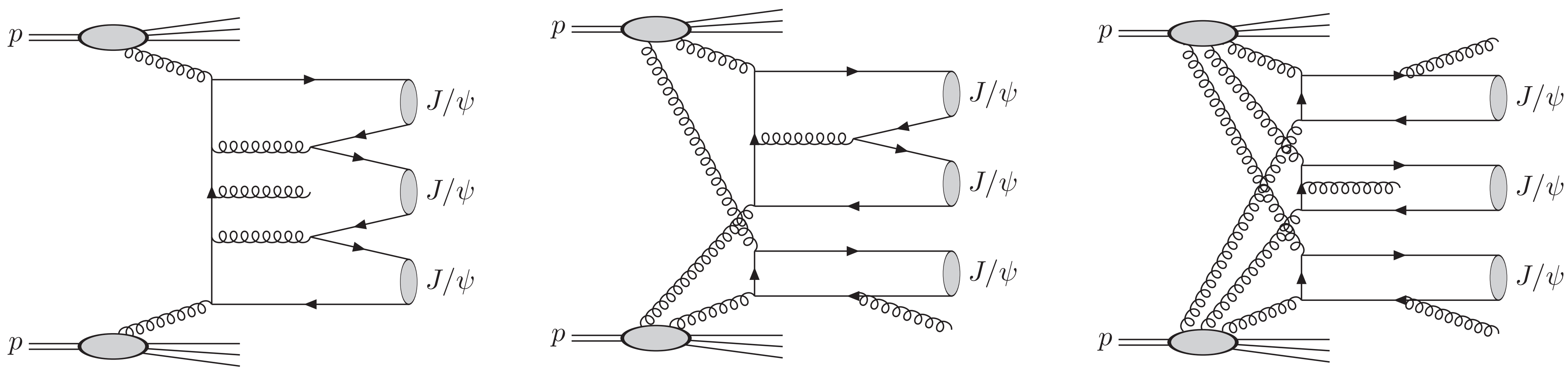
TPS in pp and DPS in pA



Hua-Sheng Shao

LPTHE
LABORATOIRE DE PHYSIQUE THEORIQUE ET HAUTES ENERGIES

SORBONNE UNIVERSITÉ
CRÉATEURS DE FUTURS DEPUIS 1257

MPI@LHC 2023, Manchester

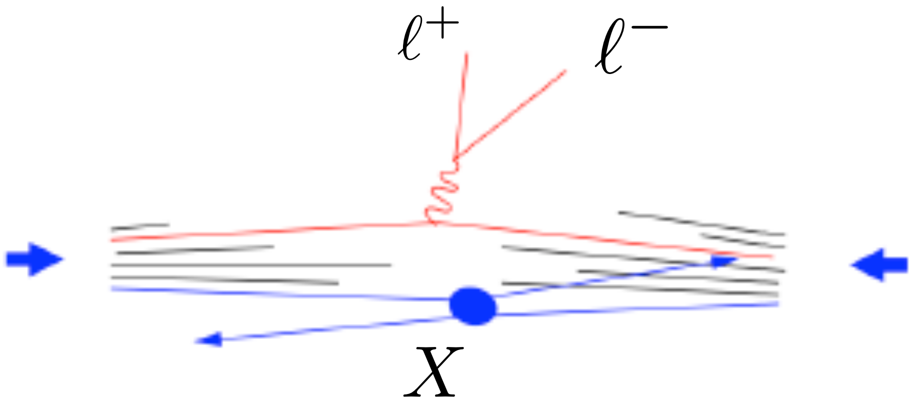
20 November 2023

A Brief Introduction

- **Cross section from factorization theorem (conjecture)**

$$\text{cross section} = \text{parton distribution} \times \text{partonic cross section}$$

- **Spectator-spectator interactions**
  - cancel in inclusive cross sections (unitarity)
  - affect final state X



- **Additional interaction (blue) will be sensitive if we probe X simultaneously**
- **If the second interaction is also hard** → **Double Parton Scattering**

e.g. $pp \to Z + H + X \to l\bar{l} + b\bar{b} + X$

- **DPS contributes to signals and to backgrounds in many analyses at the LHC**
- **Inclusive cross section:**

$$\sigma_{\rm SPS} \sim \frac{1}{Q^2} \quad \text{v.s.} \quad \sigma_{\rm DPS} \sim \frac{\Lambda^2_{\rm QCD}}{Q^4}$$

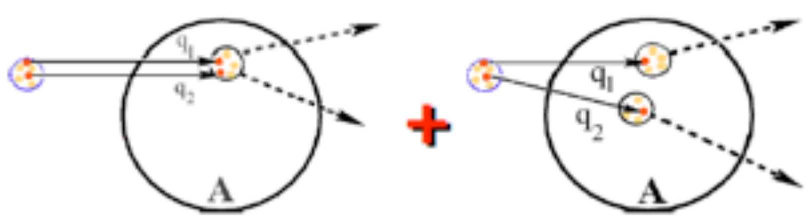
- **Higher energy** ⇨ **Larger parton density** ⇨ **enhance DPS**

$$\sigma_{\rm SPS} \propto (\text{parton density})^2 \quad \text{v.s.} \quad \sigma_{\rm DPS} \propto (\text{parton density})^4$$

A Brief Introduction

- **How to probe DPS at the LHC ?**
  - **Processes of low hard scale Q (but still in the perturbative regime)**
    - multiple hadron production, e.g. $J/\psi + J/\psi$
  - **Processes of large yields**
    - multi-jet production
  - **Processes of precision measurements**
    - multi-lepton production
  - **Special phase space regimes**
  - **Enhancement of parton luminosities**
    - higher energy [8 TeV to 14 TeV to 100 TeV (FCC-hh/SppC)]
    - probe in proton-nucleus and nucleus-nucleus collisions

[Strikman, Treleani (2002); D. d'Enterria, A. Snigirev (2013, 2014)]



$$\sigma_{\rm eff,pp}/\sigma_{\rm eff,pA} \approx 3\,A \approx 600$$

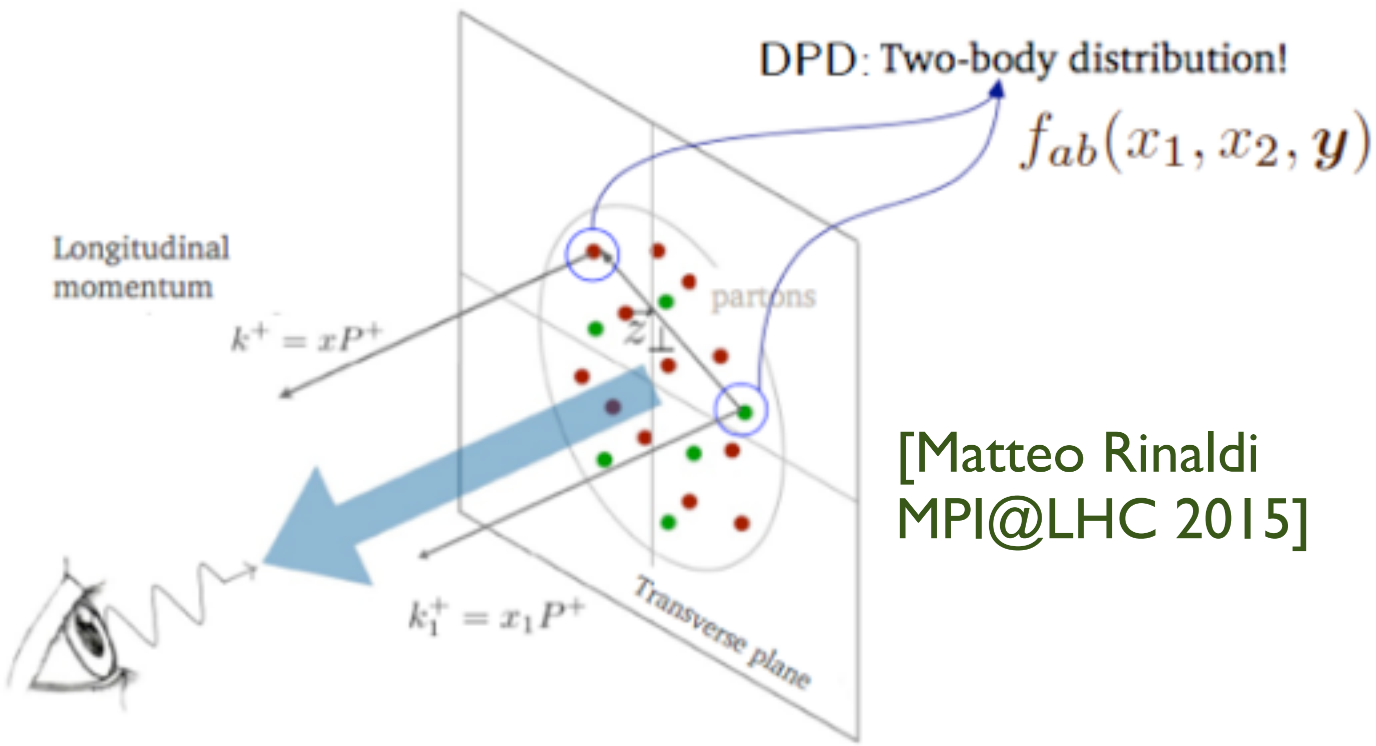
$$\sigma_{\rm eff,pp}/\sigma_{\rm eff,AA} \propto A^{3.3}/5 \simeq 9 \cdot 10^6$$

A DPS Theory Foundation

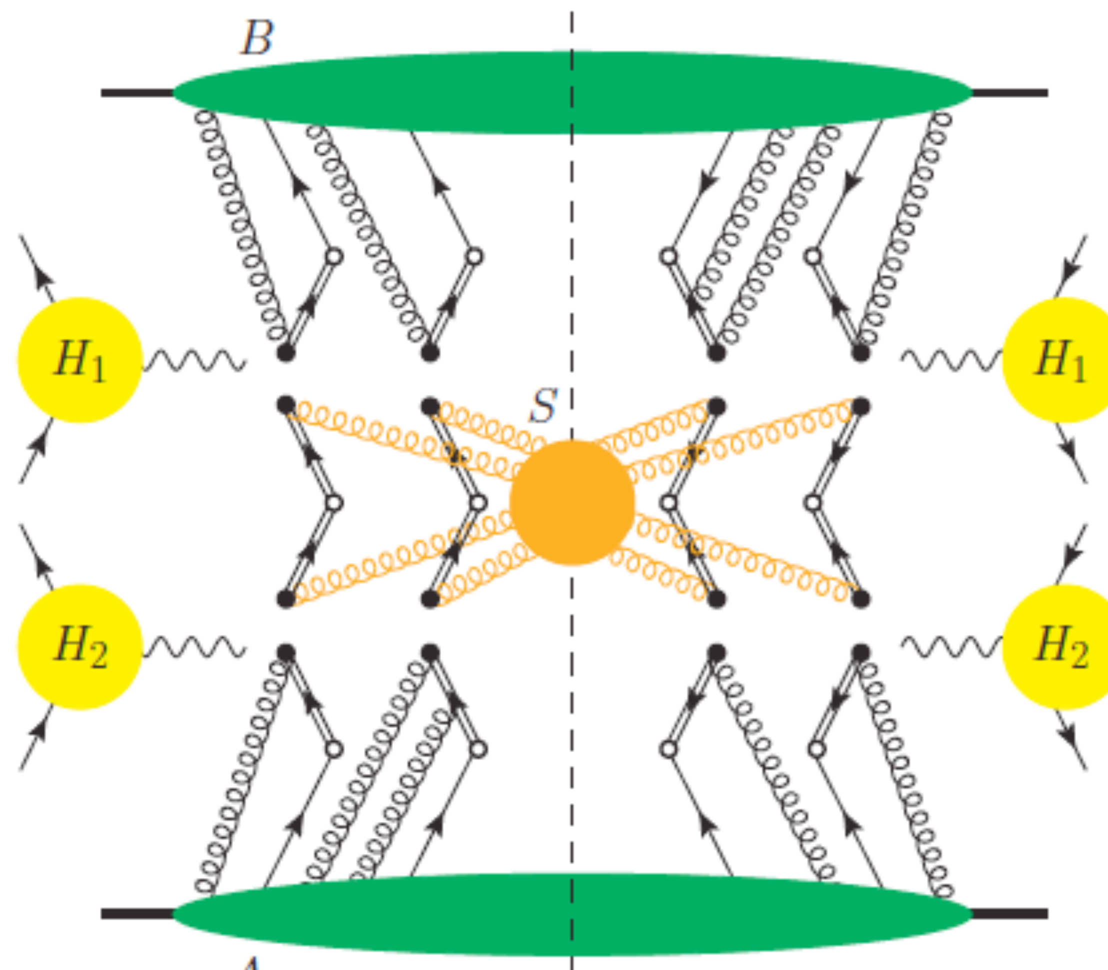
- **Like SPS, we now have a first proven factorisation theorem for DPS (double Drell-Yan)**

[Diehl, Gaunt, Ostermeier, Ploessl, Schafer (2015); Diehl, Nagar (2018)]

$$\sigma_{Q_1Q_2} = \frac{1}{1+\delta_{Q_1Q_2}} \sum_{i,j,k,l} \int dx_1 dx_2 dx_1' dx_2' d^2\mathbf{b}_1 d^2\mathbf{b}_2 d^2\mathbf{b}$$
$$\times \Gamma_{ij}(x_1, x_2, \mathbf{b}_1, \mathbf{b}_2)\, \hat{\sigma}_{ik}^{Q_1}(x_1, x_1')\, \hat{\sigma}_{jl}^{Q_2}(x_2, x_2')\, \Gamma_{kl}(x_1', x_2', \mathbf{b}_1 - \mathbf{b}, \mathbf{b}_2 - \mathbf{b}),$$



[Matteo Rinaldi MPI@LHC 2015]



A NEW WAY TO ACCESS THE INFORMATION OF THE NONPERTURBATIVE STRUCTURE OF NUCLEONS

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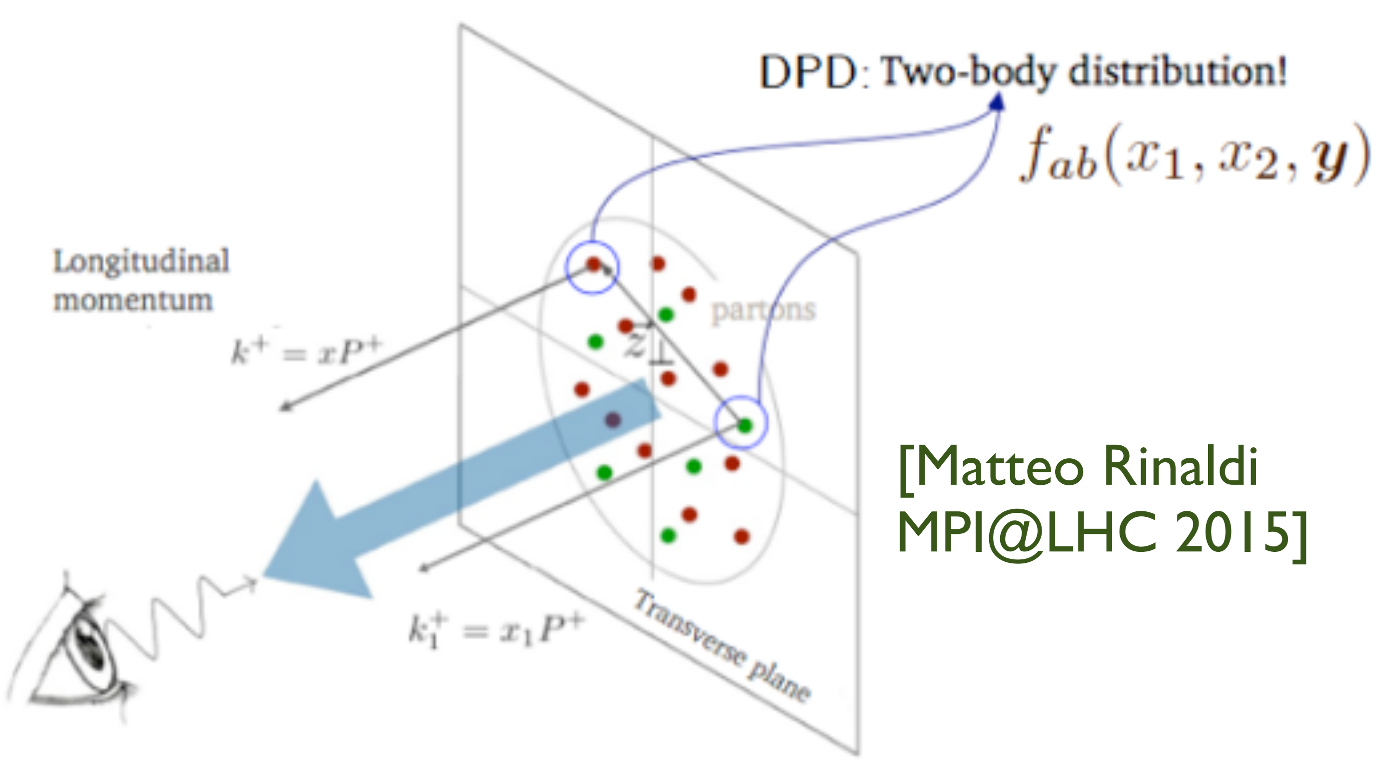
Generalised double parton distribution



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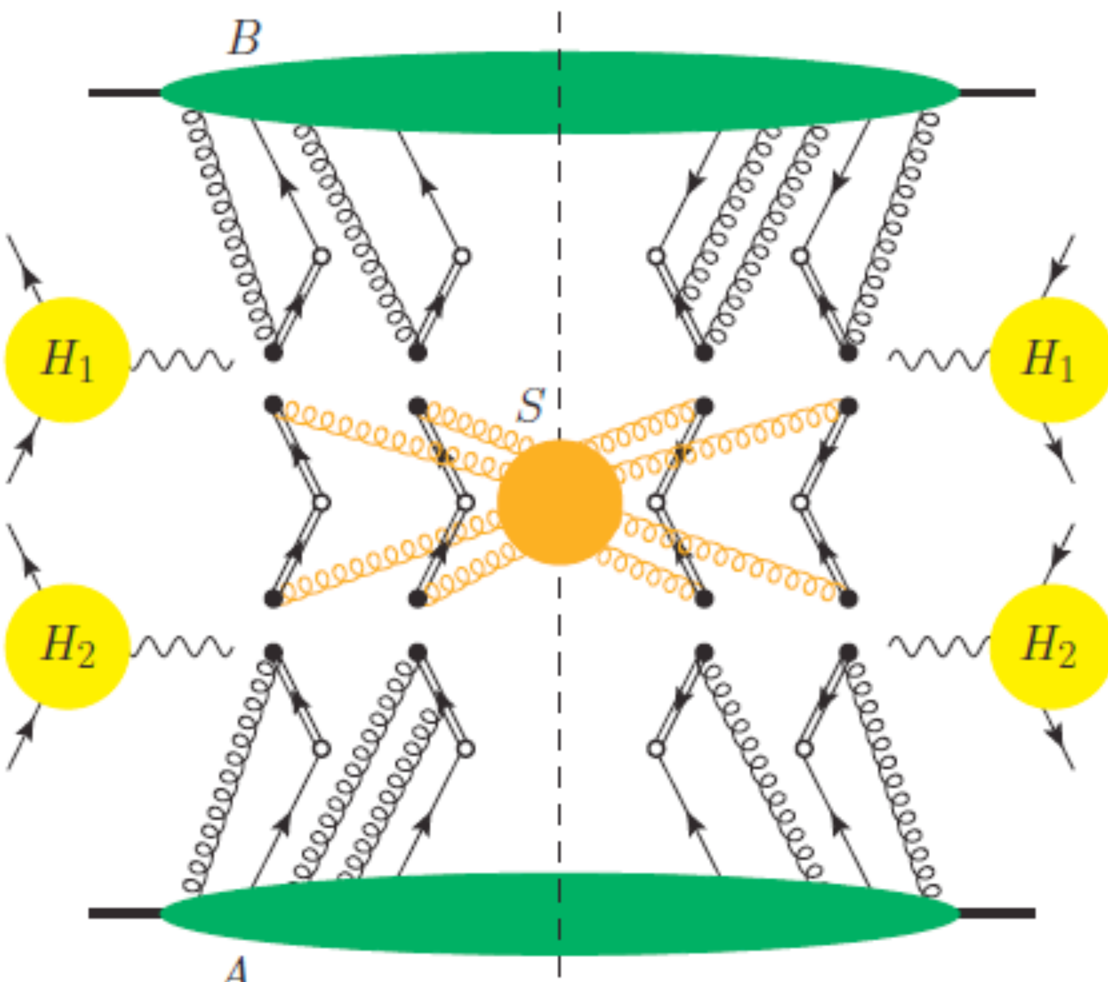

