

# Results and studies in the CUPID-Mo and CUPID experiments based on GEANT4 simulations

Léonard IMBERT on behalf of the CUPID-Mo and CUPID collaborations

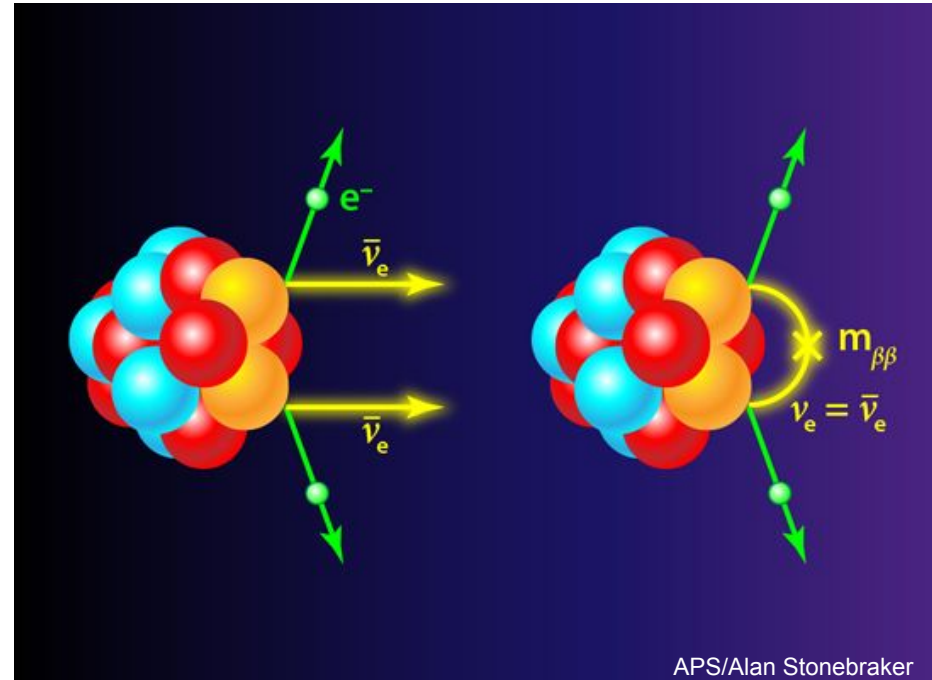
VIEWS24

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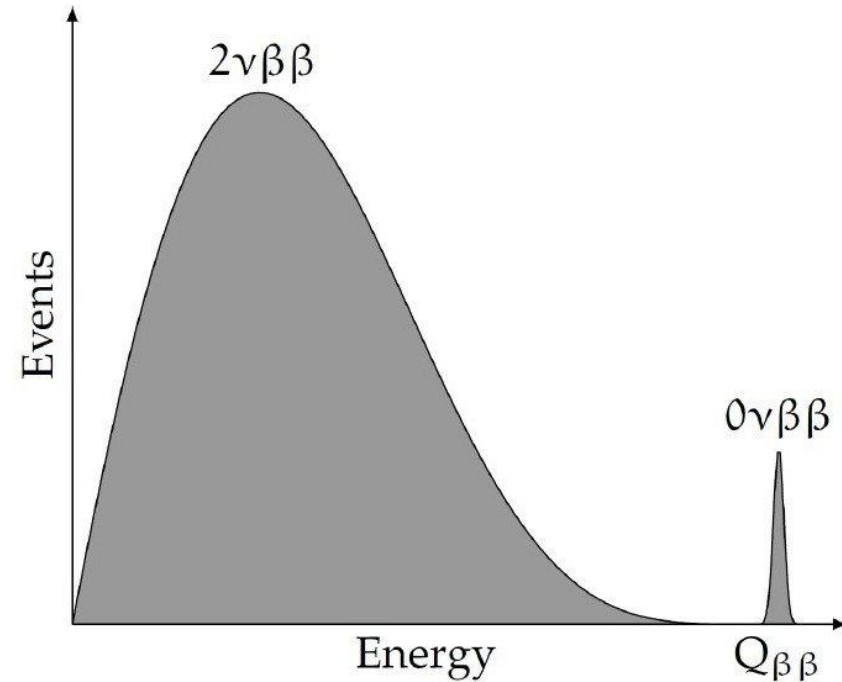
# Neutrinoless double beta decay

- $2\nu\beta\beta$ 
  - $2n \rightarrow 2p + 2e^- + 2\bar{\nu}_e$
  - Standard Model process
  - Observed for 14 nuclei
- $0\nu\beta\beta$ 
  - Hypothetical decay
  - $2n \rightarrow 2p + 2e^-$
  - Violates lepton number  $\Delta L = 2$
  - Majorana neutrino  $\nu = \bar{\nu}$



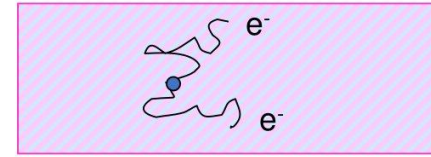
# Searching for $0\nu\beta\beta$

- $0\nu\beta\beta$  signature:
  - Peak at  $Q_{\beta\beta}$  in the sum-energy spectrum of the two electrons
  - Typically  $Q_{\beta\beta} = 2 \sim 3$  MeV
- How to do a good experiment?
  - Low background around the region of interest
  - Good energy resolution
  - High detection efficiency
  - Large mass
  - Long data taking



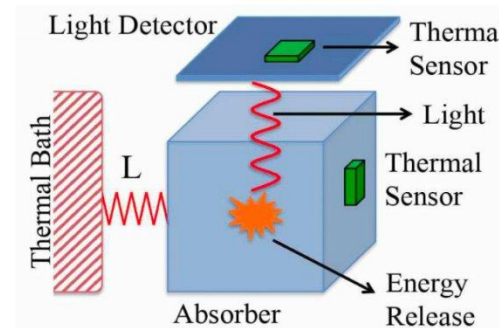
# Bolometers

- Crystals cool down to  $\sim 10 - 20$  mK
- Detector = Source  
→ High detection efficiency
- Very good energy resolution  
5 - 10 keV FWHM
  
