



Vector boson production and TMD extraction at N4LL

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<https://www.ucm.es/iparcos/>

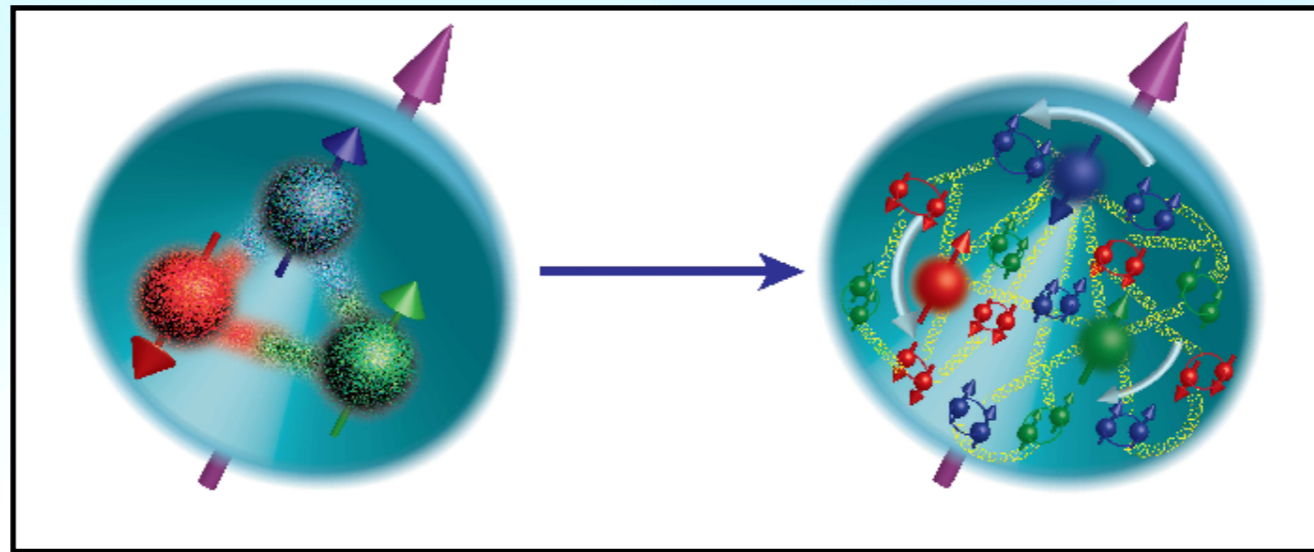
CPAN-L, SANTANDER 02/10, 2023



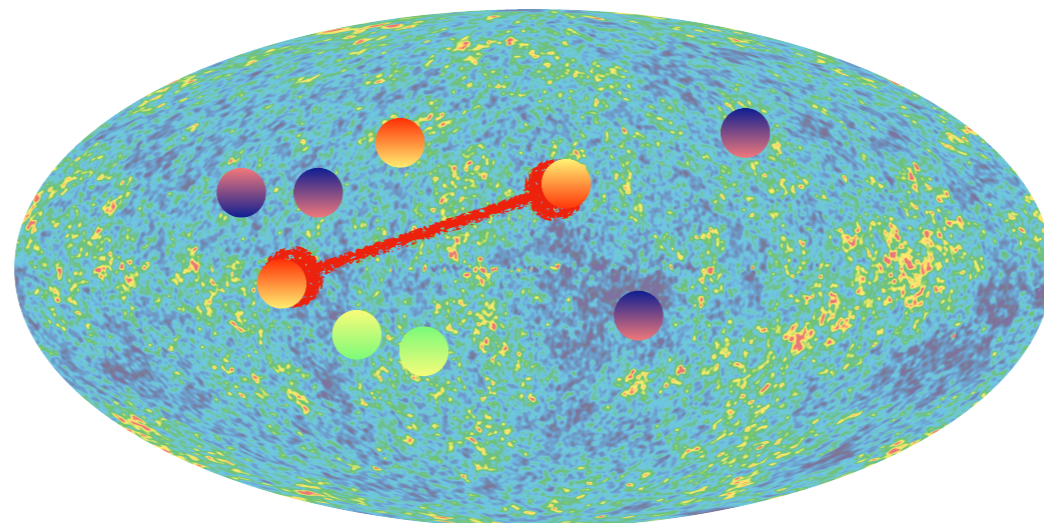
Motivation

Now suppose you have a proton.

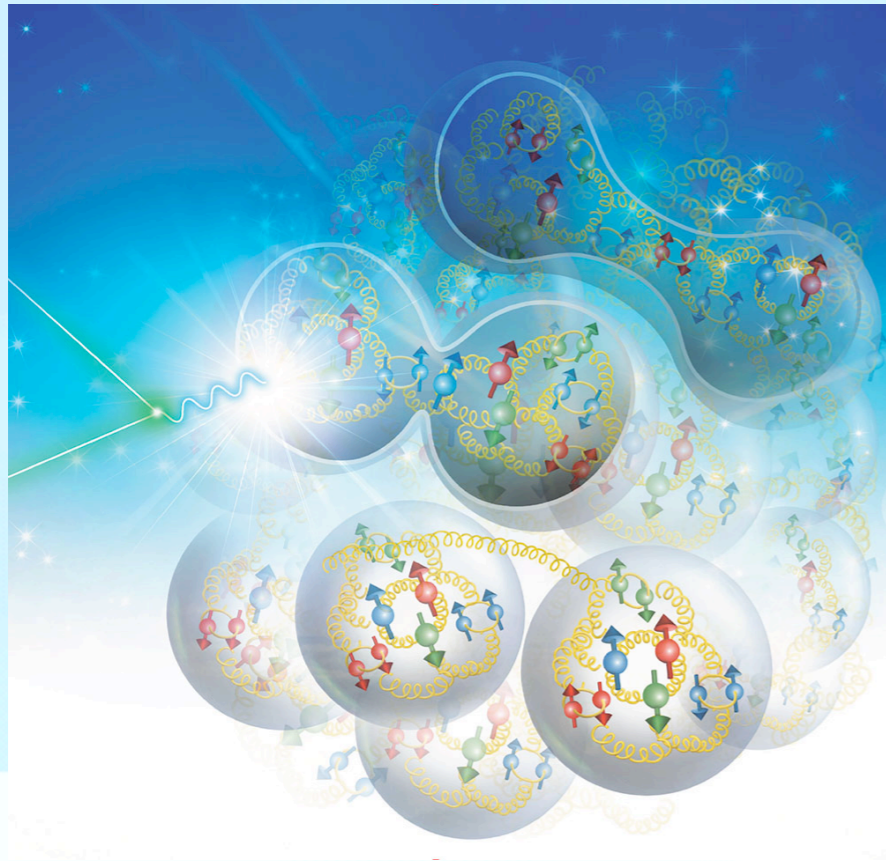
We have made experiments showing that we have 3 quarks + pairs of quarks-antiquarks + gluons



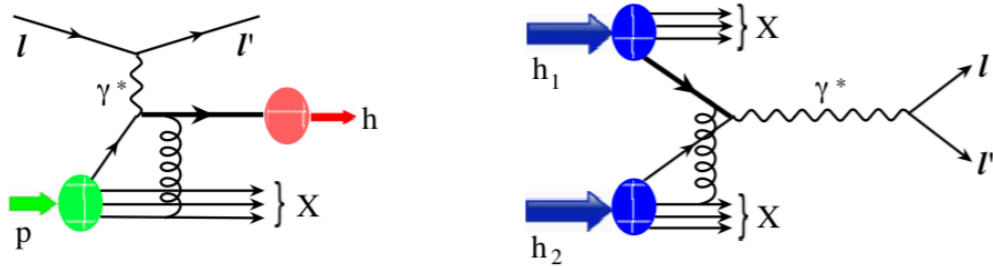
How are quarks in two distinct points correlated? Spin?



Motivation



- We need a virtual photon coupled to lepton pairs to reduce QCD uncertainties: Drell-Yan, Semi-inclusive DIS, $e^+e^- \rightarrow 2j$
- We need to address a method to identify fundamental quark distributions in the cross section: power expansion, operator product expansion (in combination with effective field theory (SCET), or background field method)
- Overcome all technical difficulties (40 years of research behind!)



TMD factorization

LP!

$$\frac{d\sigma}{dQ^2 dy dq_T^2} = \sigma_0 \sum_{f_1, f_2} \int \frac{d^2\mathbf{b}}{4\pi} e^{i(\mathbf{b}\cdot\mathbf{q}_T)} H_{f_1 f_2}(Q, Q) \{R[\mathbf{b}; (Q, Q^2)]\}^2 F_{f_1 \leftarrow h_1}(x_1, \mathbf{b}) F_{f_2 \leftarrow h_2}(x_2, \mathbf{b})$$

In recent years we have learnt a lot about this formula. For instance:

Its range of applicability is provided by $\delta = \frac{q_T}{Q} \ll 1$, fixed- q_T , $\delta \sim 0.25$

We have a non-perturbative evolution kernel (whose perturbative part is known at N3LO and allows N4LL resummation). We can work with different schemes (CSS, ζ -prescription, ..).

We have a re-factorization of TMD at large transverse momentum in Wilson coefficients (now at N3LO!!) and PDF (now at NNLO!!)

PDF are just part of a model

$$F_{f \leftarrow h}(x, b) = \sum_{f'} f_{NP}(x, b) \int_x^1 \frac{dy}{y} C_{f \leftarrow f'}(y, \mathbf{L}_{\mu_{\text{OPE}}}, a_s(\mu_{\text{OPE}})) f_{f \leftarrow h}(x/y, \mu_{\text{OPE}})$$

UNPOLARIZED TMD MATCHING TO COLLINEAR FUNCTIONS: DY AND SIDIS IN THE ASYMPTOTIC LIMIT

$$\lim_{b \rightarrow 0} f_{1,f \leftarrow h}(x, b) = \sum_{f'} \int_x^1 \frac{dy}{y} C_{f \leftarrow f'} \left(\frac{x}{y}, \mathbf{L}_{\mu_{\text{OPE}}}, a_s(\mu_{\text{OPE}}) \right) f_{1,f' \leftarrow h}(y, \mu_{\text{OPE}}),$$
$$\lim_{b \rightarrow 0} D_{1,f \rightarrow h}(z, b) = \sum_{f'} \int_z^1 \frac{dy}{y} \mathbb{C}_{f \rightarrow f'} \left(\frac{z}{y}, \mathbf{L}_{\mu_{\text{OPE}}}, a_s(\mu_{\text{OPE}}) \right) \frac{d_{1,f' \rightarrow h}(y, \mu_{\text{OPE}})}{y^2},$$

The Wilson coefficients (C, \mathbb{C}) are all known at higher orders!!

NNLO **TMDPDF / TMDFF:** T. Gehrmann et al. JHEP 06 (2014) 155, M.G. Echevarria et al. Phys. Rev. D93 (2016) 011502, JHEP 09 (2016) 004, M. X. Luo et al. JHEP 01 (2020) 040, JHEP 10 (2019) 083

NNNL **TMDPDF / TMDFF:** M. X. Luo et al. Phys.Rev.Lett. 124 (2020) 9, 092001, JHEP 06 (2021) 115, M. Ebert et al. JHEP 09 (2020) 146

TMD factorization

We can :

Perform an extraction of TMD at N⁴LL (higher order than PDF..)

