

# Quantum Sensing for light New Physics and Gravitational Waves

Elina Fuchs

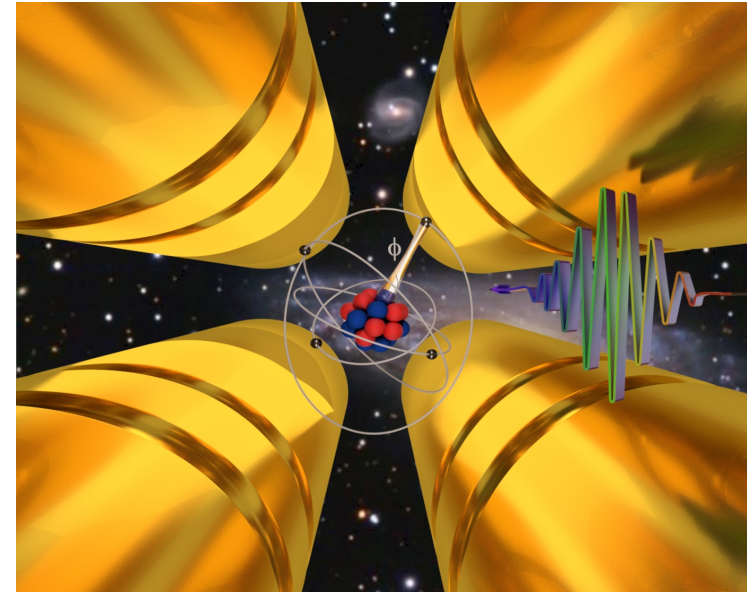
CERN

& Leibniz Universität Hannover

& PTB Braunschweig

CERN Theory Colloquium

June 14<sup>th</sup>, 2023



Leibniz  
Universität  
Hannover



QUANTUM  
TECHNOLOGY  
INITIATIVE

# Outline

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1) Motivation for light New Physics

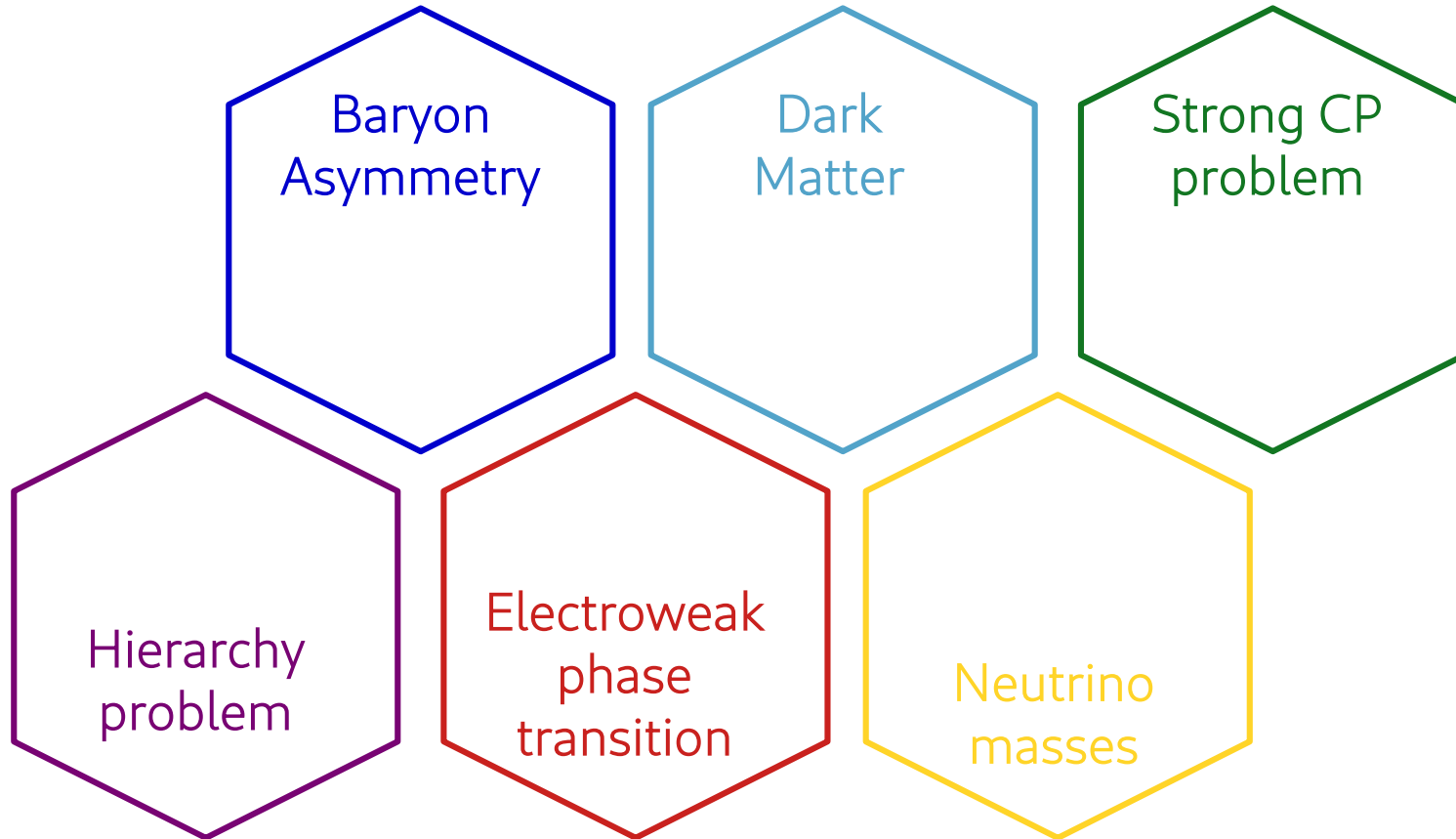
2) Quantum Sensors

3) Atomic clocks for light new bosons

4) High-frequency GWs with optical photons

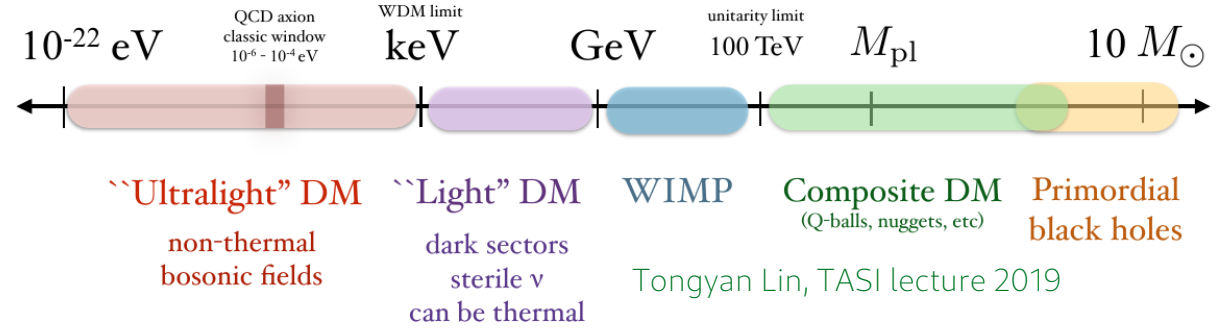
# Particle questions

# Quantum sensing



# Why light New Physics

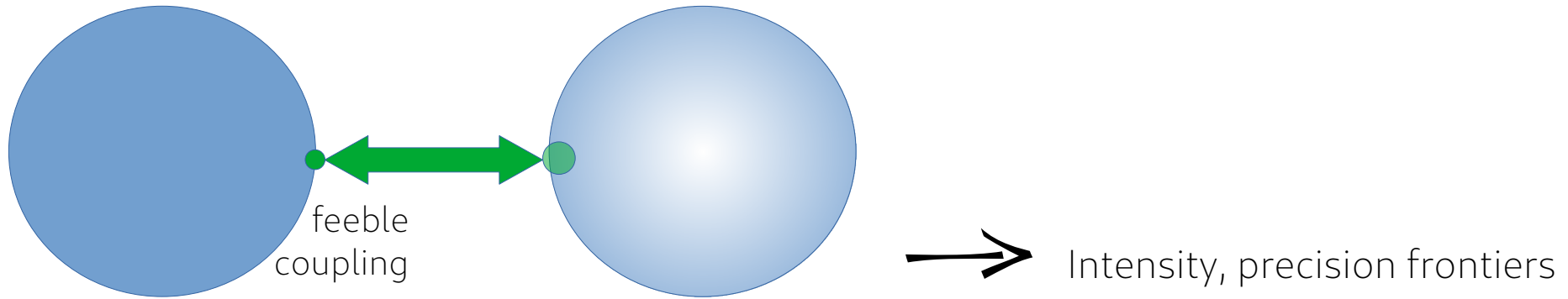
- Spontaneous breaking of exact symmetries → massless particles
  - Approximate symmetries broken → low-mass particles
- Small mixing with SM, e.g. [dark photon](#), ...
- Still a lot of unexplored model and parameter space
- DM options: mass scale



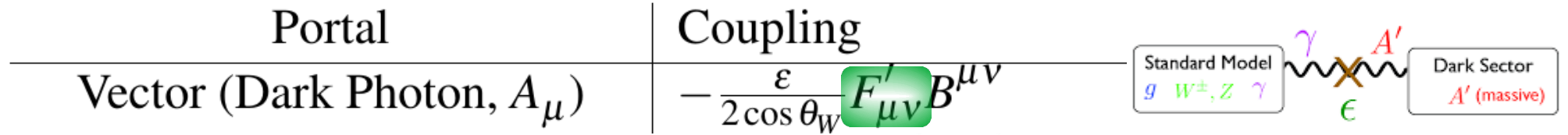
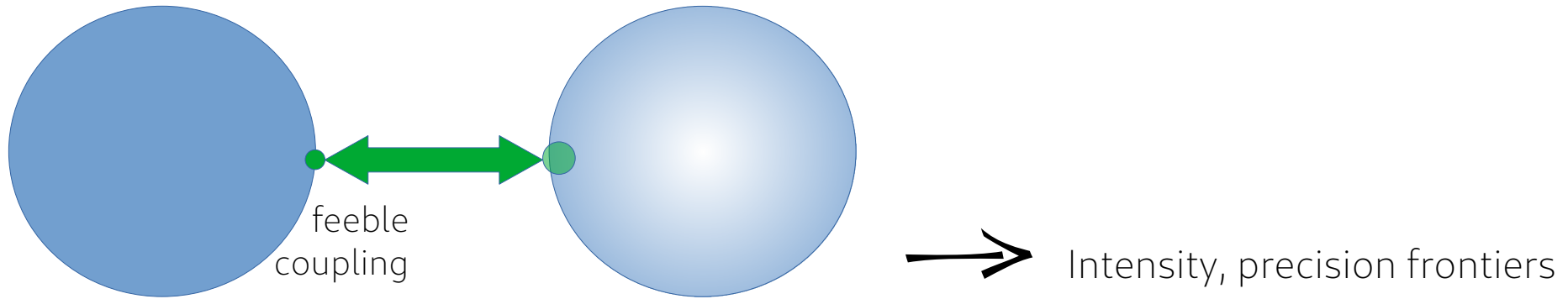
- can address SM shortcomings, e.g. [relaxion](#), [axion](#), ...
- interplay of cosmo/astro/precision/intensity/precision frontiers



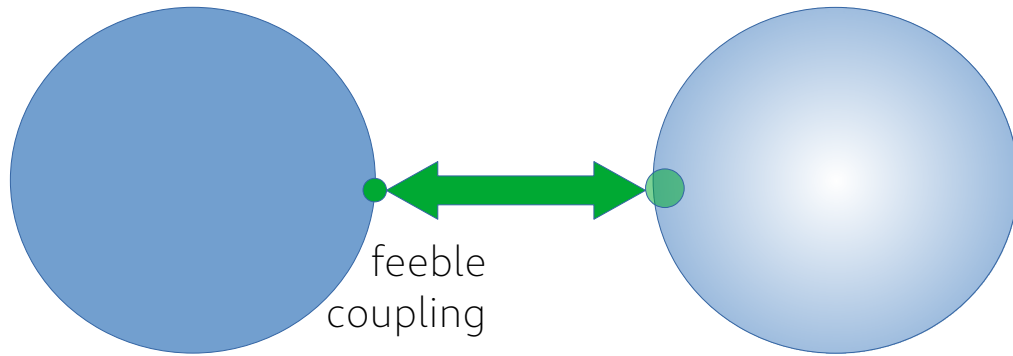
# Mediators to Dark Sector



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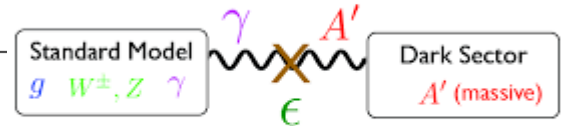


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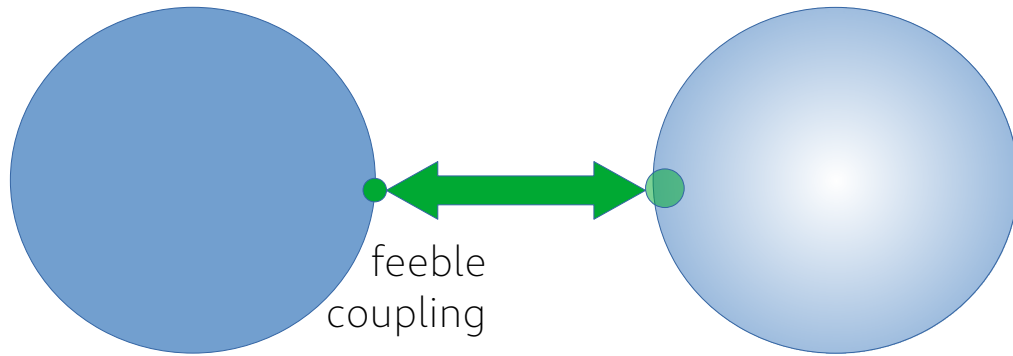


→ Intensity, precision frontiers

Portal	Coupling
Vector (Dark Photon, $A_\mu$ )	$-\frac{\epsilon}{2 \cos \theta_W} F'_{\mu\nu} B^{\mu\nu}$
Scalar (Dark Higgs, $S$ )	$(\mu S + \lambda_{HS} S^2) H^\dagger H$
Fermion (Sterile Neutrino, $N$ )	$y_N L H N$
Pseudo-scalar (Axion, $a$ )	$\frac{a}{f_a} F_{\mu\nu} \tilde{F}^{\mu\nu}, \frac{a}{f_a} G_{i,\mu\nu} \tilde{G}_i^{\mu\nu}, \frac{\partial_\mu a}{f_a} \bar{\psi} \gamma^\mu \gamma^5 \psi$



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Standard Model  
 $g W^\pm, Z \gamma$

Dark Sector  
 $A' \text{ (massive)}$

Motivation/need to search for light, feebly interacting particles

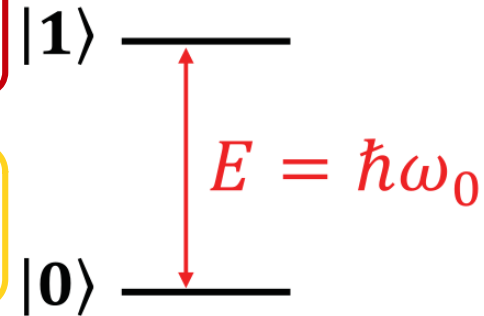
# Quantum Sensors

Degen, Reinhard, Cappallaro '16

i) Discrete, resolvable energy levels, typically 2-level system

ii) possible to initialize quantum system in known state & read it out

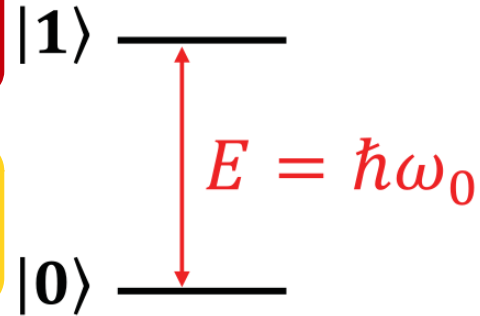
iii) quantum system can be coherently manipulated



# Quantum Sensors

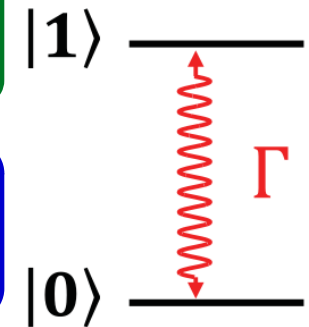
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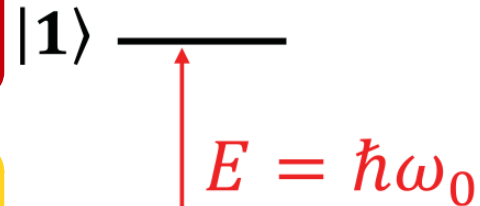


iv) interaction with external field  
→ energy shift or transition between levels

