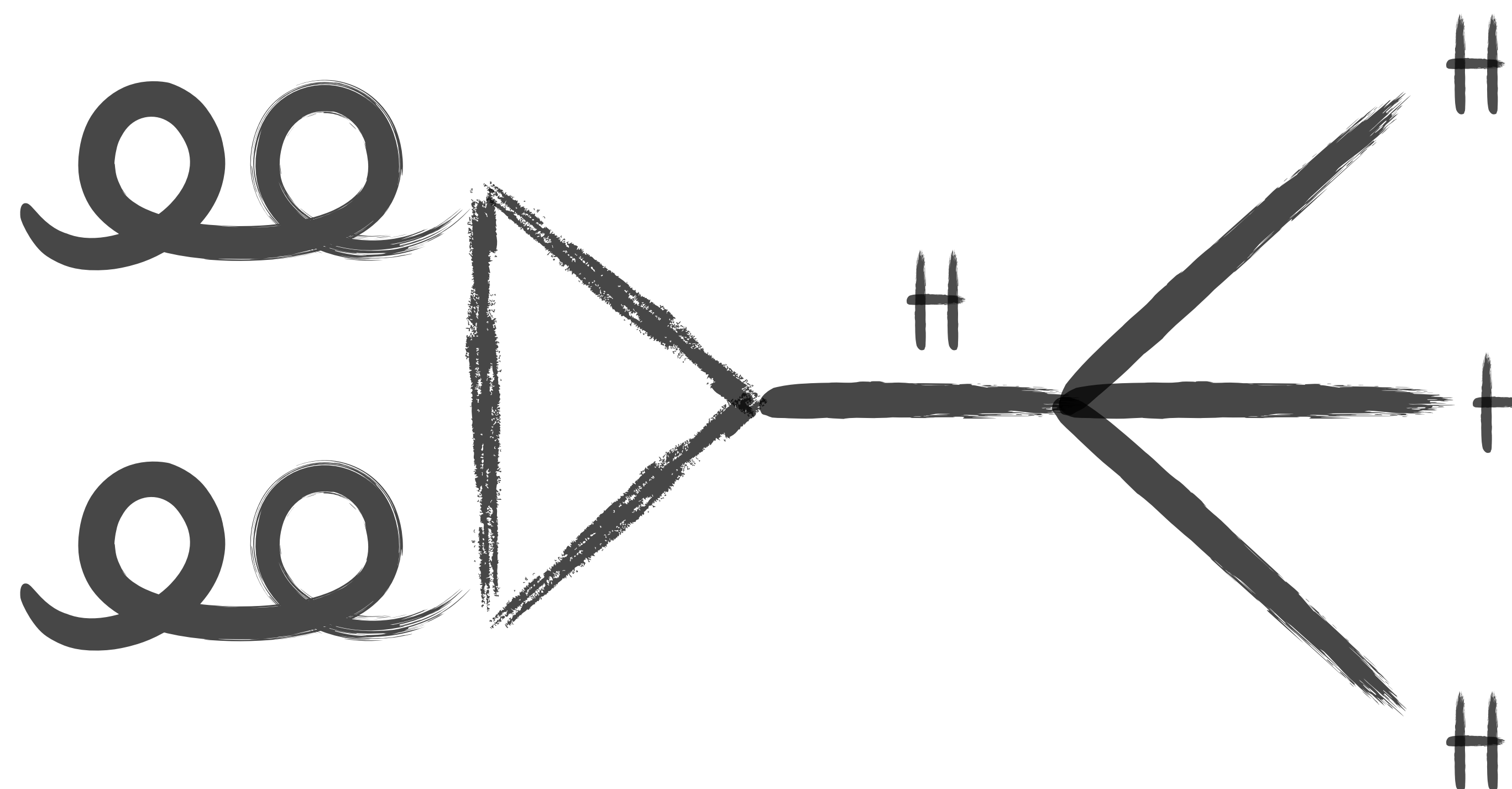


Overview of HHH physics at the LHC and summary of HHH workshop in Dubrovnik

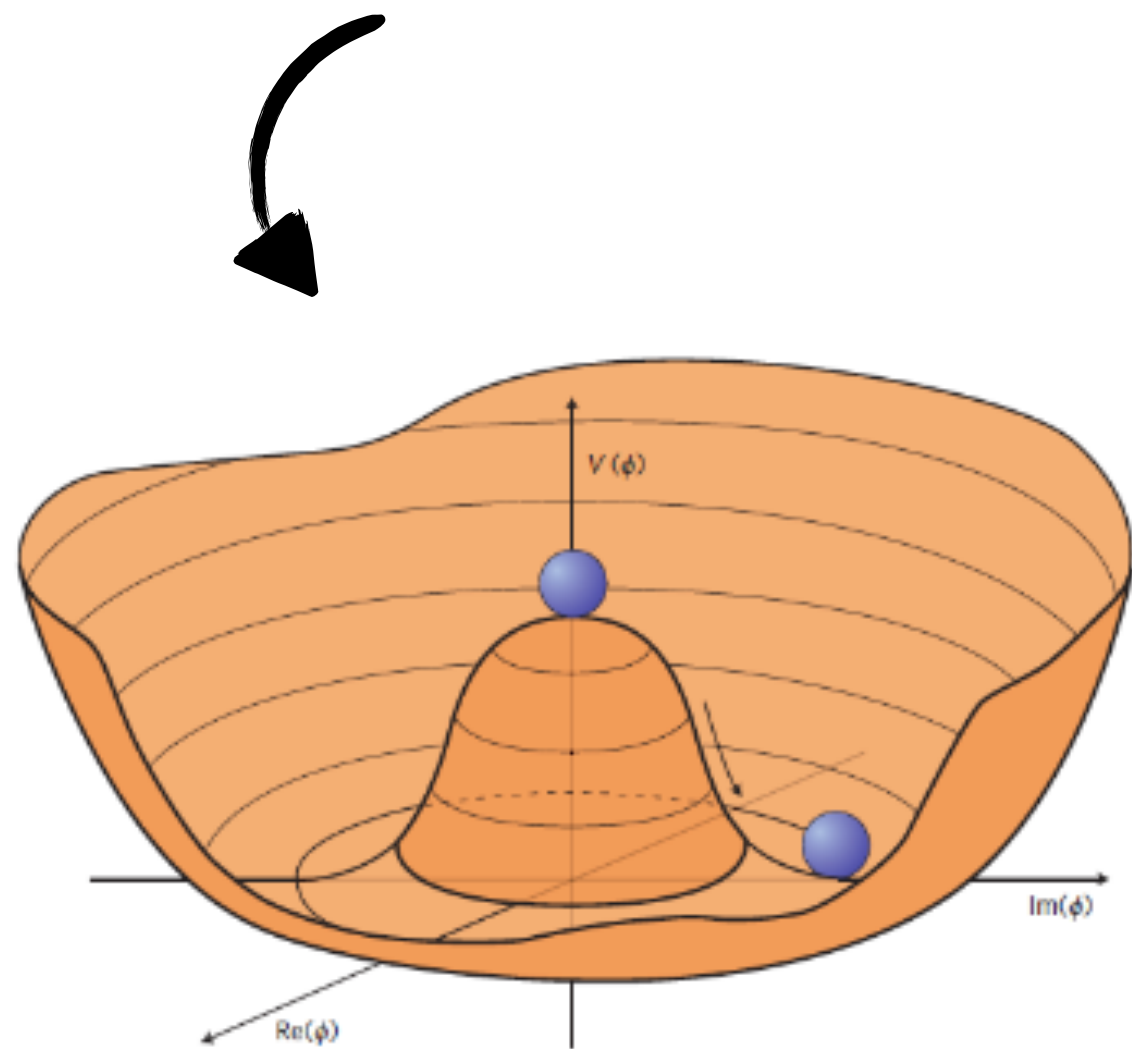


15th of November 2023

Marko Stamenkovic

Measuring the Higgs potential: motivation

$$V(H) = \frac{1}{2}m_H^2 H^2 + \lambda_3 v H^3 + \frac{1}{4}\lambda_4 H^4$$



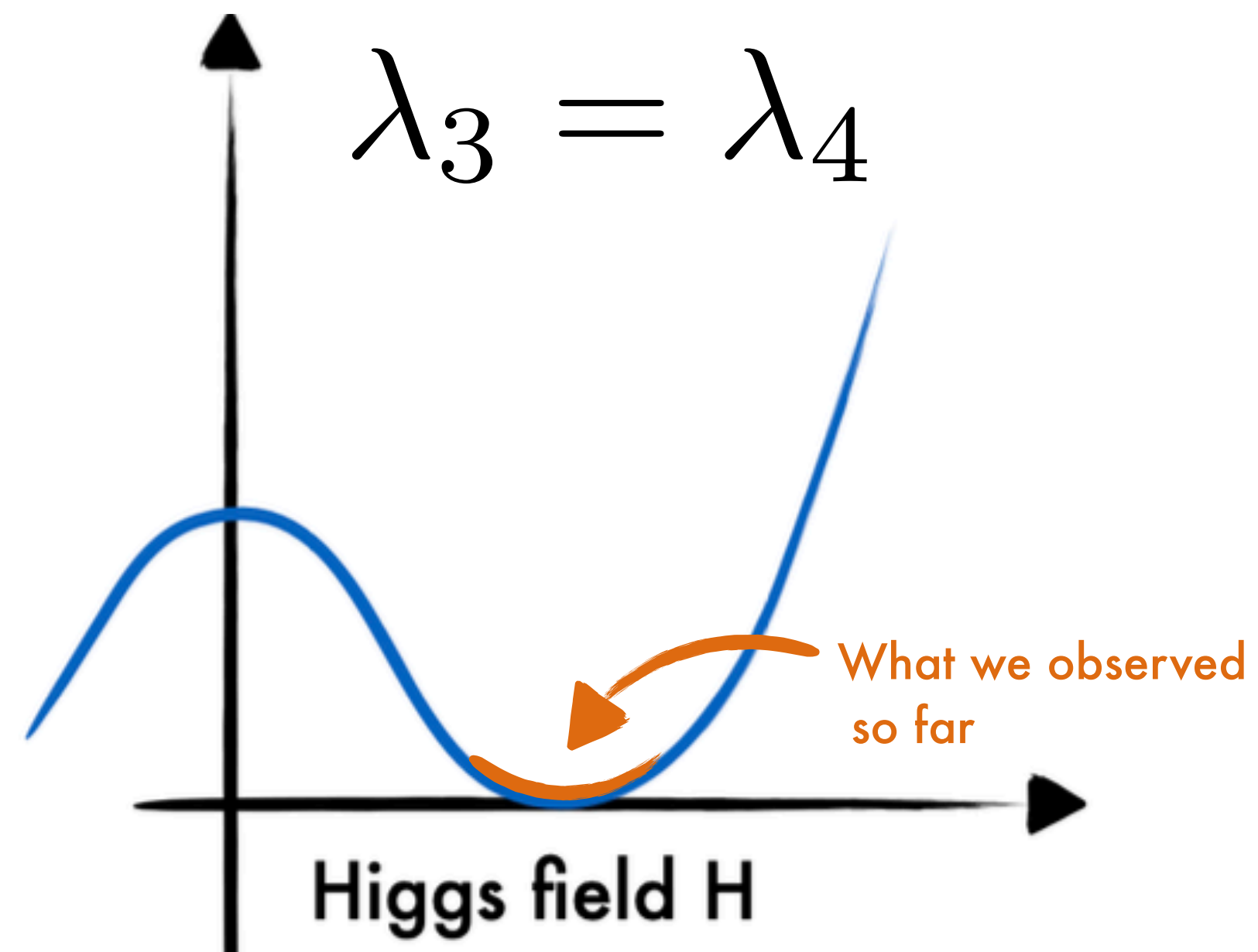
Higgs self-coupling: one of the most important properties of the Higgs boson that is not measured yet
In the Standard Model: the Higgs potential is responsible for the masses of all particles

- Directly responsible for the interaction of the Higgs boson with itself
 - Trilinear coupling: responsible for di-Higgs production
 - Quartic coupling: responsible for triple-Higgs production

Measuring the Higgs potential: motivation

$$V(H) = \frac{1}{2}m_H^2 H^2 + \lambda_3 v H^3 + \frac{1}{4}\lambda_4 H^4$$

Standard Model

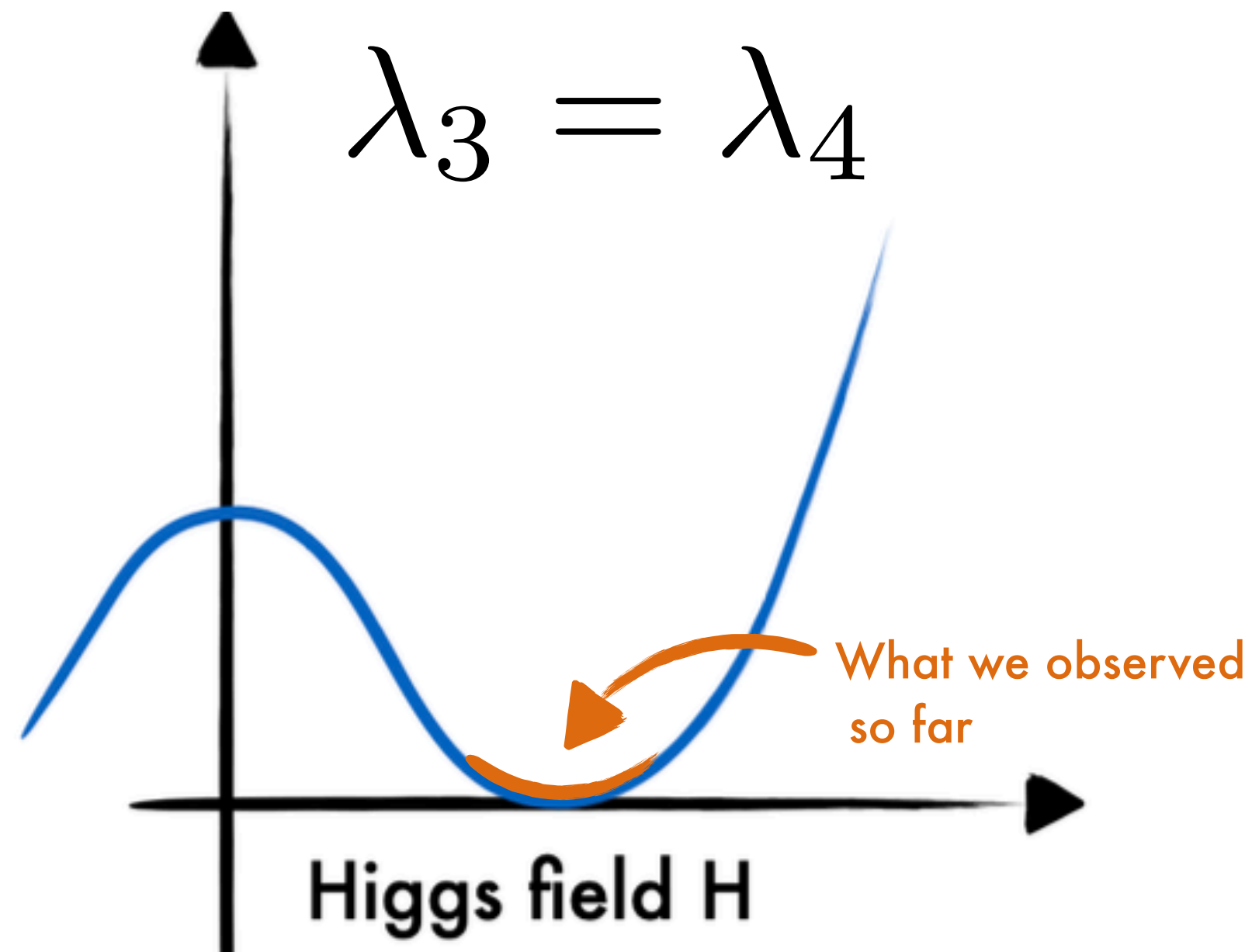


In the Standard Model: $\lambda_3 = \lambda_4$

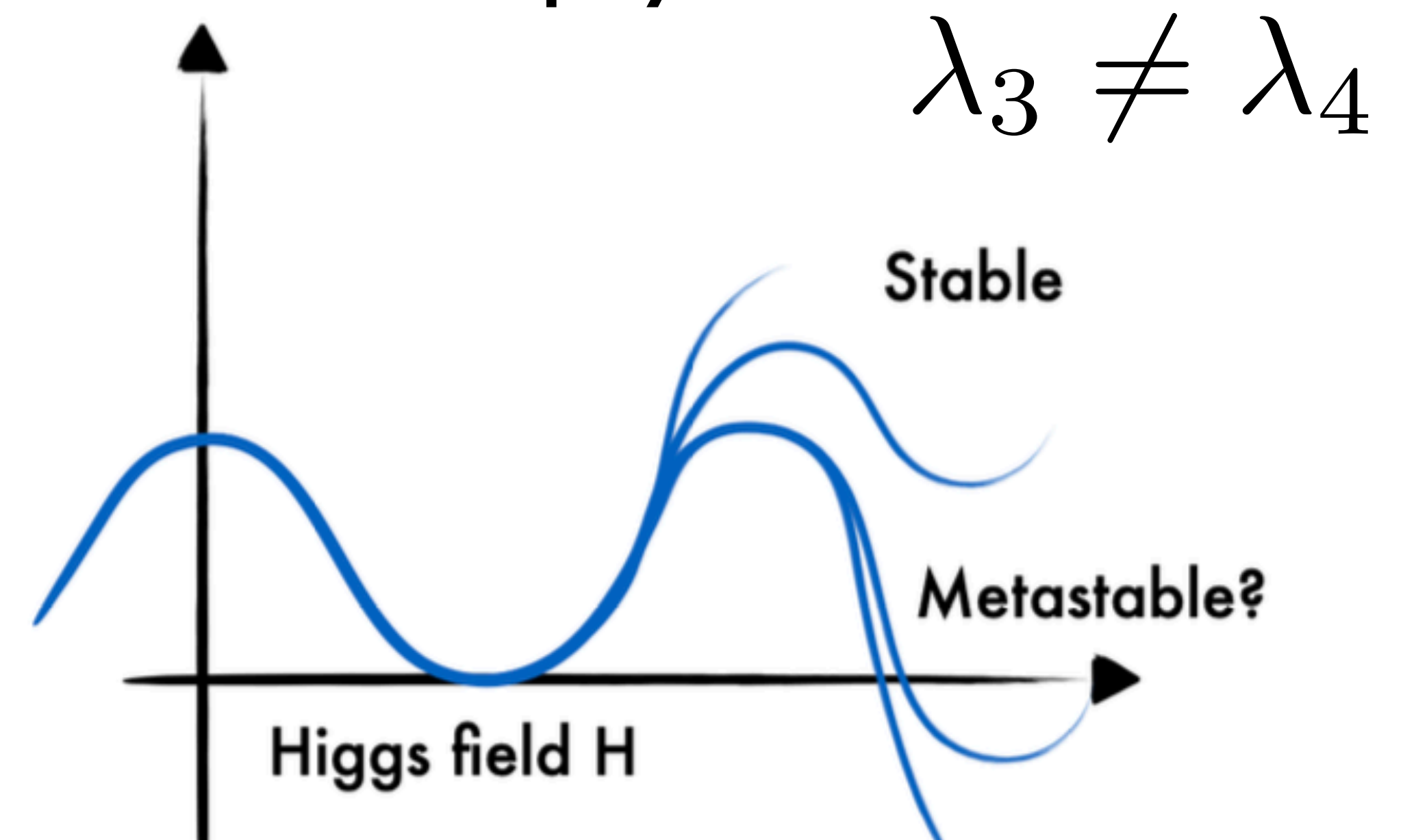
Measuring the Higgs potential: motivation

