

# Using exclusive b-hadron decays as hemisphere taggers for a precise $A_{FB}^b$ and $R_b$ determination

FCC-ee Electroweak Precision – Progress Meeting

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**04/18/2023**

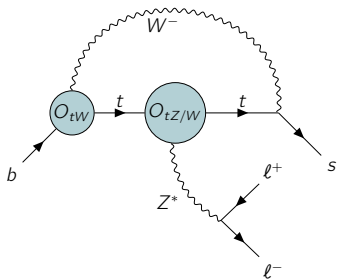
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# Motivation

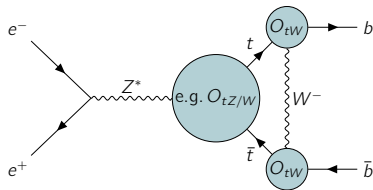
- Combination of top- and beauty energy scales to constrain dimension-6 operators in SMEFT
- Anomalies at  $\mathcal{O}(m_B)$  and  $\mathcal{O}(m_Z)$  **translate to higher energy scale**

$\mathcal{O}(m_B) \sim 5 \text{ GeV}$



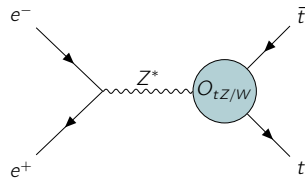
$\Rightarrow b \rightarrow s$  FCNCs

$\mathcal{O}(m_Z) \sim 90 \text{ GeV}$



$\Rightarrow \approx 1\%$  of  $R_b = \frac{\Gamma_{Z \rightarrow b\bar{b}}}{\Gamma_{Z \rightarrow q\bar{q}}}$  in the SM

$\mathcal{O}(m_t) \sim 350 \text{ GeV}$

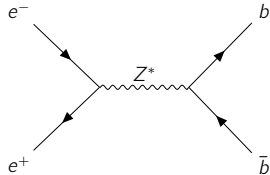


$\Rightarrow$  Modification of e. g. the  $t$  forward-backward asym.

- **High precision** and **variety of observables** is the key to extract tight constraints  
 $\rightarrow$  **To which extent can FCC-ee improve them?**

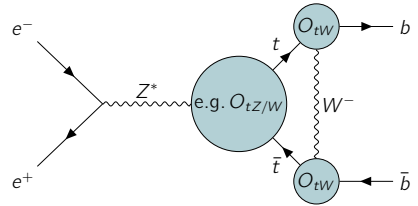
# Measurements at the $Z$ -pole: $R_b$ and $A_{\text{FB}}^b$

- $\mathcal{O}(10^{12})$   $Z \rightarrow b\bar{b}$  events @FCC-ee: measurements **systematically limited**  
 → need for novel approaches to reduce to the scale of the statistical one
- Prominent observables at the  $Z$ -pole:  $A_{\text{FB}}^b$  and  $R_b$  with potential for SM-deviation within current uncertainties



Tree-level contribution.

(+)



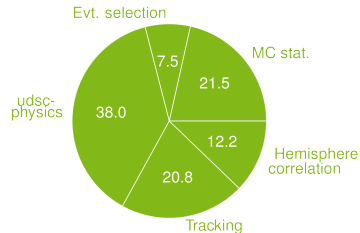
$Zbb$ -vertex correction, contribution  $\approx 1\%$ .

→ Taking  $Zbb$ -vertex corrections for  $R_b$  into account:  $\frac{\Delta R_b^{\text{LEP}}}{R_b^{\text{tree-level}} - R_b^{\text{SM}}} \approx 40\%$

- Today: guide through a novel hemisphere tagger and its proof of principle  
 → **Application on  $R_b$  (further discussed here) and  $A_{\text{FB}}^b$  and evaluation of the systematic uncertainties**

# Novel hemisphere tagger

- À la LEP: Tagging of hemispheres based on lifetime of  $b$ -hadrons and  $b/c$ -hadron mass difference
- From ALEPH collaboration [1]:  
 $R_b = 0.2167 \pm 0.0011$  (stat.)  $\pm 0.0013$  (syst.)  
→ Systematic uncertainty dominated by light-quark and  $c$ -physics + MC statistics



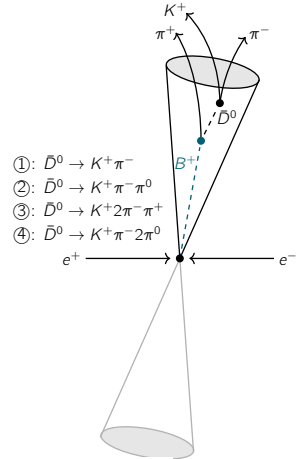
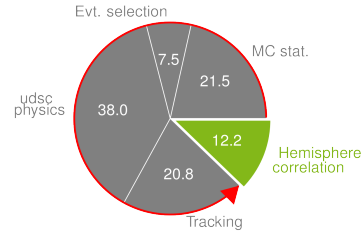
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## Novel approach to tag hemispheres

