

Cavity QED with Ion Coulomb Crystals

Michael Drewsen

The Ion Trap Group
QUANTOP

Danish National Research Foundation Center for Quantum Optics
Department of Physics and Astronomy
University of Aarhus

Why cavity QED with ion Coulomb crystals ?

I) Quantum information:

Stable and faithful light-matter interfaces for coupling of flying and stationary qubits

- I) Single photon sources
- II) Quantum memories
- III) Quantum repeaters

II) Cavity optomechanics:

- I) Cavity mediated cooling of at. and mol. ion
- II) Cavity optomechanics with Coulomb crystals
- III) Simulations of systems based on usual solids

III) Plasma physics:

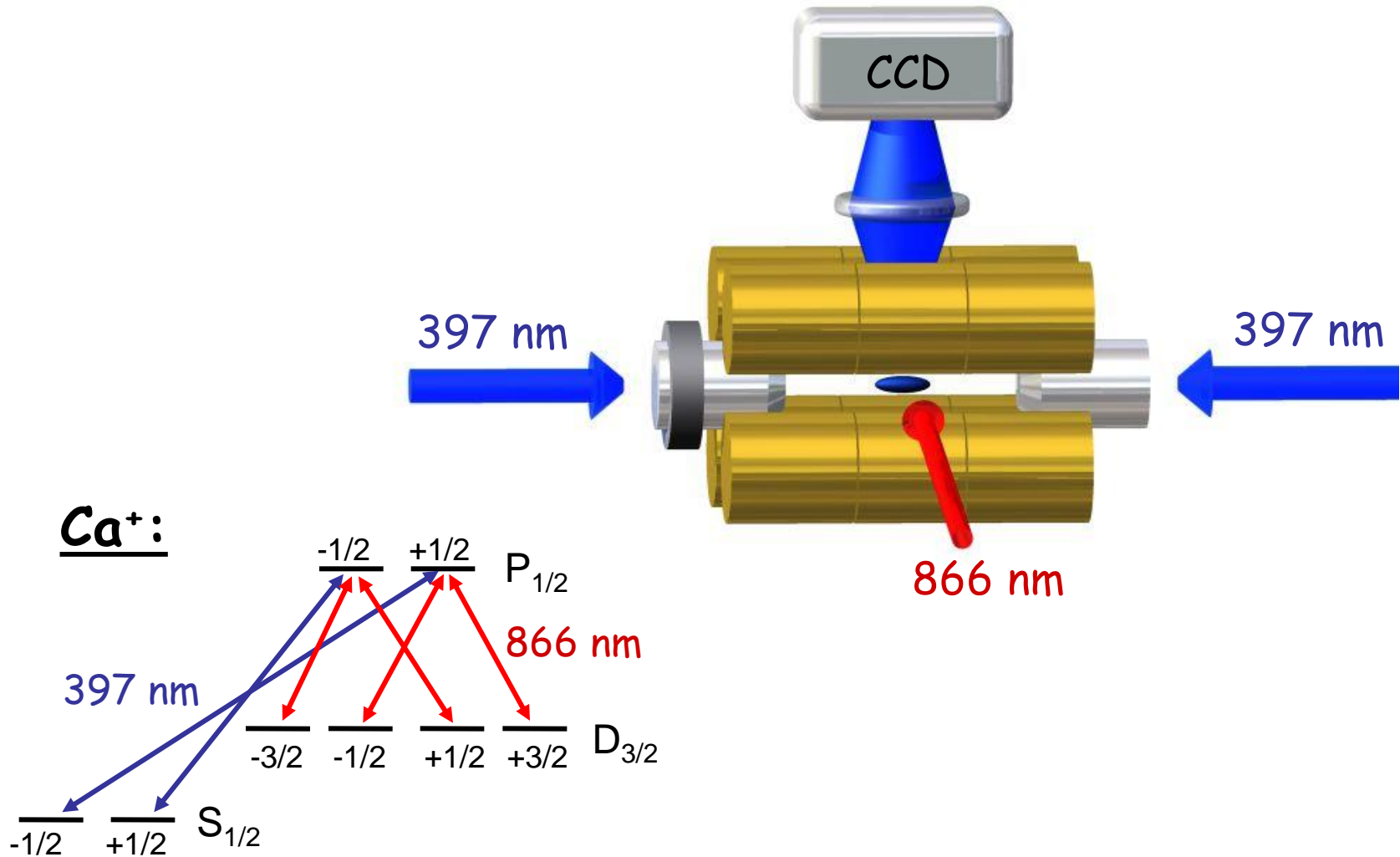
A tool to investigate the properties of strongly coupled one component plasmas (OCPs).

Outline

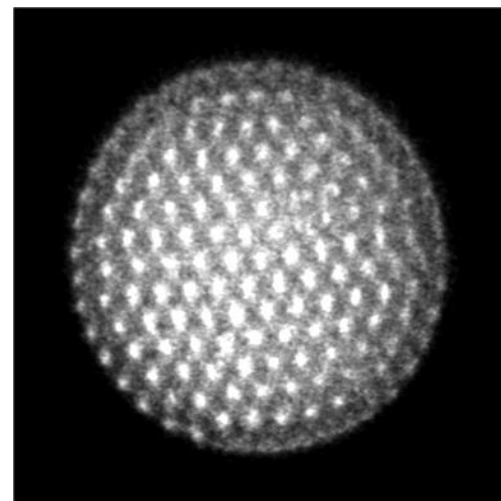
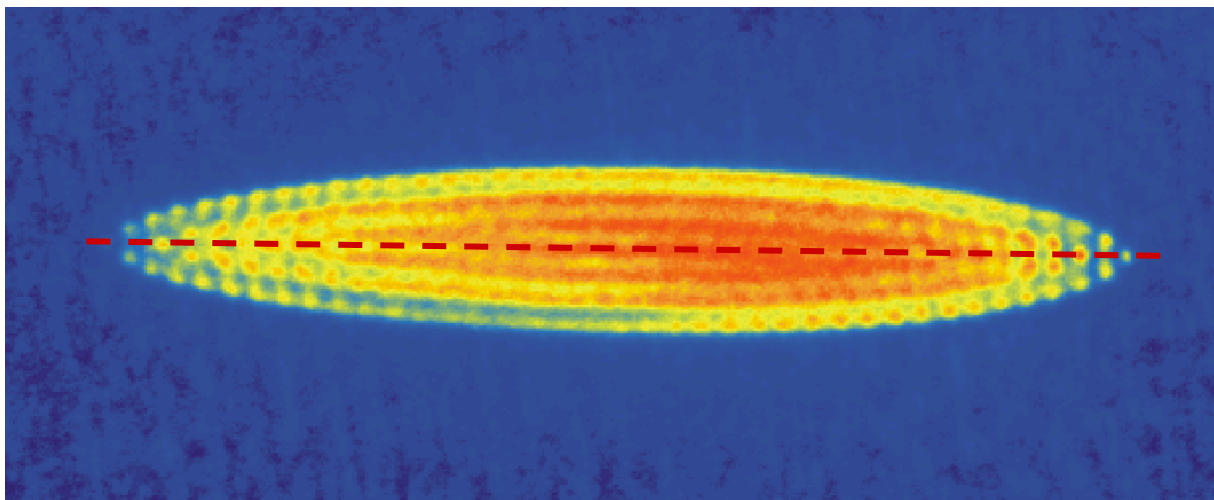
- I) Brief introduction to ion Coulomb crystals
- II) Cavity Quantum ElectroDynamics (CQED) in short
- III) CQED experiments with Coulomb crystals
 - Collective strong coupling
 - Cavity EIT
 - Cross Kerr effect and photon blockade
- IV) Conclusion

I) Brief introduction to ion Coulomb crystals

Laser cooling of trapped ions:



Ion Coulomb crystals



Phys. Rev. Lett. **96**, 103001 (2006)

Properties:

Uniform density $\sim 10^8 - 10^9$ ions/cm³

Melting point ~ 100 mK

Life times of \sim hours @ $P \sim 10^{-10}$ mBar

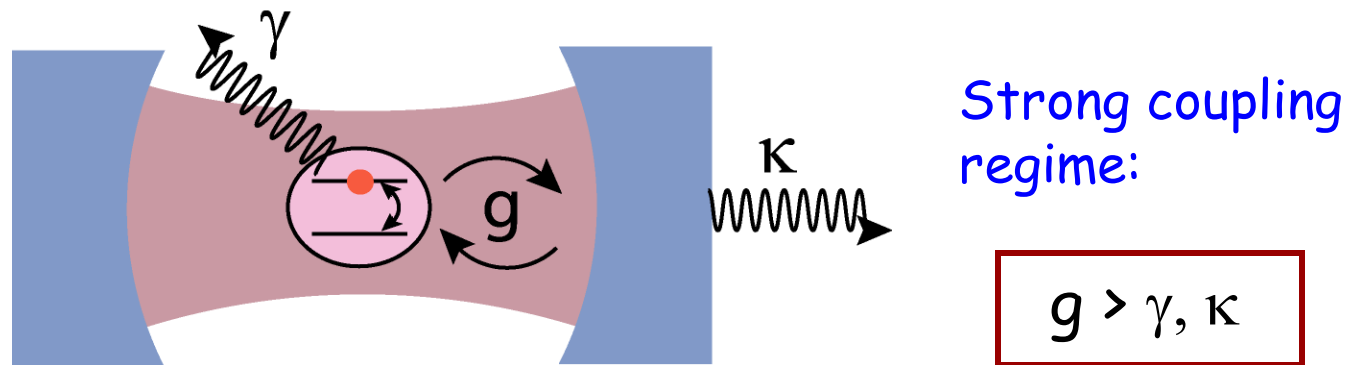
Unique feature of these solids:

The internal state of individual ions are "unperturbed" by the presence of other ions as well as the trapping fields !

II) Cavity Quantum ElectroDynamics in short

Exploration of the coupling of a quantized cavity EM-field to electromagnetic transitions in a quantum system.

A few important parameters (2-level system)

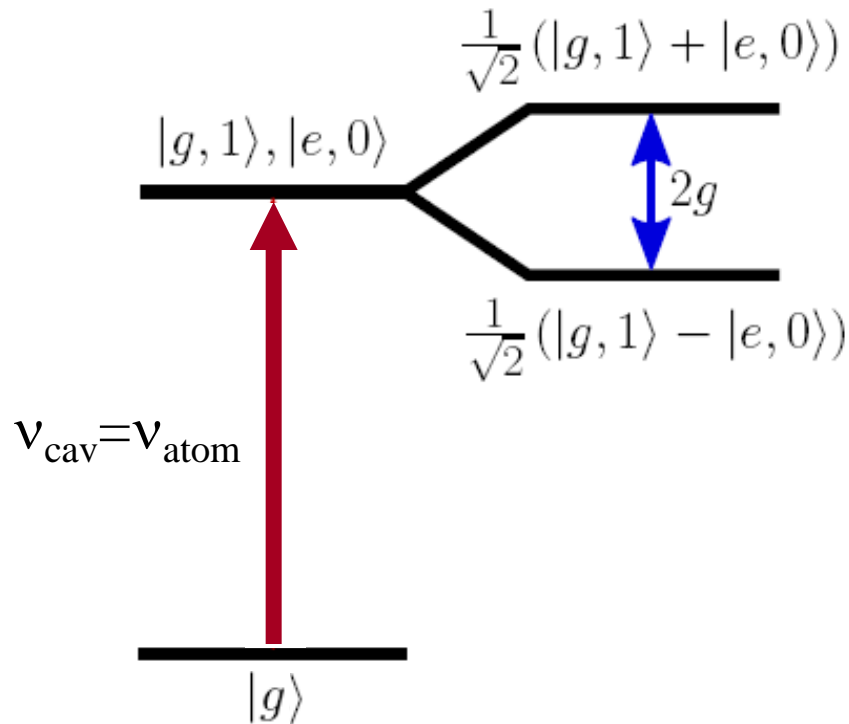


Coupling rate of a single photon to the atomic system: g

Quantum system dipole decay rate: γ

Cavity field decay rate: κ

Atomic interaction with a single photon



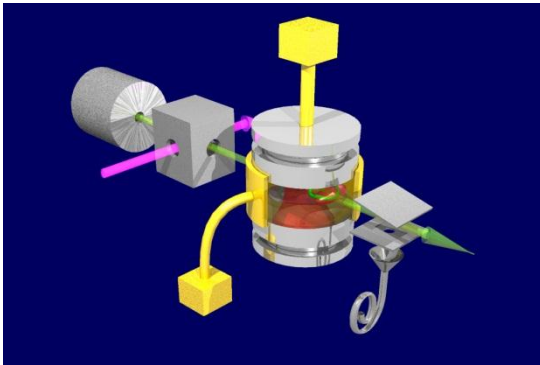
Single photon
Rabi splitting

Hallmark of CQED !

