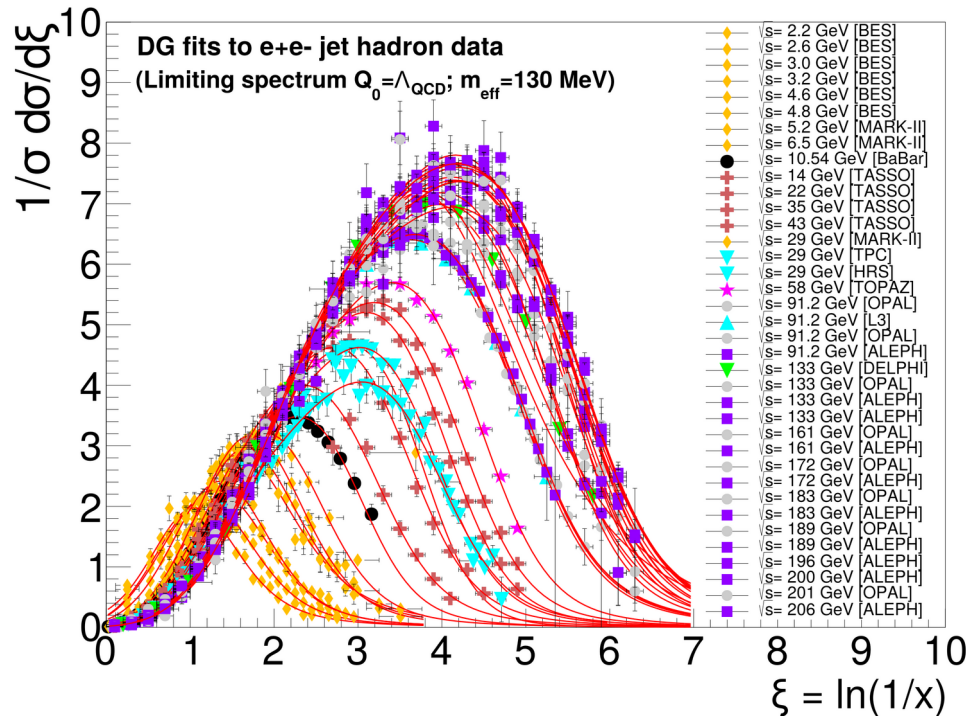
FCC-ee: improved  $\alpha_{\text{QED}}$ ,  $|V_{cs}|$ ,  $|V_{cd}|$ ,  $m_W$ ; assume N4LO QCD

Z:  $\alpha_s(m_Z) = 0.12020 \pm 0.00013_{\text{exp}} \pm 0.00005_{\text{par}} \pm 0.00022_{\text{theo}}$

W:  $\alpha_s(m_Z) = 0.11790 \pm 0.00012_{\text{exp}} \pm 0.00004_{\text{par}} \pm 0.00019_{\text{theo}}$

[D. d'Enterria, in arxiv: 2203.08271]

# 4 Soft FFs in $e^+e^-$



Charged hadrons momentum spectra  $x = 2E_h/\sqrt{s}$

FF:  $D_{a,h}(z, Q)$ ,  $z = p_h/p_a$ ,  $Q = \sqrt{s}$

Distorted Gaussian model:

$D \approx C(\alpha_s(t)) \exp(\int^t \gamma(\alpha_s(t')) dt')$

$t = \ln(Q)$ , NNLO\*+NNLL evolution of  $\gamma(\alpha_s(t'))$

$\alpha_s(m_Z) = 0.121 \pm 0.001_{\text{exp}} \pm 0.002_{\text{theo}}$

FCC-ee:  $\Delta\alpha_{S,\text{exp}} < 0.1\%$ , full NNLO+NNLL  $\Rightarrow \Delta\alpha_{S,\text{theo}} \leq 0.001?$

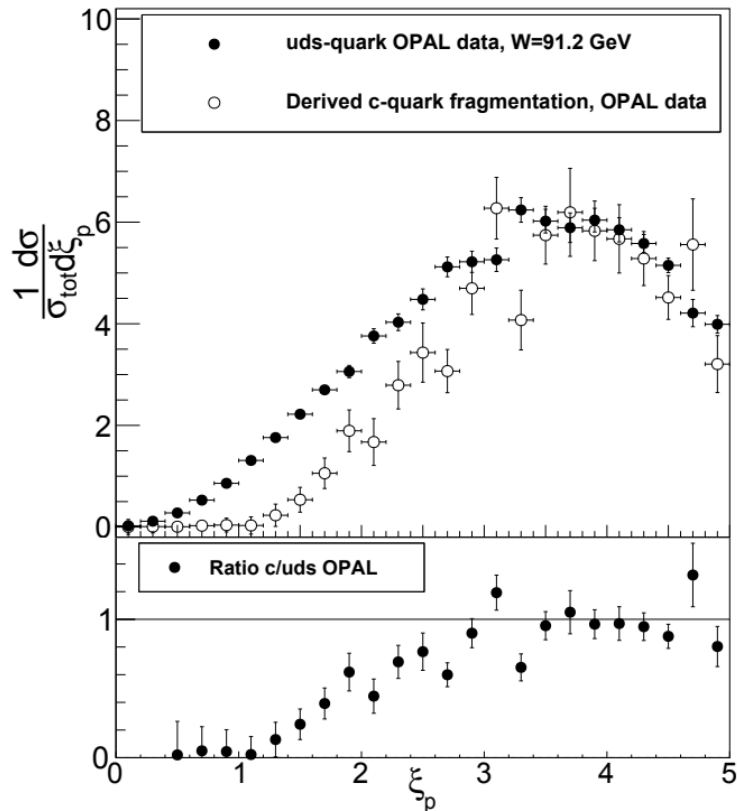
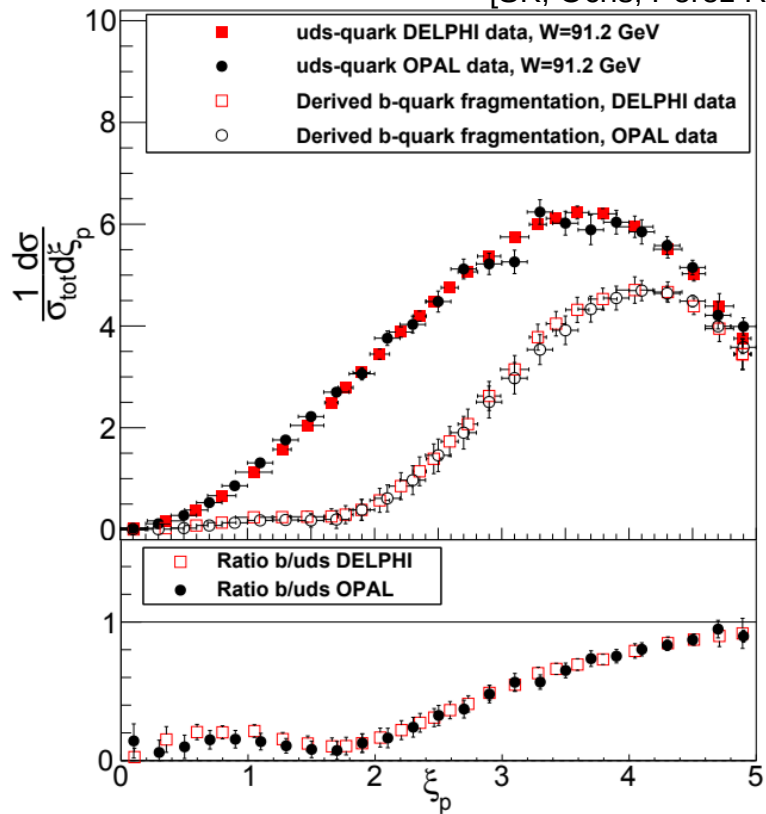
With c, b, (t) tags: study heavy quark fragmentation

[R. Perez-Ramos, D. d'Enterria, arxiv: 2203.08271]

# 4 Soft FFs in $e^+e^-$

Heavy quark  $Q$  fragmentation: dead cone effect

[SK, Ochs, Perez Ramos, arxiv: 2303.13343]