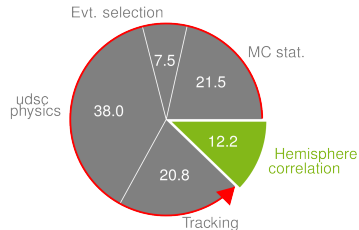
Tag the hemispheres by exclusively reconstruct  $b$ -hadrons with a potential purity of  $P = 100\%$  and an efficiency of  $\epsilon \approx 1\%$

- Efficiency of 1% in reach with a list of  $b$ -hadron ( $B^+, B^0, B_s, \Lambda_b^0$ ) decay modes (at max.  $2\pi^0$ ):
  1. **Charmonium modes**, e. g.  $B^+ \rightarrow J/\psi K^+$
  2. Modes with **one and two charm-mesons**, e. g.  $B^+ \rightarrow \bar{D}^0 \pi^+$  and  $B^+ \rightarrow \bar{D}^0 D_s^+$
  3. **Baryon decays**, e. g.  $\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^+ 2\pi^-$
- Can proof an efficiency of **1.11%** from PDG-search ✓  
 ↔ Reconstruction efficiencies not taken into account!



# Advantages and starting point

- Exclusive  $b$ -hadron reconstruction: **No contribution from light-quark and  $c$ -physics** → Reduction of major systematic uncertainty
- Proof of principle (including all uncertainty correlations):



## À la LEP with FCC-ee statistics

- Using efficiencies from ALEPH collaboration [1] by including light-quark physics
- Statistical uncertainty:  
 $\Delta R_b(\text{stat.}) = 2.022 \cdot 10^{-6}$
- $\Delta R_b(\text{syst.}) = \Delta R_b^{\text{LEP}}(\text{syst.}) = \mathcal{O}(10^{-4})$

## Exclusive $b$ -hadron decays

- No contribution from  $udsc$  physics:  
 $\epsilon_{c,uds} \rightarrow 0.0$  and  $\epsilon_b = 1\%$
- Statistical uncertainty:  
 $\Delta R_b(\text{stat.}) = 4.570 \cdot 10^{-5}$
- Reduce  $\Delta R_b(\text{syst.})$  to  $\mathcal{O}(\Delta R_b(\text{stat.}))$

↔ Reduction of major source of systematic uncertainty to the cost of statistical uncertainty, still: **factor 20 improvement wrt. LEP**

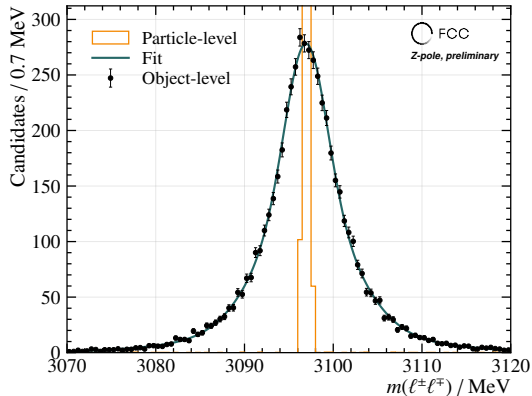
- Purity and reconstruction efficiency evaluated on winter2023 samples with  $10^7$  events each:  
 $Z \rightarrow b\bar{b}$ ,  $Z \rightarrow c\bar{c}$ ,  $Z \rightarrow s\bar{s}$ ,  $Z \rightarrow u\bar{d}u\bar{d}$
- Vertexing information (still) taken from MC + inclusion of partially reconstructed particles
- Evaluation of the vertexing assumptions WIP

# Representative decay modes

- Examined a number of representative decays:  $B^+ \rightarrow J/\psi K^+$ ,  $B^+ \rightarrow \bar{D}^0 \pi^+$ ,  $B^+ \rightarrow \bar{D}^0 D_s^+$  with  $\bar{D}^0 \rightarrow K^+ \pi^- (\pi^0)$ ,  $\bar{D}^0 \rightarrow K^+ 2\pi^- \pi^+$  and  $D_s^+ \rightarrow K^+ \pi^- \pi^+$
- To emulate vertexing resolution: charged particles have to have  $< 50 \mu\text{m}$  displacement
- **Flight distance cut:**  $B^+$ -PV displacement  $> 300 \mu\text{m} \rightarrow \epsilon_{\text{PV-displacement}} = 89.59 \%$