Analyze the source of errors

Be ready for NLP corrections

In this talk I will consider the first two points

We call the new Artemide code extraction

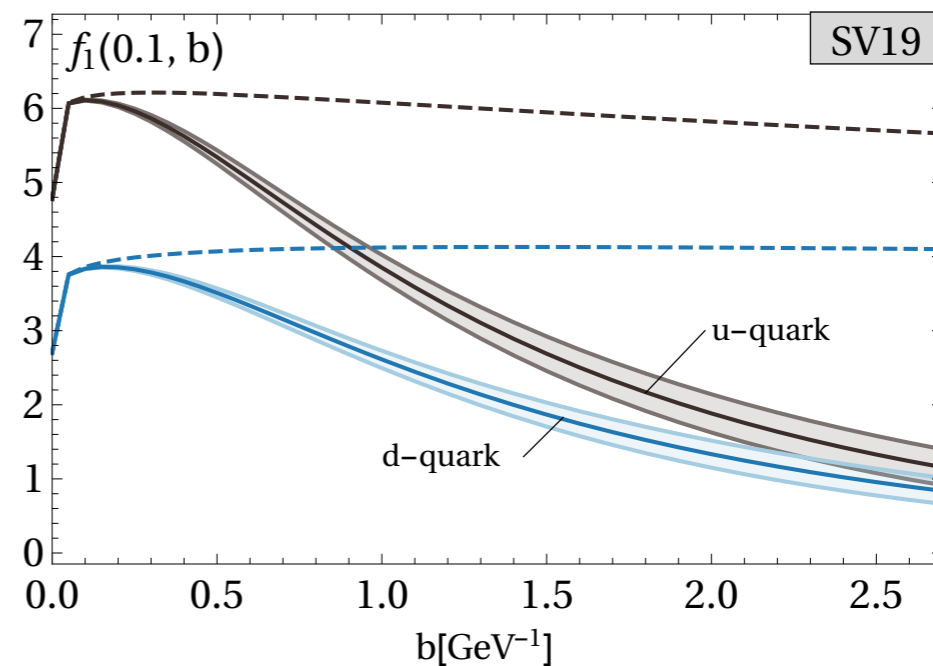
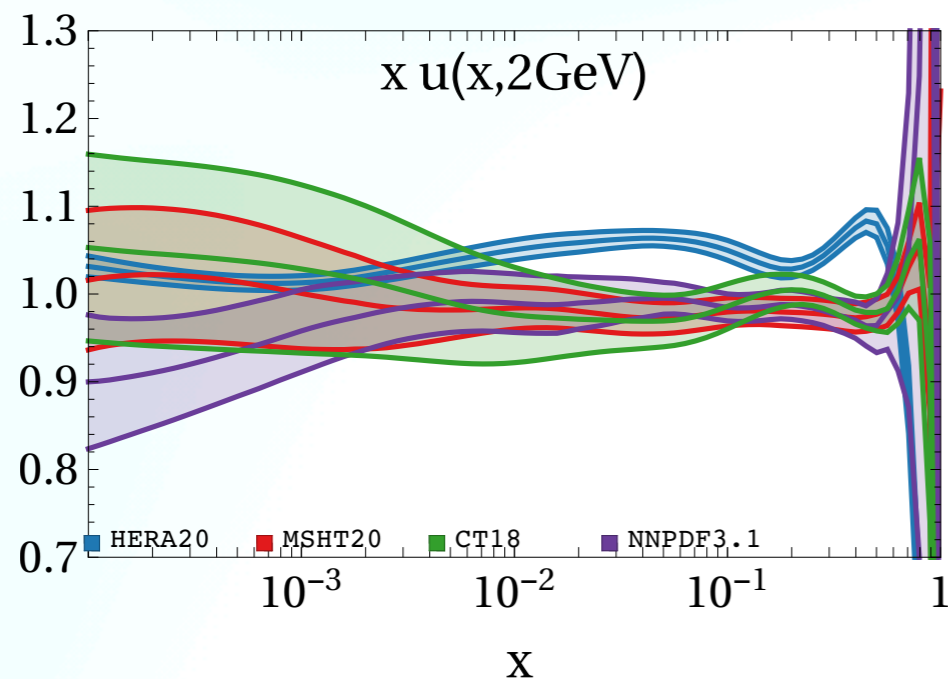
V. Moos, I.S., A. Vladimirov, P. Zurita e-Print: 2305.07473 [hep-ph]

The logo for ART23, featuring the letters 'ART' in a bold, blue, sans-serif font, followed by the number '23' in a lighter blue, sans-serif font. The '2' and '3' are slightly larger and more stylized than the 'ART'.

In SV19 we tried with several PDF sets

PDF set	χ^2_{DY}/N_{pt}
CT14	1,59
HERAPDF2.0	0,97
MMHT14	1,34
NNPDF3.1	1,14
PDF4LHC15	1,53

Also, in SV19, for $b \rightarrow 0$, the uncertainty bands $\rightarrow 0$.



The PDF bias

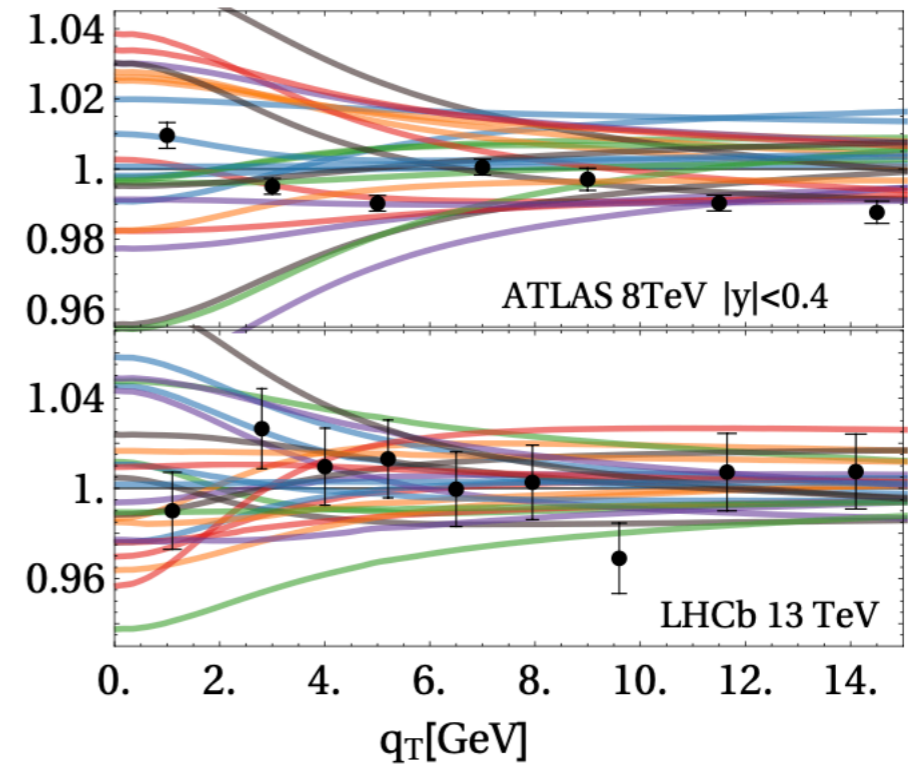
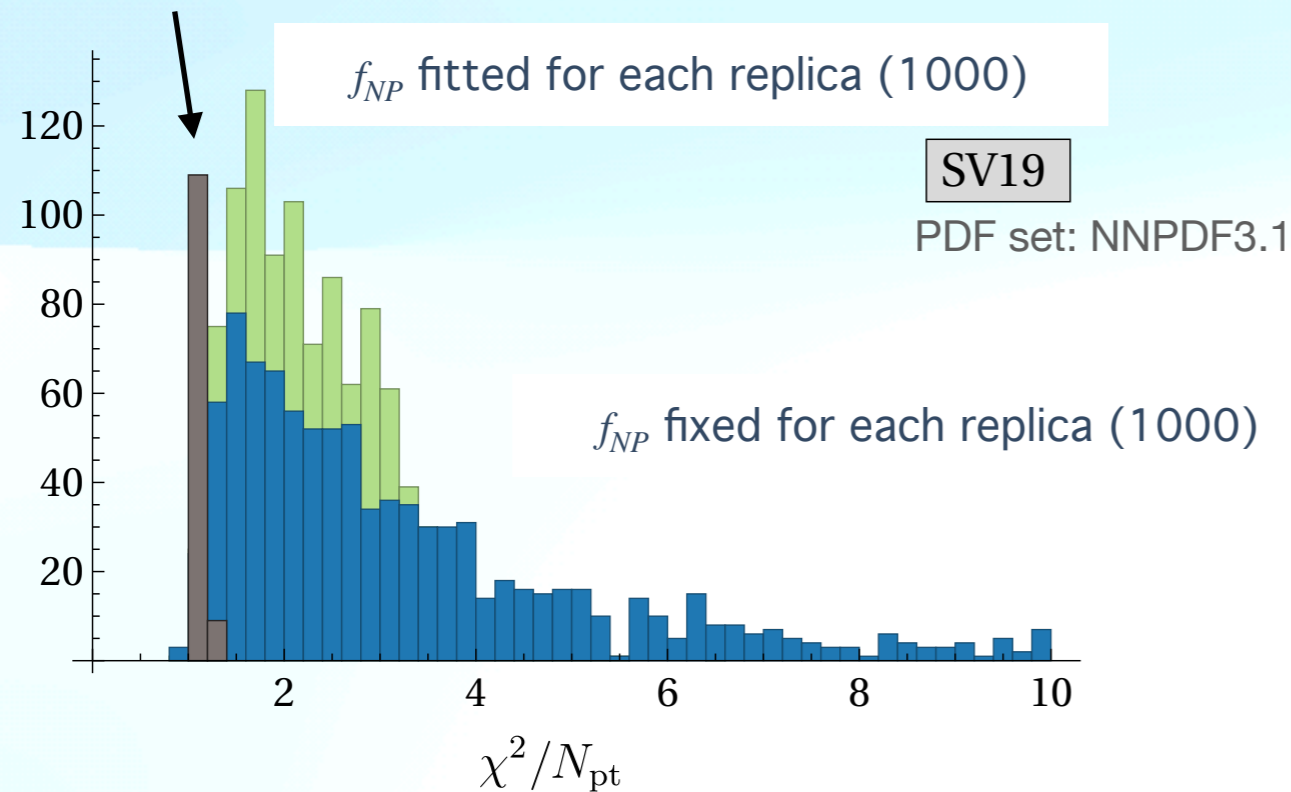
 So we have some questions to answer:

1. Can we get *good TMD fits* for different collinear PDFs?
2. Would they have sensible uncertainty bands?
3. Would they be consistent with each other?

