Explore Proton's Quark/Gluon Structure without Breaking it

☐ Challenges:

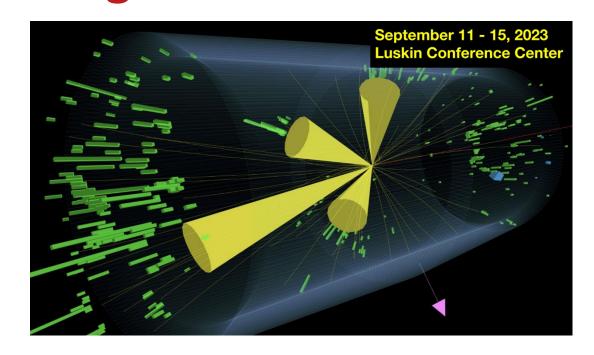
Seeing quarks and gluons without breaking the hadron

□ Factorization:

Imaging the spatial distributions of quarks and gluons inside a bound hadron with controllable approximations



Pixelating the hadron in terms of probabilities to find quarks and gluons in slices of the momentum fraction x



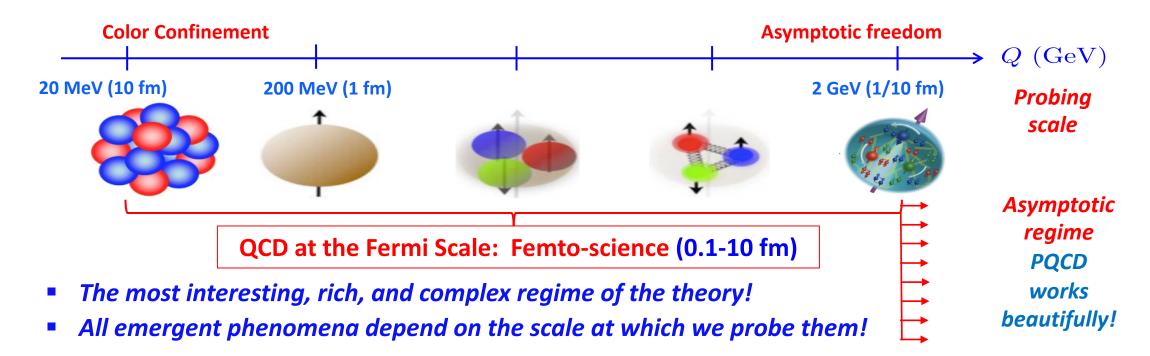


Jianwei Qiu Jefferson Lab, Theory Center



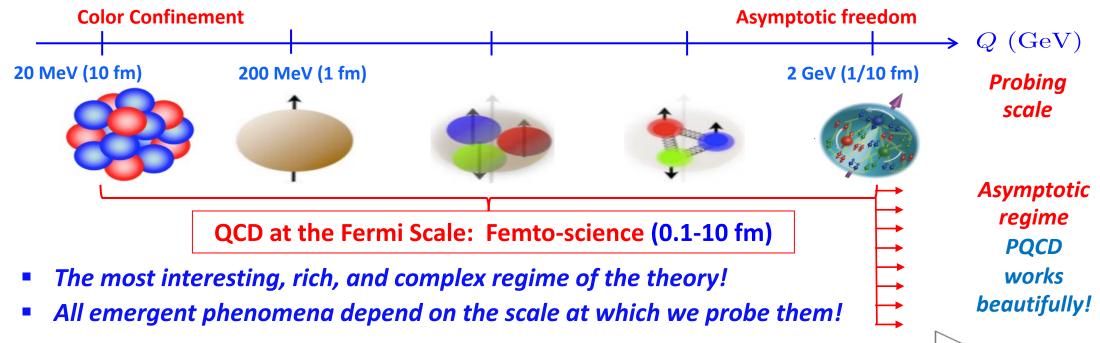


QCD Landscape of Nucleons and Nuclei





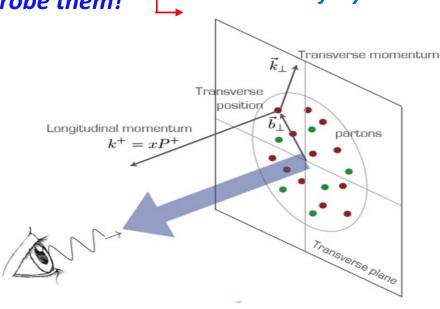
QCD Landscape of Nucleons and Nuclei



■ Need new observables with two distinctive scales:

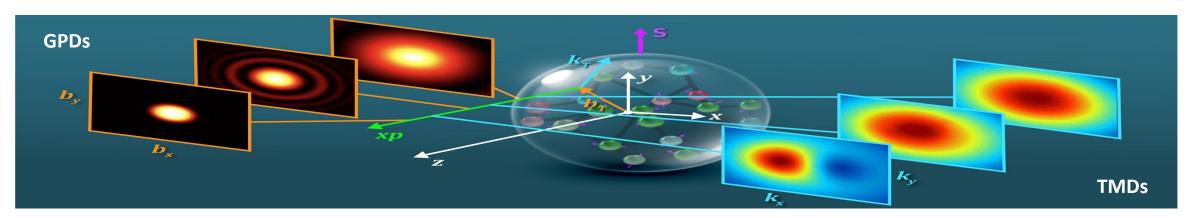
$$Q_1 \gg Q_2 \sim 1/R \sim \Lambda_{\rm QCD}$$

- Hard scale: Q_1 to localize the probe to see the particle nature of quarks/gluons
- "Soft" scale: Q_2 to be more sensitive to the emergent regime of hadron structure ~ 1/fm



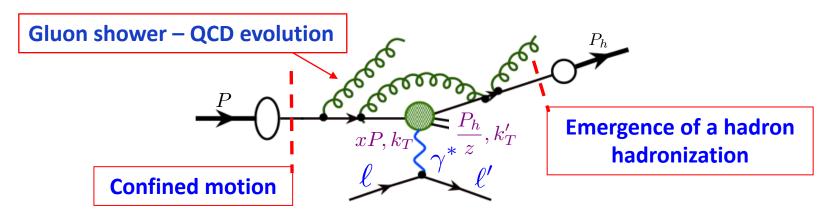
"See" Internal Structure of Hadron without seeing quarks/gluons?

☐ 3D hadron structure:



NO quarks and gluons can be seen in isolation!

☐ If the nucleon is broken, e.g., in SIDIS, ...

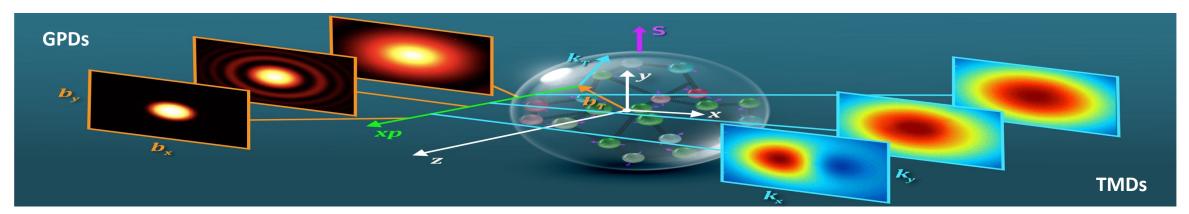


- Measured k_T is NOT the same as k_T of the confined motion!
- Too larger Q² could weaken our precision to probe the true hadron structure!



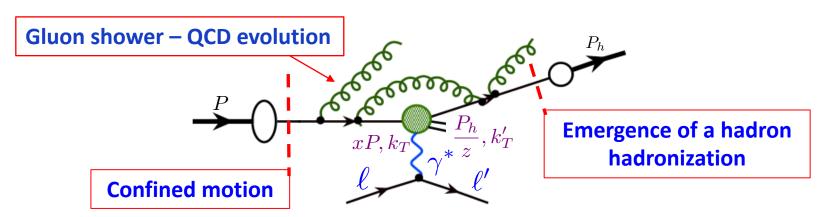
"See" Internal Structure of Hadron without seeing quarks/gluons?

