

# Physics @ Future Circular ~~$e^+e^-$~~ & $\mu^+\mu^-$ Colliders

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University of Pittsburgh

Workshop on Future Accelerators  
Corfu, April 26, 2023



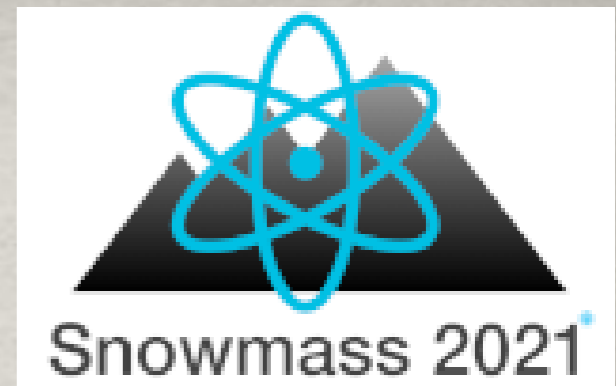
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- ~~Future Circular Collider (FCC-ee)~~
- ~~& Circular Electron-Positron Collider (CEPC)~~
- Muon colliders:  
a Higgs factory & a Multi-TeV collider
- Summary

## Complementary talks:

T. You; J. List; L. Gouskos; J. Wang; H. Baer;  
K. Kaadze; R. Torre; S. Pokorski; Alain Blondel ...

- **Snowmass 2021: A decadal study**  
**Community Planning Exercise**  
**US APS DPF-led effort**

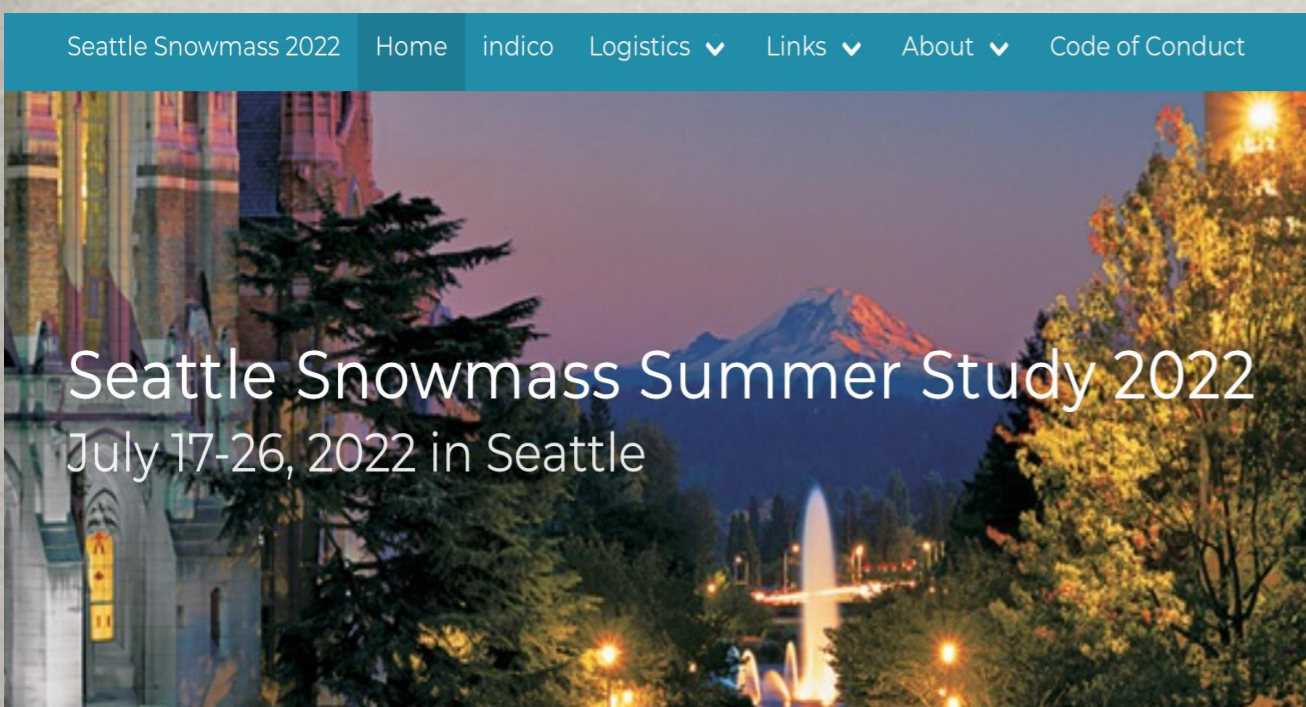


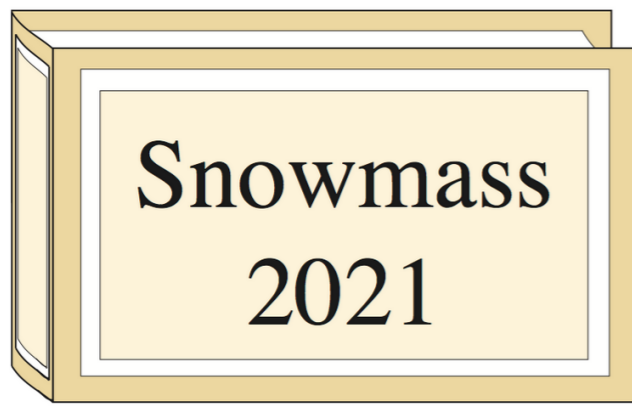
**To define the most important questions for the field of particle physics**  
**To identify promising opportunities to address them, for the decades to come**

## **Community Summer Study: Snowmass 2021**

**July 17 – 26, 2022 @ UW – Seattle**

**<http://seattlesnowmass2021.net>**





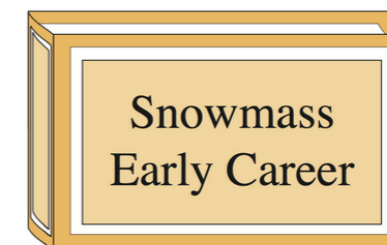
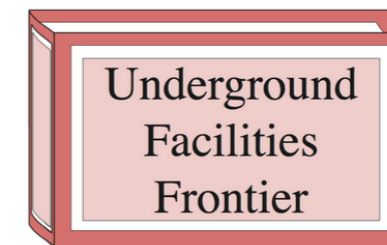
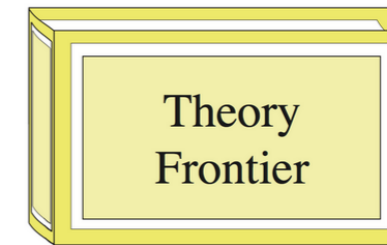
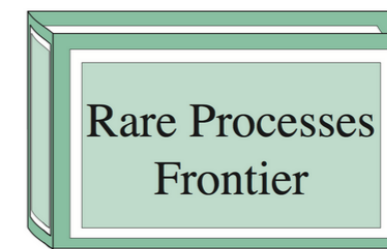
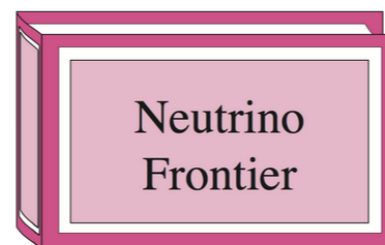
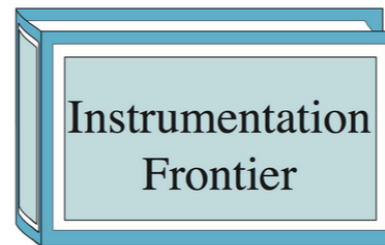
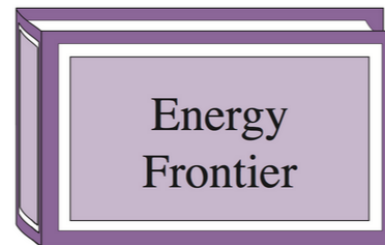
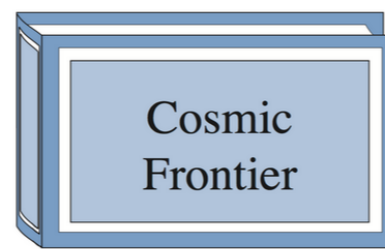
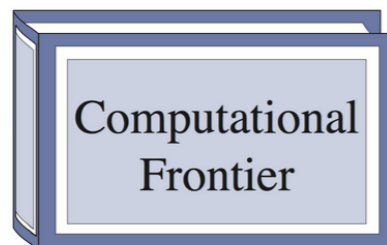
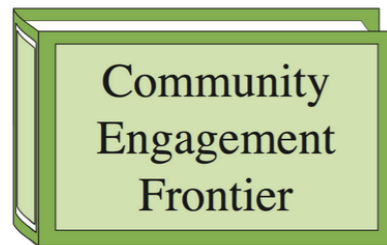
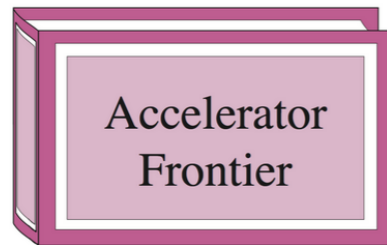
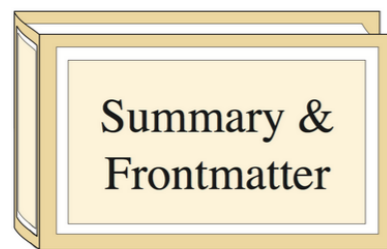
<https://www.slac.stanford.edu/econf/C210711/>



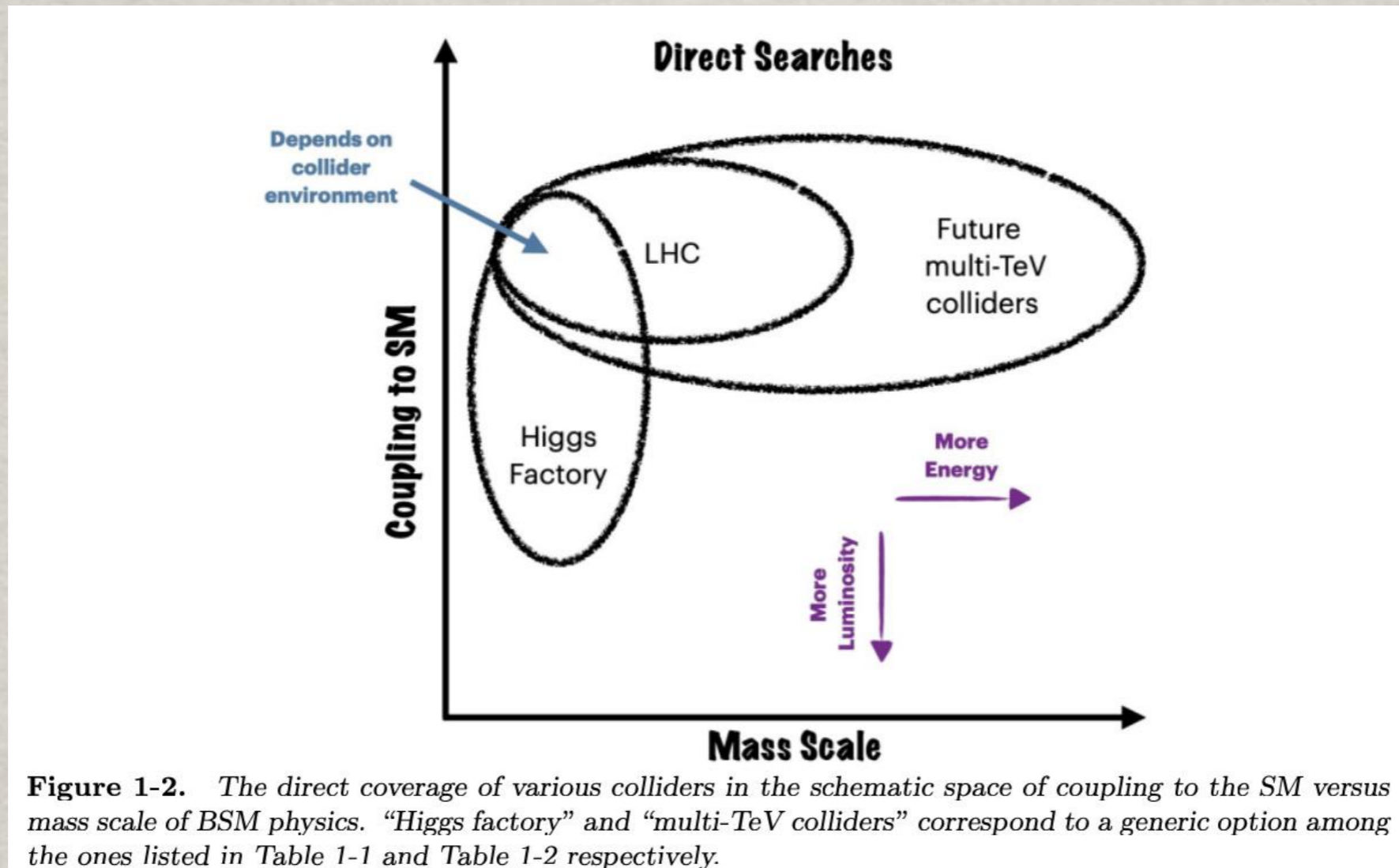
*Proceedings of the 2021 US Community Study on  
the Future of Particle Physics*

*(Snowmass 2021)*

*organized by the APS Division of Particles and Fields*



# Collider needs



## The Energy Frontier Vision

- Complete the HL-LHC program,
- Start now a targeted program for detector R&D for Higgs Factories
- Support construction of a Higgs factory
- Ensure the long-term viability of the field by developing a multi-TeV energy frontier facility such as a *muon collider* or a *hadron collider*.

- **A Higgs factory is a must !**

**ANY elementary particle needs a factory to scrutinize:**

- **Pion/Kaon ( $\mu, \nu$ )** factories: CERN, TRIUMF, FNAL, JLab ...
- **tau/charm** factories: CESR, BEPC ...
- **B-factories**: Belle, BaBar, LHCb ...
- **Z/W $^{\pm}$**  factories: SLC, LEP-I, LEP-II, Tevatron, LHC ...
- **Top-quark** factories: Tevatron, LHC.

**The Higgs boson is NO exception !**

**LHC Run 3 / HL-LHC will lead the way: 50M/ab !**

We need  **$O(10^5 - 10^6)$**  “clean” Higgs bosons:

- well-constrained kinematics in  **$e^+e^-$**  collisions
- model-independent, absolute measurements
- sub-percentage accuracy
- challenging decay processes  **$H \rightarrow \tau^{\pm} \mu^{\mp}, c\bar{c}, \dots$**

# Snowmass 2021, EF report

arXiv:2211.11084

## EF benchmark parameters for future colliders

**Table 1-1.** Benchmark scenarios for Snowmass 2021 Higgs factory studies.

Collider	Type	$\sqrt{s}$	$\mathcal{P}[\%]$ $e^-/e^+$	$\mathcal{L}_{\text{int}}$ $\text{ab}^{-1}/\text{IP}$
HL-LHC	pp	14 TeV		3
ILC & C <sup>3</sup>	ee	250 GeV	$\pm 80/\pm 30$	2
		350 GeV	$\pm 80/\pm 30$	0.2
		500 GeV	$\pm 80/\pm 30$	4
		1 TeV	$\pm 80/\pm 20$	8
CLIC	ee	380 GeV	$+80/0$	1
CEPC	ee	$M_Z$		50
		$2M_W$		3
		240 GeV		10
		360 GeV		0.5
FCC-ee	ee	$M_Z$		75
		$2M_W$		5
		240 GeV		2.5
		$2 M_{\text{top}}$		0.8
$\mu$ -collider	$\mu\mu$	125 GeV		0.02

**Table 1-2.** Benchmark scenarios for Snowmass 2021 multi-TeV collider studies.

Collider	Type	$\sqrt{s}$ (TeV)	$\mathcal{P}[\%]$ $e^-/e^+$	$\mathcal{L}_{\text{int}}$ $\text{ab}^{-1}/\text{IP}$
HE-LHC	pp	27		15
FCC-hh	pp	100		30
SPPC	pp	75-125		10-20
LHeC	ep	1.3		1
FCC-eh		3.5		2
CLIC	ee	1.5	$\pm 80/0$	2.5
		3.0	$+80/0$	5
$\mu$ -collider	$\mu\mu$	3		1
		10		10

This talk: muon colliders

- **A Muon Collider**

## Why muons?

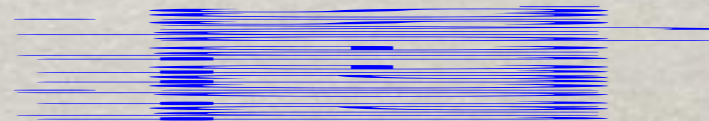
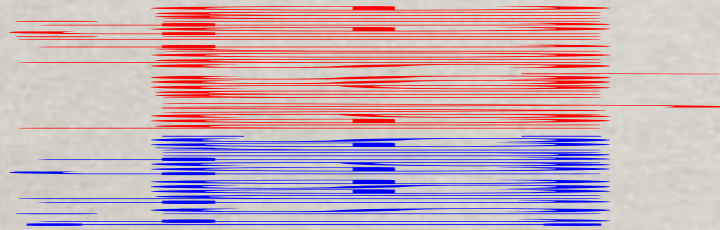
Although sharing the same EM interactions,

it isn't another electron.

$m_\mu \sim 207 m_e$   
 $\tau_\mu \sim 2.2 \mu\text{s}$   
 $c\tau \sim 660 \text{ m}$

Once accelerated:

$$E_\mu \sim 1 \text{ TeV} \rightarrow \gamma \sim 10^4 \rightarrow d = c\gamma\tau = 6,600 \text{ km}$$



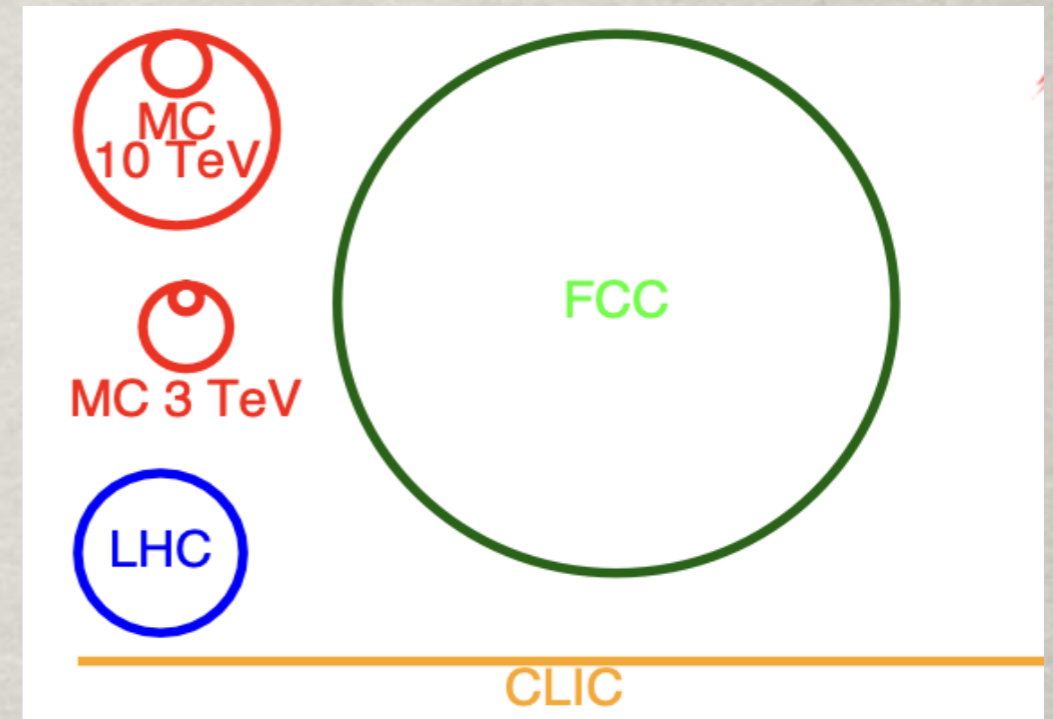


- **Advantages of a muon collider**

- Much less synchrotron radiation energy loss than e's:

$$\Delta E \sim \frac{1}{R} \left( \frac{E}{m_\mu} \right)^4$$

which would allow a smaller and a circular machine, thus likely cost-effective:



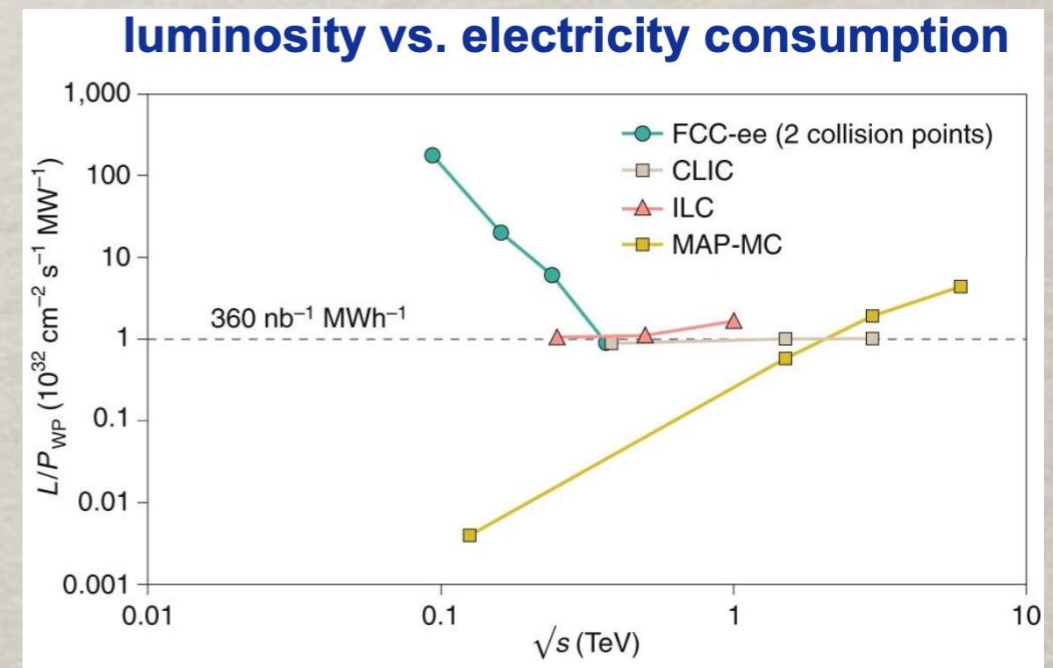
- Luminosity scales with c.m. energy/power, ideally

$$L \sim E_{CM}^2$$

- Smaller beam-energy spread:

$$\Delta E/E \sim 0.1\%$$

potentially  $\Delta E/E(m_H) \sim 0.01\% - 0.001\%$



- **Advantages of a muon collider**

- Unlike the proton as a composite particle,  $E_{CM}$  efficient in  $\mu^+\mu^-$  annihilation, to reach higher new physics threshold  $E_{CM} \sim 2 M_{new}$

- Yet, high-energy collisions result in all sort of partons from Initial States Radiation

$$\sigma_{\mu\mu} \sim (1/M_W)^2 \ln^2(E_{CM}/M_W)$$

“Buy one, get one free!”

