

Complementarity of Physics at the FCC and at the High Energy Muon Collider

JULY 6 2023

ROBERTO FRANCESCHINI (ROMA 3 UNIVERSITY)



Diverse Tools

FCC- ee + hh

- largely inspired by the LEP+LHC “recipe”
- “stand-alone” physics case of each energy stage
- synergy between energy stages
- dedicated high-intensity stages of e^+e^- runs
- “final” stage of hadron collisions for “exploration”
- “high-lumi” hadron stage can also do some precision, including through high-energy precision

High energy muon collider

- A lepton collider, but a completely new breed (not LEP-like)
- “stand-alone” physics case of each energy stage
- synergy between energy stages
- high-intensity and high-pT physics pursued in the same run
- high energy leads to interesting “partons” collision (e.g. $WW \rightarrow h$)
- naturally inclined toward highest energies (tens of TeV)
- high-energy precision can be a more than adequate substitute for pole precision

Diverse Tools

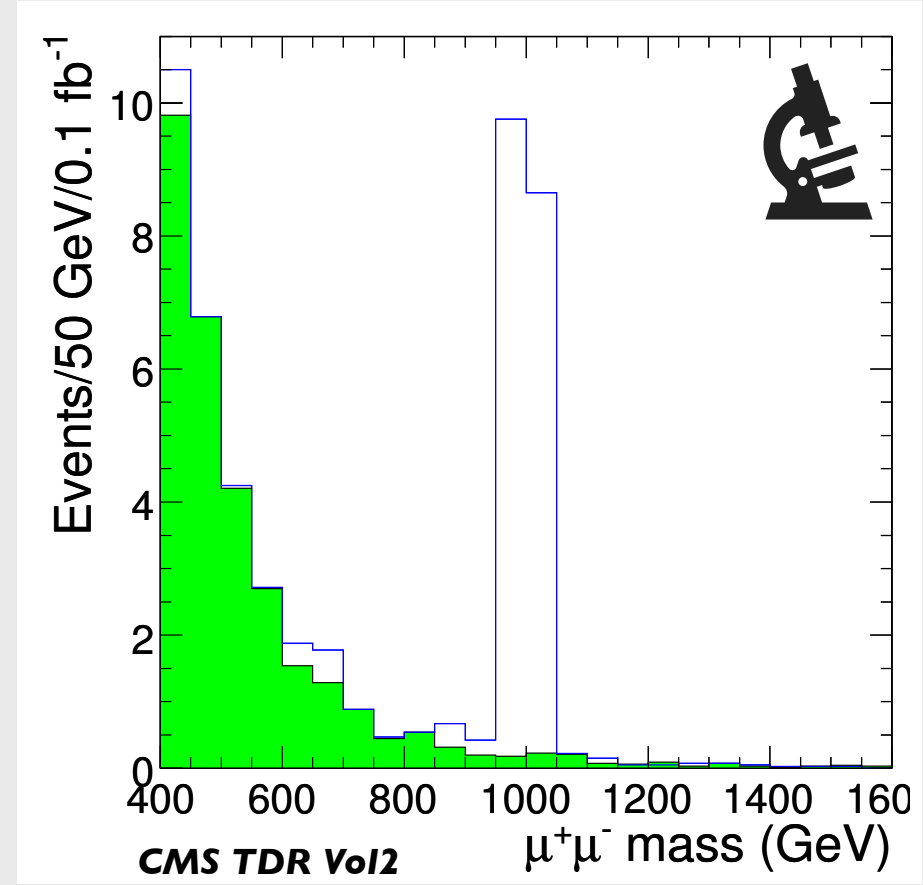
FCC-*ee* + *hh*

- largely inspired by the LEP+LHC “recipe”

summer 2003

	measurement	fit	10^{meas}	-0^{fit}	$1/\sigma^{\text{meas}}$
$\Delta\alpha_{\text{had}}^{(5)}(m_z)$	0.02761 ± 0.00036	0.02767			
m_z (GeV)	91.1875 ± 0.0021	91.1875			
Γ_z (GeV)	2.4952 ± 0.0023	2.4960			
σ_{had}^0 (nb)	41.540 ± 0.037	41.478			
R_f	20.767 ± 0.025	20.742			
$A_{\text{fb}}^{0,l}$	0.01714 ± 0.00095	0.01636			
$A_f(P_z)$	0.1465 ± 0.0032	0.1477			
R_b	0.21638 ± 0.00066	0.21579			
R_c	0.1720 ± 0.0030	0.1723			
$A_{\text{fb}}^{0,b}$	0.0997 ± 0.0016	0.1036			
$A_{\text{fb}}^{0,c}$	0.0706 ± 0.0035	0.0740			
A_b	0.925 ± 0.020	0.935			
A_c	0.670 ± 0.026	0.668			
$A_f(\text{SLD})$	0.1513 ± 0.0021	0.1477			
$\sin^2\Theta_{\text{eff}}^{\text{lept}}(Q_{\text{fb}})$	0.2324 ± 0.0012	0.2314			
m_W (GeV)	80.426 ± 0.034	80.385			
Γ_W (GeV)	2.139 ± 0.069	2.093			
m_t (GeV)	174.3 ± 5.1	174.3			
$Q_W(\text{Cs})$	-72.84 ± 0.46	-72.90			

CERN Courier

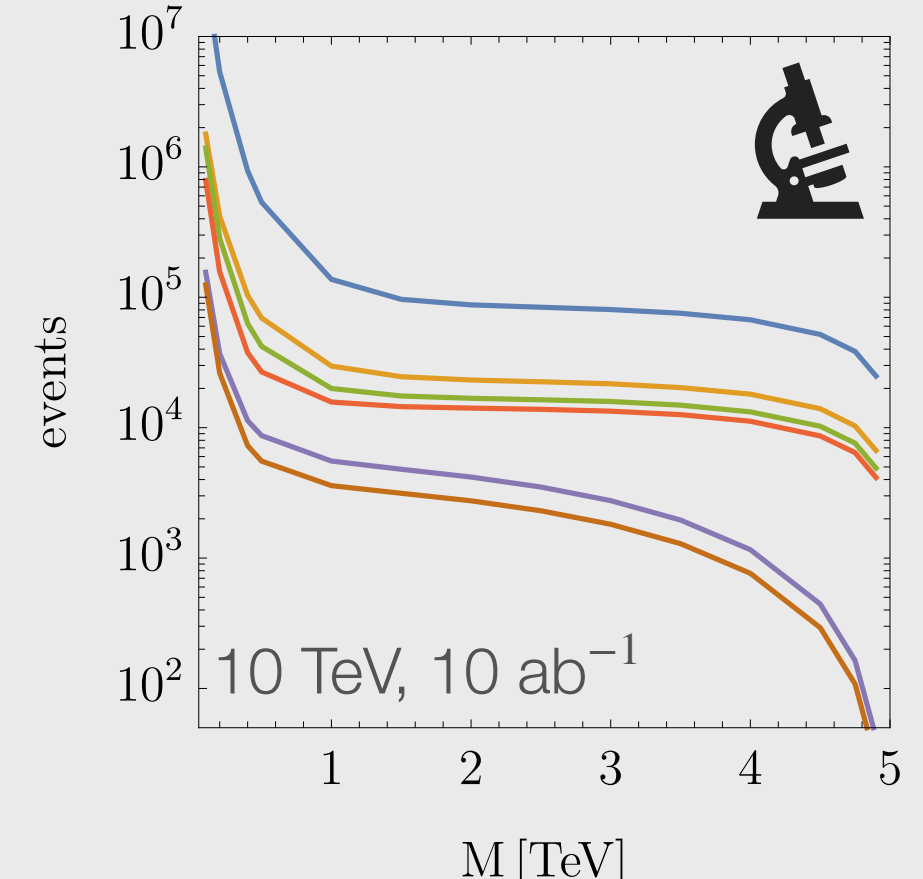
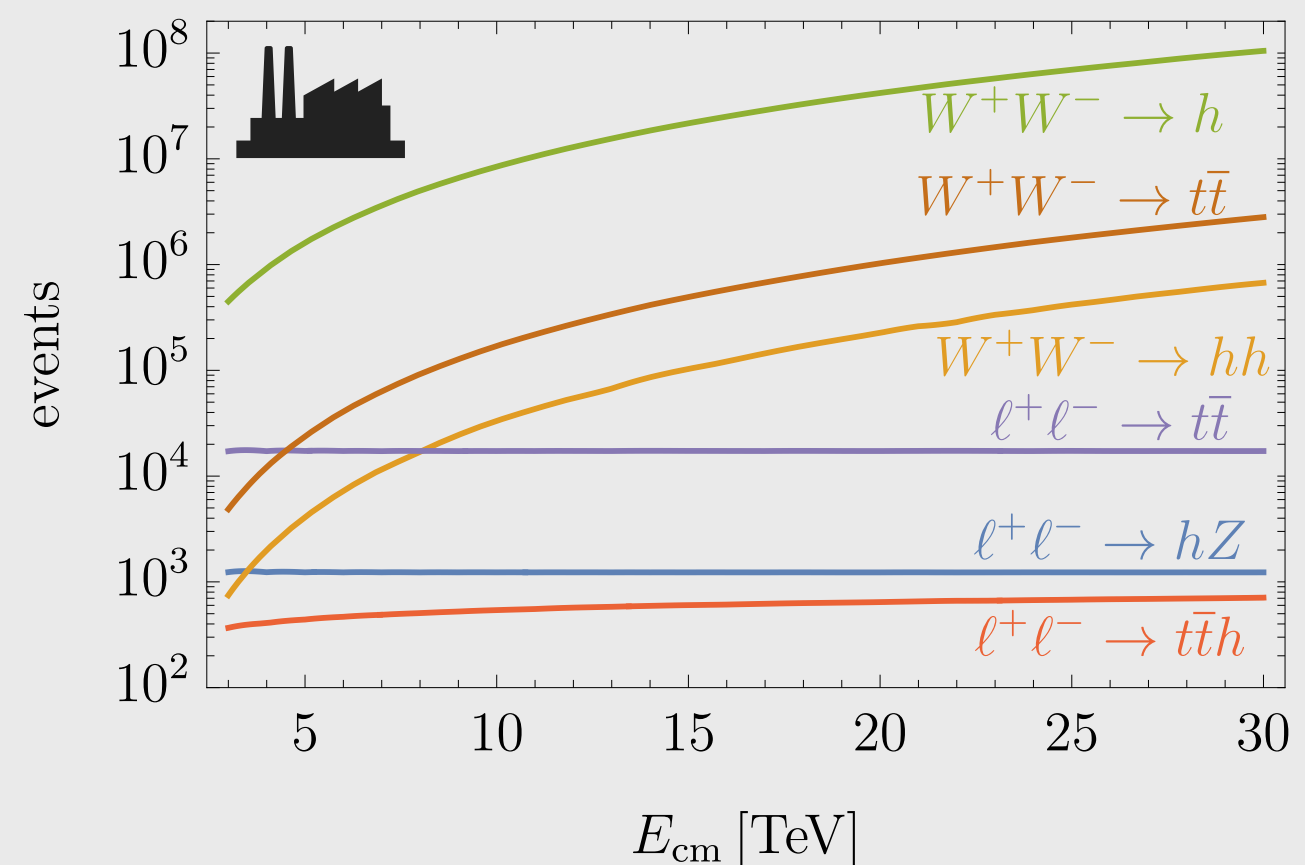


High energy muon collider

- Stages at several TeV: e.g. 3 TeV and 10 TeV
- possibility to foresee higher energy runs, e.g. 30 TeV

- $$\mathcal{L} = 10\text{ab}^{-1} \left(\frac{E_{cm}}{10 \text{ TeV}} \right)^2$$

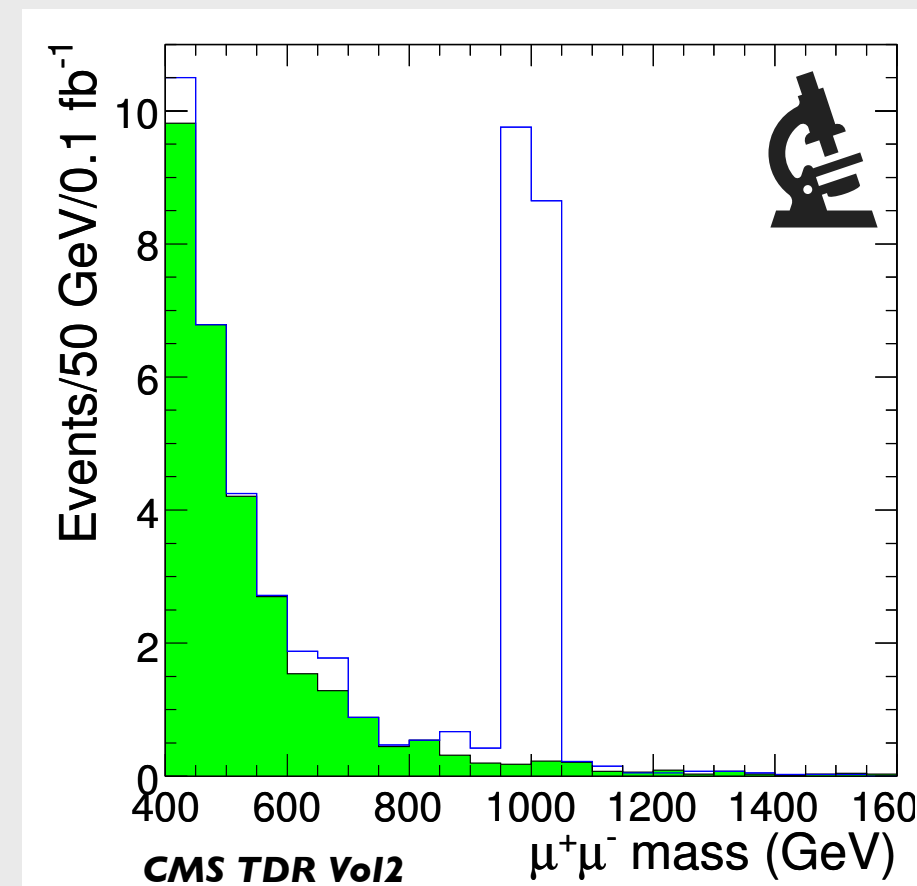
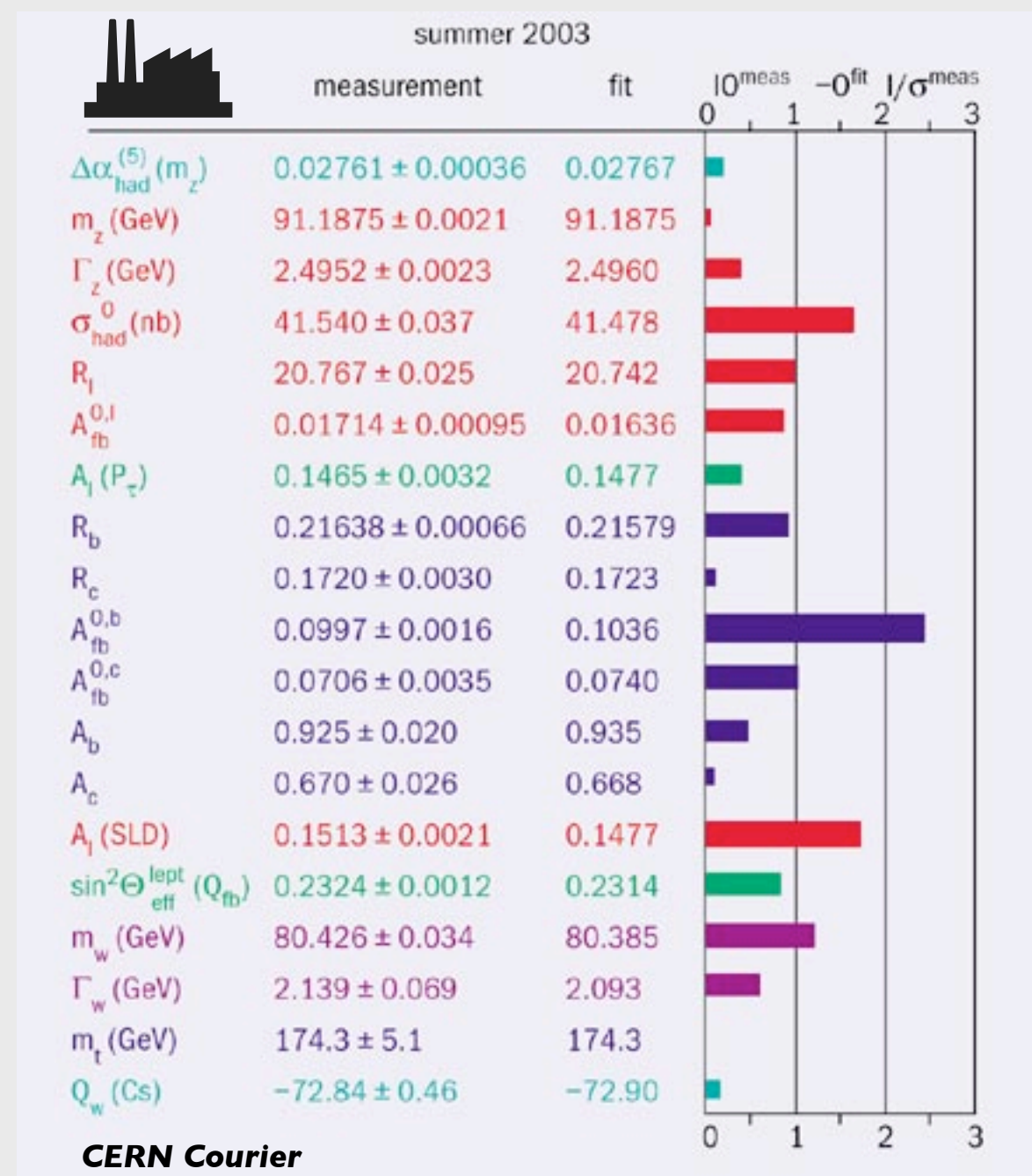
- tens of thousands of new physics states
- millions of top quarks and Higgs bosons, billions of vector bosons, ... (“multiplex” factory)



Diverse Tools

FCC- ee + hh

- largely inspired by the LEP+LHC “recipe”

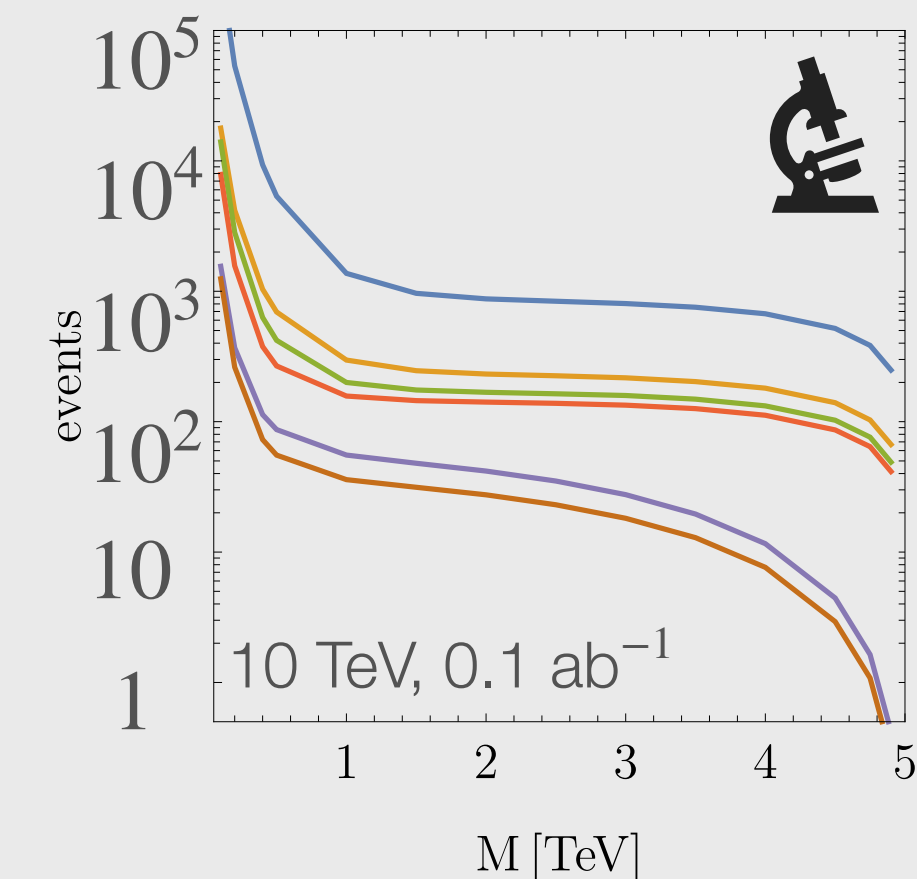
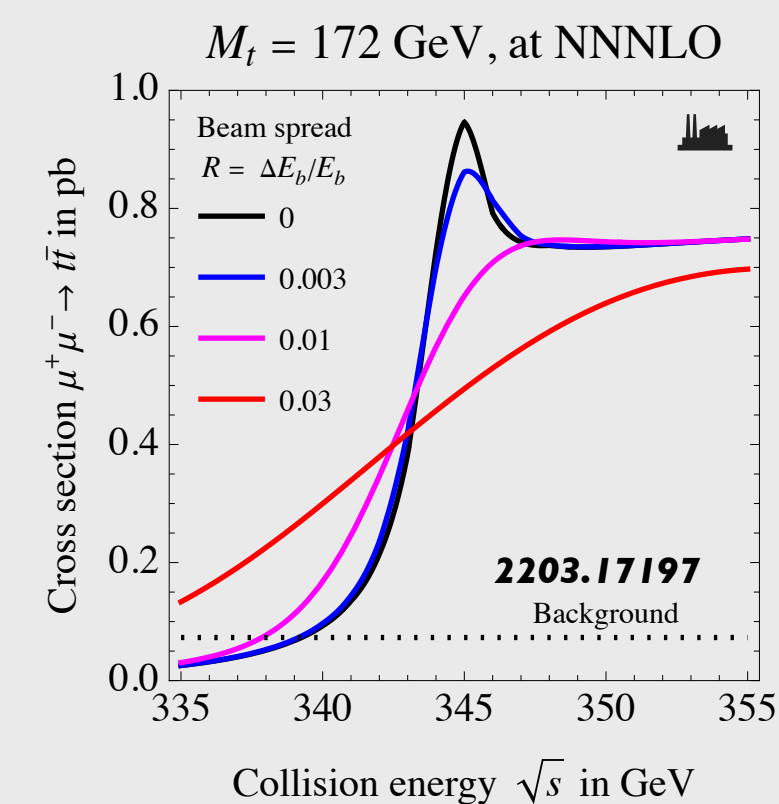


High energy muon collider

- Stages at several TeV: e.g. 3 TeV and 10 TeV
- possibility to foresee higher energy runs, e.g. 30 TeV

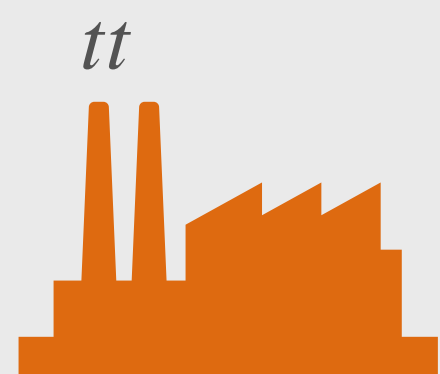
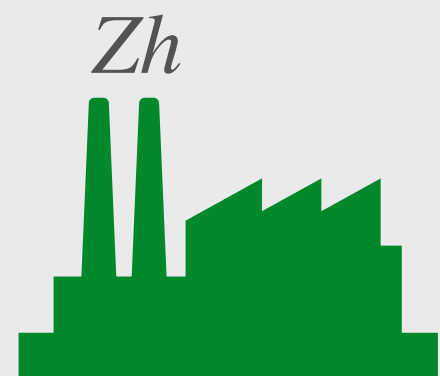
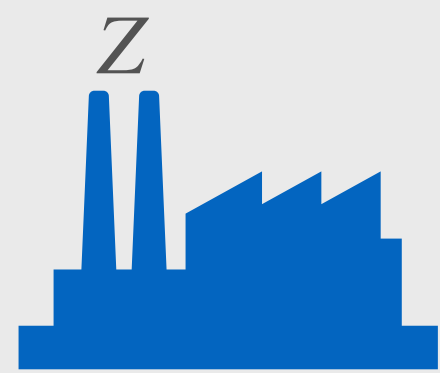
$$\mathcal{L} = 0.1 \text{ ab}^{-1} \left(\frac{E_{cm}}{10 \text{ TeV}} \right)^2$$

- hundreds of events of new physics states
- still able to perform SM measurements e.g. threshold scans

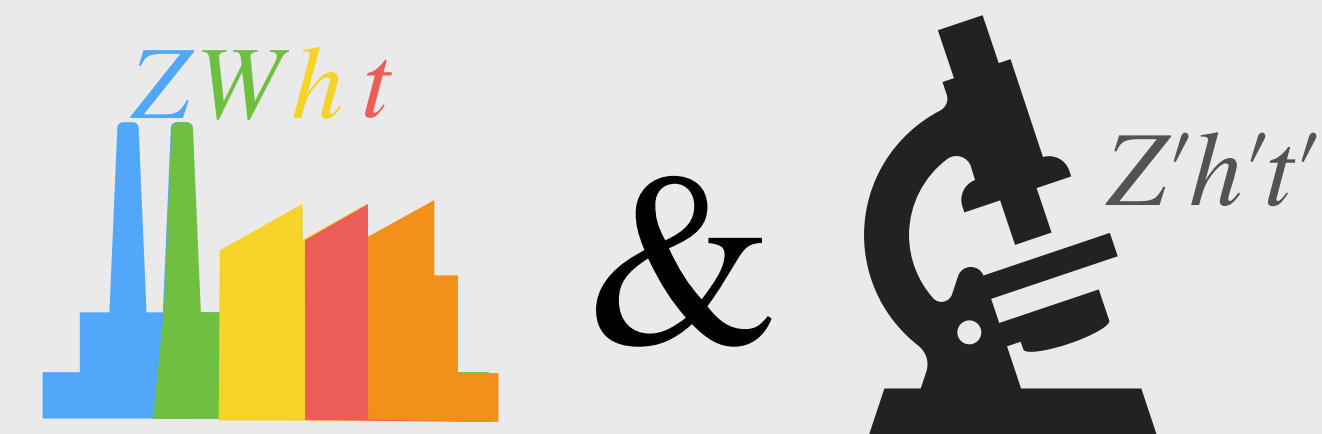


Diverse Tools

FCC- ee + hh



High energy muon collider



*drawings of the left side and right side not to a common scale

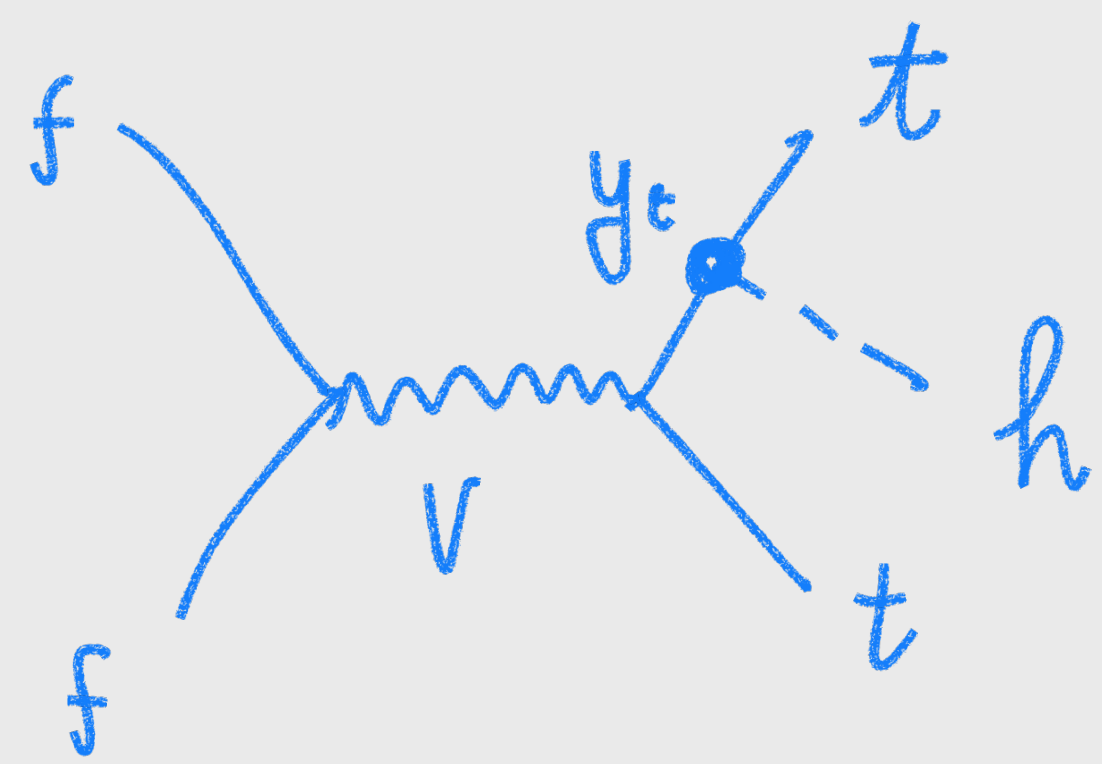
time \downarrow E_{cm}

Common problems and solutions

a typical example of complementarity on

Top quark couplings

Joint-ventures on the Yukawa of the top quark



$$\sigma \propto g_{ttV}^2 y_t^2 g_{ffV}^2$$

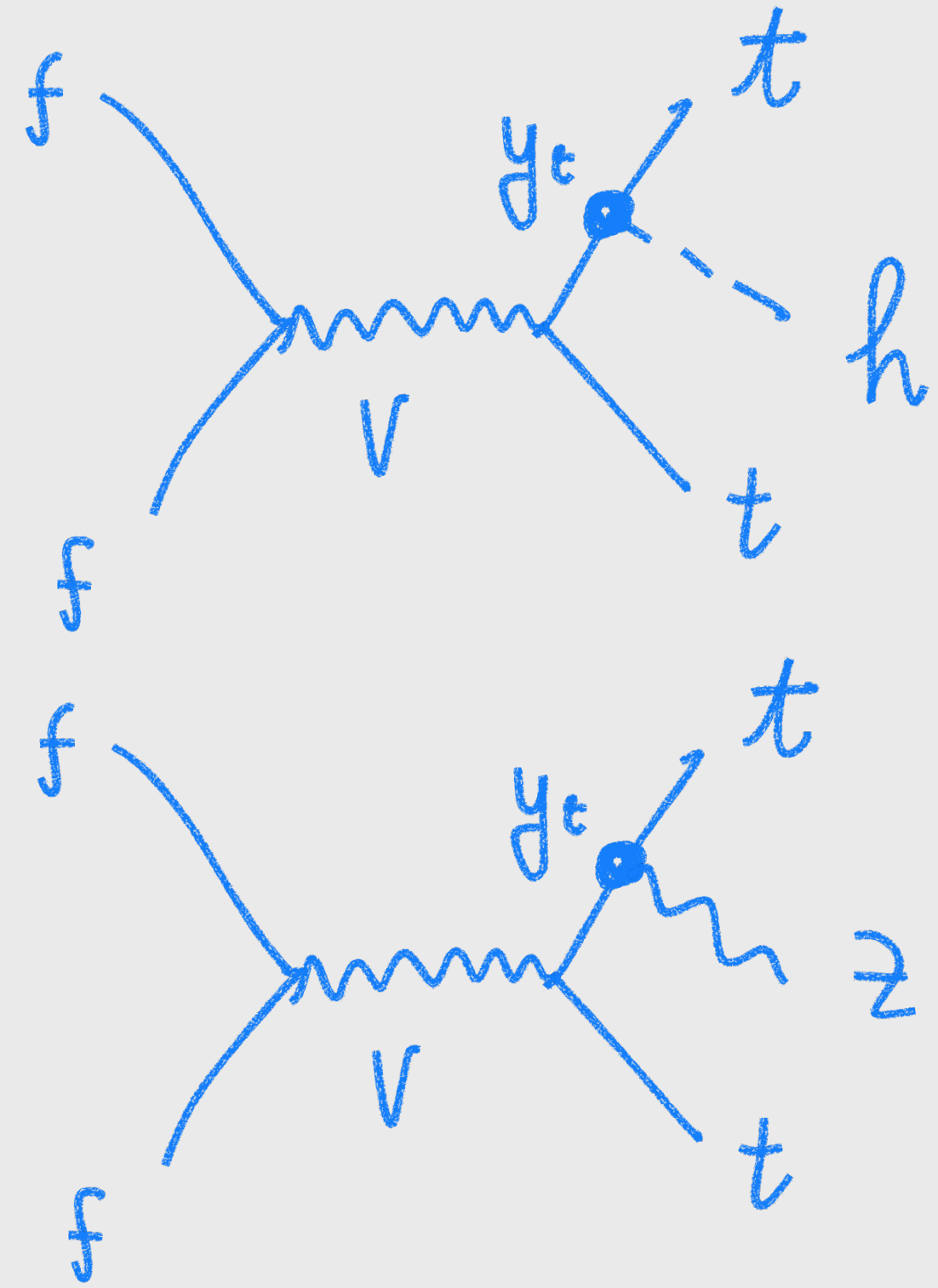
$$\sigma_{t\bar{t}h}^{100 \text{ TeV}} = 33.9 \left(1 \pm \underbrace{0.08}_{\text{SCALE VARIATION NLO}} \pm \overbrace{0.02}^{\text{VAR. PDF}} \right) \cdot 10^6 \text{ ab} \Rightarrow \text{millions of } t\bar{t}h \text{ every year!}$$

1507.08169

$H \rightarrow 4\ell$	$H \rightarrow \gamma\gamma$	$H \rightarrow 2\ell 2\nu$	$H \rightarrow b\bar{b}$
$2.6 \cdot 10^4$	$4.6 \cdot 10^5$	$2.0 \cdot 10^6$	$1.2 \cdot 10^8$

Table 6: $t\bar{t}H$ event rates for various Higgs decay modes, with 20 ab^{-1} at 100 TeV, assuming $t\bar{t} \rightarrow \ell\nu + \text{jets}$. Here and for Higgs decays, ℓ can be either an electron or a muon.

Joint-ventures on the Yukawa of the top quark

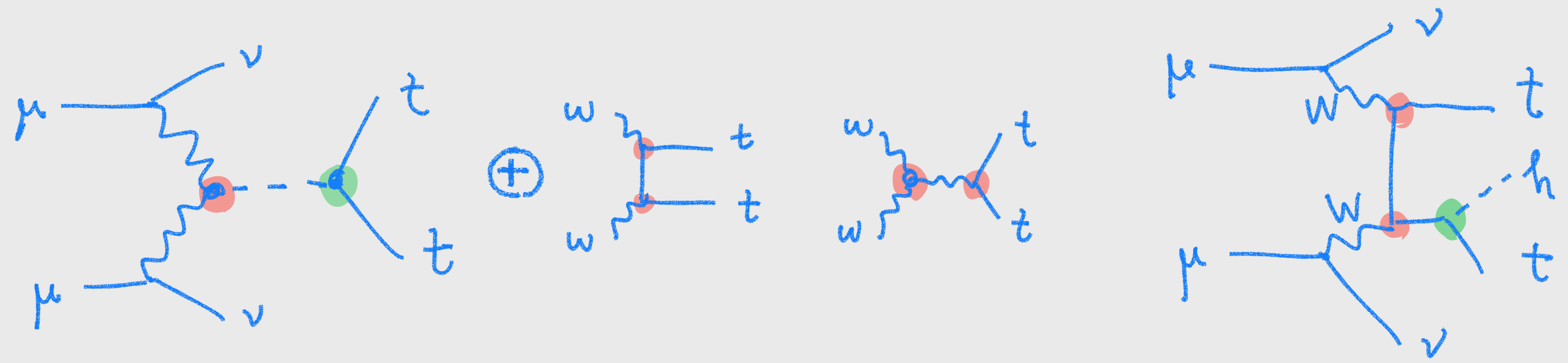


$$\sigma \propto \begin{matrix} \textcircled{g_{ttV}^2} & \textcircled{y_t^2} & \textcircled{g_{ffV}^2} \\ \sigma \propto \textcircled{g_{ttV}^2} & \textcircled{g_{ttZ}^2} & \textcircled{g_{ffV}^2} \end{matrix} \left. \vphantom{\begin{matrix} \textcircled{g_{ttV}^2} & \textcircled{y_t^2} & \textcircled{g_{ffV}^2} \\ \textcircled{g_{ttV}^2} & \textcircled{g_{ttZ}^2} & \textcircled{g_{ffV}^2} \end{matrix}} \right\} \frac{\sigma_{tth}}{\sigma_{ttZ}} \sim \frac{y_t}{g_{ttZ}}$$

FCC-*ee* provides an input to the next machine that can produce lots of *tth* but suffers uncertainty (on absolute rate)

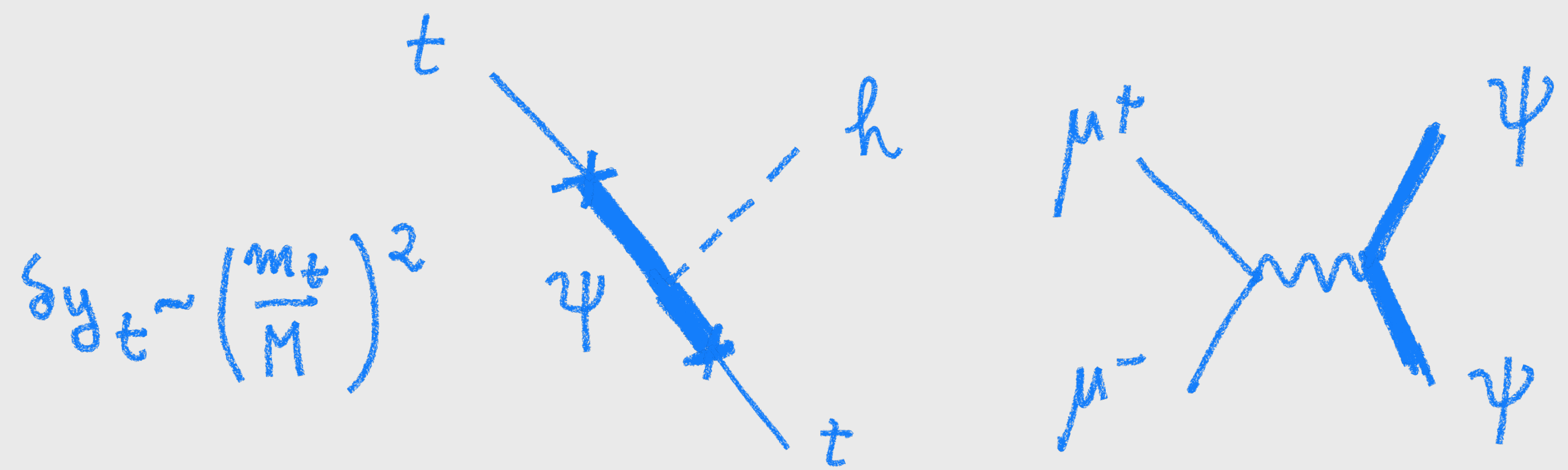
Complementarity by providing precise inputs, whose poor knowledge would spoil a future measurement

Joint-ventures on the Yukawa of the top quark 2212.11067, 2104.05770



Same need for inputs on other couplings, thus can benefit from inputs from FCC- ee
 or a global fit at the μ collider (if sufficiently precise)

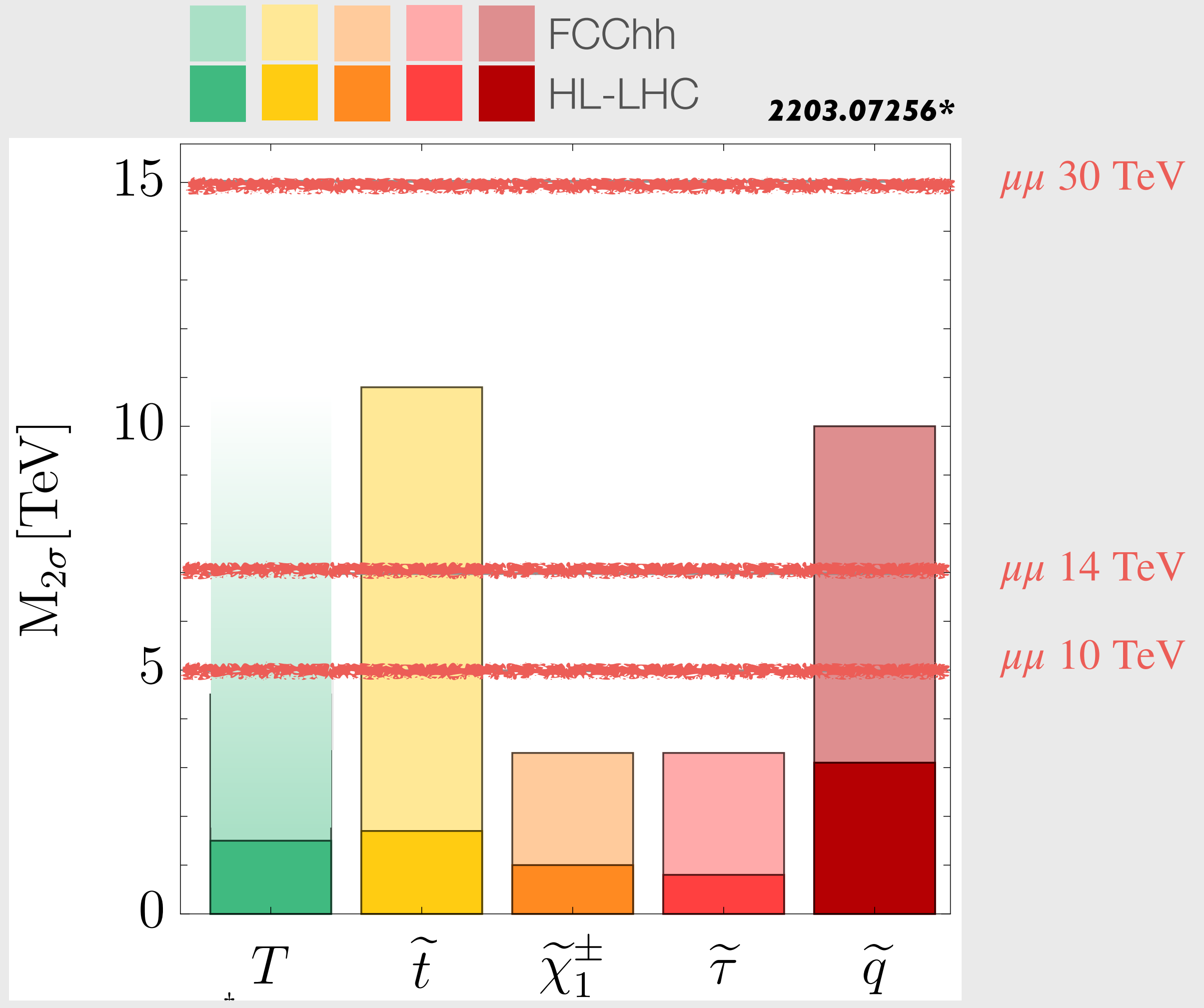
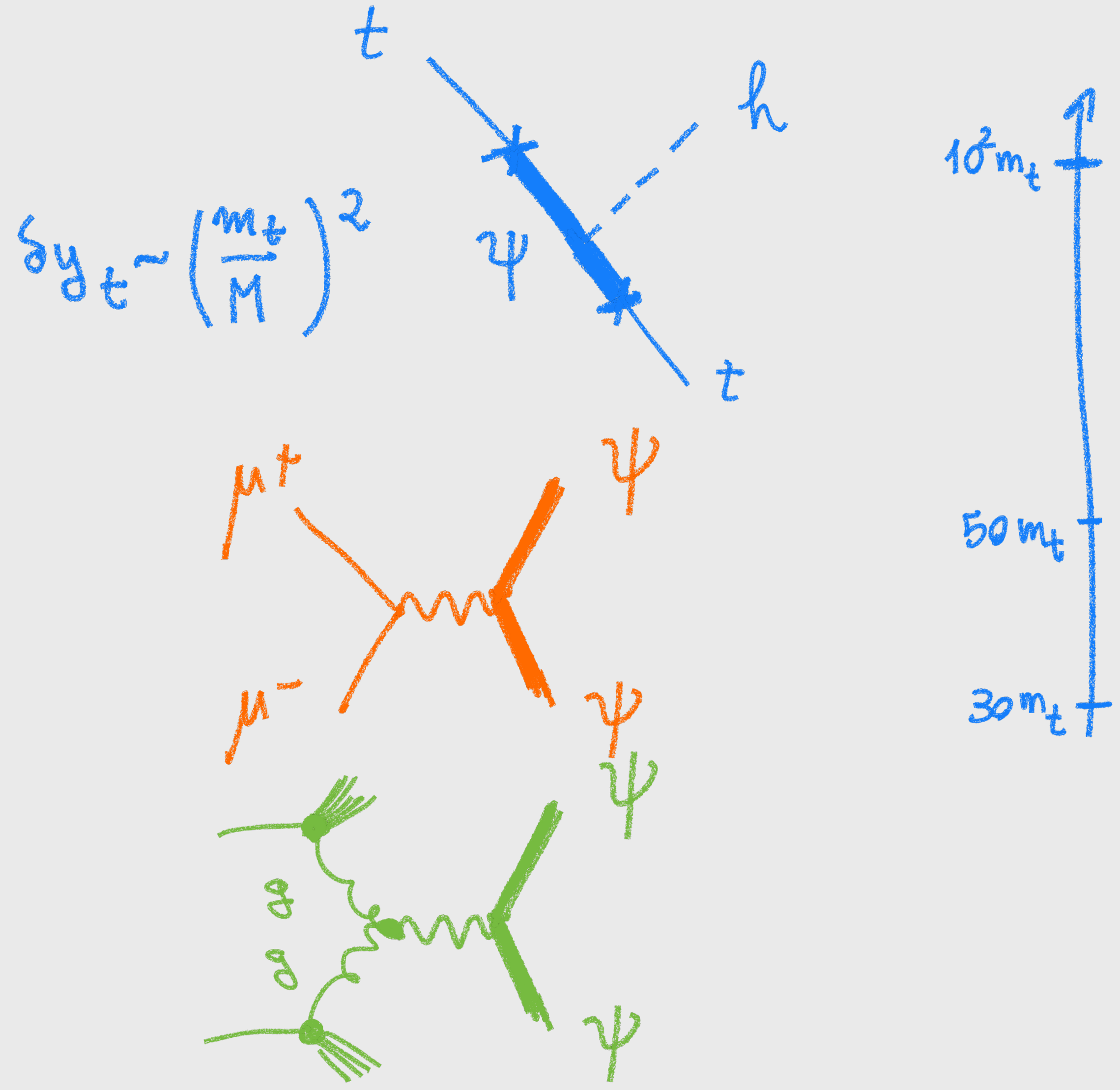
The same muon collider that acts as “top factory” can also test directly the existence of new states responsible for the deviations in the couplings



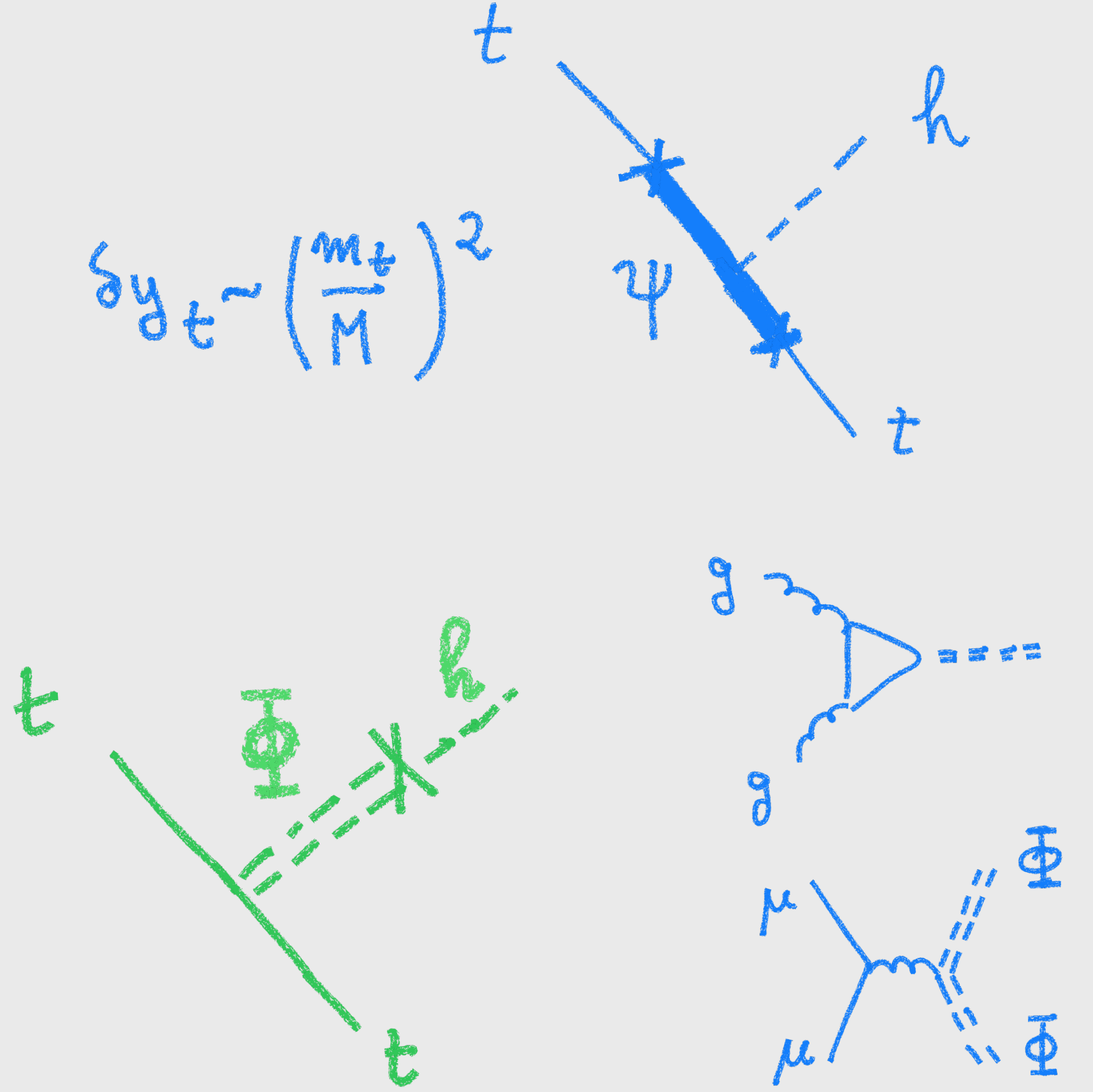
TYPICALLY MUON COLLIDER EXCLUSION UP TO $S_{\mu\mu}/2$

same machine can perform complementary direct and indirect tests of BSM

Joint-ventures on the Yukawa of the top quark

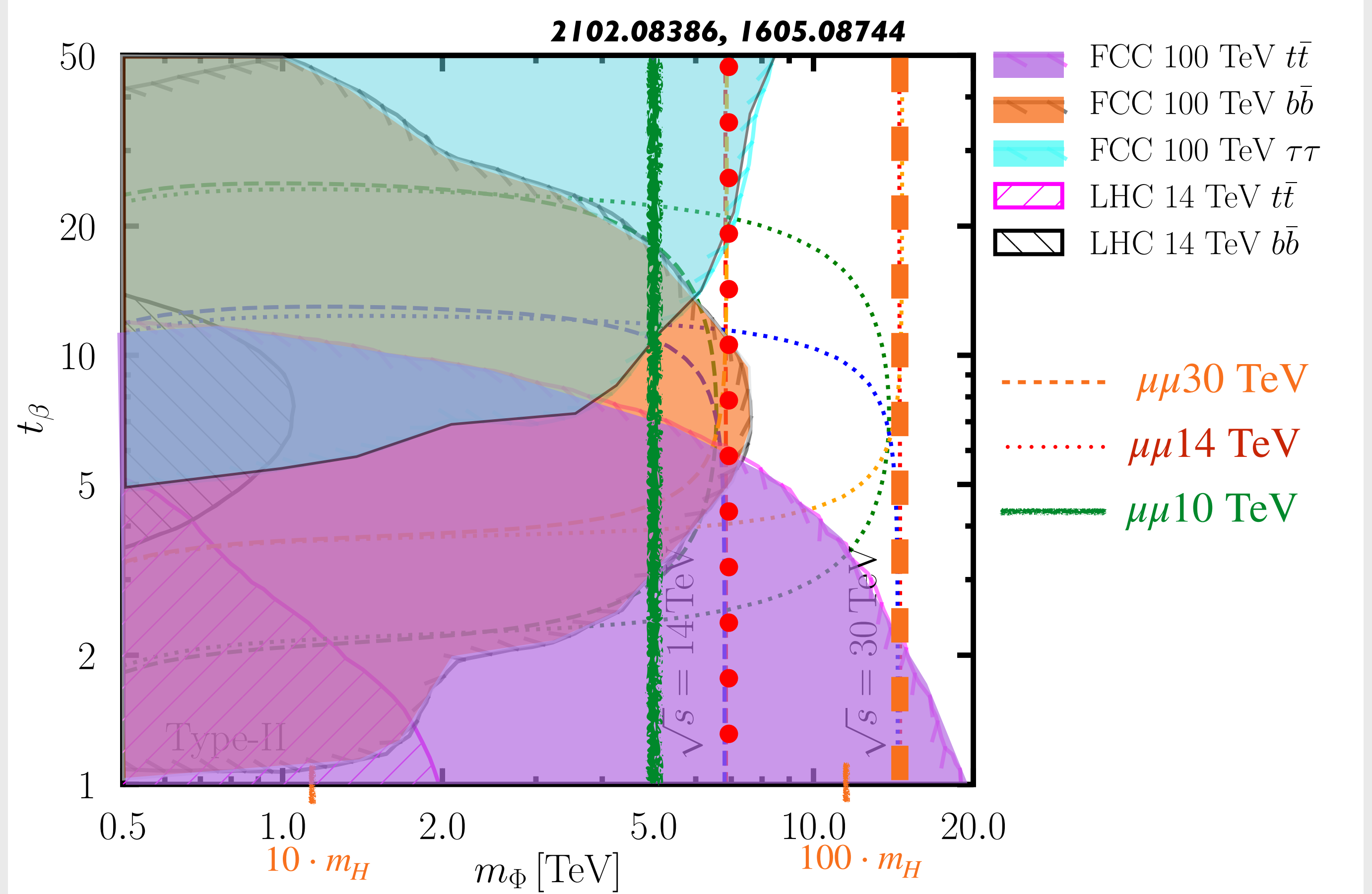
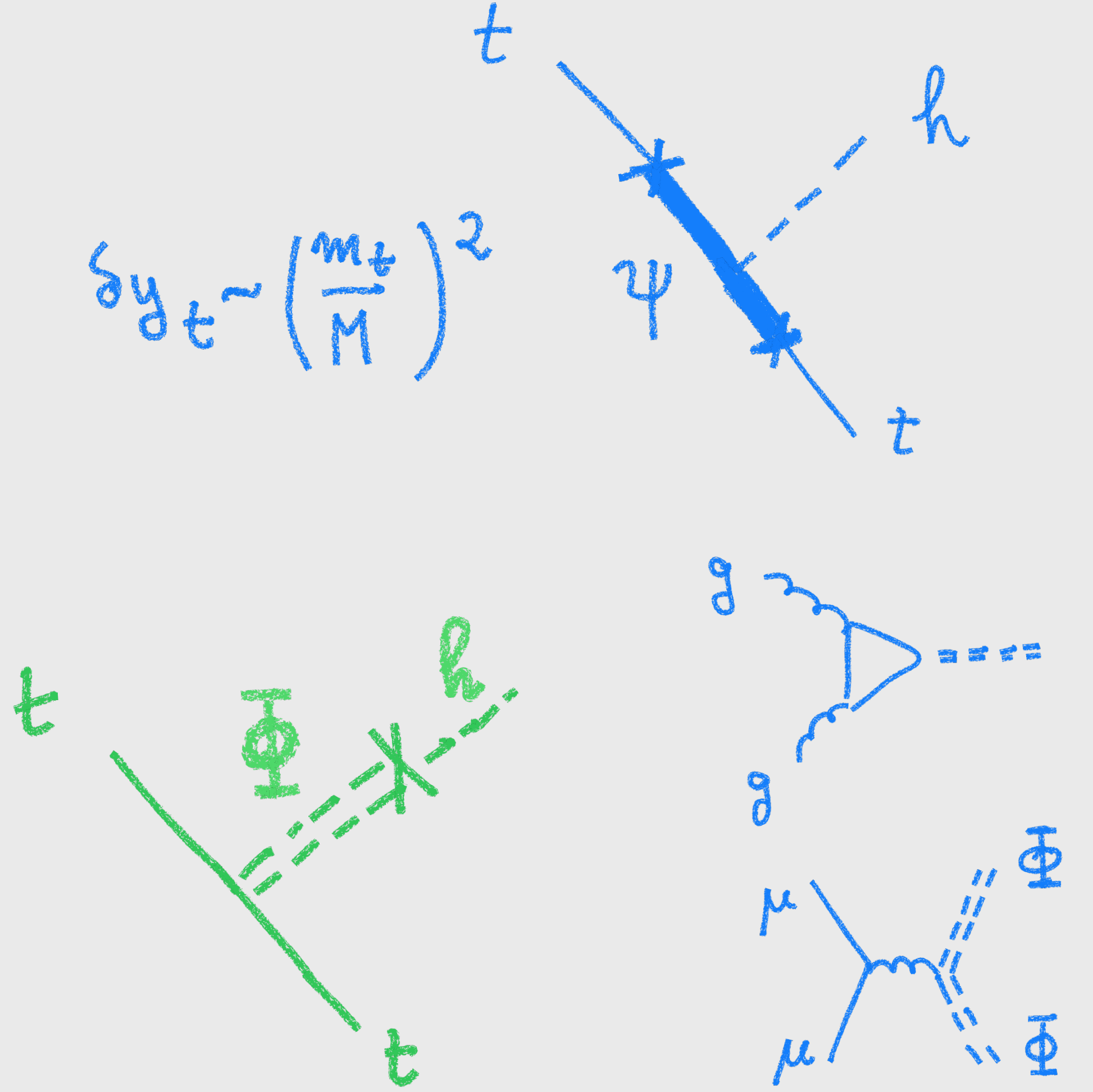


Joint-ventures on the Yukawa of the top quark



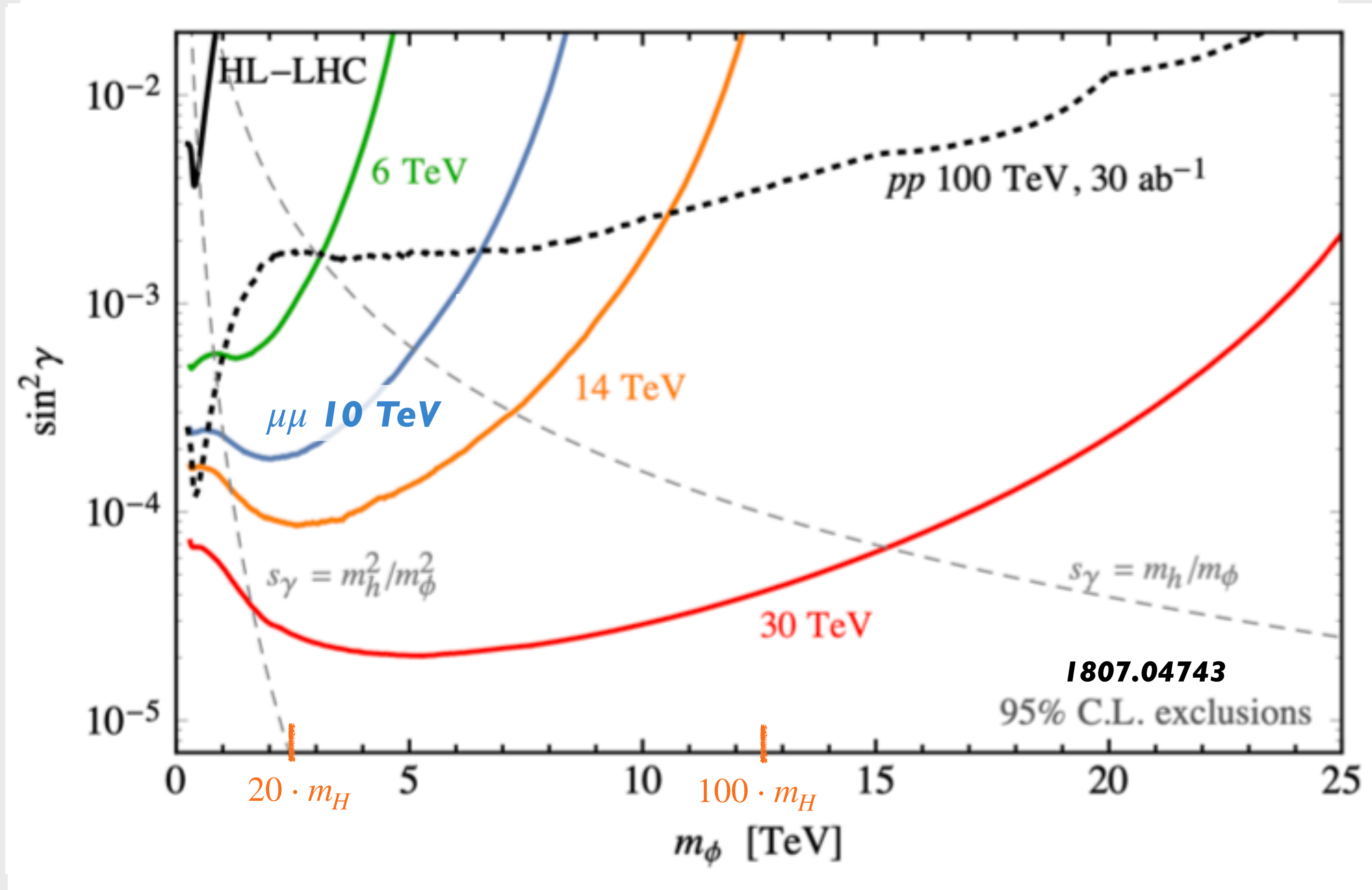
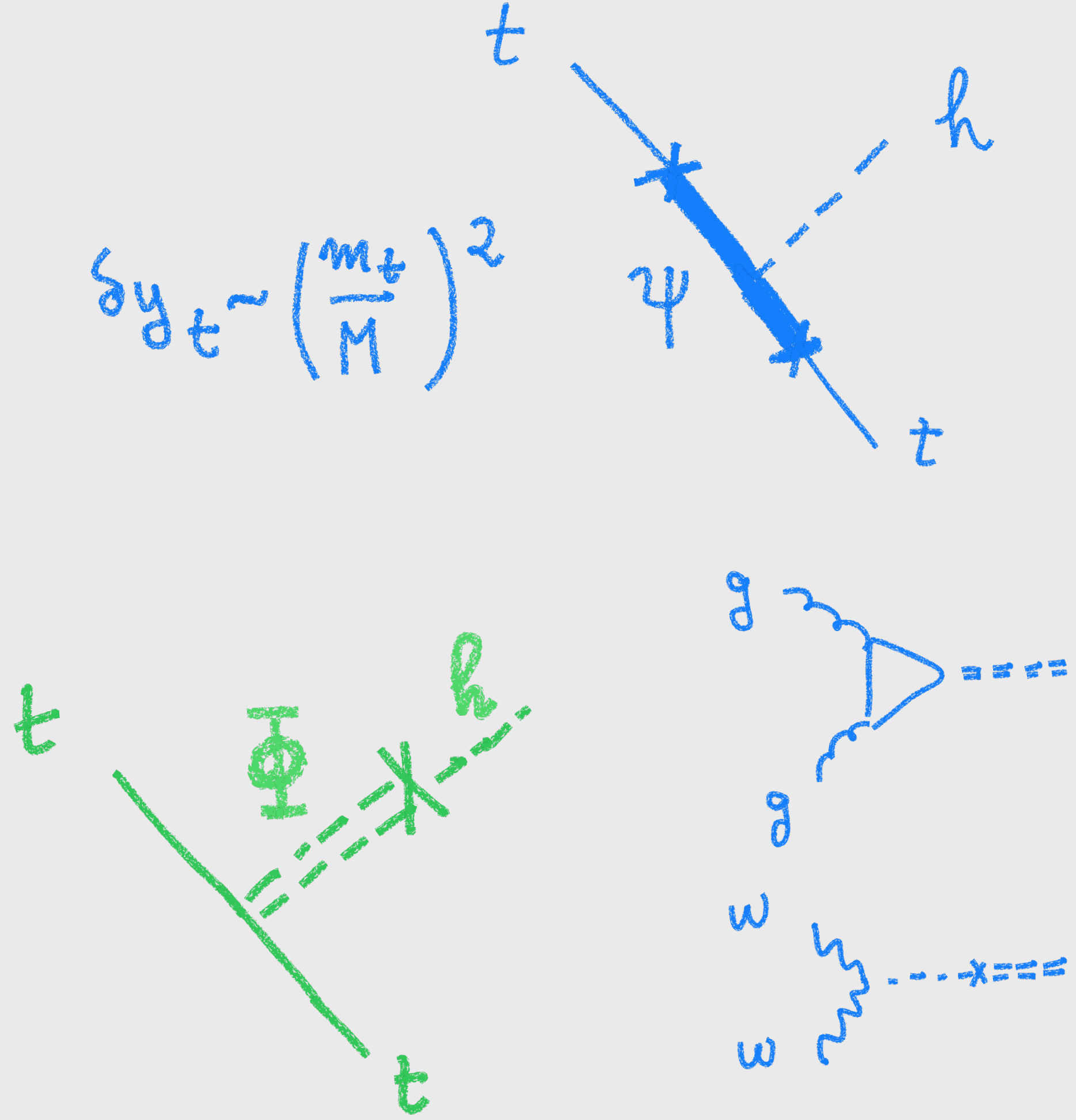
Complementarity: results from the “next” machines can feed-back in the assumptions on the precision studies of the “previous” machine. At $\mu\mu$ “next” and “previous” happen synchronously.