Pioneering CQED work

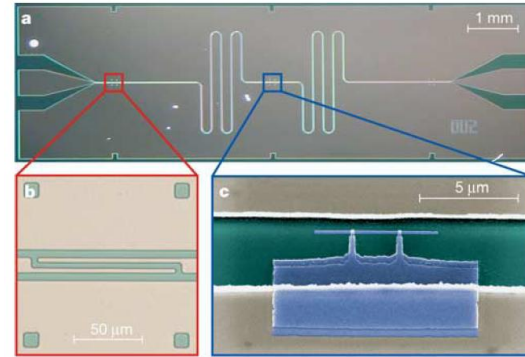
Microwaves:

Atoms



Haroche, ENS; Walther, MPQ

CPB's

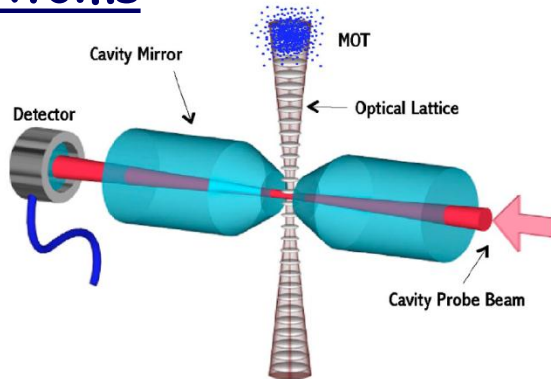


Schoelkopf, YALE;
Wallraff, ETH
Martinis, UCSB
Vion, Saclay

Optical range:

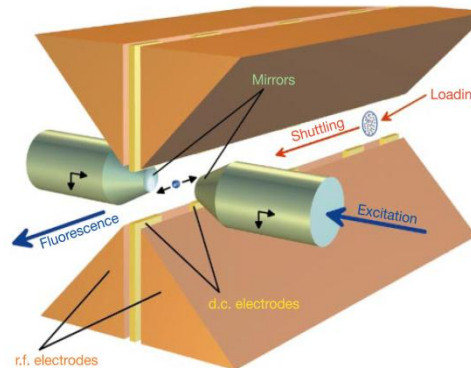
$$g = \mu_{eg} \cdot \epsilon \sqrt{\frac{\hbar \omega}{2\epsilon_0 V}}$$

Atoms



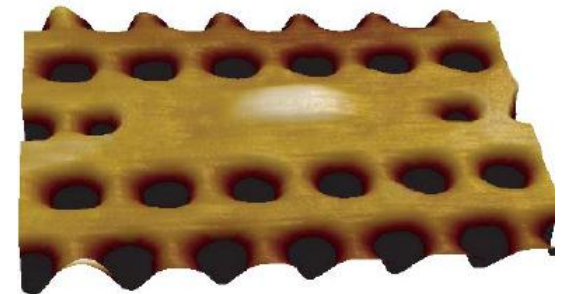
Rempe, MPQ;
Kimble, Caltec

Ions



Walther, MPQ;
Blatt, Innsbruck

Qdots

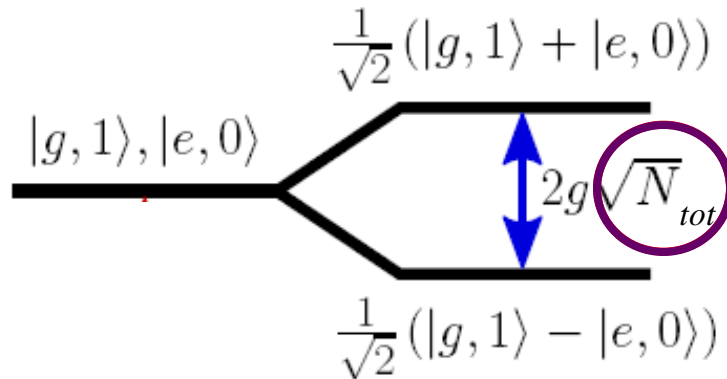


Imamoglu, ETH
Yamamoto, Stanford

III) CQED experiments with Coulomb crystals

Why Coulomb crystals ?

Interaction with a single photon



For multi-particle states:

$$|g, 1\rangle \equiv |g_1, \dots, g_{N_{tot}}, 1\rangle$$

Ideally: $|e, 0\rangle \equiv \frac{1}{\sqrt{N_{tot}}} \sum_{i=1}^{N_{tot}} |g_1, g_2, \dots, e_i, \dots, g_{N_{tot}}, 0\rangle$

Actually: $|e, 0\rangle \equiv \sum_{i=1}^{N_{tot}} c_i |g_1, g_2, \dots, e_i, \dots, g_{N_{tot}}, 0\rangle$, $\sum_{i=1}^{N_{tot}} |c_i|^2 = 1$

Effective number of ions:

$$N \equiv \sum_{i=1}^{N_{tot}} \psi^2(\vec{r}_i) \text{ , with}$$

$$\psi^2(\mathbf{r}) = \left(\frac{w_0}{w(z)} \right)^2 \exp(-2(x^2 + y^2)/w(z)^2) \sin^2 [kz - \tan(z/z_0) + k(x^2 + y^2)/2R(z)]$$

being the cavity mode function (TEM₀₀)

Why Coulomb crystals ?

Collective coupling: $g_{\text{eff}} = gN^{1/2} \Rightarrow$ Collective strong coupling regime accessible ($g_{\text{eff}} \gg \kappa, \gamma$)

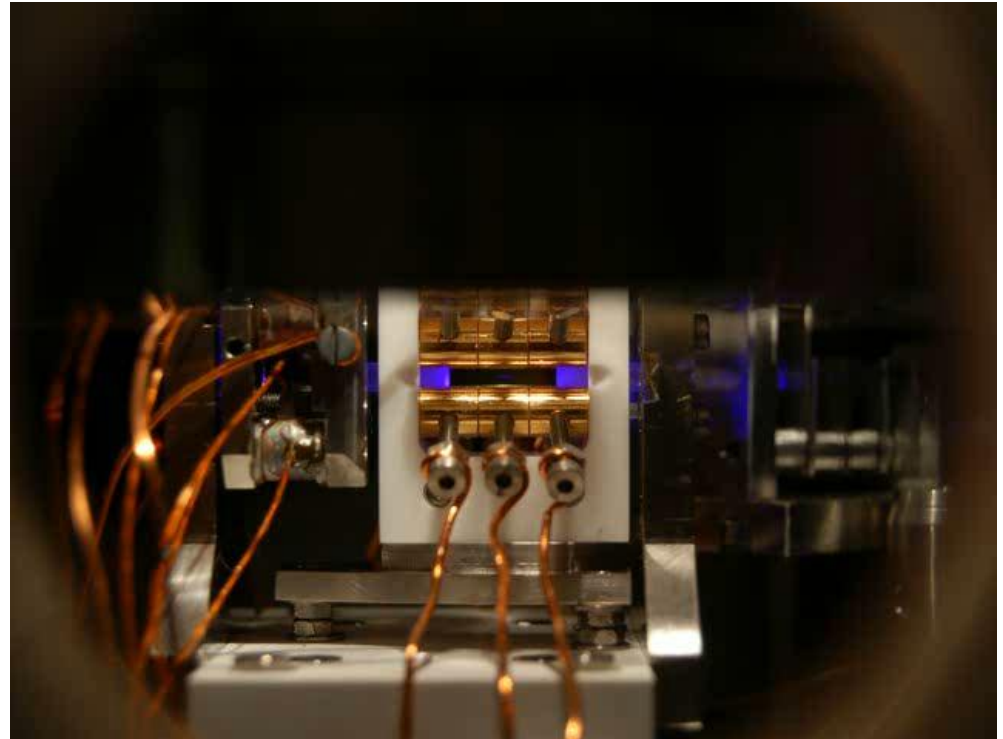
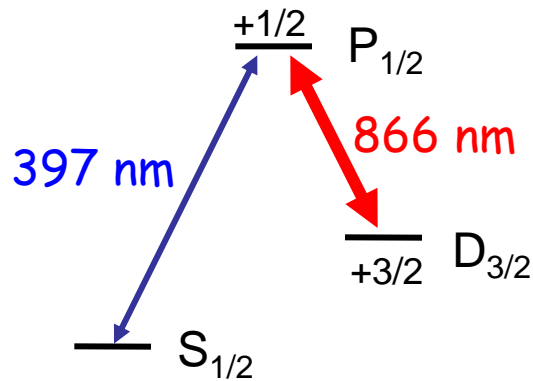
N can be varied "continuously" from 1 to ~ 2000

Good overlap between cavity mode and ions in Coulomb crystals

Micro-meter positioning control

J. Phys. B, 42, 154008 (2009)

The $^{40}\text{Ca}^+$ ion:



Why Coulomb crystals ?

Collective coupling: $g_{\text{eff}} = gN^{1/2} \Rightarrow$ Collective strong coupling regime accessible ($g_{\text{eff}} \gg \kappa, \gamma$)

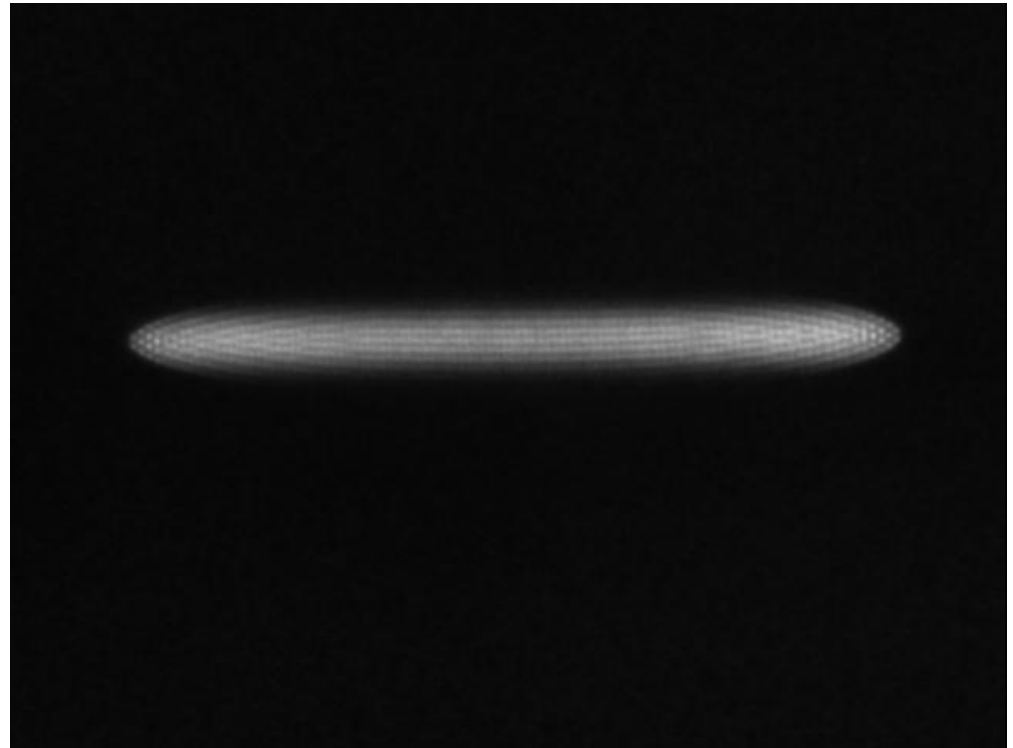
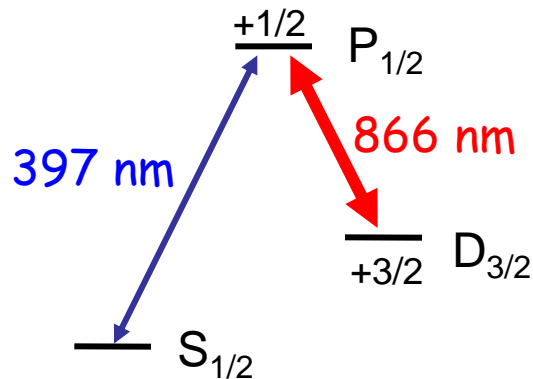
N can be varied "continuously" from 1 to ~ 2000

Good overlap between cavity mode and ions in Coulomb crystals

Micro-meter positioning control

J. Phys. B, 42, 154008 (2009)

The $^{40}\text{Ca}^+$ ion:



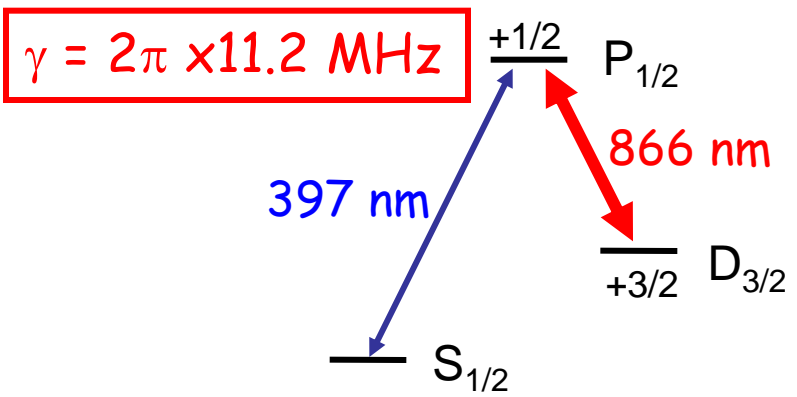
The Cavity Trap Setup

The cavity:

$L = 11 \text{ mm}$
 $w_0 = 37 \text{ } \mu\text{m}$
 $R_1 \approx 99.85\%$
 $R_2 > 99.99\%$
 $F \sim 3200$

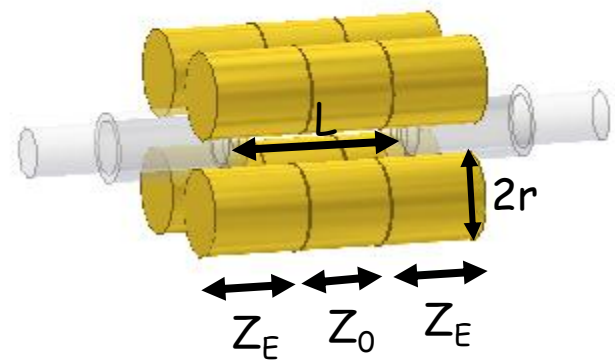
$$\kappa = 2\pi \times 2.1 \text{ MHz}$$

The $^{40}\text{Ca}^+$ ion:



The trap:

$2r = 5.2 \text{ mm}$
 $z_0 = 5.0 \text{ mm}$
 $z_E = 5.9 \text{ mm}$



The cavity-atom coupling:

$$g = 2\pi \times 0.53 \text{ MHz}$$

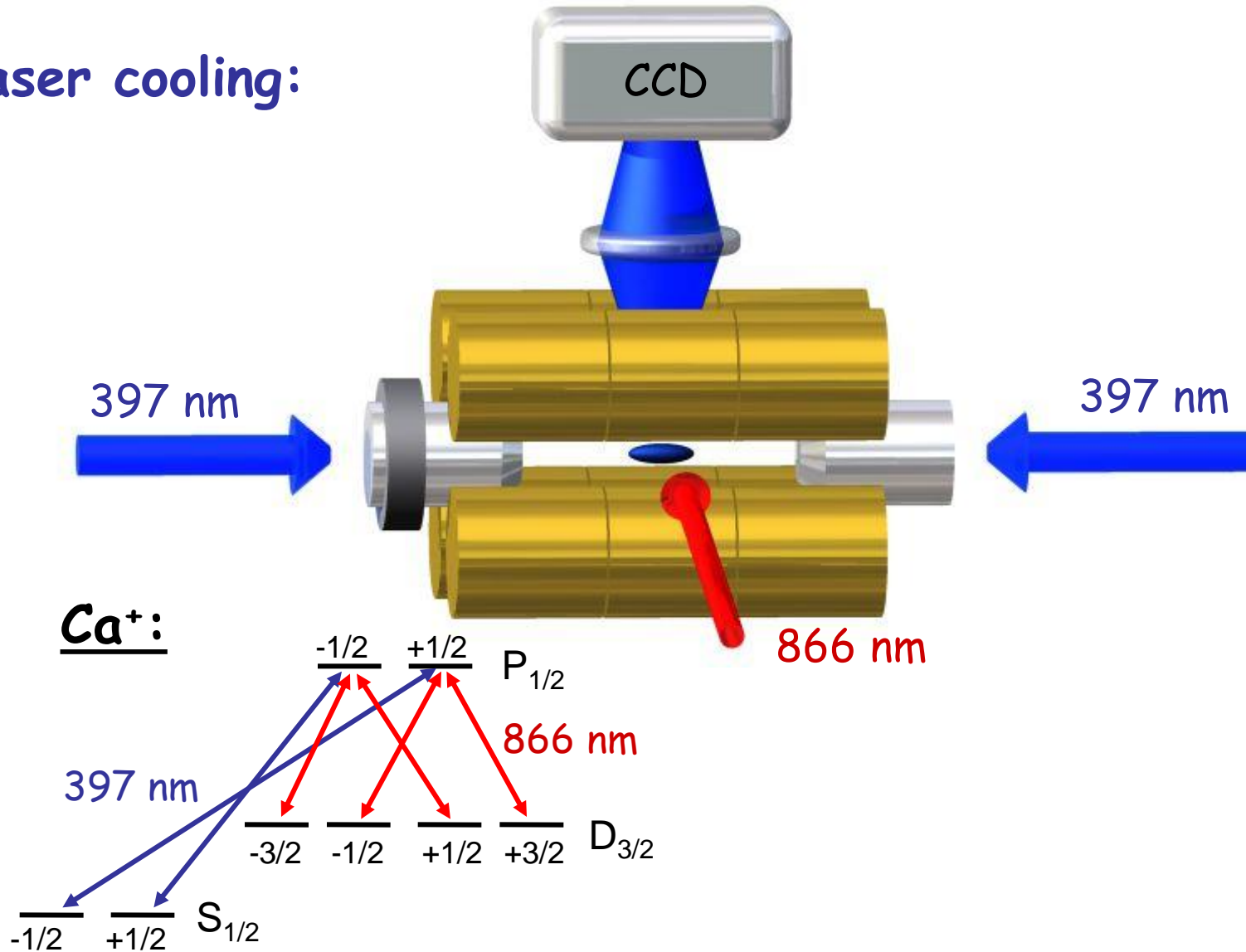
$$g_{\text{eff}} = gN^{1/2} > \gamma, \kappa \Rightarrow N > \sim 430$$

Coop. par.: $C = Ng^2 / (2\kappa\gamma)$:

$C \approx 0.006 \text{ (} N = 1 \text{)} \rightarrow C \approx 10 \text{ (} N = 1500 \text{)}$

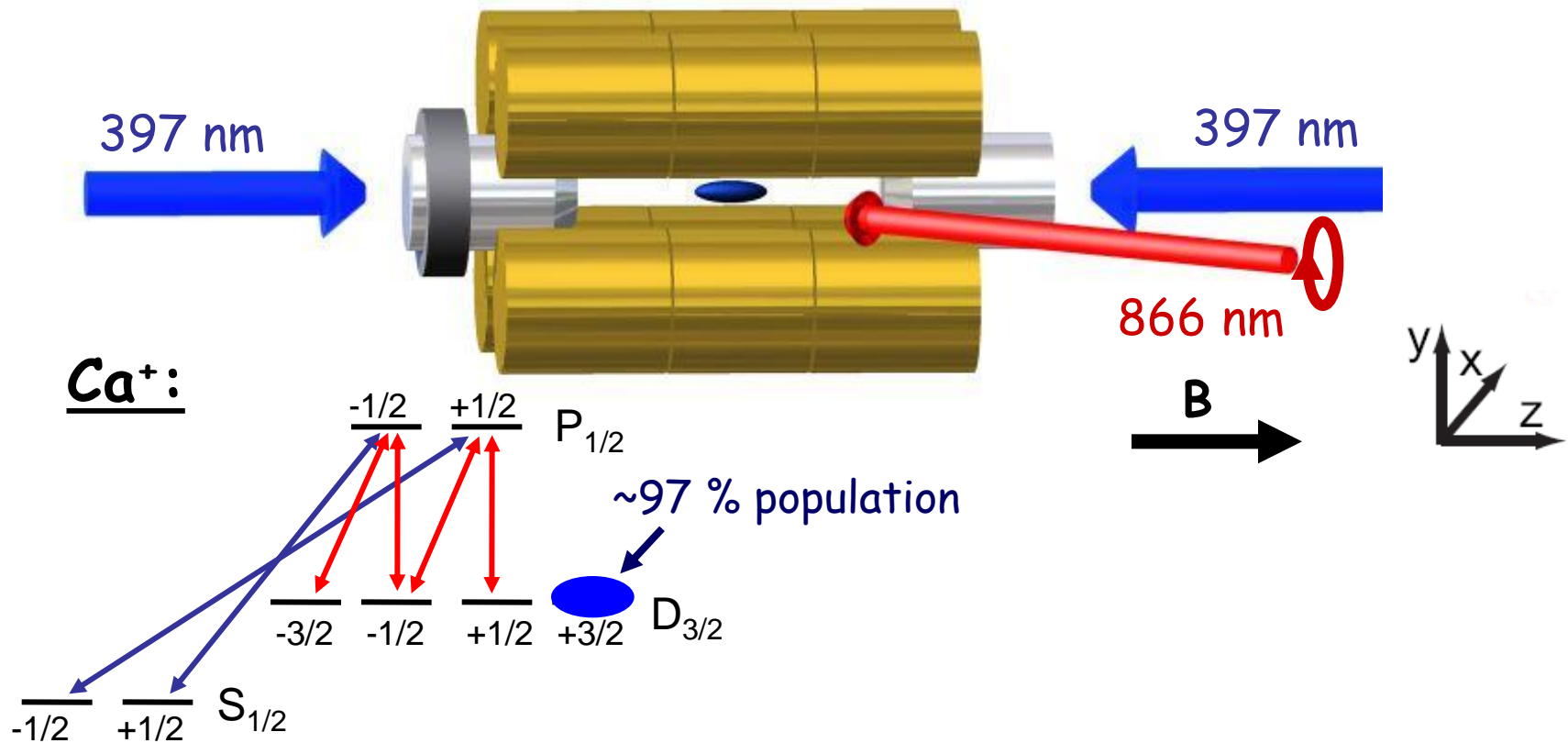
Experimental Sequence

Laser cooling:



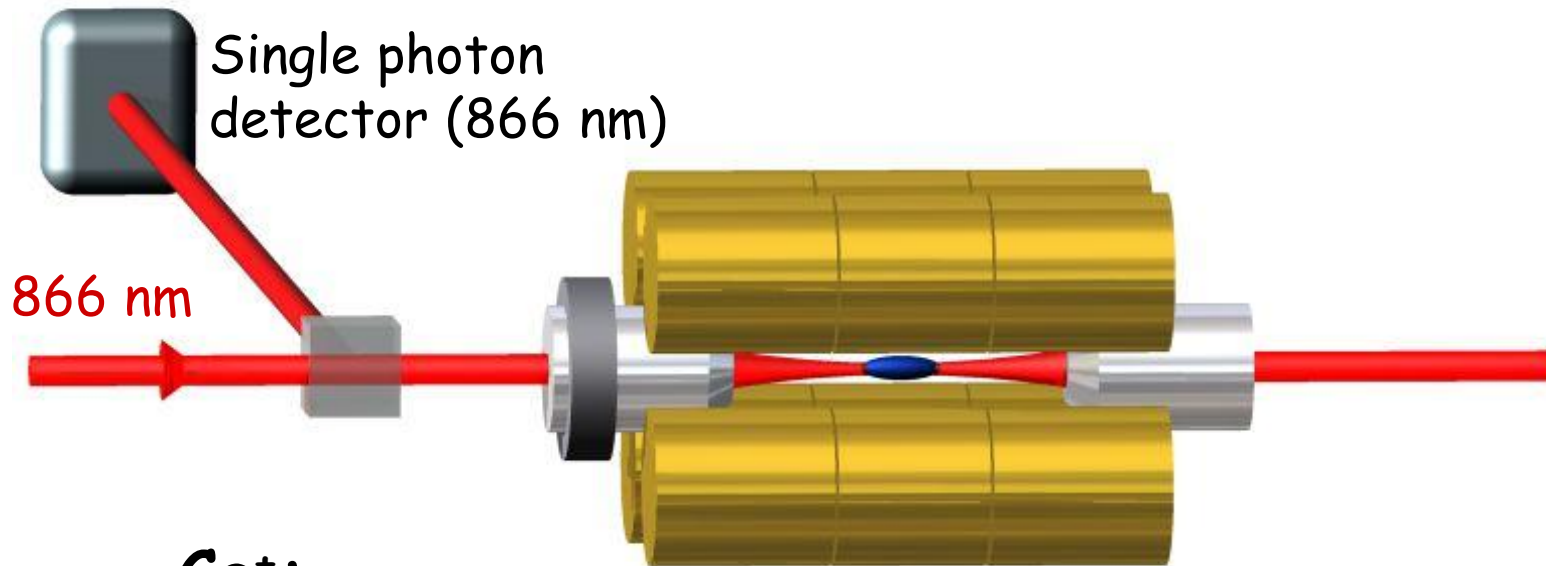
Experimental Sequence

Optical pumping:

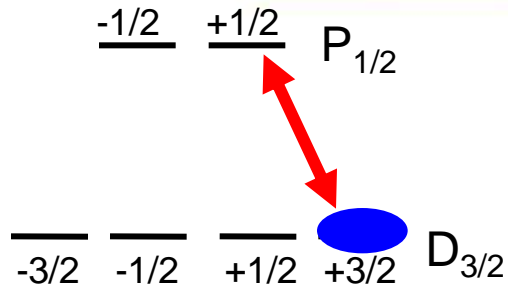


Experimental Sequence

Cavity probing:



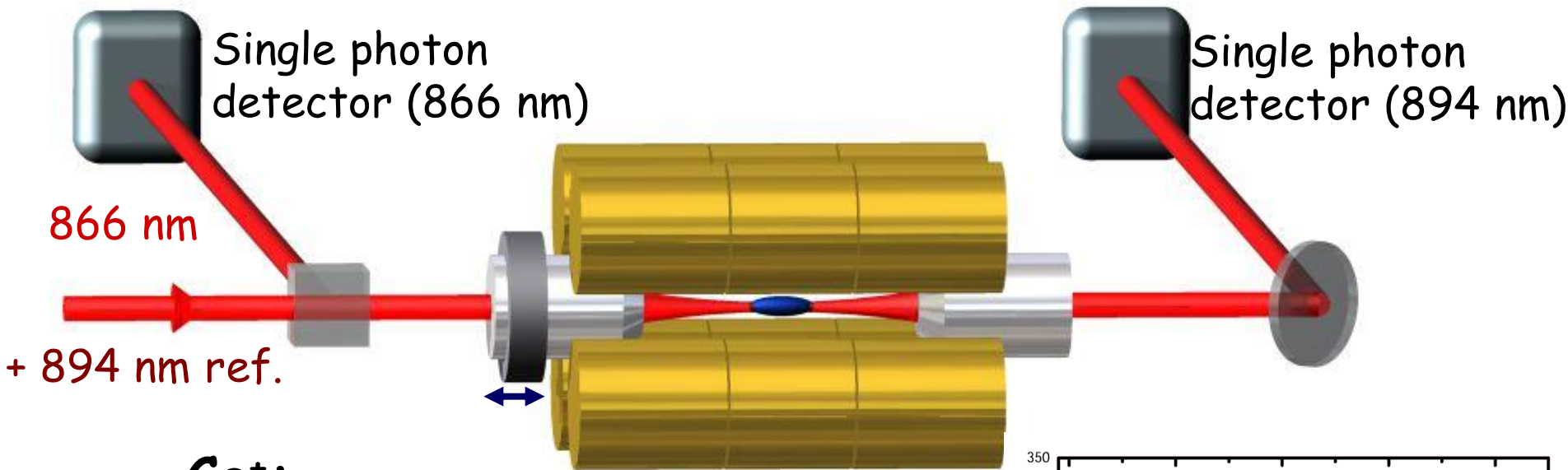
Ca⁺:



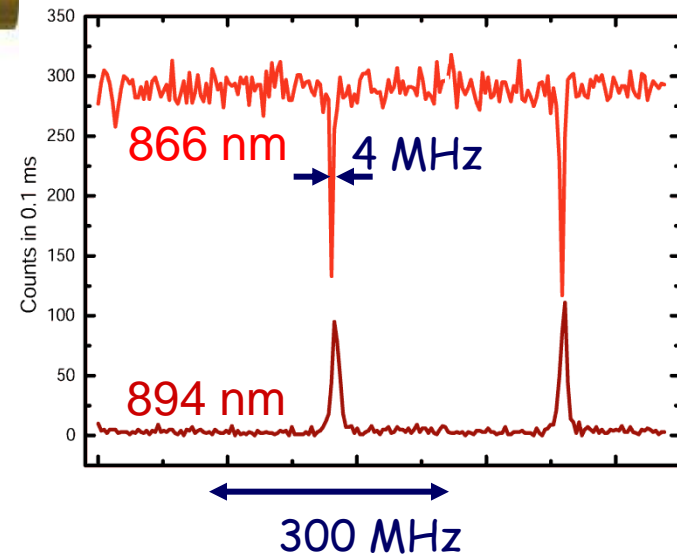
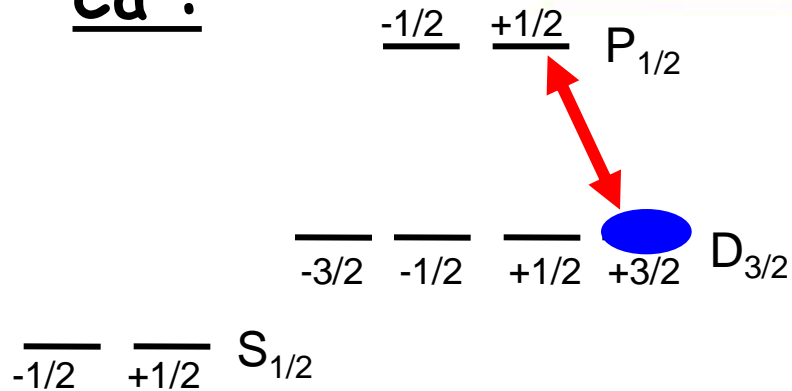
$-1/2$ $+1/2$ $S_{1/2}$

Experimental Sequence

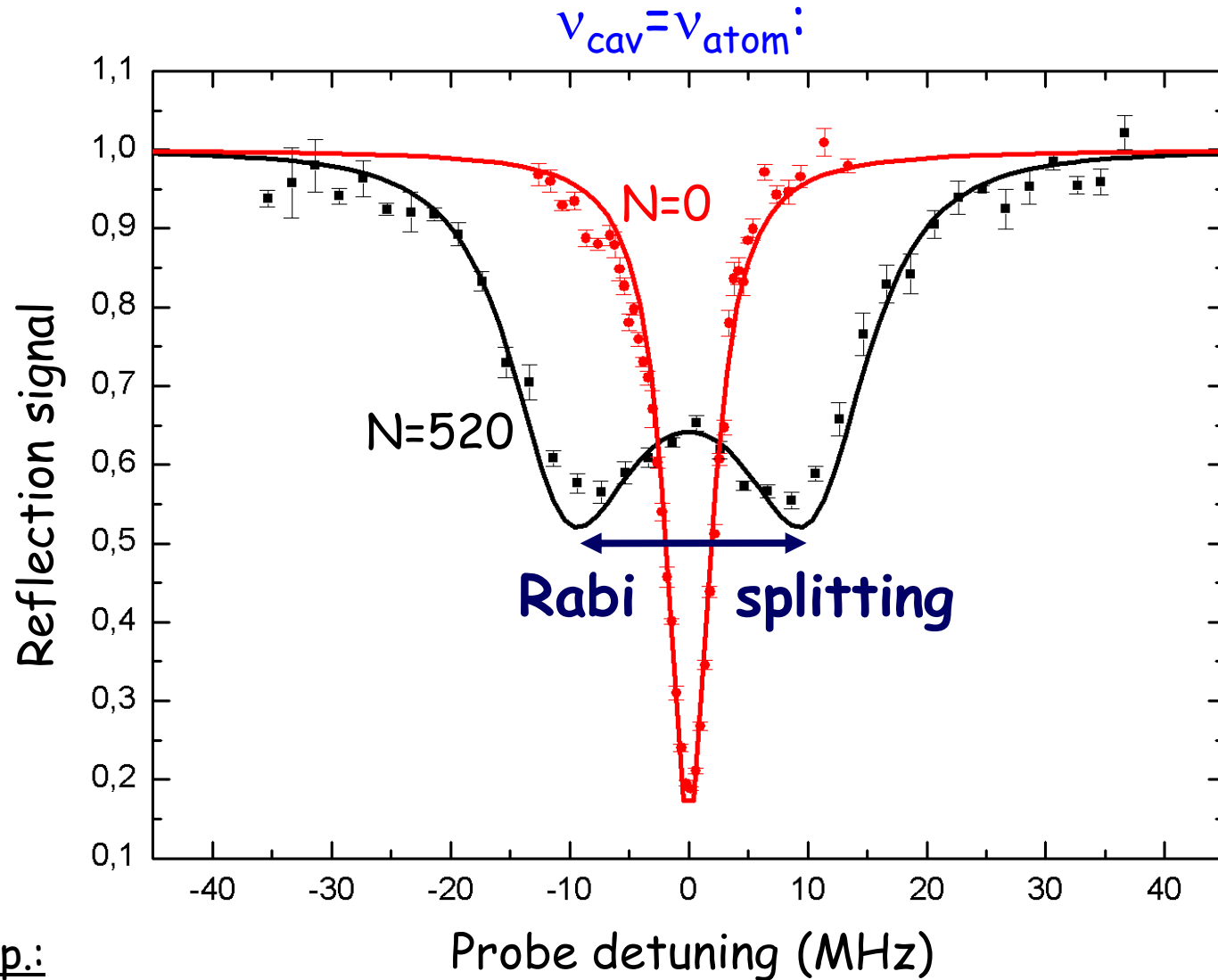
Cavity probing:



Ca⁺:



Observation of single photon Rabi splitting



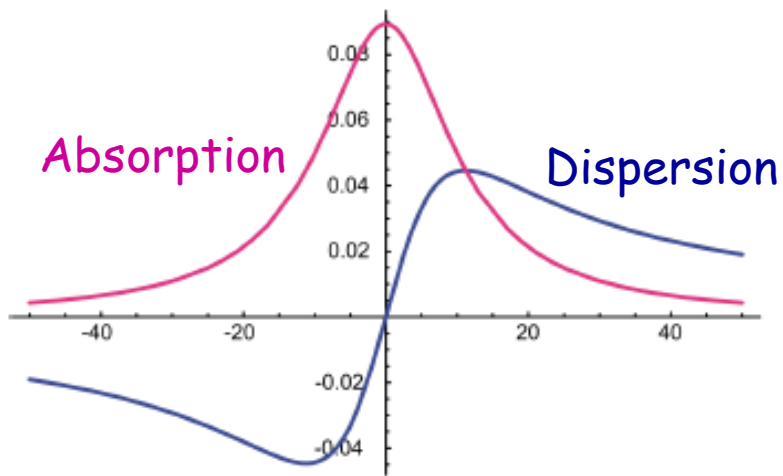
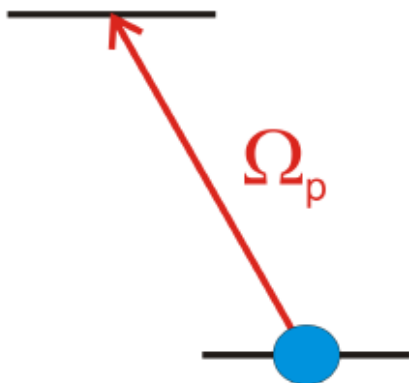
First exp.:

R. J. Thompson, G. Rempe & H. J. Kimble,
Phys. Rev. Lett. 68, 1132-1135 (1992)

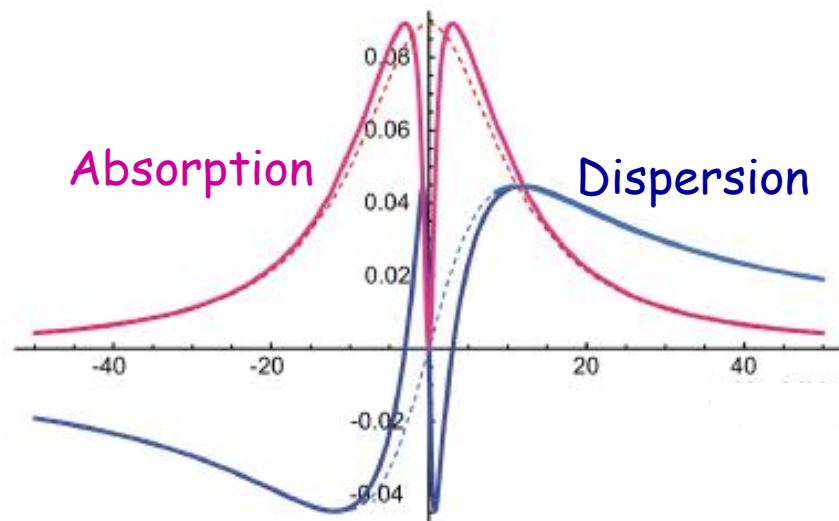
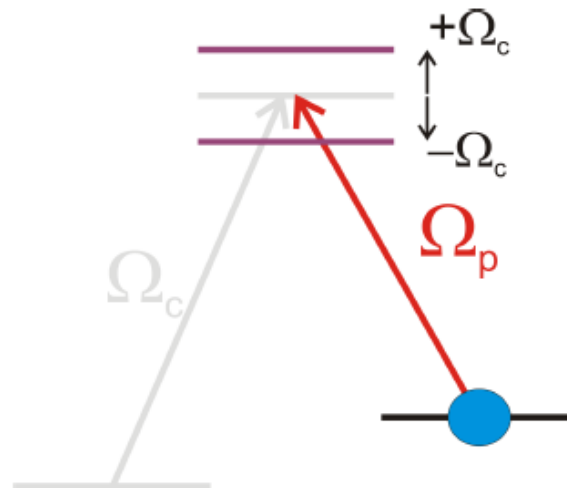
Nature Physics 5, 494 (2009)

Electromagnetically Induced Transparency (EIT)