- Lower (hadronic) background:

$$\sigma_{pp}(\text{total}) \sim 100 \text{ mb}; \quad \sigma_{\mu\mu}(\text{total}) \sim 100 \text{ nb}$$

- **Disadvantages of a muon collider**

- Production: Protons on target  $\rightarrow$  pions  $\rightarrow$  muons:  
Require sophisticated scheme for  $\mu$  capture & transport

- Very short lifetime: in micro-second,

- Muons cooling in (x,p) 6-dimensions

- $\rightarrow$  Difficult to make quality beams and a high luminosity

- Beam Induced Backgrounds (BIB)

from the decays in the ring at the interacting point

- Neutrino beam dump (environmental hazard)

$$\sigma_{\nu} \sim G_F^2 E^2 \rightarrow \text{Shielding?}$$

# Historically

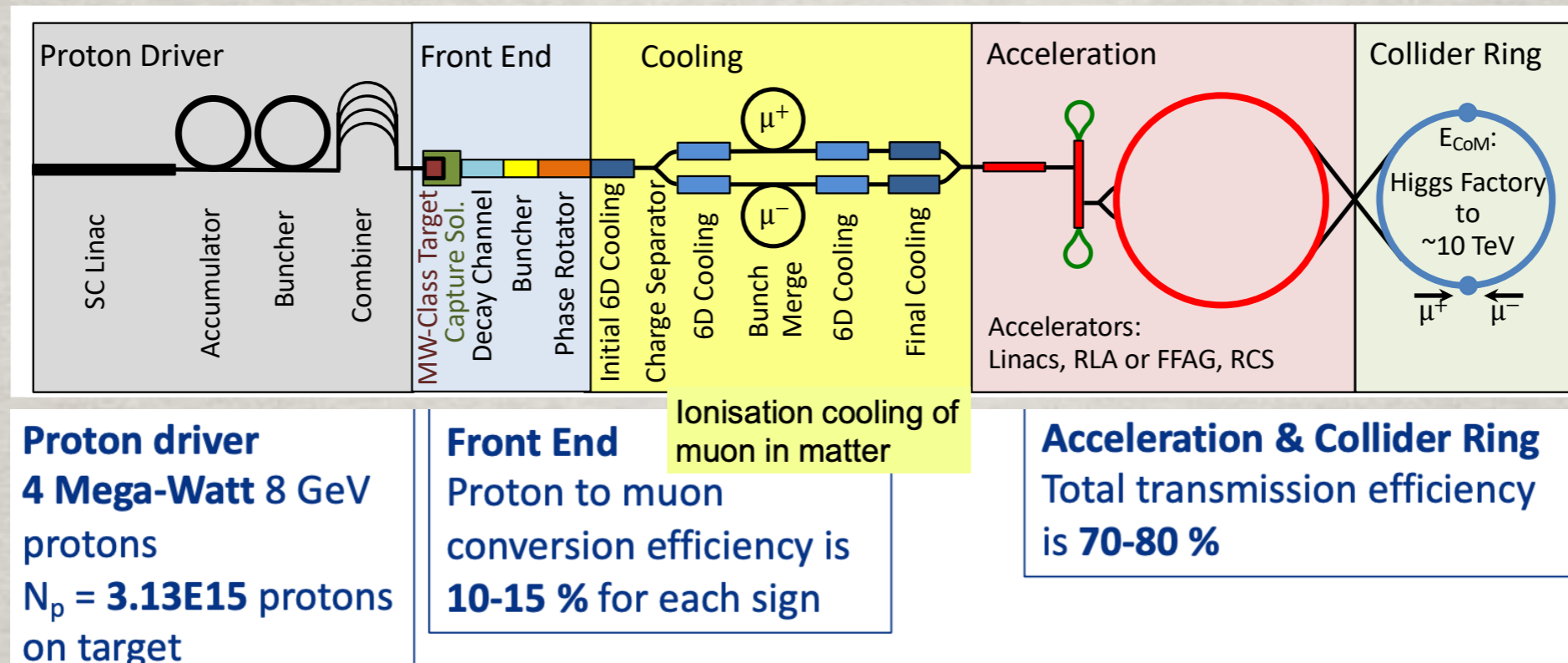
- Concepts mentioned in the 60's
- Early collider design/physics studies in the 90's [\*]
- 2011~2016: Muon Accelerator Program formed (MAP): to address key feasibility issues for  $\mu C$  with the proton driver technology
- MAP terminated in 2016, results published in <https://iopscience.iop.org/journal/1748-0221/page/extraproc46>

## [\*] Some early work:

- *Proceedings of the 1<sup>st</sup> Workshop on the physics potential and Development of the  $\mu\mu$  Colliders*, Napa, California, 1992, Nucl. Inst. Methods. Phys. Res., Sect. A 350, 24 (1994).
- *S-channel Higgs boson production at a muon collider*, Barger et al., PRL75 (1995).
- *$\mu^+ \mu^-$  Collider: Feasibility study*, Muon collider collaboration (July, 1996).
- *Higgs boson physics in the s-channel muon collider*, Barger et al., Phys Rep. 186 (1997).
- *Status of muon collider research*, Muon collider collaboration (Aug., 1999).
- *Recent progress on neutrino factory and muon collider research*,

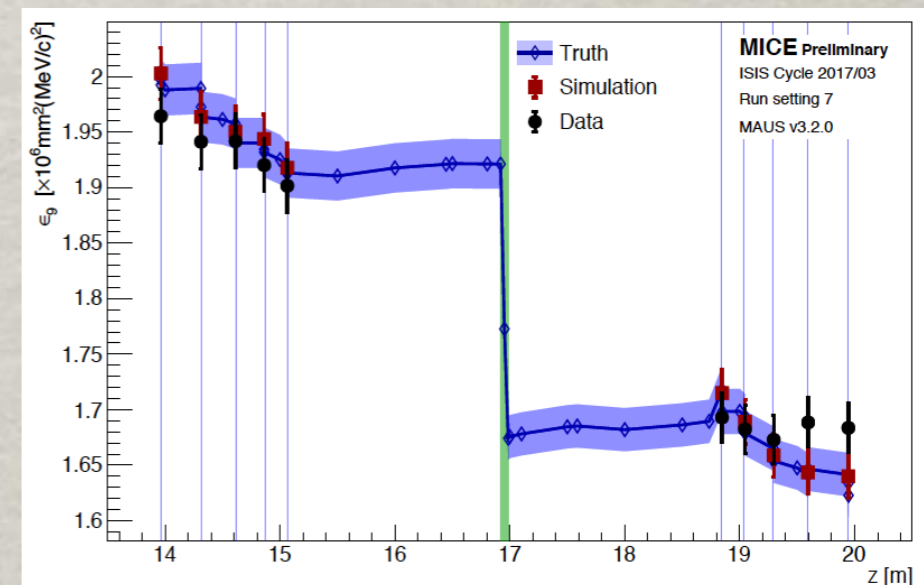
# Renewed interests

## Muon Accelerator Project (MAP)



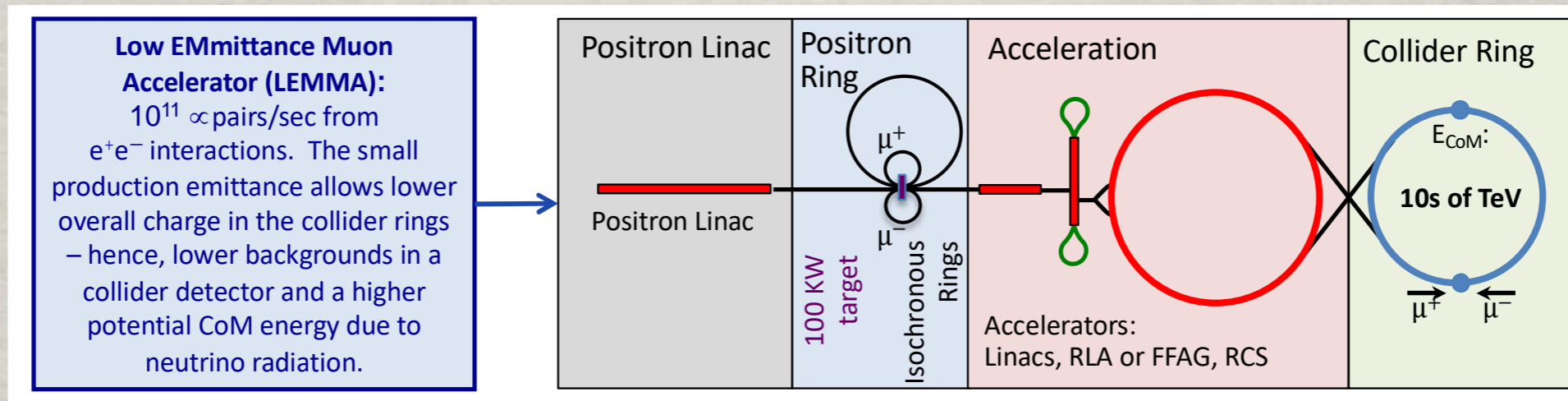
- Protons  $\rightarrow$  pions  $\rightarrow$  muons
- Transverse ionization cooling achieved by MICE
- Muon emittance exchange demonstrated at FNAL/RAL
- 6D cooling of 5-6 orders needed

Noticeable reduction of 9% emittance



<https://arxiv.org/abs/1907.08562>, J.P. Delahauge et al., arXiv:1901.06150/

# LEMMA: $e^+e^-$ (at rest) $\rightarrow \mu^+\mu^-$ (at threshold)



Low **EM**ittance **M**uon **A**ccelerator  
[web.infn.it/LEMMA](http://web.infn.it/LEMMA)



Cooling is not a problem;  
 but high luminosity is challenging:  
 large  $e^+$  flux of  $O(10^{17}/s)$ !

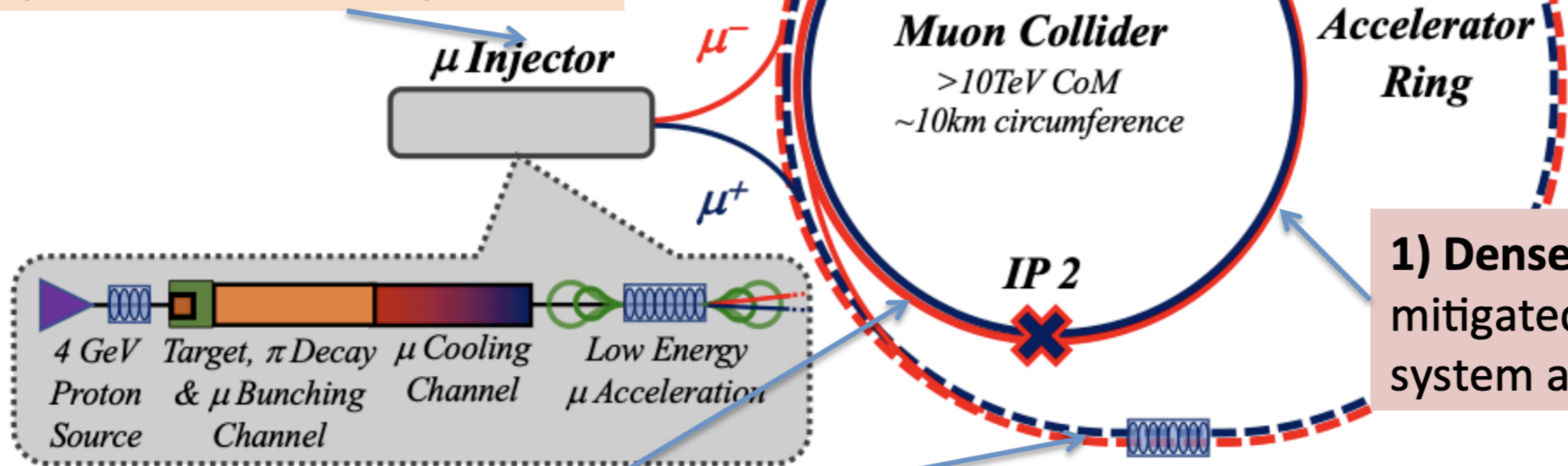
J.P. Delahauge et al., arXiv:1901.06150

# Key Challenges

4) Drives the **beam quality** quite detailed MAP design still challenging design with challenging components *optimise as much as possible*

2) **Beam induced background**

1) **Dense neutrino flux** mitigated by mover system and site selection



3) **Cost and power** consumption drivers, limit energy reach  
e.g. 30 km accelerator for 10/14 TeV,  
10/14 km collider ring  
Also impacts **beam quality**

# Collider benchmark points:

- The Higgs factory:

$$E_{\text{cm}} = m_H$$

$$L \sim 1 \text{ fb}^{-1}/\text{yr}$$

$$\Delta E_{\text{cm}} \sim 5 \text{ MeV}$$

Current Snowmass 2021 point:  $4 \text{ fb}^{-1} / \text{yr}$

Parameter	Units	Higgs
CoM Energy	TeV	0.126
Avg. Luminosity	$10^{34} \text{ cm}^{-2} \text{ s}^{-1}$	0.008
Beam Energy Spread	%	0.004
Higgs Production/ $10^7$ sec		13'500
Circumference	km	0.3

- Multi-TeV colliders:

Lumi-scaling scheme:  $\sigma L \sim \text{const.}$

$$L \gtrsim \frac{5 \text{ years}}{\text{time}} \left( \frac{\sqrt{s}_\mu}{10 \text{ TeV}} \right)^2 \cdot 2 \cdot 10^{35} \text{ cm}^{-2} \text{ s}^{-1} \quad 1 \text{ ab}^{-1} / \text{yr}$$

The aggressive choices:

$$\sqrt{s} = 3, 6, 10, 14, 30 \text{ and } 100 \text{ TeV}, \quad L = 1, 4, 10, 20, 90, \text{ and } 1000 \text{ ab}^{-1}$$

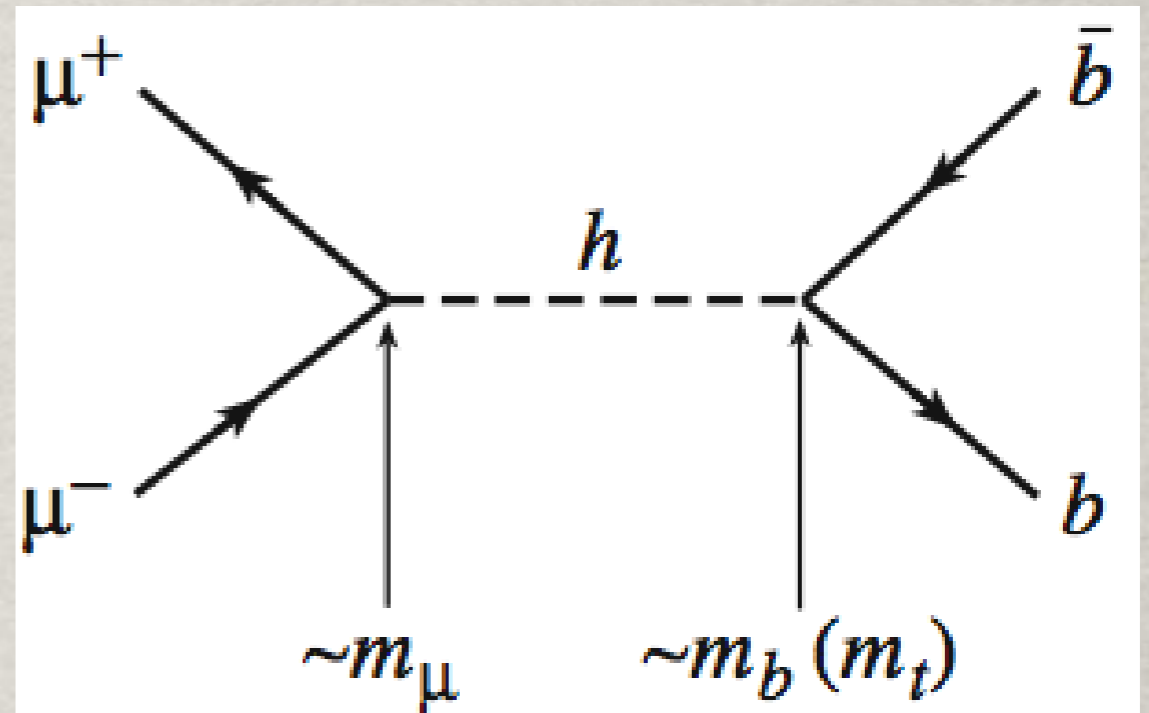
European Strategy, arXiv:1910.11775; arXiv:1901.06150; arXiv:2007.15684.



