

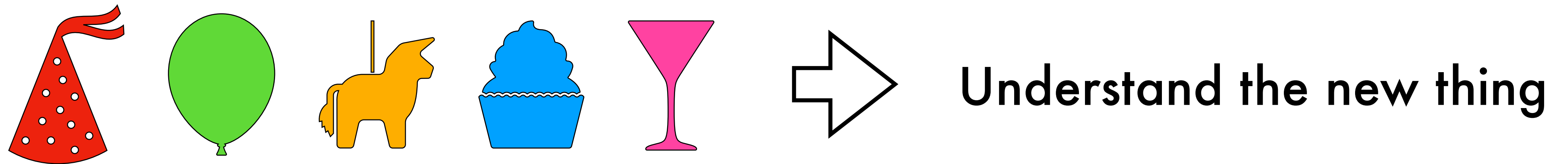
# Cornering the third generation at FCC-ee

*Sophie Renner, FCC Phenomenology Workshop, CERN, July 5th*

# Particle physics after the LHC...

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## Option 1: something new



## Option 2: *SM* still reigns

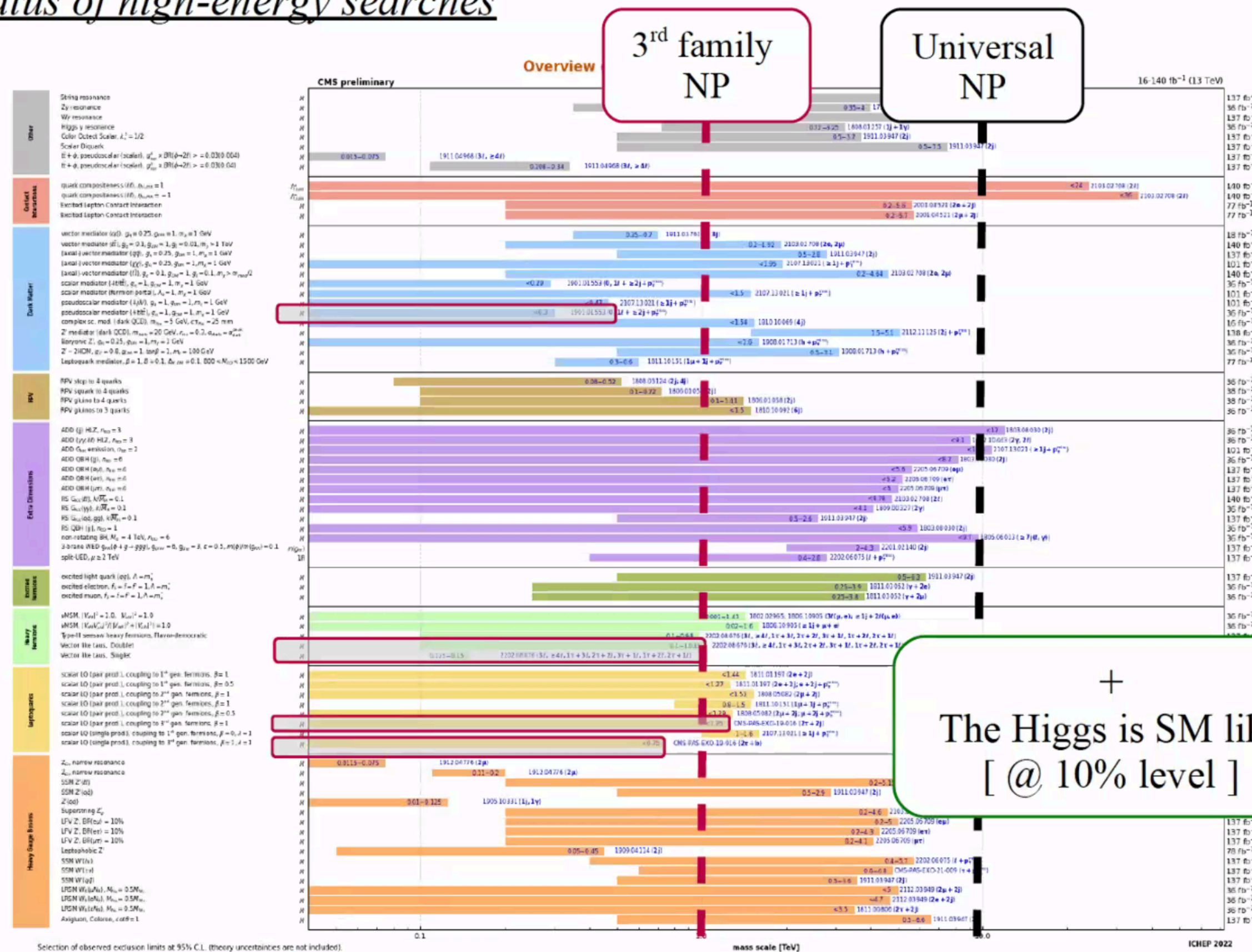
Is there still space for TeV-ish new physics? - where to look?

# Best case scenario: flavourful physics

G. Isidori – Decoding flavor hierarchies

CERN – 29<sup>th</sup> March 2023

## ► Status of high-energy searches



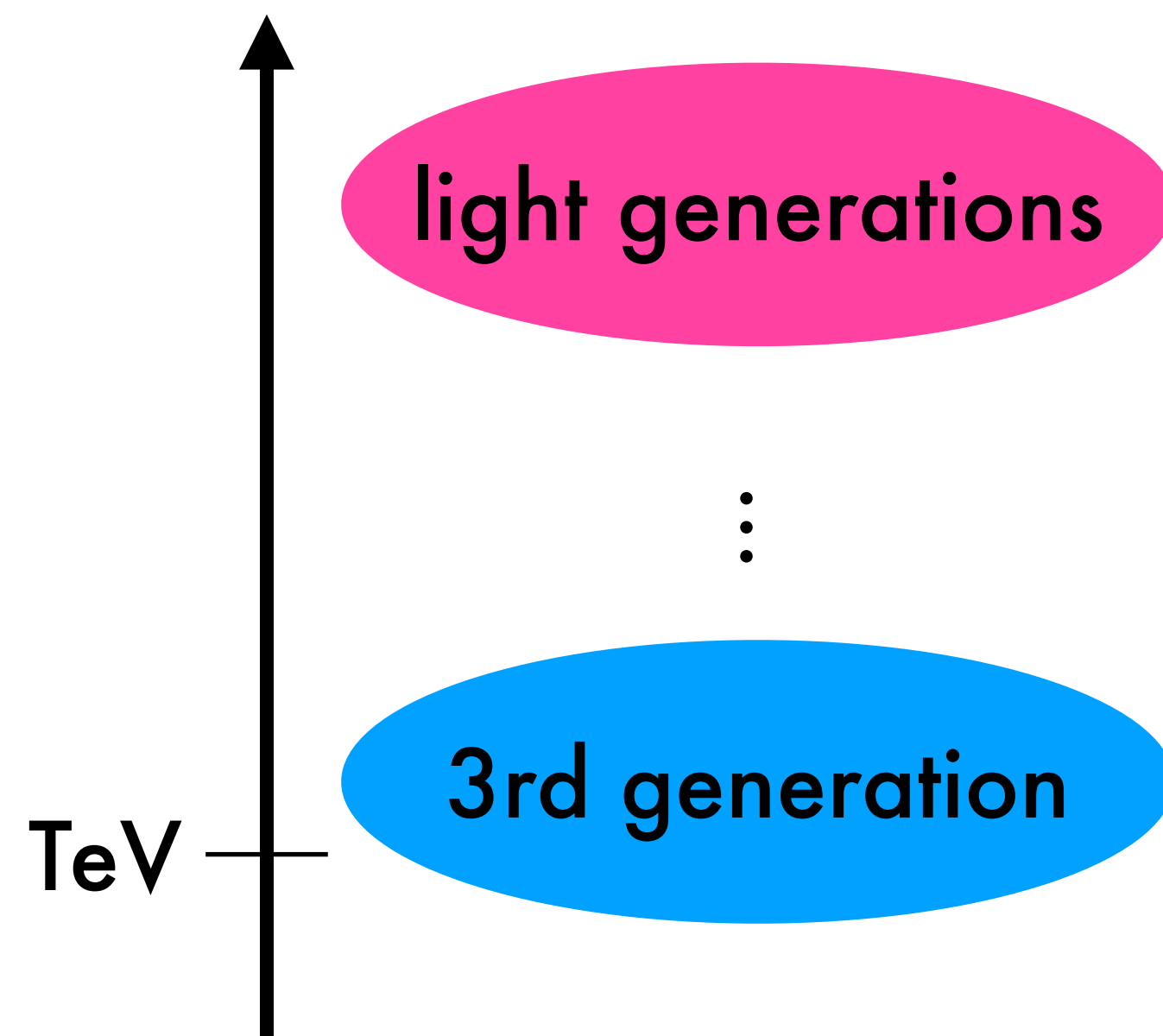
If BSM physics couples differently to different flavours, bounds change

In particular, lowest bounds if NP couples only to 3rd family

At LHC: PDF suppression  
Low energy: 3rd generations  
less precisely measured

# Is the third generation special?

Not just a convenient way to lower the scales...



## Hierarchy problem

Light top partners/stops

## Connection to *SM* flavour structure, e.g. flavour-dependent gauge interactions

Origin of Yukawas?

## B anomalies

See Joe Davighi's talk, next!

# What this means for a future collider

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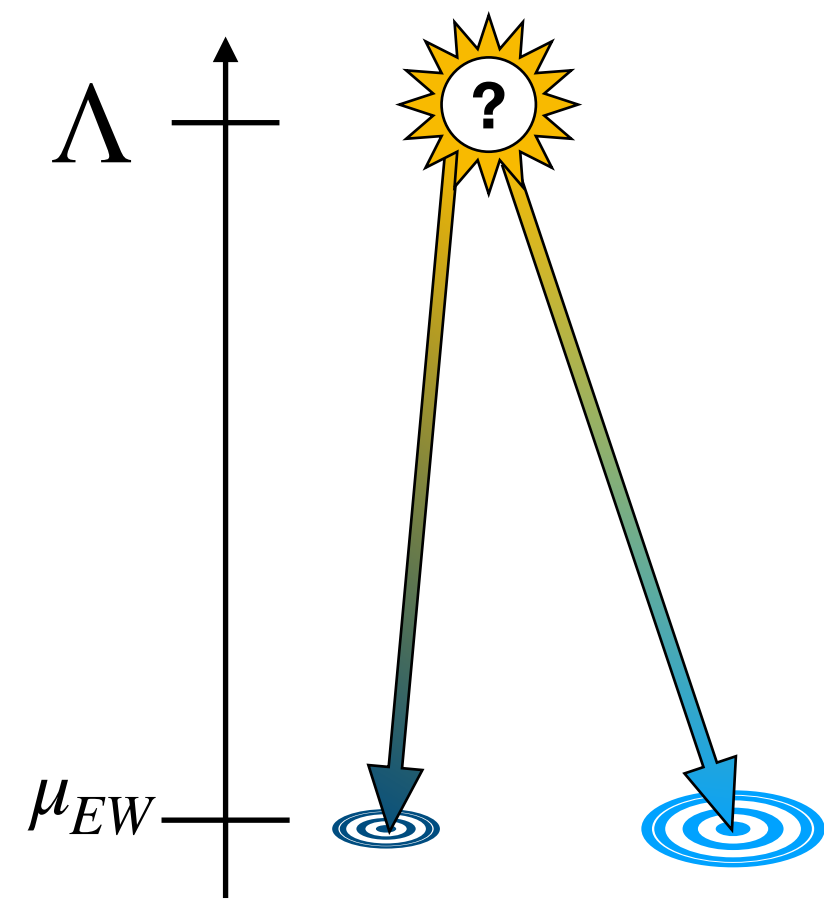
## Points to some aims for a new collider:

- ★ Testing the Yukawa sector      Higgs couplings to fermions, CKM tests
- ★ Searching for new flavour changing interactions involving 3rd generation fermions
- ★ Searching for new flavour-conserving interactions involving 3rd generation fermions

**Examples of how FCC-ee addresses each of these and what it might mean for BSM**

# The Standard Model Effective Field Theory

Approximate the effects of all possible heavy particles by writing down all possible new interactions between SM particles



$$\mathcal{L}_{\text{SMEFT}} = \frac{1}{\Lambda^2} \sum_i C_i O_i + \mathcal{O}\left(\frac{1}{\Lambda^4}\right)$$

Operators are suppressed by BSM scale

$\Lambda$

Different classes of operators built from SM fields...