# Quantum Sensors

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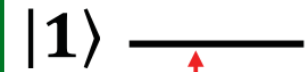
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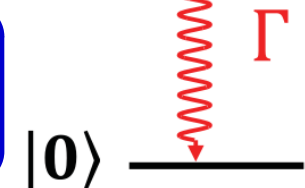
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e.g.: atoms, ions, Rydberg states, superconducting circuits, cavities, clocks, interferometers, ...  
& entanglement/squeezing → **well suited for light DM/NP, GWs, also for HEP detectors**

# Entanglement

*Goal:* enhance the measurement precision by quantum properties

**Standard Quantum Limit:** measurement uncertainty from the Heisenberg principle  
→ reduced for large number of atoms as  $\delta_{\text{SQL}} \propto N_{\text{atom}}^{-1/2}$

**Heisenberg limit:** fundamental limit

$$\delta_{\text{Heisenberg}} \propto N_{\text{entangled}}^{-1/2} N_{\text{atom}}^{-1/2} \longrightarrow N_{\text{atom}}^{-1}$$

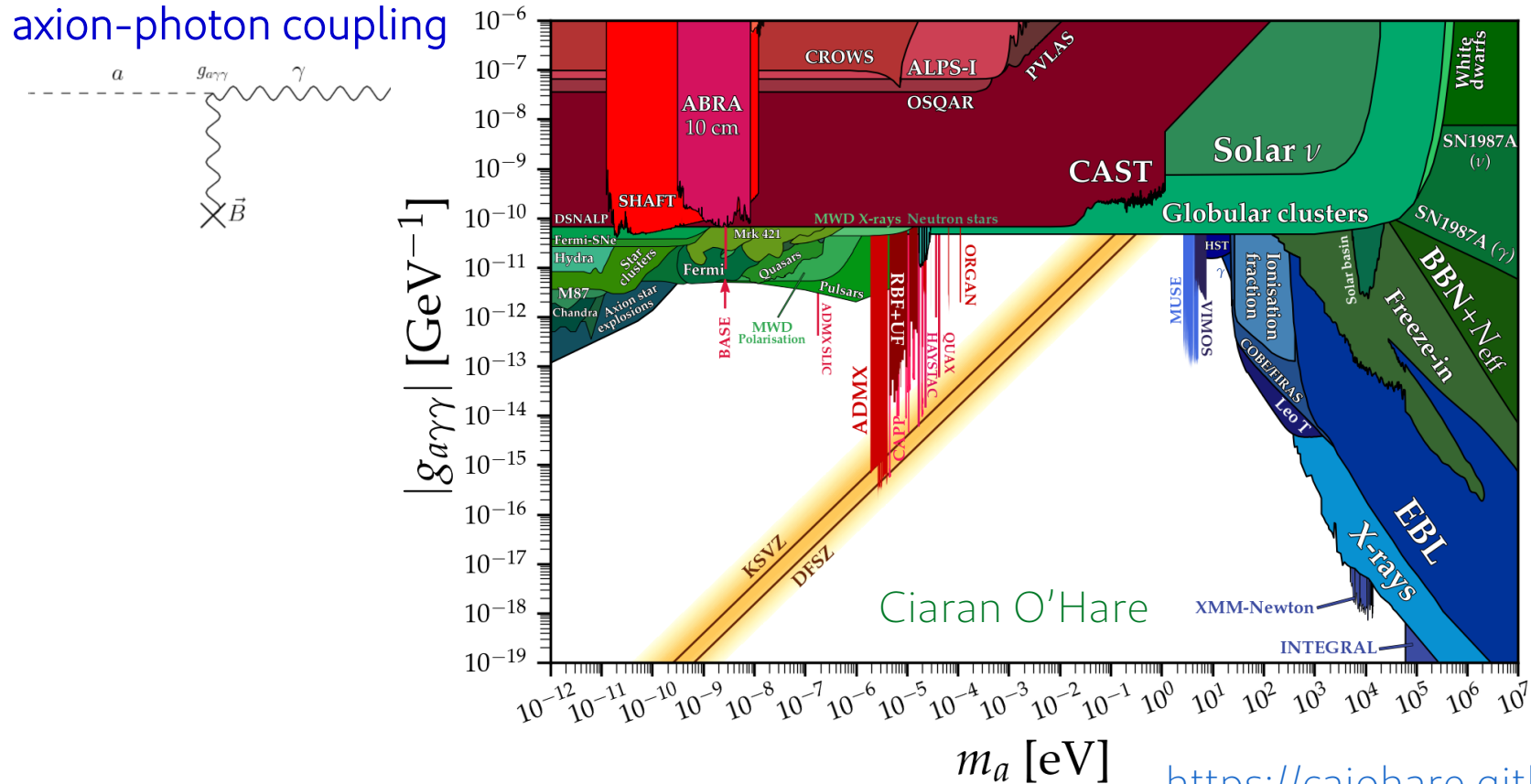
Best if all atoms entangled!

Already used:

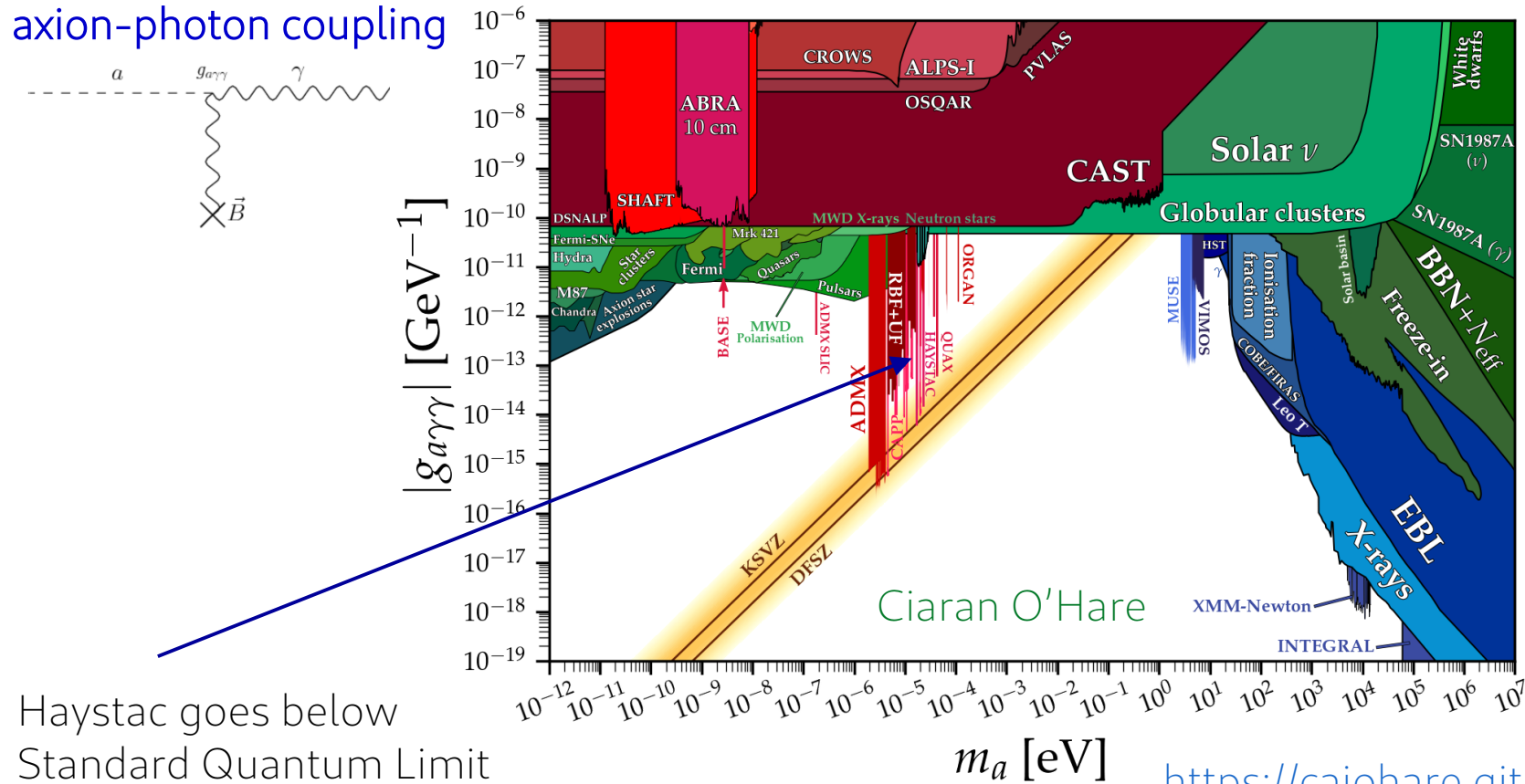
e.g. spectroscopy of entangled Sr isotopes [Ozeri et al, PRL '19]



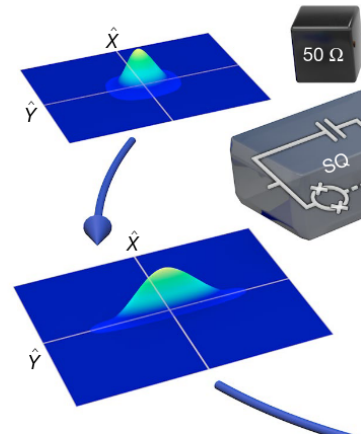
# Squeezing: e.g. in axion searches



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Squeezing  
HAYSTAC  
[Nature]



<https://cajohare.github.io/AxionLimits/>

# The virtue of frequency measurements

*“Never measure anything but frequency!”*



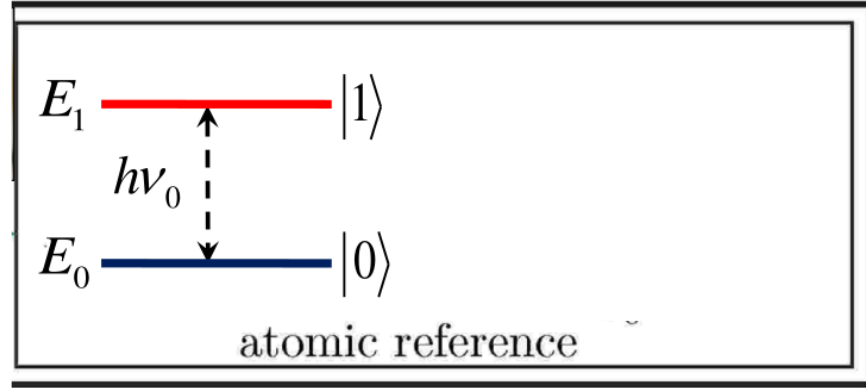
Arthur Schawlow,



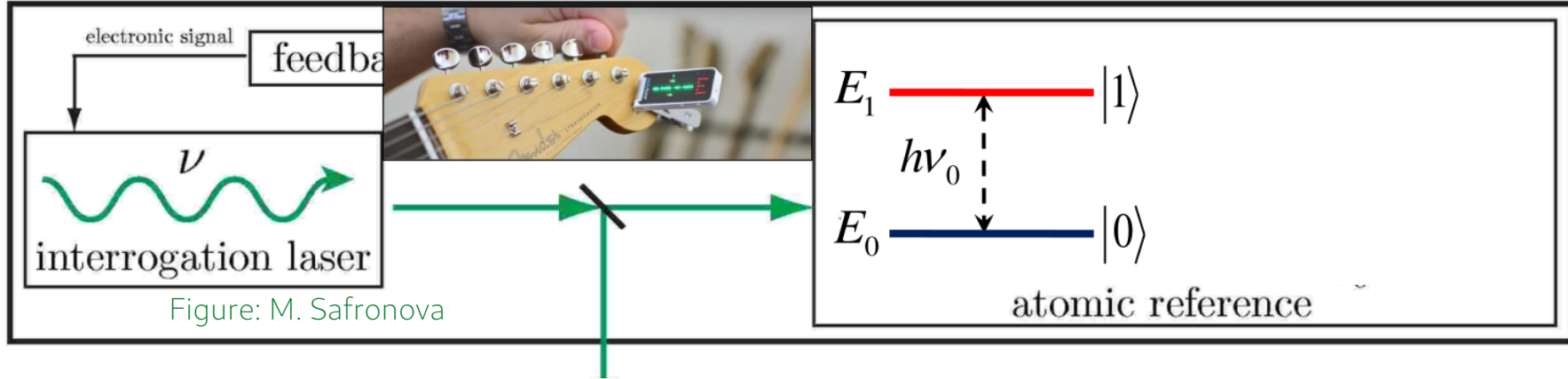
Nobel Prize in physics 1981  
for the co-development of  
the laser

*Goal:* Turn precise frequency measurements  
into a tool for particle physics

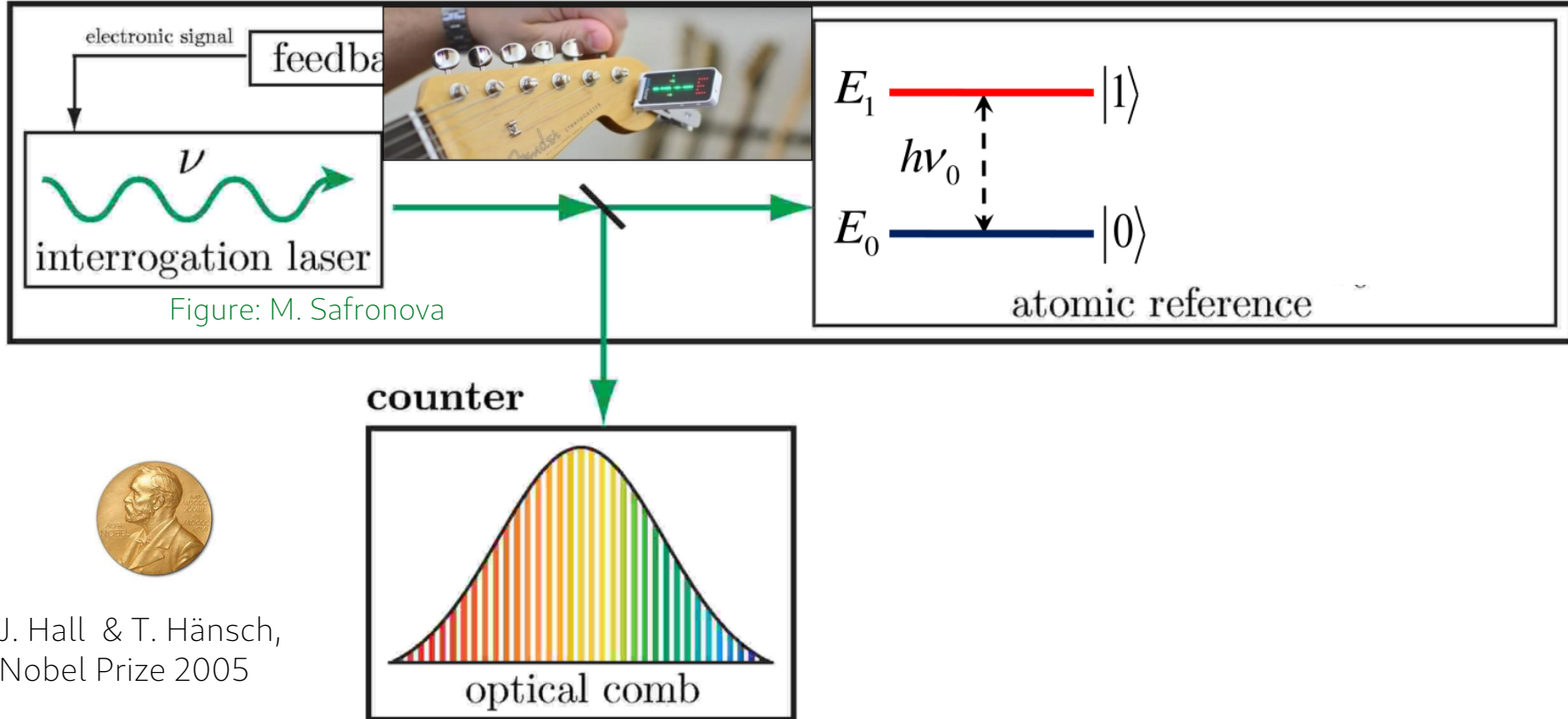
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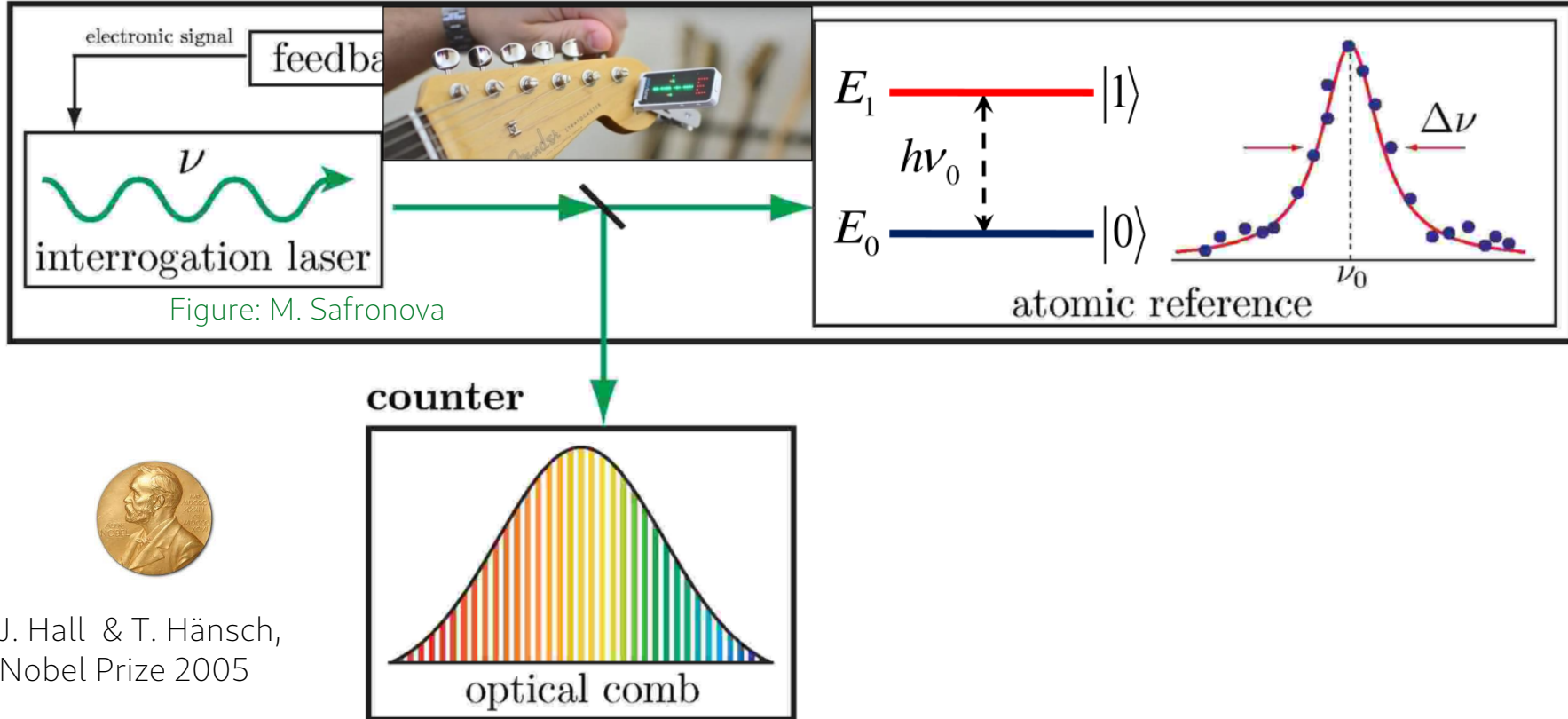