# Physics potential

## Higgs factory:

Resonant Production:



$$\sigma(\mu^+ \mu^- \rightarrow h \rightarrow X) = \frac{4\pi \Gamma_h^2 \text{Br}(h \rightarrow \mu^+ \mu^-) \text{Br}(h \rightarrow X)}{(\hat{s} - m_h^2)^2 + \Gamma_h^2 m_h^2}.$$

$$\begin{aligned} \sigma_{peak}(\mu^+ \mu^- \rightarrow h) &= \frac{4\pi}{m_h^2} \text{BR}(h \rightarrow \mu^+ \mu^-) \\ &\approx 71 \text{ pb at } m_h = 125 \text{ GeV.} \end{aligned}$$

About **O(70k)** events produced per **fb<sup>-1</sup>**

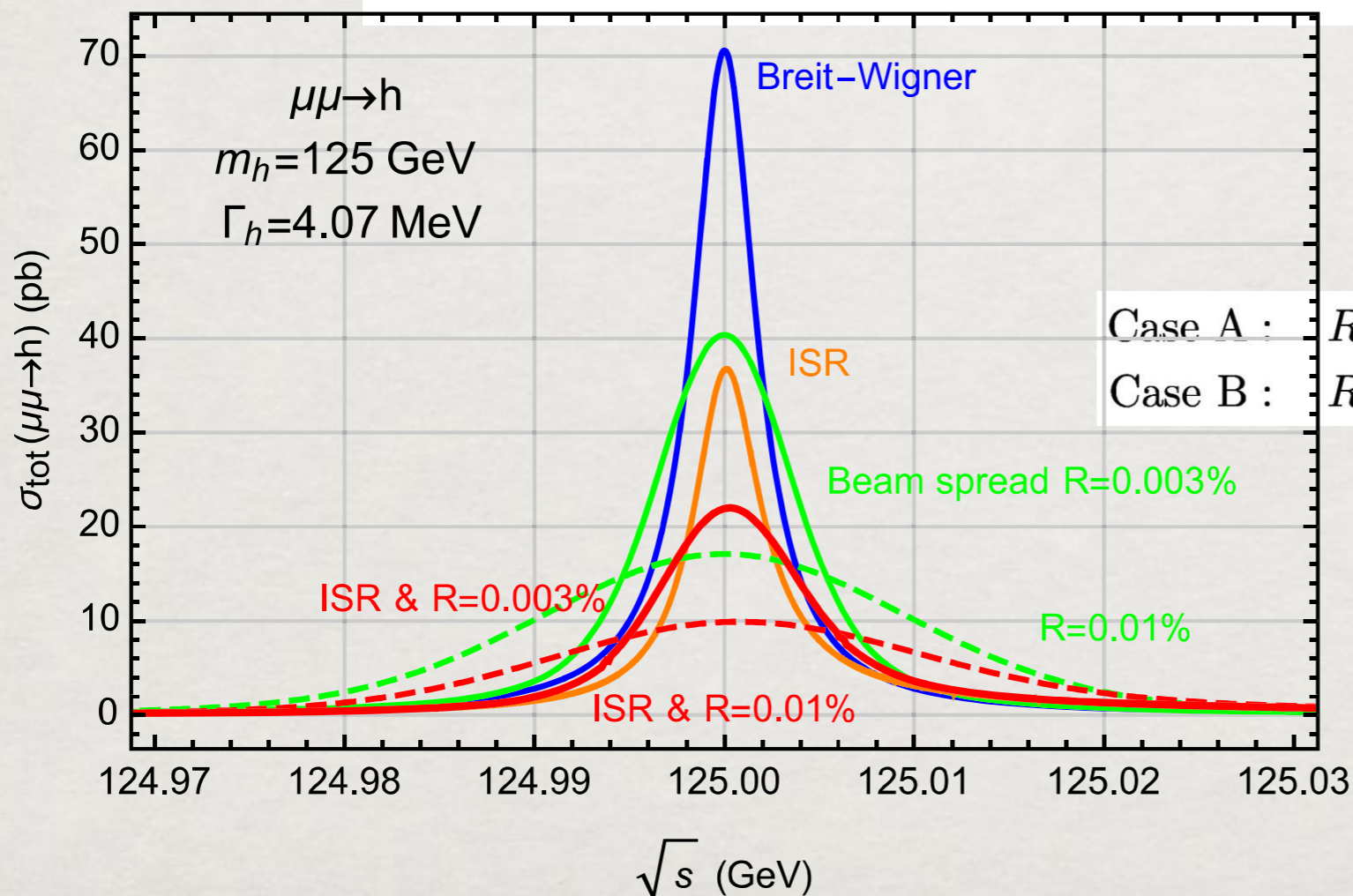
# At $m_h=125$ GeV, $\Gamma_h=4.2$ MeV

$$\frac{\exp[-(\sqrt{\hat{s}} - \sqrt{s})^2 / (2\sigma_{\sqrt{s}}^2)]}{\sqrt{2\pi}\sigma_{\sqrt{s}}}$$

$$\frac{4\pi\Gamma(h \rightarrow \mu\mu)\Gamma(h \rightarrow X)}{(\hat{s} - m_h^2)^2 + m_h^2[\Gamma_h^{\text{tot}}]^2}$$

$$\sigma_{\text{eff}}(s) = \int d\sqrt{\hat{s}} \frac{dL(\sqrt{s})}{d\sqrt{\hat{s}}} \sigma(\mu^+ \mu^- \rightarrow h \rightarrow X)$$

$$\propto \begin{cases} \Gamma_h^2 B / [(s - m_h^2)^2 + \Gamma_h^2 m_h^2] & (\Delta \ll \Gamma_h), \\ B \exp\left[-\frac{(m_h - \sqrt{s})^2}{2\Delta^2}\right] \left(\frac{\Gamma_h}{\Delta}\right) / m_h^2 & (\Delta \gg \Gamma_h). \end{cases}$$



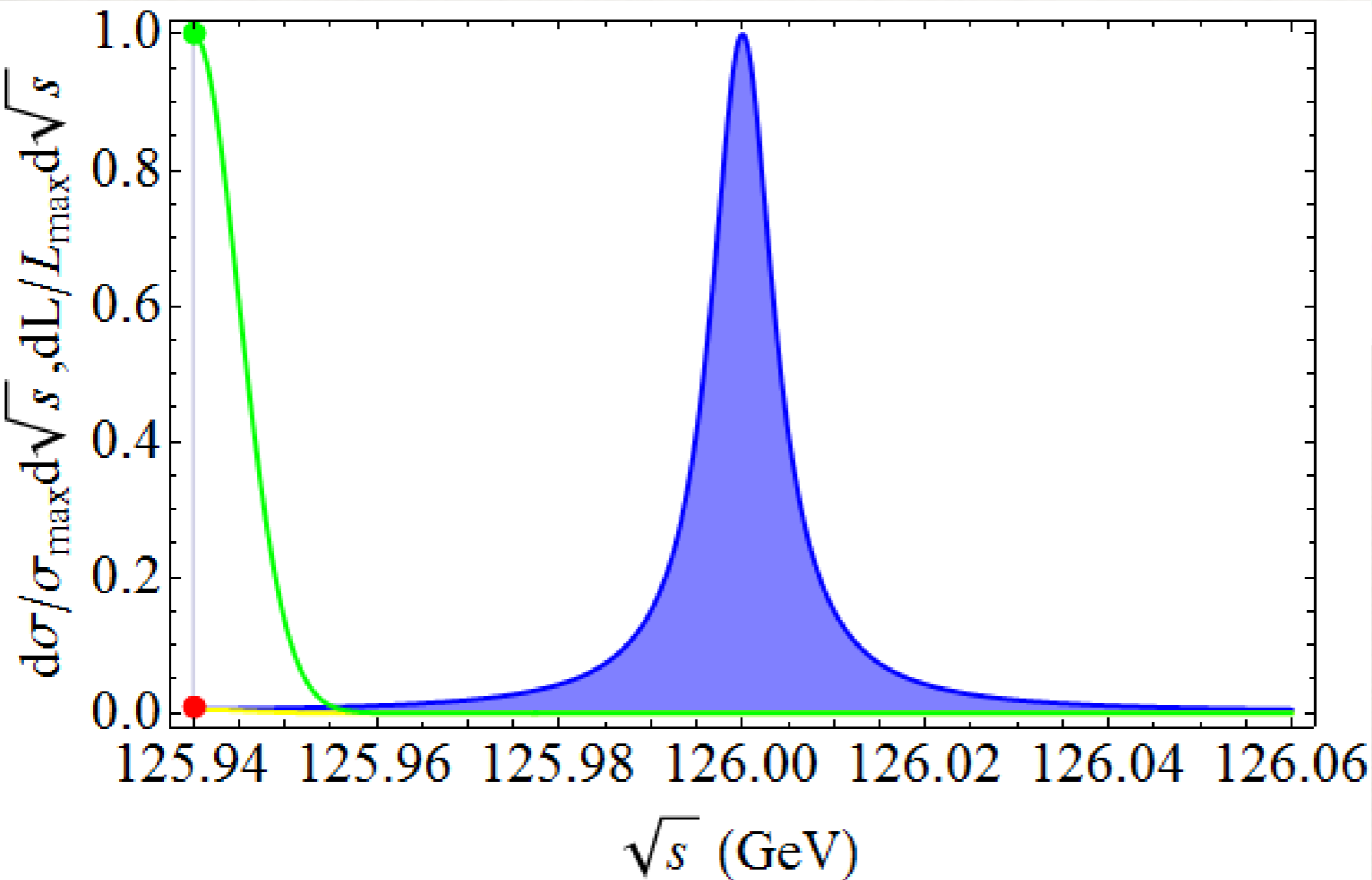
**“Muon Collider Quartet”:**  
 Barger-Berger-Gunion-Han  
 PRL & Phys. Report (1995)

Case A :  $R = 0.01\%$  ( $\Delta = 8.9$  MeV),  $L = 0.5$  fb $^{-1}$ ,  
 Case B :  $R = 0.003\%$  ( $\Delta = 2.7$  MeV),  $L = 1$  fb $^{-1}$ .

TH, Liu: 1210.7803;  
 Greco, TH, Liu: 1607.03210

# Ideal, conceivable case:

( $\Delta = 5$  MeV,  $\Gamma_h \approx 4.2$  MeV)



An optimal fitting could reach  $\delta\Gamma_h \sim 0.15$  MeV, or 3.5%

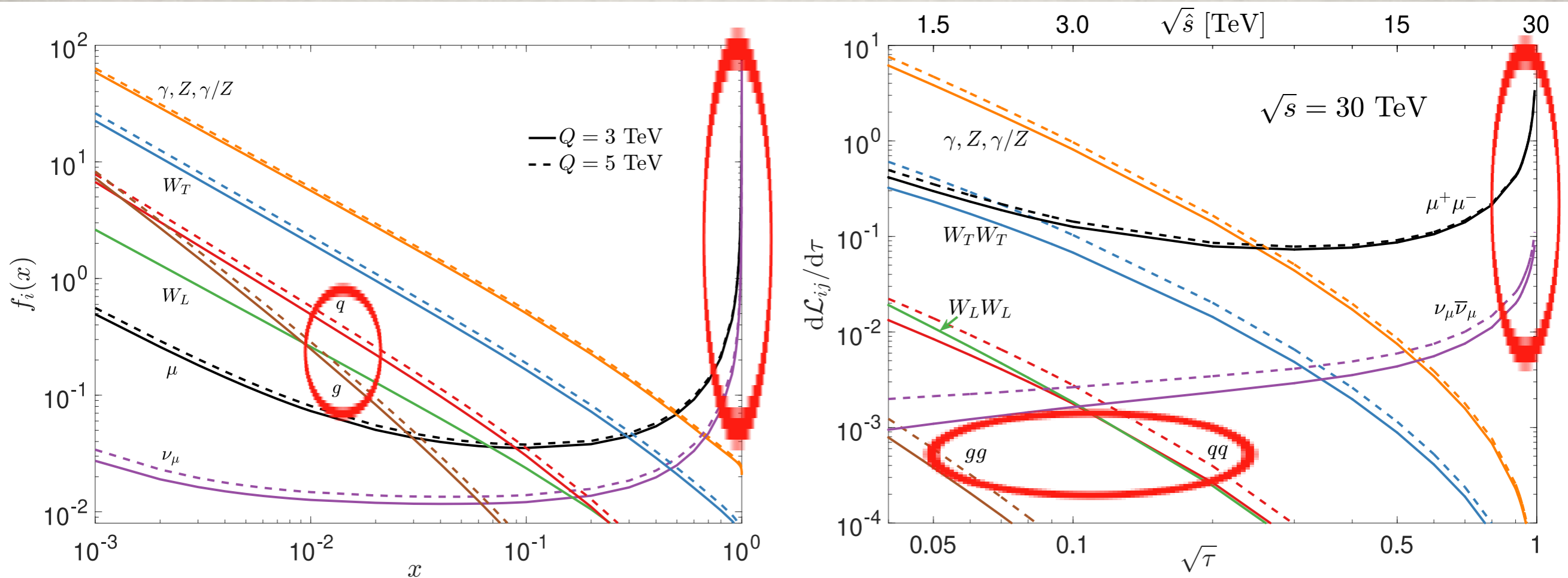
TH, Liu: 1210.7803; Greco, TH, Liu: 1607.03210

# • HE muon colliders: EW PDFs

“partons” dynamically generated

$$\frac{df_i}{d \ln Q^2} = \sum_I \frac{\alpha_I}{2\pi} \sum_j P_{i,j}^I \otimes f_j$$

TH, Yang Ma, Keping Xie,  
arXiv:2007.14300



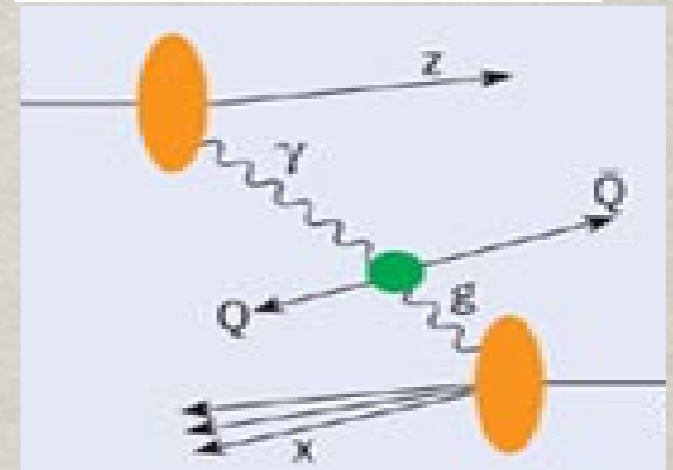
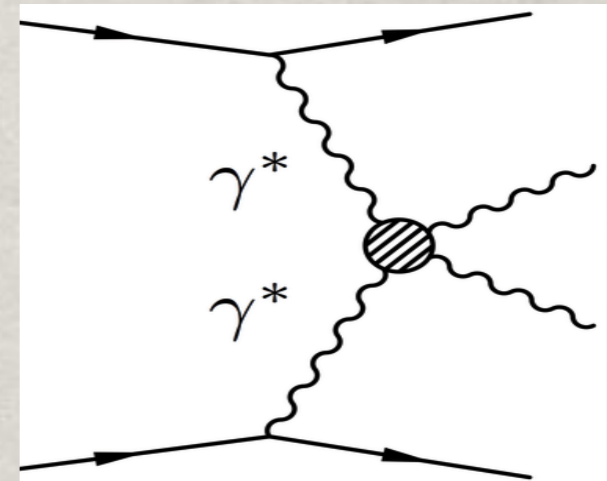
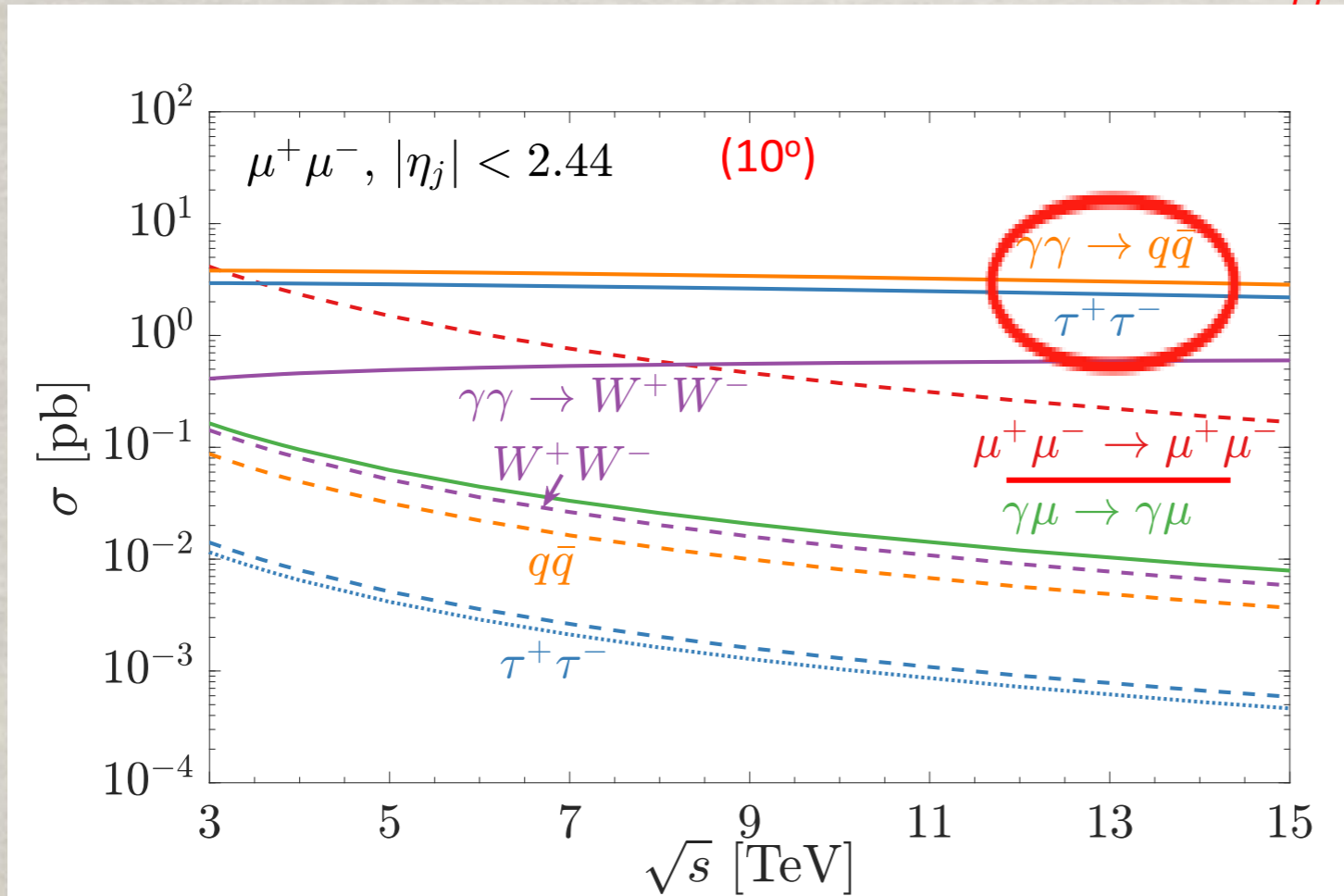
$\mu^\pm$ : the valance.  $\ell_R, \ell_L, \nu_L$  and  $B, W^{\pm,3}$ : LO sea.

- High-energy neutrino collider!
- Hadron collider! Quarks: NLO; gluons: NNLO.

# Photon-induced QED cross sections

large rates

$$\sigma_{fusion} \sim \frac{\alpha^2}{m_{jj}^2} \log^2\left(\frac{Q^2}{m^2}\right)$$



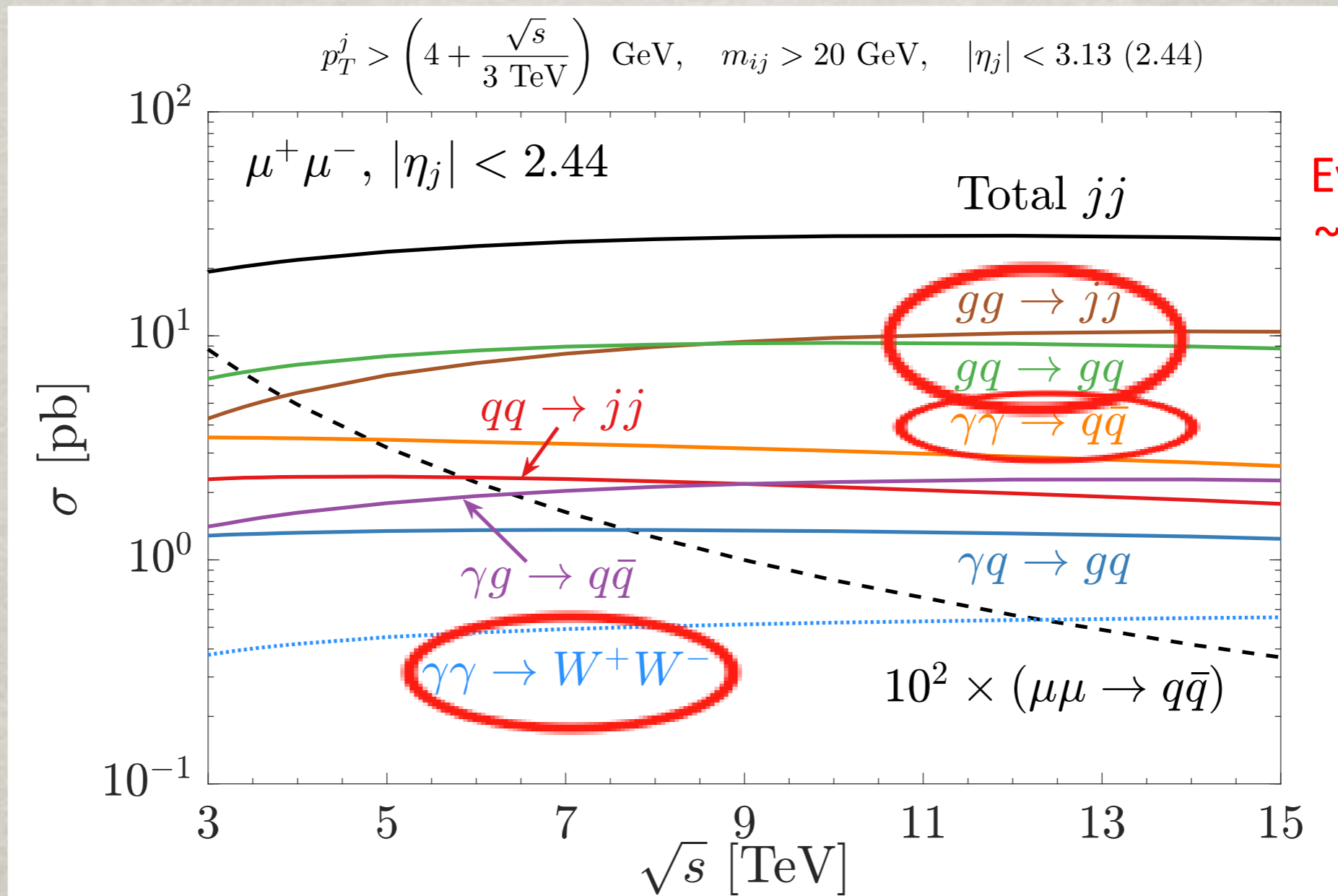
$$p_T^j > \left(4 + \frac{\sqrt{s}}{3 \text{ TeV}}\right) \text{ GeV}, \quad m_{ij} > 20 \text{ GeV}, \quad |\eta_j| < 3.13 \quad (2.44)$$

