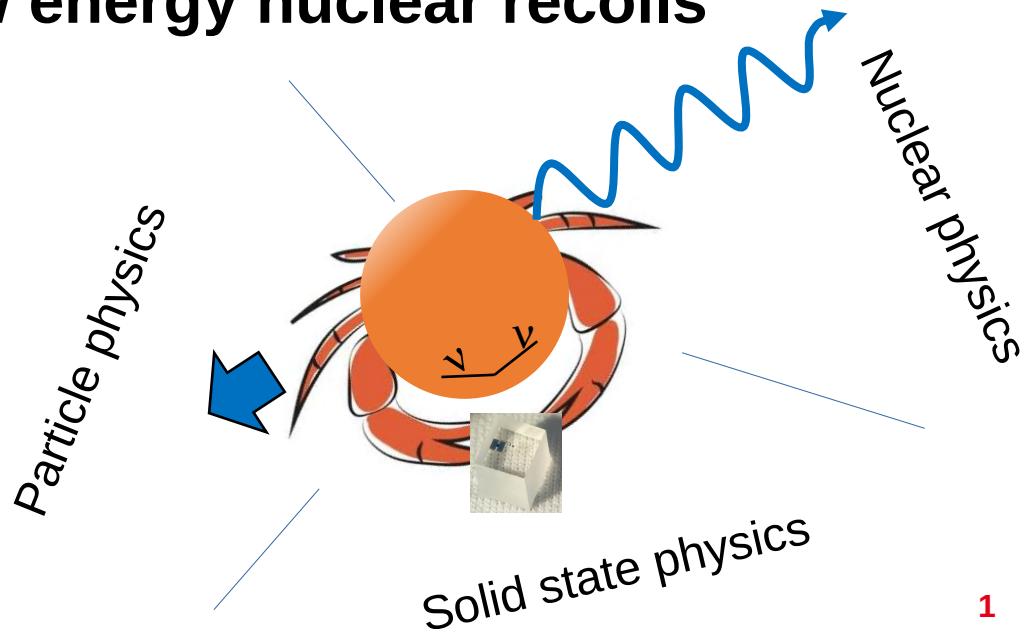


# Accurate simulations for the CRAB project: from thermal neutron production to low energy nuclear recoils

L. Thulliez on behalf of the CRAB collaboration

CEA-Saclay/DRF/Irfu/DPhN

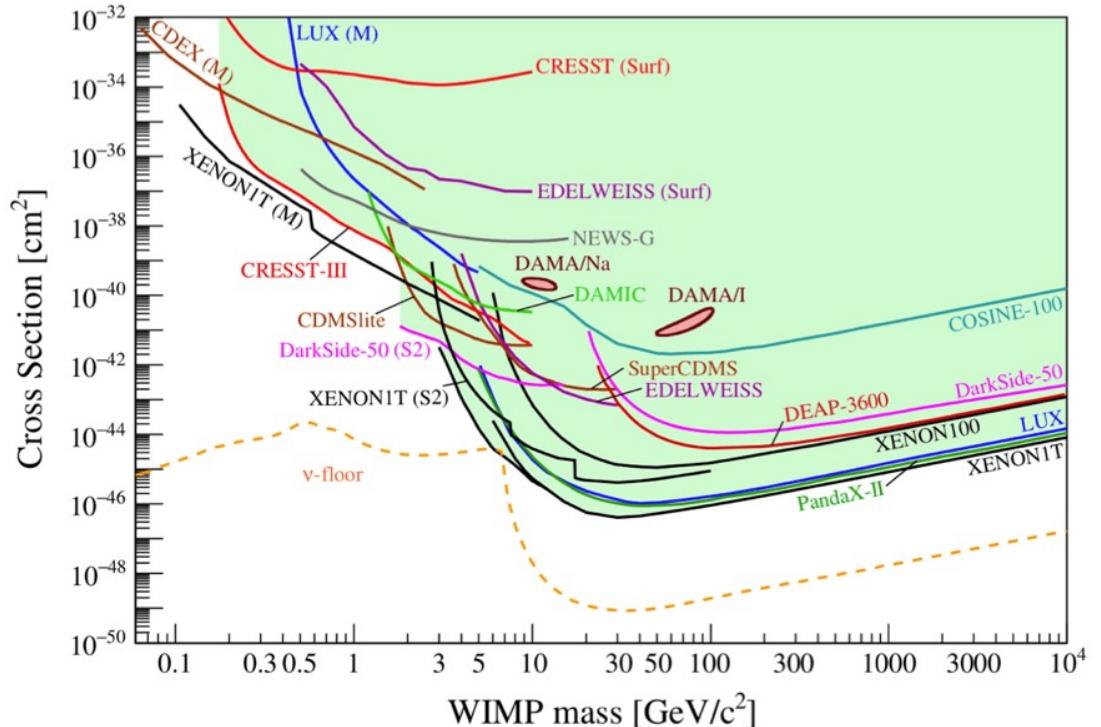
[loic.thulliez@cea.fr](mailto:loic.thulliez@cea.fr)





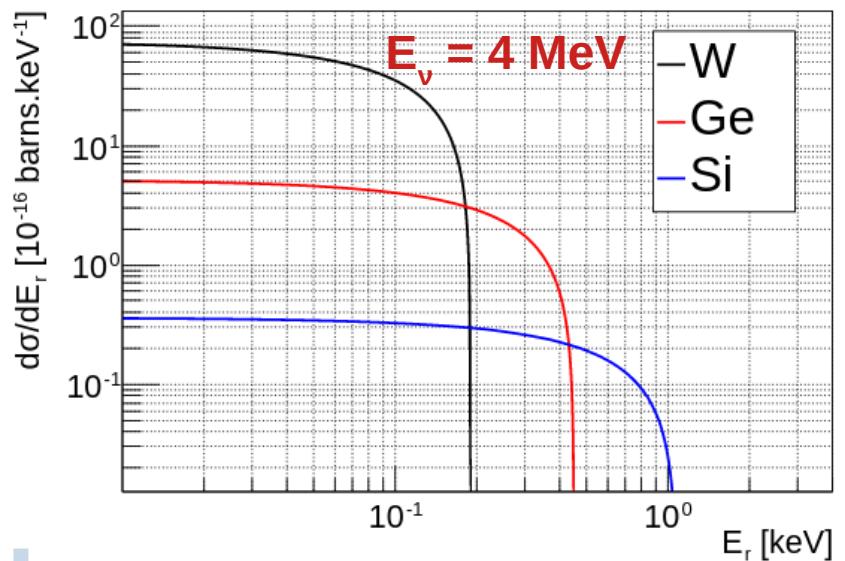
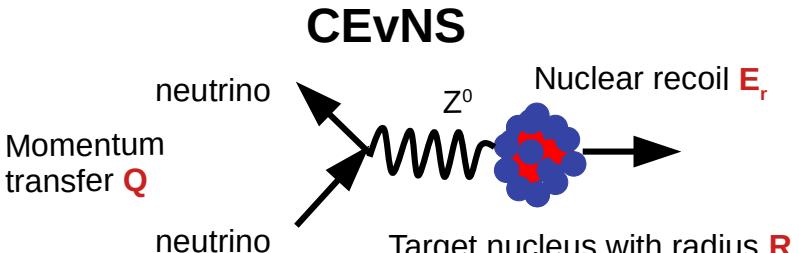
# DARK MATTER and CEvNS

## DARK MATTER



Direct Detection of Dark Matter APPEC Committee Report (2021)

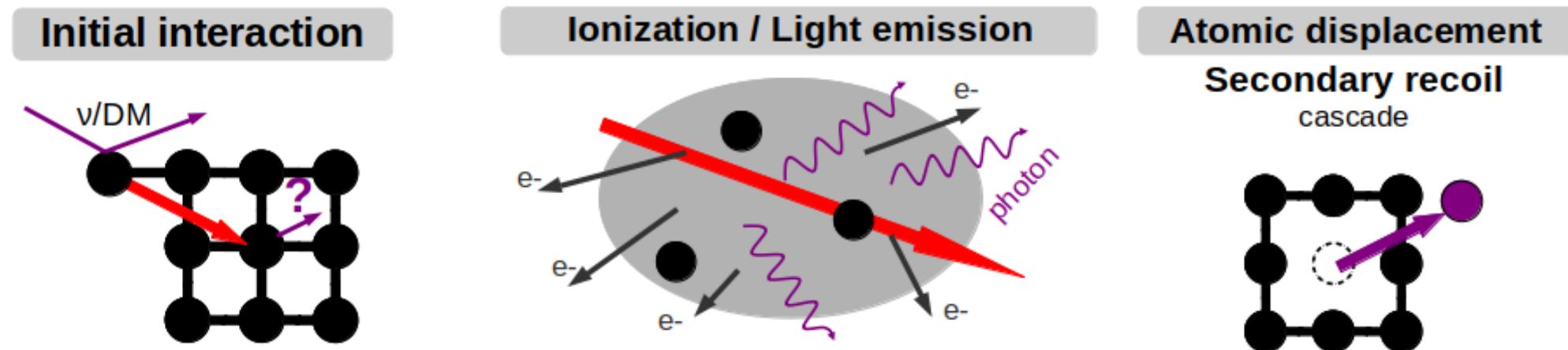
- Moving to lower mass range
- Sensitivity in large mass range approaching the neutrino-floor limit



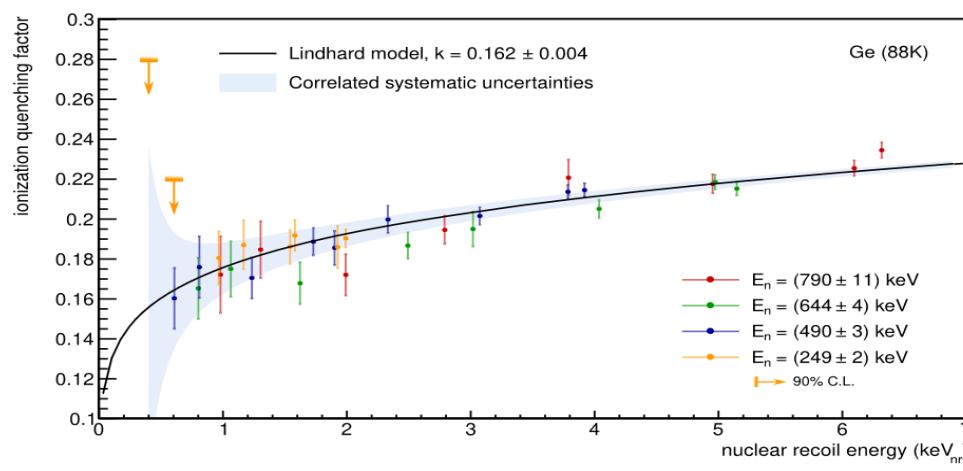
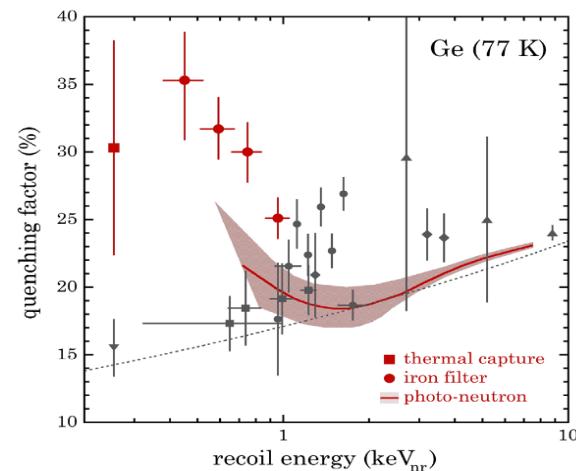
- test SM ( $\theta_W$ , etc)
- test BSM physics  
(neutrino magnetic moment, non-standard interaction, etc)
- Measure nuclear form factor (neutron skin)
- Nuclear reactor monitoring

# WHAT HAPPEN AFTER A PRIMARY RECOIL (> keV) IN THE DETECTOR ?

Complex solid state physics to understand for precise measurements



Quenching factor  $k$  ( $= E_{nr}^{ioni}/E_{e^-}^{ioni}$ ) below 1 keV ?



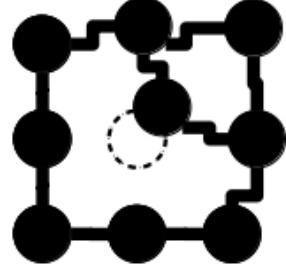
# WHAT HAPPEN AFTER A PRIMARY RECOIL (<keV) IN THE DETECTOR ?