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- **Widespread simplifications (most phenomenology relies on. Go beyond ?)**
  - factorization I $\Gamma_{ij}(x_1, x_2, \mathbf{b}_1, \mathbf{b}_2) = D_{ij}(x_1, x_2) T_{ij}(\mathbf{b}_1, \mathbf{b}_2),$ dPDF
  - factorization II $D_{ij}(x_1, x_2) = f_i(x_1) f_j(x_2),$ PDF

    $T_{ij}(\mathbf{b}_1, \mathbf{b}_2) = T_i(\mathbf{b}_1) T_j(\mathbf{b}_2),$
  - assume flavor universality in T

$$\sigma_{\text{eff}} = \left[\int d^2\mathbf{b} F(\mathbf{b})^2 \right]^{-1}.$$

$$\sigma_{Q_1Q_2} = \frac{1}{1+\delta_{Q_1Q_2}} \frac{\sigma_{Q_1}\sigma_{Q_2}}{\sigma_{\text{eff}}},$$

$$F(\mathbf{b}) = \int T(\mathbf{b}_i) T(\mathbf{b}_i - \mathbf{b}) d^2\mathbf{b}_i,$$

Pocket Formula

A DPS Theory Foundation

LPTHE LABORATOIRE DE PHYSIQUE THÉORIQUE ET HAUTES ENERGIES

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Pocket Formula

- Even these are complex objects to treat numerically

[Gaunt, Stirling; Elias, Golec-Biernat, Stasto; Diehl, Nagar, Tackmann]

DPS Theory Progress

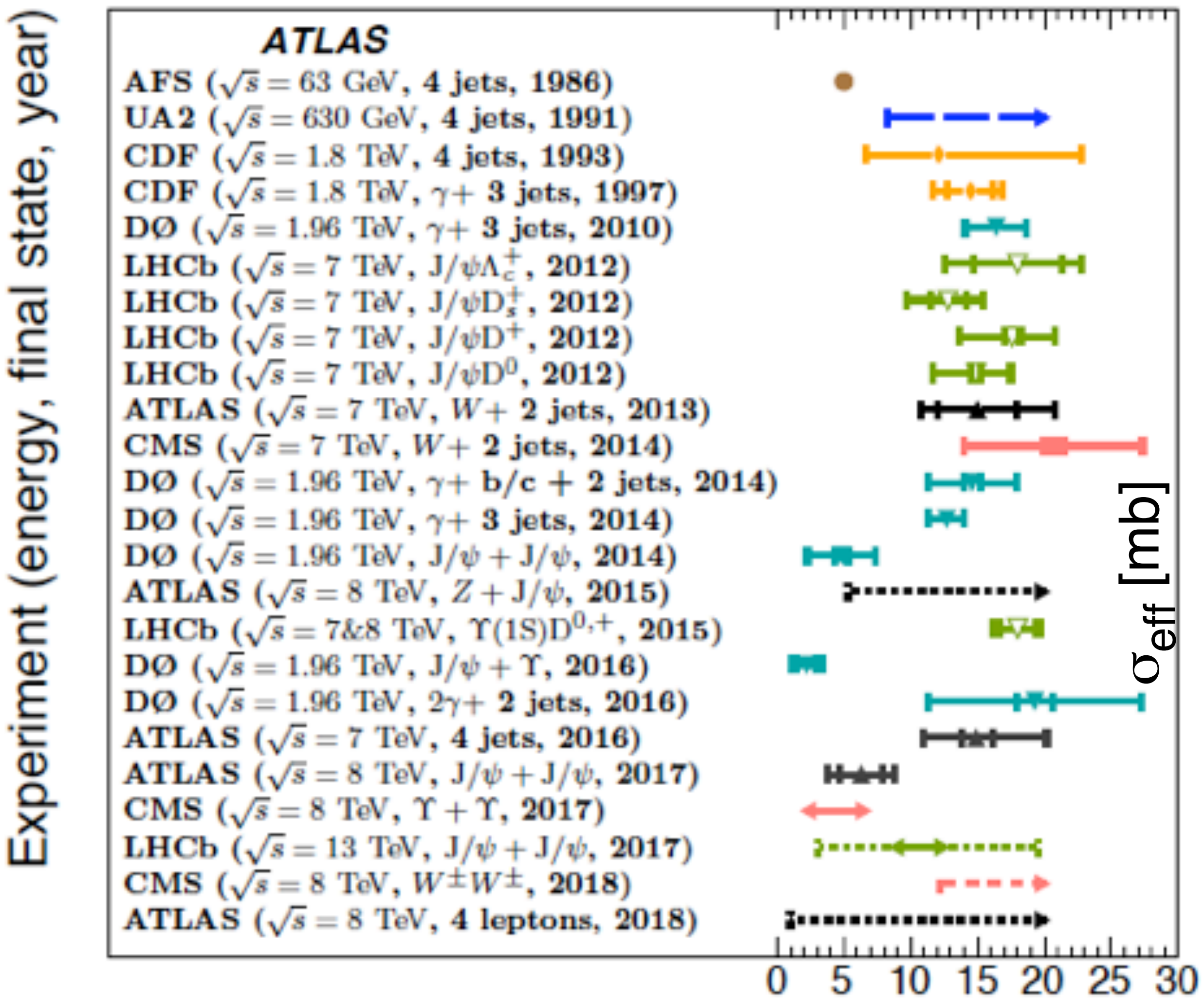
- **Let us start with the pocket formula and take any deviation wrt experiment as an indication of calling for a more rigorous treatment.**
- **Possible deviations due to parton-parton correlations:**
  - Evolution
  - 1v2 vs 2v2 and matching with ME
  - Non-perturbative correlations, e.g. colour, spin etc
- **A few recent theoretical developments**
  - DPS shower dShower [Cabouat, Gaunt,Ostrolenk (2019); Cabouat, Gaunt (2020)]
  - dDGLAP evolution beyond LO ChiliPDF [Diehl et al. (2023)]
  - Double parton distributions from lattice QCD [Bali et al. (2021); Zhang (2023); Jaarsma et al. (2023)]
  - More in this conference ...

Also see the section 7 in arXiv:2012.14161

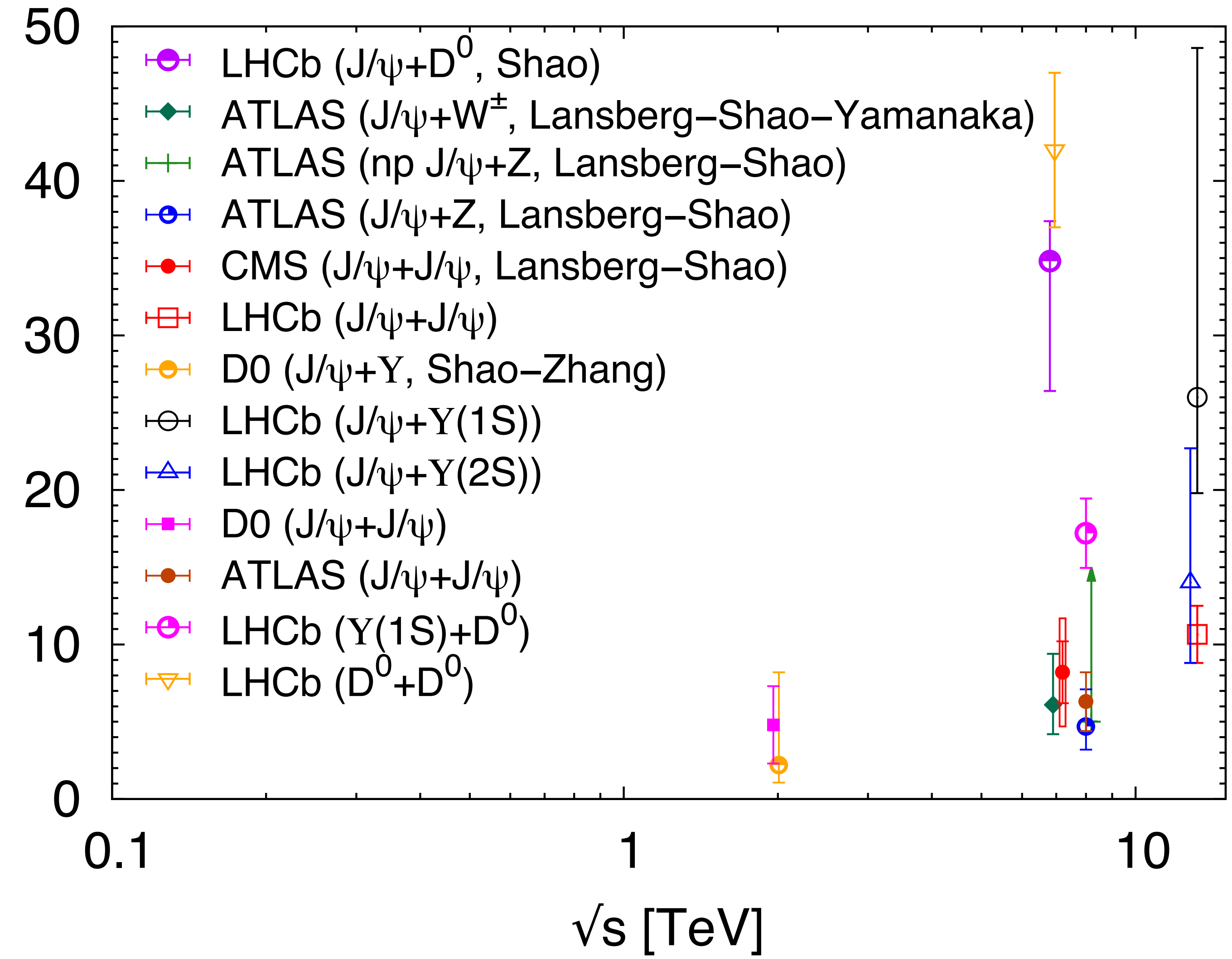
Disclaimer: by no means, the above list is inclusive

DPS Measurements

- **Many DPS measurements at the LHC (Tevatron) in pp (ppbar)**



[ATLAS (PLB'19)]



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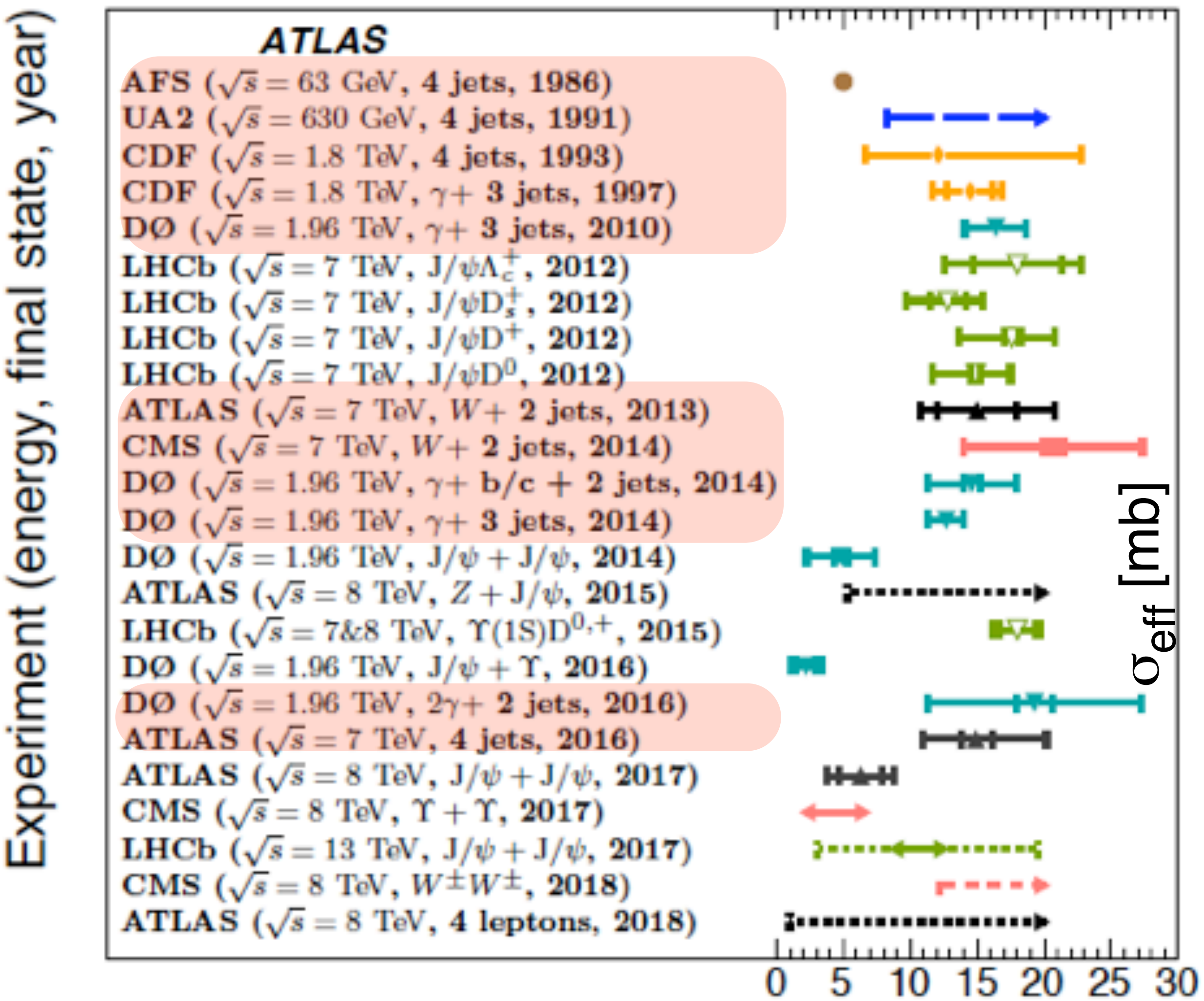

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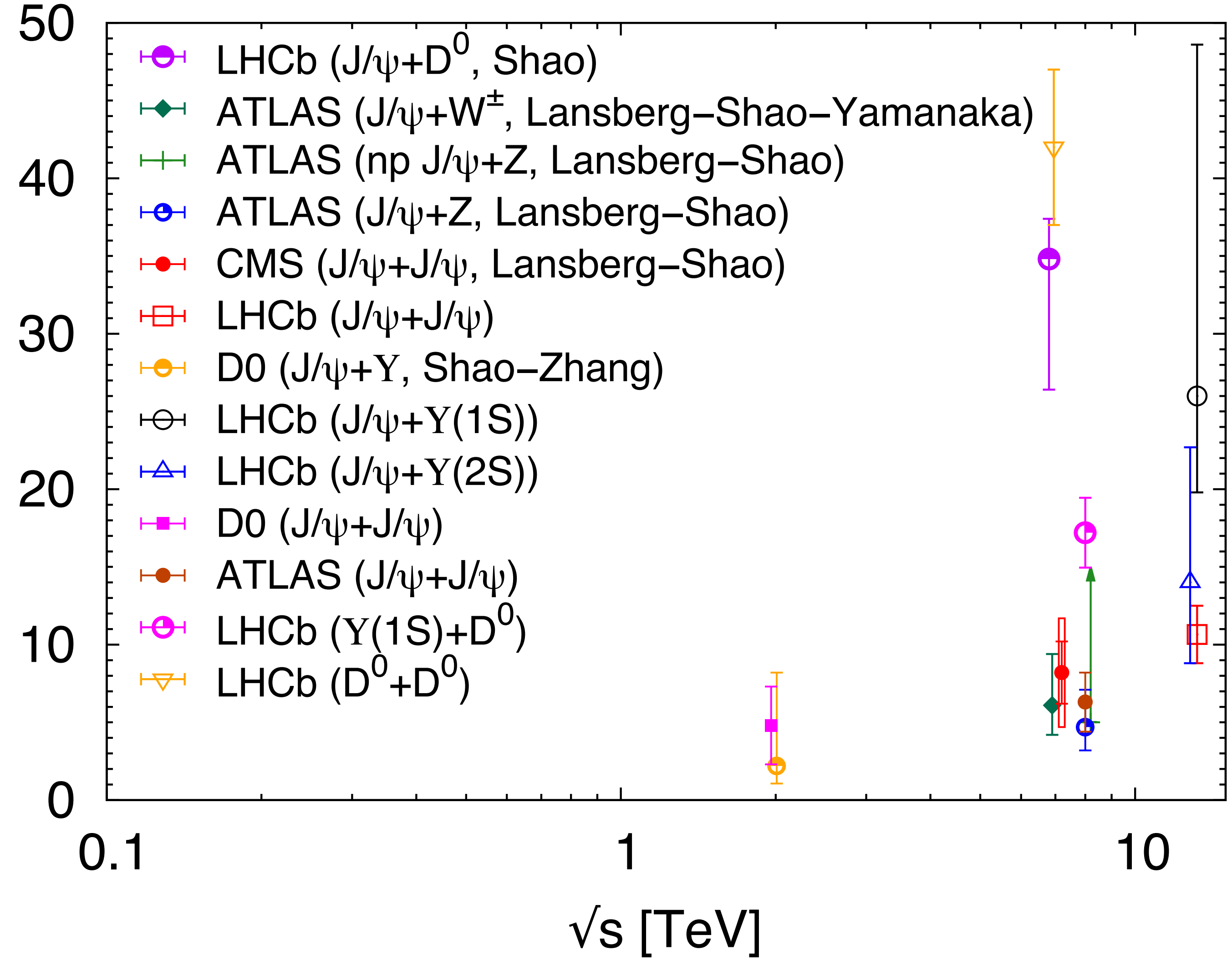
σ_{eff} [mb]



jets

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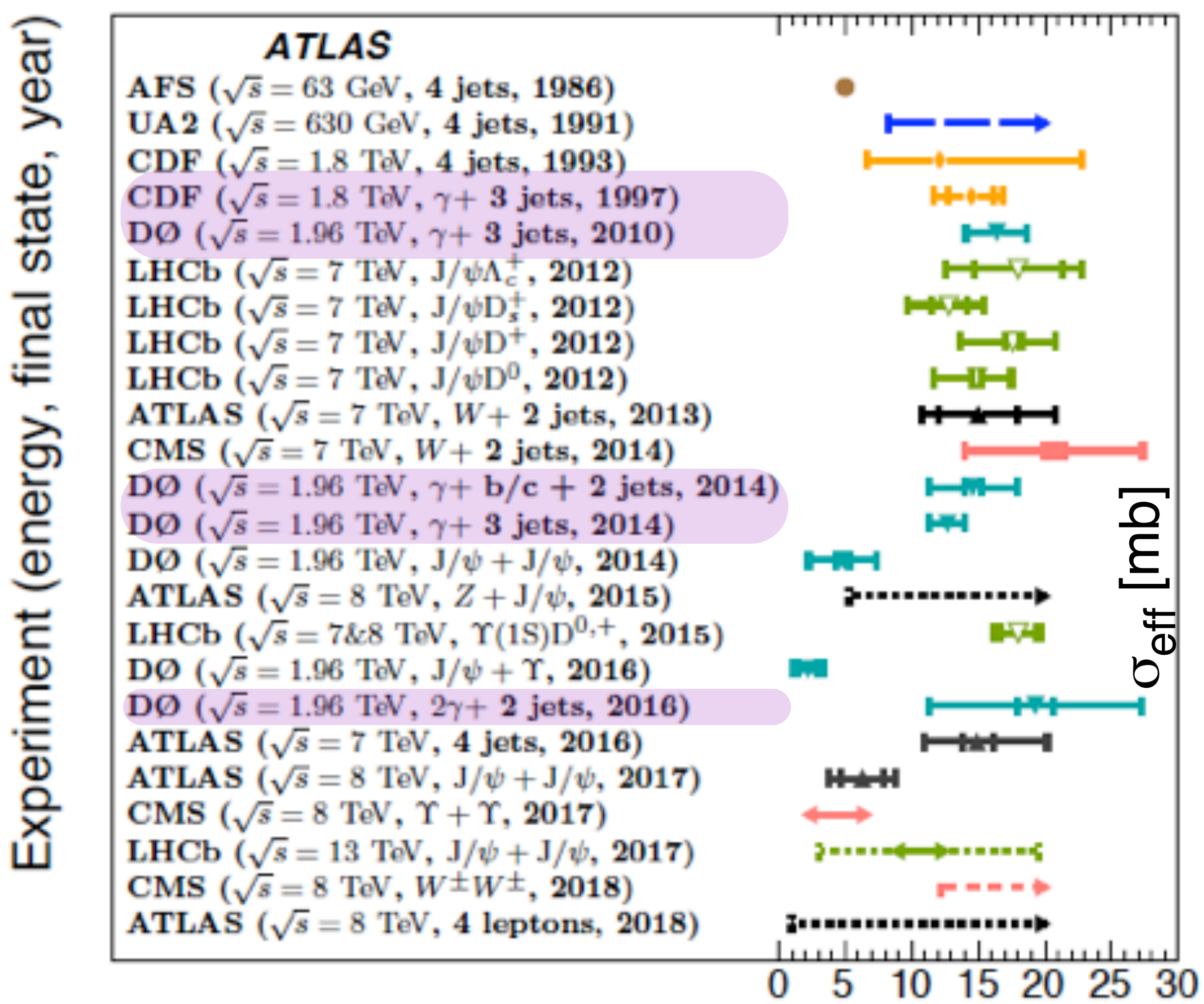