Quarks/gluons come into the picture via SM DGLAP:

$$\frac{d}{d \log Q^2} \begin{pmatrix} f_L \\ f_U \\ f_D \\ f_\gamma \\ f_g \end{pmatrix} = \begin{pmatrix} P_{\ell\ell} & 0 & 0 & 2N_\ell P_{\ell\gamma} & 0 \\ 0 & P_{uu} & 0 & 2N_u P_{u\gamma} & 2N_u P_{ug} \\ 0 & 0 & P_{dd} & 2N_d P_{d\gamma} & 2N_d P_{dg} \\ P_{\gamma\ell} & P_{\gamma u} & P_{\gamma d} & P_{\gamma\gamma} & 0 \\ 0 & P_{gu} & P_{gd} & 0 & P_{gg} \end{pmatrix} \otimes \begin{pmatrix} f_L \\ f_U \\ f_D \\ f_\gamma \\ f_g \end{pmatrix}$$

# Di-jet production, like hadron colliders

$$\begin{aligned} &\gamma\gamma \rightarrow q\bar{q}, \quad \gamma g \rightarrow q\bar{q}, \quad \gamma q \rightarrow gq, \\ &qq \rightarrow qq(gg), \quad gq \rightarrow gq, \quad \text{and} \quad gg \rightarrow gg(q\bar{q}) \end{aligned}$$

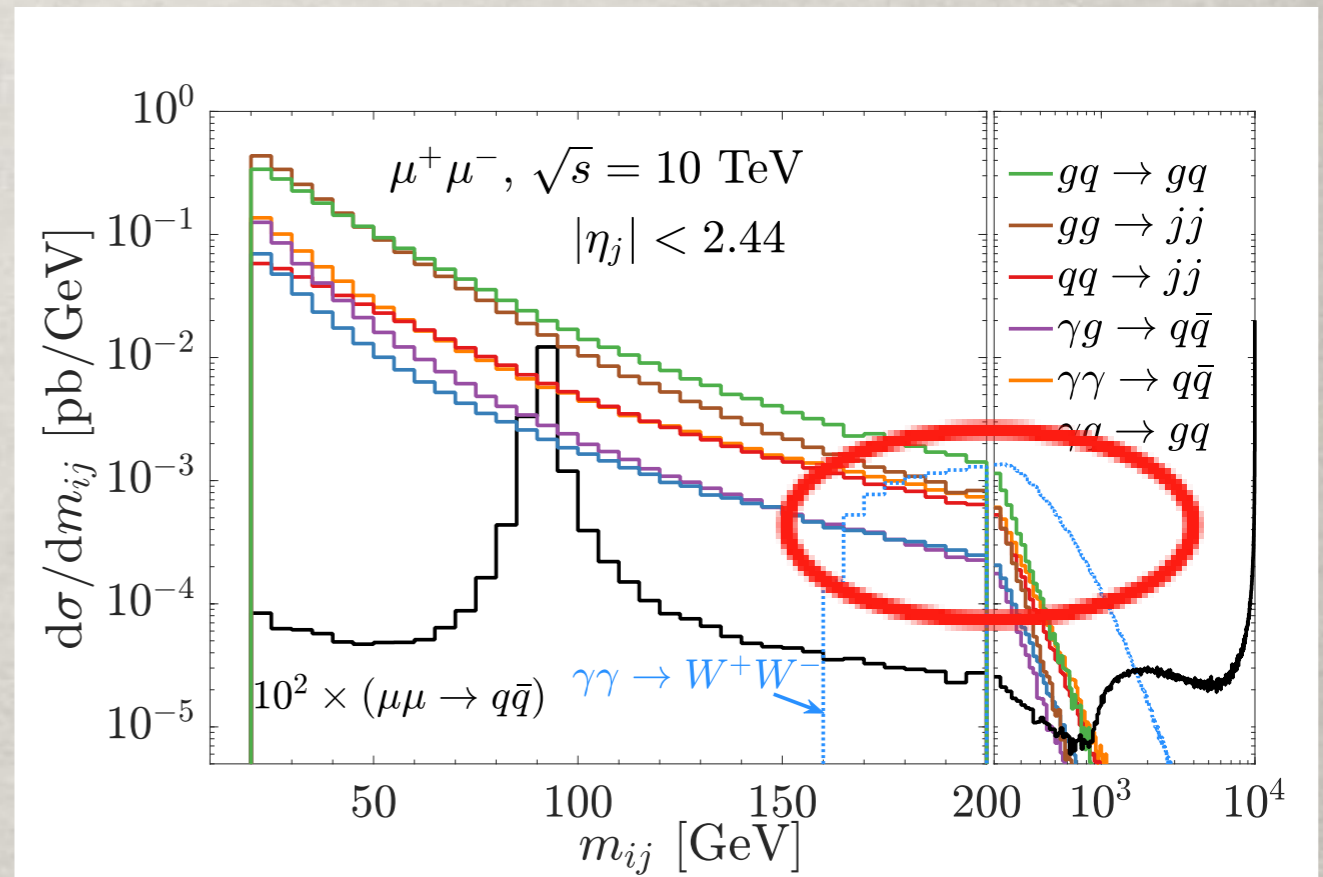
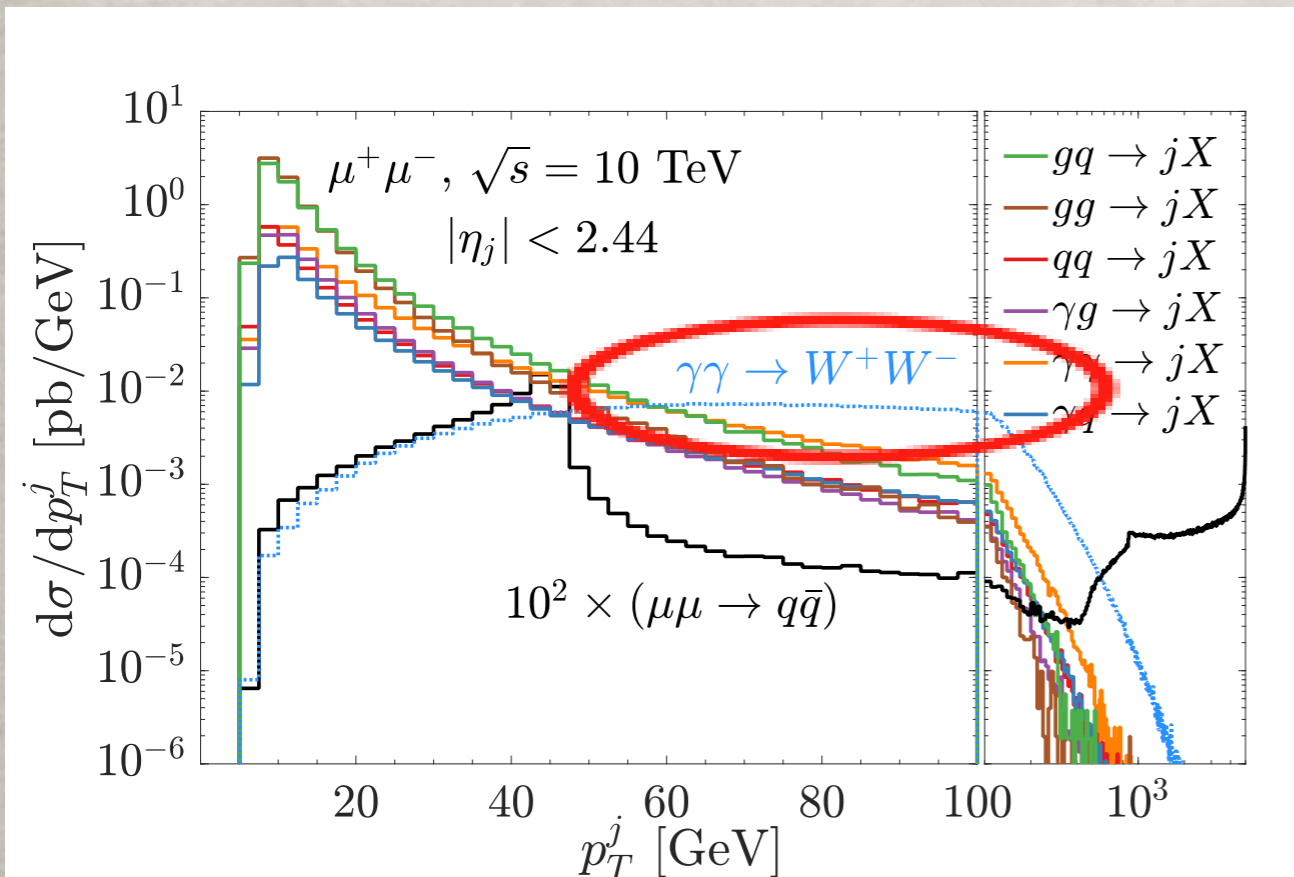


Event rate  
~ a few Hz

- Jet production dominates at low energies
- EW processes take over at high scales!

TH, Yang Ma, Keping Xie, arXiv:2103.09844.

# Di-jet kinematical features: High $p_T$ physics strikes back!



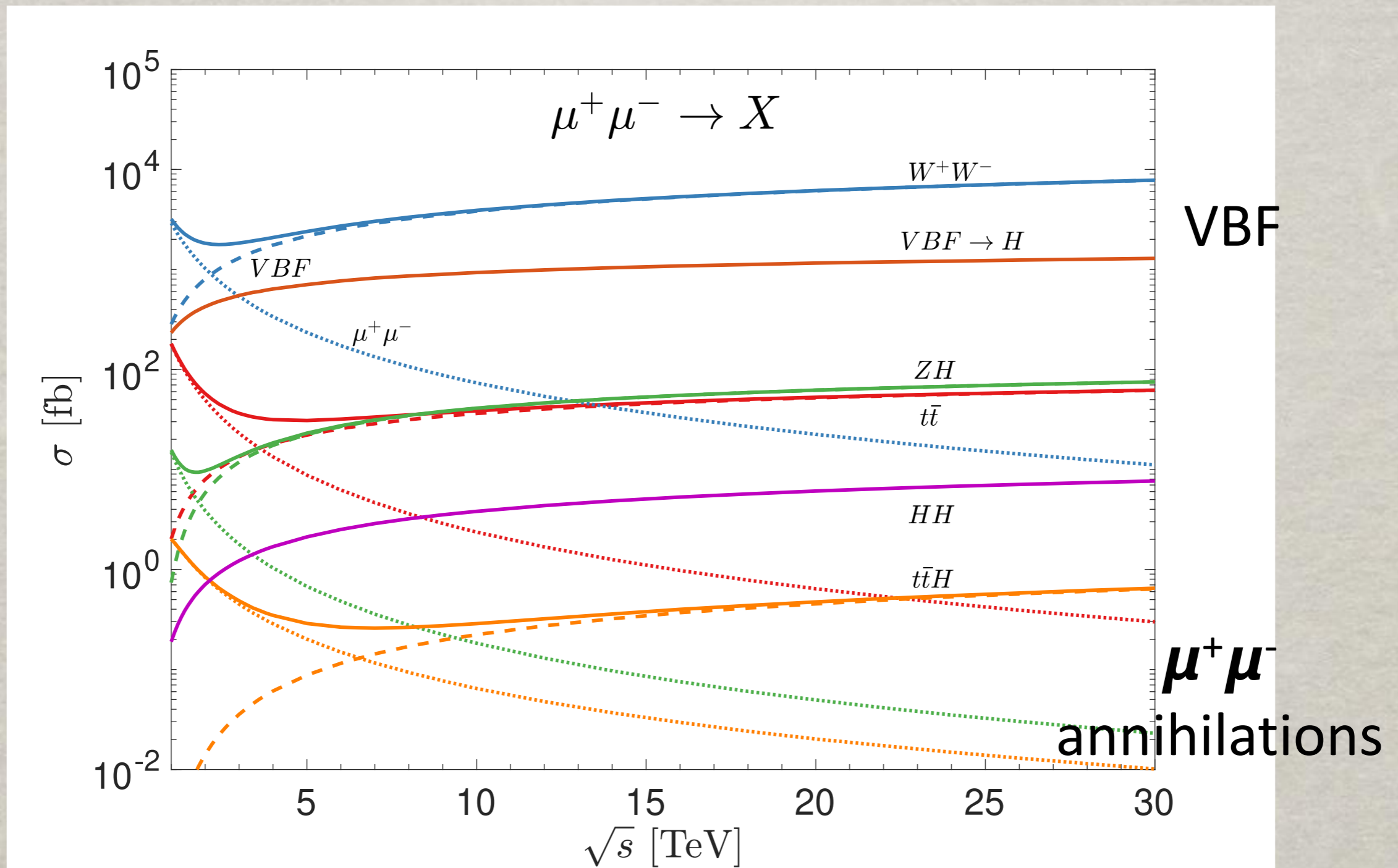
To effectively separate the QCD backgrounds:

$$p_T > 60 \text{ GeV}$$

- “Semi-inclusive” processes

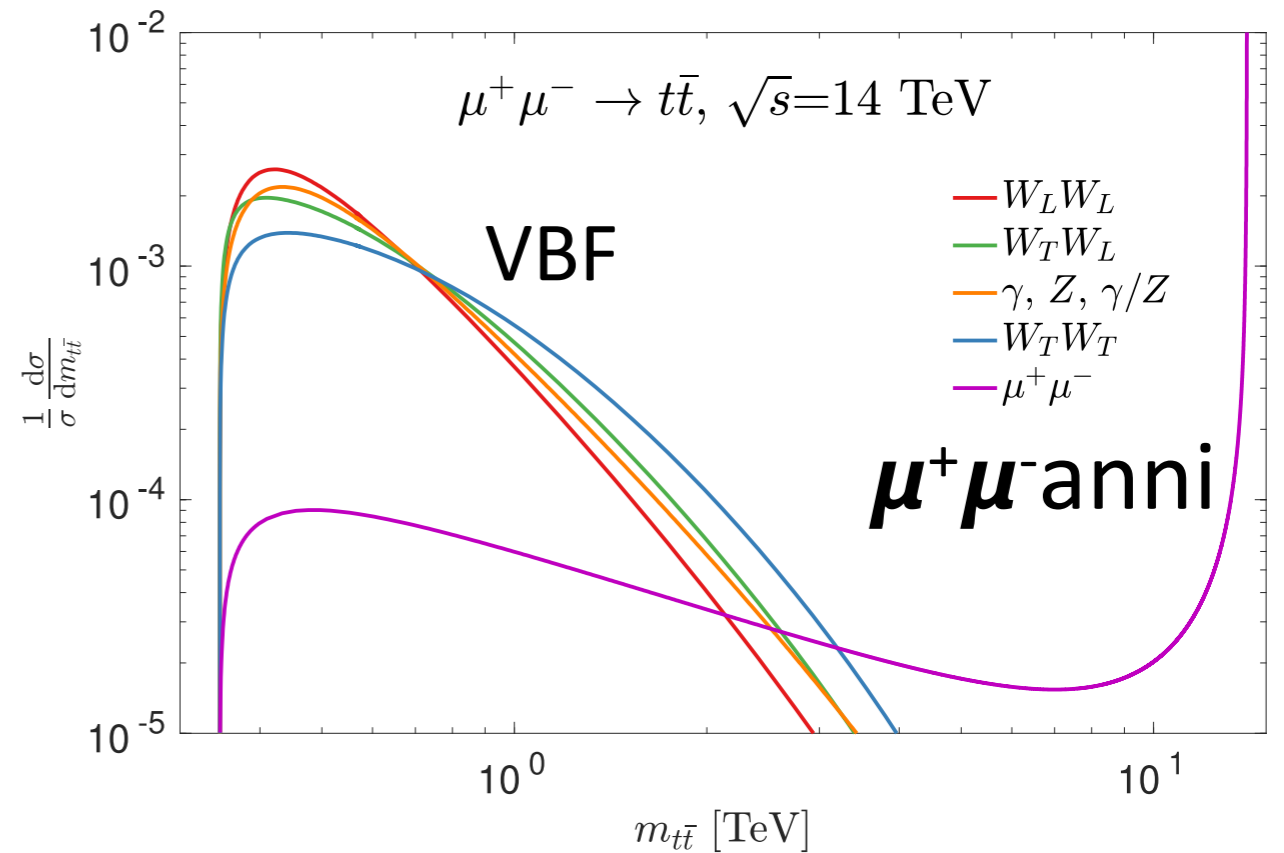
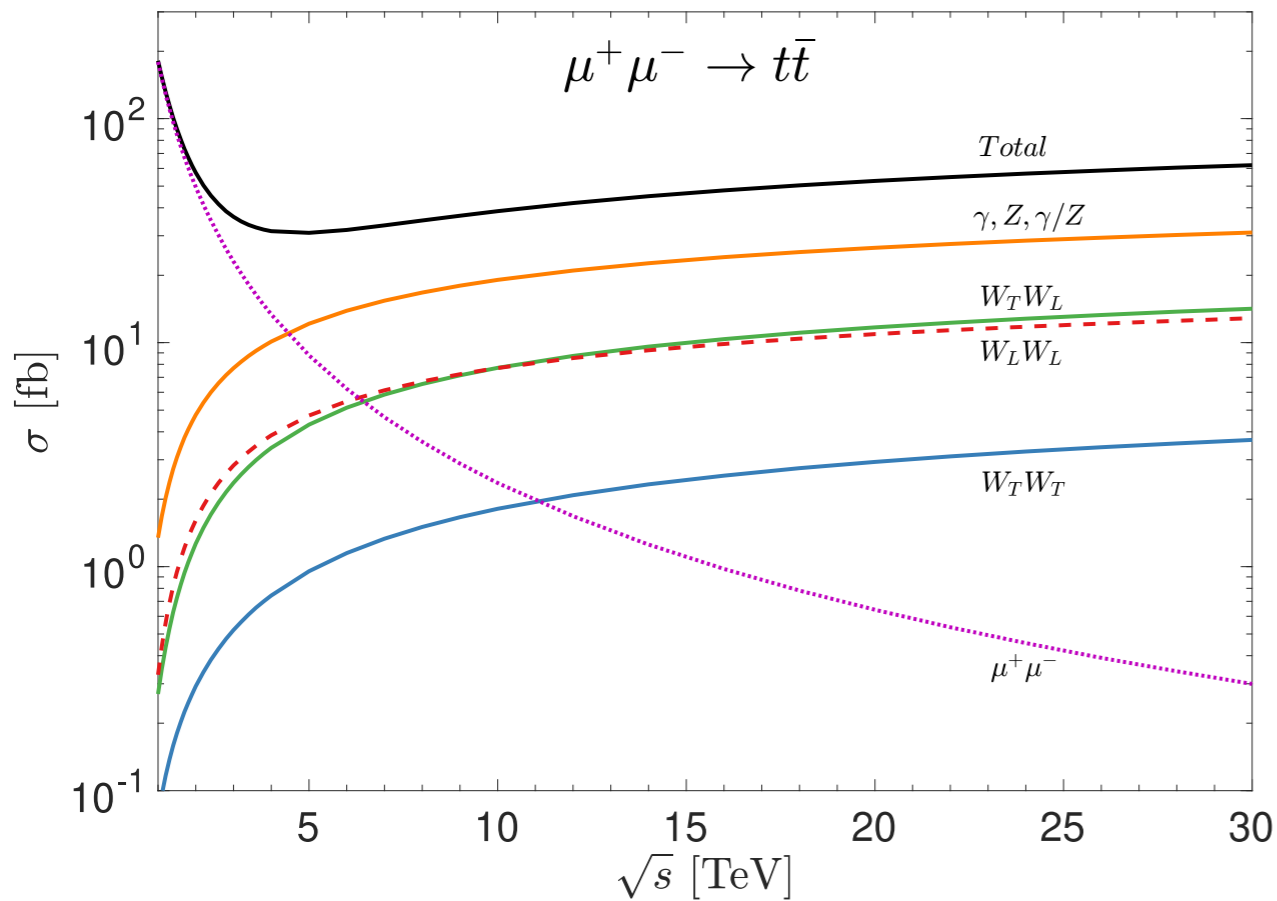
Just like in hadronic collisions:

$\mu^+ \mu^- \rightarrow$  exclusive particles + remnants



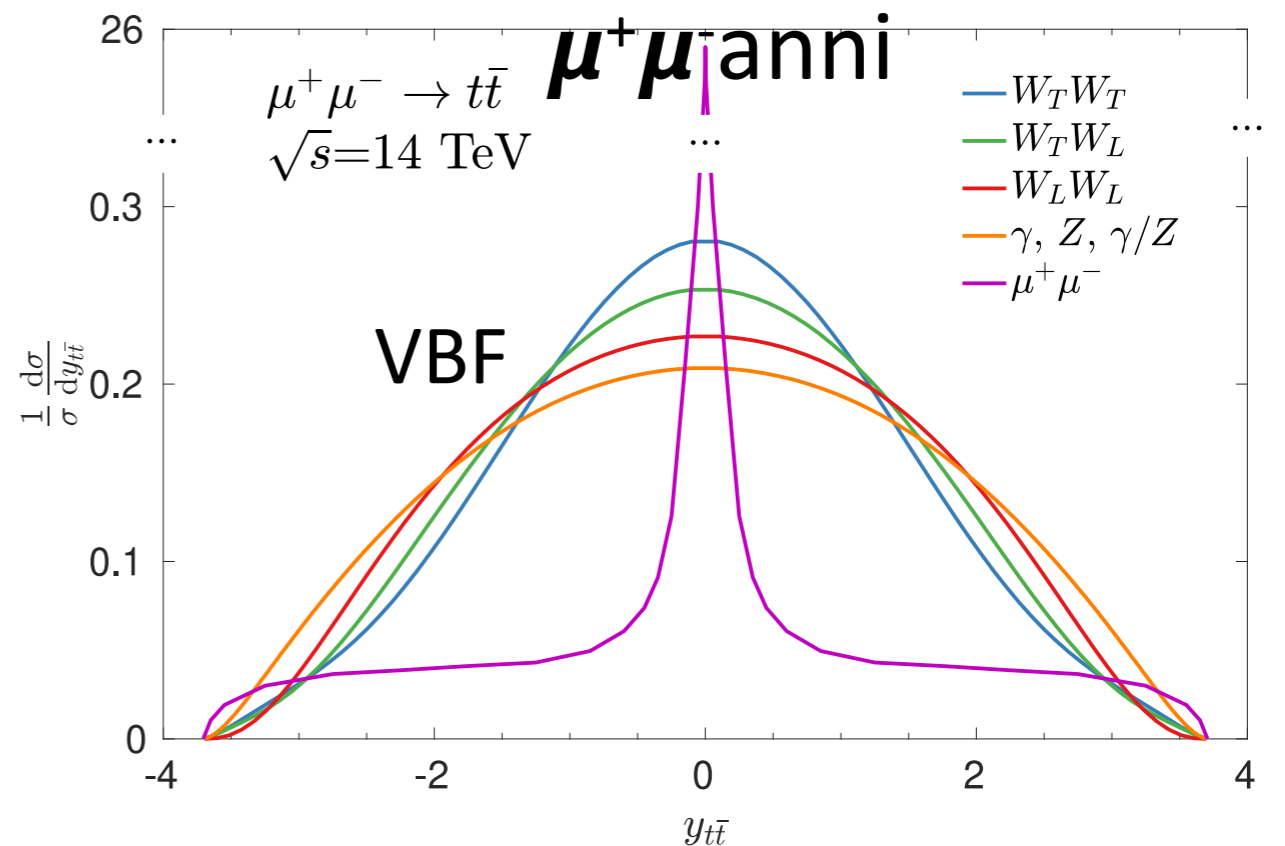


- separable sub-processes:



Partonic contributions

**$\mu^+ \mu^-$  Collider:**  
**“Buy one, get one free”**  
**Annihilation +VBF**

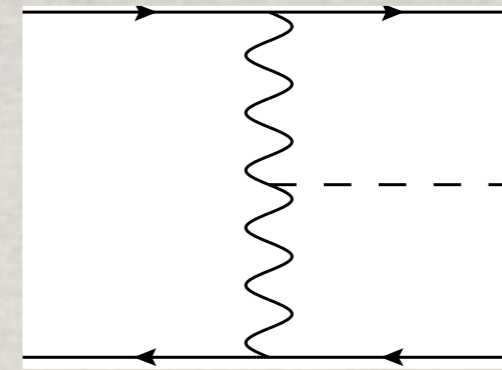


# • Precision Higgs Physics

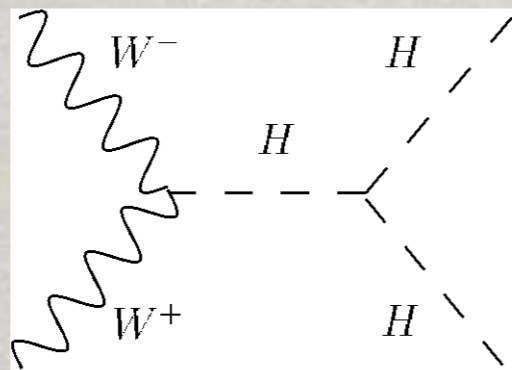
$$\mu^+ \mu^- \rightarrow \nu_\mu \bar{\nu}_\mu H \quad (WW \text{ fusion}),$$

$$\mu^+ \mu^- \rightarrow \mu^+ \mu^- H \quad (ZZ \text{ fusion}).$$

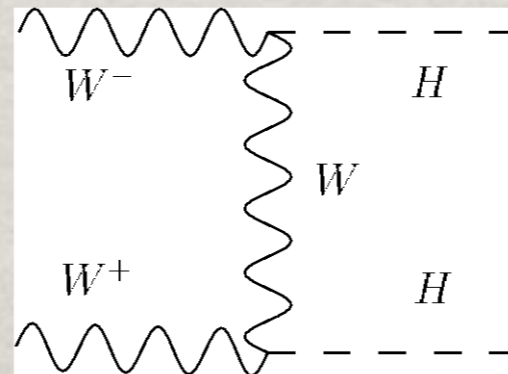
WWH / ZZH couplings



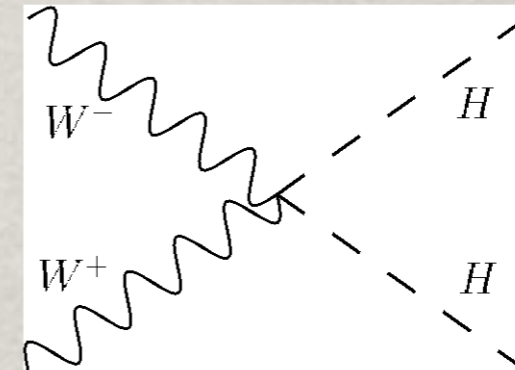
HHH / WWHH couplings:



(a)



(b)



(c)

$\sqrt{s}$ (TeV)	3	6	10	14	30
benchmark lumi ( $\text{ab}^{-1}$ )	1	4	10	20	90
$\sigma$ (fb): <u><math>WW \rightarrow H</math></u>	490	700	830	950	1200
$ZZ \rightarrow H$	51	72	89	96	120
<u><math>WW \rightarrow HH</math></u>	0.80	1.8	3.2	4.3	6.7
$ZZ \rightarrow HH$	0.11	0.24	0.43	0.57	0.91
$WW \rightarrow ZH$	9.5	22	33	42	67
$WW \rightarrow t\bar{t}H$	0.012	0.046	0.090	0.14	0.28
$WW \rightarrow Z$	2200	3100	3600	4200	5200
$WW \rightarrow ZZ$	57	130	200	260	420

10M H

500k HH

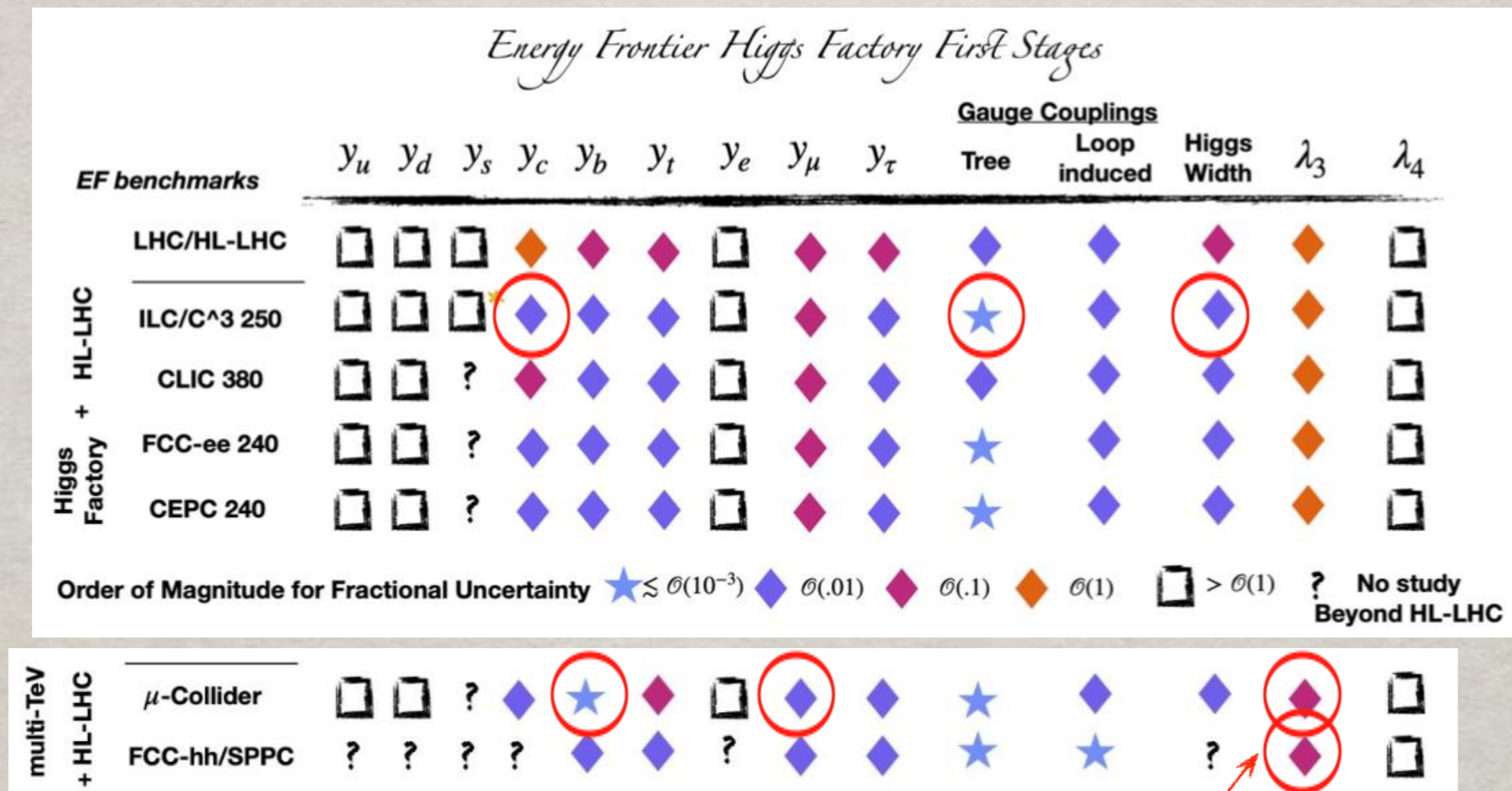
$$\Delta\lambda_{hhh} \sim 2\%,$$

$$\Delta k_{WWhh} \sim 0.2\%$$

TH, D. Liu, I. Low,  
X. Wang, arXiv:2008.12204

# Sensitivity reach for Higgs couplings for Higgs factories and multi-TeV colliders

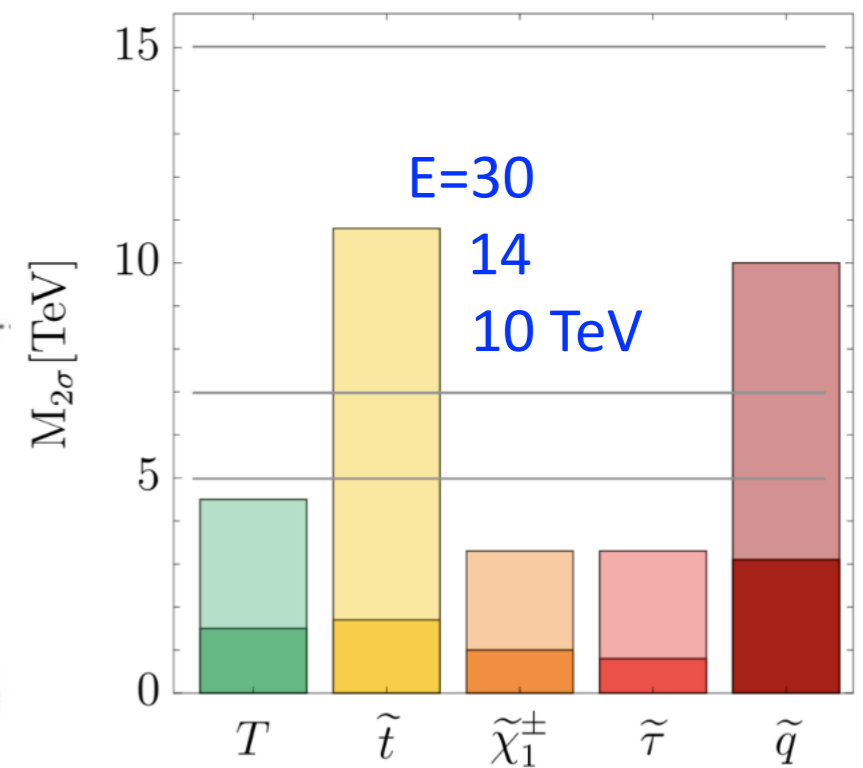
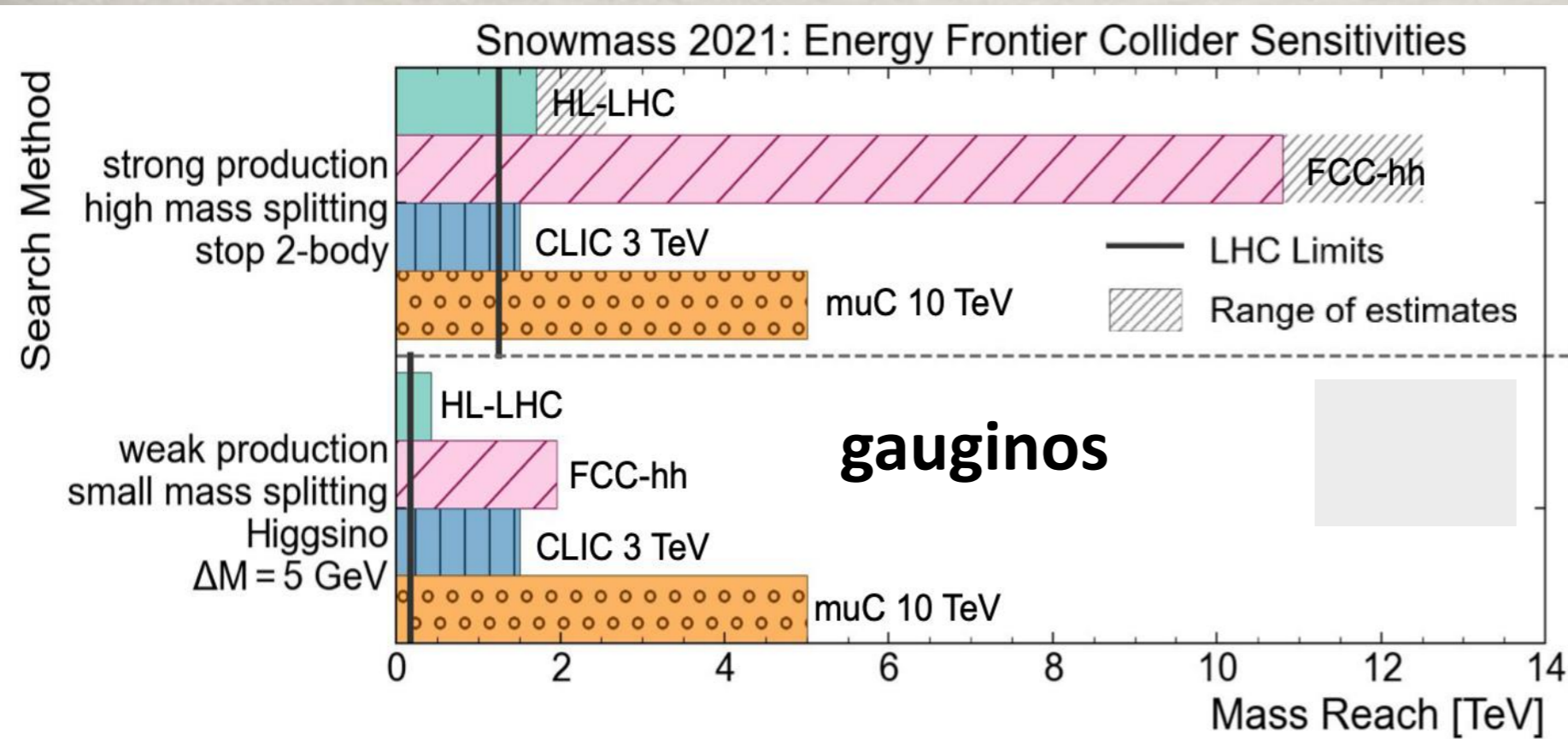
Energy Frontier report: arXiv:2211.11084



Most wanted in order to understand EWSB!

# Pushing the “Naturalness” limit

The searches for top quark partners  
(most wanted in “naturalness”);  
& gluinos, gauginos ...



→ Higgs mass fine-tune:  $\delta m_H/m_H \sim 1\% (1 \text{ TeV}/\Lambda)^2$   
Thus,  $m_{\text{stop}} > 8 \text{ TeV} \rightarrow 10^{-4}$  fine-tune!

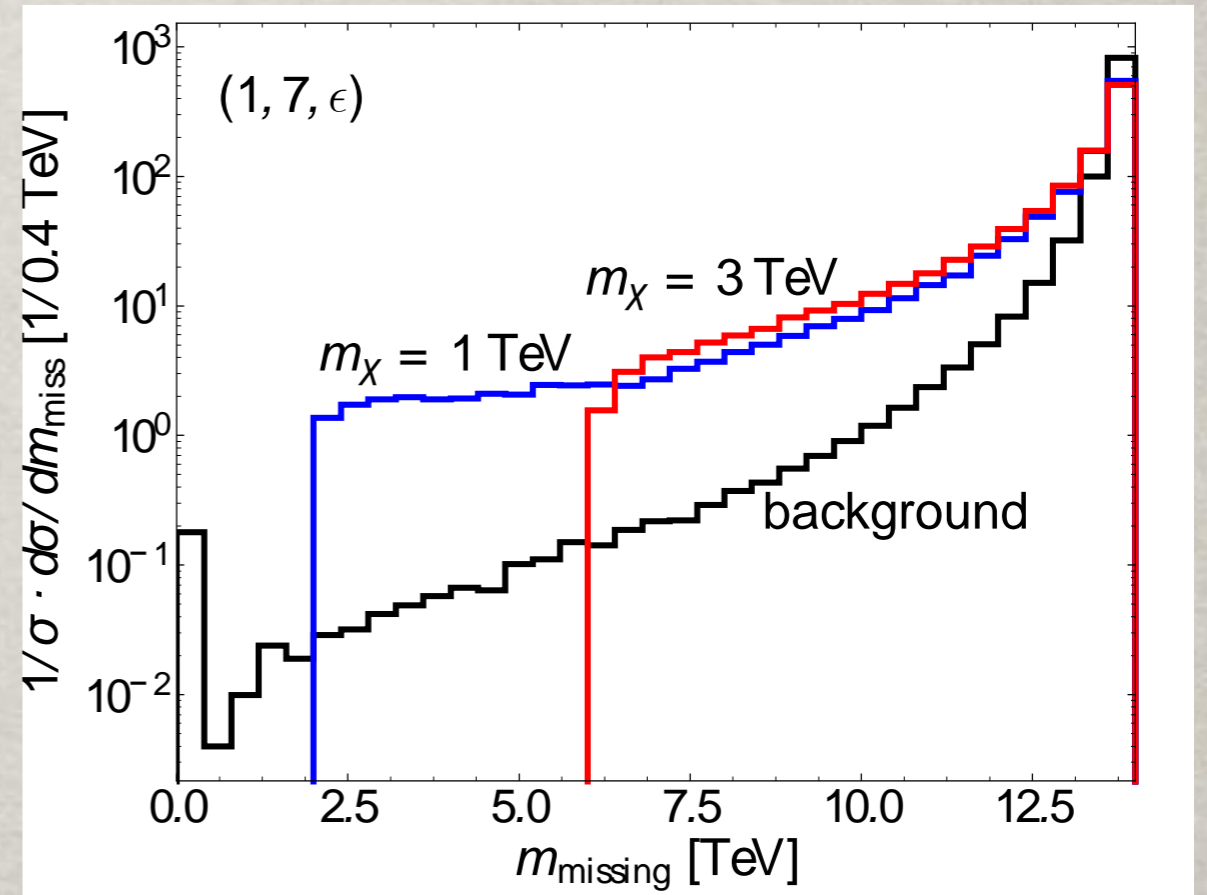
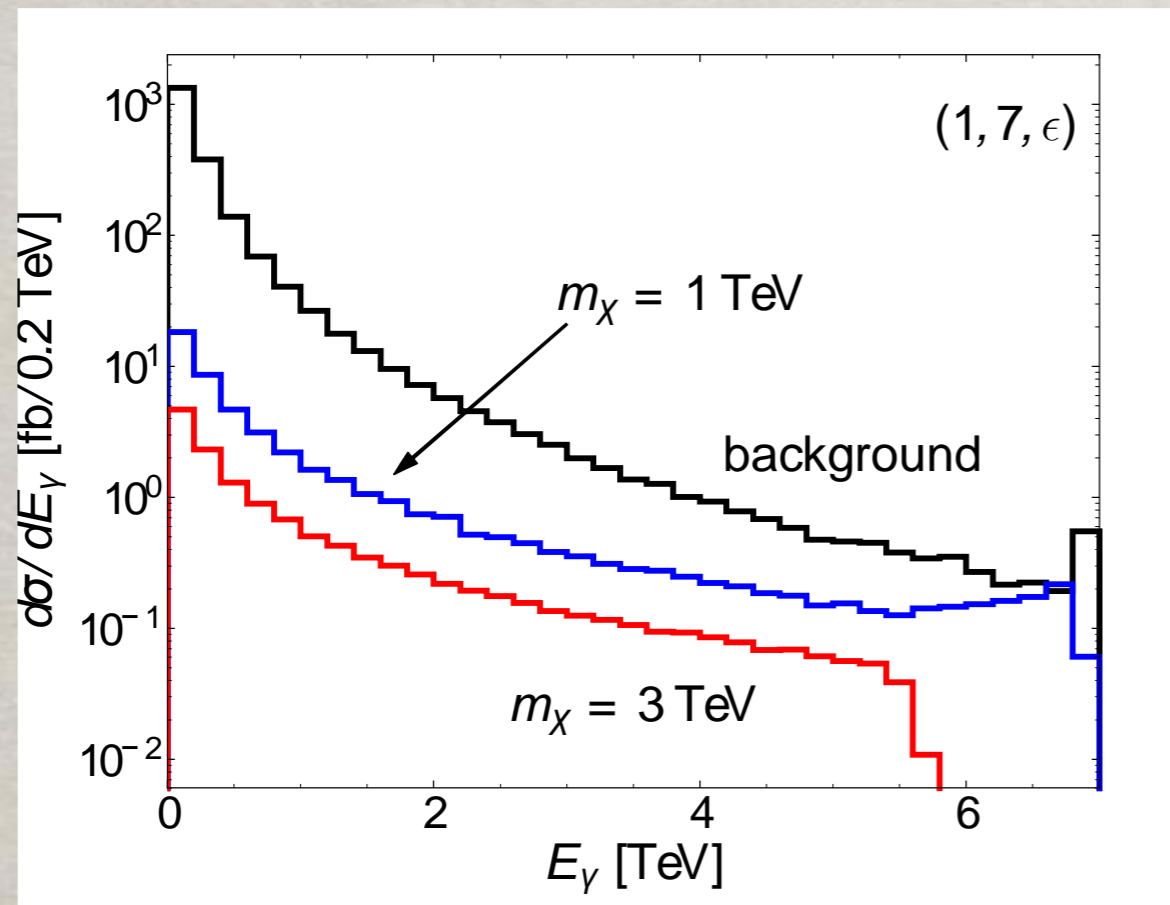
Muon Collider Forum Report: <https://arxiv.org/abs/2209.01318>