# Atomic clocks as Quantum Sensor



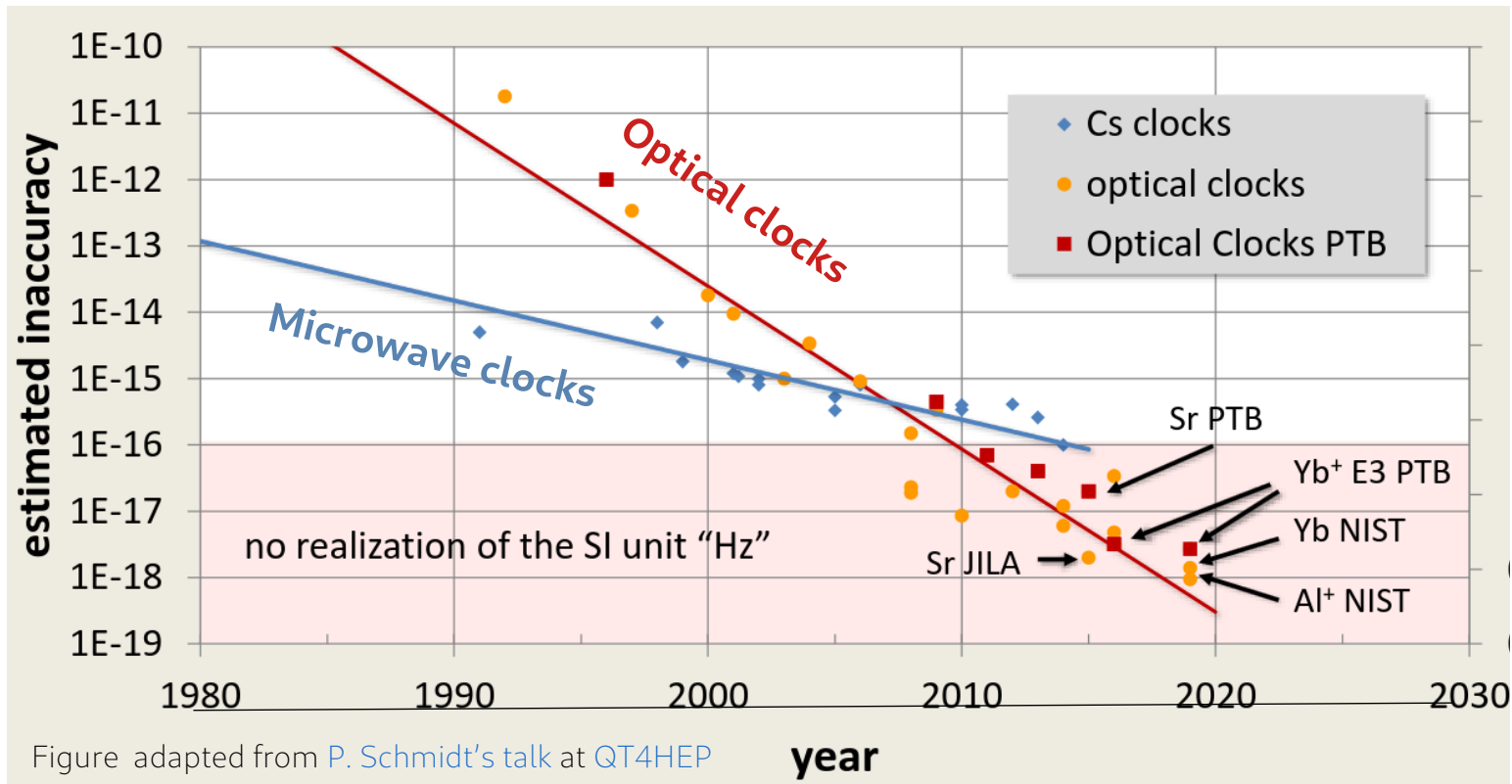
J. Hall & T. Hänsch,  
Nobel Prize 2005

# Atomic clocks as Quantum Sensor



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# Evolution of clock precision

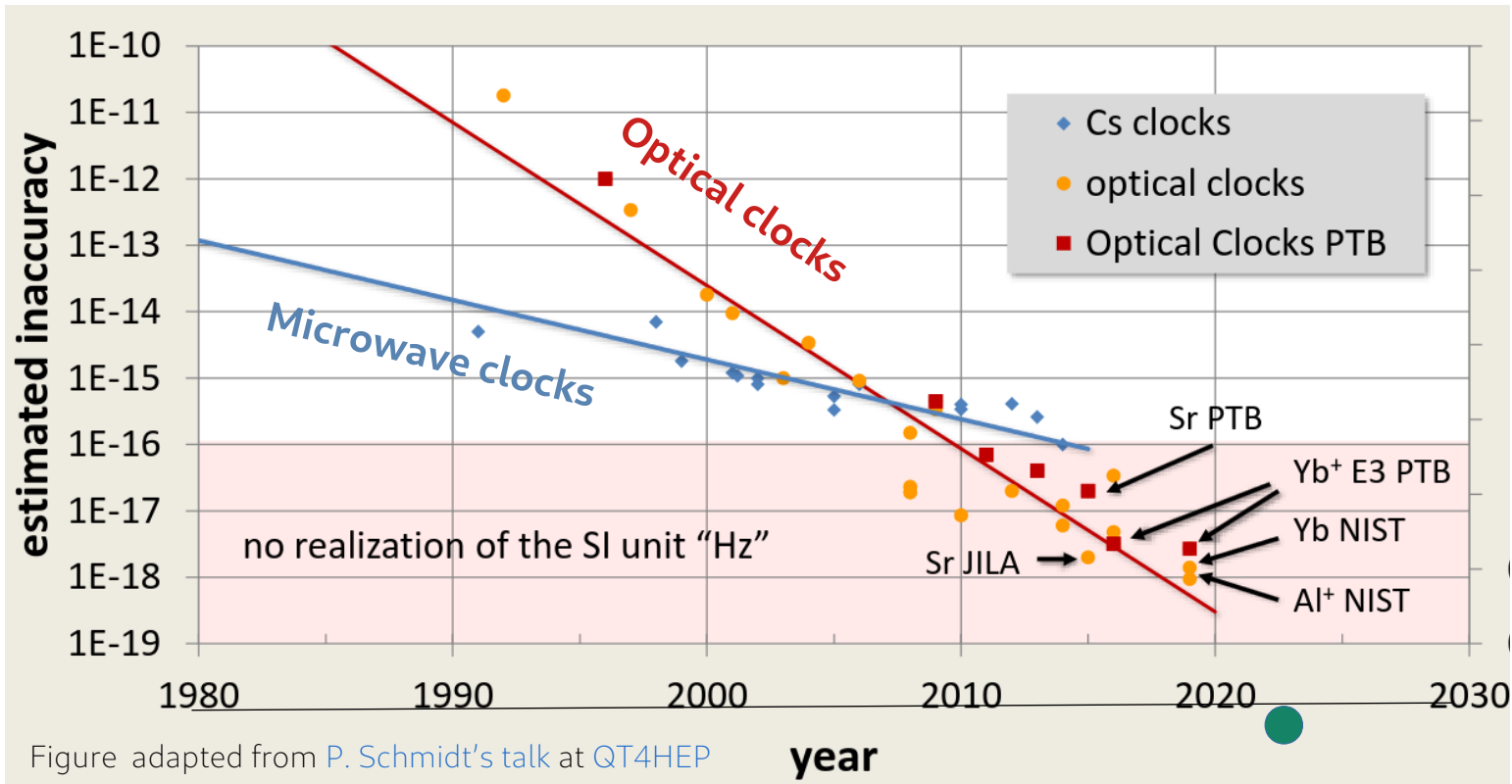


Al<sup>+</sup> clock: S-P with  $9.4 \times 10^{-19}$  precision  
Brewer et al [PRL'19](#)

Hz defined by #oscillations between 2 hyperfine levels of Cs



# Evolution of clock precision

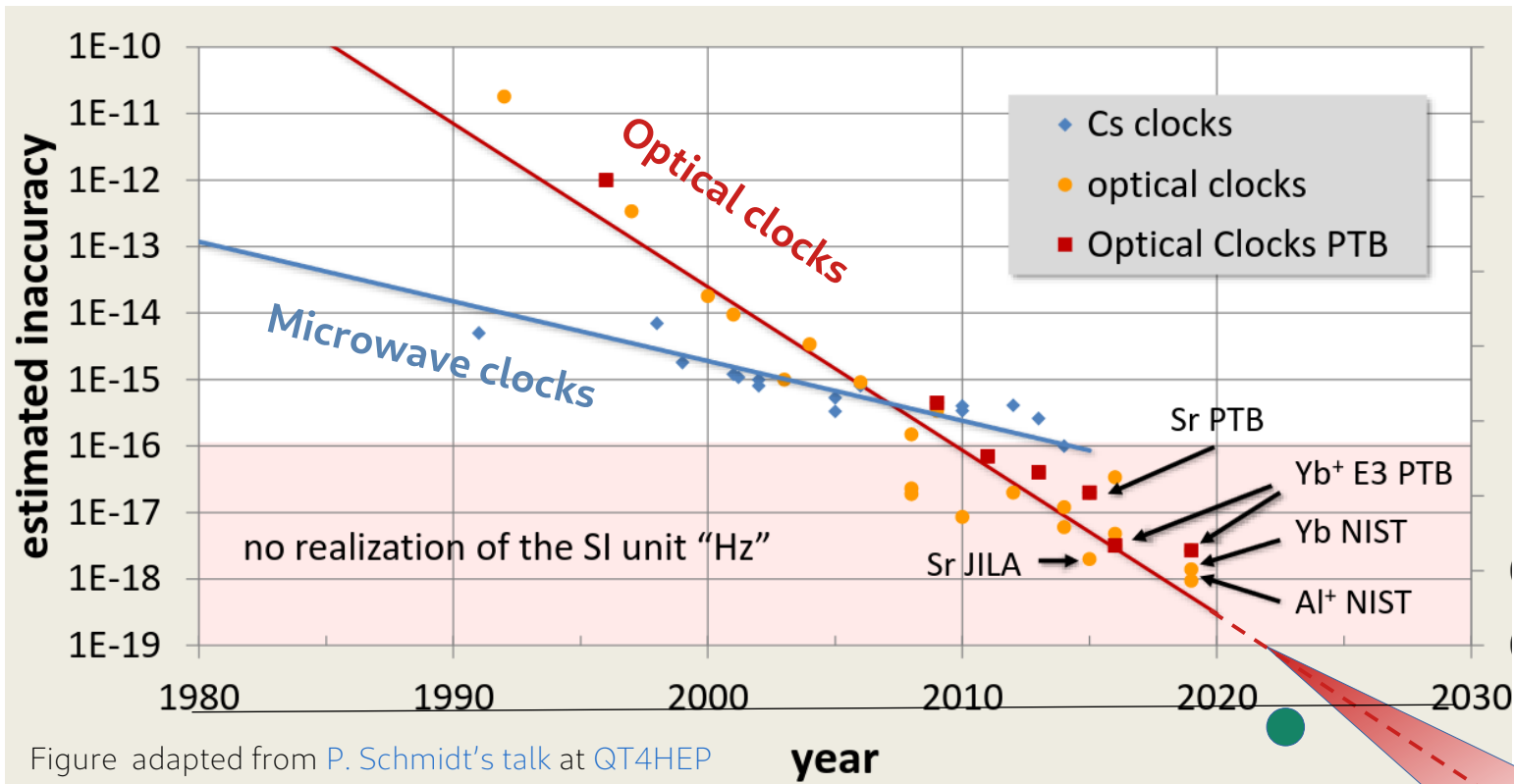


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Sr lattice clock with 100,000 atoms:  
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Bothwell et al Nature '22

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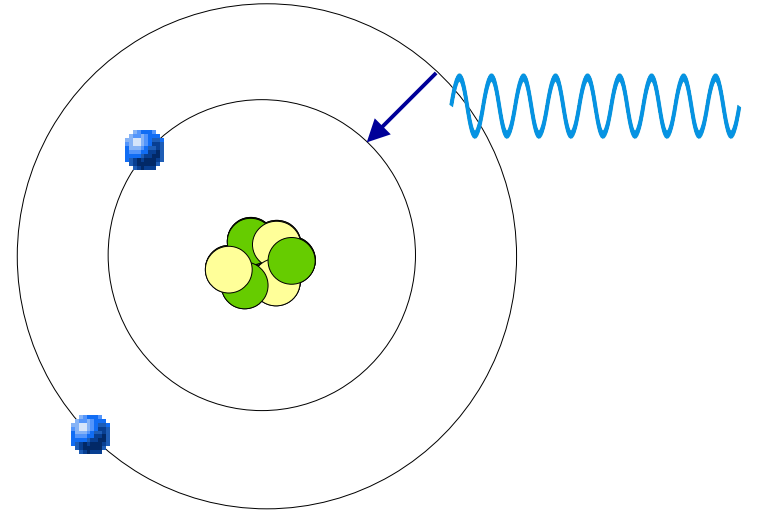
# Outline

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3) Atomic clocks for light new bosons