Complex solid state physics to understand for precise measurements

## Atomic displacement

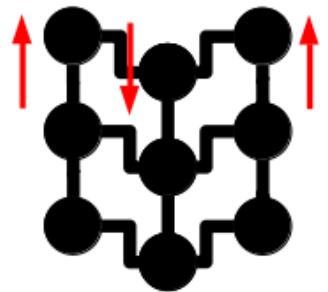
### Lattice defect creation

energy trapped in the detector  
⇒ energy biasing



### Phonon excitation

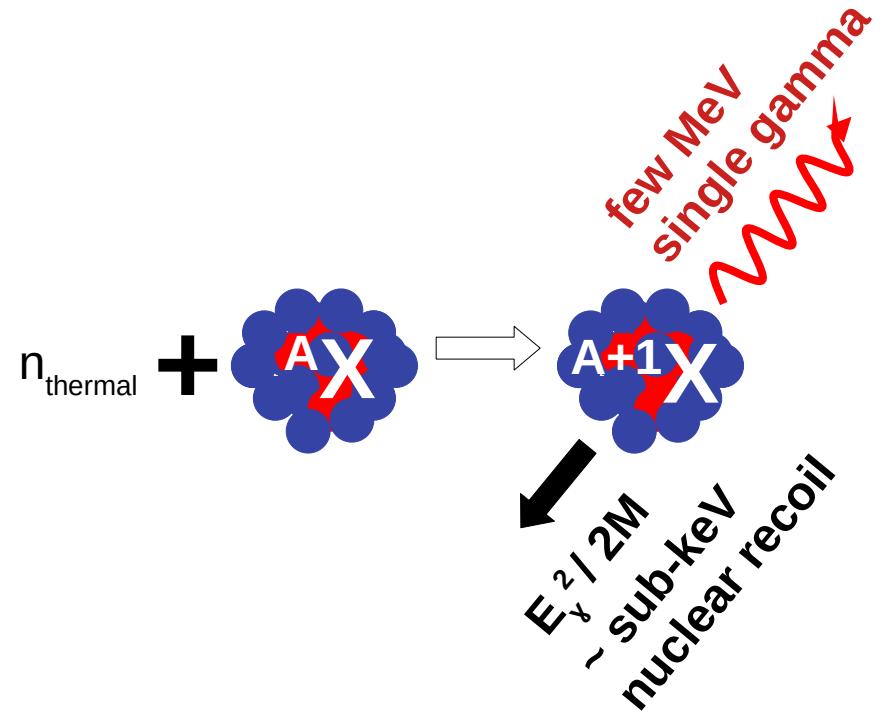
temperature increase



- Impact of energy stored in lattice defect when reaching 100 eV scale ?  
⇒ linearity study

# CRAB METHOD [1]

Absolute calibration method with thermal (~25meV) neutron radiative capture



## Advantages

- Pure nuclear recoil  $\Rightarrow$  mimic the neutrino/DM signal
- Allows to probe the whole bolometer
- Accuracy  $\Rightarrow$  well defined peak

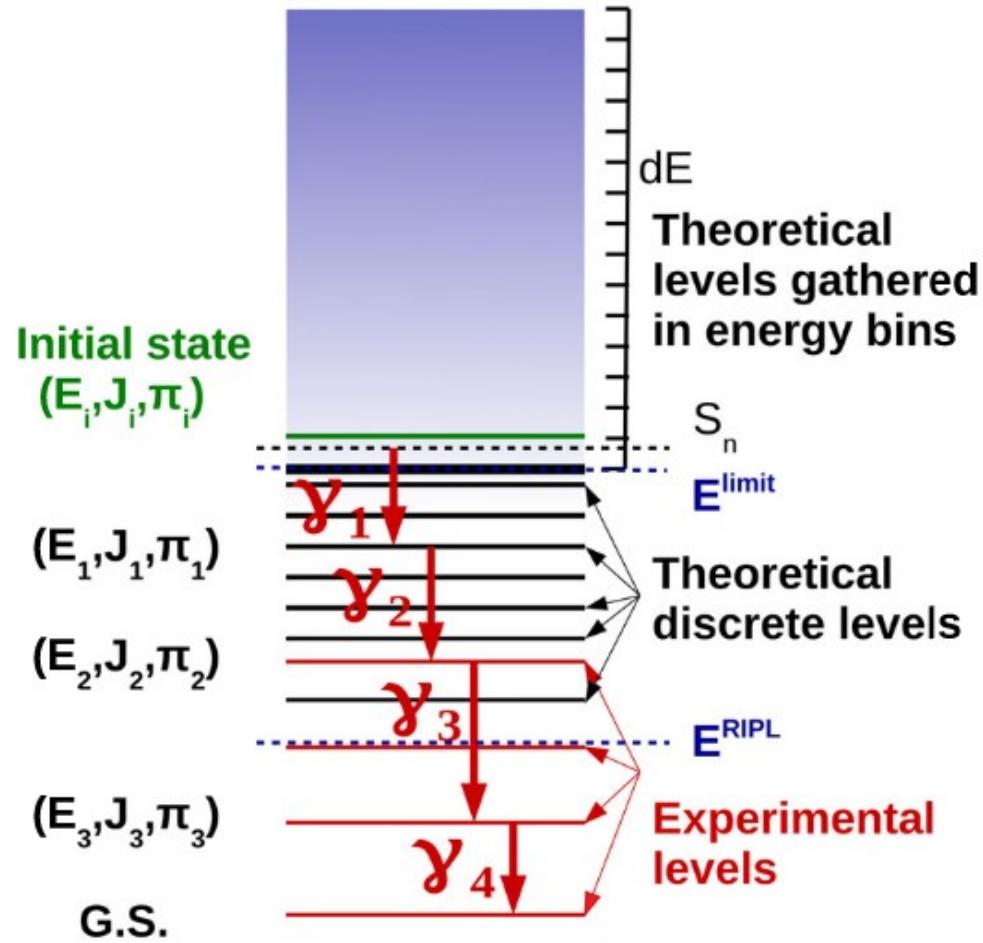
## However non-trivial nucleus de-excitation to simulate

- transition probability from  $S_n$  to GS ?  
 $\Rightarrow$  signal intensity
- multi-gamma/electron cascade ?  
 $\Rightarrow$  background evaluation in the ROI  
 $\Rightarrow$  dead-time (response time of  $\sim \text{ms}$  for cryo-detectors)

The high-energy gamma leaves the cm scale detector without energy deposition

# FIFRELIN SIMULATION [1]

Fission fragment de-excitation code developed at CEA-Cadarache [1]

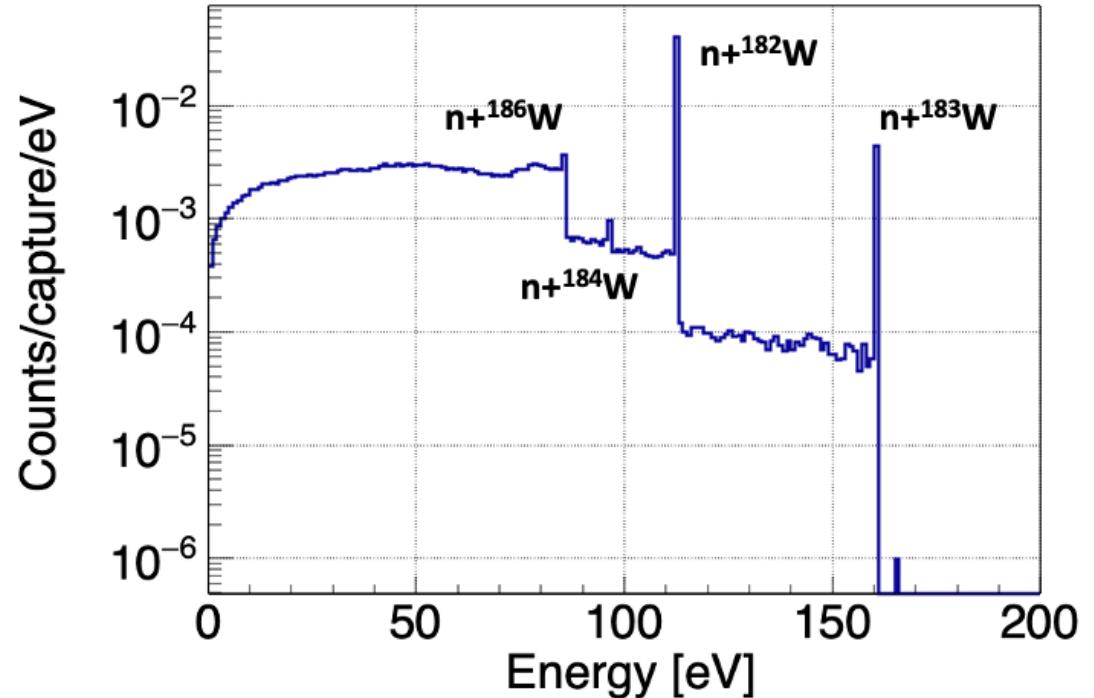


- All experimental (evaluated) data from EGAF, ENSDF, RIPL3 databases are taken into account  
⇒ for light nuclei, e.g. Al or Si the nuclear level scheme is known
- For heavy nuclei too many levels  
⇒ every levels cannot be experimentally determined  
⇒ need theoretical models
  - level density (CGCM, HFB)
  - radiative strength function (EGLO, QRPA)
  - electron conversion coefficient (BrICC)

**N. B.:** FIFRELIN executable will be released in 2024  
via the NEA website: <https://www.oecd-nea.org/>

# STUDIED CRYO-DETECTOR MATERIALS

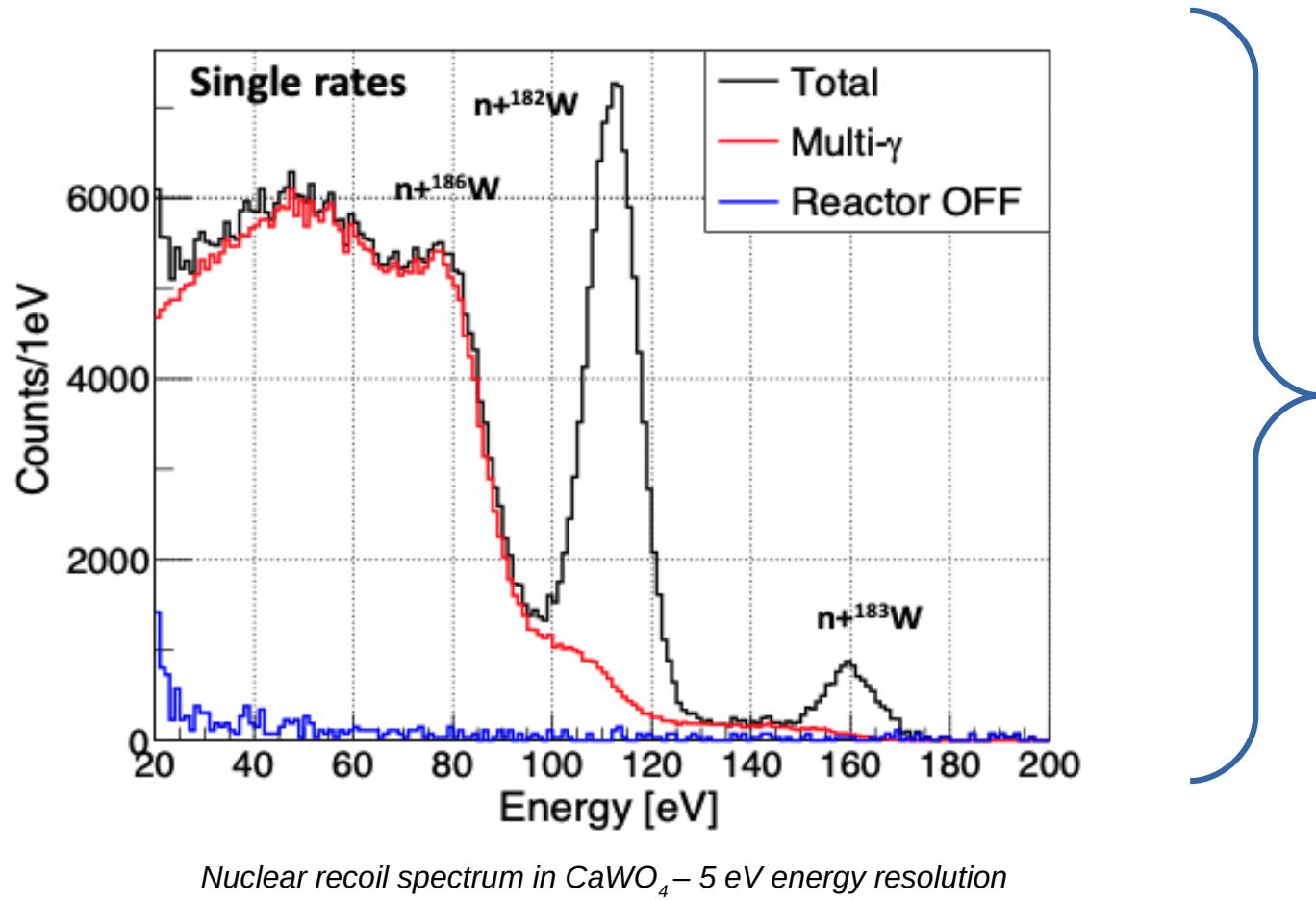
Detector	Target nucleus	$E_\gamma$ [keV]	FOM $= Y_{\text{abundance}} \times \sigma_{(n,y)} \times I_{\text{decay}}$	Nuclear recoil [eV]
<b>CaWO<sub>4</sub></b> <i>CRESST</i> <i>NUCLEUS</i>	<sup>186</sup> W	~5300 + 150	~4400	~80
	<sup>182</sup> W	6191	7506	112.5
	<sup>183</sup> W	7411	823	160.3



*Simulated recoil spectrum with an energy resolution of  $\sigma=0$  eV*

# PREDICTED NUCLEAR RECOIL SPECTRA – CaWO<sub>4</sub>

- Geant4 simulation based on TOUCANS [1] + FIFRELIN
- Mono-directionnal thermal neutron beam



- One prominent peak at 112 eV  
⇒ could easily pop-up
- Second small peak at 160 eV  
⇒ more difficult to get
- Third peak at ~80 eV  
⇒ buried in multi-γ background  
⇒ how to recover it ?



