

**ARTIMENTO** DI FISICA E GEOLOGIA DIPARTIMENTO DI ECCELLENZA



# Latest measurements of DPS using Quarkonia from all experiments (pp)

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*v 2 is the typical velocity of a heavy quark in the quarkonium rest frame*

## Quarkonia production

Quarkonium specifically refers to mesons composed of a heavy quark and its antiquark: charm-anticharm ( $\overline{c}\overline{c}$ ) or bottom-antibottom ( $\overline{bb}$ ) mesons.

- In heavy quarkonia each quark has mass m much larger than the QCD confinement scale ΛQCD → **Non-relativistic QCD**.
- Because the system is nonrelativistic, quarkonium is characterized:
	- by the heavy-quark bound-state velocity, v<<1 ( $v^2$  ~ 0.3 for charmonia,  $v^2 \sim 0.1$  for bottomia)
	- by a hierarchy of energy scales: the mass m (hard scale, H), the relative momentum p ∼ mv (soft scale, S), a and the binding energy E ∼ mv2 (ultrasoft scale, US).



[Rev.Mod.Phys.90\(2018\)015003](https://journals.aps.org/rmp/abstract/10.1103/RevModPhys.90.015003)

[Eur.Phys.J.C.71\(2011\)1534](https://link.springer.com/article/10.1140/epjc/s10052-010-1534-9)

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## Quarkonia production @ LHC







**Prompt hadron production:**

*prompt* indicates that these hadrons are created almost instantly during the interaction

**Decays of higher resonances (feed-down):**

involve the subsequent decay of higher-energy resonant states into lower-energy particles.

**Production in b-hadron decays / non-prompt (only charmonium)**

refers to the generation of charmonium states within the decay of beauty (b) hadrons.

#### SPS and DPS

#### SPS DPS DPS



- Single-Parton Scattering (SPS) involves the production of two or more particles through a single interaction between two partons.
- The kinematics are correlated, with the neglect of additional gluon emissions.



- Double-Parton Scattering (DPS) involves the production of two particles through a double interaction between two partons from the same proton pairs.
- To simplify, the hard scattering are assumed as uncorrelated.
- Described by the pocket formula:

$$
\sigma_{DPS}^{pp\rightarrow A,B}=\left(\frac{m}{2!}\right)\frac{\sigma_{SPS}^{pp\rightarrow A}\cdot\sigma_{SPS}^{pp\rightarrow B}}{\sigma_{\text{eff},DPS}}
$$



# News from LHCb at  $\sqrt{s}$  = 13 TeV

[Valeriia ZHOVKOVSKA's slide](https://indico.cern.ch/event/1258750/contributions/5606394/attachments/2740520/4768343/Charmonia_Zhovkovska.pdf)



 $\frac{3}{2}$ 

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- J/ψ + Y(nS) production: [JHEP 08 \(2023\) 093](https://doi.org/10.1007/JHEP08(2023)093)
	- integrated and differential (for Y(1S)) cross-section
	- effective cross-section σ<sub>eff</sub>



- integrated and differential cross-section
- production asymmetry
- effective cross-section
- $\bullet$  J/ $\psi$  +  $\psi$ (2S) production: [LHCb-PAPER-2023-023](https://cds.cern.ch/record/2866823/files/LHCb-PAPER-2023-023.pdf), in preparation
	- integrated and differential cross-section
	- ratio to  $J/\psi + J/\psi$

#### $V_s = 13$  TeV

[JHEP 08 \(2023\) 093](https://doi.org/10.1007/JHEP08(2023)093)

#### Associated production of prompt J/ $\Psi$  and  $\Upsilon$  mesons

**Theoretical cross section: Production cross section:**

 $\sigma_{\rm DPS}(J/\psi\text{-}\mathcal{T}) = \frac{\sigma(J/\psi)\times\sigma(\mathcal{T})}{\sigma_{\rm eff}},$ 

 $\sigma(J/\psi\text{-}\varUpsilon)=\frac{N_\text{cor}}{\mathcal{L}\times\mathcal{B}_{J/\psi\to\mu^+\mu^-}\times\mathcal{B}_{\varUpsilon\to\mu^+\mu^-}}.$ 