- Scintillating bolometers
  - Heat and Light signals
  - Discrimination between  $\beta/\gamma$  and  $\alpha$

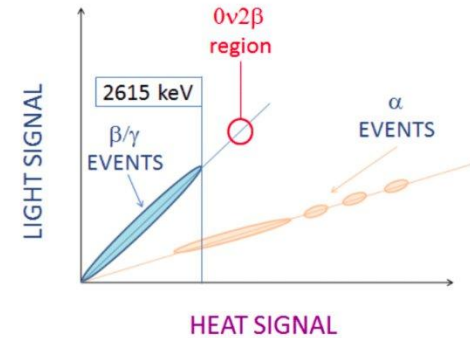


Source  $\equiv$  Detector

Scintillating Bolometer



Particle Identification

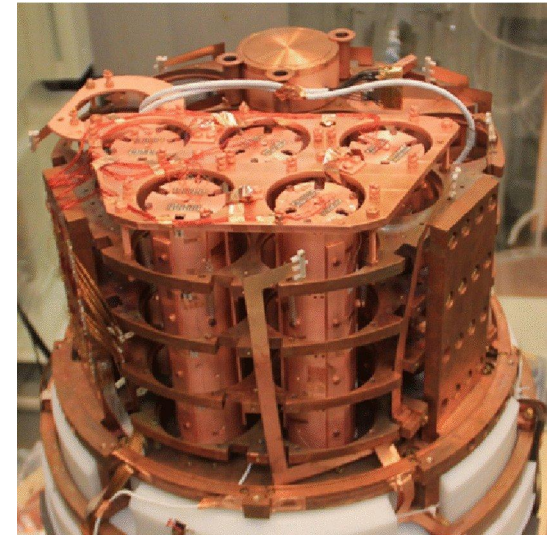
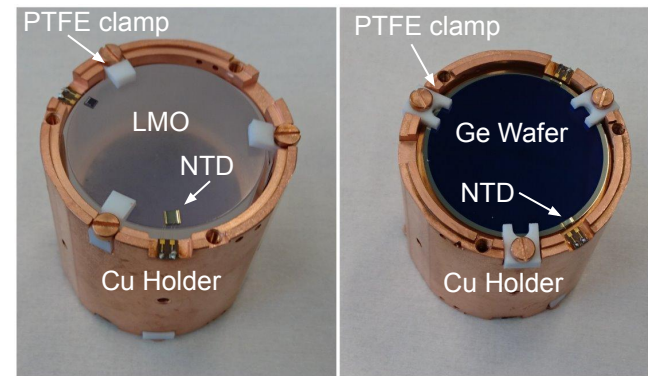


# CUPID-Mo

- Demonstrator for the next experiment CUPID
- Installed in Laboratoire Souterrain de Modane (France) in EDELWEISS cryostat
- Studied  $0\nu\beta\beta$  of  $^{100}\text{Mo}$  ( $Q_{\beta\beta} = 3034 \text{ keV}$ )
- 20  $\text{Li}_2^{100}\text{MoO}_4$  scintillating bolometers
  - 0.2 kg cylindrical crystals ( $\varnothing 44 \times 45 \text{ mm}$ )
  - $^{100}\text{Mo}$  enrichment  $\sim 97 \%$
  - Ge wafers as Light Detectors
  - NTD Ge thermistors to read the signal
  - Reflecting foils to increase light collection

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- Set a limit of :  $T_{1/2} > 1.8 \times 10^{24} \text{ yr}$  (90% C.I.)  
on the  $0\nu\beta\beta$  of  $^{100}\text{Mo}$
- Corresponds to:  $m_{\beta\beta} < (280 - 490) \text{ meV}$



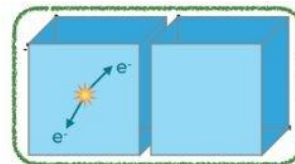
# Experimental Data

$M_{1,\beta/\gamma}$ ,  $M_2$  and  $M_{1,\alpha}$  spectra

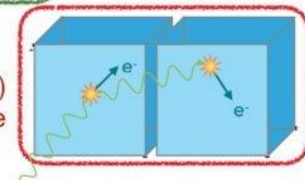
$0\nu\beta\beta$  analysis

Information on  $\gamma$  background

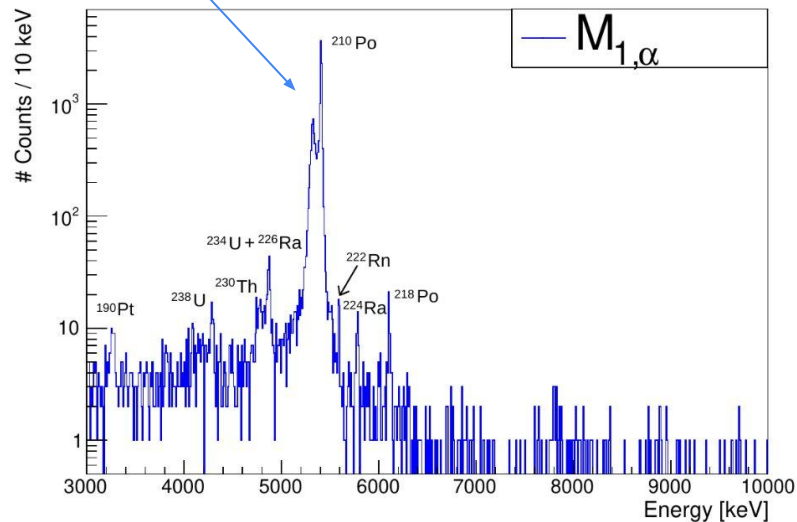
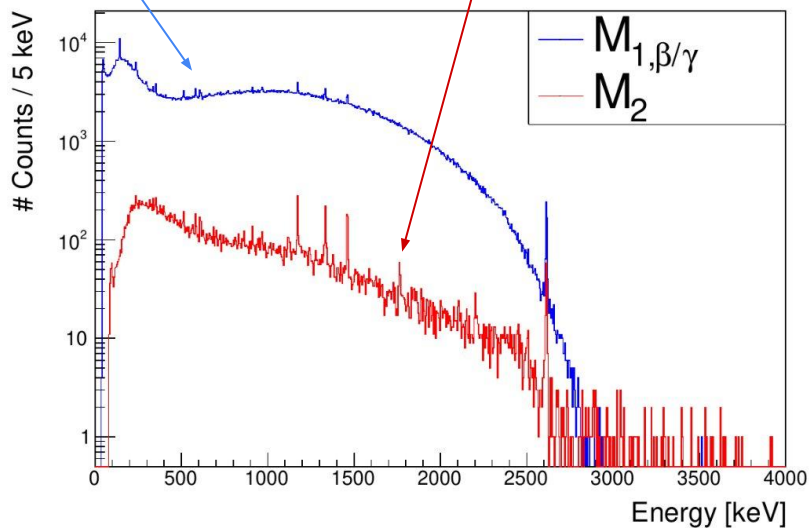
Information on crystal radiopurities