$B^+ \rightarrow J/\psi K^+ \rightarrow \ell\ell K^+$

- Reconstruction of the leptonic  $J/\psi$  mode:  $\mu = 3096.89 \text{ MeV}$ ,  $\sigma_{\text{comb.}} = 3.98 \text{ MeV}$



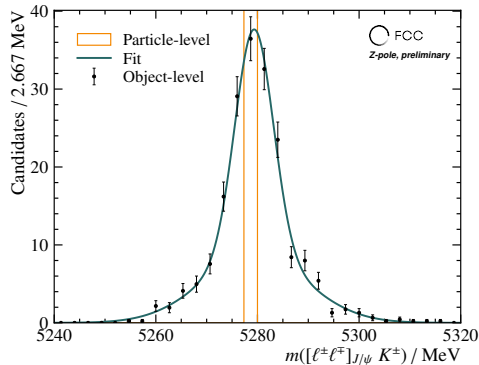
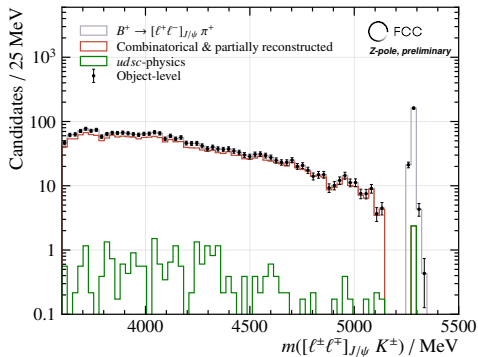
## Reconstruction efficiency

- Produced  $J/\psi \rightarrow \ell\ell$  in the sample: 26 340
- Reconstructed, truth-matched  $J/\psi \rightarrow \ell\ell$ : 25 527

$$\hookrightarrow \epsilon_{[3070,3120] \text{ MeV}}(J/\psi \rightarrow \ell\ell) = 96.91 \%$$

# $B^+ \rightarrow J/\psi K^+ \rightarrow \ell\ell K^+$ reconstruction

- $J/\psi$  candidates accepted in  $m_{\ell\ell} \in [3070, 3120]$  MeV window
- Charged kaon added to the system and vertex displacement cut applied
- Fit results to the truth-matched  $B^+$  signal (right):  $\mu = 5279.35$  MeV,  $\sigma_{\text{comb.}} = 5.00$  MeV

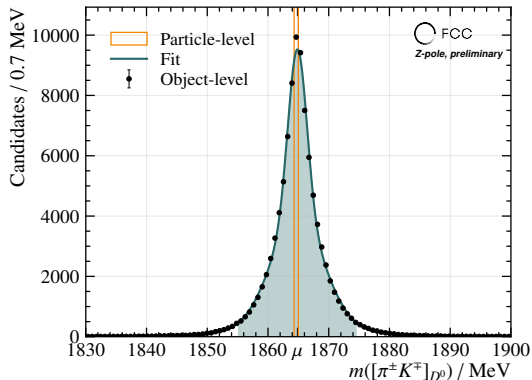


- **Reconstruction efficiency**  $B^+ \rightarrow J/\psi K^+ \rightarrow \ell\ell K^+$ : 85.67 %
  - **Purity**  $P_{B^+ \rightarrow J/\psi K^+} = 98.73$  % within  $m_{B^+} \in [5240, 5320]$  MeV
- Purity could further be improved by also accepting also partially reconstructed candidates ( $B^+ \rightarrow J/\psi K^0 \pi^+$ ,  $B^+ \rightarrow J/\psi K^+ \pi^+ \pi^-$ , ...)



# Fully charged $\bar{D}^0$ decay: $B^+ \rightarrow \bar{D}^0 \pi^+ \rightarrow K^+ \pi^- \pi^+$

- Charged pion and kaon collection combined with opposite charges to emerge from the same hemisphere
- Vertexing between kaon and pion  $< 50 \mu\text{m}$
- Triple-Gaussian distribution applied to fit the mass peak and to determine  $3\sigma$  intervals (colored region)  
 $\rightarrow \mu = 1864.85 \text{ MeV}, \sigma_{\text{comb.}} = 3.72 \text{ MeV}$