$$V(H) = \frac{1}{2}m_H^2 H^2 + \lambda_3 v H^3 + \frac{1}{4}\lambda_4 H^4$$

Standard Model



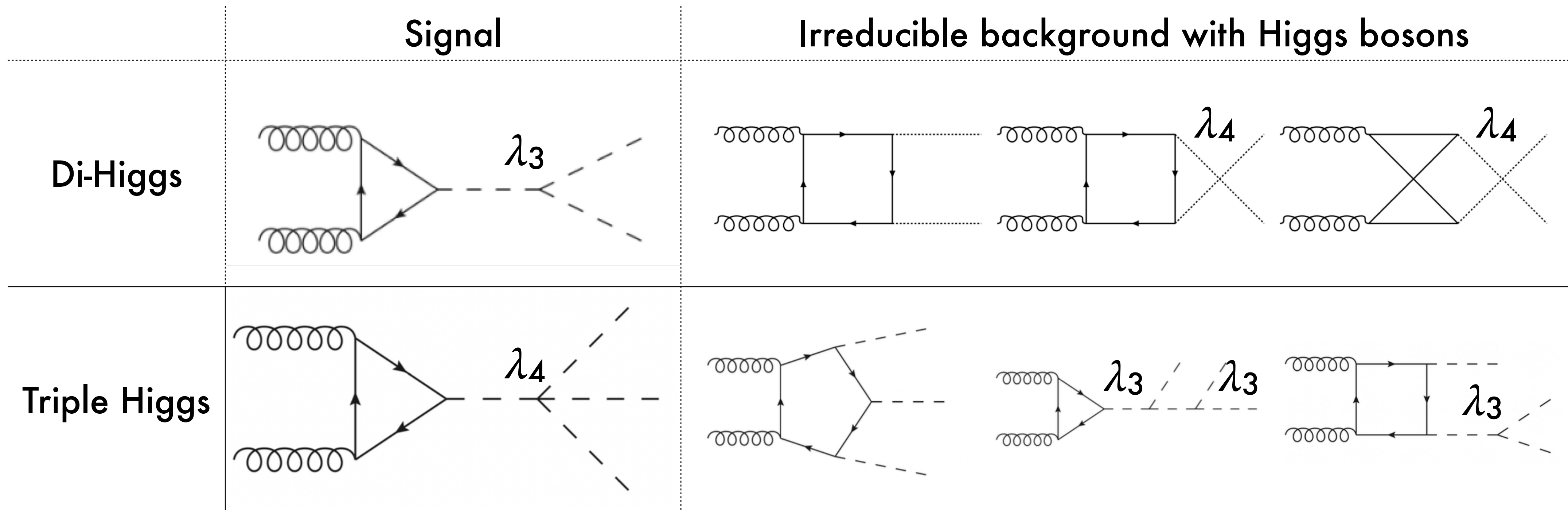
New physics



In the Standard Model: $\lambda_3 = \lambda_4$

- Not given for a fact, needs to be measured
- New physics can affect the shape of the Higgs potential → large consequences for the Universe

Probing self-interaction di-Higgs and triple Higgs



Probing the Higgs self-coupling possible through di-Higgs and triple Higgs measurements:

- Di-Higgs: nearly exclusively sensitive to λ_3 coupling (very small contribution from λ_4)
- Triple Higgs: sensitive to both λ_3 and λ_4 coupling

→ Full determination of the Higgs potential only possible through combined measurement!

Sensitivity:

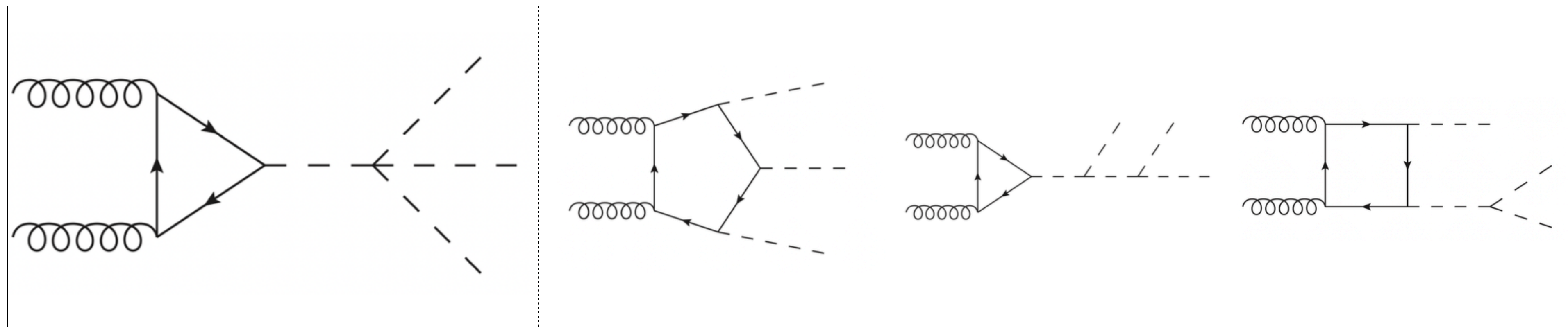
- Di-Higgs: current sensitivity $< 2.5 \times SM @ 95\% CL$ → expect evidences at HL-LHC
- Triple Higgs: considered impossible to measure at LHC → No estimated results so far!

Extrapolating HHH sensitivities from FCC to LHC

Triple Higgs projections @ FCC-hh

Main Feynman diagrams of triple Higgs production

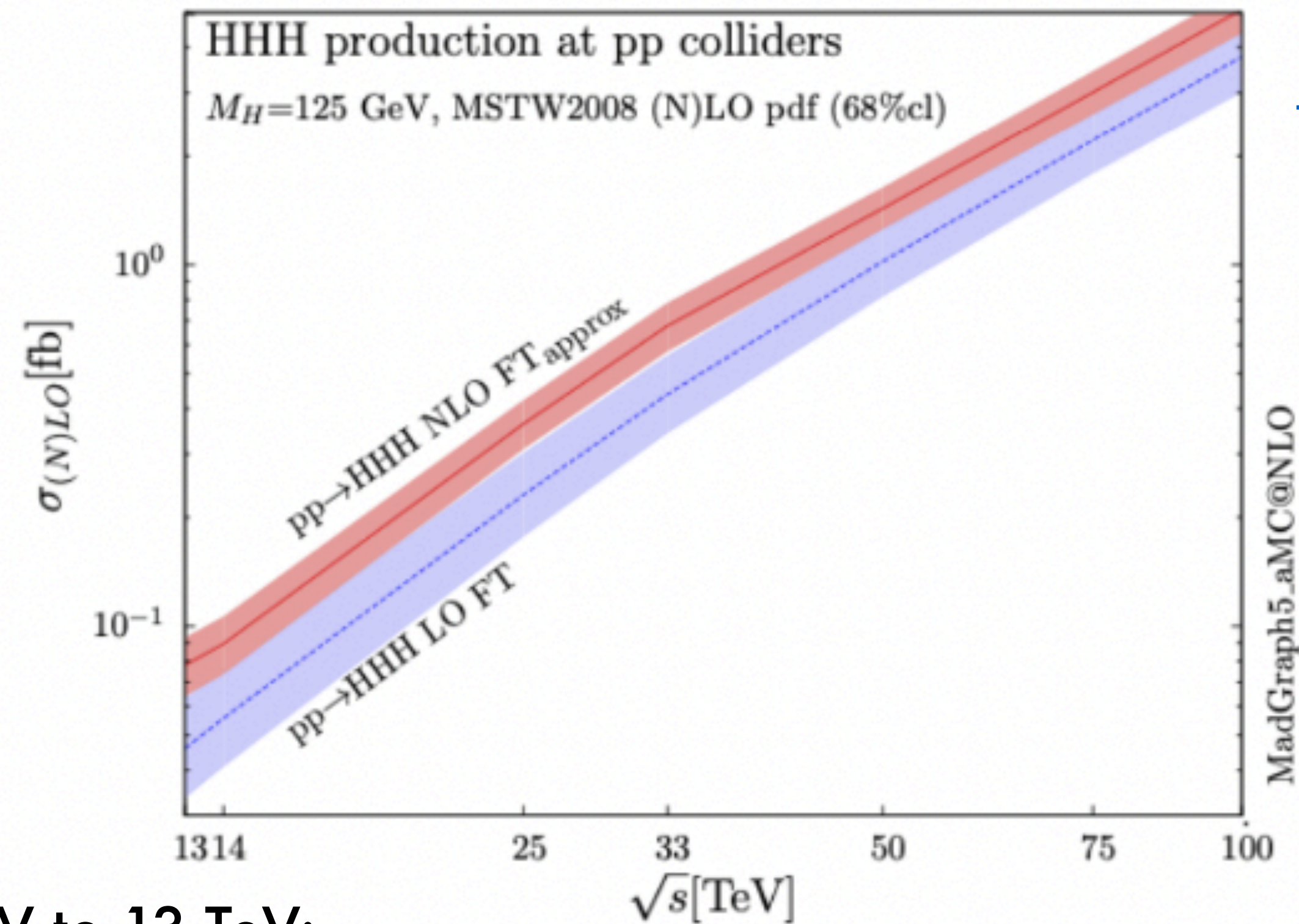
Triple Higgs



Different diagrams with three Higgs in the final state: involving both cubic and quartic coupling

- Case study: focus on three decay modes based on **theory papers at 100 TeV**
- [HHH → \(bb\) \(bb\) \(bb\) \[Eur. Phys. J. C \(2019\) 79:947\]](#): largest branching fraction + large background
- [HHH → \(bb\) \(bb\) \(γγ\) \[arXiv:1606.09408v1\]](#) : low branching ratio but clean signature with photons
- [HHH → \(bb\) \(bb\) \(ττ\) \[Phys. Lett. B771 \(2017\) 354-358\]](#) : trade off branching ratio vs background
- Also very sensitive channel in di-Higgs

Cross-sections



[Maltoni, Vryonidu, Zaro](#)

Extrapolation from 100 TeV to 13 TeV:

- $\sigma(\text{HHH})_{13\text{TeV}} / \sigma(\text{HHH})_{100\text{TeV}} = 1 / 60$
- $\sigma(\text{QCD } 6\text{-bjets})_{13\text{TeV}} / \sigma(\text{QCD } 6\text{ b-jets})_{100\text{TeV}} = 1 / 10$ (taken from [this paper](#))
- Assume 2 different scenarios:
 1. Optimistic scaling: both signal and background scale with $1 / 60$
 2. Pessimistic scaling: signal $1/60$ and background $1/10$ (more accurate for $\text{HHH} \rightarrow 6b$)
 - 'Pessimistic' in the sense that these theory papers are mostly simple cut and count, not optimised

Estimated result at LHC @ 13 TeV

Channel	\mathcal{L} at 100 TeV	Significance	\mathcal{L} at 13 TeV	Pessimistic	Optimistic
$HHH \rightarrow b\bar{b}b\bar{b}b\bar{b}$ [28]	20 ab^{-1}	1.6σ	139 fb^{-1}	$285 \times \text{SM}$	$120 \times \text{SM}$
$HHH \rightarrow b\bar{b}b\bar{b}\gamma\gamma$ [29]	20 ab^{-1}	2.1σ	139 fb^{-1}	$220 \times \text{SM}$	$90 \times \text{SM}$
$HHH \rightarrow b\bar{b}b\bar{b}\tau^+\tau^-$ [30]	30 ab^{-1}	2.0σ	139 fb^{-1}	$280 \times \text{SM}$	$115 \times \text{SM}$
Combination	20 ab^{-1}	2.9σ	139 fb^{-1}	$150 \times \text{SM}$	$64 \times \text{SM}$

\mathcal{L} at 13 TeV	Pessimistic	Optimistic
139 fb^{-1}	$150 \times \text{SM}$	$64 \times \text{SM}$
300 fb^{-1}	$100 \times \text{SM}$	$40 \times \text{SM}$
500 fb^{-1}	$80 \times \text{SM}$	$35 \times \text{SM}$
3000 fb^{-1}	$30 \times \text{SM}$	$15 \times \text{SM}$

Estimated results: 60-150x SM prediction for triple Higgs productions with 139/fb

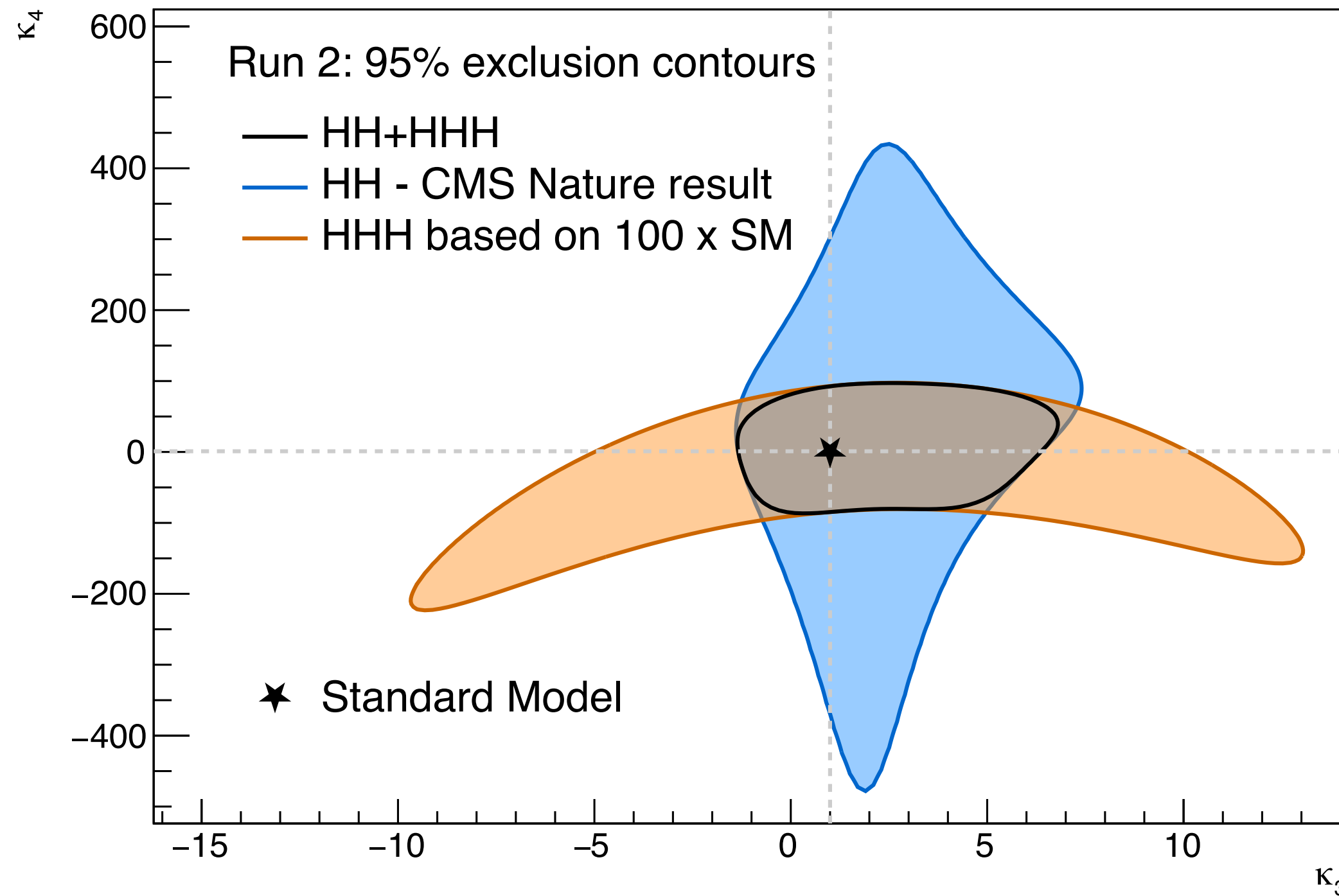
- Note: **back of the envelope estimate** based on simple theory projections
 - Missing crucial components such as detector resolutions, systematics, object reconstruction
 - Object identification performance: optimistically
- Need to test this experimentally with a dedicated analysis at the LHC

Estimating the sensitivity to the self-coupling

Probing self-interaction di-Higgs and triple Higgs

Based on
[arXiv:1810.04665v3](https://arxiv.org/abs/1810.04665v3)