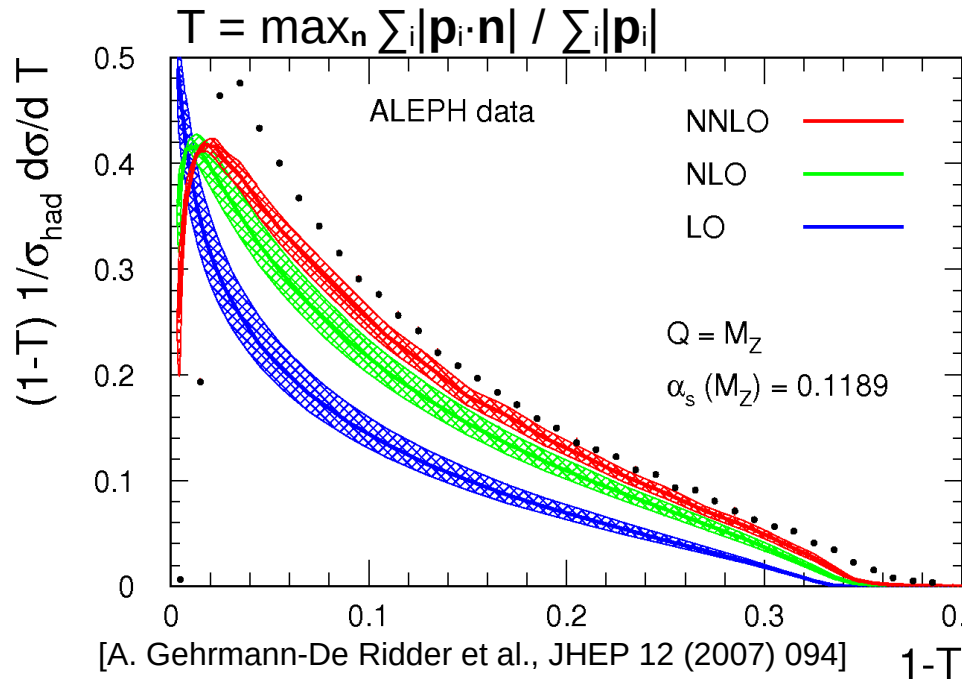


Frag'n of  $Q$  with  $v_Q/c < 1$  different from light  $q$

$Q$  jet modelling  
 $Q$  tagging

Future  $e^+e^-$ :  
Reduced stat.  
and exp. errors

# 5 Jets and event shapes in $e^+e^-$



$$1/\sigma d\sigma/dy = dA/dy \alpha_s(Q) + dC/dy \alpha_s(Q)^2 + dC/dy \alpha_s(Q)^3 + \text{h.o.} + \text{scale} + \sigma_{0 \rightarrow \text{tot}}$$

NNLO QCD (+resum.) needs np (hadronisation) corr.  $\sim 1/Q$

MC-based vs analytic models

Same structure for other event shapes and for jet production rates

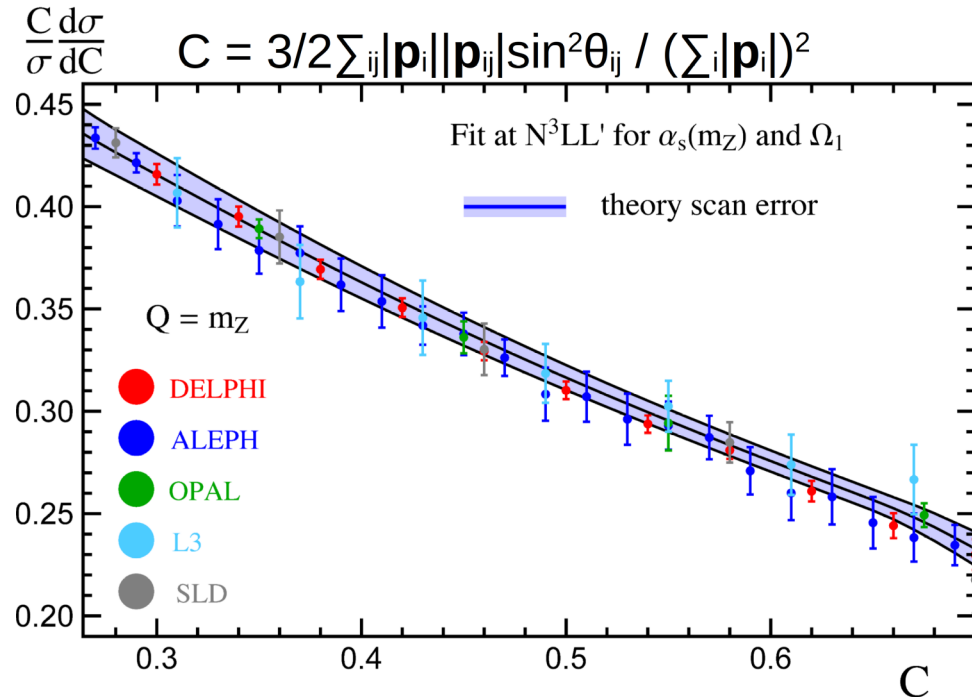
Typical differences MC vs analytic

$$\Delta \alpha_s(m_Z)_{\text{np-model}} = O(1\%)$$

[e.g. A. Hoang et al., Phys. Rev. D91 (2015) 9]



# 5 Jets and event shapes



Hadronisation unc. within  
Fitted SCET based model

Significant deviations from  
world average

$$\alpha_s(m_Z) = 0.1179 \pm 0.0009$$

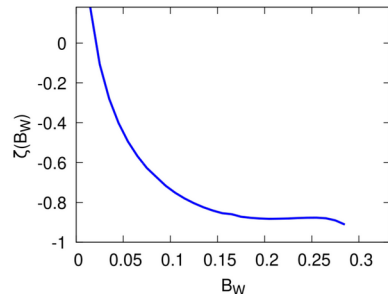
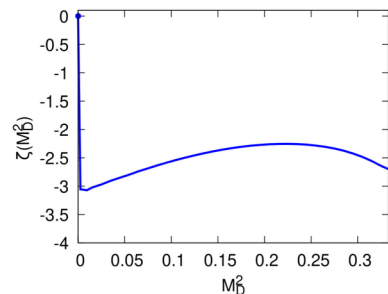
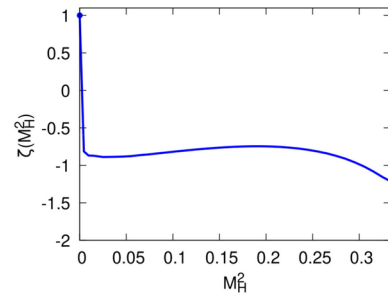
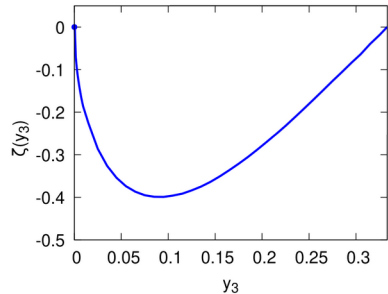
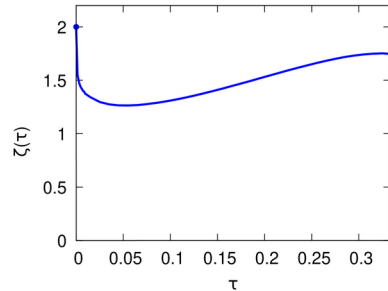
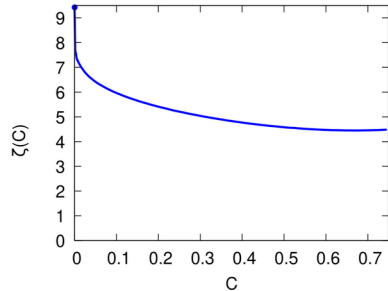
[A. Hoang et al., Phys. Rev. D91 (2015) 9]

NNLO + N3LL' (SCET), LEP/SLD/PETRA/TRISTAN data:

$$T: \alpha_s(m_Z) = 0.1134 \pm 0.0002_{\text{exp}} \pm 0.0005_{\text{had}} \pm 0.0011_{\text{theo}}$$

$$C: \alpha_s(m_Z) = 0.1123 \pm 0.0002_{\text{exp}} \pm 0.0007_{\text{had}} \pm 0.0014_{\text{theo}}$$