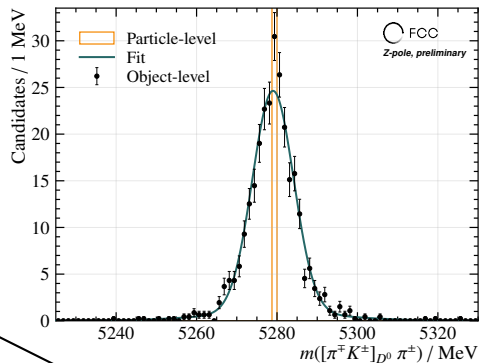
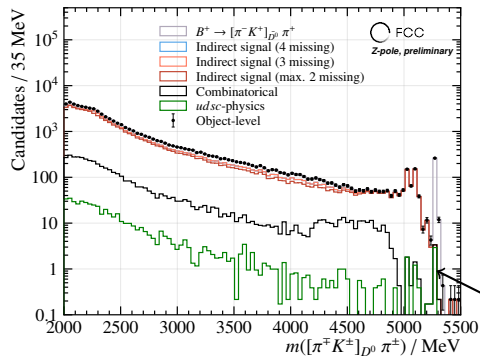


## Reconstruction efficiency

- Produced  $\bar{D}^0 \rightarrow K^+ \pi^-$  in the sample: 473 365
  - Reconstructed  $\bar{D}^0 \rightarrow K^+ \pi^-$ , truth-matched, within  $3\sigma_{\text{comb.}}$ : 425 917
- $\hookrightarrow \mathcal{E}_{3\sigma_{\text{comb.}}}(\bar{D}^0 \rightarrow K^+ \pi^-) = 89.98 \%$

# Fully charged $\bar{D}^0$ decay: $B^+ \rightarrow \bar{D}^0 \pi^+ \rightarrow K^+ \pi^- \pi^+$

- $\bar{D}^0$  candidates accepted within  $5\sigma$  interval
- Distinguished partially reconstructed particles in different categories: 2/3/4 particles missing
- Fit results to the truth-matched  $B^+$  signal (right):  $\mu = 5279.01$  MeV,  $\sigma_{\text{comb.}} = 5.00$  MeV

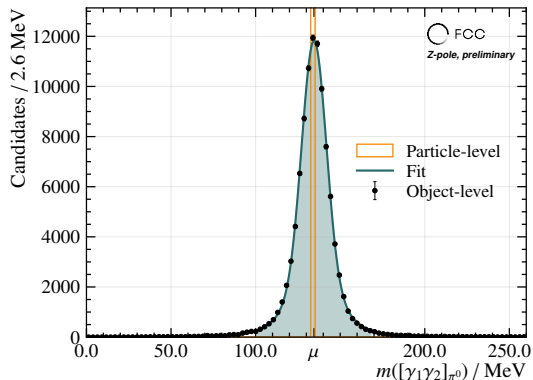


- **Reconstruction efficiency**  $B^+ \rightarrow \bar{D}^0 \pi^+ \rightarrow K^+ \pi^- \pi^+$ : 76.41 %
- **Purity**  $P_{B^+ \rightarrow \bar{D}^0 \pi^+} = 98.89$  % within  $m_{B^+} \in [5240, 5320]$  MeV

Background entering the signal region from gluon splitting

# $\bar{D}^0$ decay with one $\pi^0$ : $B^+ \rightarrow \bar{D}^0 \pi^+ \rightarrow K^+ \pi^- \pi^0 \pi^+$

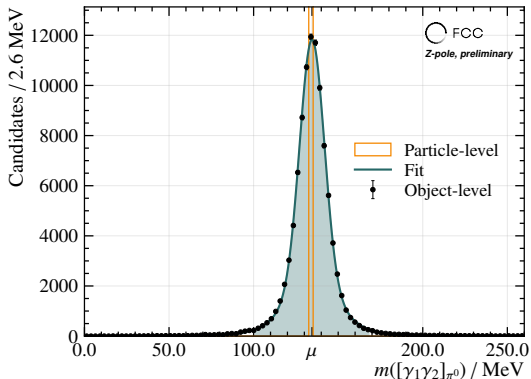
- $\pi^0$  reconstruction: Combine two photons with angle  $< 45^\circ$   
 $\rightarrow \mu = 134.53 \text{ MeV}, \sigma_{\text{comb.}} = 6.74 \text{ MeV}$



- **Reconstruction efficiency**  
 $\varepsilon_{5\sigma_{\text{comb.}}}(\pi^0 \rightarrow \gamma\gamma) = 94.06 \%$

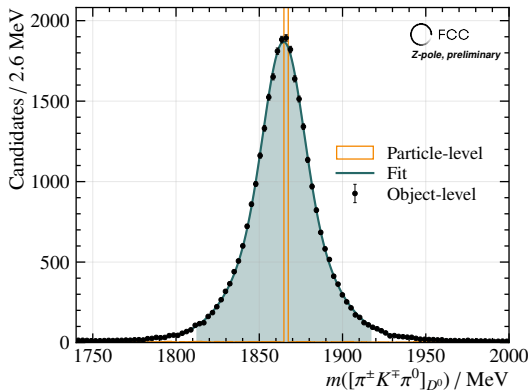
# $\bar{D}^0$ decay with one $\pi^0$ : $B^+ \rightarrow \bar{D}^0 \pi^+ \rightarrow K^+ \pi^- \pi^0 \pi^+$