Joint-ventures on the Yukawa of the top quark



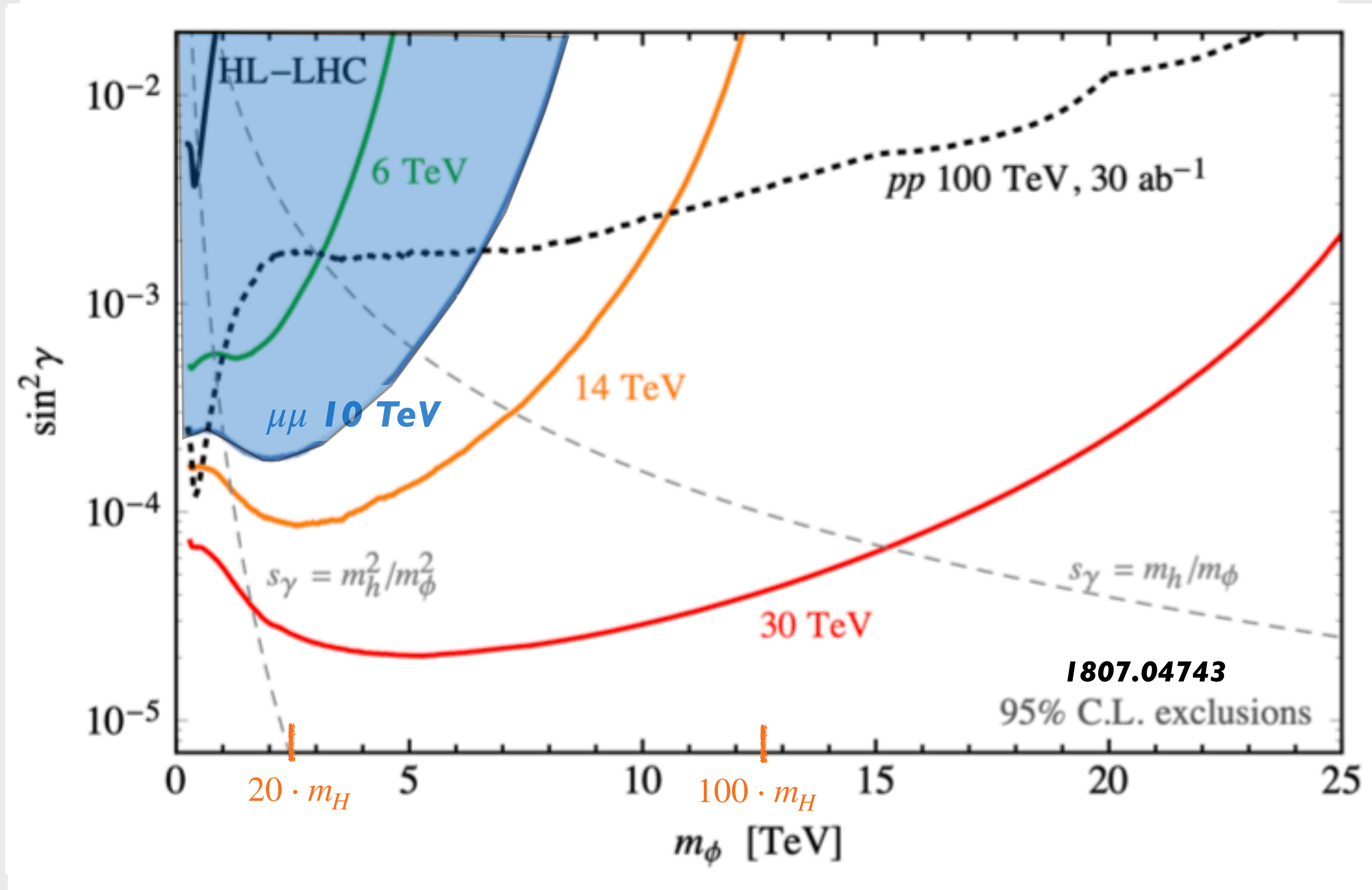
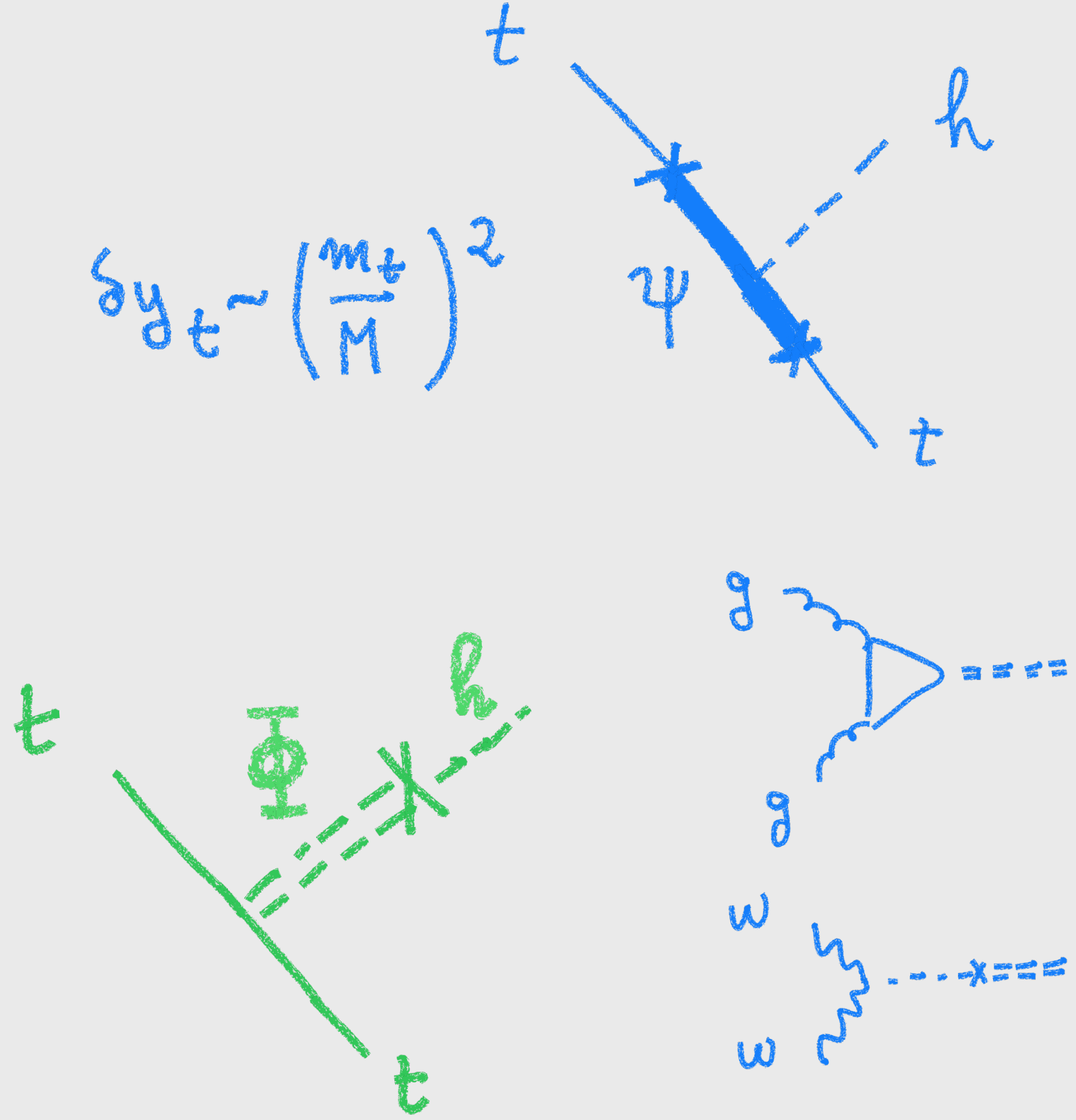
Complementarity: results from the “next” machines can feed-back in the assumptions on the precision studies of the “previous” machine. At $\mu\mu$ “next” and “previous” happen synchronously.

Joint-ventures on the Yukawa of the top quark



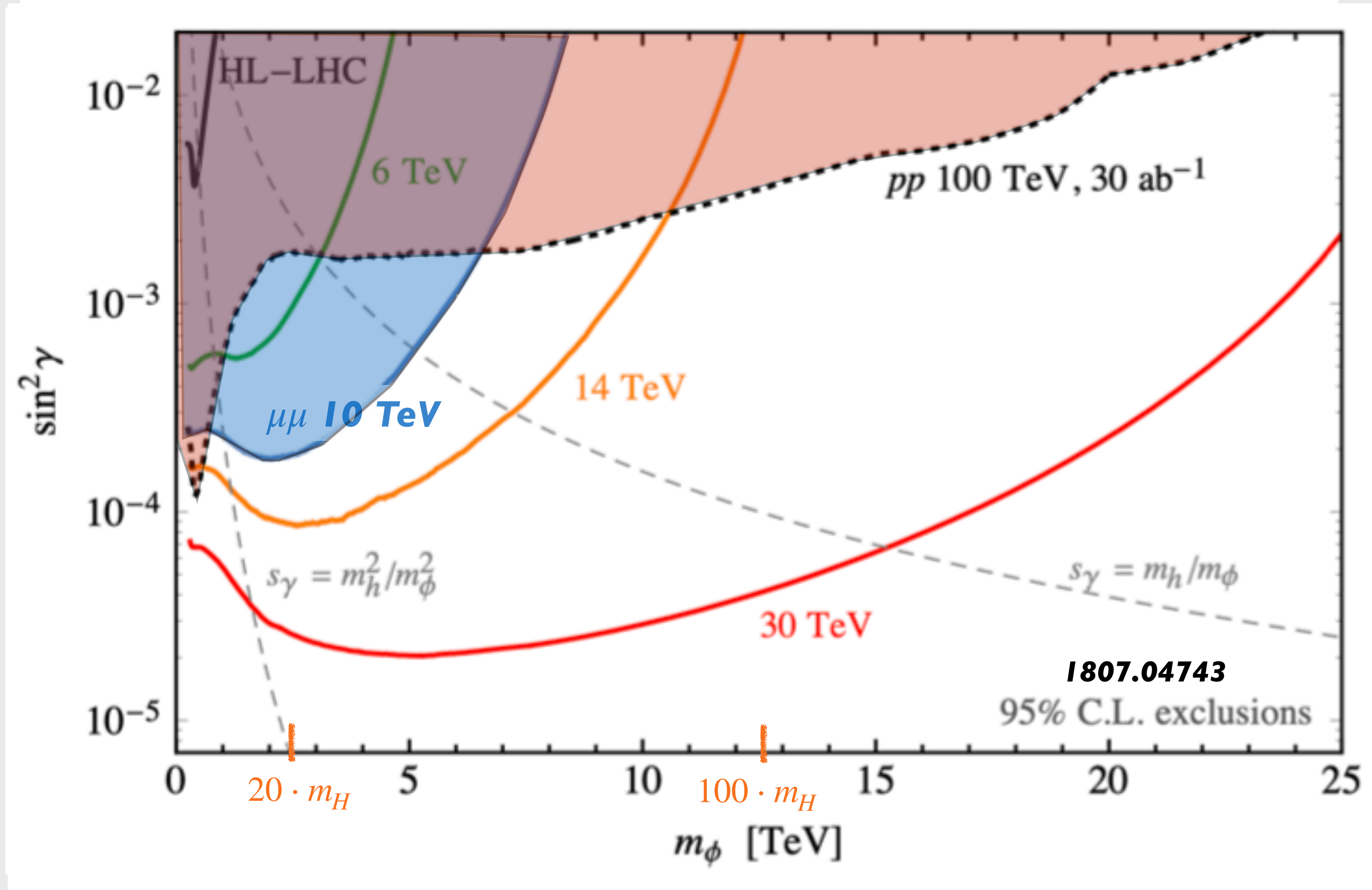
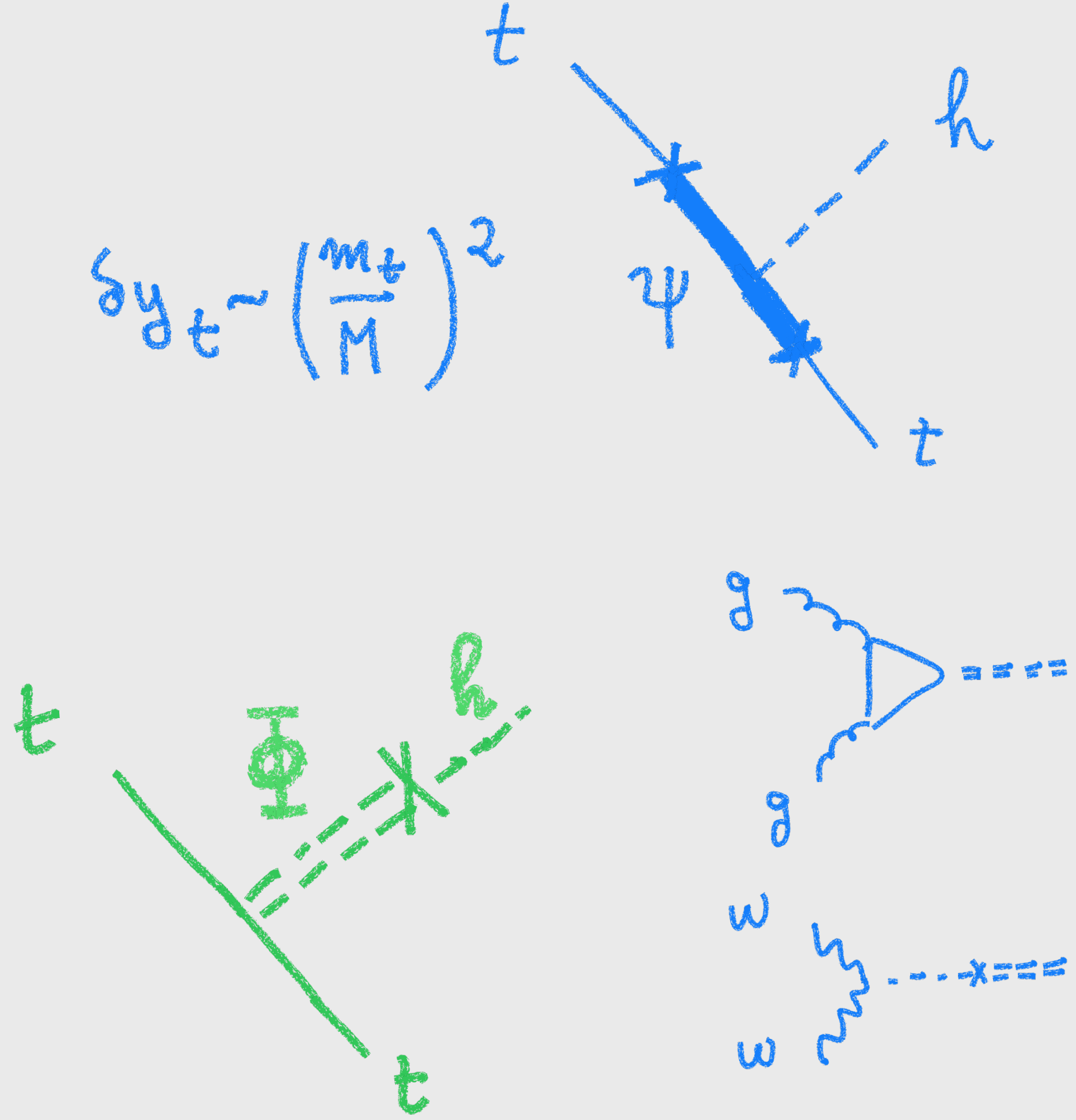
Complementarity: results from the “next” machines can feed-back in the assumptions on the precision studies of the “previous” machine. At $\mu\mu$ “next” and “previous” happen synchronously.

Joint-ventures on the Yukawa of the top quark



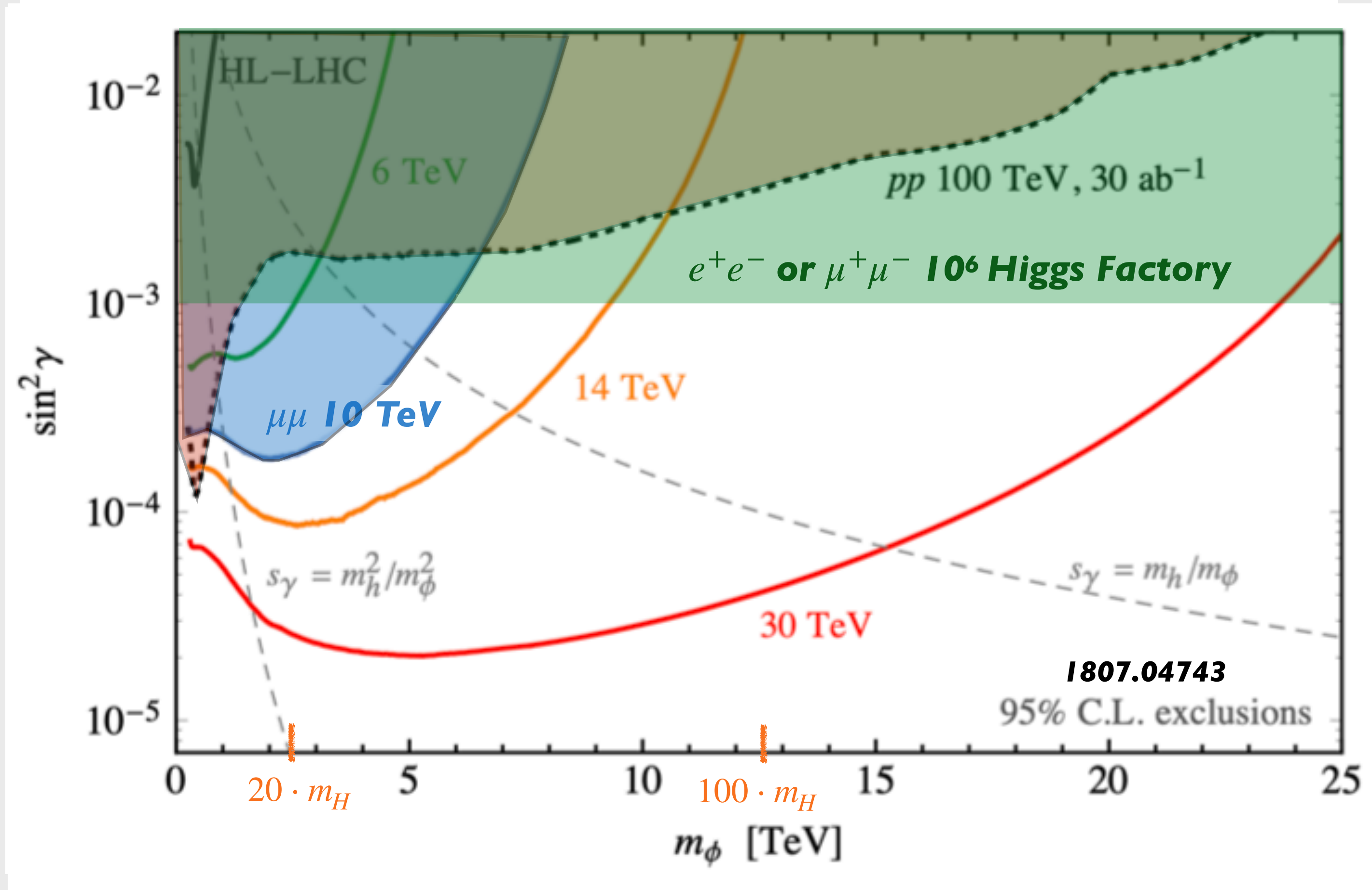
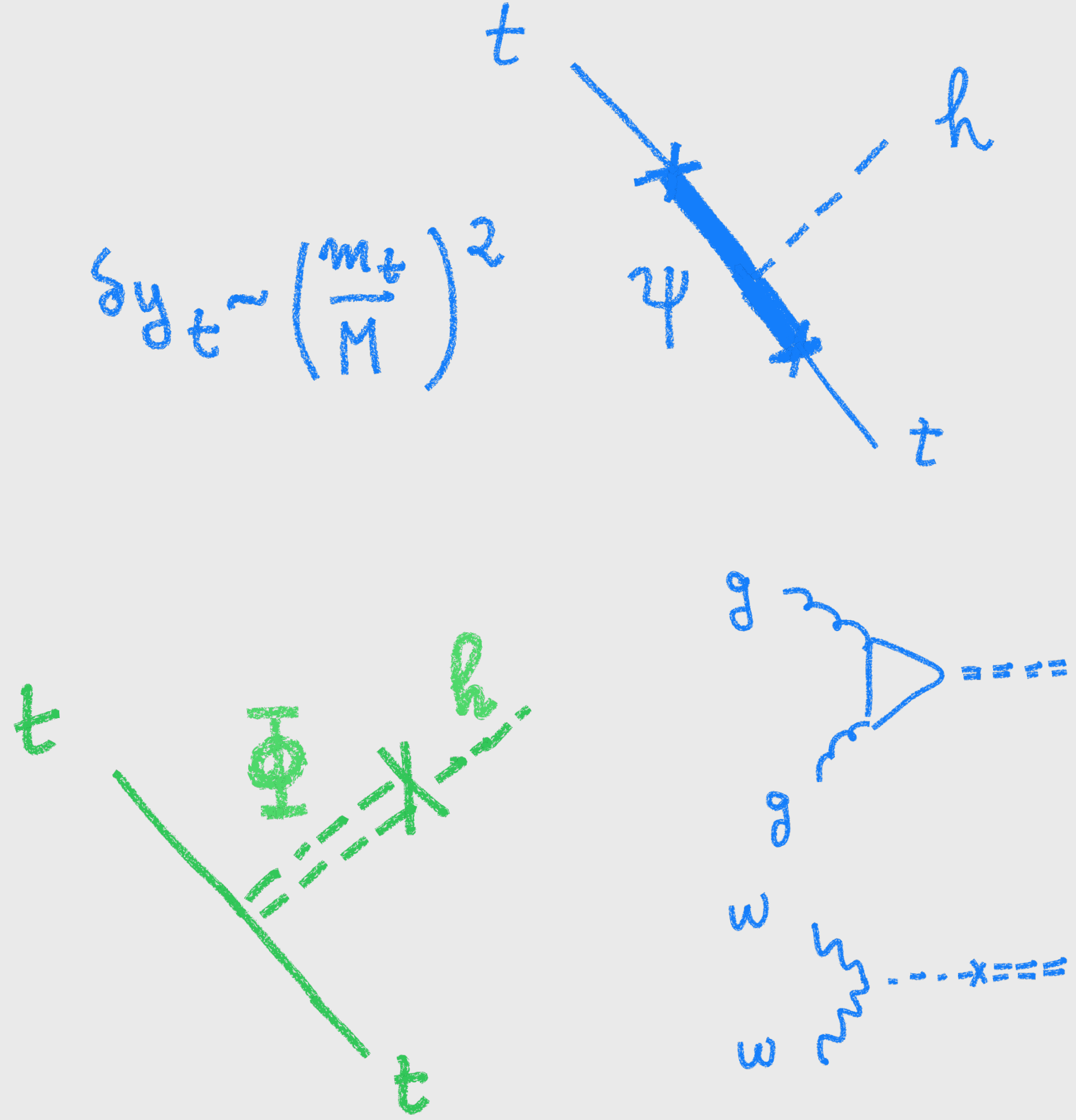
Complementarity: results from the “next” machines can feed-back in the assumptions on the precision studies of the “previous” machine. At $\mu\mu$ “next” and “previous” happen synchronously.

Joint-ventures on the Yukawa of the top quark



Complementarity: results from the “next” machines can feed-back in the assumptions on the precision studies of the “previous” machine. At $\mu\mu$ “next” and “previous” happen synchronously.

Joint-ventures on the Yukawa of the top quark

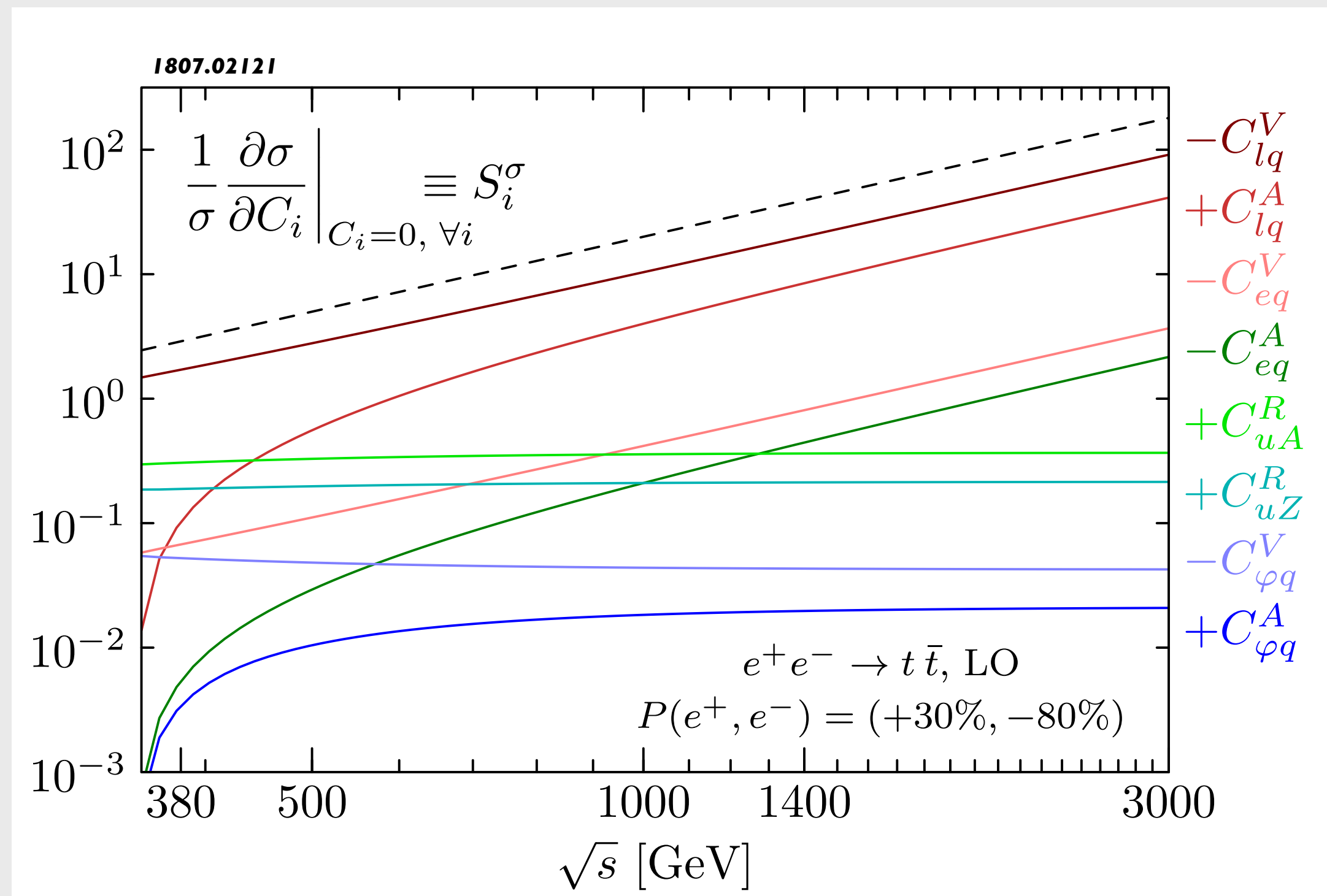


Complementarity: results from the “next” machines can feed-back in the assumptions on the precision studies of the “previous” machine. At $\mu\mu$ “next” and “previous” happen synchronously.

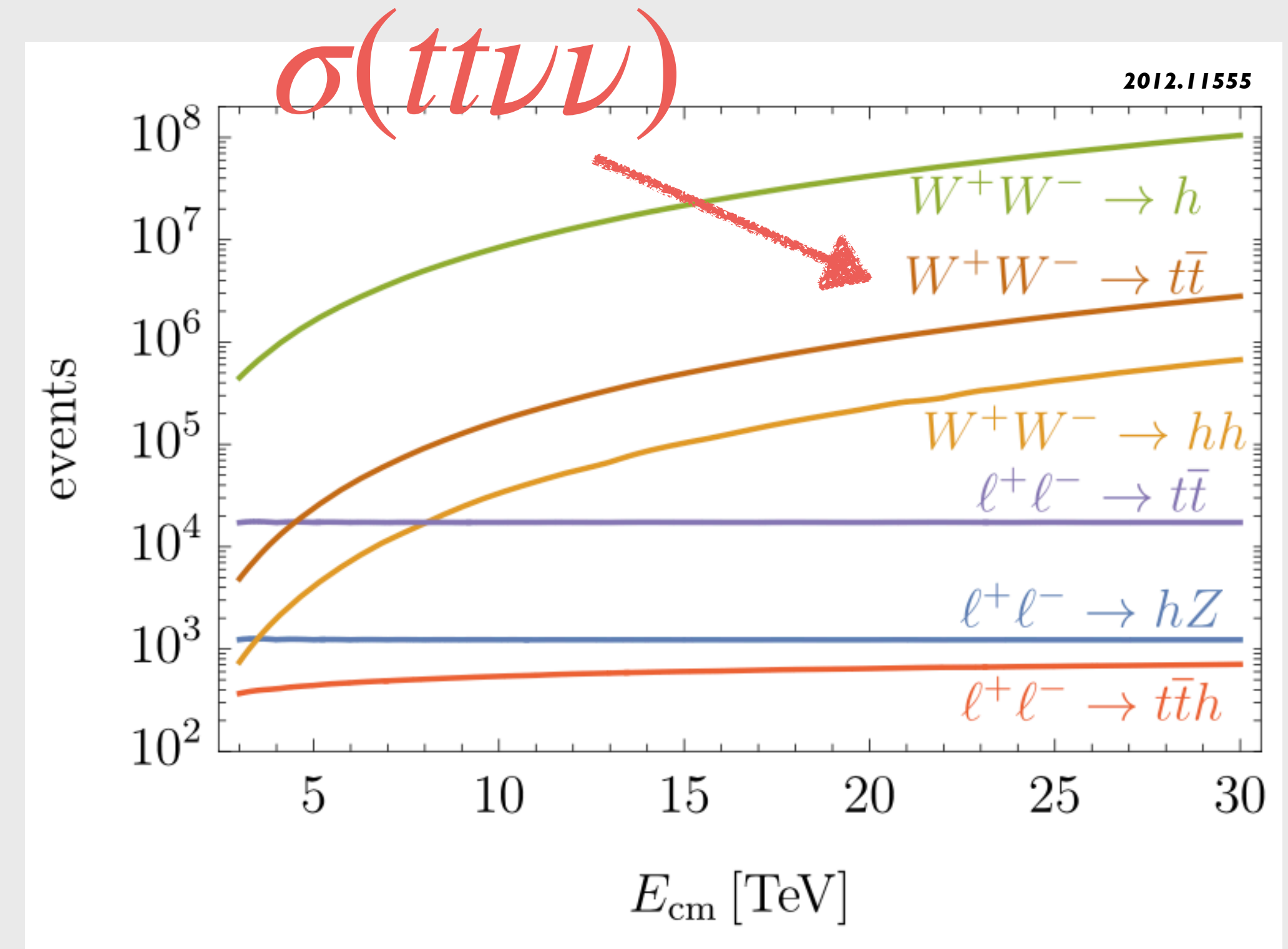
EFT

EFT benefits of multiple probes

ENERGY DEPENDENCE



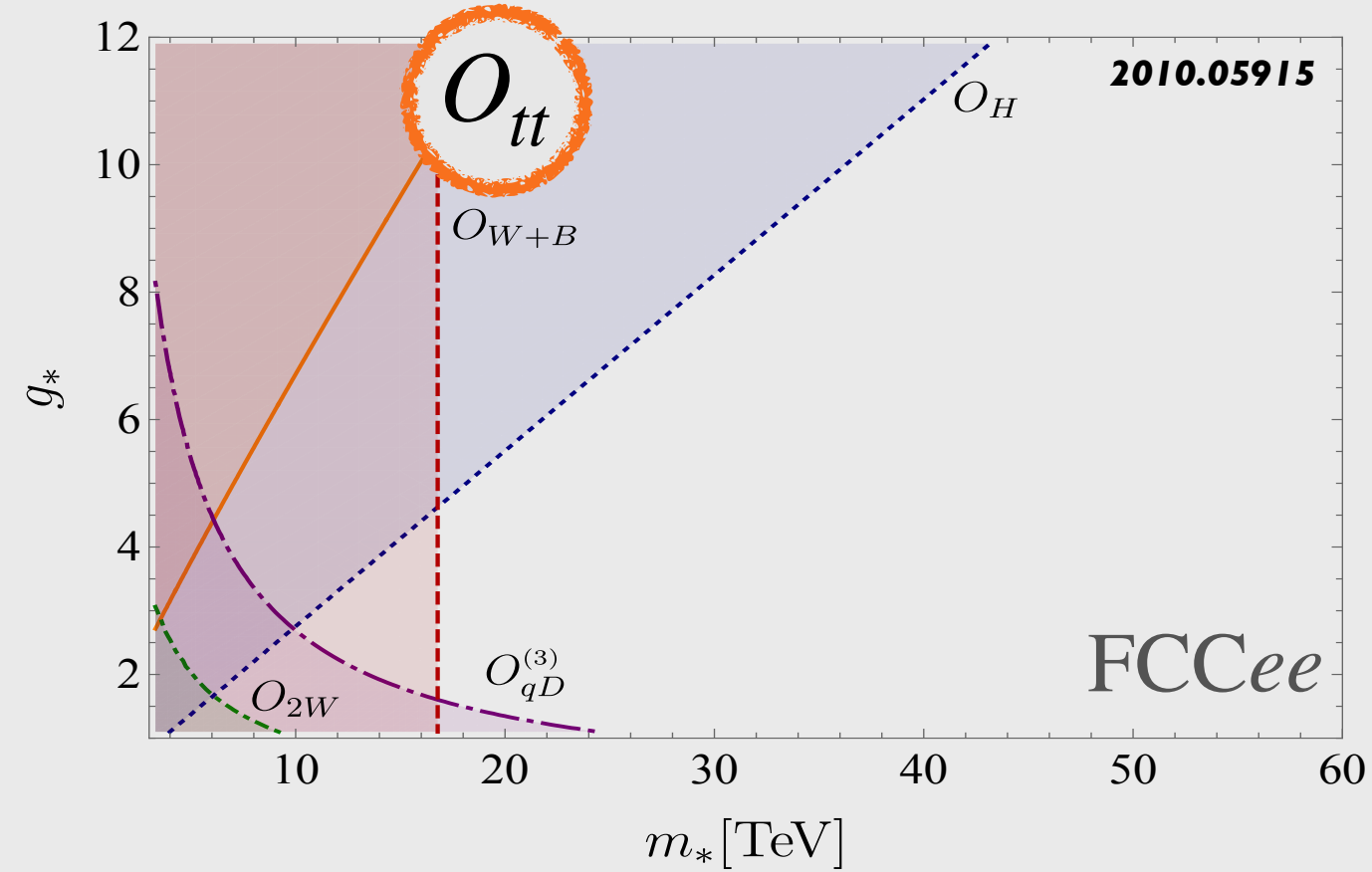
- contact interactions give energy-dependent effects
- measurements at different energies test/disentangle EFT



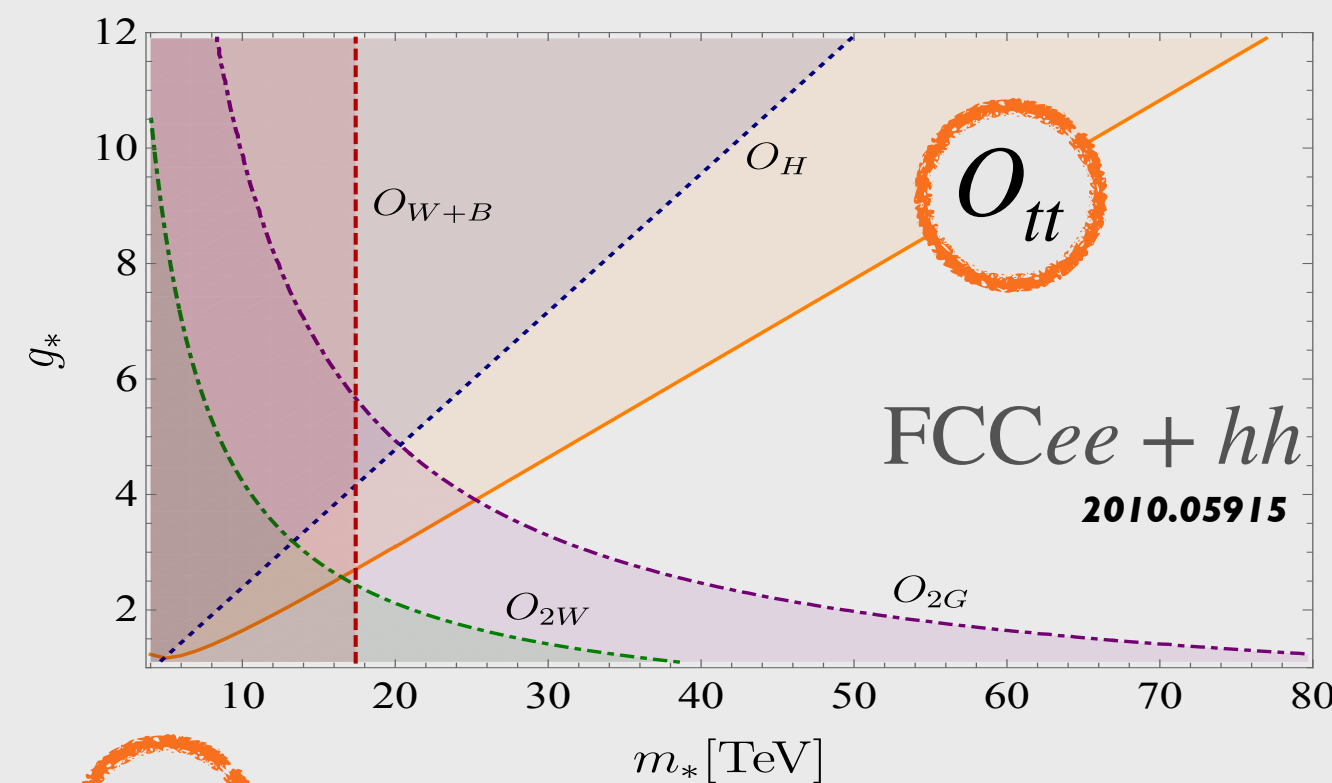
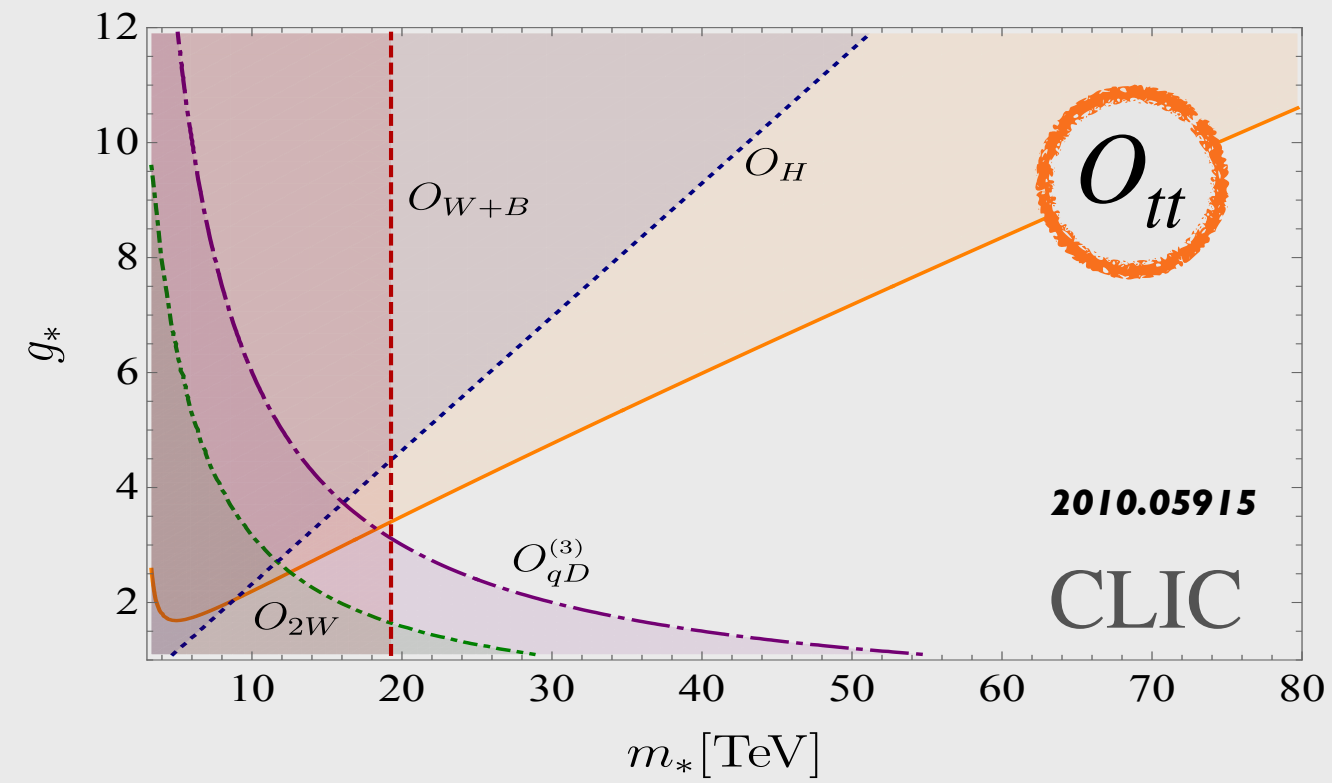
- some effects can also be seen in energy-independent effects where the high-intensity machine FCC- ee 350 can provide input earlier than $\mu\mu$ reaches $O(10^6)$ $t\bar{t}$ at 30 TeV

EFT benefits of high-energy probes

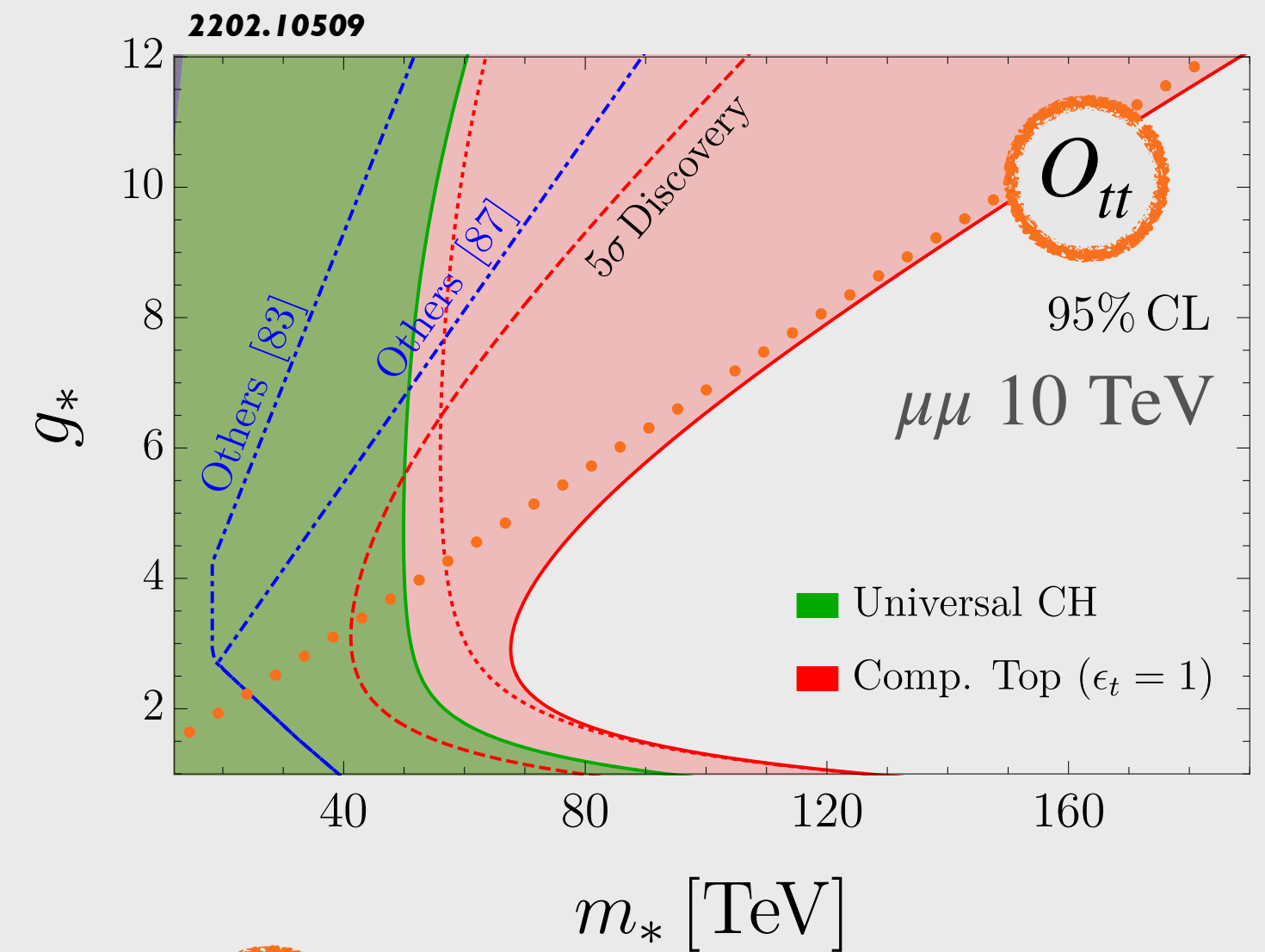
FOUR-TOP OPERATOR (t_R COMPOSITENESS)



O_{tt} at $g_\star \simeq 10 \Rightarrow m_\star \simeq 18$ TeV



O_{tt} at $g_\star \simeq 10 \Rightarrow m_\star \simeq 60 \div 70$ TeV



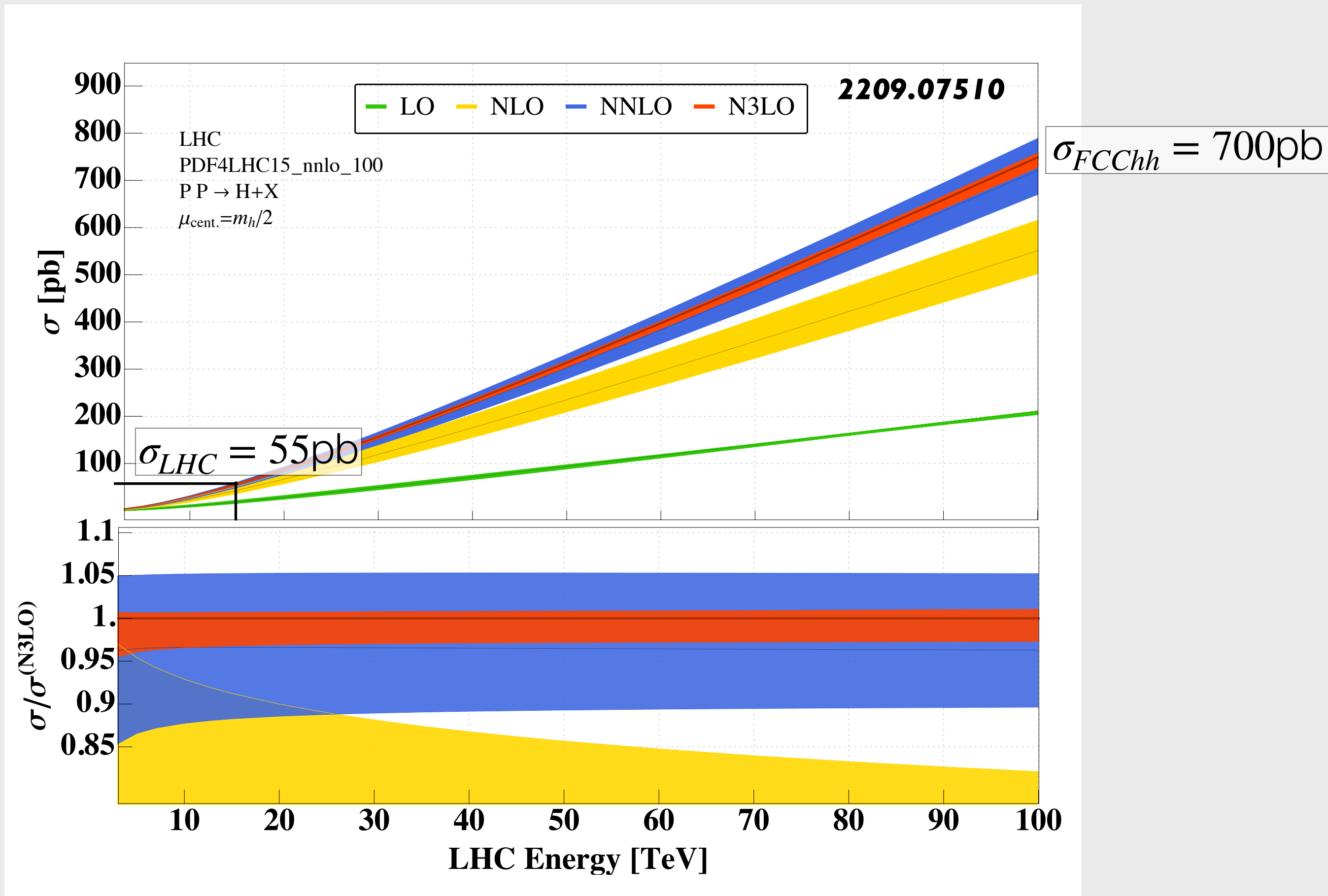
O_{tt} at $g_\star \simeq 10 \Rightarrow m_\star \simeq 180$ TeV

Higgs EFT(*s*)

$pp \rightarrow h + X$

10⁶ HIGGS BOSONS

MEGA-HIGGS FACTORY



Hadron collider famous as gluon smashers

$$\sqrt{s} = 14 \text{ TeV}$$

$$\sigma \cdot \mathcal{L} \Rightarrow O(10^8) \text{ h}$$

- large number of Higgs bosons!

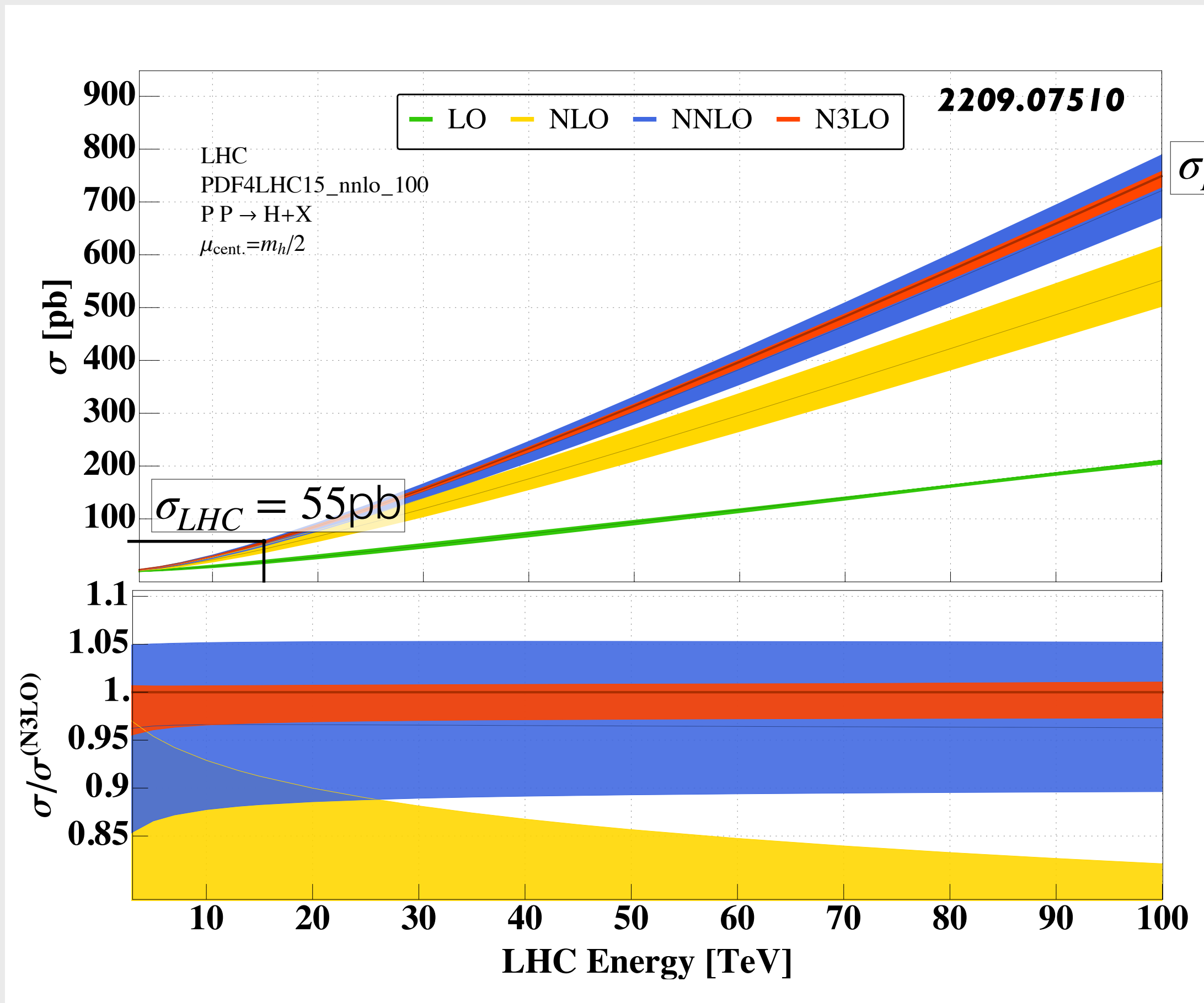
FURTHER OPPORTUNITIES

- ultra-rare Higgs decays
- differential distribution
- off-shell Higgs bosons
- rare production modes

$pp \rightarrow h + X$

10⁶ HIGGS BOSONS

MEGA-HIGGS FACTORY



$$\sqrt{s} = 100 \text{ TeV}$$

$$\sigma \cdot \mathcal{L} \Rightarrow O(10^{10}) \text{ h}$$

- large number of Higgs bosons!

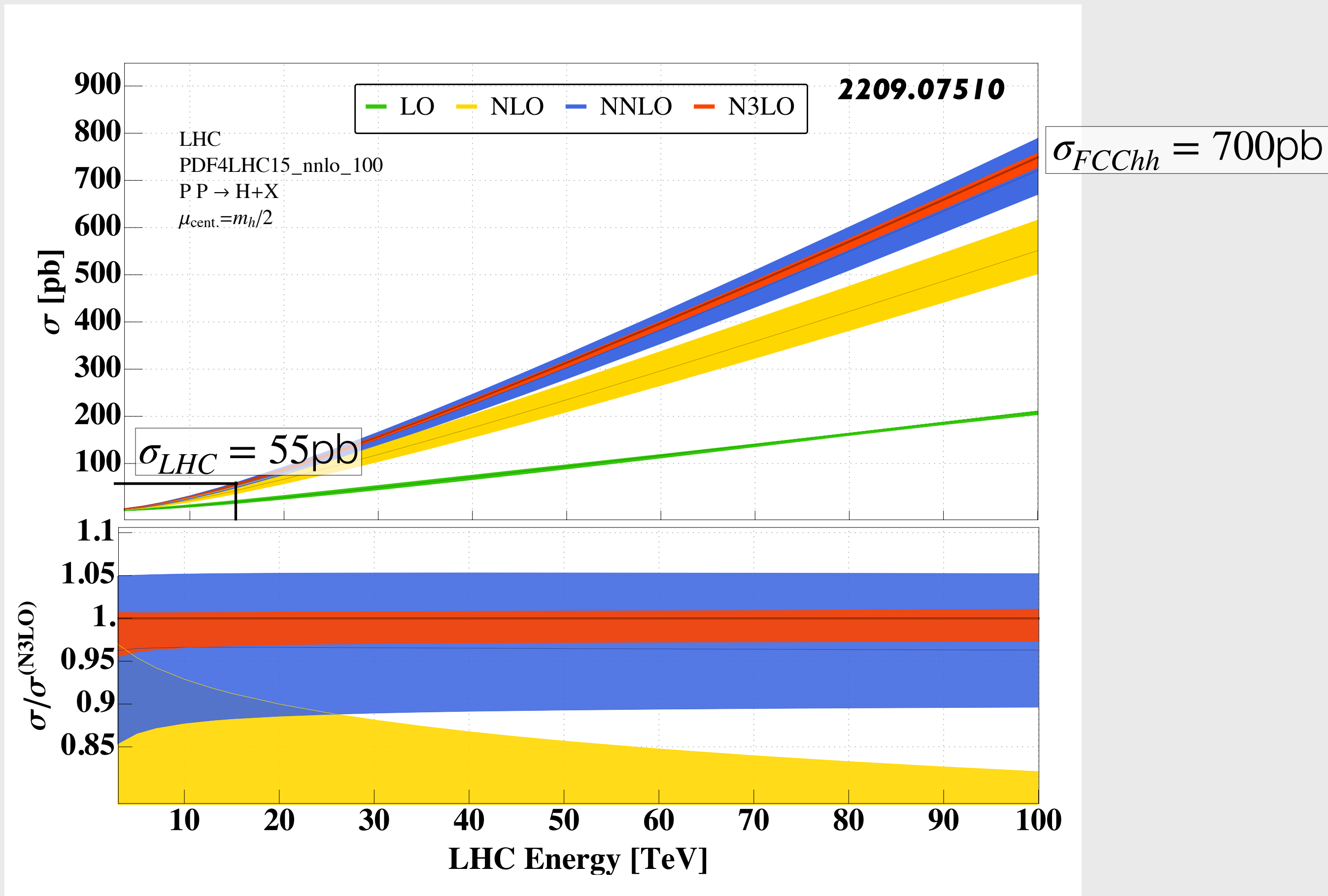
FURTHER OPPORTUNITIES

- ultra-rare Higgs decays
- differential distribution
- off-shell Higgs bosons
- rare production modes

$pp \rightarrow h + X$

10⁶ HIGGS BOSONS

MEGA-HIGGS FACTORY



$$\sqrt{s} = 100 \text{ TeV}$$

$$\sigma \cdot \mathcal{L} \Rightarrow O(10^{10}) \text{ h}$$

- large number of Higgs bosons!

FURTHER OPPORTUNITIES

- ultra-rare Higgs decays
- differential distribution
- off-shell Higgs bosons
- rare production modes

$$pp \rightarrow h + X$$

10⁶ HIGGS BOSONS

MEGA-HIGGS FACTORY



- 100 TeV: 100 × Higgs compared to HL-LHC



10 20 30 40 50 60 70 80 90 100
LHC Energy [TeV]

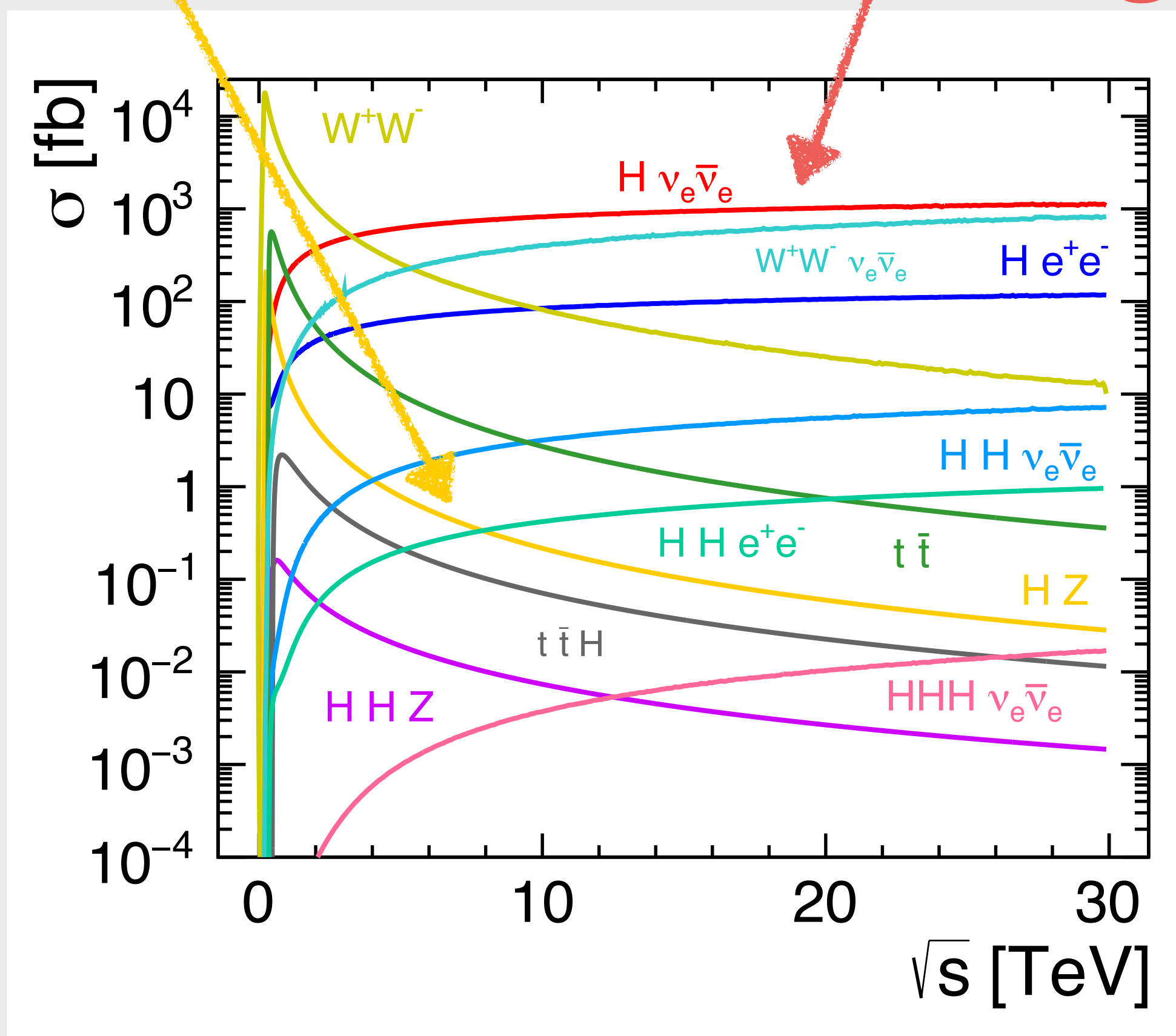
- differential distribution
- off-shell Higgs bosons
- rare production modes



10⁶ HIGGS BOSONS

MEGA-HIGGS FACTORY

$\sigma \sim 1/s$ $\sigma \sim \log(s)$



At 3 TeV the weak bosons are sufficiently light that can be radiated very efficiently

$$\sqrt{s} = 3 \text{ TeV}$$

$$\sigma \cdot \mathcal{L} \Rightarrow O(10^6) \text{ h}$$

- large number of Higgs bosons!

FURTHER OPPORTUNITIES

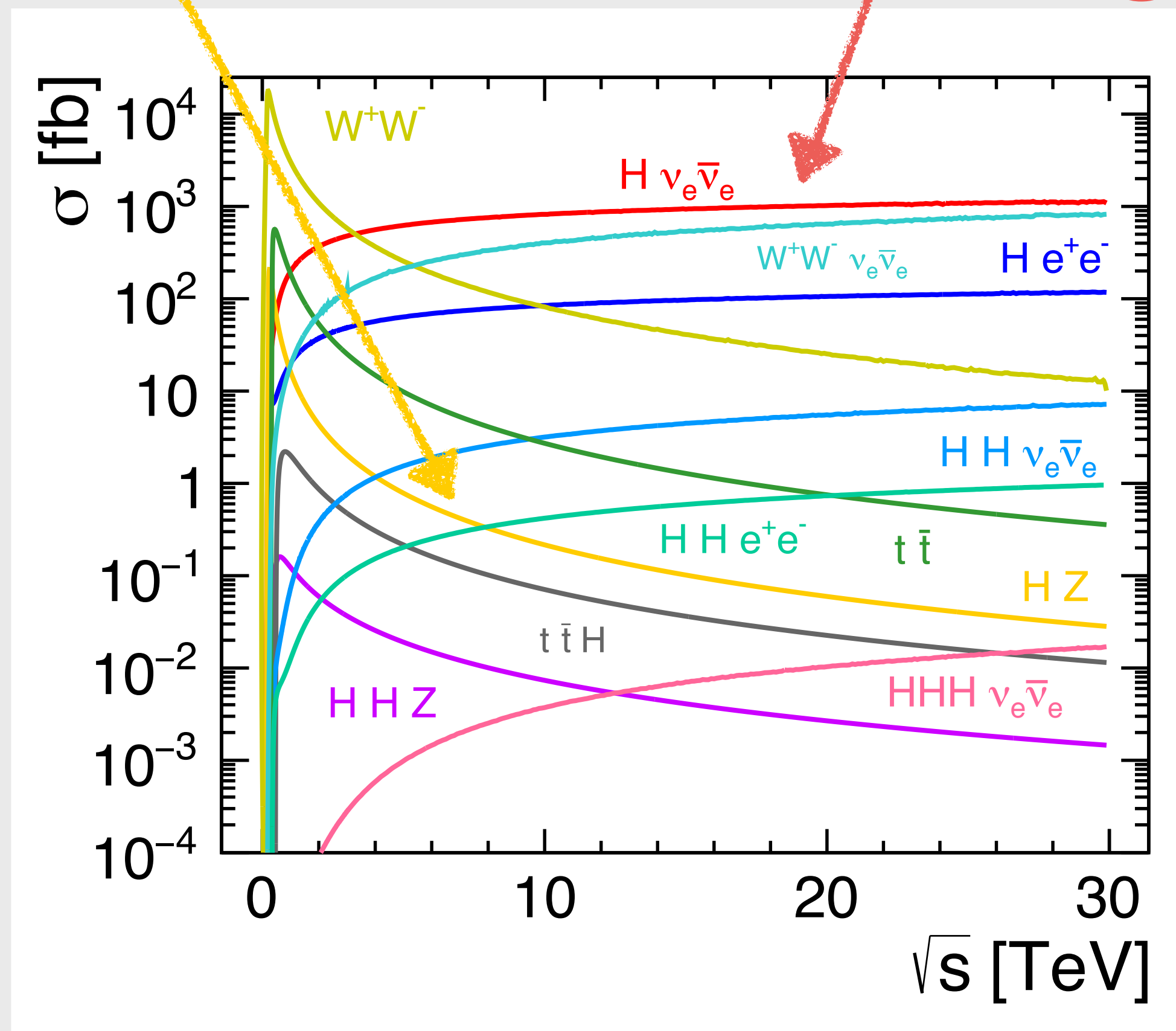
- ultra-rare Higgs decays
- differential distribution
- off-shell Higgs bosons
- rare production modes



10⁶ HIGGS BOSONS

MEGA-HIGGS FACTORY

$\sigma \sim 1/s$ $\sigma \sim \log(s)$



At 30 TeV the weak bosons are sufficiently light that can be radiated very efficiently

$$\sqrt{s} = 30 \text{ TeV}$$

$$\sigma \cdot \mathcal{L} \Rightarrow O(10^8) \text{ h}$$

- large number of Higgs bosons!