# 5 Jets and event shapes



Linear power corrections in large  $n_f$  limit in 3-jet region  $\Rightarrow$  constant shift of pert. prediction replaced by observable dependent shift  $\zeta(\cdot)$

significant  $\Delta\alpha_s(m_Z)$  w.r.t. const. shift

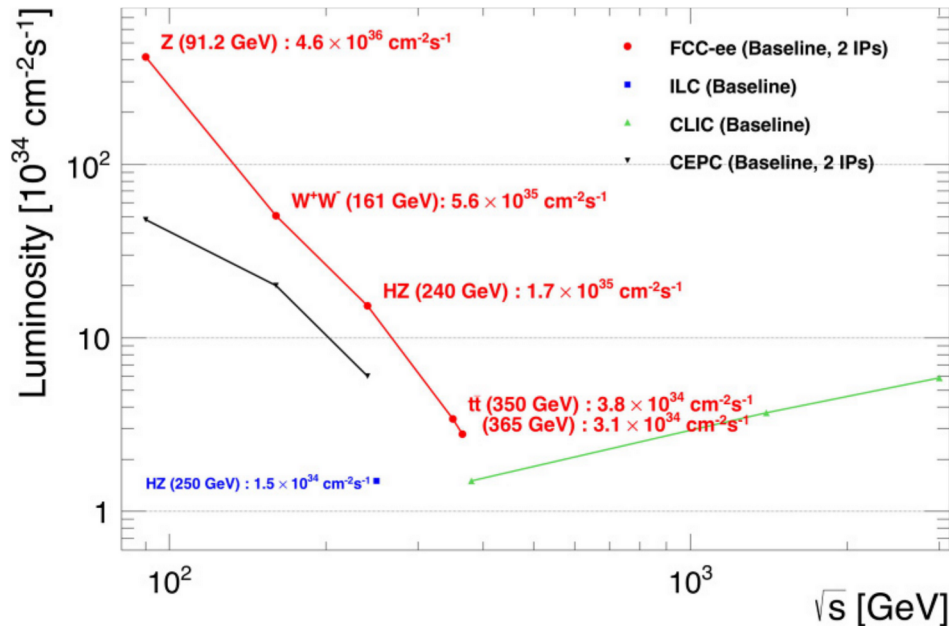
See also: new (groomed) observables, NLO+NLL-PS MCs [S. Marzani, D. Reichelt, S. Schumann, G. Soyez, arxiv: 2203.08271]

FCC-ee:  $\Delta\alpha_{S,\text{exp}} < 0.1\%$ ,  $\Delta\alpha_{S,\text{had}} < 1\%?$ ,  $\Delta\alpha_{S,\text{theo}} < 1\%?$ ,  $\Delta\alpha_{S,\text{hadron masses}} \approx 1\%?$

[P. Nason, G. Zanderighi, arxiv:2301.03607]

# 6 FCC-ee with $\sqrt{s} < m_Z$

Proposal for Snowmass 2021  
Collect  $10^9$  events with FCC-ee  
at  $\sqrt{s} = 20, 30, 40, \dots$  GeV



[A. Banfi et al., [www.snowmass21.org/docs/files/summaries/EF/SNOWMASS21-EF5\\_EF4\\_Andrii\\_Verbytskyi-208.pdf](http://www.snowmass21.org/docs/files/summaries/EF/SNOWMASS21-EF5_EF4_Andrii_Verbytskyi-208.pdf)]

Benefactors:

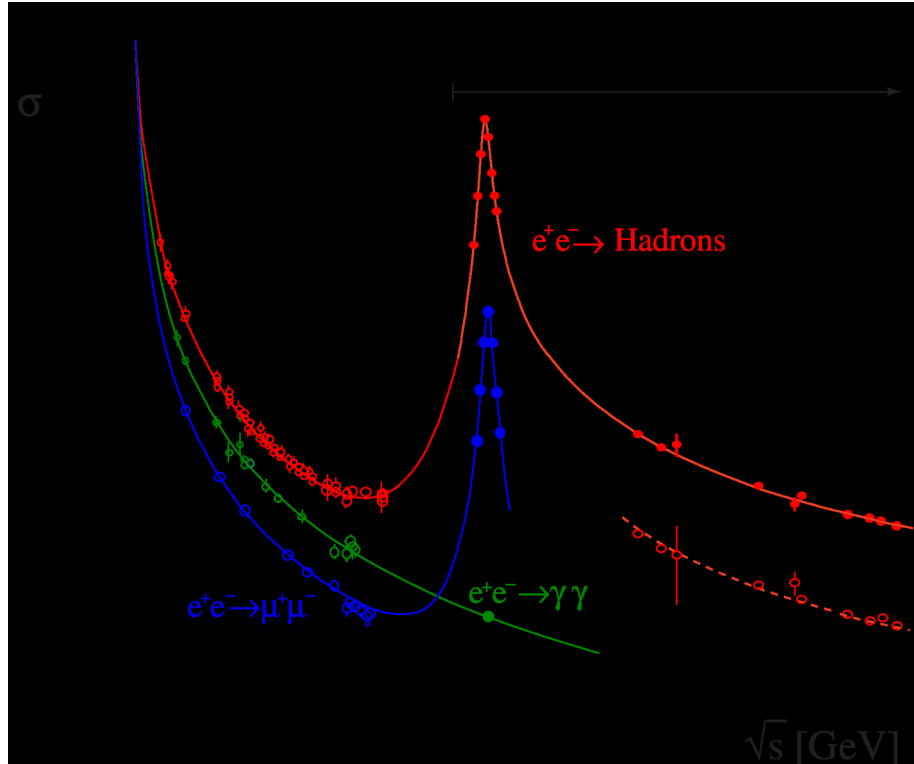
MC tuning and soft QCD ( $\rightarrow 1.3$ )  $\Rightarrow$  hadronisation systematics

$R_1^Y$  at high precision

FFs: scaling violation, long., transv., asym., soft FFs  $\xi = \ln(1/x)$ , ...

In-situ calibrations?, EW, etc pp

# 6 $R_1^Y$ at $\sqrt{s} < m_Z$ with FCC-ee



$$R_1^Y \text{ exp} = \sigma(e^+e^- \rightarrow \text{hadrons}) / \sigma(e^+e^- \rightarrow \mu^+\mu^-)$$

$$R_1^Y \text{ theo} = 3 \sum_i q_i (1 + \alpha_s/\pi + 1.441(\alpha_s/\pi)^2 + \dots)$$

[A.V. Nesterenko, in arxiv: 2203.08271]

$$\Delta R_1^Y / R_1^Y \approx \Delta \alpha_s \Rightarrow \Delta \alpha_{S, \text{stat}} \approx 0.0001 \text{ with}$$

$$\Delta R_1^Y / R_1^Y \approx 10^{-4} \Rightarrow O(10^8) \text{ events}$$

[FCC coll., Eur. Phys. J. C79 (2019) 474]

$$\Delta R_1^Z / R_1^Z \approx 5 \cdot 10^{-5} \text{ FCC-ee, dominated}$$

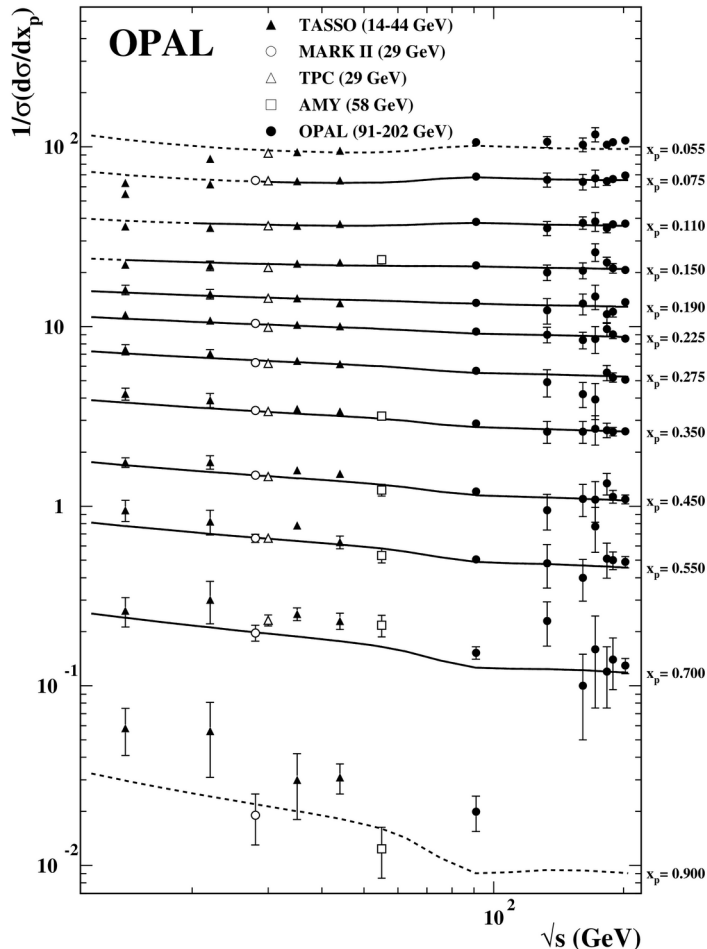
by lepton acceptance  $\Rightarrow$  similar for  $R_1^Y$