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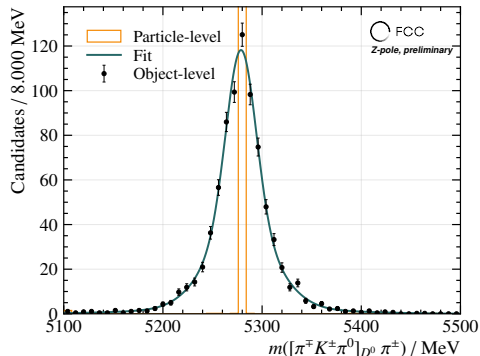
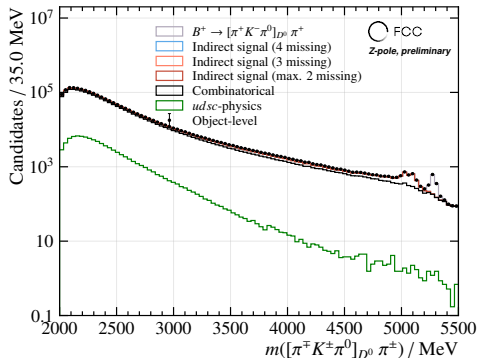
- $D^0$  reconstruction: Triple-Gaussian distribution applied to fit the truth-matched mass peak  
 $\rightarrow \mu = 1864.61 \text{ MeV}, \sigma_{\text{comb.}} = 22.82 \text{ MeV}$



- **Reconstruction efficiency**  
 $\hookrightarrow \epsilon_{2\sigma_{\text{comb.}}}(\bar{D}^0 \rightarrow K^+ \pi^- \pi^0) = 77.06 \%$

# $\bar{D}^0$ decay with one $\pi^0$ : $B^+ \rightarrow \bar{D}^0 \pi^+ \rightarrow K^+ \pi^- \pi^0 \pi^+$

- $\bar{D}^0$  candidates accepted within  $5\sigma$  interval
- Distinguished partially reconstructed particles in different categories: 2/3/4 particles missing
- Fit results to the truth-matched  $B^+$  signal (right):  $\mu = 5278.74$  MeV,  $\sigma_{\text{comb.}} = 26.59$  MeV



- **Reconstruction efficiency**  $B^+ \rightarrow \bar{D}^0 \pi^+ \rightarrow K^+ \pi^- \pi^+$ : 64.54 %
- **Purity**  $P_{B^+ \rightarrow \bar{D}^0 \pi^+} = 98.30$  % within  $m_{B^+} \in [5100, 5500]$  MeV

## $R_b$ : Concluding remarks

- Efficiency can be improved by constant purity by accepting also partially reconstructed particles  $\rightarrow$  set a lower mass cut in the  $B^+$  spectrum
- Vertexing assumptions with the updated FCCAnalyses to be evaluated

Summary of the reconstruction efficiencies (so far):

$$B^+ \rightarrow J/\psi K^+ \rightarrow \ell\ell K^+ : \varepsilon = 85.67 \%$$

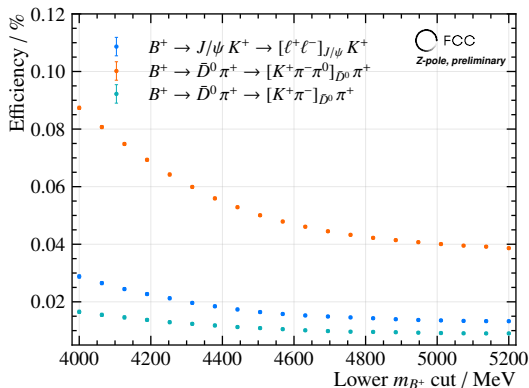
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$$B^+ \rightarrow \bar{D}^0 \pi^+ \rightarrow K^+ \pi^- \pi^0 \pi^+ : \varepsilon = 64.54 \%$$

$$B^+ \rightarrow \bar{D}^0 \pi^+ \rightarrow K^+ 2\pi^- \pi^+ \pi^+ : \text{WIP}$$

$$B^+ \rightarrow \bar{D}^0 D_s^+ \rightarrow K^+ \pi^- K^+ K^- \pi^+ : \text{WIP}$$