$$X^3 \quad H^6 \quad H^4 D^2 \quad \psi \bar{\psi} H^2 D \quad \psi \bar{\psi} H^3 \quad \psi \bar{\psi} X H \quad X^2 H^2 \quad \bar{\psi}^2 \psi^2$$

$$X = B_{\mu\nu}, G_{\mu\nu}^A, W_{\mu\nu}^I$$

$$\psi = Q, u, d, L, e$$

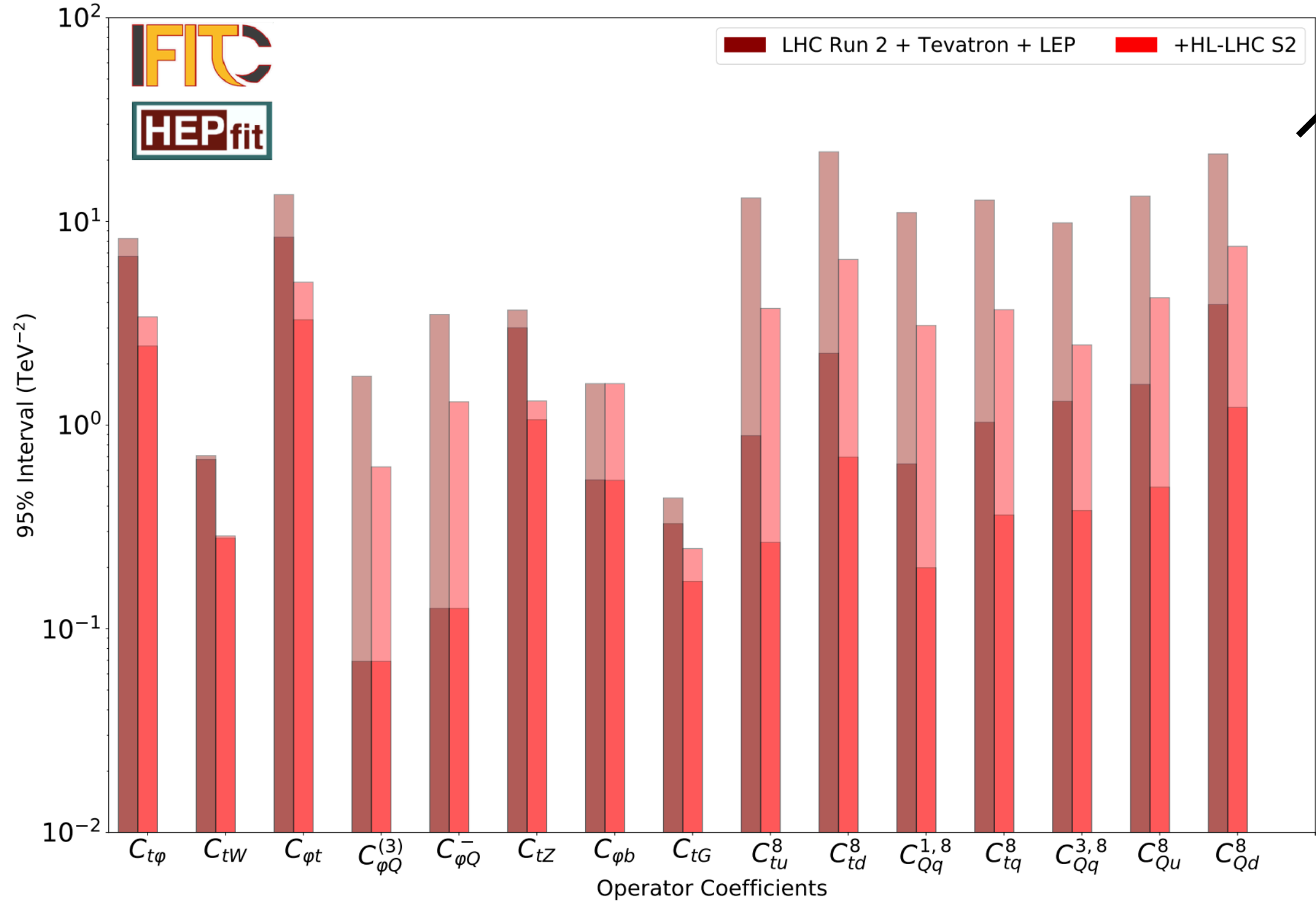
Parameters of the theory are contained in the Wilson coefficients

The search for new physics can be translated into searches in Wilson coefficient space

# SMEFT in 2040

## Projected fit to top-containing operators

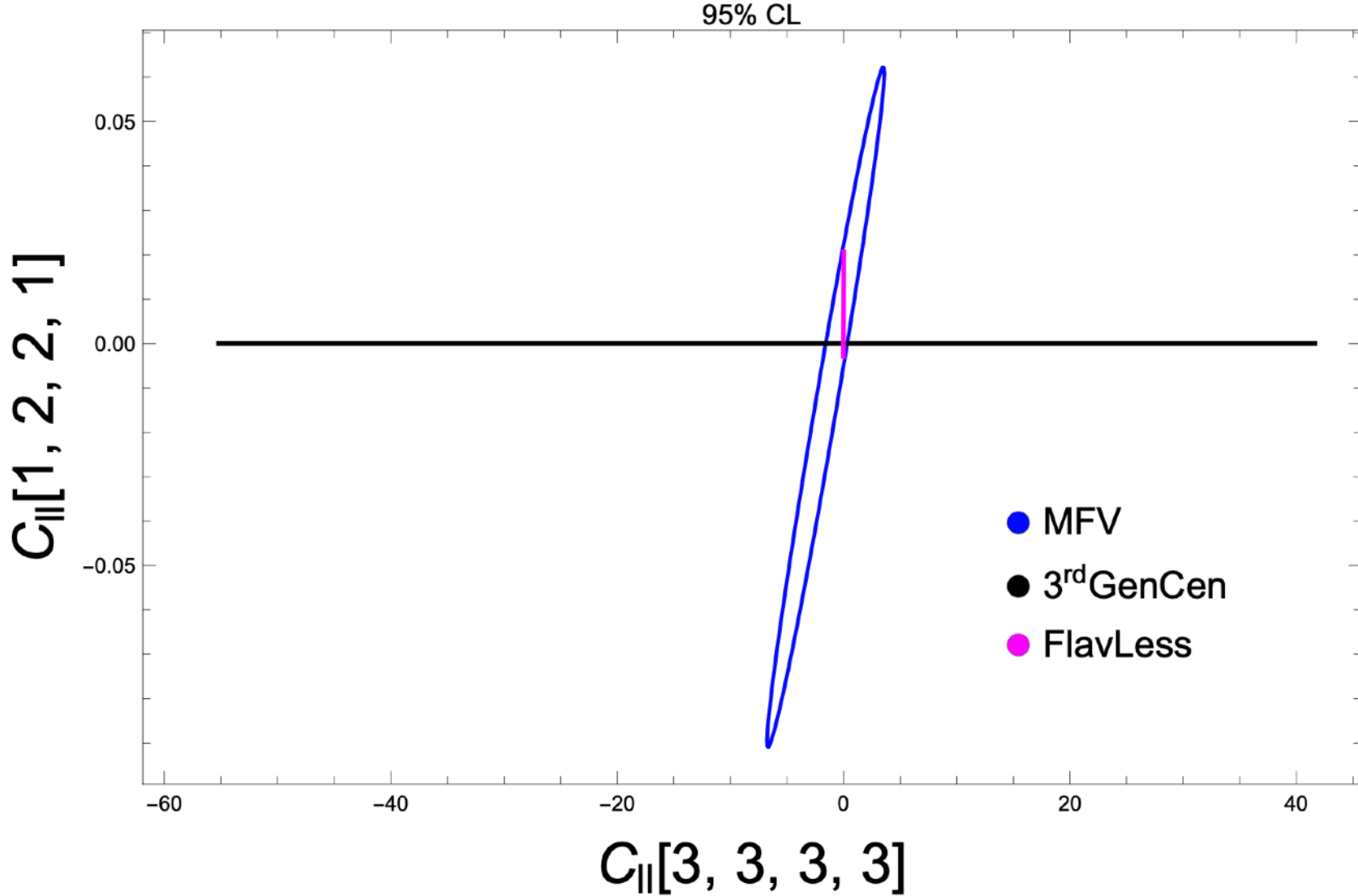
De Blas et al, 2206.08326



Lighter shade: single-parameter fit  
 Darker shade: marginalised fit

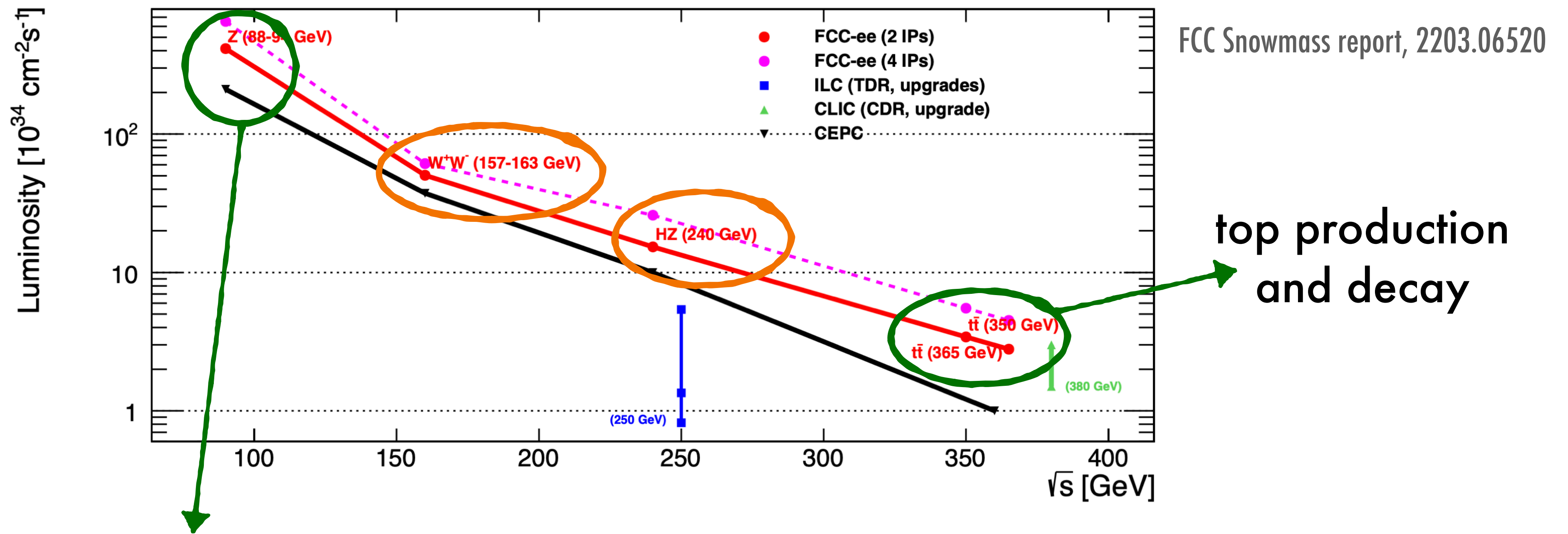
Some operators are only constrained to below 1 TeV, even after HL-LHC

Other types of flavoured operators have not been systematically studied (even using current data)



Bellafronte, Dawson,  
 Giardino  
 2304.00029

# FCC-ee is a flavour factory



Numbers for decays of  $5 \times 10^{12} Z^0$ s:

Lenz & Monteil, 2207.11055

Particle species	$B^0$	$B^+$	$B_s^0$	$\Lambda_b$	$B_c^+$	$c\bar{c}$	$\tau^-\tau^+$
Yield ( $\times 10^9$ )	310	310	75	65	1.5	600	170

$O(10^{11})$   $B$  mesons

About 15 times larger than Belle II dataset

Combines the advantages of B factories and LHCb: highly boosted particles in a clean environment

**Precise measurements of the third generation (both quarks and leptons)**

**Also Yukawa & CKM sector**



# Higgs couplings to fermions

Projected precision (%):

FCC Snowmass report, 2203.06520

FCC-ee matters most

FCC-hh matters most

Collider	HL-LHC	FCC-ee <sub>240→365</sub>	FCC-ee + HL-LHC	FCC-INT	FCC-INT + HL-LHC
Int. Lumi (ab <sup>-1</sup> )	3	5 + 0.2 + 1.5	–	30	–
Years	10	3 + 1 + 4	–	25	–
$g_{Hbb}$ (%)	5.1	0.69	0.64	0.48	0.48
$g_{Hcc}$ (%)	SM	1.3	1.3	0.96	0.96
$g_{H\tau\tau}$ (%)	1.9	0.74	0.66	0.49	0.46
$g_{H\mu\mu}$ (%)	4.4	8.9	3.9	0.43	0.43
$g_{Htt}$ (%)	3.4	–	3.1	1.0	0.95

+  $Hee$  at FCC-ee 2107.02686

Also good sensitivity to flavour changing decays at FCC-ee:  
see Michele Tamarro's talk this afternoon

In the SMEFT at dim 6, each of these decays is modified by a single operator:

$\mathfrak{5} : \psi^2 H^3 + \text{h.c.}$	
$Q_{eH}$	$(H^\dagger H)(\bar{l}_p e_r H)$
$Q_{uH}$	$(H^\dagger H)(\bar{q}_p u_r \tilde{H})$
$Q_{dH}$	$(H^\dagger H)(\bar{q}_p d_r H)$

$$\Rightarrow \frac{v^2}{2\sqrt{2}} (v + 3h + \dots) \bar{q}_L u_R$$

These operators can be generated at tree level in some models, e.g. 2HDM

$\Rightarrow$  test of BSM physics in Yukawa sector

# $V_{cb}$ at FCC-ee

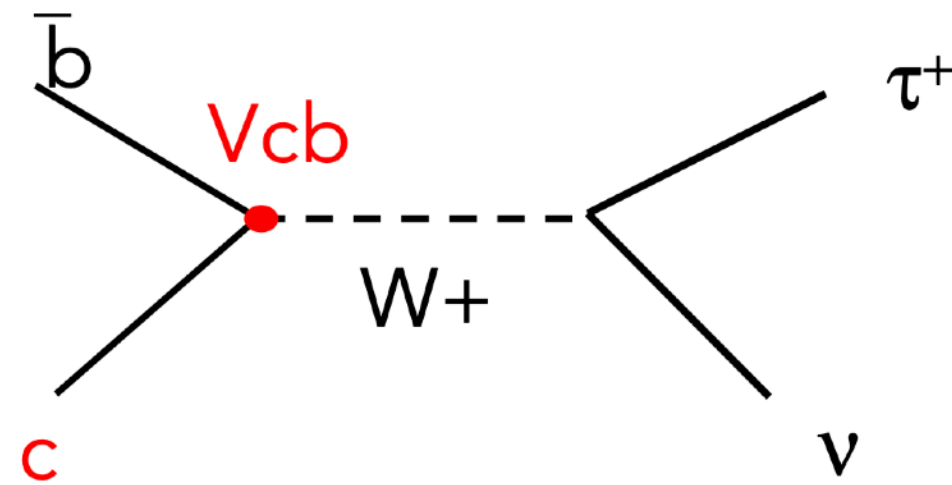
?