# HOW TO ACCURATELY OPTIMIZE A THERMAL NEUTRON SOURCE ?



**Neutron physics in Geant4 Neutron-HP package  
is now on-par with reference neutron transport codes such as MCNP, Tripoli-4, etc**

**Before 2021 :** T. Koi (original developer) then E. Mendoza et D. Cano-Ott  
E. Mendoza, D. Cano-Ott, T. Koi and C. Guerrero, IEEE Trans. Nucl. Science 61 (2014) 2357

**2022 :** L. Thulliez, C. Jouanne, and E. Dumonteil. Improvement of Geant4 Neutron-HP package: **From methodology to evaluated nuclear data library**. Nuclear Inst. and Methods Phys. Res., A 1027 (2022) 166187, doi: 10.1016/j.nima.2021.166187

**2023 :** M. Zmeskal, L. Thulliez, and E. Dumonteil. Improvement of Geant4 Neutron-HP package: **Doppler broadening of the neutron elastic scattering kernel**. Annals of Nuclear Energy, 192, 11 2023, doi: 10.1016/j.anucene.2023.109949

**2024 :** M. Zmeskal, L. Thulliez, P. Tamagno, E. Dumonteil, Improvement of Geant4 Neutron-HP package: **Unresolved Resonance Region description with Probability Tables**, already on arXiv:2404.16389 submit to Ann.of Nucl. Energy (2024),

**On-going :** Geant4 speed improvements

**Marek ZMESKAL PhD thesis at CTU-Praha**

# IMPROVEMENTS OF GEANT4 NEUTRON-HP PACKAGE – STATUS BEFORE 2021

Neutron-HP package used to transport low energy neutrons  $E_n < 20$  MeV

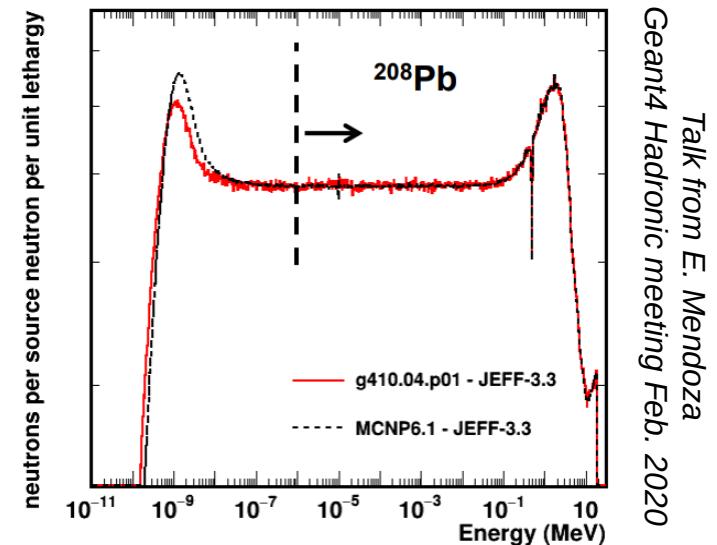
⇒ What are the different «models» used to describe the neutron/target interaction?



TSL not updated since ENDF-BVII.1

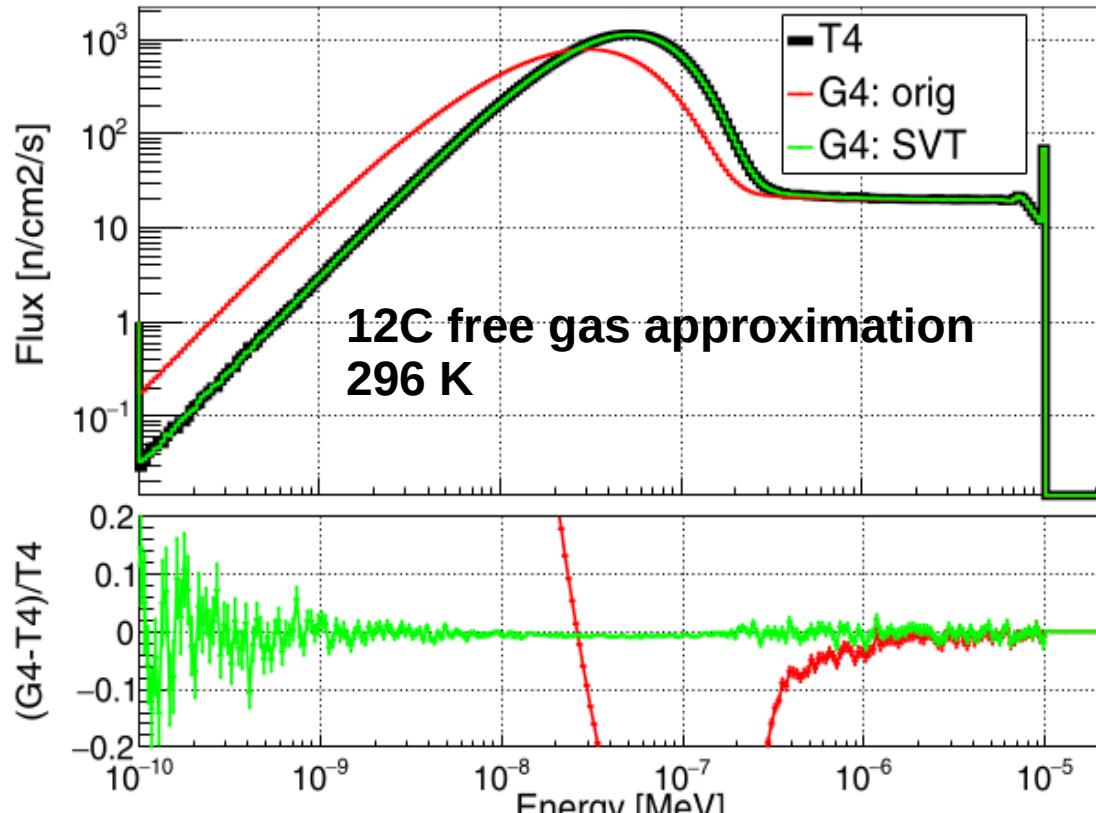
⇒ How to use updated and new materials from ENDF-BVIII.0 and JEFF-3.3?

- New TSL processing code ?
- Discrepancies between reference neutron codes (MCNP, Tripoli-4) of ~20%

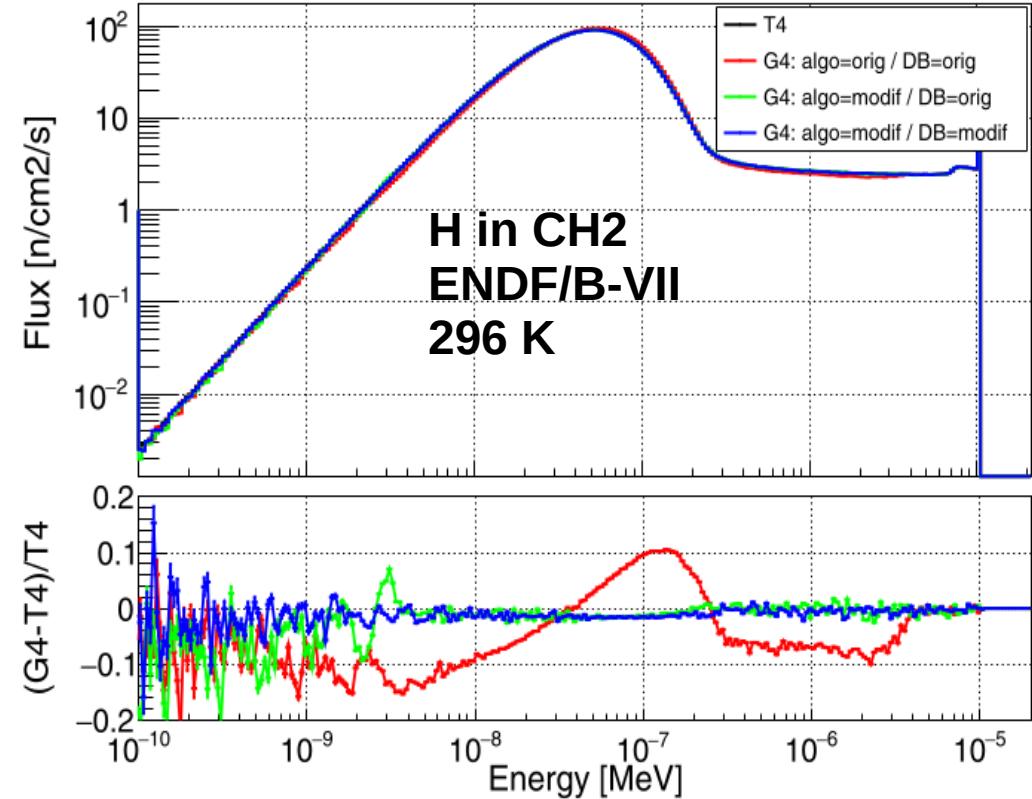


- Free gas approximation implemented in Geant4 has trouble to reproduce MCNP below 1 eV
- Problem in the algorithm?

# IMPROVEMENTS OF GEANT4 NEUTRON-HP PACKAGE – ALGORITHMS



*Correction of the Sampling of the Velocity of the Target (SVT) algorithm*

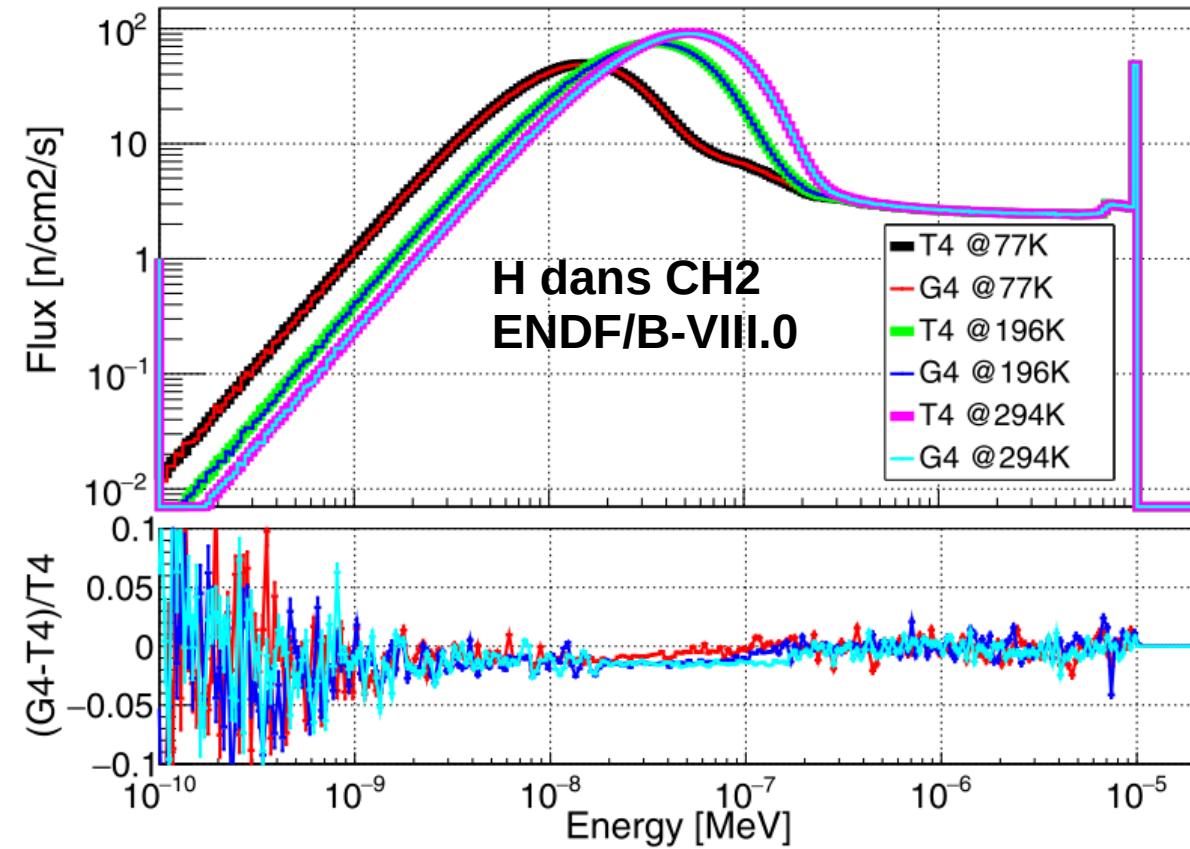


*Fix the sampling of the final state of the elastic scattering*

Geant4 agrees with reference neutron transport codes such as MCNP or Tripoli4 to better than 1 %

# IMPROVEMENTS OF GEANT4 NEUTRON-HP PACKAGE – NEW TSL DATABASES

Up-to-date databases available in GEANT4 and validated with TRIPOLI4 to better than 1 % – since 2022



## ENDF/BVII-1:

TSL-ENDFB71\_HighPrecision

TSL-ENDFB71\_LowPrecision (*only database before 2022*)

## ENDF/BVIII-0:

TSL-ENDFB80\_HighPrecision

TSL-ENDFB80\_LowPrecision

## JEFF-3.3:

TSL\_JEFF33\_HighPrecision

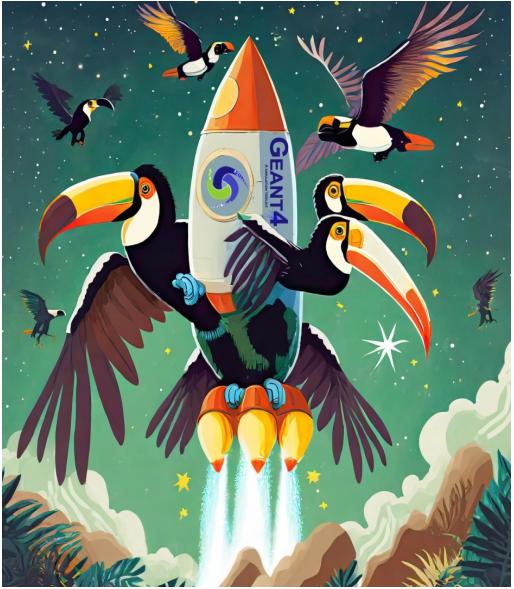
TSL\_JEFF33\_LowPrecision

**Mix JEFF-3.3 and ENDF/BVIII-0, take all TSL data from JEFF-3.3 and the ENDF/BVIII-0 materials not in JEFF-3.3:**

TSL\_mix\_JEFF33\_ENDFB80\_HighPrecision

TSL\_mix\_JEFF33\_ENDFB80\_LowPrecision

# TOUCANS : a versatile Geant4 based Monte Carlo neutron (*not only*) transport code [1]



All the possibilities offered by Geant4 are leveraged

- Simulation of a setup *via* an input file
  - ⇒ based on key / value
  - ⇒ Easy coupling to other codes
    - multi-objective optimisation code FUNZ
  - ⇒ Import CAD files
  - ⇒ New variance reduction technics: AMS
- Validated with the reference neutron transport codes Tripoli4 and MCNP
- Experimentally qualified (2019 [2]/2022 [3])