Multiplicity 1 (M1)  
Signal-like



Multiplicity 2 (M2)  
Not signal-like

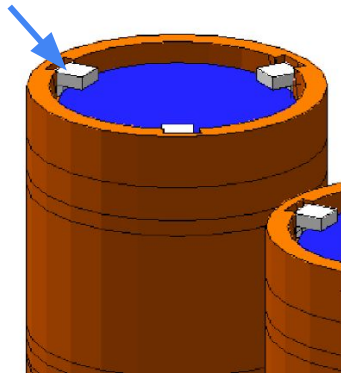


# GEANT4 Geometry

- Based on the program developed by EDELWEISS dark matter experiment
- Detailed geometry of the CUPID-Mo towers
- Reproduced the size of each crystal
- Geometry includes:

Crystals      Ge Light Detectors

PTFE clamps      Reflecting foils



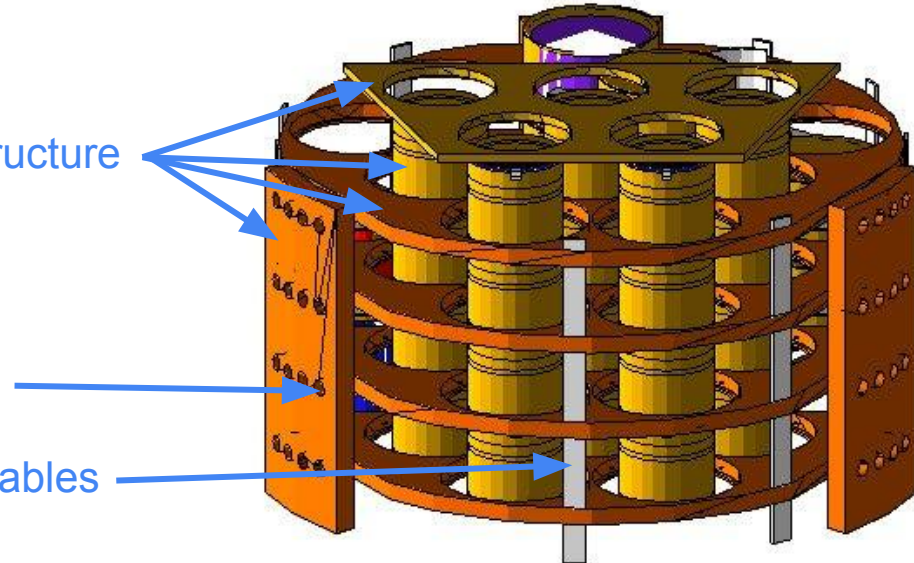
Copper structure

Springs

Screws

Readout cables

EDELWEISS detectors and readout



# GEANT4 Geometry

- Based on the program developed by EDELWEISS
- Detailed geometry of the CUPID-Mo towers
- Reproduced the size of each crystal
- Geometry includes:

Copper screens (10mK, 1K, 50K, 100K, 300K)