$$|V_{cb}|^{\text{incl.,2022}} = (42.16 \pm 0.51) \cdot 10^{-3}$$

$$|V_{cb}|^{\text{excl.,PDG}} = (39.5 \pm 0.9) \cdot 10^{-3}$$

Discrepancy between inclusive and exclusive determinations of  $V_{cb}$

With  $B_c \rightarrow \tau^+ \nu$  decays

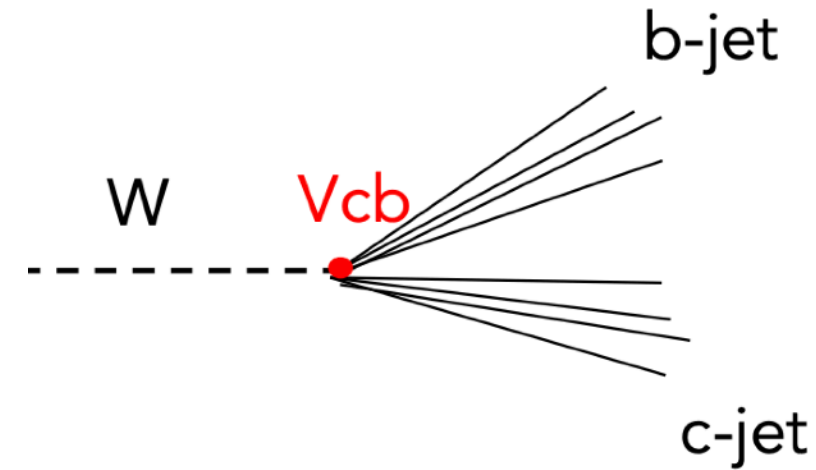


Amhis, Hartmann, Hensens, Hill, Sumensari 2105.13330  
Zheng et al, 2007.08234 (CEPC study)

No form factors, just a decay constant

But need to know  $B_c$  fraction

With  $W$  decays

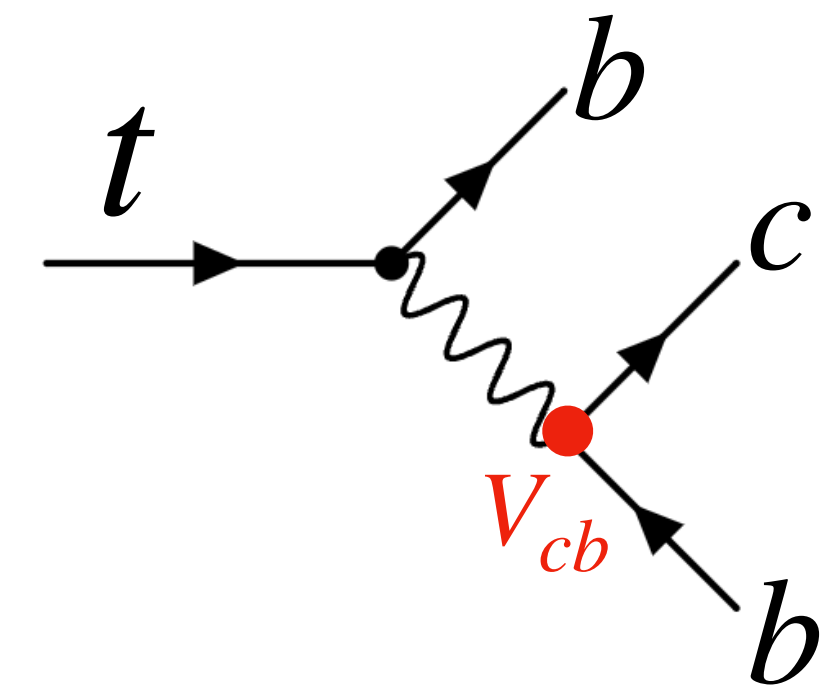


Precision depends on tagging of b and c jets

Estimated achievable precision 0.4% Marie-Helene Schune, FCC-ee workshop 2020

Similar story for  $V_{ub}$

With top decays



Harrison & Vladimirov, 1810.09424

More direct measurements of e.g.  $V_{ts}$

# 'CKM' in the SMEFT

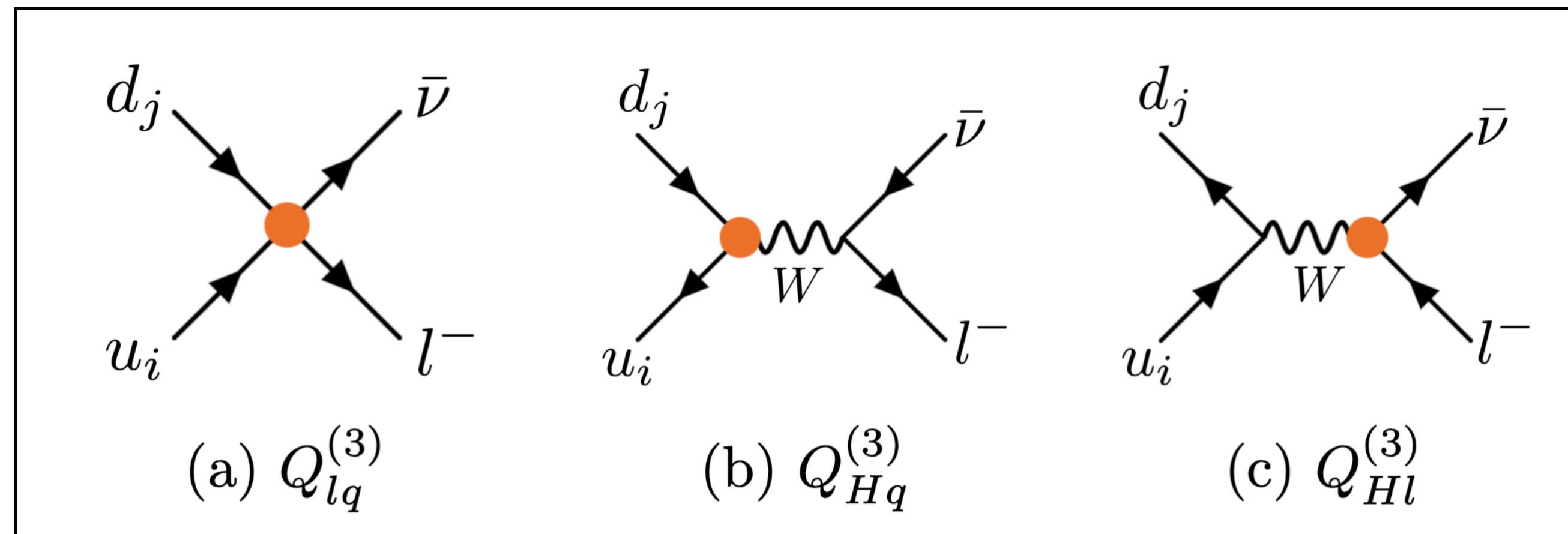
In the absence of some symmetry forbidding it (e.g. R-parity), new physics can enter at tree level in observables from which the CKM is extracted

Possible SMEFT effects in CKM fits must be carefully propagated through Descotes-Genon et al., 1812.08163

Or do a bespoke CKM fit in which SMEFT effects cancel (only possible with flavour assumptions)

Aoude, Hurth, SR, Shepherd, 2003.05432

e.g.

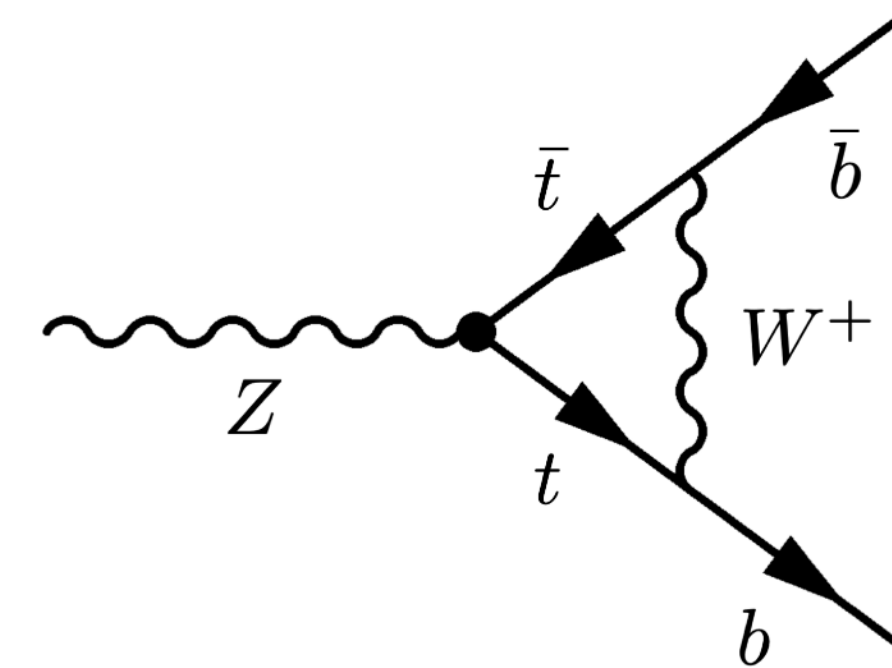
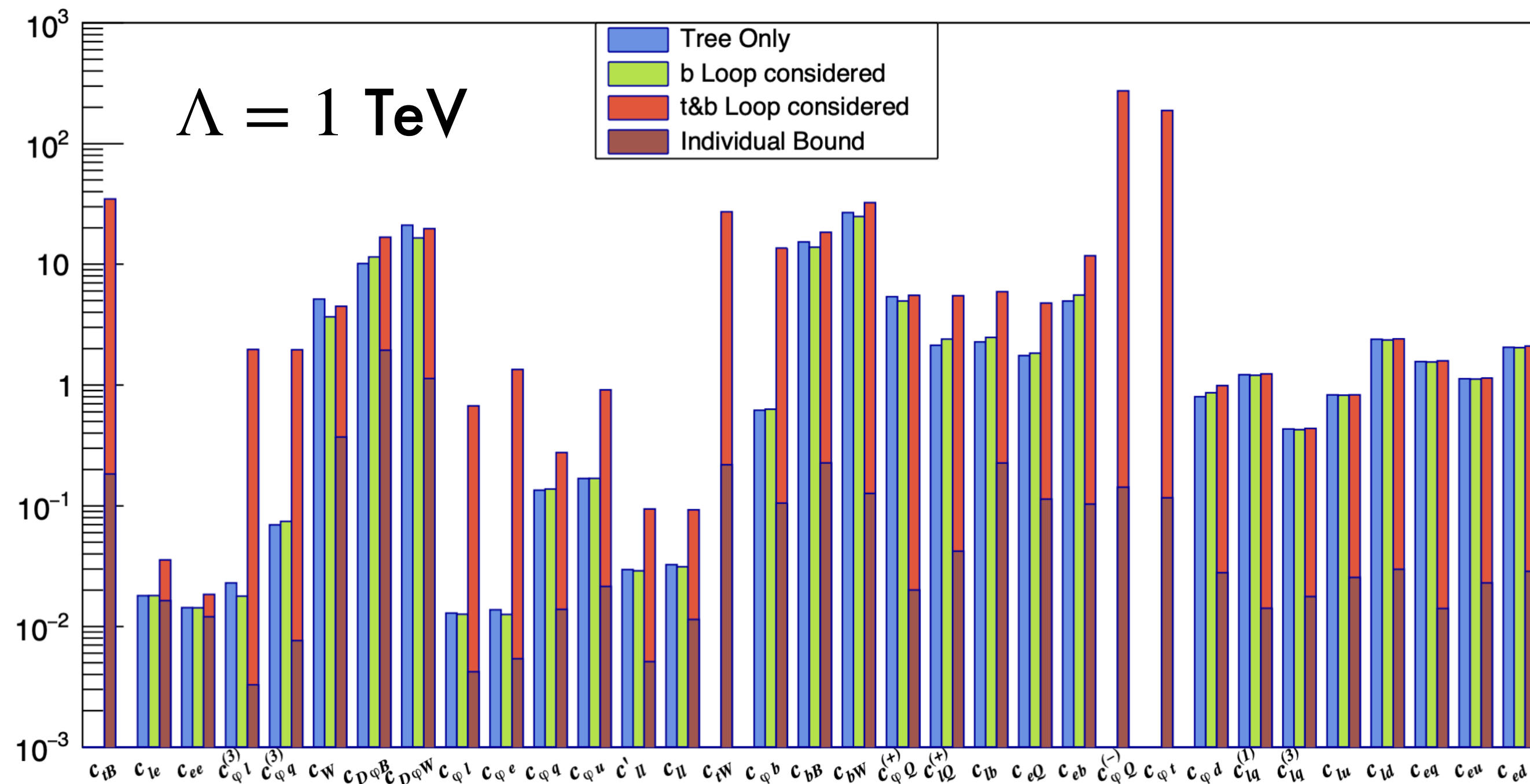


All three of these operators contribute to  $b \rightarrow c \ell \bar{\nu}$   
 But only one contributes to  $W \rightarrow \bar{b}c$

Easier to isolate new physics with more observables  
 Possibility of combined CKM + SMEFT fits?