\$ STRING	Moderator/Type	BOX	\$
\$ STRING	Moderator/Material	GRAPHITE	\$
\$ STRING	Moderator/MotherVolume	experimentalRoom	\$
\$ DOUBLELIST	Moderator/Dimensions	64      250      219	\$
\$ DOUBLELIST	Moderator/Position	147.25      -107.2      69.2	\$

Soon will be open-source

[1] L. Thulliez, B. Mom and E. Dumonteil, Nucl. Inst. and Methods in Phys. Res., A 1051 (2023) 168190

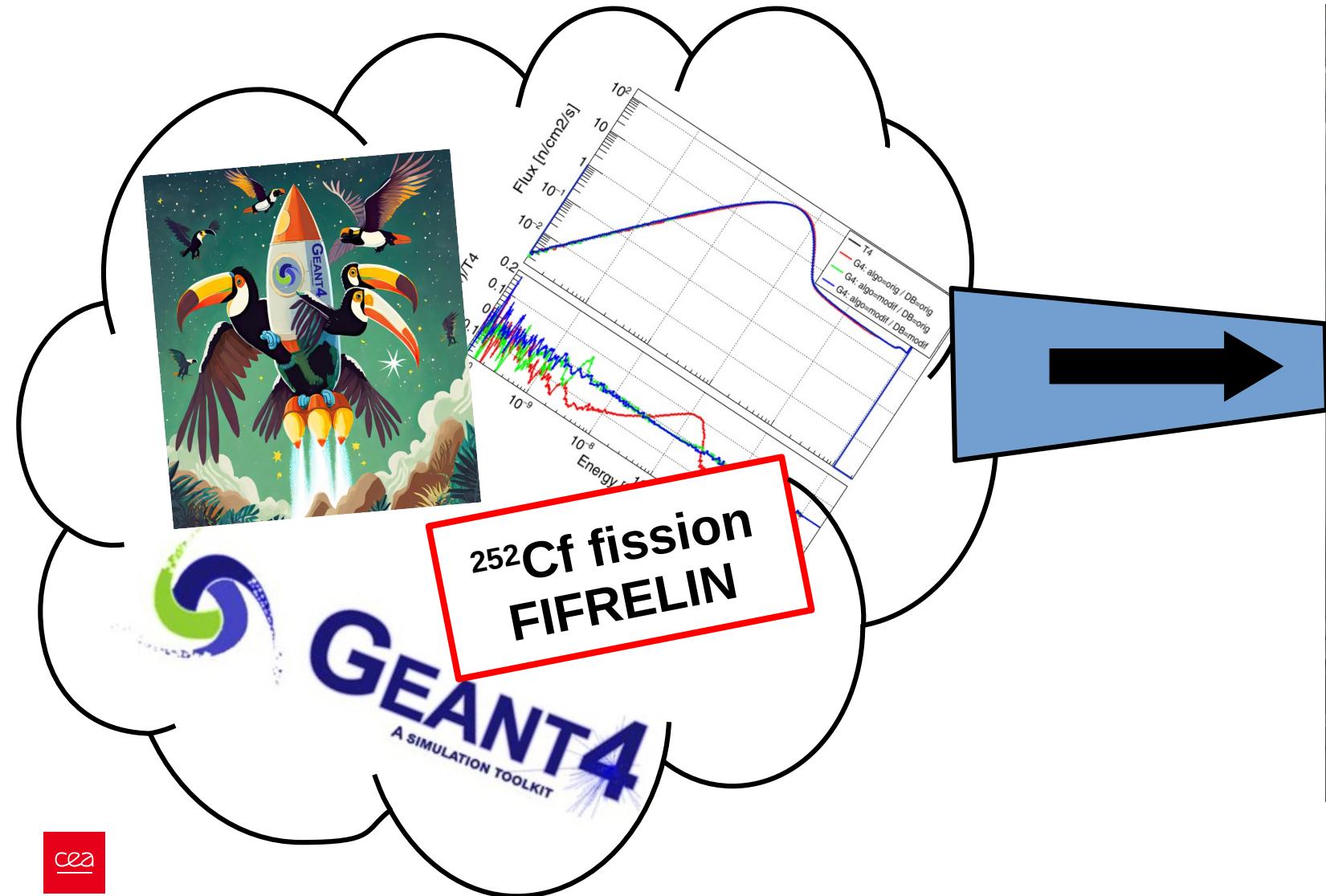
[2] L. Thulliez et al., EPJ Web of Conferences 239, 17011 (2020)

[3] J. Schwindling et al., Journal Of Neutron Research vol. 24, no. 3-4, pp. 289-298, 2022



# CRAB PORTABLE THERMAL NEUTRON SOURCE

Thermal neutrons produced with a 3.7 MBq  $^{252}\text{Cf}$  in a polyethylene and graphite moderator



# FIRST MEASUREMENT CRAB / NUCLEUS COLLABORATIONS



**NUCLEUS CaWO<sub>4</sub>**  
cryo-detector  
 $E_{th} = 50$  eV  
 $\sigma(E) = 6$  eV



Detector in a copper box spring  
decoupled from cryostat vibration

cea



More copper to thermalize the  
detector below 100 mK  
**TES transition ~10 mK**



**Thermal neutrons** produced with a 3.7 MBq  
 $^{252}\text{Cf}$  in a polyethylene and graphite moderator  
⇒  $0.25 n_{th}/\text{s}$  on the cryo-detector

# FIRST MEASUREMENT – RESULTS

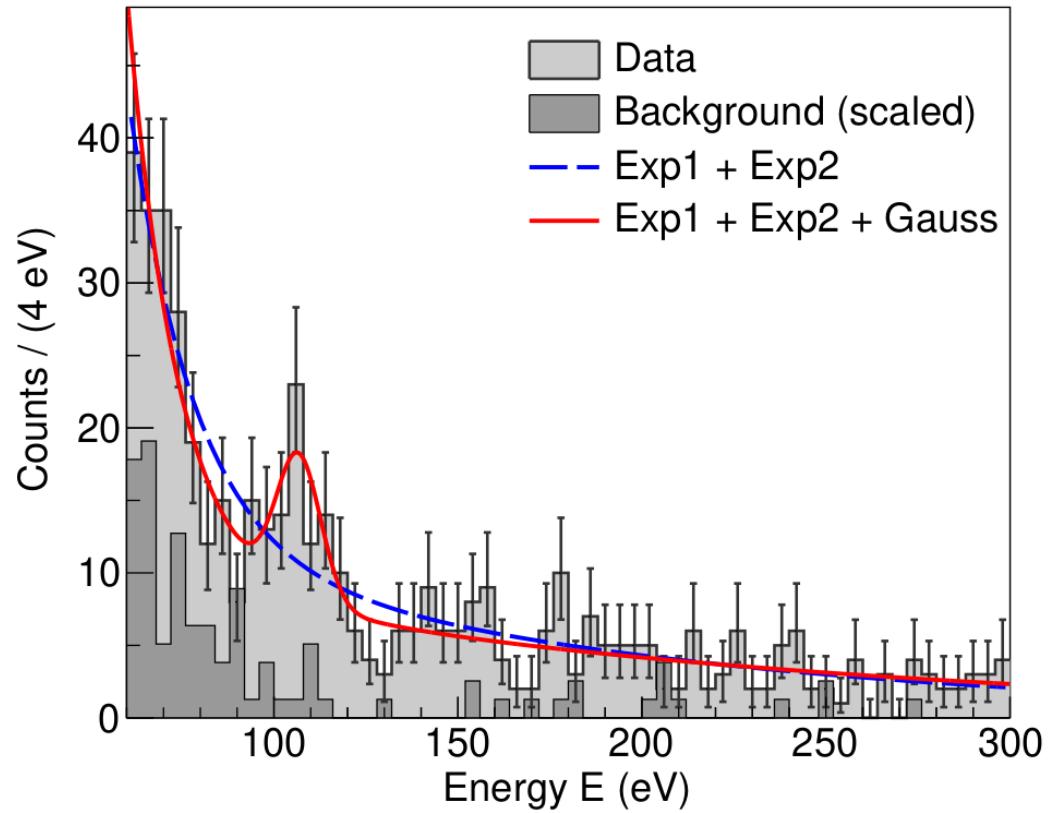
→ Background data lifetime = 18.9 h  
→ Source data lifetime = 40.2 h

Blind search peak

## Test the presence of a peak

Background = 2 exponentials

Signal = gaussian

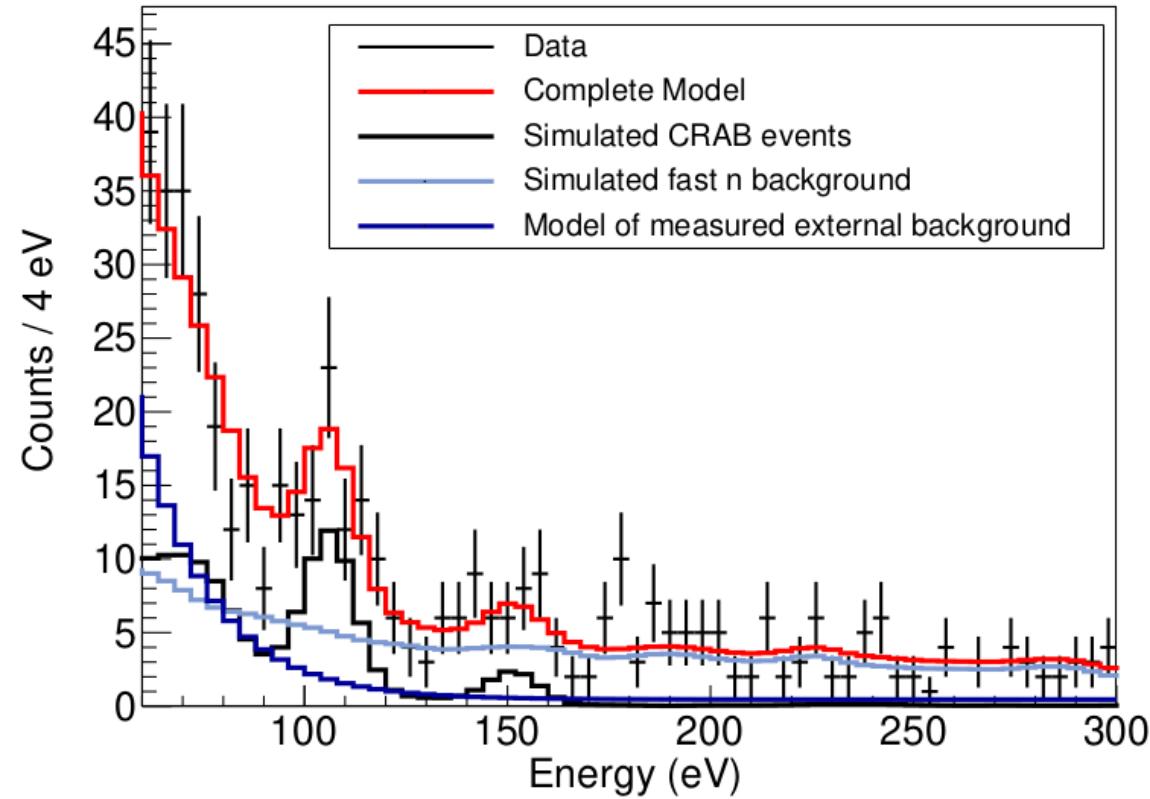


**Presence of a peak**  
⇒  $3.1\sigma$  significance (2-sided)

## Test the presence of nuclear recoils from neutron capture

Background = exponential fit to bkgd data

Signal = GEANT4 + FIFRELIN



**Presence of nuclear recoils from neutron capture**  
⇒  $6\sigma$  significance (2-sided)  
⇒  $\chi^2/\text{NDF} = 58.09/59$