 $\mathcal{L} = 4.18 \pm 0.08$  fb<sup>-1</sup>

where the  $J/\psi(Y(1S))$  has:  $p_{\rm T}$  < 10 (30) GeV/c

in rapidity range:  $2.0 < y < 4.5$ 



The raw yields from the fit, the efficiency-corrected yields (Ncor) and the signal significances:





J/



 $\mathbf{\Upsilon}$ 

#### $V = 13$  TeV

## Associated production of prompt J/ $\Psi$  and  $\Upsilon$  mesons











[JHEP 08 \(2023\) 093](https://doi.org/10.1007/JHEP08(2023)093)

### Associated production of prompt JI $\Psi$  and  $\Upsilon$  mesons

Integrated cross-sections:

#### LHCb

 $\sigma(J/\psi \text{-}\Upsilon(1S)) = 133 \pm 22 \pm 7 \pm 3 \,\text{pb}$ 

 $\sigma(J/\psi \text{-}\Upsilon(2S)) = 76 \pm 21 \pm 4 \pm 7 \text{ pb}$ 

ratio of the cross-sections of  $J/\psi$ -Y(2S) and  $J/\psi$ -Y(1S) multiplied by the respective branching ratio is calculated to be:

 $\frac{\mathcal{B}_{\Upsilon(2S)\to\mu^+\mu^-}\times\sigma(J/\psi\text{-}\Upsilon(2S))}{\mathcal{B}_{\Upsilon(1S)\to\mu^+\mu^-}\times\sigma(J/\psi\text{-}\Upsilon(1S))}=0.442\pm0.143\pm0.004$ 

Results are consistent with both DPS and SPS+DPS mechanisms present.

#### Associated production is predicted to be dominated by the DPS process.



#### $\sqrt{s}$  = 13 TeV

## Associated production of prompt J/4 and  $\Upsilon$  mesons

[JHEP 08 \(2023\) 093](https://doi.org/10.1007/JHEP08(2023)093)

DPS contribution is extracted using SPS prediction from Shao and Zhang [[Phys. Rev. Lett. 117, 062001\]](https://doi.org/10.1103/PhysRevLett.117.062001).

This allows us to extract the effective cross sections:

$$
\sigma_{eff} = \frac{\sigma_{J/\psi} \times \sigma_{\Upsilon(1S)}}{\sigma_{J/\psi-\Upsilon(1S)}^{DPS}} = 26 \pm 14_{stat} \pm 2_{syst} \frac{+22_{sps}}{-3_{sps}} \text{ mb}
$$

$$
\sigma_{eff} = \frac{\sigma_{J/\psi} \times \sigma_{\Upsilon(2S)}}{\sigma_{J/\psi-\Upsilon(2S)}^{DPS}} = 14 \pm 5_{stat} \pm 1_{syst} \frac{+7_{sps}}{-1_{sps}} \text{ mb}
$$

More data needed to extract SPS to test Colour-Singlet and Colour-Octet contributions

LHCb



#### $V$ s = 13 TeV

#### Production of J/4 + J/4: where were we?



New resonances:

- 2 models (non interference background and interference background) have been used.
- Both are **consistent with a peak around 6.9 GeV** exceeding 5σ.
- $\bullet$  decay into J/ $\psi$  +  $\psi$ (2S) has been considered showing a resonance near 6.9 GeV with 4.7σ.



 [arXiv:2306.07164v1](https://arxiv.org/pdf/2306.07164.pdf)

New resonances:

- $6552 \pm 10$  (stat)  $\pm$  12 (syst) MeV (6.5σ).
- 6927  $\pm$  9 (stat)  $\pm$  4 (syst) MeV (9.4σ), *consistent with the X(6900).*
- **•**  $7287^{+20}_{-18}$ (stat)  $\pm$  5 (syst) MeV (4.1 $\sigma$ ).
- both non interference and interference background models consistent



M. E. Ascioti - Latest measurements of DPS using Quarkonia from all experiments (pp) - Manchester, 20 November 2023



New resonance:

- with the first model (no interference with Non -Resonant SPS):  $m[X(6900)] = 6905 \pm 11 \pm 7 \text{ MeV}/c^2$ .
- with the second model (interference with NRSPS): m[*X(6900)*]= 6886 ±11 ±11 MeV/c<sup>2</sup>;



Production of J/ $\Psi$  + J/ $\Psi$ : can we learn something about DPS here?  $V_s = 13$  TeV

ATLAS CMS LHCb [Phys. Rev. Lett. 131 \(2023\) 151902](https://journals.aps.org/prl/abstract/10.1103/PhysRevLett.131.151902)

Background dominated from SPS in both the final states:  $J/\psi J/\psi$  and  $J/\psi + \psi(2S)$ .