$$\Rightarrow \Delta \alpha_{S, \text{exp}} \approx 0.0001$$

Pure  $\gamma$  couplings, low scale  
 $\Rightarrow$  less BSM “pollution”

$$\Delta \alpha_{S, \text{theo}} \approx 0.0002 \text{ as for } R_1^{Z,W} (\rightarrow 1.2)$$

# 7 Scaling violation in hard FFs



Charged hadrons  $h$  with scaled momentum  $x = 2E_h/\sqrt{s}$  at various  $\sqrt{s} = Q$

$$1/\sigma d\sigma/dx = \int_0^1 \sum_f C_f(z, \alpha_s(Q)) D_f(x/z) dz/z$$

LEP (ADO) NLO DGLAP analyses:

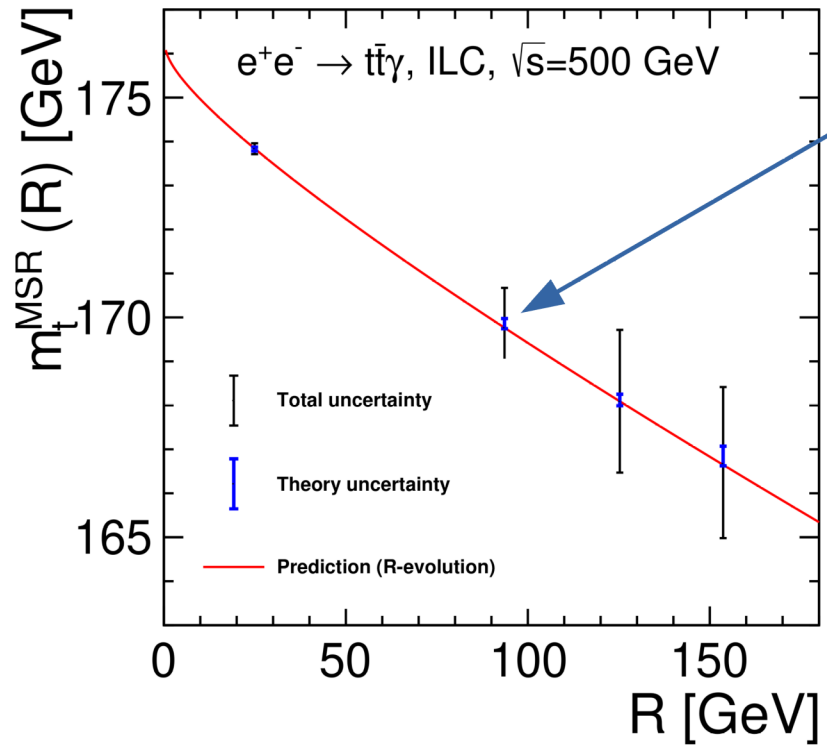
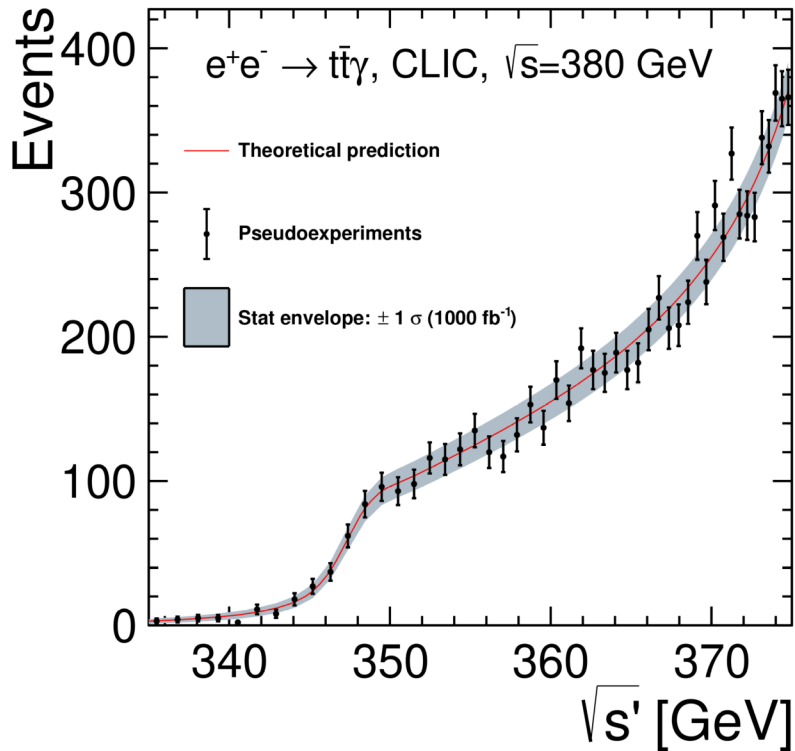
$$\alpha_s(m_Z) = 0.1192 \pm 0.0056_{\text{exp}} \pm 0.0070_{\text{theo}}$$

FCC-ee statistics and systematics  $\Rightarrow$  exp. unc.  $\Delta\alpha_{S,\text{exp}} < 1\%$  (or better?  $\sqrt{s} < m_Z$ ?)

Today NNLO DGLAP for proton pdfs  $\Rightarrow$  theo. unc.  $\Delta\alpha_{S,\text{theo}} \approx 0.001?$  (N3LO DGLAP?)

# 8 Quark mass running: top

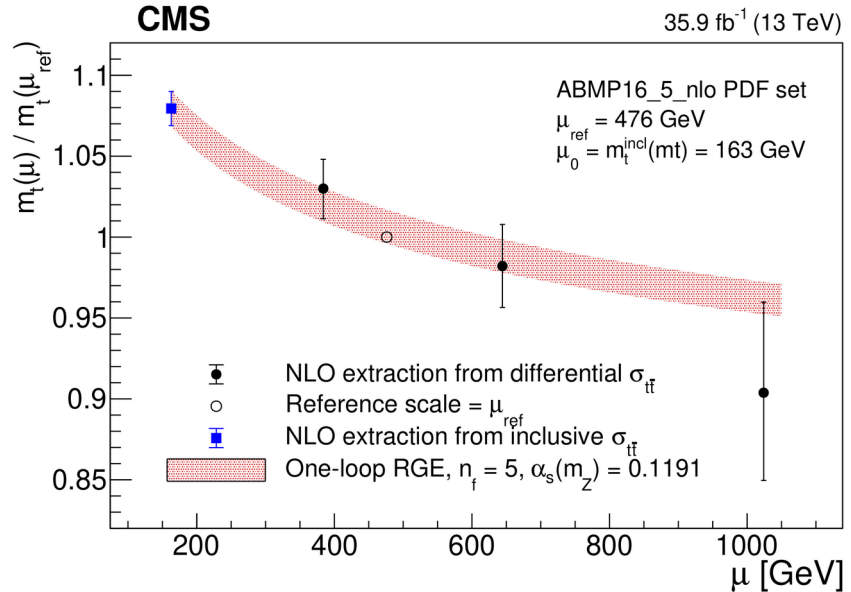
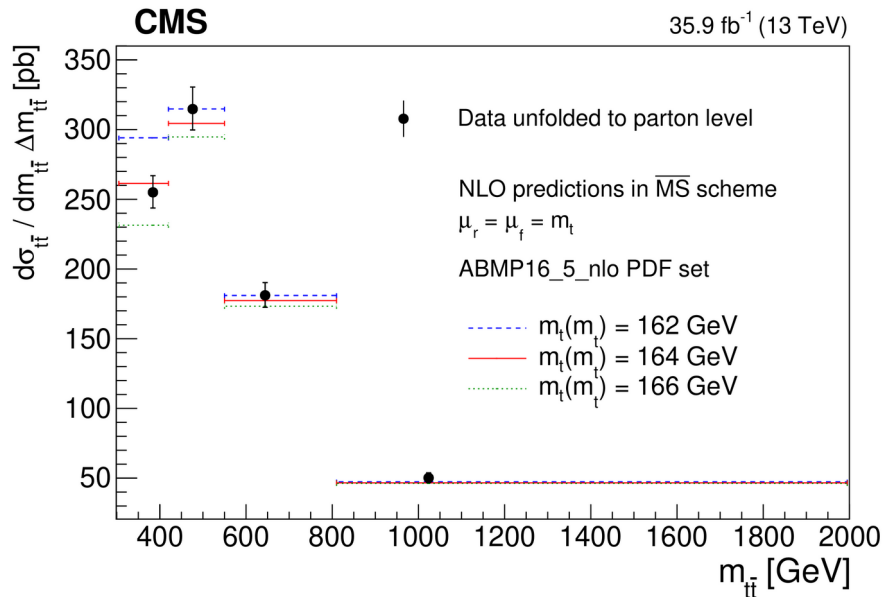
$e^+e^- \rightarrow t\bar{t}\gamma$  to access  $m_t(s')$  at production:  $s' = s(1-2E_\gamma/\sqrt{s})$