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Transverse momentum Broadening from the shower:

$$\Delta k_T^2 \propto \Lambda_{\text{QCD}}^2$$

$$\times \alpha_s(C_F, C_A)$$

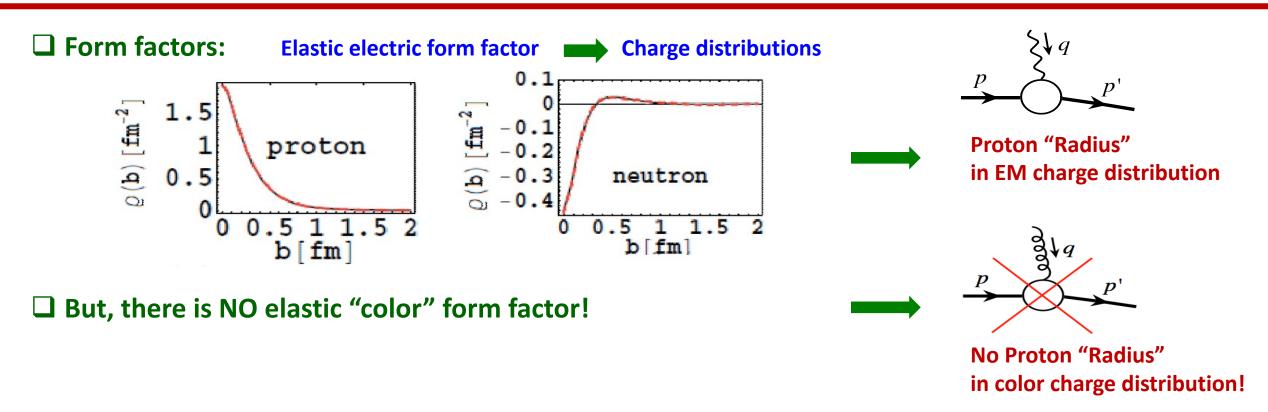
$$\times \log(Q^2/\Lambda_{\text{QCD}}^2)$$

$$\times \log(s/Q^2)$$

Structure information can be diluted by the collision induced shower!



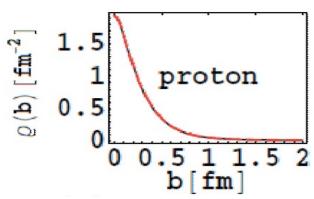
Challenges for Exploring Internal Structure of Hadron without Breaking it

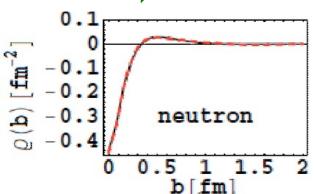


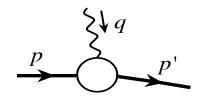


Challenges for Exploring Internal Structure of Hadron without Breaking it

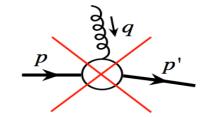
☐ Form factors: Elastic electric form factor ← Charge distributions







Proton "Radius" in EM charge distribution



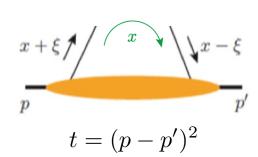
No Proton "Radius" in color charge distribution!

- ☐ But, there is NO elastic "color" form factor!
- ☐ 3D hadron tomography:

Generalized "form factor" for quark and gluon "density" distribution Generalized PDFs (GPDs) – without breaking the proton

$$F_{q/h}(x,\xi,t)$$
 skewness $\xi = \frac{(p-p')^+}{(p+p')^+}$ $t = (p-p')^2$

F.T. to get spatial distribution of quark/gluon density, quark/gluon correlations, ...





Generalized Parton Distributions (GPDs)

□ Definition:

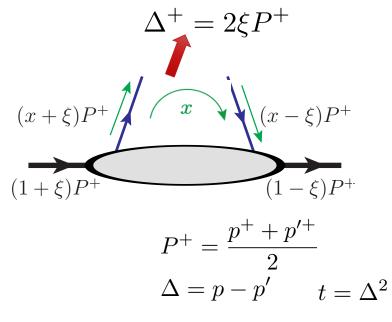
$$F^{q}(x,\xi,t) = \int \frac{\mathrm{d}z^{-}}{4\pi} e^{-ixP^{+}z^{-}} \langle p' | \bar{q}(z^{-}/2) \gamma^{+} q(-z^{-}/2) | p \rangle$$

$$= \frac{1}{2P^{+}} \left[H^{q}(x,\xi,t) \, \bar{u}(p') \, \gamma^{+} u(p) - E^{q}(x,\xi,t) \, \bar{u}(p') \, \frac{i\sigma^{+\alpha}\Delta_{\alpha}}{2m} u(p) \right],$$

$$\tilde{F}^{q}(x,\xi,t) = \int \frac{\mathrm{d}z^{-}}{4\pi} e^{-ixP^{+}z^{-}} \langle p' | \bar{q}(z^{-}/2) \gamma^{+} \gamma_{5} q(-z^{-}/2) | p \rangle$$

$$= \frac{1}{2P^{+}} \left[\tilde{H}^{q}(x,\xi,t) \, \bar{u}(p') \, \gamma^{+} \gamma_{5} u(p) - \tilde{E}^{q}(x,\xi,t) \, \bar{u}(p') \, \frac{\gamma_{5}\Delta^{+}}{2m} u(p) \right].$$

D. Müller, D. Robaschik, B. Geyer, F.-M. Dittes, J. Hořejši, *Fortsch. Phys.* 42 (1994) 101



Similar definition for gluon GPDs



Generalized Parton Distributions (GPDs)

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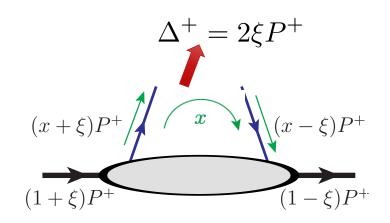
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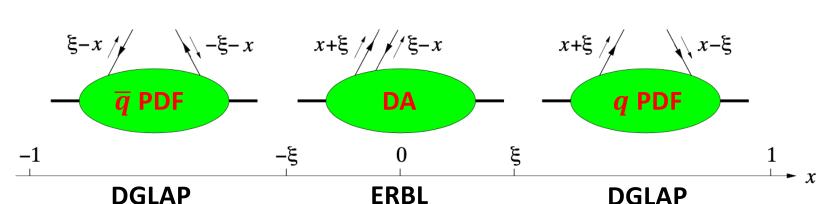


Combine <u>PDF</u> and <u>Distribution Amplitude (DA):</u>

Forward limit
$$\xi = t = 0$$
: $H^q(x,0,0) = q(x)$, $\tilde{H}^q(x,0,0) = \Delta q(x)$

$$H^q(x,0,0) = q(x),$$

$$\tilde{H}^q(x,0,0) = \Delta q(x)$$



$$P^{+} = \frac{p^{+} + p^{\prime +}}{2}$$
$$\Delta = p - p^{\prime} \qquad t = \Delta^{2}$$

Similar definition for gluon GPDs



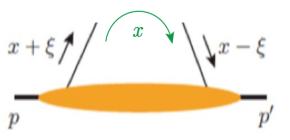
Properties of GPDs - I

☐ Impact parameter dependent parton density distribution:

$$q(x, b_{\perp}, Q) = \int d^2 \Delta_{\perp} e^{-i\Delta_{\perp} \cdot b_{\perp}} H_q(x, \xi = 0, t = -\Delta_{\perp}^2, Q)$$



Quark density in $dx d^2 b_T$



Measurement of p' fixes (t, ξ) x = momentum flow between the pair



Properties of GPDs - I

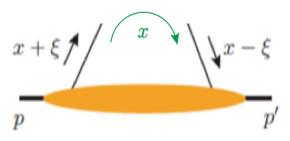
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Quark density in $dx d^2 b_T$

Tomographic image of hadron **How fast does** How far does glue glue density fall? in slice of x density spread? 0.2 0.15 0.1 Modeled by 0.05 M. Burkdart, -0.5 0.5 PRD 2000 b_{\perp} (fm)

Proton radii from quark and gluon spatial density distribution, $r_q(x)$ & $r_q(x)$



Measurement of p' fixes (t, ξ) x = momentum flow between the pair

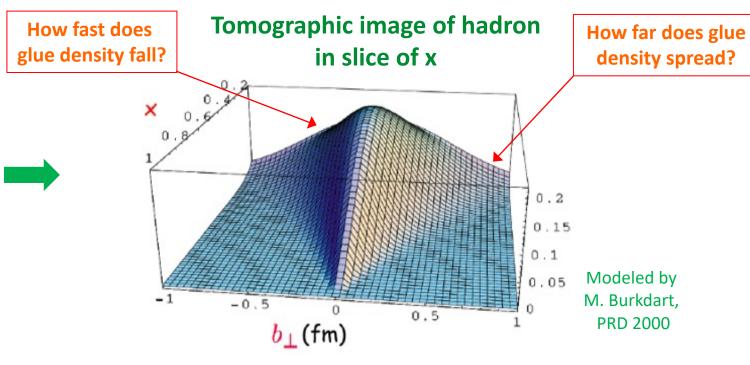


Properties of GPDs - I

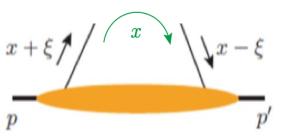
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Proton radii from quark and gluon spatial density distribution, $r_q(x)$ & $r_q(x)$



Measurement of p' fixes (t, ξ) x = momentum flow between the pair

- Should $r_q(x) > r_g(x)$, or vice versa?
- Could $r_g(x)$ saturates as $x \to 0$
- How do they compare with known radius (EM charge radius, mass radius, ...), & why?
- How the image correlate to hadron spin, ... ?
 - ... Jefferson Lab

Properties of GPDs - II

□ QCD energy-momentum tensor:

Ji, PRL78, 1997

$$T^{\mu\nu} = \sum_{i=a,a} T_i^{\mu\nu} \quad \text{with} \quad T_q^{\mu\nu} = \bar{\psi}_q \, i \gamma^{(\mu} \overleftrightarrow{D}^{\nu)} \, \psi_q - g^{\mu\nu} \bar{\psi}_q \left(i \gamma \cdot \overleftrightarrow{D} - m_q \right) \psi_q \quad \text{and} \quad T_g^{\mu\nu} = F^{a,\mu\eta} F^{a,\nu} + \frac{1}{4} g^{\mu\nu} \left(F_{\rho\eta}^a \right)^2$$

☐ "Gravitational" form factors:

$$\langle p' | T_i^{\mu\nu} | p \rangle = \bar{u}(p') \left[A_i(t) \frac{P^{\mu} P^{\nu}}{m} + J_i(t) \frac{i P^{(\mu} \sigma^{\nu) \Delta}}{2m} + D_i(t) \frac{\Delta^{\mu} \Delta^{\nu} - g^{\mu\nu} \Delta^2}{4m} + m \, \bar{c}_i(t) \, g^{\mu\nu} \right] u(p)$$

☐ Connection to GPD moments:

$$\int_{-1}^{1} dx \, x \, F_{i}(x,\xi,t) \propto \langle p'|T_{i}^{++}|p\rangle \qquad \propto \qquad \bar{u}(p') \left[\underbrace{\left(A_{i} + \xi^{2}D_{i}\right) \gamma^{+} + \left(B_{i} - \xi^{2}D_{i}\right) \frac{i\sigma^{+\Delta}}{2m}} \right] u(p)$$

$$\int_{-1}^{1} dx \, x \, H_{i}(x,\xi,t) \qquad \int_{-1}^{1} dx \, x \, E_{i}(x,\xi,t)$$

☐ Angular momentum sum rule:

i = q, g

$$J_i = \lim_{t \to 0} \int_{-1}^1 dx \, x \left[H_i(x, \xi, t) + E_i(x, \xi, t) \right]$$

3D tomography
Relation to GFF
Angular Momentum



 $C_i(t) \leftrightarrow D_i(t)/4$

Related to pressure & stress force inside h

Polyakov, schweitzer, Inntt. J. Mod. Phys. A33, 1830025 (2018) Burkert, Elouadrhiri, Girod Nature 557, 396 (2018)

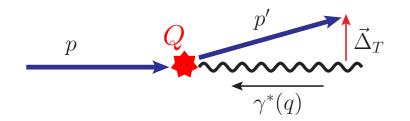
x-dependence of GPDs!



Need to know the x-dependence of GPDs to construct the proper moments!

Exclusive Diffractive Processes for Extracting GPDs

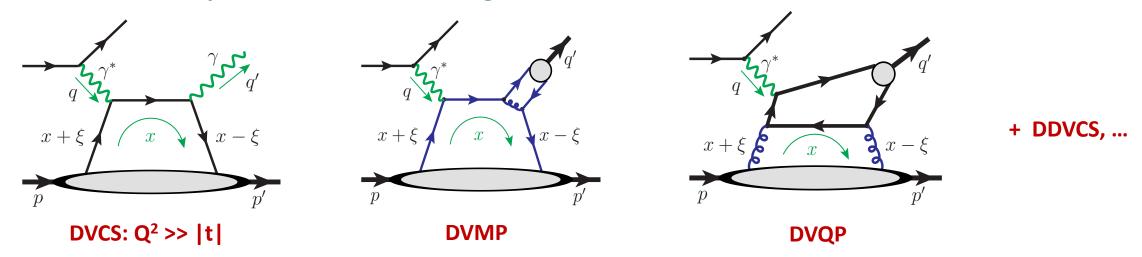
 \Box Hit the proton hard without breaking it \Rightarrow Diffractive scattering to keep proton intact



HERA discovery:

~ 10-15% of HERA events with the Proton stayed intact

☐ Known exclusive processes for extracting GPDs:



Feature: Two-scale observables

$$Q^2 \gg |t|$$

$$Q^2 \gg |t| \qquad t = (p - p')^2$$

- Hard scale Q: allows pQCD, factorization
- Low scale *t*: probes non-pert. hadron structure

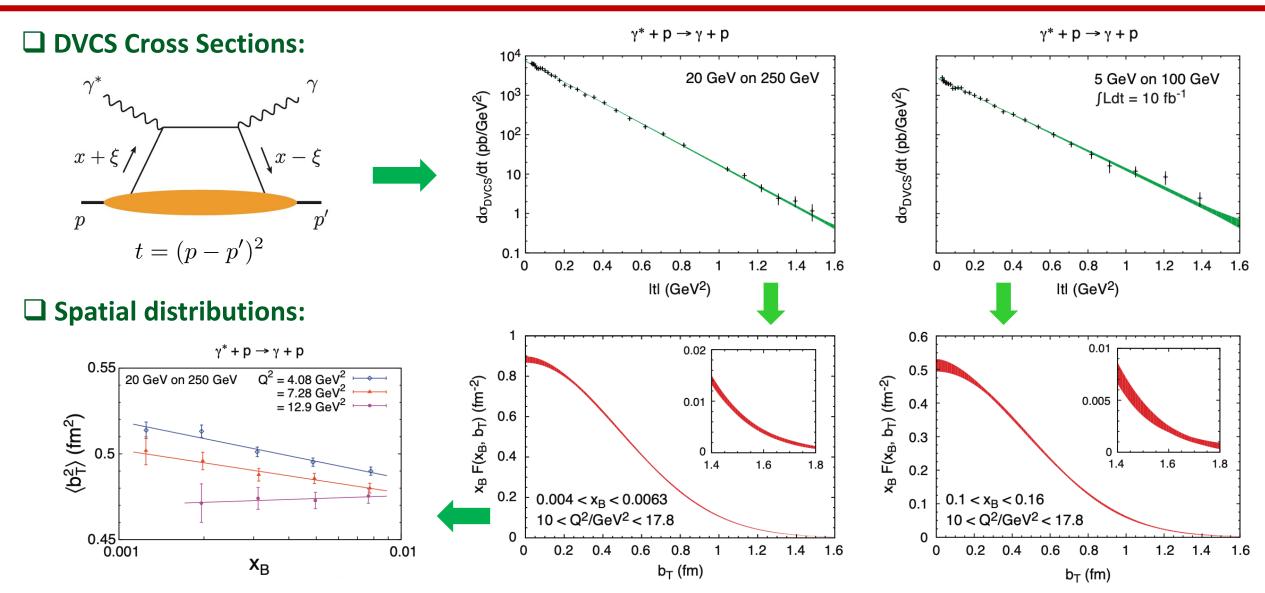


GPDs: $f_{i/h}(x,\xi,t;\mu)$





Imaging the quarks at a Future EIC (White Paper)

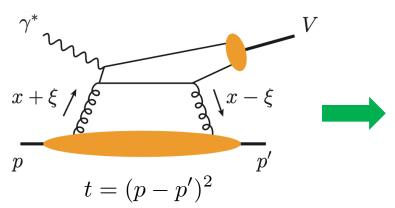


Effective "proton radius" in terms of quark distributions as a function of x_B

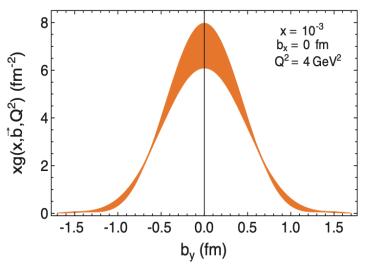


Imaging the gluons at the EIC (White Paper)

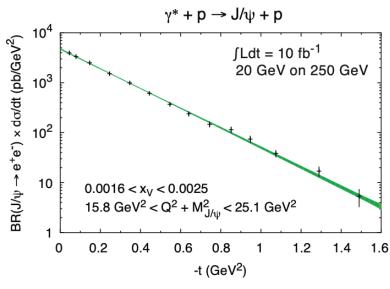
☐ Exclusive vector meson production:

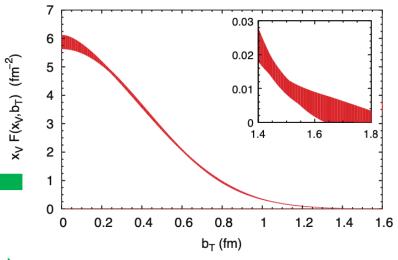


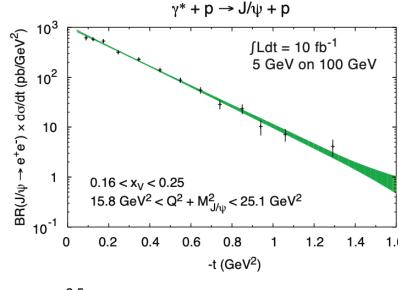
☐ Spatial distributions:

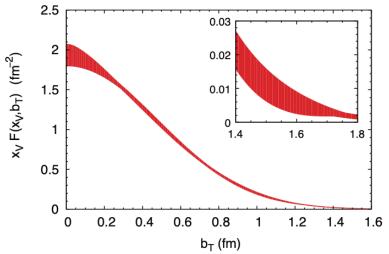


The b_T space density for gluons







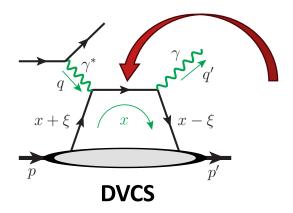


"proton radius" in terms of distribution of gluons



Difficult to Extract the *x*-dependence of GPDs?