FURTHER OPPORTUNITIES

- ultra-rare Higgs decays
- differential distribution
- off-shell Higgs bosons
- rare production modes



10⁶ HIGGS BOSONS

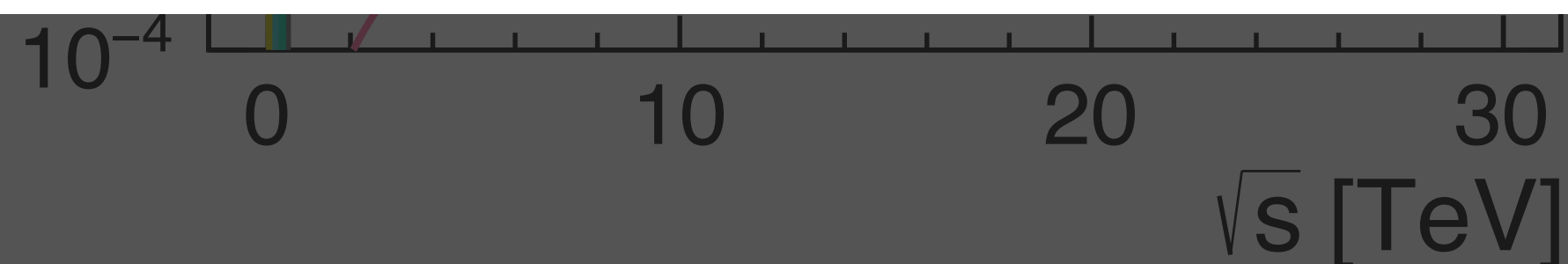
MEGA-HIGGS FACTORY

$$\sigma \sim 1/s$$

$$\sigma \sim \log(s)$$

At 30 TeV the weak bosons are sufficiently light that can be radiated very efficiently

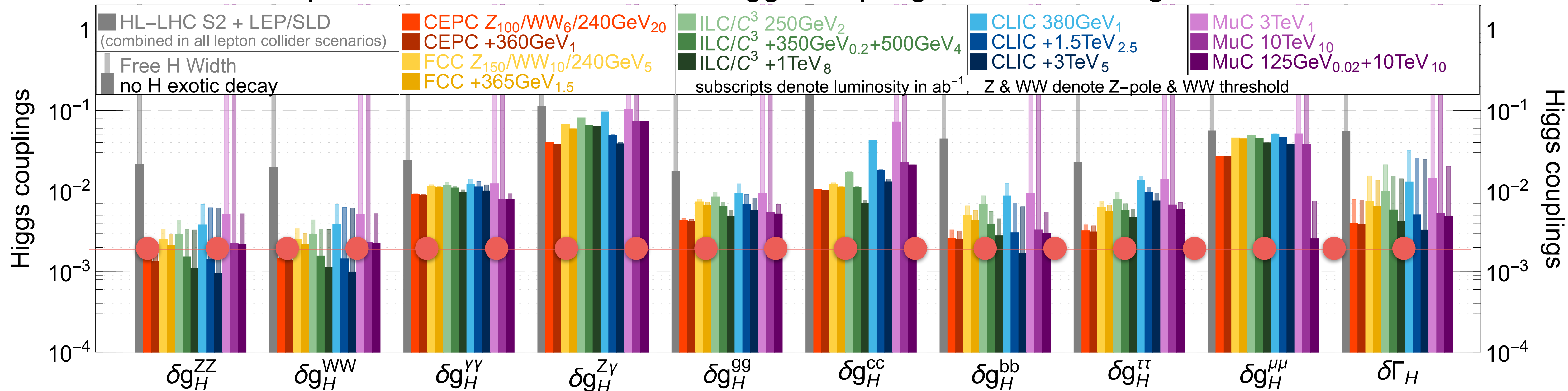
- Higgs factory at 3 TeV
- 10 × Higgs factory at 10 TeV
- 100 × Higgs factory at 30 TeV



- differential distribution
- off-shell Higgs bosons
- rare production modes

Summary: Higgs@FC (by couplings)

precision reach on effective Higgs couplings from SMEFT global fit



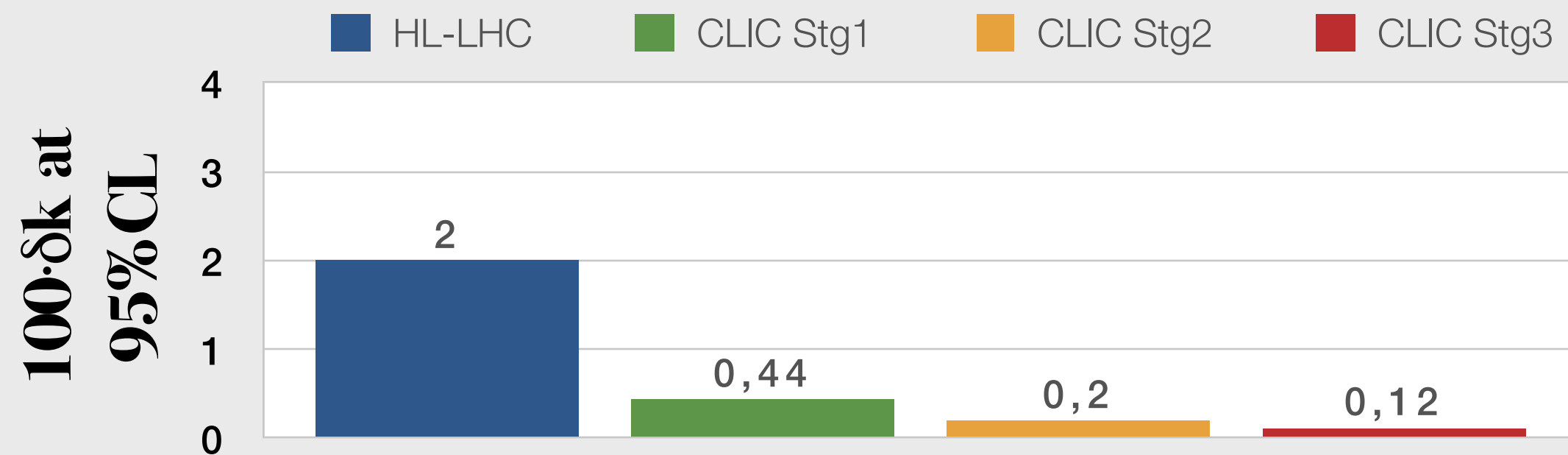
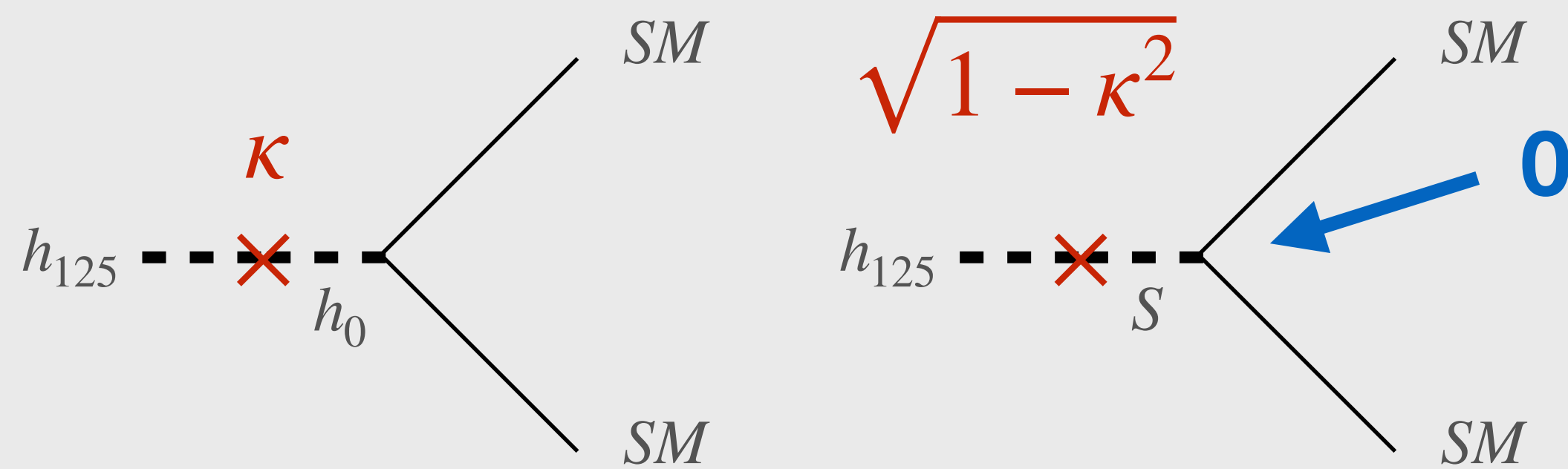
0.1% coupling precision, sensitivity to new physics at $10 \text{ TeV} \simeq 100 \cdot m_h$

A concrete case

NEW SCALAR

SM+HEAVY SINGLET

$$h_{125} = h_0 \cdot \kappa + S \cdot \sqrt{1 - \kappa^2}$$

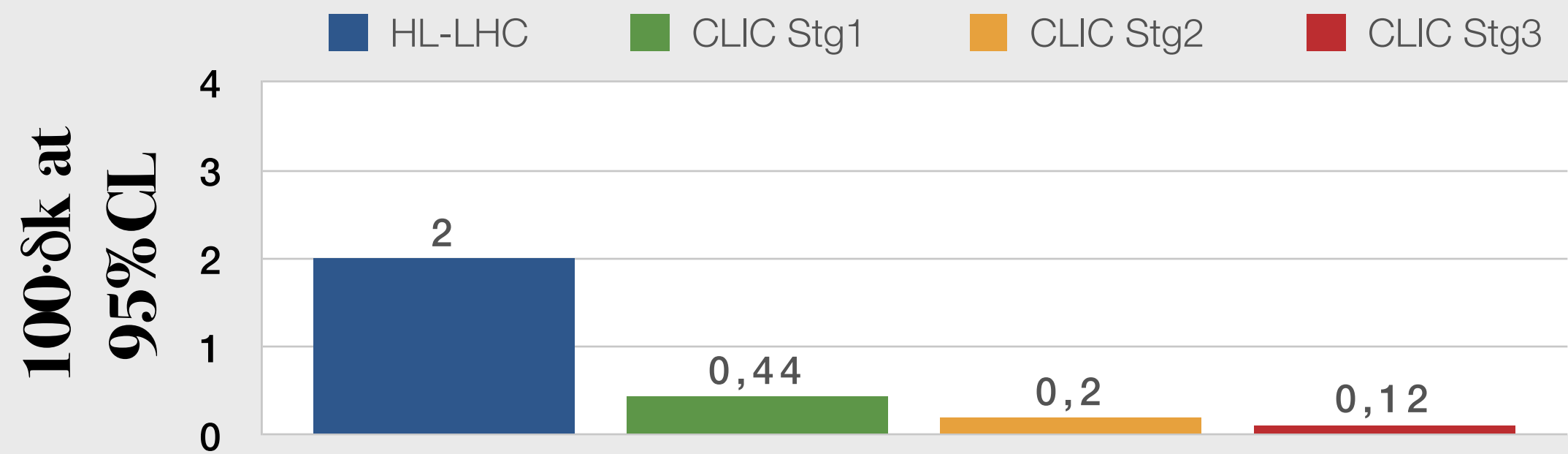
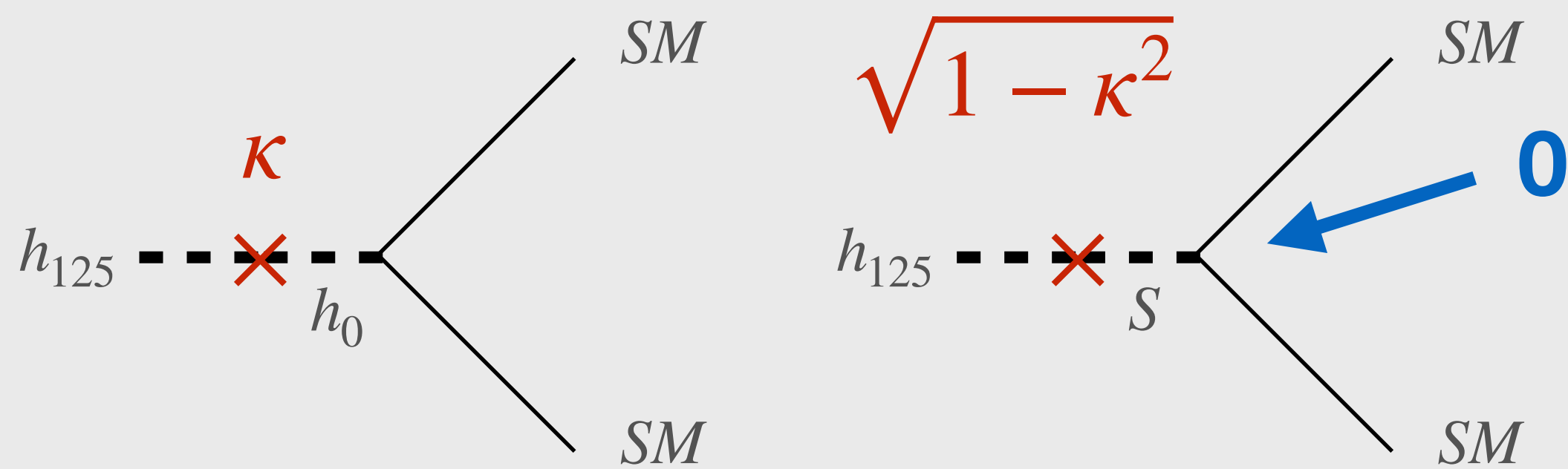


A concrete case

NEW SCALAR

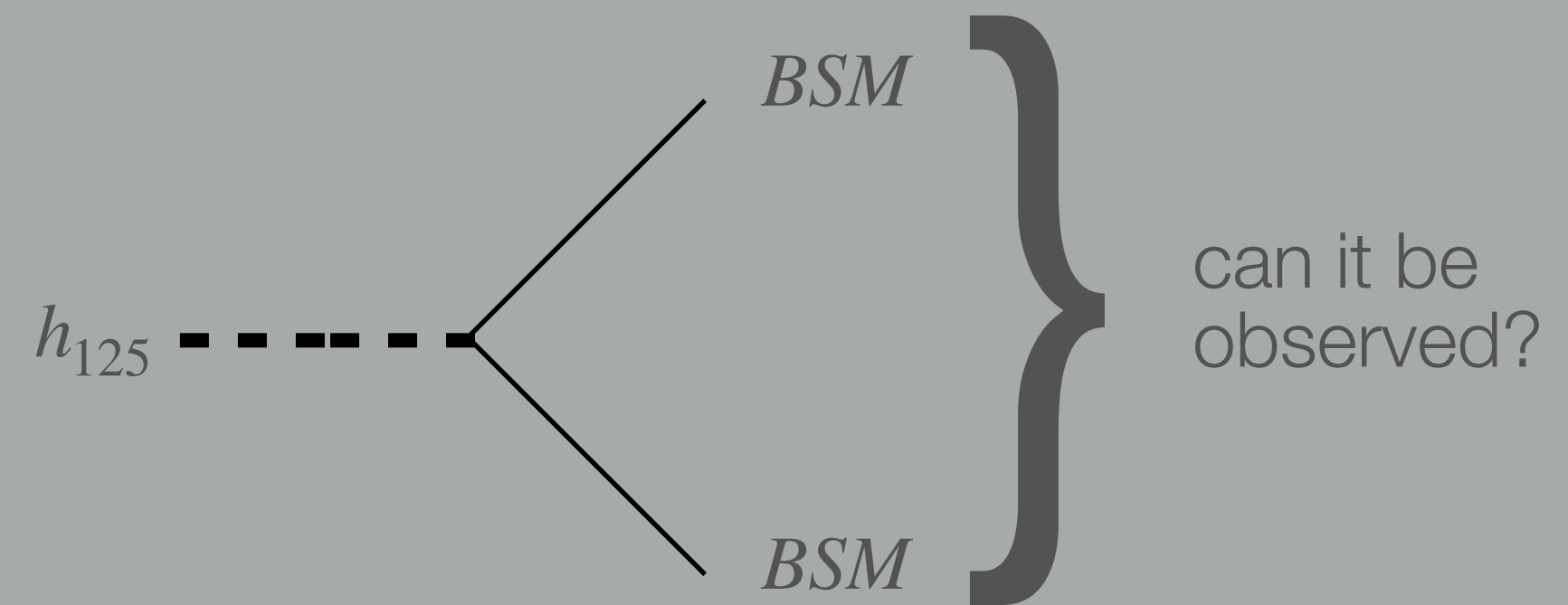
SM+HEAVY SINGLET

$$h_{125} = h_0 \cdot \kappa + S \cdot \sqrt{1 - \kappa^2}$$

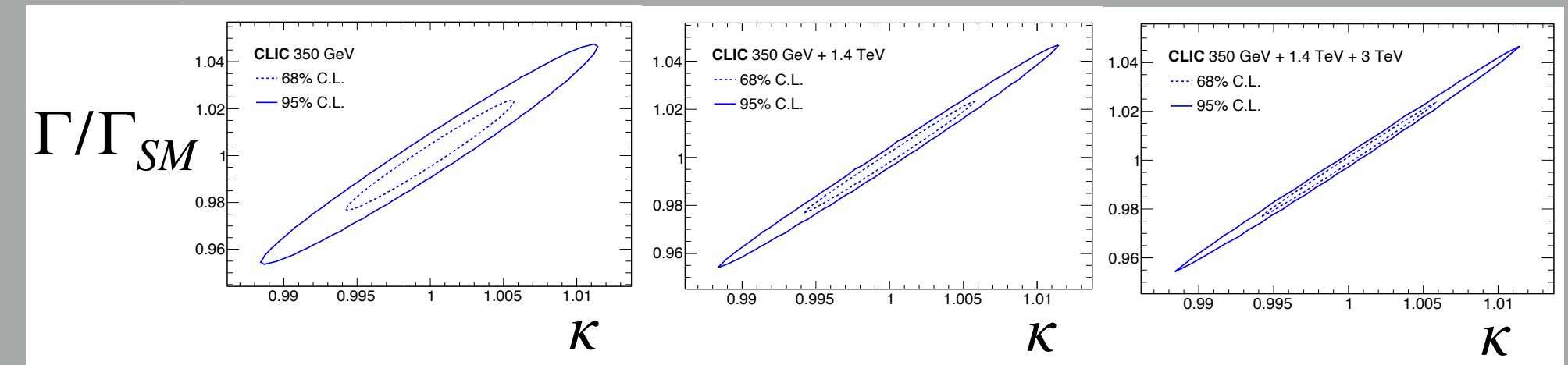


$h \rightarrow BSM$

$$\Gamma_H = k^2 \Gamma_{SM} + \Gamma_{BSM}$$



1812.02093

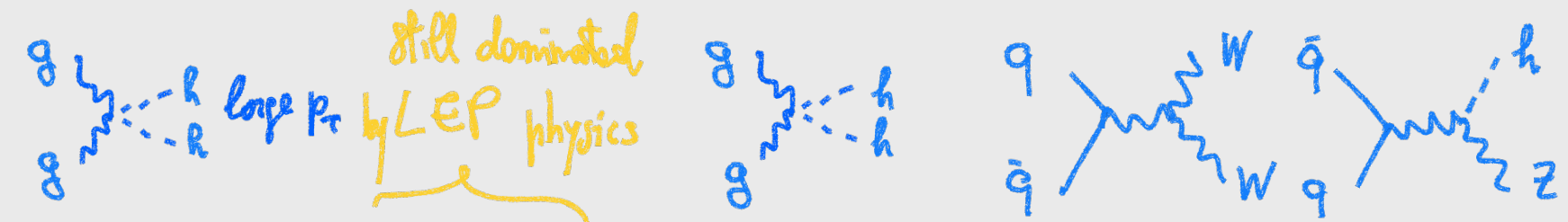


	Δg	$\Delta \Gamma_H$	$\Delta \Gamma_H$
Stage 1	0.58%	2.3%	0.47%
Stage 1+2	0.57%	2.3%	0.20%
Stage 1+2+3	0.57%	2.3%	0.13%

The size of the Higgs boson

Effects of the size of the Higgs boson

STRONGLY INTERACTING HIGGS (AND TOP)

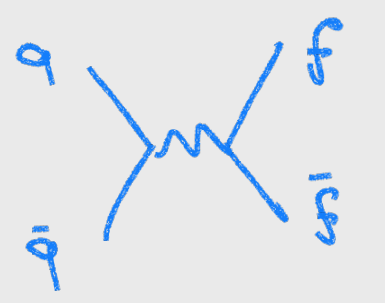


$$\mathcal{L}_{universal}^{d=6} = c_H \frac{g_*^2}{m_*^2} \mathcal{O}_H + c_T \frac{N_c \epsilon_q^4 g_*^4}{(4\pi)^2 m_*^2} \mathcal{O}_T + c_6 \lambda \frac{g_*^2}{m_*^2} \mathcal{O}_6 + \frac{1}{m_*^2} [c_W \mathcal{O}_W + c_B \mathcal{O}_B]$$

$$1/f \sim g_*/m_*$$

$$+ \frac{g_*^2}{(4\pi)^2 m_*^2} [c_{HW} \mathcal{O}_{HW} + c_{HB} \mathcal{O}_{HB}] + \frac{y_t^2}{(4\pi)^2 m_*^2} [c_{BB} \mathcal{O}_{BB} + c_{GG} \mathcal{O}_{GG}]$$

$$1/(g_* f) \sim 1/m_*$$

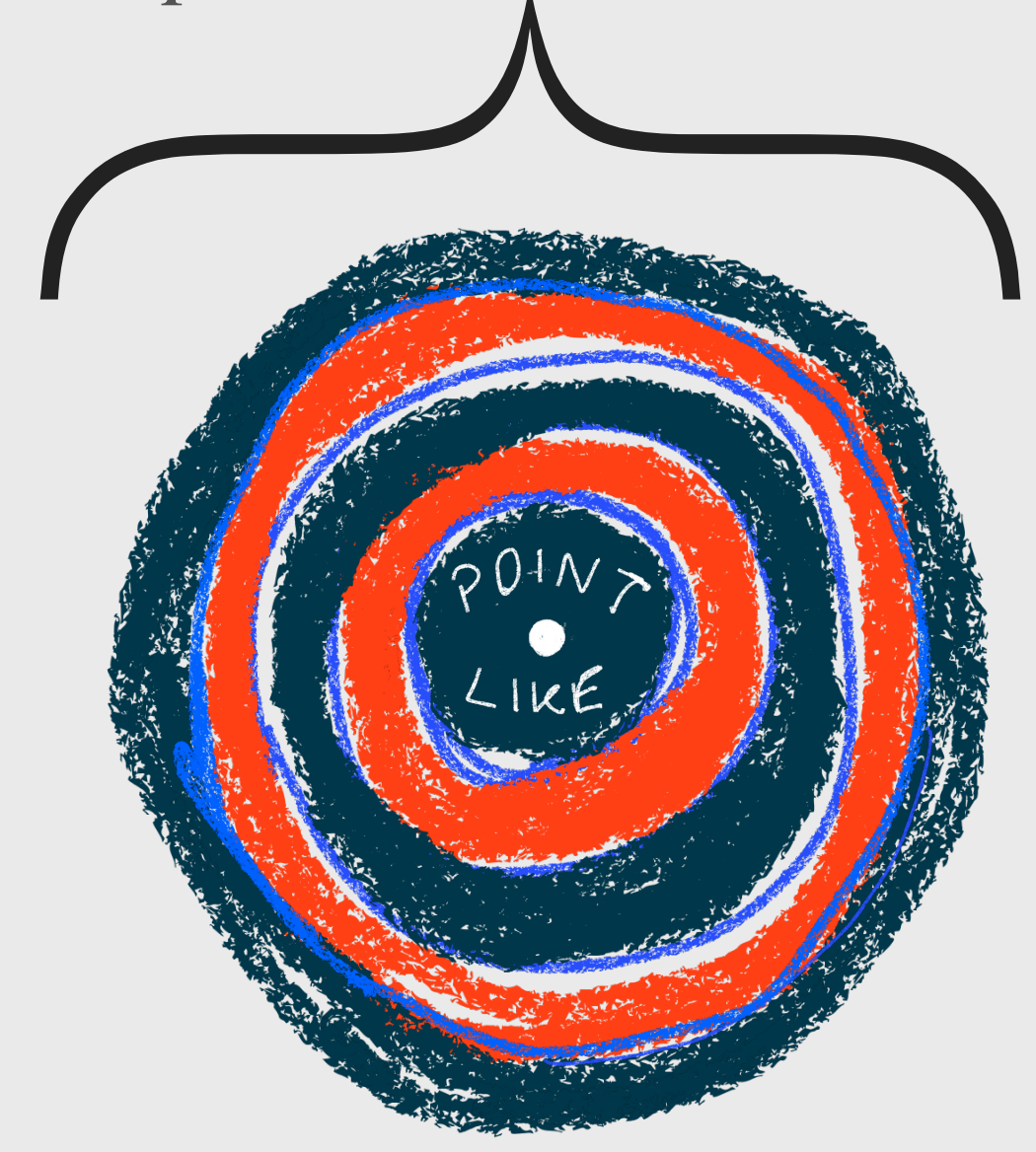


$$+ \frac{1}{g_*^2 m_*^2} [c_{2W} g^2 \mathcal{O}_{2W} + c_{2B} g'^2 \mathcal{O}_{2B}] + c_{3W} \frac{3! g^2}{(4\pi)^2 m_*^2} \mathcal{O}_{3W}$$

$$g_{SM}/(g_* f) \sim g_{SM}/m_*$$

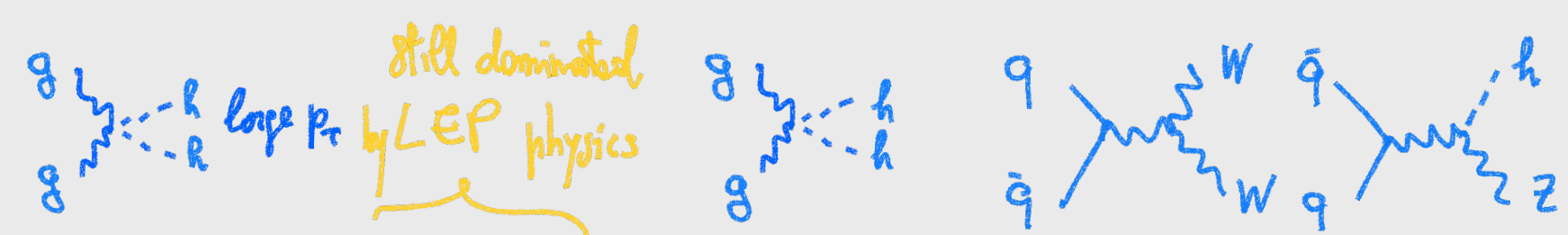
$$+ c_{y_t} \frac{g_*^2}{m_*^2} \mathcal{O}_{y_t} + c_{y_b} \frac{g_*^2}{m_*^2} \mathcal{O}_{y_b}$$

$$\ell_{top} \sim 1/m_* \sim \ell_{Higgs}$$



Effects of the size of the Higgs boson

STRONGLY INTERACTING HIGGS (AND TOP)



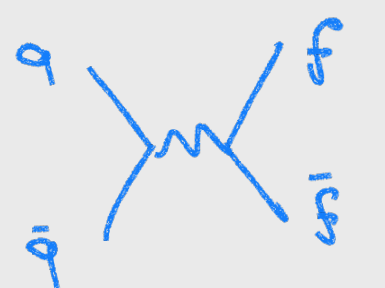
still dominated by LEP physics

$$\mathcal{L}_{universal}^{d=6} = c_H \frac{g_*^2}{m_*^2} \mathcal{O}_H + c_T \frac{N_c \epsilon_q^4 g_*^4}{(4\pi)^2 m_*^2} \mathcal{O}_T + c_6 \lambda \frac{g_*^2}{m_*^2} \mathcal{O}_6 + \frac{1}{m_*^2} [c_W \mathcal{O}_W + c_B \mathcal{O}_B]$$

$$1/f \sim g_*/m_*$$

$$+ \frac{g_*^2}{(4\pi)^2 m_*^2} [c_{HW} \mathcal{O}_{HW} + c_{HB} \mathcal{O}_{HB}] + \frac{y_t^2}{(4\pi)^2 m_*^2} [c_{BB} \mathcal{O}_{BB} + c_{GG} \mathcal{O}_{GG}]$$

$$1/(g_* f) \sim 1/m_*$$



$$+ \frac{1}{g_*^2 m_*^2} [c_{2W} g^2 \mathcal{O}_{2W} + c_{2B} g'^2 \mathcal{O}_{2B}] + c_{3W} \frac{3! g^2}{(4\pi)^2 m_*^2} \mathcal{O}_{3W}$$

$$g_{SM}/(g_* f) \sim g_{SM}/m_*$$

$$+ c_{y_t} \frac{g_*^2}{m_*^2} \mathcal{O}_{y_t} + c_{y_b} \frac{g_*^2}{m_*^2} \mathcal{O}_{y_b}$$



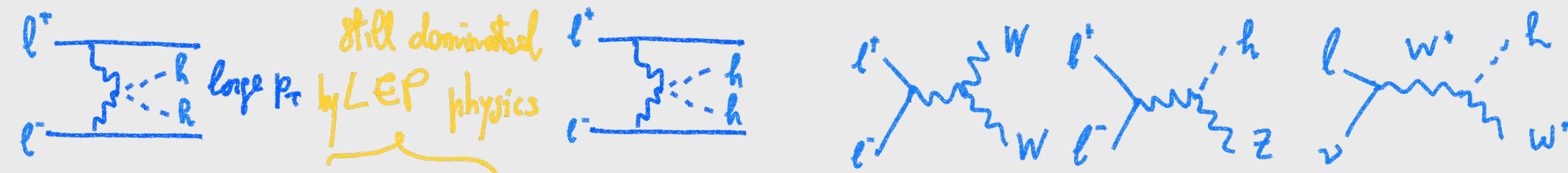
$$+ c_{tD} \frac{g_*^2}{m_*^2} \mathcal{O}_{tD}$$

$$\ell_{top} \sim 1/m_* \sim \ell_{Higgs}$$



Effects of the size of the Higgs boson

STRONGLY INTERACTING HIGGS (AND TOP)

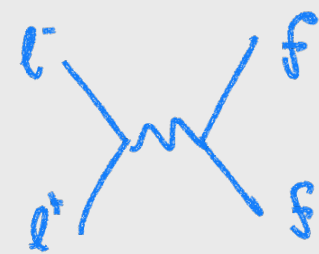


$$\mathcal{L}_{universal}^{d=6} = c_H \frac{g_*^2}{m_*^2} \mathcal{O}_H + c_T \frac{N_c \epsilon_q^4 g_*^4}{(4\pi)^2 m_*^2} \mathcal{O}_T + c_6 \lambda \frac{g_*^2}{m_*^2} \mathcal{O}_6 + \frac{1}{m_*^2} [c_W \mathcal{O}_W + c_B \mathcal{O}_B]$$

$$1/f \sim g_*/m_*$$

$$+ \frac{g_*^2}{(4\pi)^2 m_*^2} [c_{HW} \mathcal{O}_{HW} + c_{HB} \mathcal{O}_{HB}] + \frac{y_t^2}{(4\pi)^2 m_*^2} [c_{BB} \mathcal{O}_{BB} + c_{GG} \mathcal{O}_{GG}]$$

$$1/(g_* f) \sim 1/m_*$$

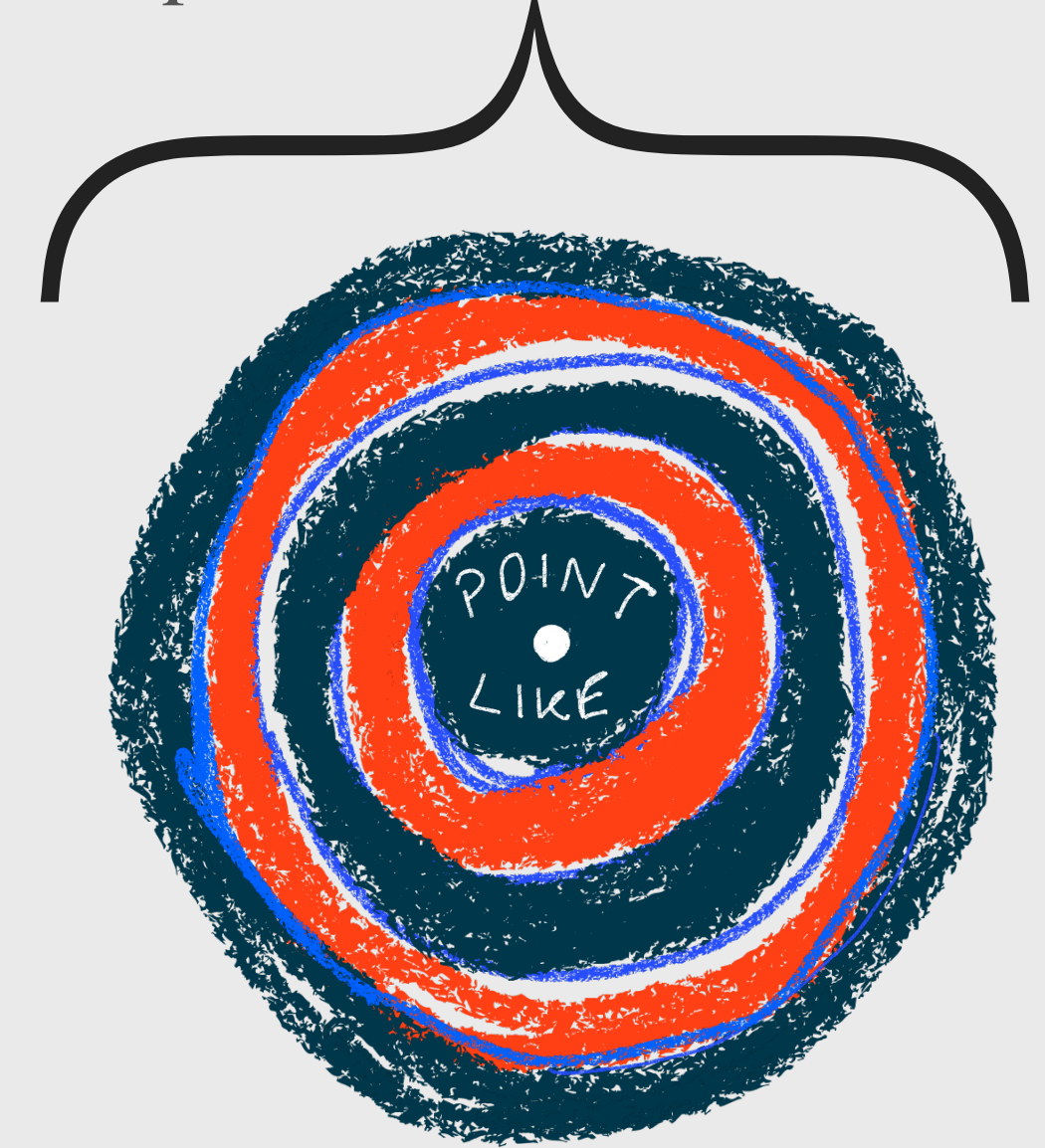


$$+ \frac{1}{g_*^2 m_*^2} [c_{2W} g^2 \mathcal{O}_{2W} + c_{2B} g'^2 \mathcal{O}_{2B}] + c_{3W} \frac{3! g^2}{(4\pi)^2 m_*^2} \mathcal{O}_{3W}$$

$$g_{SM}/(g_* f) \sim g_{SM}/m_*$$

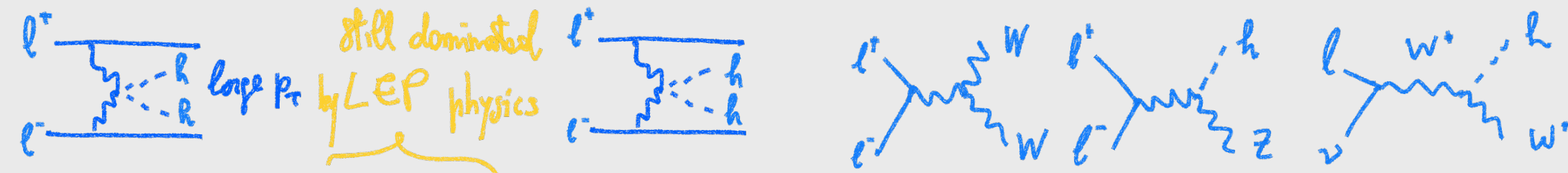
$$+ c_{y_t} \frac{g_*^2}{m_*^2} \mathcal{O}_{y_t} + c_{y_b} \frac{g_*^2}{m_*^2} \mathcal{O}_{y_b}$$

$$\ell_{top} \sim 1/m_* \sim \ell_{Higgs}$$



Effects of the size of the Higgs boson

STRONGLY INTERACTING HIGGS (AND TOP)

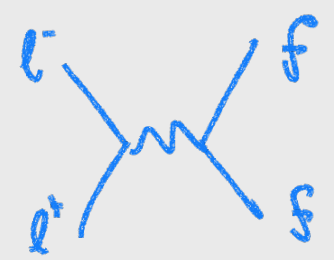


$$\mathcal{L}_{universal}^{d=6} = c_H \frac{g_*^2}{m_*^2} \mathcal{O}_H + c_T \frac{N_c \epsilon_q^4 g_*^4}{(4\pi)^2 m_*^2} \mathcal{O}_T + c_6 \lambda \frac{g_*^2}{m_*^2} \mathcal{O}_6 + \frac{1}{m_*^2} [c_W \mathcal{O}_W + c_B \mathcal{O}_B]$$

$$1/f \sim g_*/m_*$$

$$+ \frac{g_*^2}{(4\pi)^2 m_*^2} [c_{HW} \mathcal{O}_{HW} + c_{HB} \mathcal{O}_{HB}] + \frac{y_t^2}{(4\pi)^2 m_*^2} [c_{BB} \mathcal{O}_{BB} + c_{GG} \mathcal{O}_{GG}]$$

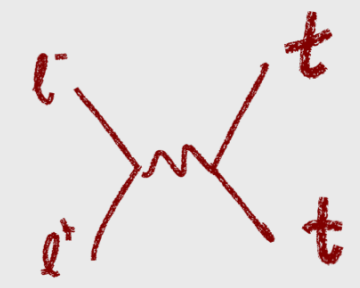
$$1/(g_* f) \sim 1/m_*$$



$$+ \frac{1}{g_*^2 m_*^2} [c_{2W} g^2 \mathcal{O}_{2W} + c_{2B} g'^2 \mathcal{O}_{2B}] + c_{3W} \frac{3! g^2}{(4\pi)^2 m_*^2} \mathcal{O}_{3W}$$

$$g_{SM}/(g_* f) \sim g_{SM}/m_*$$

$$+ c_{y_t} \frac{g_*^2}{m_*^2} \mathcal{O}_{y_t} + c_{y_b} \frac{g_*^2}{m_*^2} \mathcal{O}_{y_b}$$



$$+ c_{tD} \frac{g_*^2}{m_*^2} \mathcal{O}_{tD}$$

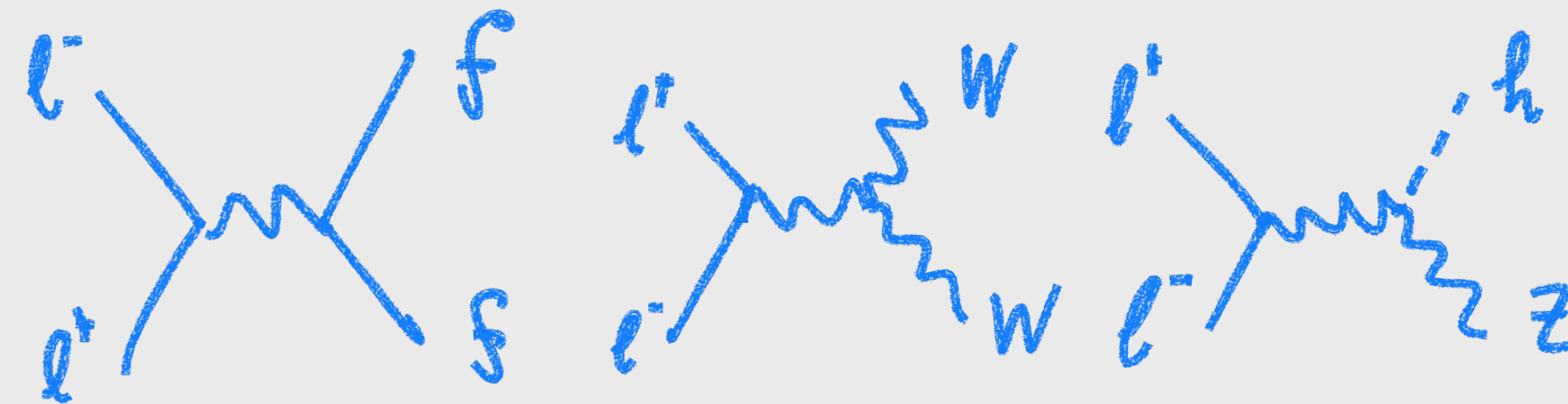
$$\ell_{top} \sim 1/m_* \sim \ell_{Higgs}$$



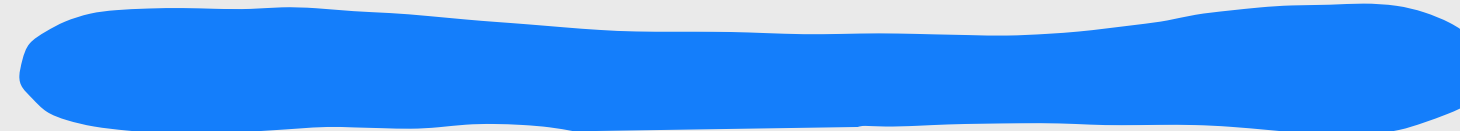
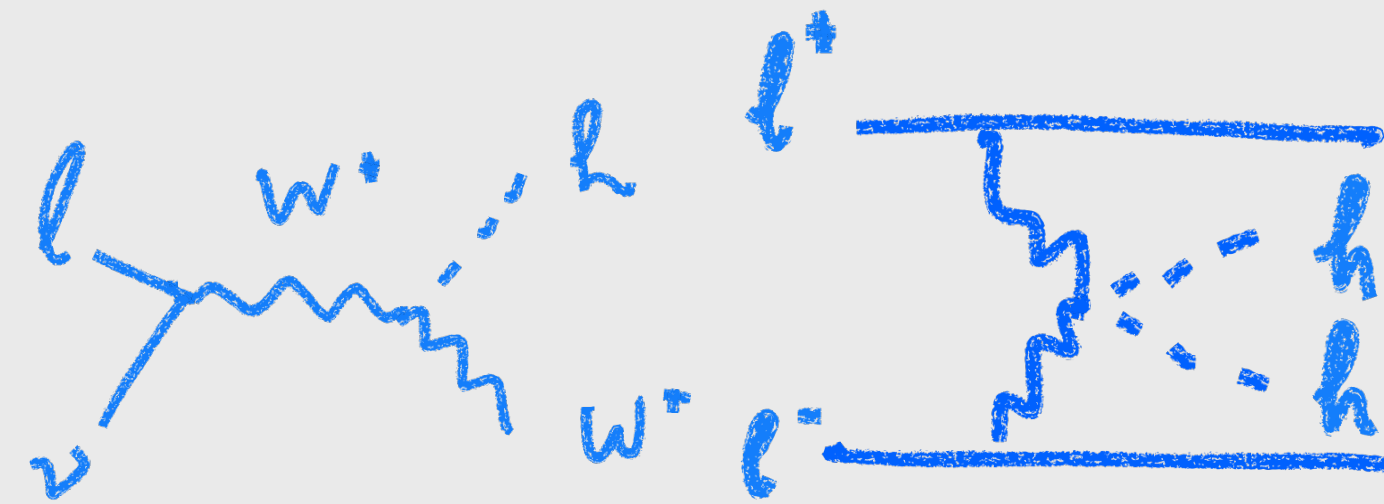
Effects of the size of the Higgs boson

STRONGLY INTERACTING HIGGS (AND TOP)

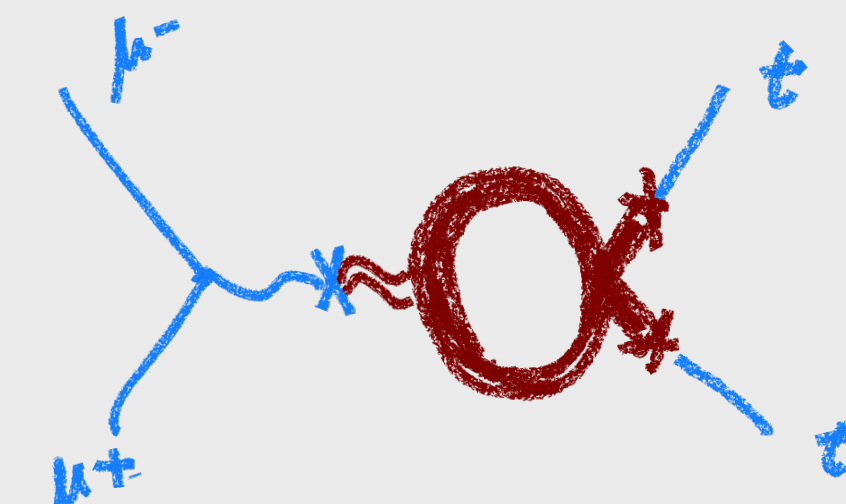
point-like beams



“partons”, radiative processes



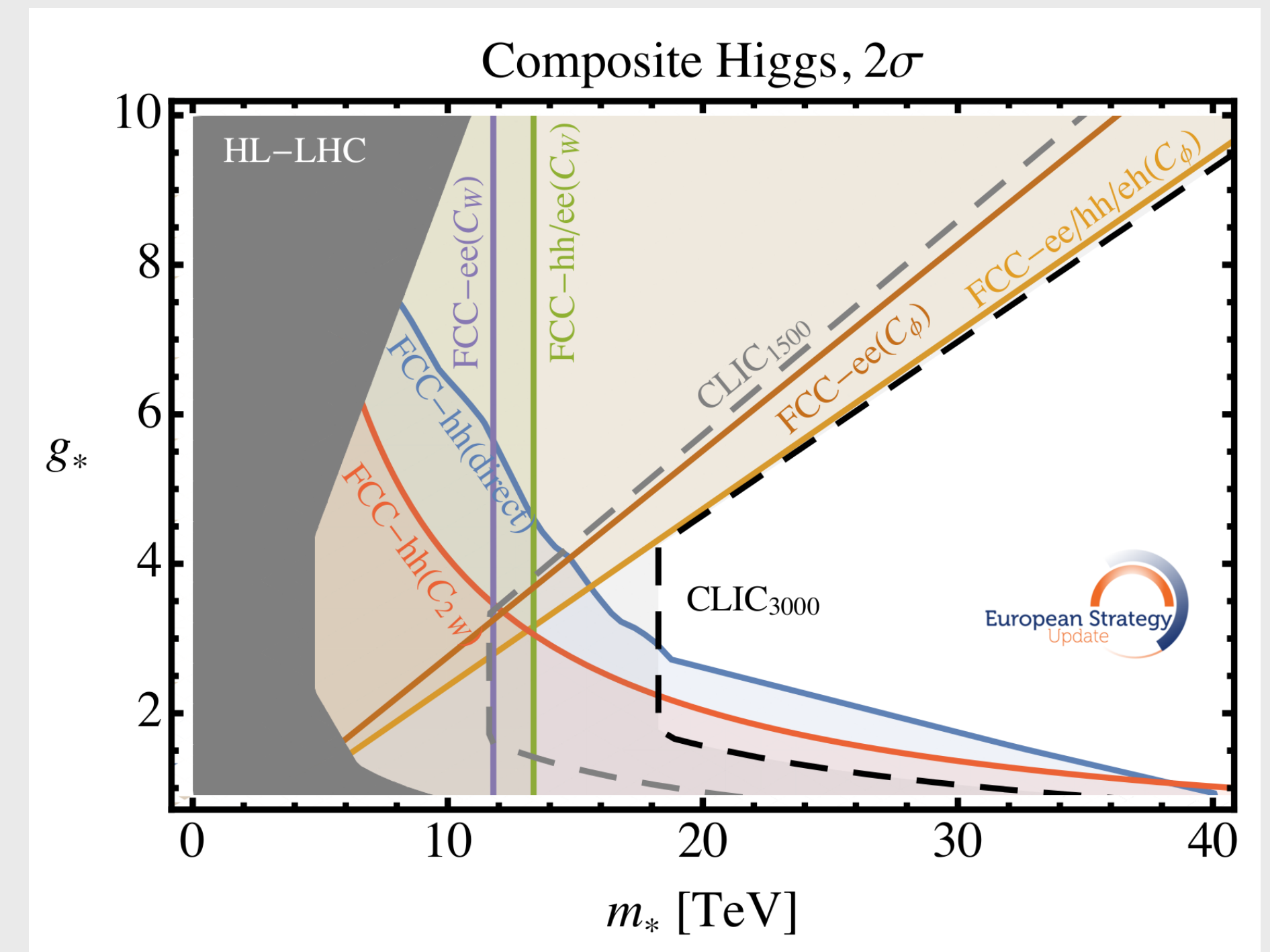
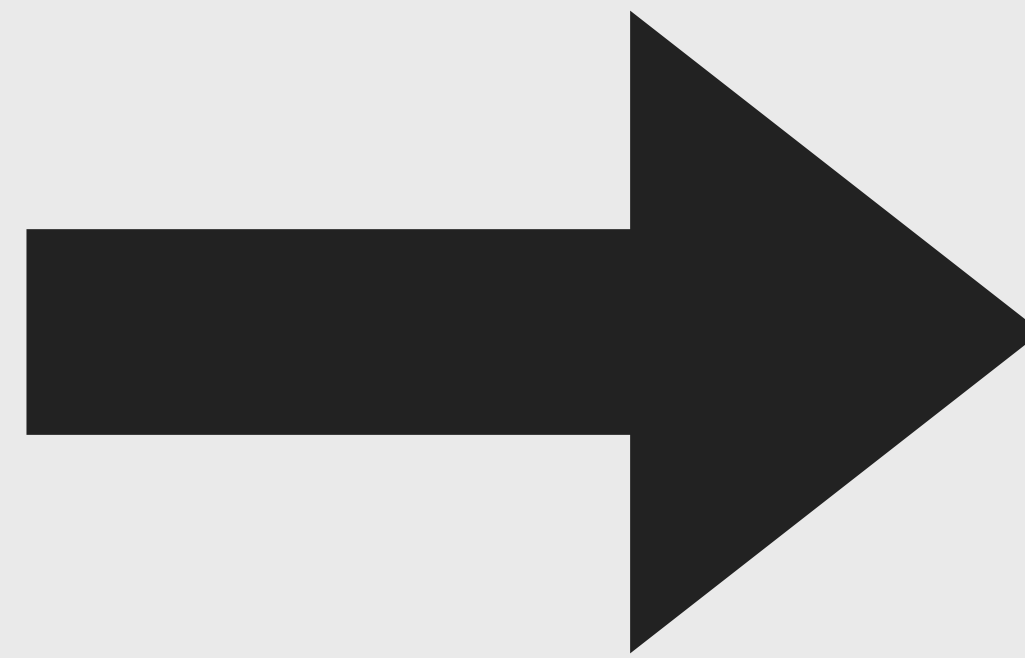
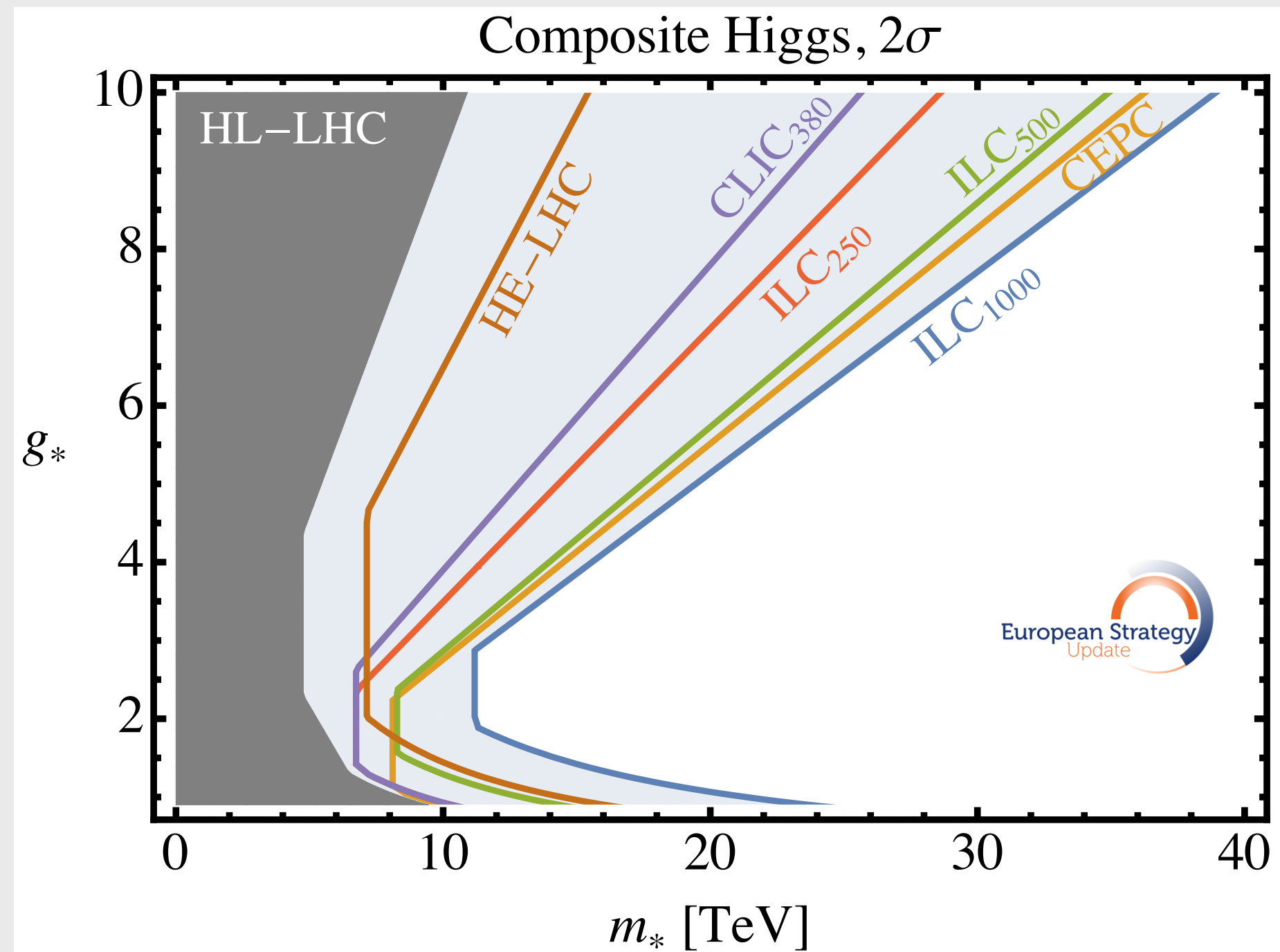
contact interactions



$$\ell_{top} \sim 1/m_{\star} \sim \ell_{Higgs}$$



Higgs compositeness

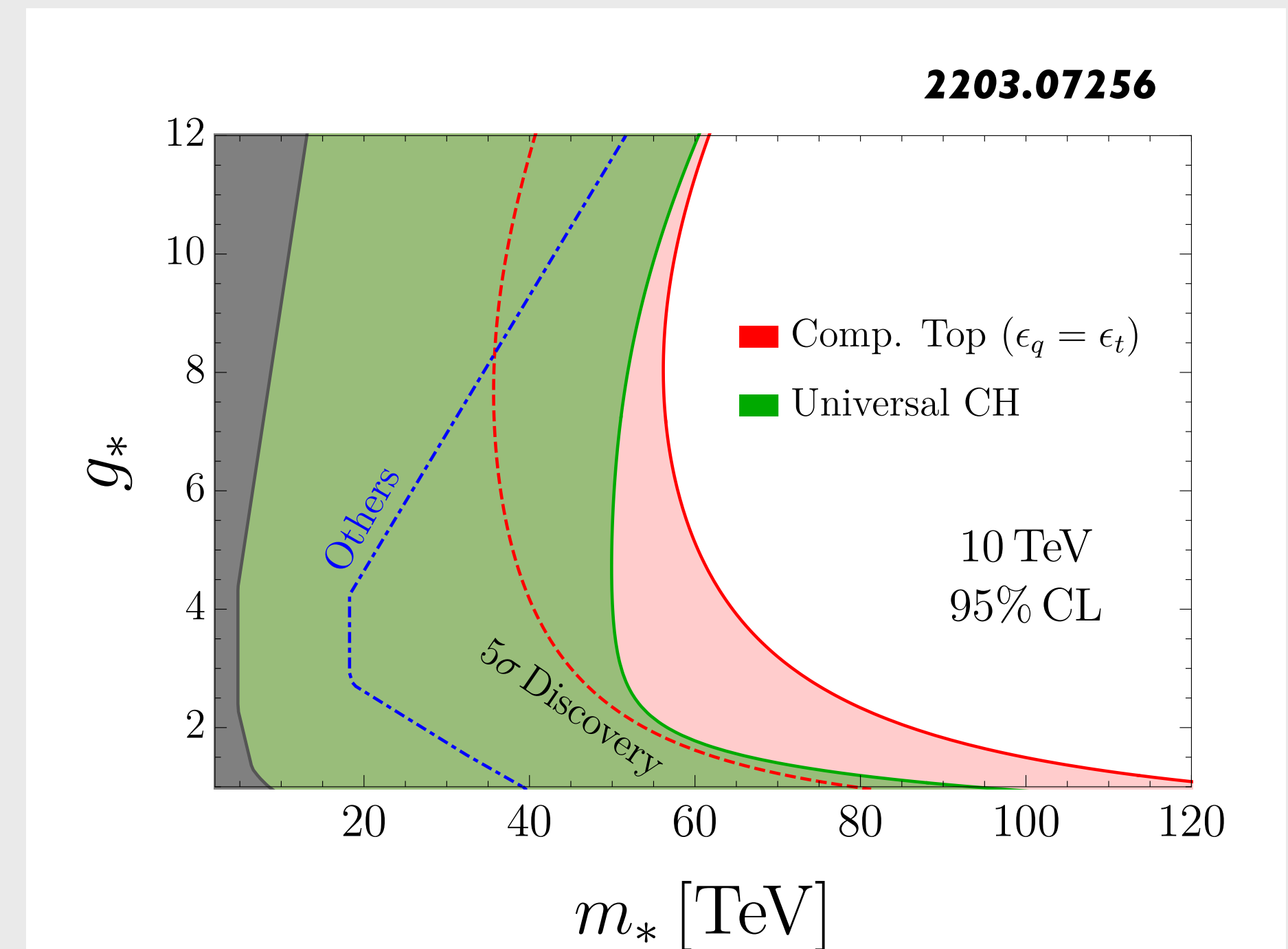
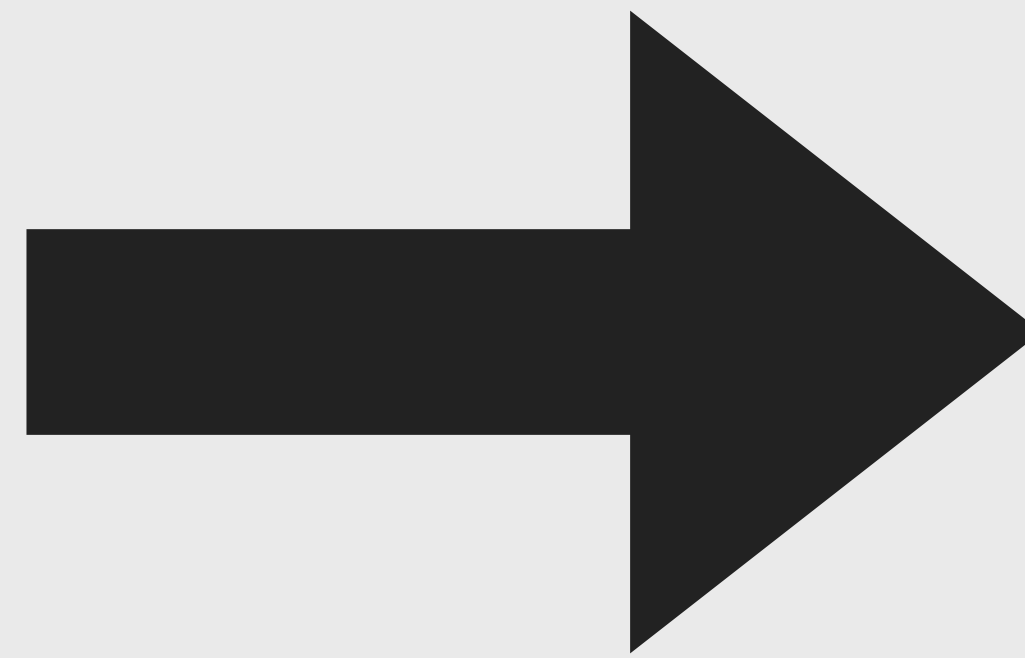
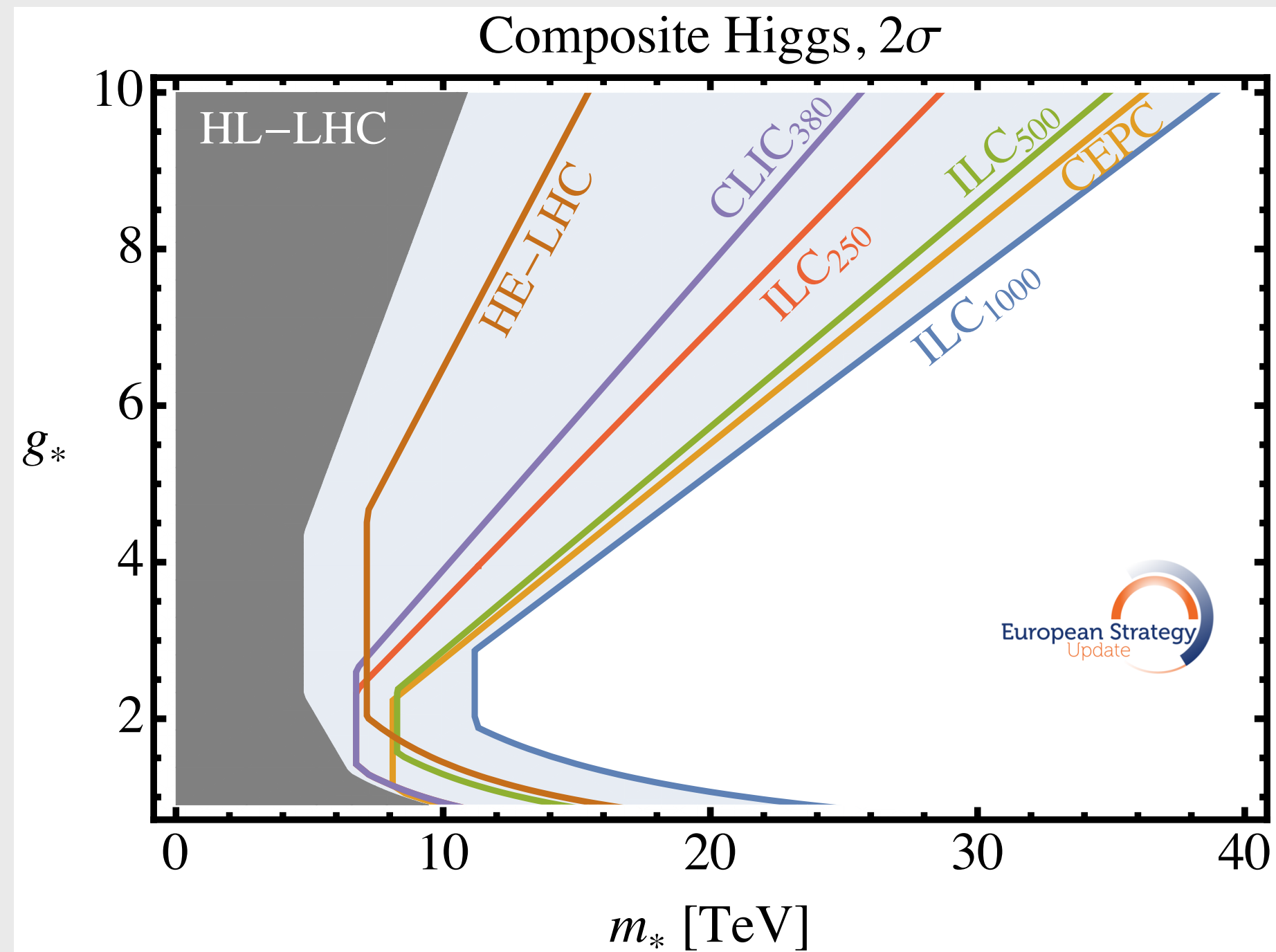


**compositeness at
few TeV @ HL-LHC**

**compositeness at
few 10 TeV**

Higgs compositeness

UNIQUE AVENUE TO EXPLORE WEAK INTERACTIONS
FAR OFFSHORE FROM THE WEAK SCALE



compositeness at
few TeV @ HL-LHC

compositeness at
few 100 TeV

Higgs BSM decays

$h \rightarrow \phi\phi$

EW PHASE TRANSITION

DRIVEN BY A LIGHT SCALAR

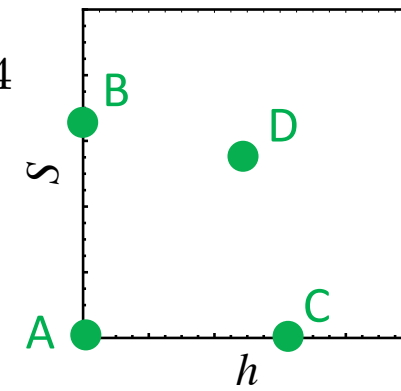
a minimal $B(h \rightarrow \phi\phi)$ to insure a strong first order phase transition

Relation between a_2 and phase transition

<https://indico.cern.ch/event/1149554/>

Condition for two degenerate vacua

$$V = -\frac{\mu^2 - c_h T^2}{2} h^2 + \frac{\lambda}{4} h^4 + \frac{a_2}{4} h^2 S^2 + \frac{b_2 + c_S T^2}{2} S^2 + \frac{b_4}{4} S^4$$



Some facts: [1909.02014]

1. ABCD could be either local extrema or saddle points;
2. If D is a minimum then BC are saddle points;
3. If A is a minimum then BC are saddle points, while D is NOT a minimum.
4. The only case of two degenerate vacua is BC, which requires $b_2 < 0$.