# Light scalar in atomic spectrum?

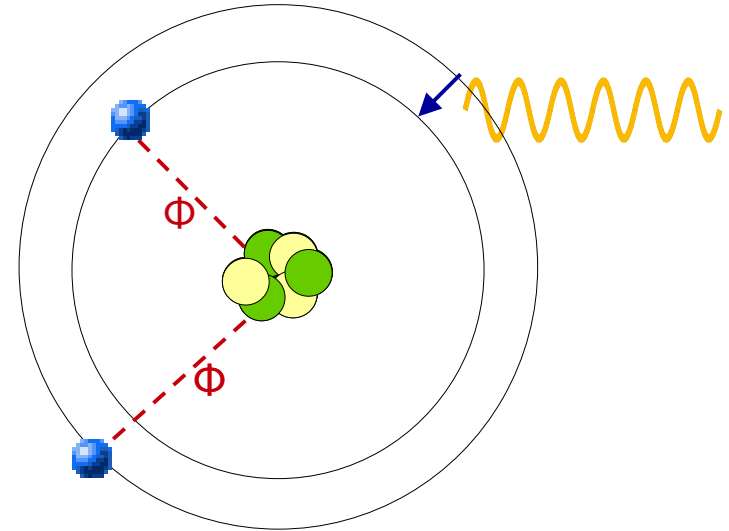
- Motivation: search for light new boson  $\phi$  that couples to electrons and neutrons
- $\phi$  perturbs electron levels  $\rightarrow$  only tiny frequency change



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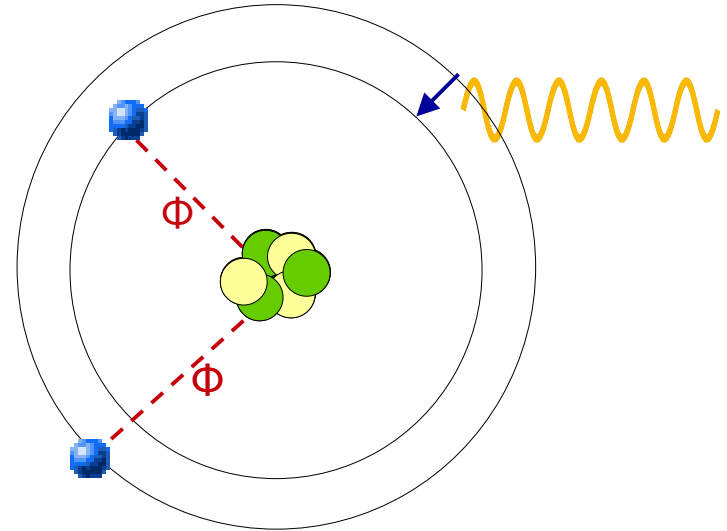
$$V_{NP} = \frac{y_e y_n}{4\pi r} e^{-m_\phi r}$$



# Challenge of theory-exp comparison

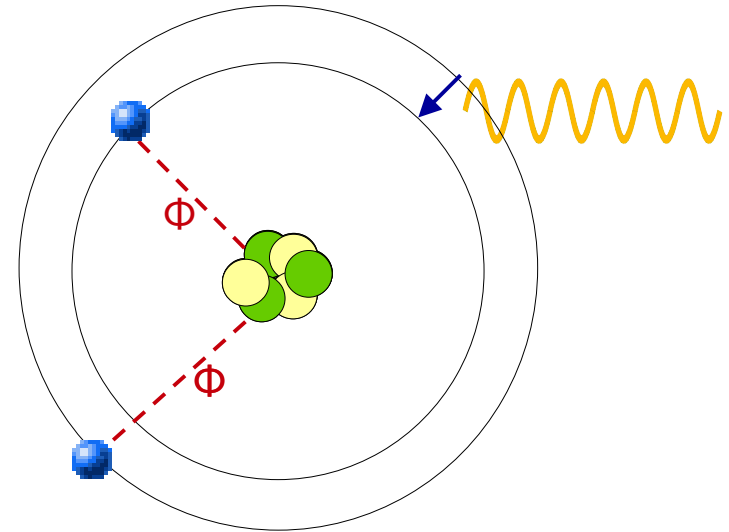
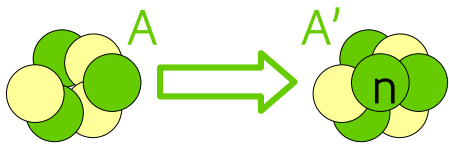
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# Data-driven atomic search for light scalar

- **Motivation:** search for light new boson  $\Phi$  that couples to electrons and neutrons
- $\Phi$  perturbs electron levels  $\rightarrow$  only tiny frequency change
- **Challenge:** theory, nuclear uncertainties  $\gg$  uncertainties of frequency measurements
- **Our method:** Measure **2 transitions, 3 isotope pairs** very precisely



- Berengut, Budker, Delaunay, Flambaum, Frugiuele, EF, Grojean, Harnik, Ozeri, Perez, Soreq; PRL 120 (2018) 091801
- Solaro, Meyer, Fisher, Berengut, EF, Drewsen; PRL 125, 123003 (2020)

# King plot of Isotope Shifts

Mass shift (MS)      Field shift (FS)

$$\nu_i^{AA'} \equiv \nu_i^A - \nu_i^{A'} = K_i \mu_{AA'} + F_i \delta \langle r^2 \rangle_{AA'}$$



electronic  
nuclear

Poorly known  
nuclear charge  
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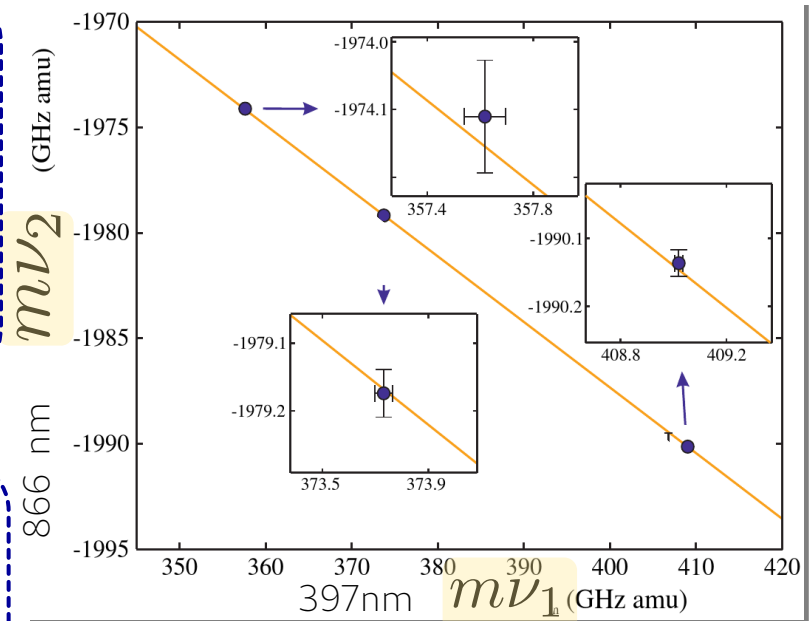
$i = 1, 2$

2<sup>nd</sup> transition to eliminate charge radius

[King '63]

Linear King relation (at leading order):

$$m\nu_2 = F_{21} m\nu_1 + K_{21}$$



[Gebert, Wan, Wolf, Angstmann, Berengut, Schmidt; PRL 115, 053003 (2015)]

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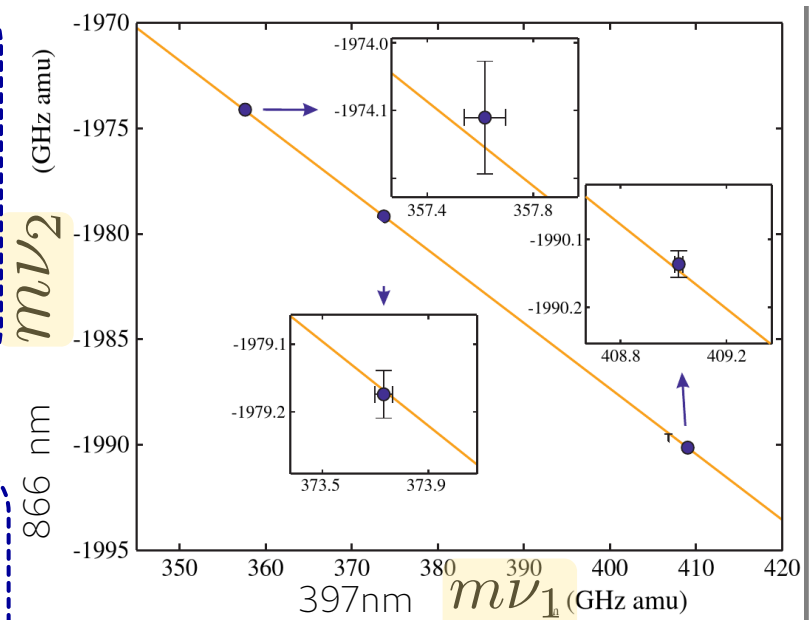
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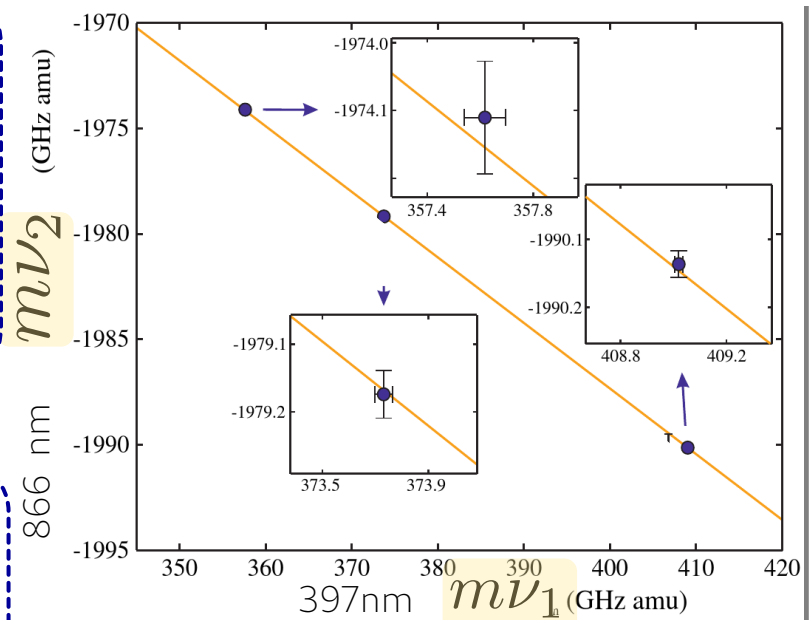
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check if 3 points (= 3 isotope pairs) on straight line

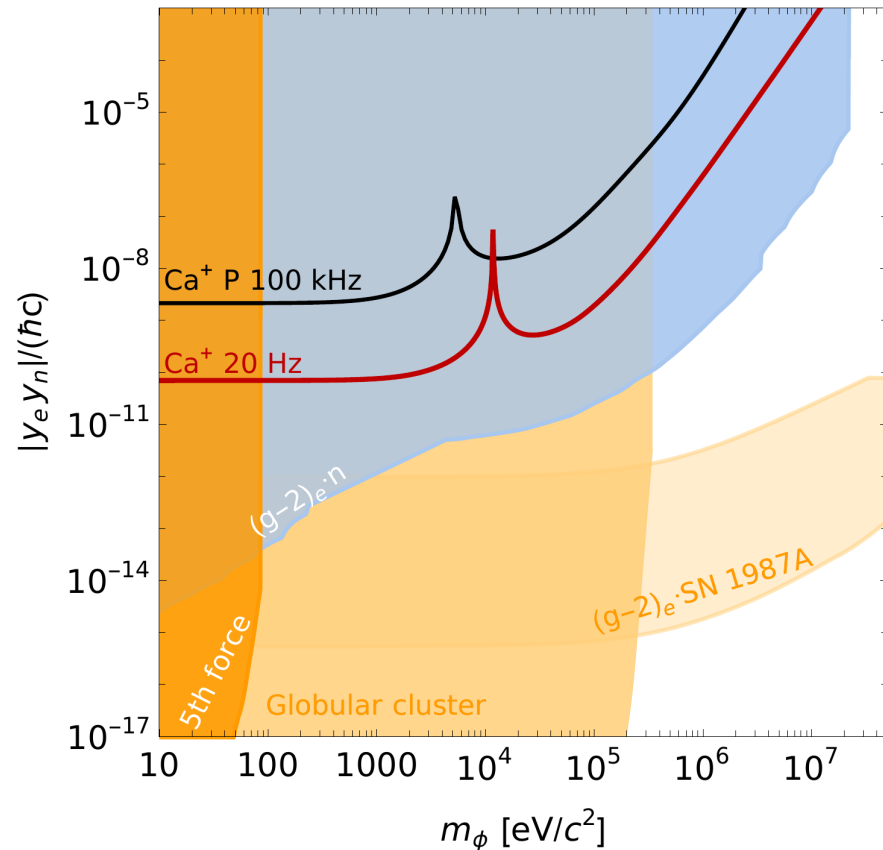


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# Ca<sup>+</sup> Isotope Shift Bounds on $\Phi$

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Solaro, Meyer, Fisher, Berengut, EF, Drewsen; PRL 2020

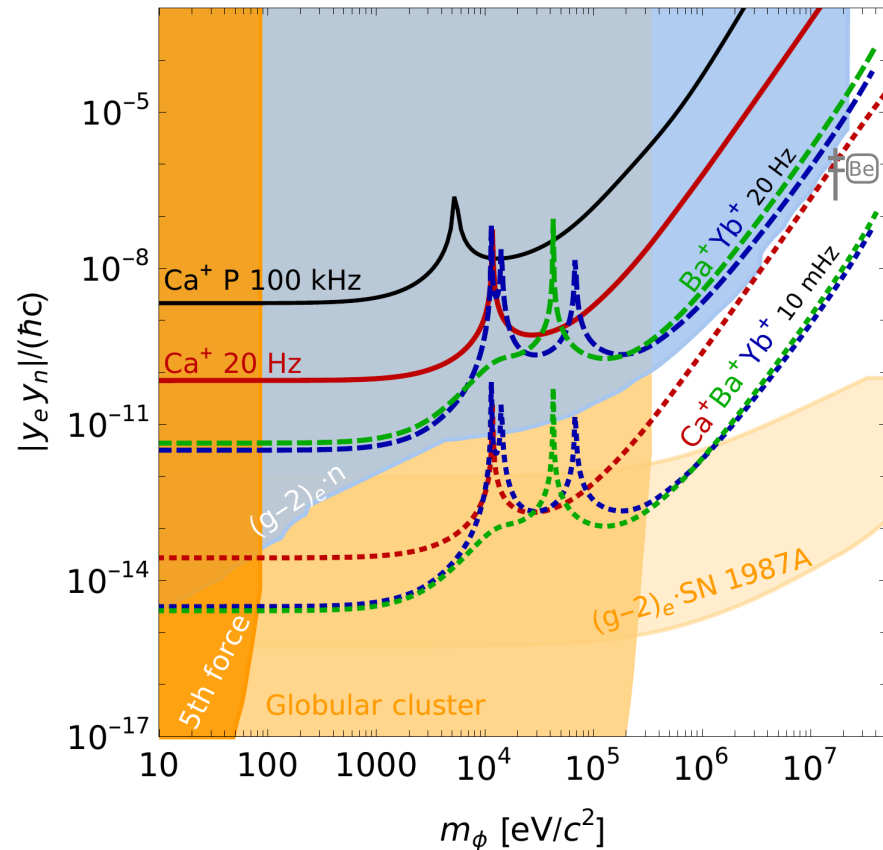


- Ca<sup>+</sup> King plot: D-fine splitting, 4 isotope pairs
- Improvement of former Ca bound by factor 30

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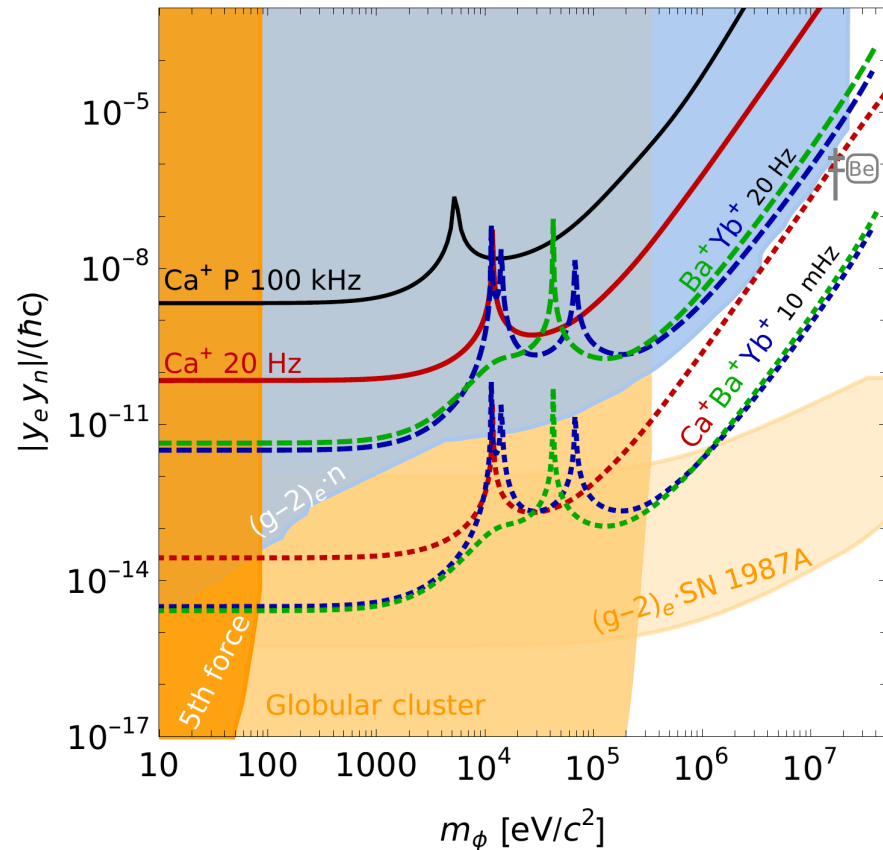