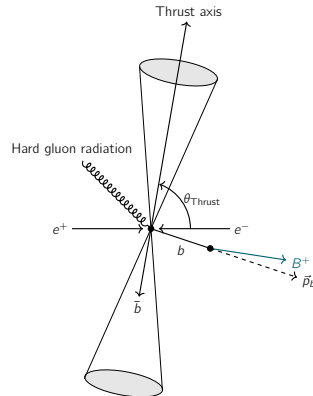
$\rightarrow$  Evaluation of the hemisphere correlation uncertainty from a full simulation sample with the CLD detector



# $A_{\text{FB}}^b$ in detail

For  $A_{\text{FB}}^b$ , things look a bit different [2]:

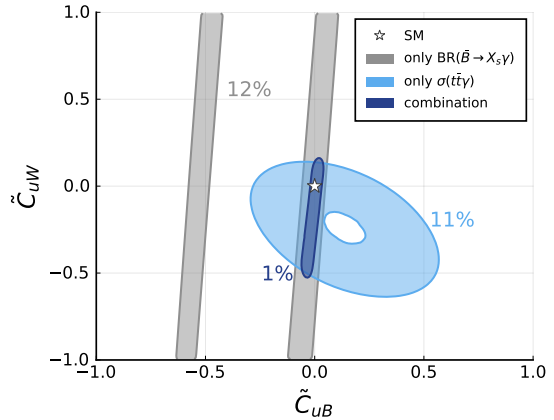
- $R_b$  asks, *if* a  $b$ -quark was produced, regardless of its charge or direction
- Forward-backward asymmetry needs an estimator of the **charge** and the **direction**: definition of *forward/backward*
- **Overcoming LEP-limitations** with exclusive  $b$ -hadron tags:
  1. **Mixing dilution** with lepton tags:  $B_{(s)}^0 \leftrightarrow \bar{B}_{(s)}^0$  mixing confuses the lepton charge. Consider  $B^+$  and  $\Lambda_b^0$  reconstruction for tagging
  2. **Contamination** from light-quark and  $c$ -physics
  3. **Gluon radiation** alters angle up to confusion of the hemispheres  
 → new angle from  $\vec{p}_{B^+}$  potentially mitigating the effect



Measurement	Result	Uncertainties	
		total systematic	QCD related
ALEPH [3]	$0.0998 \pm \dots \pm 0.0017$ (syst.)	1.7 %	0.6 %
OPAL [4]	$0.0989 \pm \dots \pm 0.0013$ (syst.)	1.3 %	1.1 %
		} $\mathcal{O}(1\%)$	

# Conclusions and Outlook

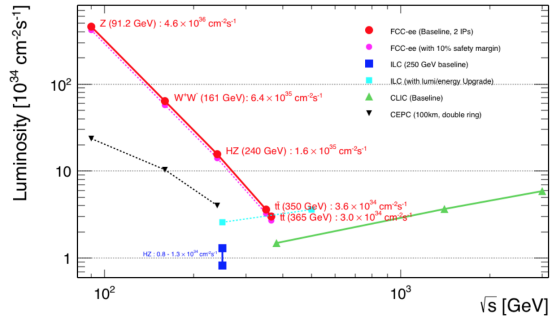
- **Goal:** Exploit SM-deviations consistently at different scales with EFT operators  
→ Combination of the top- and beauty scale at FCC-ee for global interpretation





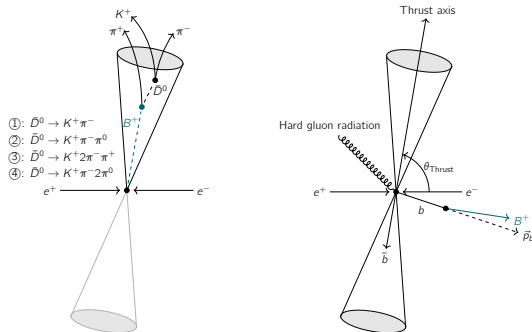
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- FCC-ee at the Z-pole: measurements with  $\mathcal{O}(10^{12})$  events **systematically limited**



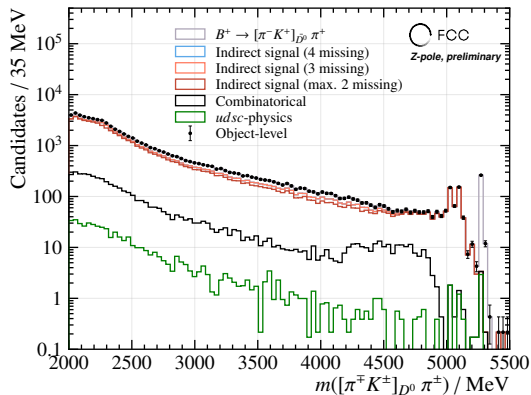
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- For (*b*-)tagging-based observable measurements: presented the promising idea of using **exclusively reconstructed b-hadrons as tagger**  
→ Reduction of major sources of systematic uncertainties to the cost of statistical precision