# Bounds from EW precision on flavour of BSM?

Liu, Wang, Zhang, Zhang, Gu 2205.05655



## Individual bounds

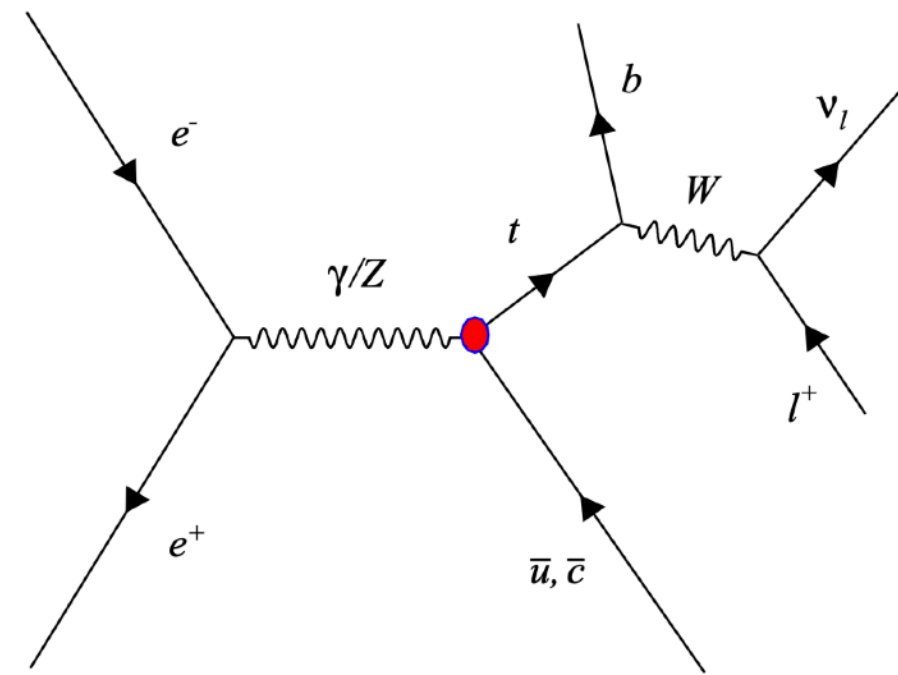
	$c_{\varphi t}$	$c_{\varphi Q}^{(-)}$	$c_{tW}$	$c_{tB}$
Electroweak	0.233	0.286	0.438	0.36
LHC data	2.275	1.22	0.06	0.145

**LEP outperforms LHC on some top operators**

See Joe Davighi's talk for EW precision and models of flavour

# Top FCNCs

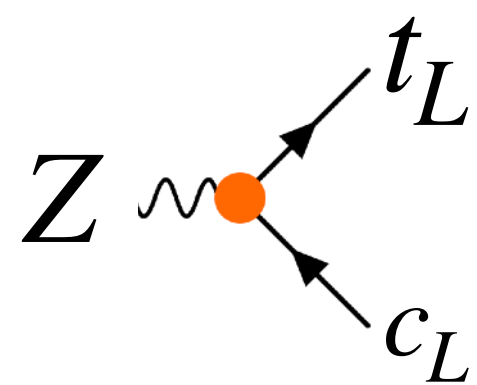
Top FCNCs can be searched for in top decay at  $t\bar{t}$  run of FCC-ee



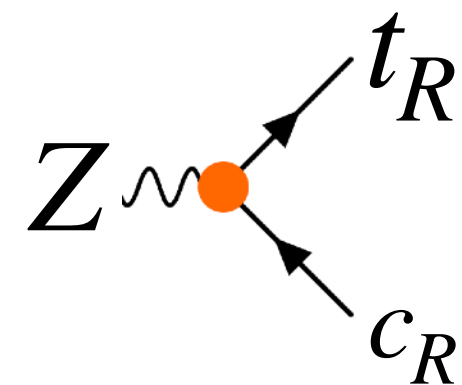
Also in single top production at  $\sqrt{s} = 240$  GeV (HZ) run  
Khanpour et al, 1408.2090

Effective operators contributing to t-q-Z coupling:

$$O_{\phi q}^{(1,3)}$$

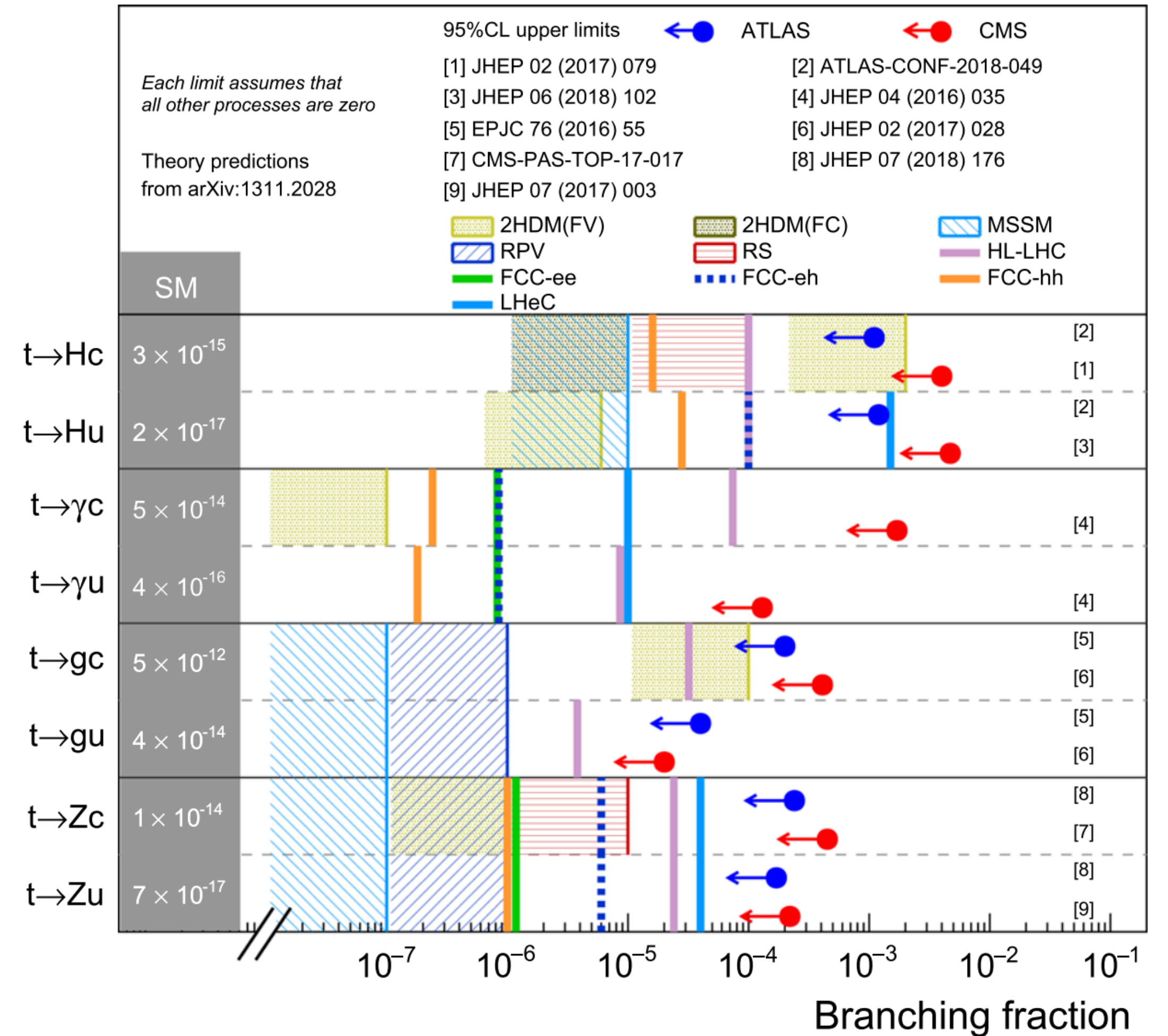


$$O_{\phi u}$$



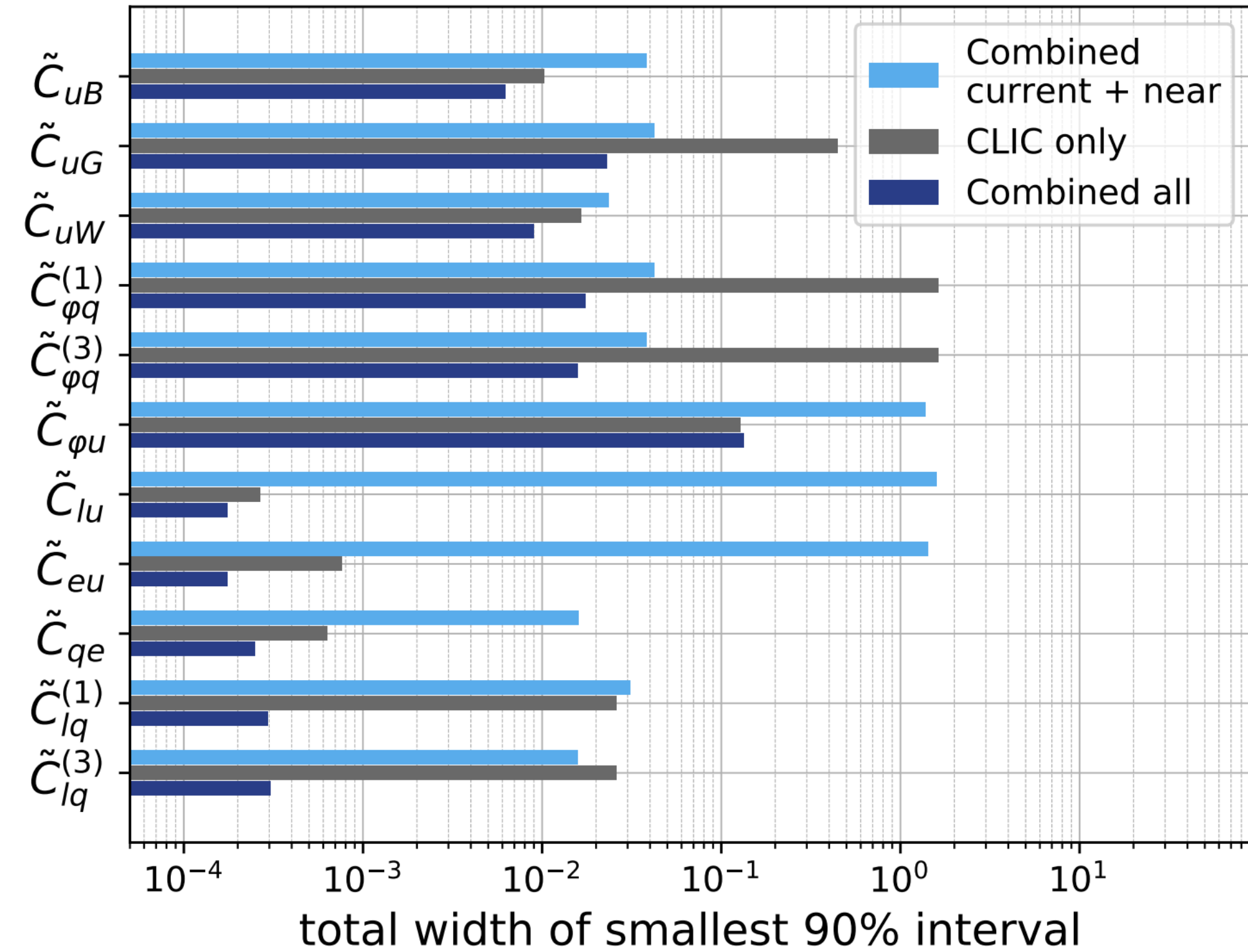
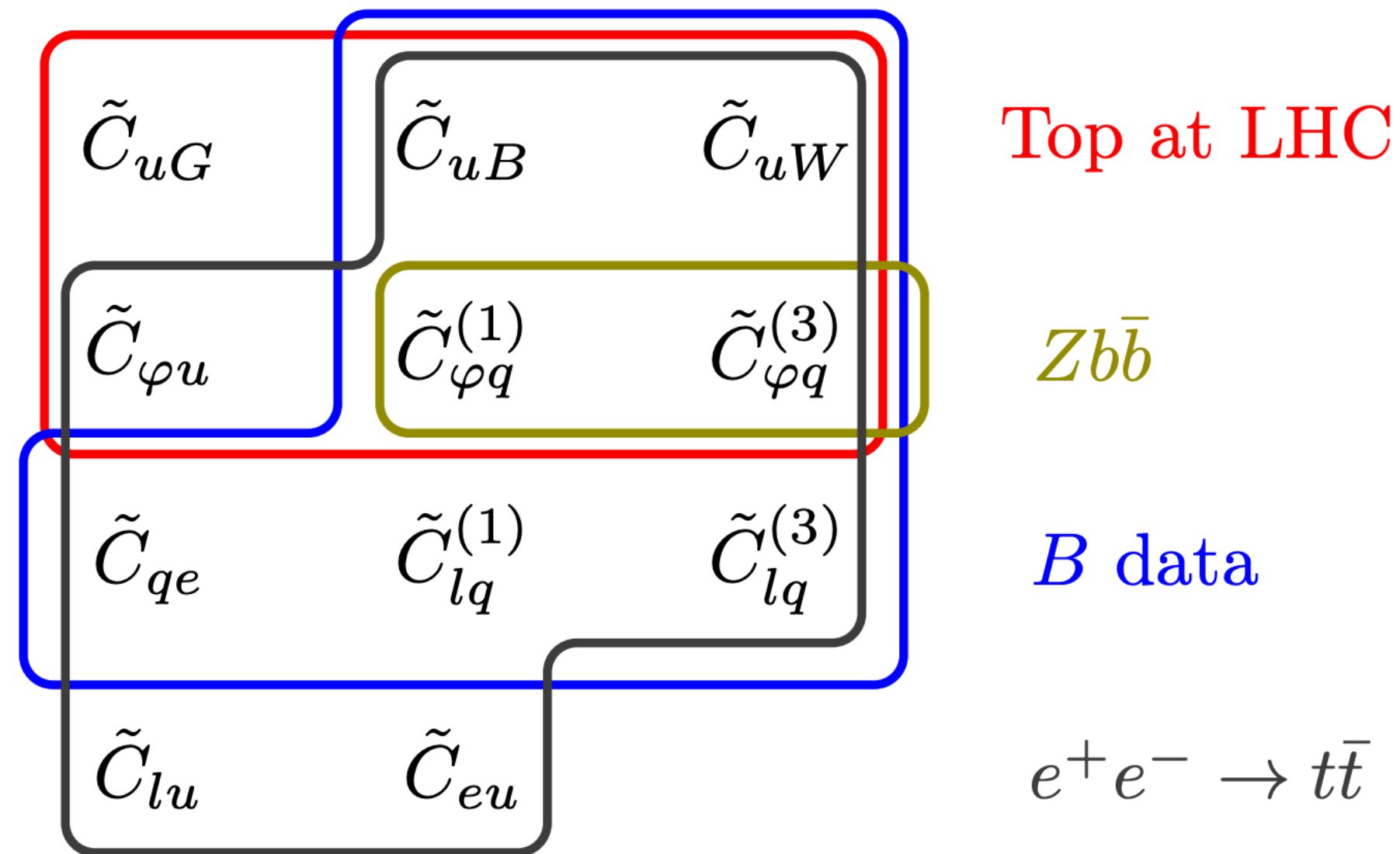
Also gives Z-b-s coupling