DPS contribution maybe more present in J/ψ + ψ(2S)?

 $+$  Data

 $X(6900)$ 

 $350 - ATLAS$ 

Here the DPS is a background but we learned that:

- the NR-SPS contribution is expected to dominate the DPS contribution near the J/ψJ/ψ threshold
- the DPS contribution is dominating at masses above 11 GeV.

**CMS** Supplementar

[LHCb-PAPER-2023-022](https://cds.cern.ch/record/2866822/files/LHCb-PAPER-2023-022.pdf)  [arXiv:2306.07164v1](https://arxiv.org/pdf/2306.07164.pdf) [Valeriia ZHOVKOVSKA's slide](https://indico.cern.ch/event/1258750/contributions/5606394/attachments/2740520/4768343/Charmonia_Zhovkovska.pdf)<sup>s</sup>

We expect to learn something about:

- small SPS Color-Octet contributions
- DPS contribution is important at large  $J/\psi$ Δy
- test gluon Transverse Momentum Dependent parton distribution functions (TMDs)





 $ADLATLAS$ 

 $\sqrt{s}$  = 13 TeV 140 fb<sup>-1</sup>

s<sub>ps</sub>

LHCb preliminary

 $4.2$  fb

 $+$  sps+DPS

**No SPS** 

2.5

 $+$  DPS

 $+$ sps

#### Production of J/ $\Psi$  + J/ $\Psi$ : can we learn something about DPS here?  $V_s = 13$  TeV

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Background dominated from SPS in both the final states:  $J/\psi J/\psi$  and  $J/\psi + \psi(2S)$ .

DPS contribution maybe more present in J/ψ + ψ(2S)?





#### Production of J/4 + J/4: can we learn something about DPS here?  $V_s = 13$  TeV

Ba**That seems a good** th the place to look for  $^{1028}$ . DP<sup>D</sup> compution maybe more present in  $J/\psi + \psi(2S)$ ?

SPOILER ALERT! Maybe you can hear some news about it soon... $\left( \infty \right)$ 

Here the DPS is a background but we learned that:

- the NRSPS contribution is expected to dominate the DPS contribution near the J/ψJ/ψ threshold
- the DPS contribution is dominating at masses above 11 GeV.





#### Production of J/ $\Psi$  + J/ $\Psi$ : can we learn something about DPS here?  $V$ s = 13 TeV



#### Production of J/ $\Psi$  + J/ $\Psi$ : can we learn something about DPS here?  $V_s = 13 TeV$

 $(a)$ 

$$
\sigma(\mathbf{J}/\psi\,\mathbf{J}/\psi) = \frac{N}{\mathscr{L}_{\mathrm{int}} \times \varepsilon \times B^2(\mathbf{J}/\psi \to \mu^+\mu^-)}
$$

 **Inclusive cross section:**

- inclusive:  $\sigma(J/\psi J/\psi) = 10.3 \pm 2.3$  (stat.)  $\pm 1.3$  (syst.) nb.
- prompt:  $\sigma_{\text{prompt}}(J/\psi J/\psi) = 7.3 \pm 1.7 \text{(stat.)}^{+1.9}_{-2.1} \text{(syst.)}$  nb  in  $2.5 < y < 4.0$  with

#### **Effective DPS cross-section:**

• inclusive: 
$$
\frac{1}{2} \frac{\sigma(\mathbf{J}/\boldsymbol{\psi})^2}{\sigma(\mathbf{J}/\boldsymbol{\psi}\mathbf{J}/\boldsymbol{\psi})} = 6.2 \pm 1.4 \text{ (stat.)} \pm 1.1 \text{ (syst.) mb.}
$$

$$
\bullet \qquad \text{prompt:} \qquad \frac{1}{2} \frac{\sigma_{\text{prompt}}(J/\psi)^2}{\sigma_{\text{prompt}}(J/\psi \, J/\psi)} = 6.7 \pm 1.6 \, (\text{stat.}) \pm 2.7 \, (\text{syst.}) \text{ mb}
$$