\square Amplitude nature: $x \sim \text{loop momentum}$

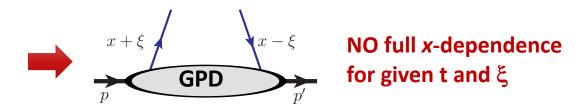


Smaller propagator = bigger amplitude

$$\propto rac{1}{x-\xi+iarepsilon}$$
PRD56 (1997) 5524
PRD58 (1998) 094018
PRD59 (1999) 074009

$$i\mathcal{M} \propto \int_{-1}^{1} d\mathbf{x} \frac{F(\mathbf{x}, \xi, t)}{\mathbf{x} - \xi + i\varepsilon} \equiv F_0(\xi, t)$$

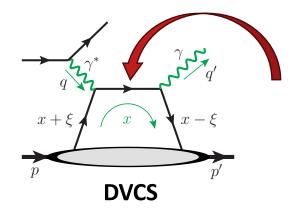
- also true for most other processes
- x-dependence is only constrained by a "moment"
- x-integration decouples from external Q²





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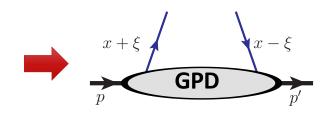
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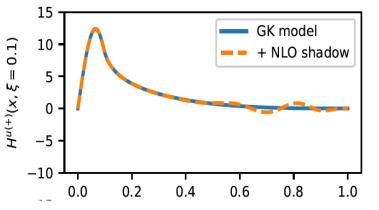


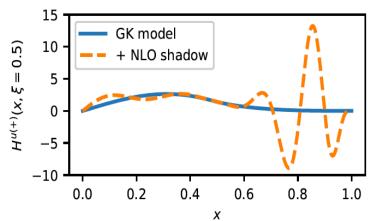
NO full x-dependence for given t and ξ

"Shadow GPDs"

PRD103 (2021) 114019

$$F(x,\xi,t) \to F(x,\xi,t) + S(x,\xi,t)$$
 with
$$\int_{-1}^{1} dx \, \frac{S(x,\xi,t)}{x-\xi+i\varepsilon} = 0$$





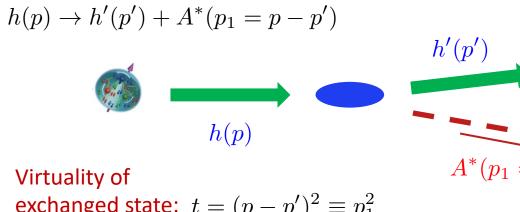
Blue and dashed Fit the same CFFs!



Diffractive $2 \rightarrow 3$ hard exclusive processes:

Qiu & Yu, JHEP 08 (2022) 103, PRD 107 (2023) 1 2305.15397 (PRL in press)

Single diffractive – keep the hadron intact:



exchanged state: $t = (p - p')^2 \equiv p_1^2$

Hard probe: $2 \rightarrow 2$ high q_T exclusive process:

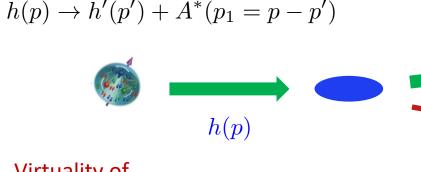
$$A^*(p_1) + B(p_2) \to C(q_1) + D(q_2)$$

Probing time: $\sim 1/|q_{1T}| \approx 1/|q_{2T}|$



- Diffractive $2 \rightarrow 3$ hard exclusive processes:
 - Single diffractive keep the hadron intact:





Virtuality of

exchanged state: $t = (p - p')^2 \equiv p_1^2$

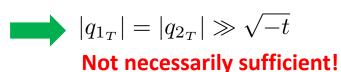


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Probing time: $\sim 1/|q_{1T}| \approx 1/|q_{2T}|$



Lifetime of $A^*(p_1)$ is much longer than collision time of the probe!



 $A^*(p_1 = p - p')$



The single diffractive $2 \rightarrow 3$ exclusive hard processes (SDHEP):

 $B(p_2) = e, \gamma, \pi$

$$h(p) + B(p_2) \to h'(p') + C(q_1) + D(q_2)$$

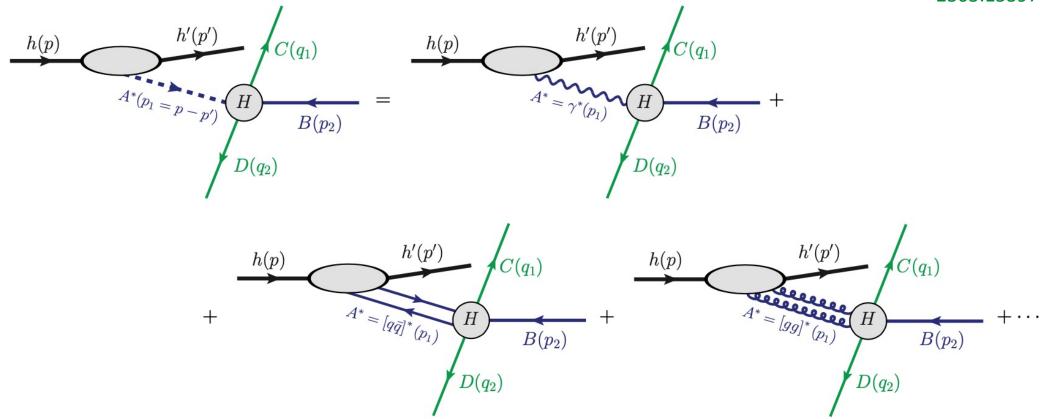
A 2-scale observable!

Qiu & Yu, JHEP 08 (2022) 103,



 \square Two-stage diffractive $2 \rightarrow 3$ hard exclusive processes:

Qiu & Yu, JHEP 08 (2022) 103, PRD 107 (2023) 1 2305.15397 (PRL in press)



The exchanged state $A^*(p-p')$ is a sum of all possible partonic states, $\sum_{n=1,2}^{\infty}$, allowed by

- Quantum numbers of h(p) h'(p')
- Symmetry of producing non-vanishing H



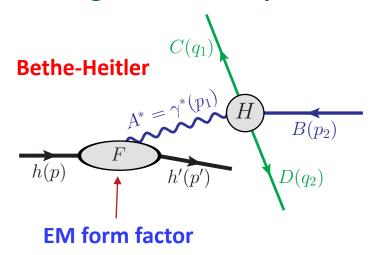
Qiu & Yu, JHEP 08 (2022) 103, Two-stage diffractive $2 \rightarrow 3$ hard exclusive processes: PRD 107 (2023) 1 **EM form factor** 2305.15397 (PRL in press) h'(p')h'(p') $C(q_1)$ $B(p_2)$ $B(p_2)$ **Bethe-Heitler-type** $D(q_2)$ \geq 3 parton connection: **Power suppressed** h'(p')h'(p')h(p)h(p)+ $B(p_2)$ $B(p_2)$ $D(q_2)$ To be factorized into GPD The exchanged state $A^*(p-p')$ is a sum of all possible partonic states,

- Quantum numbers of h(p) h'(p')
- Symmetry of producing non-vanishing *H*



Qiu & Yu, PRD 107 (2023) 1

☐ Exchange of a virtual photon — "GPD background":



$$\mathcal{M}^{(1)} = \frac{ie^2}{t} \langle h'\left(p'\right) | J^{\mu}(0) | h(p) \rangle \langle C\left(q_1\right) D\left(q_2\right) | J_{\mu}(0) | B\left(p_2\right) \rangle$$

$$\equiv \frac{ie^2}{t} F^{\mu}\left(p, p'\right) \mathcal{H}_{\mu}\left(p_1, p_2, q_1, q_2\right)$$
Leading component
$$F^{+}\mathcal{H}^{-} = \frac{1}{p_1^{+}} F^{+}\left(p_1^{+}\mathcal{H}^{-}\right) = \frac{1}{p_1^{+}} F^{+}\left(p_1 \cdot \mathcal{H} + p_{1\perp} \cdot \mathcal{H}_{\perp} - p_1^{-}\mathcal{H}^{+}\right) \sim \mathcal{O}(\sqrt{|t|})$$

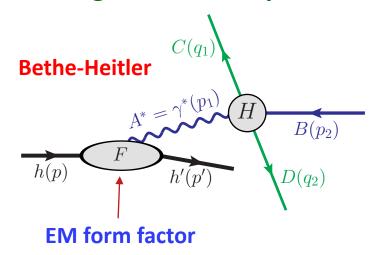
$$\mathcal{M}^{(1)} \sim \mathcal{O}(1/\sqrt{|t|})$$