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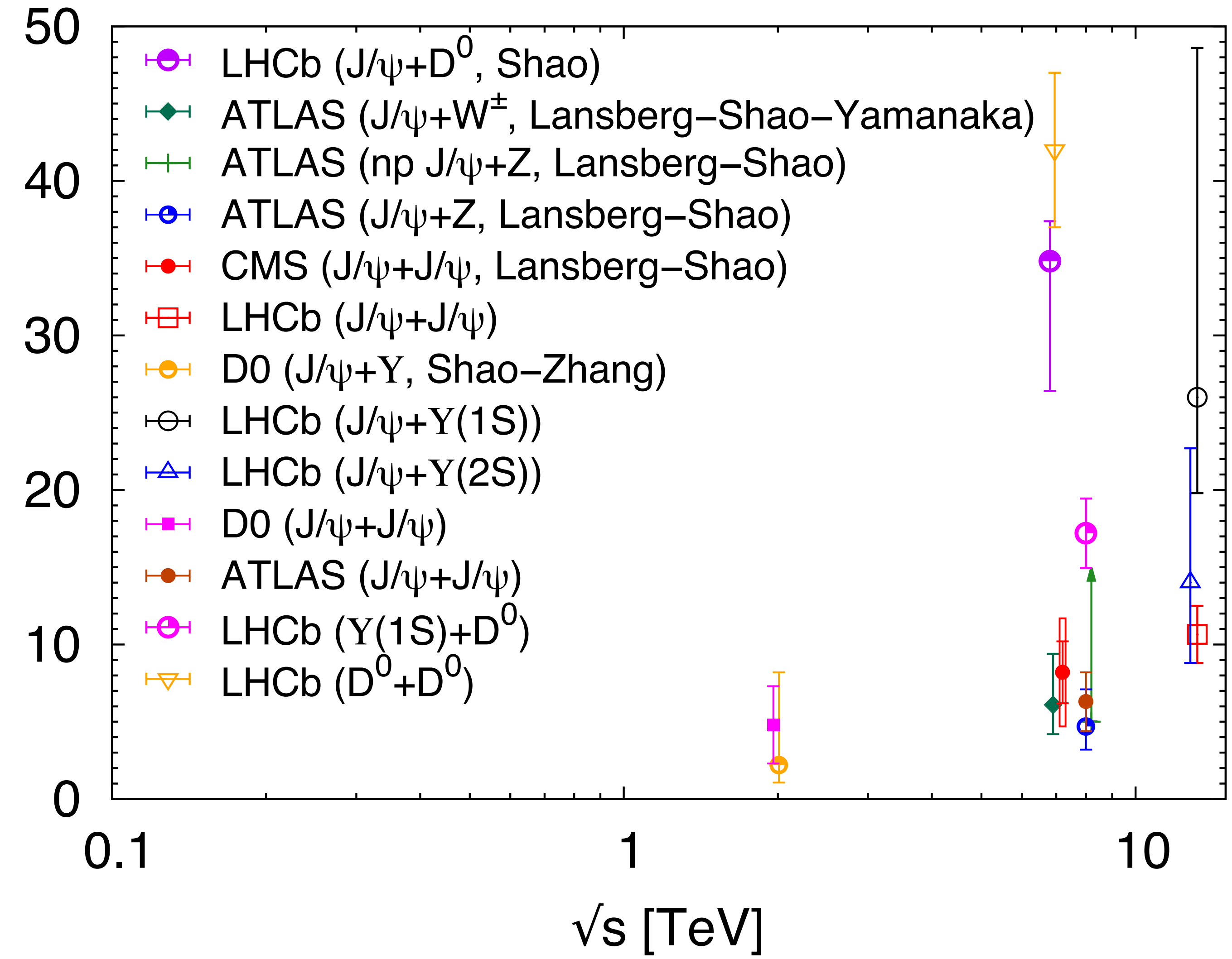

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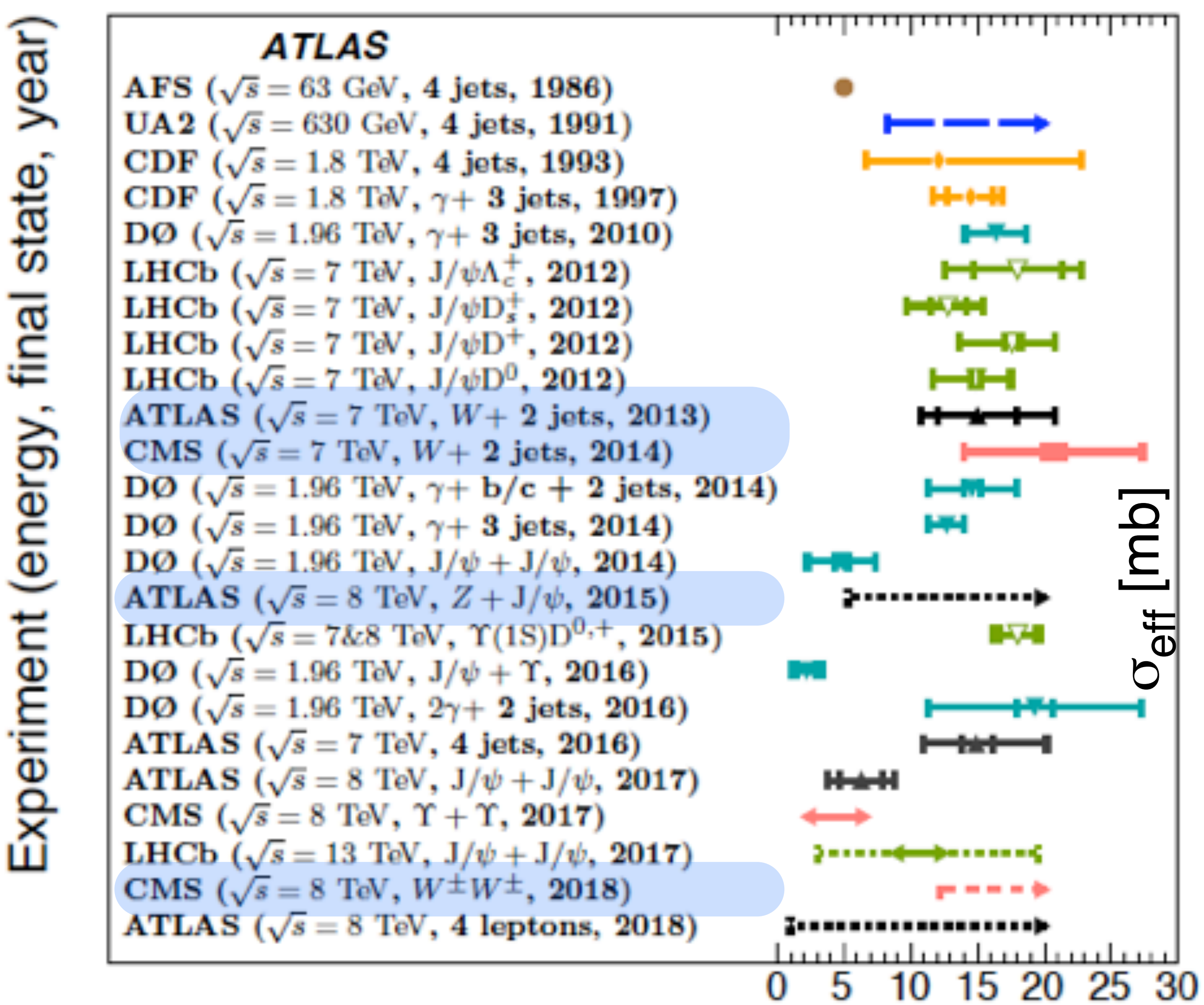

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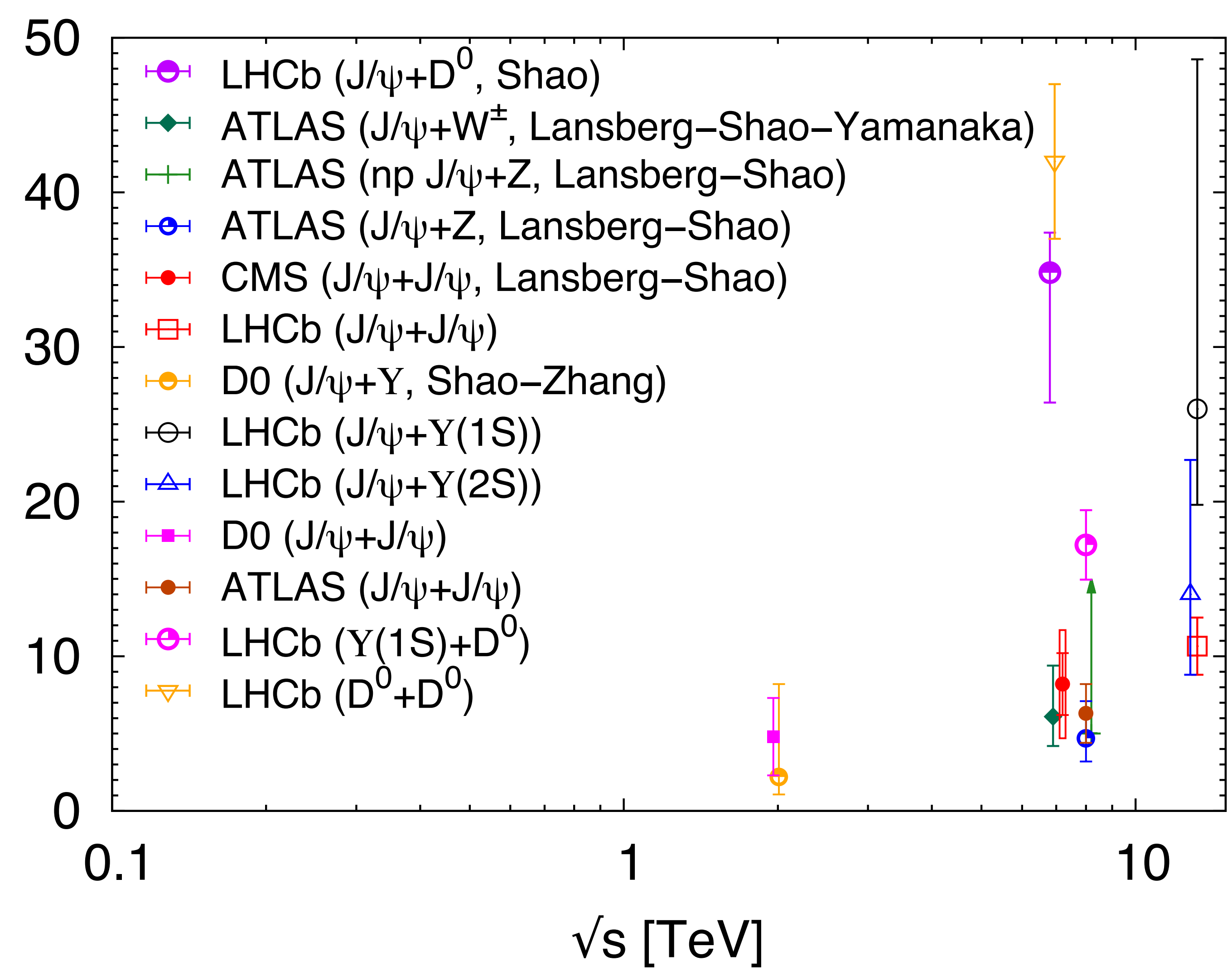

jets

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W & Z

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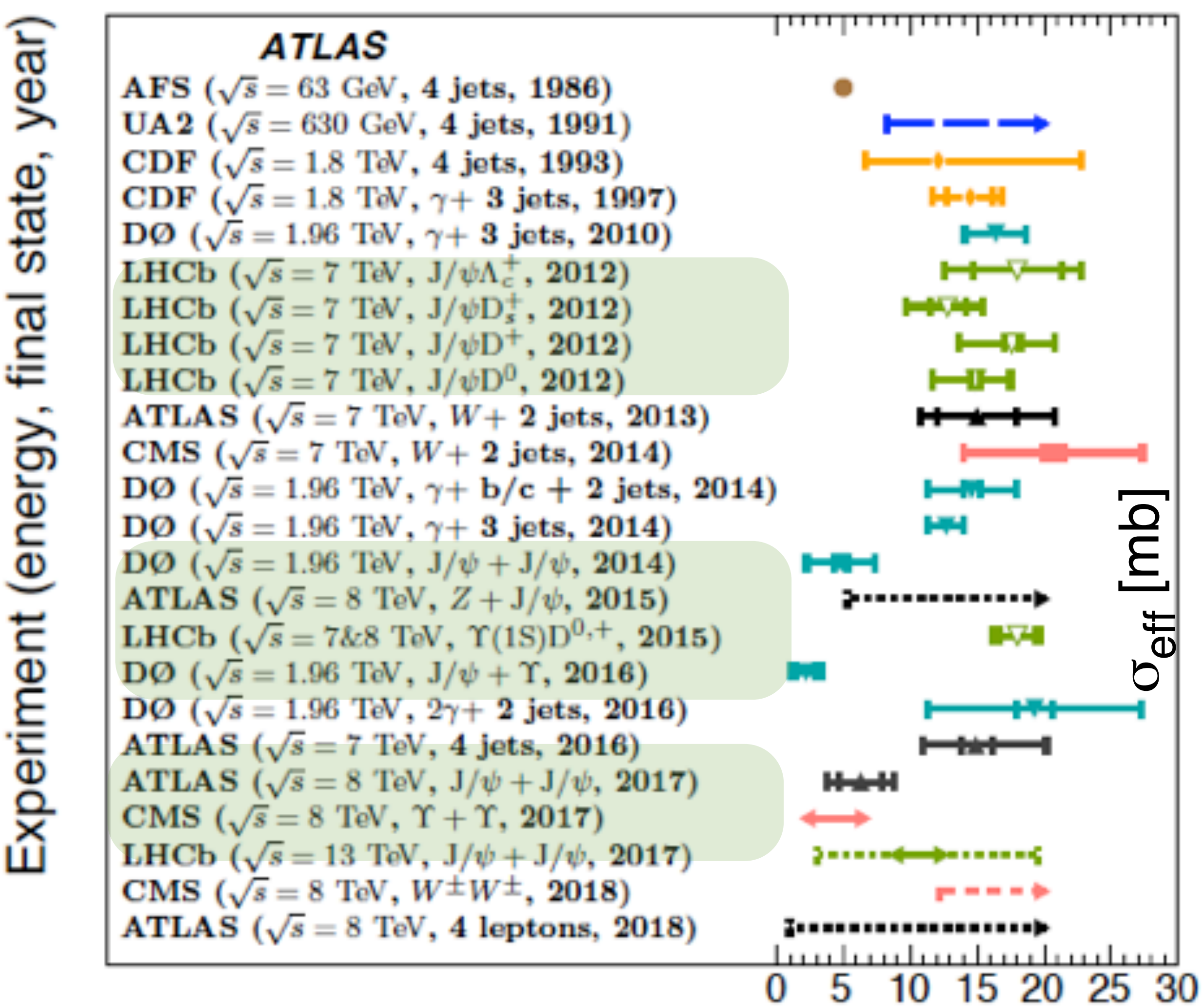