# Key feature different from LHC: the “missing mass”

$$m_{\text{missing}}^2 = \mathcal{H}(\sum_i (p_{\mu^+} + p_{\mu^-} - p_i^{\text{obs}})^2)$$

$$E_\gamma < (s - 4m_\chi^2)/2\sqrt{s}$$

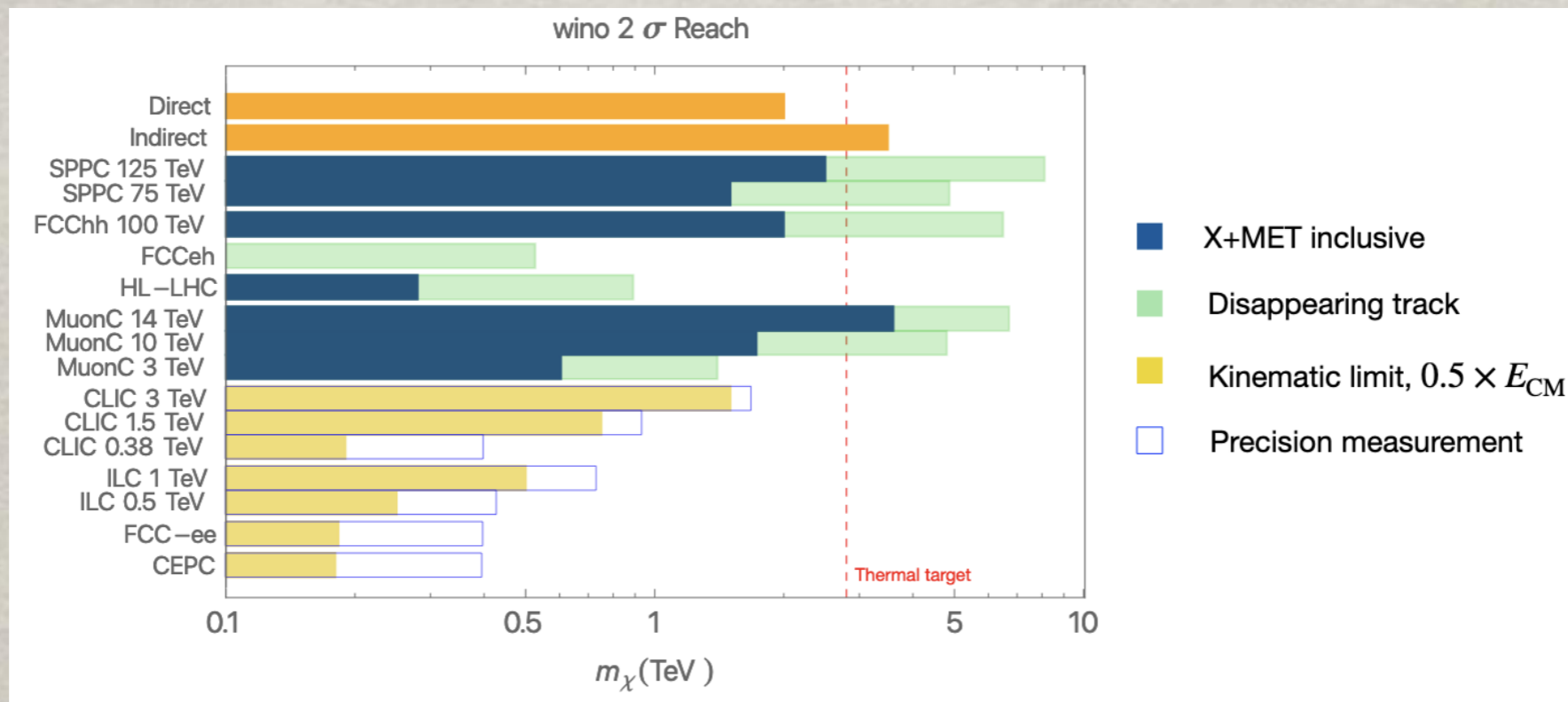
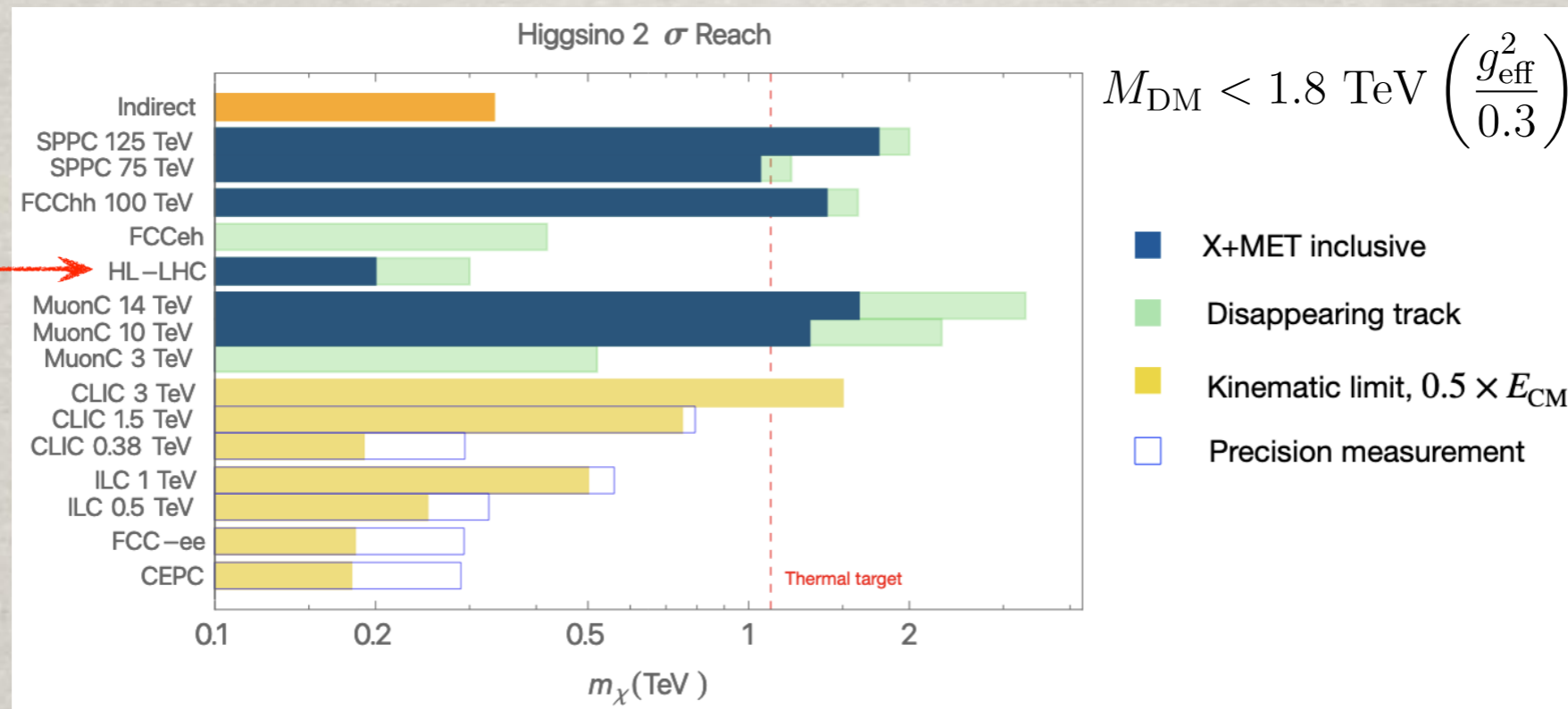
$$m_{\text{missing}}^2 = \mathcal{H}(\sum_i (p_{\mu^+} + p_{\mu^-} - p_\gamma)^2) > 4m_\chi^2$$



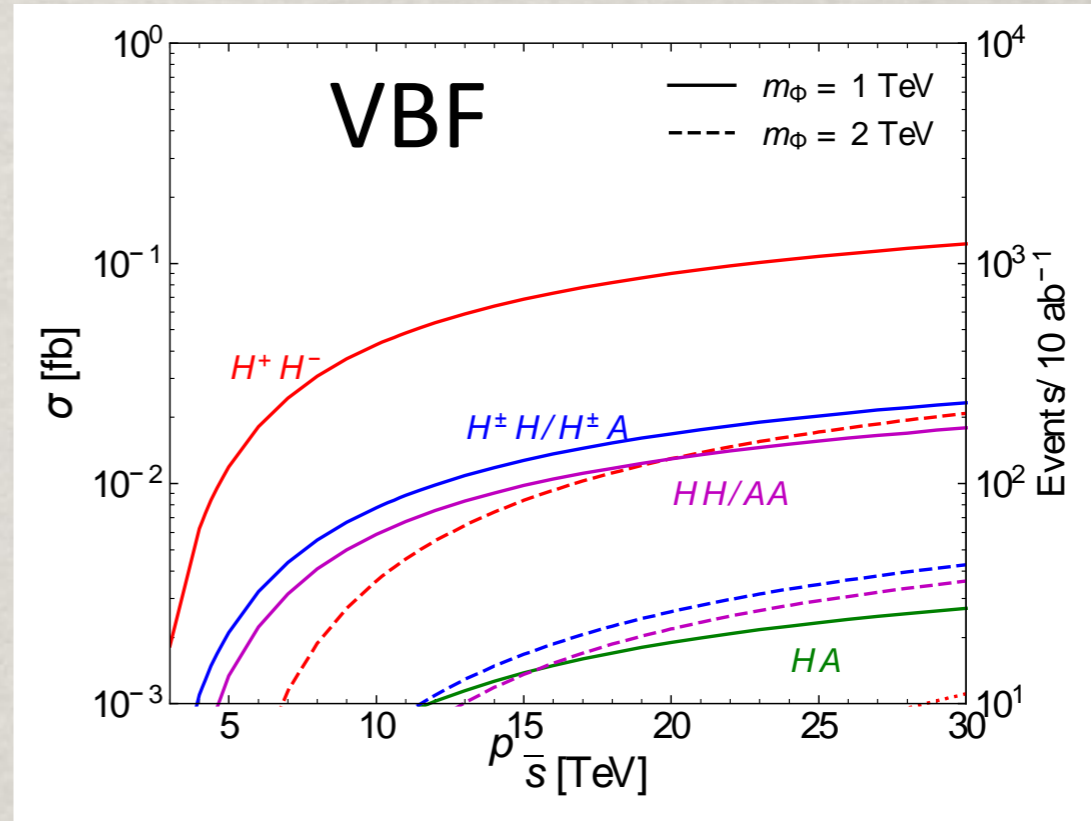
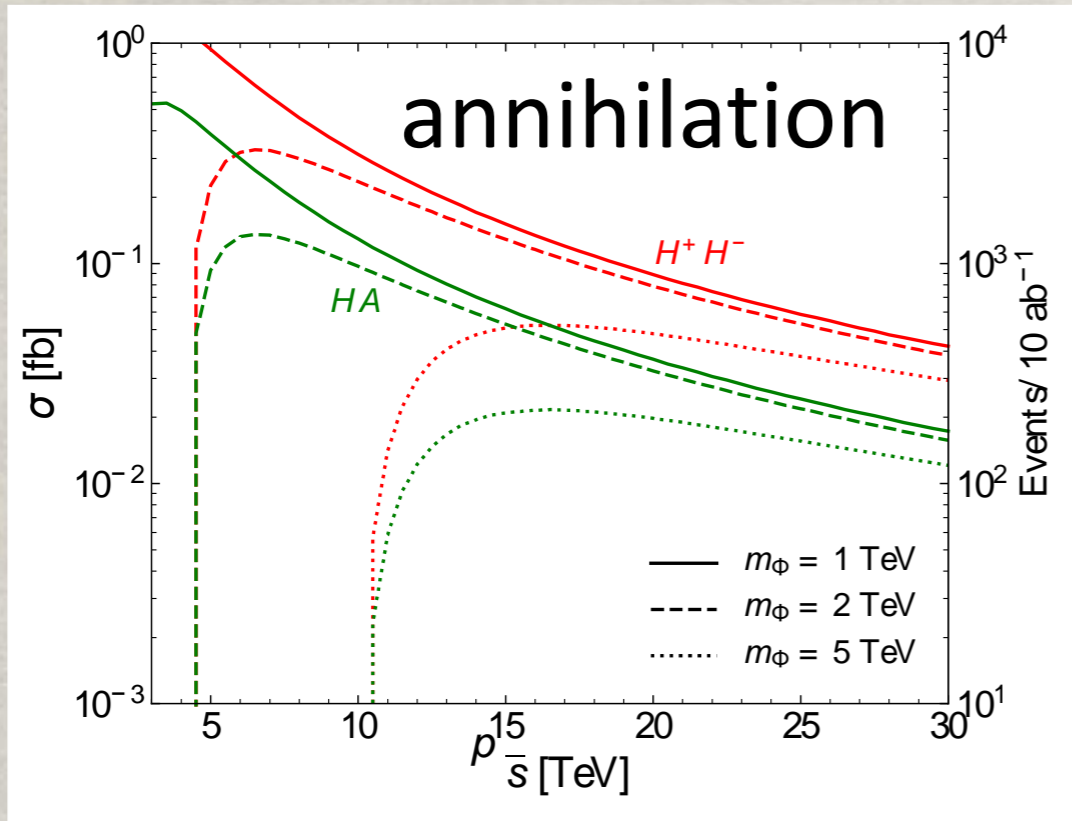
a cone angle cut:  $10^\circ < \theta < 170^\circ$

# WIMP Dark Matter @ Colliders

## Covering the thermal target

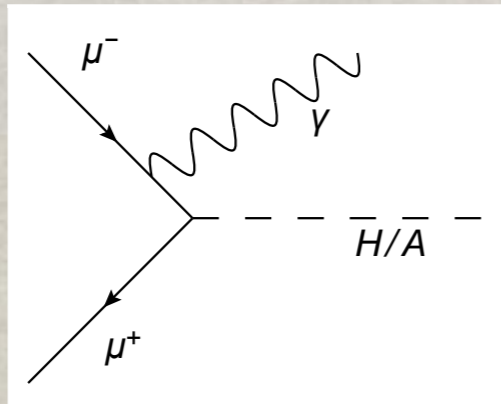


# • Cross/close the threshold: Heavy Higgs Bosons

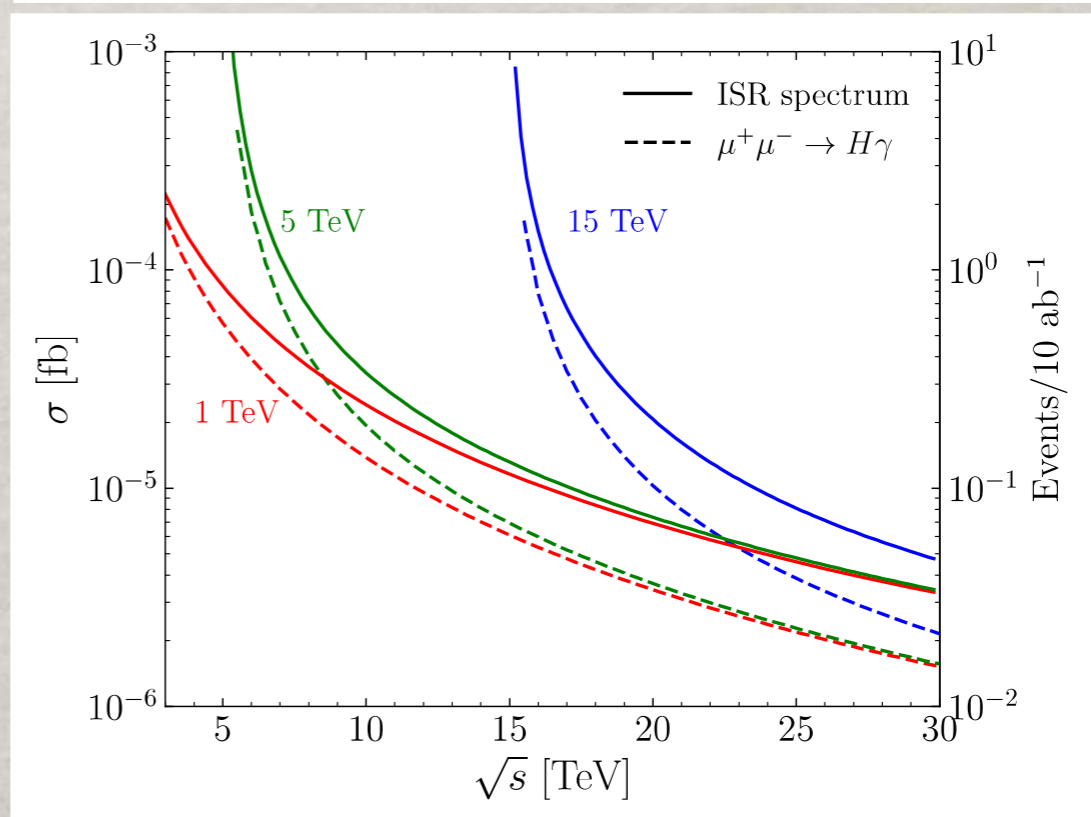


**Radiative returns:**

$$\hat{\sigma}(\mu^+ \mu^- \rightarrow H) = \frac{\hat{Y}_\mu^2}{4} \delta(\hat{s} - m_H^2) = \frac{\hat{Y}_\mu^2}{4s} \delta\left(\frac{s}{M^2} - \frac{m_H^2}{s}\right)$$



Reach  $M \sim E_{\text{cm}}$ !



TH, S. Li, S. Su, W. Su, Y. Wu, arXiv:2102.08386.