FLAVOR INDEPENDENT F_{NP}

Most of replicas (64%) have $\chi^2/N > 2$.
Each replica has a peculiar shape

EXP error



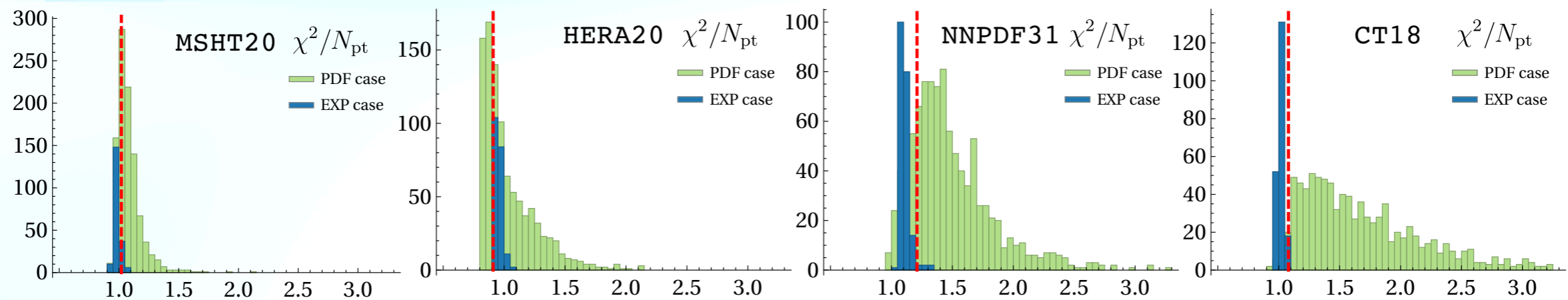
PDF uncertainties and flavour dependence

M. Bury, F. Hautmann, S. Leal-Gomez, I. Scimemi, A. Vladimirov, PZ, **JHEP 10 (2022) 118**



Flavor separation make fits more PDF set independent and modeling simpler

$$f_{NP}^f(x, b) = \exp\left(-\frac{\lambda_1^f(1-x) + \lambda_2^f x}{\sqrt{1 + \lambda_0 x^2 b^2}} \mathbf{b}^2\right) \quad f = u, \bar{u}, d, \bar{d}, sea$$



ALL PDF DISTRIBUTIONS HAVE SIMILAR χ^2

THE SPREAD OF χ^2 OF PDF REPLICA IS HIGHLY REDUCED

FINAL χ^2 : MSHT20 (1.12), HERA20 (0.91), NNPDF31 (1.21), CT18 (1.08)

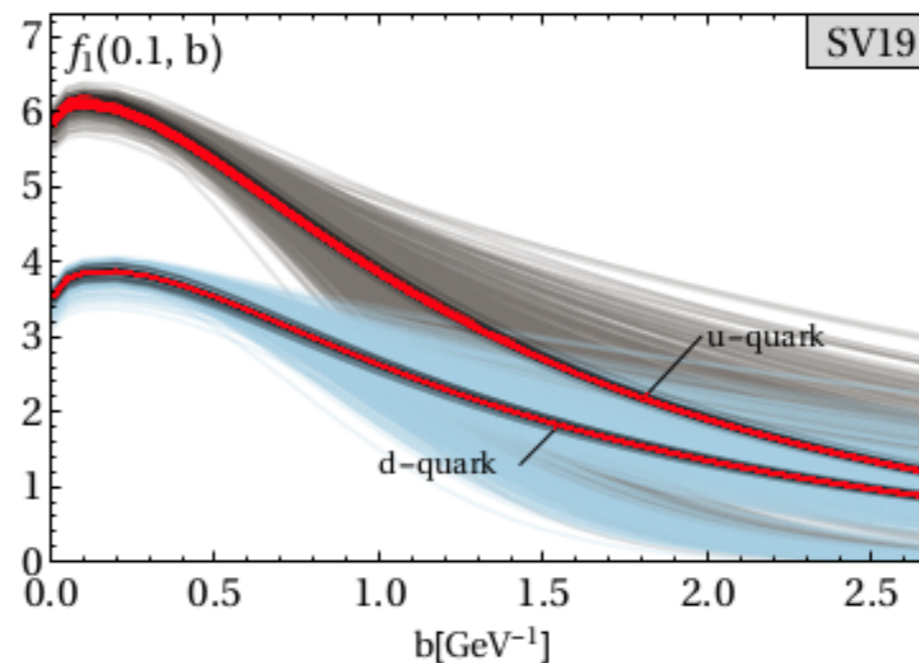
PDF uncertainties and flavour dependence

M. Bury, F. Hautmann, S. Leal-Gomez, I. Scimemi, A. Vladimirov, PZ, **JHEP 10 (2022) 118**

• We include the PDF uncertainties while keeping f_{NP} fixed.

• We re-fit TMD, for each PDF replica.

• We get reasonable uncertainty bands.

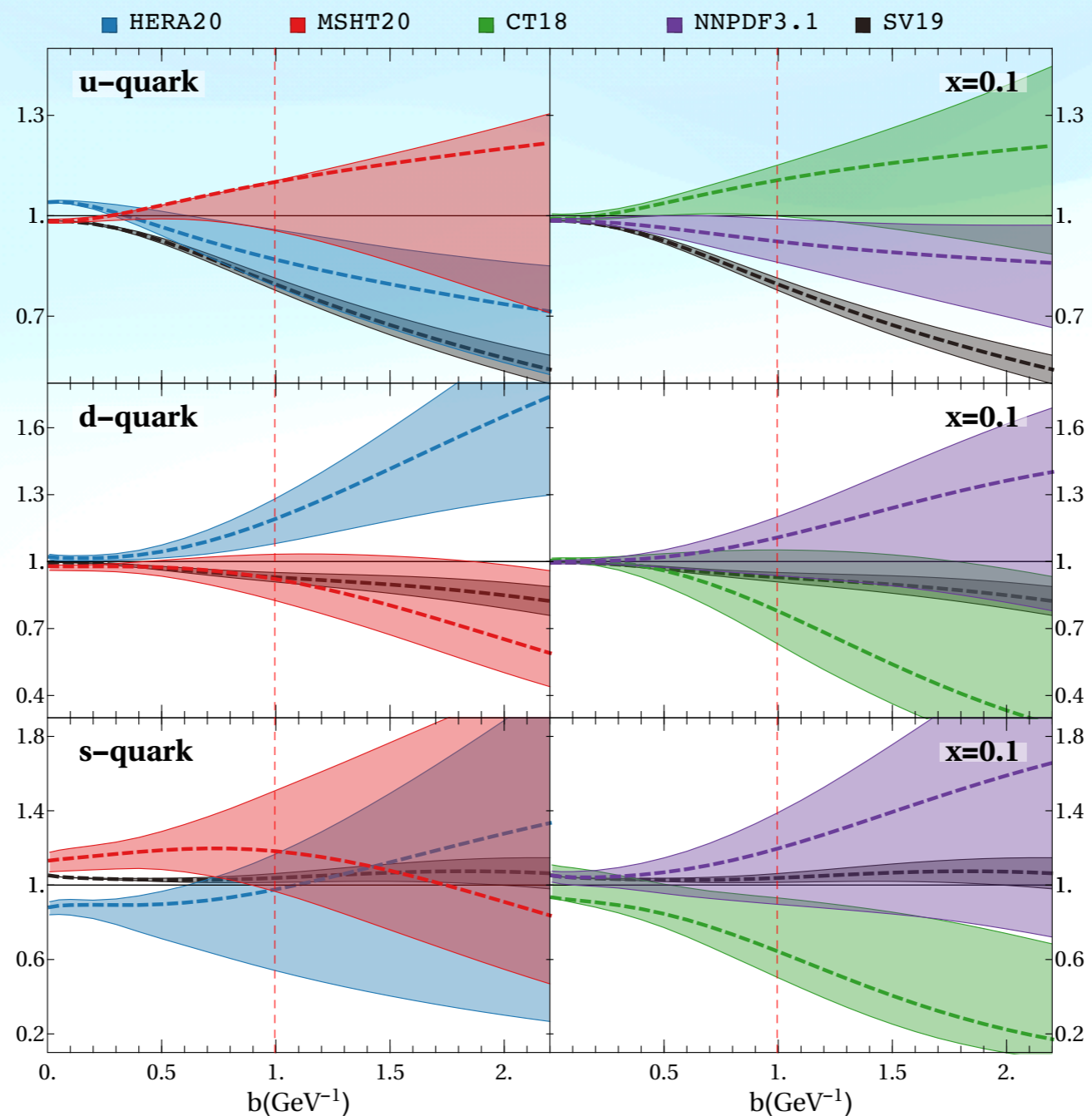


PDF uncertainties and flavour dependence

M. Bury, F. Hautmann, S. Leal-Gomez, I. Scimemi, A. Vladimirov, PZ, **JHEP 10 (2022) 118**



The TMD obtained from different sets agree reasonably




ART23

- 📌 Flavor dependence.
- 📌 All the latest datasets!
- 📌 W-boson production!
- 📌 Increased perturbative accuracy! (N^4LL)
- 📌 Includes collinear PDF uncertainties!
- 📌 A full new fit to Drell-Yan data.


ART23: details

Evolution:

- We use the ζ prescription (I.S., A. Vladimirov *JHEP* 08 (2018) 003)
- We use the integral form of the evolution kernel to introduce a scale dependence similar to CSS for direct comparison

$$\mathcal{D}(b, \mu) = \mathcal{D}_{\text{small-}b}(b^*, \mu^*) + \int_{\mu^*}^{\mu} \frac{d\mu'}{\mu'} \Gamma_{\text{cusp}}(\mu') + \mathcal{D}_{\text{NP}}(b) \quad b^*(b) = \frac{b}{\sqrt{1 + \frac{b^2}{B_{\text{NP}}^2}}} = \frac{2e^{-\gamma_E}}{\mu^*}$$


- We discover that we are sensitive to log corrections to the NP part of the evolution kernel

$$\mathcal{D}_{\text{NP}}(b) = bb^* \left[c_0 + c_1 \ln \left(\frac{b^*}{B_{\text{NP}}} \right) \right]$$