Future Circular Collider Conceptual Design Report Volume 1



# Top pairs at $e^+e^-$ vs B observables

Top pair production probes some of the same operators as B decays

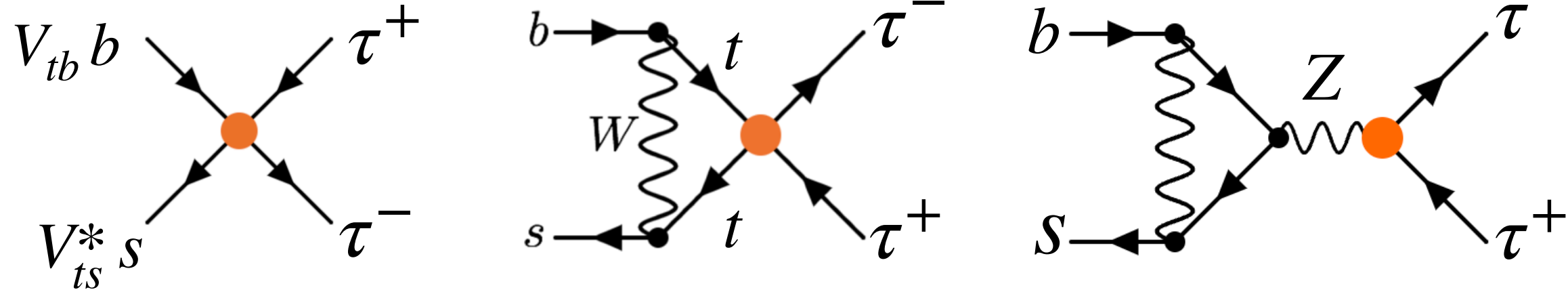


Bißmann, Grunwald, Hiller, Kröninger, 2012.10456

Observable	$\sqrt{s}$	Polarization ( $e^-, e^+$ )	Ref. experiment	SM Ref.
$\sigma_{t\bar{t}}, A_{\text{FB}}$	380 GeV	( $\pm 80\%$ , 0)	[27]	[40]
$\sigma_{t\bar{t}}, A_{\text{FB}}$	1.4 TeV	( $\pm 80\%$ , 0)	[27]	[40]
$\sigma_{t\bar{t}}, A_{\text{FB}}$	3 TeV	( $\pm 80\%$ , 0)	[27]	[40]

# B decays into $\tau s$

Likely that new physics that speaks only to 3rd gen should show up here:



$$B \rightarrow K \tau^+ \tau^-$$

SM branching ratio:  $(1.44 \pm 0.15) \times 10^{-7}$  HPQCD, 1306.0434

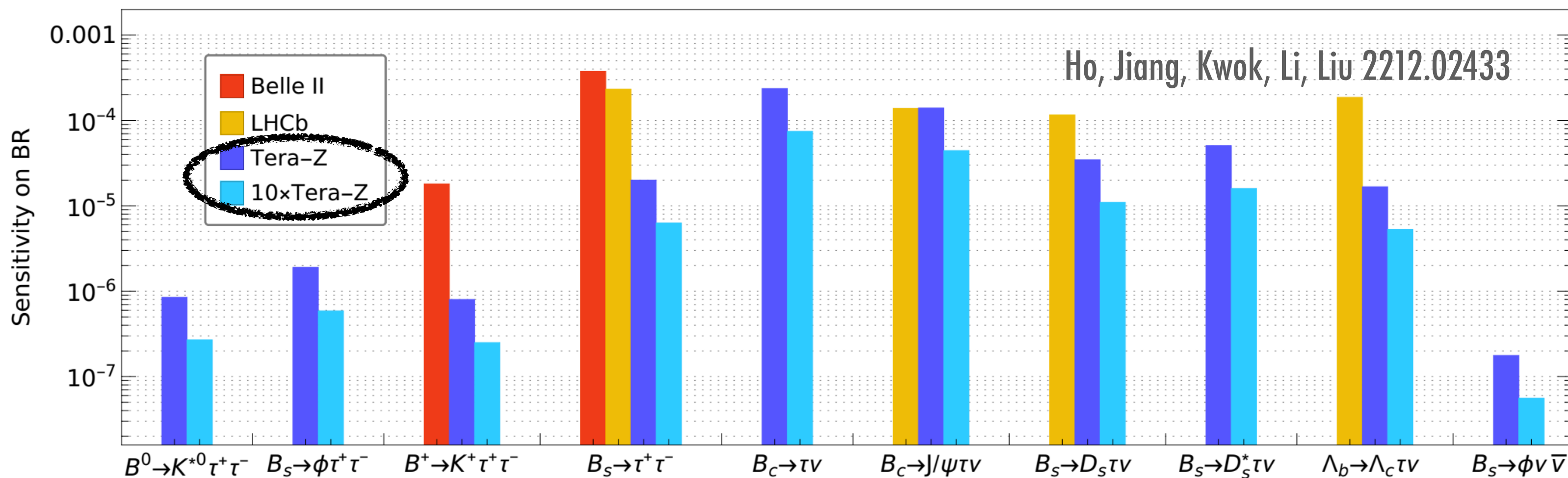
Current limits: 5 orders of magnitude above SM

After Belle II:  $BR \leq 10^{-4} - 10^{-5}$

$$B_s \rightarrow \tau^+ \tau^-$$

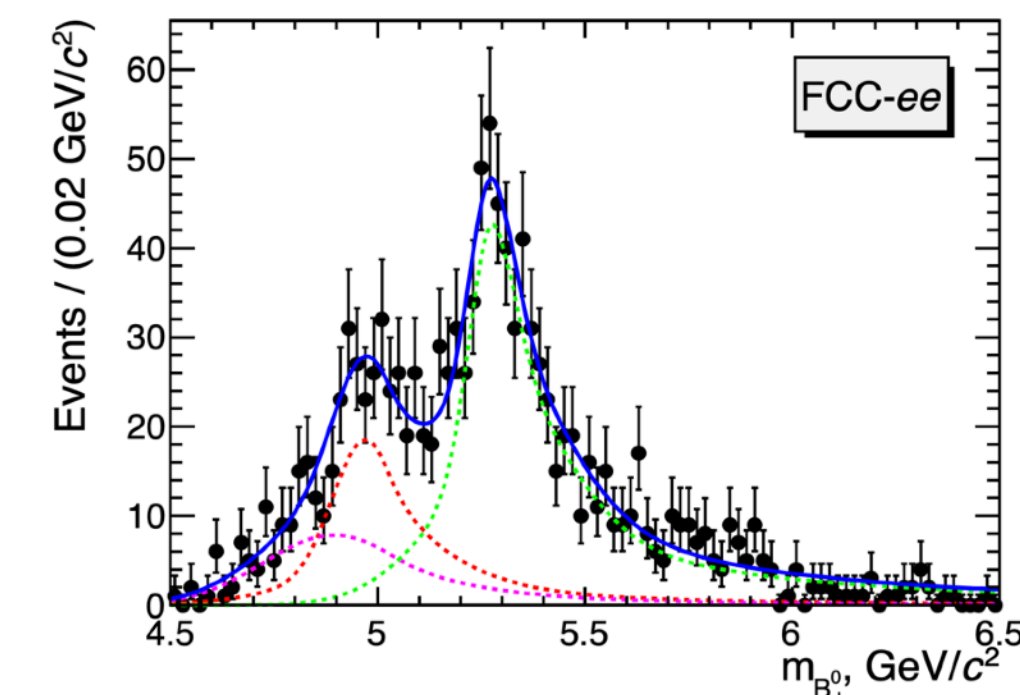
$\text{Br}(B_s \rightarrow \tau^+ \tau^-)_{\text{SM}} = (7.73 \pm 0.49) \times 10^{-7}$  Bobeth, 1405.4907

$\text{Br}(B_s \rightarrow \tau^+ \tau^-)_{\text{EXP}} \leq 6.8 \times 10^{-3}$  LHCb, 1703.02508



$$B \rightarrow K^* \tau^+ \tau^-$$

$\mathcal{O}(10^3)$  reconstructed  $B \rightarrow K^* \tau^+ \tau^-$  events  
Can measure  $\tau$  polarization observables



Kamenik, Monteil, Semkiv,  
Silva, 1705.11106

# $B \rightarrow K^{(*)} \tau^+ \tau^-$ in the SMEFT

$$O_{lq}^{(1)ijkl} = (\bar{L}^i \gamma_\mu L^j) (\bar{Q}^k \gamma^\mu Q^l)$$

$$O_{lq}^{(3)ijkl} = (\bar{L}^i \gamma_\mu \tau^I L^j) (\bar{Q}^k \gamma^\mu \tau^I Q^l)$$