# Global activities

## European Strategy activities:

Under CERN Council,  
the Laboratory Directors Group developed

### **European Strategy for Particle Physics Accelerator R&D Roadmap**

Input to European Strategy of Particle Physics:  
High-priority future initiatives:

an international design study for a muon collider, as it represents a unique opportunity to achieve a multi-TeV energy domain beyond the reach of e<sup>+</sup>e<sup>-</sup>-colliders, and potentially within a more compact circular tunnel than for a hadron collider. The biggest challenge remains to produce an intense beam of cooled muons, but novel ideas are being explored;

[arXiv:1901.06150](https://arxiv.org/abs/1901.06150),

CERN-2022-001: [arXiv:2201.07895](https://arxiv.org/abs/2201.07895);

<http://muoncollider.web.cern.ch>

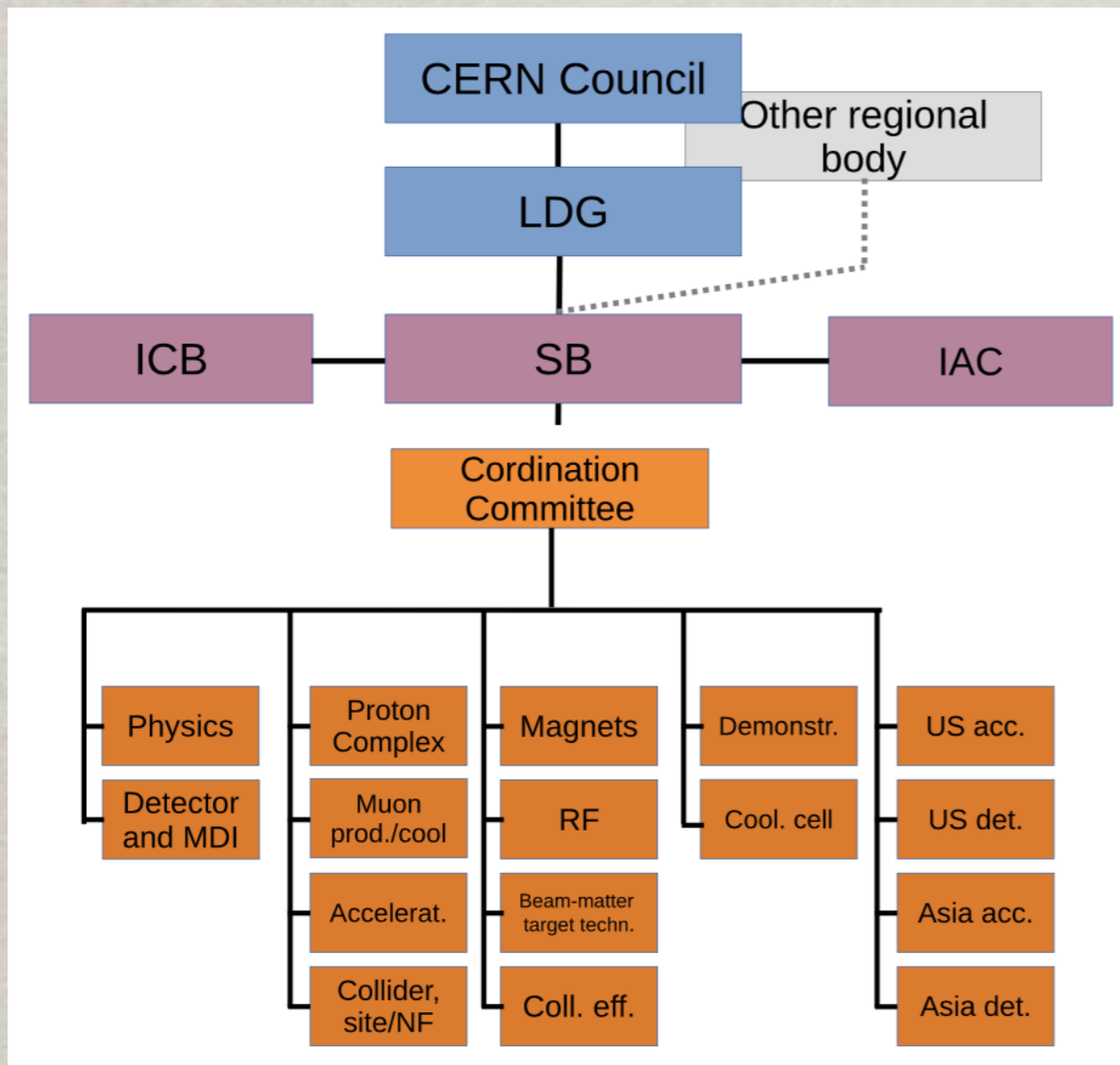




International  
Muon Collider  
Collaboration

# International Muon Collider Collaboration (IMCC, 2022)

European Commission grant: HORIZON INFRA-DEV



## Cordination Committee

- Alexej Grudiev
- Andrea Wulzer
- Antoine Chance
- Anton Lechner
- Chris Rogers
- Christian Carli
- Claude Marchand
- Daniel Schulte (Study Leader)
- Donatella Lucchesi
- Elias Metral
- Jingyu Tang
- Luca Bottura
- Lucio Rossi
- Mark Palmer
- Nadia Pastrone (Collaboration Board Chair)
- Natalia Milas
- Roberto Losito
- Sergo Jindariani
- Steinar Stapnes (Steering Board Chair)

Physics	Andrea Wulzer
Detector and MDI	Donatella Lucchesi

US (detector)	Sergo Jindariani
US (accelerator)	Mark Palmer
Asia (China)	Jingyu Tang

# Snowmass 2021:

In 2020, AF+EF+TF created **Muon Collider Forum**

[https://snowmass21.org/energy/muon\\_forum](https://snowmass21.org/energy/muon_forum)

## Coordinators:

- Kevin Black (University of Wisconsin)
- Sergo Jindariani (FNAL)
- Derun Li (LBNL)
- Fabio Maltoni
- Patrick Meade (Stony Brook University)
- Diktys Stratakis (FNAL)

- Monthly meetings and dedicated workshops
- 160 e-mail subscribers, 50-100 regular participants
- 412 registrants and ~200 participants in the Muon Collider Agora

<https://indico.fnal.gov/event/53010/>

New mailing list: [MuCUS@listserv.fnal.gov](mailto:MuCUS@listserv.fnal.gov)

You can subscribe to the mailing a message to [listserv@fnal.gov](mailto:listserv@fnal.gov)

Leave the subject line blank, and “SUBSCRIBE MUCUS FIRSTNAME LASTNAME”.

**Muon Collider Forum Report delivered**

<https://arxiv.org/abs/2209.01318>

<https://muoncollider.web.cern.ch>

Fermilab on site:

## Site filler Accelerator

➤ **Largest**

**Radius is ~2.65 km**

- **~16.5 km Circumference**
- **~2/3 LHC**

**~RCS accelerator**

If  $B_{ave} = 3\text{ T} \rightarrow E_{\mu} = 2.4\text{ TeV}$   
 ( $B_{max} = 8\text{ T}, B_{pulse} = \pm 2\text{ T}$ )

**Doubled ?**

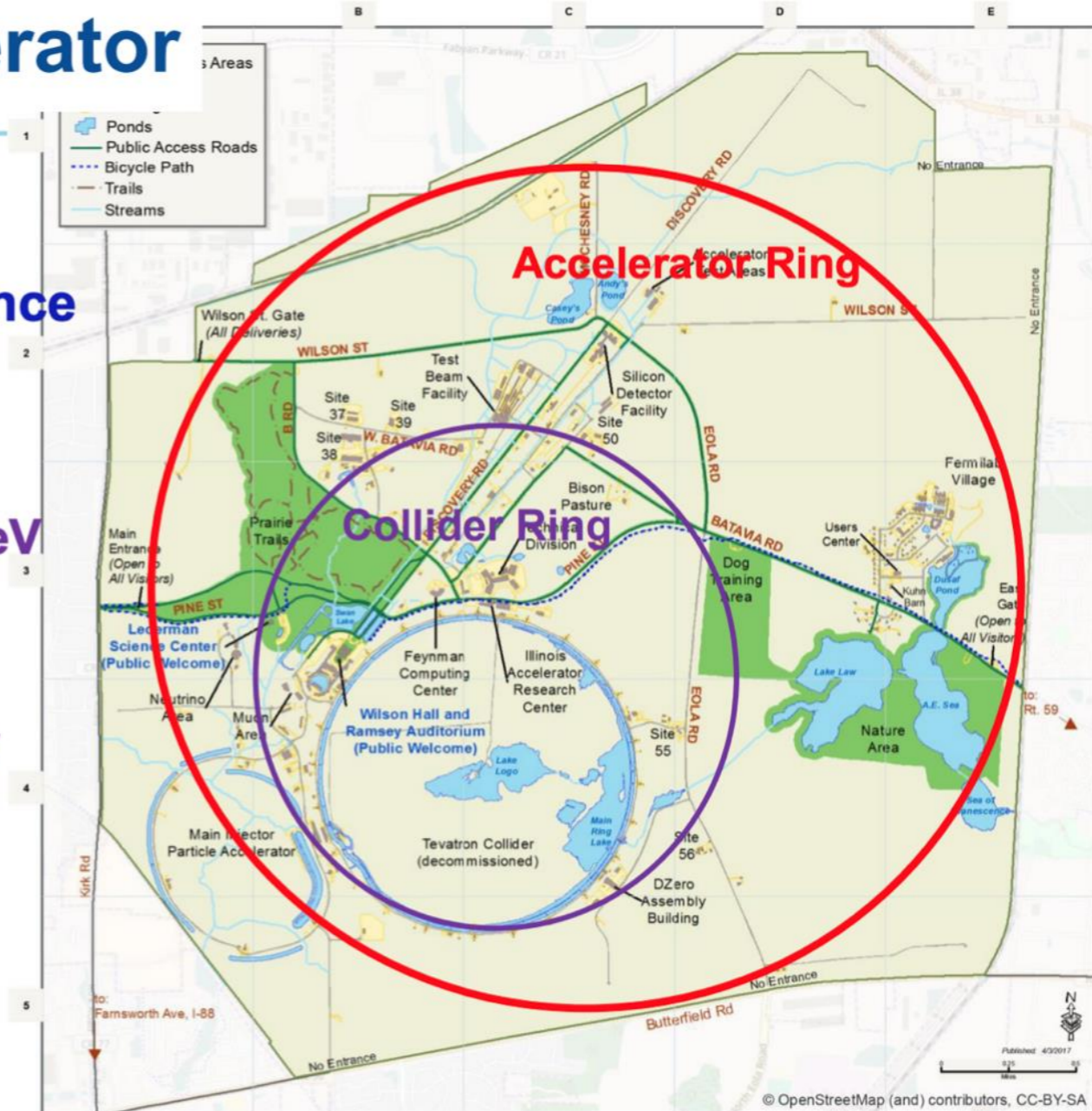
$B_{ave} = 6.3\text{ T} \rightarrow E_{\mu} = 5\text{ TeV}$   
 ( $B_{max} = 16\text{ T}, B_{pulse} = \pm 4\text{ T}$ )

**10 TeV collider**

**Collider Ring ~10 km**

$B_{ave} = 10\text{ T}$

$\tau_{\mu} = 0.104\text{ s}$



# Summary

- **HEP is in an exciting time:**

The SM is complete, and is potentially valid to a very high energy scale. Yet, there are strong indications for the existence of new physics not far above the EW scale.

- **The Higgs factory  $\sim 250$  GeV is the clear target:**

→ New physics under the Higgs lamp-post.

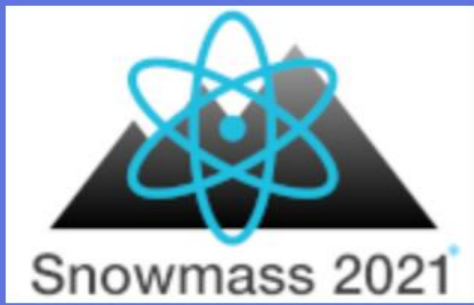
- **Multi-TeV lepton colliders will lead the way:**

**$\mu$  - Col. = Cool !**

→ Promise great opportunities for discoveries for BSM physics.

**Exciting journey ahead !**





DPF Community Planning Exercise

The Particle Physics Community Planning Exercise (a.k.a. "Snowmass") is organized by the Division of Particles and Fields (DPF) of the American Physical Society. Snowmass is a scientific study. It provides an opportunity for the entire particle physics community to come together to identify and document a scientific vision for the future of particle physics in the U.S. and its international partners. Snowmass will define the most important questions for the field of particle physics and identify promising opportunities to address them.

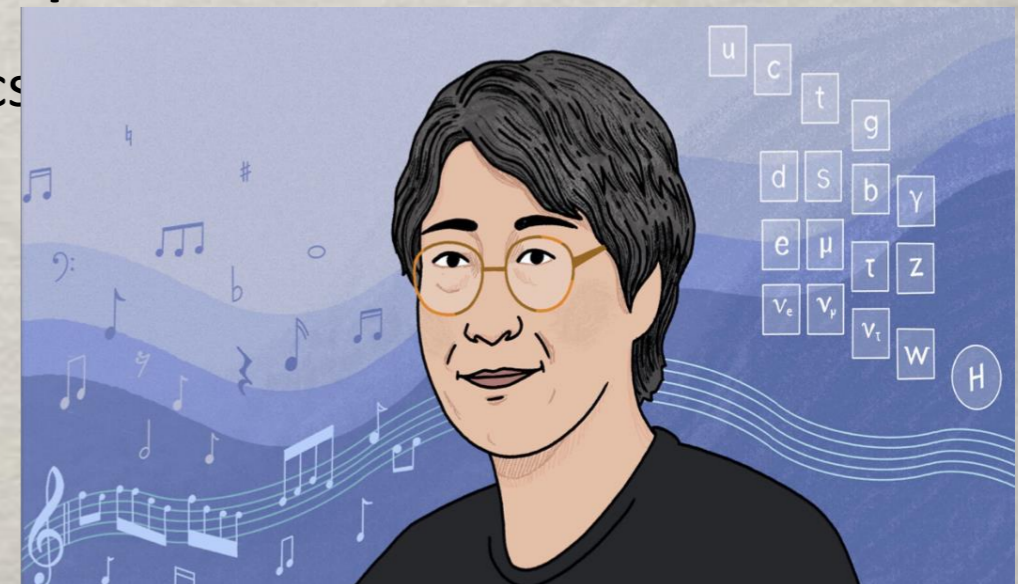
## Snowmass frontiers:

<https://snowmass21.org>

- Energy Frontier
- Neutrino Physics Frontier
- Rare Processes and Precision
- Cosmic Frontier
- Theory Frontier
- Accelerator Frontier
- Instrumentation Frontier
- Computational Frontier
- Underground Facilities
- Community Engagement
- Snowmass Liaisons
- Snowmass Early Career

With this year-long study, the Snowmass output will provide inputs for the prioritization of the research directions of the field in the decade to come: the "P5" process

The P5 chair:  
Prof. Hitoshi Murayama



and

# Several Useful References:

1. Overview of accelerators – V.Shiltsev, [Physics Today \*\*73\*\*, 4, 32 \(2020\)](#).
2. RMP colliders – V.Shiltsev, F.Zimmermann, [Rev.Mod.Phys. \*\*93\*\*, 015006 \(2021\)](#).
3. Ultimate limits of colliders – V.Shiltsev, [Proc. IPAC'21, WEPAB017 \(2021\)](#).
4. Snowmass Accelerator Frontier report – [arxiv:2209.14136](#)
5. ITF Report – T.Roser, V.Shiltsev, et al, [arXiv:2208.06030](#)
6.  $\alpha\beta\gamma$  cost model – V.Shiltsev, [JINST \*\*9\*\* T07002 \(2014\)](#).
7. Crystal collider – V.Shiltsev, [Physics Uspekhi, \*\*55\*\* \(10\), 1033 \(2012\)](#).
8. *CPT*-theorem – V.Shiltsev, [Mod. Phys. Lett. A, \*\*26\*\*, 11, 761 \(2011\)](#)

# Technically Limited Timeline



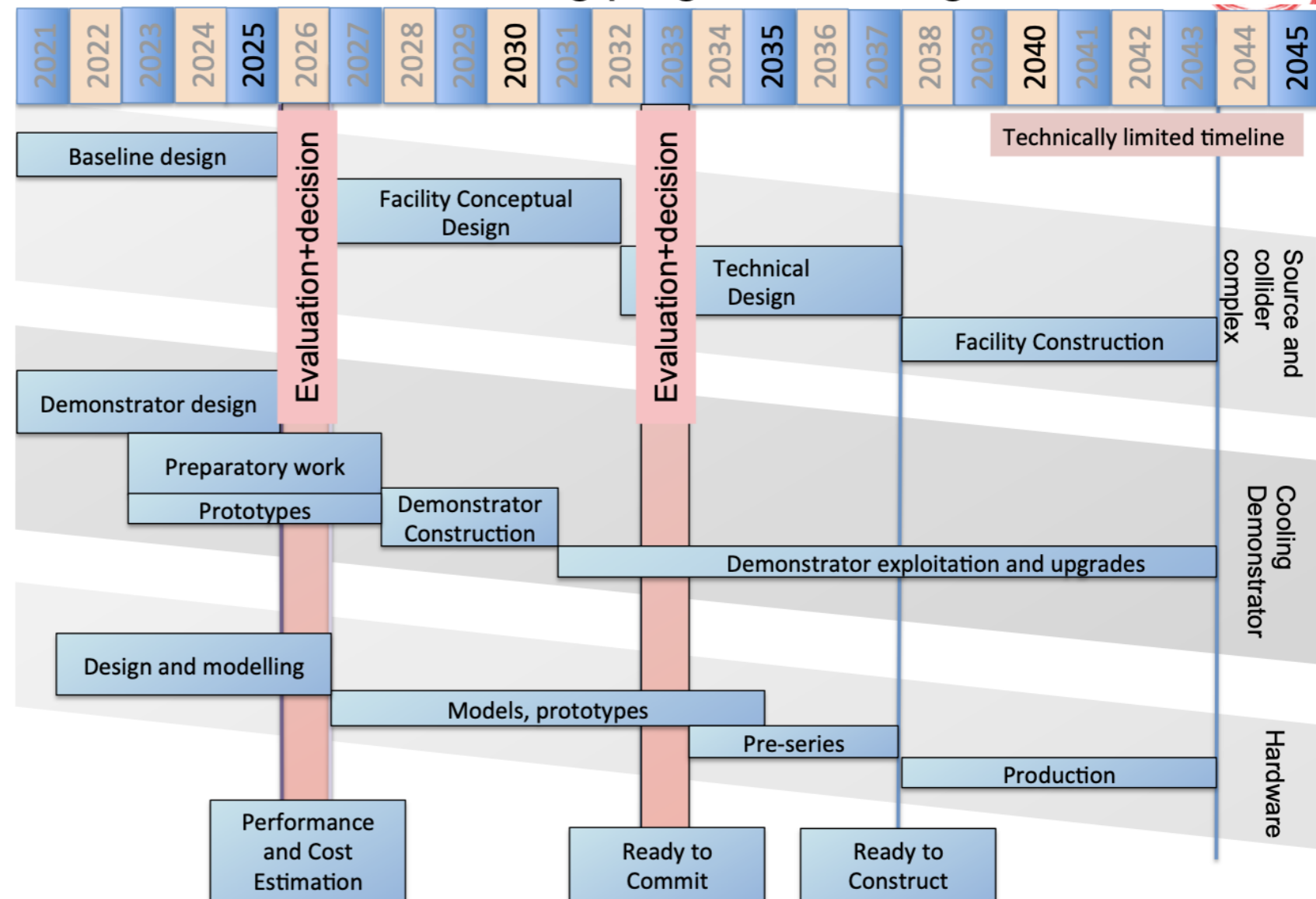
International  
UON Collider  
Collaboration

Muon collider important in the long term

Prudently explore if MuC can be **option as next project**

- e.g. in Europe if higgs factory built elsewhere
- **sufficient funding required now**
- **very strong ramp-up required after 2026**
- might require compromises on initial scope and performance
  - 3 TeV