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- Realistic precision: **10 mHz**
  - Ca, Ba, Yb can probe untested parameter space

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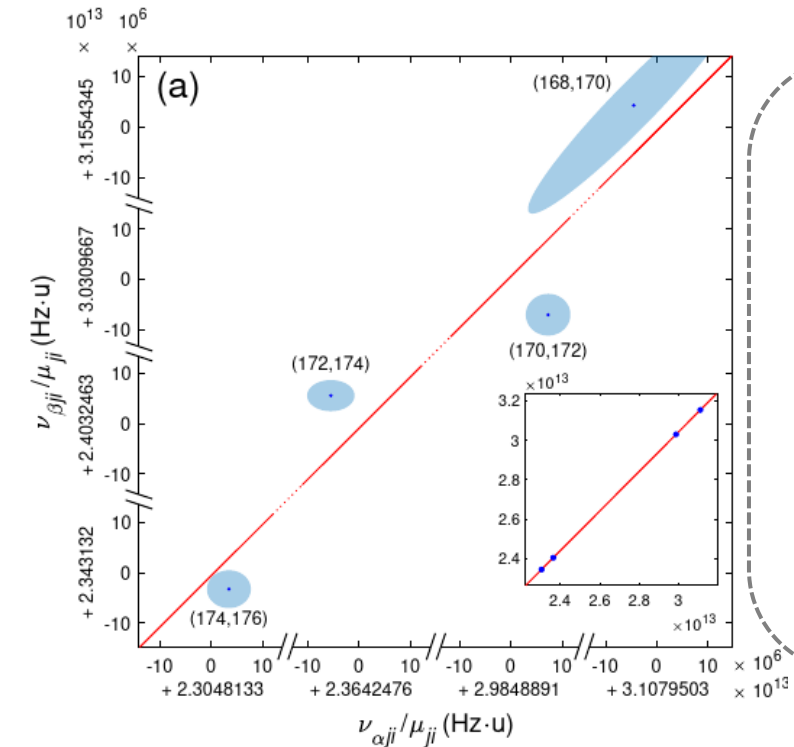
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Particle model applications: B-L, dark photon, chameleon  
 Frugiuele, EF, Perez, Schlaffer '16

few-electron systems:  
 Delaunay, Frugiuele, EF, Soreq '17

# Nonlinearity in Yb<sup>+</sup> isotope shifts

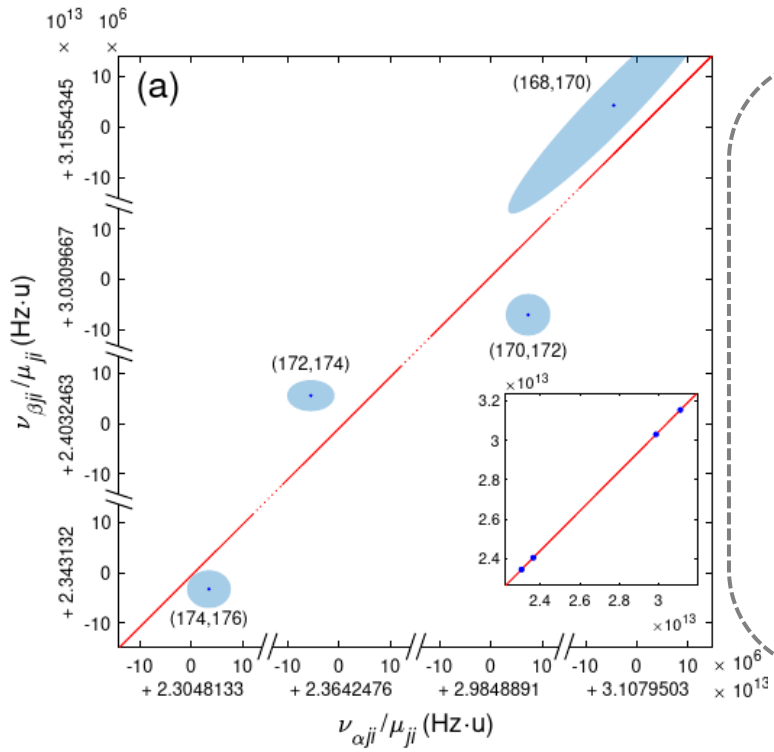
[Counts, Hur, Craik, Jeon, Leung, Berengut, Geddes, Kawasaki, Jhe, Vuletić, PRL 125, 123003 (2020)]  
+updates MIT, Mainz, PTB



- $3\sigma$  nonlinearity
- Nuclear deformation?
- SM can induce nonlinearity at higher order
  - 2<sup>nd</sup> order mass & field shift
  - Nuclear polarizability, deformation

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DECEMBER 4, 2020 **FEATURE**

**Researchers observe what could be the first hints of dark bosons**

by Ingrid Fadelli · Phys.org

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 ✉ Email

BSM or nuclear physics?

**Strategy:** consider predicted SM NL and constrain residual NL



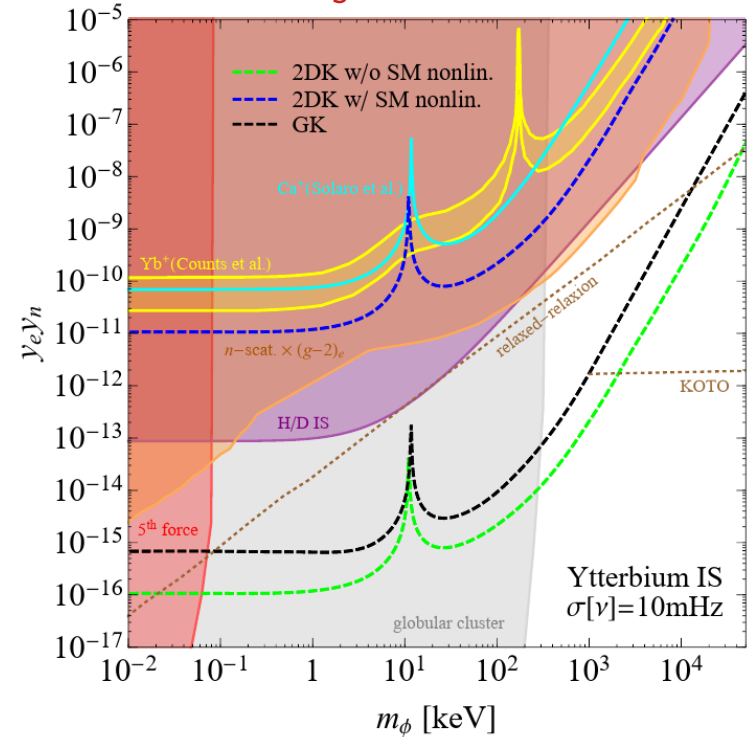
# Generalized King plot

$$m\nu_i^a = K_i + \sum_{l=1}^{m-1} F_{il} m \lambda_{l,a} + \alpha_{\text{NP}} X_i h_a$$

sum of higher-order SM terms  
(without calculating them)

- **replace unknowns** by additional isotope shifts
- Number of clock transitions, isotopes and higher-order terms has to match

[Berengut, Delaunay, Geddes, Soreq '20]  
Higher-orders included



→ see also C. Delaunay's QTI talk

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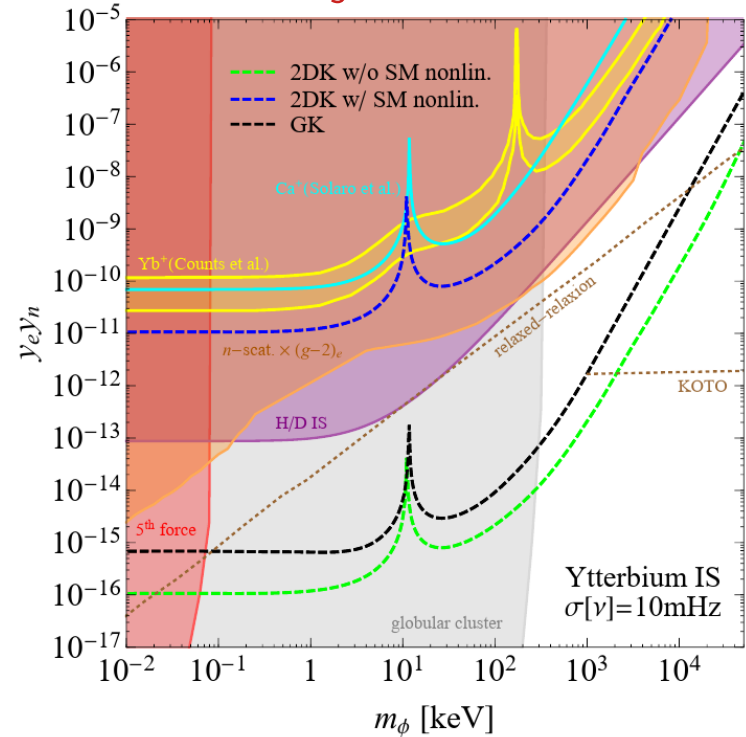
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For any #transitions,  
isotope pairs and to  
combine elements:  
**Global fit** to all King plots

[Delaunay, EF, Kirk,  
Mariotti, Robbiati;  
in progress]

[Berengut, Delaunay, Geddes, Soreq '20]  
Higher-orders included



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# Highly Charged Ions (HCI)

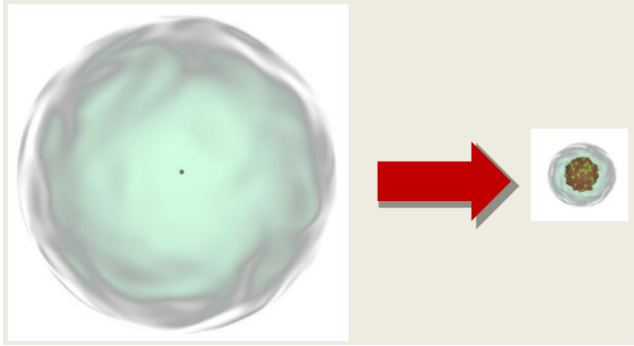


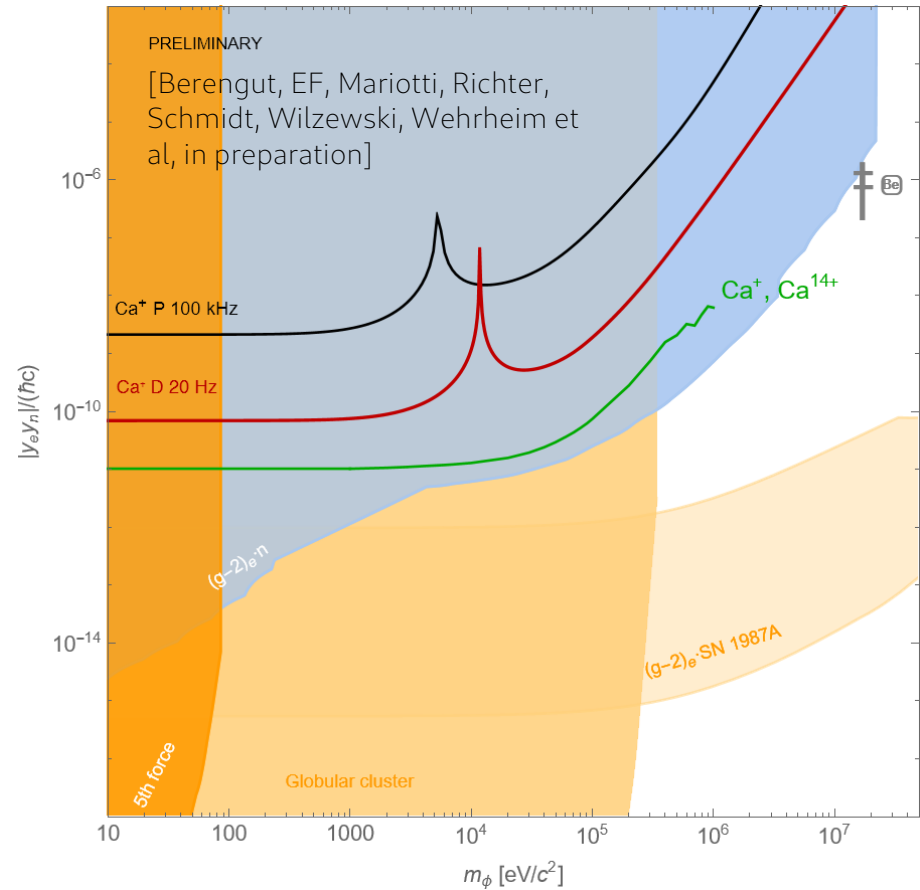
Figure: P. Schmidt

- Electrons removed  $\rightarrow$  less multi-body effects
- QED effects amplified  $\sim Z^4$
- Systematic shifts reduced, Stark shifts  $\sim Z^{-6}$   
 $\rightarrow$  high accuracy in traps
- electrons more closely bound  
 $\rightarrow$  test shorter interaction range?

- ✓ Very sensitive to time-variation of fundamental constants    test ultralight DM
- ✓ Precise optical clock, e.g.  $\text{Ar}^{13+}$  ( $2 \times 10^{-17}$ ) [PTB&MPIK, King et al Nature '22]
- ✓ Precise isotope shift measurements possible    test light mediators

# HCI clock: New Physics bound

- PTB:  $\text{Ca}^{14+} P_0 \rightarrow P_1$  @1Hz  
A. Wilzewski, M. Wehrheim, P. Schmidt et al [preliminary]
- Combined with  $\text{Ca}^+ S \rightarrow D_{5/2}$  @10 /20Hz  
Knollmann et al PRA '19, Solaro, EF et al PRL '20



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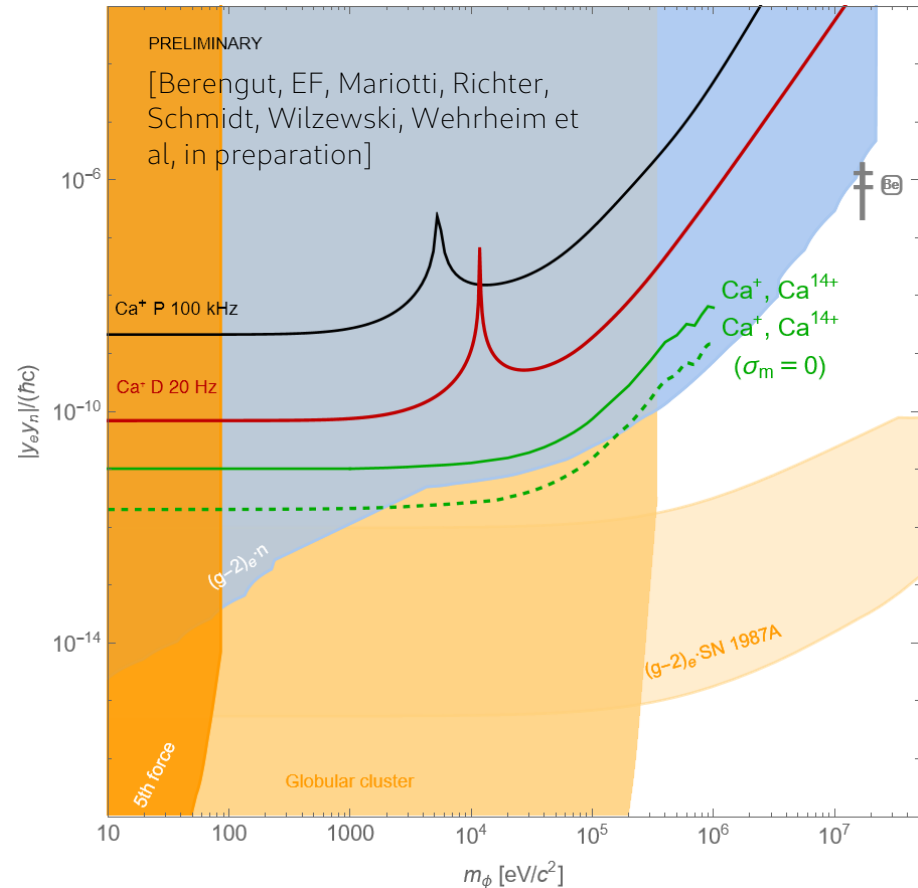
NP sensitivity **limited by isotope masses**