$$O_{qe}^{ijkl} = (\bar{e}^i \gamma_\mu e^j) (\bar{Q}^k \gamma^\mu Q^l)$$

$$R_D^{(*)} \propto C_{lq}^{(3)}$$

$$B \rightarrow K^{(*)} \bar{\nu} \nu \propto C_{lq}^{(1)} - C_{lq}^{(3)}$$

$$B \rightarrow K^{(*)} \tau^+ \tau^- \propto C_{lq}^{(1)} + C_{lq}^{(3)}$$

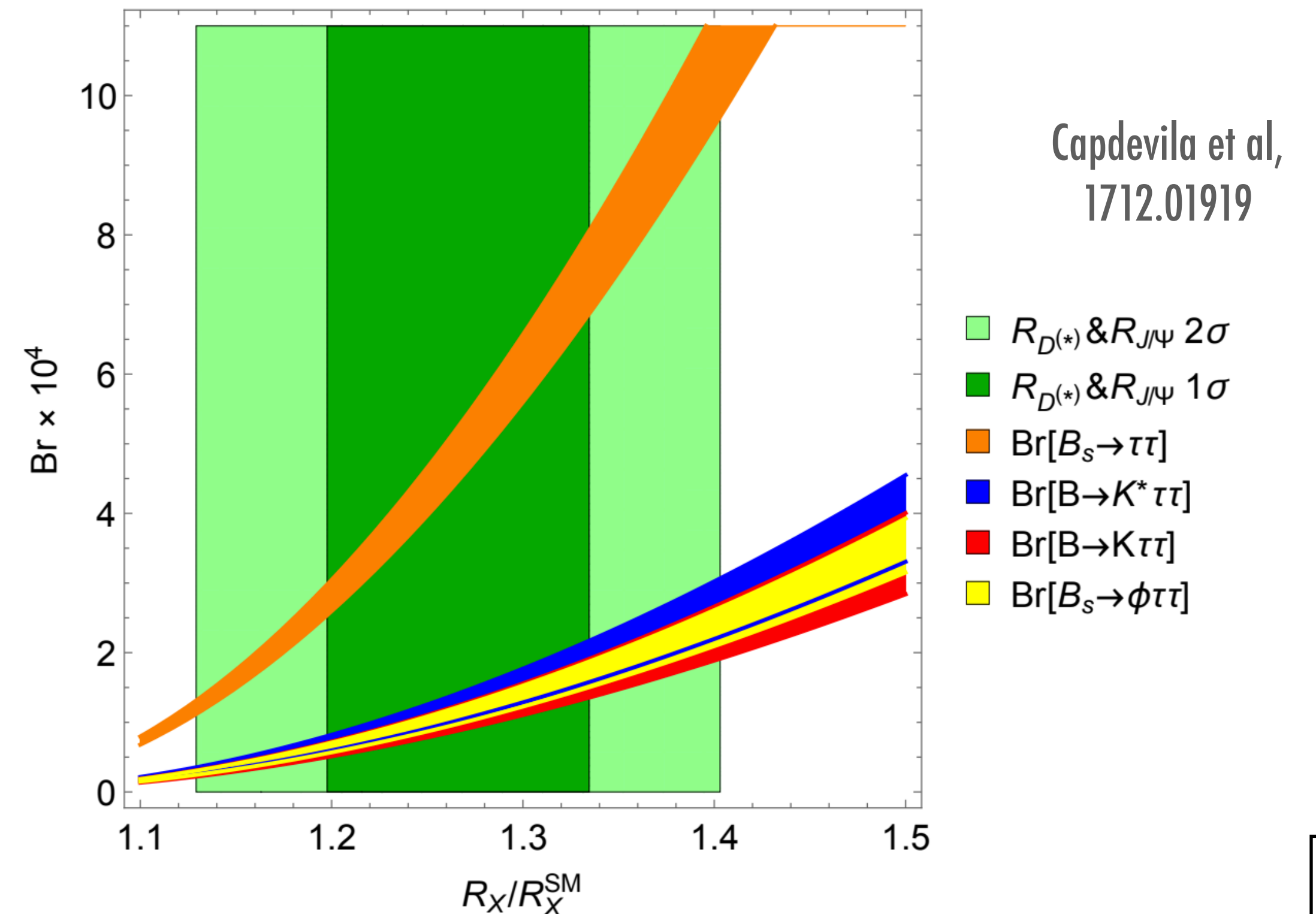
Can have large  $R_D^{(*)}$  without disagreement with  $B \rightarrow K^{(*)} \bar{\nu} \nu$  if

$$C_{lq}^{(1)} = C_{lq}^{(3)}$$

If the anomalies in  $R_D^{(*)}$  persist, expect large deviations in  $B \rightarrow K^{(*)} \tau^+ \tau^-$  and  $B_s \rightarrow \tau^+ \tau^-$

If not, these observables combined will constrain the relevant operators to  $O(10 \text{ TeV})$

Ho, Jiang, Kwok, Li, Liu 2212.02433





# Tests of lepton flavour universality in tau decays

$\mu - e$  universality

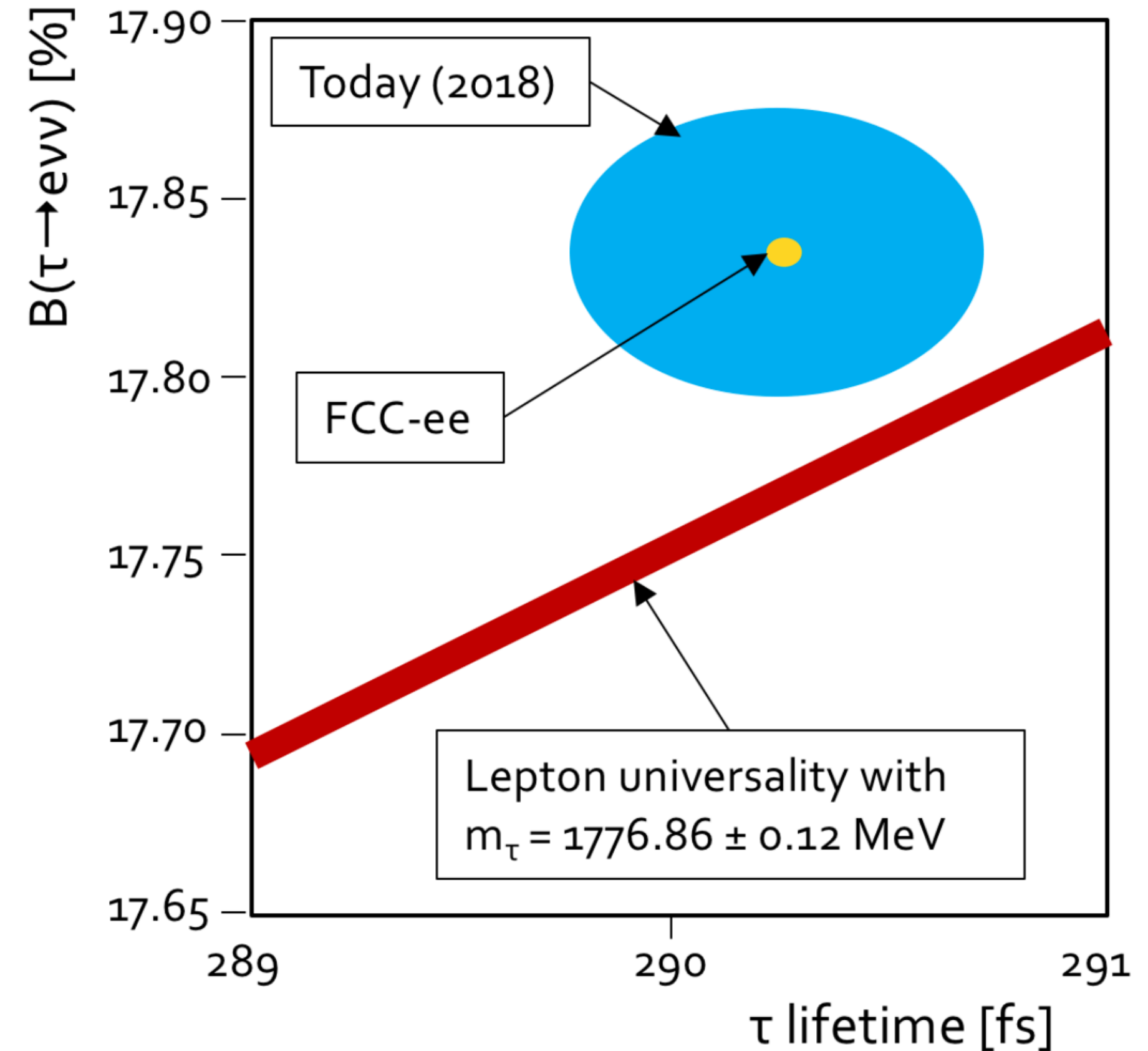
$$\left(\frac{g_\mu}{g_e}\right)^2 = \frac{\mathcal{B}(\tau \rightarrow \mu \bar{\nu} \nu)}{\mathcal{B}(\tau \rightarrow e \bar{\nu} \nu)} \cdot \frac{f_{\tau e}}{f_{\tau \mu}}$$

$\tau - \mu$  universality

$$\left(\frac{g_\tau}{g_\ell}\right)^2 = \frac{\mathcal{B}(\tau \rightarrow \ell \bar{\nu} \nu)}{\mathcal{B}(\mu \rightarrow \ell \bar{\nu} \nu)} \cdot \frac{\tau_\mu m_\mu^5}{\tau_\tau m_\tau^5} \cdot \frac{f_{\mu e}}{f_{\tau \ell}} \cdot \frac{R_\gamma^\mu R_W^\mu}{R_\gamma^\tau R_W^\tau}$$

Observable	Present value $\pm$ error	FCC-ee stat.	FCC-ee syst.
$m_\tau$ (MeV)	$1776.86 \pm 0.12$	0.004	0.1
$\mathcal{B}(\tau \rightarrow e \bar{\nu} \nu)$ (%)	$17.82 \pm 0.05$	0.0001	0.003
$\mathcal{B}(\tau \rightarrow \mu \bar{\nu} \nu)$ (%)	$17.39 \pm 0.05$	0.0001	0.003
$\tau_\tau$ (fs)	$290.3 \pm 0.5$	0.001	0.04

Dam, 1811.09408



# Lepton flavour universality tests

All the tests of LFUV can be tests of the same physics

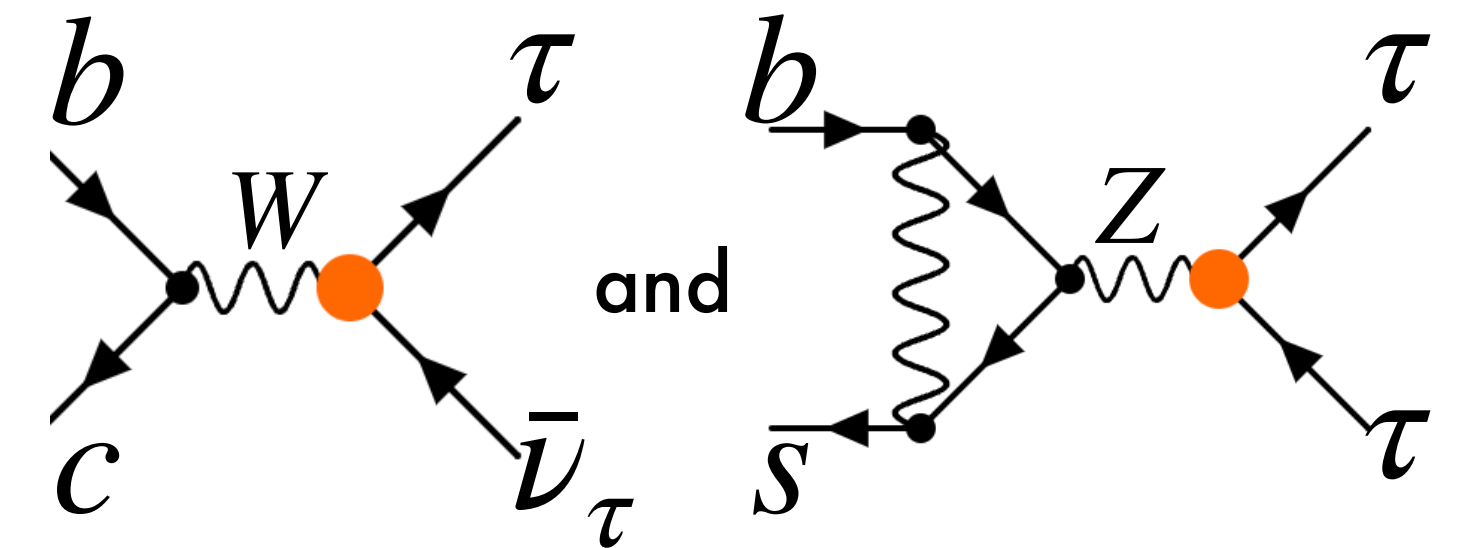
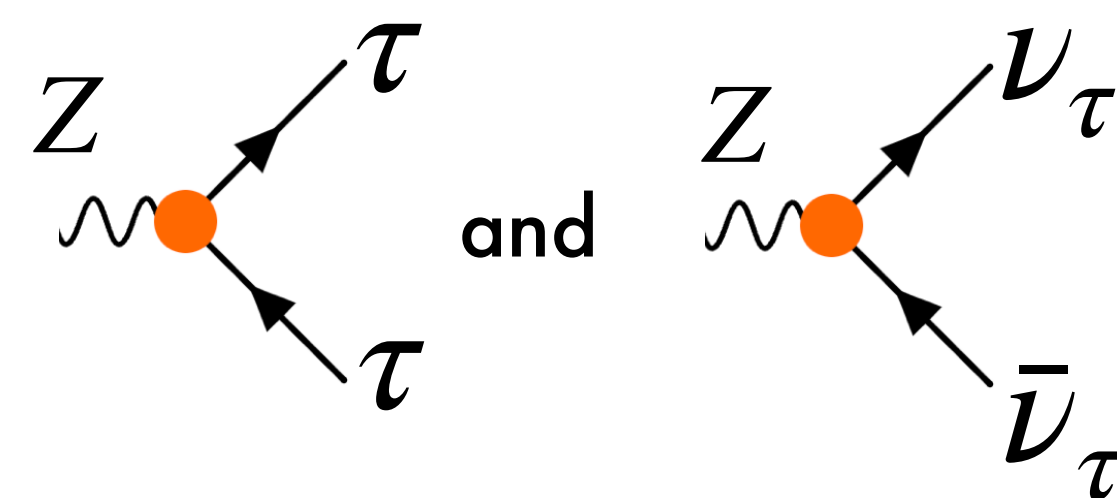
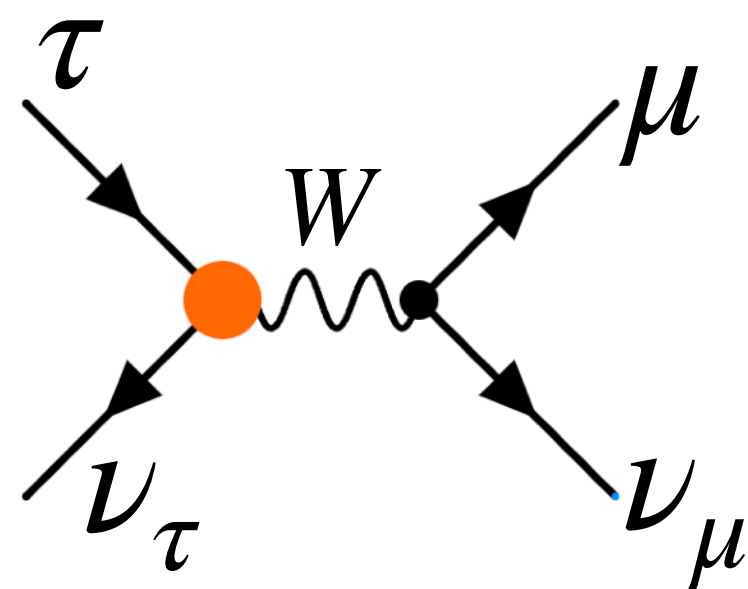
Tau decays