#### Production of J/ $\Psi$  + J/ $\Psi$ : can we learn something about DPS here?  $V_s = 13 TeV$

100 k

Production cross section:

\n
$$
\sigma(J/\psi J/\psi) = \frac{N}{\mathcal{L}_{int} \times \varepsilon \times B^2(J/\psi \to \mu^+ \mu^-)}
$$
\nat Xiv:2303.13431v

\n
$$
\sigma(J/\psi J/\psi) = \frac{N}{\mathcal{L}_{int} \times \varepsilon \times B^2(J/\psi \to \mu^+ \mu^-)}
$$

 **Inclusive cross section:**

#### measurement conducted by ALICE! inclusive: prompt: This is the first double quarkonium

in  $2.5 < y < 4.0$  with

**Effective DPS cross-section:**

inclusive:  $\frac{1}{2} \frac{\sigma (J/\psi)^2}{\sigma (J/\psi J/\psi)} = 6.2 \pm 1.4 \text{ (stat.)} \pm 1.1 \text{ (syst.) mb.}$ 

prompt:

$$
\frac{1}{2} \frac{\sigma_{\text{prompt}}(J/\psi)^2}{\sigma_{\text{prompt}}(J/\psi J/\psi)} = 6.7 \pm 1.6 \, (\text{stat.}) \pm 2.7 \, (\text{syst.}) \, \text{mb}
$$



24.11 pb-1

[arXiv:2303.13431v3](https://arxiv.org/pdf/2303.13431.pdf)

#### $V_s = 13 TeV$

[Valeriia ZHOVKOVSKA's slide](https://indico.cern.ch/event/1258750/contributions/5606394/attachments/2740520/4768343/Charmonia_Zhovkovska.pdf)

#### Associated production of prompt J/4 and 4(2S) mesons

Data sample:

$$
\mathcal{L} = 4.18 \pm 0.08 \text{ fb}^{-1}
$$

with:

$$
p_{\text{T}}^{J/\psi,\psi(2S)} < 14 \text{ GeV/c}
$$
 and  $2.0 < y^{J/\psi,\psi(2S)} < 4.5$ 

The integrated cross section is:

$$
\sigma_{J/\psi-\psi(2S)} = 4.49 \pm 0.71_{stat} \pm 0.26_{syst}
$$
 nb

Ratio between  $J/\psi + \psi(2S)$  and  $J/\psi + J/\psi$  production

$$
\mathcal{R} = \frac{\sigma_{J/\psi - \psi(2S)}}{\sigma_{J/\psi - J/\psi}} = 0.274 \pm 0.044_{stat} \pm 0.008_{syst} \frac{\mathcal{R}}{\mathcal{R}}
$$

**Consistent with DPS prediction + Measurements are consistent with NLO\* CS predictionfrom Lansberg and Shao [[Phys. Rev. Lett. 111, 122001](https://doi.org/10.1103/PhysRevLett.111.122001)]**



Future perspectives **3**

#### SPS and DPS and... TPS: the future is here!

#### [Nat. Phys. 19, 338–350 \(2023\)](https://www.nature.com/articles/s41567-022-01838-y#citeas)  $\sigma_{eff,IPS} = 0.82 \sigma_{eff,DFS} = 2.2 \text{ mb}$



Pocket formula for TPS:

$$
\sigma^\text{pp\to\psi_1\psi_2\psi_3+X}_\text{TPS} = \left(\frac{\mathfrak{m}}{3!}\right)\frac{\sigma^\text{pp\to\psi_1+X}_\text{SPS}\sigma^\text{pp\to\psi_2+X}_\text{SPS}\sigma^\text{pp\to\psi_3+X}_\text{SPS}}{\sigma^2_\text{eff,TPS}}
$$



m = 1, 3, or 6 (depending on whether all three, two, or none of the  $\psi_i$  states are identical).