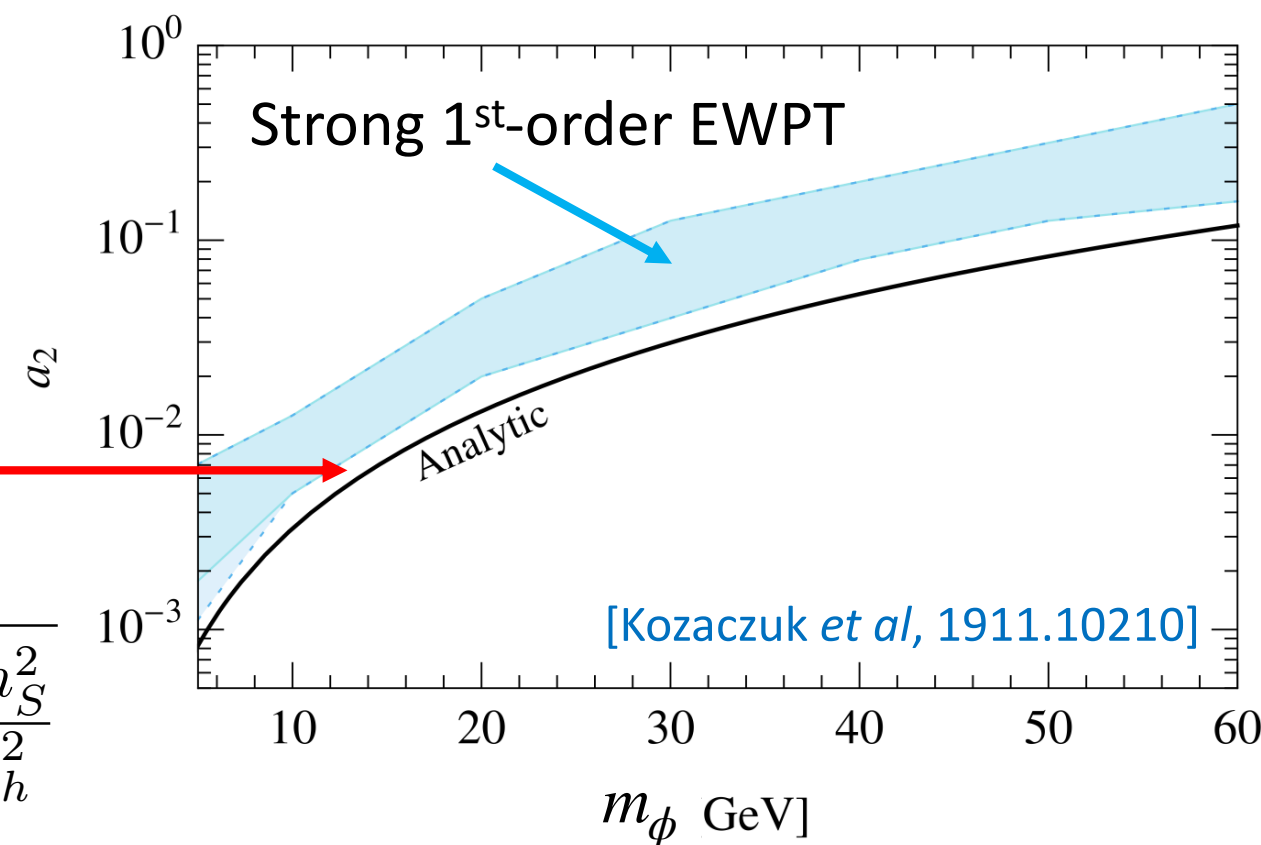
$$m_\phi = \sqrt{b_2 + \frac{a_2^2}{2} v_{EW}^2}$$

Therefore we get

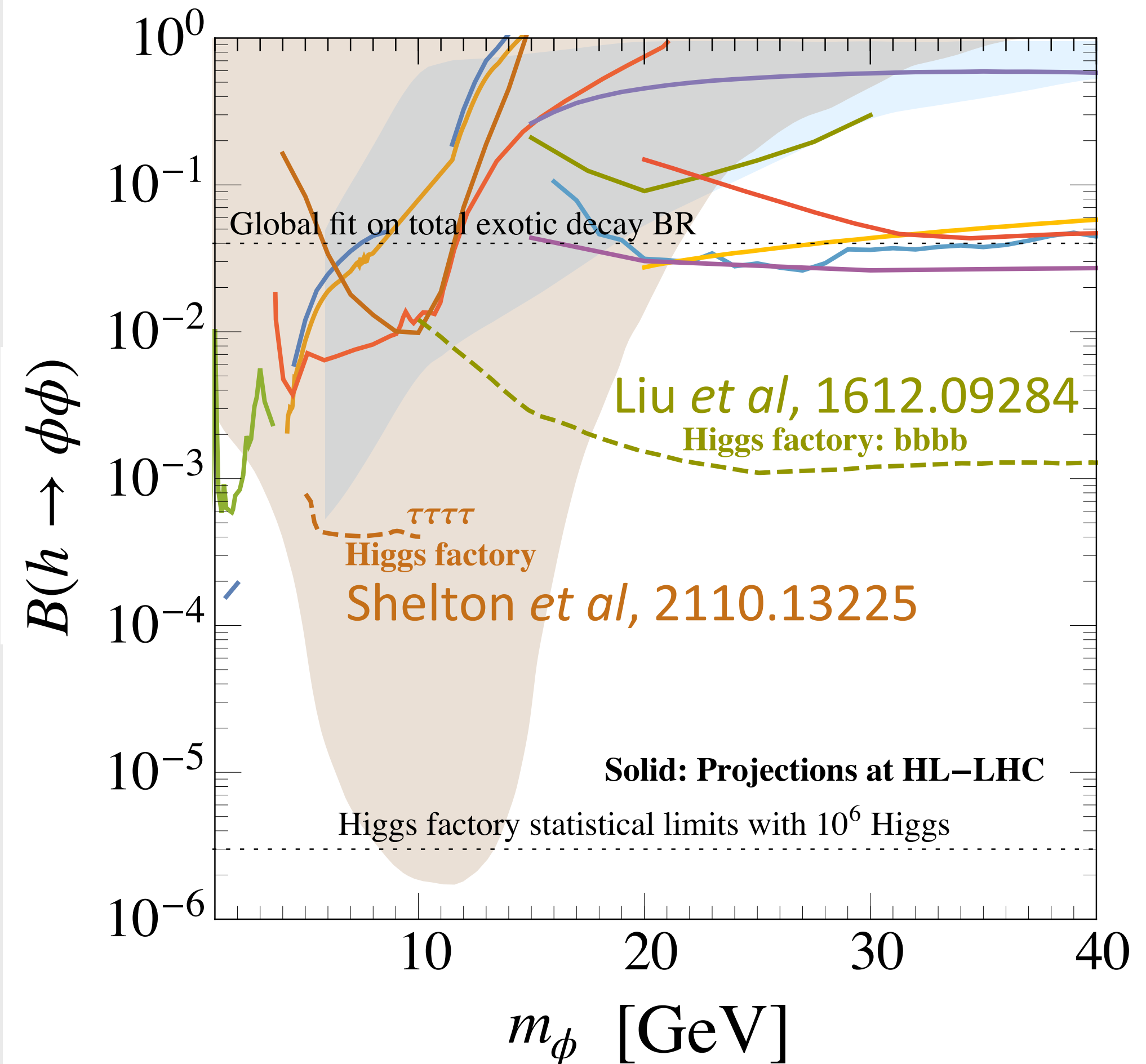
$$a_2 > \frac{2m_\phi^2}{v_{EW}^2}$$

Which is a lower limit on

$$\Gamma(h \rightarrow SS) = \frac{a_2^2 v_{EW}^2}{32\pi m_h} \sqrt{1 - \frac{4m_S^2}{m_h^2}}$$



Ke-Pan Xie, U of Nebraska-Lincoln



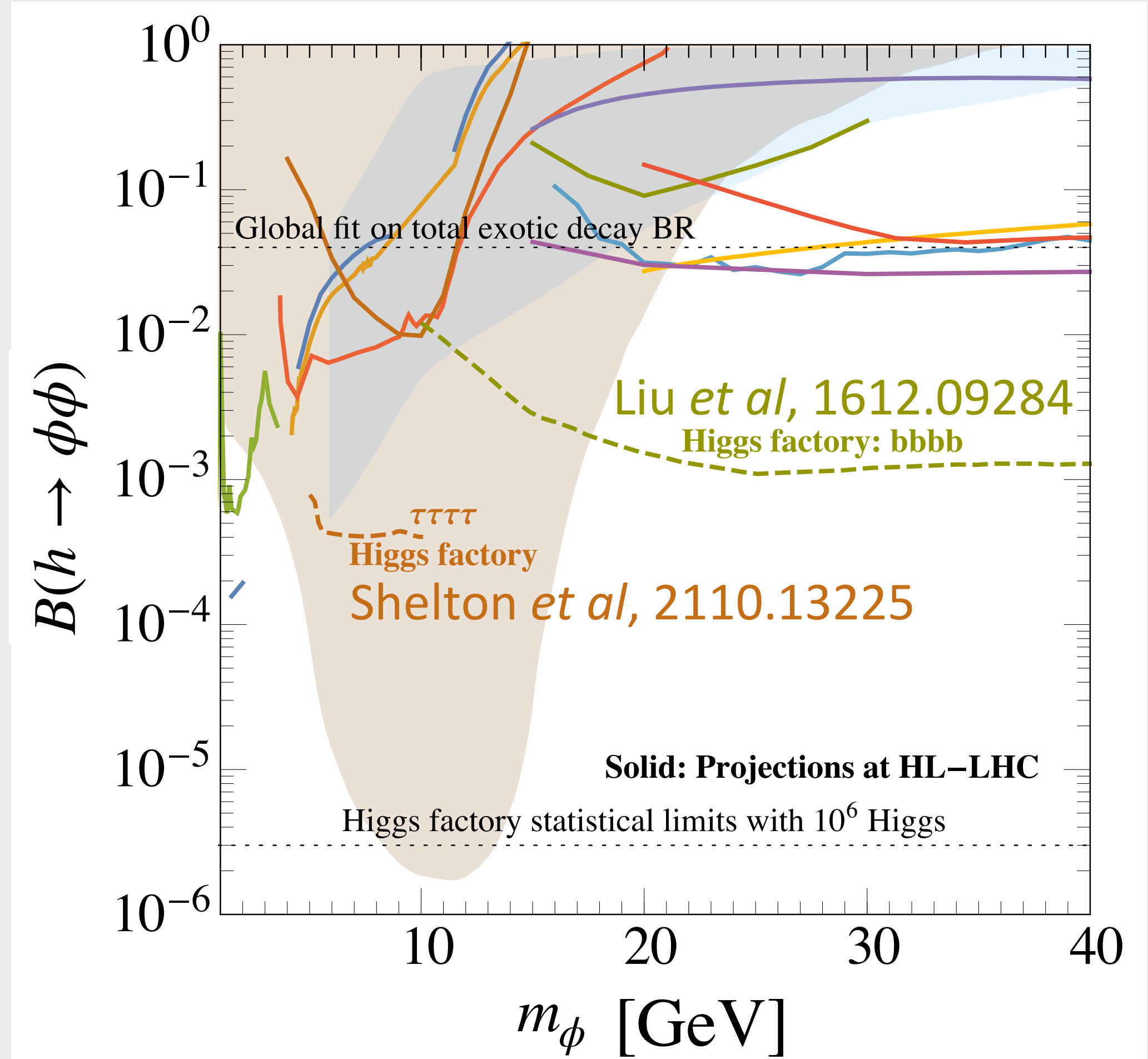
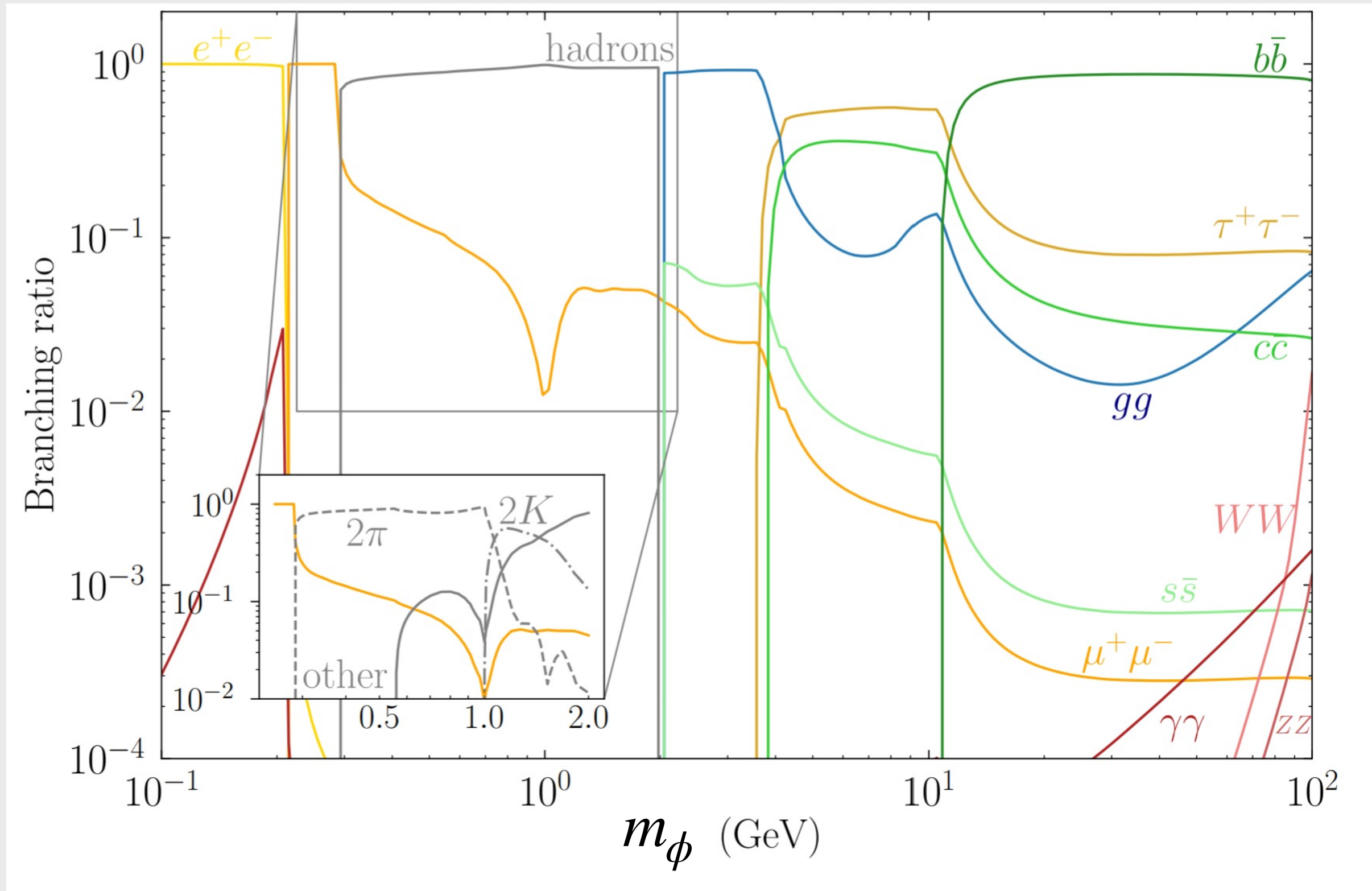
$h \rightarrow \phi\phi$

EW PHASE TRANSITION

DRIVEN BY A LIGHT SCALAR

a minimal $B(h \rightarrow \phi\phi)$ to insure a strong first order phase transition

2012.07864



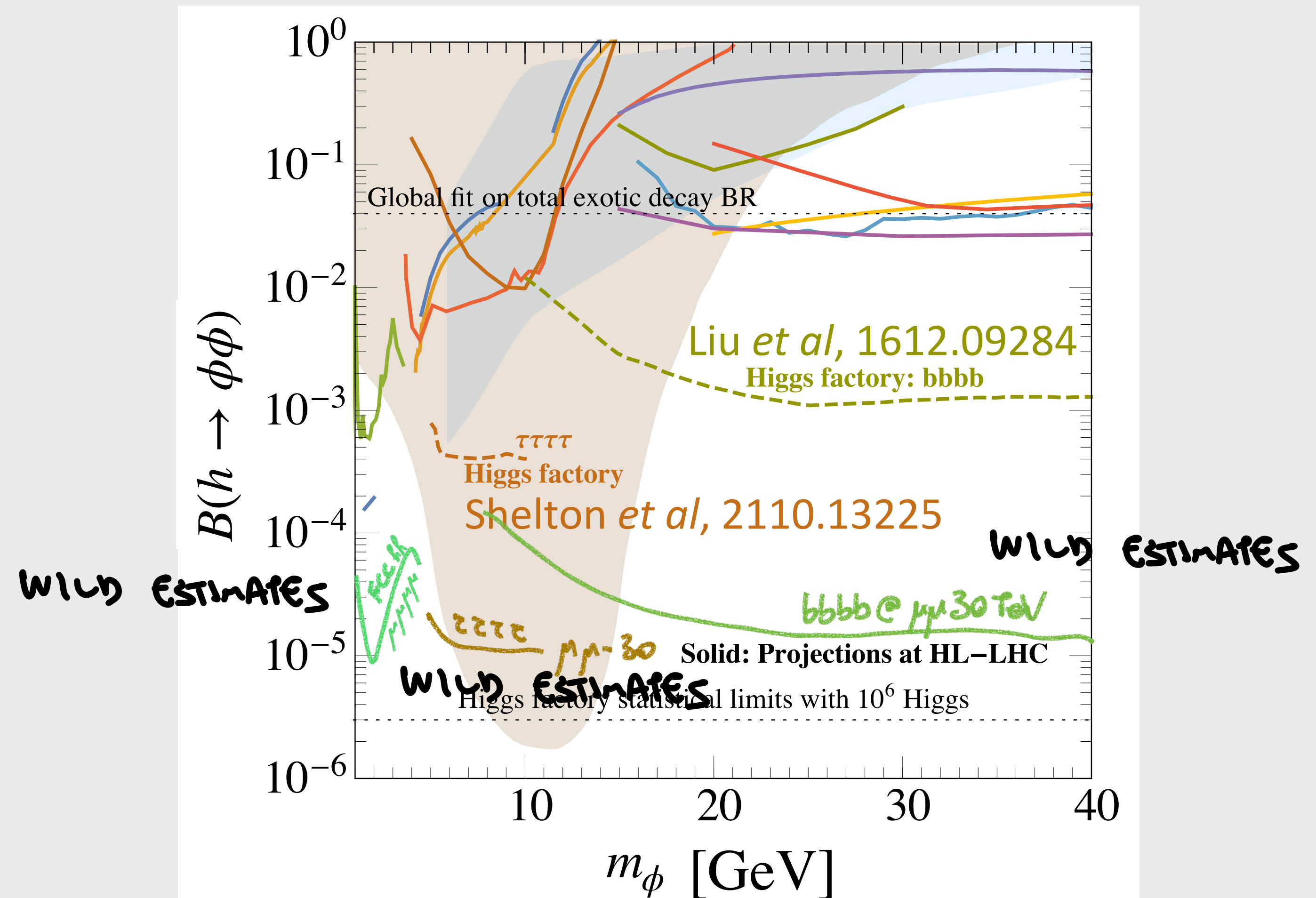
$h \rightarrow \phi\phi$

EW PHASE TRANSITION

DRIVEN BY A LIGHT SCALAR

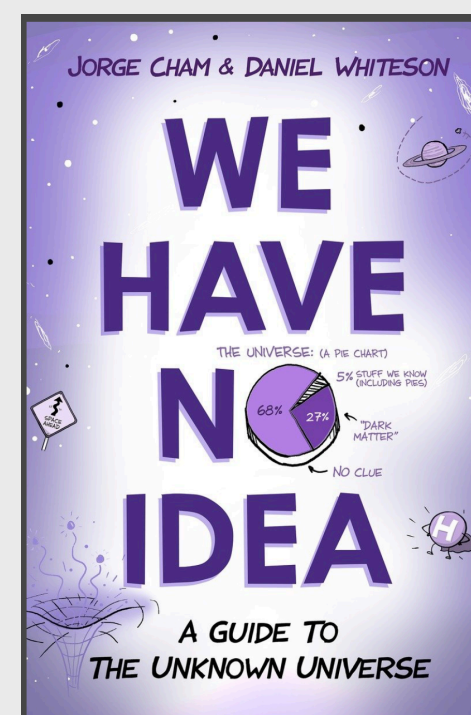
a minimal $B(h \rightarrow \phi\phi)$ to insure a strong first order phase transition

- opportunities both for FCC- hh and $\mu\mu$ to contribute new lines on this plot
- potential to be sensitive to the entire region of first order phase transition (only) by a combination of results from multiple machines



Neutrino mass models

a wide landscape of possibilities that benefits from multiple approaches



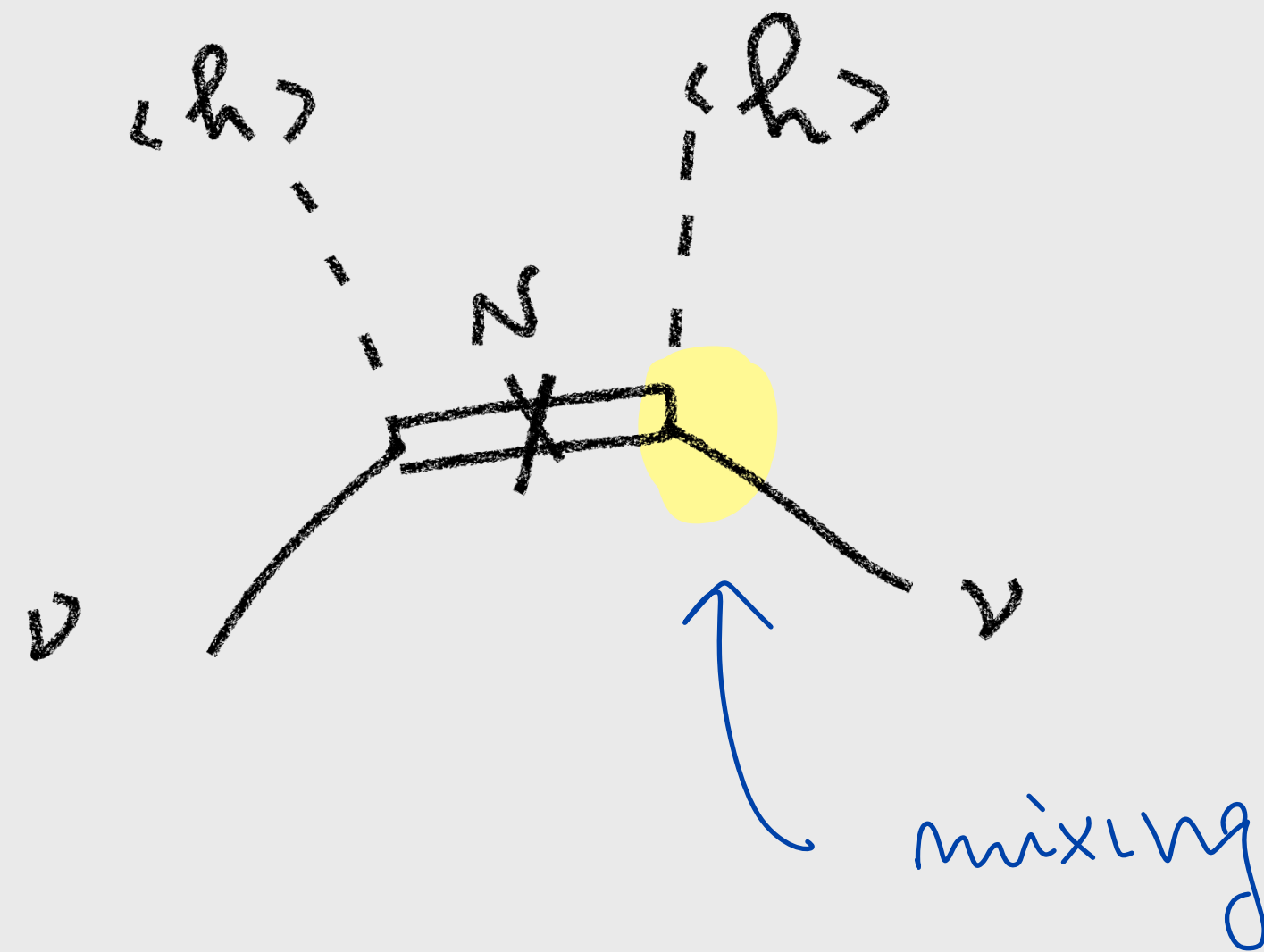
$(LH)(LH)$ from “the” seesaw

KEY INGREDIENT

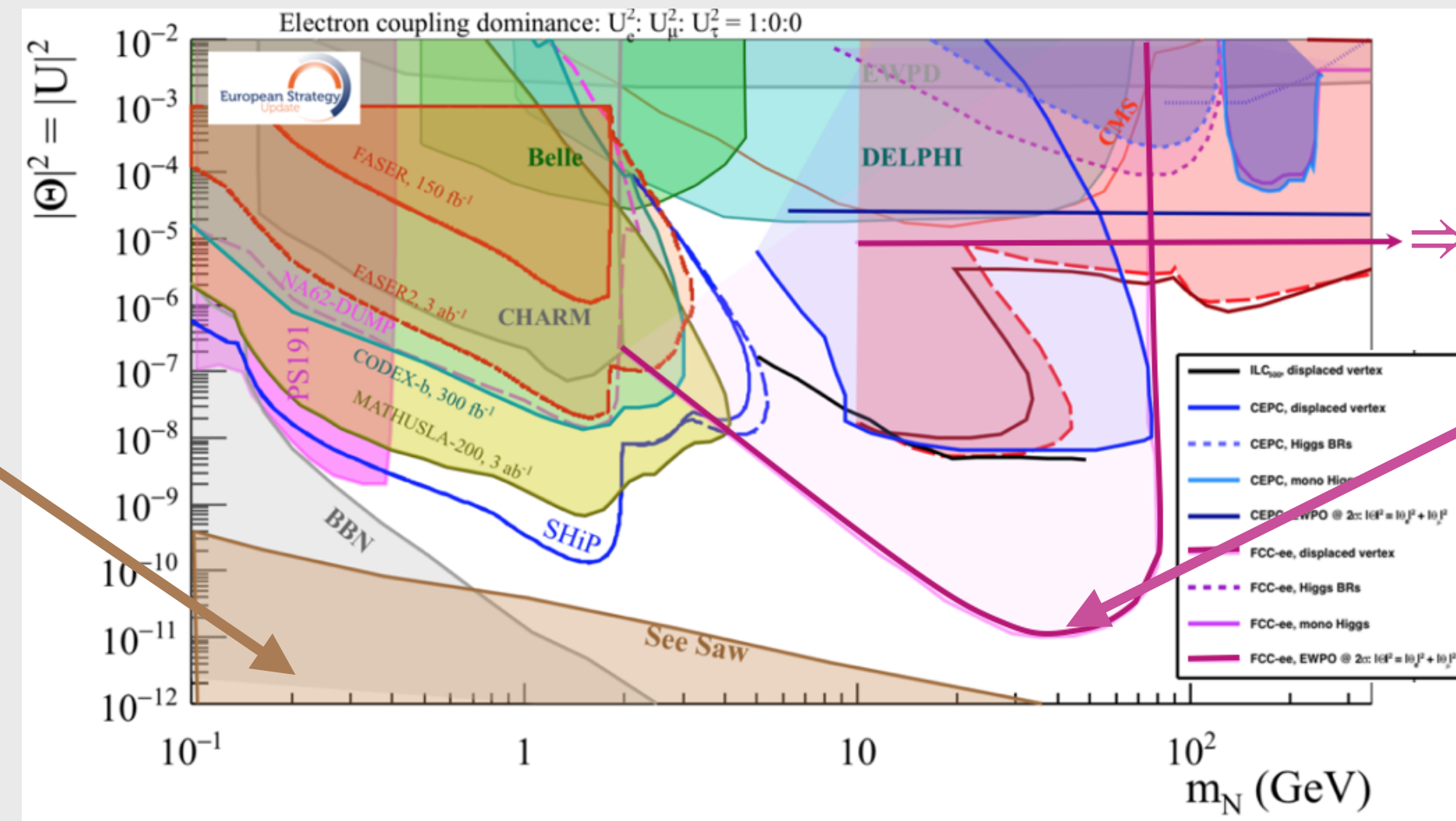
LEPTON NUMBER BREAKING MAJORANA MASS TERM

- light neutrino masses governed by mixing with heavy neutrinos and mass of the heavier neutrino

$$m_\nu \sim \frac{y^2 v^2}{M} = \Theta^2 M$$



$$\Theta \approx \sqrt{\frac{eV}{M}}$$



indirect from high-precision Z pole up to $M \gg 100$ GeV
 $\Rightarrow \Theta \lesssim 0.3 \cdot 10^{-2}$

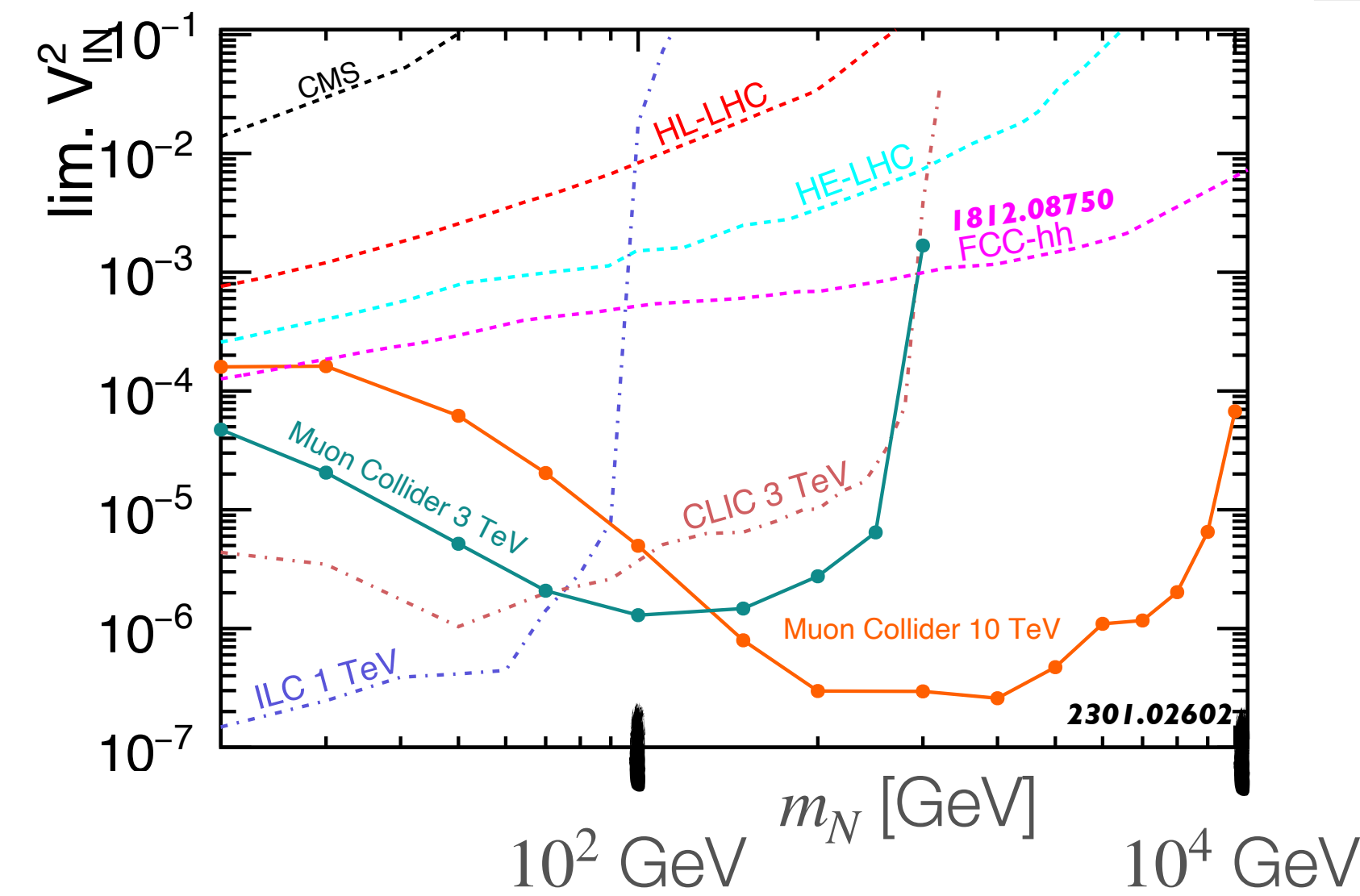
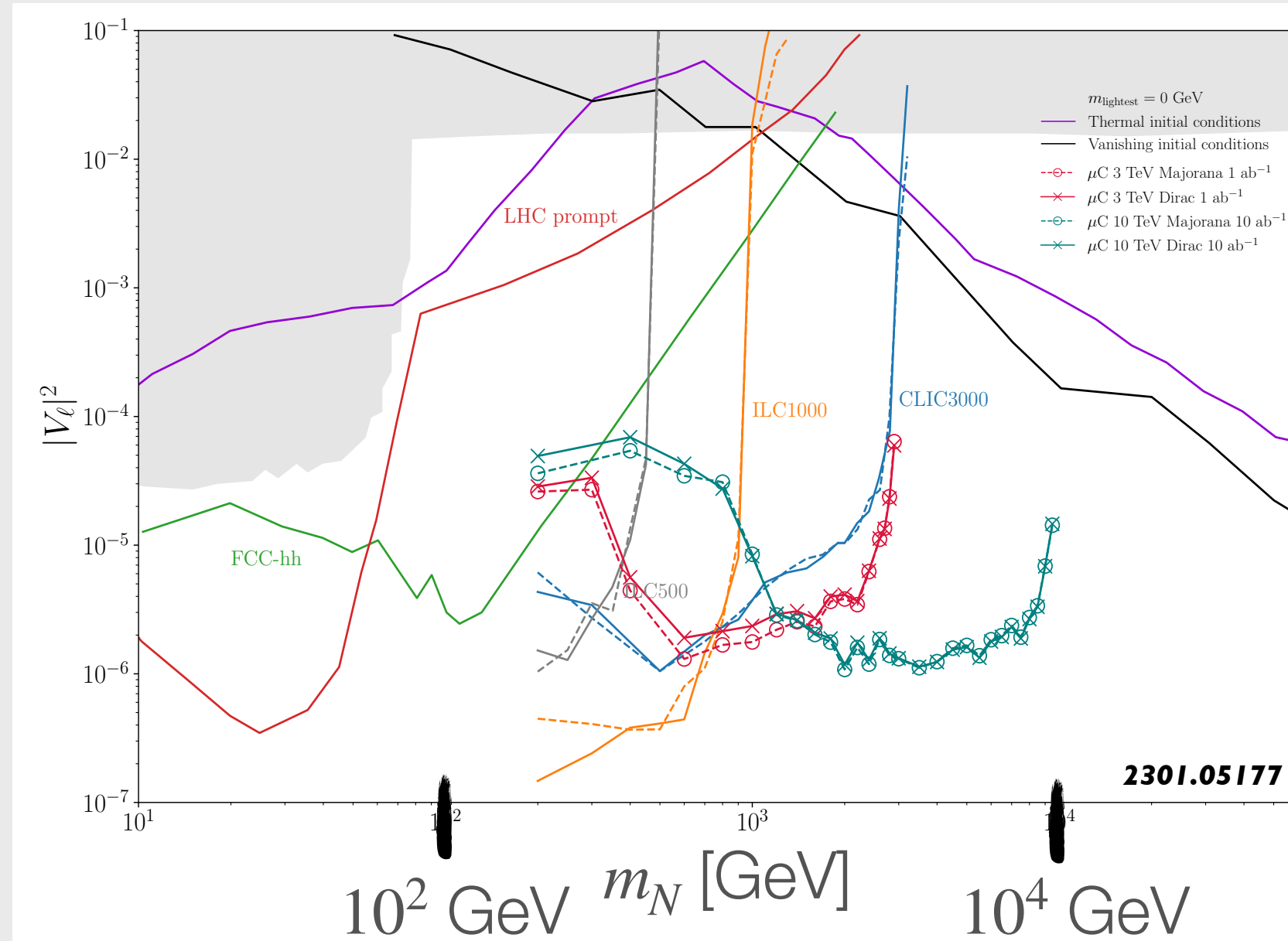
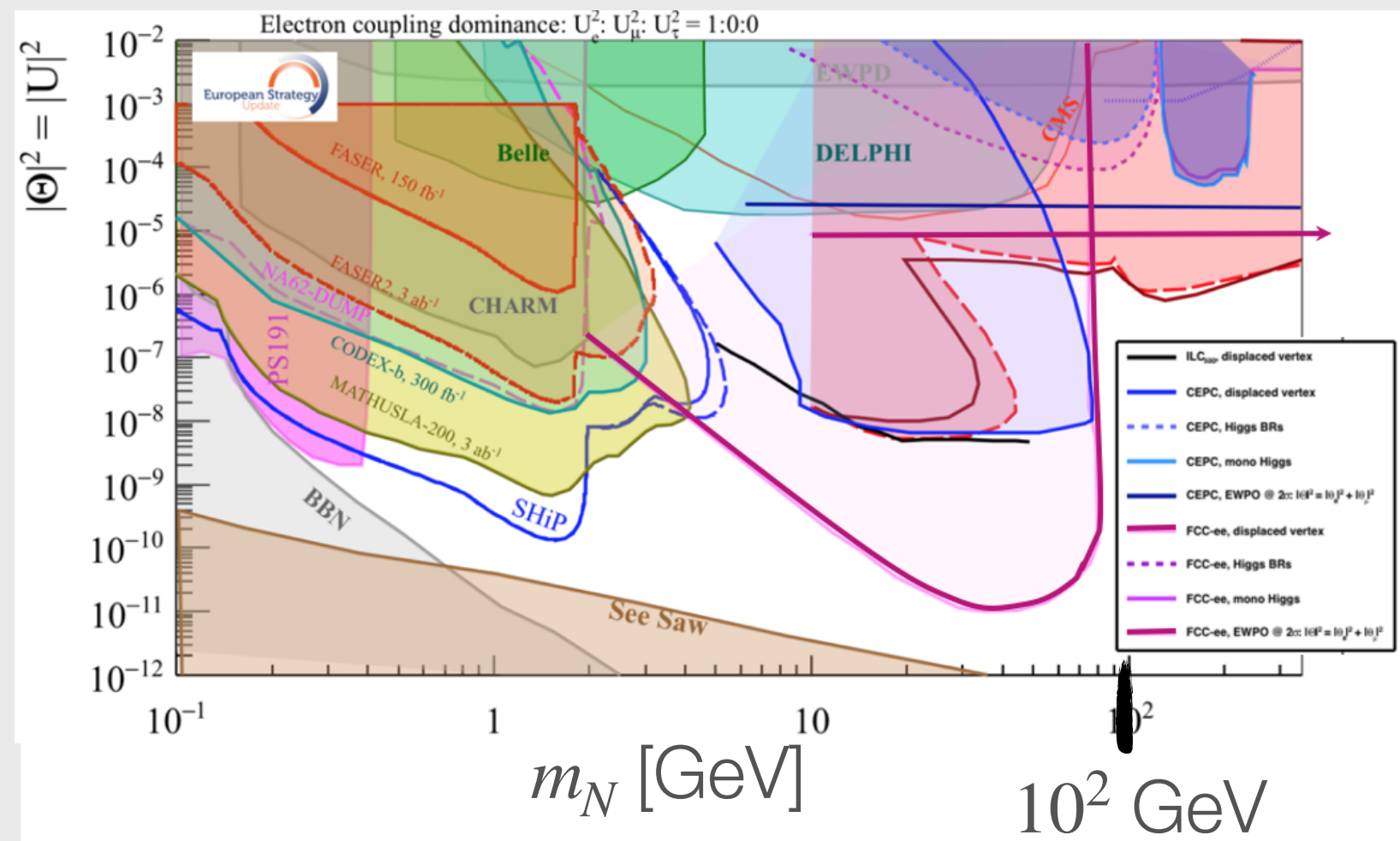
$\Rightarrow \Theta \lesssim 3 \cdot 10^{-6}$
 $M \simeq 100$ GeV

FCCee has fantastic sensitivity, but only to light N

$(LH)(LH)$ from “the” seesaw

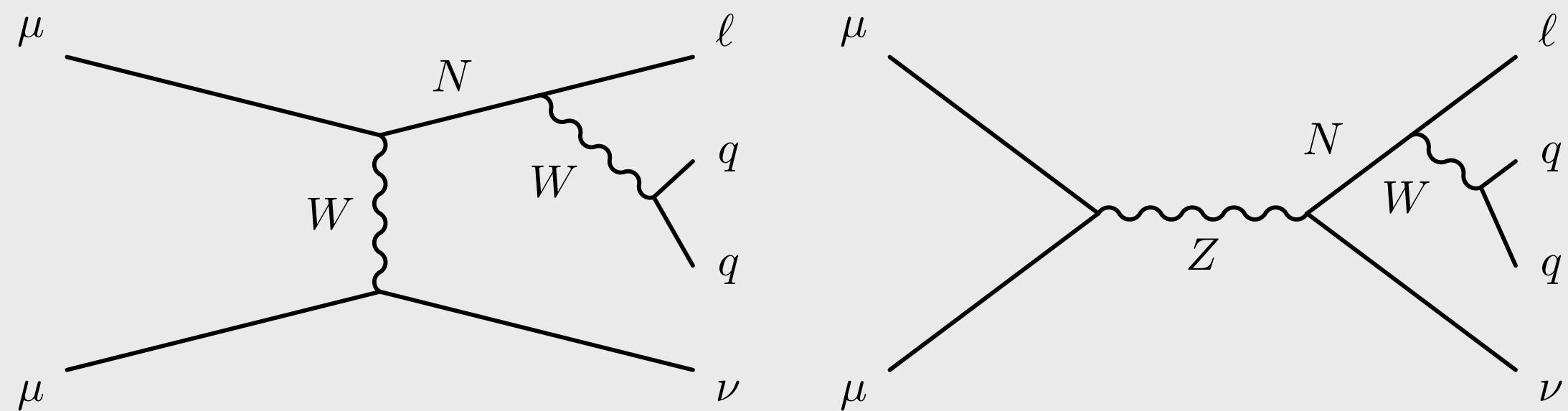
KEY INGREDIENT

LEPTON NUMBER BREAKING MAJORANA MASS TERM



FCC ee has fantastic sensitivity, but only to light N

heavy N can be tested at FCC hh and even deeper at $\mu\mu$

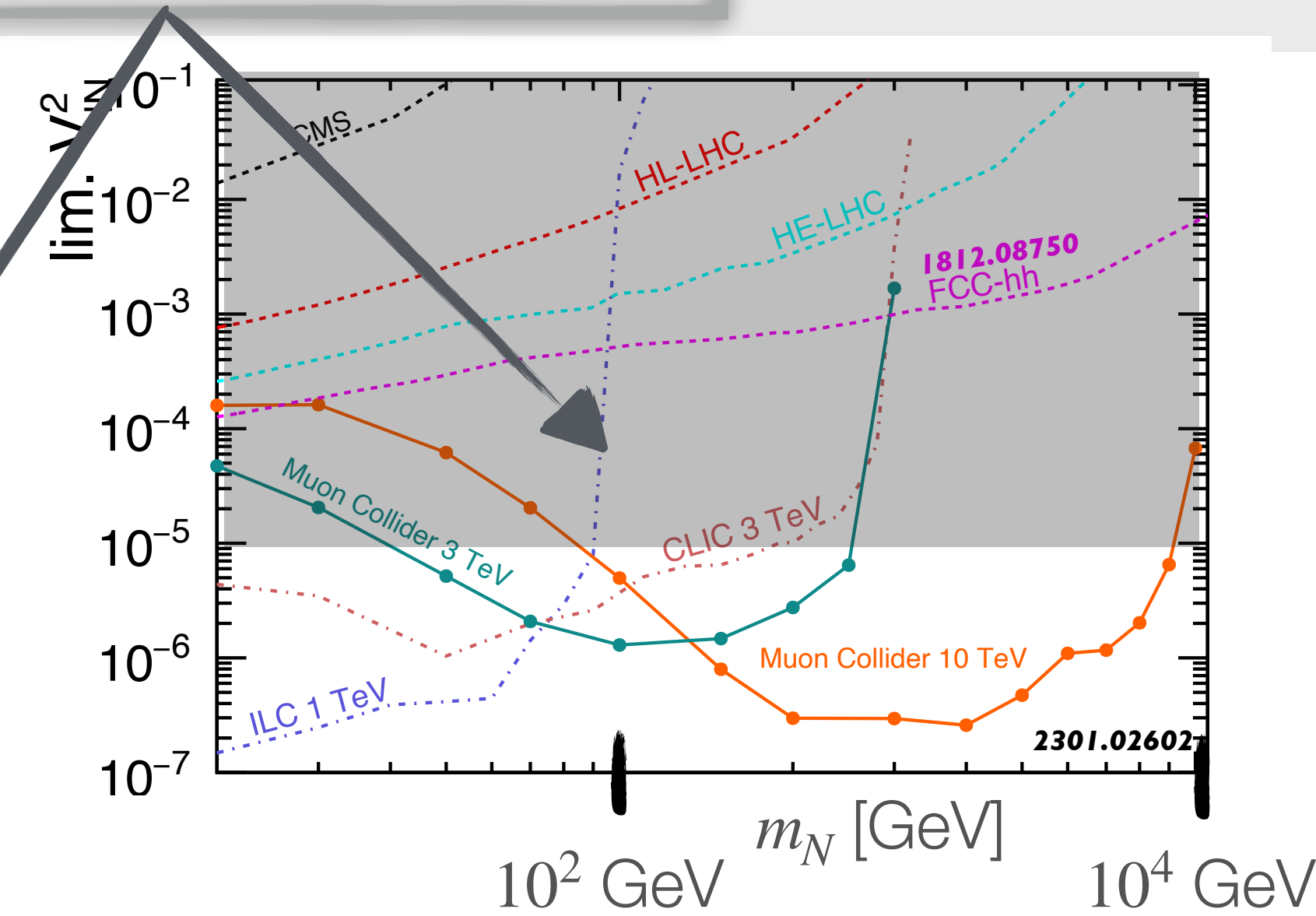
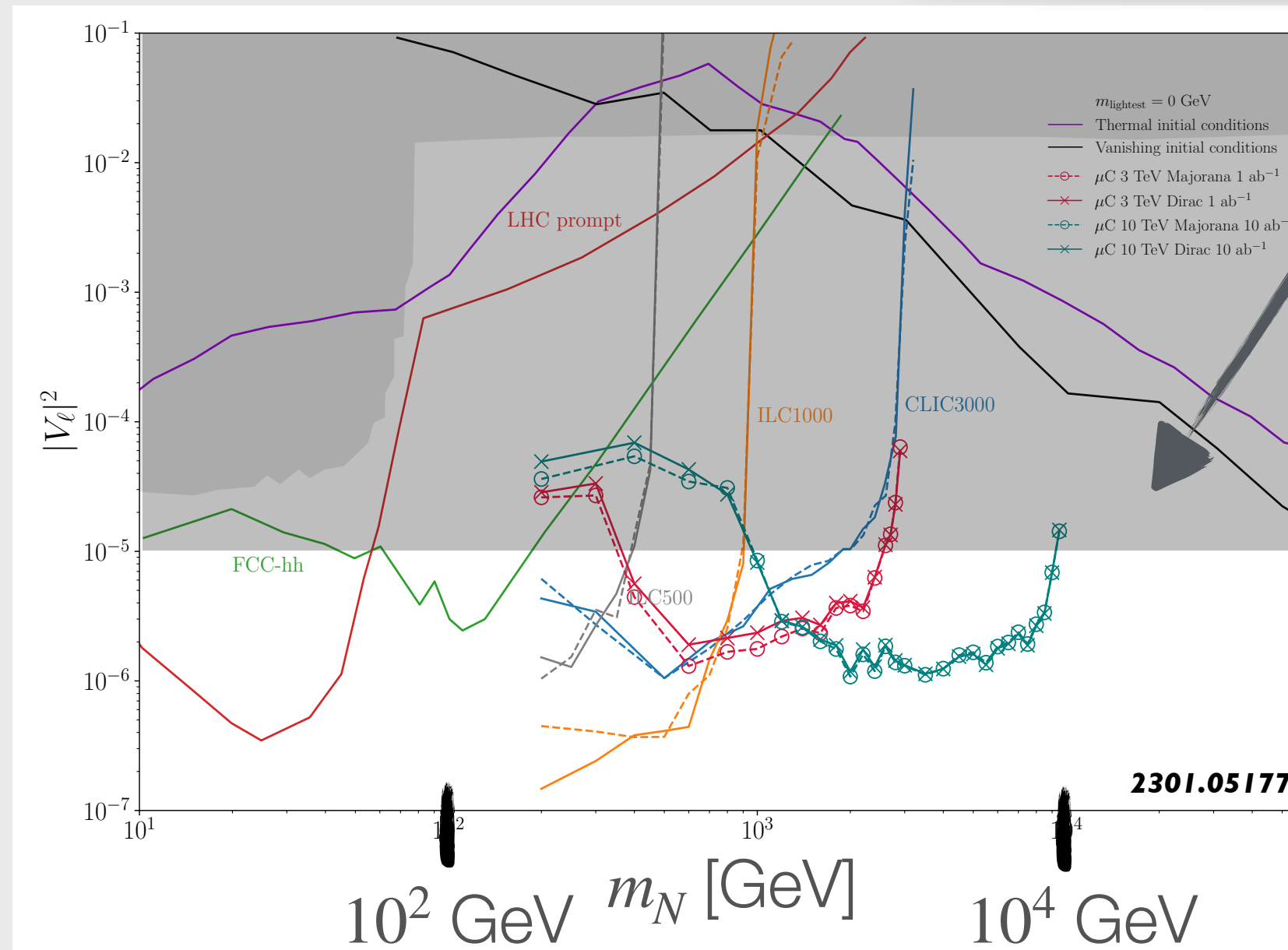
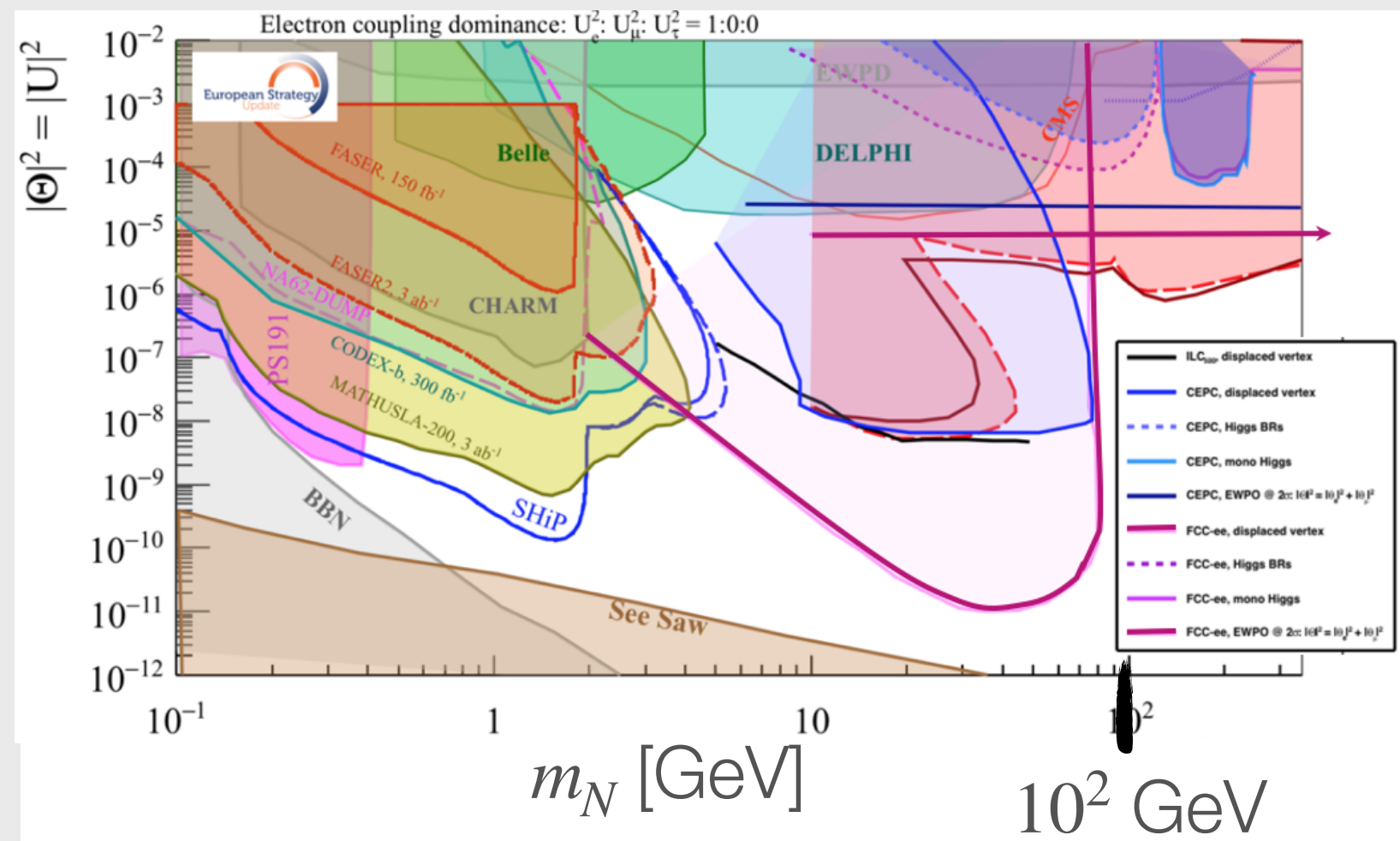


$(LH)(LH)$ from “the” seesaw

KEY INGREDIENT

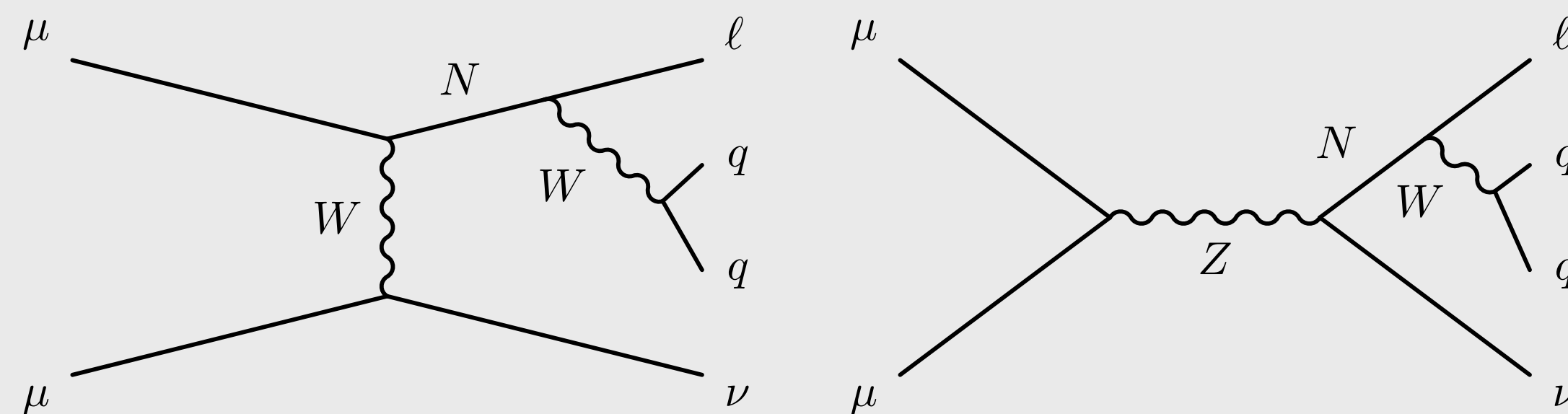
LEPTON NUMBER BREAKING MAJORANA MASS TERM

if Z pole high-precision theory delivers



FCC ee has fantastic sensitivity, but only to light N

heavy N can be tested at FCC hh and even deeper at $\mu\mu$

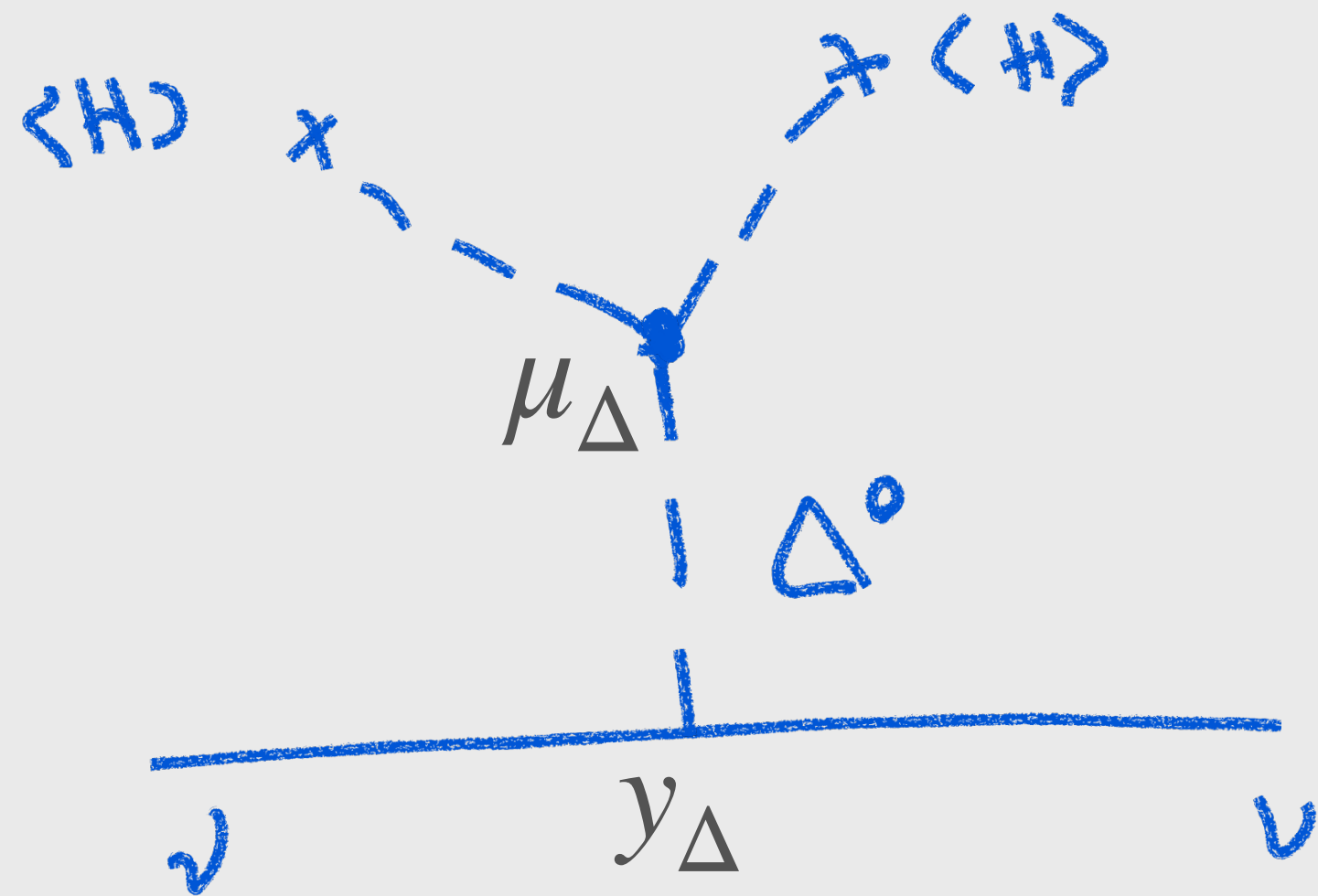


$(LH)(LH)$ from one of “the other” seesaws

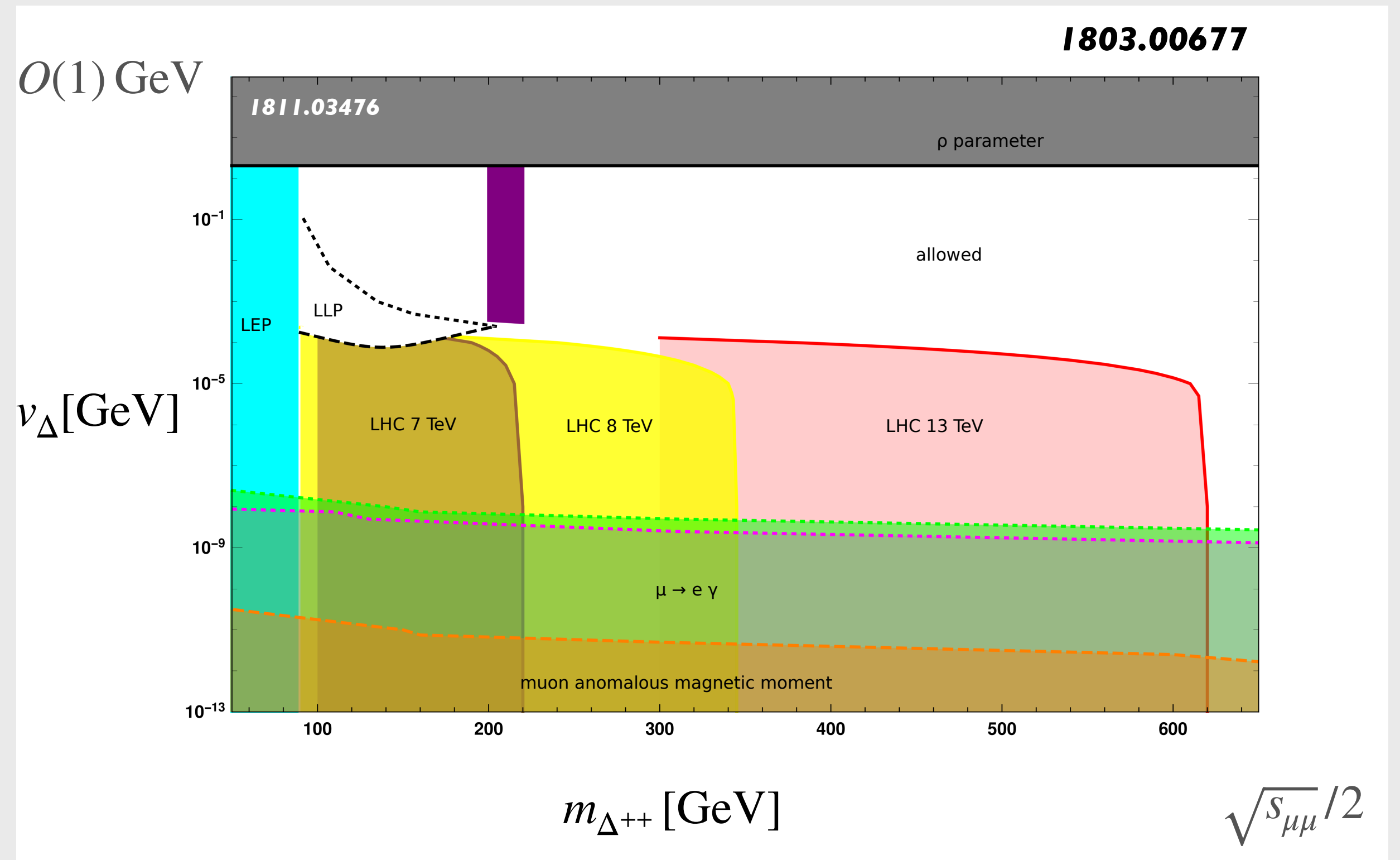
KEY INGREDIENT

LEPTON NUMBER BREAKING MAJORANA MASS TERM

- neutrino masses governed by scalar potential term of the heavy triplet scalar and mass of the heavy scalar



$$m_\nu \sim \frac{y_\Delta \mu_\Delta}{m_\Delta^2}$$

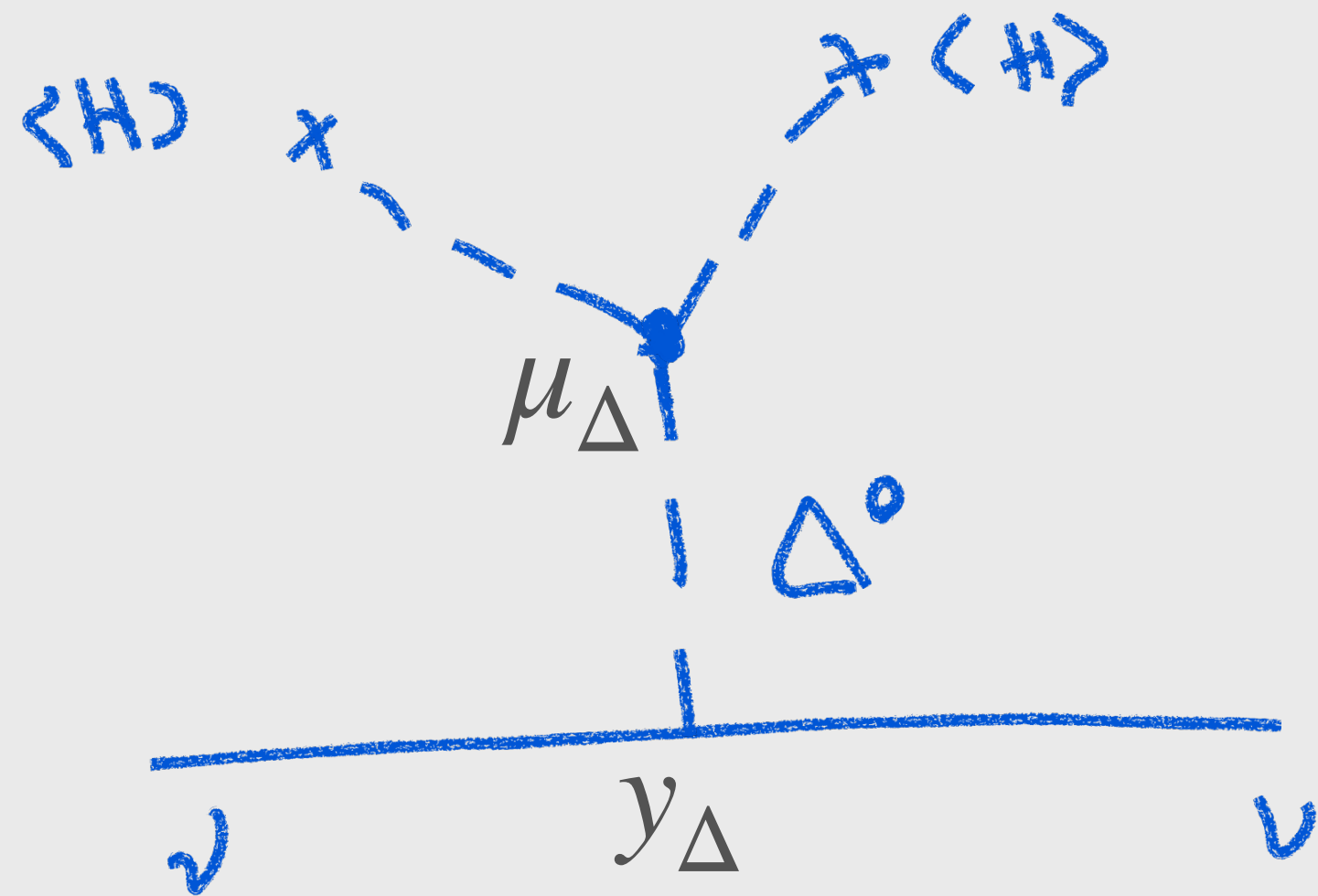


$(LH)(LH)$ from one of “the other” seesaws

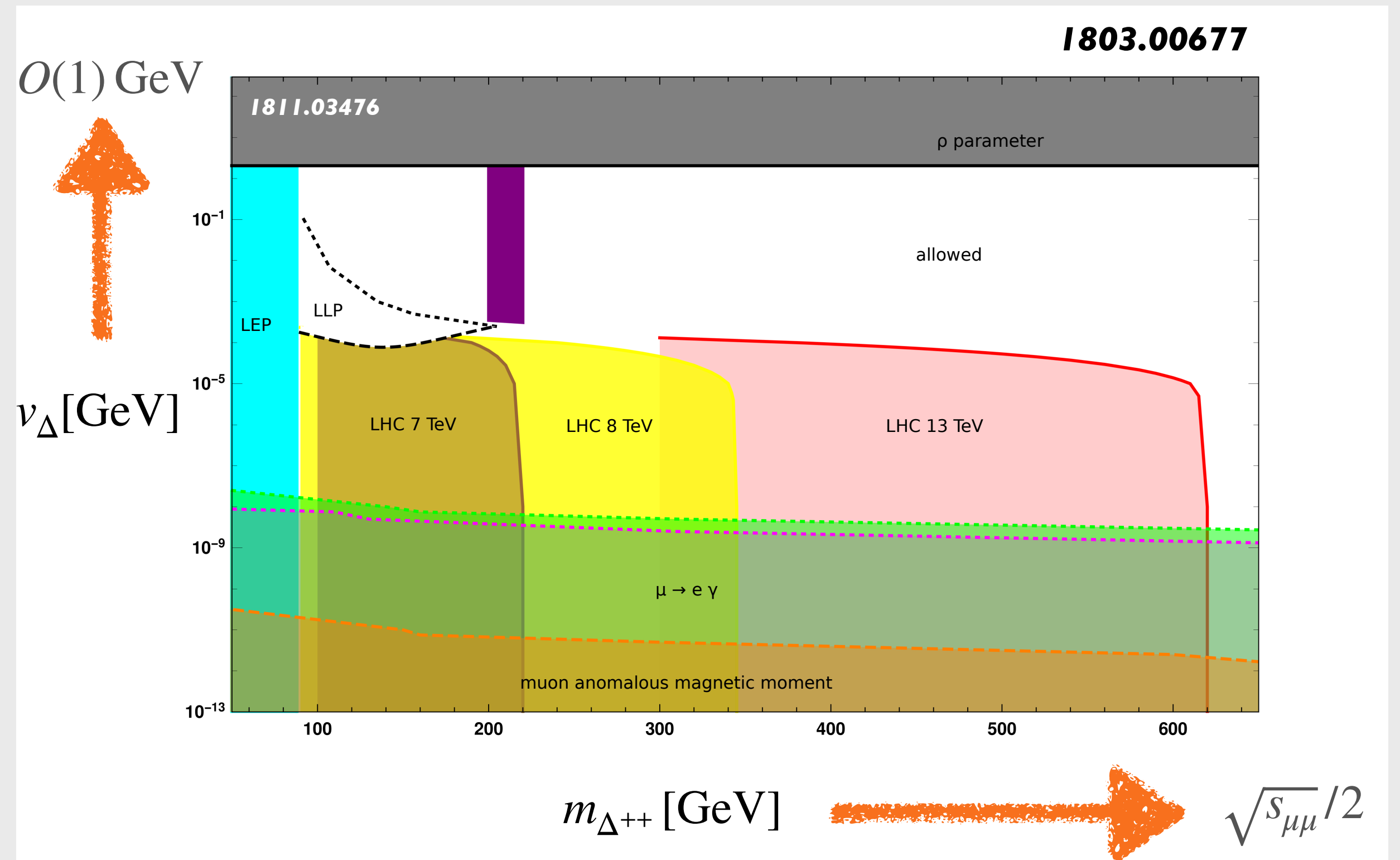
KEY INGREDIENT

LEPTON NUMBER BREAKING MAJORANA MASS TERM

- neutrino masses governed by scalar potential term of the heavy triplet scalar and mass of the heavy scalar