ART23: details

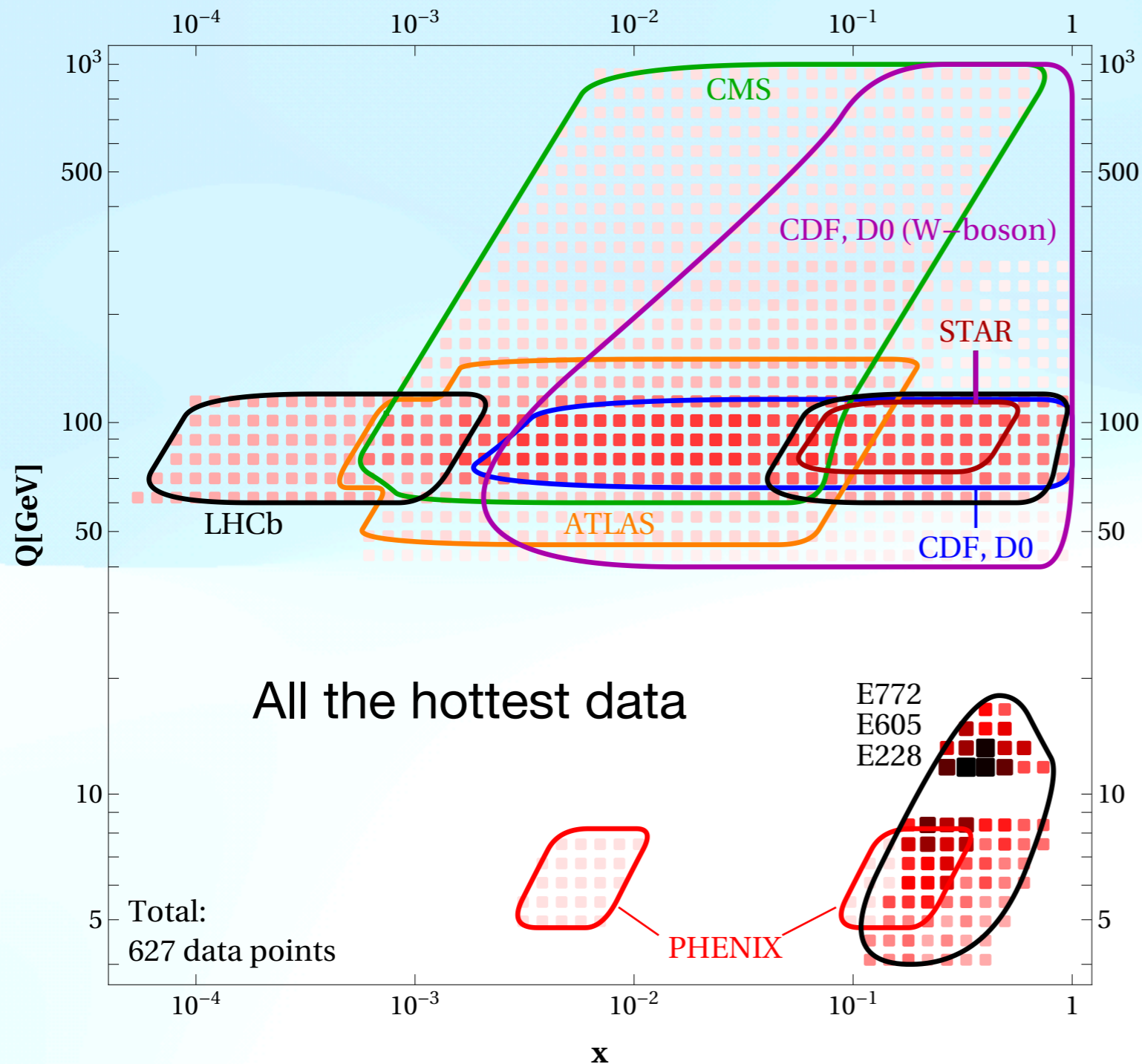
Simple Parameterization: $f_{NP}^f(x, b) = \frac{1}{\cosh\left(\left(\lambda_1^f(1-x) + \lambda_2^f x\right)b\right)}$

$f = u, \bar{u}, d, \bar{d}, sea$

In total, 13 parameters

Reference PDFs: MSHT20

ART23: details



627 data points

New in!

PHENIX: DY data at $\sqrt{s} = 200$ GeV

STAR: Z/ γ -boson production at $\sqrt{s} = 510$ GeV (preliminary).

CMS and **LHCb:** y-differential Z-boson production at $\sqrt{s} = 13$ TeV.

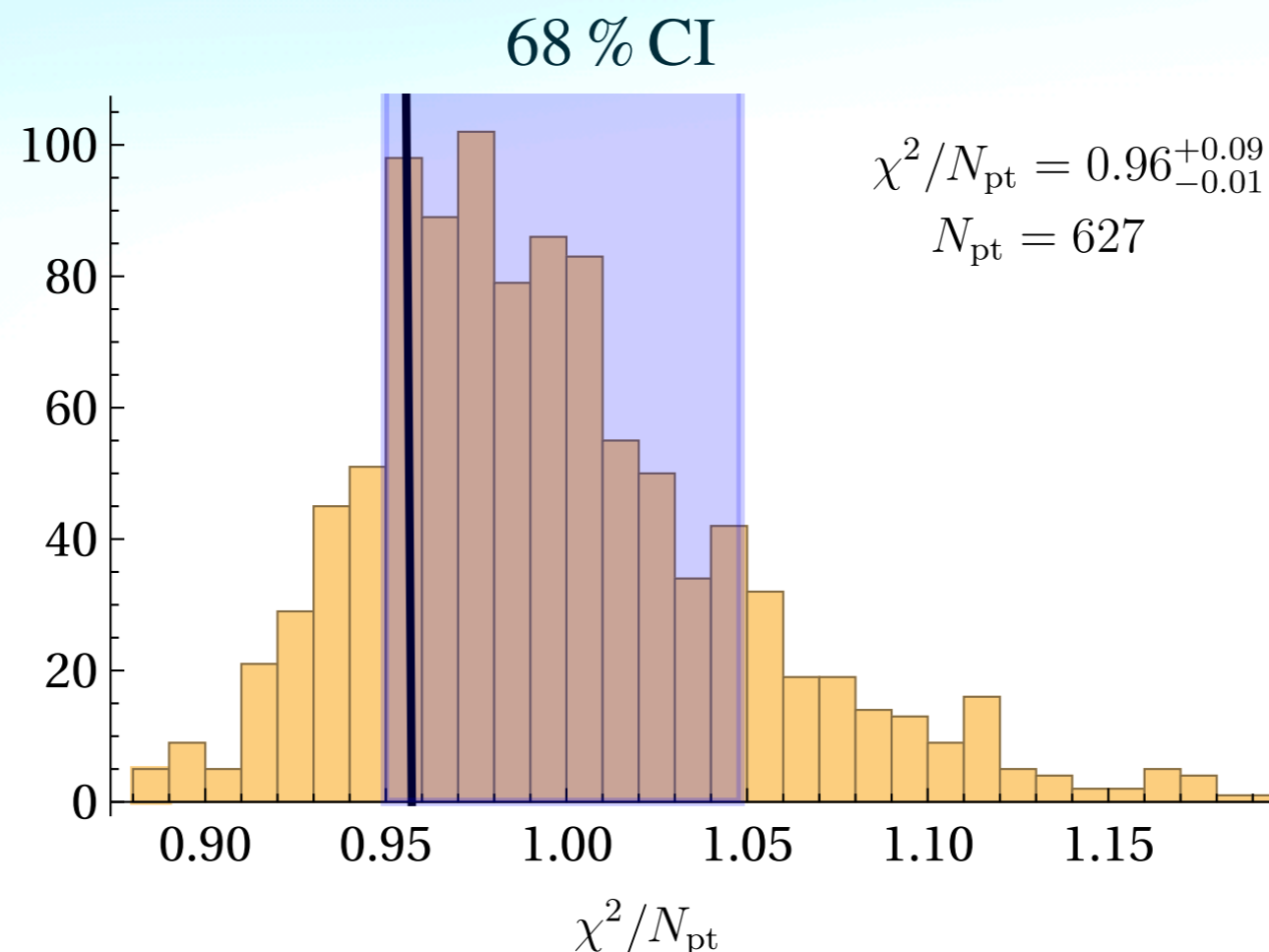
ATLAS: high precision differential Z-boson cross-section.

CMS: high-Q neutral-boson production.

Tevatron: W-boson production.

ART23: details

- 📌 Fitting procedure: construct simultaneous replicas of the **data AND** the **PDFs**. Then fit.
- 📌 The number of replicas needed to have a faithful representation of the TMDPDF distribution was deemed to be 1000.



ART23: results

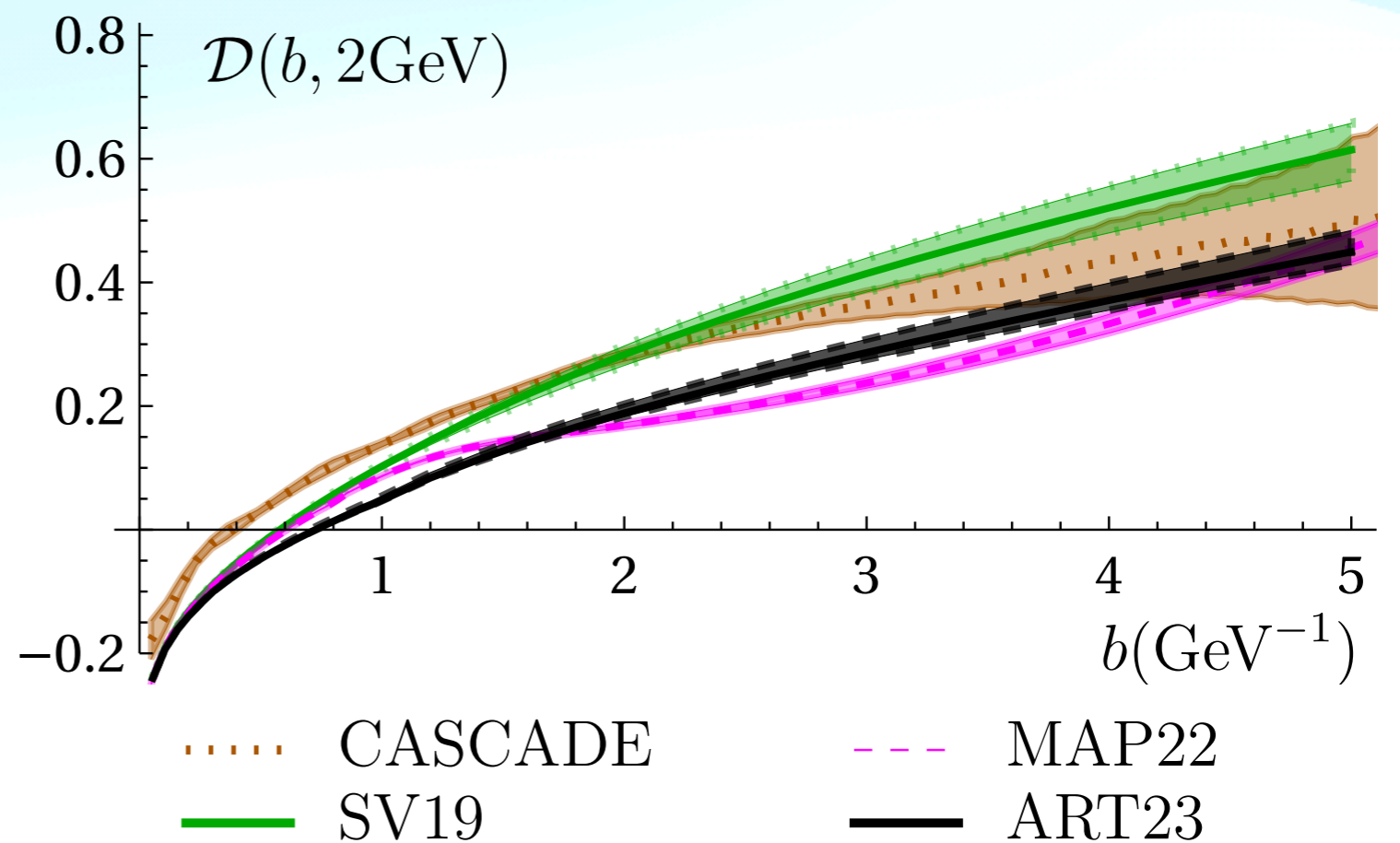
- overall improvement w.r.t. SV19. Specially for the LHC data. Higher precision plays a key role here.
- more realistic uncertainty bands than in SV19.