Analyzing the whole RUNII ( $\mathcal{L}$  = 133 fb<sup>-1</sup>) **5 events** have been found. The expected contributions from SPS, DPS and **TPS** processes to the total triple-J/ψ cross-section amount to about 6%, 74% and **20%**, respectively.

The fiducial cross section is:

 $272^{+141}_{-104}$  (stat)  $\pm$  17 (syst) fb

*more on Hua Sheng's slides from yesterday*

## SPS and DPS and... TPS: the future is here!





#### Summary and conclusions



#### Take home message:

- Quarkonia have a lot to teach us about QCD.
- Especially for LHCb and CMS seem to be good chances to get important results on DPS using quarkonia.
- There is a lot work left to do:
	- $\circ$  more insights on the non-universality effective cross-section  $\sigma_{\rm eff}$ are needed.
	- probably a lot of interesting final states produced via DPS are waiting for us.

# Thanks for your time!

BACKUP

## Color octet and color singlet

- **Colour-singlet model (CS)**: intermediate QQ state is colourless and has the same JPC as the final-state quarkonium;
- **Colour-octet model (CO)** (encapsulated in NRQCD): all viable colours and JPC allowed for the intermediate QQ state;





#### The main characters (here)



#### ATLAS

- **Pseudorapidity Range:** ATLAS covers a broad pseudorapidity range, |η| < 4.9.
- **Tracking System:** tracking system comprising pixel detectors, semiconductor trackers, and transition radiation trackers. This setup enables precise tracking of charged particles, with momentum measurements characterized by a relative uncertainty typically ranging from 0.05% to 0.2%.
- **Particle Identification (PID):** Charged hadrons are identified through tracking information and calorimetry. Photons, electrons are distinguished using electromagnetic calorimeters. Muons are identified using dedicated muon spectrometer with multiple technologies such: Thin Gap Chambers, Resistive Plate Chambers, Monitored Drift Tubes, Small-Strip Thin-Gap Chambers and Micromegas.



- **Pseudorapidity Range:** CMS covers a wide pseudorapidity range of  $|n| < 5$ .
- **Tracking System:** the tracking system consisting of silicon detectors, both pixel and strip detectors particles. The relative uncertainty in momentum measurements typically ranges from 0.5% to 1.0%.
- **Particle Identification (PID):** charged hadrons are identified using tracking information and the energy deposited in the calorimeters. Photons, electrons, are identified and measured using electromagnetic calorimeters. Muons are identified through dedicated muon detectors composed of layers of iron and multiple detector technologies like Drift Tubes (DT), Cathode Strip Chambers (CSC), and Resistive Plate Chambers (RPC).

#### The main characters (here)





#### LHCb

- **Pseudorapidity Range:** ALICE focuses on covering -0.9 < η < 0.9. This range is optimized for studying heavy-ion collisions and quark-gluon plasma formation.
- **Tracking System:** Its main tracking system consists of Inner Tracking System (ITS) with high-resolution silicon detectors and a Time Projection Chamber (TPC).
- **• Particle Identification (PID):** it uses the ITS and TPC for tracking and identification of charged particles, while specific detectors like Time-Of-Flight (TOF) detectors and Transition Radiation Detectors (TRD) aid in distinguishing between different particle types such as pions, kaons, protons, and electrons.
- **Pseudorapidity Range:** LHCb is optimized for studying forward production in the pseudorapidity range of  $2 < n < 5$ .
- **Tracking System:** LHCb's tracking system includes a Vertex Locator (VELO), which is a silicon microstrip detector located very close to the collision point. Additionally, it utilizes a combination of silicon strip detectors and straw tubes that cover the entire spectrometer region.
- **Particle Identification (PID):** It utilizes Ring Imaging Cherenkov (RICH) detectors for identifying charged hadrons based on their velocity, electromagnetic and hadronic calorimeters for photons, electrons, and hadrons, and dedicated muon detectors, including Multi-Wire Proportional Chambers (MWPC) and scintillators, to identify muons.



#### Associated production of prompt J/ $\Psi$  and  $\Upsilon$  mesons



#### $V_s = 13$  TeV

#### Production of J/ $\Psi$  + J/ $\Psi$ : Model 1



In model 1, the X(6900) structure is considered as a resonance, whereas the threshold enhancement is described through a superposition of two resonances. The lineshapes of these resonances are described by S-wave relativistic BW functions multiplied by a two-body phase-space distribution.