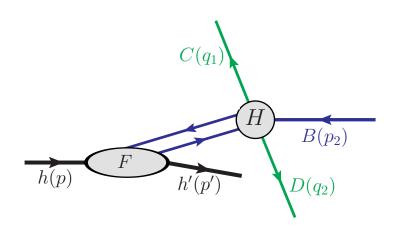


General Discussion on n=1 state: γ^*

Qiu & Yu, PRD 107 (2023) 1

☐ Exchange of a virtual photon — "GPD background":





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$$F^{+}\mathcal{H}^{-} = \frac{1}{p_1^{+}} F^{+}\left(p_1^{+}\mathcal{H}^{-}\right) = \frac{1}{p_1^{+}} F^{+}\left(p_1 \cdot \mathcal{H} + p_{1\perp} \cdot \mathcal{H}_{\perp} - p_1^{-}\mathcal{H}^{+}\right) \sim \mathcal{O}(\sqrt{|t|})$$

$$\mathcal{M}^{(1)} \sim \mathcal{O}(1/\sqrt{|t|})$$

$$\mathcal{M}^{(2)} \sim \mathcal{O}(1/Q)$$

$$\mathcal{M}^{(1)}/\mathcal{M}^{(2)} \sim \mathcal{O}(Q/\sqrt{|t|})$$

 γ^* channel is of a <u>more leading power</u> than GPD contribution, but higher power in $\alpha_{\rm EM}$

Generally allowed, except

- (1) flavor changing $(p \rightarrow n, n \rightarrow p, \text{etc.})$
- (2) forbidden by symmetry in the hard part



☐ QCD Facts:

50 years of QCD 2212.11107

Any scattering cross section with identified hadron(s) cannot be calculated fully in QCD perturbation theory



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50 years of QCD 2212.11107

- Any scattering cross section with identified hadron(s) cannot be calculated fully in QCD perturbation theory
- QCD factorization is a controllable approximation with following 3 key features:
 - All process-dependent nonperturbative contributions to factorizable cross sections are suppressed by powers of 1/(RQ), which could be neglected if the hard scale Q is sufficiently large;
 - All factorizable nonperturbative contributions are process independent, representing the characteristics of identified hadron(s); and
 - Process dependence of factorizable contributions is perturbatively calculable from partonic scattering at the short-distance.
- Predictions follow when cross sections with different hard scatterings but the same nonperturbative longdistance effect of identified hadron are compared



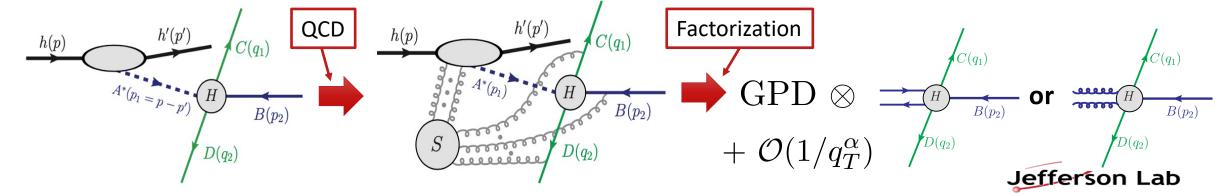
☐ QCD Facts:

26

50 years of QCD 2212.11107

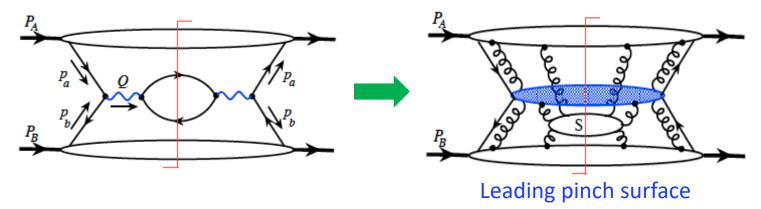
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- ☐ Factorization for 2-parton channels Very nontrivial:

Qiu & Yu, JHEP 08 (2022) 103, PRD 107 (2023) 1



Collins, Soper, Sterman 1989

☐ Lessons learned from QCD factorization for hadronic collisions (e.g., Drell-Yan):



Hard: all lines off-shell by Q

Collinear:

♦ lines collinear to A and B

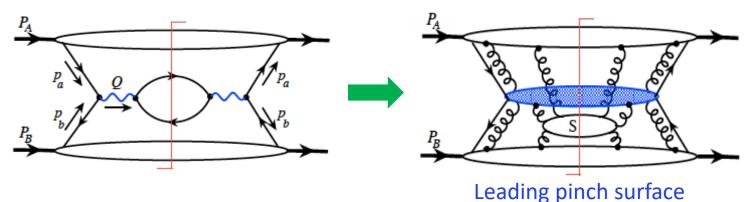
♦ One "physical parton" per hadron

Soft: all components are soft



Collins, Soper, Sterman 1989

☐ Lessons learned from QCD factorization for hadronic collisions (e.g., Drell-Yan):



☐ Collinear and longitudinally polarized gluons:

Easy to factorize:

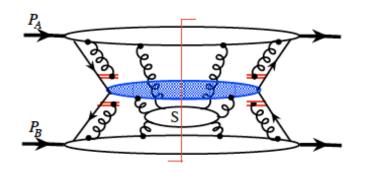
- Apply Ward Identity to decouple them from the hard part
- Reconnect them the gauge links

Hard: all lines off-shell by Q

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- ♦ lines collinear to A and B
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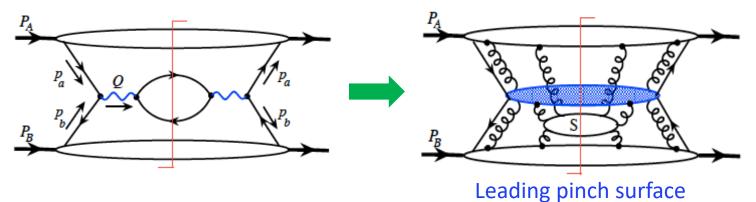
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Collins, Soper, Sterman

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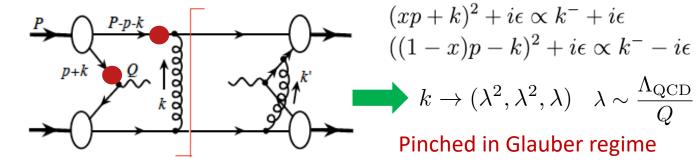


☐ Collinear and longitudinally polarized gluons:

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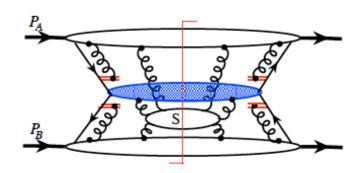


Hard: all lines off-shell by Q

Collinear:

- ♦ lines collinear to A and B
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Soft: all components are soft



Solution:

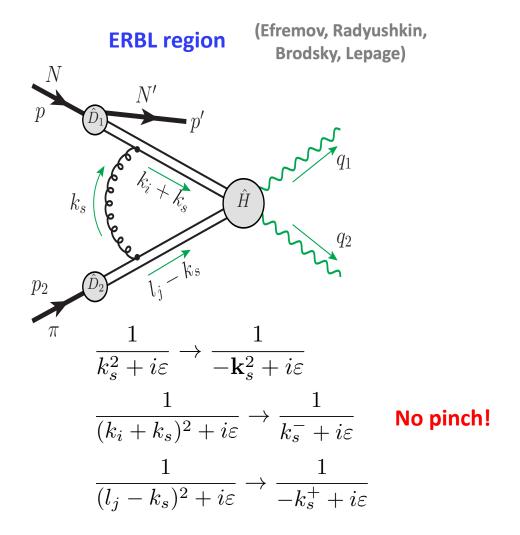
- Sum over all final states,
- Cancelation of all poles in one-half plane (remove pinches)

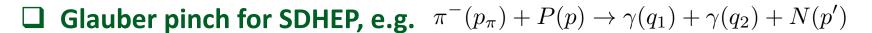
Difficulty for exclusive processes:

No final-states to sum!



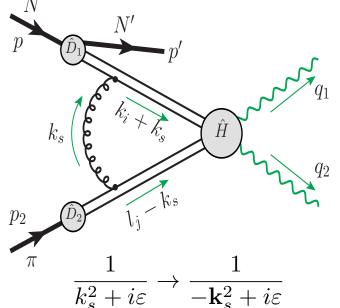
 \square Glauber pinch for SDHEP, e.g. $\pi^-(p_\pi) + P(p) \to \gamma(q_1) + \gamma(q_2) + N(p')$





 $\lambda \sim m_{\pi}/Q, \qquad Q \sim q_T$

(Efremov, Radyushkin, **ERBL** region **Brodsky**, Lepage)

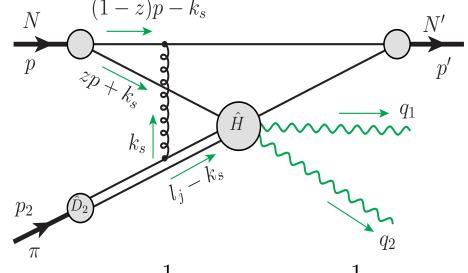


$$\frac{1}{(k_i + k_s)^2 + i\varepsilon} \to \frac{1}{k_s^- + i\varepsilon}$$

$$\frac{1}{(l_i - k_s)^2 + i\varepsilon} \to \frac{1}{-k_s^+ + i\varepsilon}$$

No pinch!