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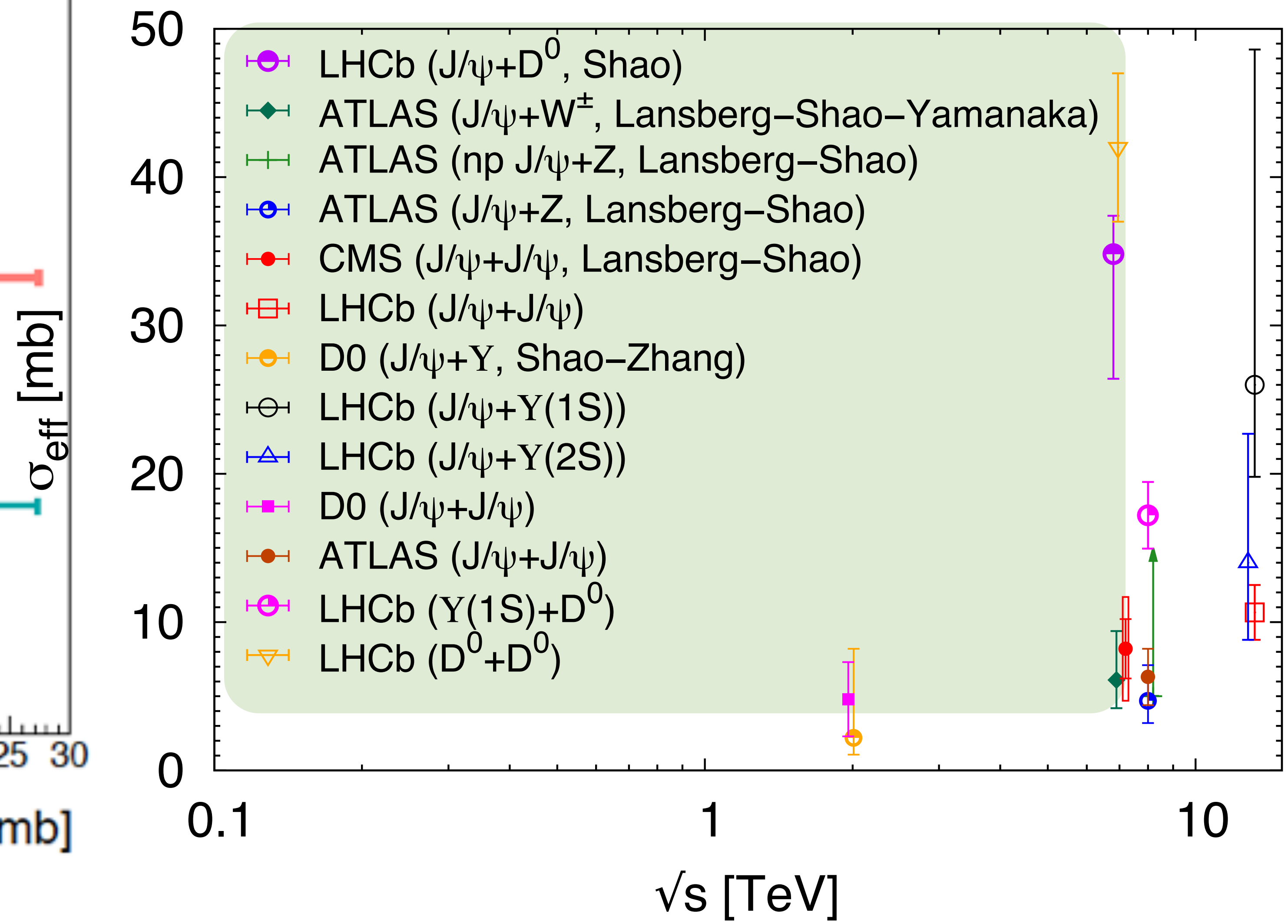

jets | photons | W & Z | heavy flav. & onia

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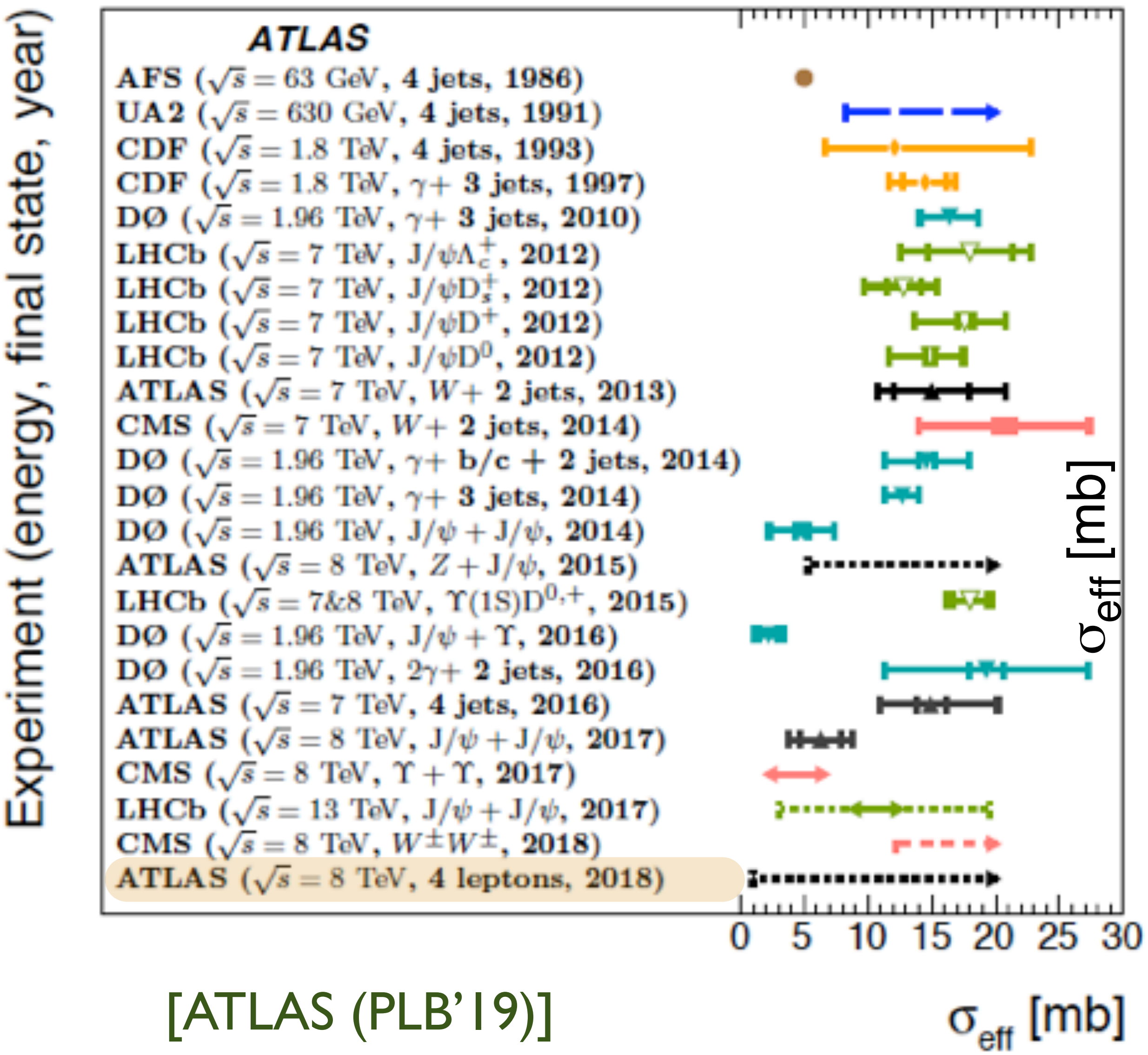

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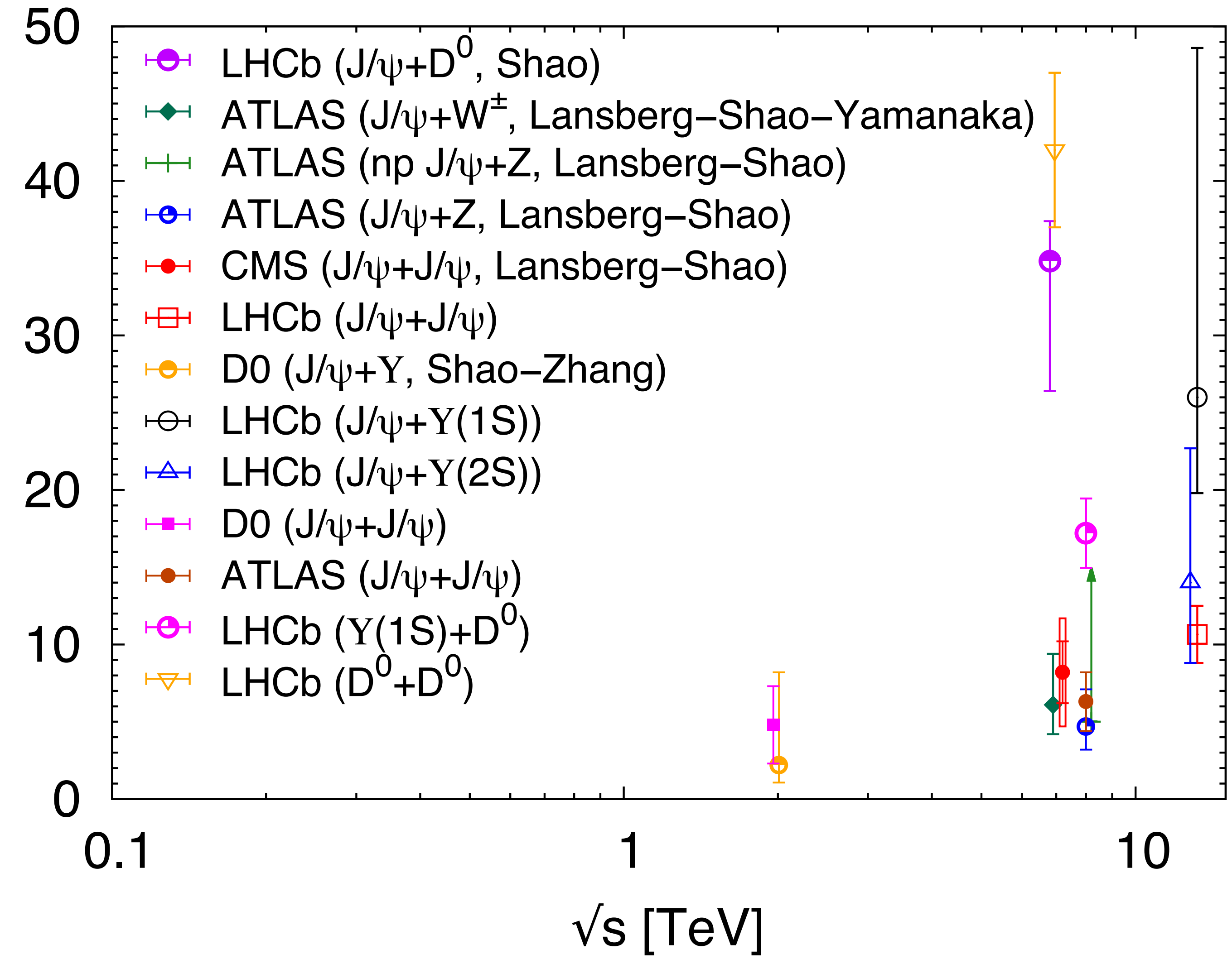

jets | photons | W & Z | heavy flav. & onia | double DY

DPS Measurements

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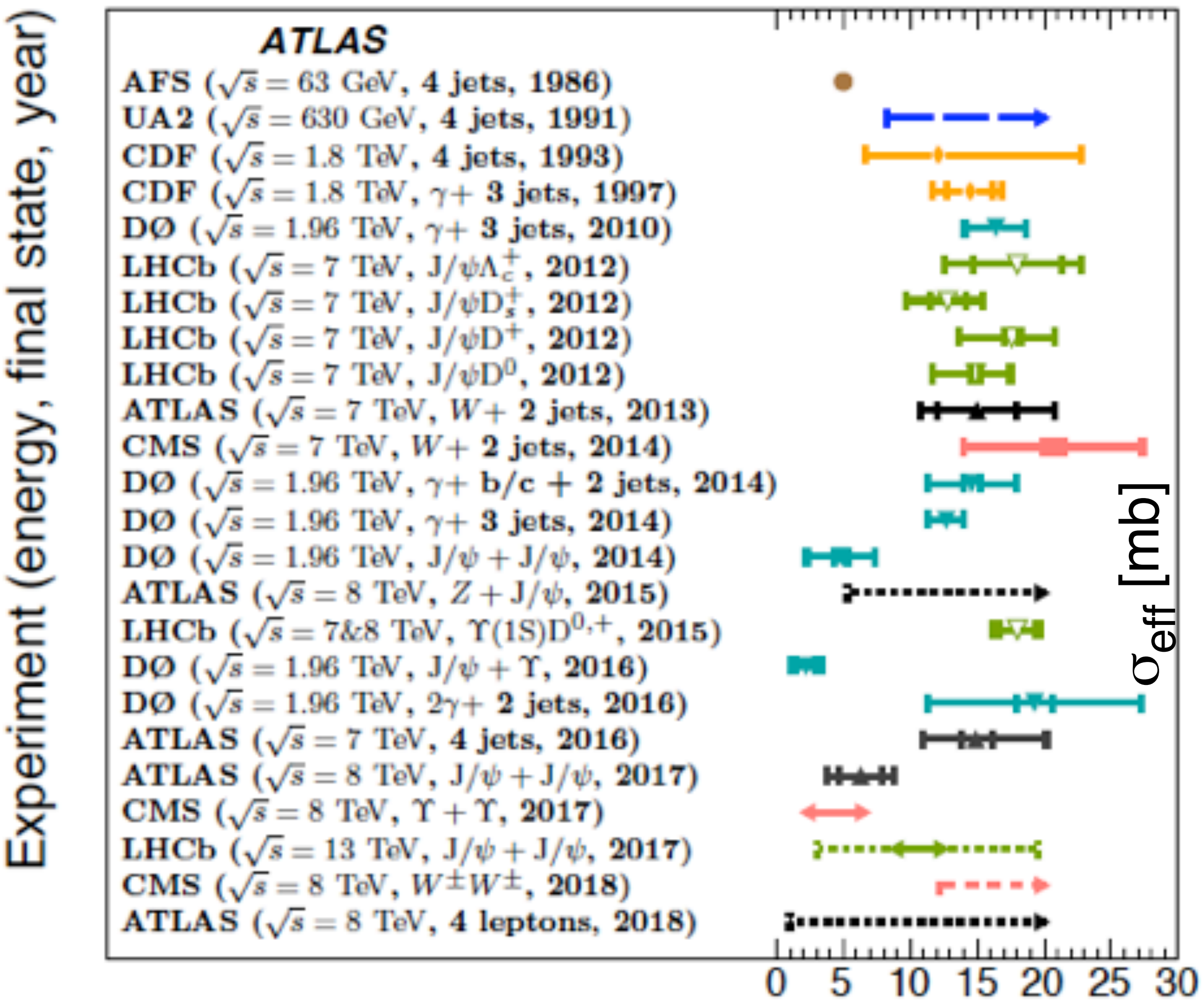
$\sigma_{\rm eff}$:
- flavour dependent ?
- energy dependent ?
- kinematic dependent ?



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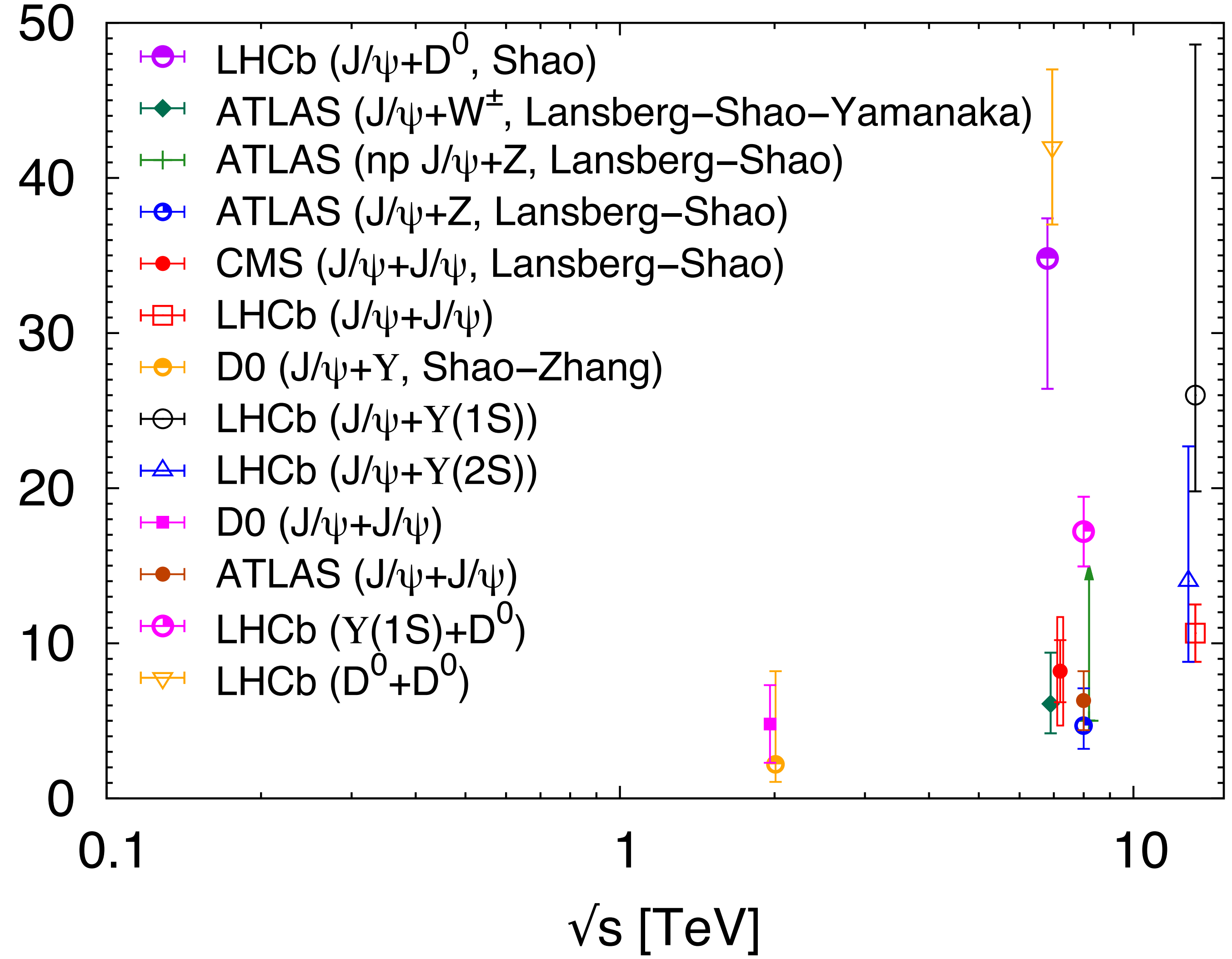

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- **Many DPS measurements at the LHC (Tevatron) in pp (ppbar)**
  - Caveats with different extractions (challenging in differ. SPS & DPS)
    - How good are we understanding/controlling SPS ?

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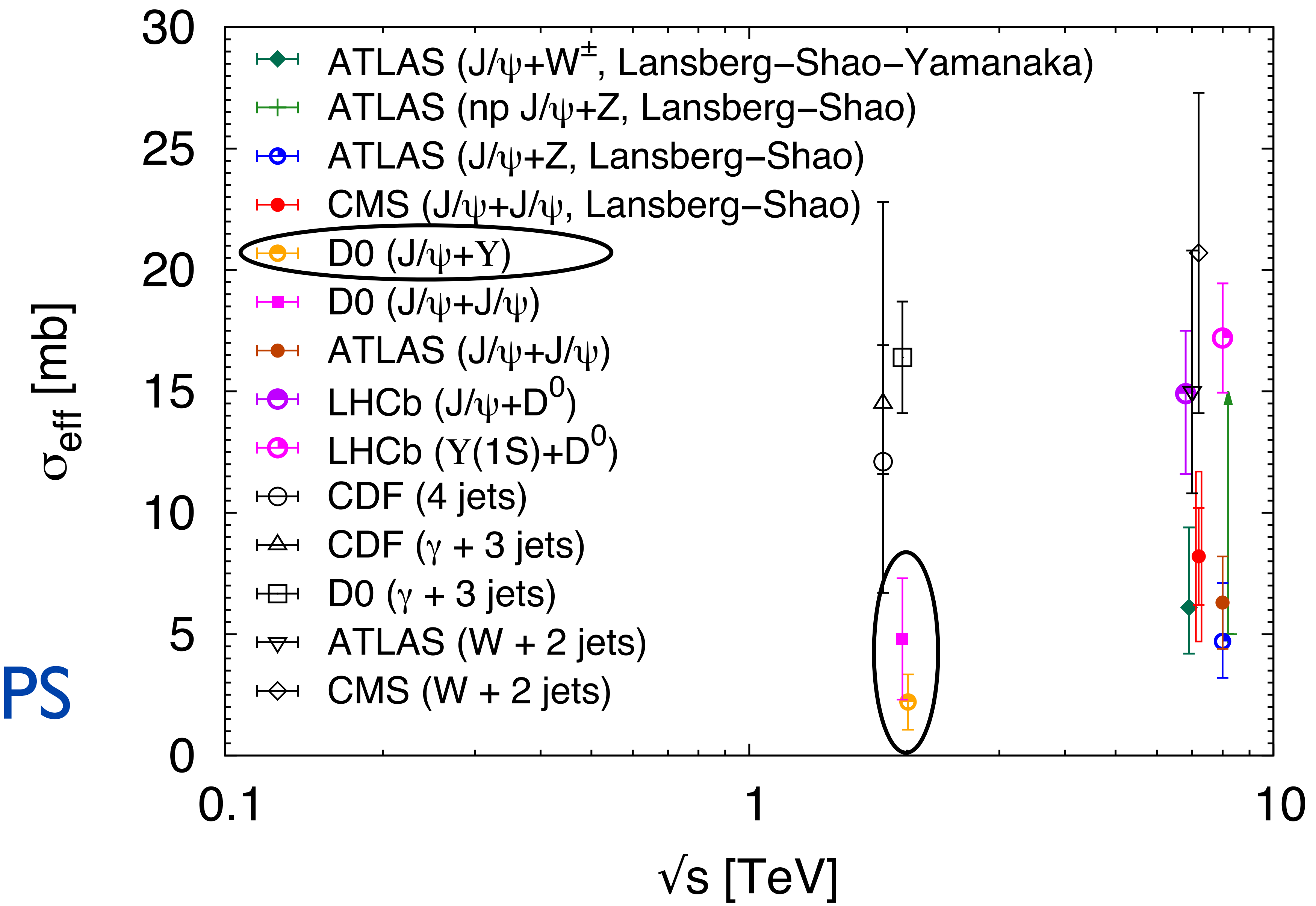
w/o SPS