Internal Polyethylene shielding

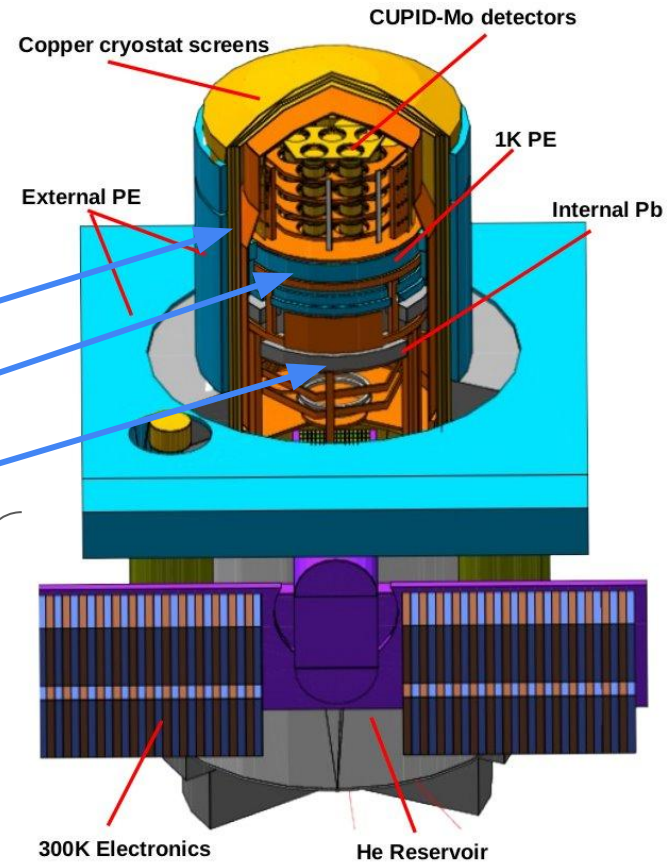
Lead shielding

Dilution unit

300K electronics

Pumps

He Reservoir





# GEANT4 simulations

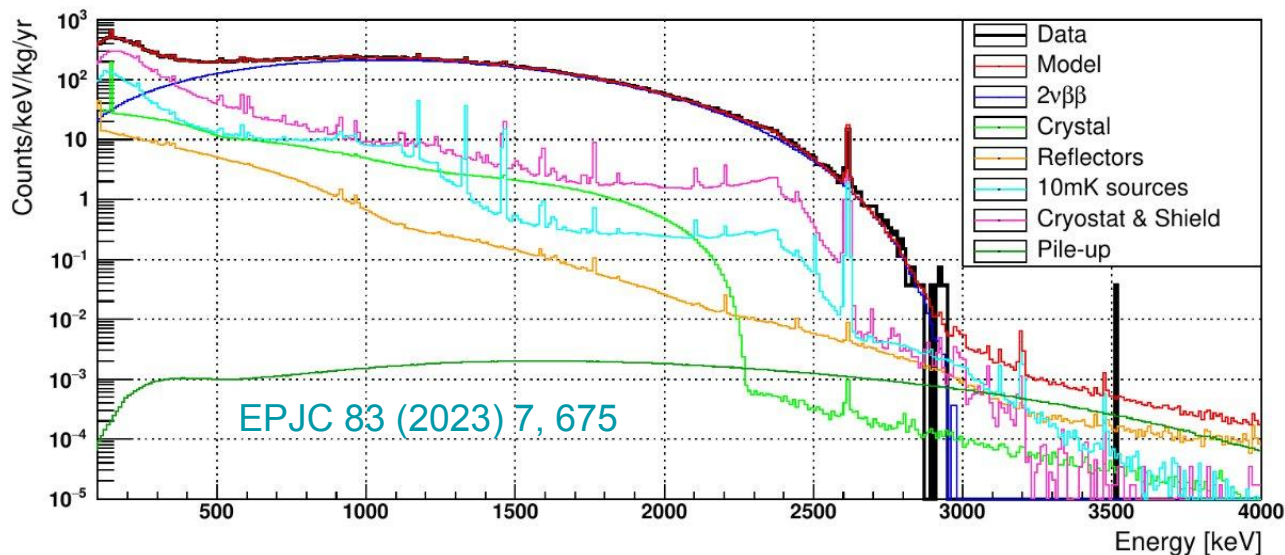
- G4RadioactiveDecay
  - Used for close sources to generate decay chains considering break in secular equilibrium
    - $^{232}\text{Th}$  ●  $^{228}\text{Ra}$  to  $^{228}\text{Th}$  ●  $^{228}\text{Th}$  to  $^{208}\text{Pb}$
    - $^{238}\text{U}$  to  $^{234}\text{U}$  ●  $^{234}\text{U}$  ●  $^{230}\text{Th}$  ●  $^{226}\text{Ra}$  to  $^{210}\text{Pb}$  ●  $^{210}\text{Pb}$  to  $^{206}\text{Pb}$
  - Allows to register the time of event needed for the modelisation of the detector response
- Decay0
  - Used for all the other decays (not directly facing the crystals)
  - Read input files in the PrimaryGeneratorAction class to set particle type and momentum
- $2\nu\beta\beta$ 
  - Sampled from theoretical two-dimensional single electron energy spectrum

# GEANT4 simulations

- Surface contaminations
  - Used for the crystals and the reflecting foils
  - Modelled with an exponential density profile  $e^{-x/\lambda}$
  - We did simulations with  $\lambda = 10$  nm and  $10$   $\mu\text{m}$  for crystals and reflectors
- Livermore Physics list
- Production cuts:  $1$   $\mu\text{m}$  for  $e^-/e^+$  and  $10$   $\mu\text{m}$  for  $\gamma$ 's
  - It corresponds to  $1$  keV for both  $e^-/e^+$  and  $\gamma$ 's in the crystal
  - Using a production cut corresponding to  $250$  eV was giving comparable spectra

# Background Model

- Describe the experimental data by a linear combination of the GEANT4 simulation spectra
- Simultaneous fit of  $M_{1,\beta/\gamma}$ ,  $M_2$  and  $M_{1,\alpha}$  spectra
- Done with the JAGS software based on Monte-Carlo Markov Chains
- We used 67 sources in the fit