To be reviewed considering progress, funding and decisions



D. Schulte

Muon Collider, CERN, March 2023

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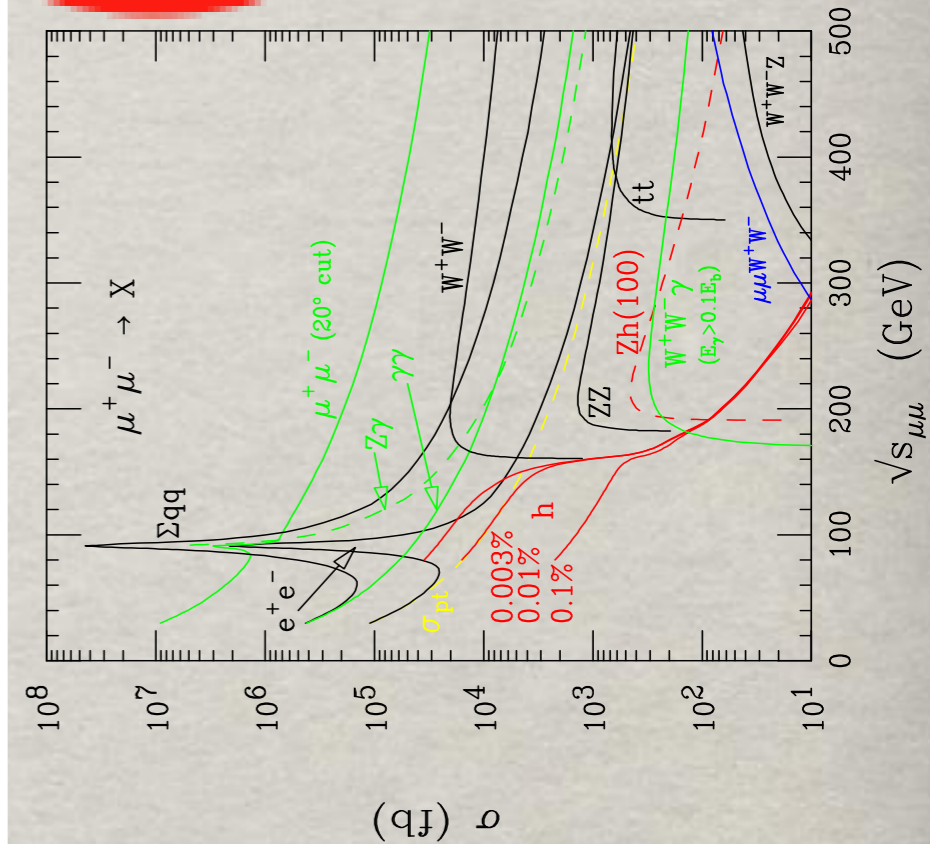
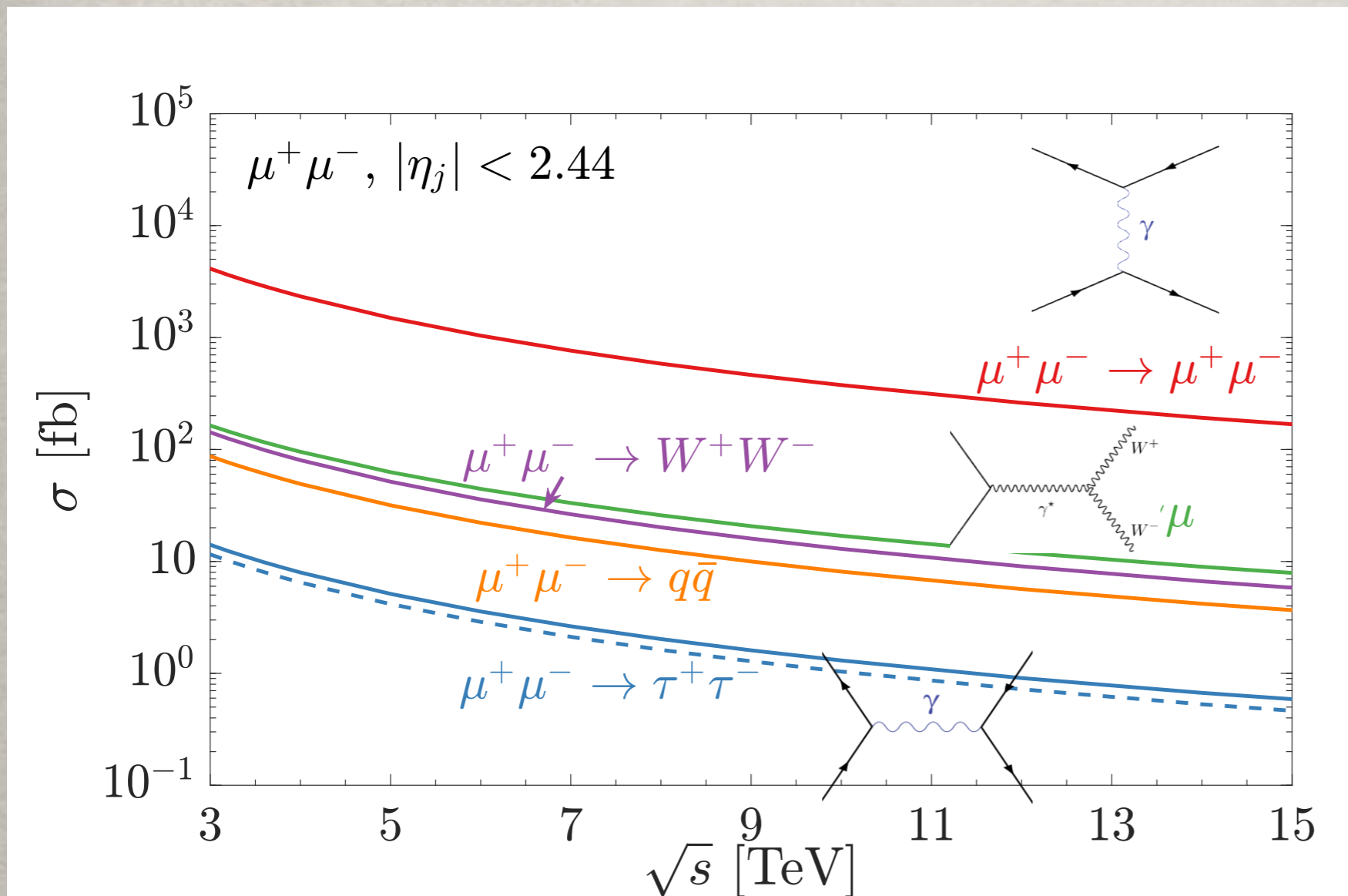
## Implementation Task Force recommendations:

Proposal Name	c.m. energy [TeV]	Luminosity/yr [10 <sup>34</sup> cm <sup>-2</sup> s <sup>-1</sup> ]	Yrs. pre-project R&D	Yrs. to 1st physics	Constr. cost [2021 B\$]	Electr. power [MW]
FCC-ee <sup>1,2</sup>	0.24	7.7 (28.9)	0-2	13-18	12-18	290
CEPC <sup>1,2</sup>	0.24	8.3 (16.6)	0-2	13-18	12-18	340
ILC <sup>3</sup> -0.25	0.25	2.7	0-2	<12	7-12	140
CLIC <sup>3</sup> -0.38	0.38	2.3	0-2	13-18	7-12	110
CCC <sup>3</sup>	0.25	1.3	3-5	13-18	7-12	150
HELEN <sup>3</sup>	0.25	1.4	5-10	13-18	7-12	110
FNAL $e^+e^-$ circ.	0.24	1.2	3-5	13-18	7-12	200
CERC <sup>3</sup>	0.24	78	5-10	19-24	12-30	90
ReLiC <sup>1,3</sup>	0.24	165 (330)	5-10	>25	7-18	315
ERLC <sup>3</sup>	0.24	90	5-10	>25	12-18	250
XCC $\gamma\gamma$	0.125	0.1	5-10	19-24	4-7	90
$\mu\mu$ -Higgs	0.13	0.01	>10	19-24	4-7	200
ILC-3	3	6.1	5-10	19-24	18-30	~400
CLIC-3	3	5.9	3-5	19-24	18-30	~550
CCC-3	3	6.0	3-5	19-24	12-18	~700
ReLiC-3	3	47(94)	5-10	>25	30-50	~780
$\mu\mu$ Collider <sup>1-3</sup>	3	2.3(4.6)	>10	19-24	7-12	~230
LWFA-LC-3	3	10	>10	>25	12-80	~340
PWFA-LC-3	3	10	>10	19-24	12-30	~230
SWFA-LC-3	3	10	5-10	>25	12-30	~170
FNAL $\mu\mu$ <sup>1</sup>	6-10	20(40)	>10	19-24	12-18	~300
LWFA-LC-15	15	50	>10	>25	18-80	~1030
PWFA-LC-15	15	50	>10	>25	18-50	~620
SWFA-LC-15	15	50	>10	>25	18-50	~450
FNAL $pp$ circ.	24	3.5(7)	>10	>25	18-30	~400
FCC-hh <sup>1</sup>	100	30(60)	>10	>25	30-50	~560
SPPS <sup>1</sup>	125	13(26)	>10	>25	30-50	~400
LHeC	1.2	1	0-2 ?	13-18	<4	~140
FCC-eh	3.5	1	0-2 ?	>25	<4	~140
CEPC-SPPC-ep	5.5	0.37	3-5	>25	<4	~300

# A Multi-TeV Muon Collider

Naïve expectation: leading-order  $\mu^+\mu^-$  annihilation:

$$\sigma_{ann} \sim \frac{\alpha^2}{s}$$



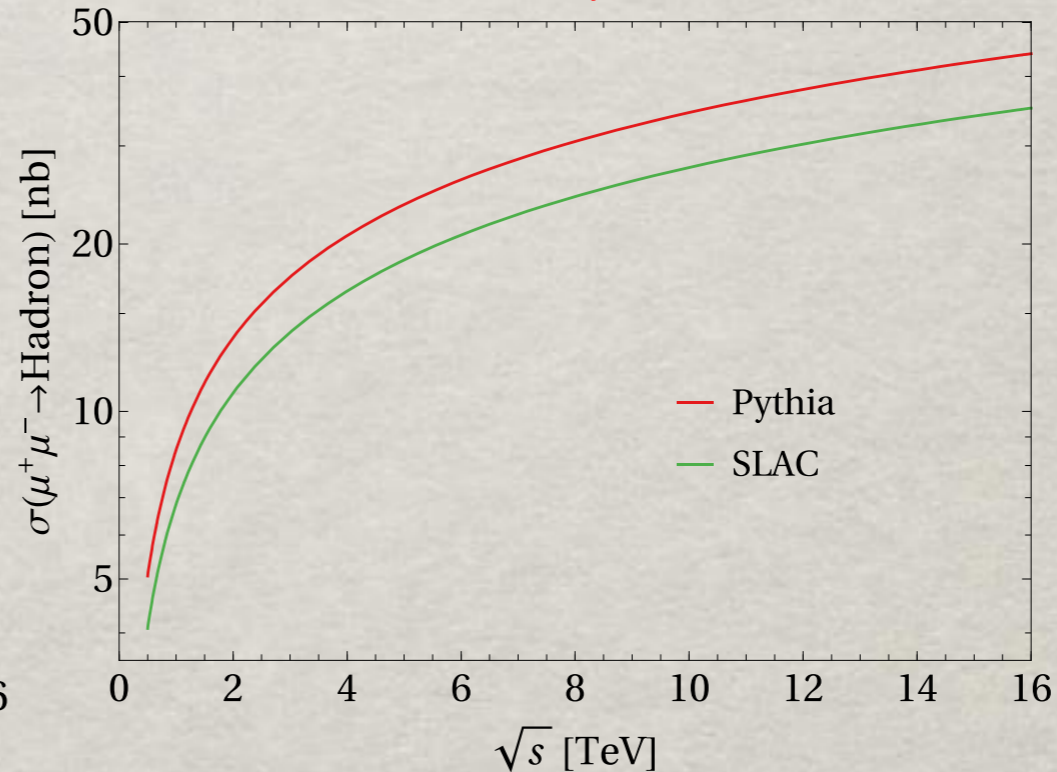
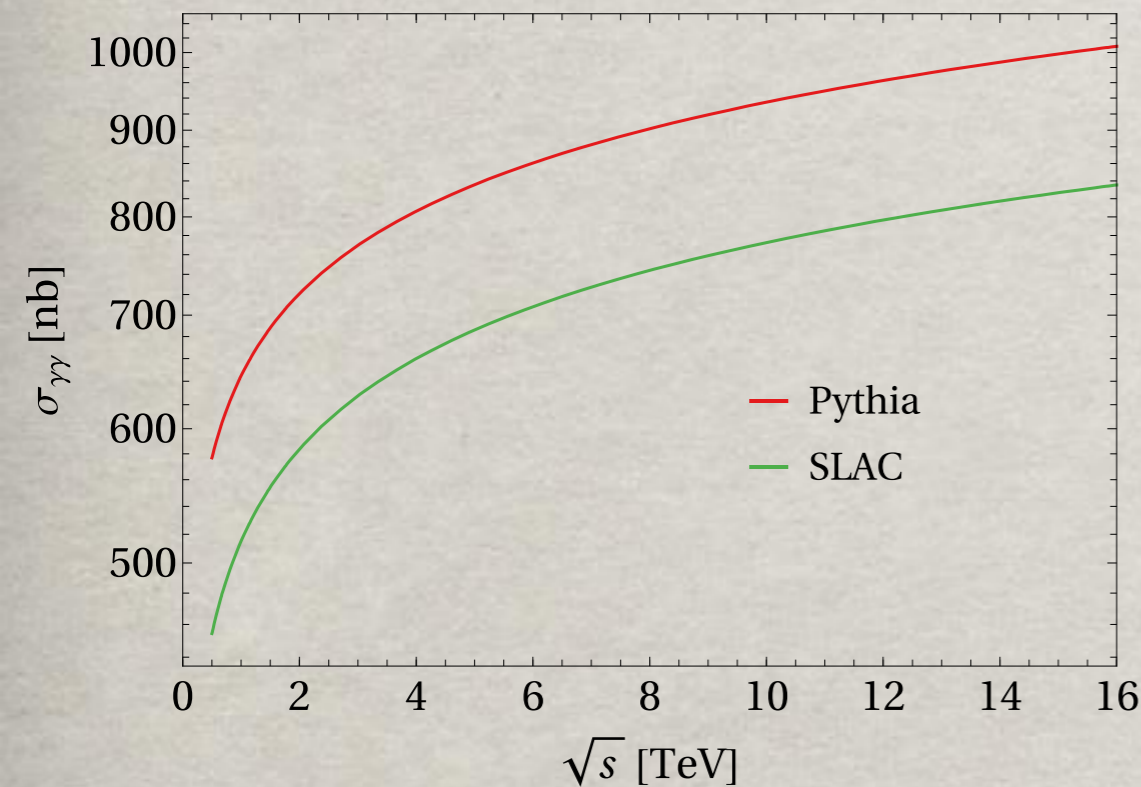
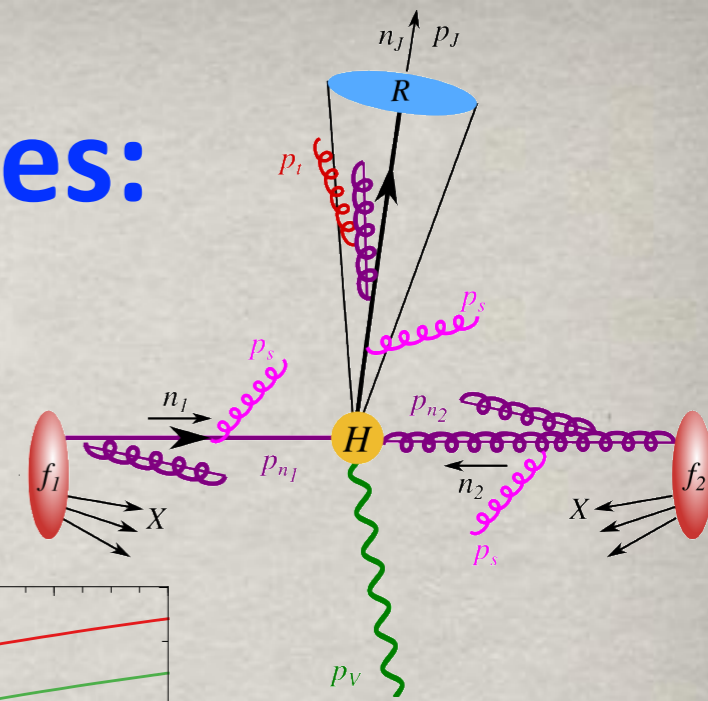
Those aren't what you would first see when you turned on the machine!

# Total cross section @ high energies:

$\gamma\gamma$  and  $\mu^+\mu^- \rightarrow$  hadrons

$$\sigma_{\gamma\gamma}(E_{\text{cm}}^2) = 200 \text{ nb} (1 + 0.0063 [\ln(E_{\text{cm}}^2 \text{ GeV}^{-2})]^{2.1} + 1.96 (E_{\text{cm}}^2 \text{ GeV}^{-2})^{-0.37})$$

Event rate @ 10,000 Hz!



Note:  $\sigma_{pp}(\text{total}) \sim 100 \text{ mb}$ ;  $\sigma_{\mu\mu}(\text{total}) \sim 50 \text{ nb}$

Events populated at  $p_{\text{T}}^{\text{hadrons}} < \text{a few GeV}$

TH, Yang Ma, Keping Xie, arXiv:2103.09844.

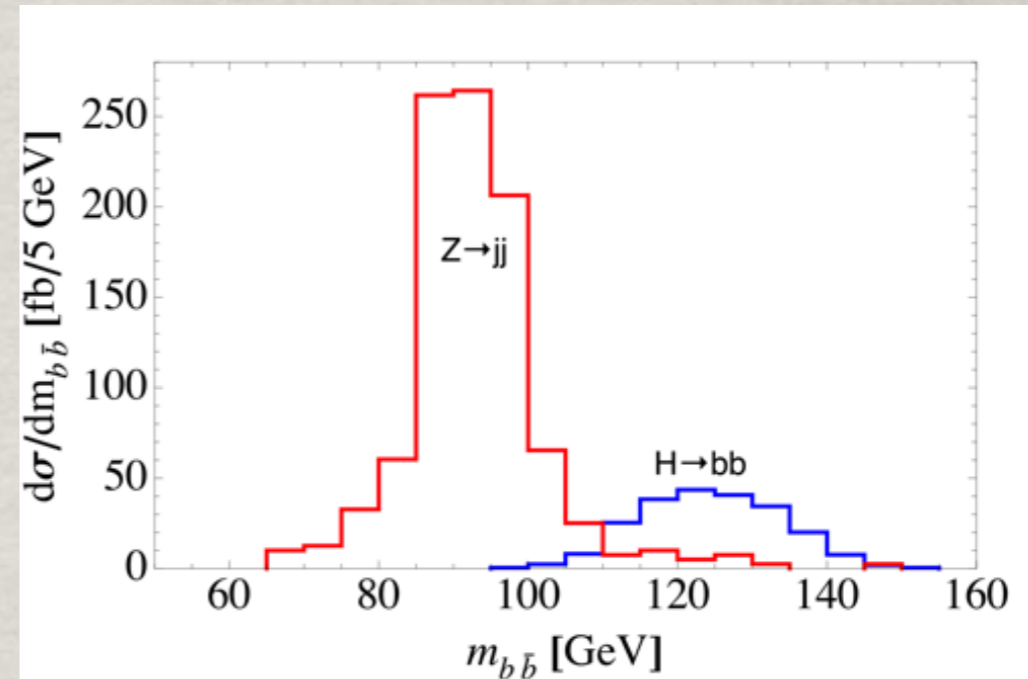
T. Barklow, D. Dannheim, M.O. Sahin & D. Schulte, LCD-Note-2011-020.

# Achievable accuracies

Leading channel  $H \rightarrow bb$ :

$$\Delta E/E = 10\%.$$

$$10^\circ < \sqrt{\mu^\pm} < 170^\circ.$$



$$\mathcal{L} \supset \left( M_W^2 W_\mu^+ W^{-\mu} + \frac{1}{2} M_Z^2 Z_\mu Z^\mu \right) \left( \kappa_V \frac{2H}{v} + \kappa_{V_2} \frac{H^2}{v^2} \right) - \frac{m_H^2}{2v} \left( \kappa_3 H^3 + \frac{1}{4v} \kappa_4 H^4 \right)$$

$\rho_{\bar{s}}$ (lumi.)	3 TeV (1 ab <sup>-1</sup> )	6 (4)	10 (10)	14 (20)	16 (90)	Comparison
$WWH$ ( $\Delta \kappa_W$ )	0.26%	0.12%	0.073%	0.050%	0.023%	0.1% [41]
$\sqrt{\rho_{\bar{c}_i}}$ (TeV)	4.7	7.0	9.0	11	16	(68% C.L.)
$ZZH$ ( $\Delta \kappa_Z$ )	1.4%	0.89%	0.61%	0.46%	0.21%	0.13% [17]
$\sqrt{\rho_{\bar{c}_i}}$ (TeV)	2.1	2.6	3.2	3.6	5.3	(95% C.L.)
$WWHH$ ( $\Delta \kappa_{W_2}$ )	5.3%	1.3%	0.62%	0.41%	0.20%	5% [36]
$\sqrt{\rho_{\bar{c}_i}}$ (TeV)	1.1	2.1	3.1	3.8	5.5	(68% C.L.)
$HHH$ ( $\Delta \kappa_3$ )	25%	10%	5.6%	3.9%	2.0%	5% [22, 23]
$\sqrt{\rho_{\bar{c}_i}}$ (TeV)	0.49	0.77	1.0	1.2	1.7	(68% C.L.)

Table 7: Summary table of the expected accuracies at 95% C.L. for the Higgs couplings at a variety of muon collider energies and luminosities.