2-level atoms

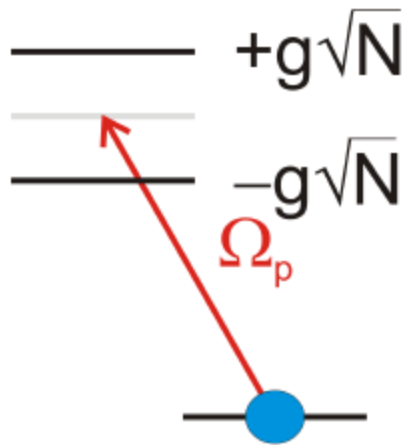


3-level atoms

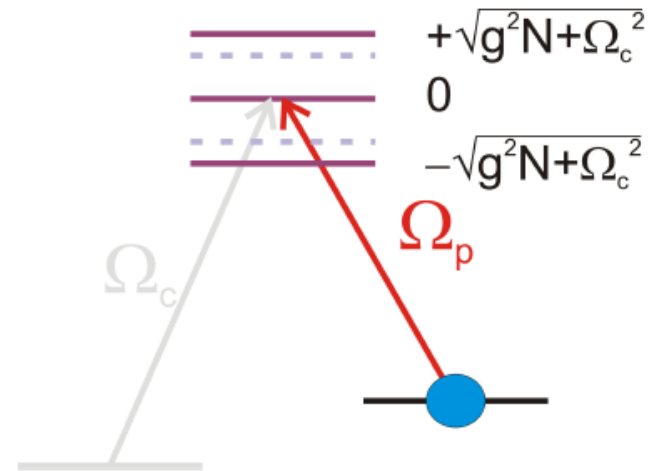


EIT in a cavity

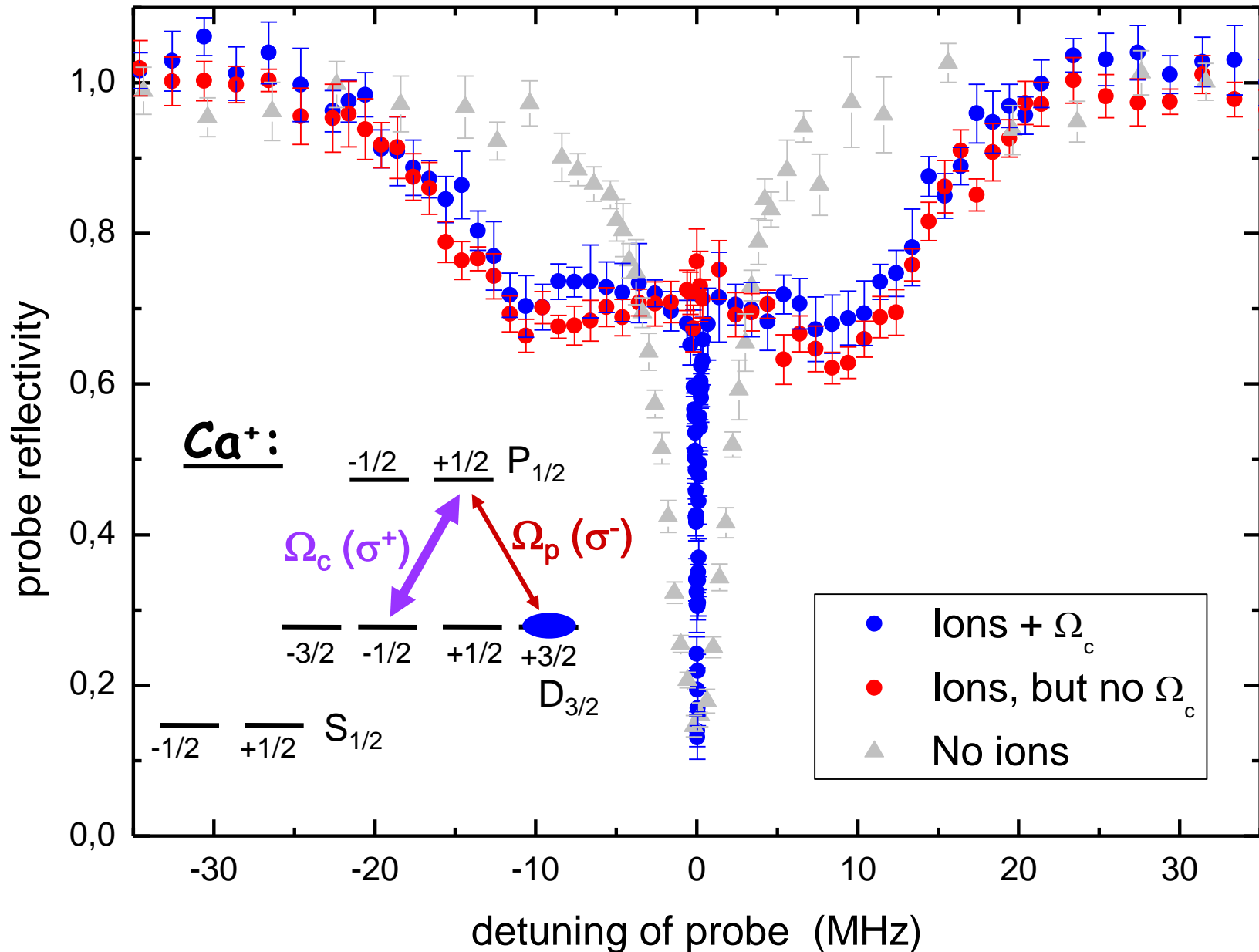
2-level atoms in cavity



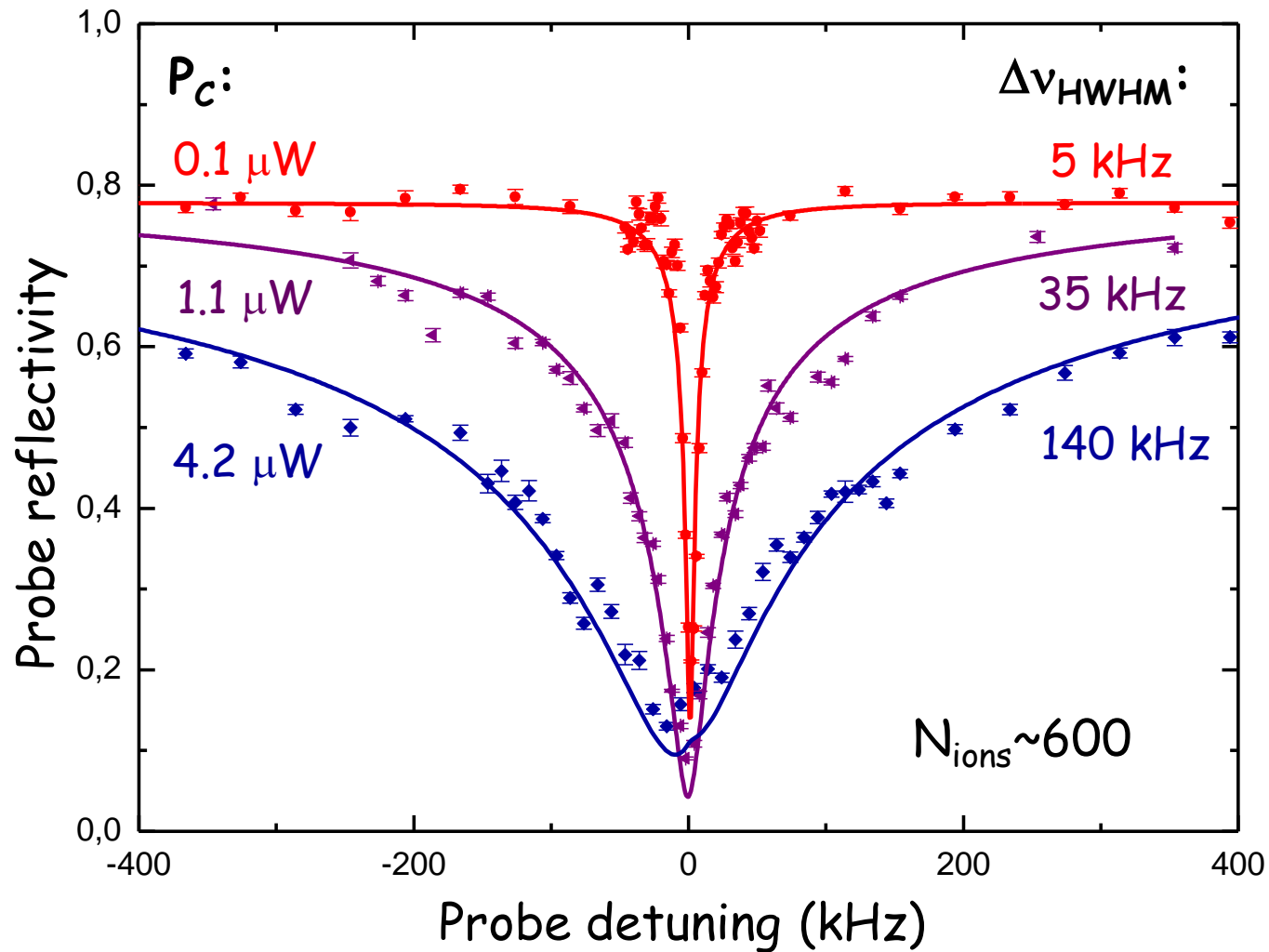
3-level atoms in cavity



Observation of triplet structure in reflection

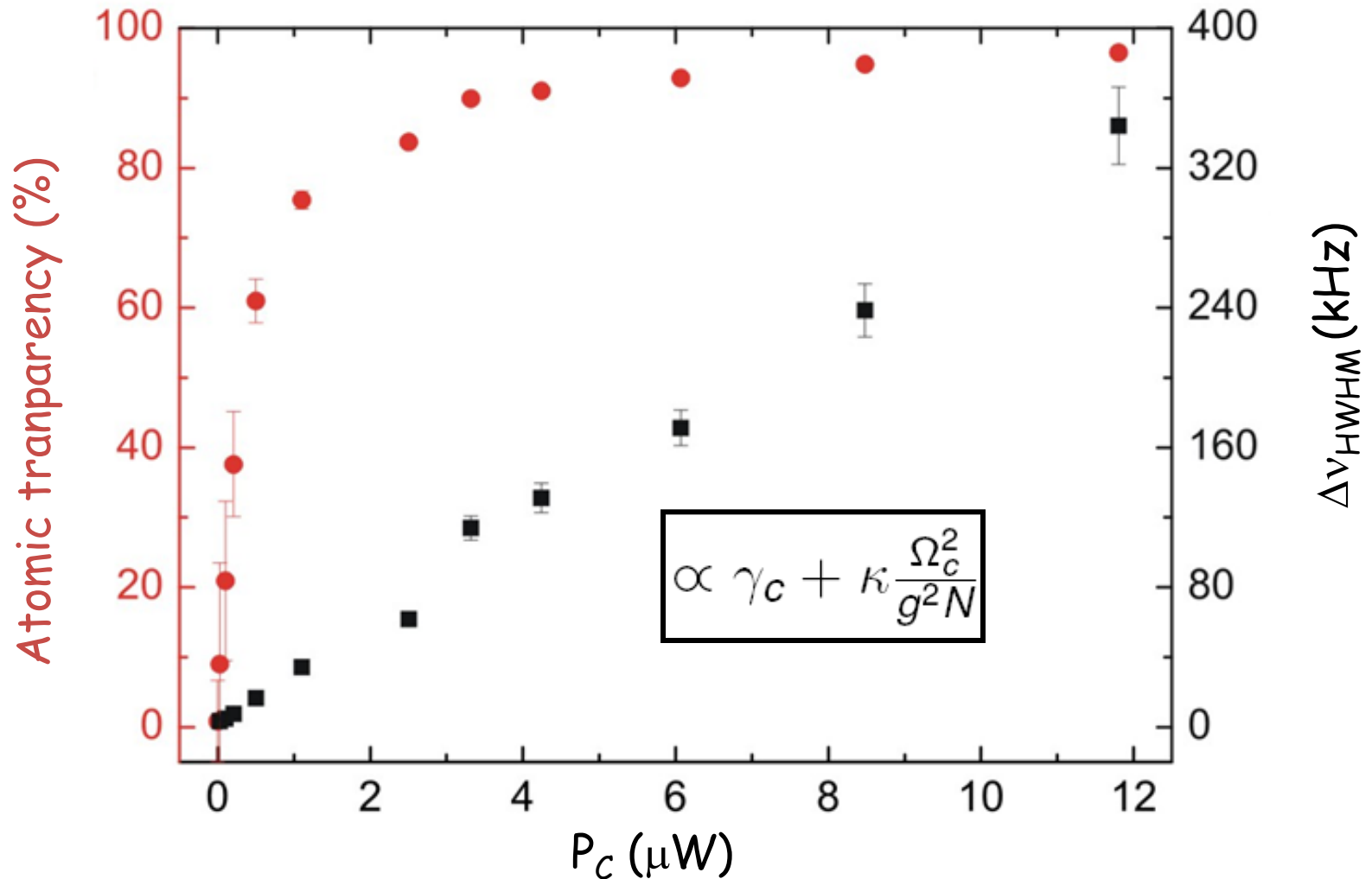


EIT feature vs. coupling laser power



Non-Lorentzian line shapes due to Gaussian mode profile

EIT feature vs. coupling laser power



> 90 % transparency for $\Delta\nu_{\text{HWHM}} \sim 100$ kHz

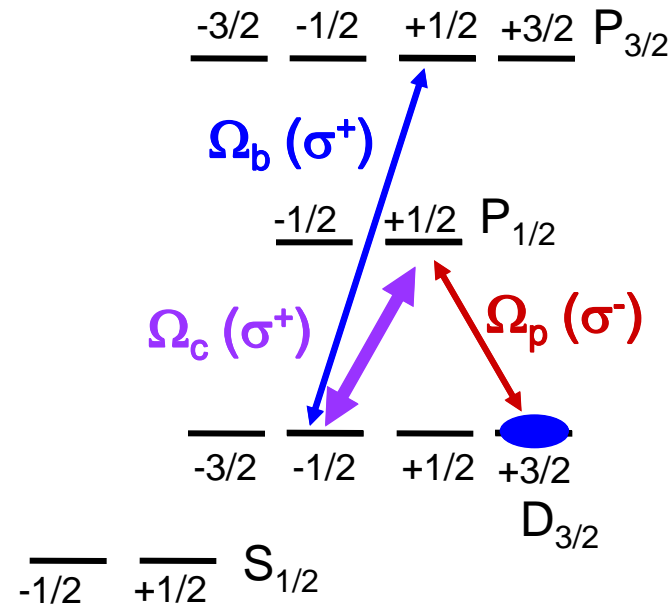
$\gamma_c \sim 1$ kHz

Cross Kerr effect and photon blockade

Schmidt and Imamoglu, opt. Lett. 21, 1936 (1996);