Simulating κ_3 and κ_4 coupling modifications



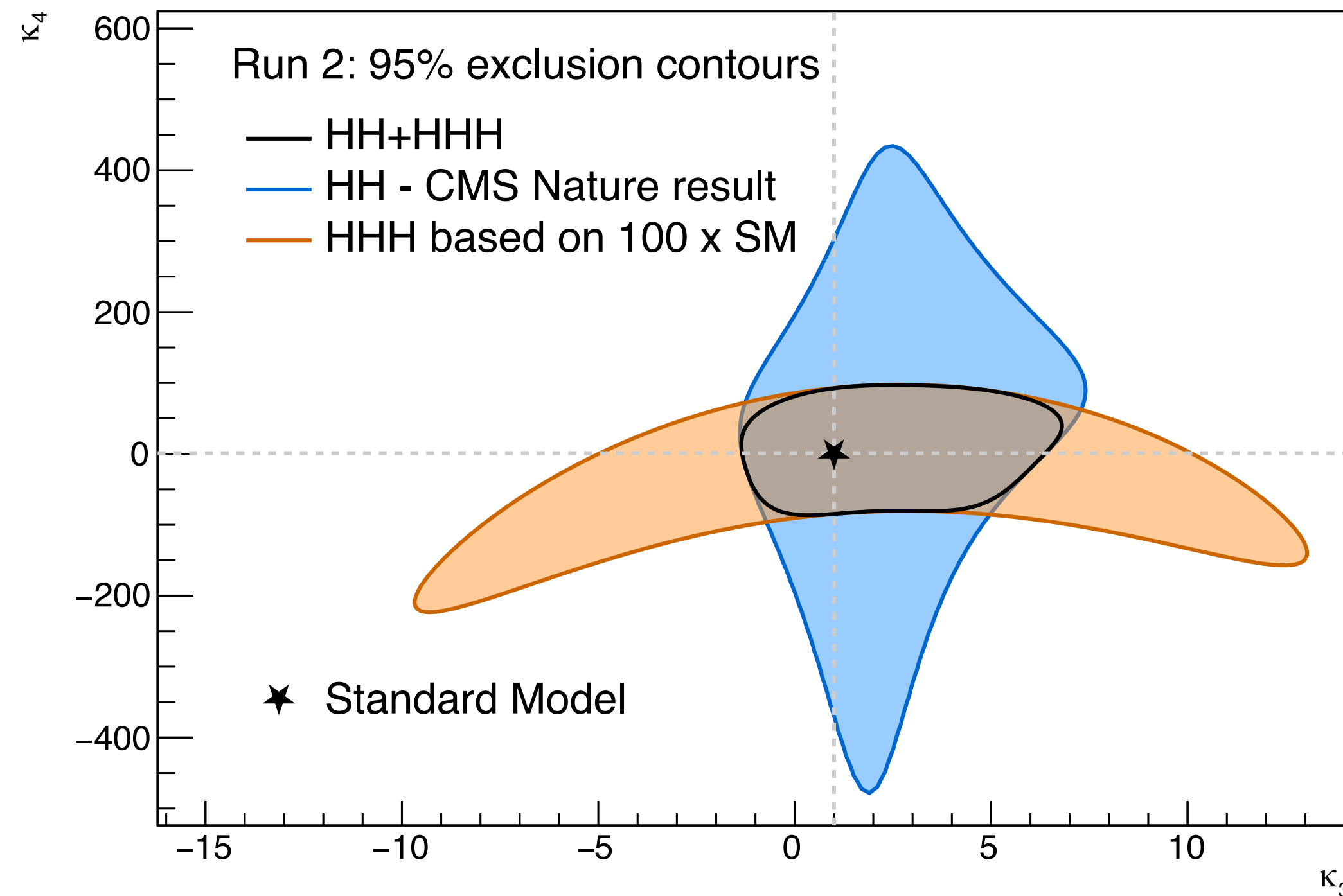
HH and HHH parametrisation with trilinear κ_3 and κ_4 quartic coupling modifiers

- Current HH analyses: neglect κ_4 coupling modifier → additional assumption
- Relax assumption $\lambda_3 = \lambda_4$ in combined HH and HHH measurement

Probing self-interaction di-Higgs and triple Higgs

Based on
[arXiv:1810.04665v3](https://arxiv.org/abs/1810.04665v3)

Simulating κ_3 and κ_4 coupling modifications



CMS searches	Limit at 95% CL
HH→bbbb (boosted)	$-9.9 < \kappa_3 < 16.9$
HH→bbbb (resolved)	$-2.3 < \kappa_3 < 9.4$
HH→bb $\tau\tau$	$-3.0 < \kappa_3 < 9.0$
HH→bb $\gamma\gamma$	$-3.3 < \kappa_3 < 8.5$
HH combination (Nature paper)	$-1.2 < \kappa_3 < 6.5$
Projection for HHH assuming $\mu_{HHH} < 100x$ SM (Normalisation only)	$-5 < \kappa_3 < 10$

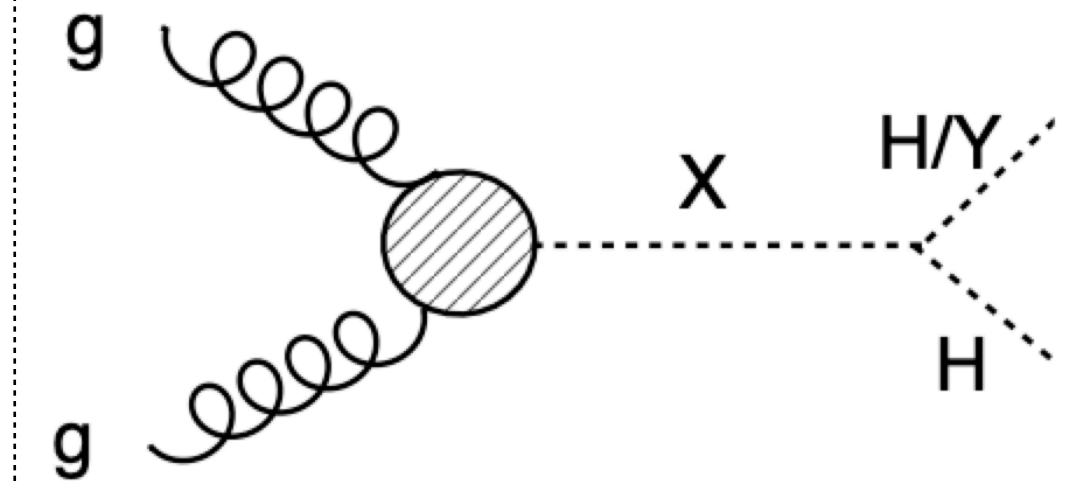
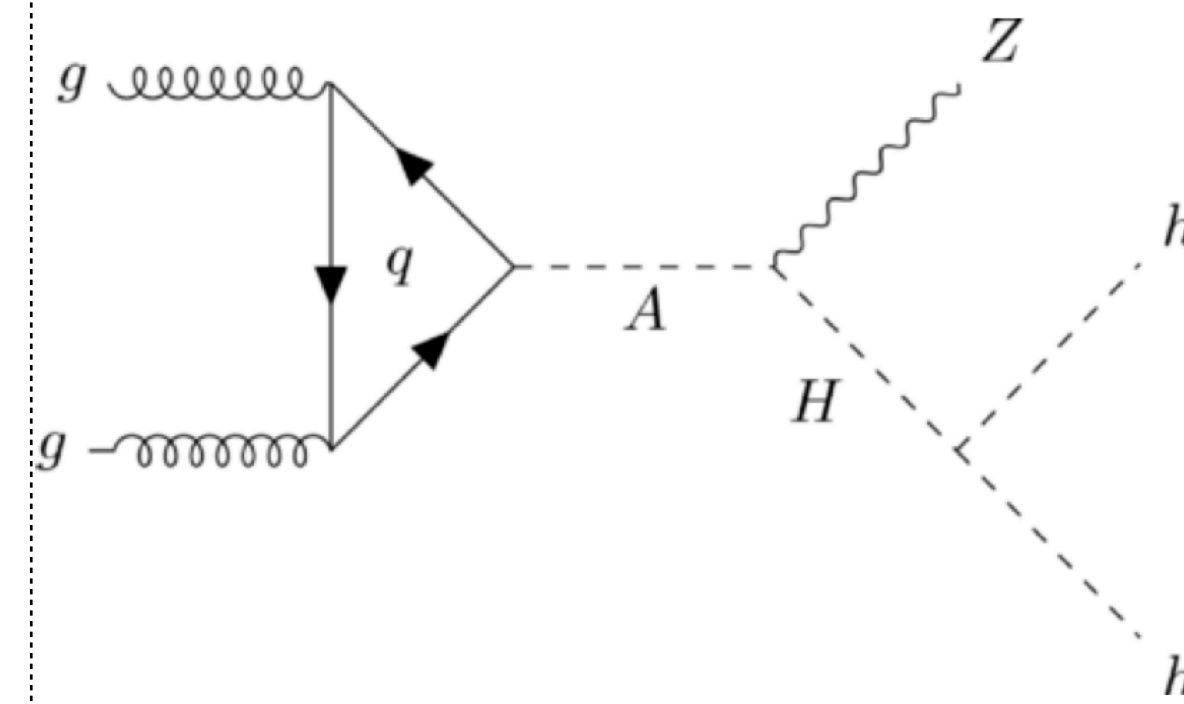
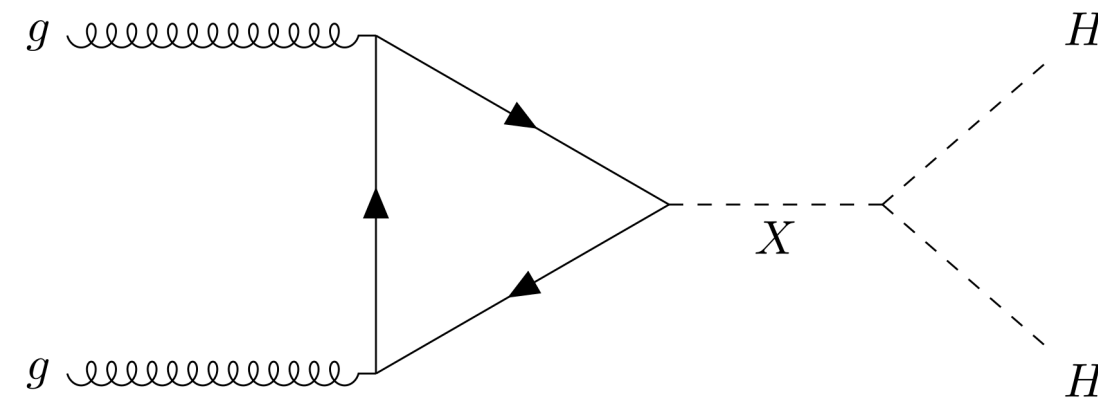
HH and HHH parametrisation with trilinear κ_3 and κ_4 quartic coupling modifiers

- Current HH analyses: neglect κ_4 coupling modifier → additional assumption
 - Relax assumption $\lambda_3 = \lambda_4$ in combined HH and HHH measurement
- Assuming HHH sensitivity about 100x SM: competitive limit on κ_3 possible w.r.t HH channels
 → Can we reach 100x SM HHH sensitivity with Run 2?

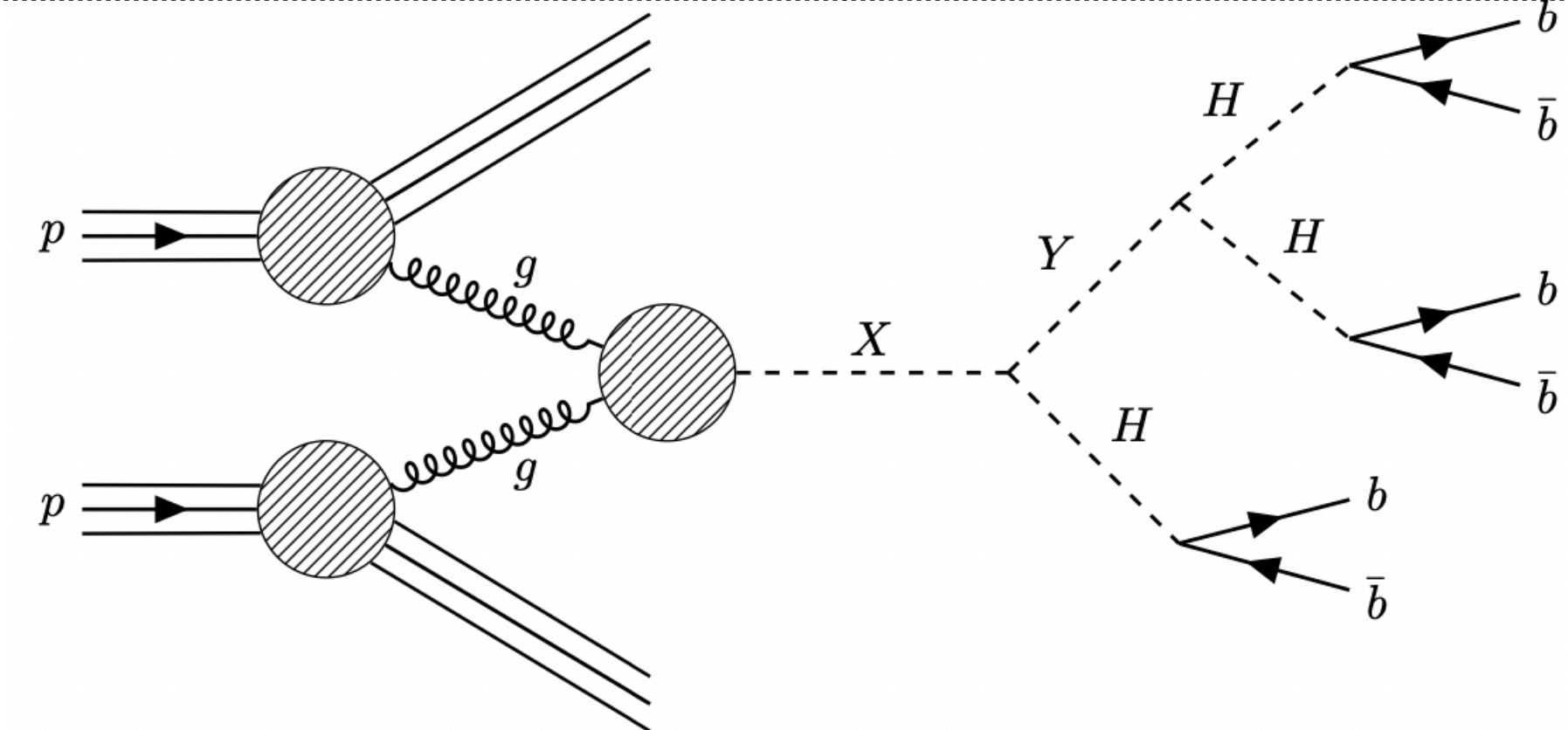
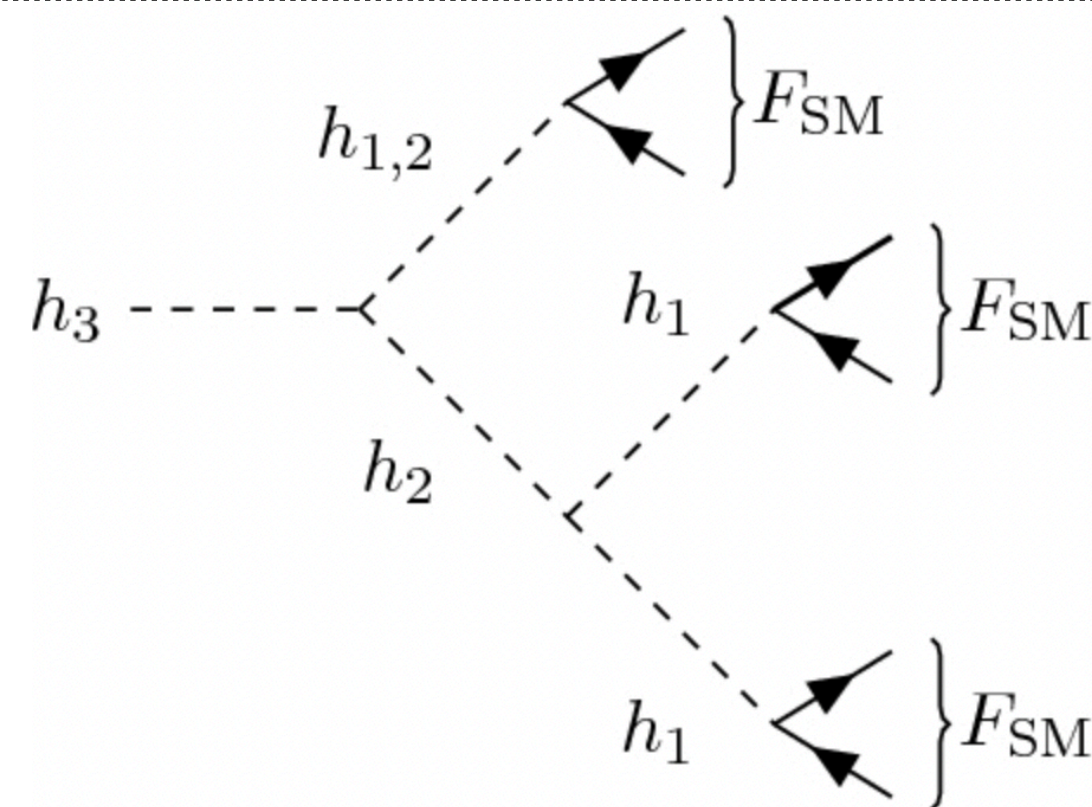
HH and HHH: probe for BSM

[Eur. Phys. J. C 80, 151 \(2020\)](#)
[JHEP 05 \(2021\) 193](#)
[Phys. Rev. D 103, 115005 \(2021\)](#)
[Eur. Phys. J. C 80, 884 \(2020\)](#)

BSM HH



BSM HHH



HH and HHH sensitive to new physics:

- New resonances with spin0, spin2, two Higgs doublet, new scalars
- Any enhancement of HH and HHH production = sign of new physics!