CS kernel close to the one from the global fit MAP22

$$B_{\text{NP}} = 1.56^{+0.13}_{-0.09} \text{ GeV}$$

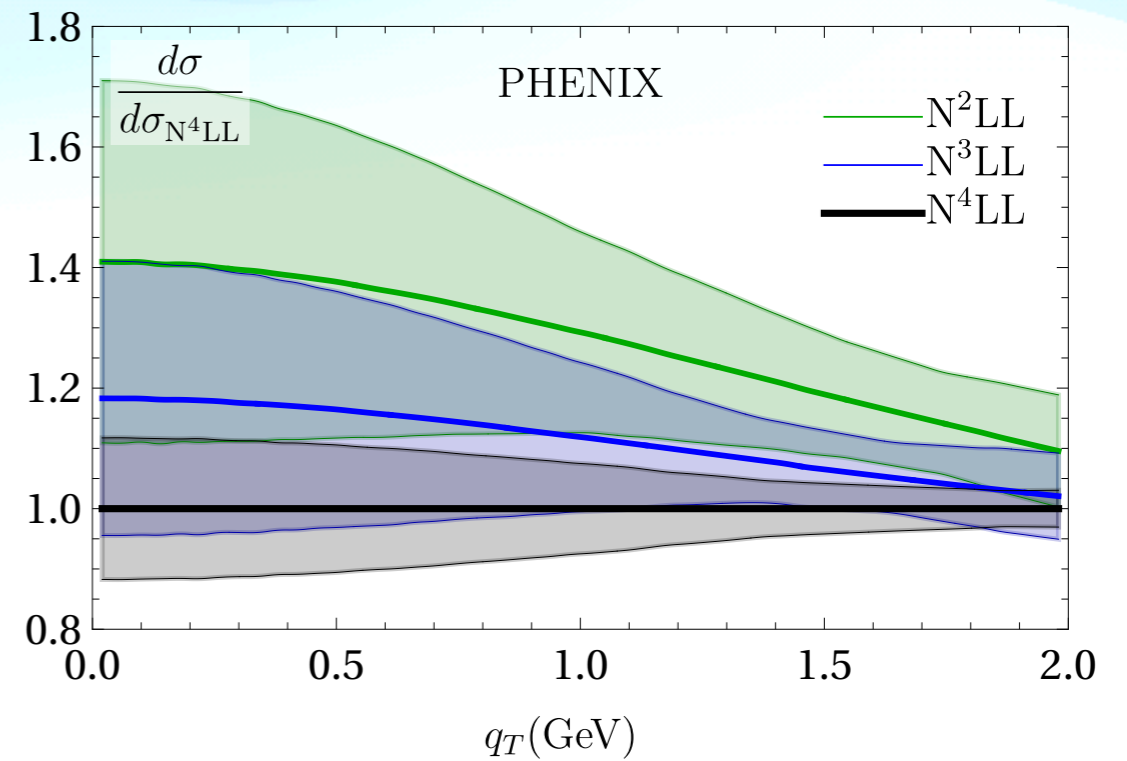
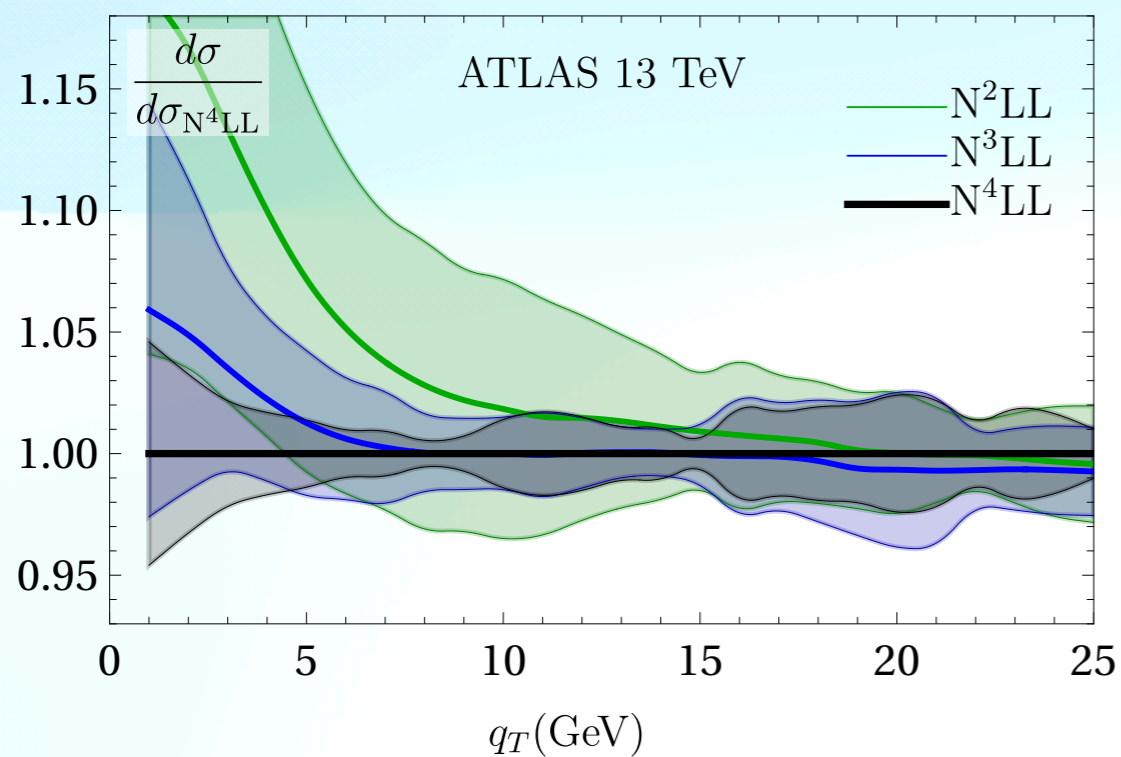
$$c_0 = 3.69^{+0.65}_{-0.61} \cdot 10^{-2}$$

$$c_1 = 5.82^{+0.64}_{-0.88} \cdot 10^{-2}$$



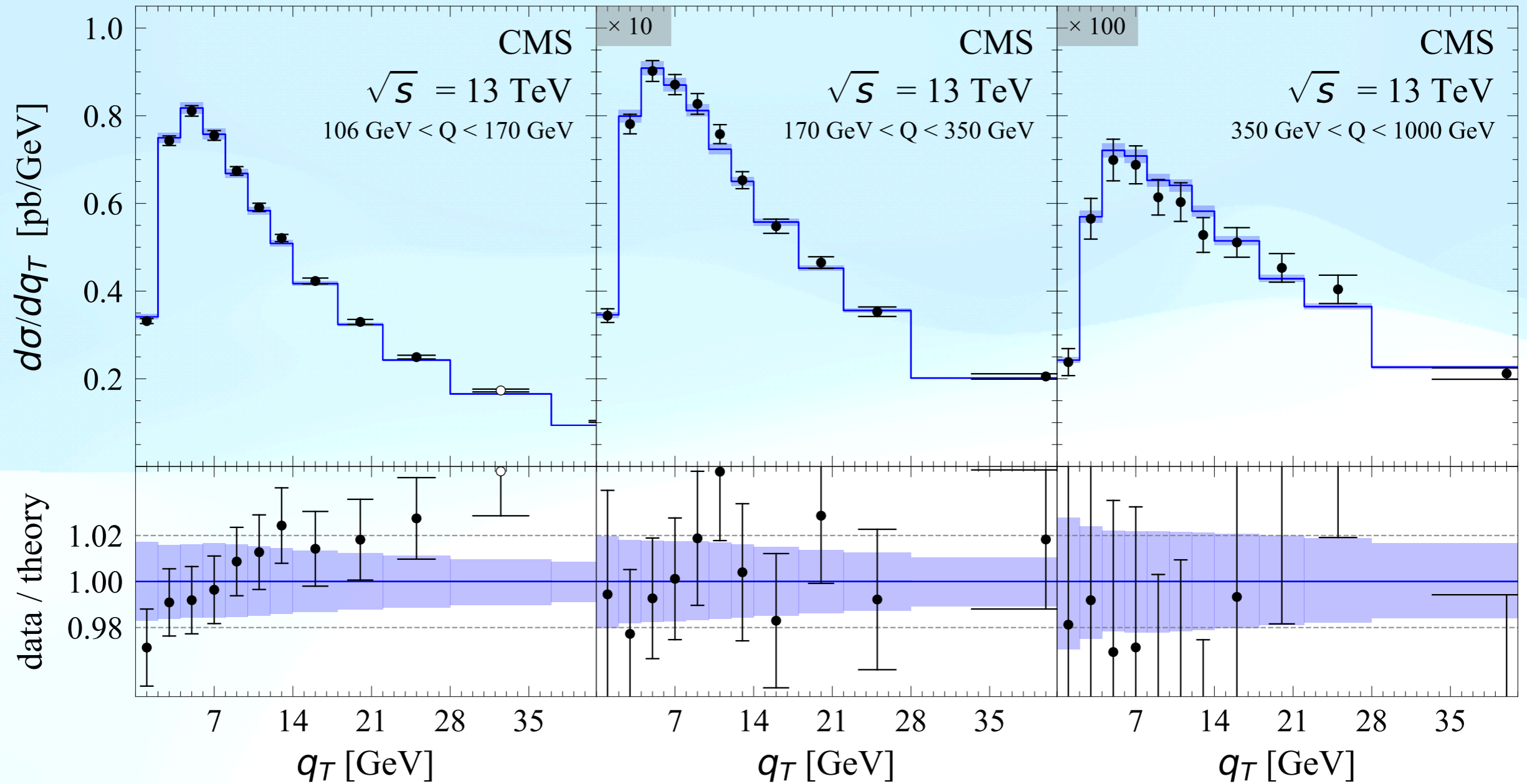
ART23: results

Scale variations $\left\{ \mu \rightarrow s_2 \mu, \mu^* \rightarrow s_3 \mu^*, \mu_{\text{OPE}} \rightarrow s_4 \frac{2e^{-\gamma_E}}{b} + 2\text{GeV} \right\}$.