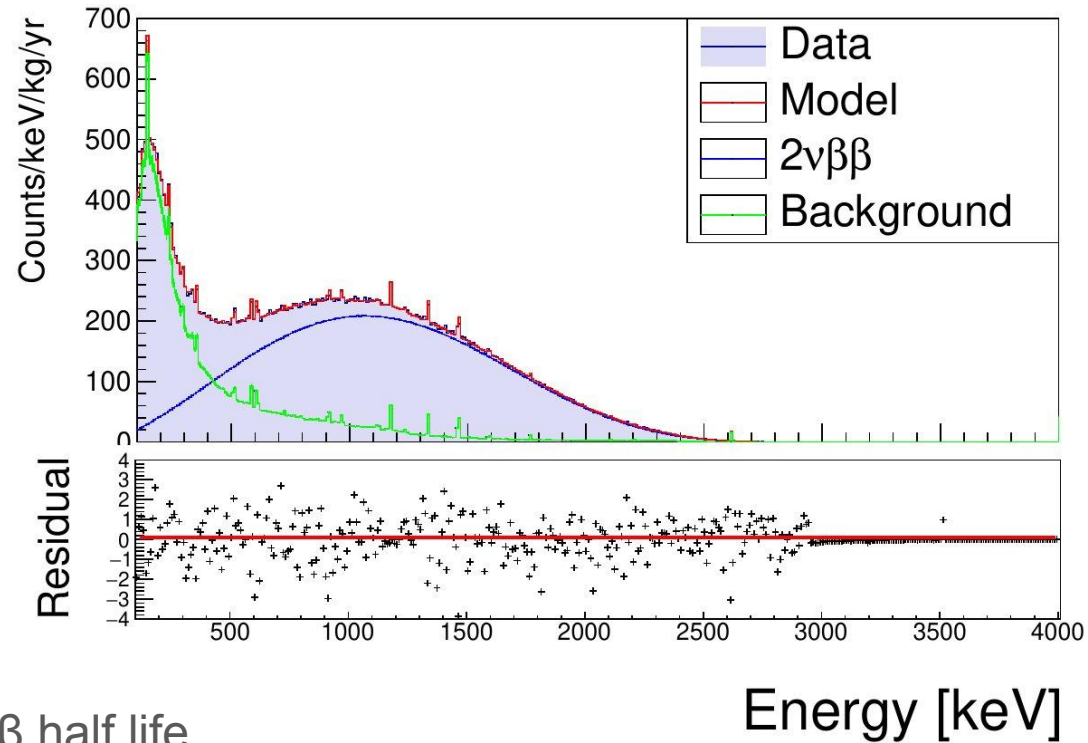
Background index

=

$$2.7^{+1.3}_{-0.8} \times 10^{-3} \text{ cts/keV/kg/yr}$$

EPJC 83 (2023) 7, 675

# $2\nu\beta\beta$ spectrum



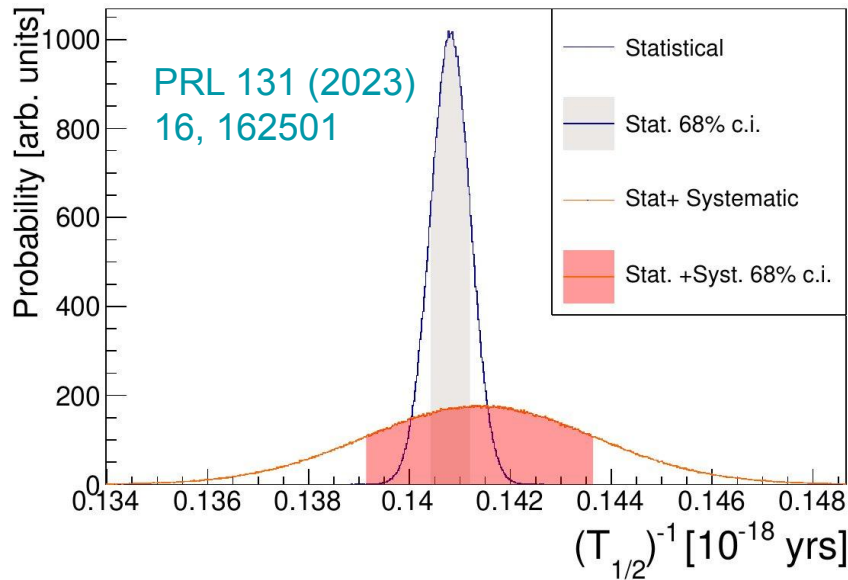
Excellent signal to background ratio

Allows for:

- Precise measurement of the  $2\nu\beta\beta$  half life
- Studies of the  $2\nu\beta\beta$  spectral shape

# 2νββ half life

- Measurement comes directly from the background model fit
- Systematics evaluated by varying assumptions on the background model



Related to the background model

We vary in GEANT4 the bremsstrahlung cross section by +/- 10 %

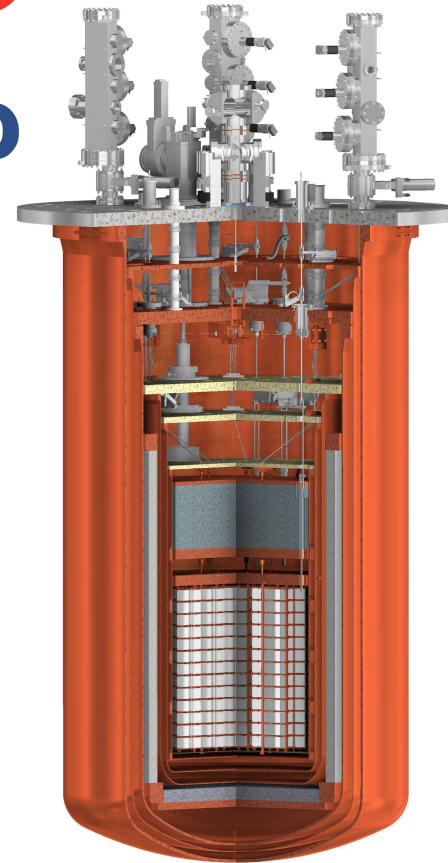
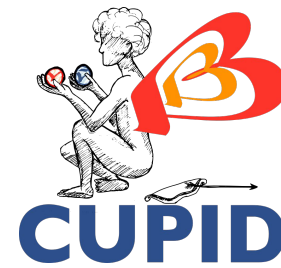
Systematic test	Uncertainty $T_{1/2}$ [%]
Binning	+/- 0.37
Energy Bias	+0.11 -0.16
Bremsstrahlung	+0.13 -0.22
MC statistic	+/- 0.11
Source location	+/- 0.83
Minimal model	+/- 0.24
$^{90}\text{Sr} + ^{90}\text{Y}$	+ 1.0 (uniform distribution)
Efficiency	+/- 1.2
Isotope abundance	+/- 0.2