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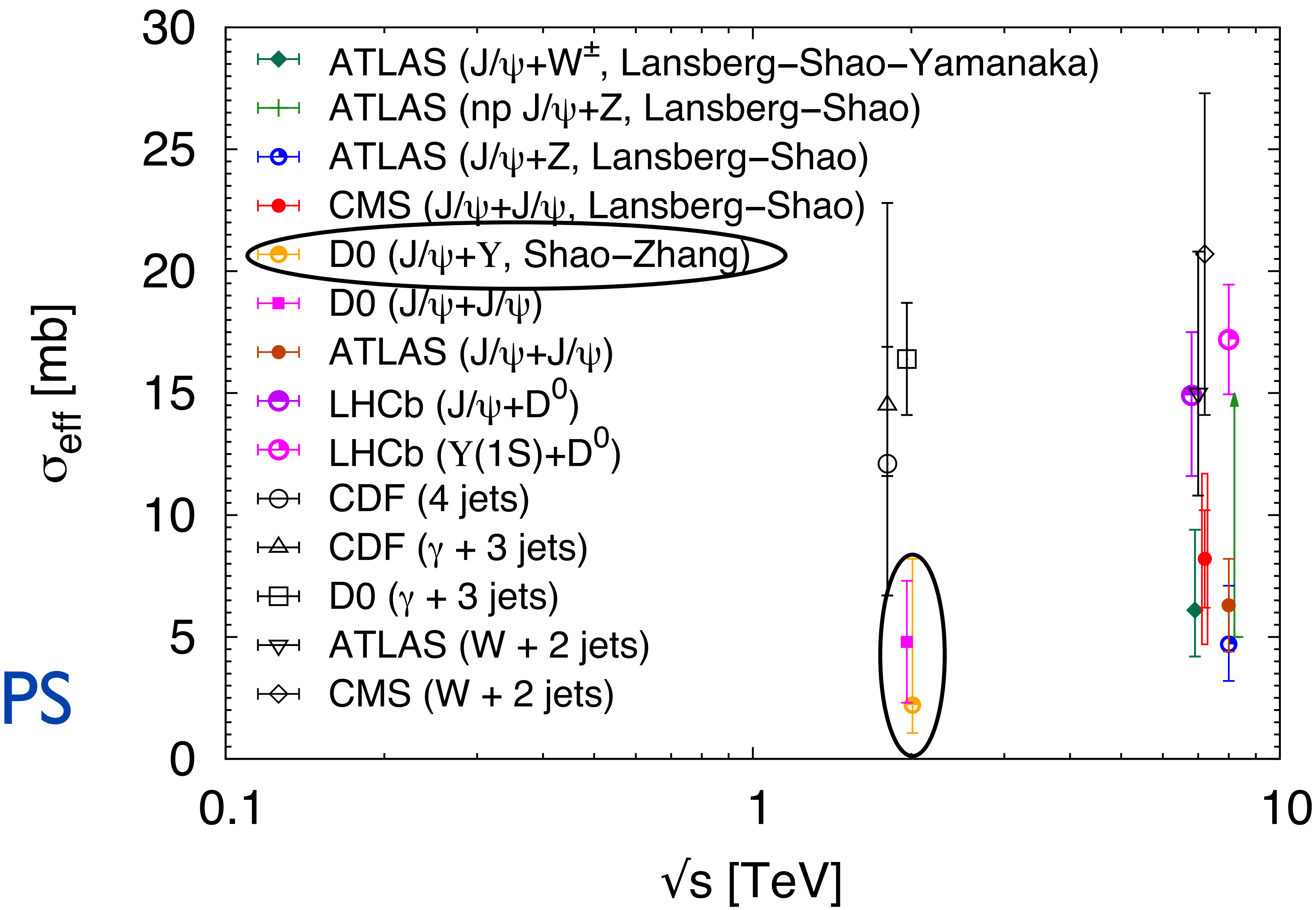

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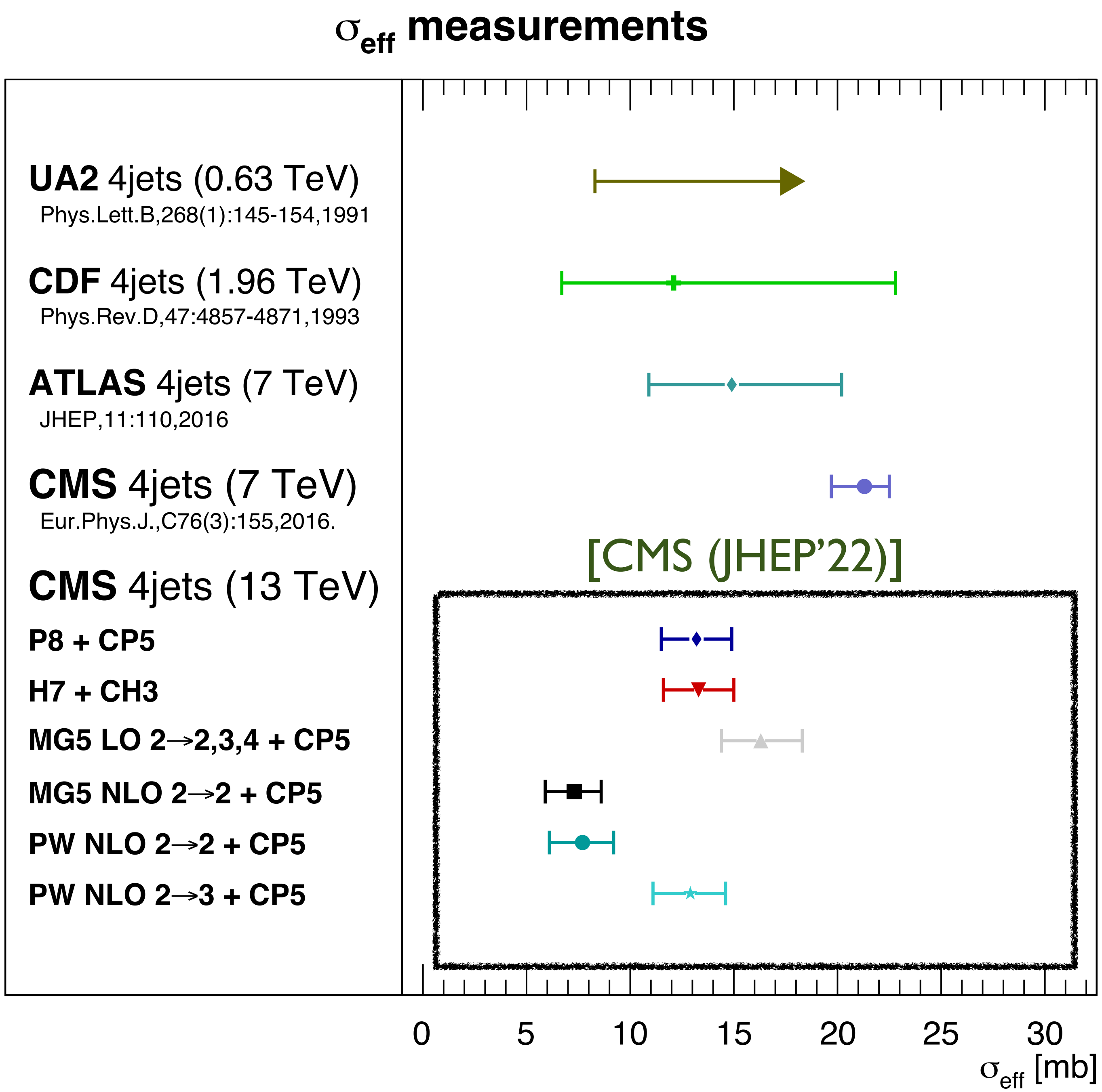


Same observable but different ME+MC

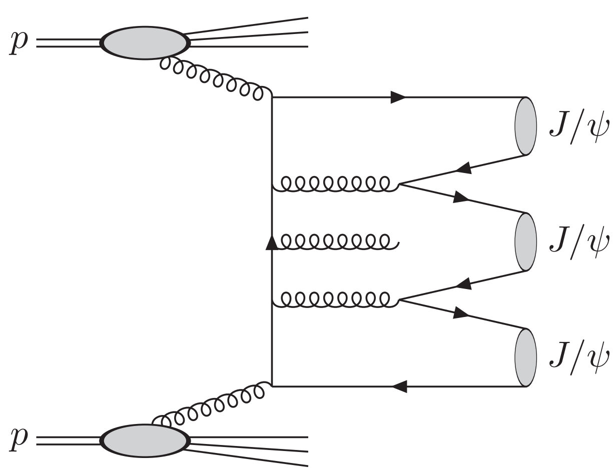
Two novel observables

- **In the rest of the talk, I will focus on two novel observables that have been firstly measured by CMS and LHCb respectively**

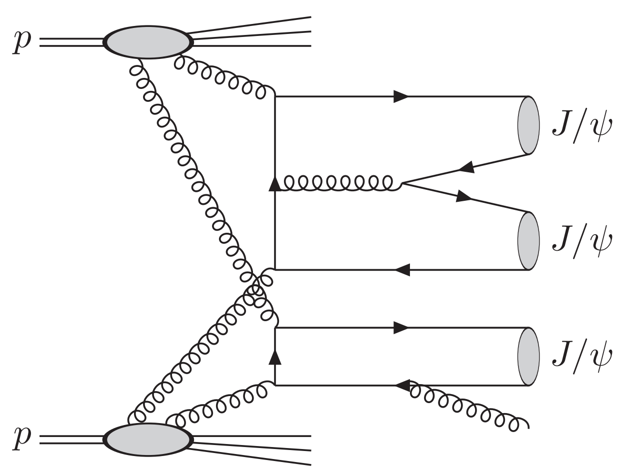
Triple Parton Scattering in pp

DPS in heavy-ion collisions

Triple Parton Scattering in pp



SPS



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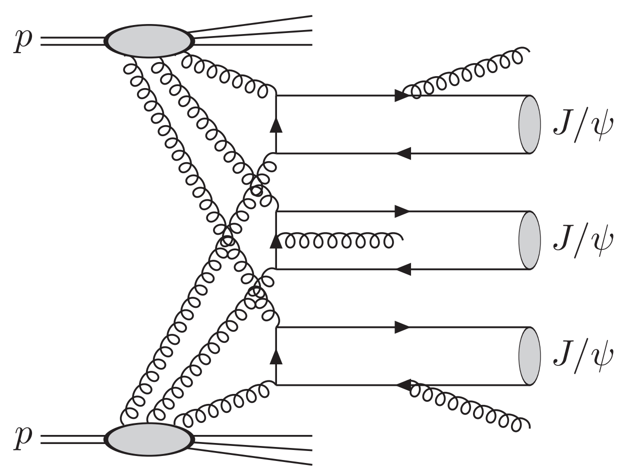

TPS

Triple Parton Scattering in pp

- **Analogously, ignoring the parton correlations, the NPS pocket formula:**

[D. d'Enterria, A. Snigirev (1708.07519)]

Also see the talk of D. D'Enterria on Wed

$$\sigma^{\rm NPS}_{f_1\cdots f_N} = \frac{m}{N!}\frac{\prod_{i=1}^{N}\sigma^{\rm SPS}_{f_i}}{\left(\sigma_{{\rm eff},N}\right)^{N-1}}$$

- **A pure geometric consideration leads to**

[D. d'Enterria, A. Snigirev (PRL'17)]

$$\sigma_{{\rm eff},3} = (0.82 \pm 0.11) \times \sigma_{{\rm eff},2}$$

- **In general, the inclusive cross sections scale as**

$$\sigma_{\rm SPS} \sim \frac{1}{Q^2} \quad \text{v.s.} \quad \sigma_{\rm DPS} \sim \frac{\Lambda^2_{\rm QCD}}{Q^4} \quad \text{v.s.} \quad \sigma_{\rm TPS} \sim \frac{\Lambda^4_{\rm QCD}}{Q^6}$$

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- **Any chance to see TPS at the LHC ?**

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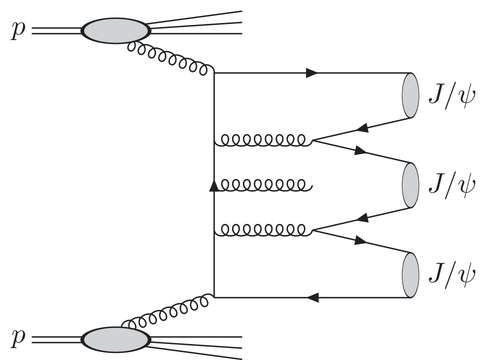
$$\Rightarrow\quad J/\psi J/\psi J/\psi \to \mu^+\mu^-\mu^+\mu^-\mu^+\mu^-$$

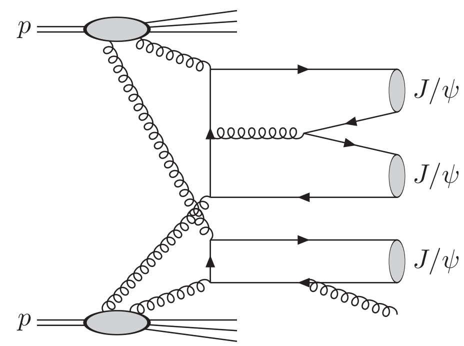
Triple Parton Scattering in pp

- **A first complete study of prompt triple J/psi as a probe of TPS**

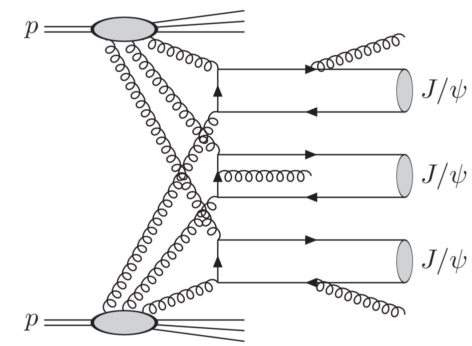
[HSS, Zhang (PRL'19)]



SPS



DPS



TPS

		inclusive	$2.0 < y_{J/\psi} < 4.5$	$\lvert y_{J/\psi}\rvert < 2.4$
13 TeV	SPS	$0.41^{+2.4}_{-0.34} \pm 0.0083$	$(1.8^{+11}_{-1.5} \pm 0.18) \times 10^{-2}$	$(8.7^{+56}_{-7.5} \pm 0.098) \times 10^{-2}$
	DPS	$(190^{+501}_{-140}) \times \frac{10\text{ mb}}{\sigma_{\text{eff},2}}$	$(7.0^{+18}_{-5.1}) \times \frac{10\text{ mb}}{\sigma_{\text{eff},2}}$	$(50^{+140}_{-37}) \times \frac{10\text{ mb}}{\sigma_{\text{eff},2}}$
	TPS	$130 \times \left(\frac{10\text{ mb}}{\sigma_{\text{eff},3}}\right)^2$	$1.3 \times \left(\frac{10\text{ mb}}{\sigma_{\text{eff},3}}\right)^2$	$18 \times \left(\frac{10\text{ mb}}{\sigma_{\text{eff},3}}\right)^2$
27 TeV	SPS	$0.46^{+2.9}_{-0.39} \pm 0.022$	$(3.2^{+22}_{-2.8} \pm 0.21) \times 10^{-2}$	$(5.8^{+39}_{-5.1} \pm 0.29) \times 10^{-2}$
	DPS	$(560^{+2900}_{-480}) \times \frac{10\text{ mb}}{\sigma_{\text{eff},2}}$	$(19^{+97}_{-16}) \times \frac{10\text{ mb}}{\sigma_{\text{eff},2}}$	$(120^{+630}_{-100}) \times \frac{10\text{ mb}}{\sigma_{\text{eff},2}}$
	TPS	$570 \times \left(\frac{10\text{ mb}}{\sigma_{\text{eff},3}}\right)^2$	$5.0 \times \left(\frac{10\text{ mb}}{\sigma_{\text{eff},3}}\right)^2$	$57 \times \left(\frac{10\text{ mb}}{\sigma_{\text{eff},3}}\right)^2$
75 TeV	SPS	$0.59^{+4.4}_{-0.52} \pm 0.016$	$(3.0^{+25}_{-2.7} \pm 0.23) \times 10^{-2}$	$(7.2^{+63}_{-6.5} \pm 0.38) \times 10^{-2}$
	DPS	$(1900^{+11000}_{-1600}) \times \frac{10\text{ mb}}{\sigma_{\text{eff},2}}$	$(57^{+340}_{-50}) \times \frac{10\text{ mb}}{\sigma_{\text{eff},2}}$	$(310^{+2000}_{-270}) \times \frac{10\text{ mb}}{\sigma_{\text{eff},2}}$
	TPS	$3900 \times \left(\frac{10\text{ mb}}{\sigma_{\text{eff},3}}\right)^2$	$27 \times \left(\frac{10\text{ mb}}{\sigma_{\text{eff},3}}\right)^2$	$260 \times \left(\frac{10\text{ mb}}{\sigma_{\text{eff},3}}\right)^2$
100 TeV	SPS	$1.1^{+8.4}_{-1.0} \pm 0.044$	$(4.5^{+33}_{-4.0} \pm 0.72) \times 10^{-2}$	$(36^{+290}_{-32} \pm 1.8) \times 10^{-2}$
	DPS	$(3400^{+19000}_{-2900}) \times \frac{10\text{ mb}}{\sigma_{\text{eff},2}}$	$(100^{+550}_{-86}) \times \frac{10\text{ mb}}{\sigma_{\text{eff},2}}$	$(490^{+3000}_{-430}) \times \frac{10\text{ mb}}{\sigma_{\text{eff},2}}$
	TPS	$6500 \times \left(\frac{10\text{ mb}}{\sigma_{\text{eff},3}}\right)^2$	$45 \times \left(\frac{10\text{ mb}}{\sigma_{\text{eff},3}}\right)^2$	$380 \times \left(\frac{10\text{ mb}}{\sigma_{\text{eff},3}}\right)^2$

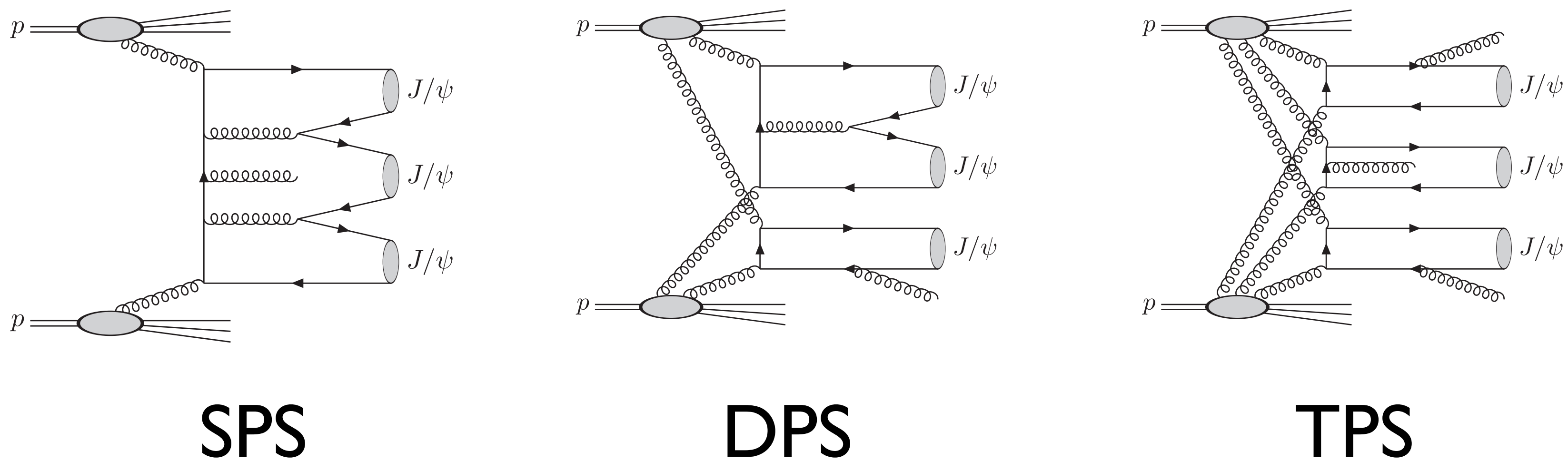
- With our knowledge of single J/psi and double J/psi, the process is predicted to be DPS and TPS dominant