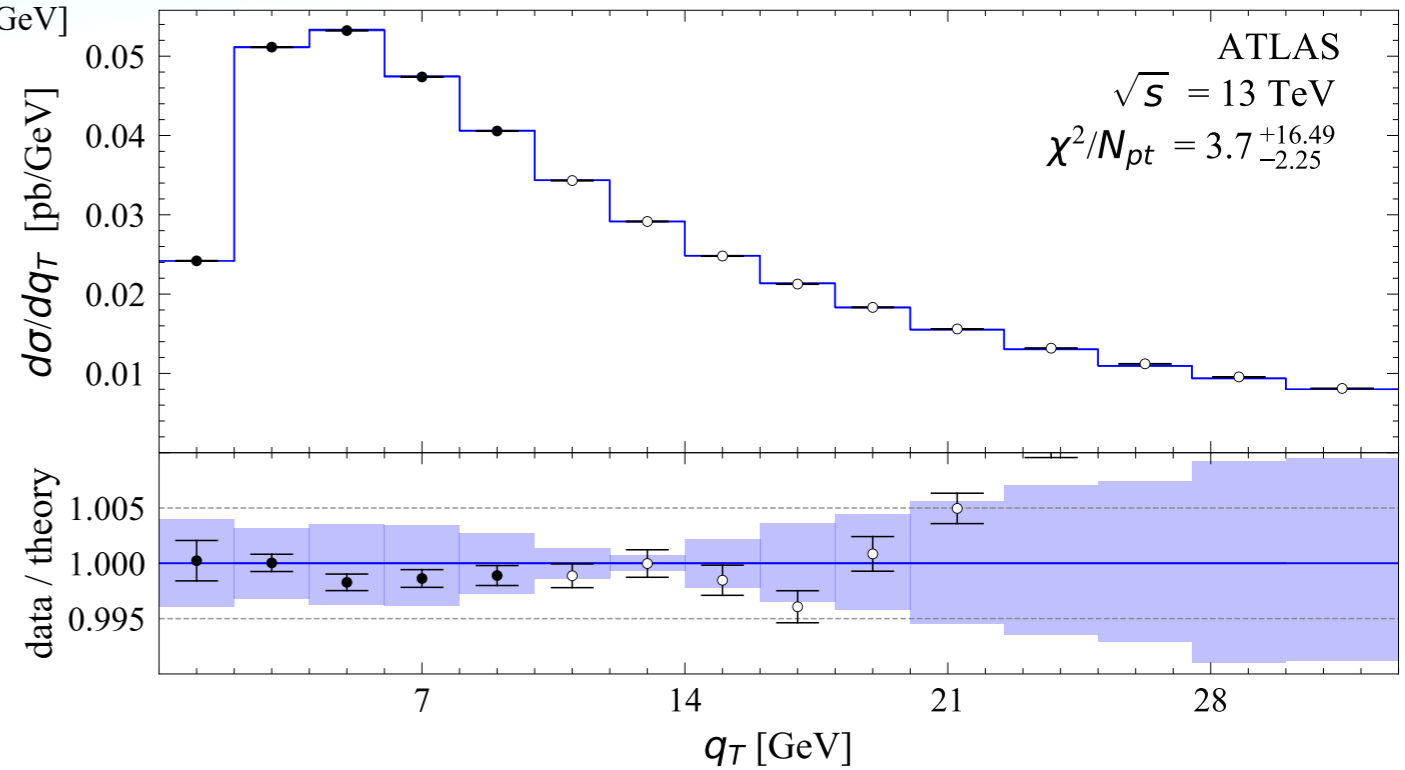
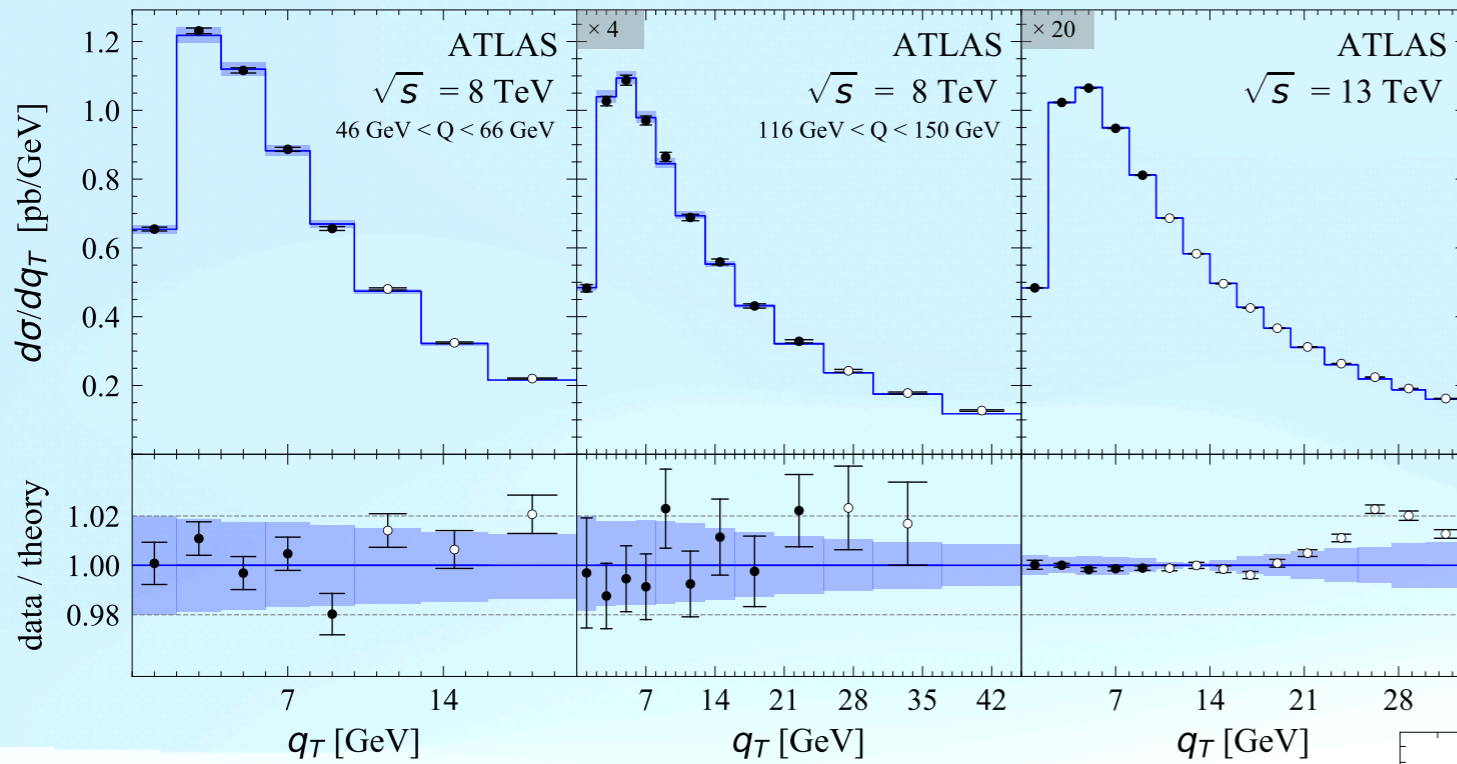


Γ_{cusp}	γ_V	β	$\mathcal{D}_{\text{small-b}}$	$C_{f \leftarrow f'}$	C_V	PDF
$a_s^5 (\Gamma_4)$	$a_s^4 (\gamma_4)$	$a_s^6 (\beta_4)$	$a_s^4 (d^{(4,0)})$	$a_s^3 (C_{f \leftarrow f'}^{[3]})$	a_s^4	NNLO