DGLAP region
$$(1-z)p-k_s$$



$$\frac{1}{((1-z)p - k_s)^2 + i\varepsilon} \to \frac{1}{k_s^- - i\varepsilon}$$

$$\frac{1}{k_s^- - i\varepsilon}$$

Pinched!

Same conclusion if k_s flows through N'!



Gluons pinched in the Glauber region: $k_s = (\lambda^2, \lambda^2, \lambda) Q$

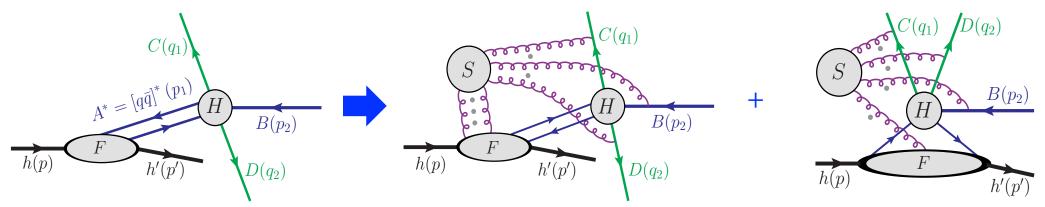




Factorization for SDHEP in the Two-stage Paradigm

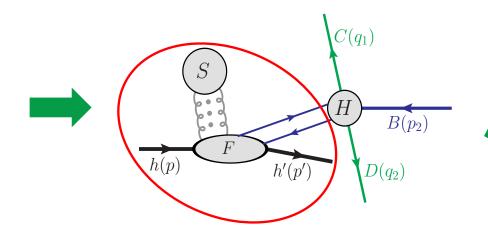
☐ Factorization for 2-parton channels (CO gluons are easy to factorize):

Qiu & Yu, JHEP 08 (2022) 103, PRD 107 (2023) 1



ERBL region: $[q\overline{q}'] \sim \text{meson}$

☐ Soft gluons cancel when coupling to color neutral hadrons:



Glauber gluons of SDHEP (only k_s^- is pinched in Glauber region):

$$k_s^+ \mapsto k_s^+ \pm i\mathcal{O}(Q) \longrightarrow k_s = (\lambda^2, \lambda^2, \lambda) \rightarrow (1, \lambda^2, \lambda)$$

 $C(q_1)$ $B(p_2)$ $B(p_2)$ $C(q_1)$ $B(p_2)$ $B(p_2)$

DGLAP region: Glauber pinch

Hard probes

Jefferson Lab

CO gluons

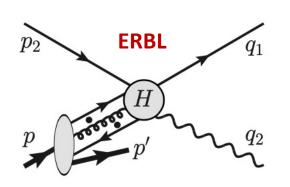
SDHEP with a Lepton Beam – JLab, EIC

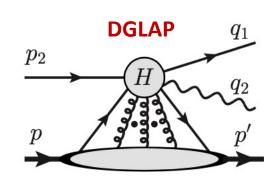
PRD56 (1997) 5524; PRD58 (1998) 094018; PRD59 (1999) 074009

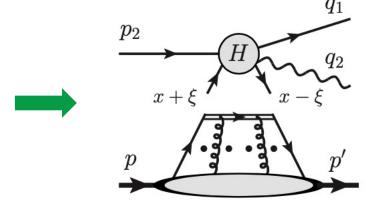
DVCS:

$$h(p) = \operatorname{Proton}(p), \ h'(p') = \operatorname{Proton}(p'), \ B(p_2) = \operatorname{electron}(p_2), \ C(q_1) = \operatorname{electron}(q_1), \ D(q_2) = \operatorname{photon}(q_2)$$

Leading pinch region:





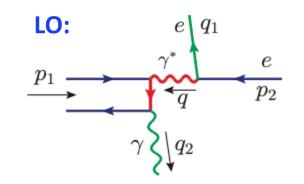


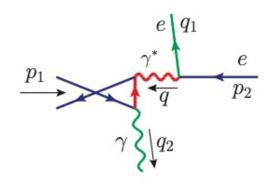
$$x = \frac{(k+k')^{+}}{(p+p')^{+}}$$
$$\xi = \frac{(p-p')^{+}}{(p+p')^{+}}$$

Factorization formula:

$$\mathcal{M}_{he \to h'e\gamma}^{(2)} = \sum_{i} \int_{-1}^{1} dx \, F_{i}^{h}(x, \xi, t) \, C_{ie \to e\gamma}(x, \xi, q_{T}),$$

$$C^{(0)} \propto \frac{1}{x - \xi + i\varepsilon} - \frac{1}{x + \xi - i\varepsilon}$$









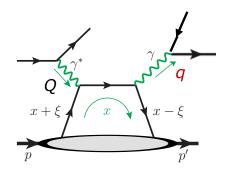
What kind of process/observable could be sensitive to the x-dependence?

☐ Create an entanglement between the internal x and an externally measured variable?

$$i\mathcal{M} \propto \int_{-1}^{1} \mathrm{d} {f x} rac{F({f x},\xi,t)}{x-x_p(\xi,{m q})+iarepsilon}$$
 Change external ${m q}$ to sample different part of ${f x}$.



$$x_p(\xi, \mathbf{q}) = \xi\left(\frac{1 - \mathbf{q}^2/Q^2}{1 + \mathbf{q}^2/Q^2}\right) \to \xi$$
 same as DVCS if $\mathbf{q} \to 0$

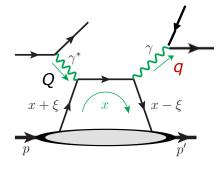




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$$i\mathcal{M} \propto \int_{-1}^1 \mathrm{d} x \frac{F(x,\xi,t)}{x-x_p(\xi,q)+i\varepsilon}$$
 Change external $extit{q}$ to sample different part of x.



Double DVCS (two scales):

$$x_p(\xi, \mathbf{q}) = \xi\left(\frac{1 - \mathbf{q}^2/Q^2}{1 + \mathbf{q}^2/Q^2}\right) \to \xi$$
 same as DVCS if $\mathbf{q} \to 0$

Production of two back-to-back high pT particles (say, two photons):

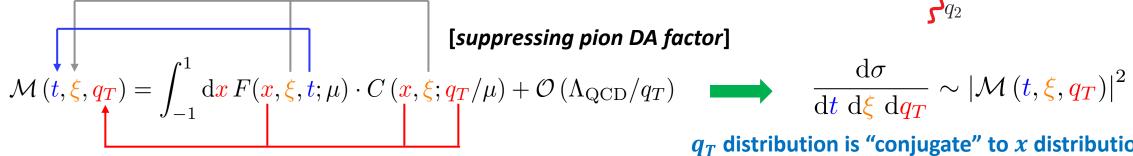
$$\pi^{-}(p_{\pi}) + P(p) \to \gamma(q_1) + \gamma(q_2) + N(p')$$

Qiu & Yu

Hard scale: $q_T\gg \Lambda_{\rm QCD}$ Soft scale: $t\sim \Lambda_{\rm QCD}^2$

JHEP 08 (2022) 103

Factorization:



[suppressing pion DA factor]

$$T$$
)

$$rac{\mathrm{d}\sigma}{\mathrm{d}t\ \mathrm{d}\xi\ \mathrm{d}q_T} \sim \left|\mathcal{M}\left(t,\xi,q_T
ight)\right|^2$$

 q_T distribution is "conjugate" to x distribution

$$x \leftrightarrow q_T$$



GPD Models for Testing the x-dependence

☐ Simplified GK models:

$$H_{pn}(x,\xi,t) = \theta(x) x^{-0.9 (t/\text{GeV}^2)} \frac{x^{\rho} (1-x)^{\tau}}{B(1+\rho,1+\tau)}$$

$$H_{pn}(x,\xi,t) = \theta(x) x^{-0.9 (t/\text{GeV}^2)} \frac{x^{\rho} (1-x)^{\tau}}{B(1+\rho,1+\tau)}$$
$$\widetilde{H}_{pn}(x,\xi,t) = \theta(x) x^{-0.45 (t/\text{GeV}^2)} \frac{1.267 x^{\rho} (1-x)^{\tau}}{B(1+\rho,1+\tau)}$$

• Neglect E, \widetilde{E} . Neglect evolution effect.