[M. Boronat et al, Phys. Lett. B804 (2020) 135353]

# 8 Quark mass running: top

Measure  $d\sigma/dm_{t\bar{t}}$  in pp collisions:  $m_{t\bar{t}}^2 = 2m_t^2 + 2(E_t E_{\bar{t}} - \mathbf{p}_t \cdot \mathbf{p}_{\bar{t}})$

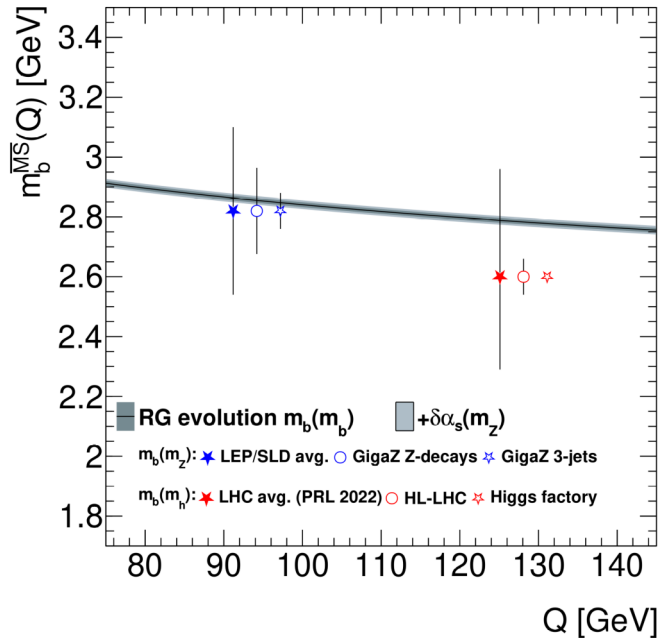
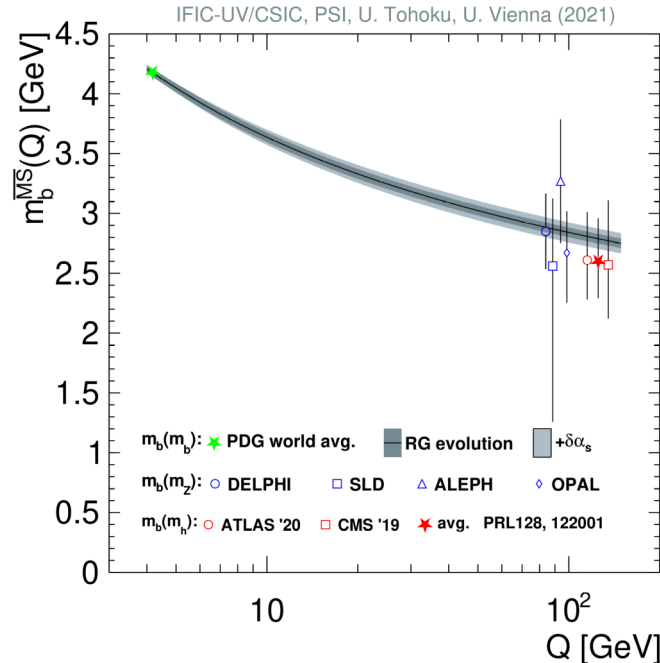


Expect much larger  $m_{t\bar{t}}$  reach with FCC-hh

[CMS, Phys. Lett. B803 (2020) 135263]

# 8 Quark mass running: b

$$e^+e^- \rightarrow Z \rightarrow b\bar{b} + \text{jet}, R_{0,b} = \Gamma_{Z \rightarrow b\bar{b}} / \Gamma_{Z \rightarrow \text{had}} \sim (m_b/m_Z)^2, \Gamma_{H \rightarrow b\bar{b}} / \Gamma_{H \rightarrow ZZ} \sim m_b^2$$



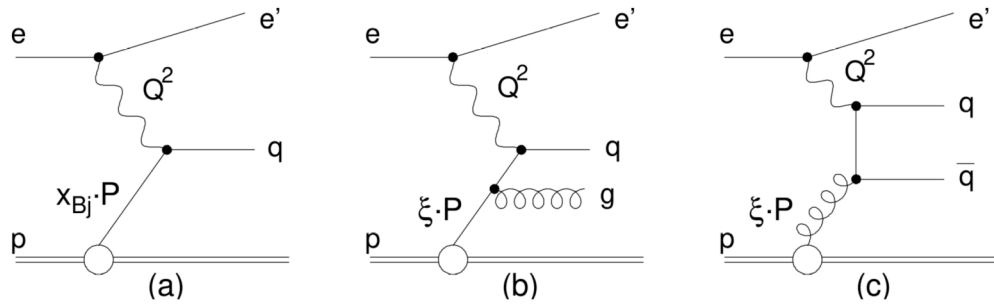
[J. Aparisi et al,  
arxiv: 2203.16994]

SM Yukawa  $y_b = m_b / (\sqrt{2}v_{\text{ev}}) \Rightarrow y_b$  or  $m_b$  from  $H \rightarrow b\bar{b}$