The mass, natural width and yield are determined to be:

$$
m[X(6900)]=6905\pm11\,\, {\rm MeV}\, / {c^2}, \Gamma[X(6900)]=80\pm19\,\, {\rm MeV}
$$





#### Production of J/4 + J/4: Model 2

LHCb [SB.65\(2020\)23,1983-1993](https://www.sciencedirect.com/science/article/pii/S2095927320305685?via%3Dihub)

Model 2, allows for interference between the NRSPS component and a resonance for the threshold enhancement. The coherent sum of the two components is defined as:

$$
\left| A {\rm e}^{{\rm i} \phi} \sqrt{f_{\rm nr}\left(M_{{\rm di}\text{-}{J/\psi}}\right)} + {\rm BW}\big(M_{{\rm di}\text{-}{J/\psi}}\big) \right|^2
$$

where A and  $\phi$  are the magnitude and phase of the nonresonant component, relative to the BW lineshape for the resonance, assumed to be independent of di-J/ $\psi$  mass, and  $f_{\text{nr}}(M_{di-J/\psi})$  is an exponential function. The interference term is then added incoherently to the BW function describing the X(96000) structure and the DPS description.

In this case:

$$
m[X(6900)]=6886\pm11\,\, {\rm MeV}\, / {c^2}\,\, ,\Gamma[X(6900)]=168\pm33\,\, {\rm MeV}
$$



#### $\sqrt{s}$  = 13 TeV

### Production of J/4 + J/4: early measurements

#### **DPS** here was already expected: [arXiv:1612.07451](https://arxiv.org/pdf/1612.07451.pdf)

LHCb

The J/ $\psi$  pair production **cross-section** with both J/ $\psi$  mesons in the region 2.0 < y < 4.5 and pT < 10 GeV/c is measured to be **15.2±1.0 (stat)±0.9 (syst) nb**, using pp collision data collected by LHCb at  $\sqrt{s}$  = 13 TeV, corresponding to an integrated luminosity of 279 pb<sup>-1</sup>.

A fit to the differential cross-sections using simple DPS plus SPS models **indicates a significant DPS contribution**. The data can be reasonably well described with a sum of DPS and SPS colour-singlet contributions, with no evidence for a large SPS colour-octet contribution.

A large DPS contribution results in values of **σ<sub>eff</sub> that are smaller than the values of σ<sub>eff</sub> measured previously by the LHCb collaboration in the processes of multiple associated heavy quark production**, and slightly larger than those measured from central J/ψ pair production at the CMS and ATLAS experiments.



#### Production of J/ $\Psi$  + J/ $\Psi$ : can we learn something about DPS here?  $V = 13$  TeV

 $\sigma_{\text{non-prompt}}(J/\psi J/\psi) = 2.97 \pm 0.09 \, (\text{stat.})_{-0.76}^{+0.68} (\text{syst.})$  nb



 $\sigma_{\text{prompt}}(J/\psi J/\psi) = \sigma(J/\psi J/\psi) - \sigma_{\text{non-normal}}(J/\psi J/\psi) = 7.3 \pm 1.7 \text{(stat.)}^{+1.9}_{-2.1} \text{(syst.)}$  nb

 $\sigma_{\text{non-prompt}}(J/\psi) = 2 \times \sigma_{\text{L}\bar{\text{L}}}^{\text{total}} \times \beta \times B(h_b \to J/\psi + X) = 1.41 \pm 0.04 \text{ (stat.)} \pm 0.19 \text{ (syst.)} \mu b$  $\sigma_{\text{prompt}}(J/\psi) = \sigma(J/\psi) - \sigma_{\text{non-prompt}}(J/\psi) = 9.89 \pm 0.32 \text{(stat.)}^{+1.47}_{-1.48} \text{(syst.)} \mu\text{b}$ 

$$
\frac{\sigma_{\text{prompt}}(J/\psi \, J/\psi)}{\sigma_{\text{prompt}}(J/\psi)} = (7.4 \pm 1.7 \, (\text{stat.}) \pm 2.2 \, (\text{syst.})) \times 10^{-4}
$$