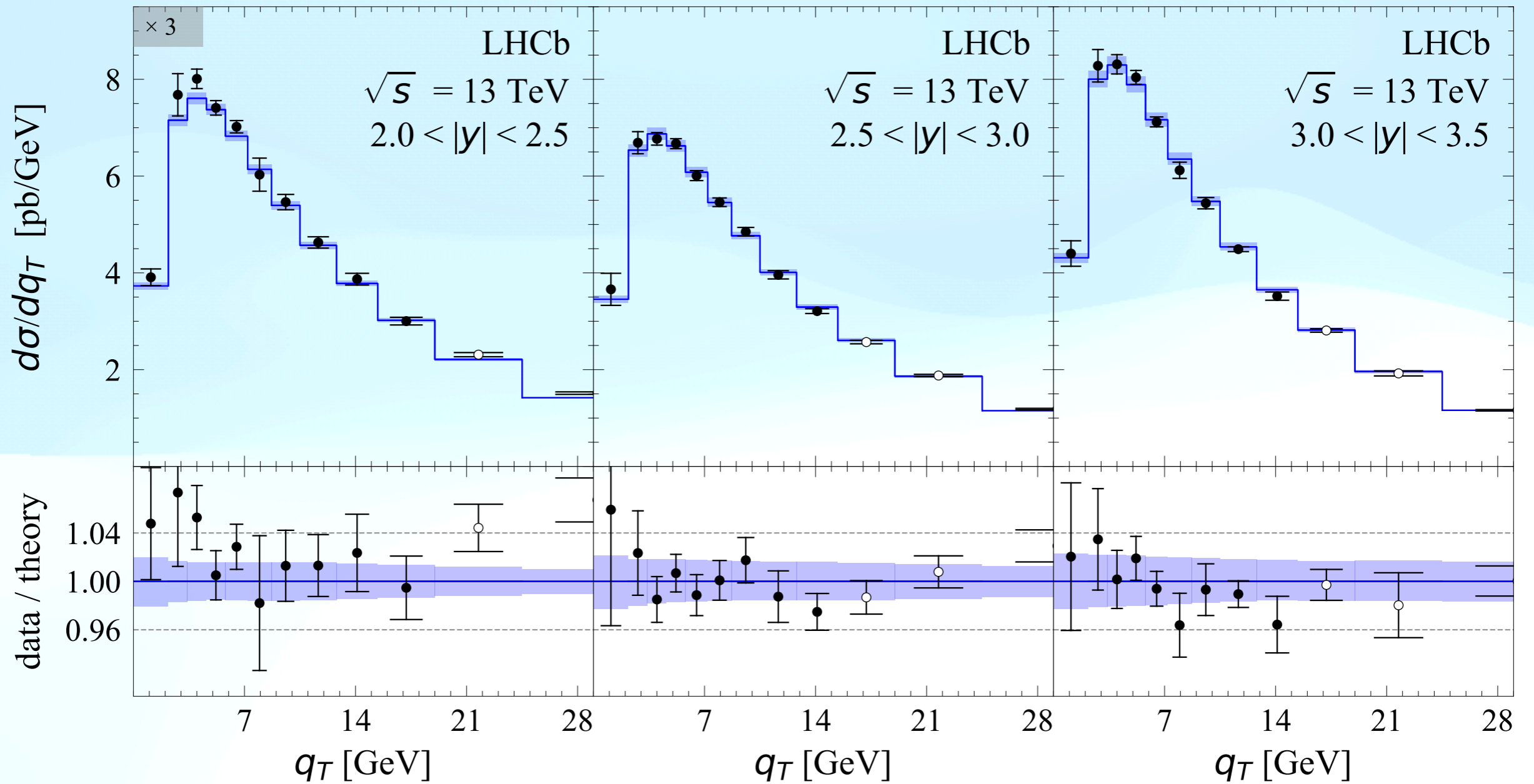
ART23: results



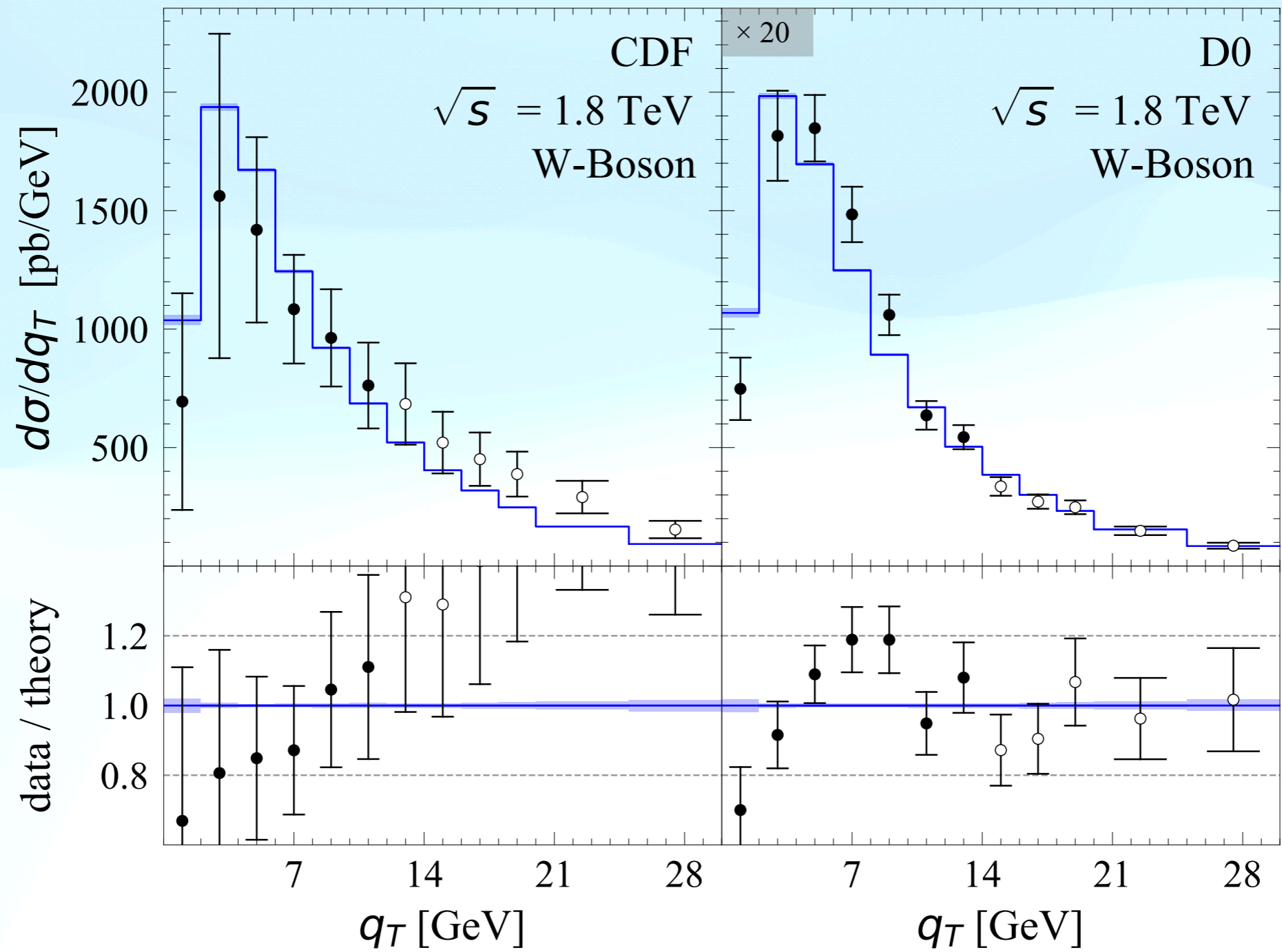
ART23: results



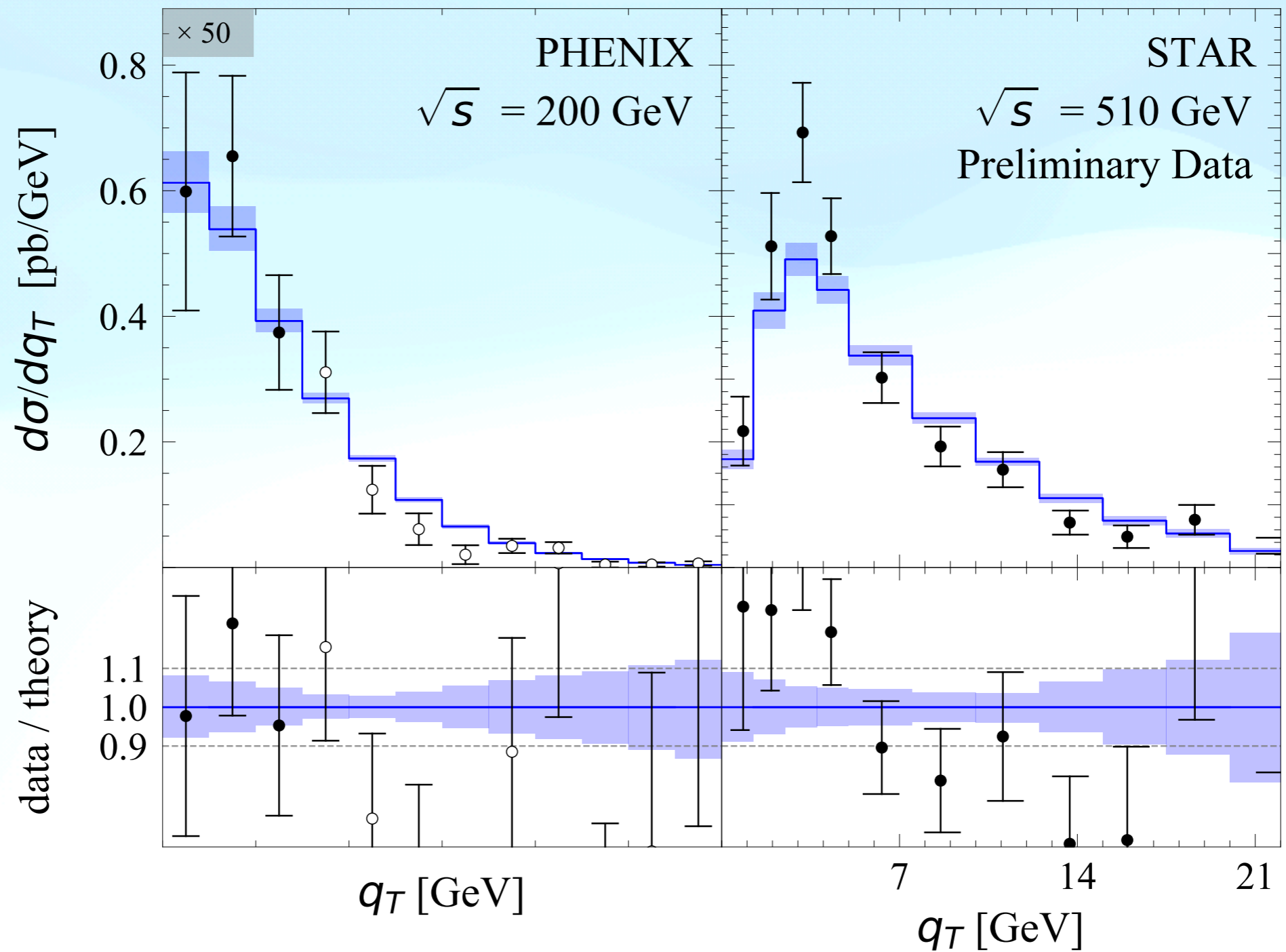
ART23: results



ART23: results



ART23: results



ART23: results

$$\lambda_1^u = 0.87^{+0.10}_{-0.10},$$

$$\lambda_1^d = 0.99^{+0.09}_{-0.12},$$

$$\lambda_1^{\bar{u}} = 0.35^{+0.23}_{-0.22},$$

$$\lambda_1^{\bar{d}} = 0.12^{+0.13}_{-0.11},$$

$$\lambda_1^{sea} = 1.32^{+0.23}_{-0.24},$$

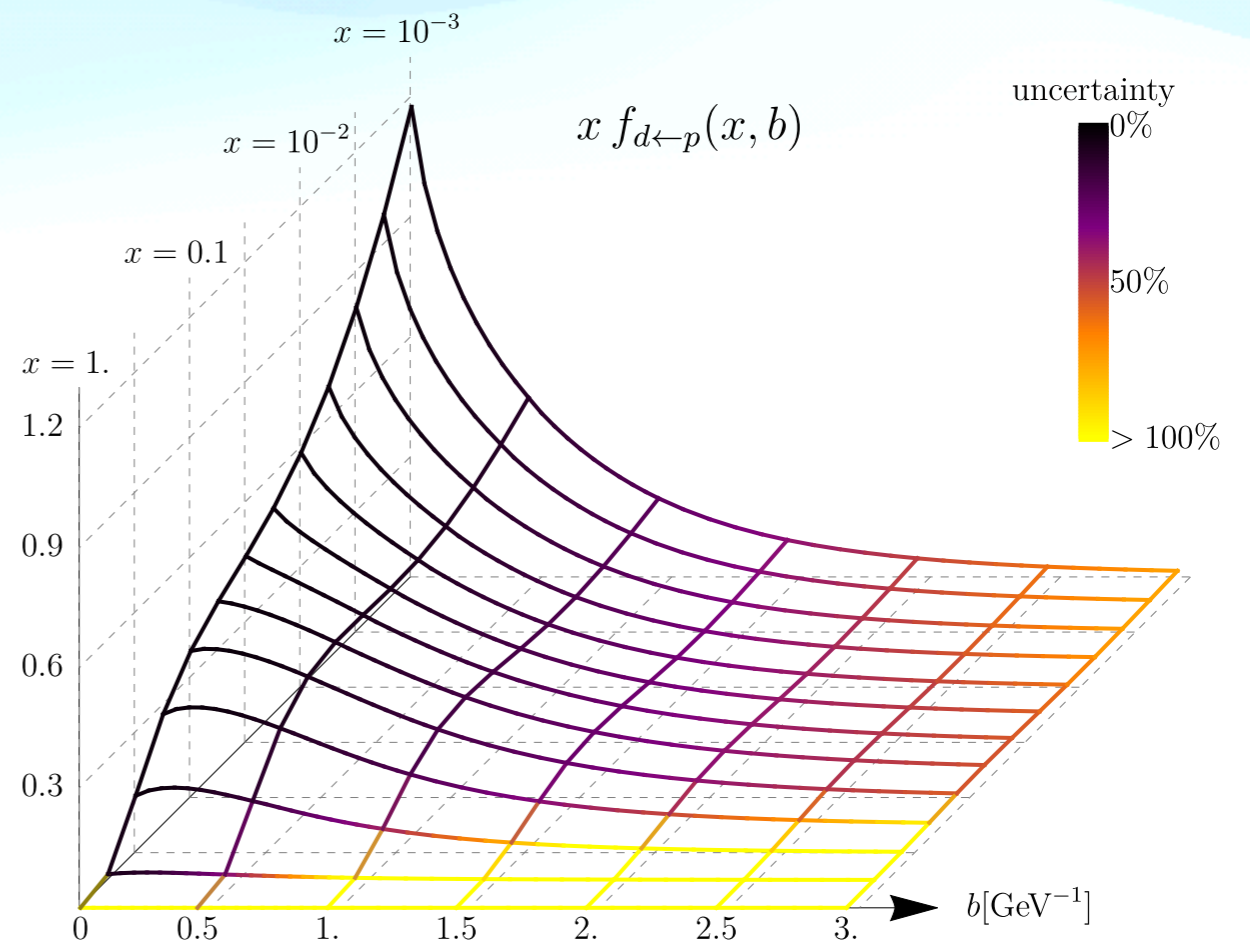
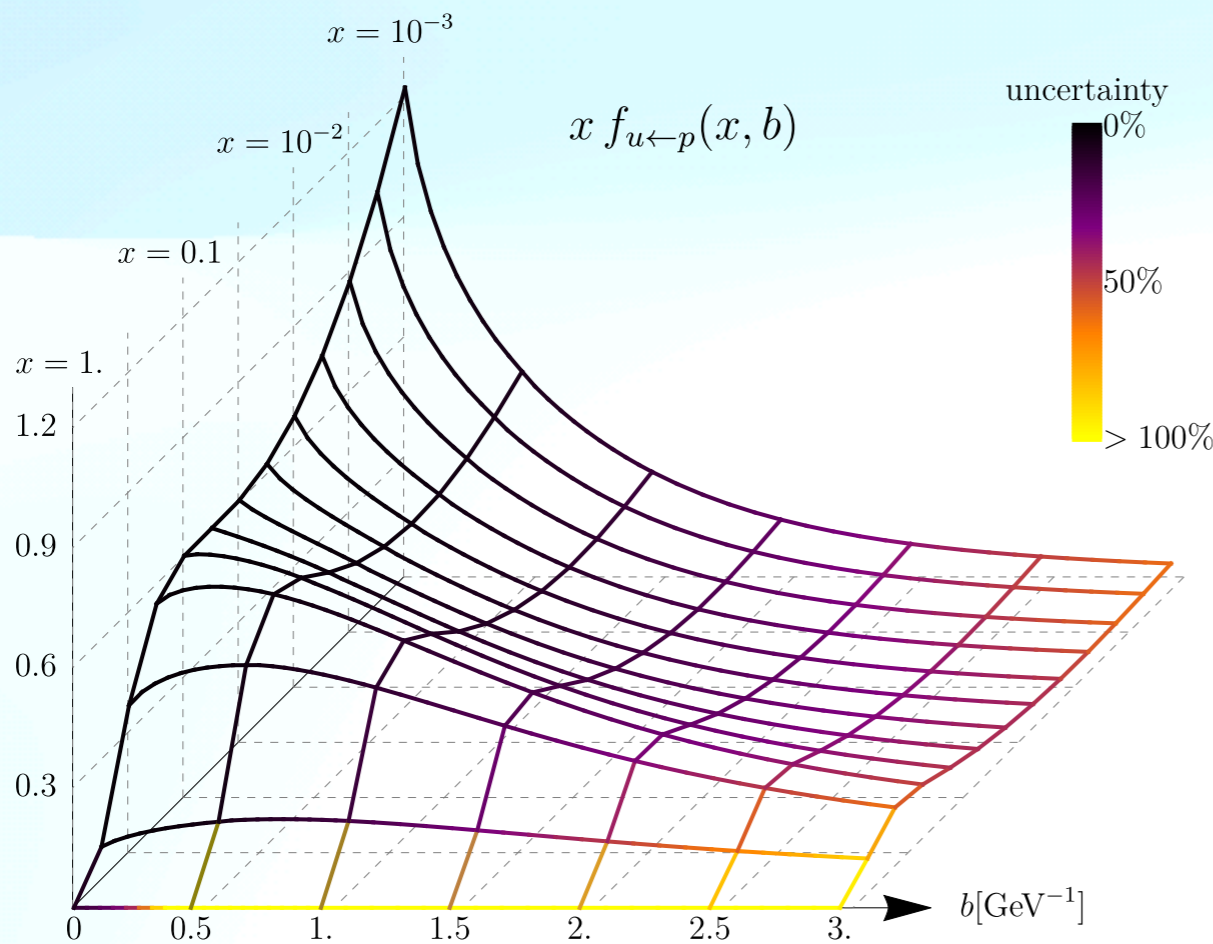
$$\lambda_2^u = 0.91^{+0.33}_{-0.29},$$