→ MPIK Heidelberg (K. Blaum's group) will improve precision

→ trade isotope masses 3<sup>rd</sup> frequency

→ A. Mariotti's & J. Richter's QTI talk tomorrow

Isotope shifts about to test new parameter space



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- Combined with  $\text{Ca}^+ S \rightarrow D_{5/2}$  @10 /20Hz

Knollmann et al PRA '19, Solaro, EF et al PRL '20

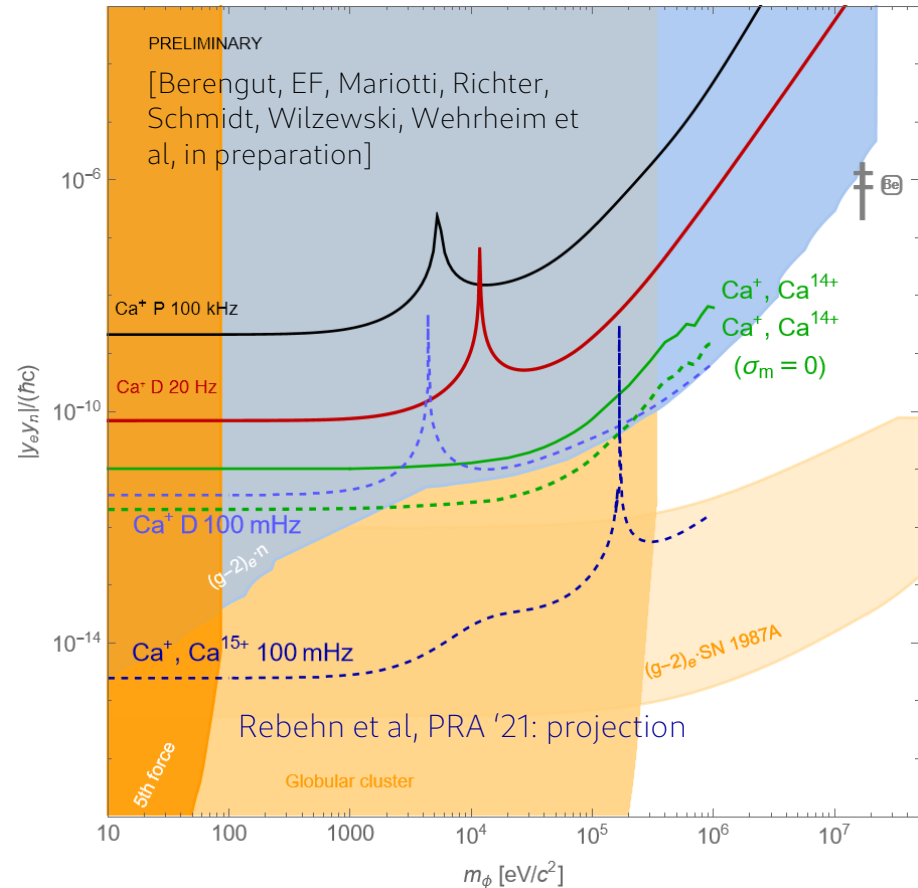
NP sensitivity **limited by isotope masses**

→ MPIK Heidelberg (K. Blaum's group) will improve precision

→ trade isotope masses 3<sup>rd</sup> frequency

→ A. Mariotti's & J. Richter's QTI talk tomorrow

Isotope shifts about to test new parameter space



# Variation of fundamental constants

Scalar ultralight DM  $\phi$

Antypas et al, Snowmass 2203.14915

$$\mathcal{L}_{\text{int}}^{\text{lin}} = \kappa\phi \left\{ \left[ \frac{d_e F_{\mu\nu} F^{\mu\nu}}{4} - d_{m_e} m_e \bar{\psi}_e \psi_e \right] - \left[ \frac{d_g \beta_3 G_{\mu\nu}^a G^{a\mu\nu}}{2g_3} + \sum_{q=u,d,s} (d_{m_q} + \gamma_m d_g) m_q \bar{\psi}_q \psi_q \right] \right\}$$

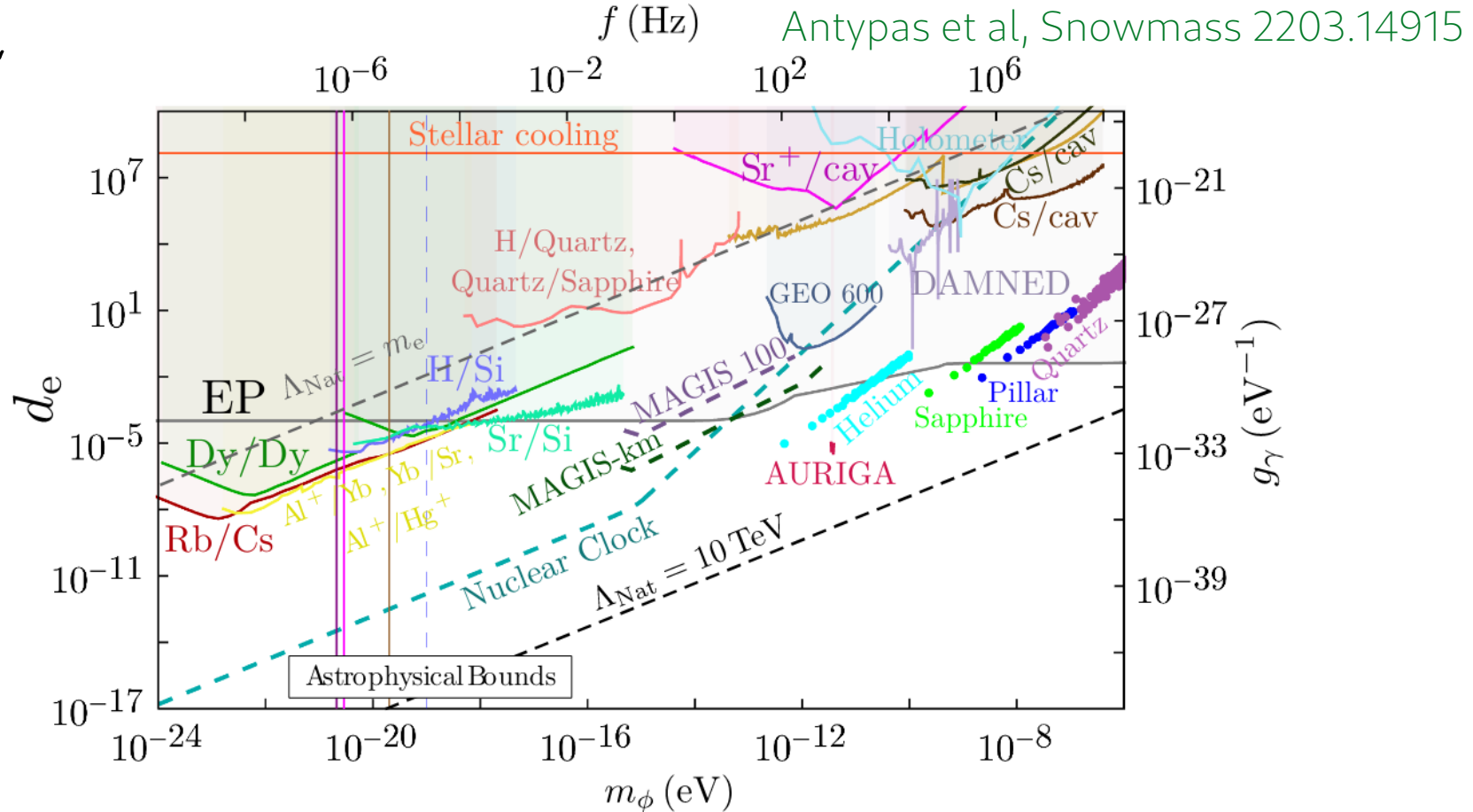
→ induces **oscillations** of  $\alpha_{\text{em}}$  and fermion masses:

$$\phi(t) \approx \phi_0 \cos(m_\phi t)$$

$$\alpha \rightarrow \frac{\alpha}{1 - g_\gamma \phi} \approx \alpha(1 + g_\gamma \phi), \quad m_\psi \rightarrow m_\psi + g_\psi \phi$$

# Ultralight scalar DM-photon coupling

$$\kappa \frac{d_e}{4} \phi F_{\mu\nu} F^{\mu\nu}$$





# Outline

---

Domcke, Kopp, EF, Bringmann 2304.10579

## 4) High-frequency GWs with optical photons

# GW sources and detectors

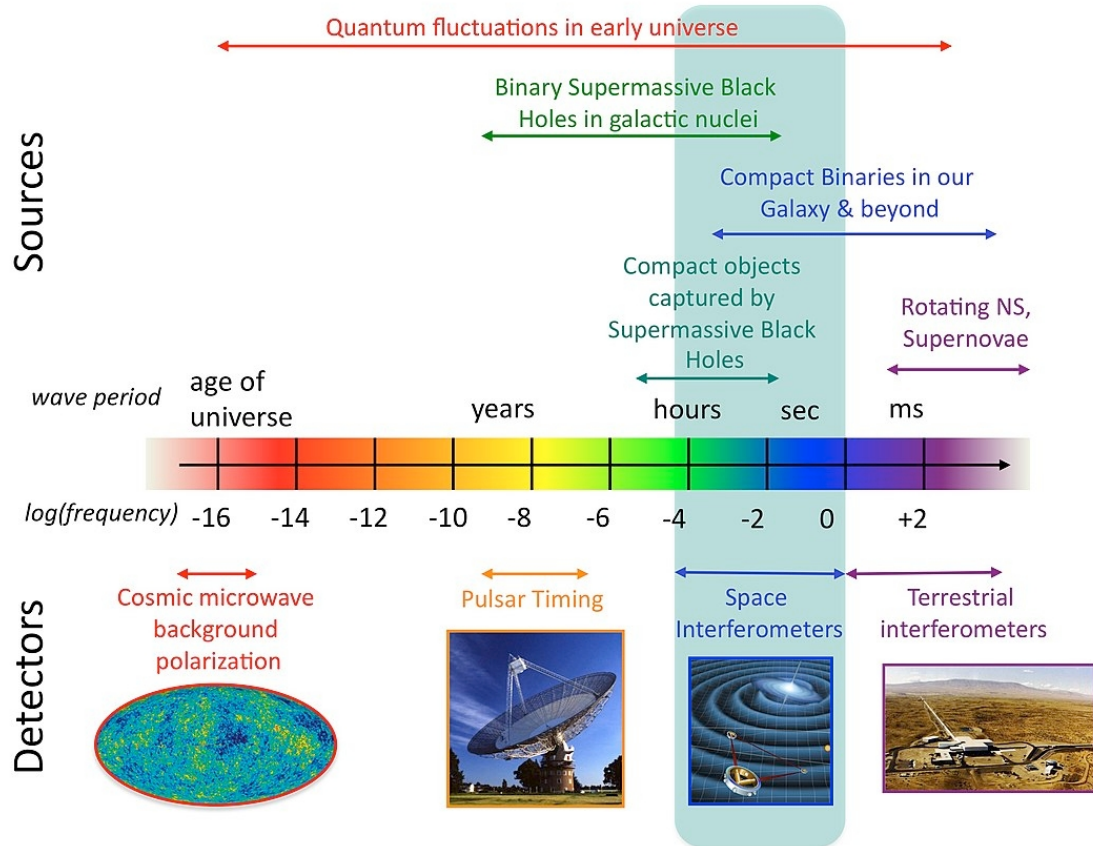
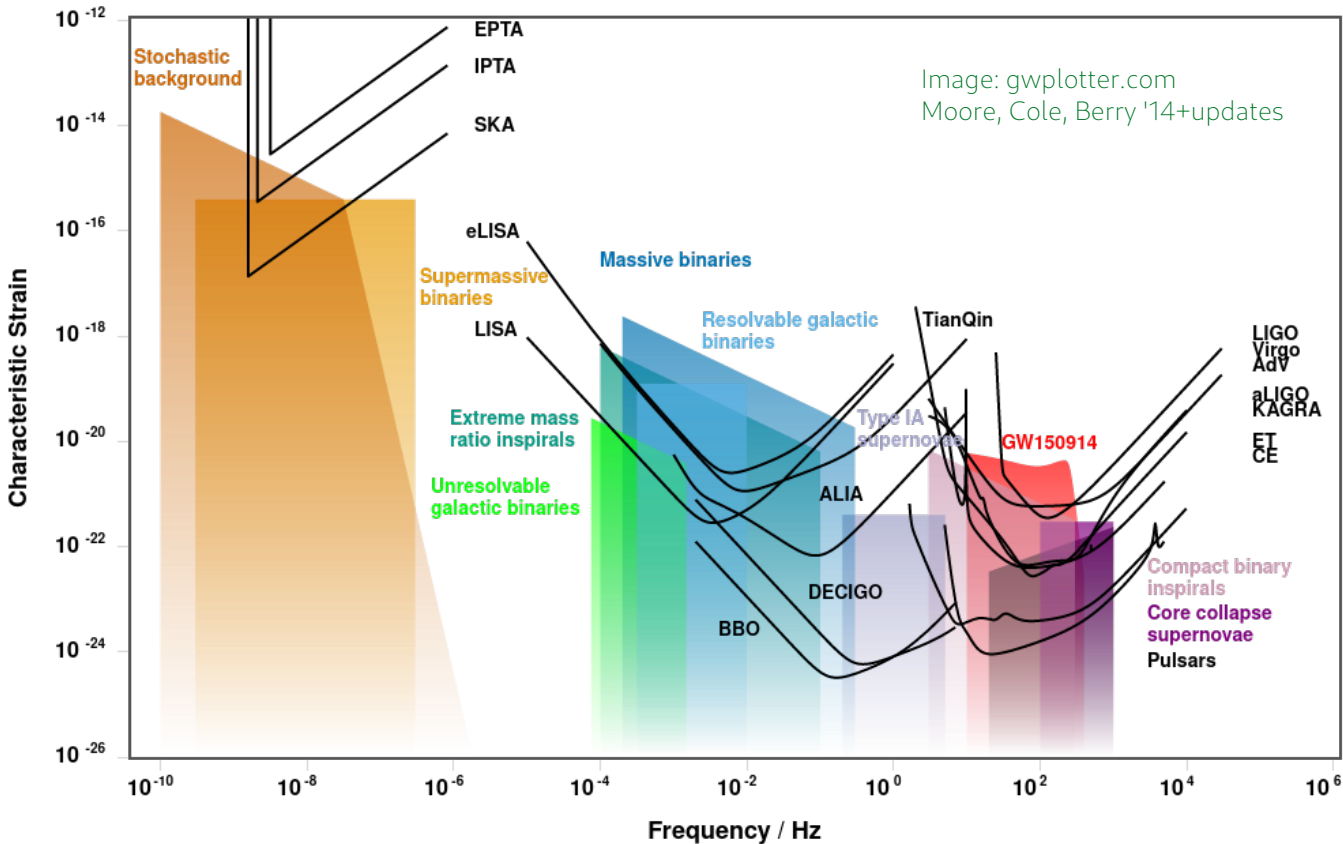
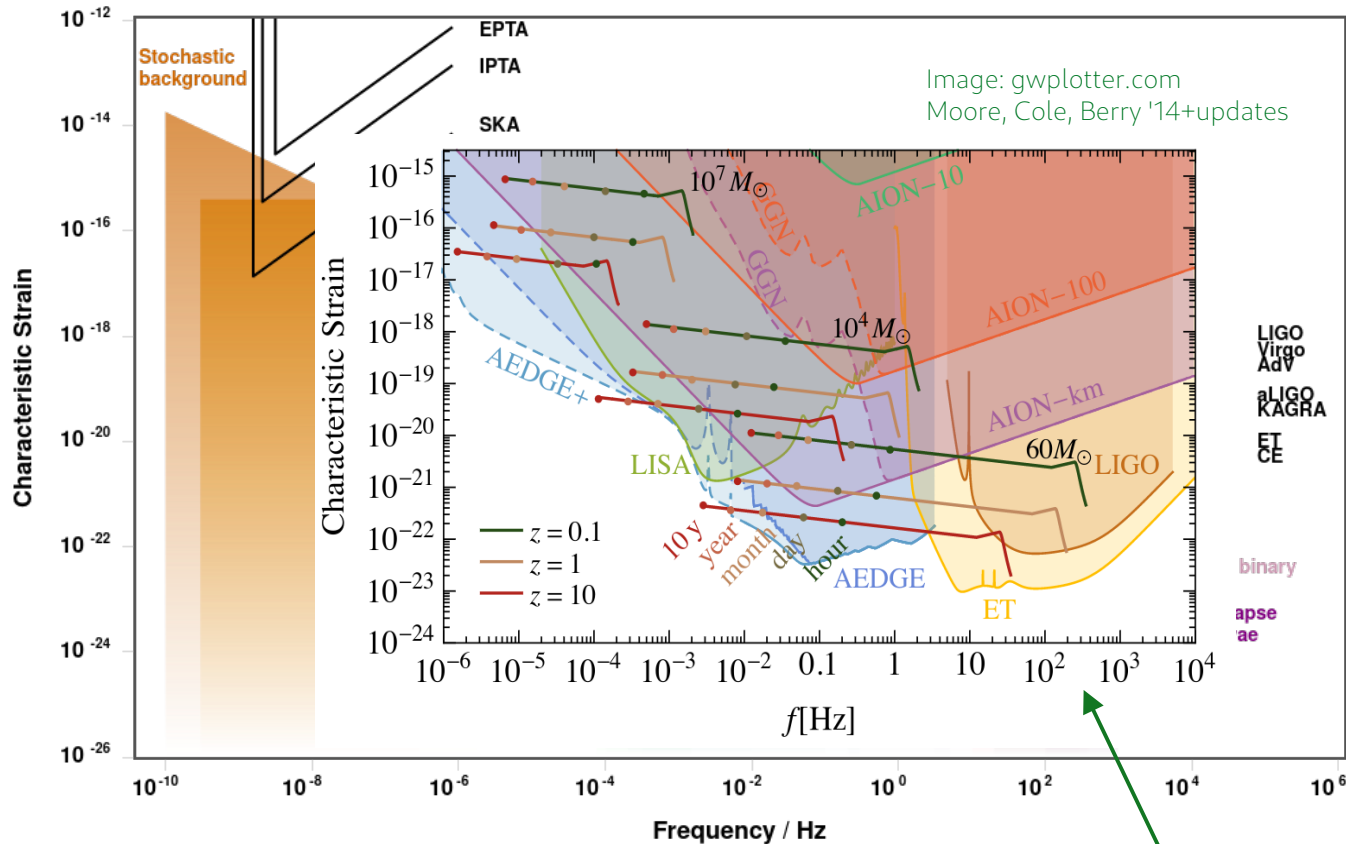