HHH workshop

14-16th of July 2023 Dubrovnik / Croatia

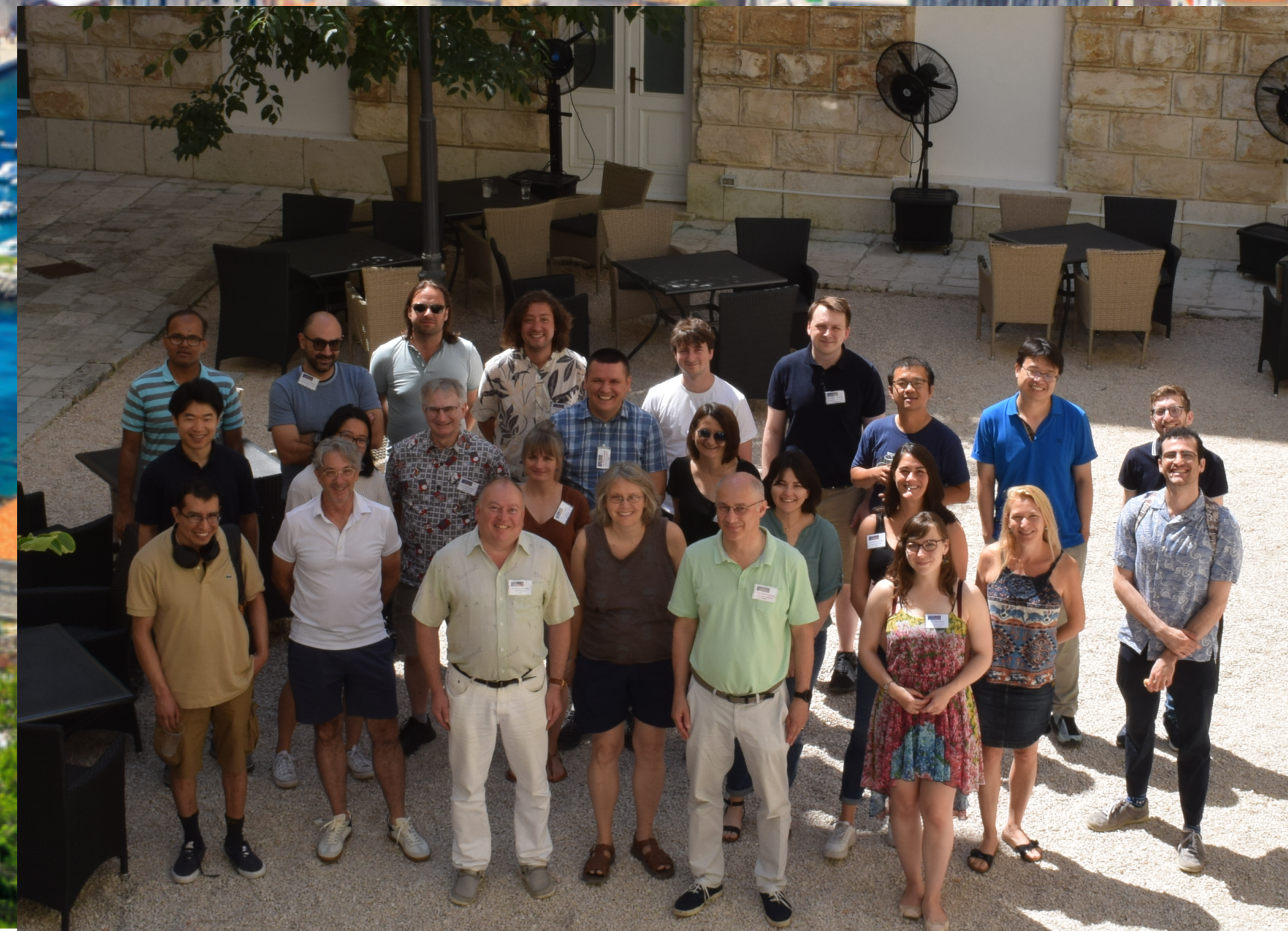


Organising committee

Vuko Brigljević, Ruđer Bošković Institute
Dinko Ferenček, Ruđer Bošković Institute
Greg Landsberg, Brown University
Tania Robens, Ruđer Bošković Institute
Marko Stamenkovic, Brown University
Tatjana Šuša, Ruđer Bošković Institute



<https://indico.cern.ch/e/hhh2023>



HHH workshop overview

Day 1

HHH theory

**Lessons from
ATLAS and CMS
HH**

ML for HHH

**+
HHH
phenomenology**

Day 2

ATLAS vs CMS

**Flavour tagging
Trigger**

**BSM HHH
3HDMs**

**Experimental
thoughts**

Day 3

**BSM
enhancements in
HH and HHH**

FCC projections

Overview

Excursion

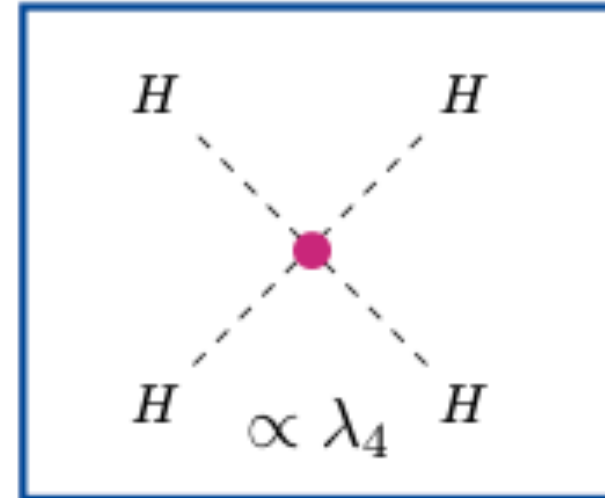
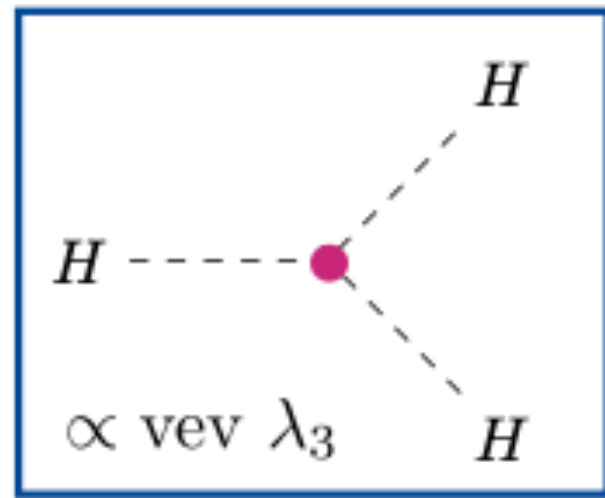
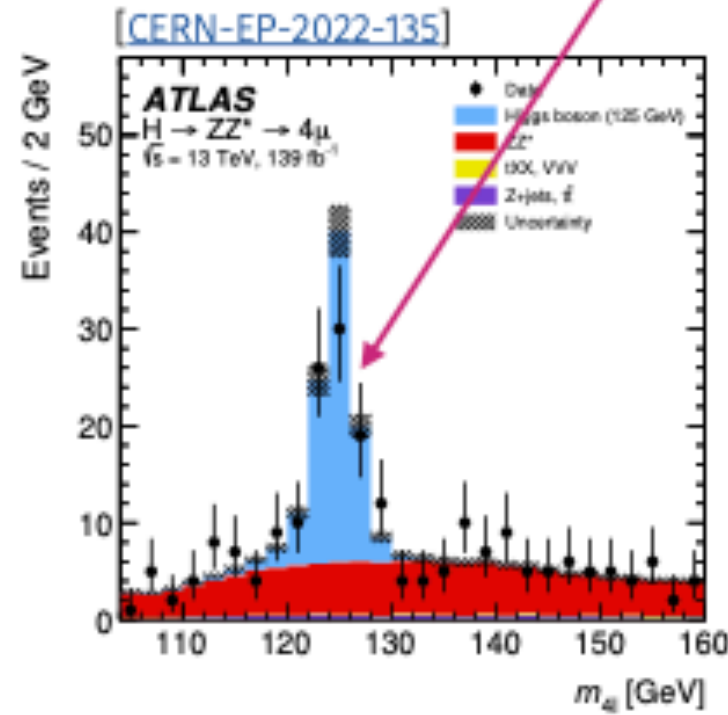
Successful 3 days workshop with theorists and experimentalists from both ATLAS and CMS

- A lot of interesting discussions, summarised non-exhaustively in the next few slides
- All the presentations available on the indico: [HHH 2023 workshop in Dubrovnik](#)

Higgs trilinear and quartic coupling

B. Moser

$$V(H) = \frac{1}{2}m_H^2 H^2 + \lambda_3 \text{ vev } H^3 + \frac{1}{4}\lambda_4 H^4$$



In SM:
 $\lambda_3 = \lambda_4 = \lambda = \frac{m_H}{2v^2} \sim \frac{1}{8}$

Parameterize:

$$\kappa_3 = \frac{\lambda_3}{\lambda_3^{\text{SM}}}$$

$$\kappa_4 = \frac{\lambda_4}{\lambda_4^{\text{SM}}}$$

[with SM = $\kappa_3 = \kappa_4 = 1$]

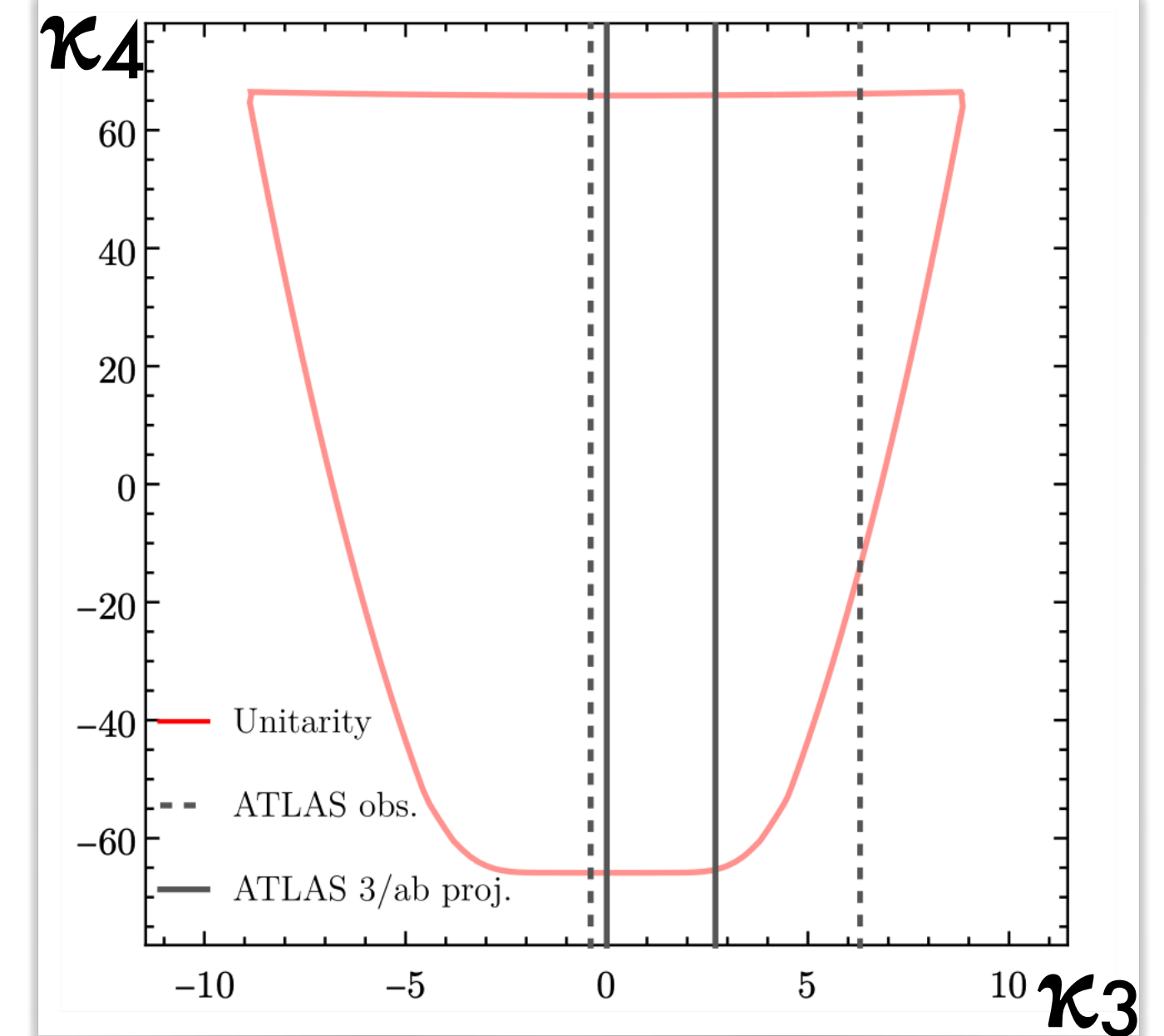
P. Stylianou

Higgs potential: responsible for self-coupling of the Higgs

- Measuring multi-Higgs production = critical probe of the SM
- No explanation for the shape of the Higgs potential
- Sensitive to new physics

Unitarity constraints: provide some constraints on λ_3 and λ_4

- HH combination: scratching κ_3 values not excluded by unitarity
 - With some assumptions on the quartic coupling
- LHC is the only machine in the world capable of probing λ_4 ?



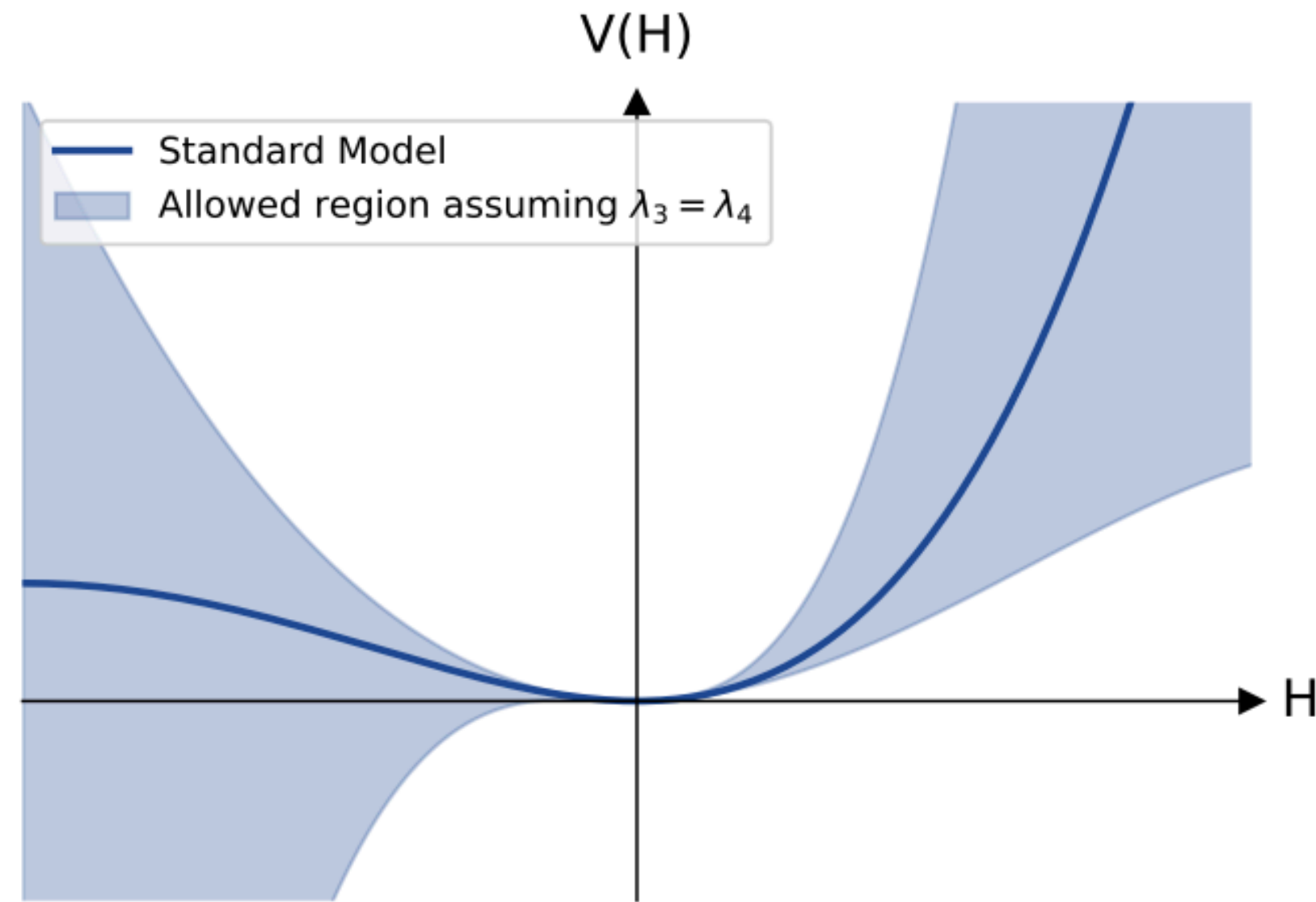
Higgs potential $V(H)$

B. Moser

Constraining $V(H)$ - where do we stand?