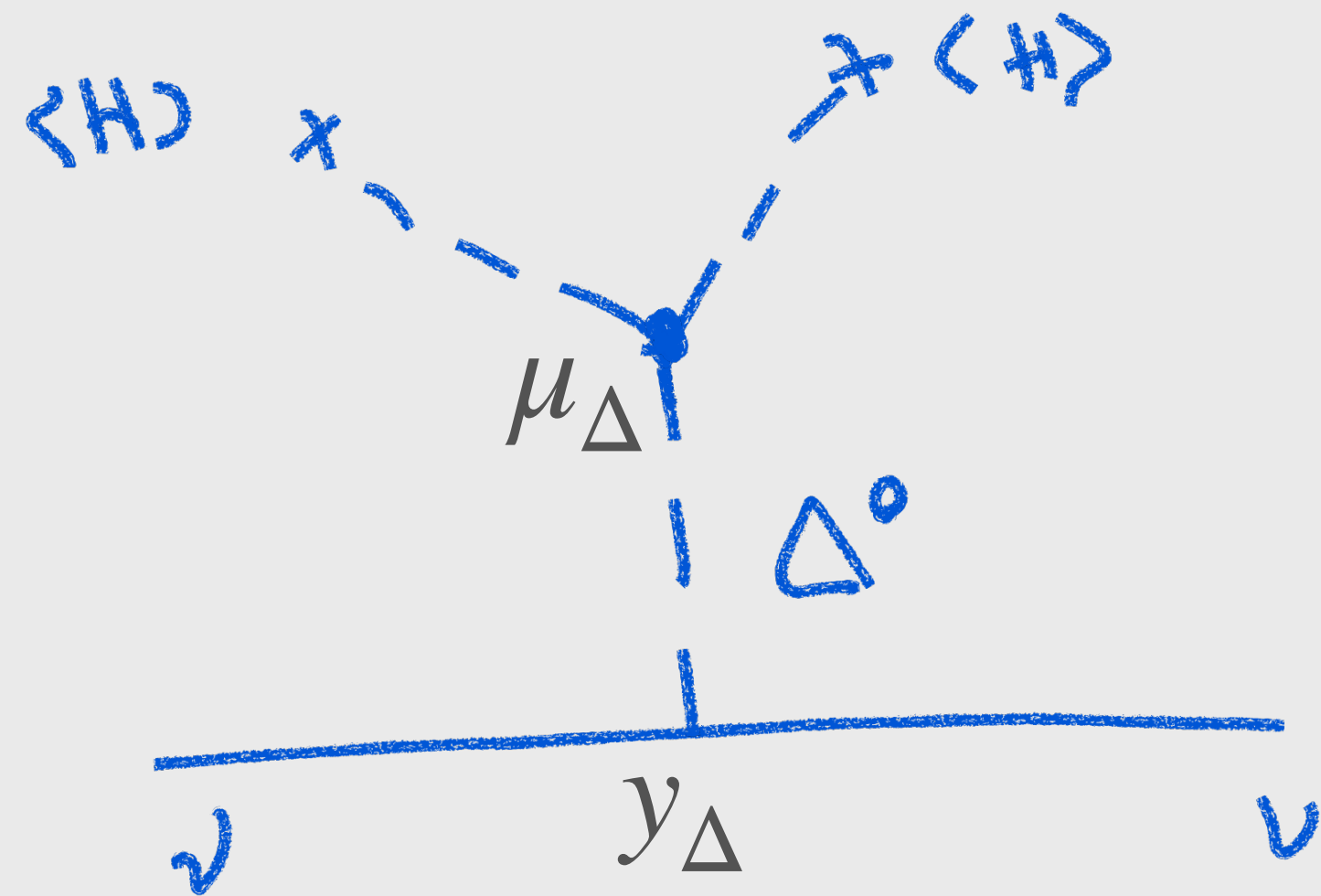
$$m_\nu \sim \frac{y_\Delta \mu_\Delta}{m_\Delta^2}$$



$(LH)(LH)$ from one of “the other” seesaws

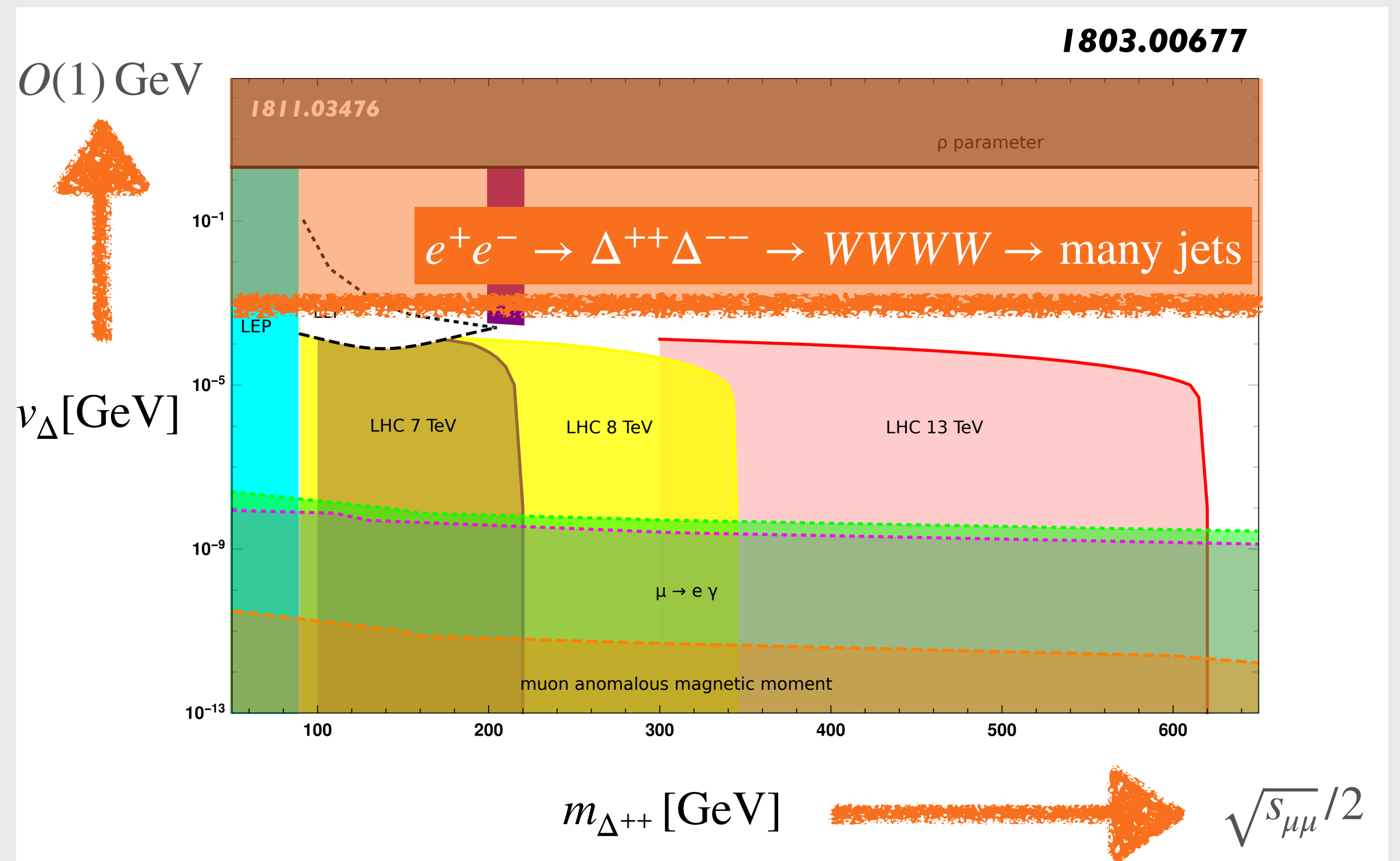
KEY INGREDIENT

LEPTON NUMBER BREAKING MAJORANA MASS TERM



$$m_\nu \sim \frac{y_\Delta \mu_\Delta}{m_\Delta^2}$$

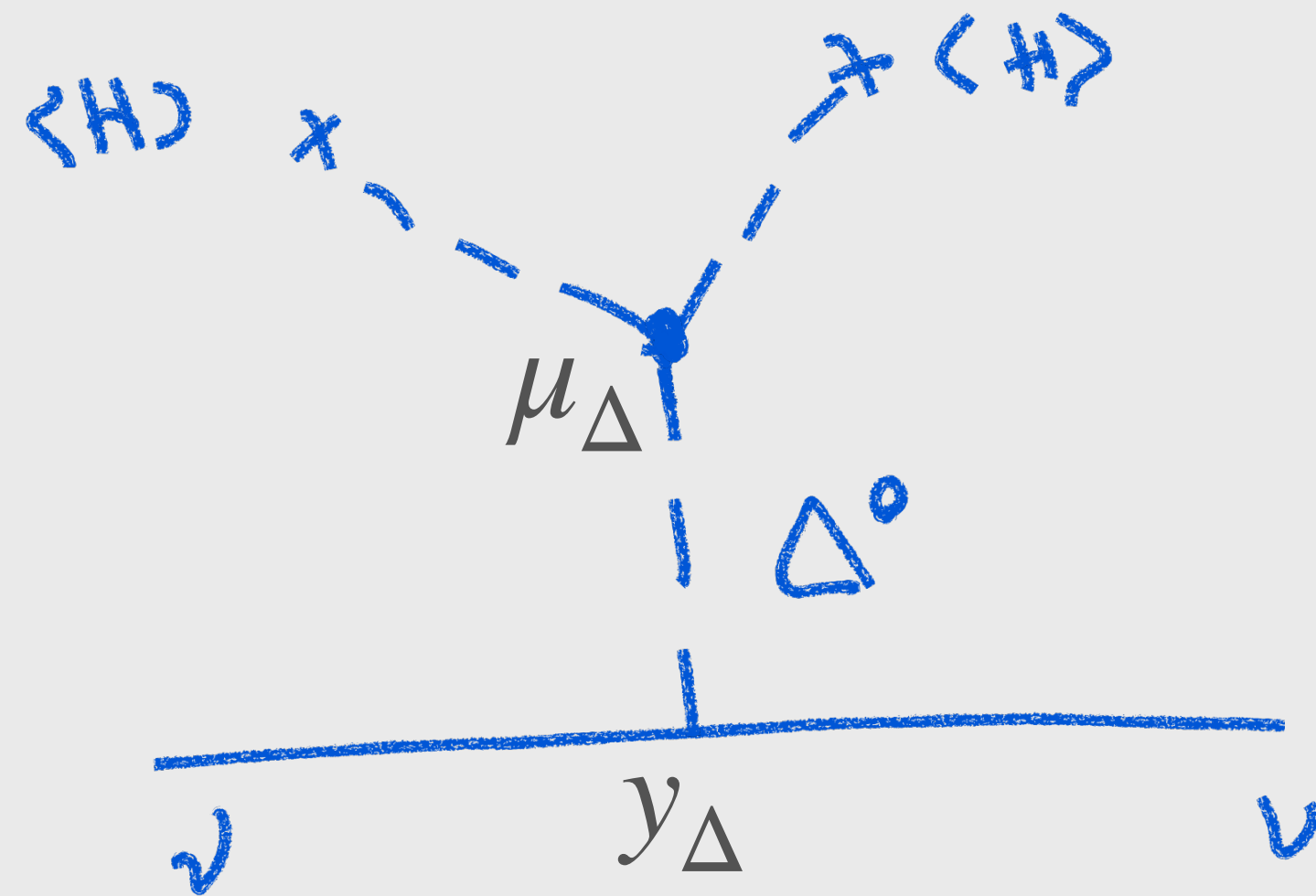
- neutrino masses governed by scalar potential term of the heavy triplet scalar and mass of the heavy scalar



$(LH)(LH)$ from one of “the other” seesaws

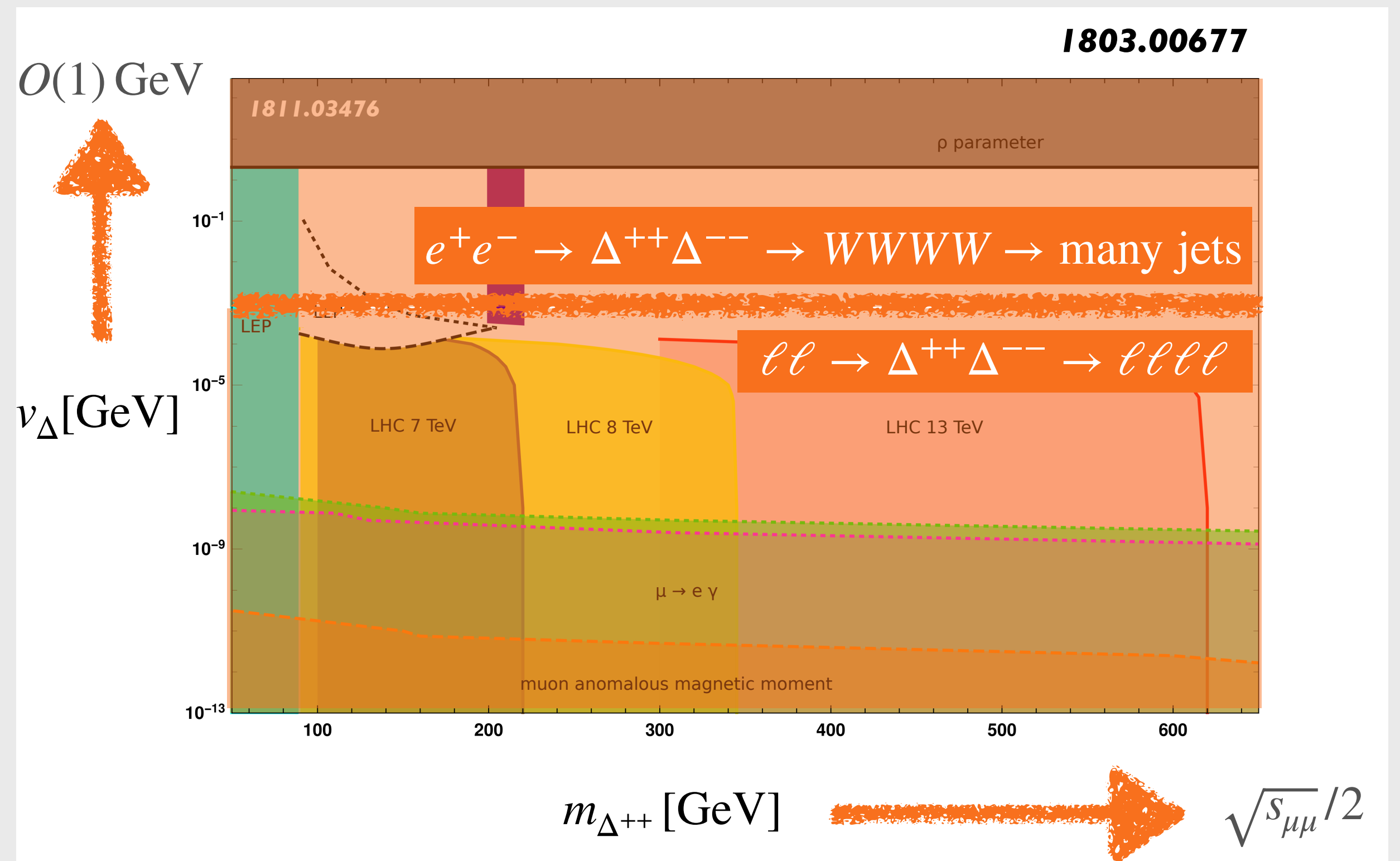
KEY INGREDIENT

LEPTON NUMBER BREAKING MAJORANA MASS TERM



$$m_\nu \sim \frac{y_\Delta \mu_\Delta}{m_\Delta^2}$$

- neutrino masses governed by scalar potential term of the heavy triplet scalar and mass of the heavy scalar



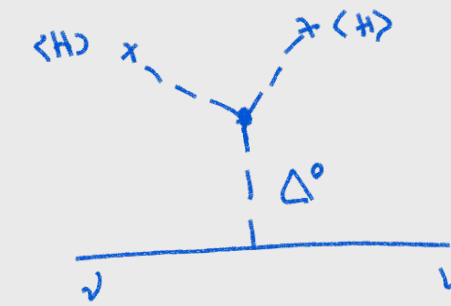
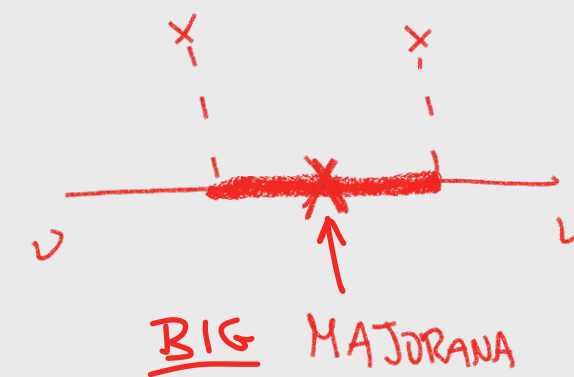
Neutrino mass mechanisms

LEPTON

NUMBER BREAKING

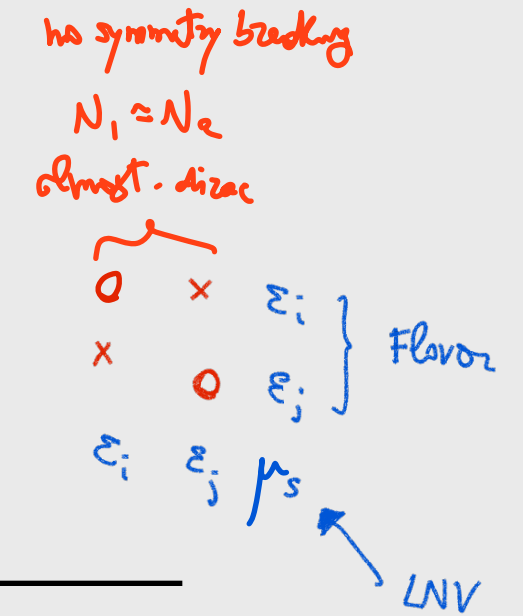
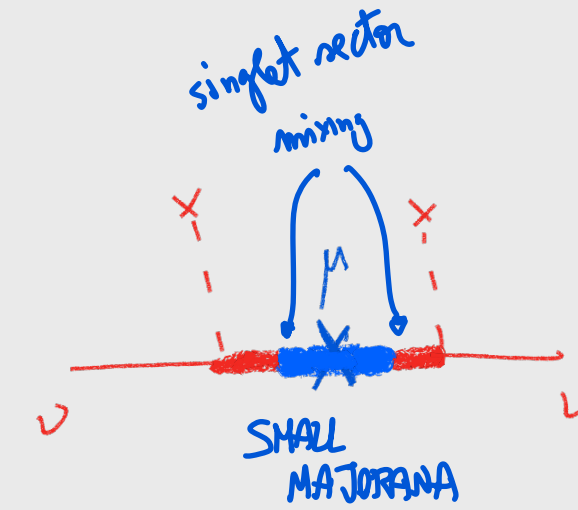
L – violation

(1,1,0) (at least 2)



(1,3,1) (1 is enough)

(1,1,0) (at least 2+1)



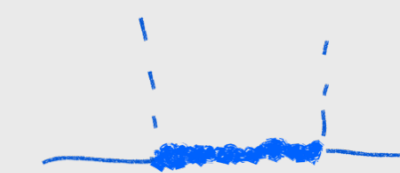
L – not accidental

new physics before 2012

$d = 5$ (1,2,1/2)

$$\frac{(LH)^2}{\Lambda}$$

UV

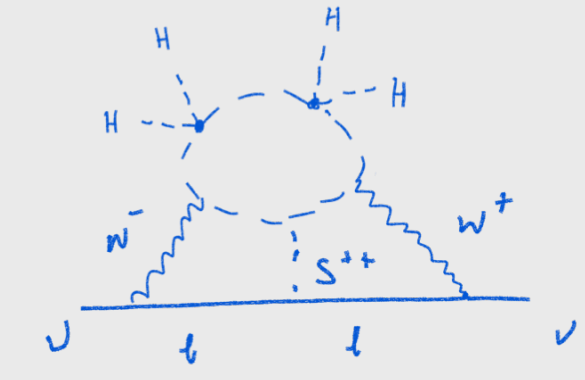
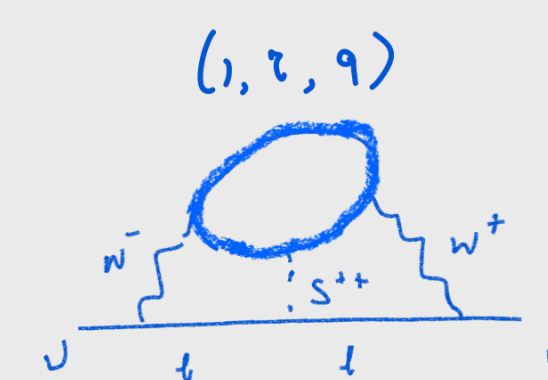


(1, 2, 9)

$d = 7$ (1,1,2)

$$\frac{(DH\sigma_2 H)^2 S^{--}}{\Lambda^3}$$

UV



L – gauged, SSB

$$SU(3) \otimes SU(2)_L \otimes SU(2)_L \otimes U(1)_{B-L}$$

(1,2,1,1), (1,1,2,1), (1,2,2,1), (1,1,1,2),

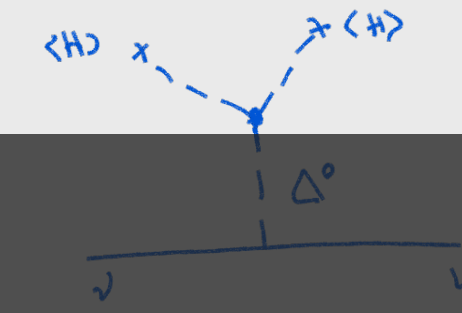
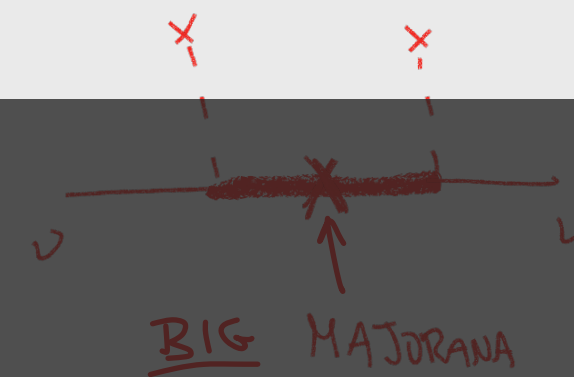
Neutrino mass mechanisms

LEPTON

NUMBER BREAKING

L – violation

$(1,1,0)$ (at least 2)



$(1,3,1)$ (1 is enough)

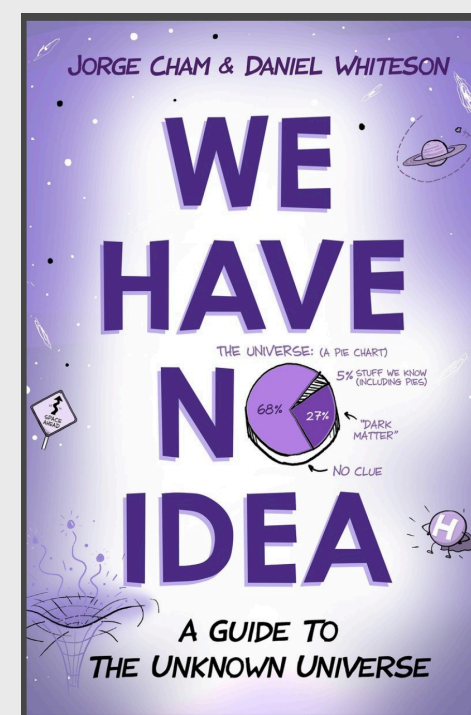
- A wide-open problem that benefits from multiple angles of attack

L – gauged, SSB

$$SU(3) \otimes SU(2)_L \otimes SU(2)_L \otimes U(1)_{B-L}$$

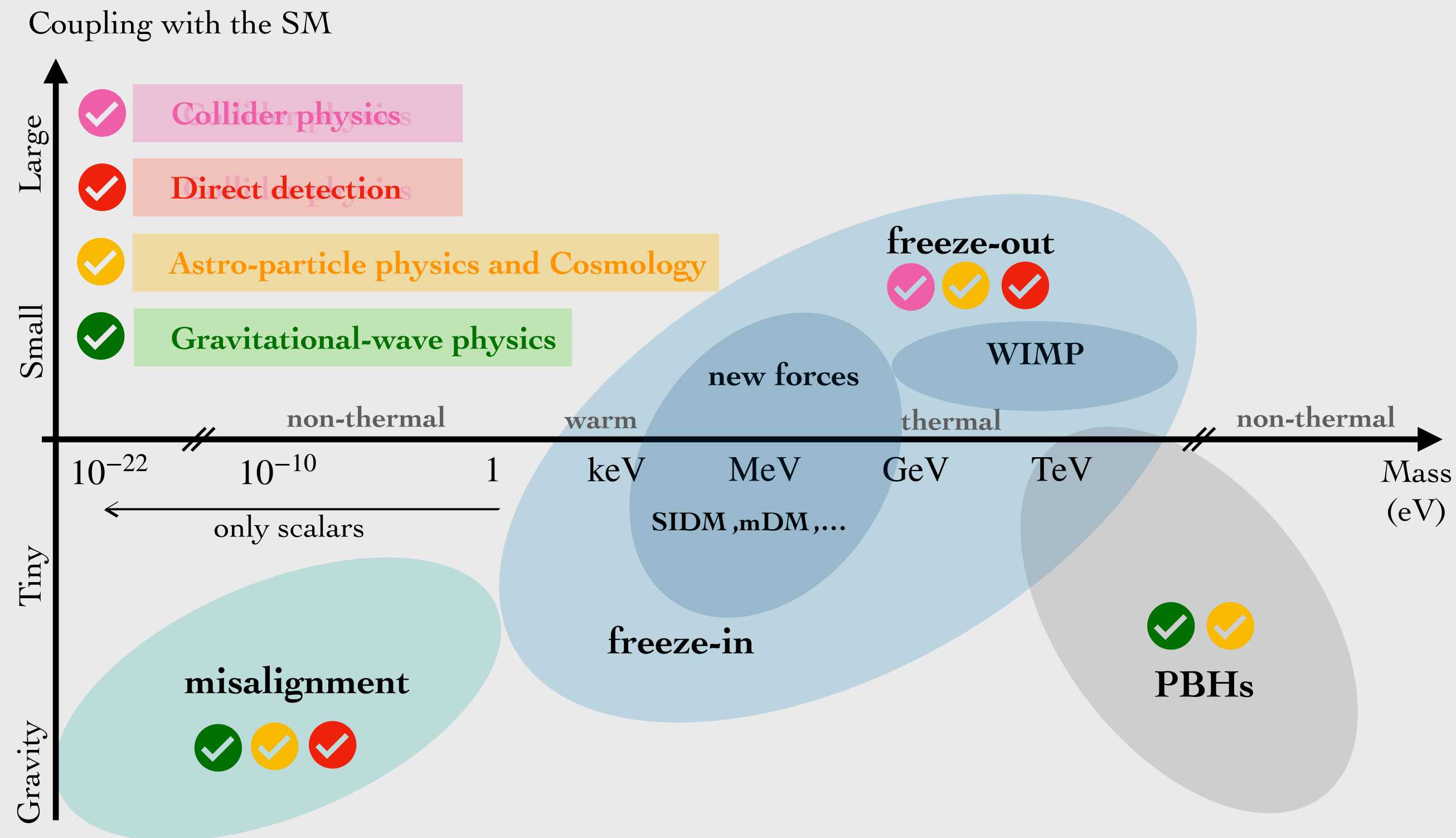
$$(1,2,1,1), (1,1,2,1), (1,2,2,1), (1,1,1,2),$$

Dark matter



The Chase Is Wide Open

- The chessboard of DM is very large!

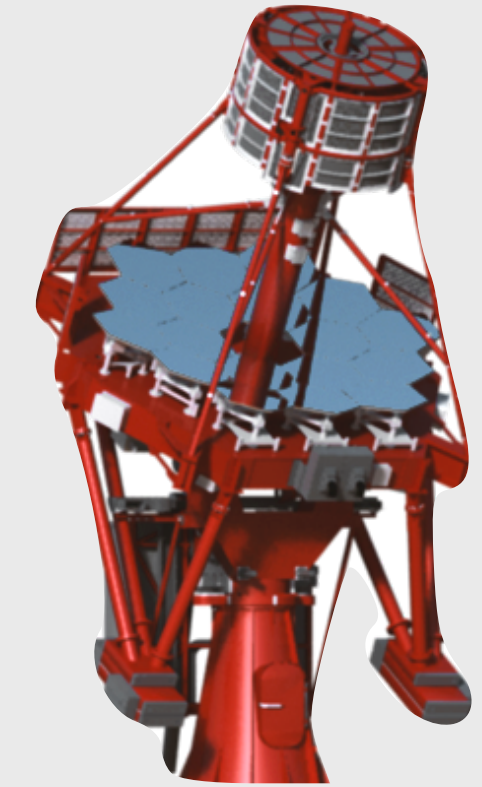
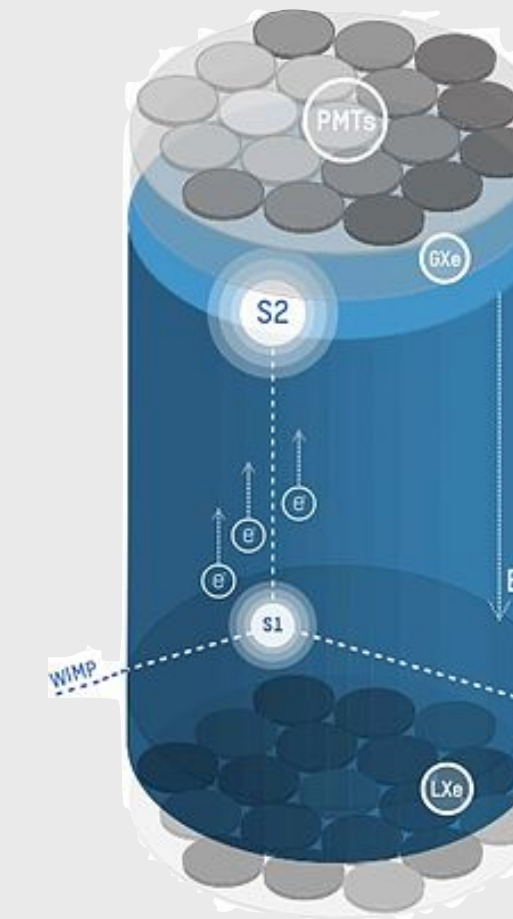


- High energy colliders are excellent and very robust probes of WIMPs!

Diverse Tools

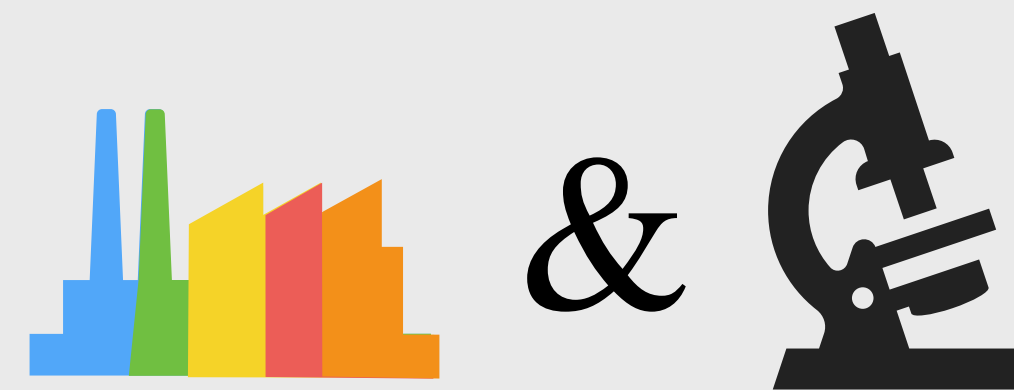
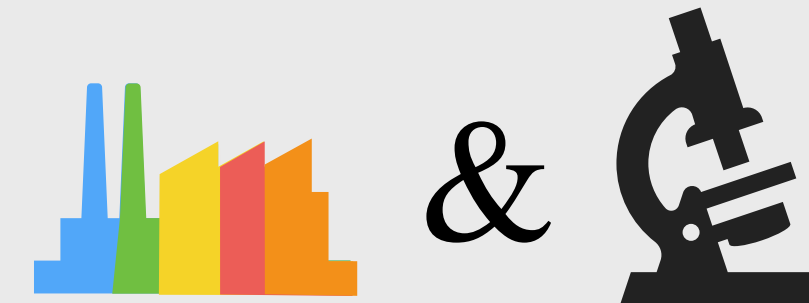
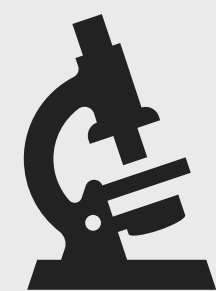
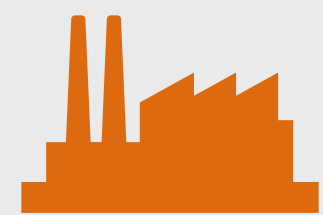
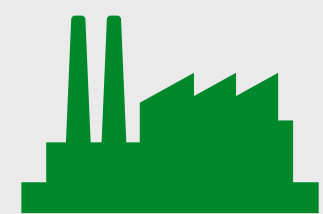
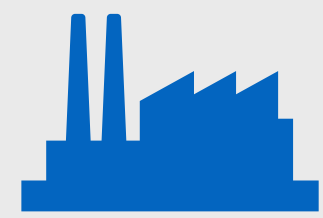


until late 2040s



FCC-*ee* + *hh*

High energy muon collider



time ↓ E_{cm}

*drawings of the left side and right side not to a common scale

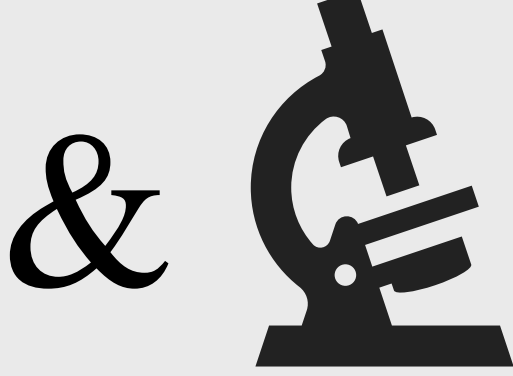
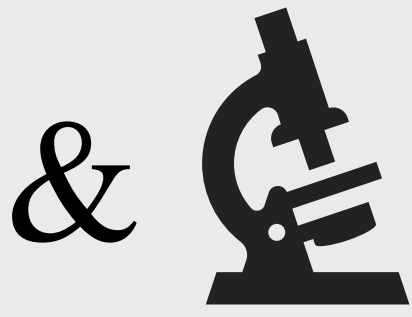
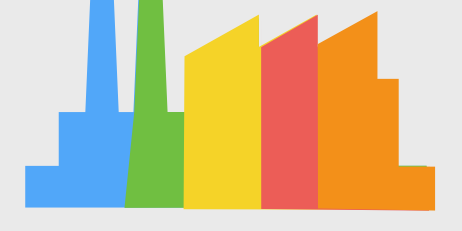
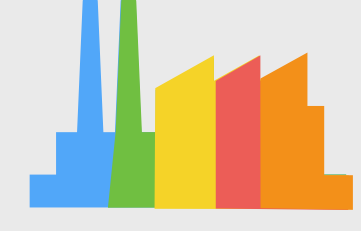
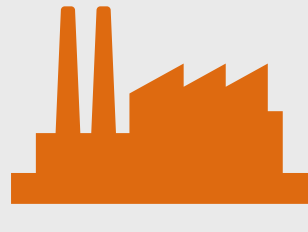
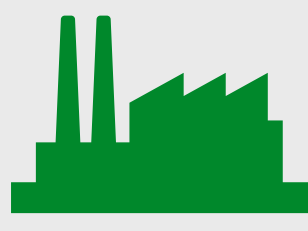
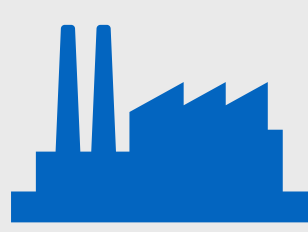
Diverse Tools



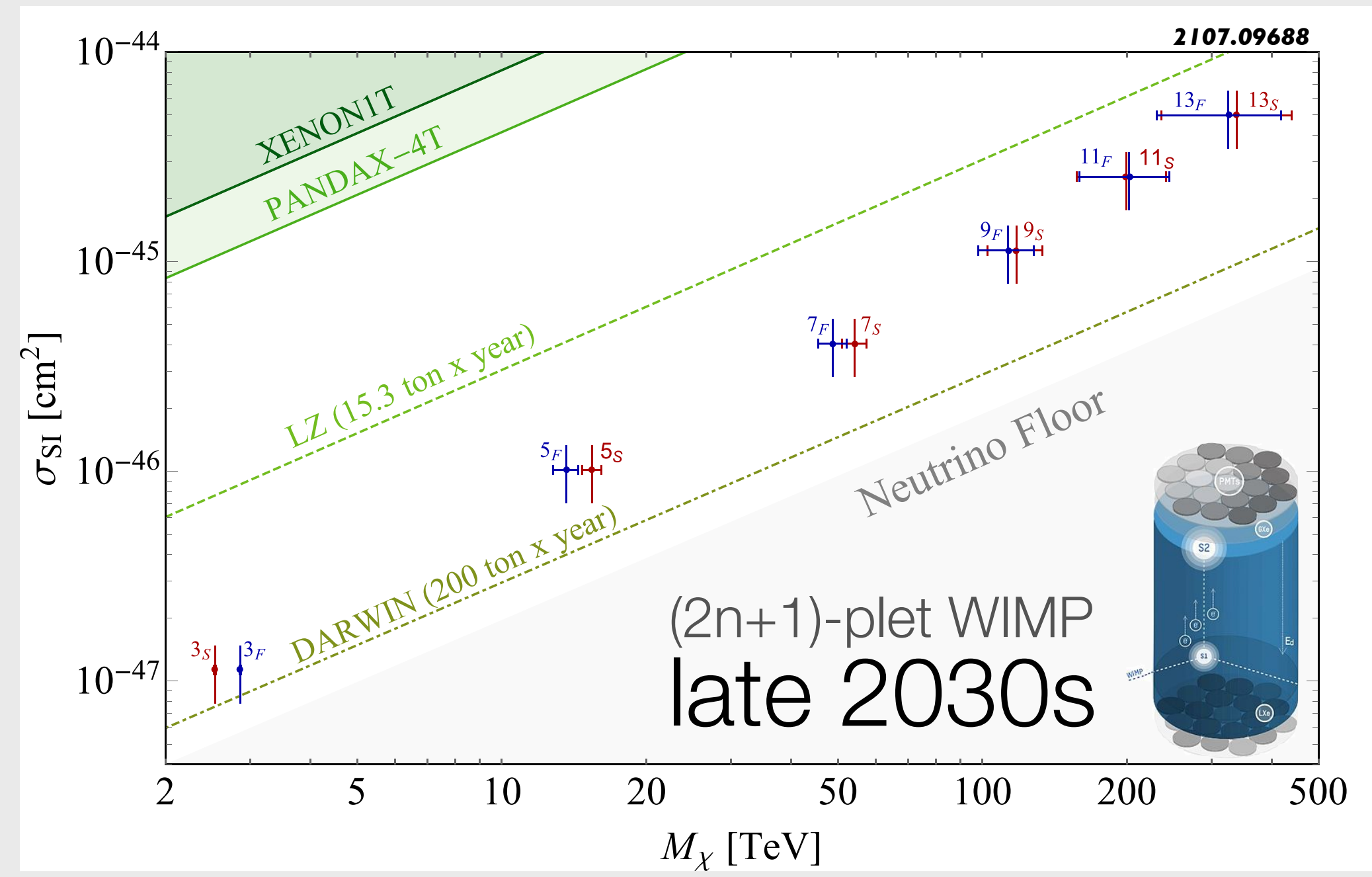
until late 2040s

FCC-*ee* + *hh*

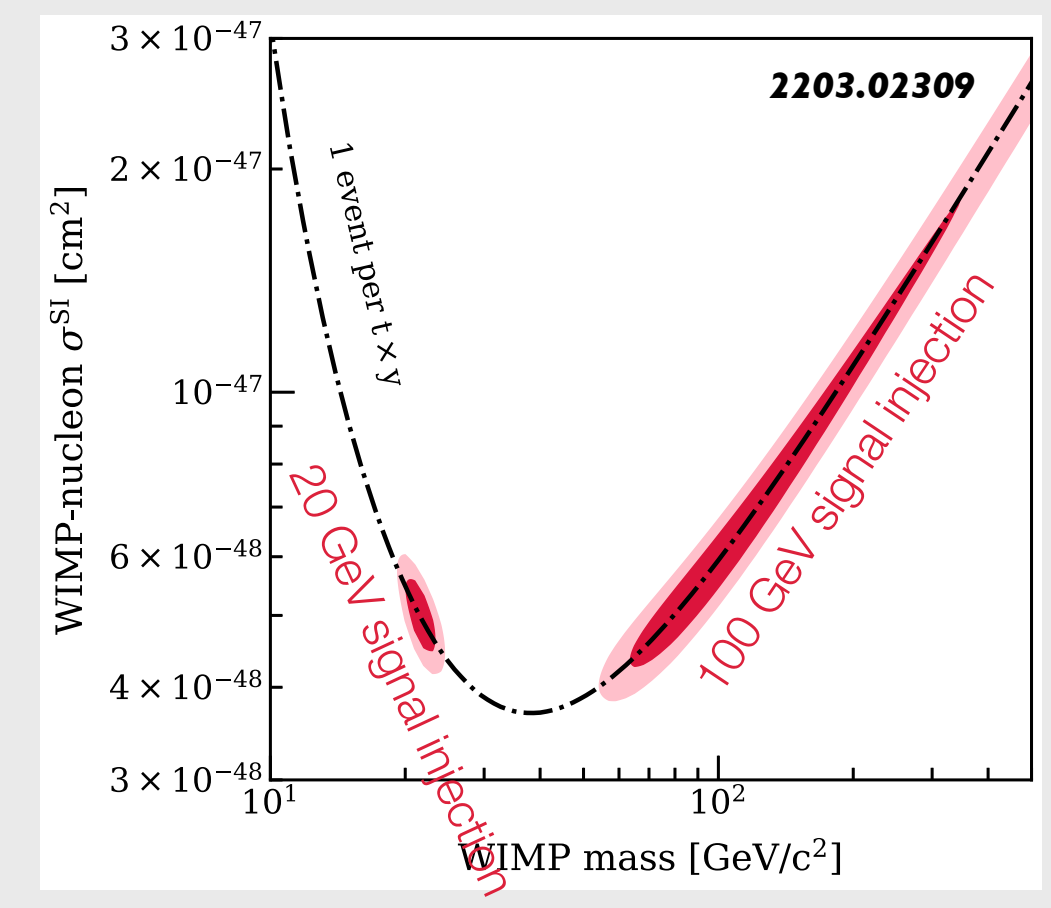
High energy muon collider



drawings of the left side and right side not to a common scale



Sc1: no hints of WIMPs at Xenon, might be Higgsino
 Sc2: hints of WIMPs at Xenon! little hints on its mass



URGENT NEED FOR A HIGH-ENERGY MACHINE BOTH IN SC1 AND SC2

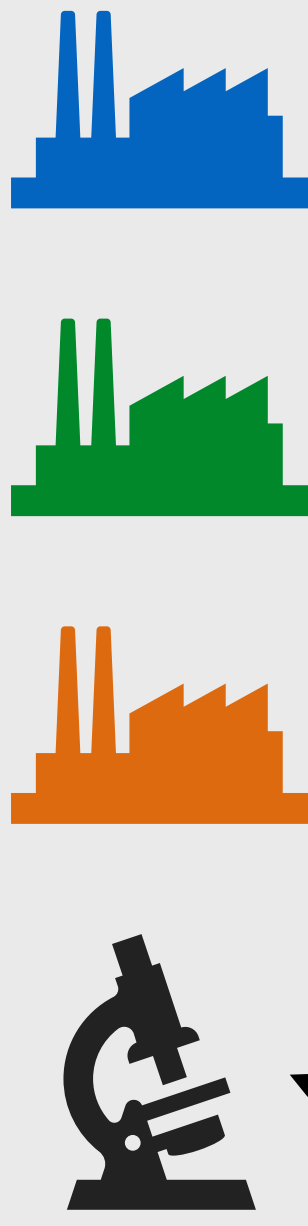
Diverse Tools



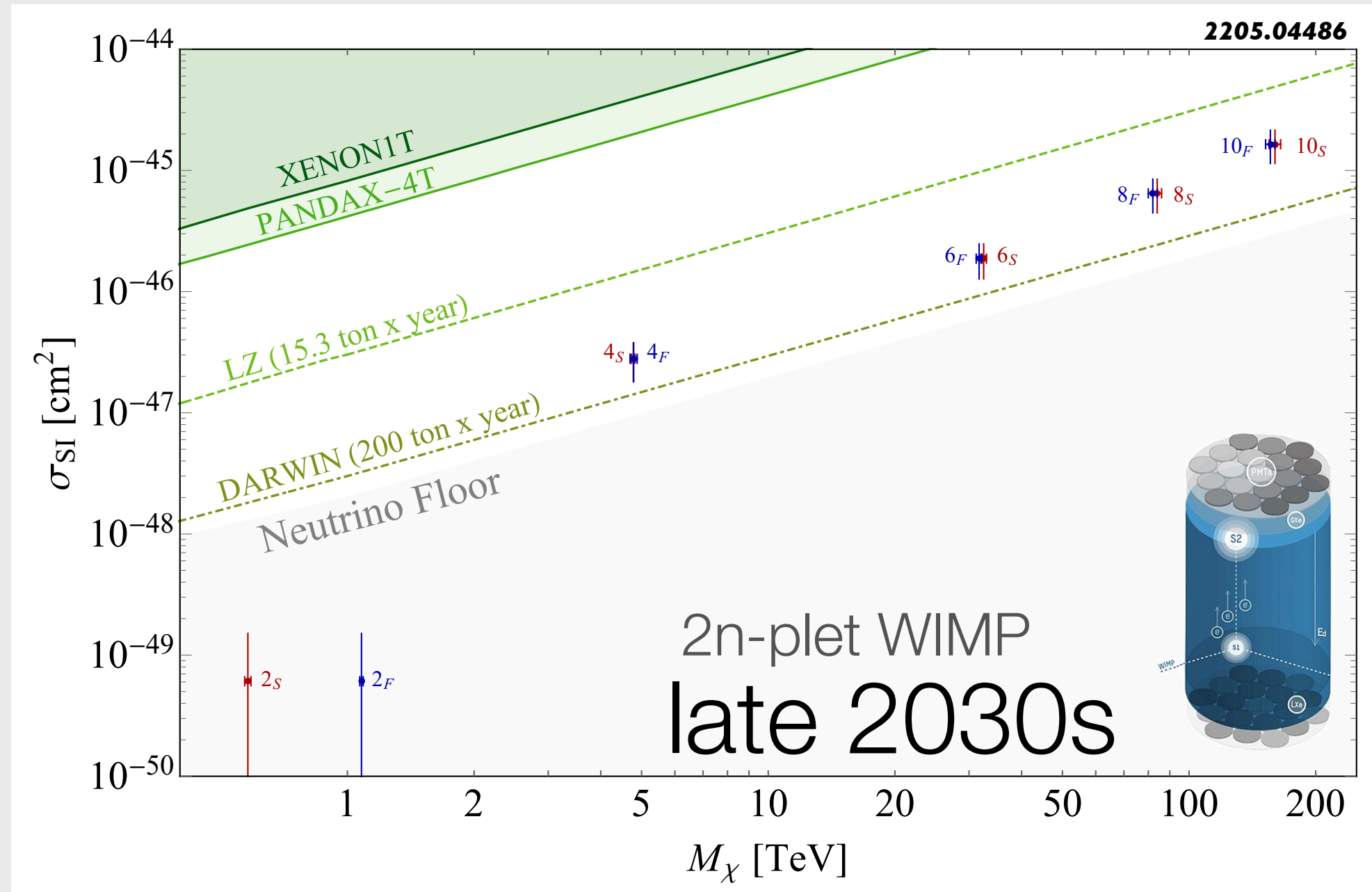
until late 2040s

FCC-*ee* + *hh*

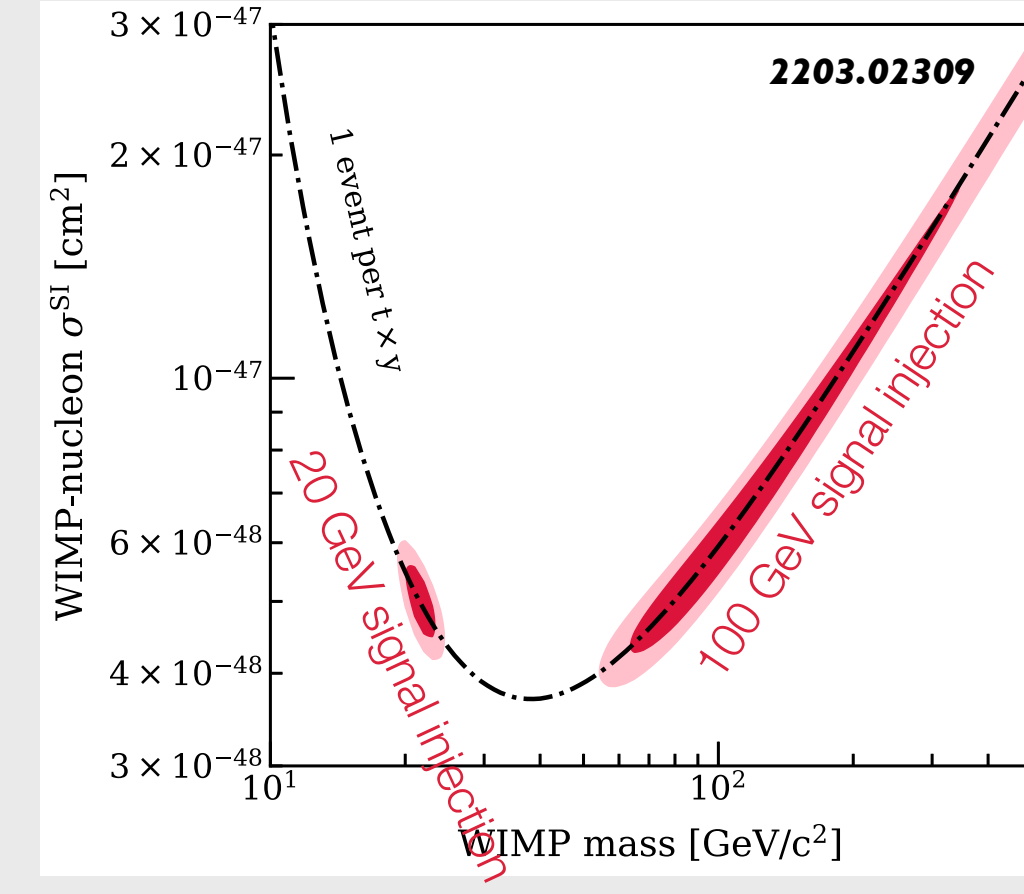
High energy muon collider



drawings of the left side and right side not to a common scale



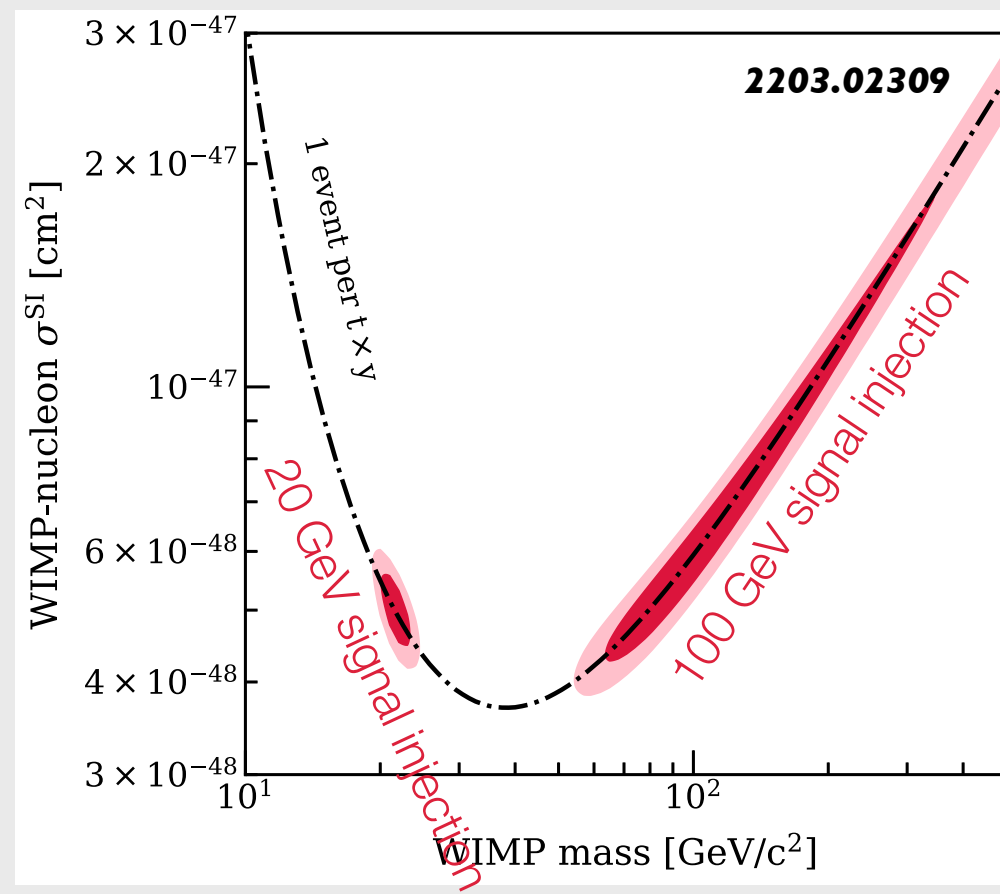
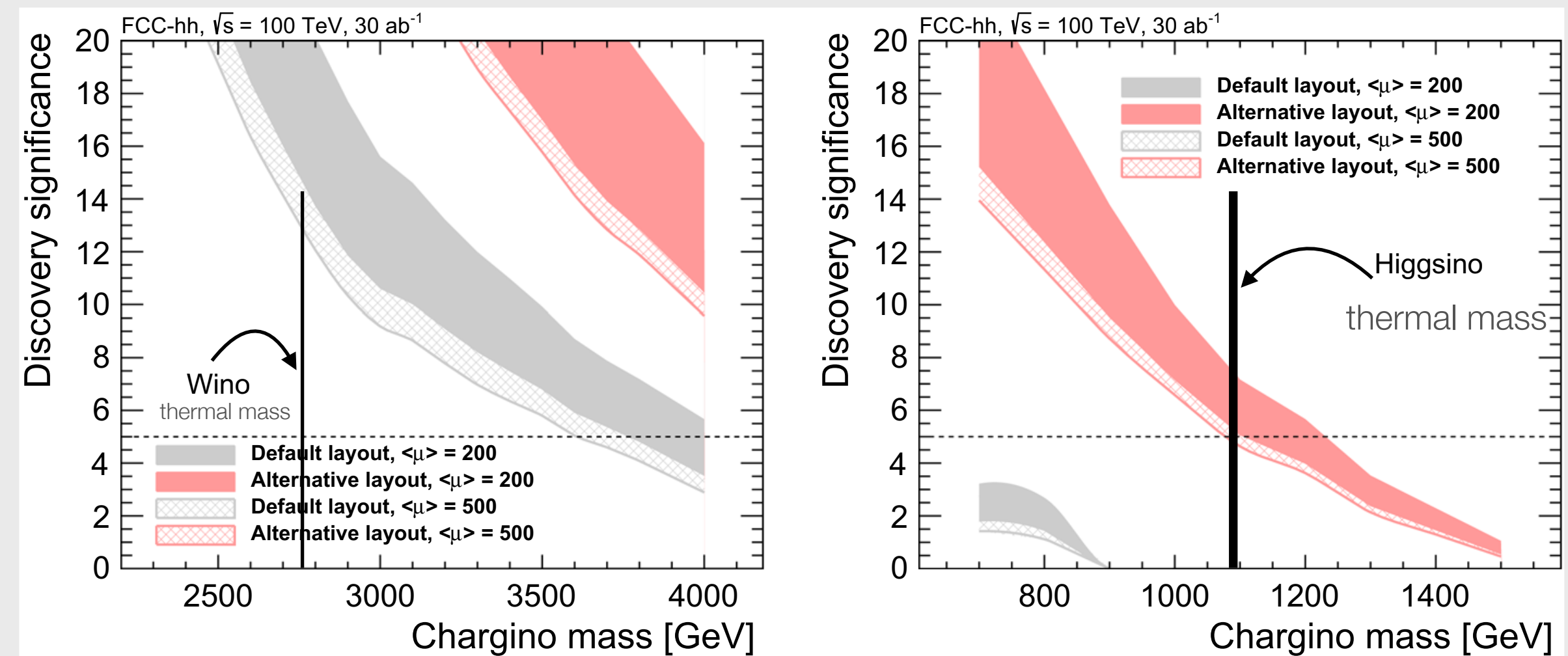
Sc1: no hints of WIMPs at Xenon, might be Higgsino
 Sc2: hints of WIMPs at Xenon! little hints on its mass