Image: NASA

# Sensitivity to GW sources

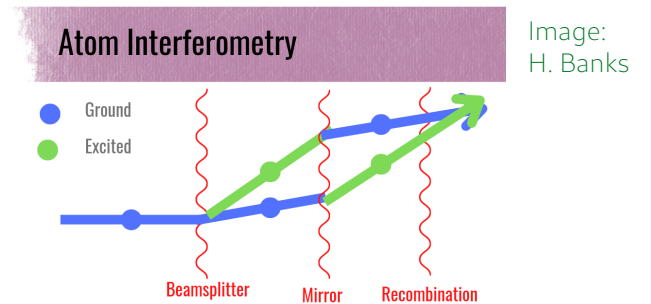


# Sensitivity to GW sources



Badurina, Buchmueller, Ellis, Lewicki, McCabe, Vaskonen '21

Atom Interferometers sensitive to mid-frequency GWs

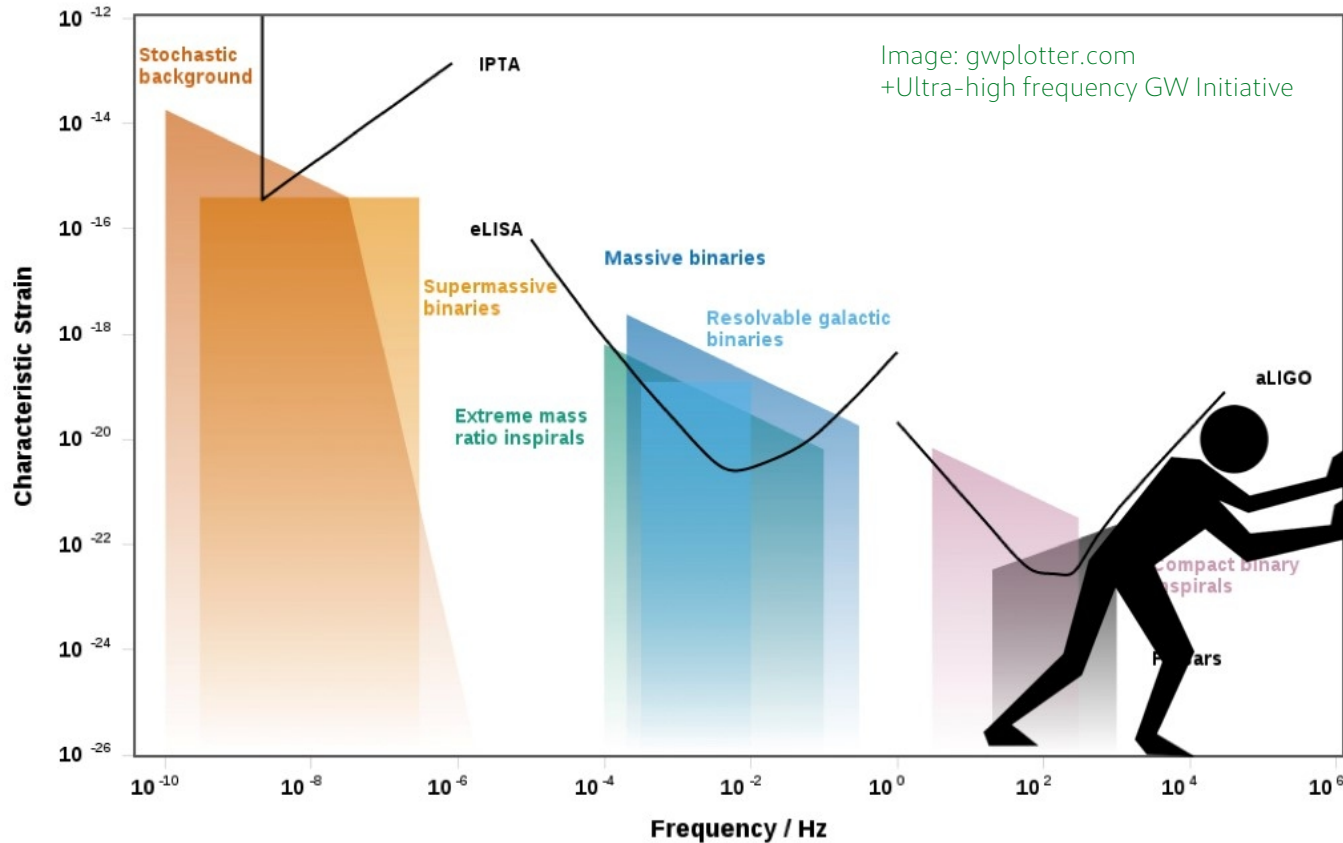


Measure phase difference between matter waves

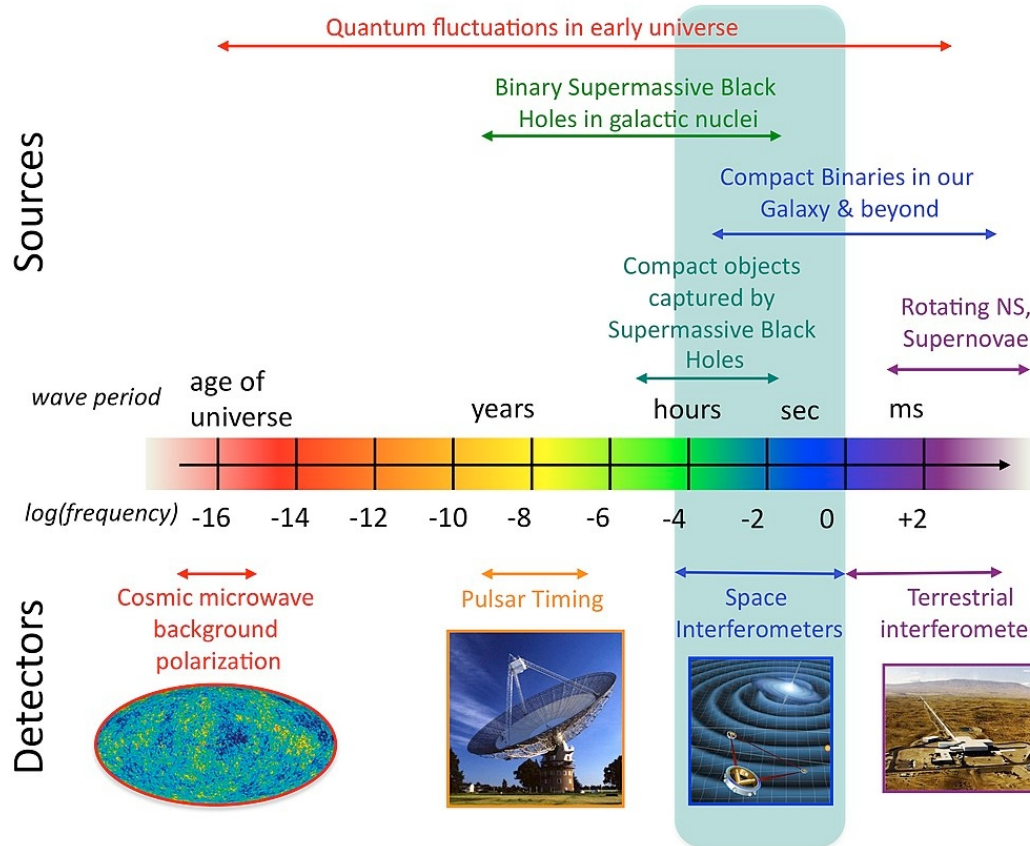
**As a GW Detector:**

GW modifies distance between 2 atom interferometers → phase shift

# Pushing towards high frequencies



# GW sources and detectors



Any sources for high-frequency GWs expected?



If yes, how can one detect them?

Image: NASA

# GW sources: high frequency

Ultrahigh frequency  
>10kHz:  
no known astrophysical  
sources with large enough  
signal

Potential sources:

- 1<sup>st</sup> order phase transition in Early Universe at  $T \gg 100$  GeV
- Primordial Black Hole mergers

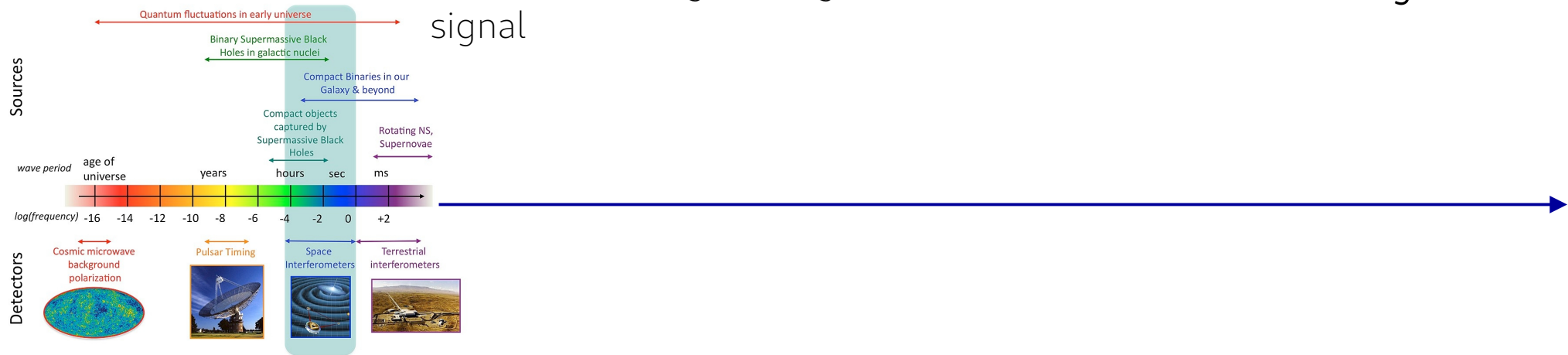


Image: NASA

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 $>10\text{kHz}$ :  
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- 1<sup>st</sup> order phase transition in Early Universe at  $T \gg 100 \text{ GeV}$
- Primordial Black Hole mergers
- Phase transition in neutron star mergers if QCD has 1<sup>st</sup> order PT, nuclear matter compressed during merger  $\rightarrow \text{MHz GW}$

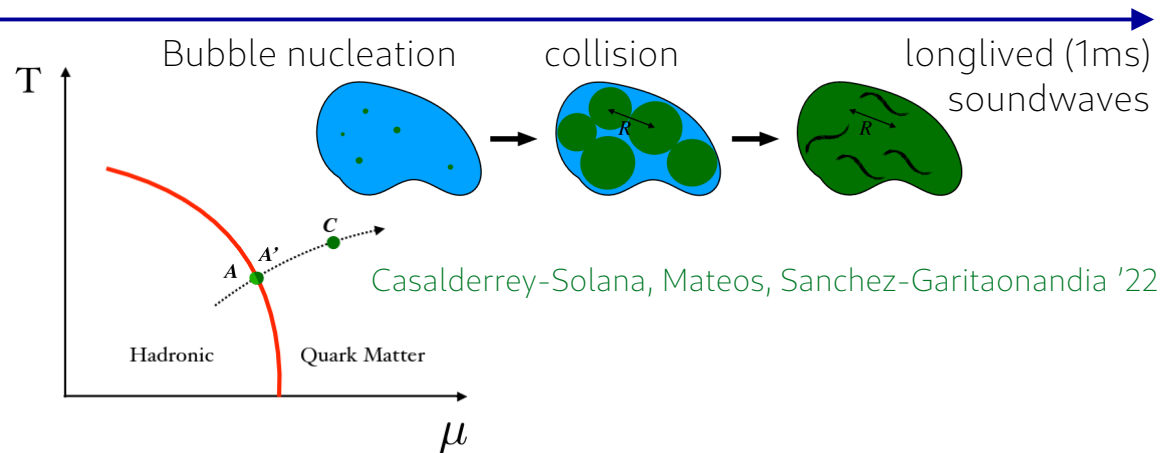
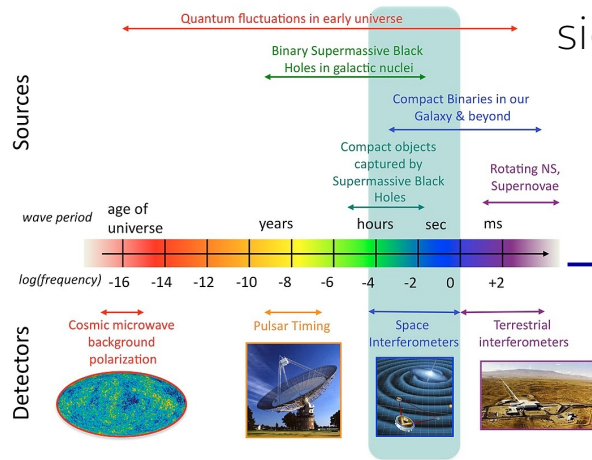