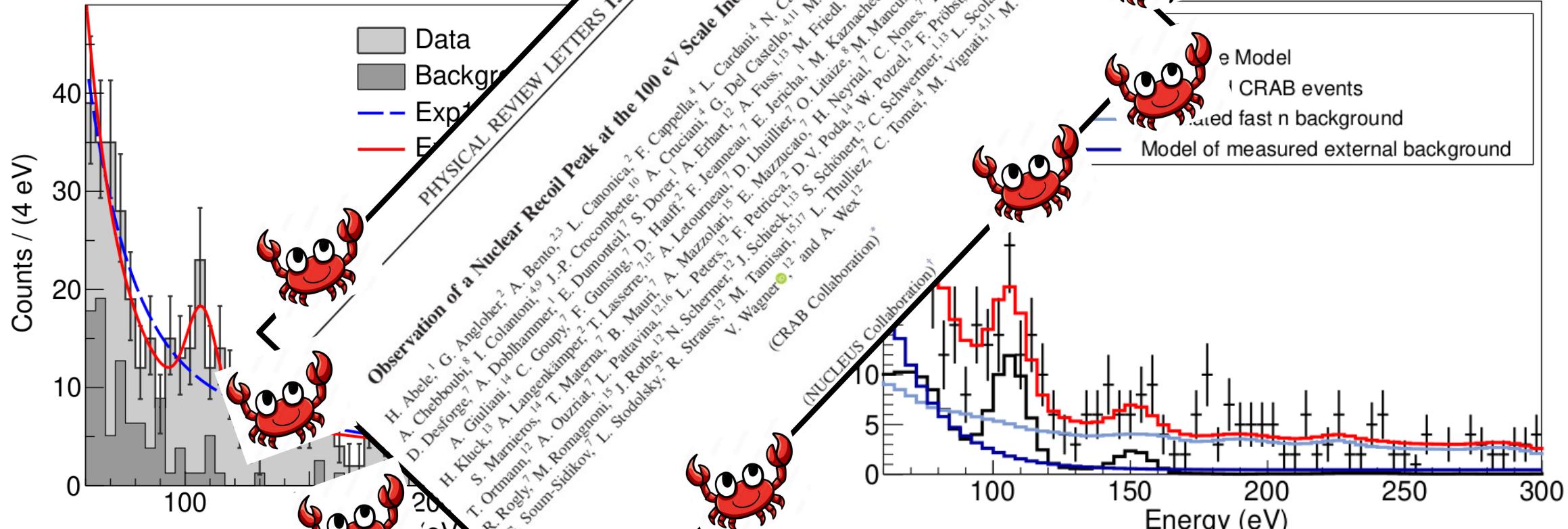
# FIRST MEASUREMENT – RESULTS

Blind search peak

**Test the presence of a peak**

Background = 2 exponentials

Signal = gaussian



**Presence of a peak**  
⇒  $3.1\sigma$  significance (2-sided)

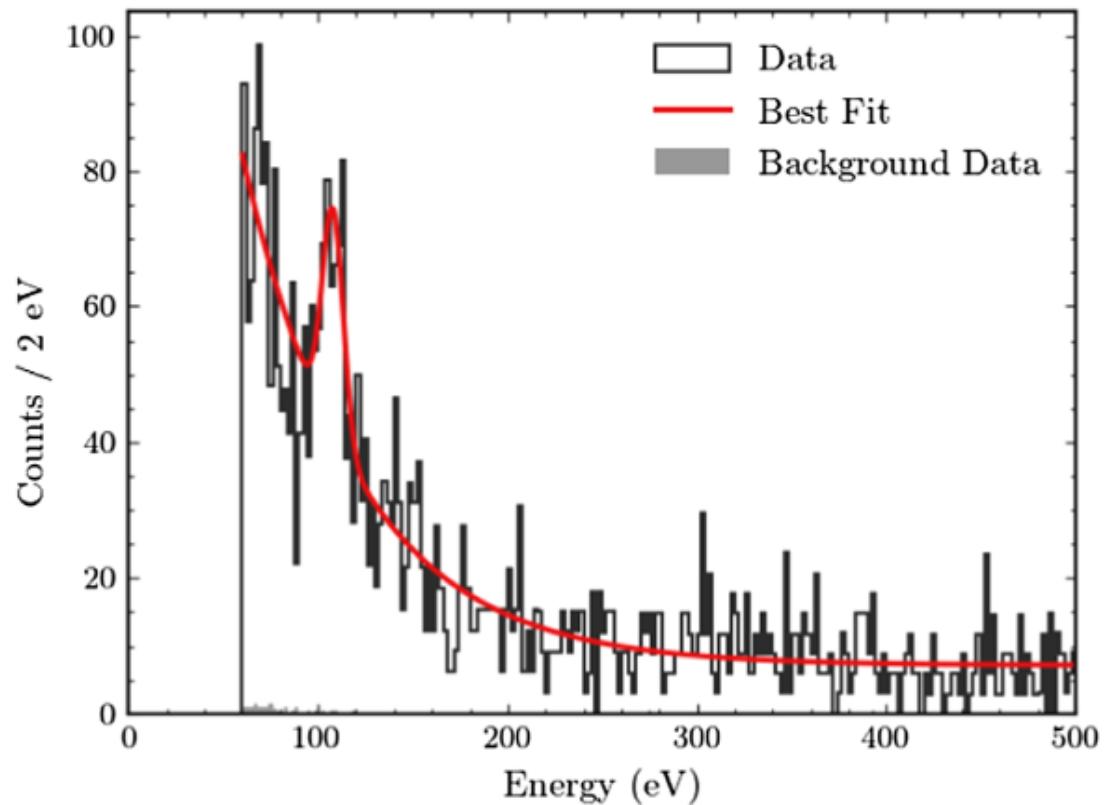
Presence of nuclear recoils from neutron capture  
⇒  $6\sigma$  significance (2-sided)  
⇒  $\chi^2/\text{NDF} = 58.09/59$

# FIRST MEASUREMENT CONFIRMED BY OTHERS !

**CRESST** = dark matter with  $\text{CaWO}_4$  cryo-detector

→ confirmation of our first CRAB signal with 3 detectors

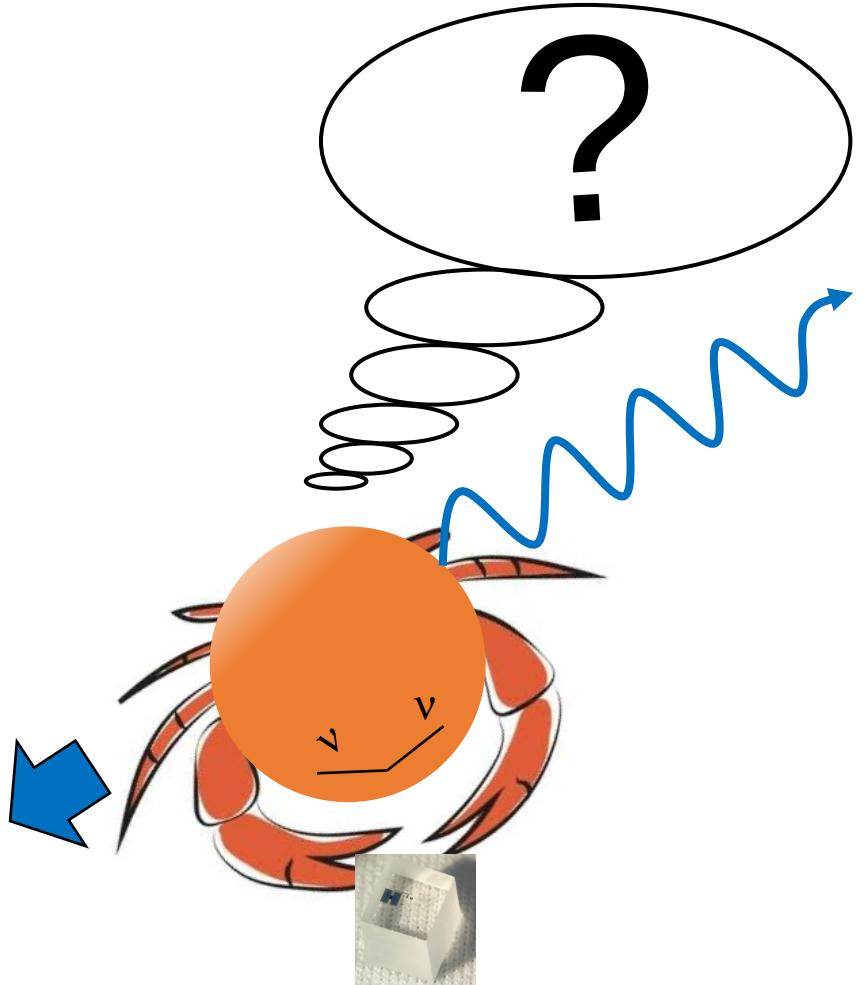
G. Angloher et al. (CRESST collaboration) Phys. Rev. D 108, 022005 (2023)



**CRAB has already a big impact in the dark matter and neutrino communities !**



# WHAT IS NEXT ?





# STUDIED OTHER CRYO-DETECTOR MATERIALS

Detector	Target nucleus	$E_\gamma$ [keV]	FOM $= Y_{\text{abundance}} \times \sigma_{(n,y)} \times I_{\text{decay}}$	Nuclear recoil [eV]
<b>Al<sub>2</sub>O<sub>3</sub></b> <i>MINER NUCLEUS</i>	<sup>27</sup> Al	7693 + 30.6	79	1135.7
	<sup>27</sup> Al	7724	616	1144.8
<b>Si</b> <i>SuperCDMS DAMIC SENSEI Skipper-CCD CONNIE</i>	<sup>28</sup> Si	7200 + 1273	116	990.4
	<sup>28</sup> Si	8474	36	1330.1
<b>Ge</b> <i>EDELWEISS RICOCHET</i>	<sup>74</sup> Ge	6253 + 253	220	280.6
	<sup>74</sup> Ge	6506	54	303.2
	<sup>73</sup> Ge	8733 + 868+ 596	117	561.8
	<sup>70</sup> Ge	6708 + 708	287	344.3
	<sup>70</sup> Ge	6117 + 1299	261	296
	<sup>70</sup> Ge	7416	122	416.2
<b>CaWO<sub>4</sub></b> <i>CRESST NUCLEUS</i>	<sup>186</sup> W	~5300 + ~200	~4400	~80
	<sup>183</sup> W	7411	823	160.3
	<sup>182</sup> W	6191	7506	112.5

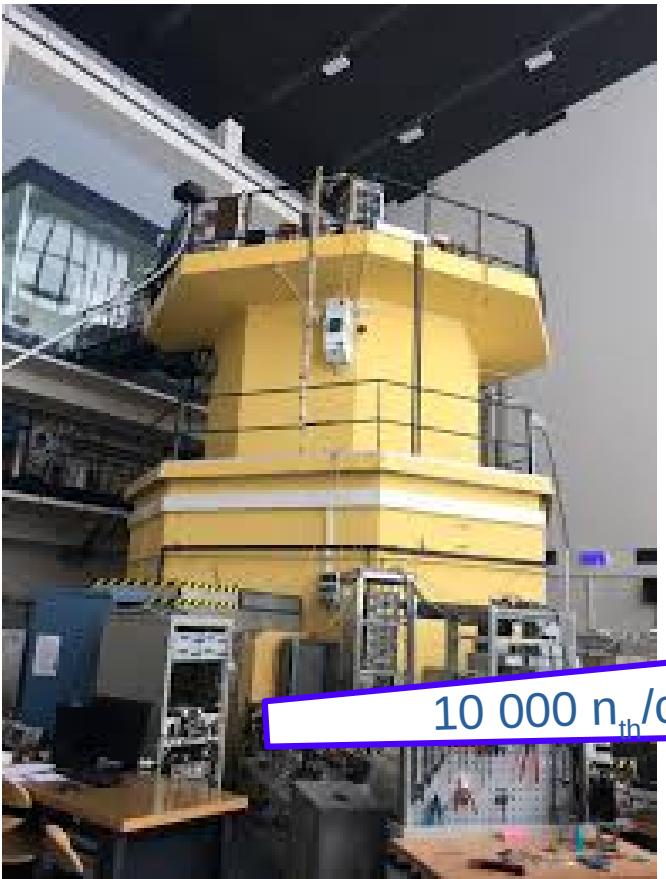
FIFRADINA datasets available : <https://doi.org/10.5281/zenodo.7936552>

Fifrelin4Geant4 classes is open-source : <https://doi.org/10.5281/zenodo.7933381>  
<https://gitlab.com/lthullie/fifrelin4geant4>



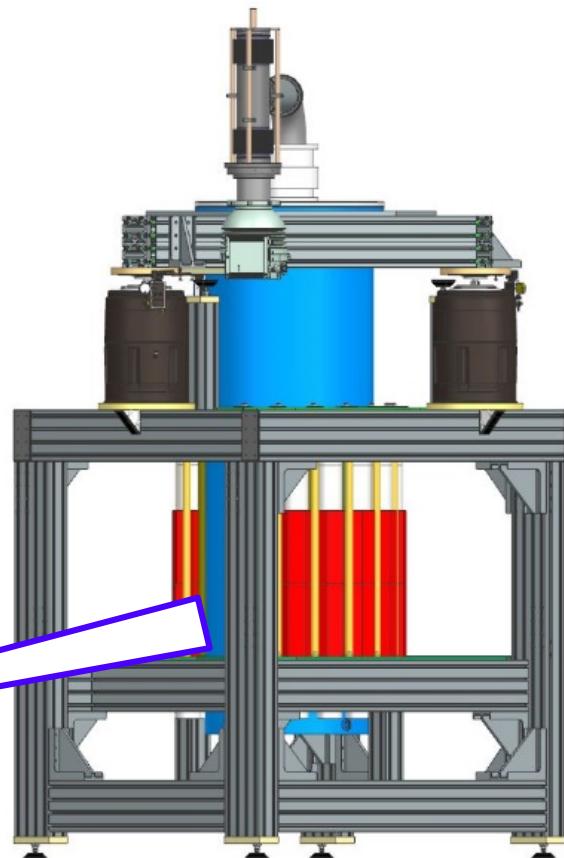
# CRAB Phase 2 – HIGH PRECISION MEASUREMENTS (in 2024)