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- For (*b*-)tagging-based observable measurements: presented the promising idea of using **exclusively reconstructed b-hadrons as tagger**  
→ Reduction of major sources of systematic uncertainties to the cost of statistical precision
- **High purity** of representative *B*-meson decay modes proven from simulation





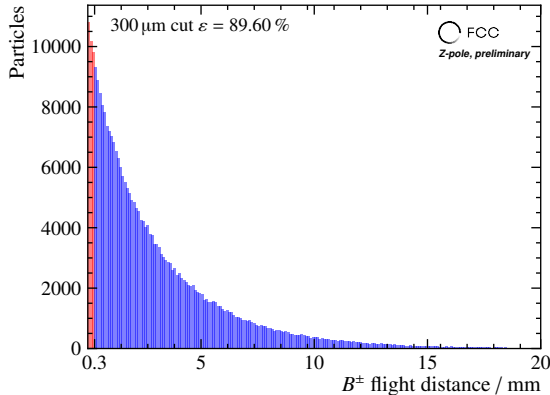
# Appendix I

- $B^+$  mean flight-distance via  $\langle L \rangle = \langle \beta\gamma \rangle c\tau$ . With  $\langle E_{B^+} \rangle \approx 0.75 \langle E_{b\text{-quark}} \rangle = 0.75 \cdot 45.2 \text{ MeV}$

$$\langle \beta\gamma \rangle = \frac{\langle p \rangle}{m_{B^+}} = \frac{\sqrt{0.75^2 \langle E_{b\text{-quark}} \rangle^2 - (5279.23 \text{ MeV})^2}}{5279.23 \text{ MeV}} \approx 6.57$$

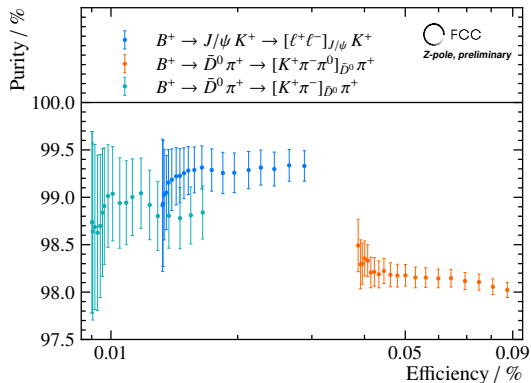
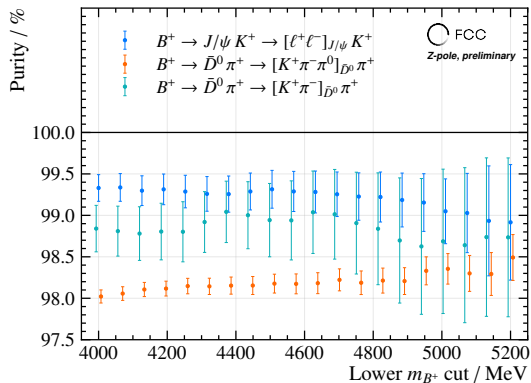
With  $\tau = 1638 \cdot 10^{-15} \text{ s} \rightarrow \langle L \rangle = 3 \text{ mm}$ . Distance cut of  $d > 300 \mu\text{m}$ :  $e^{-\frac{300 \mu\text{m}}{\langle L \rangle}} \approx 90.5\%$  remain

- Proof from simulation



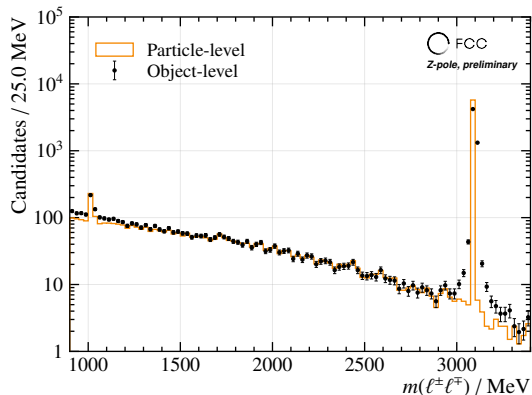
## Appendix II

- With a lower mass cut in the  $m_{B^+}$  spectrum, the purity can be kept constant