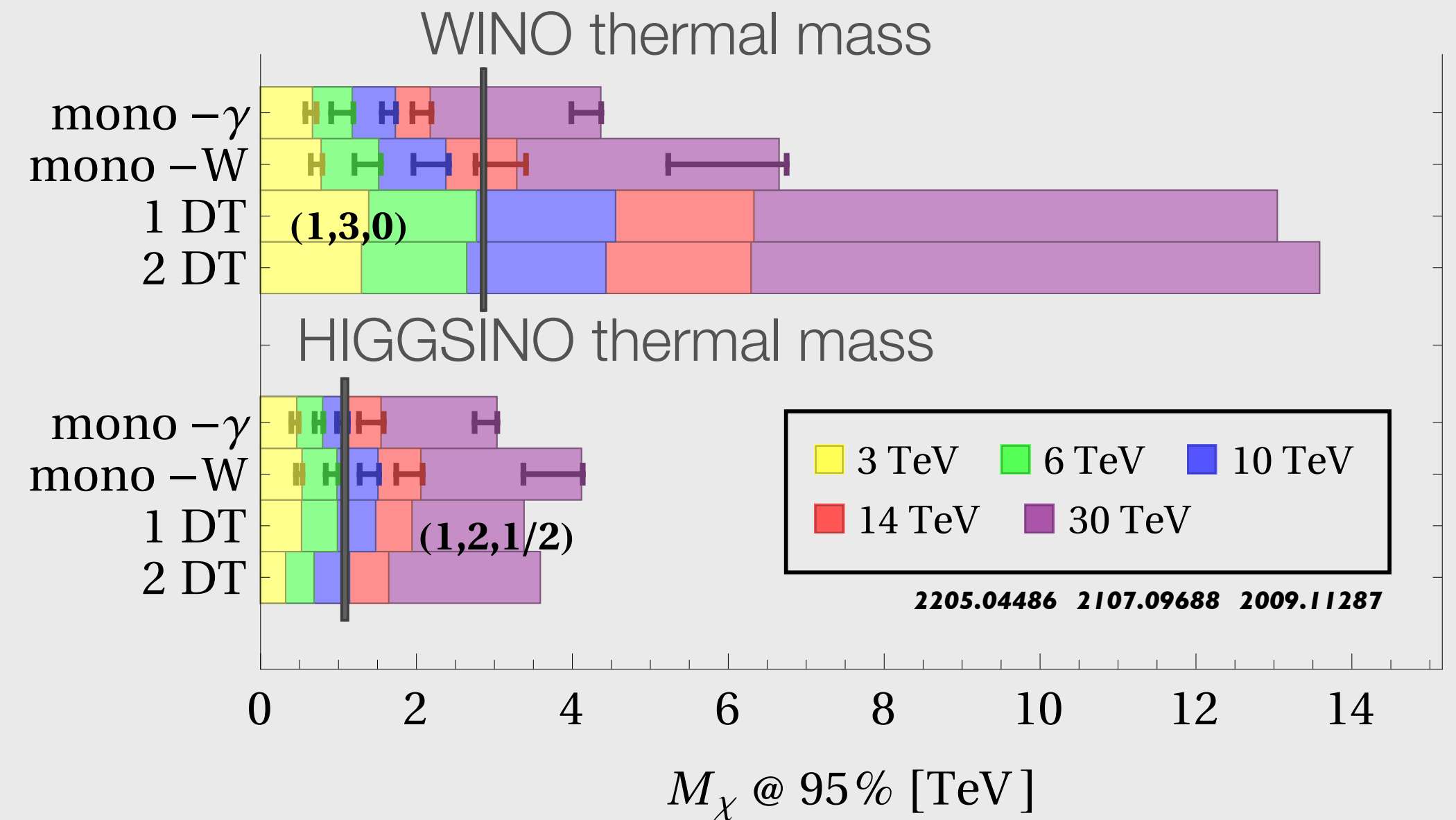
URGENT NEED FOR A HIGH-ENERGY MACHINE BOTH IN SC1 AND SC2

Diverse Tools

Sc1: no hints of WIMPs at Xenon, might be Higgsino
 Sc2: hints of WIMPs at Xenon! little hints on its mass



URGENT NEED FOR A HIGH-ENERGY MACHINE BOTH IN SC1 AND SC2

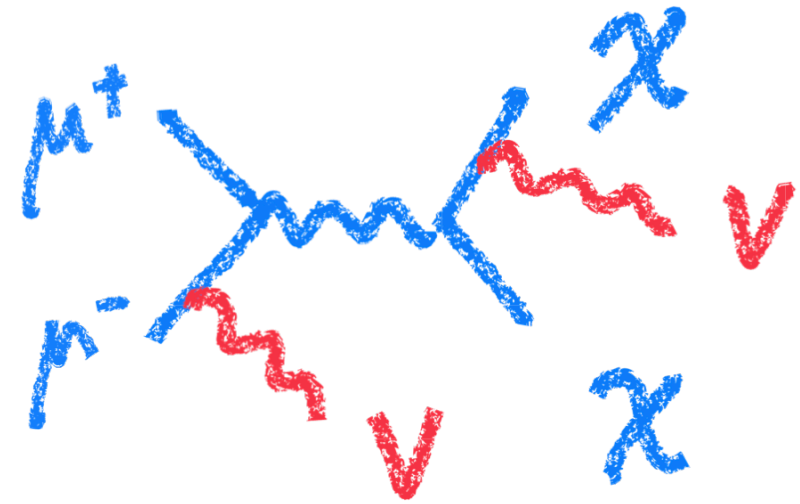


- Absence of Xe signals would require a 100 TeV pp or 6-10 TeV $\mu\mu$ to conclusively probe WIMPs by testing Higgsino
- Xe signal of heavy WIMP opens the chase from 1 TeV to fraction of PeV mass

Projects specialties

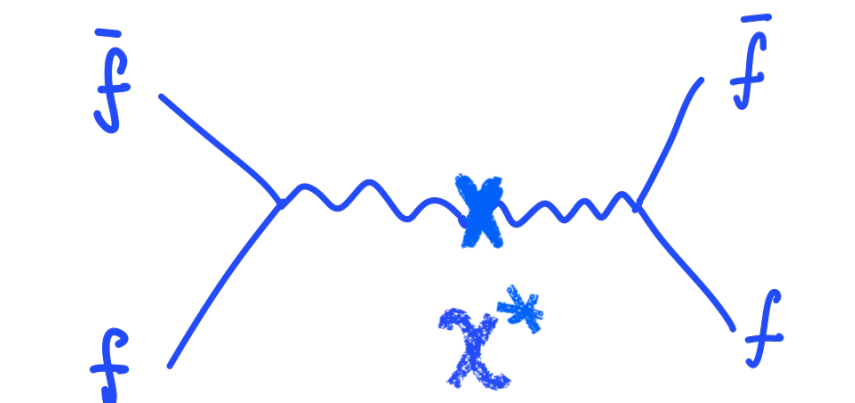
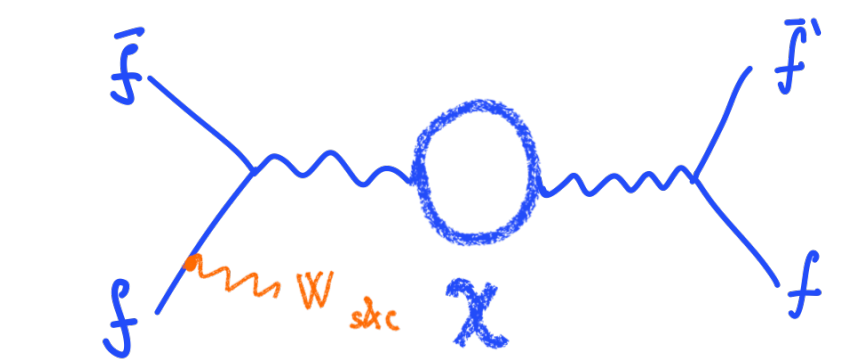
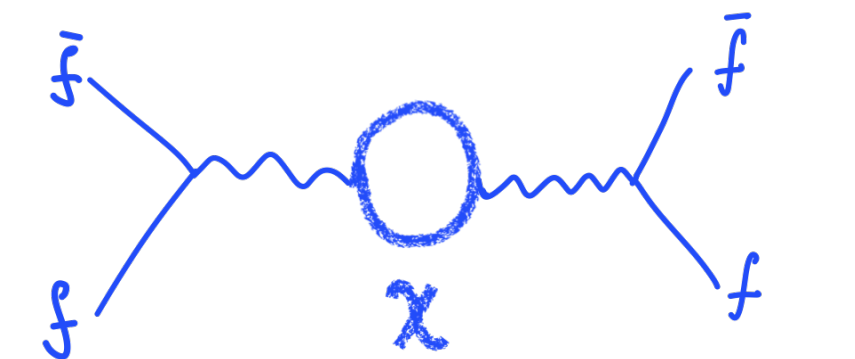
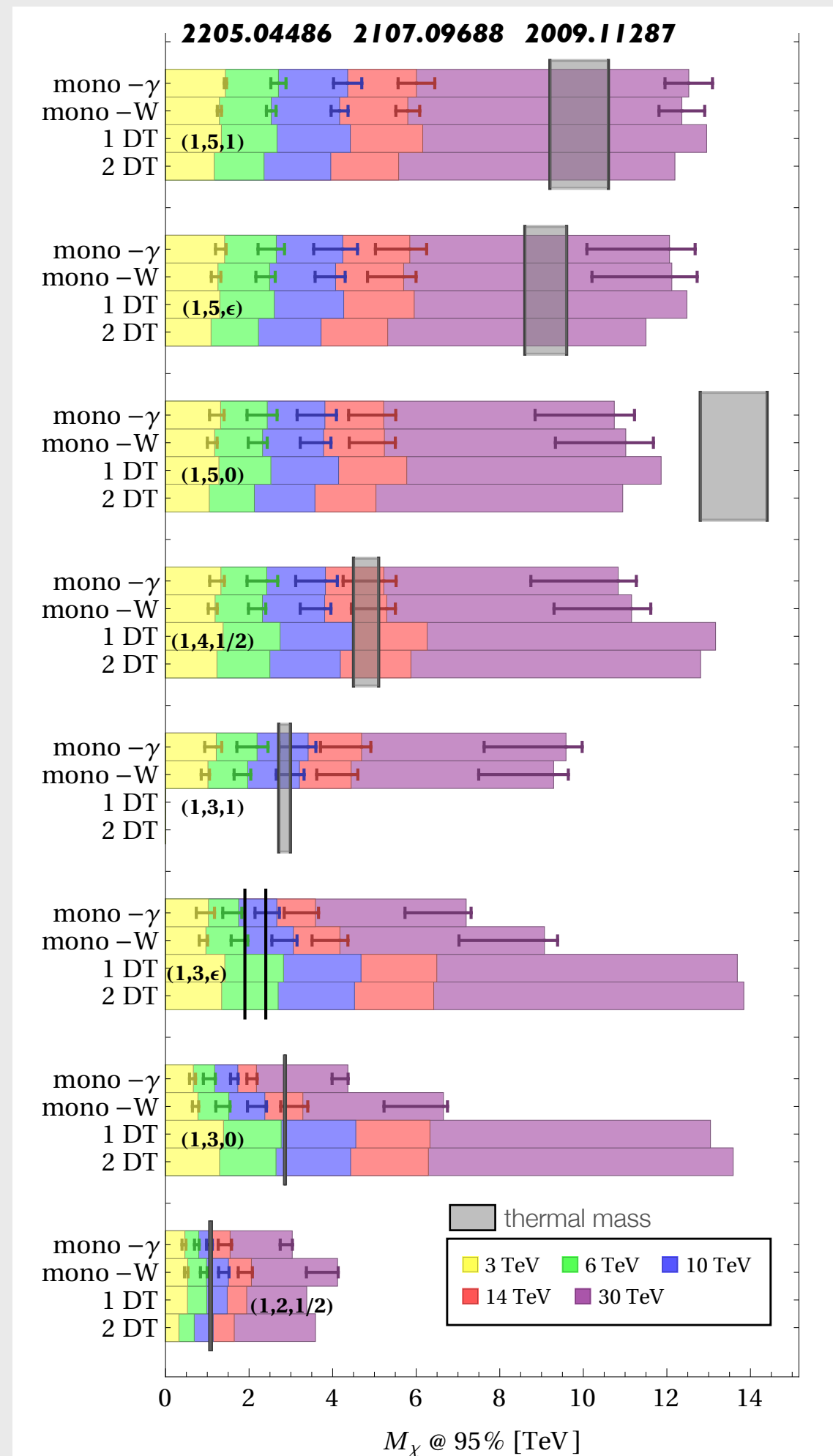
Search for EW matter at $\mu\mu$

- χ signal of heavy WIMP opens the chase from 1 TeV to fraction of PeV mass
- most solutions to open issues of the SM require new EW particles

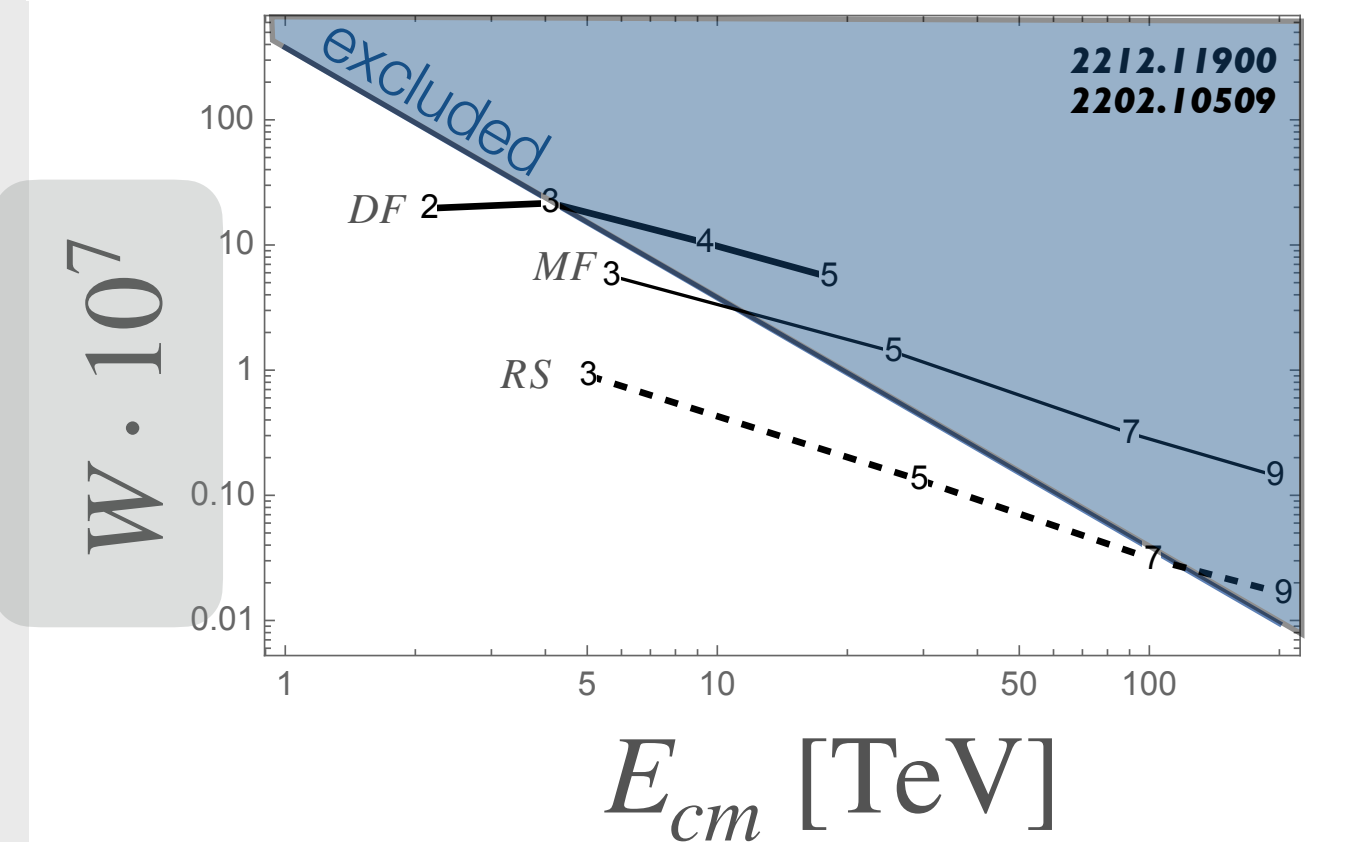
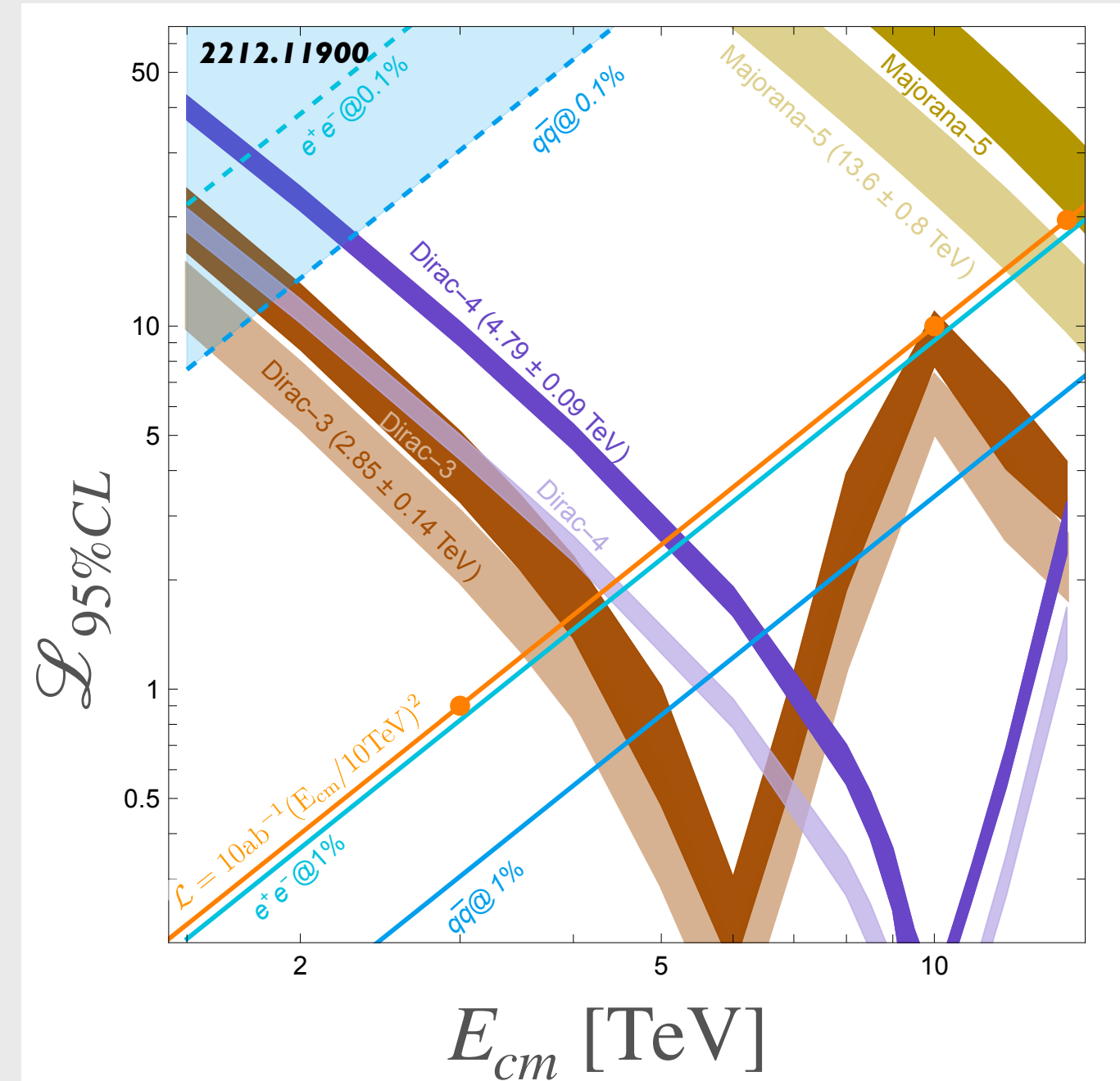


Large χ mass needs CoM energy!

Weak radiation yield the most constraining channel "mono-W"

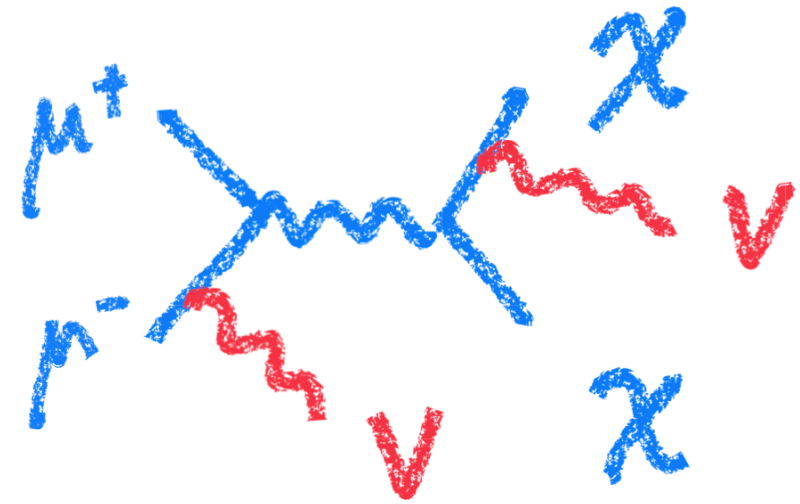


$$O_{2W} \propto (D_\mu W^{\mu\nu})^2$$



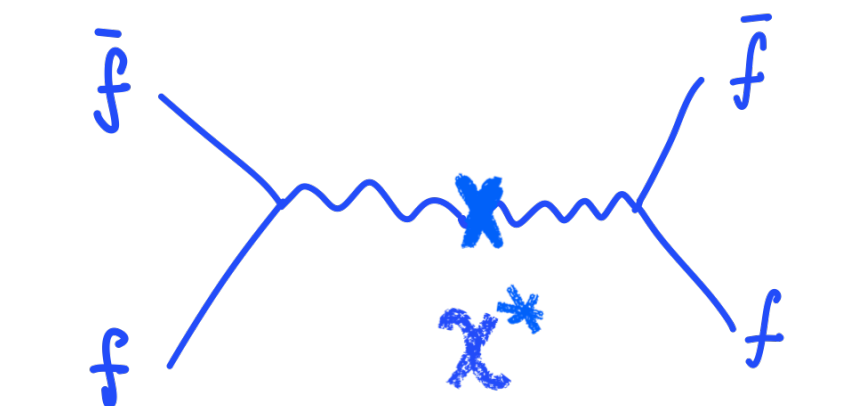
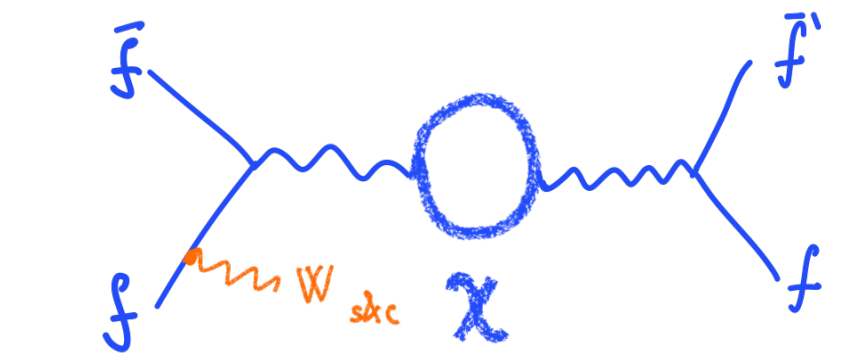
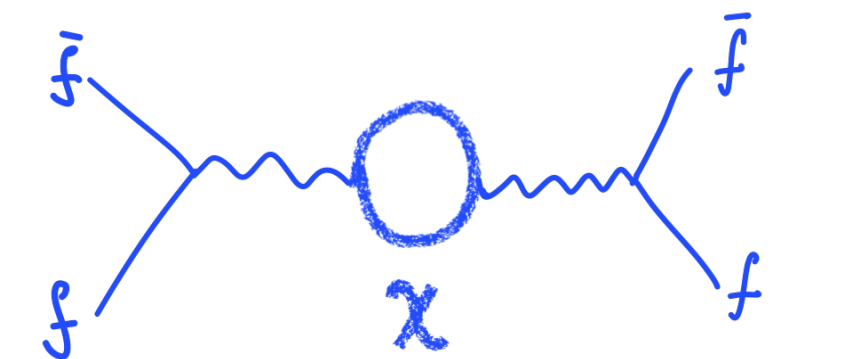
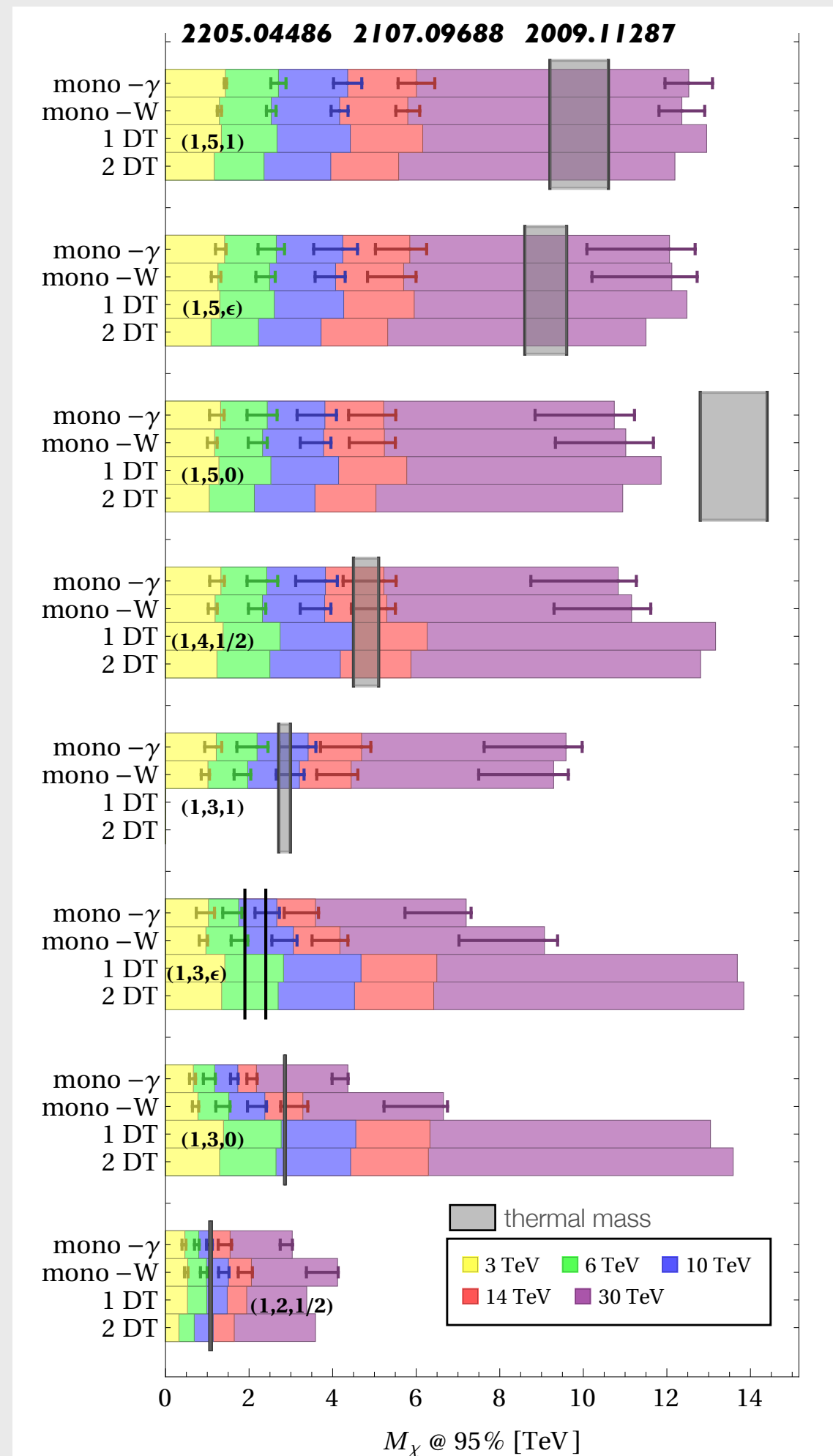
Search for EW matter at $\mu\mu$

- Xe signal of heavy WIMP opens the chase from 1 TeV to fraction of PeV mass
- most solutions to open issues of the SM require new EW particles



Large χ mass needs CoM energy!

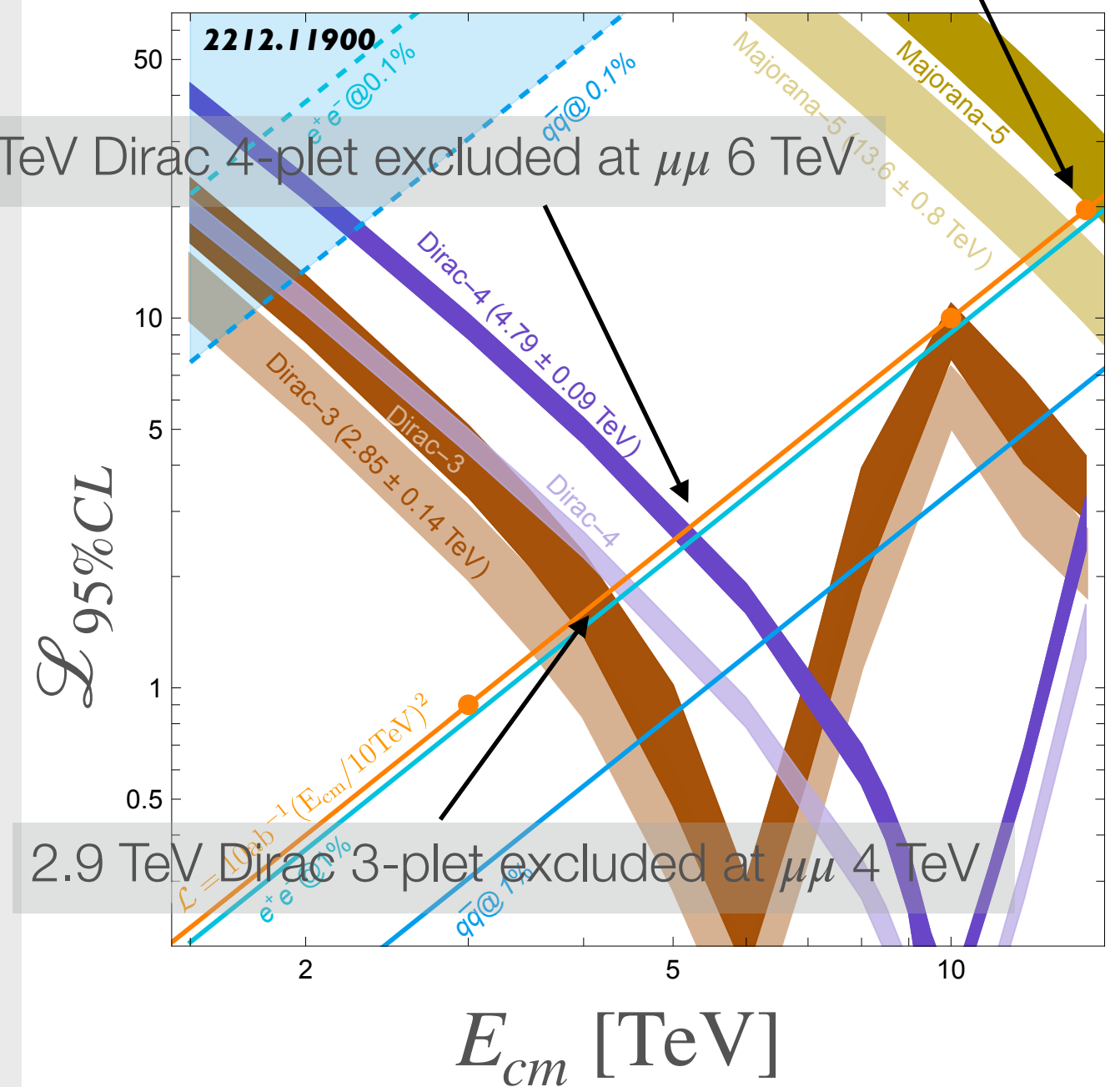
Weak radiation yield the most constraining channel "mono-W"



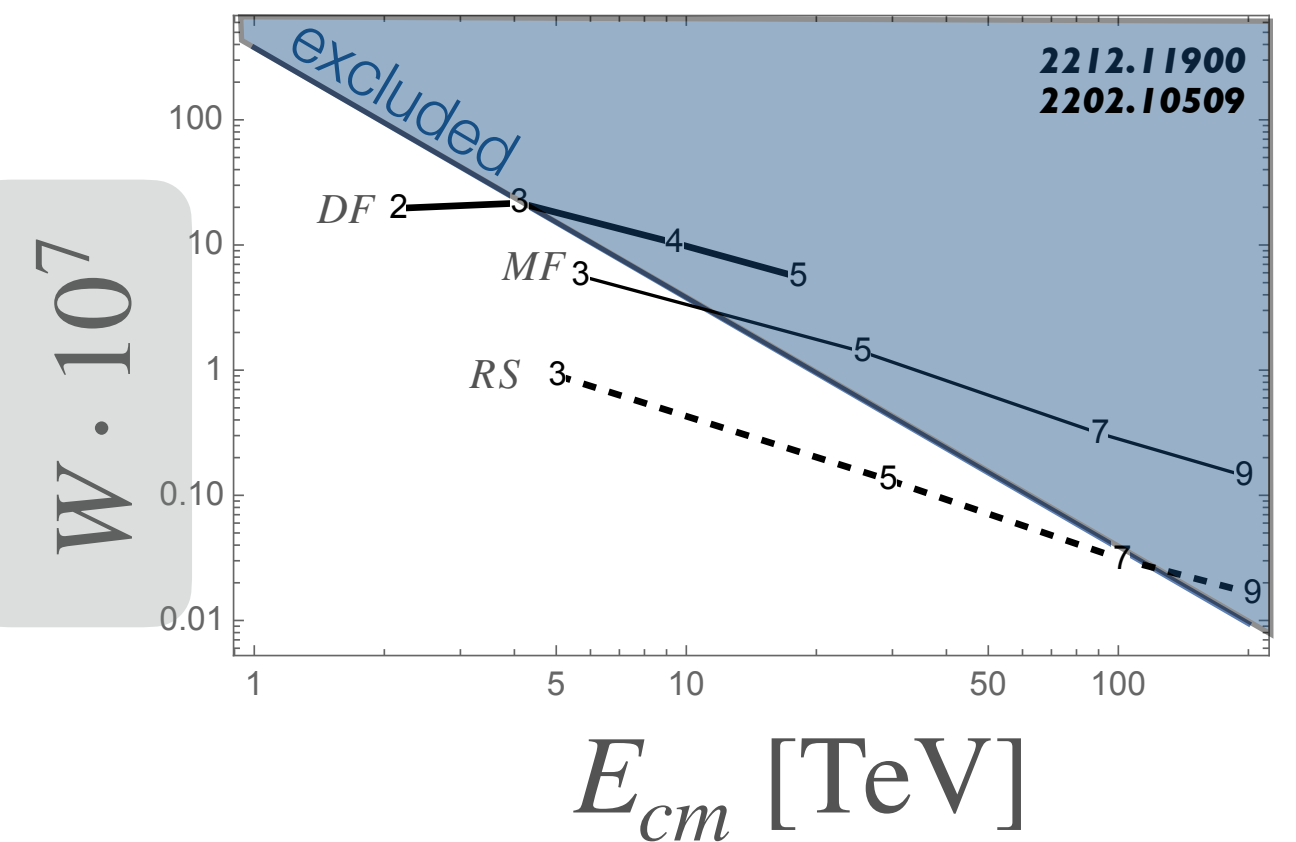
$$O_{2W} \propto (D_\mu W^{\mu\nu})^2$$

14 TeV Majorana 5-plet excluded at $\mu\mu$ 14 TeV

4.8 TeV Dirac 4-plet excluded at $\mu\mu$ 6 TeV



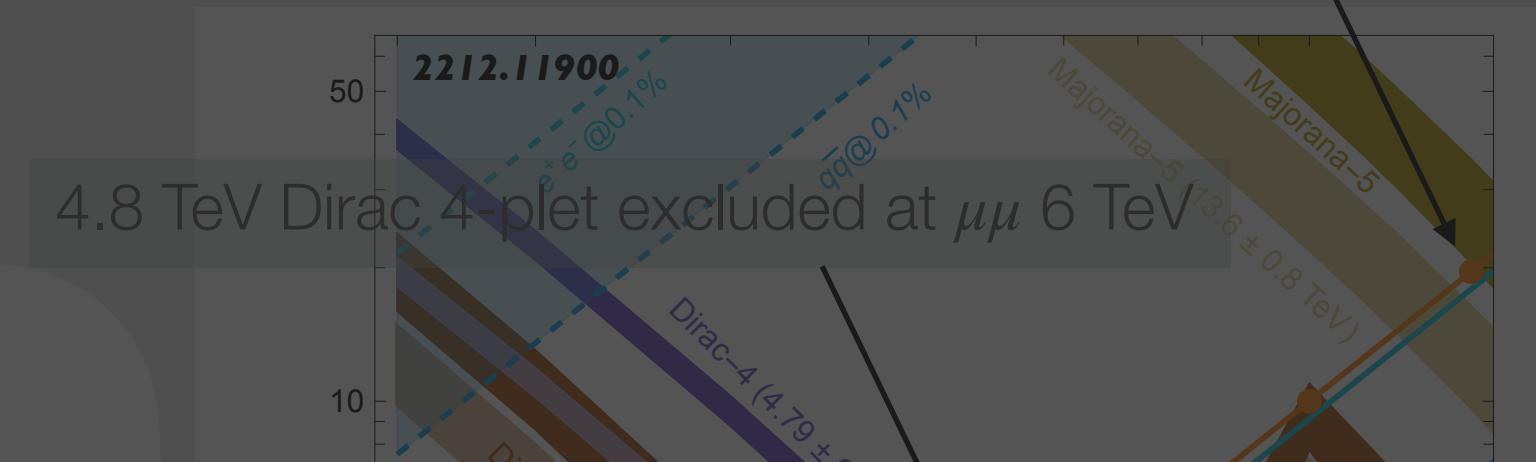
2.9 TeV Dirac 3-plet excluded at $\mu\mu$ 4 TeV



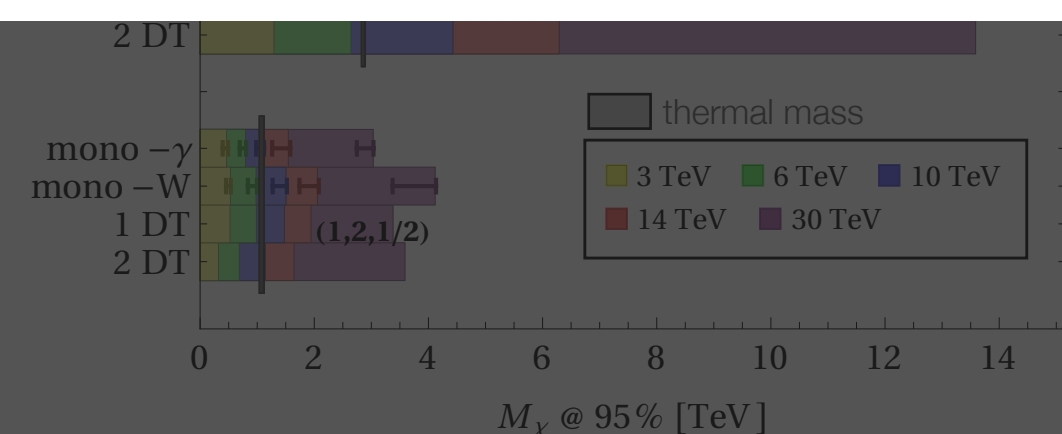
Search for EW matter at $\mu\mu$

14 TeV Majorana 5-plet excluded at $\mu\mu$ 14 TeV

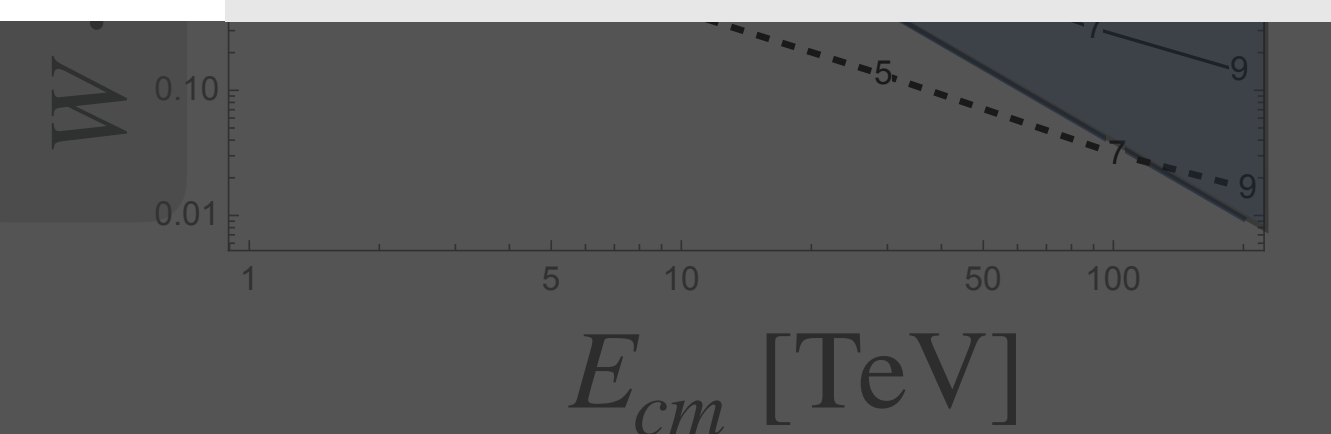
- Xe signal of heavy WIMP opens the chase from 1 TeV to fraction of PeV mass
- most solutions to open issues of the SM require new EW particles



- Potential to probe directly all WIMPs up to $\sqrt{s}/2$
- Potential to probe indirectly all WIMPs up to thermal limit $O(100)$ TeV

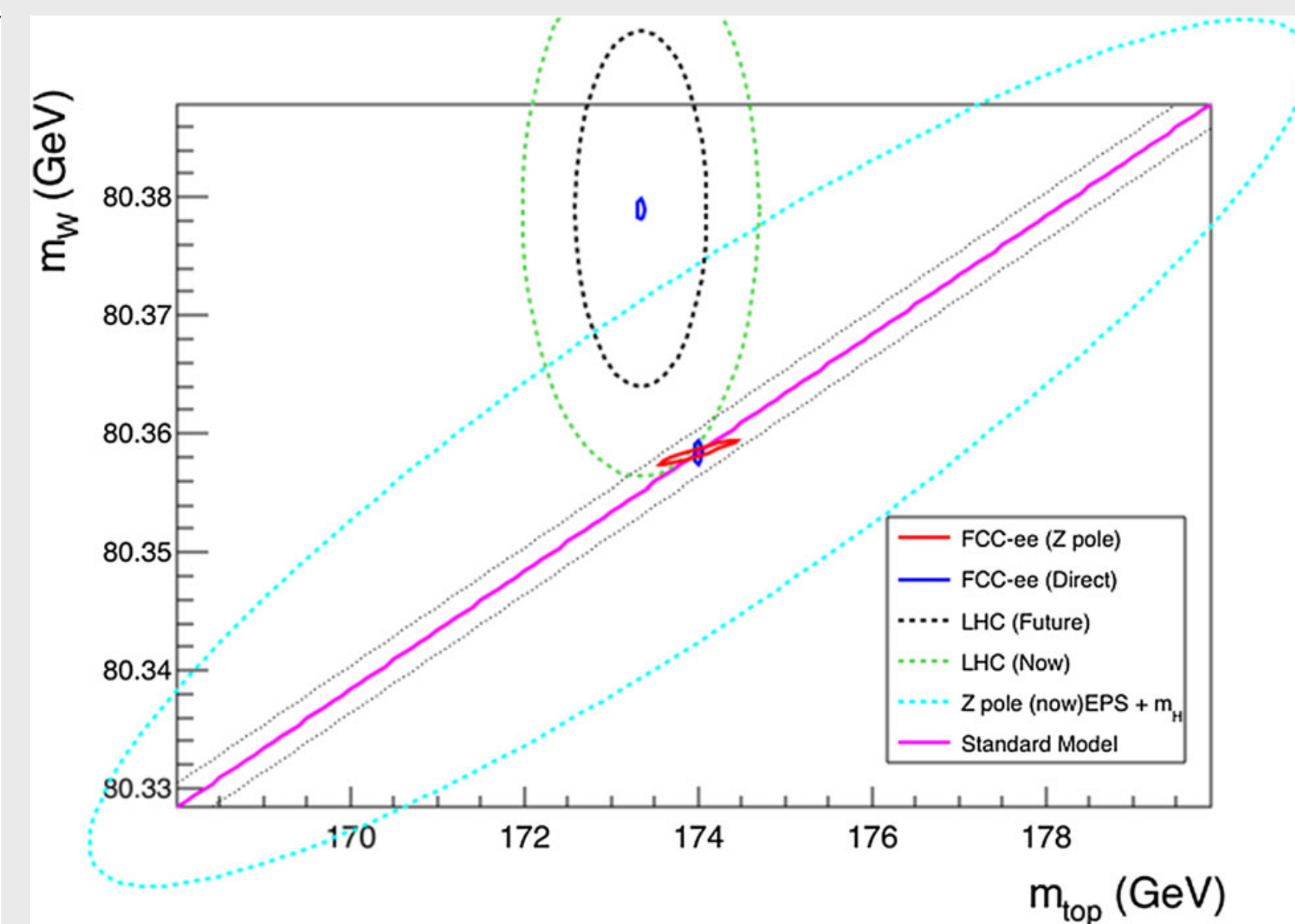
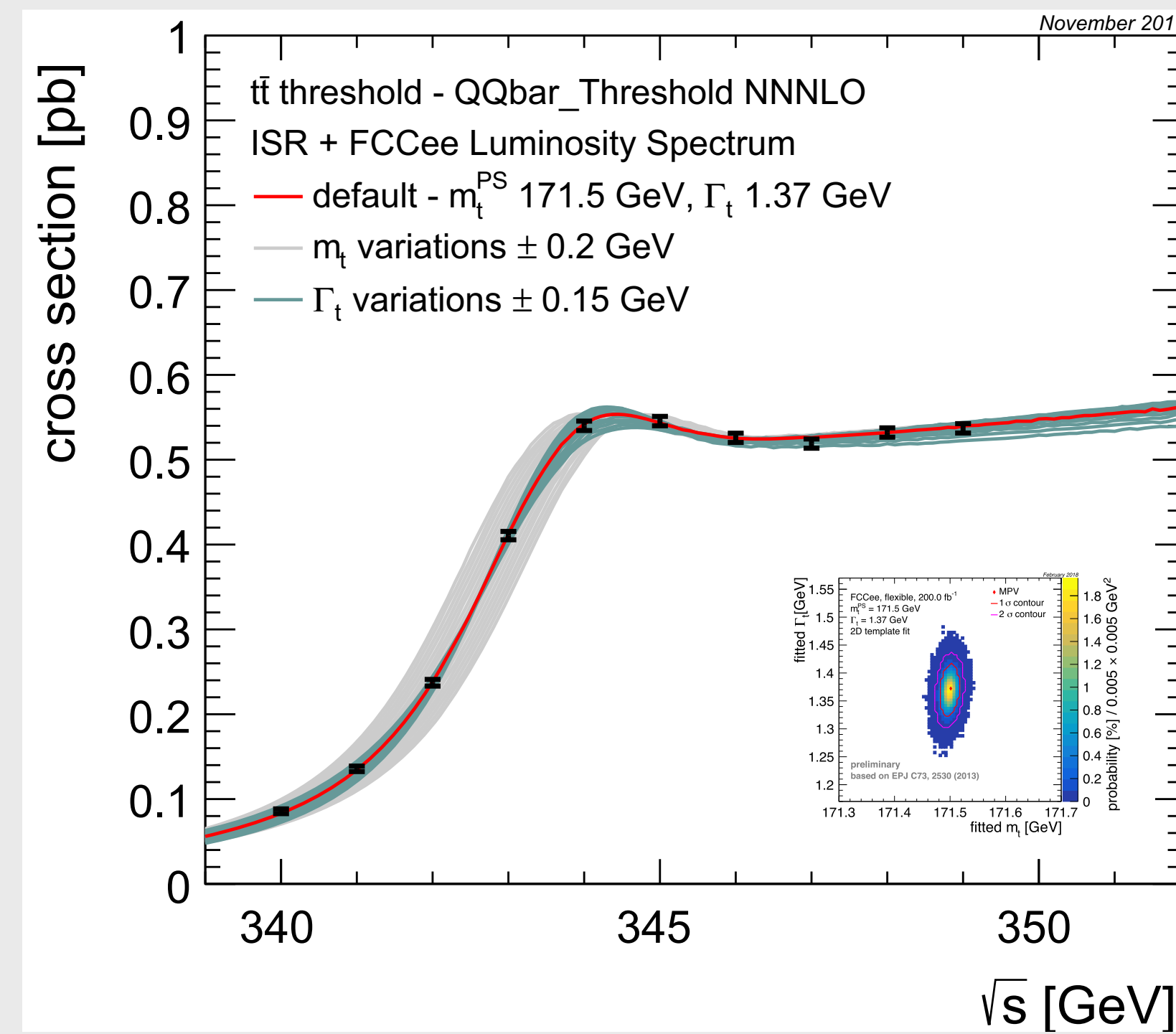
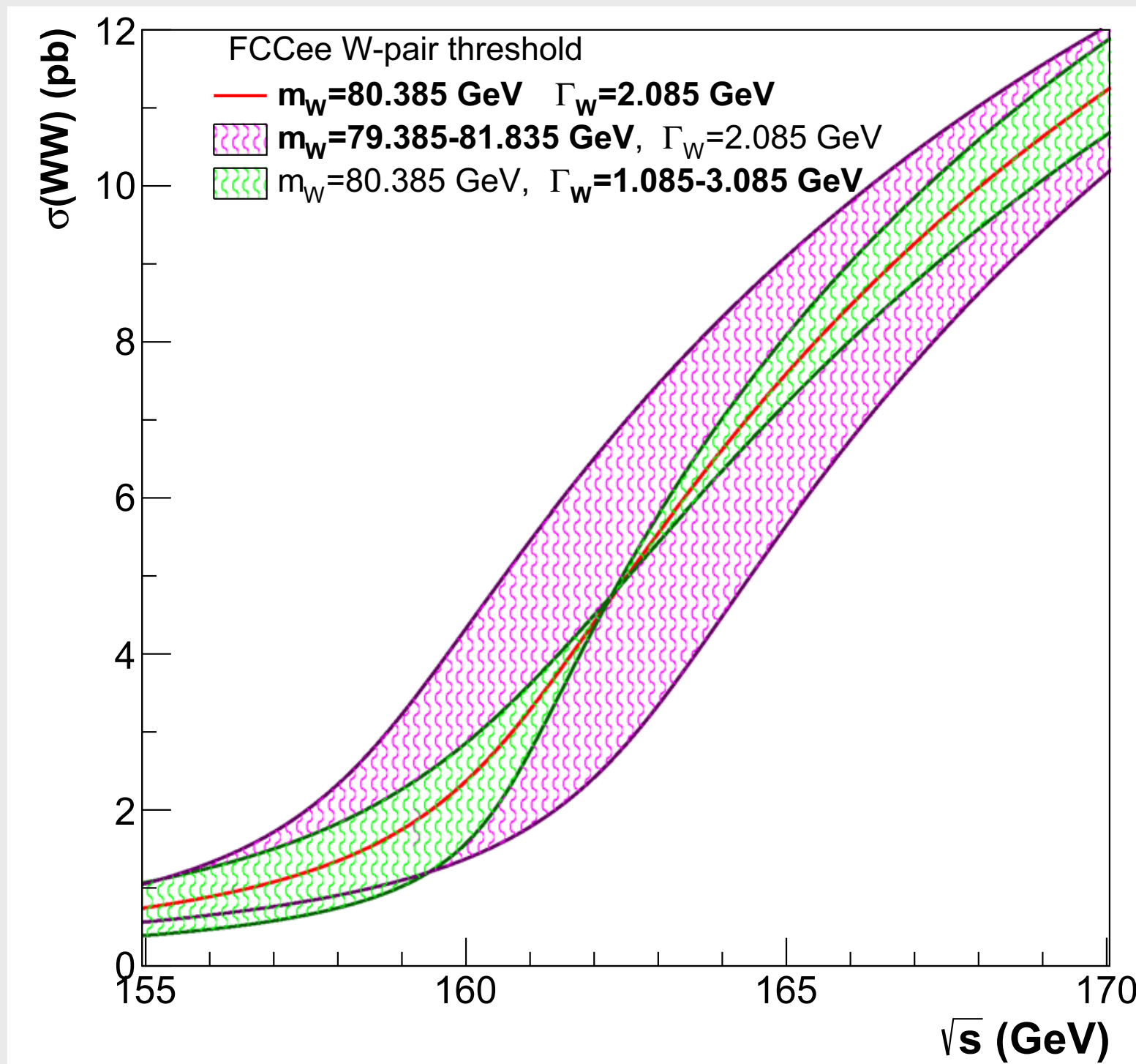


$$O_{2W} \propto (D_\mu W^{\mu\nu})^2$$



Threshold Scan Mass Measurement

- anomalies in the electroweak fit, hints of electroweak new physics at LHC



$$\delta m_W \lesssim 1 \text{ MeV}$$

$$\delta m_t \lesssim 10 \text{ MeV}$$

Theory Challenges In Both Paths!

- Z pole $N^k LO \Rightarrow$ learning how to think about scattering at such high precision
- Non perturbative power corrections to QCD jets
- fragmentation functions (e.g for $b \rightsquigarrow B$ and $c \rightsquigarrow D$) high precision measurement, needs matching theory development (parton showers, universality, ...)
- ultra-rare phenomena(l) *backgrounds to exotic NP*
- Threshold computations for W^+W^- and $t\bar{t}$ to exploit total/fiducial rate measurements and further differential measurements
- Weak corrections essential to every process from $\sqrt{\hat{s}_{ij}} \equiv \sqrt{s_{\mu\mu}} \gtrsim 10$ TeV
- Non-abelian charge exclusive scattering initial state $|i\rangle = |\uparrow\uparrow\rangle_{SU(2)_W}$ in nearly unbroken phase
- Weak partons and μ $PDFs$
- *Electroweak jets* at $\sqrt{s_{\mu\mu}} \geq$ few TeV

Theory $\mu^+ \mu^- \rightarrow SM SM \nu \bar{\nu}$

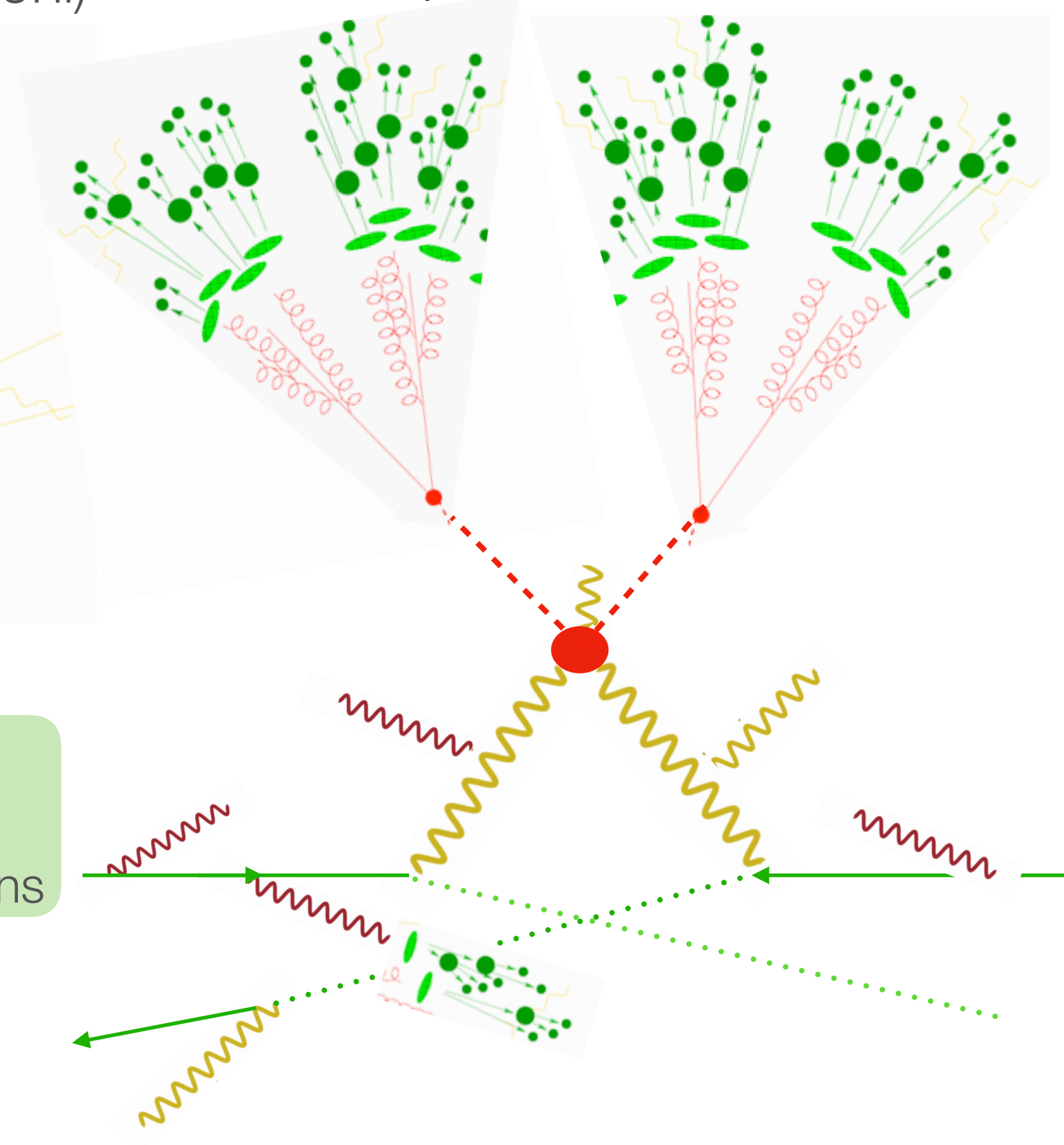
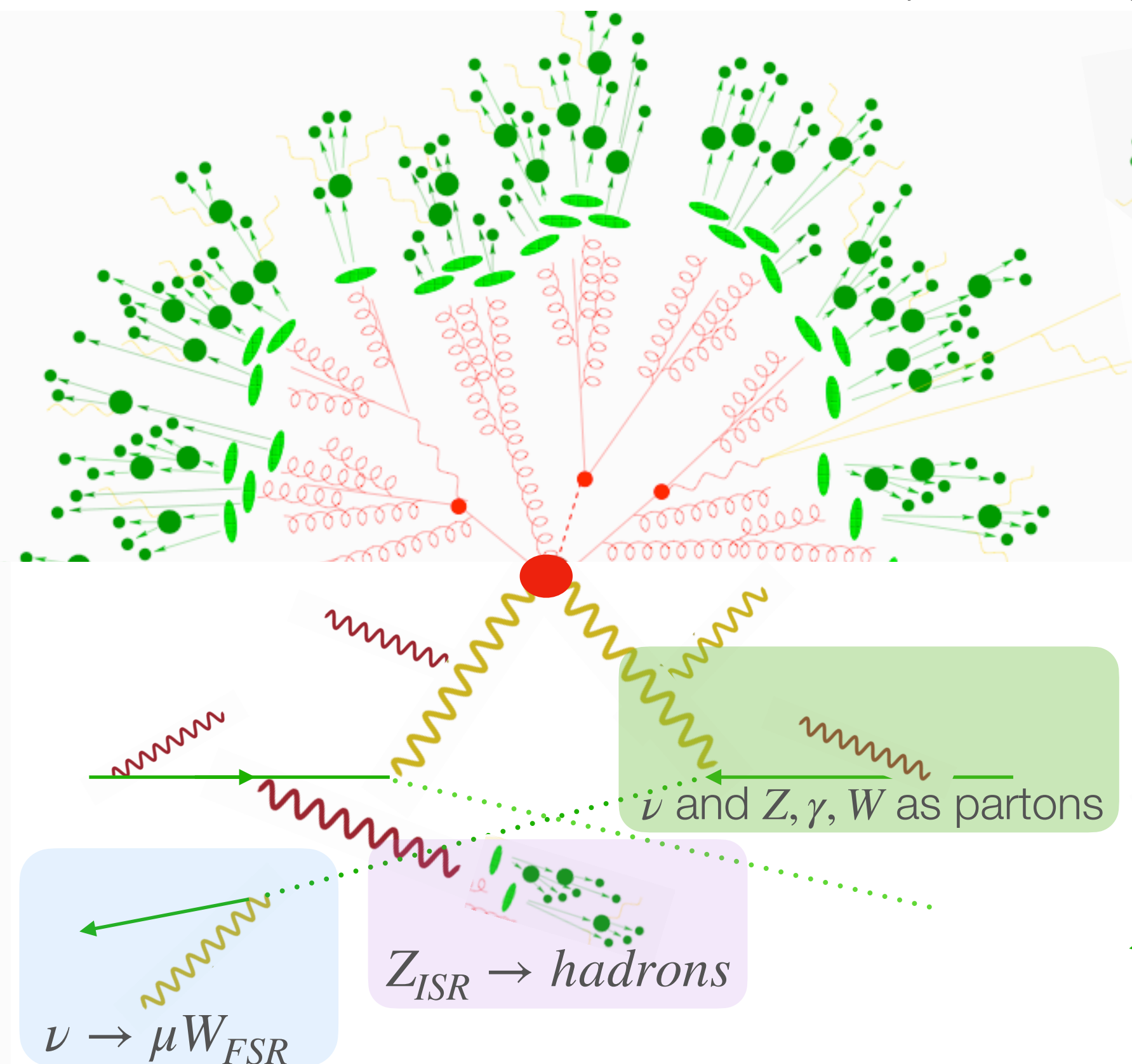
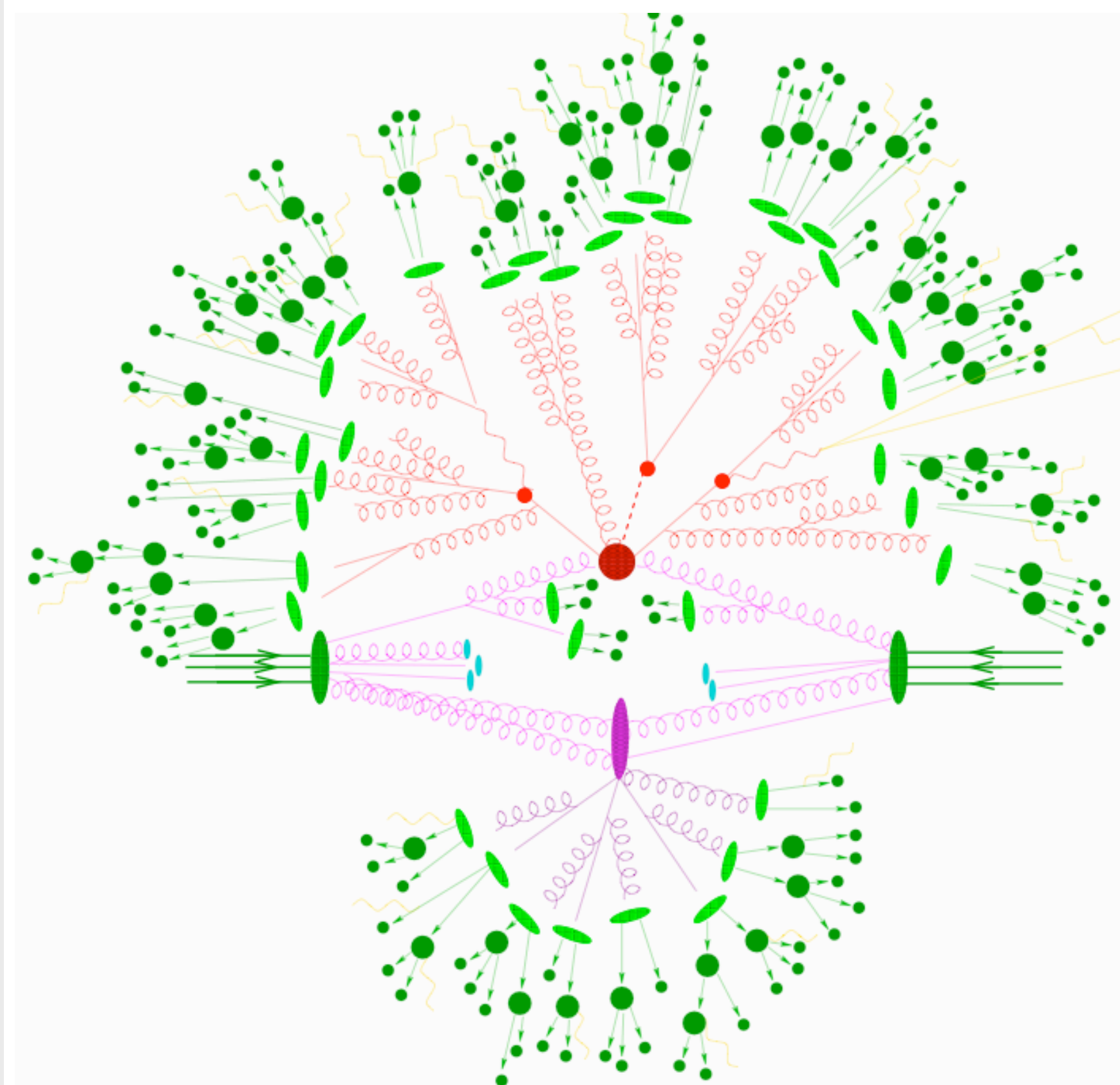
STANDARD MODEL

“FACTORY”

tth production at the LHC (Fully hadronic)

tth production at the muC 100 TeV (F. Maltoni)