**TRIGA Mark-II nuclear reactor (250 kW)**  
TU-Wien – Atominstitut



Thermal neutron beam line

**Wet cryostat**  
Oxford kelvinox 400



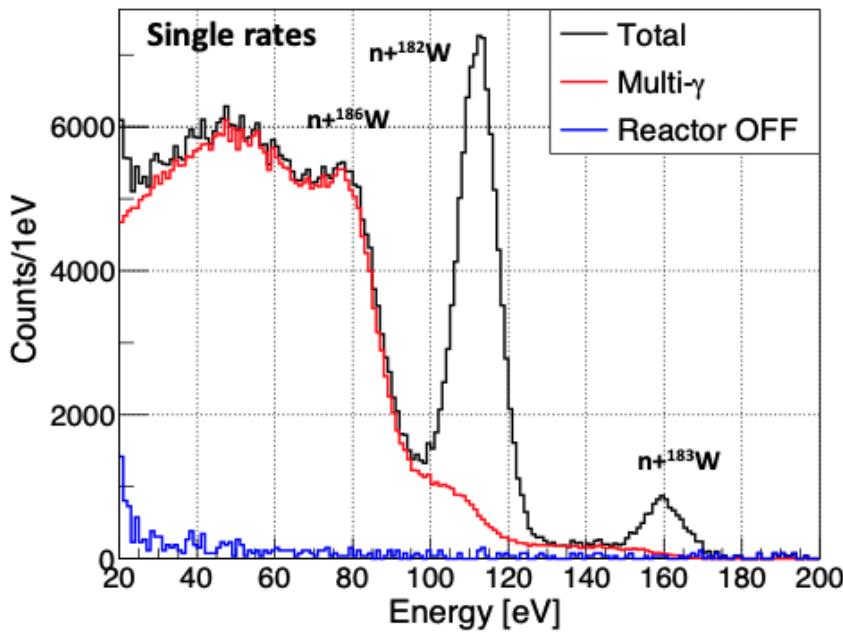
Monochromator  
Graphite crystal

**Array of 28 hexagonal BaF<sub>2</sub>  
gamma detectors (2" x 6")**



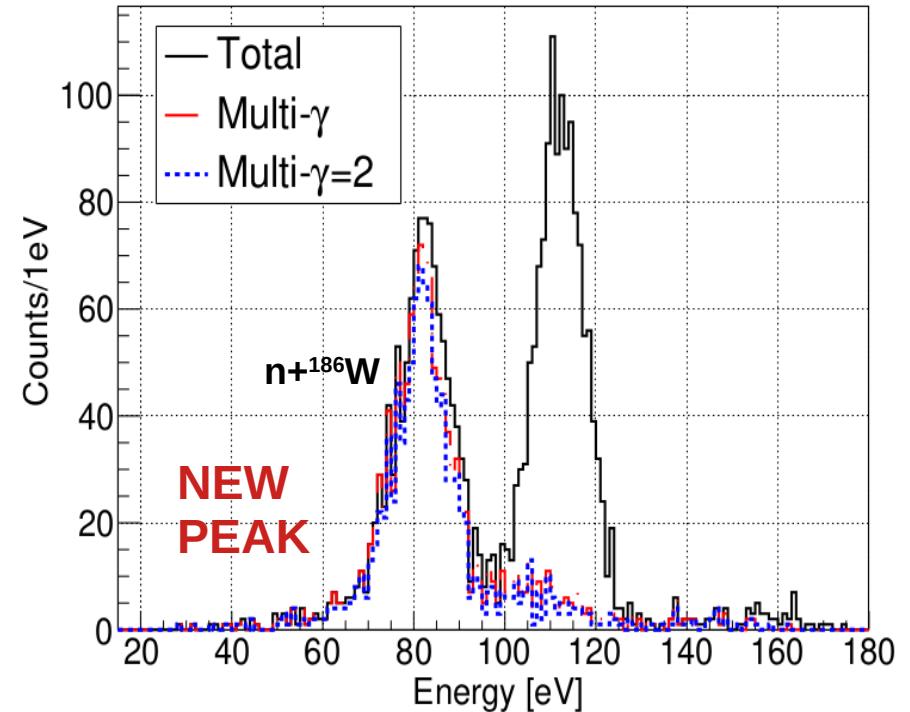
# STUDY OF THE DETECTOR LINEARITY

Single spectrum with high statistics



~6 full days of data taking  
 ⇒ sub- % statistical precision

Gamma tagging is a powerful tool



Recoil spectrum after gamma tagging with  
 $E_{\gamma} = 5.5 \pm 0.2 \text{ MeV}$

$\gamma$ -tagging is a powerful tool to get a 3<sup>rd</sup> peak at 80 eV for CaWO<sub>4</sub>  
 ⇒ study of the detector linearity !

# CRAB SENSITIVE TO CRYSTAL DEFECT CREATIONS

How to quantify the energy stored in the crystal lattice ?

*Gabrielle Soum-Sidikov PhD thesis  
J.-P. Crocombette (CEA/DES)*

## Machine learning inter-atomic potential

Training database from DFT calculations (VASP)



A.M. Goryaeva, J.-B. Maillet, M.-C. Marinica  
*Comp. Mater. Sci.* 166:200 (2019)

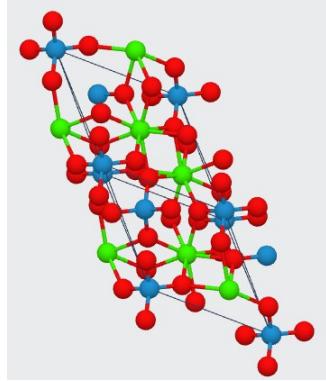


## Molecular dynamics simulations

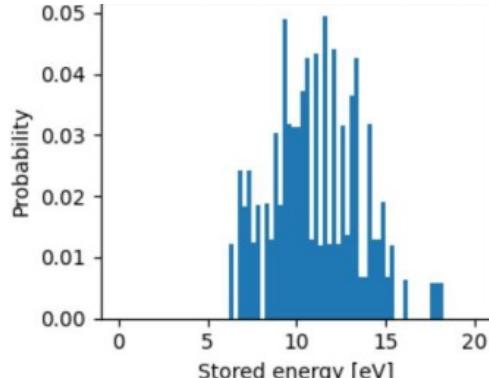
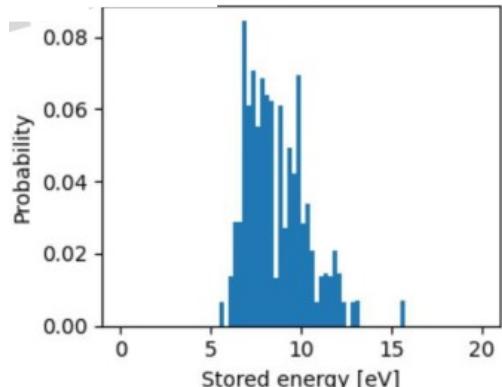
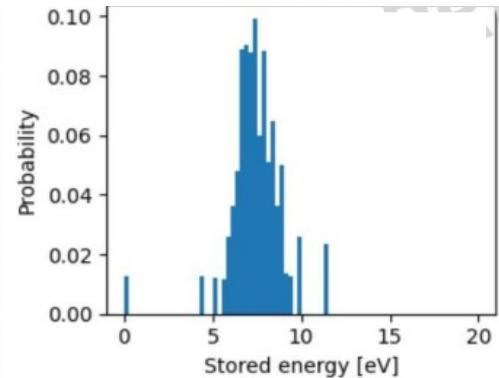
80 Å size box with 50000 atoms

Simulation time ~8 ps

Zero point energy taken into account



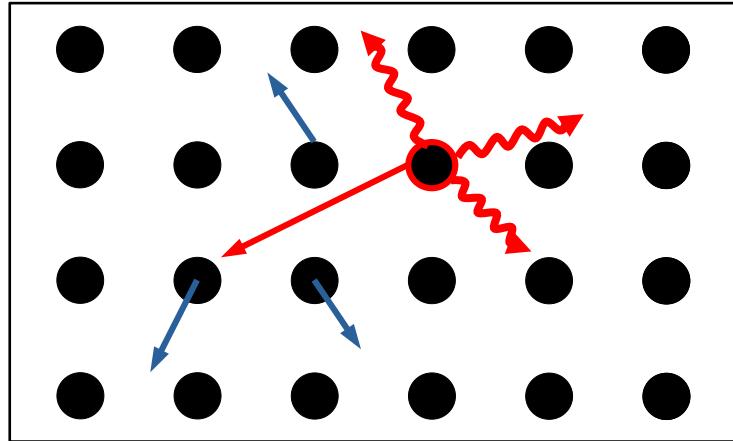
$E_{\text{recoil}}$ [eV]	81	112	160
$E_{\text{stored}}$ [eV]	7.4	8.9	11.0
If linear $E_{\text{stored}}$ [eV]	7.4	10.23	14.6



# TIMING EFFECT – EXTREME HYPOTHESES

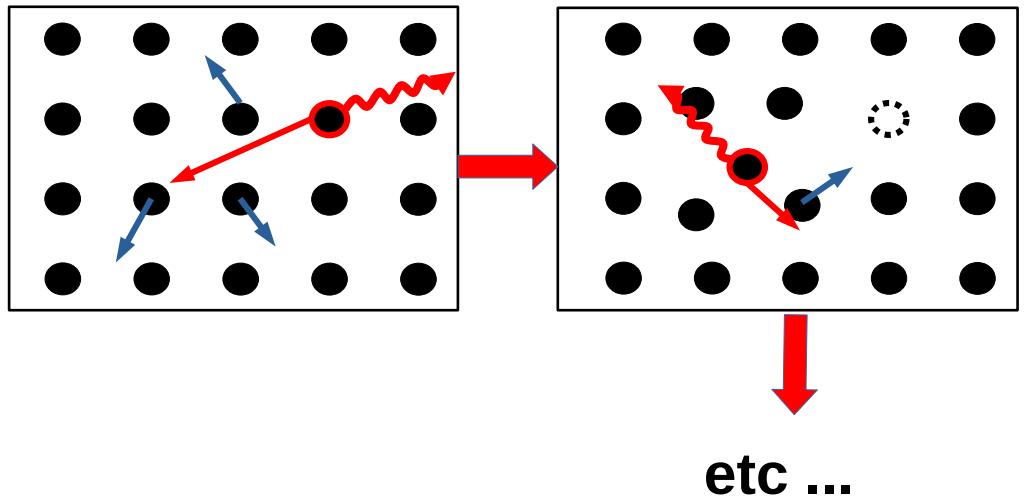
## Fast hypothesis

$$\tau_{recoil} \gg \tau_{cascade} \quad E_{recoil} = \left( \sum_i \vec{p}_i \right)^2 / 2M$$



## Slow hypothesis

$$\tau_{recoil} \ll \tau_{cascade} \quad E_{recoil} = \sum_i E_{recoil,i} = \sum_i p_i^2 / 2M$$

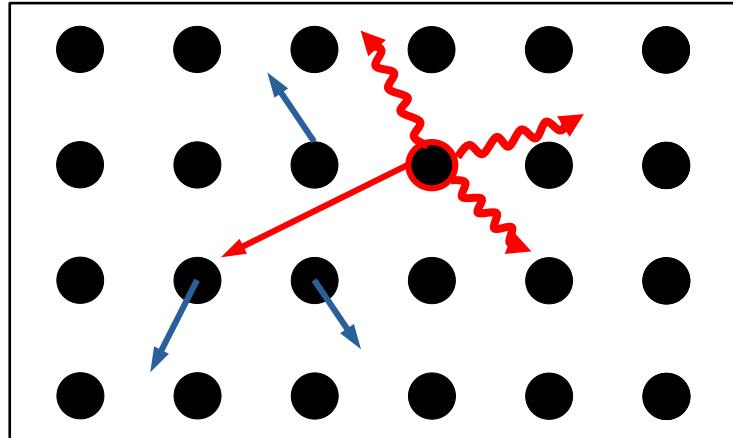




# TIMING EFFECT – EXTREME HYPOTHESES

## Fast hypothesis

$$\tau_{recoil} \gg \tau_{cascade} \quad E_{recoil} = \left( \sum_i \vec{p}_i \right)^2 / 2M$$

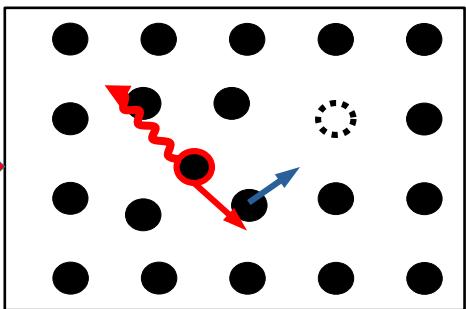
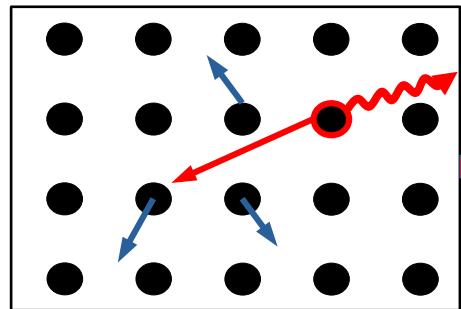


## Slow hypothesis

$$\tau_{recoil} \ll \tau_{cascade} \quad E_{recoil} = \sum_i E_{recoil,i} = \sum_i p_i^2 / 2M$$

Reality in between

Coupling FIFRELIN  
and IRADINA [1]

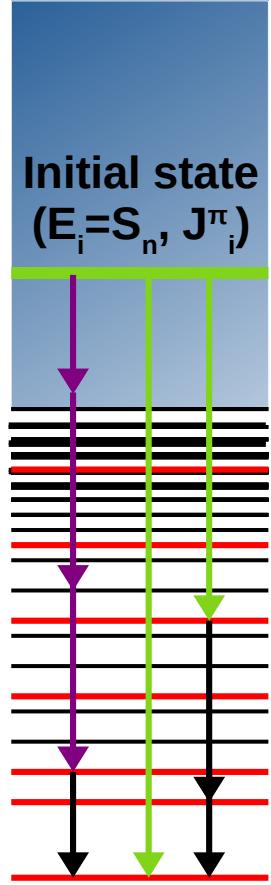


etc ...