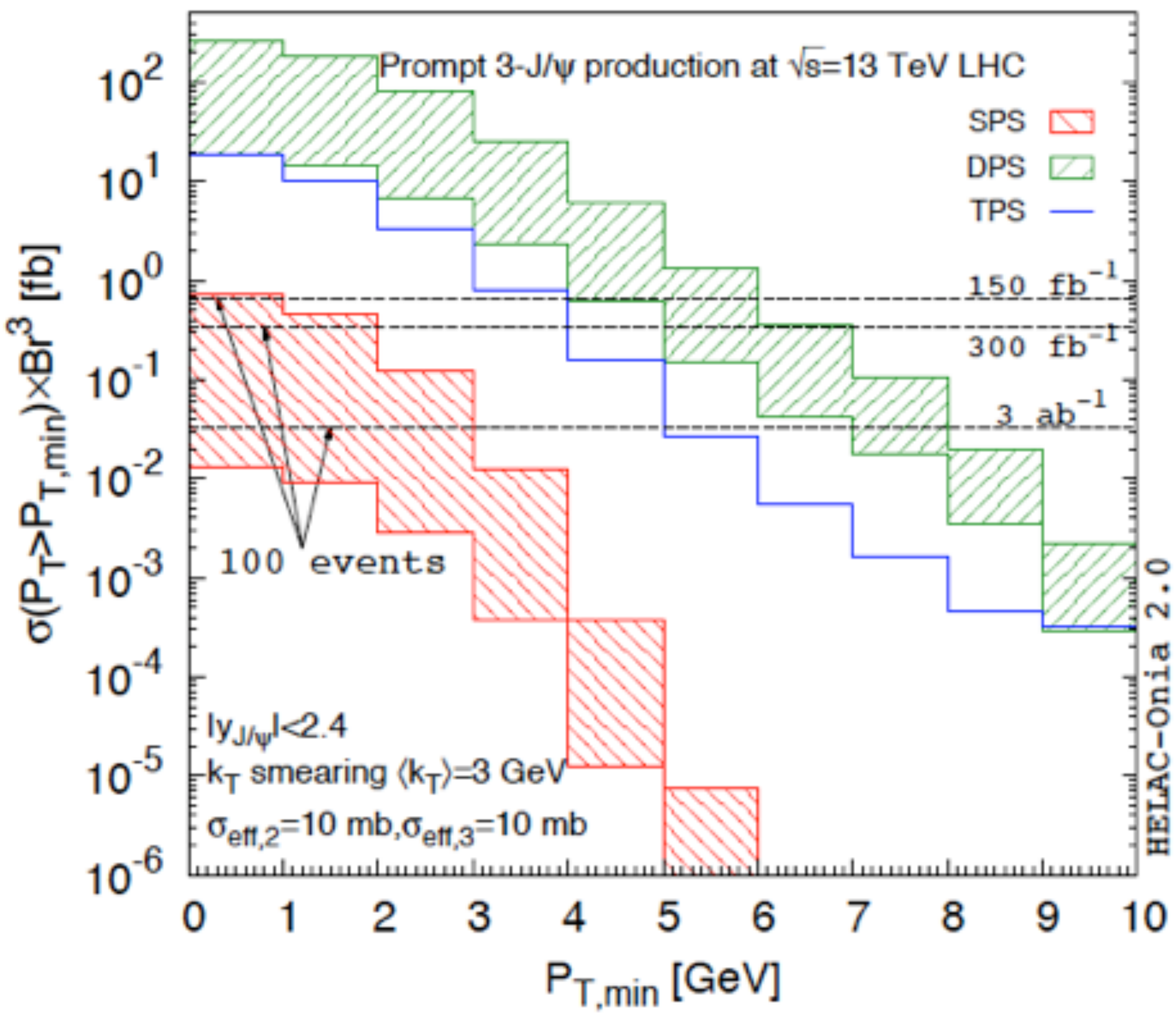
- The number of events is large enough to be seen at the LHC unless $\sigma_{\text{eff},2}$ and $\sigma_{\text{eff},3}$ are significantly larger than 10 mb

Triple Parton Scattering in pp

- **A first complete study of prompt triple J/psi as a probe of TPS**

[HSS, Zhang (PRL'19)]





- Cross sections drop fast with transverse momentum cut of J/psi
- Complementary between ATLAS/ CMS (larger luminosity but higher p_T) and ALICE/LHCb (lower luminosity but lower p_T).

Triple Parton Scattering in pp

- **A first complete study of prompt triple J/psi as a probe of TPS**

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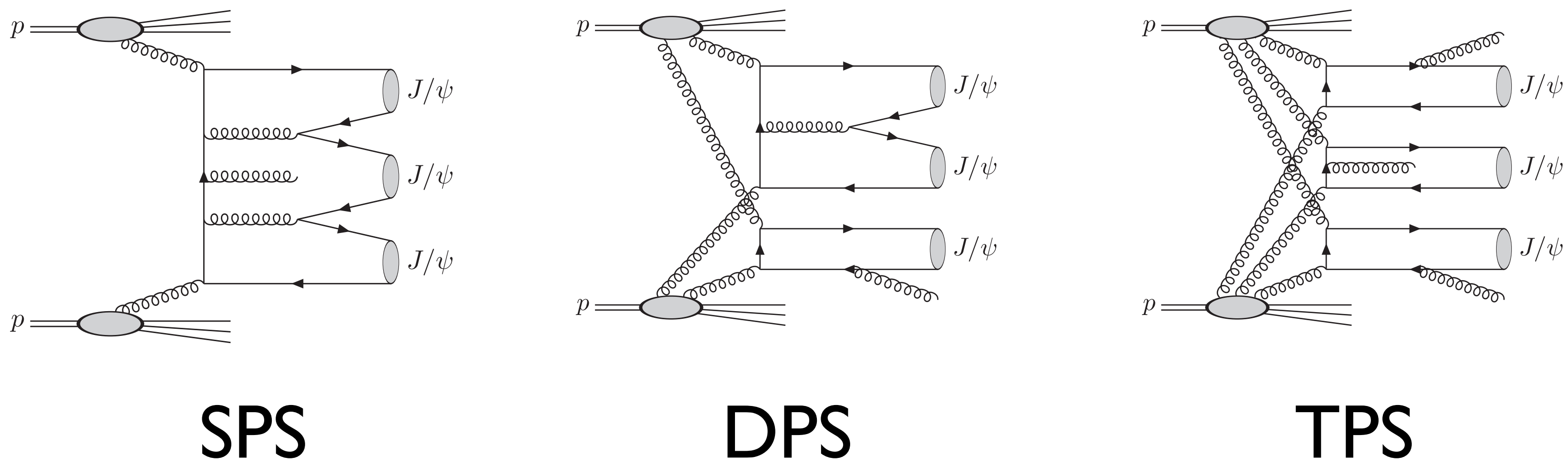
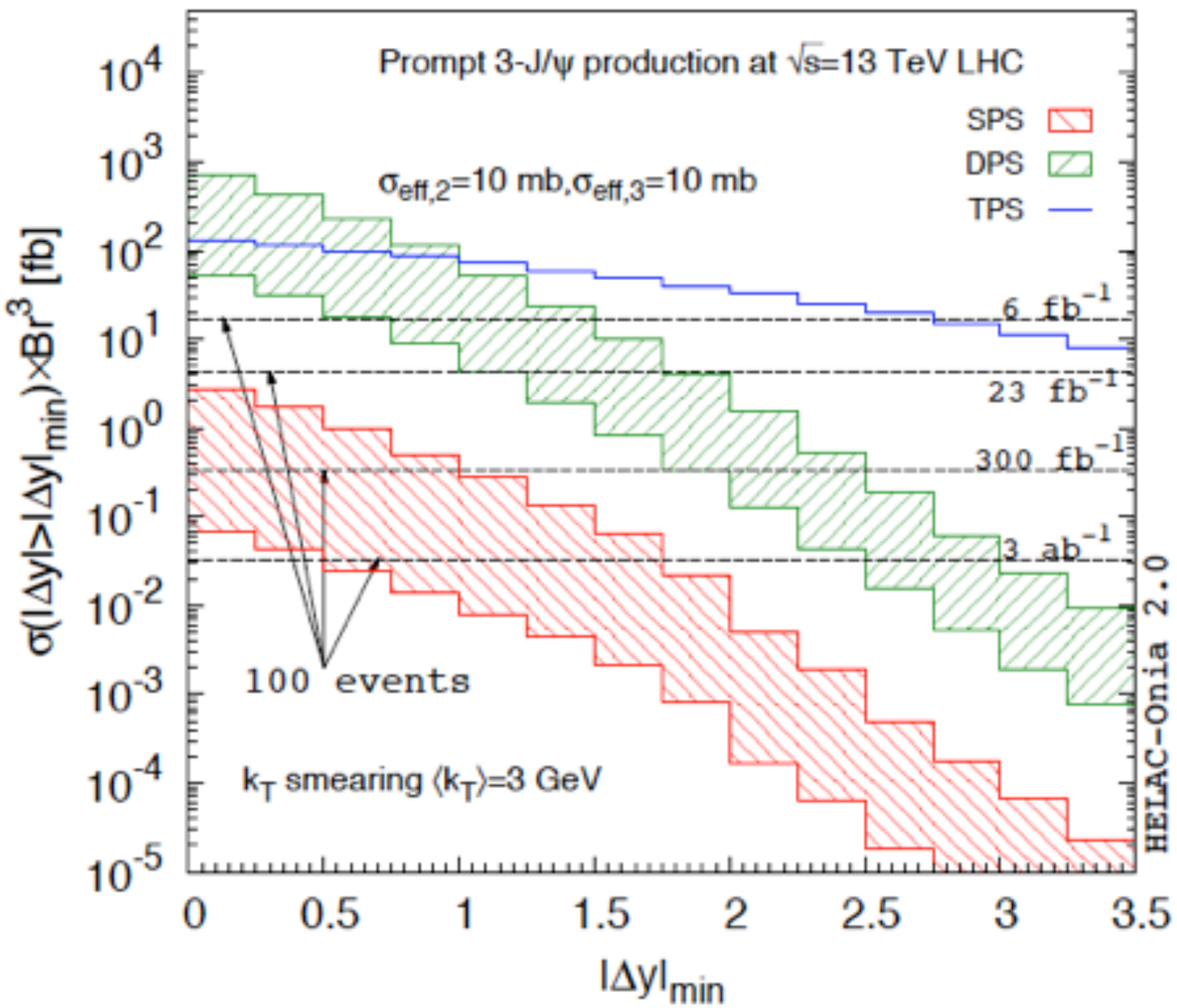
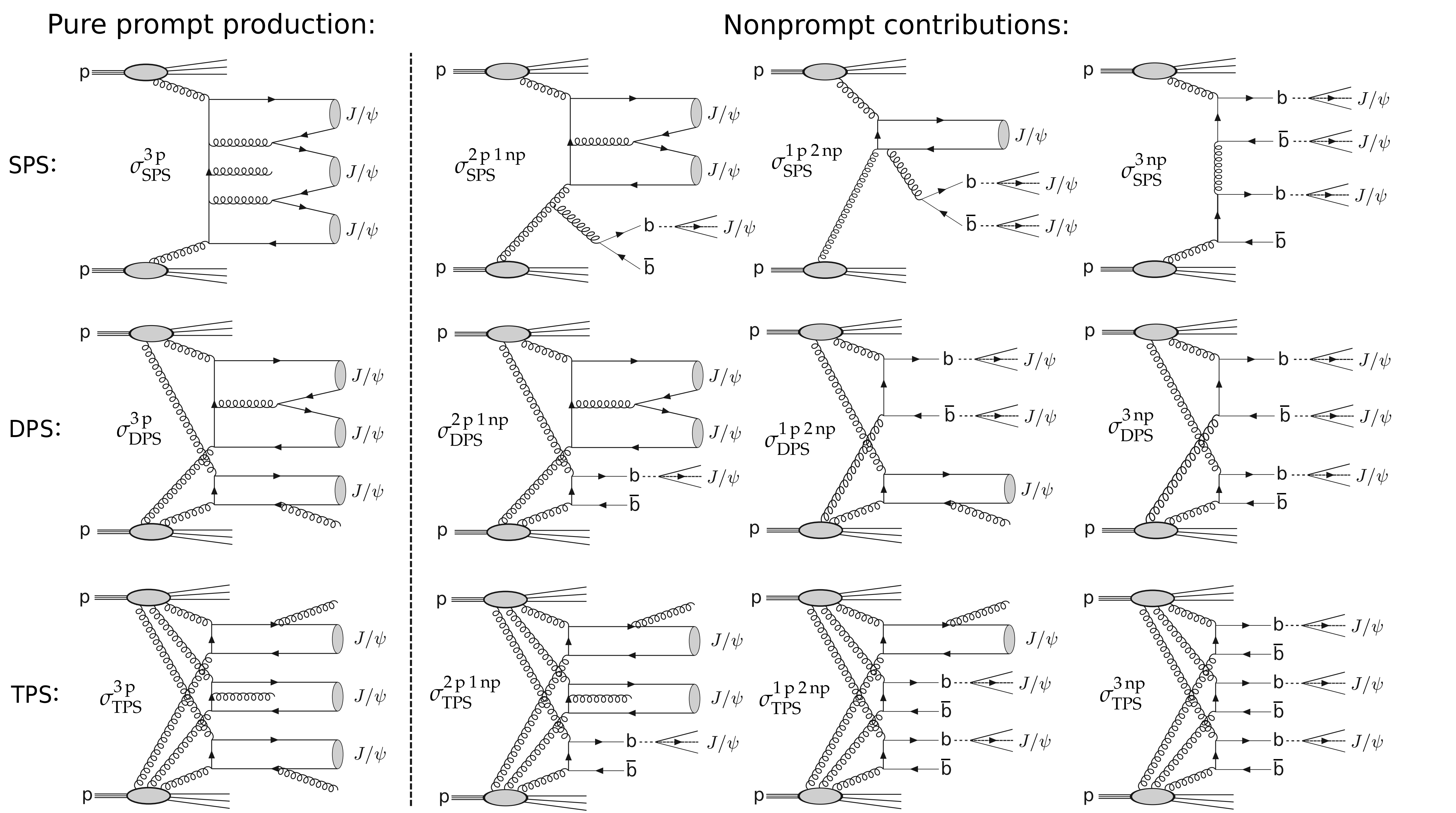




- A mean to separate TPS alone with sufficient statistics -> rapidity gaps among triple J/psi particles

- **First observation by CMS at 13 TeV in pp**

[CMS (Nature Physics'23)]



Triple Parton Scattering in pp

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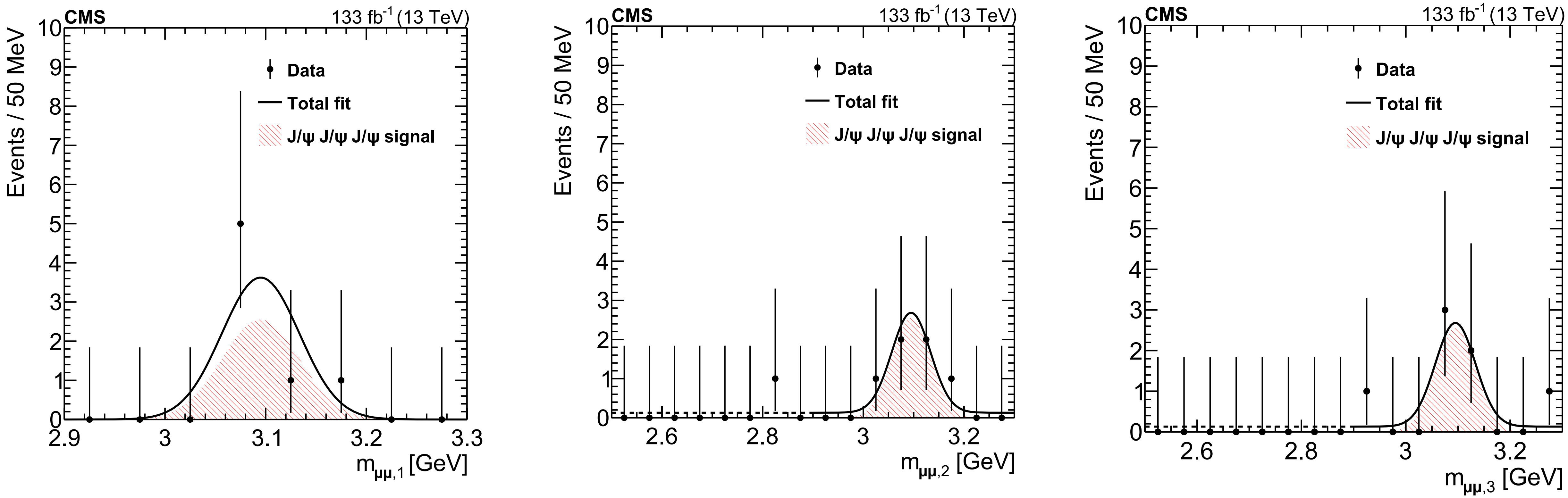


- **Observation: 5 signal events + 1 background event**

- **The measurement of fiducial cross section**

$$\sigma(pp \to J/\psi J/\psi J/\psi X) = 272^{+141}_{-104}(\text{stat}) \pm 17(\text{syst})\ \text{fb}$$

Triple Parton Scattering in pp

- **Theoretical interpretation of the CMS measurement** [CMS (Nature Physics'23)]
  - Using the pocket formula, we need to know the following theoretical inputs

SPS single-J/ψ production		SPS double-J/ψ production			SPS triple-J/ψ production			
HO(DATA)	MG5NLO+PY8	HO(NLO*)	HO(LO)+PY8	MG5NLO+PY8	HO(LO)	HO(LO)+PY8	HO(LO)+PY8	MG5NLO+PY8
$\sigma_{\rm SPS}^{\rm 1p}$	$\sigma_{\rm SPS}^{\rm 1np}$	$\sigma_{\rm SPS}^{\rm 2p}$	$\sigma_{\rm SPS}^{\rm 1p1np}$	$\sigma_{\rm SPS}^{\rm 2np}$	$\sigma_{\rm SPS}^{\rm 3p}$	$\sigma_{\rm SPS}^{\rm 2p1np}$	$\sigma_{\rm SPS}^{\rm 1p2np}$	$\sigma_{\rm SPS}^{\rm 3np}$
570 ± 57 nb	600^{+130}_{-220} nb	40^{+80}_{-26} pb	24^{+35}_{-16} fb	430^{+95}_{-130} pb	< 5 ab	$5.2^{+9.6}_{-3.3}$ fb	14^{+17}_{-8} ab	12 ± 4 fb