$$\lambda_2^d = 6.06^{+1.36}_{-1.34},$$

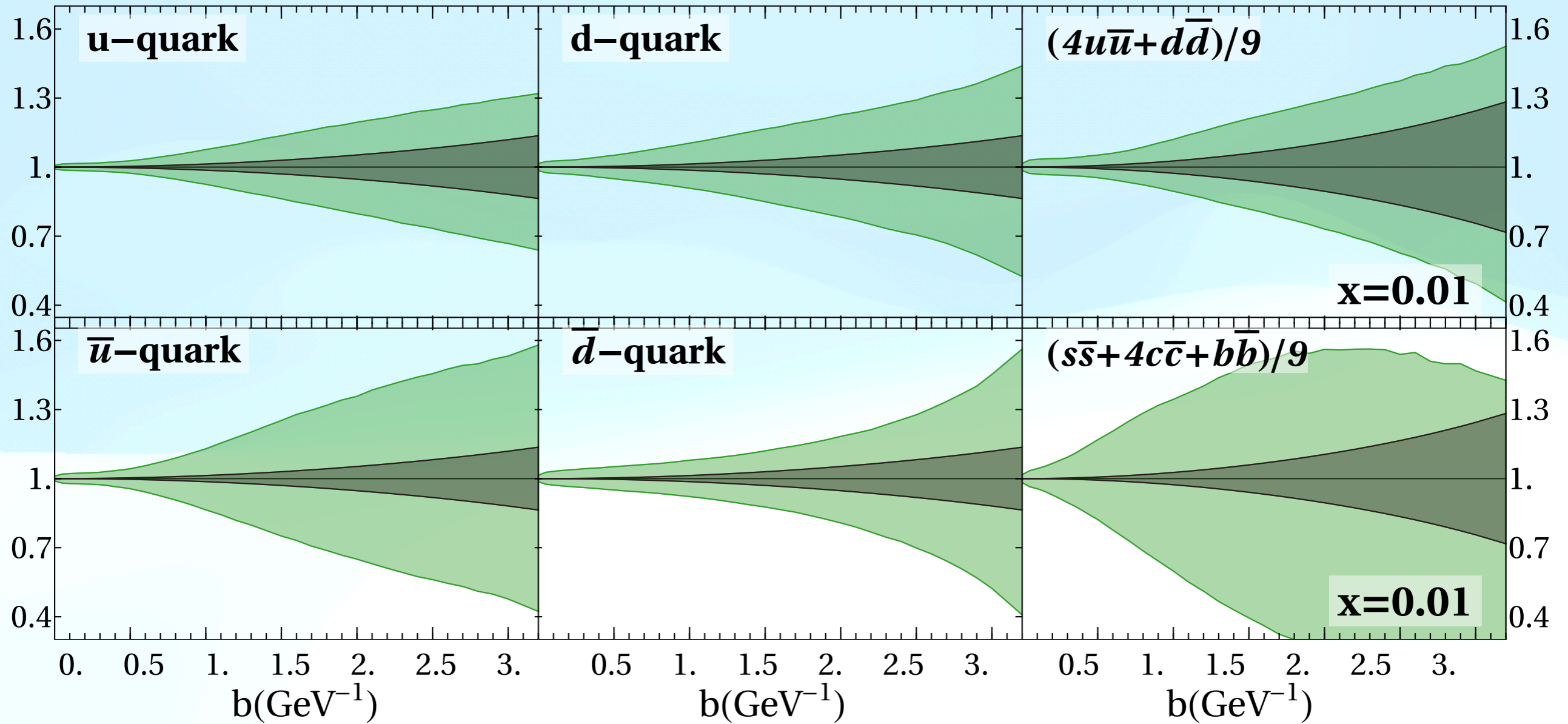
$$\lambda_2^{\bar{u}} = 46.6^{+7.9}_{-8.1},$$

$$\lambda_2^{\bar{d}} = 1.53^{+0.54}_{-0.17},$$

$$\lambda_2^{sea} = 0.46^{+0.13}_{-0.45},$$



ART23: results

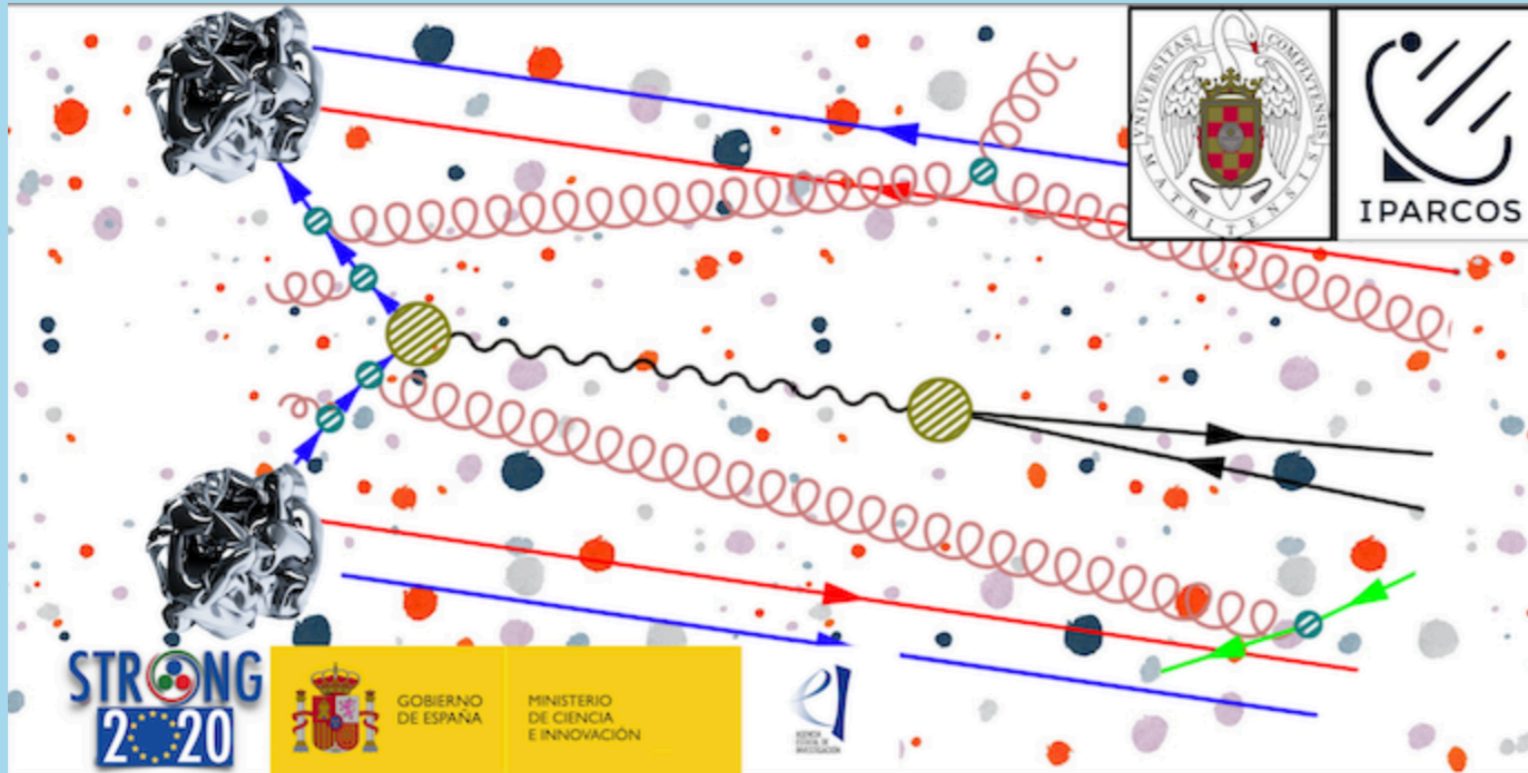


Light green: ART23
Dark green: SV19

Summary

The factorization of transverse momentum distributions has a long story, but recent understanding make it spectacular (and more to come)!

- 📌 **TMDPDF are now extracted at N4LL (No other distribution uses the number of perturbative QCD orders)**
- 📌 We have performed a novel TMDPDF extraction: [ART23](#).
- 📌 We used all the newest measurements and also W-boson production data, finding a good description.
- 📌 For the first time, the PDF uncertainties are systematically included. And we have realistic uncertainty bands.
- 📌 The flavor dependence in the NP ansatz is crucial to reduce the PDF bias.
- 📌 The global fit (including SIDIS data) is ... closer



Resummation, Evolution, Factorization 2023 (REF2023)

23-27 octubre 2023
Facultad de Físicas
Europe/Madrid timezone

<https://indico.fis.ucm.es/event/19/>

Back-up



VNiVERSiDAD
D SALAMANCA

IUFFyM

Instituto Universitario
de Física Fundamental y Matemáticas

SCET 2024

Salamanca (Spain)

April 15-18, 2024

Organizers:

Vicent Mateu

Teresa F. Caramés

German Sborlini

Ignazio Scimemi

Alexey Vladimirov

Student support:

Miguel Angel Benítez, Alberto Martín



NNPDF3.1: COMPARISON