PRL 131 (2023) 16, 162501

$$T_{1/2} = 7.07 \pm 0.11 \times 10^{18} \text{ yr}$$

# CUPID

- Next generation bolometric  $0\nu\beta\beta$  experiment
- To be installed at LNGS in the CUORE cryostat
- Focus will be a search for  $0\nu\beta\beta$  of  $^{100}\text{Mo}$  with  $\text{Li}_2^{100}\text{MoO}_4$  crystals
  - Enriched at  $\sim 95\%$  in  $^{100}\text{Mo}$
  - Cubic crystals:  $45 \times 45 \times 45$  mm
  - 1596 crystals: 240 kg of  $^{100}\text{Mo}$
  - Ge Light Detectors with Neganov-Luke amplification for  $\alpha$ 's and pile-ups rejection
- Goals
  - Background Index =  $10^{-4}$  cts/keV/kg/yr
  - Energy resolution = 5 keV FWHM @ 3034 keV

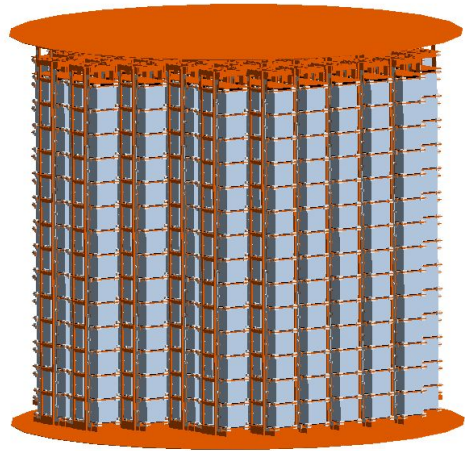


$0\nu\beta\beta$   $3\sigma$  discovery sensitivity

- $T_{1/2} = 10^{27}$  yr
- $m_{\beta\beta} = 12 - 20$  meV

# CUPID simulations

- CUPID detector geometry implemented in the geometry of the CUORE cryostat
- G4RadioactiveDecay
- Livermore Physics list
- The geometry includes:



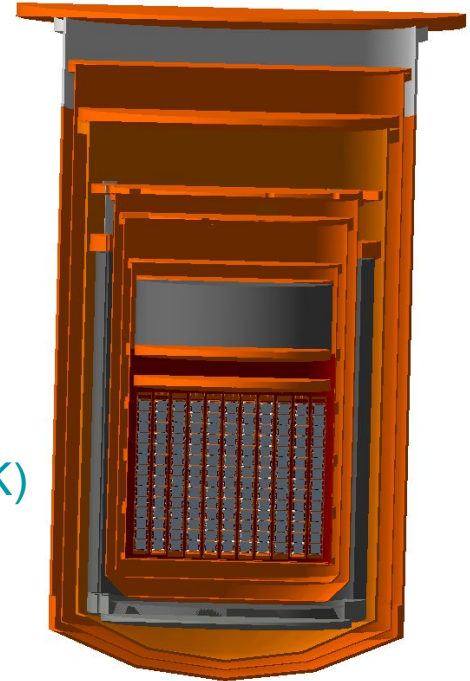
Crystals  
Light Detectors

PTFE pieces  
CuPEN readout  
Copper holders

10mK Screen  
10mK Tiles  
10mK Plate

Cryostat screens  
(50mK, 600mK, 4K, 300K)

Lead shieldings

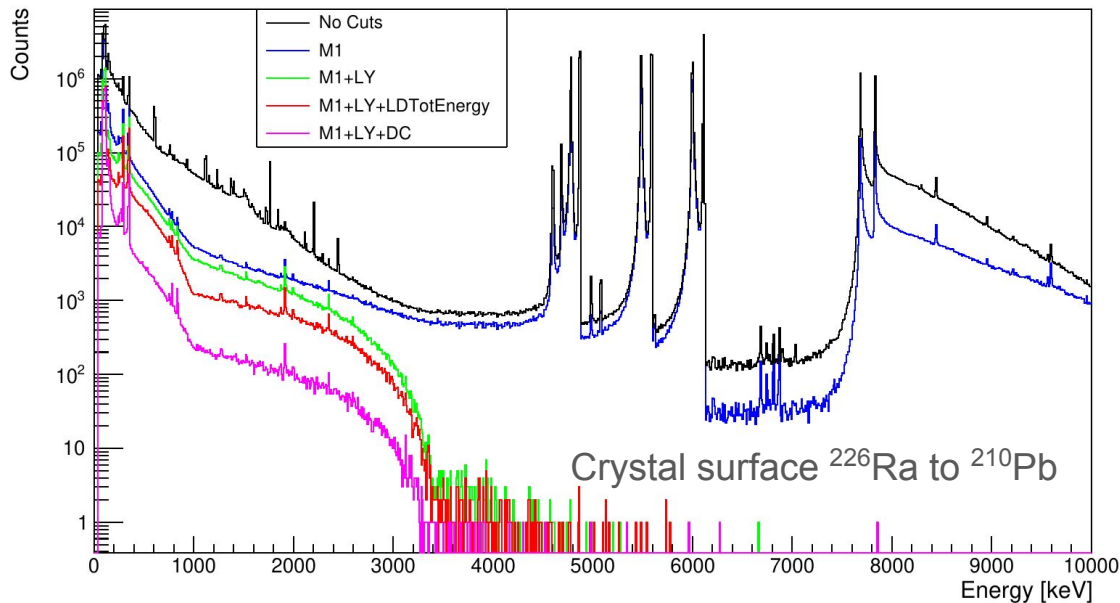


# CUPID Background projections

- Detector effects are convolved into MC spectra

- We generated a total of 85 simulations of the various components of the set-up

- We used input activities from the CUPID-Mo (crystals) and the CUORE background model