HH \rightarrow 4b production at a multi-TeV muC



Theory $\mu^+ \mu^- \rightarrow SM SM \nu \bar{\nu}$

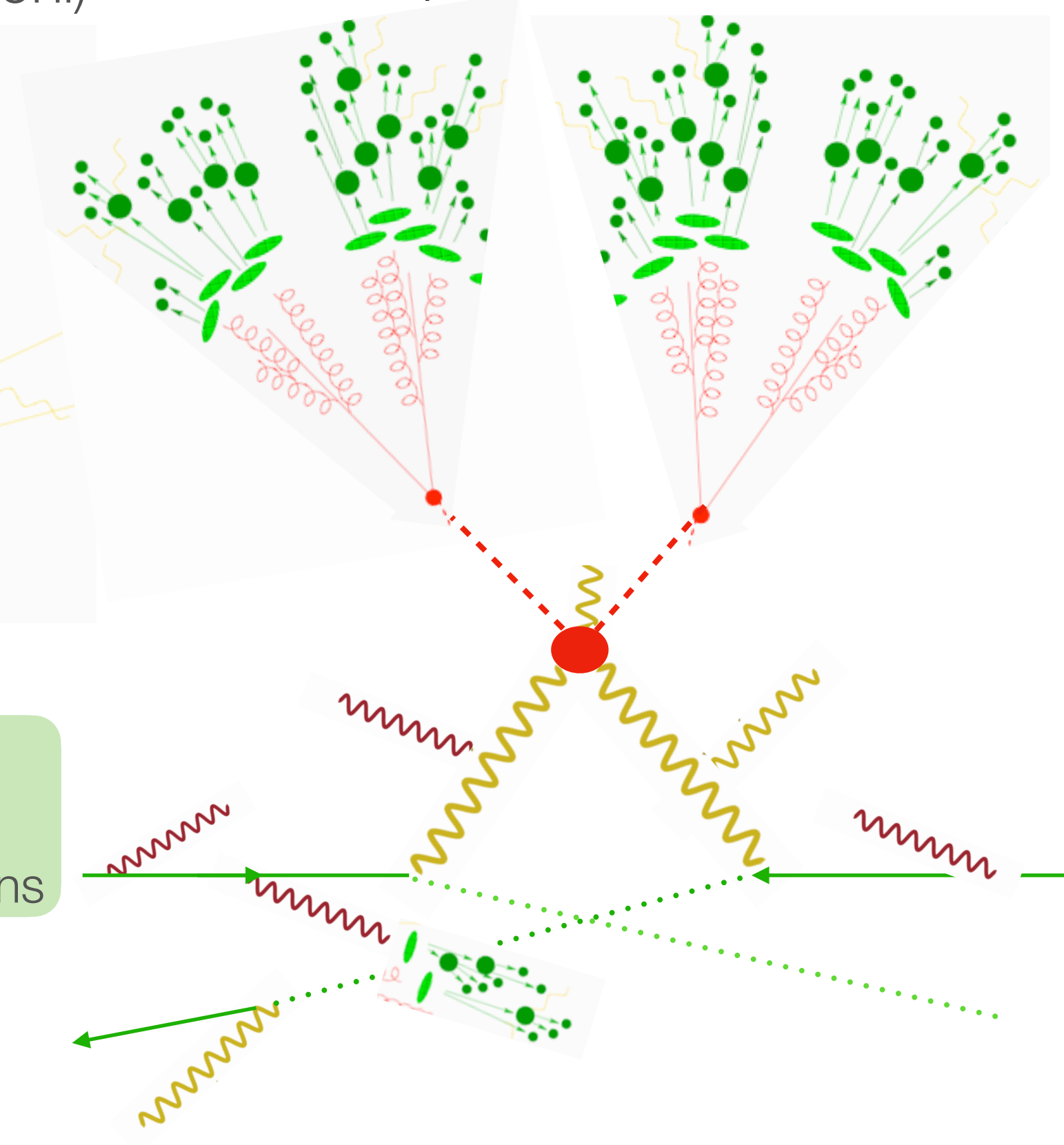
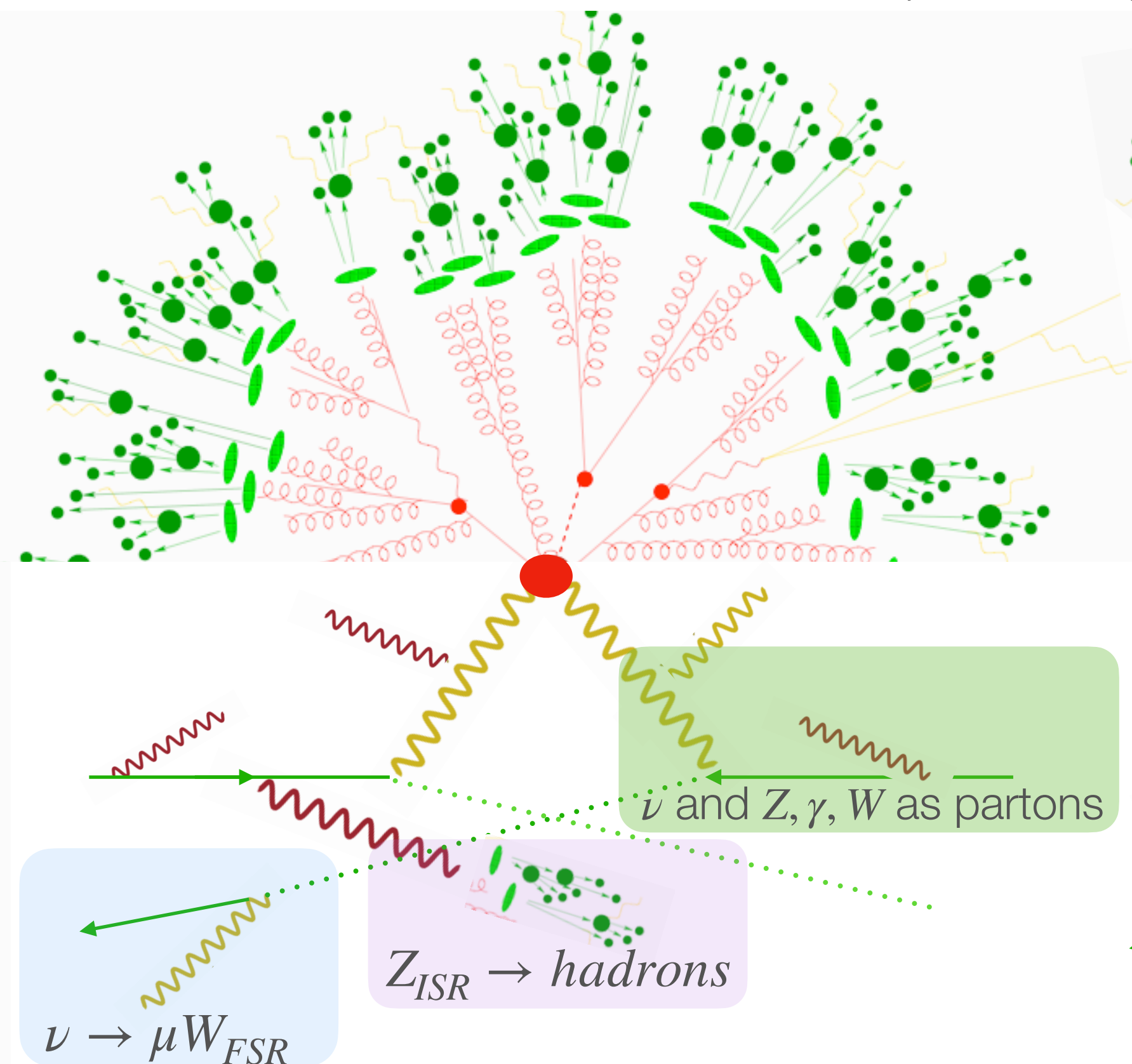
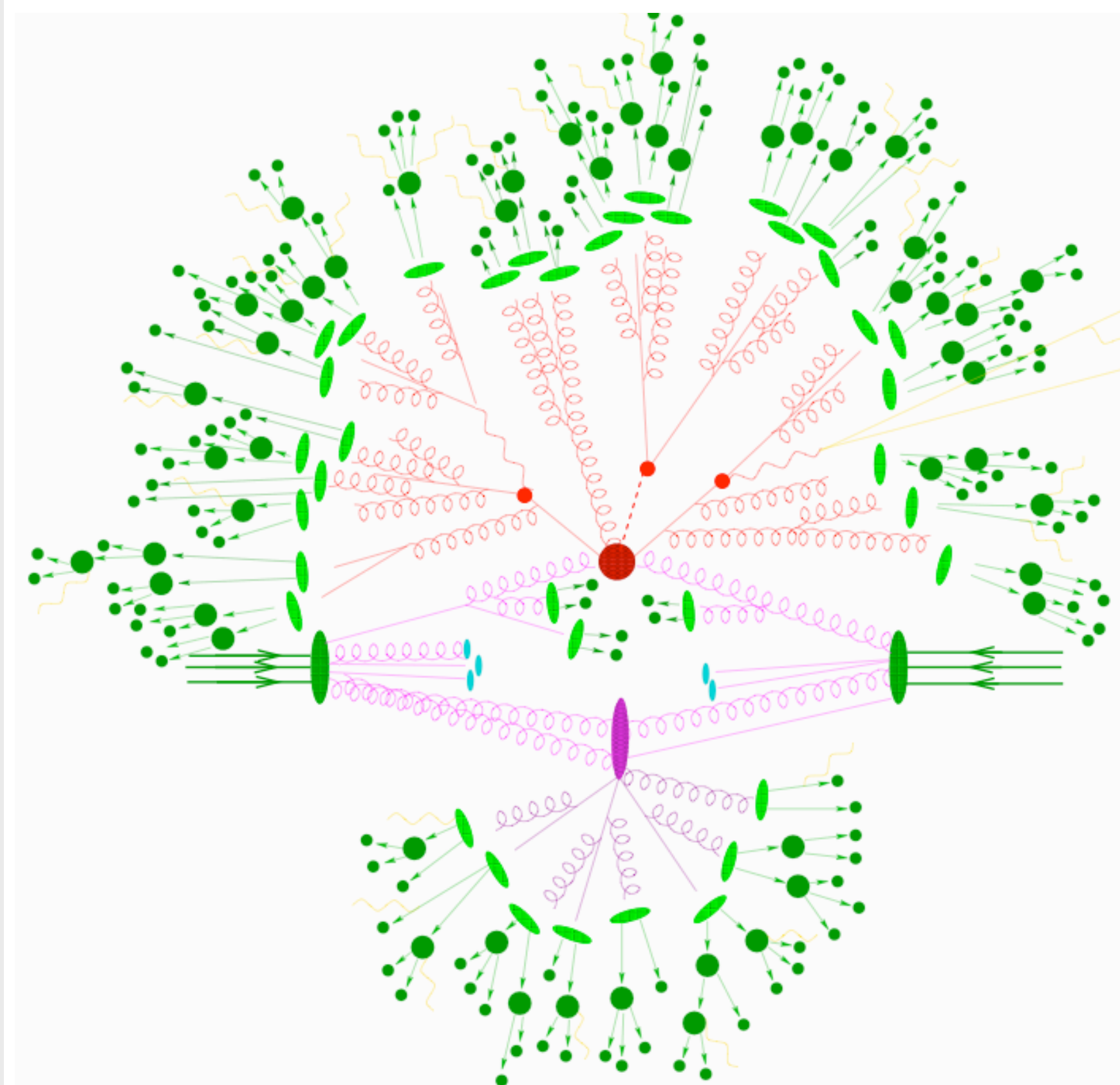
STANDARD MODEL

“FACTORY”

tth production at the LHC (Fully hadronic)

tth production at the muC 100 TeV (F. Maltoni)

HH \rightarrow 4b production at a multi-TeV muC



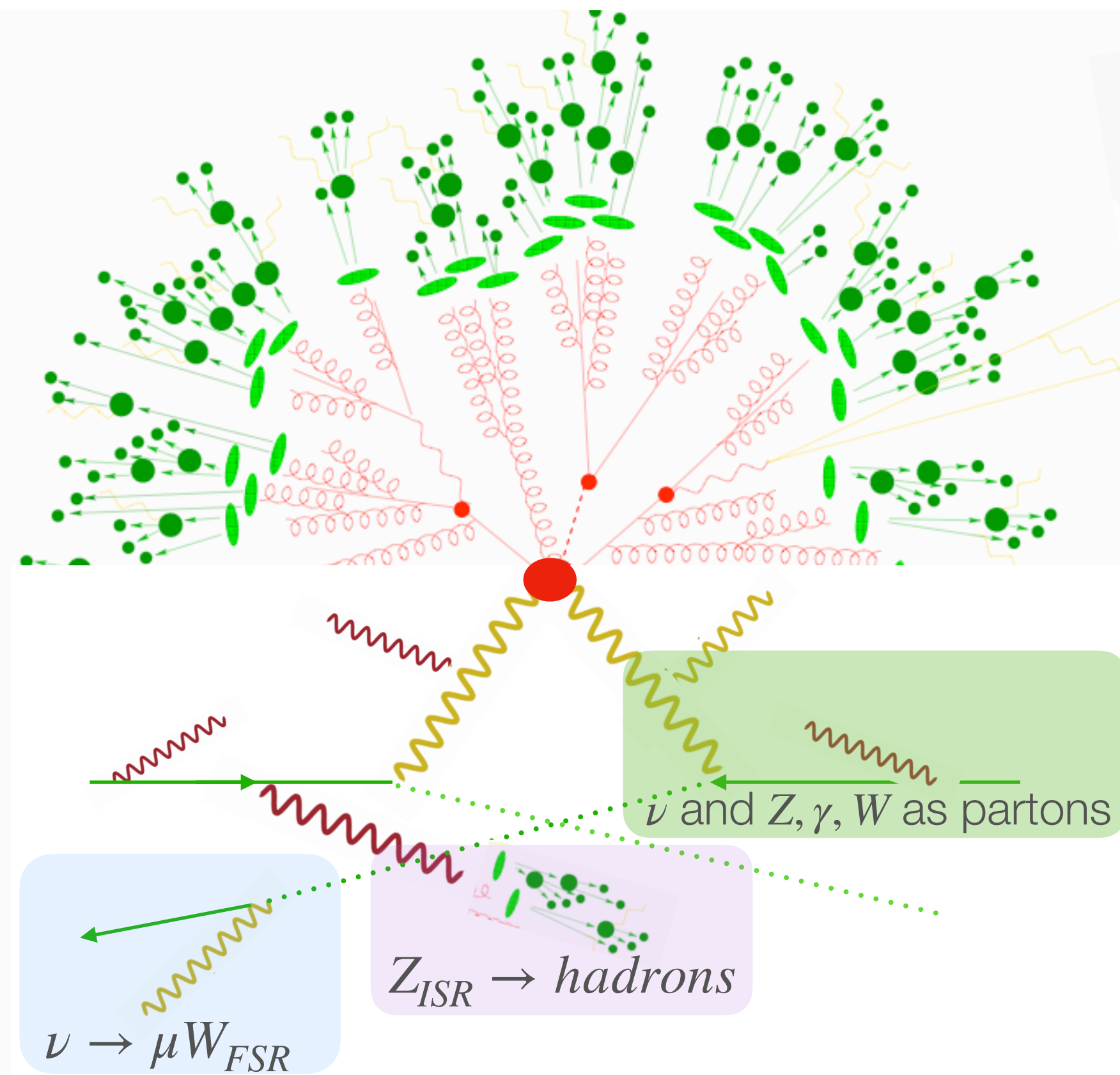
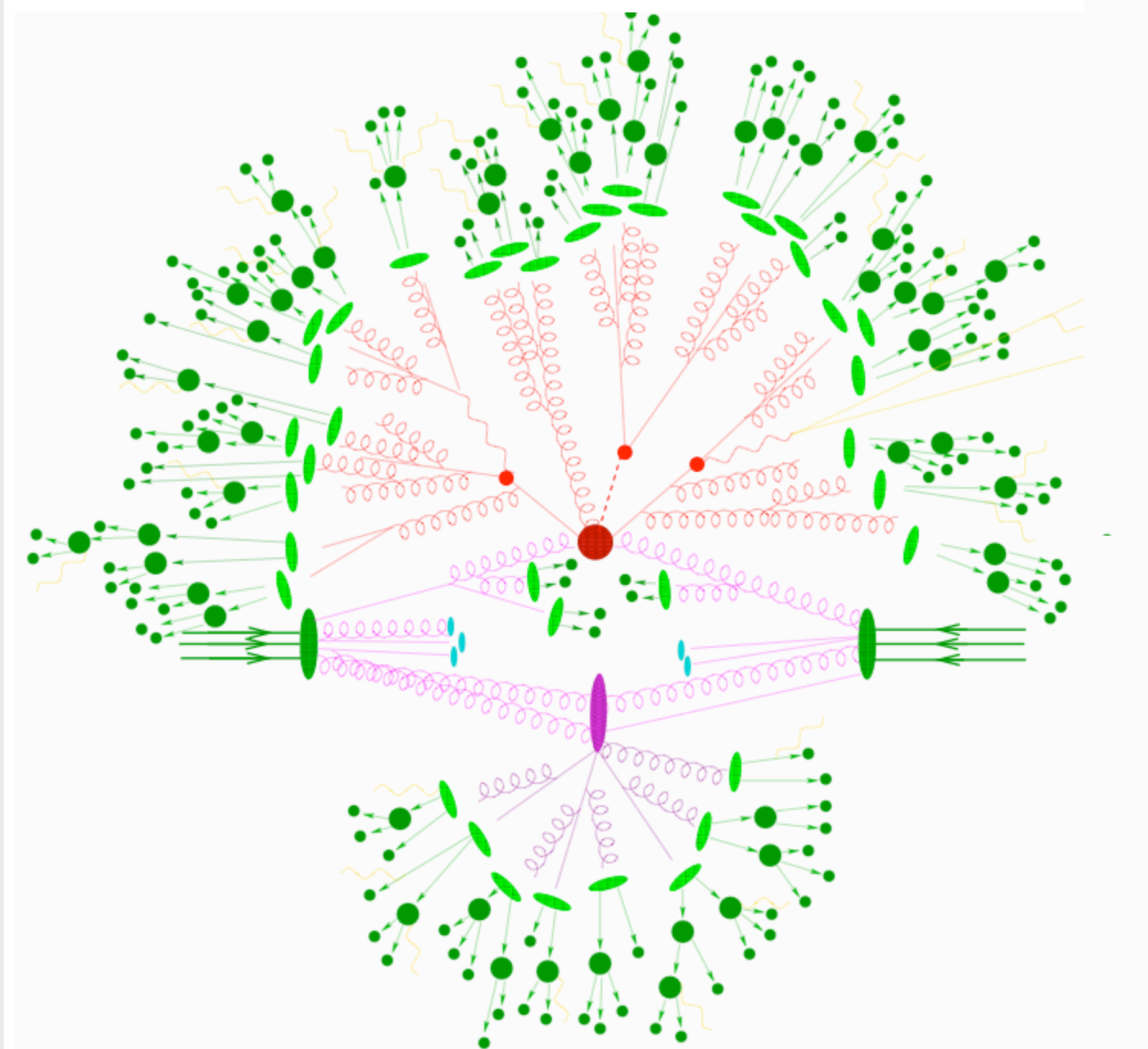
Theory $\mu^+ \mu^- \rightarrow SM SM \nu \bar{\nu}$

STANDARD MODEL

“FACTORY”

tth production at the LHC (Fully hadronic)

tth production at the muC 100 TeV (F. Maltoni)



NEW PHENOMENA AND
NEW REGIMES IN pQFT

- weak corrections become “ordinary”
- weak “partons”
- large EW logarithms

Conclusions

- dedicated e^+e^- factory stages prove to be the “easiest” factories to operate (and to interpret) when it comes to precision measurements ($\delta m_W, \delta m_t, \delta m_Z, \dots$)
- high-energy machines (pp or $\mu\mu$) can often probe the microscopic phenomena that motivate the precision measurements and often surpass it by far (see t_R compositeness example, EWPT in SMEFT)
- in many instances the $\mu\mu$ collider can play the role of the hh in finishing the job started by ee with the bonus of potentially operating in the same years while also contributing as a “multiplex”-factory)
- well motivated scenarios require inputs from all projects to reach a conclusion ($h \rightarrow \phi\phi$ for ϕ driving EWpt, mechanisms for neutrino mass, ...)

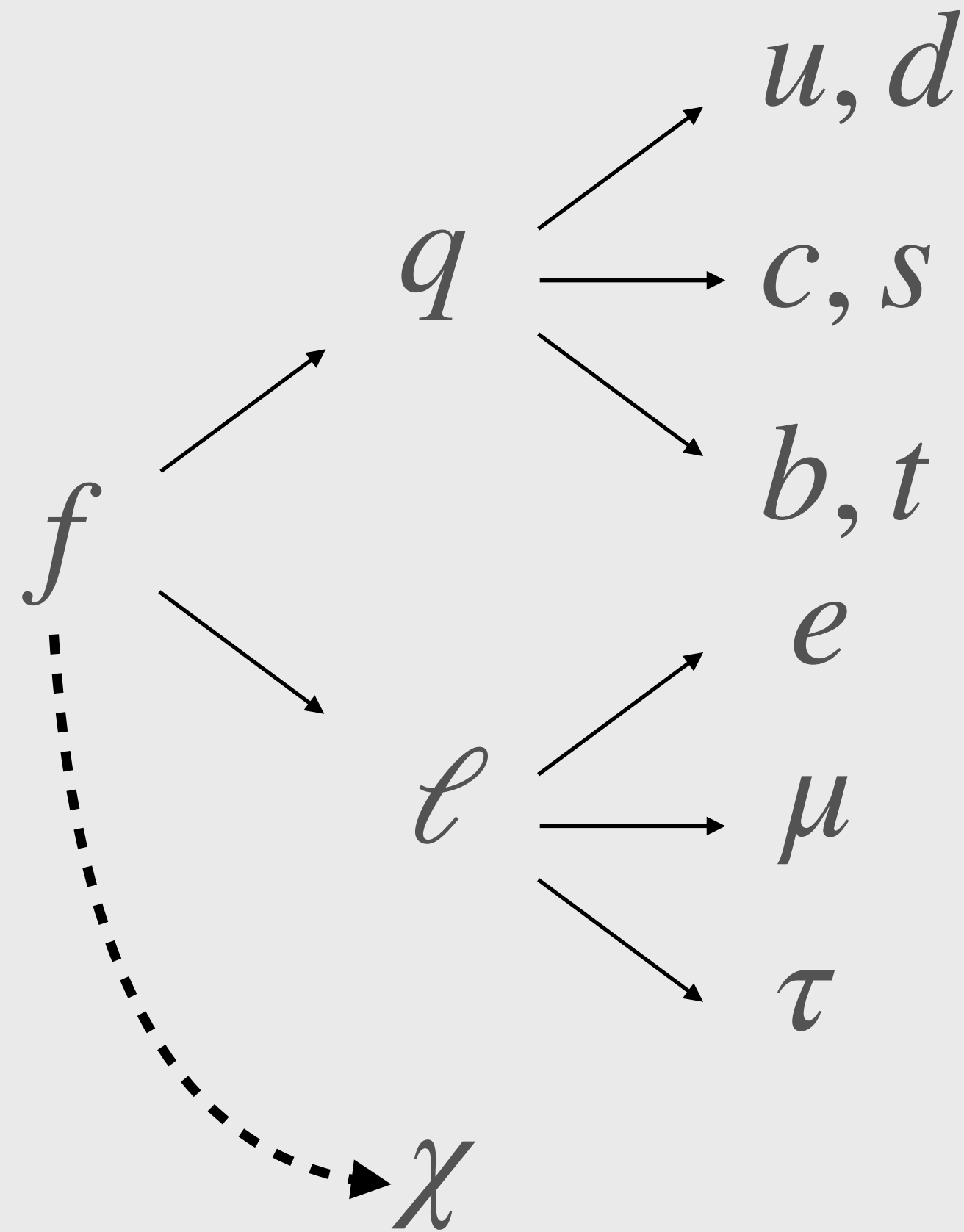
- interactions between timelines of the projects is highly non-trivial



- during the long time from now to the next collider results from outside highest-energy colliders might give a strong hint of where BSM might lie (e.g. for WIMPs, flavor, GWs, EDMs)

Thank you!

Flavor



always offers more possibilities

Flavor Physics FCCee

Particle production (10^9)	B^0/\bar{B}^0	B^+/B^-	B_s^0/\bar{B}_s^0	$\Lambda_b/\bar{\Lambda}_b$	$c\bar{c}$	$\tau^+\tau^-$
Belle II	27.5	27.5	n/a	n/a	65	45
FCC-ee	1000	1000	250	250	550	170

progress by production of more and more flavored particles

- LFV $h, Z^0 \rightarrow \ell_j^+ \ell_k^-$
- $\ell_i \rightarrow \ell_k$ (cLFV)
- B and D fragmentation functions measurement
 \Rightarrow matching theory development (parton showers, ...)



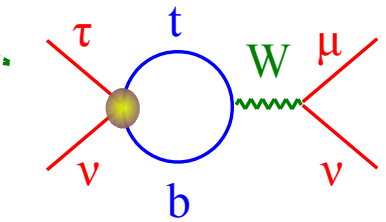
Brief intro to Flavor Physics @ FCC-ee

Gino Isidori
 [University of Zürich]

E.g.: (I) LFU tests in tau decays

	$\Gamma_{\tau \rightarrow \mu} / \Gamma_{\tau \rightarrow e}$	$\Gamma_{\pi \rightarrow \mu} / \Gamma_{\pi \rightarrow e}$	$\Gamma_{K \rightarrow \mu} / \Gamma_{K \rightarrow e}$	$\Gamma_{K \rightarrow \pi \mu} / \Gamma_{K \rightarrow \pi e}$	$\Gamma_{W \rightarrow \mu} / \Gamma_{W \rightarrow e}$
$ g_\mu / g_e $	1.0018 (14)	1.0021 (16)	0.9978 (20)	1.0010 (25)	0.996 (10)
	$\Gamma_{\tau \rightarrow e} / \Gamma_{\mu \rightarrow e}$	$\Gamma_{\tau \rightarrow \pi} / \Gamma_{\pi \rightarrow \mu}$	$\Gamma_{\tau \rightarrow K} / \Gamma_{K \rightarrow \mu}$	$\Gamma_{W \rightarrow \tau} / \Gamma_{W \rightarrow \mu}$	
$ g_\tau / g_\mu $	1.0011 (15)	0.9962 (27)	0.9858 (70)	1.034 (13)	
	$\Gamma_{\tau \rightarrow \mu} / \Gamma_{\mu \rightarrow e}$	$\Gamma_{W \rightarrow \tau} / \Gamma_{W \rightarrow e}$			
$ g_\tau / g_e $	1.0030 (15)	1.031 (13)			

A. Pich '13



“Model-independent”
 $O(10^{-3})$ correction
 linked to the CC
 anomalies

Feruglio, Paradisi, Pattori '16

- NP expectation from motivated NP up to current bounds (i.e. $\sim 2 \times 10^{-3}$)
- SM theory precision $\sim 10^{-5}$
- Belle-II can (at most) reach an error $\sim 0.3 \times 10^{-3}$

FCC-ee could go below 10^{-4} !

Unique opportunity !

E.g.: (III) Rare B decays

The kinematical configuration with boosted b's and tau's (from Z decays) + “clean” environment, gives to the FCC-ee b-physics program a special advantage (compared to B-factories & LHC-b) to a series of very interesting rare B decays

III.a All decays into tau leptons:

$B \rightarrow K^* (K) \tau^+ \tau^-$: $BR_{SM} \sim 10^{-7}$
 [Golden modes related to present anomalies \rightarrow potential huge NP effects]

- $BR_{exp} (B \rightarrow K \tau^+ \tau^-)$: $< 2 \times 10^{-3}$ [Babar]
- Belle-II ($B \rightarrow K^* \tau^+ \tau^-$): ~ 1 event @ SM rate (with small S/B)

Flavor Physics At $\mu\mu$

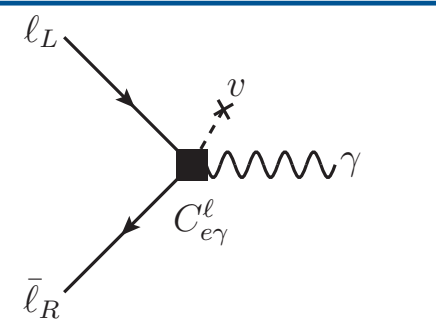
Buttazzo - IMCC annual meeting June 2023

Muon g-2 @ muon collider

- ♦ If new physics is light enough (i.e. weakly coupled), a Muon Collider can directly produce the new particles **direct searches: model-dependent**
Capdevilla et al. 2006.16277
- ♦ If new physics is heavy: EFT!
One dim. 6 operator contributes at tree-level: $\mathcal{L}_{g-2} = \frac{C_{e\gamma}}{\Lambda^2} H(\bar{\ell}_L \sigma_{\mu\nu} e_R) e F^{\mu\nu} + \text{h.c.}$

At low energy

$$\Delta a_\mu = \frac{4m_\mu v}{\Lambda^2} C_{e\gamma} \approx 3 \times 10^{-9} \times \left(\frac{140 \text{ TeV}}{\Lambda}\right)^2 C_{e\gamma}$$



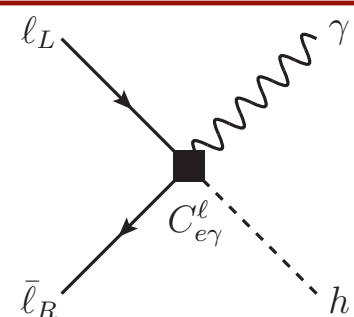
Dipole operator generates both Δa_μ and $\mu\mu \rightarrow h\gamma$

B, Paradisi 2012.02769

At high energy

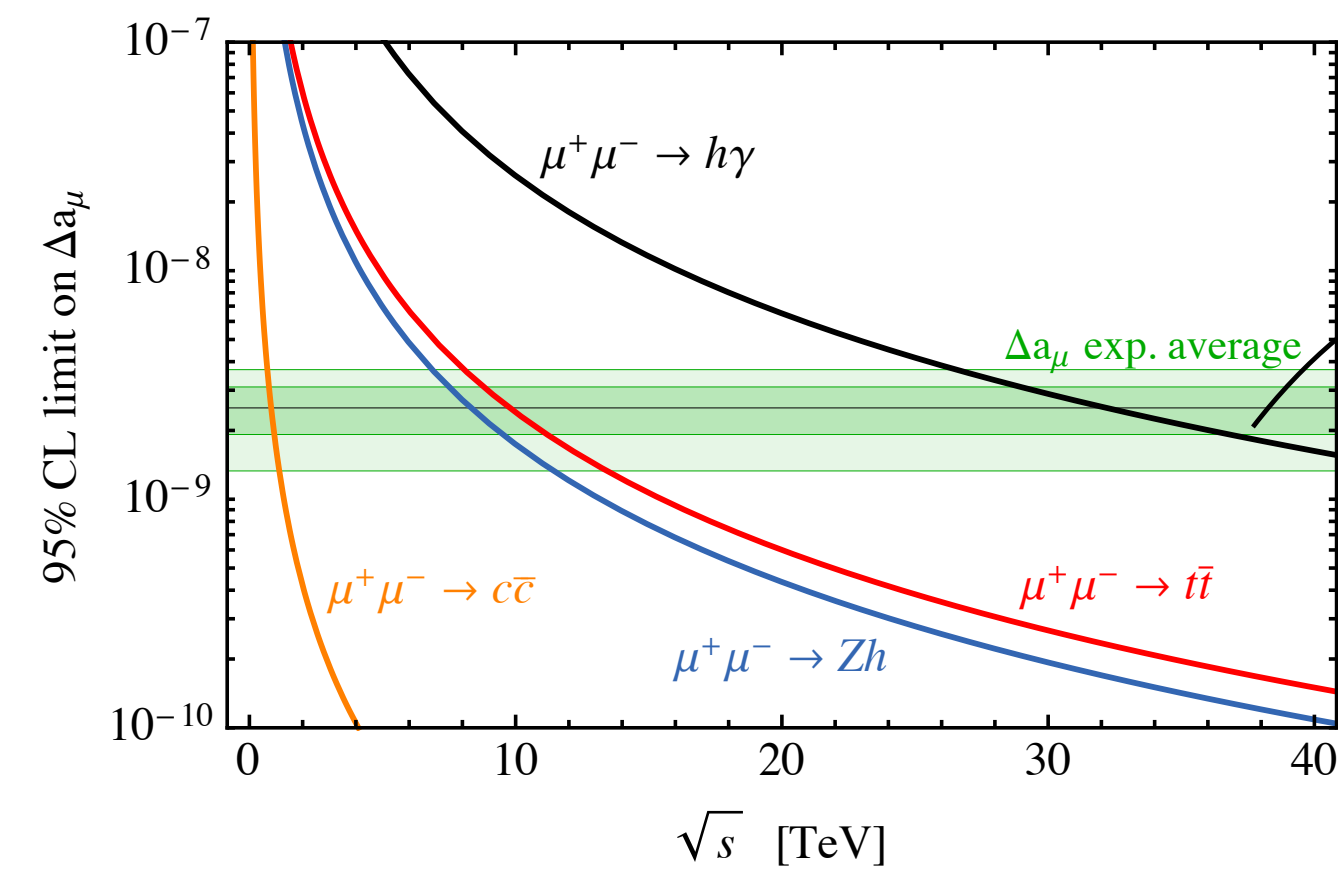
$$\sigma_{\mu^+\mu^- \rightarrow h\gamma} = \frac{s}{48\pi} \frac{|C_{e\gamma}|^2}{\Lambda^4} \approx 0.7 \text{ ab} \left(\frac{\sqrt{s}}{30 \text{ TeV}}\right)^2 \left(\frac{\Delta a_\mu}{3 \times 10^{-9}}\right)^2$$

$$N_{h\gamma} = \sigma \cdot \mathcal{L} \approx \left(\frac{\sqrt{s}}{10 \text{ TeV}}\right)^4 \left(\frac{\Delta a_\mu}{3 \times 10^{-9}}\right)^2 \quad \text{need } E > 10 \text{ TeV}$$



8

Muon g-2 @ muon collider



Exp. value of Δa_μ can be tested at 95% CL at a 30 TeV collider! (with reasonable assumptions on detector performance)

This result is completely model-independent!

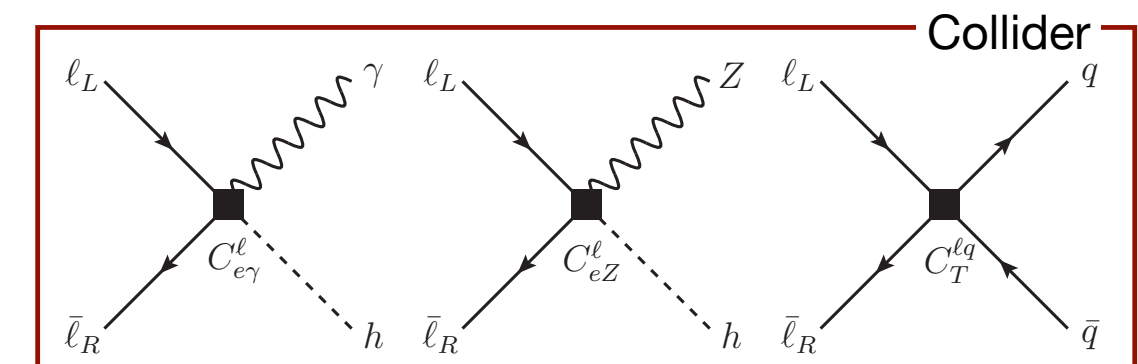
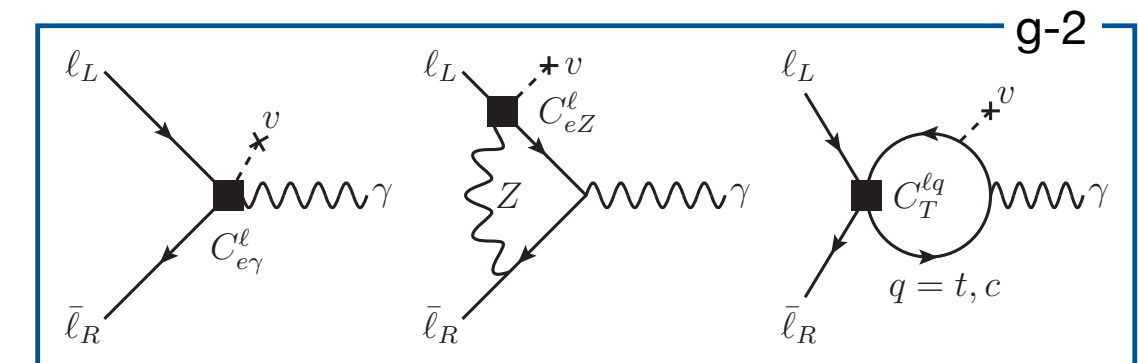
B, Paradisi 2012.02769

- ♦ Other operators enter g-2 at 1 loop:

$$\Delta a_\mu \approx \left(\frac{250 \text{ TeV}}{\Lambda^2}\right)^2 \left(C_{e\gamma} - \frac{C_{Tt}}{5} - \frac{C_{Tc}}{1000} - \frac{C_{eZ}}{20}\right)$$

- ♦ Full set of operators with $\Lambda \geq 100 \text{ TeV}$ can be probed at a high-energy muon collider

9



Flavor Physics At $\mu\mu$

Buttazzo - IMCC annual

Muon g-2 @ muon

- ♦ If new physics is light enough, it can directly produce the new physics
- ♦ If new physics is heavy: One dim. 6 operator constrains

At low energy

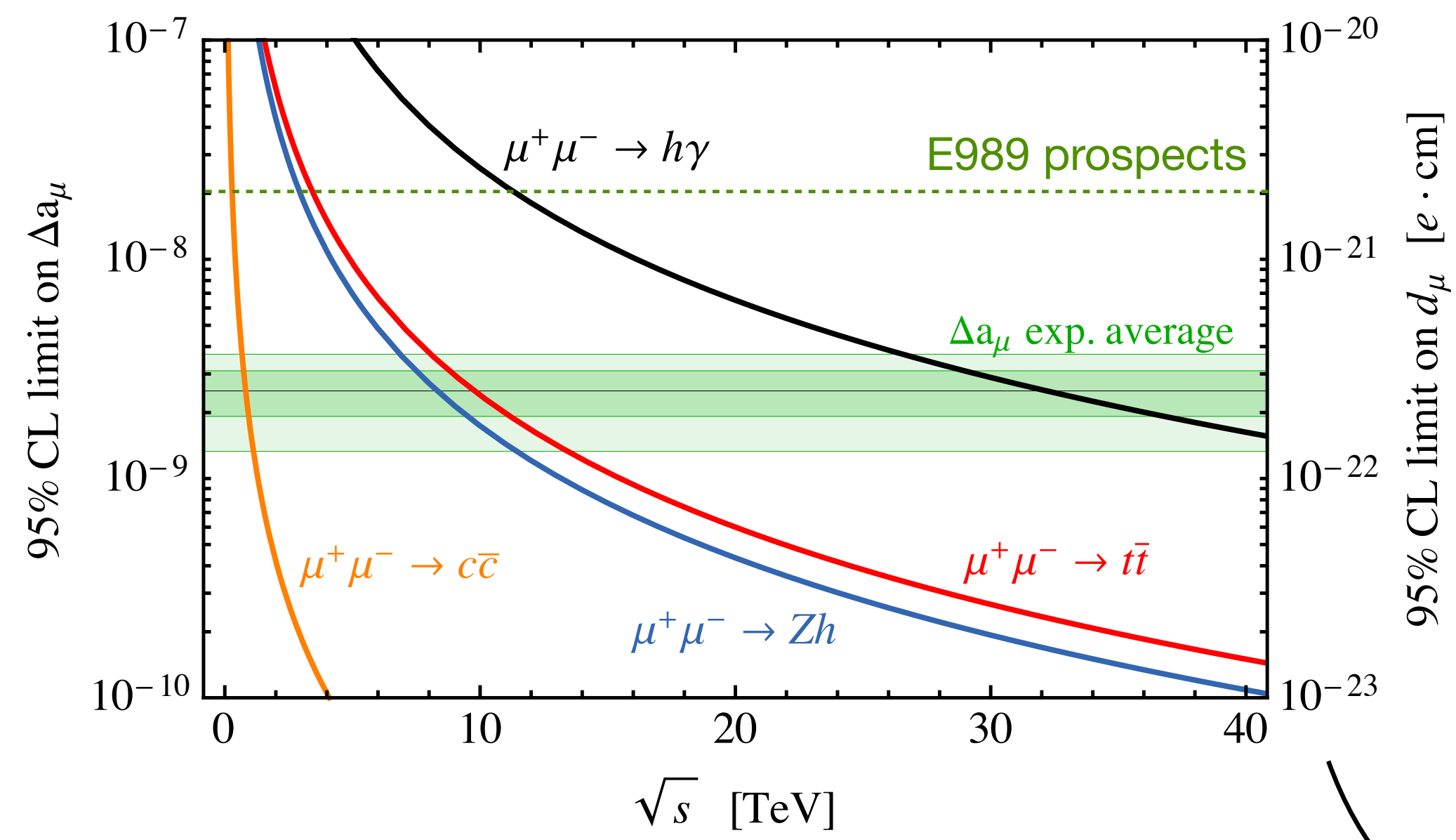
$$\Delta a_\mu = \frac{4m_\mu v}{\Lambda^2} C_{e\gamma} \approx 3 \times 10^{-9} \left(\frac{v}{\Lambda} \right)^2 |C_{e\gamma}|$$

Dipole operator generates

At high energy

$$\sigma_{\mu^+\mu^- \rightarrow h\gamma} = \frac{s}{48\pi} \frac{|C_{e\gamma}|^2}{\Lambda^4}$$

$$N_{h\gamma} = \sigma \cdot \mathcal{L} \approx \left(\frac{\sqrt{s}}{10 \text{ TeV}} \right)^2 |C_{e\gamma}|^2$$



$$\Delta a_\mu = \frac{4vm_\mu \text{Re}(C_{e\gamma})}{\Lambda^2}$$

$$d_\mu = \frac{2v \text{Im}(C_{e\gamma})}{\Lambda^2} = \frac{\Delta a_\mu}{2m_\mu} \tan \phi_\mu e$$

Collider constrains $|C_{e\gamma}|^2$

$$\Rightarrow d_\mu \lesssim 10^{-22} e \cdot \text{cm} \quad (\text{comparable with future } d_\mu \lesssim 0.6 \cdot 10^{-22} e \cdot \text{cm})$$

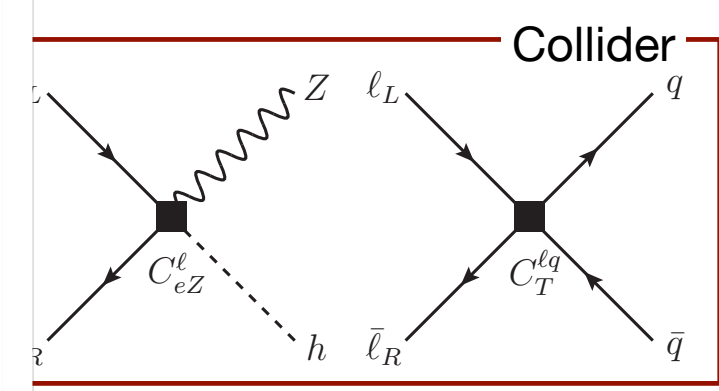
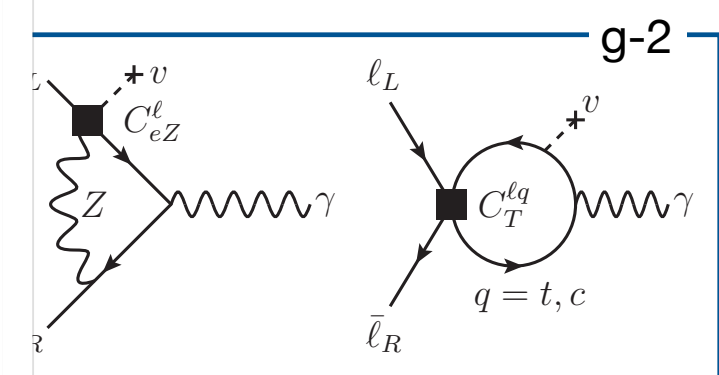
3 o.o.m. stronger than present bound! @ $10^{-19} e \cdot \text{cm}$

2102.08838

Exp. value of Δa_μ can be tested at 95% CL at a 30 TeV collider! (with reasonable assumptions on detector performance)

This result is completely model-independent!

B, Paradisi 2012.02769



Flavor Physics At $\mu\mu$

Buttazzo - IMCC annual meeting June 2023

Lepton g-2 from rare Higgs decays

- ♦ Tau magnetic dipole moment: enhanced due to the larger mass

$$\Delta a_\tau = \frac{4v m_\tau}{\Lambda^2} C_{e\gamma}^\tau \approx \Delta a_\mu \frac{m_\tau^2}{m_\mu^2} \approx 10^{-6}$$

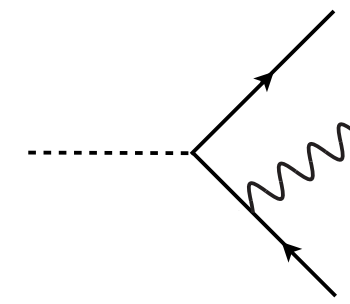
if $C_{e\gamma}^\ell$ scales as y_ℓ

Present bound: $\Delta a_\tau \lesssim 10^{-2}$
 from LEP $e^+e^- \rightarrow e^+e^-\tau^+\tau^-$
[hep-ex/0406010](https://arxiv.org/abs/hep-ex/0406010)

Can be improved to few 10^{-3}
 at HL-LHC [1908.05180](https://arxiv.org/abs/1908.05180)

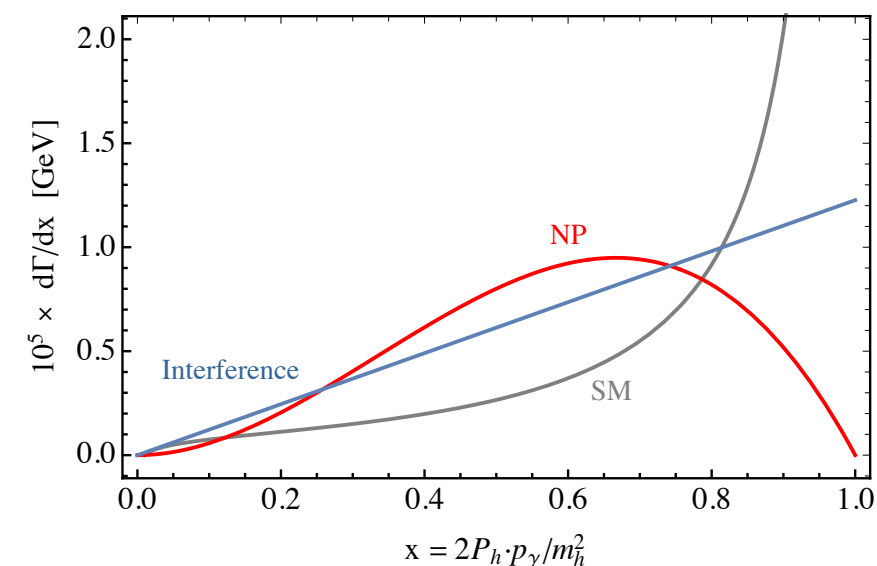
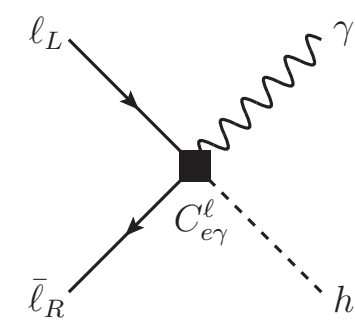
- ♦ Contribution to $h \rightarrow \tau\tau\gamma$ decays:

$$\text{BR}_{h \rightarrow \tau^+\tau^-\gamma}^{(\text{SM})} \approx 5 \times 10^{-4} \quad (\text{with cut on soft collinear photon})$$



could be measured at few % level by Higgs factory

$$\text{BR}_{h \rightarrow \tau^+\tau^-\gamma}^{(\text{NP})} \approx 0.2 \times \Delta a_\tau$$



12

Lepton g-2 from rare Higgs decays

$$\text{BR}_{h \rightarrow \tau^+\tau^-\gamma}^{(\text{SM})} \approx 5 \times 10^{-4}$$

$$\text{BR}_{h \rightarrow \tau^+\tau^-\gamma}^{(\text{NP})} \approx 0.2 \times \Delta a_\tau$$

- ♦ **MuC:** 10^7 Higgs bosons @ 10 TeV \Rightarrow 5k $H \rightarrow \tau\tau\gamma$ events, 2% precision on SM,

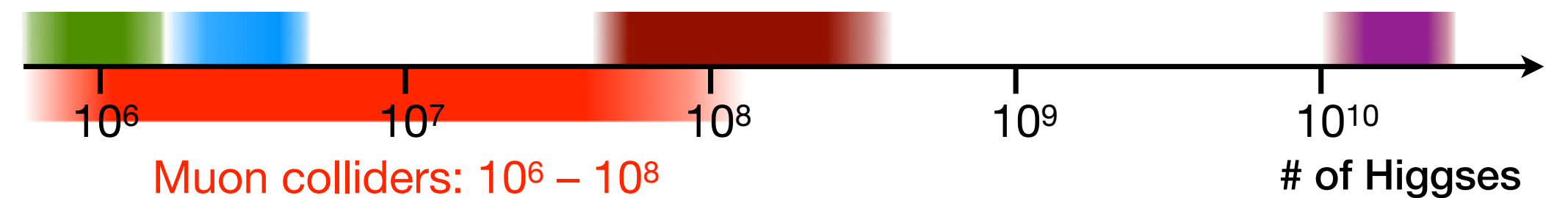
$$\Delta a_\tau \lesssim 3 \times 10^{-5} \quad (\text{signal only}) \quad \text{3 o.o.m. improvement of current limit!}$$

Low energy
 e^+e^- factories
 (FCC-ee, CEPC,
 ILC, CLIC380)

TeV-scale
 e^+e^- factories
 (CLIC, ILC1000)

LHC: few $\times 10^7$
 HL-LHC: few $\times 10^8$

FCC-hh:
 few $\times 10^{10}$



- ♦ **e^+e^- factory:** $\sim 400 H \rightarrow \tau\tau\gamma$ events \Rightarrow 5% precision on SM, $\Delta a_\tau \lesssim \text{few} \times 10^{-4}$

- ♦ **LHC:** large number of Higgs bosons, but large backgrounds
 Rescaling $H \rightarrow \tau\tau$ searches ~ 350 reconstructed $H \rightarrow \tau\tau\gamma$ events at HL-LHC,
 but 10x more background \Rightarrow 20% precision on SM, $\Delta a_\tau \lesssim 5 \times 10^{-4}$

13

Flavor Physics At $\mu\mu$

Buttazzo - IMCC annual

Lepton g-2 from

- ◆ Tau magnetic dipole

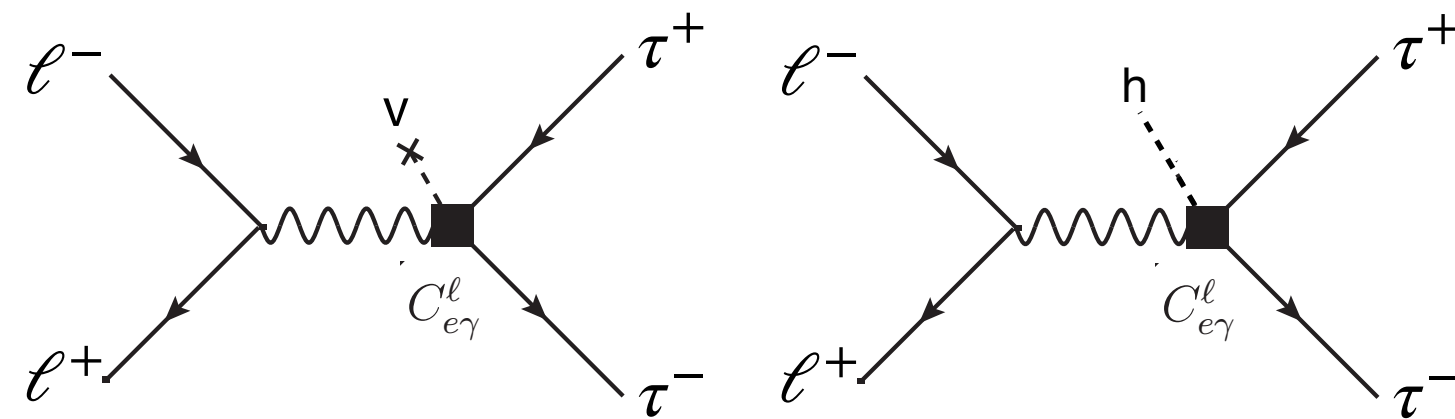
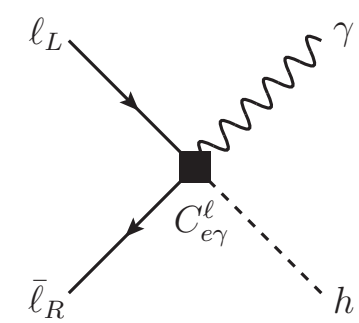
$$\Delta a_\tau = \frac{4v m_\tau}{\Lambda^2} C_{e\gamma}^\tau \approx$$

- ◆ Contribution to $h \rightarrow$

$$\text{BR}_{h \rightarrow \tau^+ \tau^- \gamma}^{(\text{SM})} \approx 5 \times 10^{-6}$$

could be measured

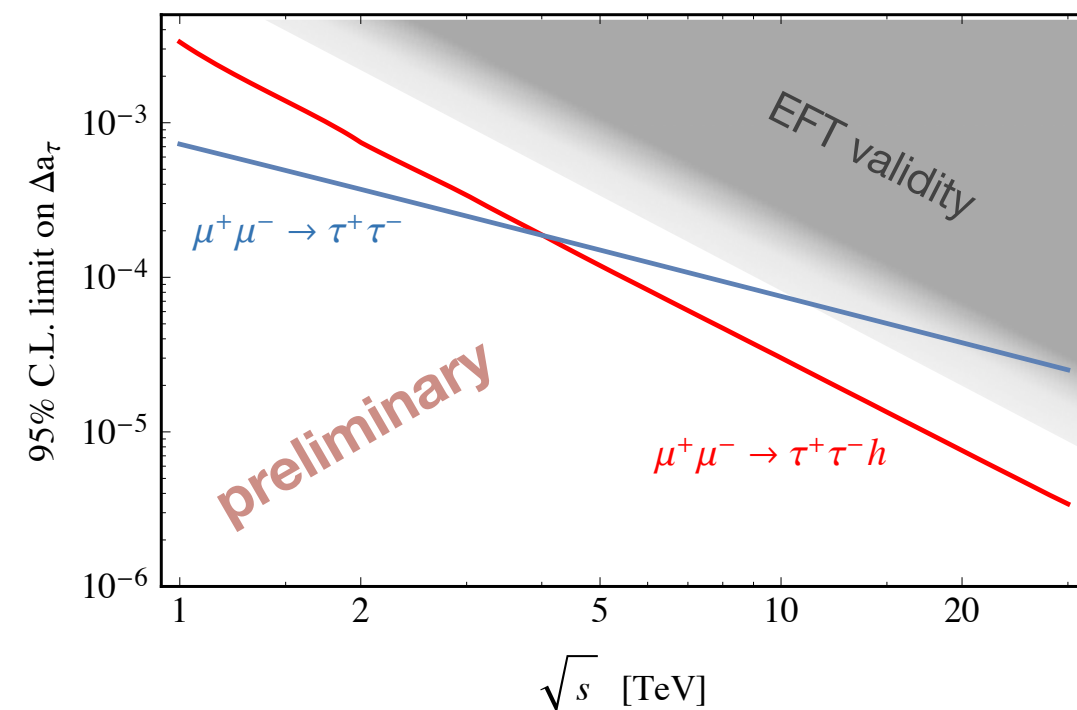
$$\text{BR}_{h \rightarrow \tau^+ \tau^- \gamma}^{(\text{NP})} \approx 0.2 \times$$



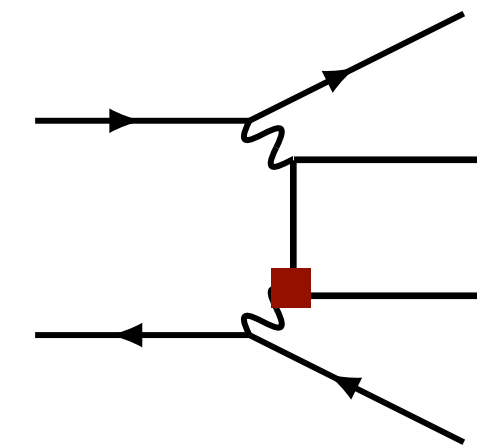
work in progress with Levati, Paradisi, Maltoni, Wang

- ▶ Main background from $\mu\mu \rightarrow Z\gamma$ (where Z is mistaken for H)

Could probe $\Delta a_\tau \sim 10^{-5}$ @ 10 TeV



also a bound on tau EDM!



$$\sim \left(\frac{C_{e\gamma}}{\Lambda^2} \right)^2 + \mathcal{O}(m_\tau^2/\Lambda^2)$$

- ▶ Caveat: VBF is a “soft” process, EFT mainly affects high-mass region

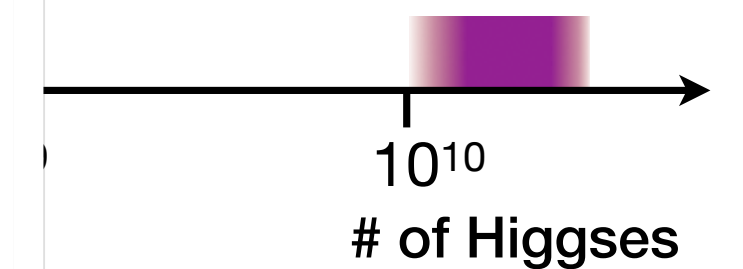
Still, could probe $\Delta a_\tau \sim \text{few } 10^{-5}$



Δa_τ

events, 2% precision on SM, improvement of current limit!