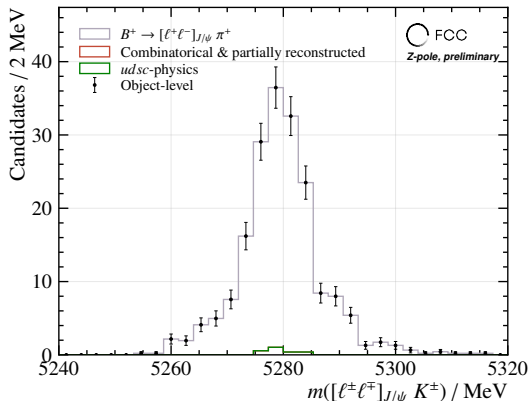


## Appendix III

- Full range invariant mass distribution for the  $\ell^\pm \ell^\mp$  pairs

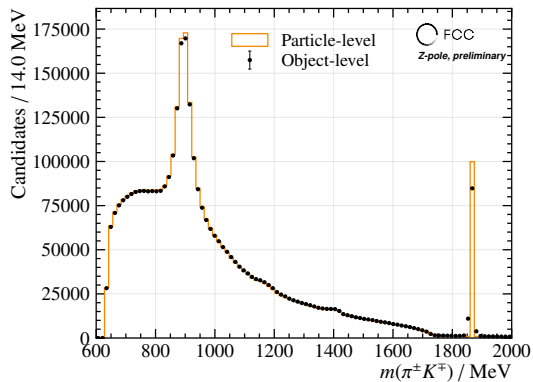


- Linear representation of the  $B^+$  mass range with all backgrounds included

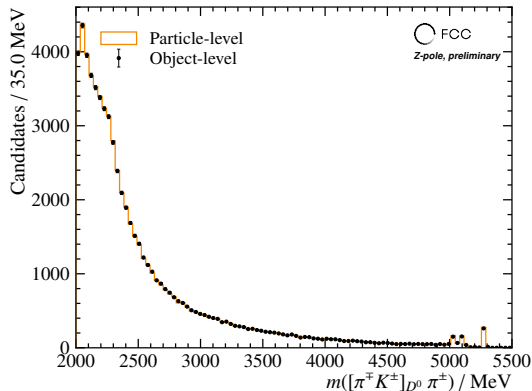


## Appendix IV

- Full range invariant mass distribution for the  $K^\pm \pi^\mp$  pairs



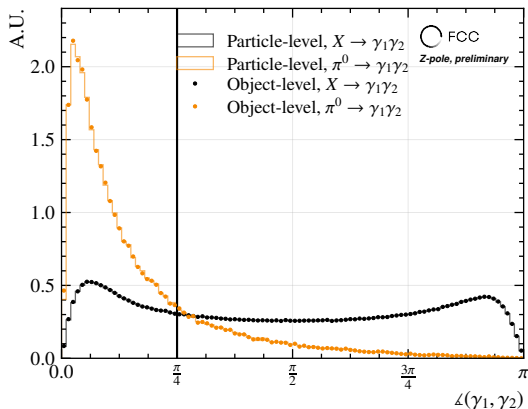
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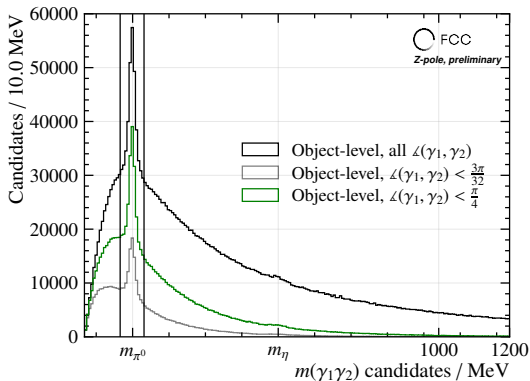


# Appendix V

- Photon angle distribution of truth-matched ( $\pi^0$ 's) and all particles

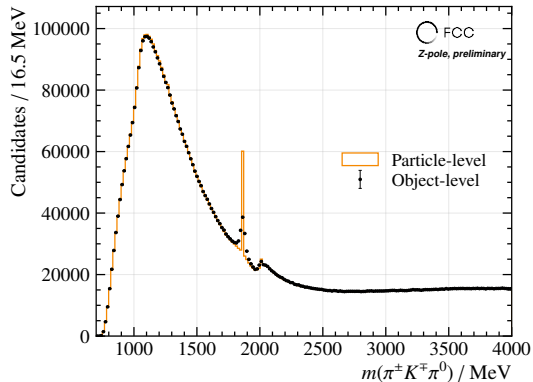


- Angular cuts applied in the  $m_{\gamma\gamma}$  mass spectrum, chosen  $\Delta(\gamma_1, \gamma_2): \frac{\pi}{4}$



# Appendix VI

- Full range invariant mass distribution for the  $K^\pm \pi^\mp \pi^0$  pairs



- Linear representation of the full mass range with all backgrounds included