Z decays

B decays

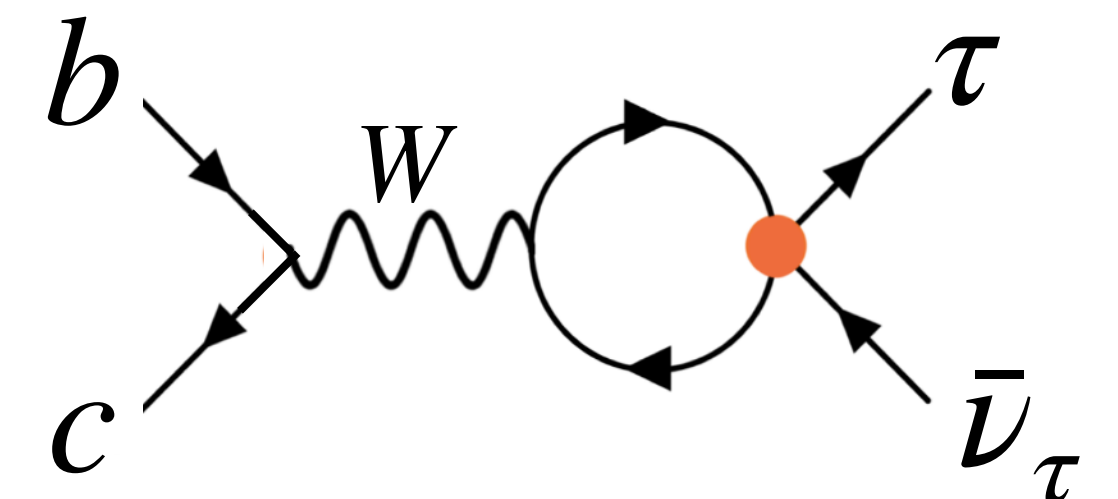
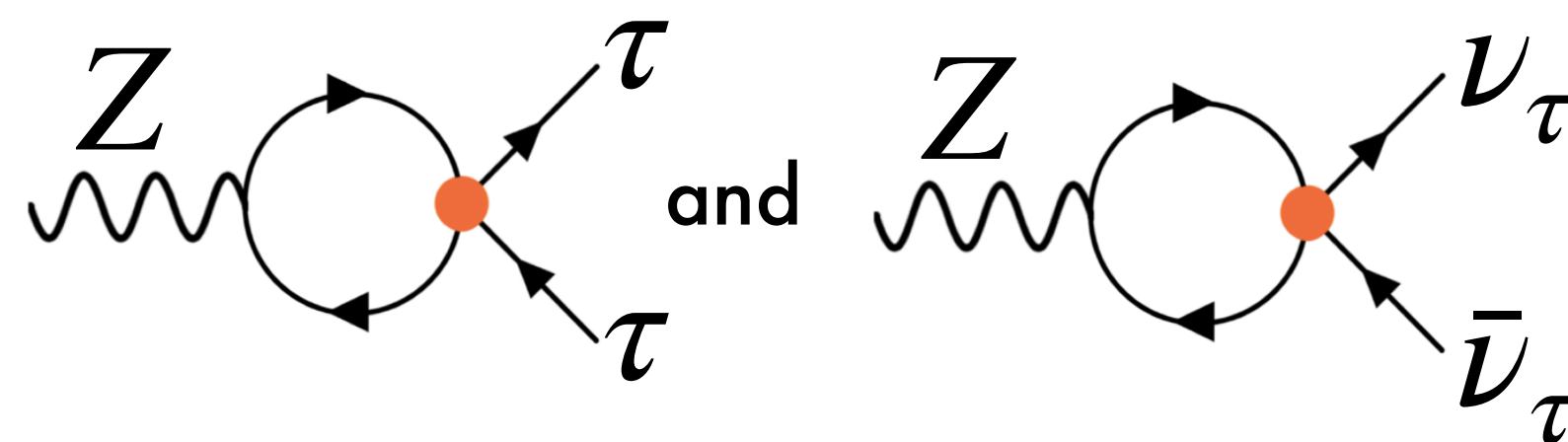
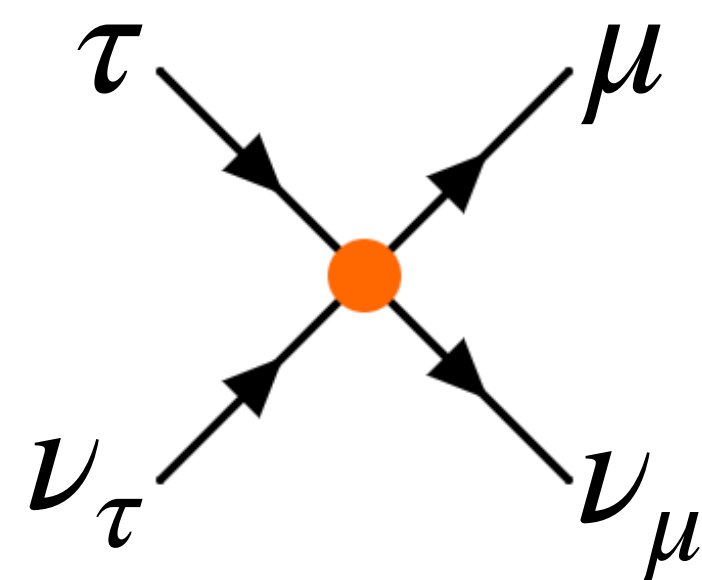
$$O_{\phi l}^{(1,3)}$$

$$(\phi^\dagger D_\mu \tau^a \phi)(\bar{L}^3 \gamma^\mu L^3)$$



$$O_{ll}$$

$$(\bar{L}^2 \gamma_\mu L^2)(\bar{L}^3 \gamma^\mu L^3)$$

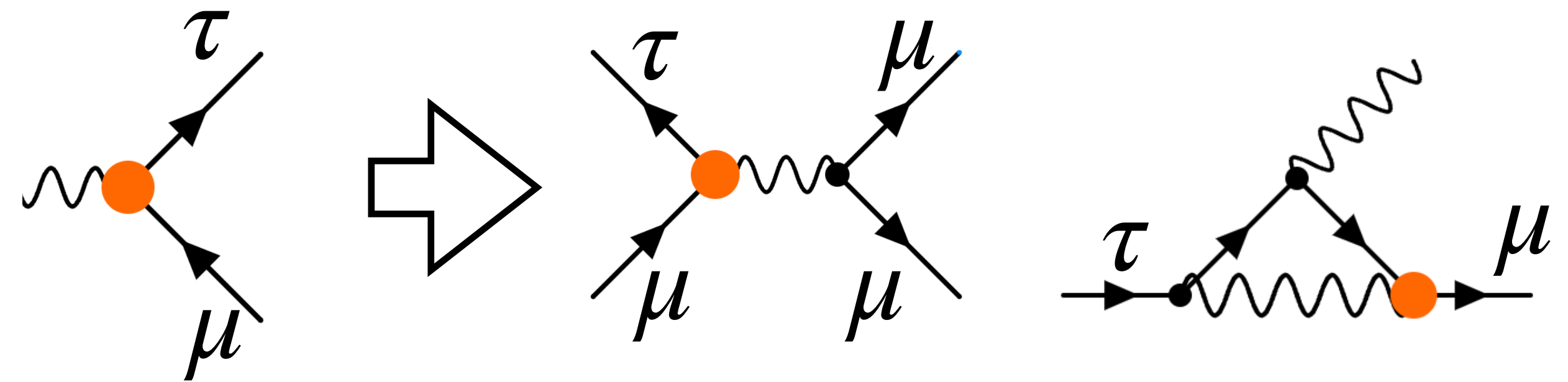


# Lepton flavour violation at FCC-ee

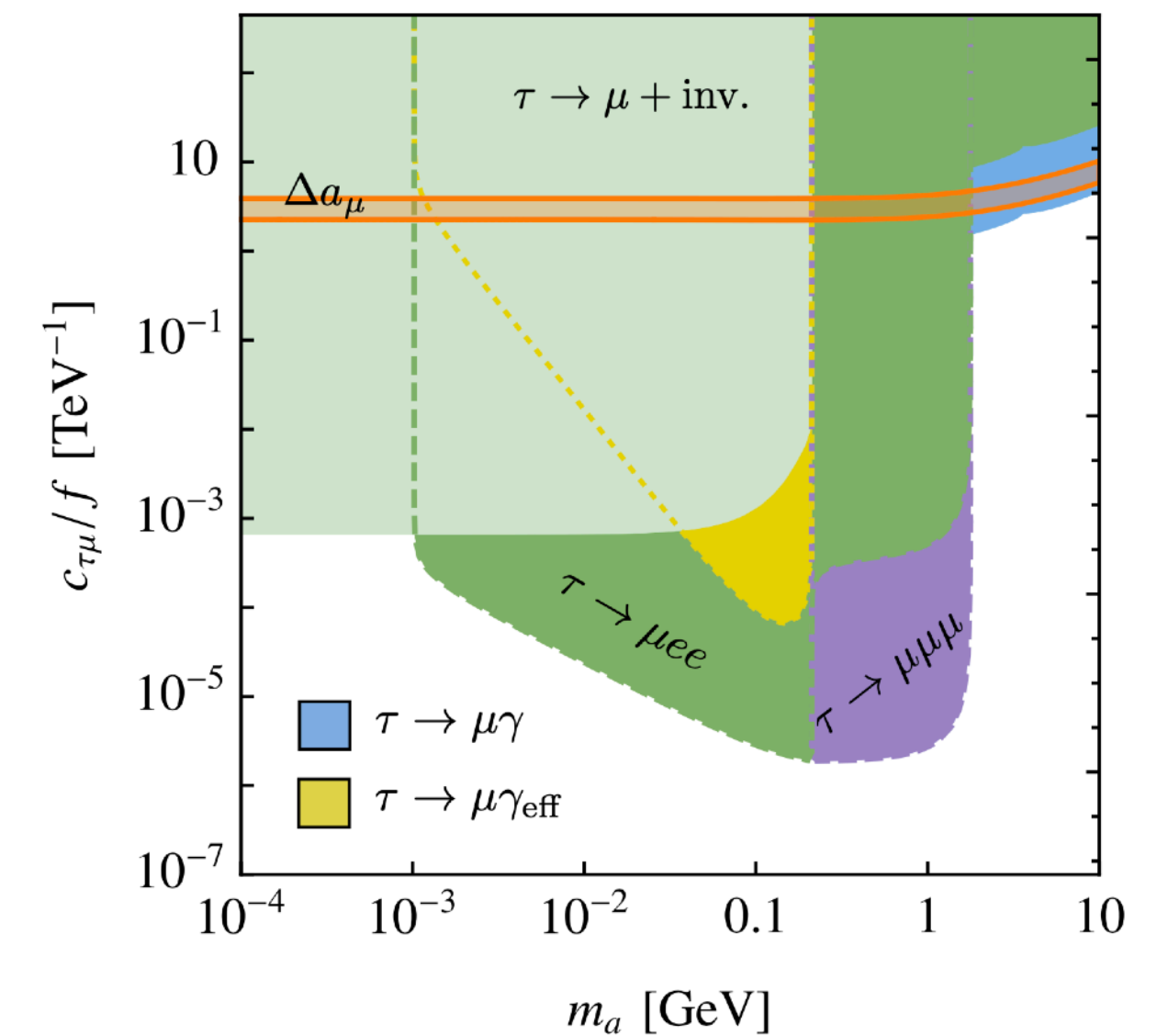
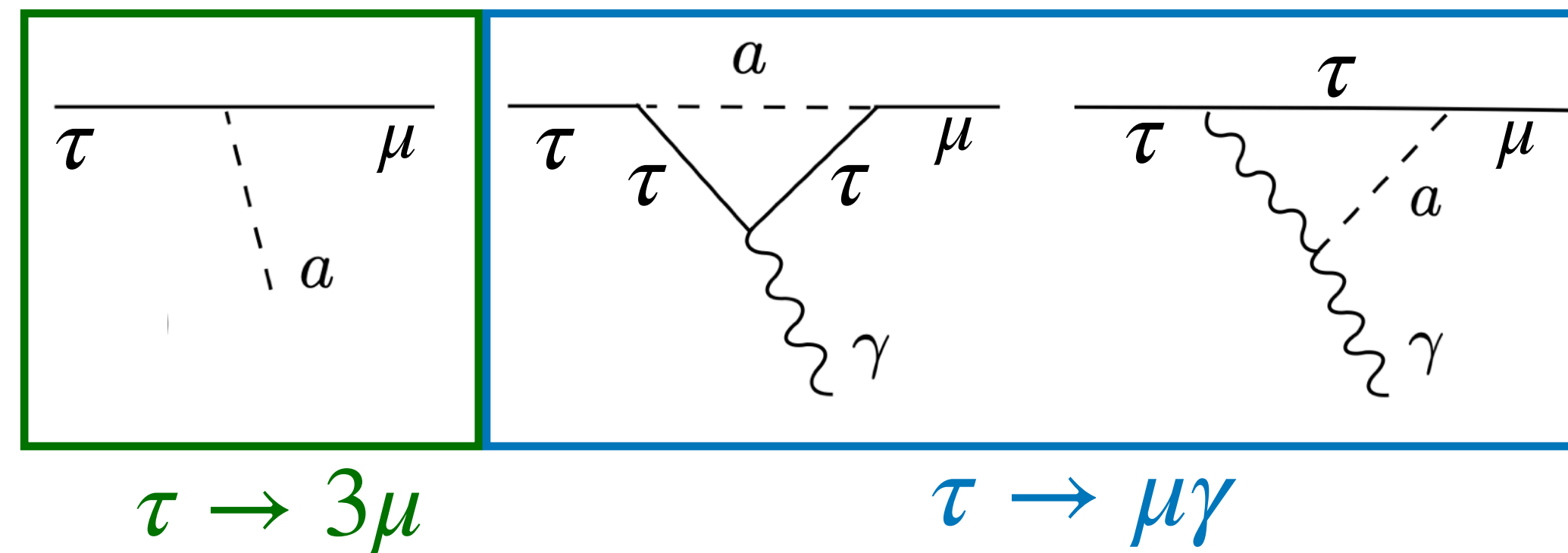
FCC Snowmass report, 2203.06520