[1] G. Soum-Sidikov et al., Study of collision and  $\gamma$ -cascade times following neutron-capture processes in cryogenic detectors, Phys. Rev. D 108, 072009 (2023)

# FIFRELIN + IRADINA = FIFRADINA [1]

**FIFRELIN** : Fission fragment de-excitation code



## Level scheme

- Continuum
- Sampled levels
- RIPL-3 levels

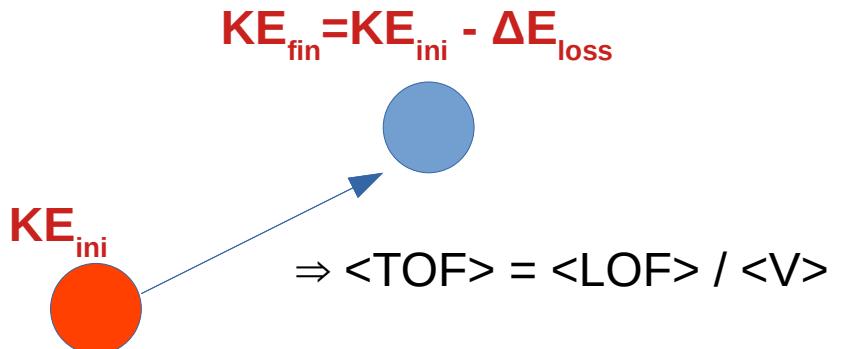
## Transition probability

- EGAF (primary) transition  
*Timing* : Weisskopf estimate
- RSF transition  
*Timing* : radiative partial width
- RIPL-3 transition  
*Timing* :  
RIPL-3 if known  
else Weisskopf estimate

**Gabrielle SOUM PhD thesis at CEA**

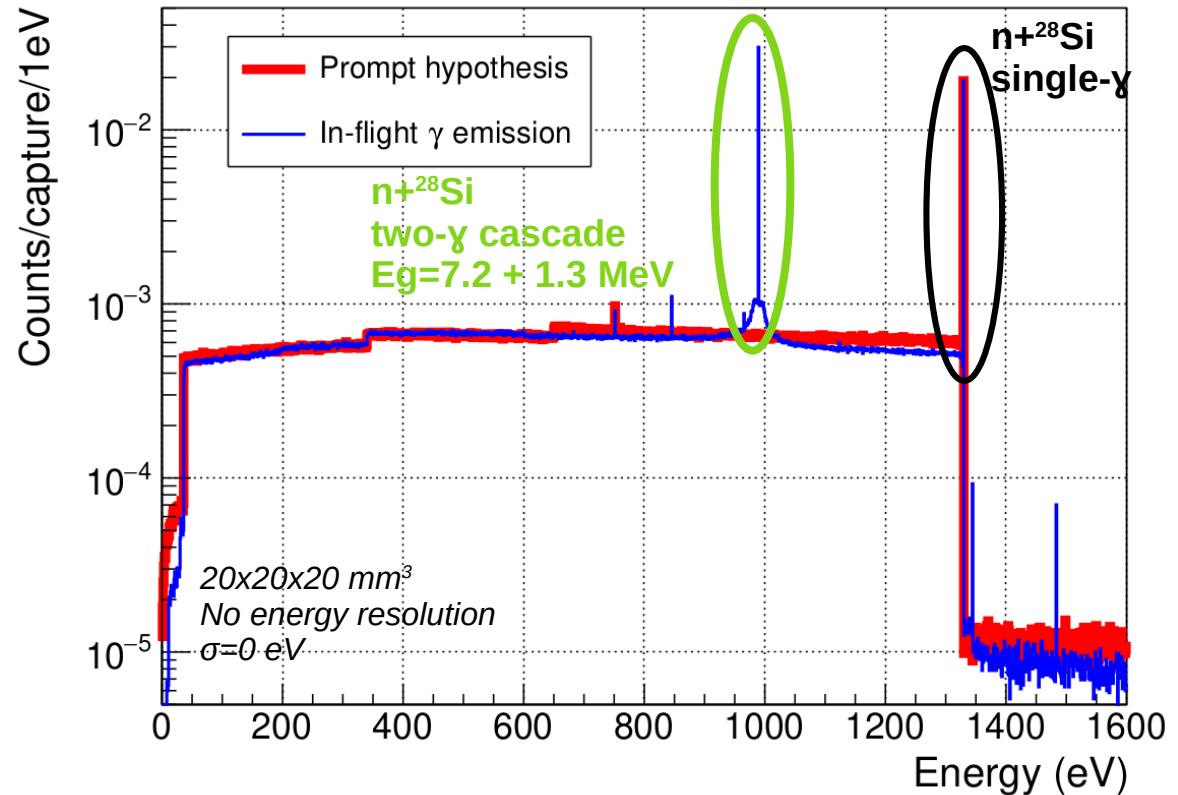
**IRADINA** (similar to SRIM):  
Binary Collision Approximation code  
Ingredients: → amorphous structure  
→ atoms described as a free gas

Sample a target (and collision parameters)



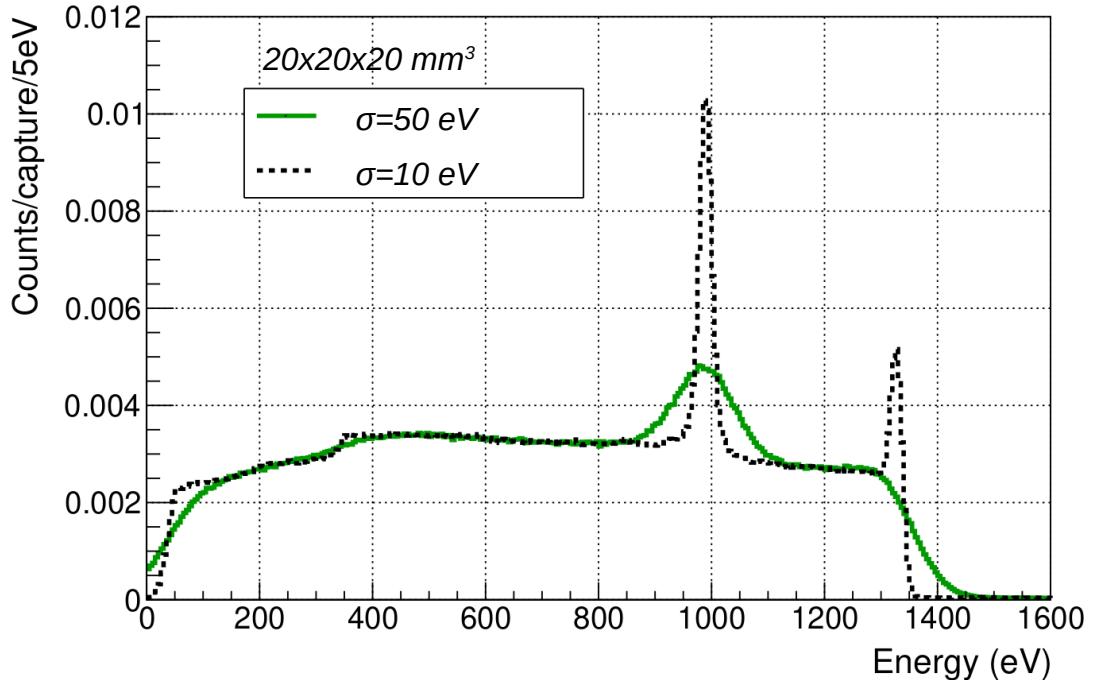
[1] G. Soum-Sidikov et al., Study of collision and  $\gamma$ -cascade times following neutron-capture processes in cryogenic detectors, Phys. Rev. D 108, 072009 (2023)

# TIMING EFFECTS – SILICON



Most of the half-lives are in the databases  
(collective effects taken into account)

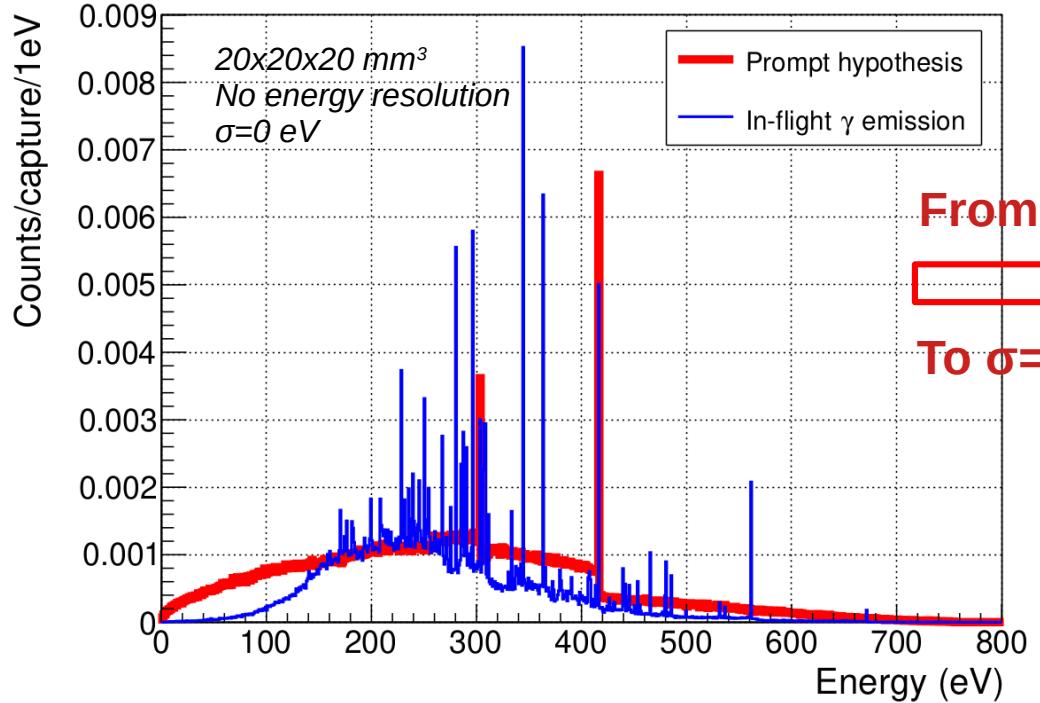
In-flight gamma emission  $\Rightarrow$  probe nucleus de-excitation time  
 $\Rightarrow$  sensitive to directionality effects



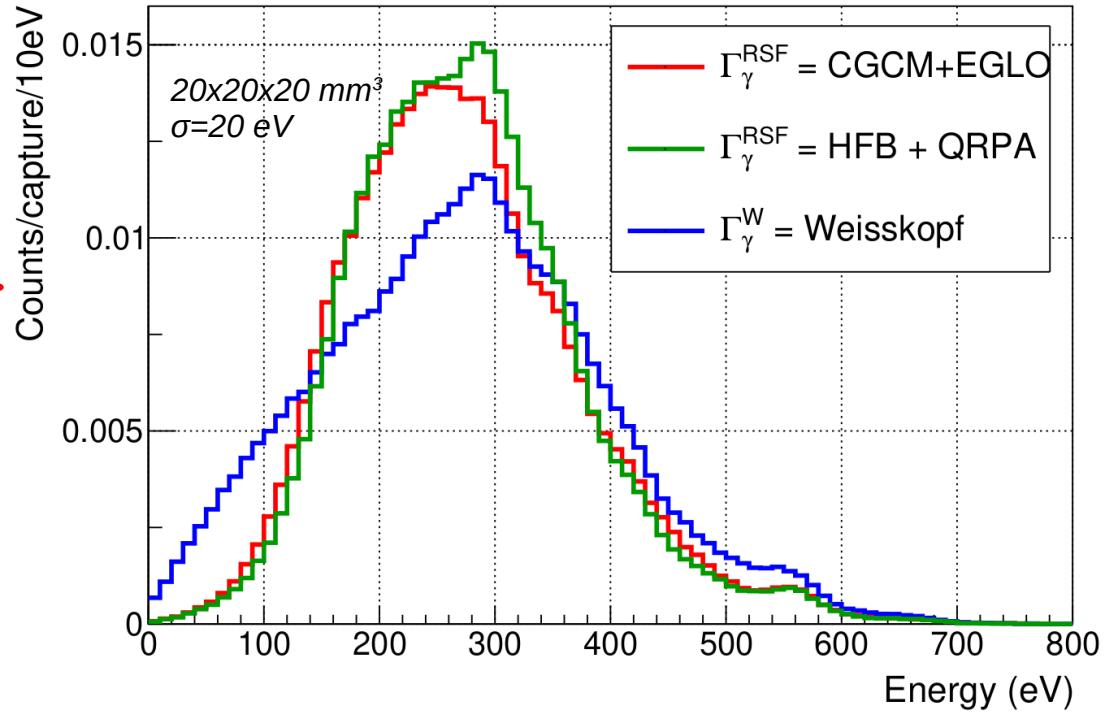
Two- $\gamma$  cascade robust against poorer energy resolution

[1] G. Soum-Sidikov et al., Study of collision and  $\gamma$ -cascade times following neutron-capture processes in cryogenic detectors, Phys. Rev. D 108, 072009 (2023)