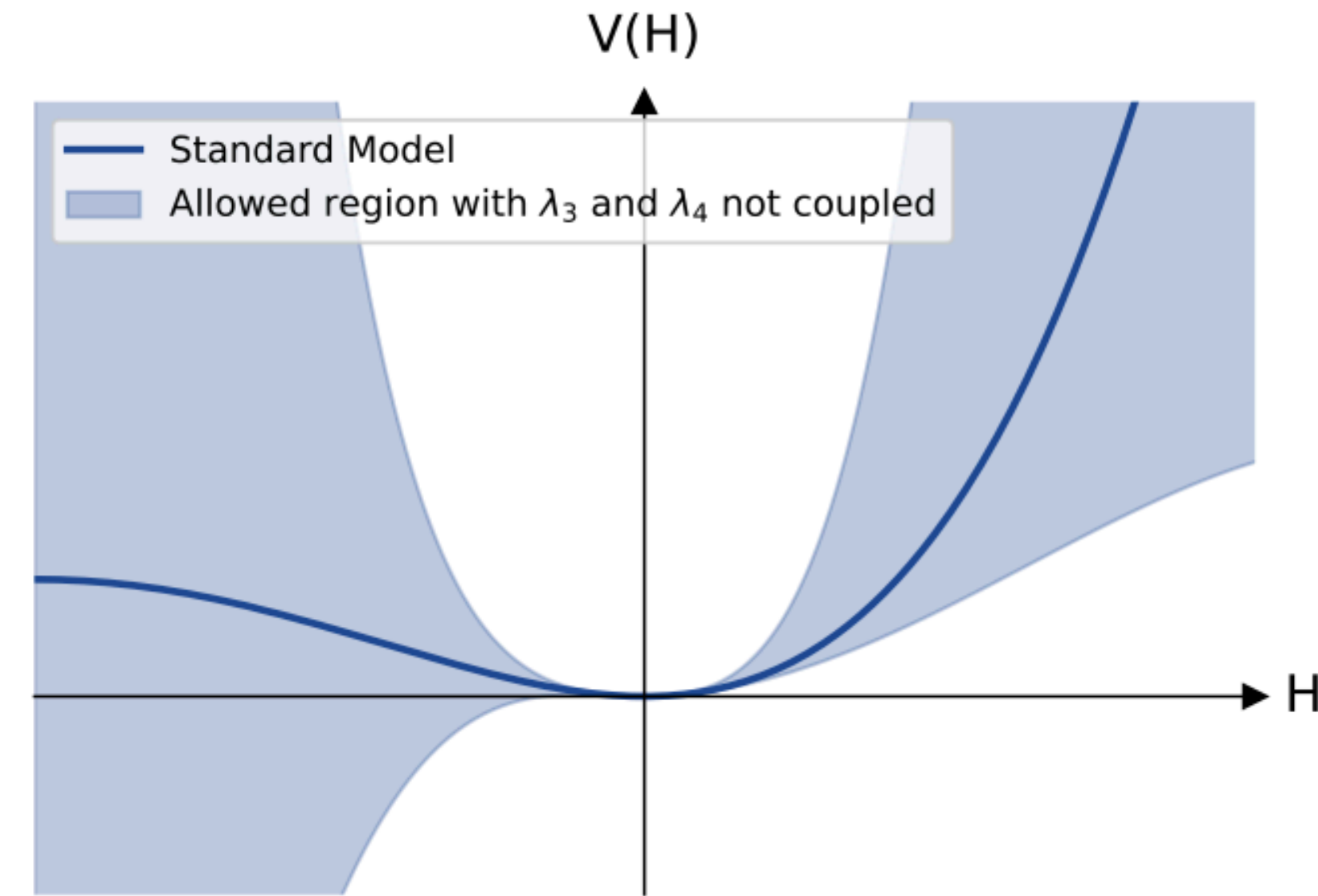
[using Run 2 ATLAS constraints from [Phys. Lett. B 843 \(2023\) 137745](#)]

Assuming 1 free parameter $\lambda_3 = \lambda_4 = \lambda$



[plot style inspired by Nathaniel Craig]

Assuming 2 free parameters λ_3 and λ_4



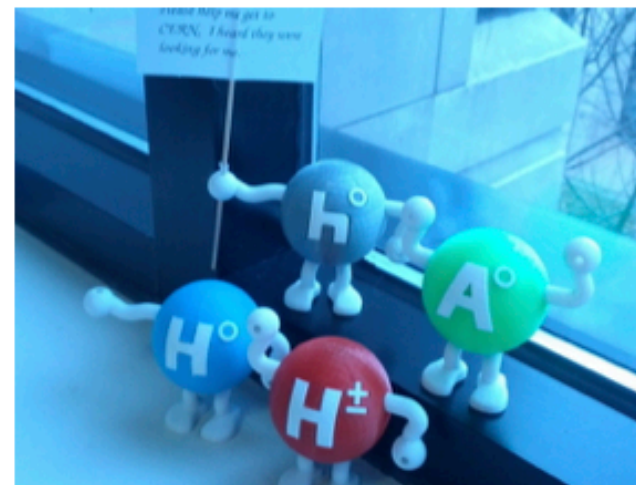
Measuring the Higgs potential:

- Current knowledge \rightarrow large amount of shapes still allowed, with different minima still allowed
 - Experimentally establishing the Higgs potential is one of the highest priority of the LHC program
 - With as little approximations / hypotheses possible

New physics in HHH

T. Robens

- A priori: **no limit to extend scalar sector**
- **make sure you**
 - have a **suitable ew breaking mechanism**, including a **Higgs candidate at ~ 125 GeV**
 - can explain **current measurements**
 - are **not excluded by current searches** and precision observables
- **nice add ons:**
 - can **push vacuum breakdown to higher scales**
 - can **explain additional features**, e.g. dark matter, or hierarchies in quark mass sector
 - ...
- Multitude of models out there
- adding ew gauge singlets/ doublets/ triplets...
 \Rightarrow **new scalar states** \Leftarrow



- 3 scalar states h_1, h_2, h_3 that mix

concentrate on
 $pp \rightarrow h_3 \rightarrow h_2 h_1 \rightarrow h_1 h_1 h_1 \rightarrow b\bar{b} b\bar{b} b\bar{b}$

(M_2, M_3) [GeV]	$\sigma(pp \rightarrow h_1 h_1 h_1)$ [fb]	$\sigma(pp \rightarrow 3b\bar{b})$ [fb]	sig $_{300\text{fb}^{-1}}$	sig $_{3000\text{fb}^{-1}}$
(255, 504)	32.40	6.40	2.92	9.23
(263, 455)	50.36	9.95	4.78	15.11
(287, 502)	39.61	7.82	4.01	12.68
(290, 454)	49.00	9.68	5.02	15.86
(320, 503)	35.88	7.09	3.76	11.88
(264, 504)	37.67	7.44	3.56	11.27
(280, 455)	51.00	10.07	5.18	16.39
(300, 475)	43.92	8.68	4.64	14.68
(310, 500)	37.90	7.49	4.09	12.94
(280, 500)	40.26	7.95	4.00	12.65

discovery, exclusion
 \Rightarrow **at HL-LHC, all points within reach** \Leftarrow

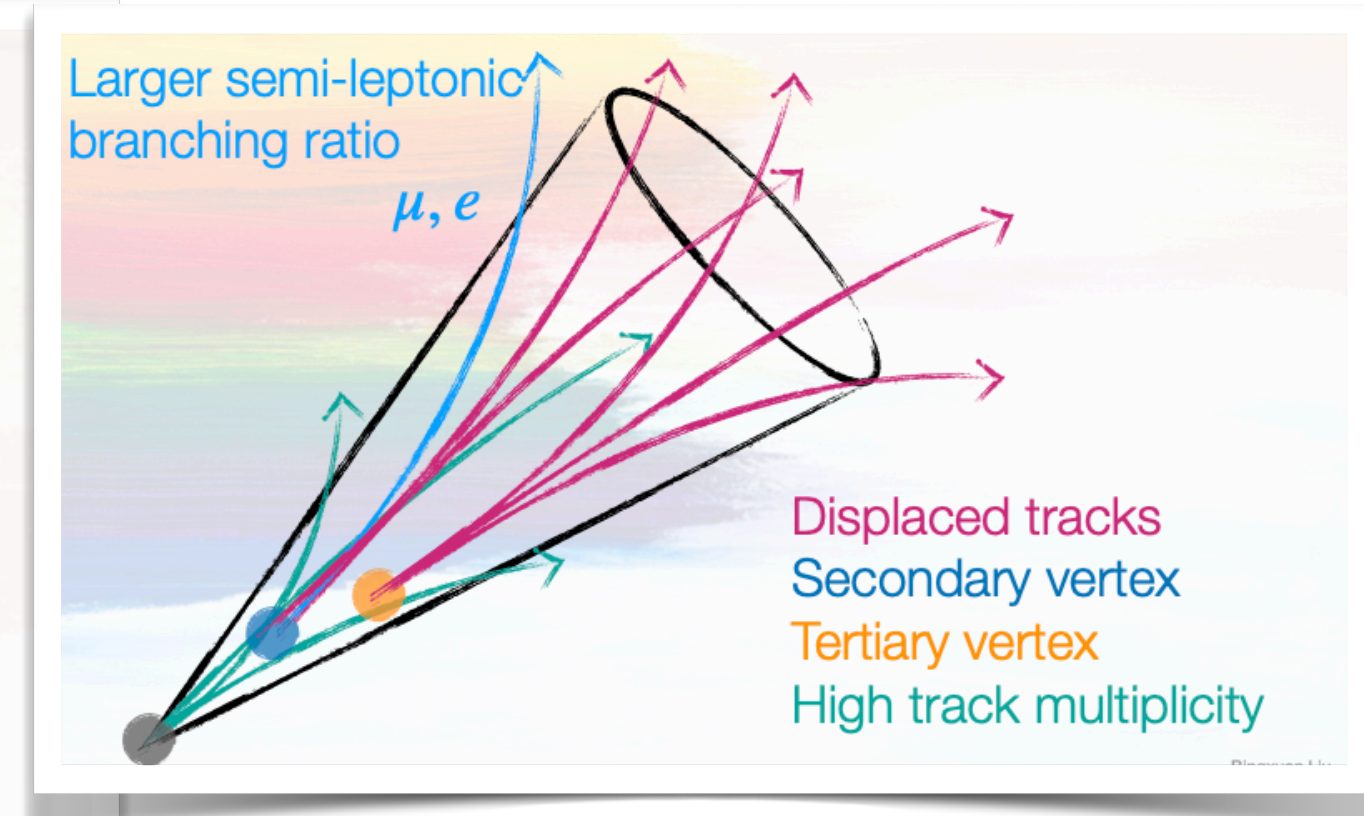
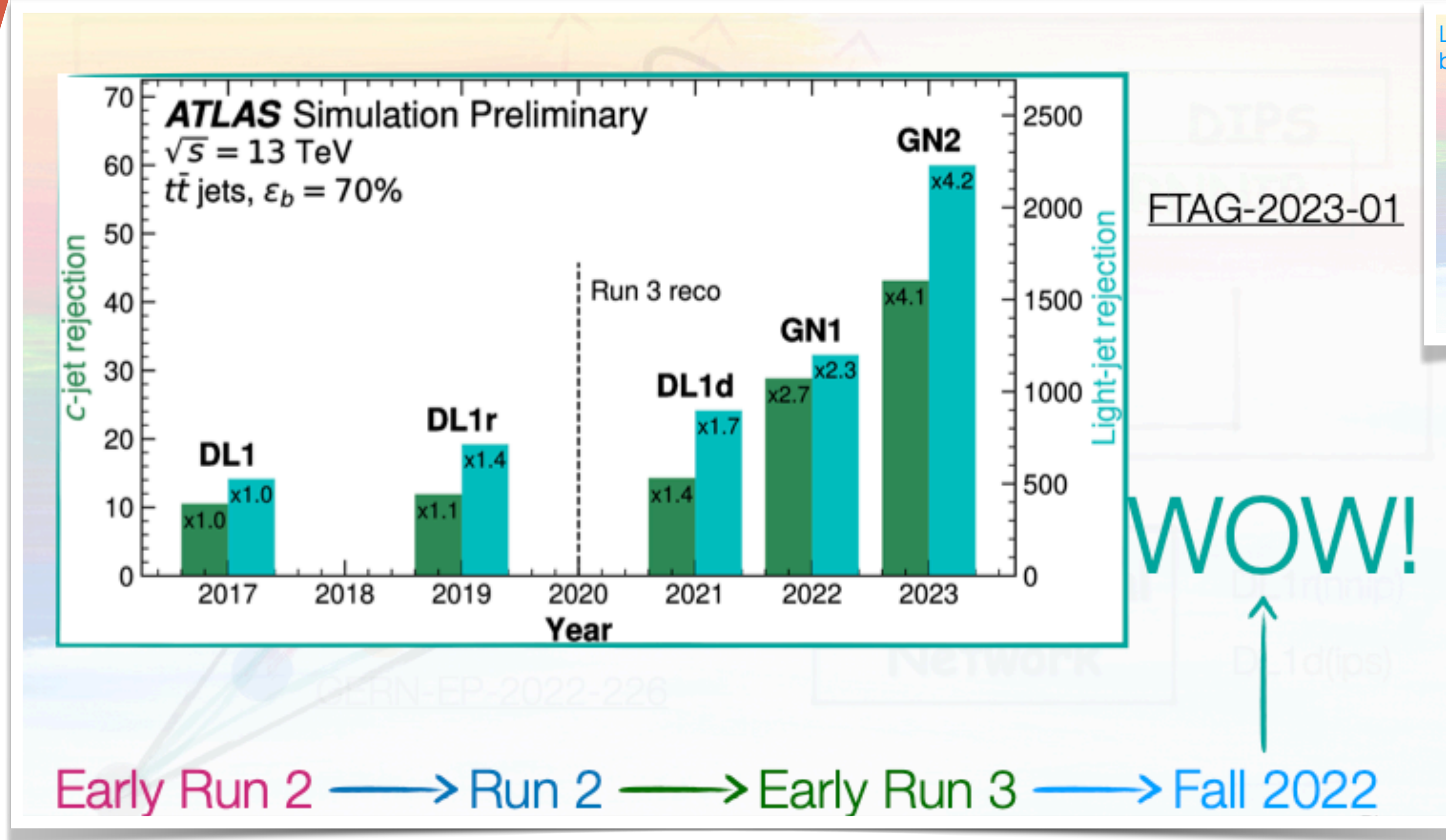
HHH: rich phenomenology

- Capable of probing various BSM scenarios
- Including extended sectors with scalars, 3HDMs

Experimental overview

Flavour tagging

B. Liu

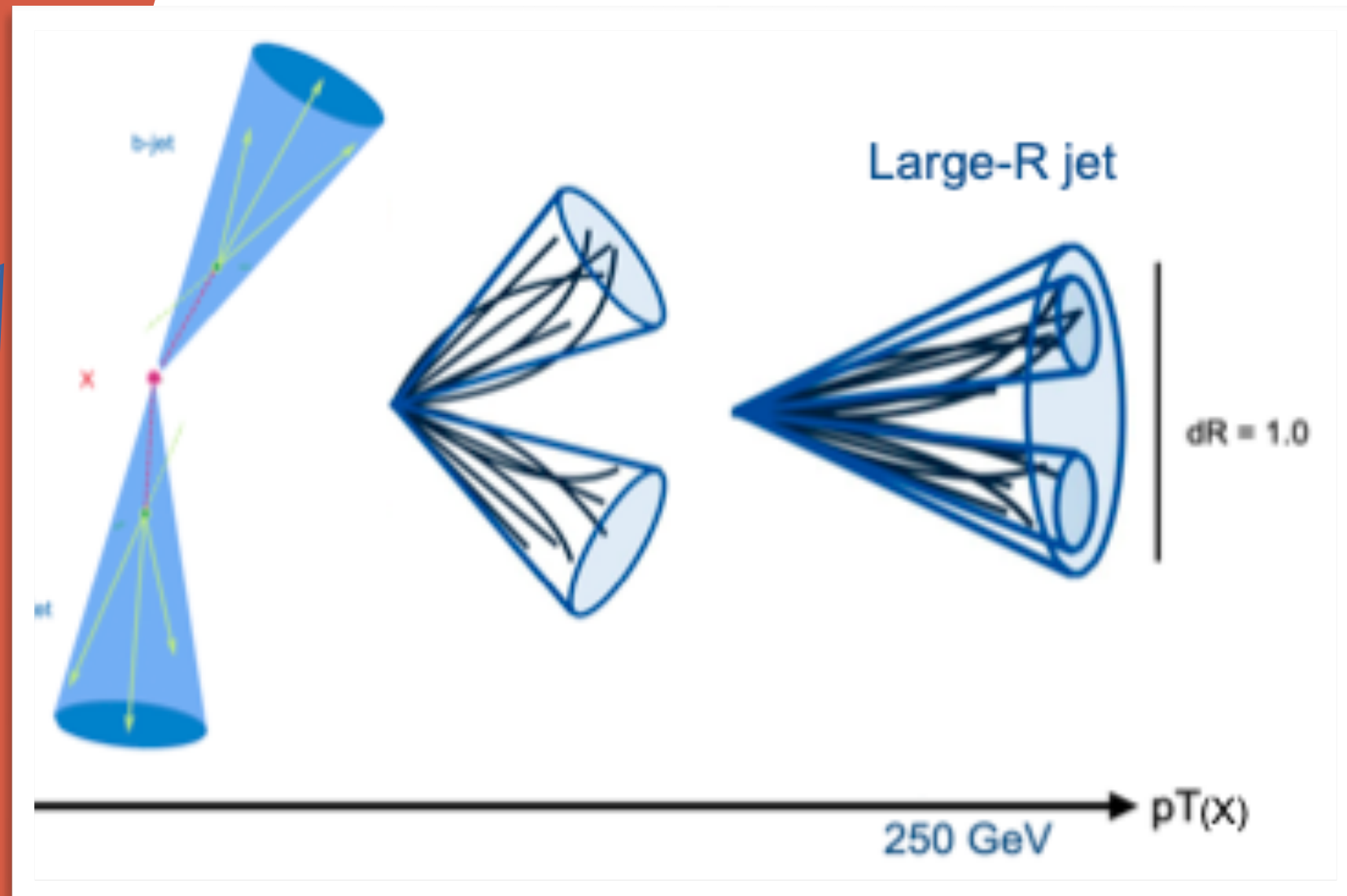


Experimentally: extraordinary progress achieved every year

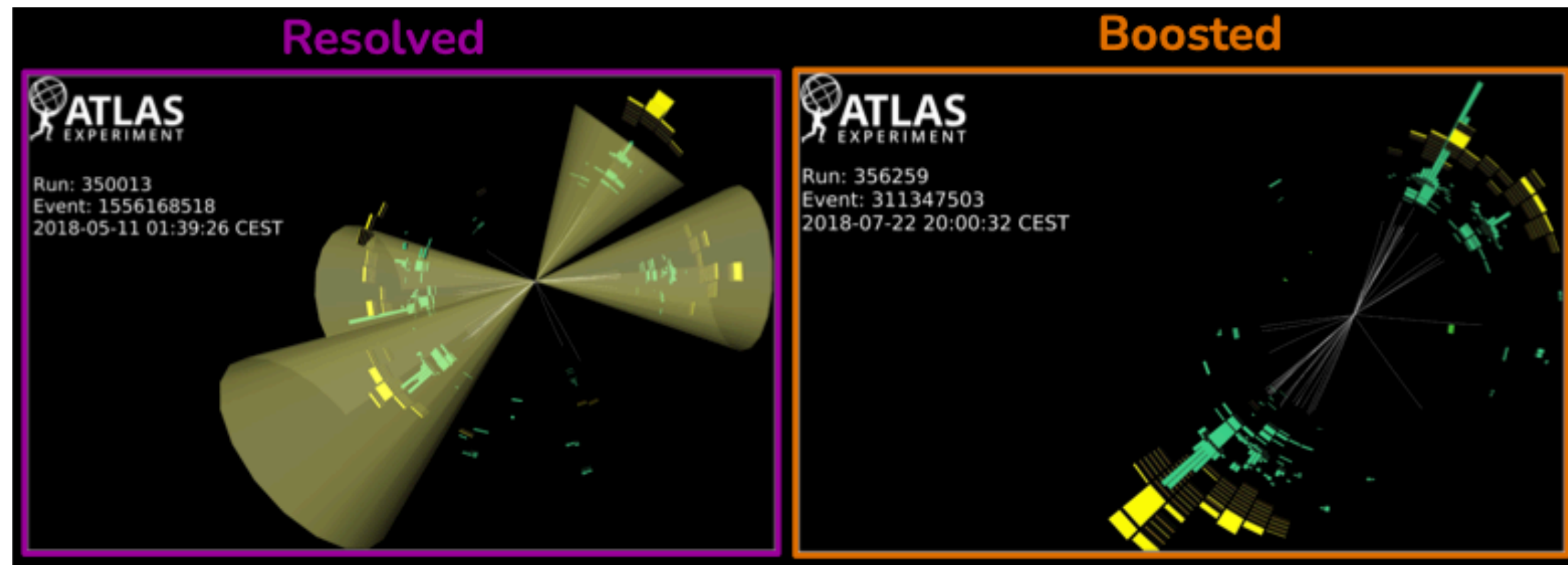
- Flavour tagging to identify b-jets in the detector: improved by a factor 4 in the span of 6 years!
- For the same identification of b-jets: remove 4x more background than before!
- Similar progress in both ATLAS and CMS: crucial for HH and HHH!