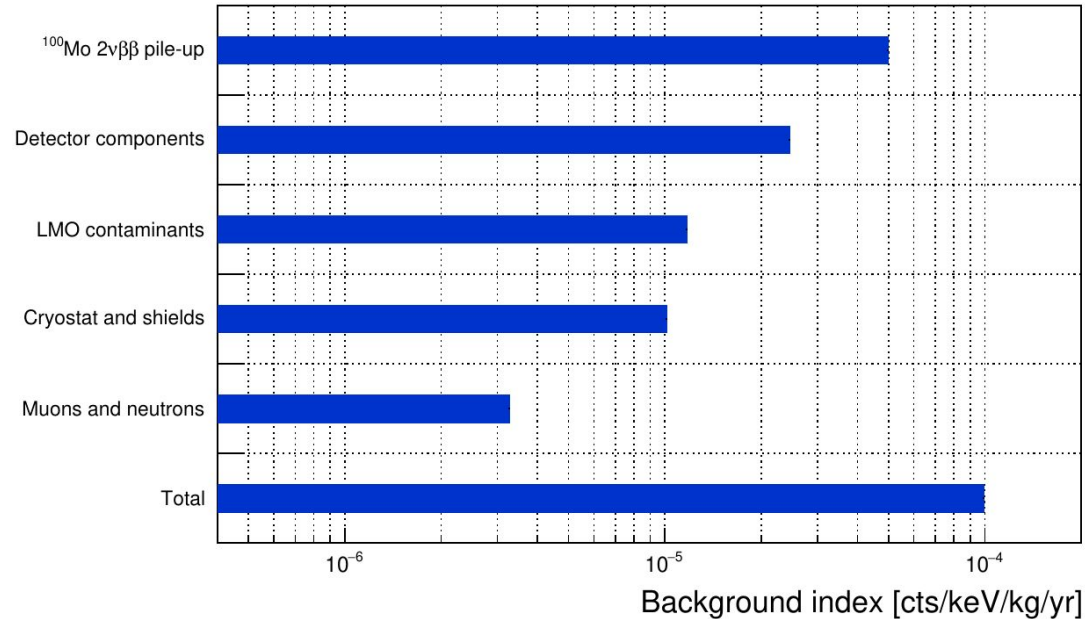




# CUPID Background budget

CUPID background budget is based on results from precursor experiments (CUORE and CUPID-Mo) and on improved new design

- LMO  $^{100}\text{Mo}$  pile-up:
  - Demonstrated performance on baseline NTL detectors
- Detector components:
  - Surface driven
- LMO contaminants:
  - Surface driven
- Cryostat & shields:
  - Bulk
- Muons and neutrons



# CUPID Background projections

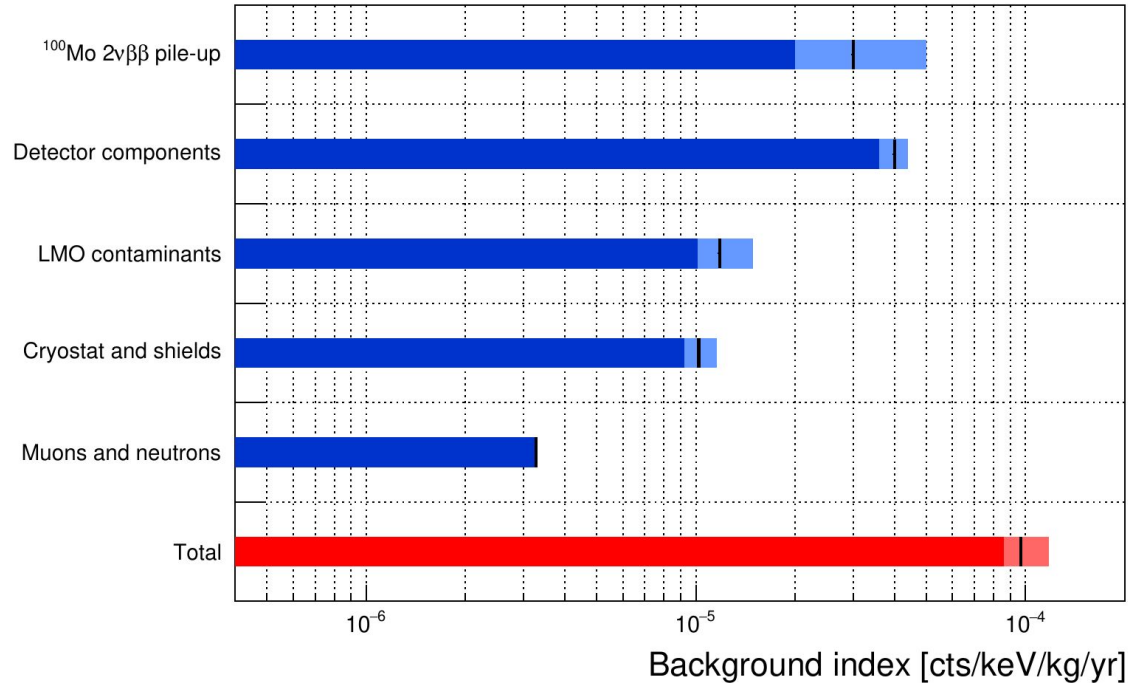
Backgrounds come from:

- Pile-up
  - random coincidence between two  $2\nu\beta\beta$  events
  - extrapolated from measured performances of NTL light detectors
- Detectors components
  - driven by surface of copper holders
- LMO crystal contaminants
  - surface driven
  - includes bulk and cosmogenic
- Cryostat & shields
- Muons and neutrons
  - based on initial design and MC simulation