Imamoglu *et al.*, Phys. Rev. Lett **79**, 1467 (1997)

Ca⁺:



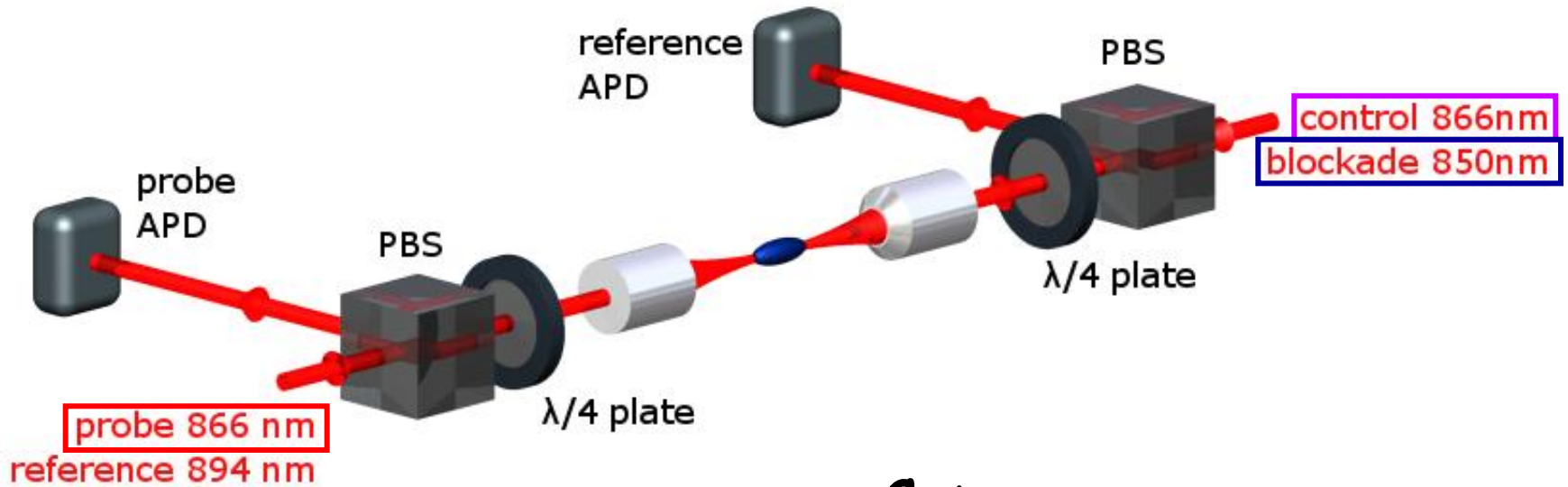
If the light shift due to Ω_b is larger than the EIT width then EIT ceases => Photon blockade !

At the single photon level this would enable

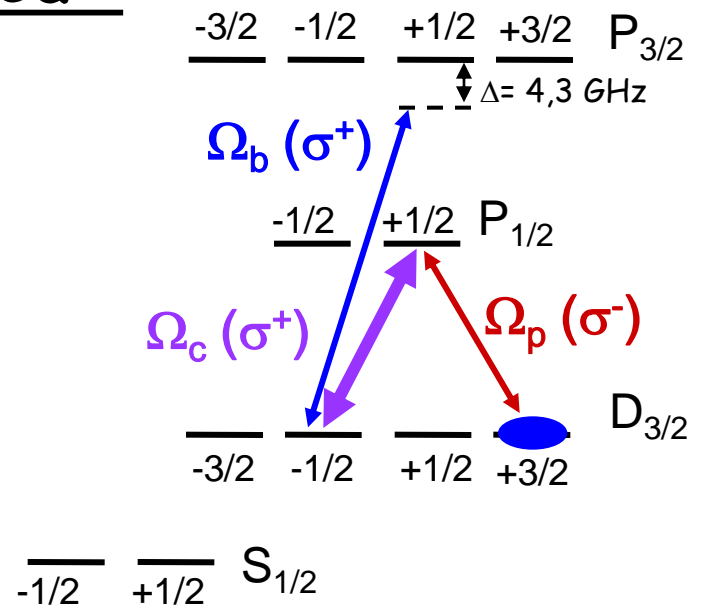
I) Single photon transistor

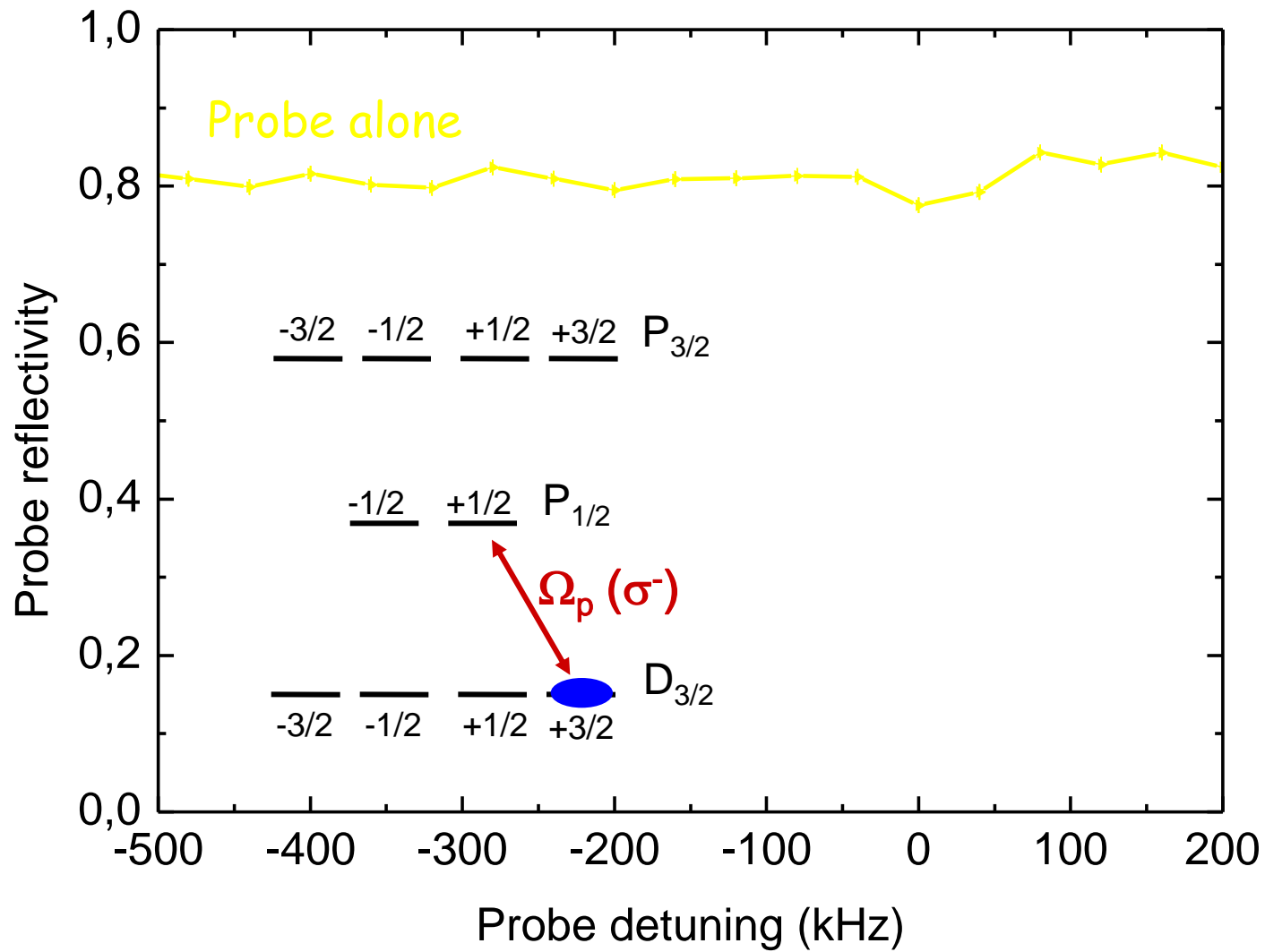
Very challenging !!