Decay	Present bound	FCC-ee sensitivity
$Z \rightarrow \mu e$	$0.75 \times 10^{-6}$	$10^{-10} - 10^{-8}$
$Z \rightarrow \tau \mu$	$12 \times 10^{-6}$	$10^{-9}$
$Z \rightarrow \tau e$	$9.8 \times 10^{-6}$	$10^{-9}$
$\tau \rightarrow \mu \gamma$	$4.4 \times 10^{-8}$	$2 \times 10^{-9}$
$\tau \rightarrow 3\mu$	$2.1 \times 10^{-8}$	$10^{-10}$

In SMEFT, if you have  $Z \rightarrow \tau \mu$ , then you generate  $\tau \rightarrow 3\mu$  and  $\tau \rightarrow \mu \gamma$



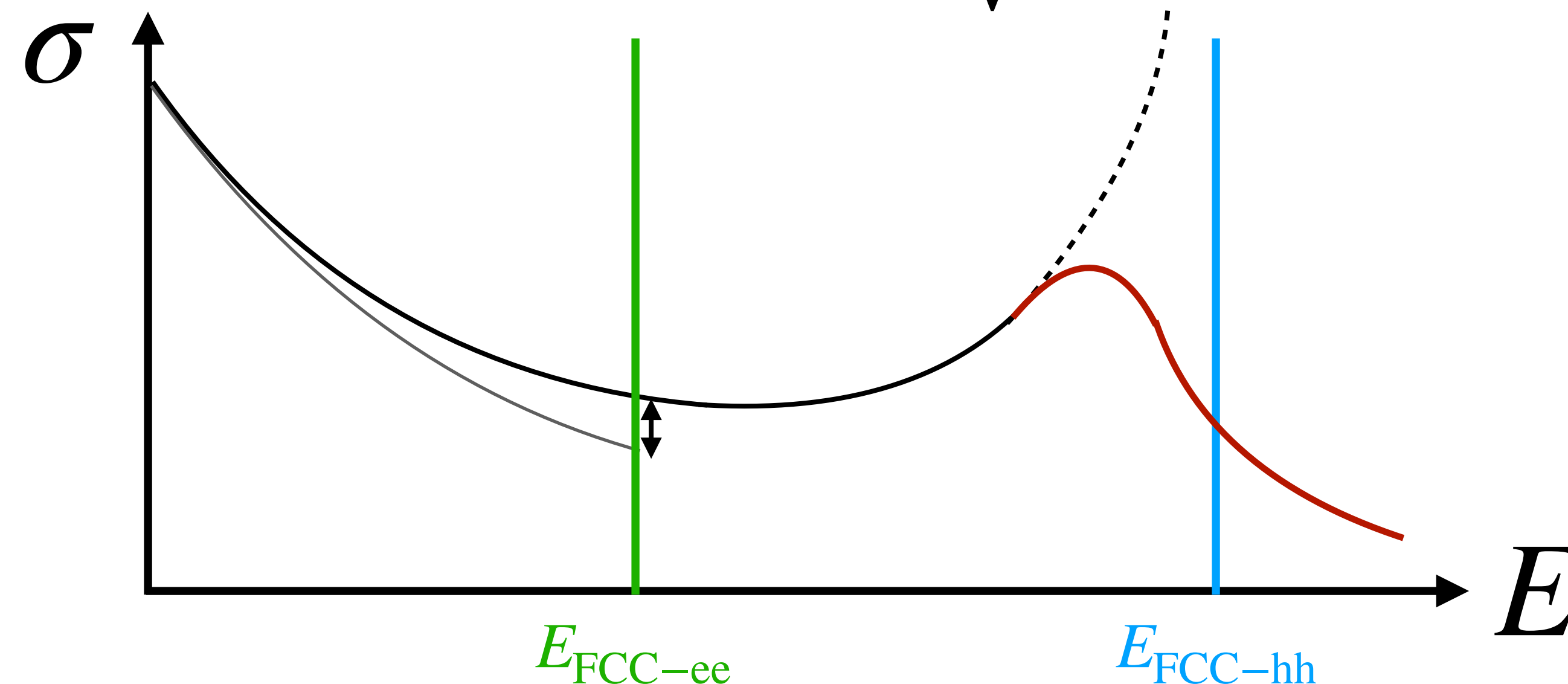
With light new physics, can get a resonant enhancement of  $\tau \rightarrow 3\mu$



# From FCC-ee to FCC-hh

A measured non-zero value of SMEFT Wilson coefficient(s) could provide a no-lose theorem for FCC-hh

Measure  $\frac{C_i}{\Lambda^2} = x \implies$  at energies  $E \lesssim \frac{4\pi}{\sqrt{x}}$ , amplitude violates unitarity



If not, any new physics at FCC-hh will have to pass stringent indirect tests, à la S, T parameters of LEP: informs search strategies

# Summary

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After the LHC, questions will still remain about the third generation of fermions and about the Yukawa sector of the SM

FCC-ee provides multiple lines of attack to close in on these, including:

- *Flavour factory* via copious  $b$ ,  $c$  mesons and  $\tau$ s produced at the Z pole
- *Measurements of Higgs couplings to fermions*
- *Precision Z pole and W pole measurements*
- *Top precision*

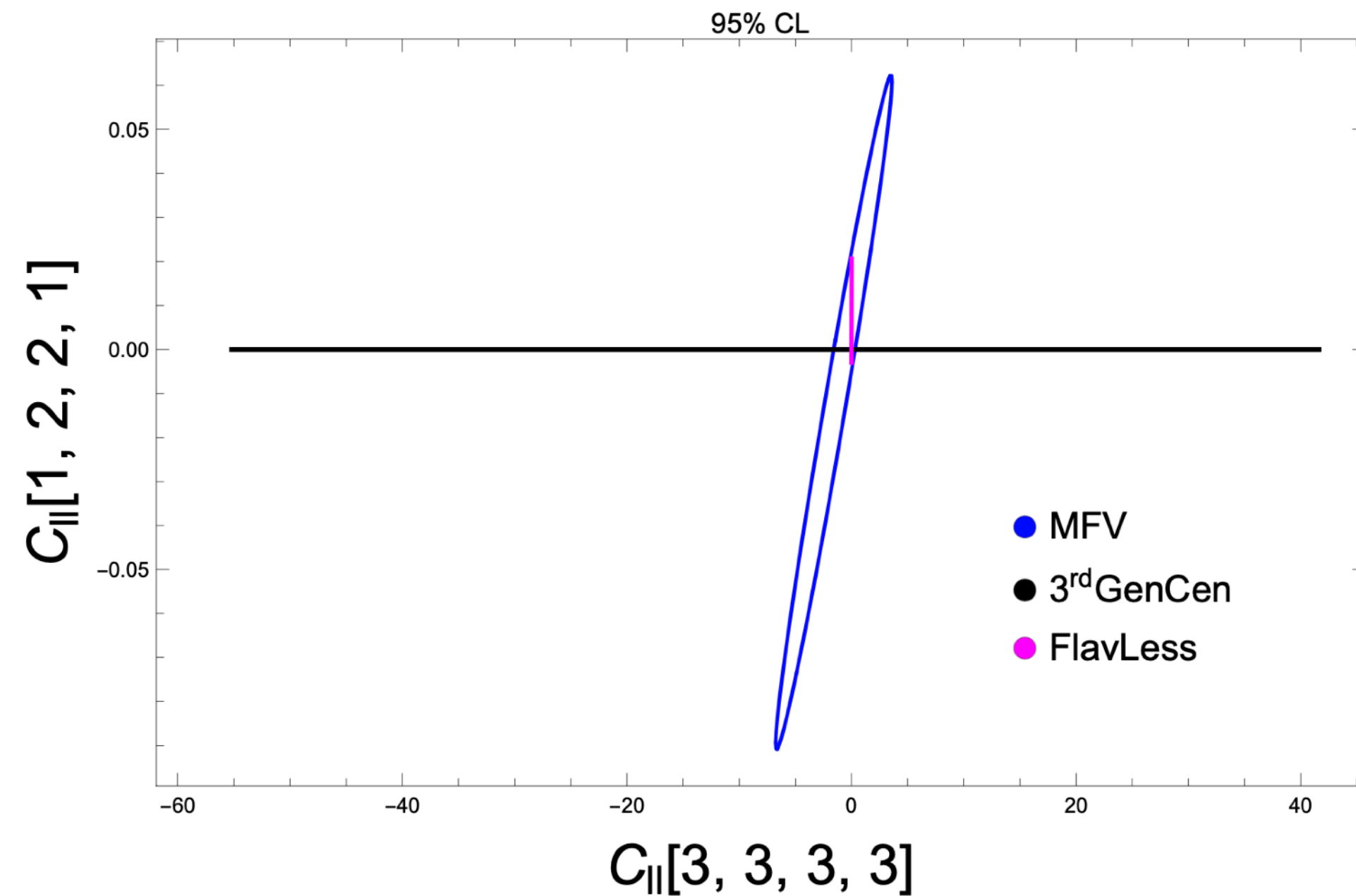
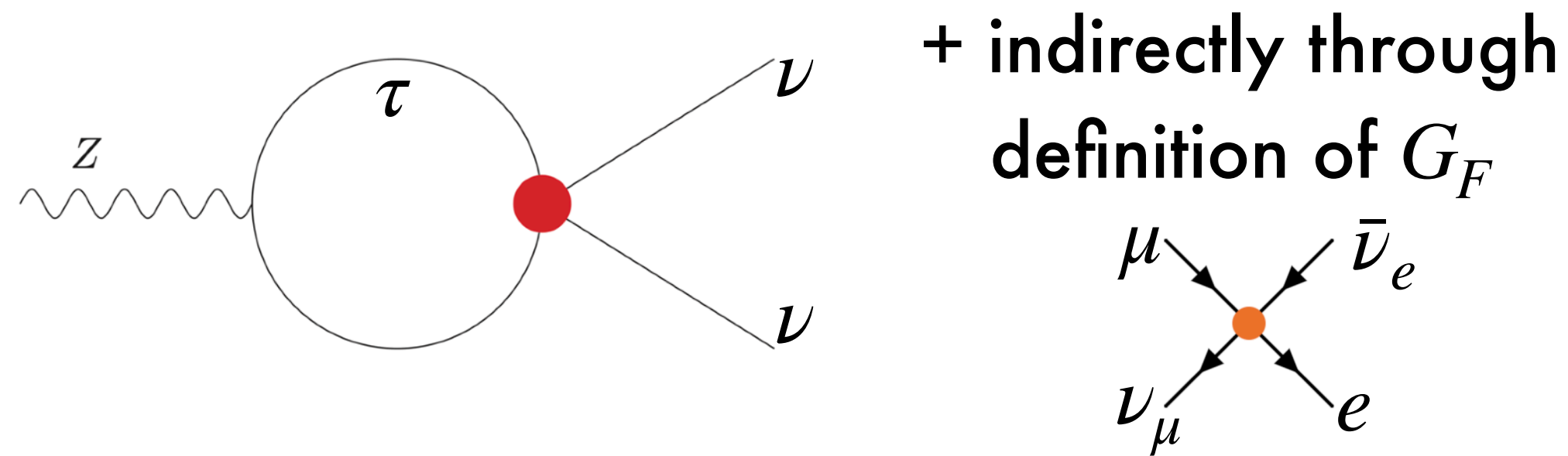
**All of these play an important role, and their combination will help understand the SM and beyond**

**backup**

# Flavour and EW precision

For Z pole measurements, flavour matters

## 4-lepton operators



Bellafronte, Dawson, Giardino  
2304.00029

## Z-quark operators