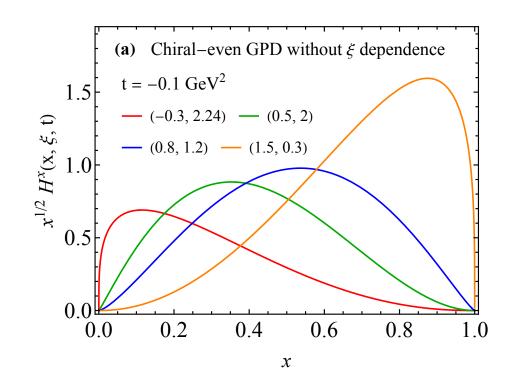
• Tune (ρ, τ) to control x shape.

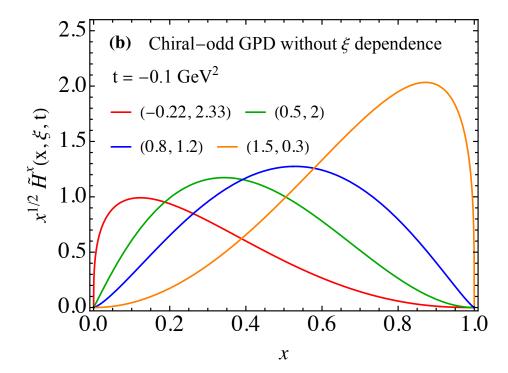
• Fix DA: $D(z) = N z^{0.63} (1-z)^{0.63}$

Goloskokov, Kroll hep-ph/0501242 arXiv: 0708.3569

arXiv: 0906.0460

Qiu & Yu, arXiv:2305.15397



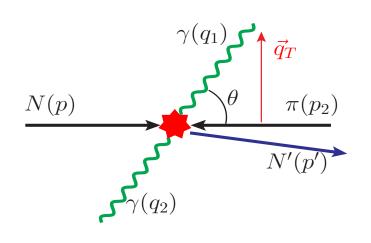




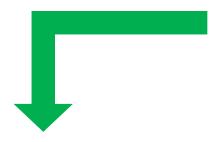
Enhanced Sensitivity on x-dependence of GPDs

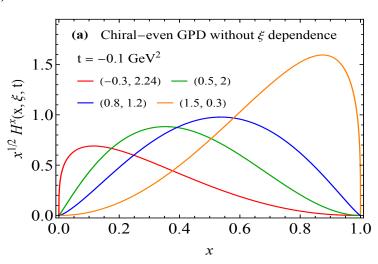
 \blacksquare Two-photon production: $\pi^-(p_\pi) + P(p) \to \gamma(q_1) + \gamma(q_2) + N(p')$ J-PARC, COMPASS

Qiu & Yu, JHEP 08 (2022) 103

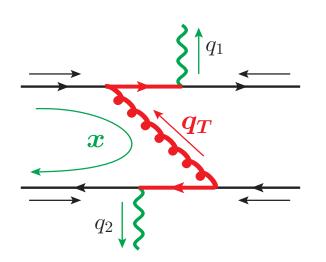


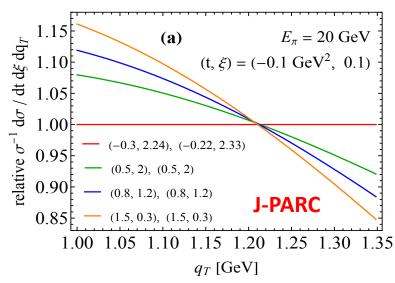


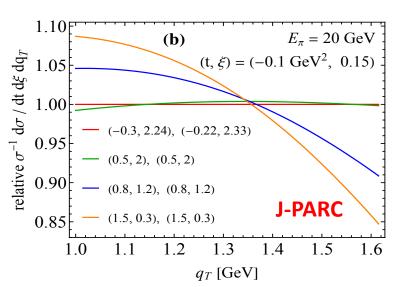






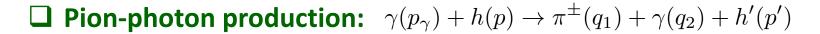




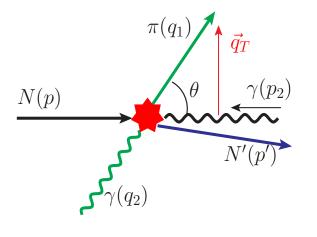




Enhanced Sensitivity on x-dependence of GPDs



JLab-Hall D, other Halls & EIC with a quasi-photon beam

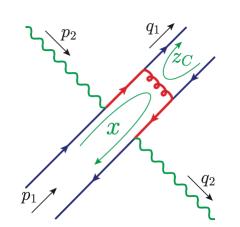


 $i\mathcal{M}$ contains the entanglement between **x** and **qT**

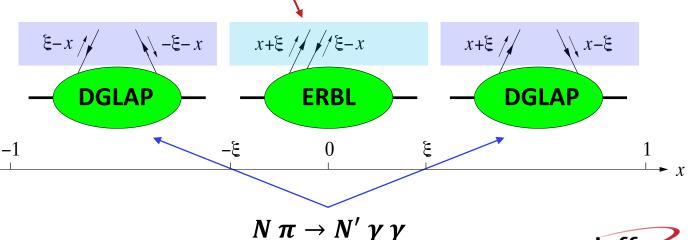
$$I'(t,\xi;z,\theta) = \int_{-1}^{1} \frac{dx F(x,\xi,t)}{x - \rho'(z;\theta) + i\epsilon}$$

Qiu & Yu, arXiv:2305.15397

$$\rho'(z;\theta) = \xi \cdot \left[\frac{\cos^2(\theta/2)(1-z) - z}{\cos^2(\theta/2)(1-z) + z} \right] \in [-\xi, \xi]$$

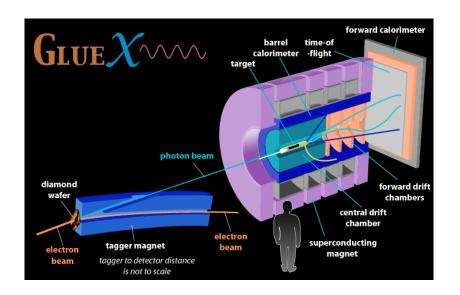


Complementary sensitivity:



Exclusive Photo-Production of a $\pi \gamma$ Pair – Hall D at JLab





☐ Polarization asymmetries

$$\frac{d\sigma}{d|t| d\xi d\cos\theta d\phi} = \frac{1}{2\pi} \frac{d\sigma}{d|t| d\xi d\cos\theta} \cdot \left[1 + \lambda_N \lambda_\gamma A_{LL} + \zeta A_{UT} \cos 2 (\phi - \phi_\gamma) + \lambda_N \zeta A_{LT} \sin 2 (\phi - \phi_\gamma)\right]$$

$$\frac{d\sigma}{d|t|\,d\xi\,d\cos\theta} = \pi \left(\alpha_e \alpha_s\right)^2 \left(\frac{C_F}{N_c}\right)^2 \frac{1-\xi^2}{\xi^2 s^3} \Sigma_{UU}$$

$$\hat{y}_{1ab} \hat{s}_{T}$$

$$\hat{z}_{1ab}$$

$$\hat{z}_{1a}$$

$$\Sigma_{UU} = |\mathcal{M}_{+}^{[\widetilde{H}]}|^{2} + |\mathcal{M}_{-}^{[\widetilde{H}]}|^{2} + |\widetilde{\mathcal{M}}_{+}^{[H]}|^{2} + |\widetilde{\mathcal{M}}_{-}^{[H]}|^{2},$$

$$A_{LL} = 2\Sigma_{UU}^{-1} \operatorname{Re} \left[\mathcal{M}_{+}^{[\widetilde{H}]} \widetilde{\mathcal{M}}_{+}^{[H]*} + \mathcal{M}_{-}^{[\widetilde{H}]} \widetilde{\mathcal{M}}_{-}^{[H]*} \right],$$

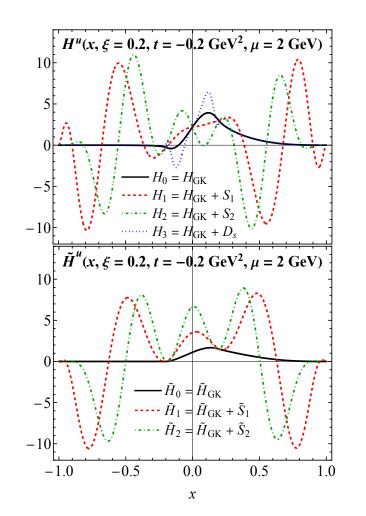
$$A_{UT} = 2\Sigma_{UU}^{-1} \operatorname{Re} \left[\widetilde{\mathcal{M}}_{+}^{[H]} \widetilde{\mathcal{M}}_{-}^{[H]*} - \mathcal{M}_{+}^{[\widetilde{H}]} \mathcal{M}_{-}^{[\widetilde{H}]*} \right],$$