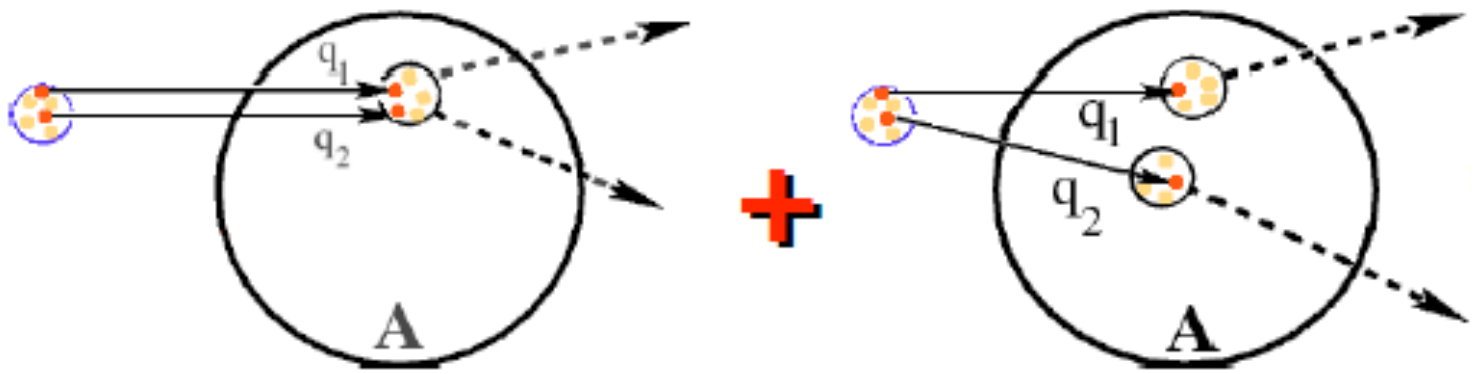
HO: *HELAC-Onia*
MG5NLO: *MadGraph5_aMC@NLO*
PY8: *Pythia8.2*

- Fixing $\sigma_{\rm eff,3} = (0.82 \pm 0.11) \times \sigma_{\rm eff,2}$ and fitting $\sigma_{\rm eff,2}$

$$\sigma_{\rm eff,2} = 2.7^{+1.4}_{-1.0}({\rm exp})^{+1.5}_{-1.0}({\rm theo})\ {\rm mb}$$

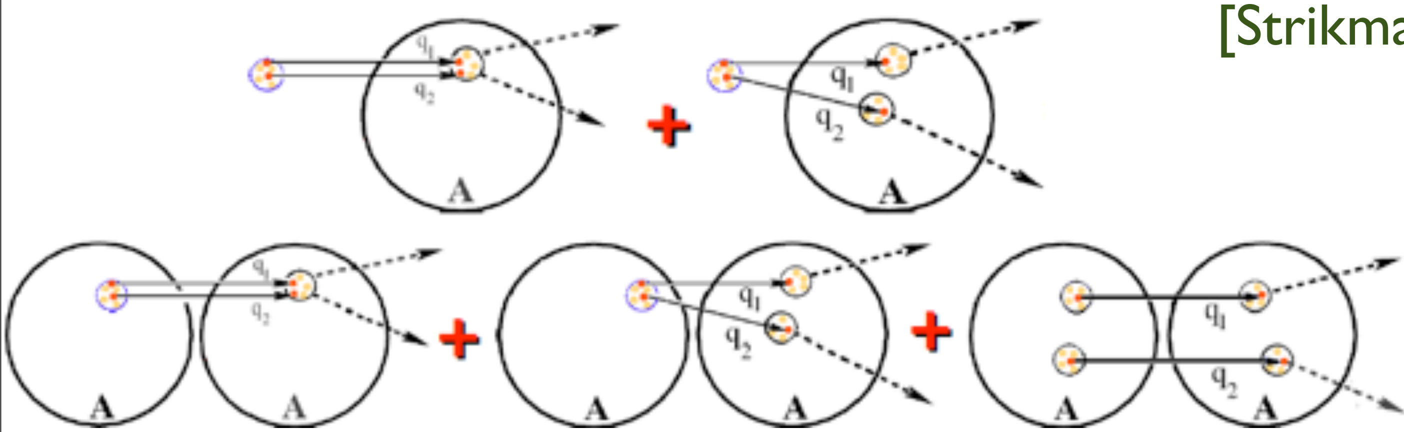
- Triple-J/psi fractions: ~6% SPS, ~74% DPS, ~20% TPS

DPS in heavy-ion collisions



DPS in Heavy-Ion Collisions

- **Geometrical enhancement because of several nucleons in a nucleus**



[Strikman, Treleani (2002); D. d'Enterria, A. Snigirev (2013, 2014)]

$$\sigma_{pA}^{\rm DPS} \approx 3A\sigma_{pp}^{\rm DPS}, \sigma_{pA}^{\rm SPS} \approx A\sigma_{pp}^{\rm SPS}$$

$$\sigma_{AA}^{\rm DPS} \approx \frac{A^{3.3}}{5}\sigma_{pp}^{\rm DPS}, \sigma_{AA}^{\rm SPS} \approx A^2\sigma_{pp}^{\rm SPS}$$

Assumptions: no nuclear modification and $\sigma_{{\rm eff},pp} \simeq 15$ mb

DPS in Heavy-Ion Collisions

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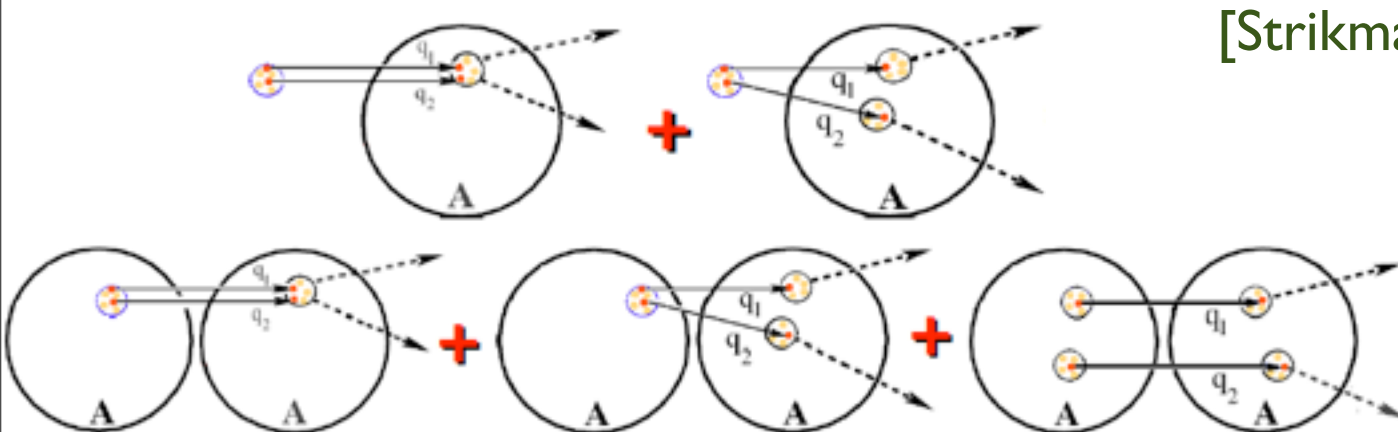
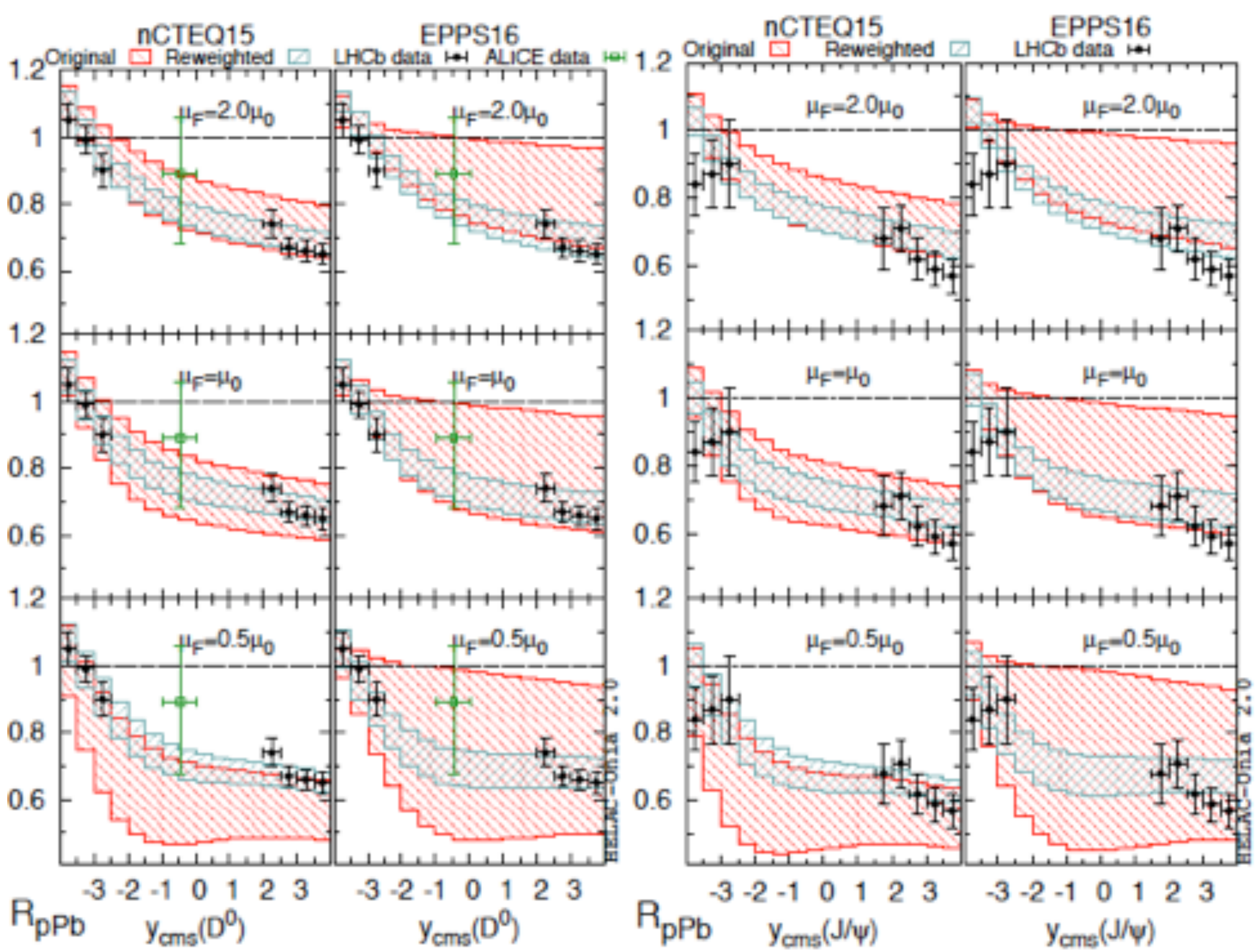
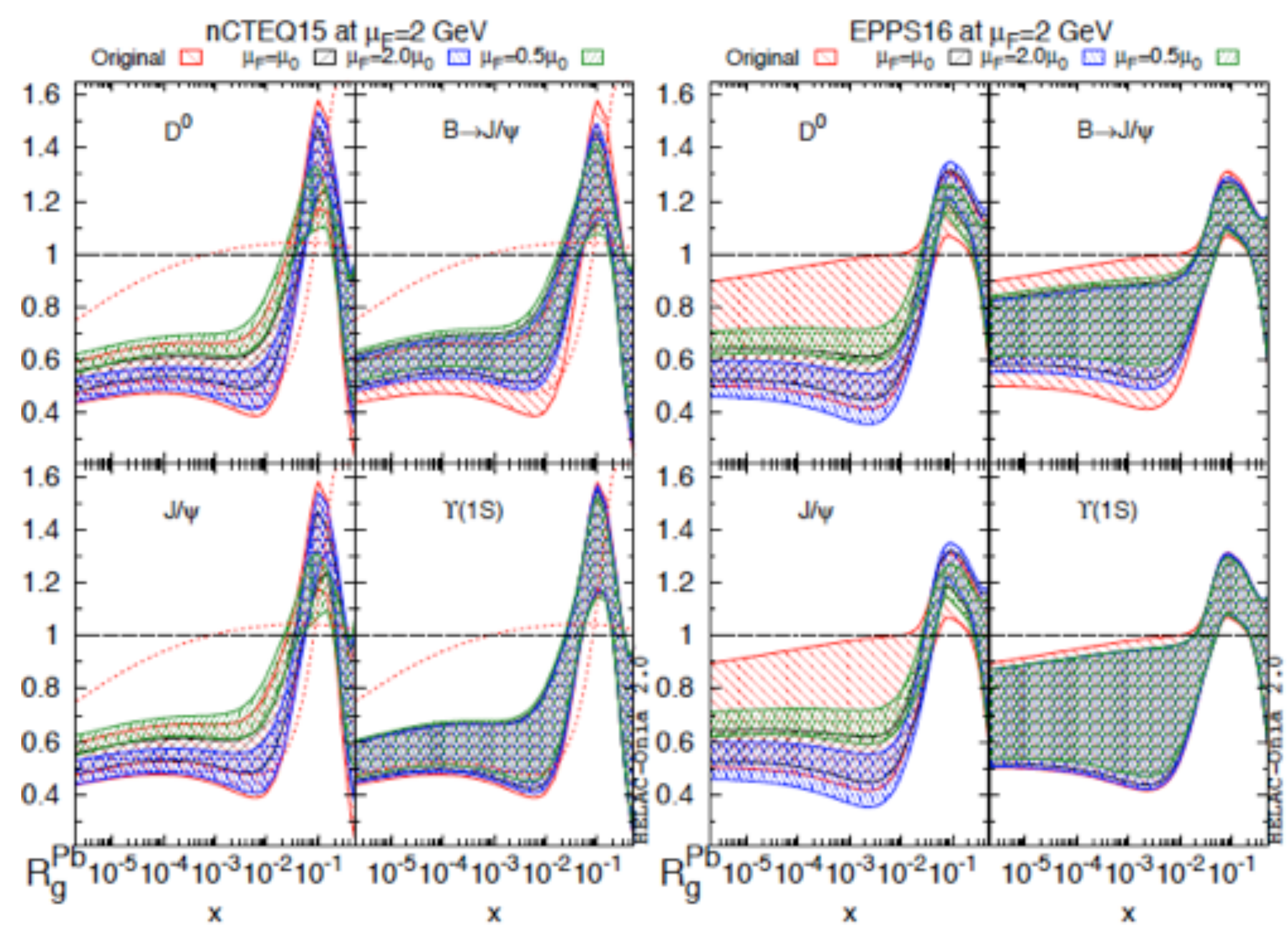


$$\sigma_{pA}^{\rm DPS} \approx 3A\sigma_{pp}^{\rm DPS}, \sigma_{pA}^{\rm SPS} \approx A\sigma_{pp}^{\rm SPS}$$

$$\sigma_{AA}^{\rm DPS} \approx \frac{A^{3.3}}{5}\sigma_{pp}^{\rm DPS}, \sigma_{AA}^{\rm SPS} \approx A^2\sigma_{pp}^{\rm SPS}$$

- **Of course, we know we cannot neglect the nuclear modifications ...**
  - E.g. gluon (anti)shadowing for heavy flavour and quarkonia [Kusina, et al. (PRL'18)]

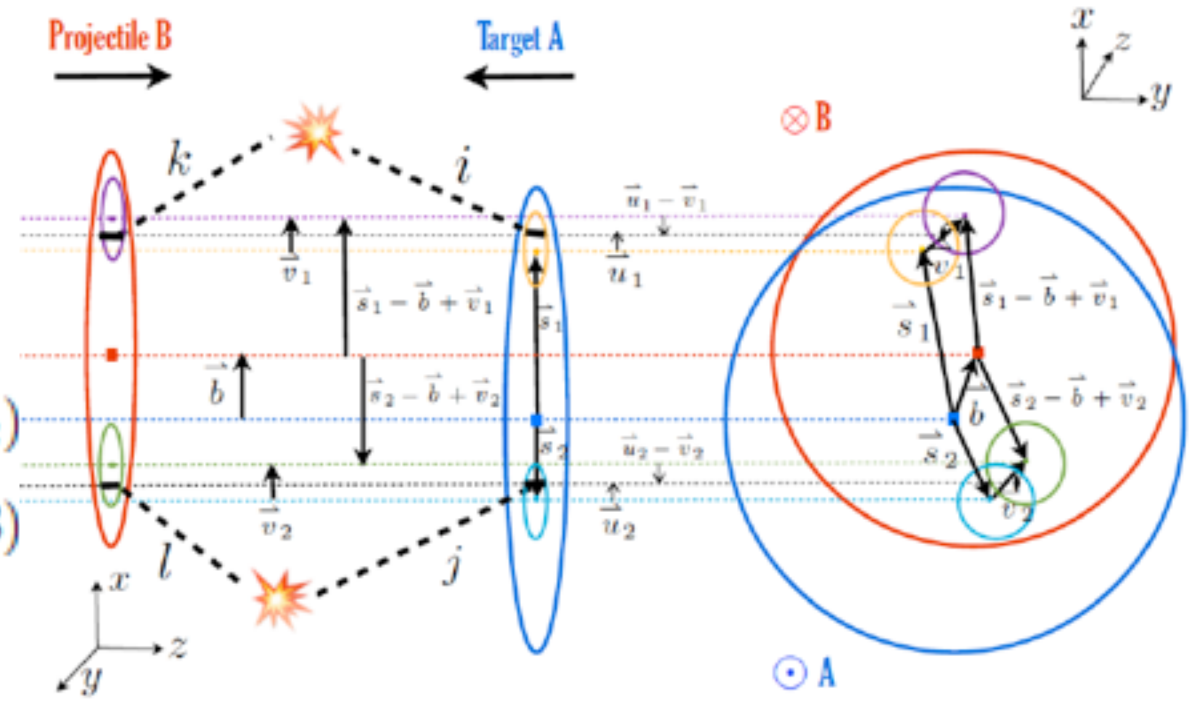




- **Let us accommodate both nPDF and geometric effect** [HSS (PRD'20)]

$$\sigma_{Q_1Q_2} = \frac{1}{1+\delta_{Q_1Q_2}} \sum_{i,j,k,l} \int dx_1 dx_2 dx_1' dx_2' d^2\mathbf{b}_1 d^2\mathbf{b}_2 d^2\mathbf{b} \times \Gamma_{ij}(x_1, x_2, \mathbf{b}_1, \mathbf{b}_2)\, \hat{\sigma}_{ik}^{Q_1}(x_1, x_1')\, \hat{\sigma}_{jl}^{Q_2}(x_2, x_2')\, \Gamma_{kl}(x_1', x_2', \mathbf{b}_1 - \mathbf{b}, \mathbf{b}_2 - \mathbf{b}),$$

$$\sigma^{\rm DPS}_{AB\to f_1 f_2} = \frac{1}{1+\delta_{f_1 f_2}} \sum_{i,j,k,l} \int dx_1 dx_2 dx_1' dx_2' \, \Gamma_A^{ij}(x_1, x_2, \vec{s}_1, \vec{s}_2, \vec{u}_1, \vec{u}_2) \hat{\sigma}_{ik}^{f_1}(x_1, x_1') \hat{\sigma}_{jl}^{f_2}(x_2, x_2') \times \Gamma_B^{kl}(x_1', x_2', \vec{s}_1 - \vec{b} + \vec{v}_1, \vec{s}_2 - \vec{b} + \vec{v}_2, \vec{u}_1 - \vec{v}_1, \vec{u}_2 - \vec{v}_2) \, d^2\vec{u}_1 d^2\vec{u}_2 d^2\vec{v}_1 d^2\vec{v}_2 d^2\vec{s}_1 d^2\vec{s}_2 d^2\vec{b}, \quad (8)$$



(a) Side view (b) Beam view

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$$\times\Gamma_{ij}(x_1,x_2,\mathbf{b}_1,\mathbf{b}_2)\,\hat{\sigma}_{ik}^{Q_1}(x_1,x_1')\,\hat{\sigma}_{jl}^{Q_2}(x_2,x_2')\,\Gamma_{kl}(x_1',x_2',\mathbf{b}_1-\mathbf{b},\mathbf{b}_2-\mathbf{b}),$$