Boosted Higgs tagging

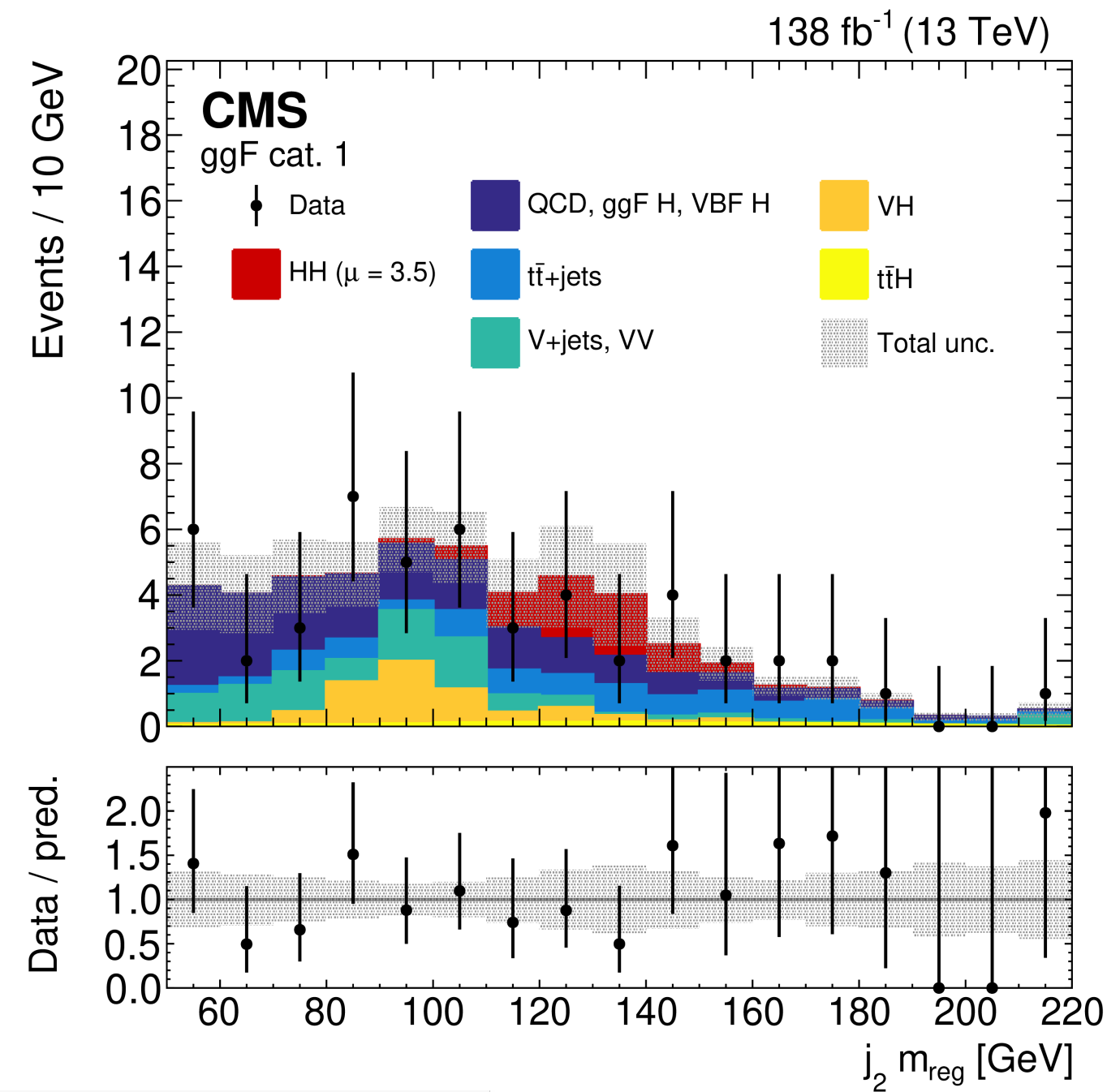
O. Karkout



W. Balunas

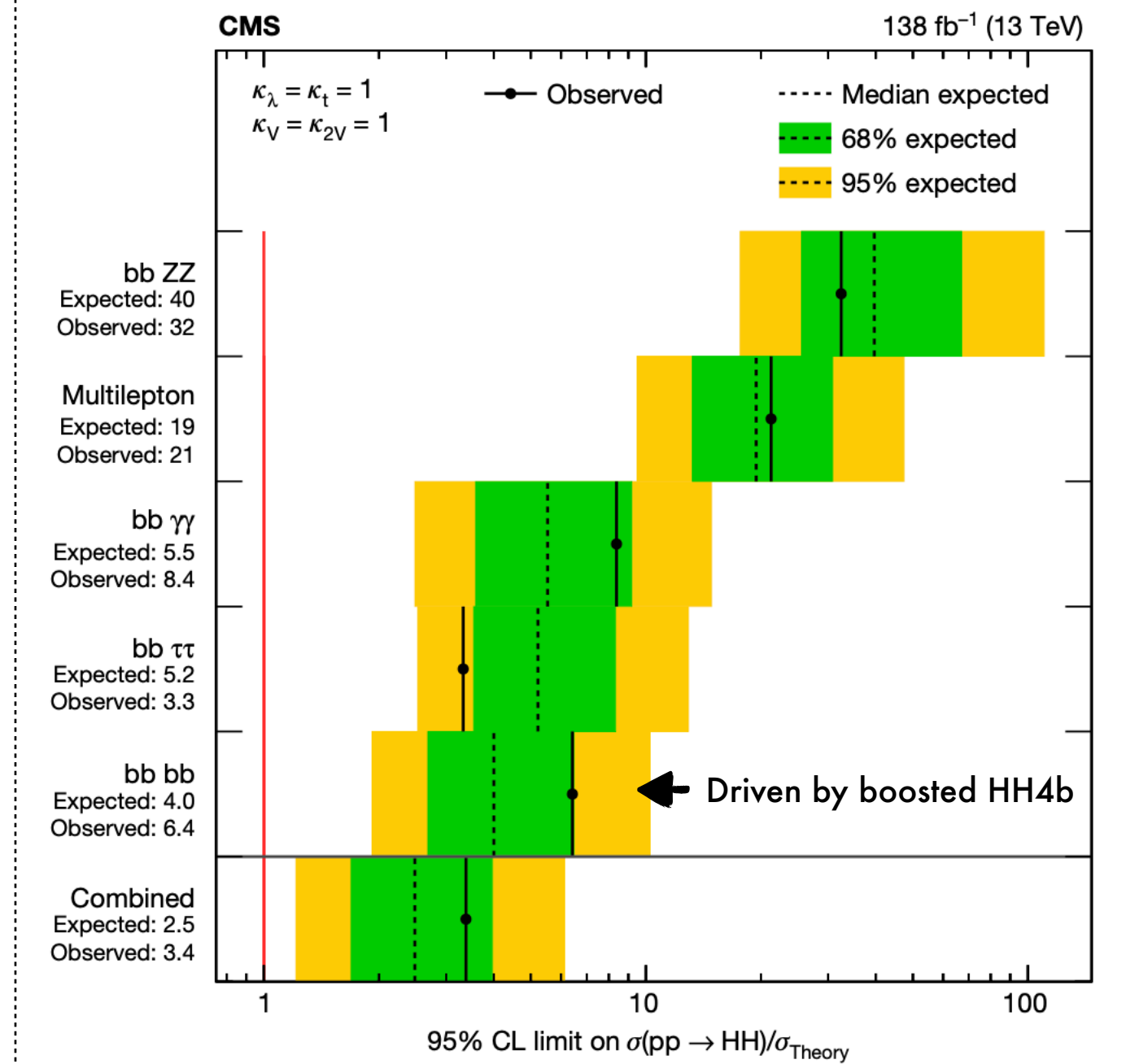


Boosted HH4b



HH combination

MS

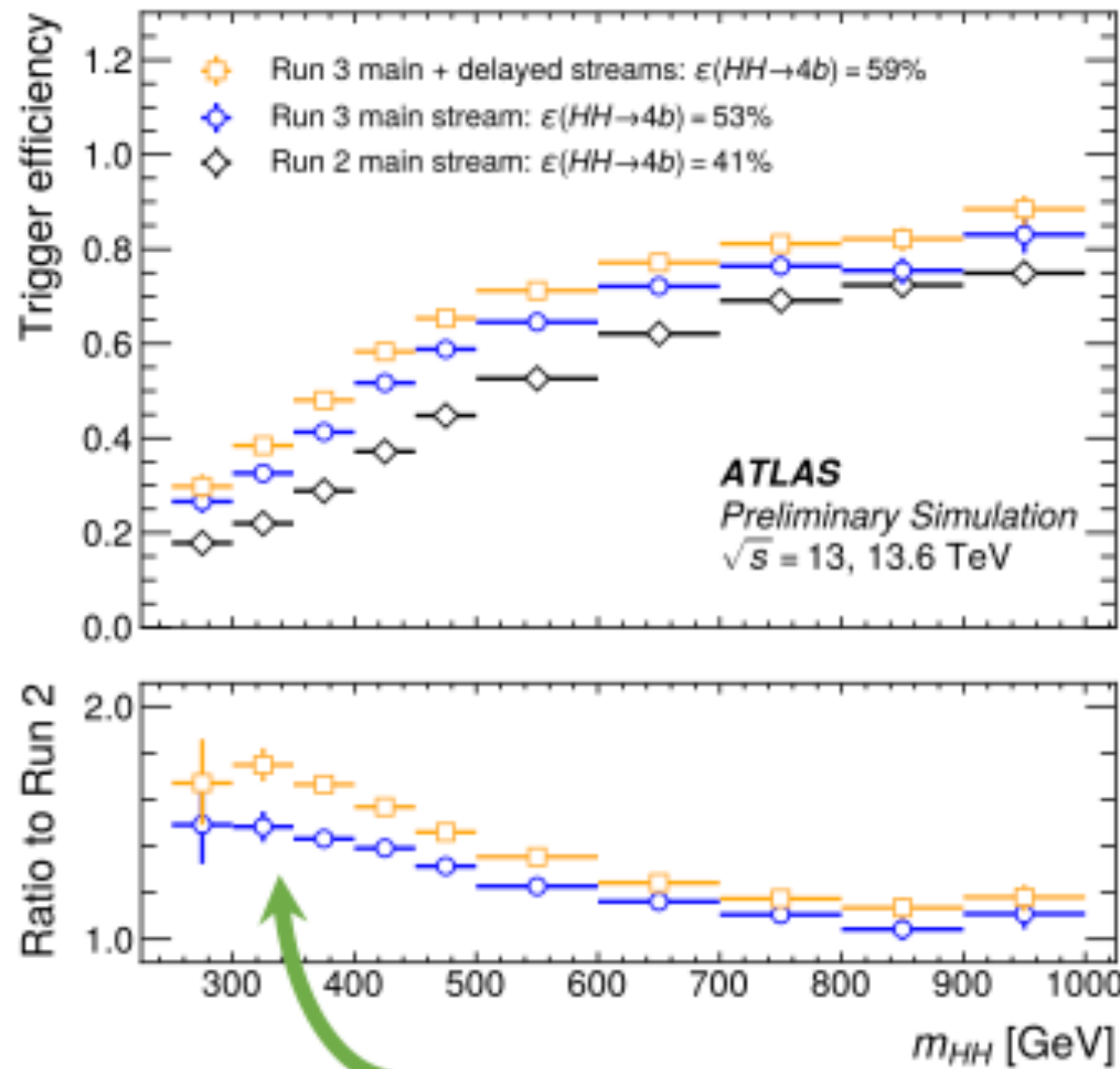


Extraordinary progress in Hbb tagging:

- Boosted Higgs identification crucial for HH
 - Lower background
 - Better Higgs identification, resolution
 - Less combinatorial background
- Will play a crucial role in HHH too!

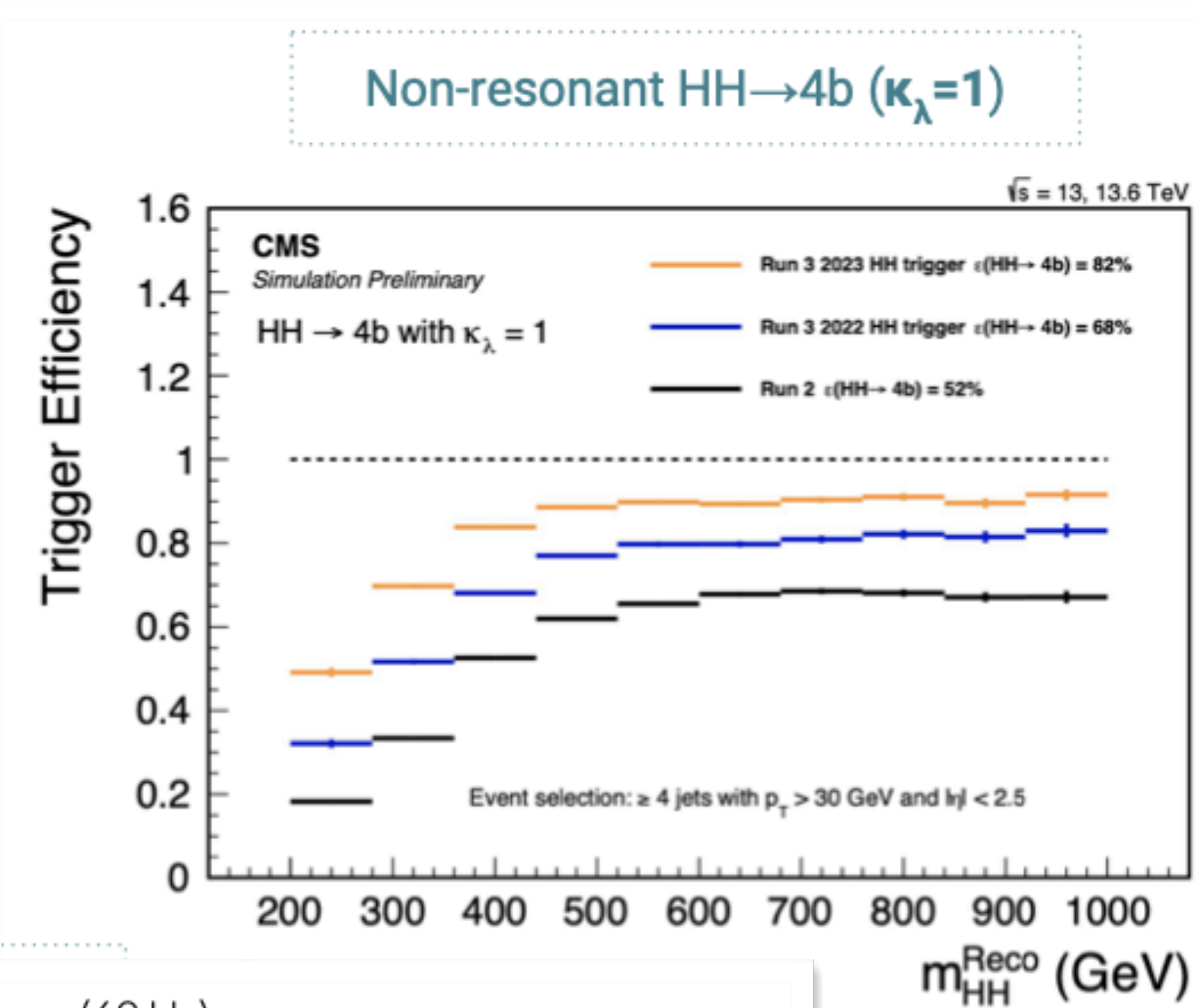
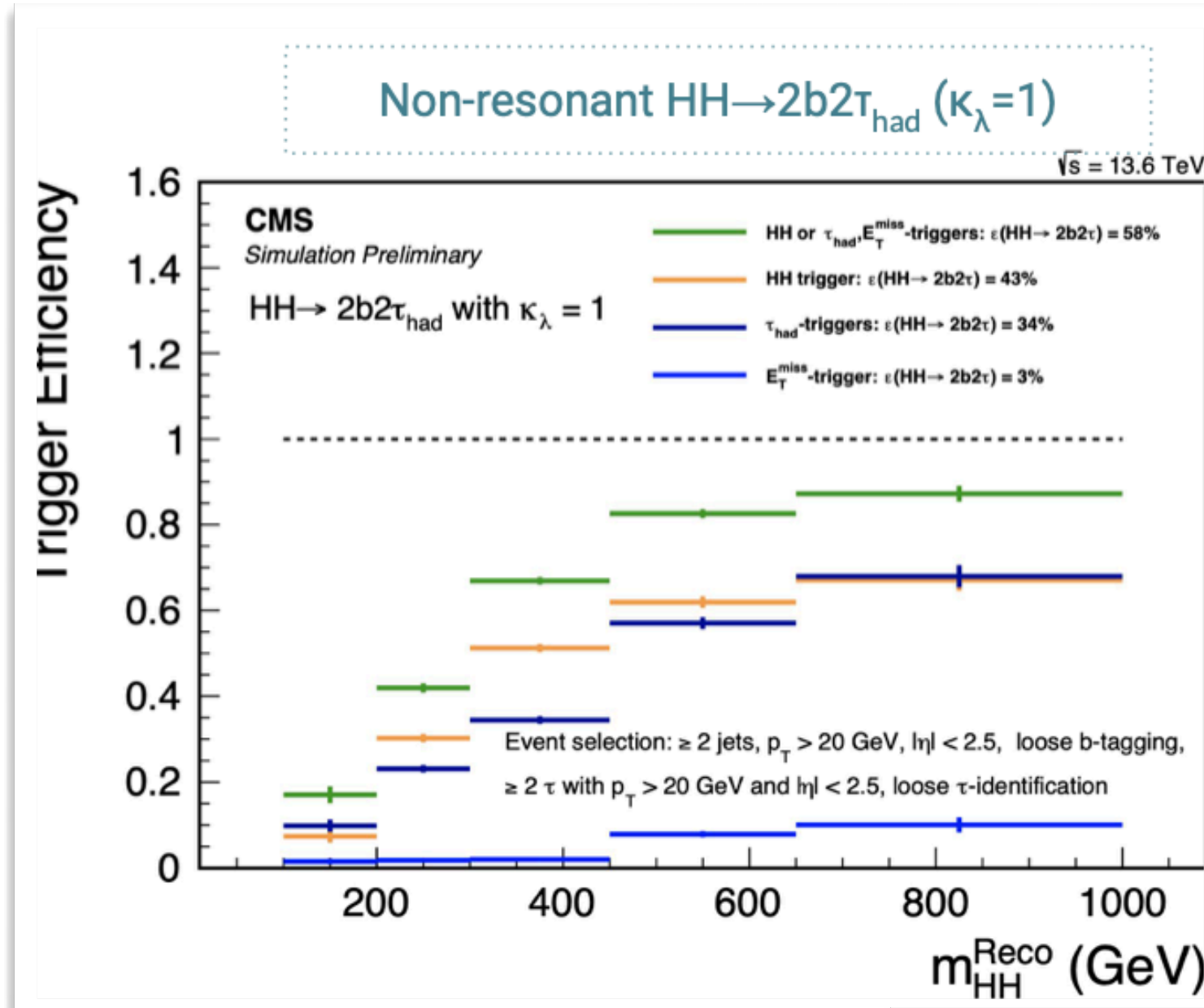
Triggers for Run 3