FCC-hh:
few $\times 10^{10}$



on SM, $\Delta a_\tau \lesssim \text{few } \times 10^{-4}$

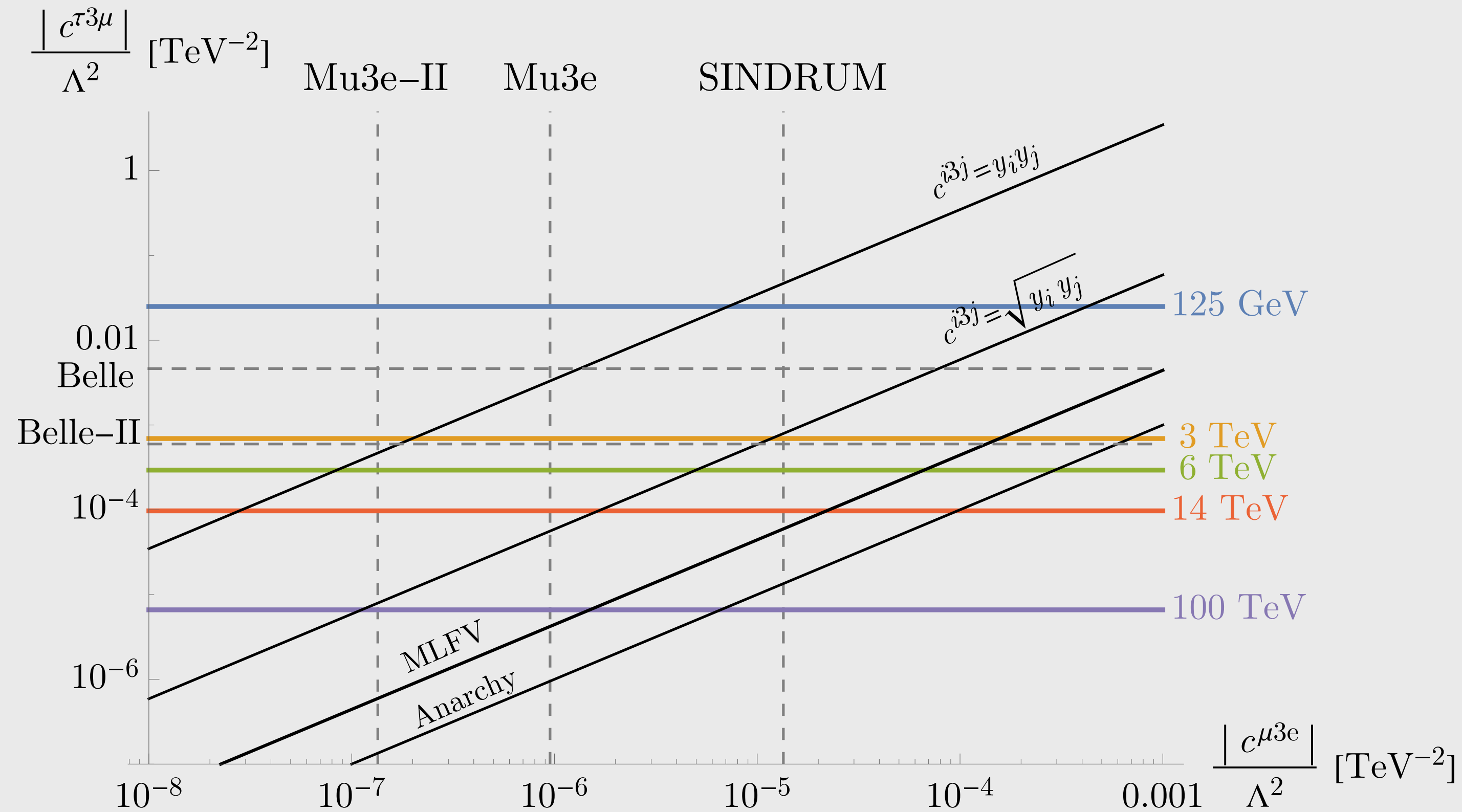
unds

$\tau\tau\gamma$ events at HL-LHC,

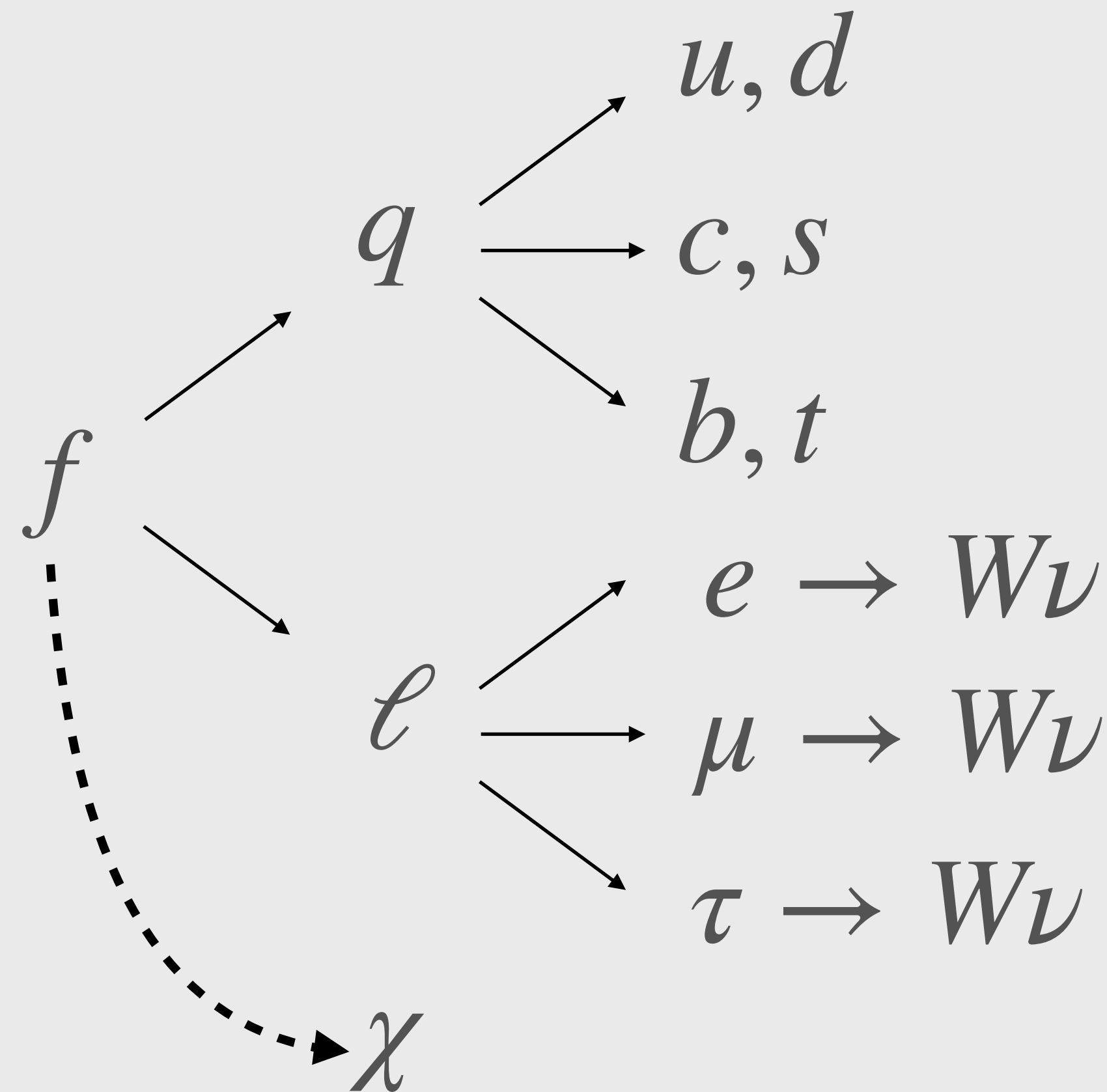
$\Delta a_\tau \lesssim 5 \times 10^{-4}$

Flavor Physics At $\mu\mu$

$$\tau \rightarrow 3\mu \Leftrightarrow \mu\mu \rightarrow \mu\tau$$

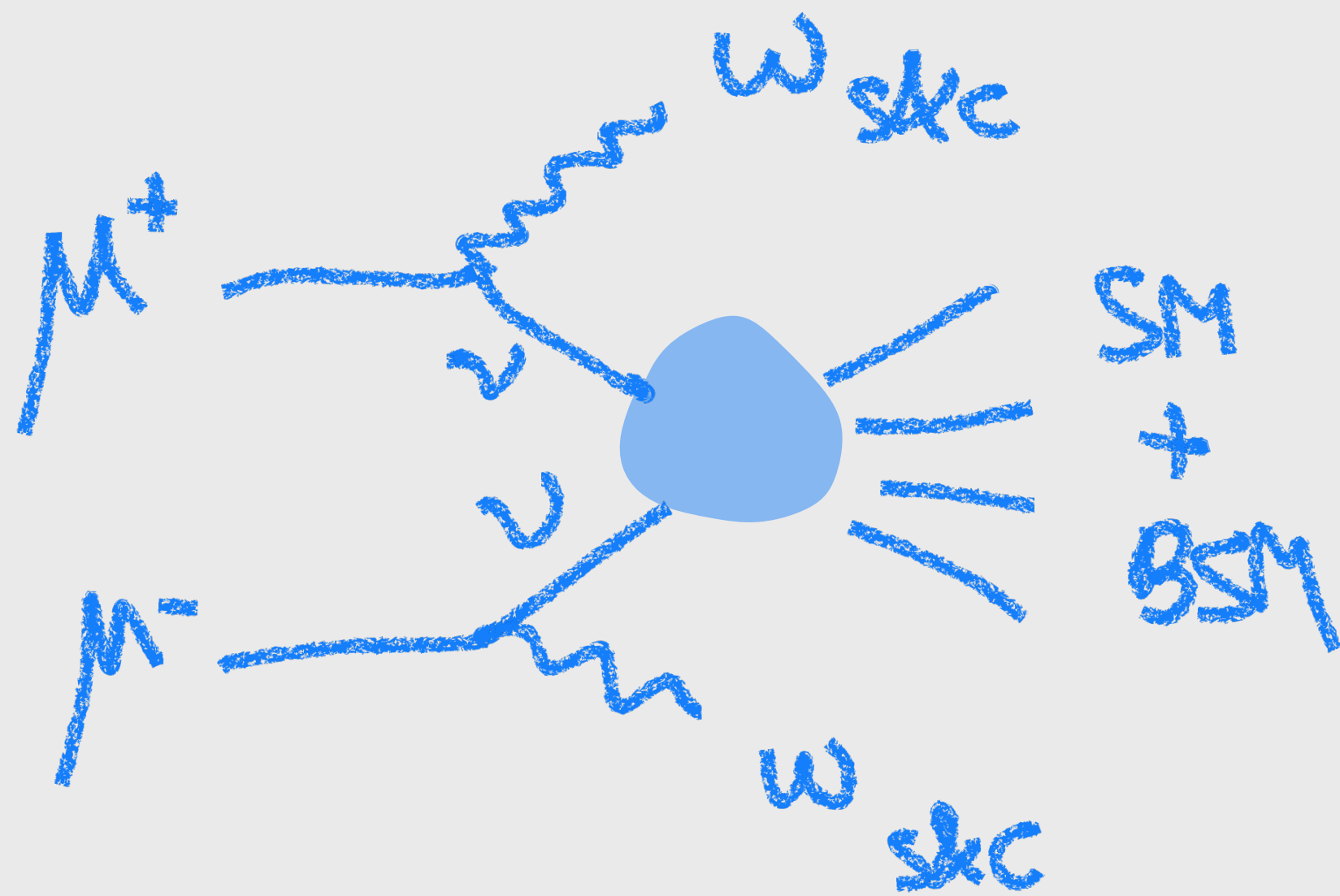


Flavor



always offers more possibilities

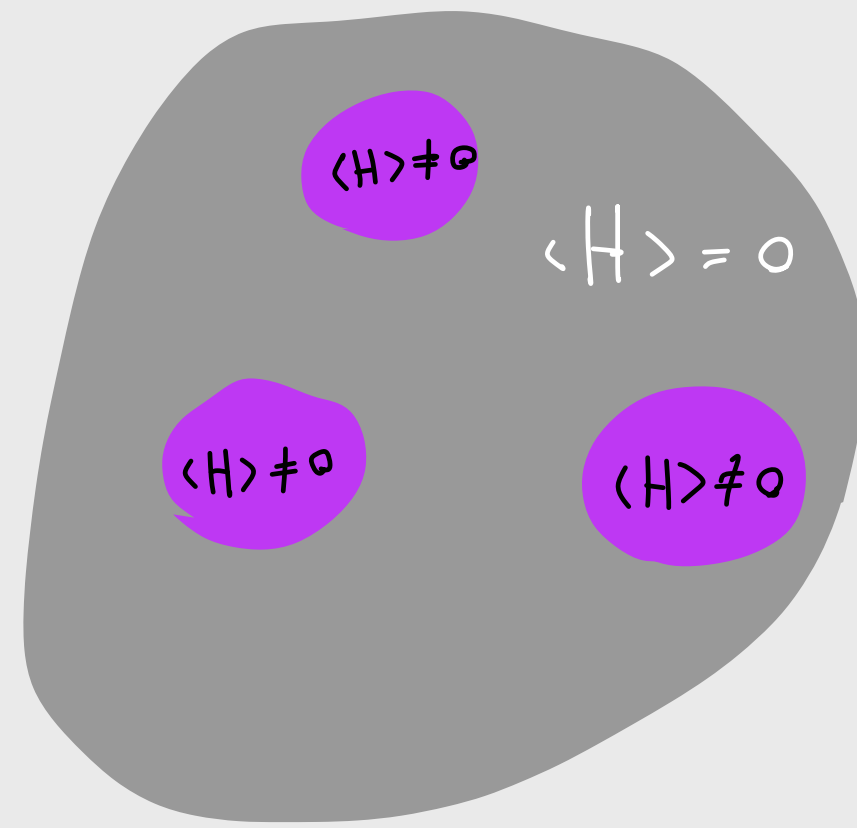
Flavor Physics At “ $\nu\nu$ ”



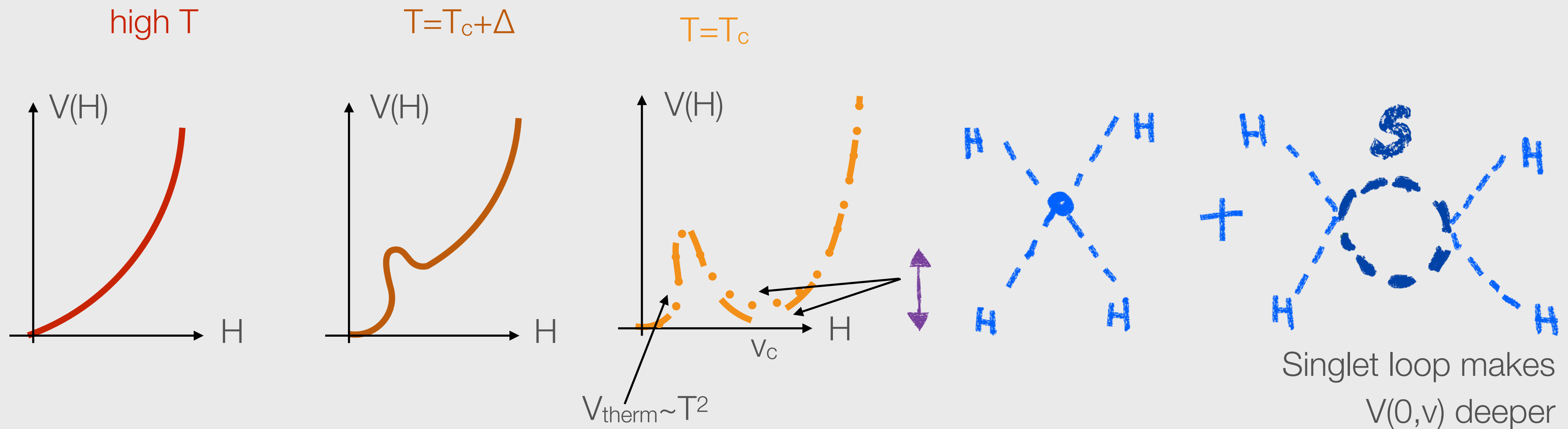
flashing concrete results for

Electroweak phase transition

Electroweak phase transition



- Modifications of the Higgs potential \Rightarrow Out of Equilibrium transition from one vacuum to a new energetically favorable one



Electroweak phase transition

- We need to study all possible new states that induce a change in the Higgs boson potential.
- For these new state to have sizable effects in the early Universe they must be light, around 1 TeV at most.
- All searches for new Higgs bosons (or general electroweak particles) probe such fundamental issue of the origin of matter in the early Universe!

$$V_{\text{therm}} \sim T^2$$

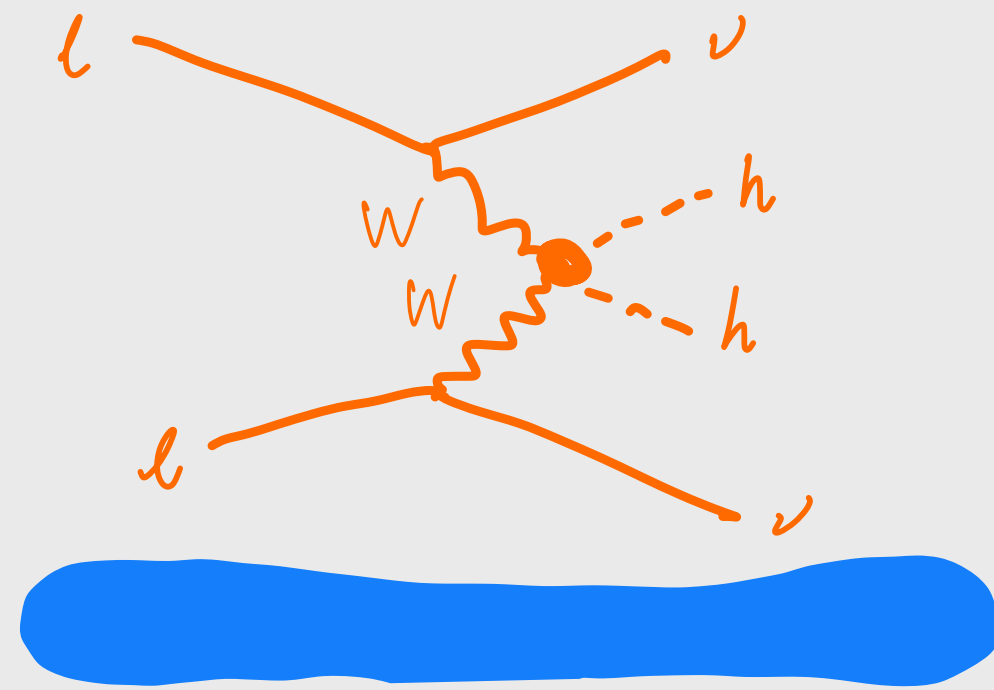
$V(0,v)$ deeper

pp or $\ell^+\ell^- \rightarrow hh$

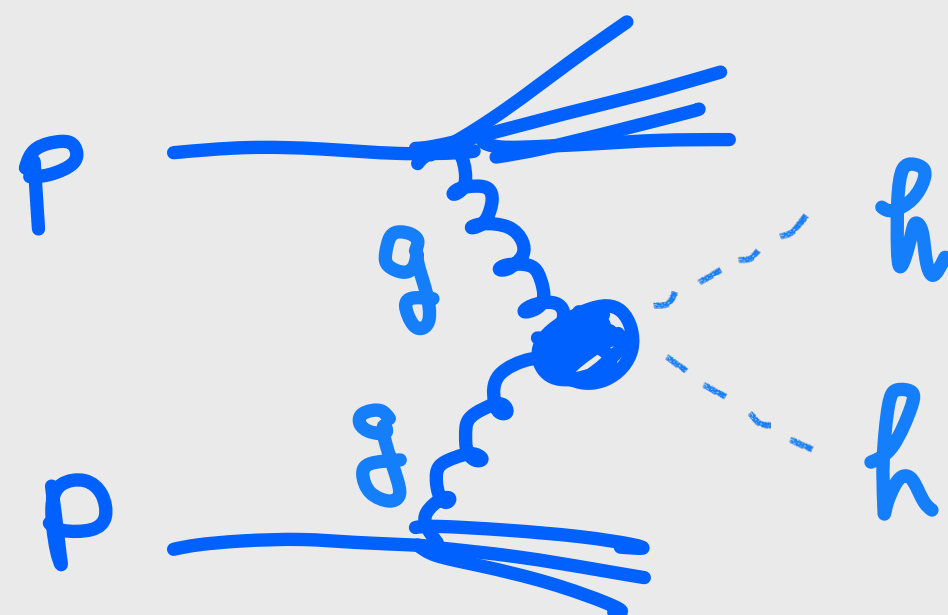
W BOSON

COLLIDER

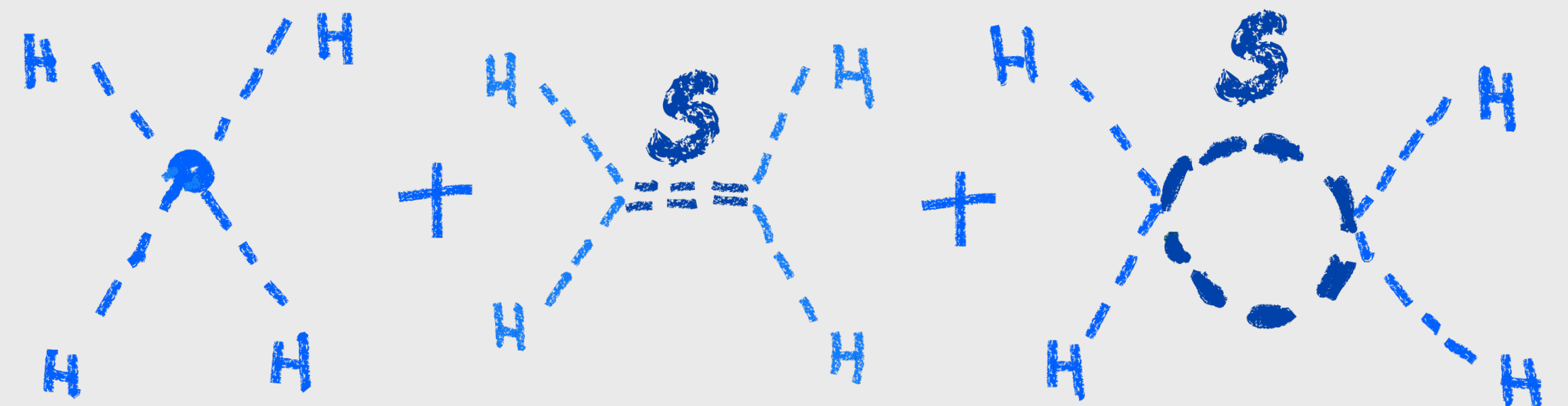
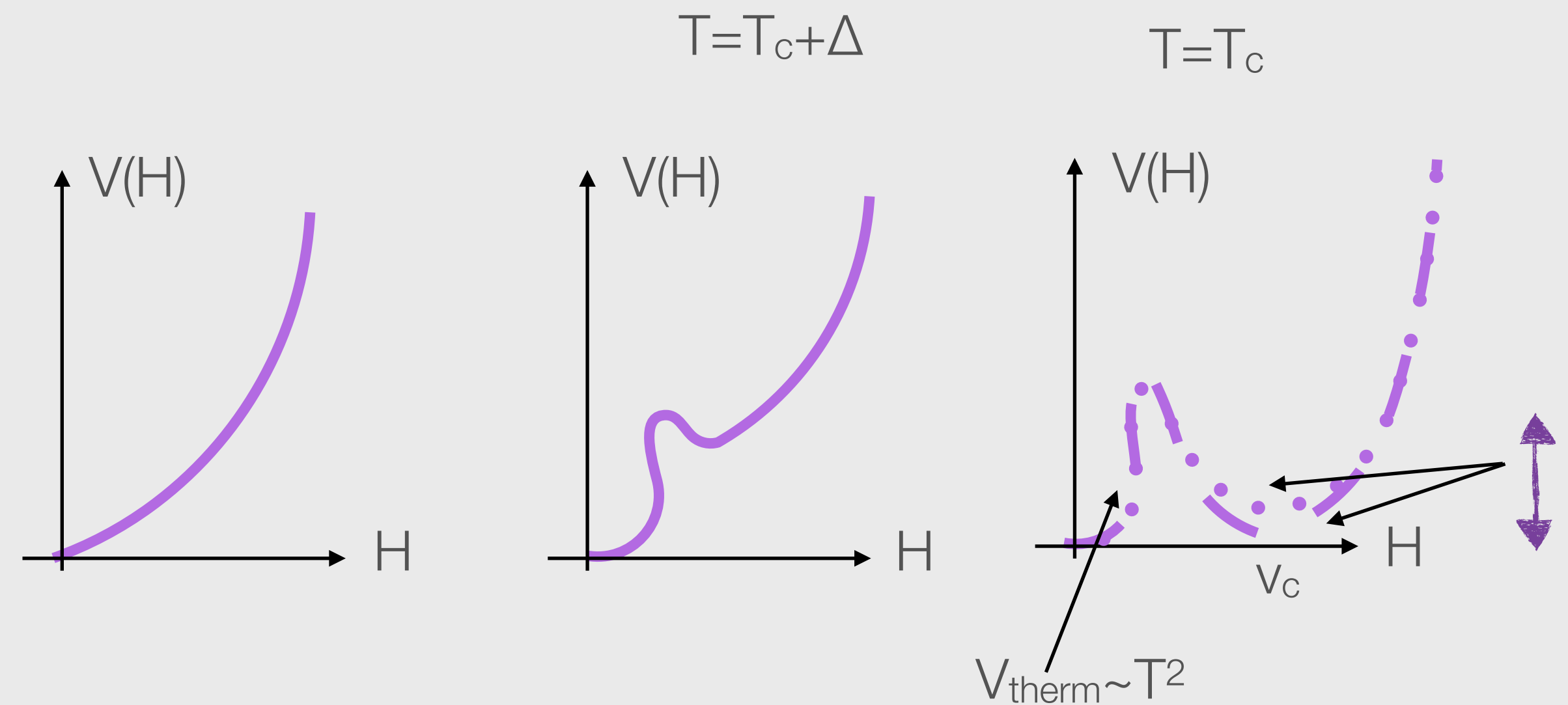
- High-Energy lepton collider has large flux of “partonic” W bosons



- gg collisions as usual



Electroweak phase transition



Singlet tree and loop makes $V(0,v)$ deeper

EW phase transition

DIRECT & INDIRECT

INTERPLAY

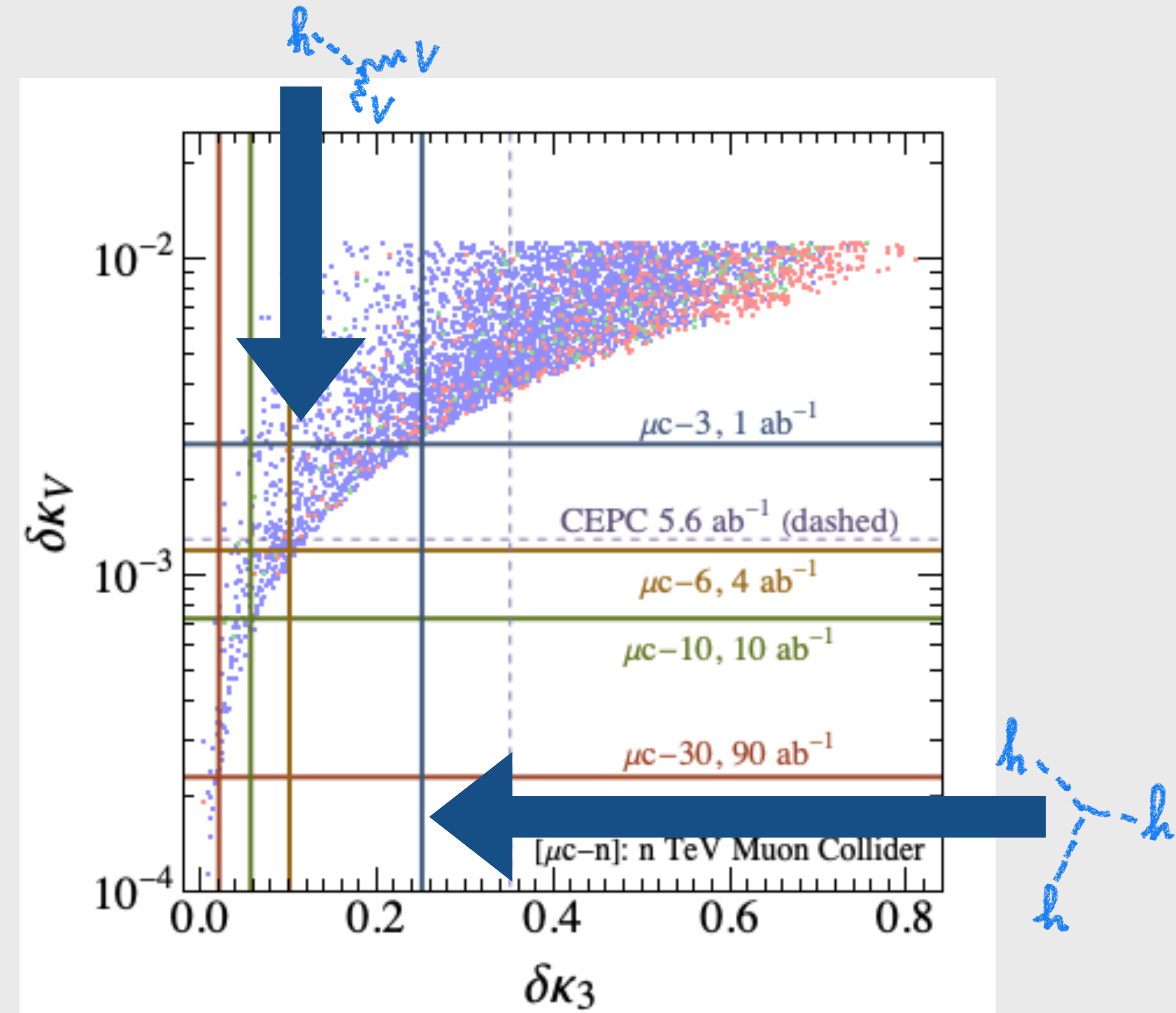
$$V(\Phi, S) = -\mu^2 (\Phi^\dagger \Phi) + \lambda (\Phi^\dagger \Phi)^2 + \frac{a_1}{2} (\Phi^\dagger \Phi) S + \frac{a_2}{2} (\Phi^\dagger \Phi) S^2 + b_1 S + \frac{b_2}{2} S^2 + \frac{b_3}{3} S^3 + \frac{b_4}{4} S^4.$$

independent parameters

$$\{M_{h_2}, \theta, v_s, b_3, b_4\}$$

strong First Order EW phase transition on all points

× ● ● → Gravity Wave SNR



EW phase transition

DIRECT & INDIRECT

INTERPLAY

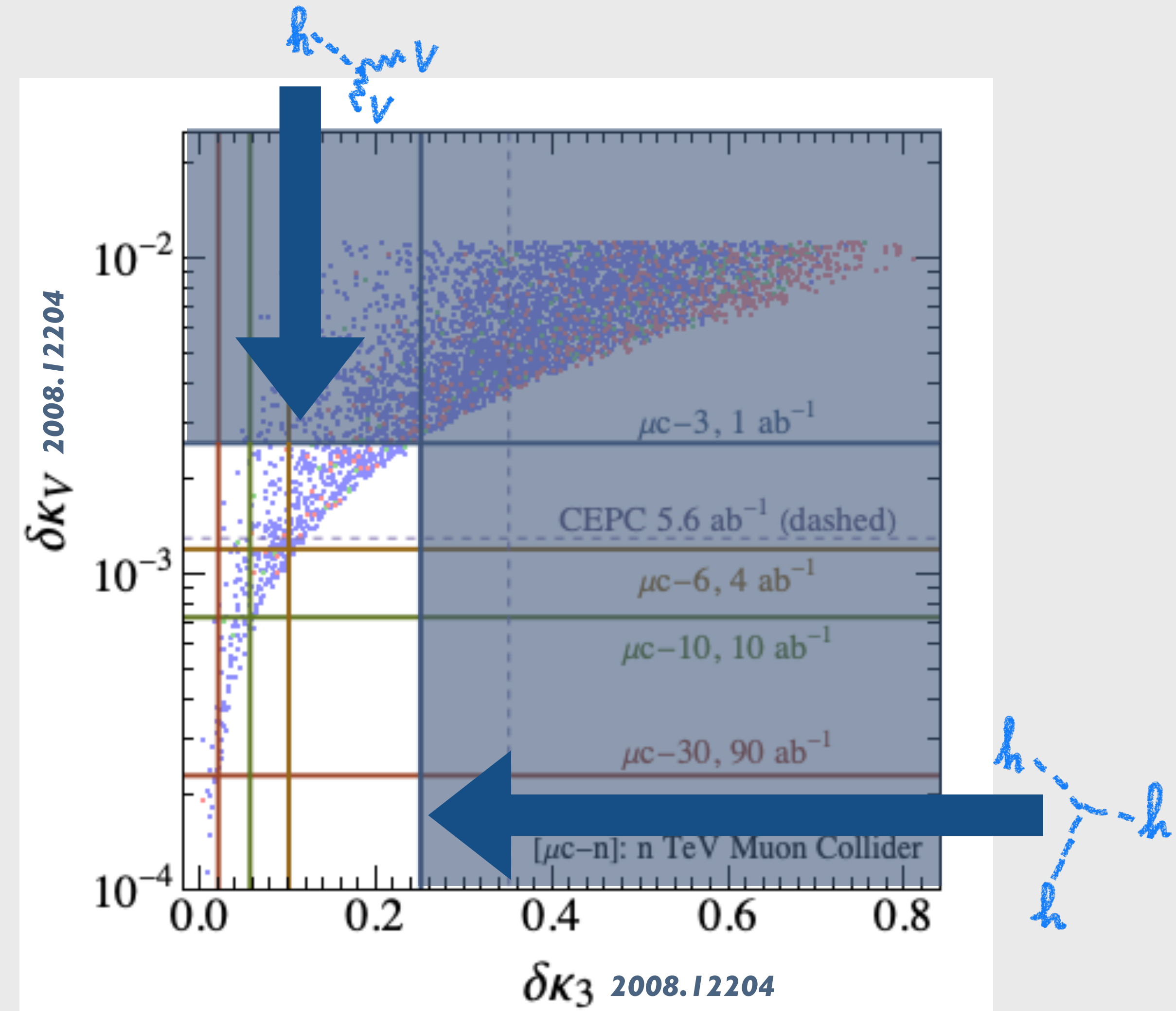
$$V(\Phi, S) = -\mu^2 (\Phi^\dagger \Phi) + \lambda (\Phi^\dagger \Phi)^2 + \frac{a_1}{2} (\Phi^\dagger \Phi) S + \frac{a_2}{2} (\Phi^\dagger \Phi) S^2 + b_1 S + \frac{b_2}{2} S^2 + \frac{b_3}{3} S^3 + \frac{b_4}{4} S^4.$$

independent parameters

$$\{M_{h_2}, \theta, v_s, b_3, b_4\}$$

strong First Order EW phase transition on all points

× ● ● → Gravity Wave SNR



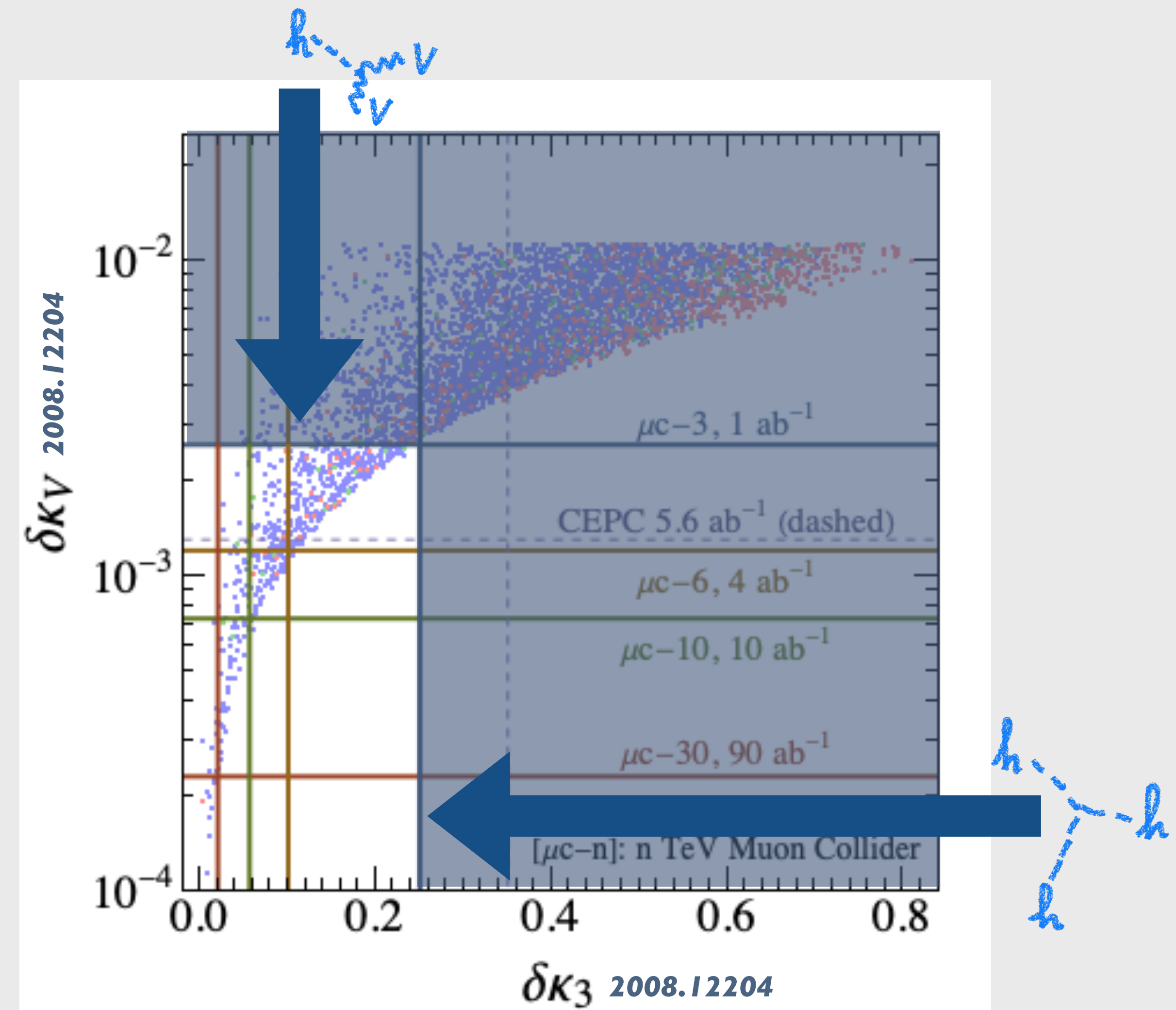
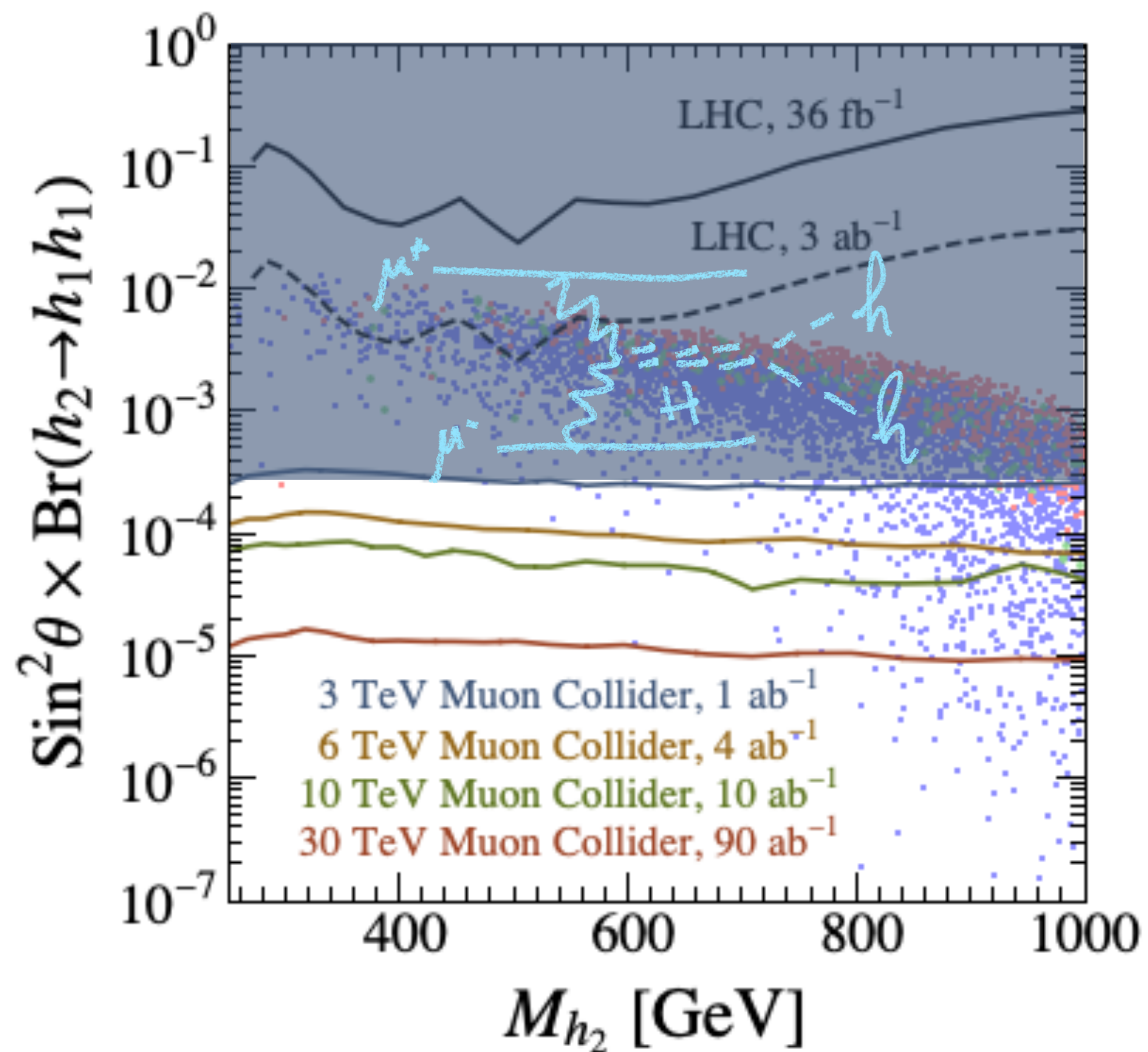
EW phase transition

strong First Order EW phase transition on all points

×
●
●
 → Gravity Wave SNR

DIRECT & INDIRECT

INTERPLAY



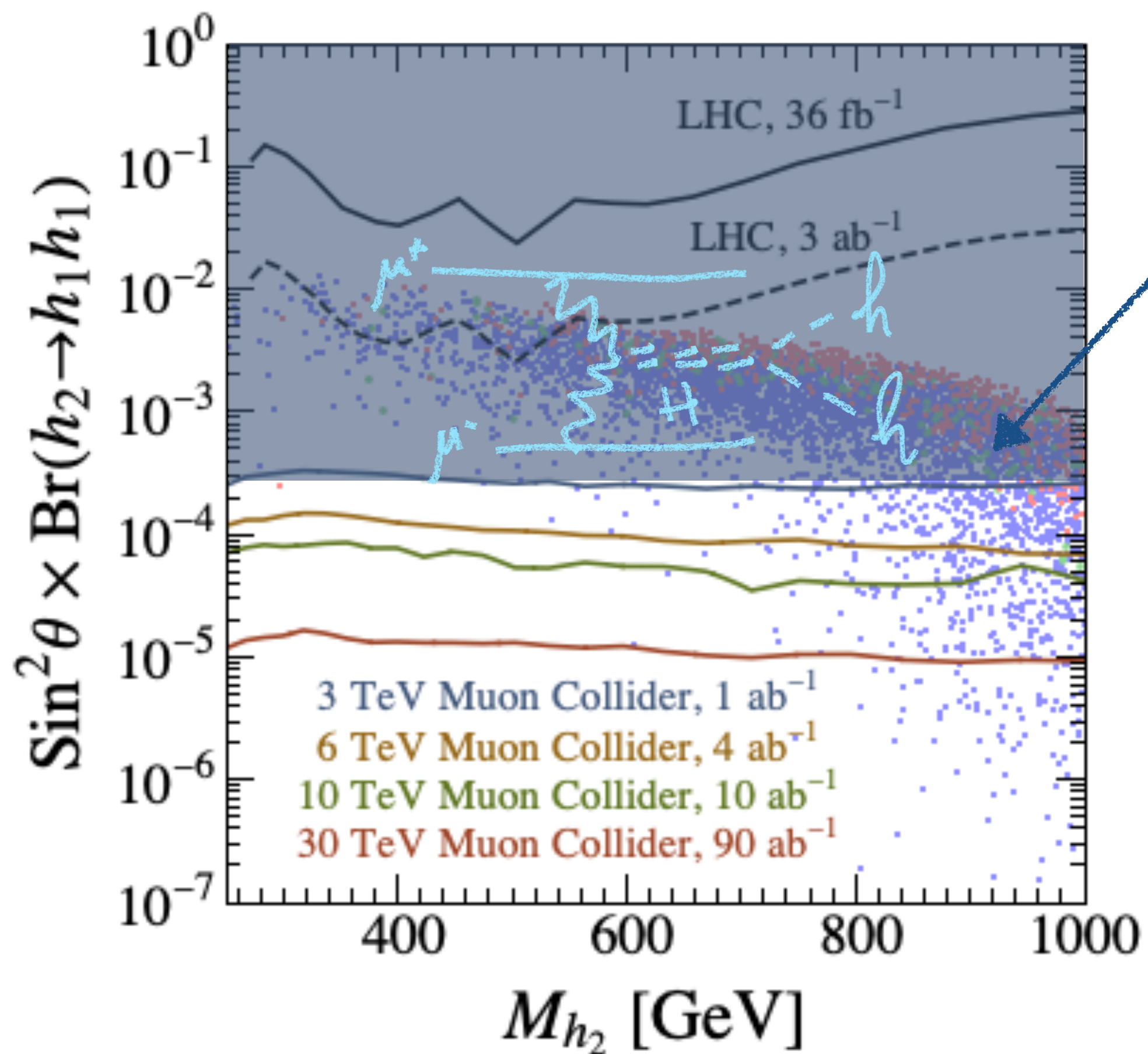
EW phase transition

strong First Order EW phase transition on all points

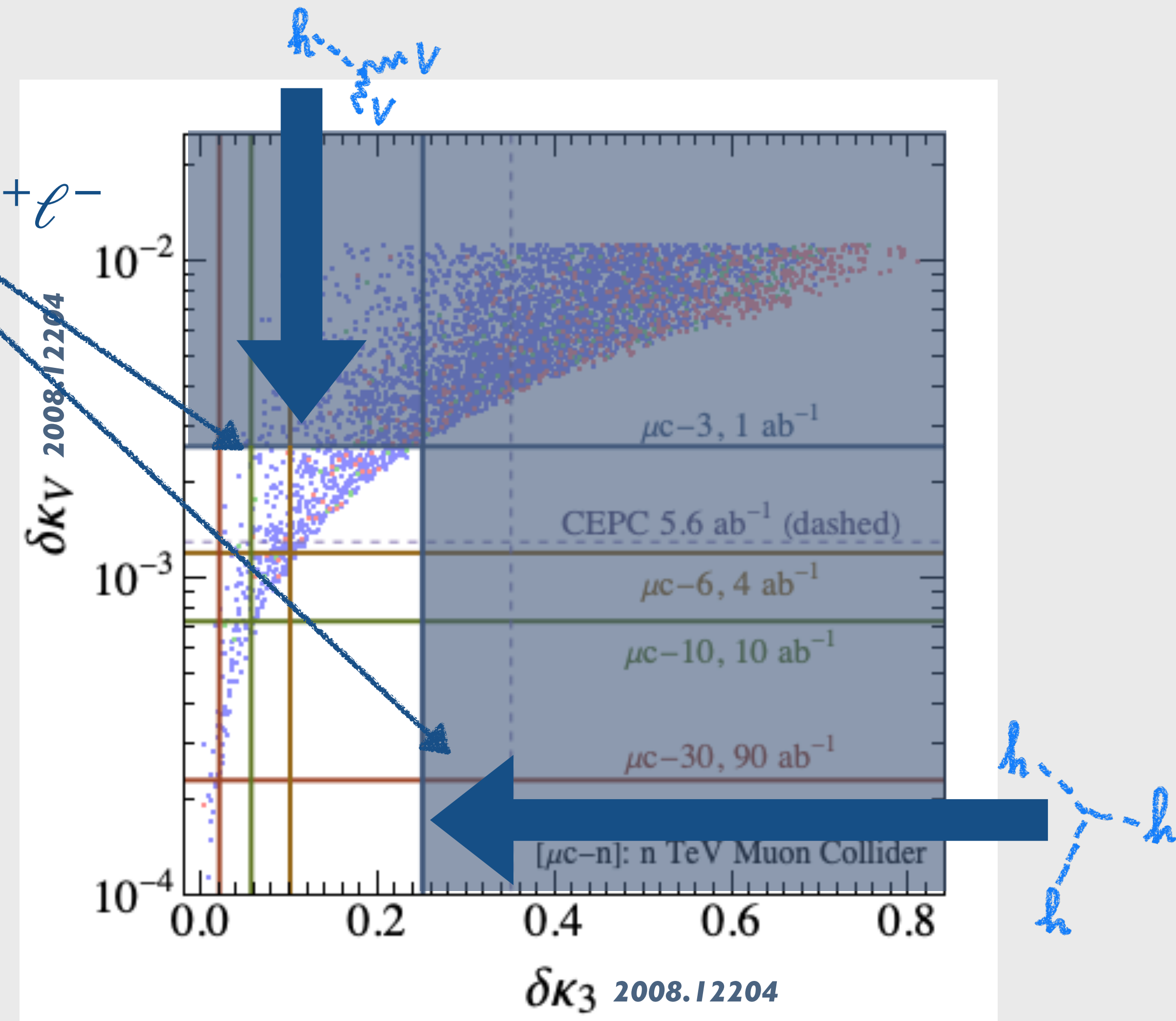
⊗ ⊙ ⊚ → Gravity Wave SNR

DIRECT & INDIRECT

INTERPLAY



3 TeV $\ell^+\ell^-$



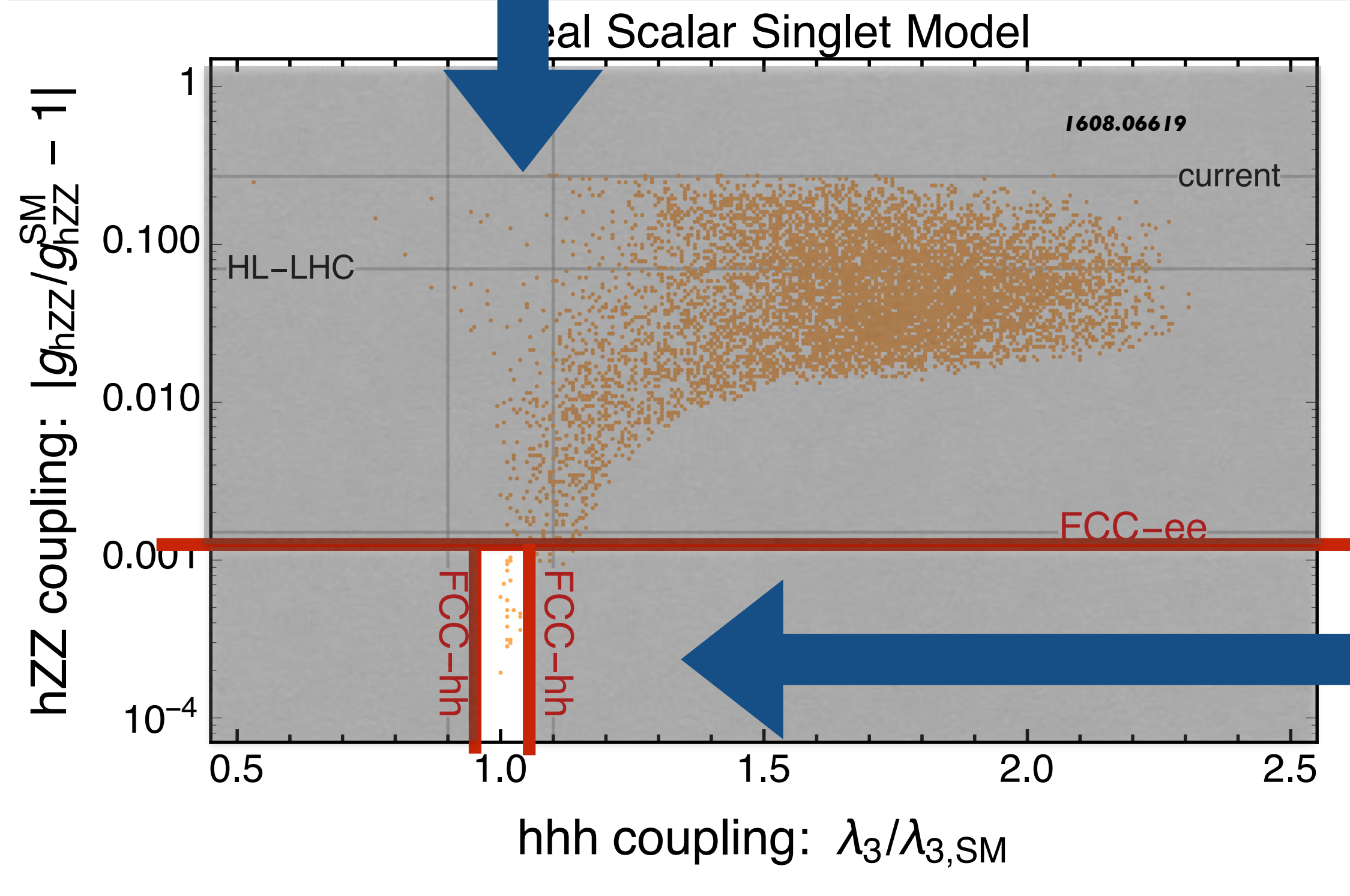
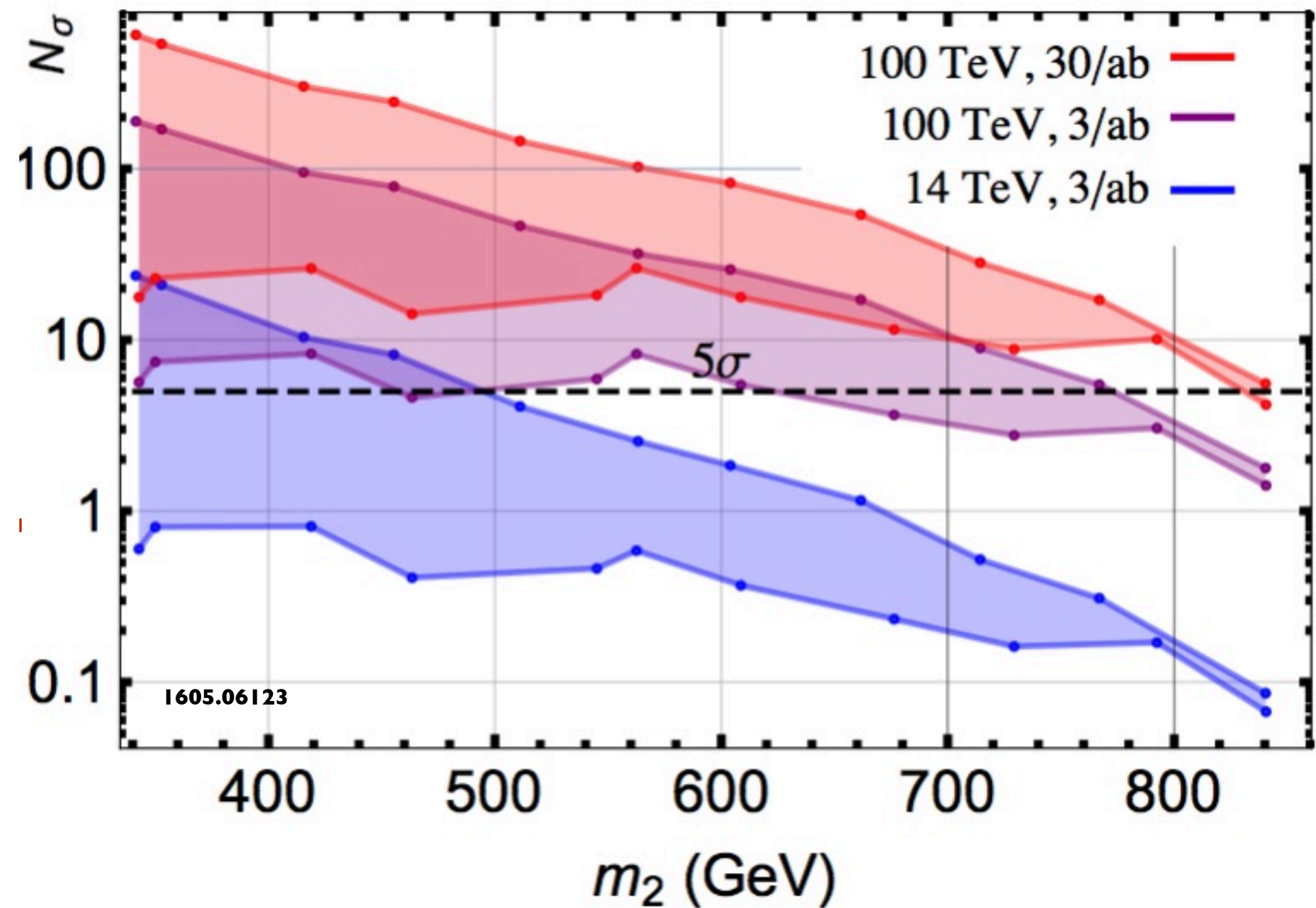
parameters space of 1st order phase transition accessible by **several measurements available at the 3 TeV $\ell^+\ell^-$ collider**

EW phase transition

DIRECT & INDIRECT

INTERPLAY

$$pp \rightarrow h_2 \rightarrow h^{(125)} h^{(125)}$$



h₂ → h⁽¹²⁵⁾ h⁽¹²⁵⁾

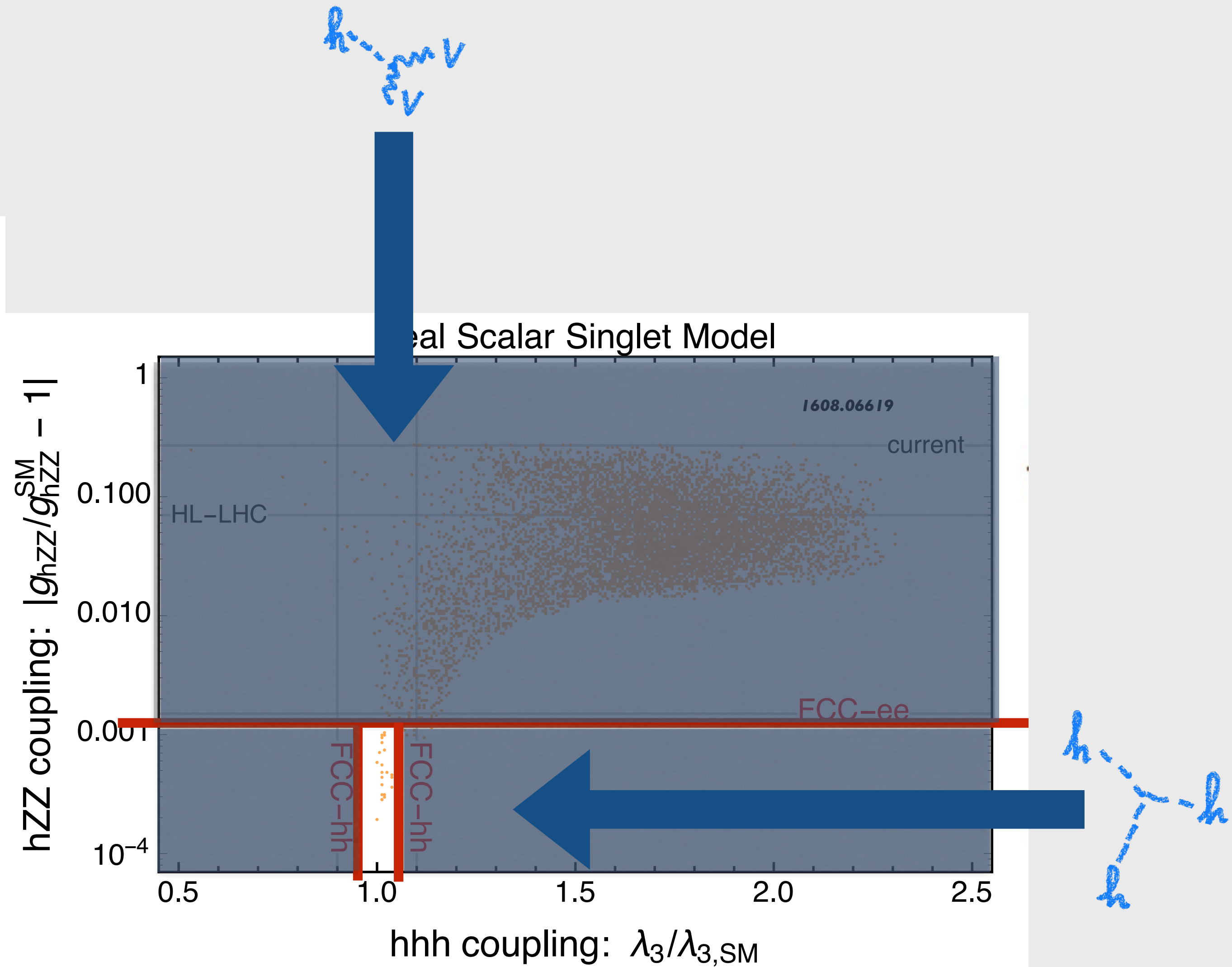
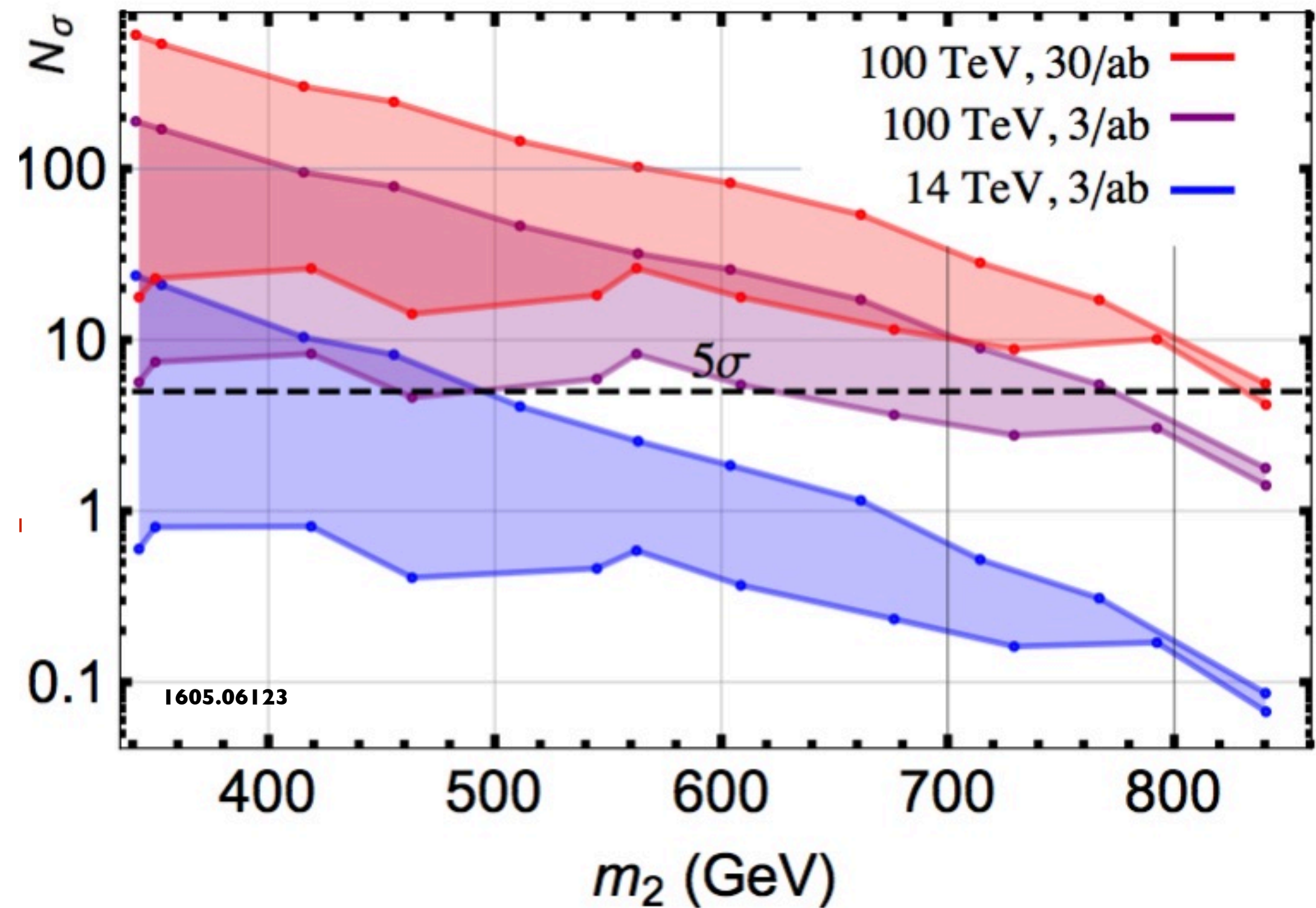
h-h-h

EW phase transition

DIRECT & INDIRECT

INTERPLAY

$$pp \rightarrow h_2 \rightarrow h^{(125)} h^{(125)}$$

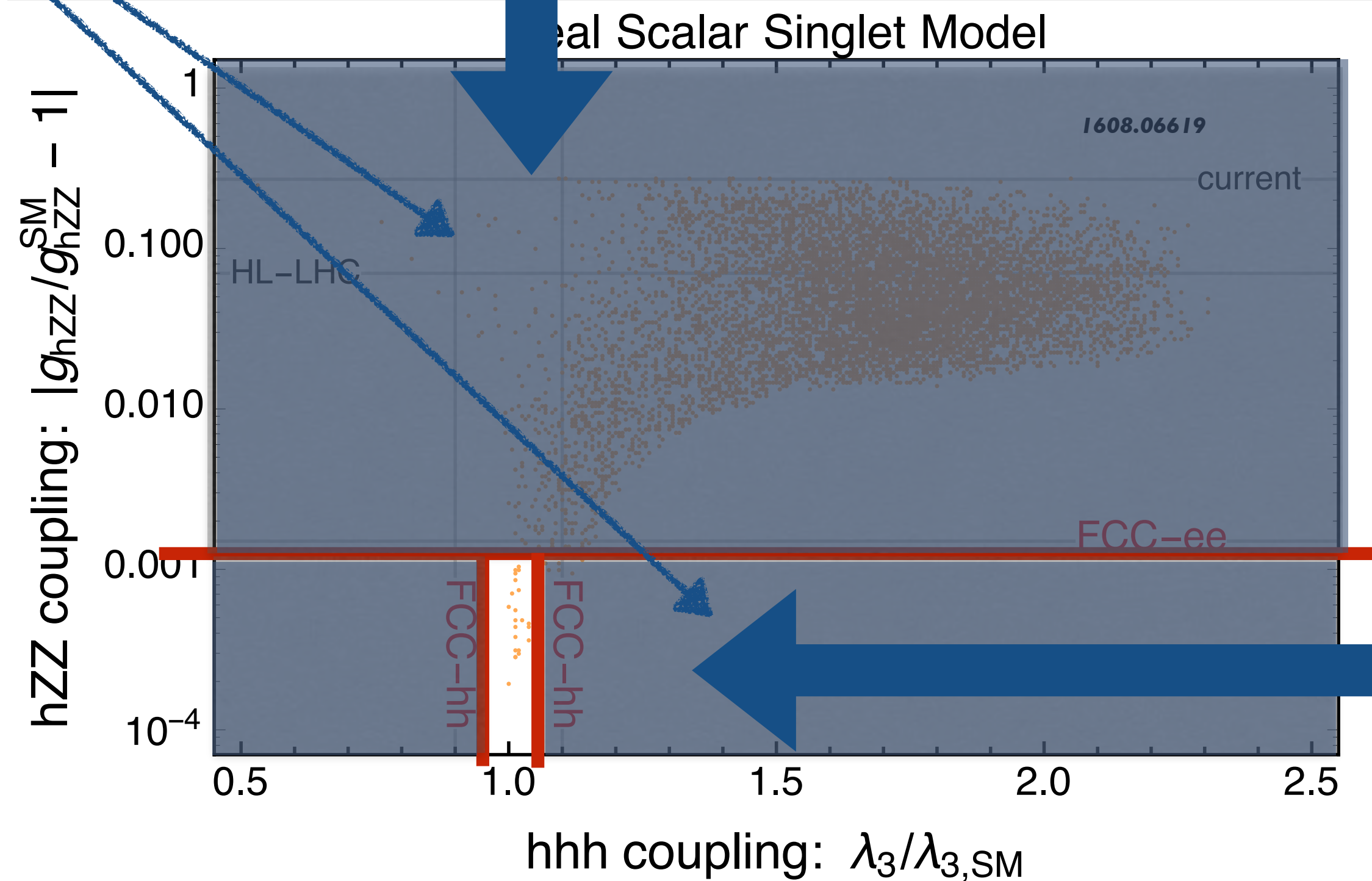
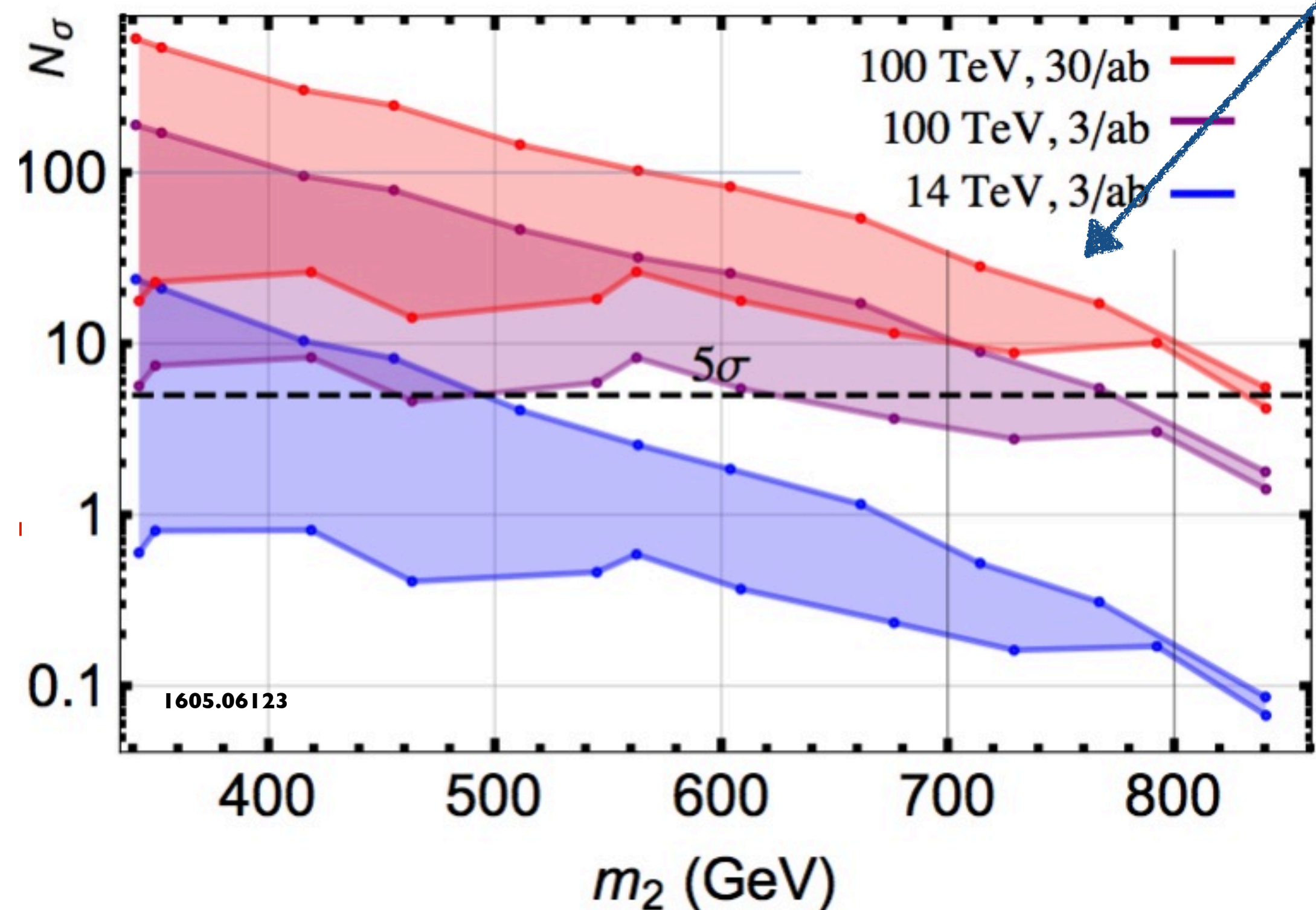


EW phase transition

DIRECT & INDIRECT

INTERPLAY

$$pp \rightarrow h_2 \rightarrow h^{(125)} h^{(125)} \quad 100 \text{ TeV } pp$$



parameters space of 1st order phase transition accessible by **several measurements available at the 100 TeV pp collider**