**Total projected background:**

$$BI = 0.97^{+0.21}_{-0.11} \times 10^{-4} \text{ cts/keV/kg/yr}$$

Work continues on further improvements in the overall background level

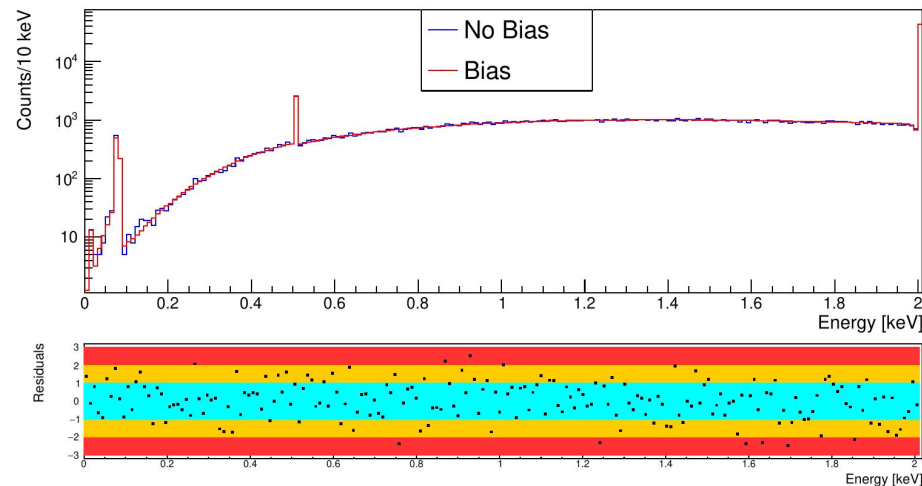
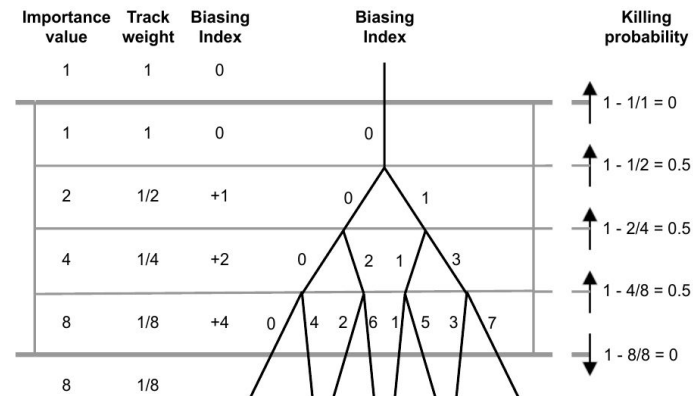


# Importance Biasing

- Simulate the environmental background
  - External lead shield of 25 cm
- Simulate the internal contaminations of the lead shieldings
- Importance biasing is implemented in a separate code based on example extended/biasing/B01
- We then use the output of this code as an input in the main CUPID code
- Validation was done with 2 MeV  $\gamma$  going through 10 cm of Lead

Thanks to the help of Birgit Zatschler

See her presentation for details on importance biasing



# Conclusion

- In CUPID-Mo, GEANT4 simulations permitted the construction of the Background Model, leading to:
  - Evaluation of the Background Index [EPJC 83 \(2023\) 7, 675](#)
  - Evaluation of Crystal contaminations → Important for CUPID [EPJC 83 \(2023\) 7, 675](#)
  - Most precise measurement of the  $2\nu\beta\beta$  half-life of  $^{100}\text{Mo}$  [PRL 131 \(2023\) 16, 162501](#)
  - First measurement of spectral shape theoretical parameters of the  $2\nu\beta\beta$  of  $^{100}\text{Mo}$   
[PRL 131 \(2023\) 16, 162501](#)
- In CUPID, GEANT4 simulations are used for background projections
  - We find that background estimations agree with CUPID goals

# BACK-UP

# Neutrinoless double beta decay

- $2\nu\beta\beta$

- $2n \rightarrow 2p + 2e^- + 2\nu_e$
- Standard Model process
- Observed for 14 nuclei

- $0\nu\beta\beta$

- Hypothetical decay
- $2n \rightarrow 2p + 2e^-$
- Violates lepton number  $\Delta L = 2$
- Majorana neutrino  $\nu = \bar{\nu}$

Phase space factor:

- Known and calculated to good accuracy

Nuclear Matrix Element:

- Differences between various nuclear models

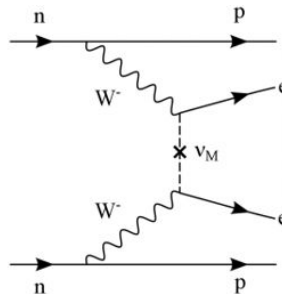
$$\left(T_{1/2}^{0\nu}\right)^{-1} = G^{0\nu} \left(g_A^{0\nu}\right)^4 \left(M^{0\nu}\right)^2 \left|\frac{m_{\beta\beta}}{m_e}\right|^2$$

Weak axial-vector coupling strength:

- Question of possible  $g_A$  quenching under study

Effective Majorana mass:

- $m_{\beta\beta} = \left| |U_{e1}|^2 m_1 + e^{i\alpha_1} |U_{e2}|^2 m_2 + e^{i\alpha_2} |U_{e3}|^2 m_3 \right|$



# CUPID-Mo Detector Response Model

- We processed the MC simulations to account for:
  - Energy resolution
  - Energy threshold of 40 keV
  - Event Multiplicity
  - Scintillation Light and Light Detector (LD) resolution
    - We parameterised the scintillation light and the resolution measured by the LD as a function of the energy, the crystal, and the LD (which have different performances)
    - We then generated a random scintillation light for each event
  - Cut efficiencies
  - Inactive periods of detectors
  - Pile-up and delayed coincidences in decay chains

# 2νββ spectral shape measurement

- Measuring the 2νββ spectral shape constrains nuclear models for Nuclear Matrix Element calculations
- We implemented an improved description of the 2νββ in our fit:

$$\frac{d\Gamma}{dE} = (g_A^{\text{eff}})^4 |M_{GT-1}^{2\nu}|^2 \left( \frac{dG_0^{2\nu}}{dE} + \xi_{31} \frac{dG_2^{2\nu}}{dE} + \frac{1}{3} \xi_{31}^2 \frac{dG_{22}^{2\nu}}{dE} + \left( \frac{1}{3} \xi_{31}^2 + \xi_{51} \right) \frac{dG_4^{2\nu}}{dE} \right)$$

PRC 97 (2018) 034315

Spectral shape parameters

- We used a gaussian prior on  $\xi_{51}/\xi_{31}$  based on theory
- We obtained  $\xi_{31} = 0.45 \pm 0.06$  and  $g_A(\text{pn-QRPA}) = 1.0 \pm 0.2$

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