M. Chen



Largest improvement in the low m_{HH} region

M. Kolosova



Run 3 2022 HH trigger (60 Hz):

- L1 $H_T > 360 \text{ GeV}$
- ≥ 4 jets with $p_T > 70, 50, 40, 35 \text{ GeV}$
- 2 leading-in-ParticleNet jets have average b-disc > 0.65

Run 3 2023 HH trigger (180 Hz):

- L1 $H_T > 280 \text{ GeV}$
- ≥ 4 jets with $p_T > 30 \text{ GeV}$
- 2 leading-in-ParticleNet jets have average b-disc > 0.55

Data Parking

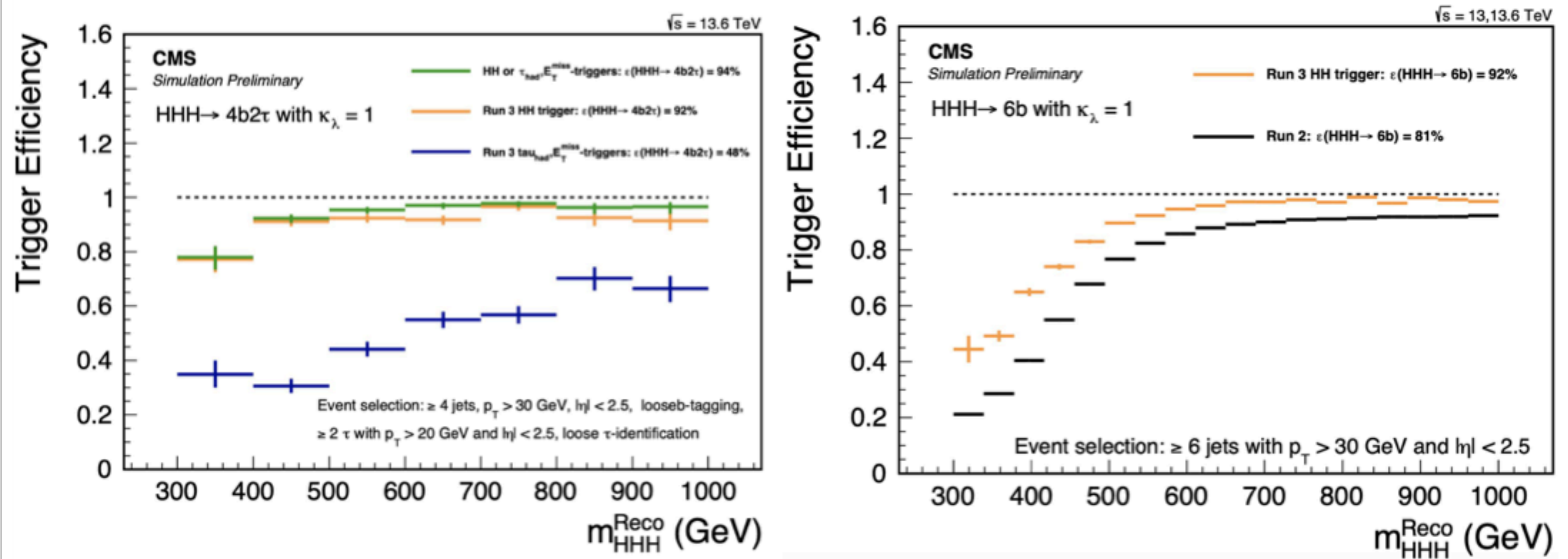
Extraordinary work on trigger by both ATLAS and CMS

- In 2018: only **50%** of $HH4b$ events produced recorded
- With latest improvements in taggers:
 - Up to 80-90% of events will recorded in all channels!

Triggers for Run 3: targeting HHH too

M. Kolosova

Same trigger(s) can be used in the search for triple Higgs production in the $4b2\tau_{\text{had}}$ and $6b$ final states, achieving **94%** and **92%** overall efficiency, respectively!



New trigger strategy benefitting from taggers and additional HLT rate: highly optimal for HHH

Attention networks

HHH reconstruction

Graph networks

SPA-Net Output

Inputs: 50
10 jets
pT, Eta, cos(Phi),
sin(phi), b-tagging



- H1 assignment probability (10x10 matrix)
- H2 assignment probability (10x10 matrix)
- H3 assignment probability (10x10 matrix)
- H1 detection probability (Float number)
- H2 detection probability (Float number)
- H3 detection probability (Float number)

Inputs: start from signal samples HHH used for analysis
• Inputs: 10 AK5 jets with pT, eta, phi, b-tagging, mass

Advantages of SPANET:

- Exploit kinematic information of all jets (not just 6)
- Dynamical: each event has a different number of jets, AK8, ...
- Interesting interplay between boosted and resolved

HH4b: combinatorially easy

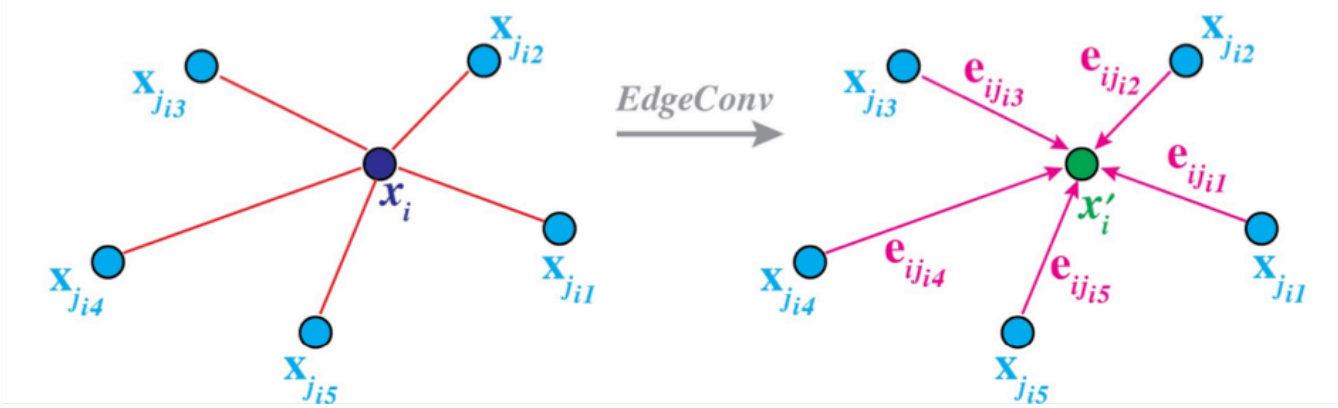
HHH6b:

- 3 Higgses with same mass!
- However, can we reconstruct them?

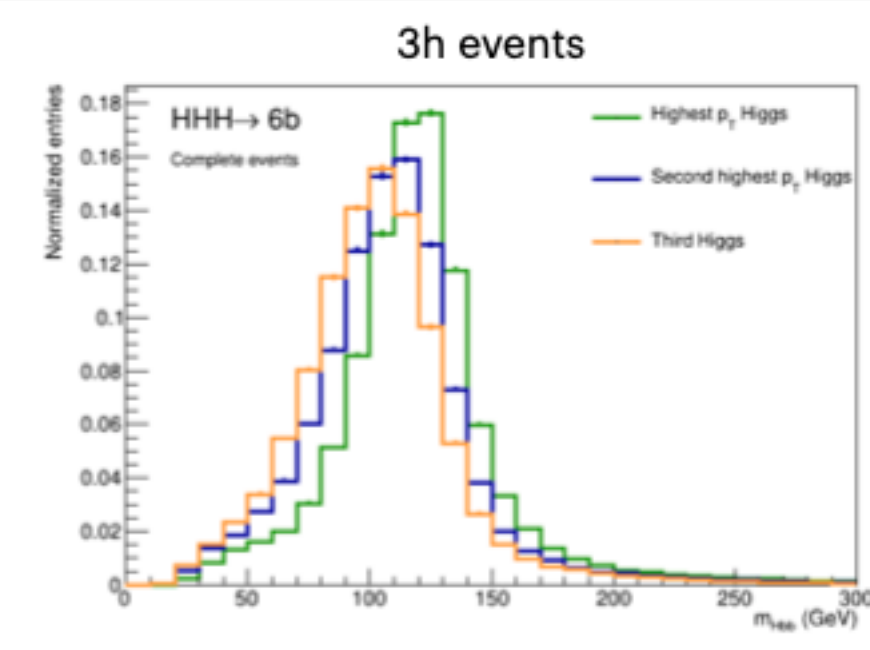
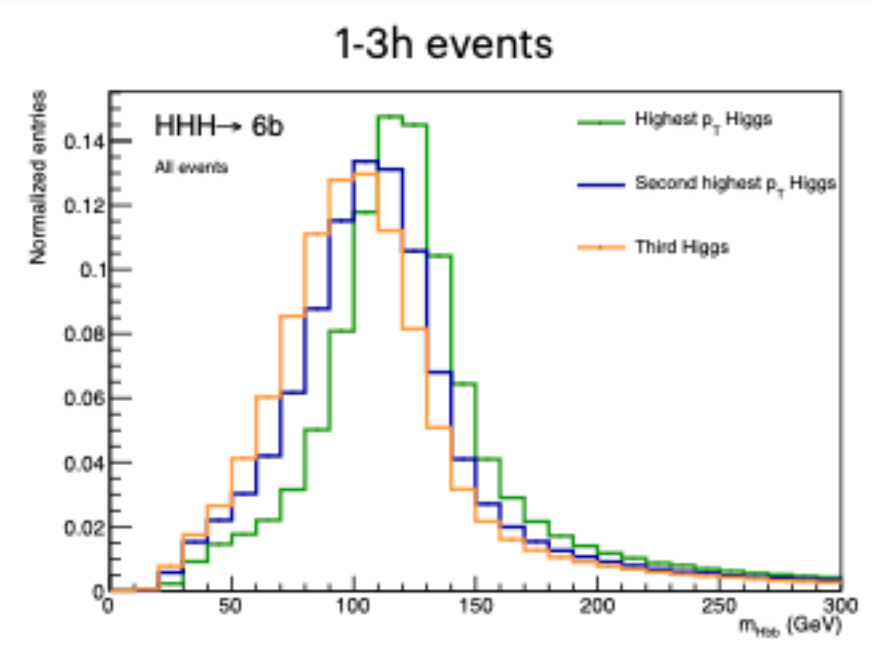
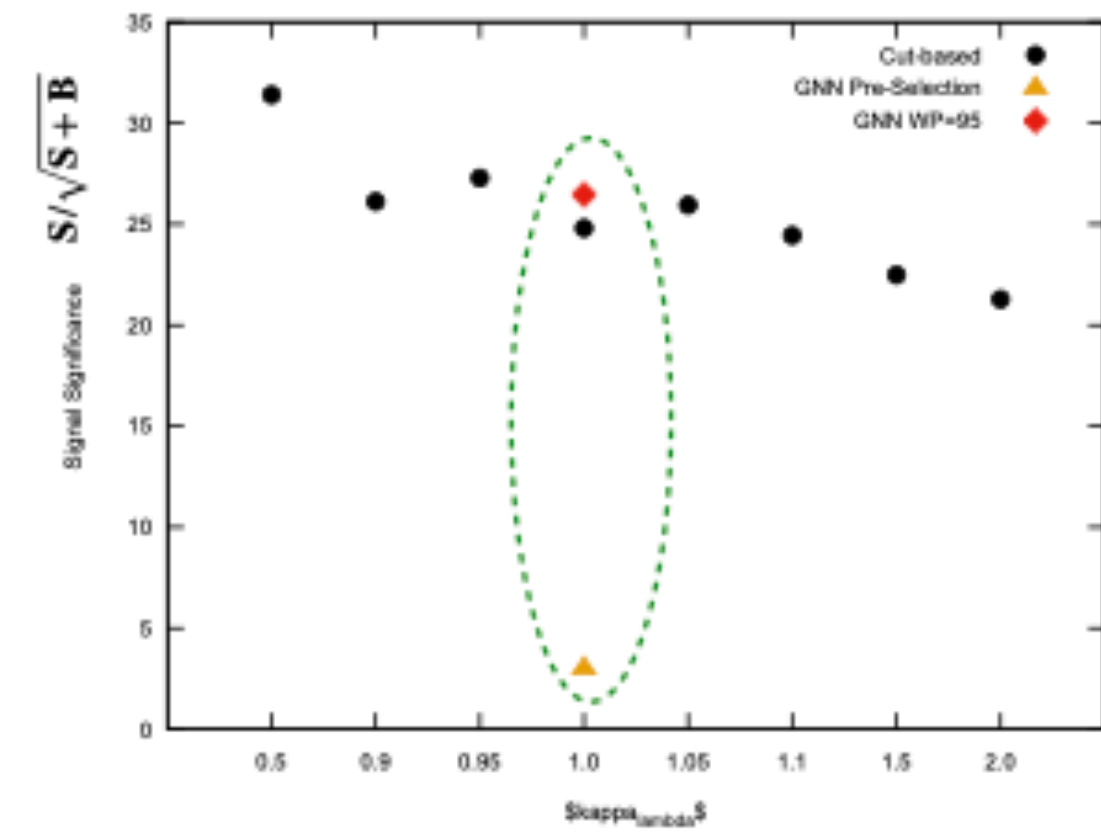
In a graph, each node can “learn” about the state of neighboring node through message passing operation

$$(x^l)_i^{l+1} = \max_{j \in \mathcal{N}(i)} \Theta_x(x_j^l - x_i^l) + \Phi_x(x_i^l)$$

$$(e^l)_i^{l+1} = \text{mean}_{j \in \mathcal{N}(i)} \Theta_e(e_j^l - e_i^l) + \Phi_e(e_i^l)$$



H purity	1-3h		3h	
	Chi2 baseline	SPA-Net	Chi2 baseline	SPA-Net
6 jets	46.3%	53.4% (+15%)	64.1%	67.8% (+6%)
7 jets	40.2%	53.3% (+33%)	47.0%	61.9% (+32%)
>= 8 jets	33.8%	49.8% (+47%)	36.4%	54.2% (+49%)
Full	38.6%	51.7% (+33%)	43.1%	58.2% (+35%)



- ✓ For multi-b final states event level classifiers are capable of increasing sensitivity
- ✓ These preliminary studies (for FCC-hh) are generalizable across hh or hhh searches
- ✓ Compared two different GNN models : probably a general GNN will do the required job.
- ✓ The individual tagging score and pairing scores should improve the sensitivity.