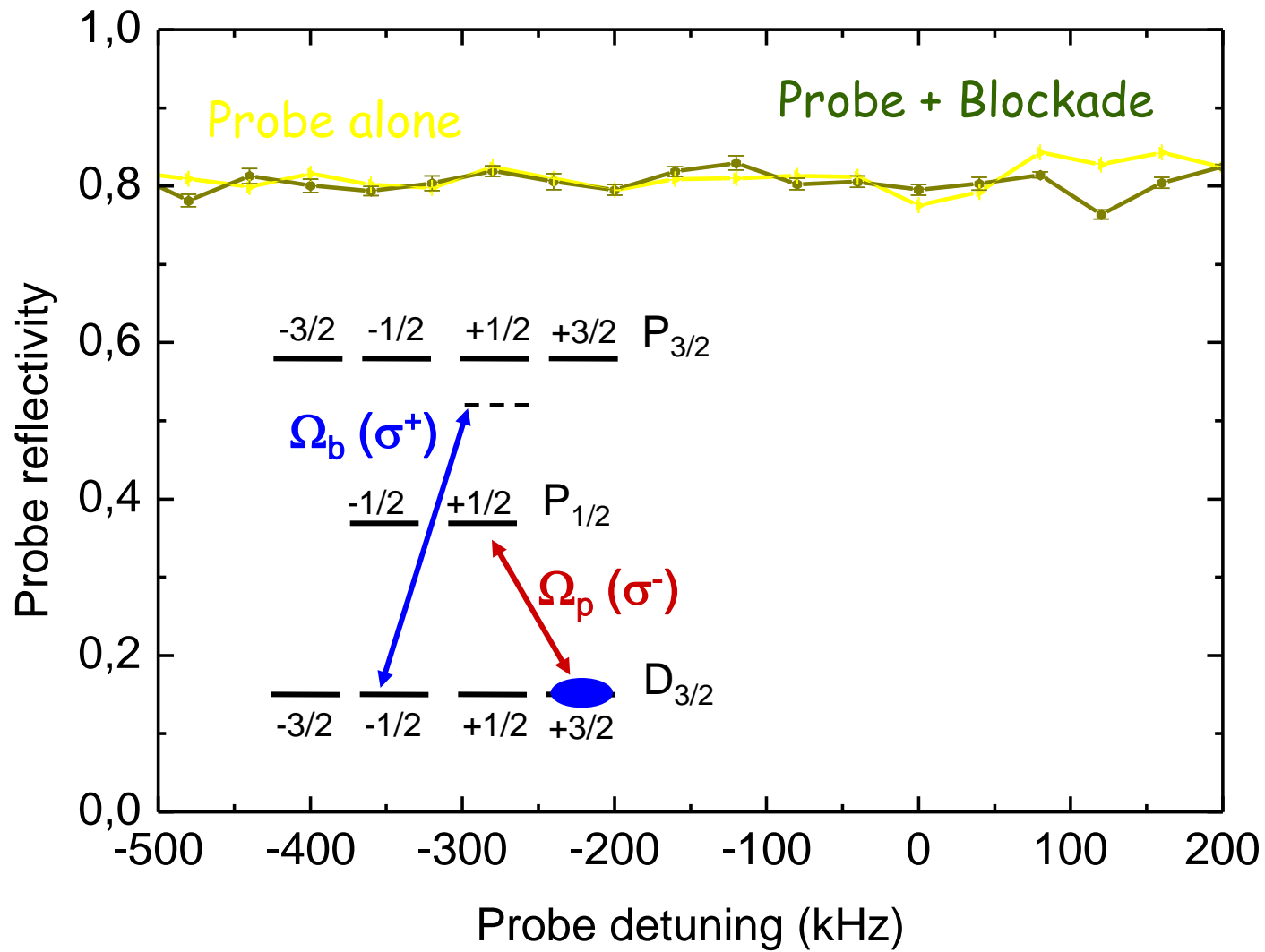
Sketch of experimental setup

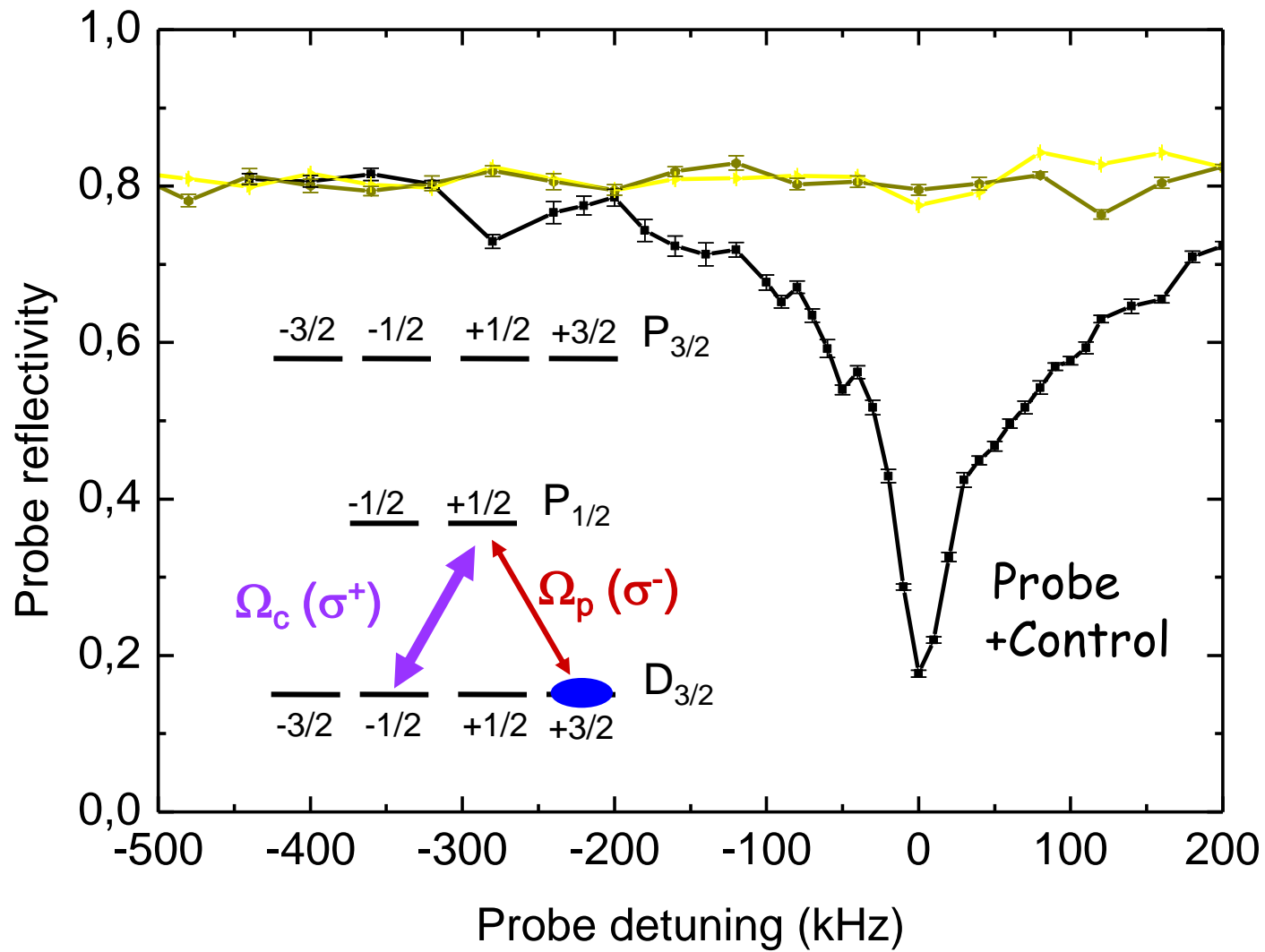


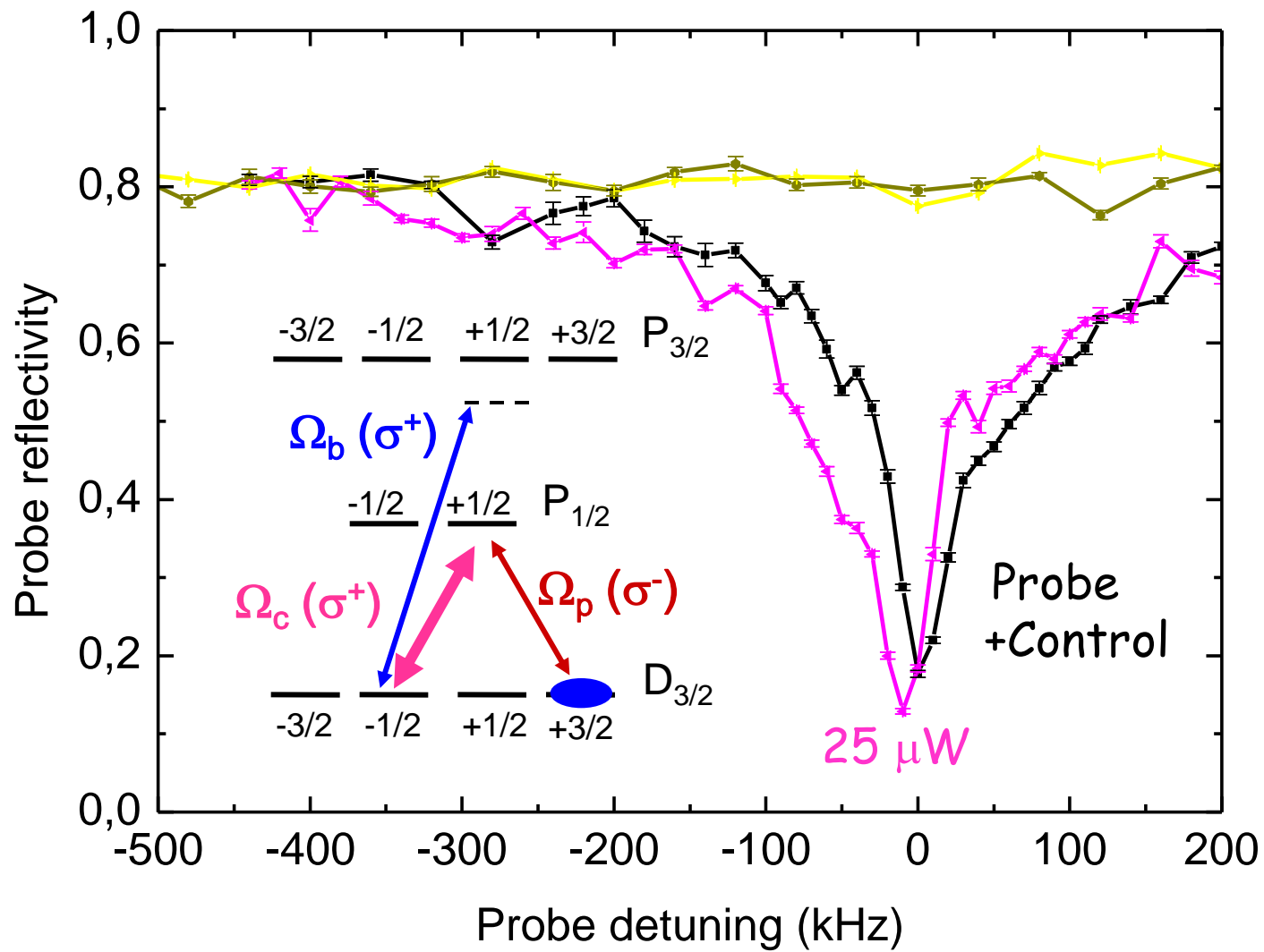
Ca⁺:

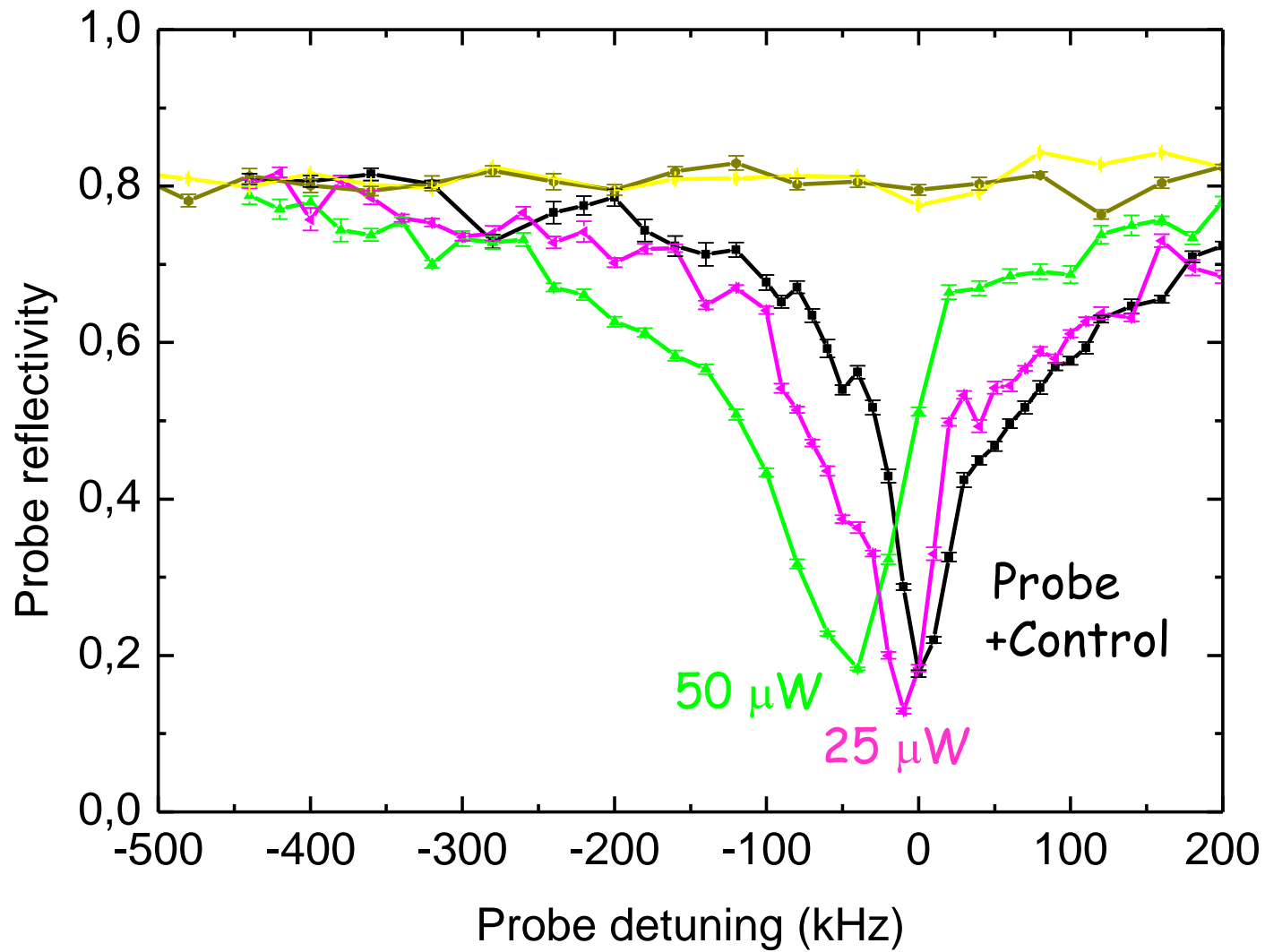


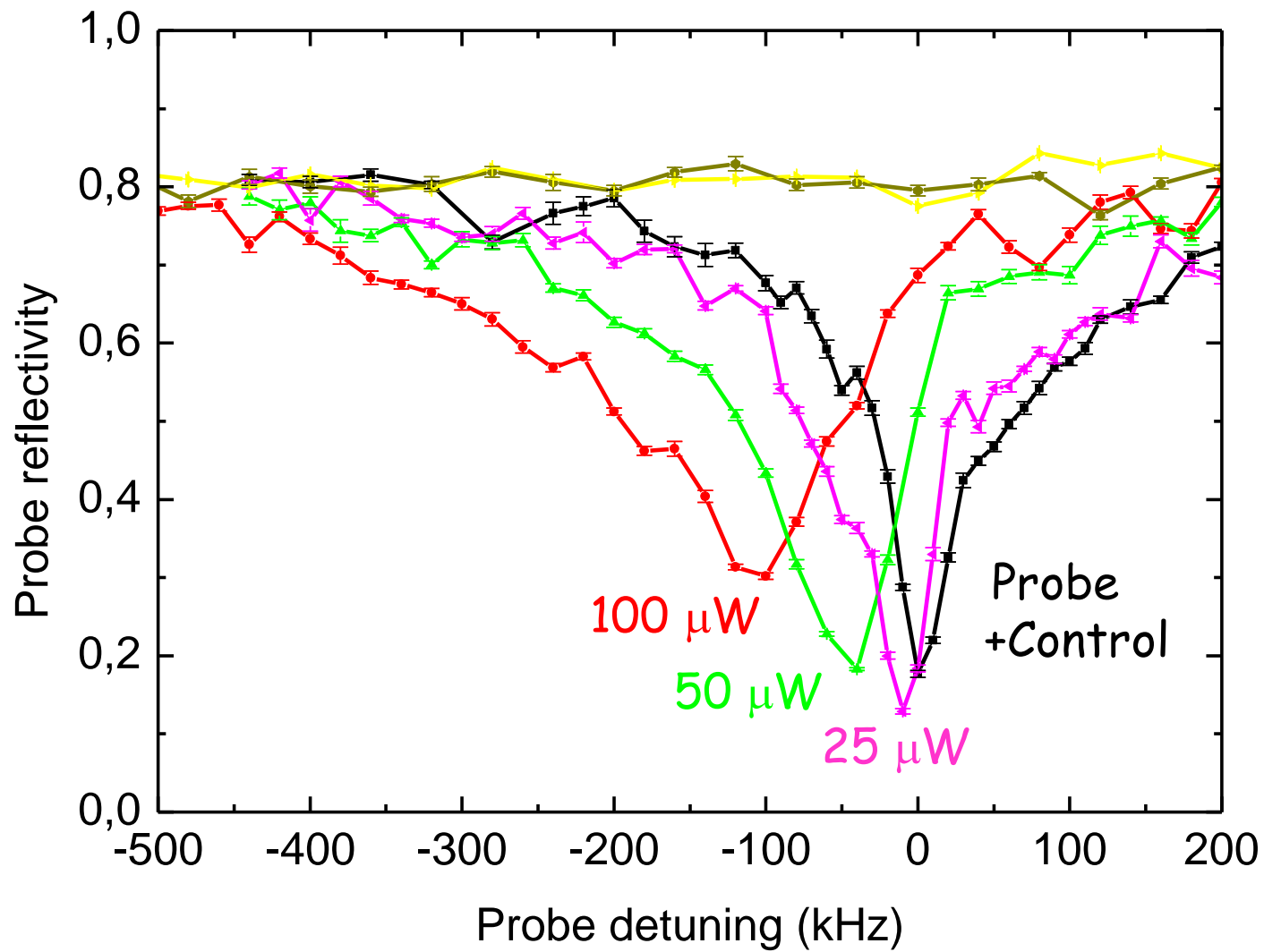


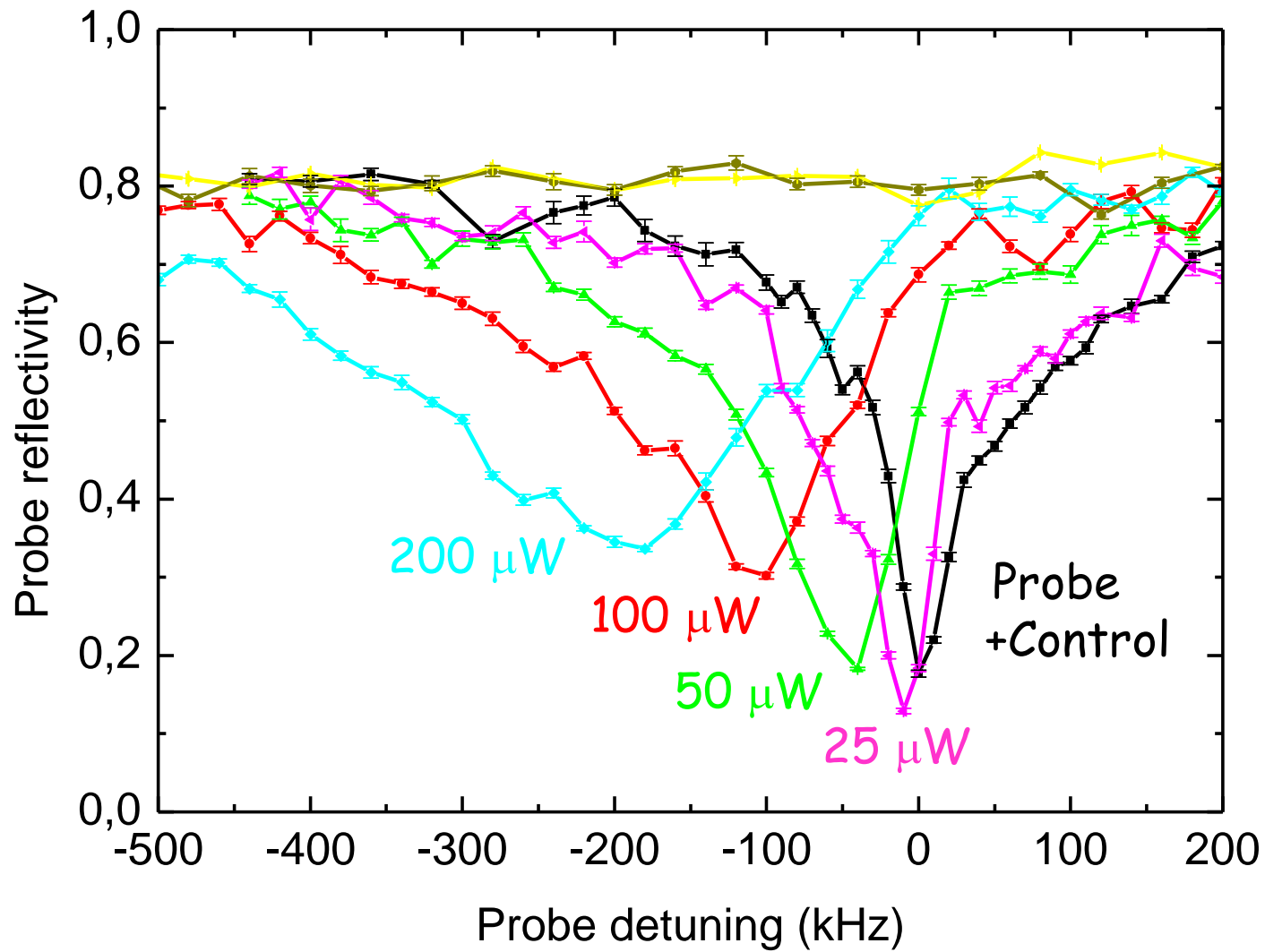




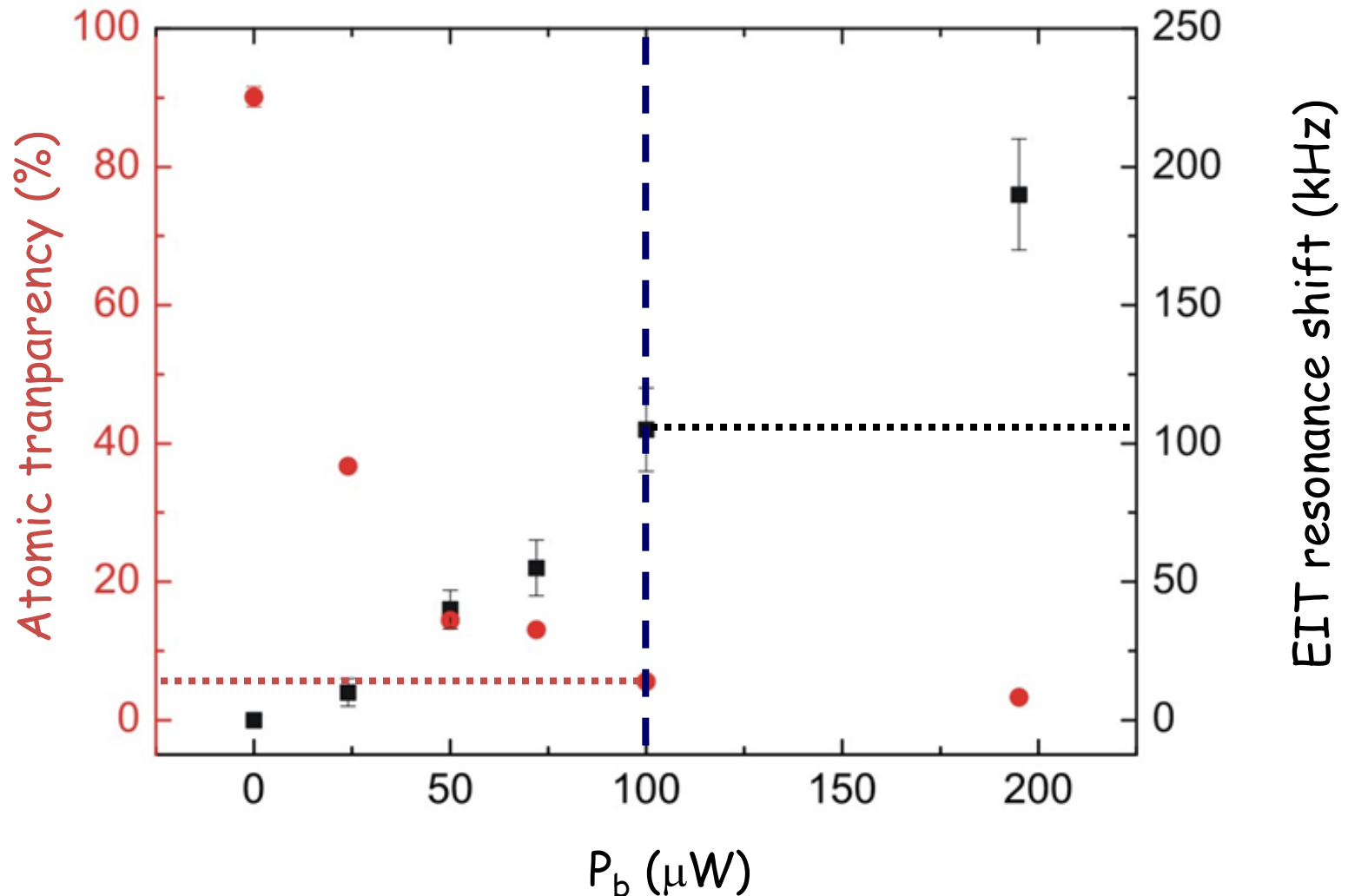








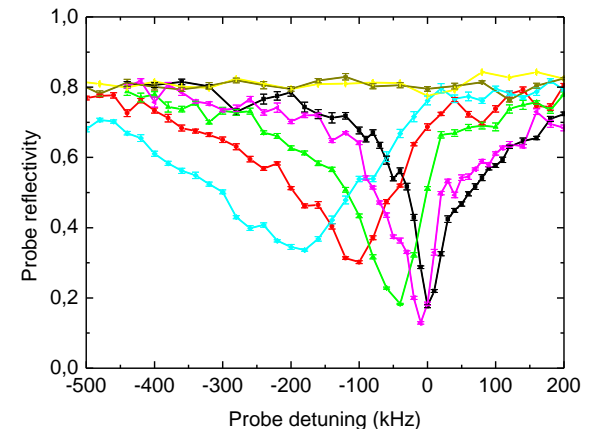
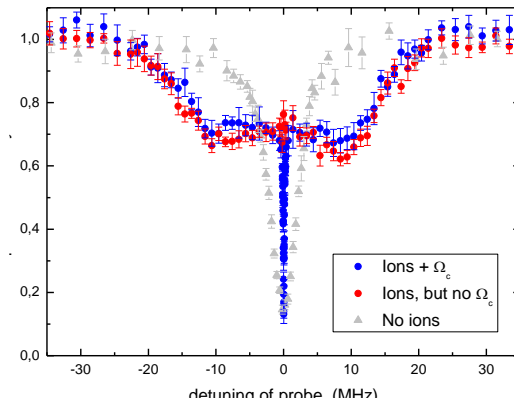
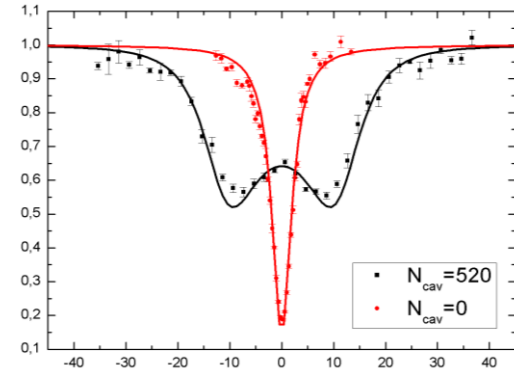
Photon blockade vs. blockade laser power



Corresponds to $\sim 25,000$ blockade photons in cavity at a detuning of 4.3 GHz
The same shift obtainable for a few photons tuned close to resonance !

IV) Conclusion

- Collective strong coupling has been realized with ion Coulomb crystals.
- Cavity EIT in the collective strong coupling regime has been demonstrated.
- A photon blockade mechanism has been demonstrated via a 4-level scheme in the $^{40}\text{Ca}^+$ ion.
- More to come ...



People involved:

Aurelien Dantan (Post Doc)

Joan Marler (Post Post Doc)

Peter Herskind (Post PhD)

Magnus Albert (PhD)

Rasmus B. Linnet (PhD)

Martin Larsen (MSc)

Open PhD position !

Jens Lykke Sørensen (Post Doc)

Anders Mortensen (PhD/Post Doc)

Maria Langkilde-Lauesen (MSc)

Esben S. Nielsen (MSc)