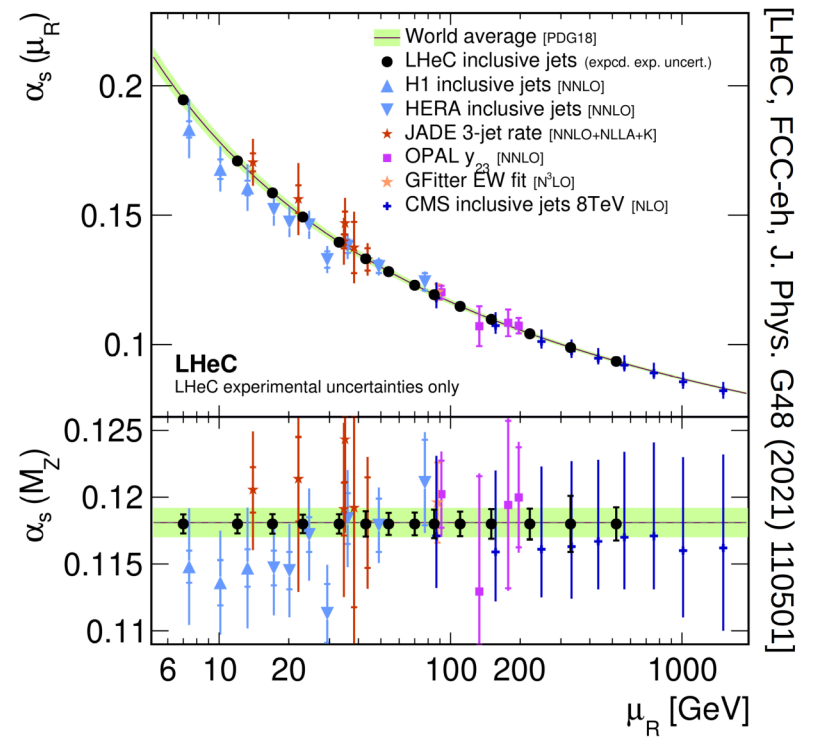
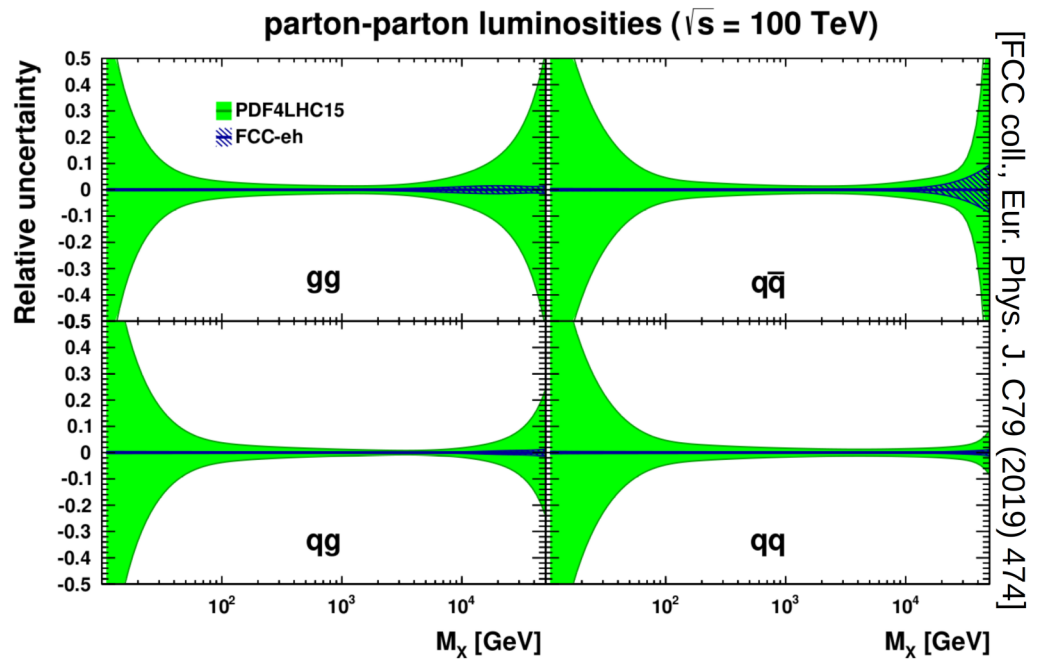
Extrapolation of “GigaZ 3-jets” needs NNLO for  $e^+e^- \rightarrow b\bar{b} + \text{jet}$



# 9 eP colliders: LHeC and FCC-eh



	$E_p$ [TeV]	$E_e$ [GeV]	$\sqrt{s}$ [TeV]
LHeC:	7	50/60	1.2/1.3
FCC-eh:	50	60	3.5



# 10 Di-jets in pp

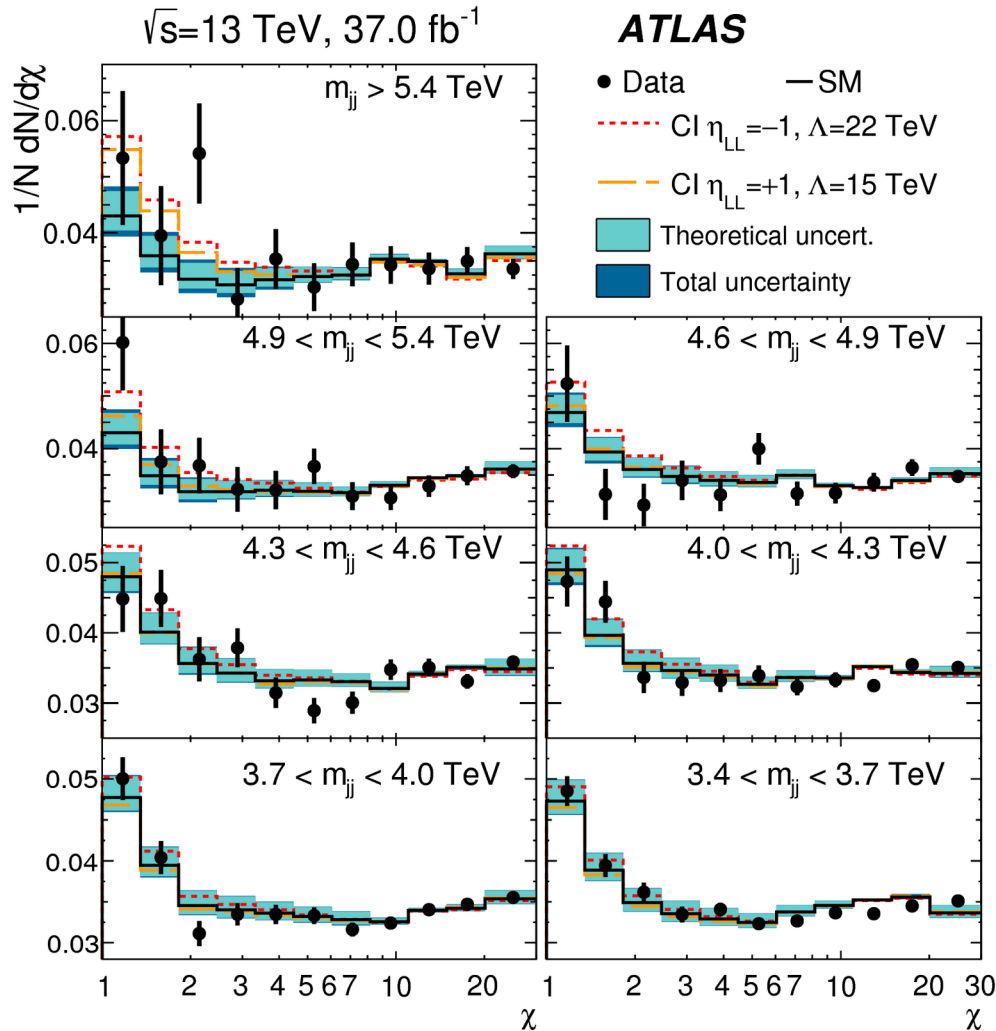
Anti- $k_t$  jets  $R=0.4$

$p_{t,jet1} > 440$  GeV,  $p_{t,jet2} > 60$  GeV

$$\chi = \cot^2(\theta^*/2) \approx e^{(\eta_1 - \eta_2)}$$

Expect much larger  $m_{jj}$  reach at  
HL-LHC and FCC-hh ( $\approx 50$  TeV)