Strategy discussions

[G. Landsberg](#)

Branching Fractions

- $H(bb) = 58.1\%$, $H(\tau\tau) = 6.26\%$, $H(WW) = 21.5\%$, $H(gg) = 8.18\%$, $H(ZZ) = 2.6\%$, $H(\gamma\gamma) = 0.23\%$
- $\sigma_{HHH}(14 \text{ TeV, NNLO}) = 0.1 \text{ fb}$
- Aim at $\sigma^{95} = 100 \times \sigma_{HHH} = 10 \text{ fb}$; Run 2 $\times \sigma^{95} \sim 1000$ events; Run 2 $\times \sigma^{95} \times \epsilon \sim 100$ events
- To set a limit, need expected yield of 3 signal events: do not consider $Br < 3\%$ for now
- **HHH \rightarrow 6b: 19.5%**
- **HHH \rightarrow bbbb $\tau\tau$: 6.3%; bbbb $\tau_h\tau_h$: 2.7%**
- **HHH \rightarrow bbbbWW \rightarrow 4b4j: 9.9%**
- **HHH \rightarrow bbbb gg \rightarrow 4b2j: 8.3%**
- HHH \rightarrow bbbbWW \rightarrow 4b2j $\ell\nu$: 5.9%
- HHH \rightarrow bb $\tau\tau$ WW \rightarrow 2b2 τ 4j: 2.1%
- HHH \rightarrow bbbbWW \rightarrow 4b2 ℓ 2 ν : 0.9%
- HHH \rightarrow bb $\tau\tau\tau\tau$: 0.68%
- HHH \rightarrow bbbb $\gamma\gamma$: 0.23%



41% - Focus on these topologies: 4b + jets

N.B. 1: this is SIMPLER than $HH \rightarrow 4b$
All the techniques developed for that analysis can be reused if desired
Backgrounds by construction are order of magnitude or more lower

N.B. 2: $WW \rightarrow \ell\nu j$, while promising, doesn't have a mass peak

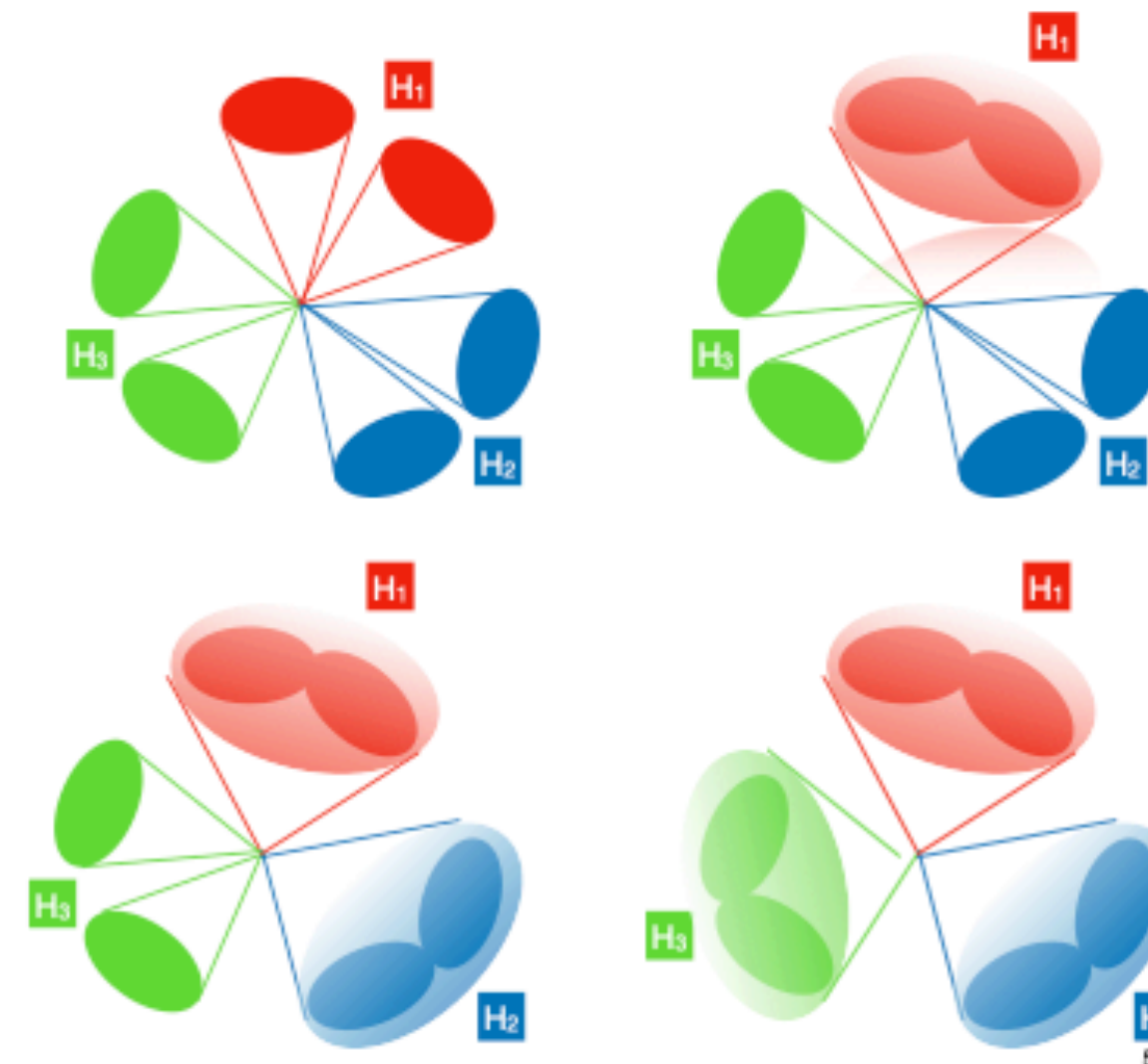
HHH:

- 41% of the cross-section accessible via fully hadronic decays
- 4b + jets

Exploit boosted topologies

- Focus on 2 Hbb to maximise the sensitivity
- Use large radius jets to simplify the pairing

Toward Merged Topologies



- Our experience: merged jet topologies offer better performance than resolved ones
 - Smaller combinatorics
 - Substructure variables are apparently more powerful than what we use in the resolved case
- Idea: why bother with resolved, fully merged, and partially merged topologies?
 - Work with CA1.5-2.0 jets and have at least two out of three Higgs boson decays merged!
 - No combinatorics, and the advantage of using jet substructure techniques!

Summary of the workshop / HHH at LHC

J. Konigsberg

Final remarks



- HHH SM prospects @ LHC

- ◆ Bleak, dim, hopeless?

- ◆ But $H \Rightarrow bb$ was thought of the same... done and done

- ◆ So was HH... and we'll get to it - promise!

- We are doing the right thing here in figuring out how

- ◆ Our knowledge & tools evolve continuously

- ◆ Workshops catalyze the process

- There is anyway [earlier/good] hope for BSM HHH

- ◆ Many opportunities for discovery

- Also, experimentally, we should just search. period.

—————▶ Hbb observed in 2018!

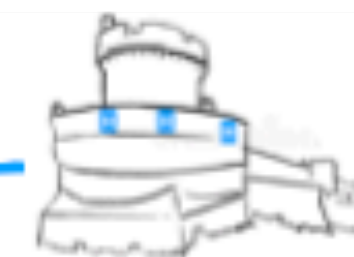
—————▶ ATLAS and CMS improving tools
to accelerate the discovery

Summary of the workshop / HHH at LHC

J. Konigsberg

- HHH SM prospects @ LHC
 - ◆ Bleak, dim, hopeless?
 - ◆ But $H \Rightarrow bb$ was thought of the same... done and done
 - ◆ So was HH... and we'll get to it - promise!
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 - ◆ Our knowledge & tools evolve continuously
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- There is anyway [earlier/good] hope for BSM HHH
 - ◆ Many opportunities for discovery
- Also, experimentally, we should just search. period.

Final remarks



What's next ?



2024 ?

*City of Dubrovnik interested in HHHH workshop, please get in touch



Mark the date: HHH workshop 2024

had a very nice *HHH* workshop in Dubrovnik this year

[<https://indico.cern.ch/event/1232581/>]



⇒ da capo next year (by popular demand): ⇐
IUC, Dubrovnik, 29.-31.7.2024

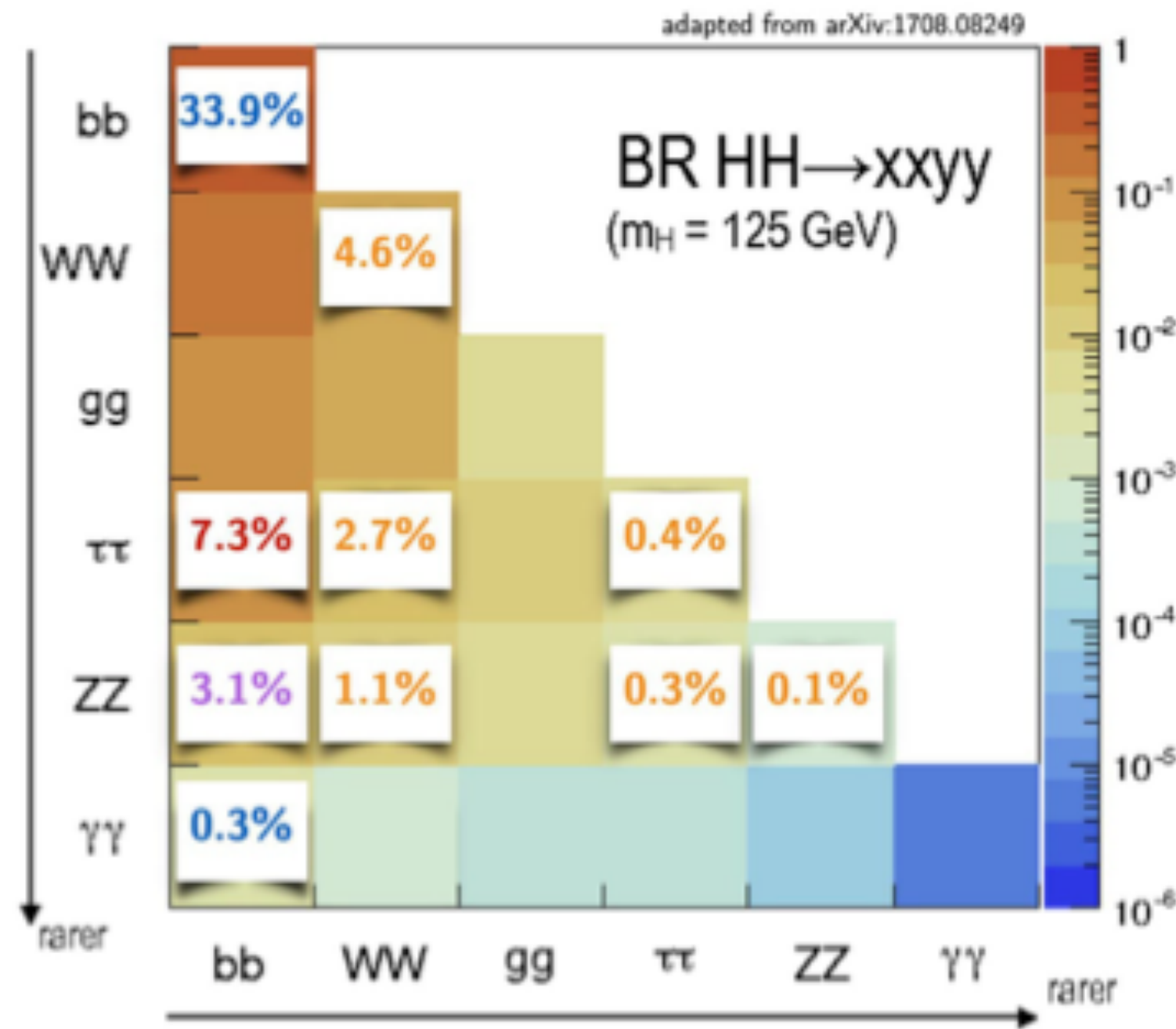
! Save the date !

Back-up

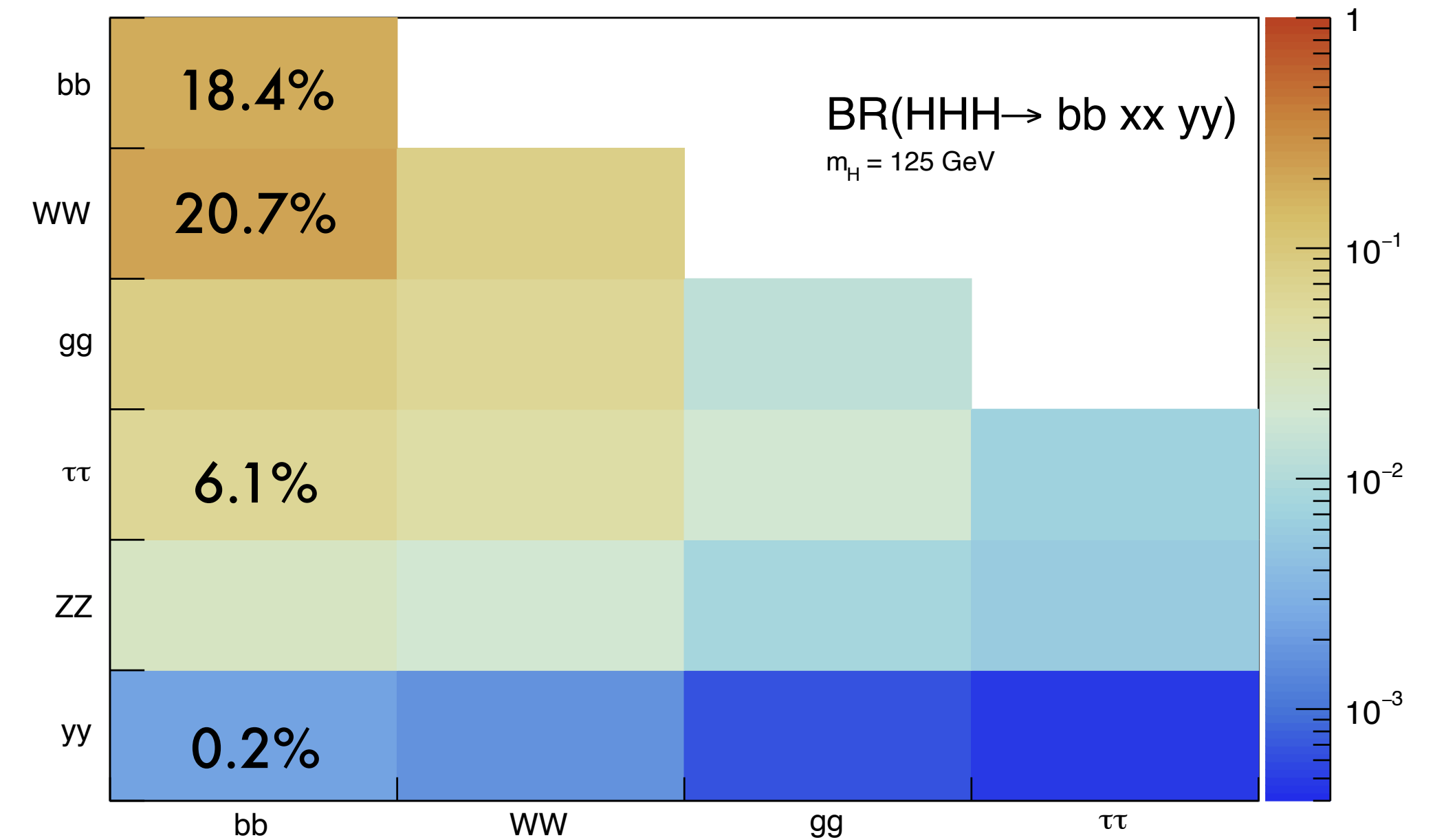
Phenomenology

Phenomenology of HH and HHH

HH branching ratio



HHH → bb XX YY branching ratio



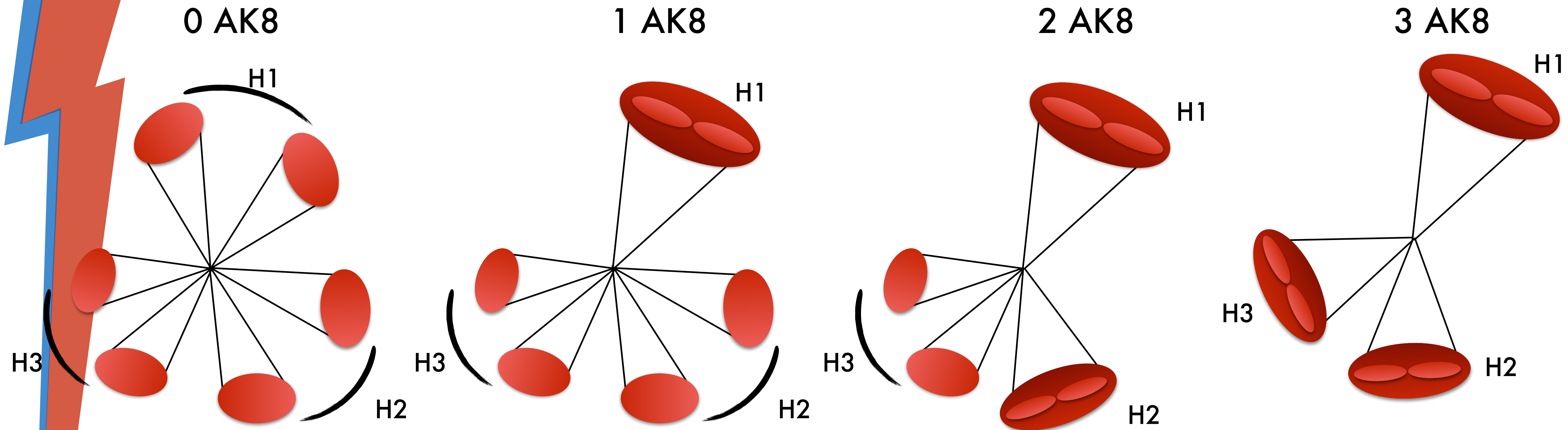
Main HH decay modes experimentally accessible:

- $HH \rightarrow 4b \Rightarrow$ largest branching ratio, challenging due to high b-jet multiplicity and QCD background
- $HH \rightarrow 2b2\tau \Rightarrow$ sizeable branching ratio, lower QCD background
- $HH \rightarrow 2b2\gamma \Rightarrow$ rare process however clean signature due to photons

$HHH \rightarrow 6b$, $HHH \rightarrow 4b2\tau$ and $HHH \rightarrow 4b2W$: approximately 45% of total cross-section!

- Similar challenges as HH with large b-jets multiplicity, what are the lessons from HH useful for HHH?
- Will focus on non-resonant HH, however main challenges and lessons similar to resonant HH

HHH6b: analysis strategy



Non-resonant HHH6b process: $\sigma(\text{HHH}) \times \text{BR}(\text{HHH} \rightarrow 6b) \sim 0.1 \text{ fb} \times 20\%$

- Complex mixing between resolved and boosted reconstruction
- Interesting mixing of resolved versus boosted topologies
 - Exploit kinematics