## TIMING EFFECTS – GERMANIUM



In-flight  $\gamma$  emission  $\Rightarrow$  more calibration peaks



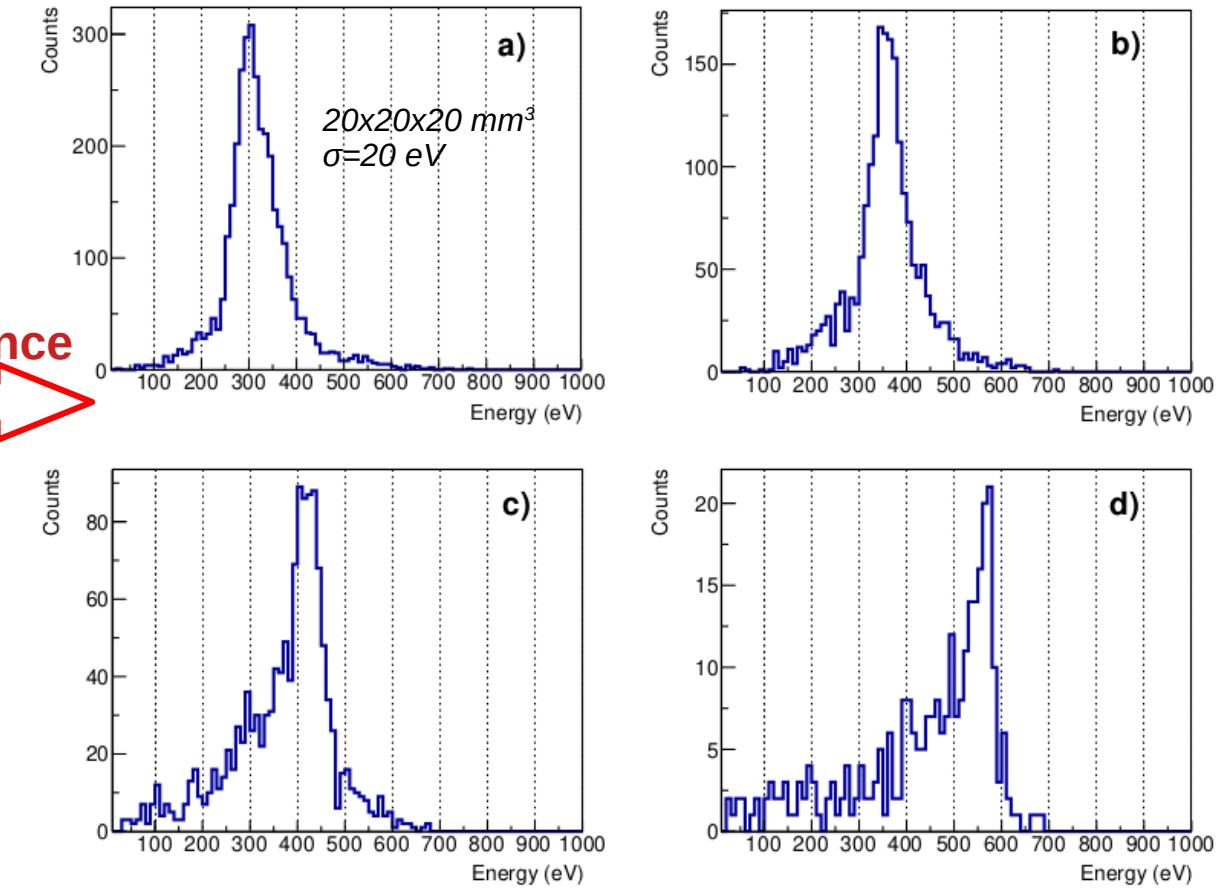
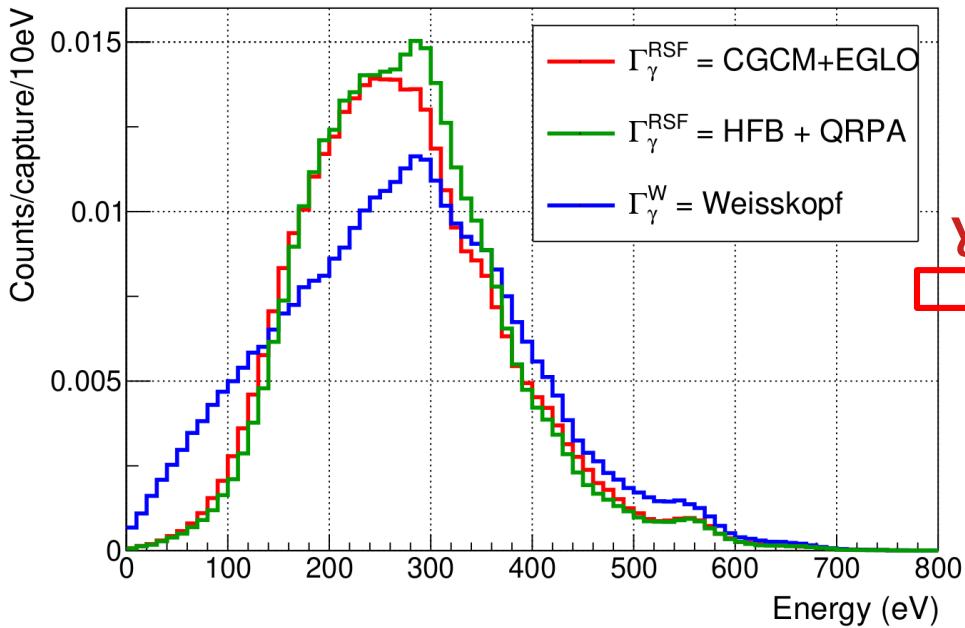
Recoil energy spectrum sensitive to nuclear models !  
 $\Rightarrow$  could help set constraints on models

- **With timing effects, more calibration peaks !**
- **Timing modelling sensitive to the underlying nuclear physics**  
 $\Rightarrow$  test of nuclear models
- **Resolution is a critical parameter**

[1] G. Soum-Sidikov et al., Study of collision and  $\gamma$ -cascade times following neutron-capture processes in cryogenic detectors, Phys. Rev. D 108, 072009 (2023)



# TIMING EFFECTS – GERMANIUM



Resolution is a critical parameter  
 BUT gamma coincidence allows to overcome this limitation !

[1] G. Soum-Sidikov et al., Study of collision and  $\gamma$ -cascade times following neutron-capture processes in cryogenic detectors, Phys. Rev. D 108, 072009 (2023) 29



## CONCLUSIONS

- **CRAB method** promising for a **sub-kev calibration** of the majority of cryo-detector materials in DM/CEvNS communities currently used (**CaWO<sub>4</sub>, Ge, Si, Al<sub>2</sub>O<sub>3</sub>**)
- Successfull first measurement with a NUCLEUS CaWO<sub>4</sub> and a portable neutron source
  - ⇒ presence of a peak at ~112 eV with 3.1σ significance (confirmation by the CRESST collaboration)
  - ⇒ presence of nuclear recoils with 6σ significance : agreement between data and GEANT4-FIFRELIN
- CRAB with **gamma tagging** is a powerful tool to **increase S/B** and **access lower energy** recoils, study the linearity of the bolometer response and tag the direction of the recoil (directionality)



## CODES / DATA TO TAKE AWAY

- Liquid scintillator experiments (STEREO collaboration) :  
**Gadolinium** thermal neutron capture **FIFRELIN** dataset : <https://doi.org/10.5281/zenodo.6861341>
- Cryo-detectros experiments (CRAB collaboration):  
**W / Ge / Al / Si** thermal neutron capture **FIFRADINA** datasets : <https://doi.org/10.5281/zenodo.7936552>
- **Fifrelin4Geant4** classes is open-source (STEREO/CRAB): <https://doi.org/10.5281/zenodo.7933381>  
<https://gitlab.com/lthullie/fifrelin4geant4>
- All the improvements of the Neutron-HP package are in the latest Geant4 release !  
⇒ stay tune for the incoming speed improvements
- FIFRELIN executable will be released in 2024 via the NEA website: <https://www.oecd-nea.org/>

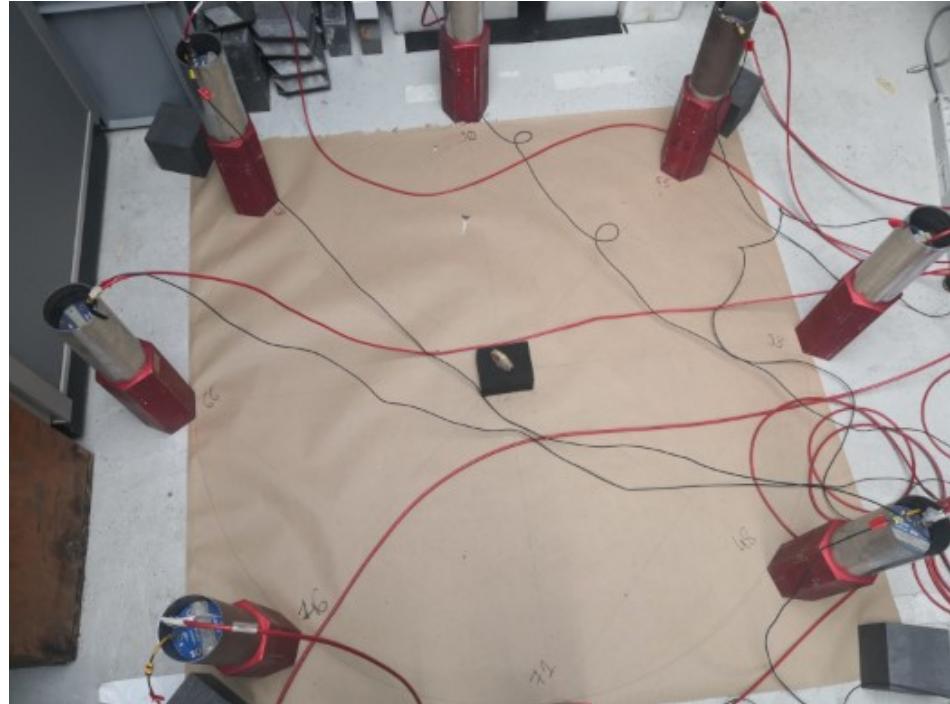
**Do not hesitate to contact us if you want to study specific isotopes !**

# PERSPECTIVES

- CRAB High Precision measurements at the TRIGA-Mark II reactor at TU-Wien in 2024 with CaWO<sub>4</sub>
- Promissing case of Ge detectors. Impact of crystal defects to be calculated soon.
- On the long term, it will be a facility available to the community to characterise their detectors



Wet cryostat @TUM



Gamma tagging development  
@CEA-Saclay



Neutron beam line construction  
and characterisation @TU-Wien



irfu

THANK YOU

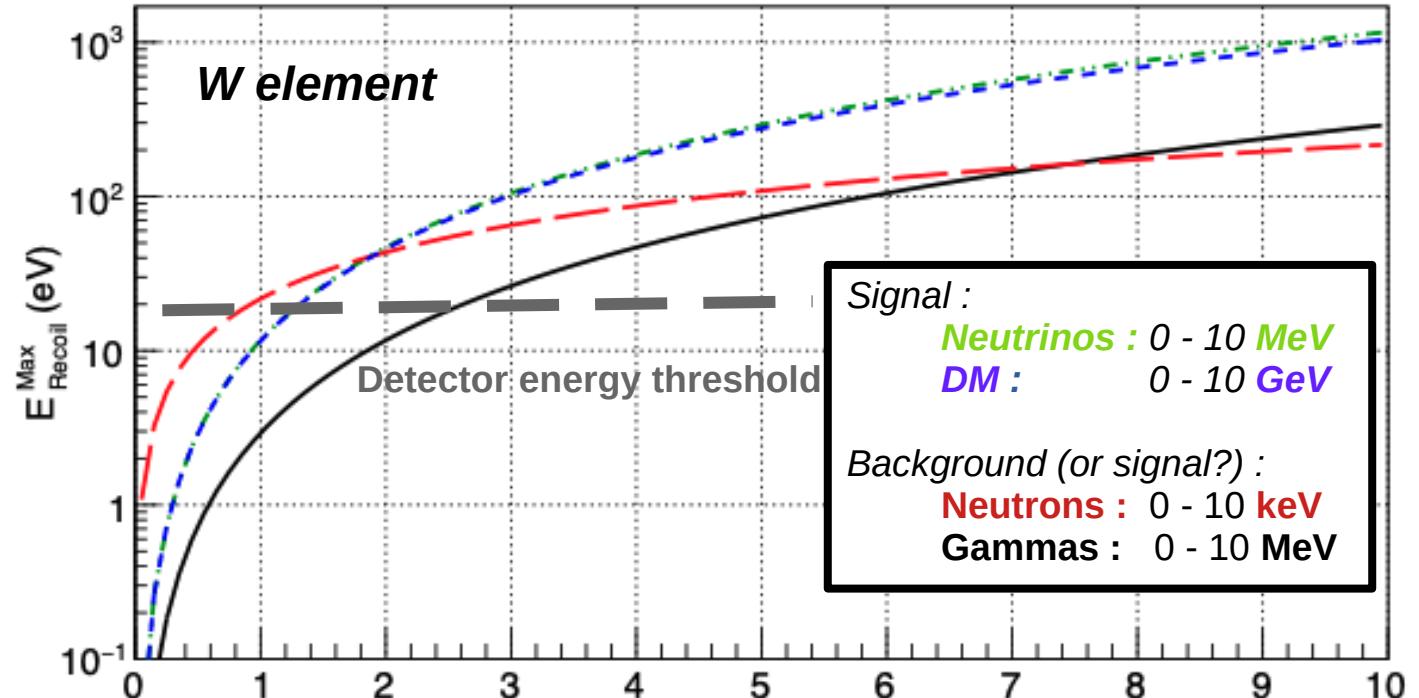


*The CRAB collaboration*

# NEED SUB-keV CALIBRATION METHODS

State-of-the-art calibration techniques :

- mainly electron recoils for *in-situ* calibration with LED [1], XRF source BUT surface calibration
- alphas BUT surface calibration
- epithermal/fast neutrons produced at accelerator are limited by TOF and angular precisions



What about thermal neutrons ?

- gammas from  $(n,\gamma)$  reaction

First indirect measurement by Jones and Kramer [2]