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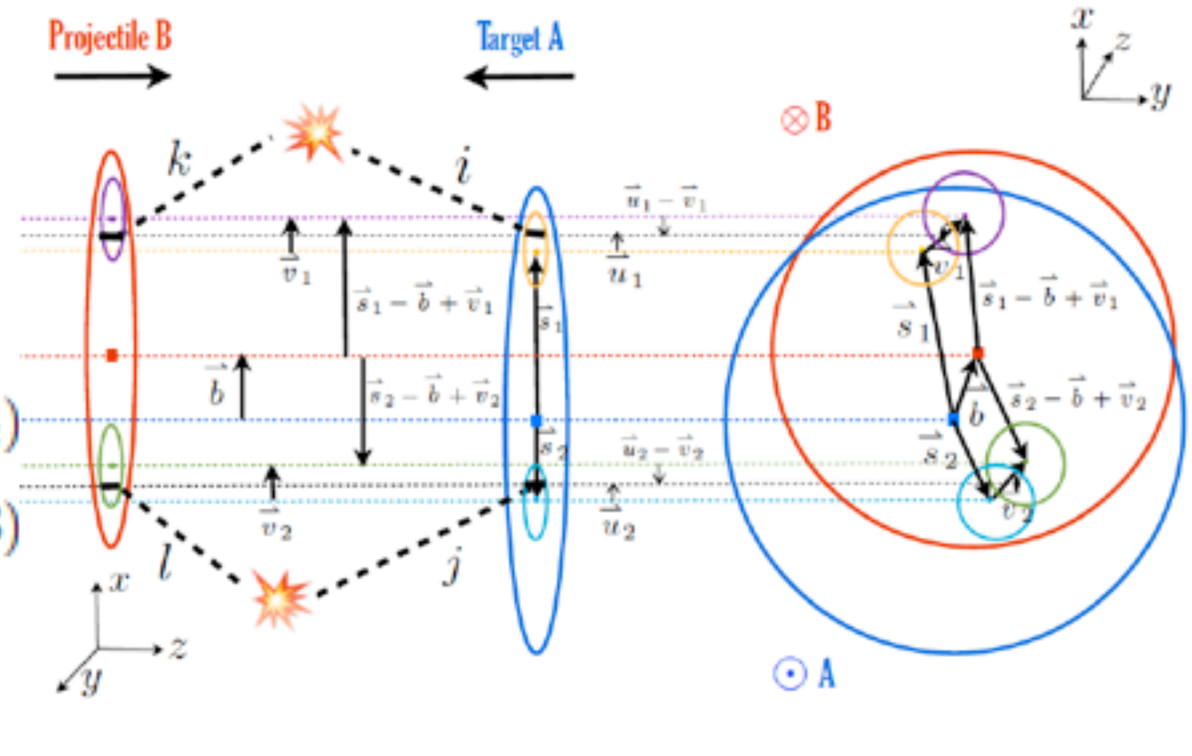
$$\Gamma_A^{ij}(x_1,x_2,\vec{s}_1,\vec{s}_2,\vec{u}_1,\vec{u}_2)\hat{\sigma}_{ik}^{f_1}(x_1,x_1')\hat{\sigma}_{jl}^{f_2}(x_2,x_2')\times$$
$$\Gamma_B^{kl}(x_1',x_2',\vec{s}_1-\vec{b}+\vec{v}_1,\vec{s}_2-\vec{b}+\vec{v}_2,\vec{u}_1-\vec{v}_1,\vec{u}_2-\vec{v}_2)$$
$$d^2\vec{u}_1d^2\vec{u}_2d^2\vec{v}_1d^2\vec{v}_2d^2\vec{s}_1d^2\vec{s}_2d^2\vec{b}, \quad (8)$$



(a) Side view (b) Beam view

- **We also need the knowledge of nuclear modification at different positions**

$$R_k^A(x,\vec{b})-1=\left(R_k^A(x)-1\right)G\left(\frac{T_A(\vec{b})}{T_A(\vec{0})}\right) \qquad k=g,q,\bar{q}$$

  - Ubiquitous in centrality-dependent observables
  - ...but mostly assume $G\left(\frac{T_A(\vec{s})}{T_A(\vec{0})}\right)=\frac{AT_A(\vec{s})}{T_{AA}(\vec{0})}$

DPS in Heavy-Ion Collisions

- **For example, considering** $p\mathrm{Pb} \to D^0 D^0 X$ [HSS (PRD'20)]

$$R^{\mathrm{DPS}}_{p\mathrm{Pb}\to D^0+D^0} = R^{D^0}_{p\mathrm{Pb}} R^{D^0}_{p\mathrm{Pb}} \left[\frac{3^{1-2a}(a+3)^{2a}}{2a+3} + \frac{\sigma_{\mathrm{eff},pp}}{\pi R_A^2}(A-1)\frac{9^{1-a}(a+3)^{2a}}{4(a+2)}\right]$$

$$+\left(R^{D^0}_{p\mathrm{Pb}} + R^{D^0}_{p\mathrm{Pb}}\right)\left[1 - \frac{3^{1-2a}(a+3)^{2a}}{2a+3} + \frac{\sigma_{\mathrm{eff},pp}}{\pi R_A^2}(A-1)\left(\frac{3^{2-a}(a+3)^{a}}{2(a+4)} - \frac{9^{1-a}(a+3)^{2a}}{4(a+2)}\right)\right]$$

$$+\left[-1 + \frac{3^{1-2a}(a+3)^{2a}}{2a+3} + \frac{\sigma_{\mathrm{eff},pp}}{\pi R_A^2}(A-1)\left(\frac{9}{8} + \frac{9^{1-a}(a+3)^{2a}}{4(a+2)} - \frac{3^{2-a}(a+3)^{a}}{(a+4)}\right)\right]$$

$$G\left(\frac{T_A(\vec{b})}{T_A(\vec{0})}\right) \propto \left(\frac{T_A(\vec{b})}{T_A(\vec{0})}\right)^a$$

$$R^f_{pA} \equiv \frac{\sigma_{pA\to f}}{A\sigma_{pp\to f}}$$

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$$G\left(\frac{T_A(\vec{b})}{T_A(\vec{0})}\right) \propto \left(\frac{T_A(\vec{b})}{T_A(\vec{0})}\right)^a$$

Either calculable or fixable by other measurements

$$R^f_{pA} \equiv \frac{\sigma_{pA\to f}}{A\sigma_{pp\to f}}$$

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$$\boxed{\frac{\sigma_{\mathrm{eff},pp}}{\pi R_A^2}(A-1) \simeq 5.23\left(\frac{\sigma_{\mathrm{eff},pp}}{34.8\ \mathrm{mb}}\right)}$$

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DPS in Heavy-Ion Collisions

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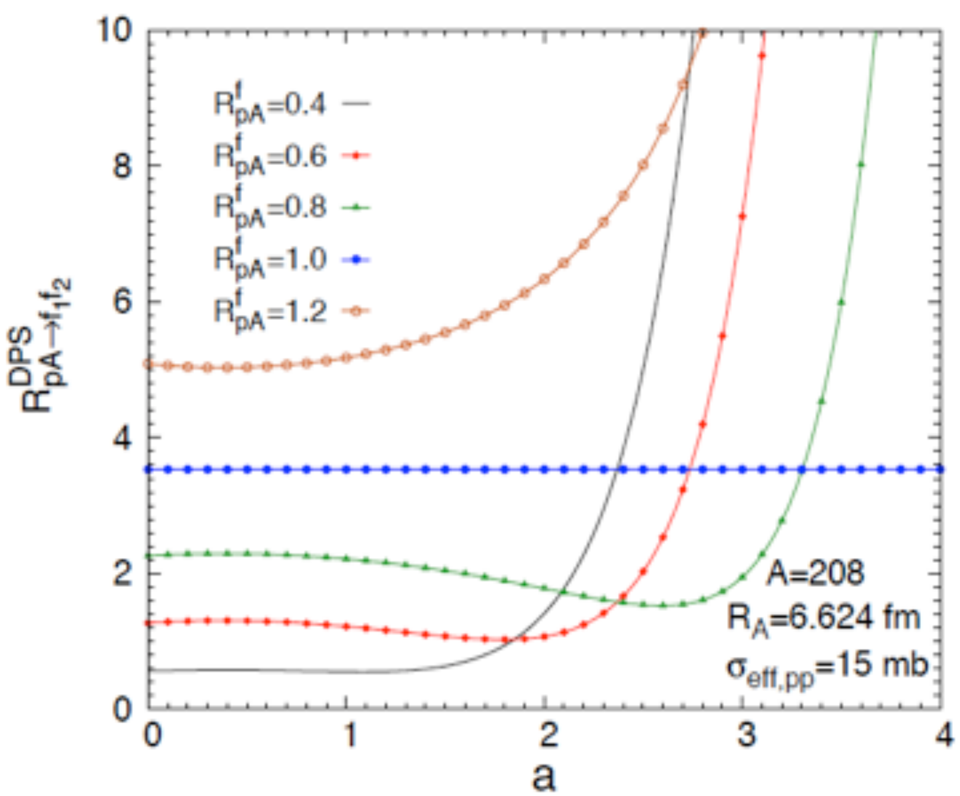


$$R^f_{pA} \equiv \frac{\sigma_{pA\to f}}{A\sigma_{pp\to f}}$$

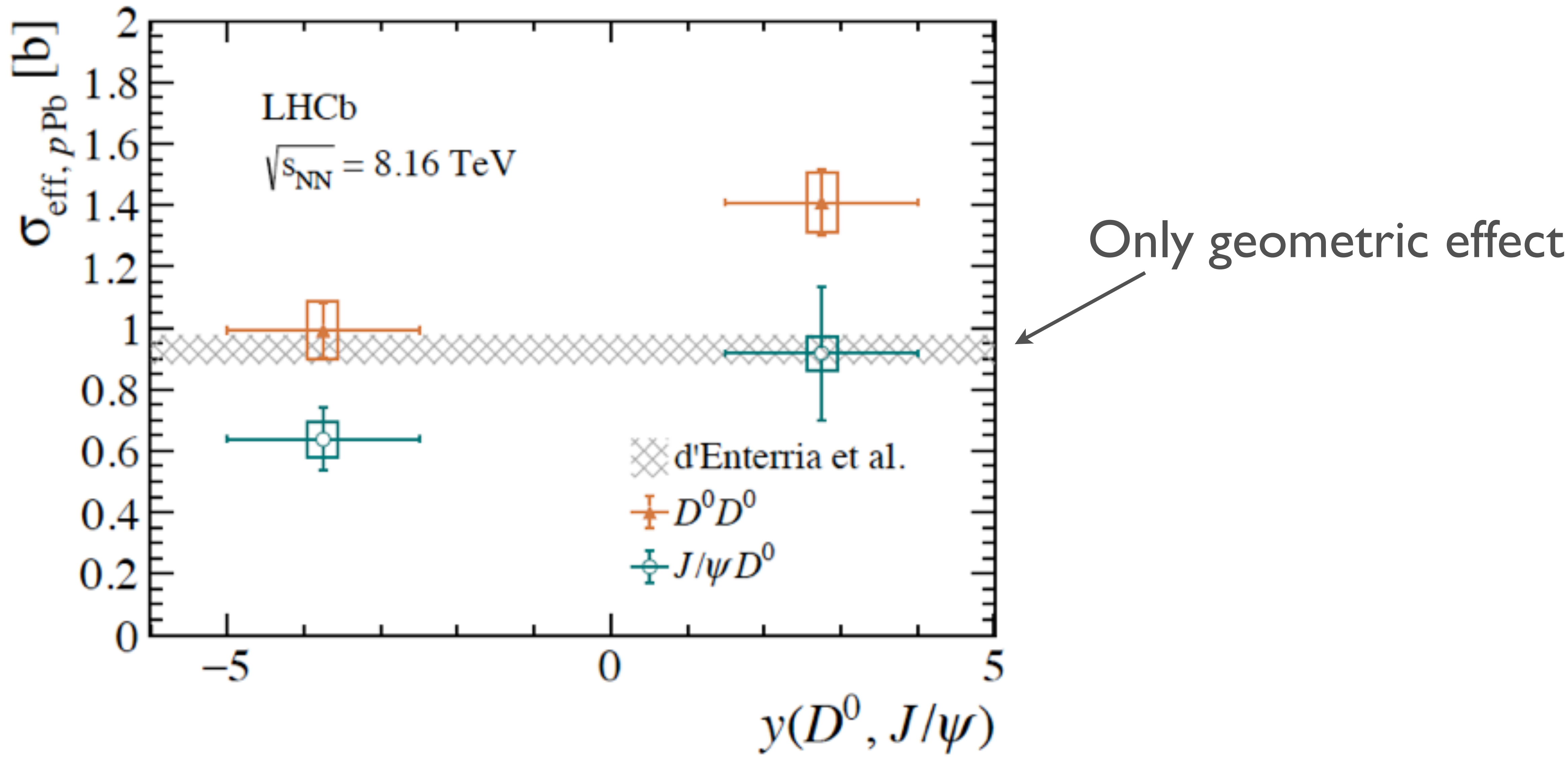
- DPS in heavy-ion potential to constrain G() !

DPS in Heavy-Ion Collisions

- **First DPS measurement in heavy-ion collisions by LHCb** [LHCb (PRL'20)]

$$\sigma_{\rm eff} = \frac{1}{1+\delta_{f_1 f_2}} \frac{\sigma_{p{\rm Pb}\to f_1}\sigma_{p{\rm Pb}\to f_2}}{\sigma_{p{\rm Pb}\to f_1 f_2}}$$

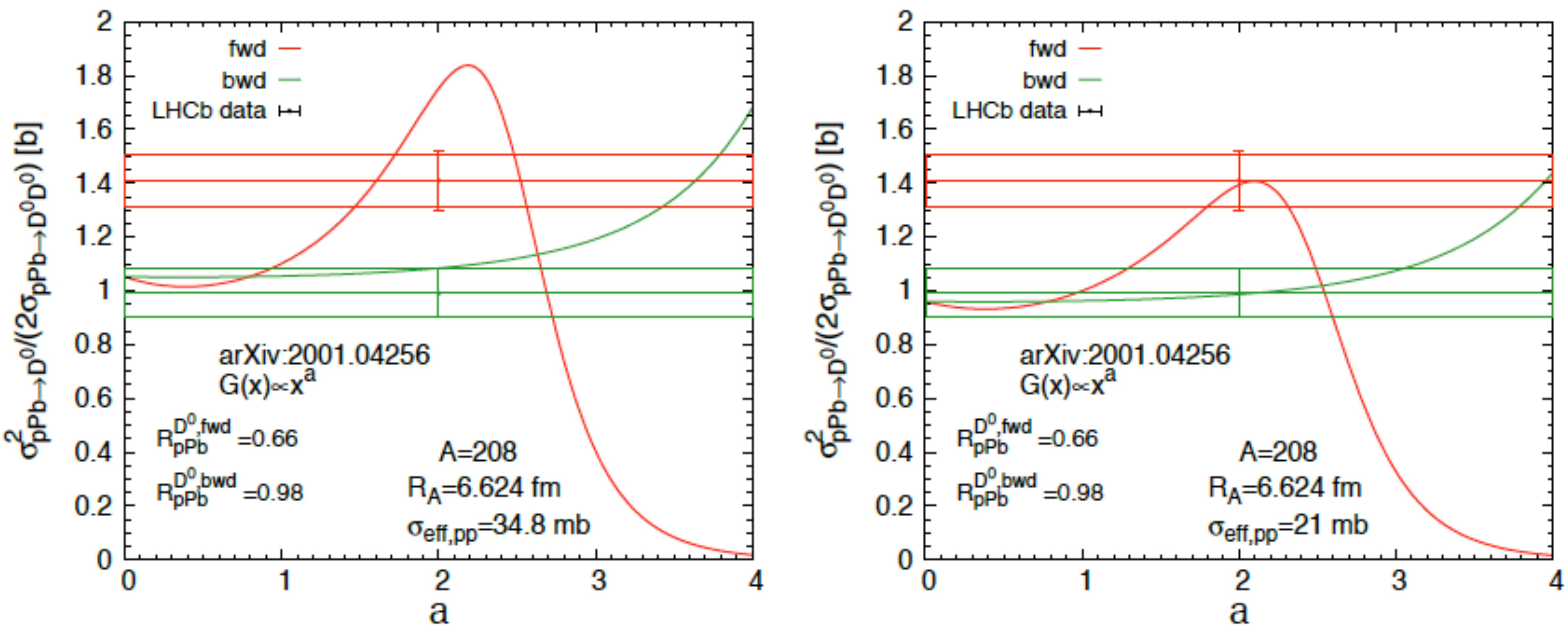
Caveats: $\sigma_{\rm eff} \equiv \sigma_{{\rm eff},p{\rm Pb}} \neq \sigma_{{\rm eff},pp}$



- Observe ~3A enhancement in DPS wrt ~A enhancement in SPS by comparing pA vs pp xs
- The pure geometric effect cannot explain the rapidity dependence

DPS in Heavy-Ion Collisions

- **Theoretical interpretation of the LHCb measurement**
  - J/psi+D^0 has the sizable SPS component [HSS (PRD'20)]
  - The SPS of D^0+D^0 is negligible in NLO pQCD caclulations [Helenius, Paukkunen (PLB'20)]
  - The b-dependent gluon shadowing can explain the rapidity dependence [HSS (PRD'20)]



$$G\left(\frac{T_A(\vec{b})}{T_A(\vec{0})}\right) \propto \left(\frac{T_A(\vec{b})}{T_A(\vec{0})}\right)^a$$

favoring a~2 and disfavoring a~1

Conclusion

- **LHC program offers an unprecedented avenue to study DPS & TPS.**
- **A lot of theoretical, phenomenological and experimental progress.**
- **NPS will reveal the first-ever multiple-body parton correlations in nucleon and nucleus**
- **Some novel observables can even tell us more (e.g. the impact parameter-dependent gluon shadowing)**
- **Don't be shy to attempt a 1st-ever measurement (e.g. TPS in pPb or DPS in PbPb ?)**

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Thank you for your attention !

Backup Slides

DPS in Heavy-Ion Collisions

- **As a concrete example, let us take** $p\mathrm{Pb} \to J/\psi + D^0$ [HSS (PRD'20)]

$$R^{\mathrm{DPS}}_{p\mathrm{Pb}\to J/\psi+D^0} = R^{J/\psi}_{p\mathrm{Pb}} R^{D^0}_{p\mathrm{Pb}} \left[\frac{3^{1-2a}(a+3)^{2a}}{2a+3} + \frac{\sigma_{\mathrm{eff},pp}}{\pi R_A^2}(A-1)\frac{9^{1-a}(a+3)^{2a}}{4(a+2)}\right]$$

$$+\left(R^{J/\psi}_{p\mathrm{Pb}} + R^{D^0}_{p\mathrm{Pb}}\right)\left[1 - \frac{3^{1-2a}(a+3)^{2a}}{2a+3} + \frac{\sigma_{\mathrm{eff},pp}}{\pi R_A^2}(A-1)\left(\frac{3^{2-a}(a+3)^{a}}{2(a+4)} - \frac{9^{1-a}(a+3)^{2a}}{4(a+2)}\right)\right]$$

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$$+ \left(R^{J/\psi}_{p\mathrm{Pb}} + R^{D^0}_{p\mathrm{Pb}}\right)\left[1 - \frac{3^{1-2a}(a+3)^{2a}}{2a+3} + \frac{\sigma_{\mathrm{eff},pp}}{\pi R_A^2}(A-1)\left(\frac{3^{2-a}(a+3)^{a}}{2(a+4)} - \frac{9^{1-a}(a+3)^{2a}}{4(a+2)}\right)\right]$$
$$+ \left[-1 + \frac{3^{1-2a}(a+3)^{2a}}{2a+3} + \frac{\sigma_{\mathrm{eff},pp}}{\pi R_A^2}(A-1)\left(\frac{9}{8} + \frac{9^{1-a}(a+3)^{2a}}{4(a+2)} - \frac{3^{2-a}(a+3)^{a}}{(a+4)}\right)\right]$$

$$G\left(\frac{T_A(\vec{b})}{T_A(\vec{0})}\right) \propto \left(\frac{T_A(\vec{b})}{T_A(\vec{0})}\right)^a$$

Either calculable or fixable by other measurements

DPS in Heavy-Ion Collisions

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