Searches, but also (absence of)  
quark substructure



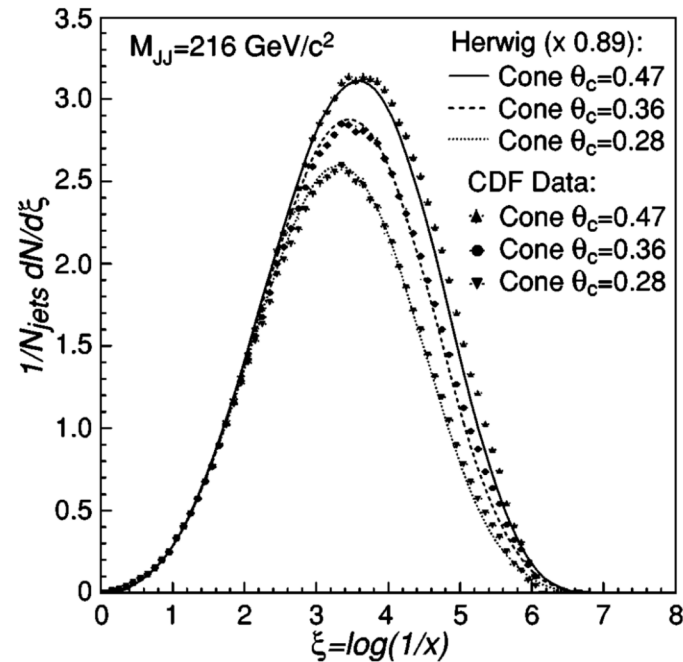
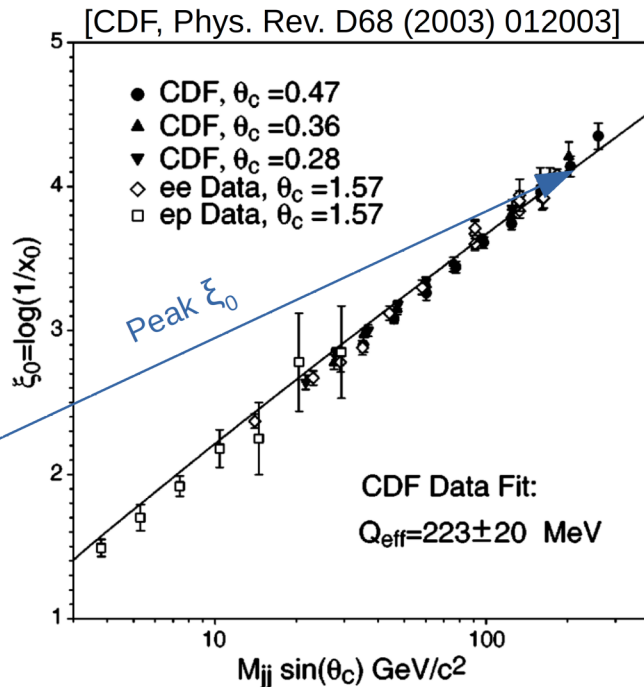
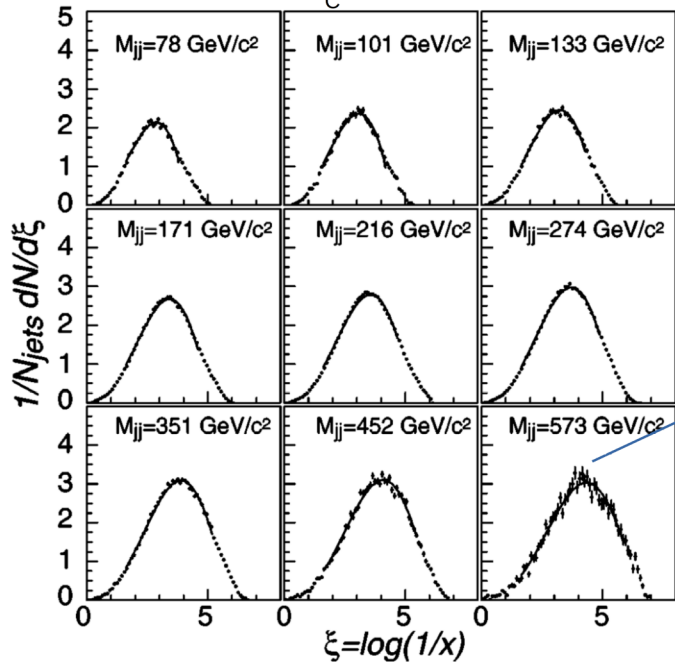
[ATLAS, Phys. Rev. D96, 052004 (2017)]

# 10 Di-jets in pp fragmentation

CDF cone jets  $R = 0.28, 0.36, 0.47$ ,  $x = p/E_{\text{jet}}$ ,  $\xi = \log(1/x)$

$\bar{pp}$  at 1.8 TeV, select balanced central di-jet events

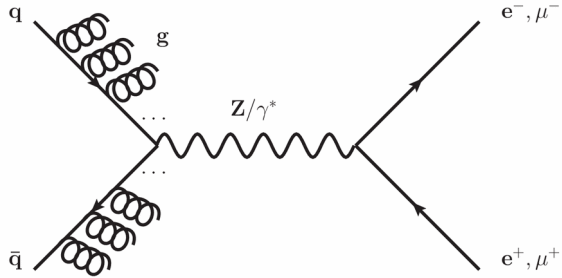
$\theta_c = 0.36$



QCD MLLA\* fit, probe of MC PS+had.,  $m_{jj} \approx 50$  TeV at FCC-hh

# 11 Drell-Yan in pp

Lepton pairs  $m_{\bar{l}l} \approx m_Z$  in pp

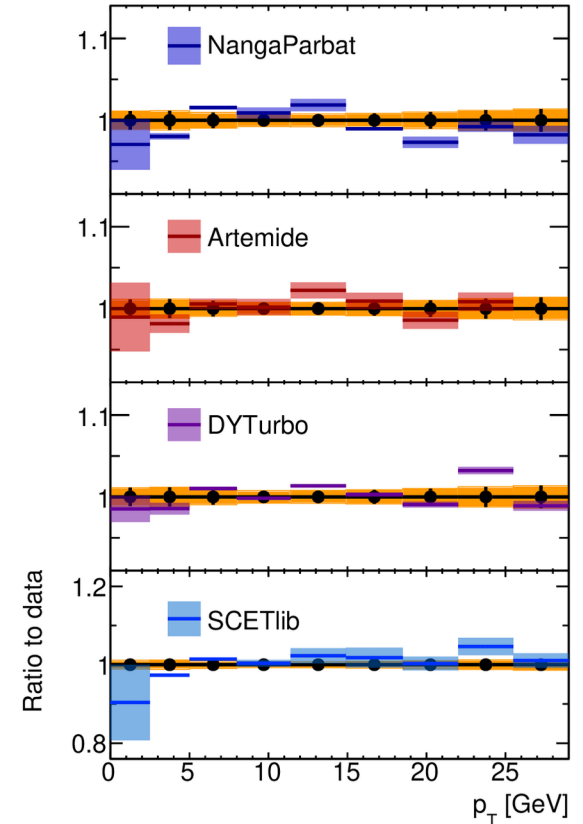
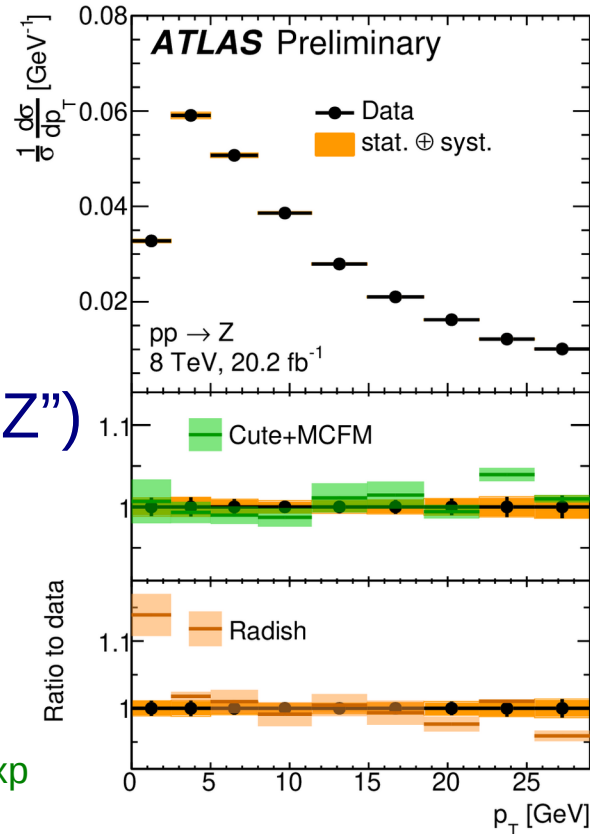


$p_t$  spectrum of  $\bar{l}l$  system ("Z")  
sensitive to  $\alpha_s(m_Z)$

N3LO+N3LL result:

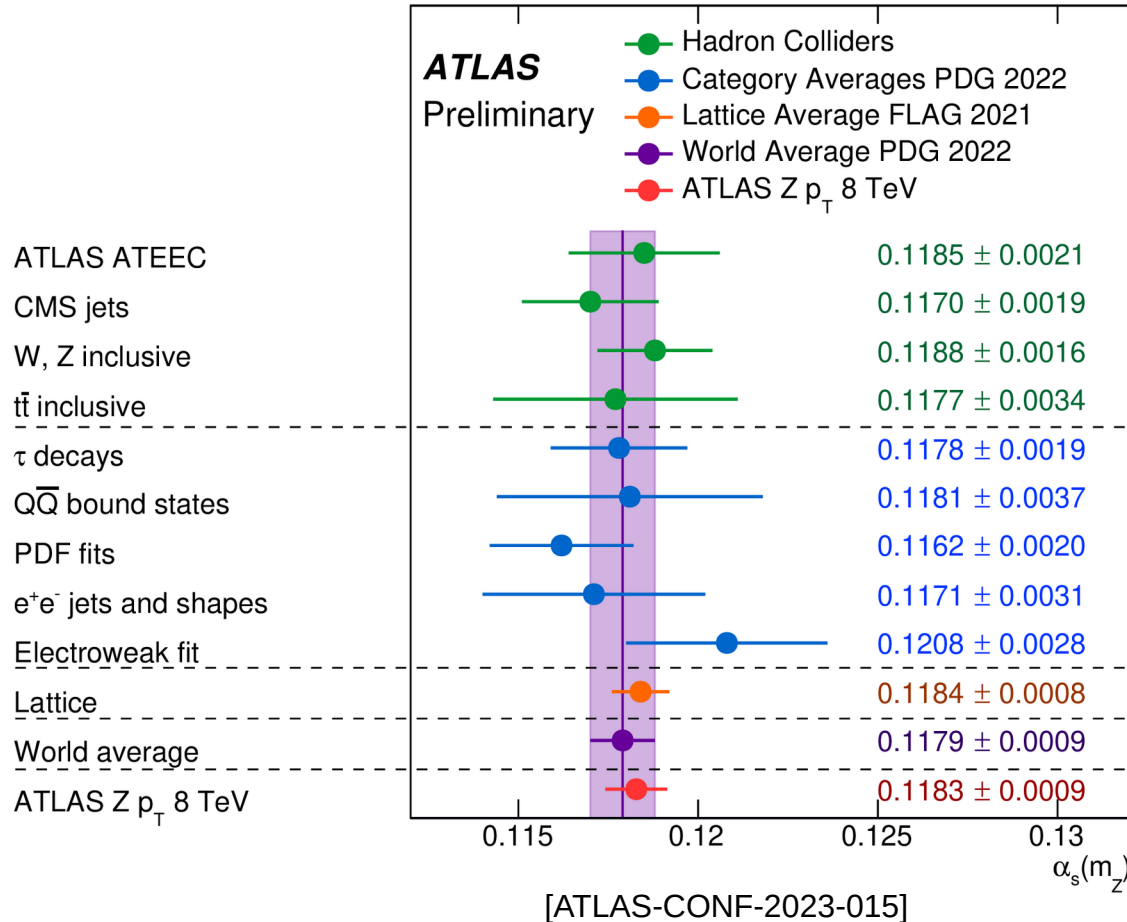
$$\alpha_s(m_Z) = 0.1178 \pm 0.0004_{\text{exp}} \pm 0.0005_{\text{pdf}} \pm 0.0007_{\text{scale}}$$

[ATLAS-CONF-2023-013/15]



# 12 Summary

## Future $\Delta\alpha_s(m_Z)$ estimates

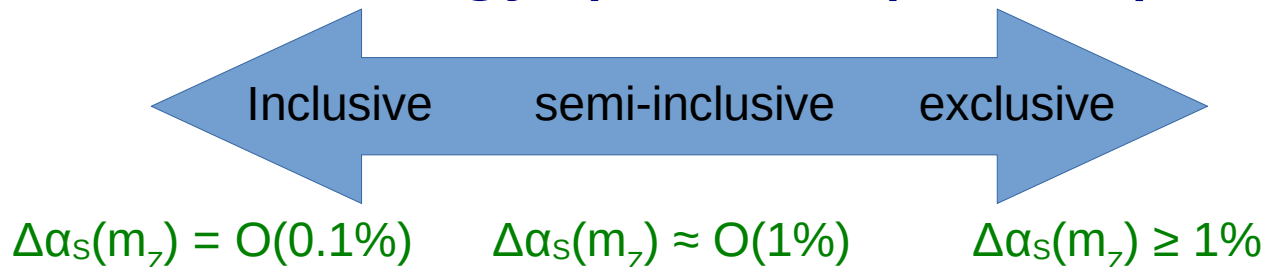


- |
- |
- | 1.5% (theory,pdfs)
- |
- <1% (theory, spec.func.)
- 1.5% (theory)
- 0.2% (future ep pdfs)
- 1% (theory)
- 0.1% (future ee)
- 0.1% (theory)
- <1% (theory,pdfs)

[D. d'Enterria, S. Kluth, G. Zanderighi (eds.), arxiv: 2203.08271]

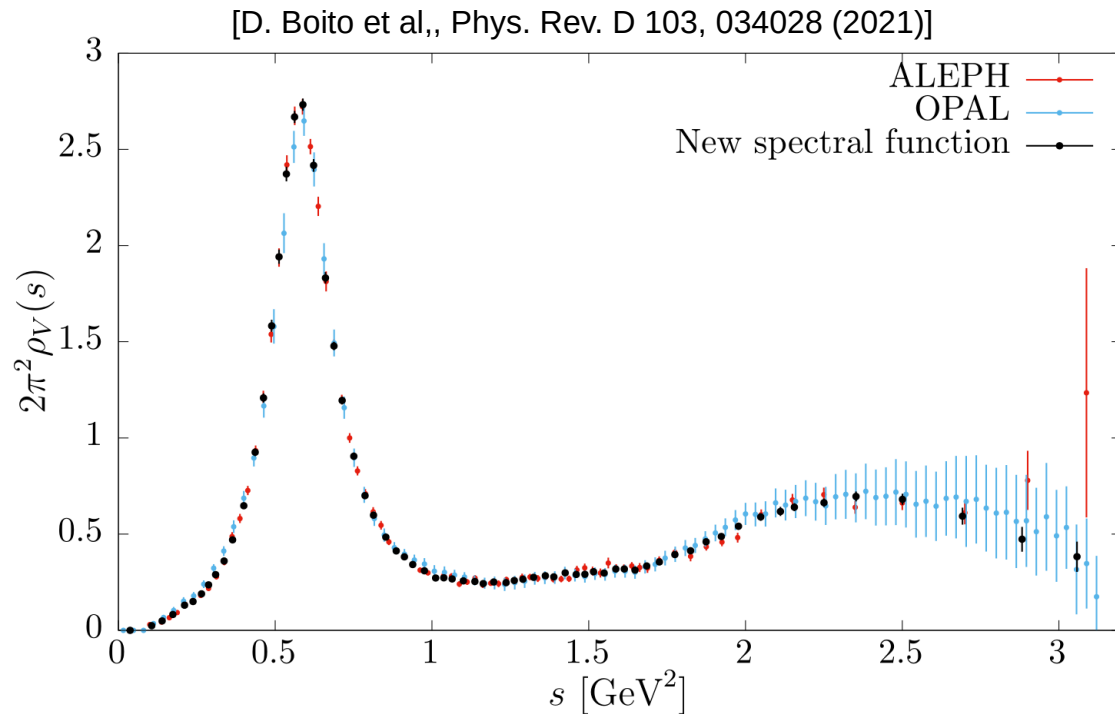
# 12 Summary

- FCC et al great potential for QCD
  - Running strong coupling and quark masses
- FCC et al ultimate top quark measurements
- FCC-ee, ep colliders (FCC-eh, LHeC) and Lattice QCD for  $\Delta\alpha_s(m_Z) \approx 0.1\%$
- FCC-ee low energy ( $\sqrt{s} < m_Z$ ) runs promising!



# 1.2 Inclusive: $\tau$ decays

Moments of vector (even  $\pi$ s) and axial-vector (odd  $\pi$ s) “spectral functions” with N3LO QCD + np terms  $\Rightarrow \alpha_s(m_\tau) \Rightarrow \alpha_s(m_Z)$



Improved spectral functions:  
errors at large  $s$ , rare and  
strange  $\tau$  decays  $\Rightarrow$  better  
analysis of np effects

[M. A. Benitez-Rathgeb et al., in arxiv: 2203.08271]

Theory improvements:  
FOPT vs CIPT understanding,  
N4LO calculation  $\Rightarrow$   
 $\Delta\alpha_s(m_Z) < 1\%$  feasible

m\_top: ee: top  $\rightarrow$  ttbar threshold scan, top event shapes, etc  
Hh: X + leptons, boosted top jets, groomed top jets

Gamma\_top: ee: threshold scan



# 3.3 single top