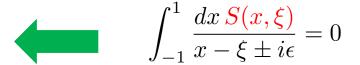
$$A_{LT} = 2\Sigma_{UU}^{-1} \operatorname{Im} \left[\mathcal{M}_{+}^{[\widetilde{H}]} \widetilde{\mathcal{M}}_{-}^{[H]*} + \mathcal{M}_{-}^{[\widetilde{H}]} \widetilde{\mathcal{M}}_{+}^{[H]*} \right].$$

Exclusive Photo-Production of a $\pi \gamma$ Pair – Hall D at JLab

☐ GPD Models:

= GK model + shadow GPDs



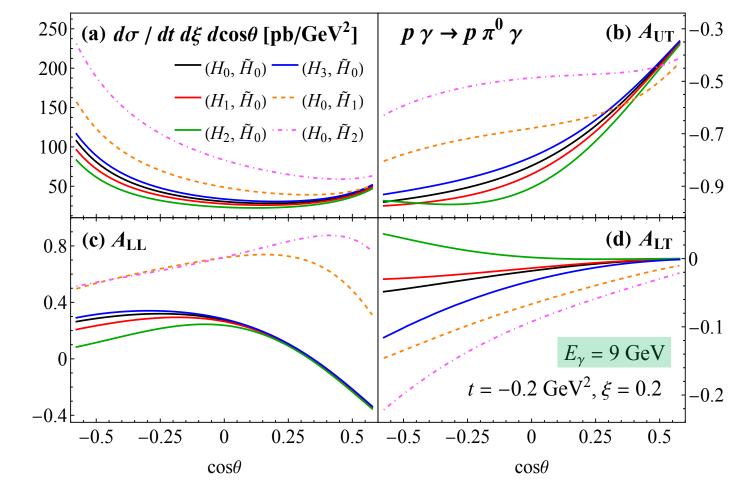


Goloskokov, Kroll, `05, `07, `09

Bertone et al. `21

Moffat et al. `23

Qiu & Yu, arXiv:2305.15397





Exclusive Photo-Production of a $\pi \gamma$ Pair – Hall D at JLab

☐ GPD Models:

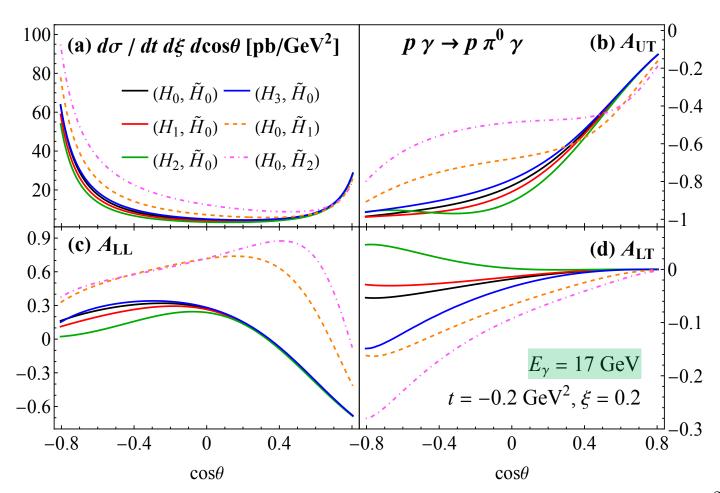
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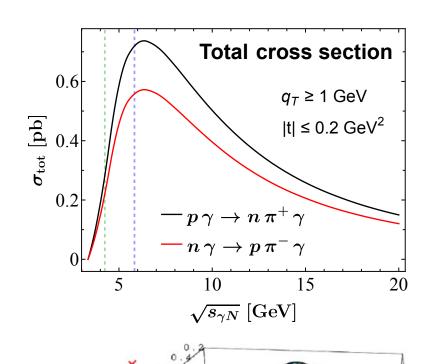


$$\int_{-1}^{1} \frac{dx \, S(x, \xi)}{x - \xi \pm i\epsilon} = 0$$

Goloskokov, Kroll, '05, '07, '09 Bertone et al. `21 Moffat et al. '23 Qiu & Yu, arXiv:2305.15397

0.5

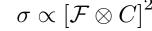




-0.5

 b_{\perp} (fm)

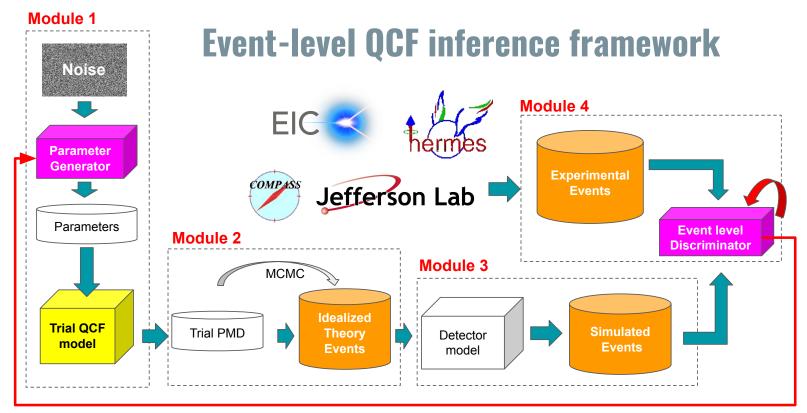
Extracting GPDs is a challenging inverse problem! $\sigma \propto \left[\mathcal{F} \otimes C\right]^2$



QuantOm Collaboration – a 5-year SciDAC project

☐ Femtoscale Imaging of Nuclei using Exascale Platforms:

Pixelating hadron in terms of probabilities to find quarks and gluons in slices of the momentum fraction x



Optimize QCF parameters (or pixelated images)

PMD: Particle Momentum Distribution - Observables QCF: Quantum Correlation Functions: PDFs, TMDs, GPDs, ...



NP: ANL(Lead), JLab, VT ASCR: FASTMath, RAPIDs

Exp Events (PMD):

• DIS:

1 particle inclusive

• SIDIS:

2 particle inclusive

SDHEP:

3 particle exclusive

Generated Events:

Many templates from trial QCFs & trusted theory

Inference:

Optimized QCFs or pixelated images in trusted phase space

New regimes:

Go beyond the trusted phase space

Jefferson Lab

Summary and Outlook

- SDHEP provides a reliable way to explore tomography of nuclei without breaking them:
 - GPDs are fundamental functions carrying the pixelated images of a bound hadron/nucleus,
 - Carry rich information on emergent hadron properties (mass, spin, ...) from QCD dynamics,
 - Provide the much needed hints on how confined quarks/gluons respond to the hard probes, ...

Extracting their x-dependence from experimental observable(s) is non-trivial, but, full of opportunities, ...

- **□** 50 years of QCD established it as the right theory of strong interactions:
 - Many challenges and open questions remain, including confinement, emergent phenomena, ...
 - QCD at the femto-scale (0.1 10 fm) is the most interesting, rich, and complex regime of the theory



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I would like to thank all pioneers who discovered the QCD and methods allowing us to explore the QCD!

I would like to thank Prof. Al Mueller who introduced me to the QCD and its excitements, and Prof. George Sterman who introduced me to the factorization and the predictive power of perturbative QCD!

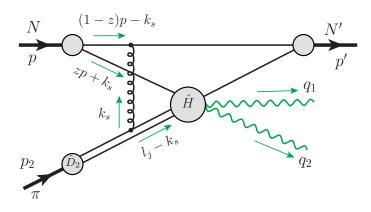
I would like to thank the organizers for hosting such a nice and historic meeting, and the opportunity to speak and to celebrate the 50 years of QCD with all of you!



Why *single* diffractive?

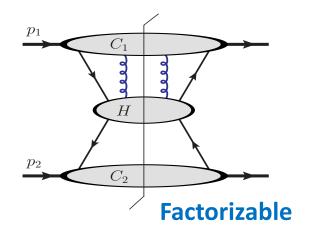
□ Double diffractive process

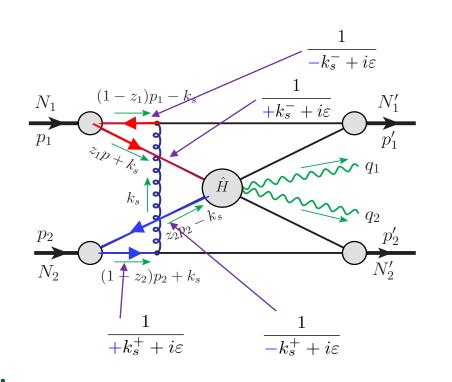
Glauber pinch for diffractive scattering



Factorizable if all pion momentum flows into hard part

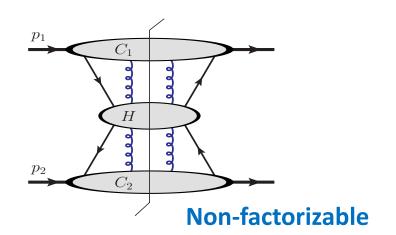
☐ Compare: Drell-Yan process at high twist:





Both k_s^+ and k_s^- are pinched in Glauber region!

Break of factorization



Only the 1st sub-leading twist is factorizable!

Qiu & Sterman, NPB, 1991