Image: NASA

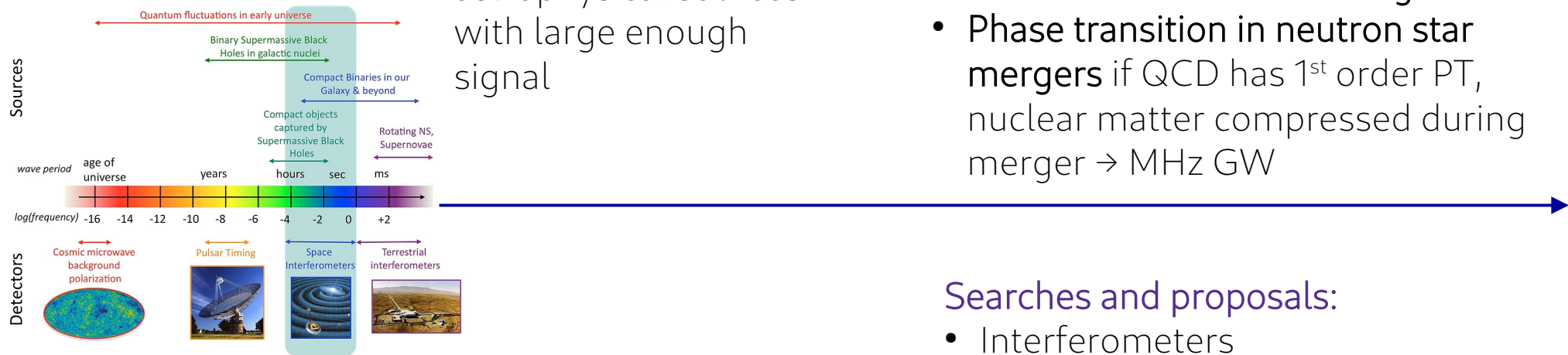


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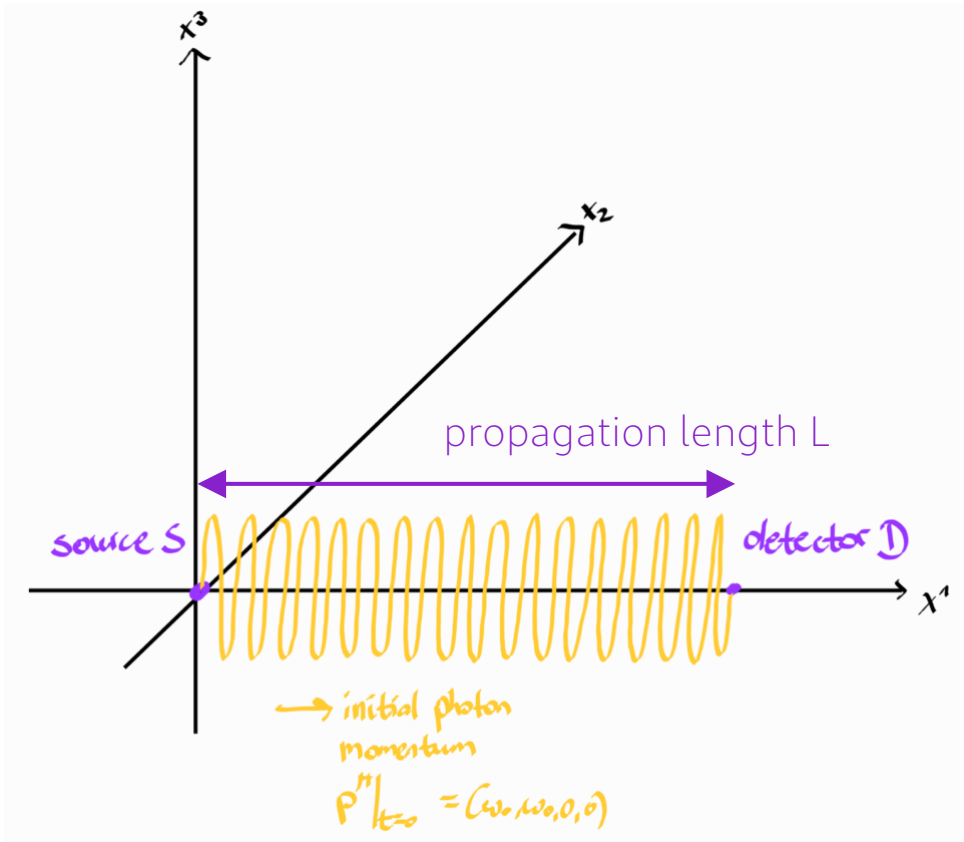


Searches and proposals:

- Interferometers
- Levitated sensors
- Radio cavities

Image: NASA

# Photon in gravitational field

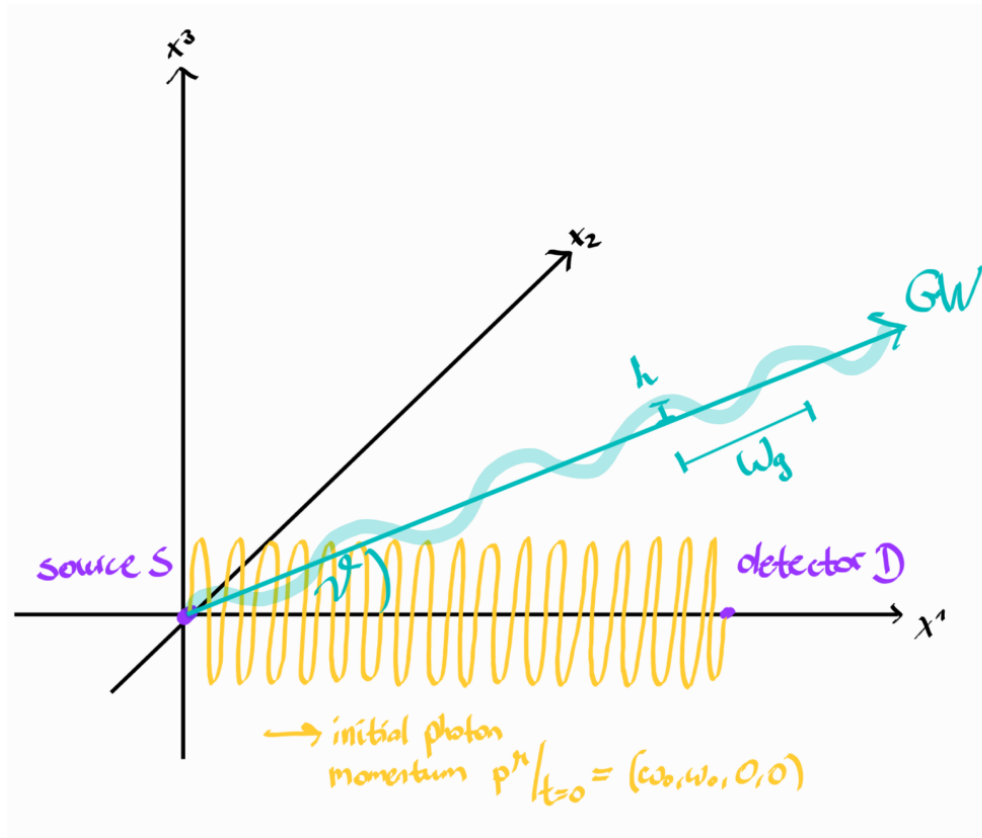


**Goal:** compare frequency of photon measured by S and D

Free-falling observer moving with 4-velocity  $u^\mu$  measures at D

$$\omega_\gamma = -g_{\mu\nu} p^\mu u^\nu$$

# Photon in gravitational field



**Goal:** compare frequency of photon measured by S and D

**Gravitational Wave:** perturbs metric

$$g_{\mu\nu} = \eta_{\mu\nu} + h_{\mu\nu}$$

$$p^\mu = (\omega_0, \omega_0, 0, 0) + \delta p^\mu \sim h \text{ (GW strain)}$$

$$u^\mu = (1, 0, 0, 0) + \delta u^\mu$$

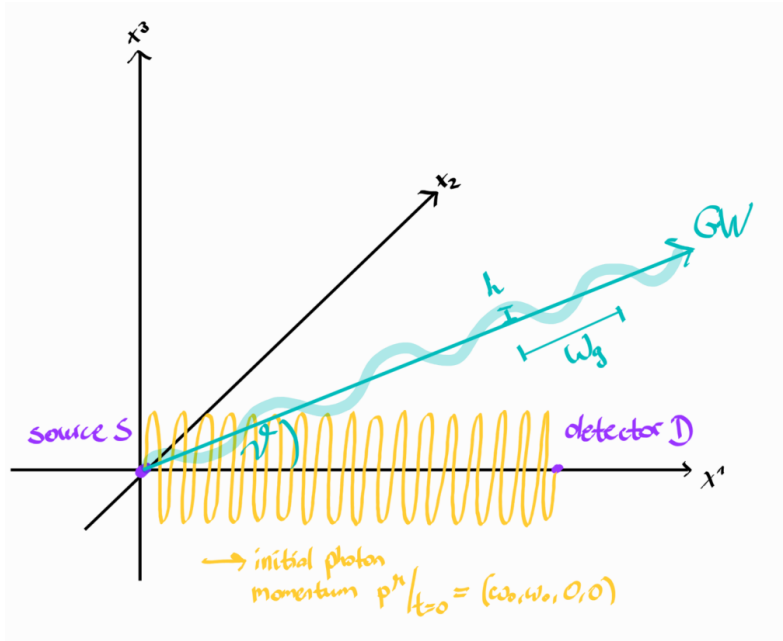
Geodesic equation  $\rightarrow \dots \rightarrow$  master formula for frequency change at  $O(h)$ :

$$\frac{\omega_\gamma^D - \omega_\gamma^S}{\omega_\gamma^D} = -\frac{\omega_0}{2} \int_0^{\lambda_D} d\lambda' \partial_0 [h_{00} + 2h_{10} + h_{11}]_{x^\mu = x_{\lambda', 0}^\mu}$$

$$+ [\delta u^0 - \delta u^1](\lambda_D) - [\delta u^0 - \delta u^1](\lambda_S).$$

# Free-falling detectors – TT frame

- S and D in free fall (move freely at least in direction of photon propagation)
  - most convenient in **transverse traceless (TT) gauge**  $h_{\mu 0}^{TT} = 0$ ,  $\partial^i h_{ij}^{TT} = 0$ ,  $\eta^{ij} h_{ij}^{TT} = 0$  where observers at rest remain at rest



$$h_{11}^{TT}(x^\mu) = h_+ s_\vartheta^2 \cos[\omega_g(x^0 - c_\vartheta x^1 - s_\vartheta x^3) + \varphi_0]$$

Plane wave

Frequency shift by GW (in + polarization)

$$\frac{\omega_\gamma^D - \omega_\gamma^S}{\omega_\gamma^D} = h_+ c_\vartheta^2 / 2 \left\{ \cos \varphi_0 - \cos[\omega_g L(1 - c_\vartheta) + \varphi_0] \right\},$$

# Rigid ruler – PD frame

- Proper-detector (PD) frame: distances an observer with a rigid ruler would measure

$$\frac{\omega_{\gamma}^D - \omega_{\gamma}^S}{\omega_{\gamma}^D} = \frac{h_+}{2} \left\{ \cos \varphi_0 - \omega_g L \sin(\omega_g L + \varphi_0) + \left( \frac{1}{2} \omega_g^2 L^2 - 1 \right) \cos(\omega_g L + \varphi_0) \right\}$$

Enhanced sensitivity for large  $\omega_g L \gg 1$  ?

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✘ no material is perfectly rigid at high frequencies!

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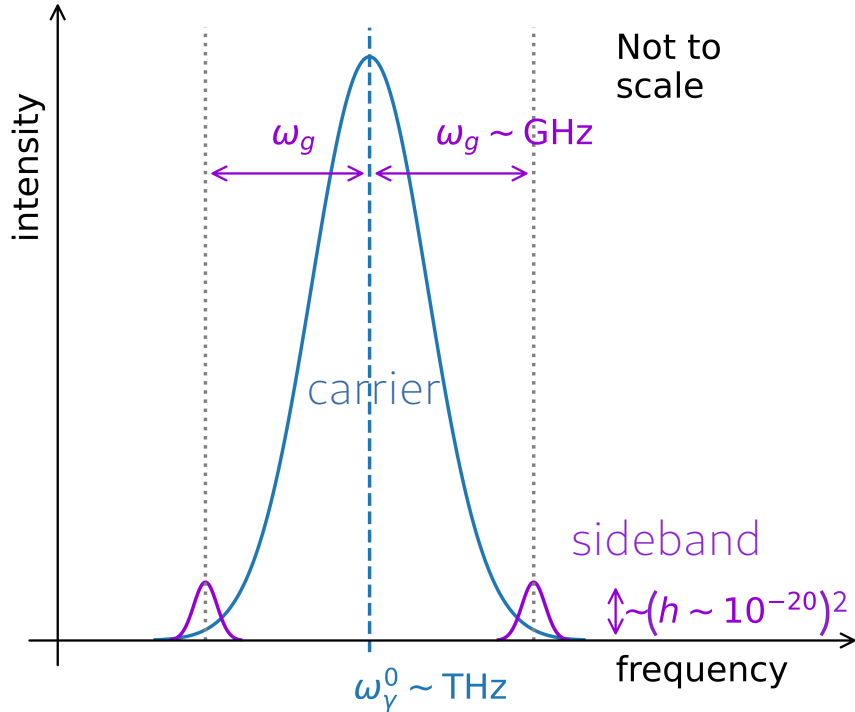
Enhanced sensitivity for large  $\omega_g L \gg 1$  ?

✗ no material is perfectly rigid at high frequencies!

→ generic implication for detector design:

this equation is not directly applicable for  $\omega_g L \gg v_s$

# Detection: 1) Sidebands



- Naive expectation was: GW changes photon frequency
- Instead: **tiny sidebands**
  - separated from carrier (original photon frequency) by **GW frequency  $\omega_g$**
  - suppressed by the **GW amplitude  $h^2 \sim 10^{-40}$**

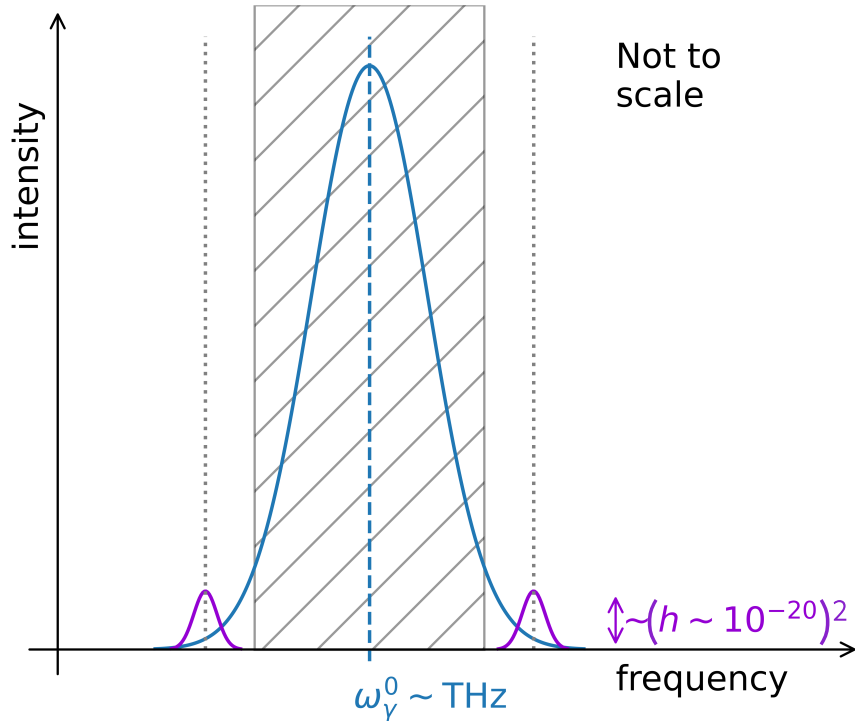
➡ Advantage for **high-frequency GWs**

Still: tails from intense carrier line can hide the sidebands

➡ How to make the sidebands detectable?

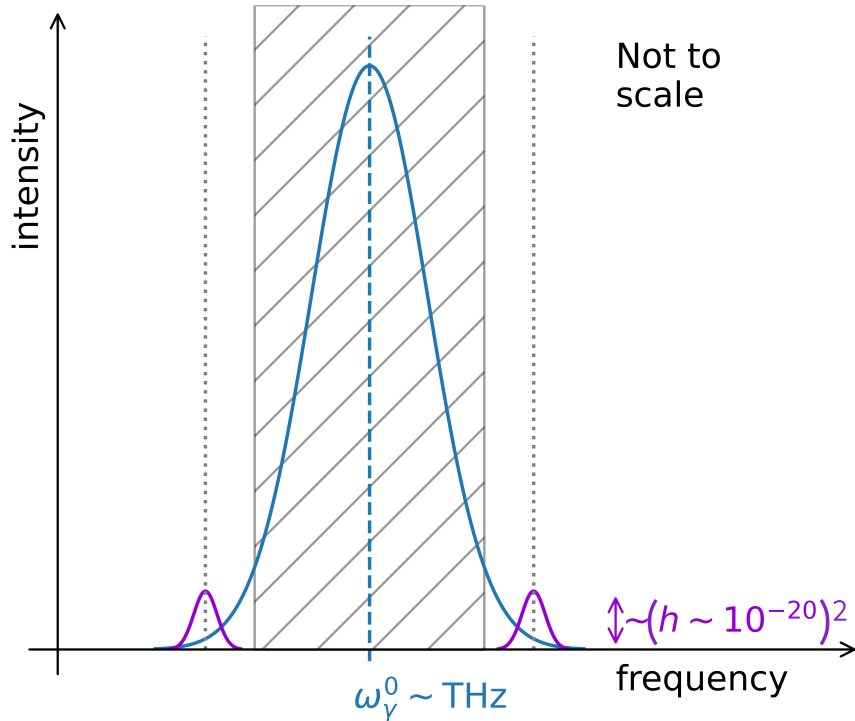


# Detection: 1) Sidebands



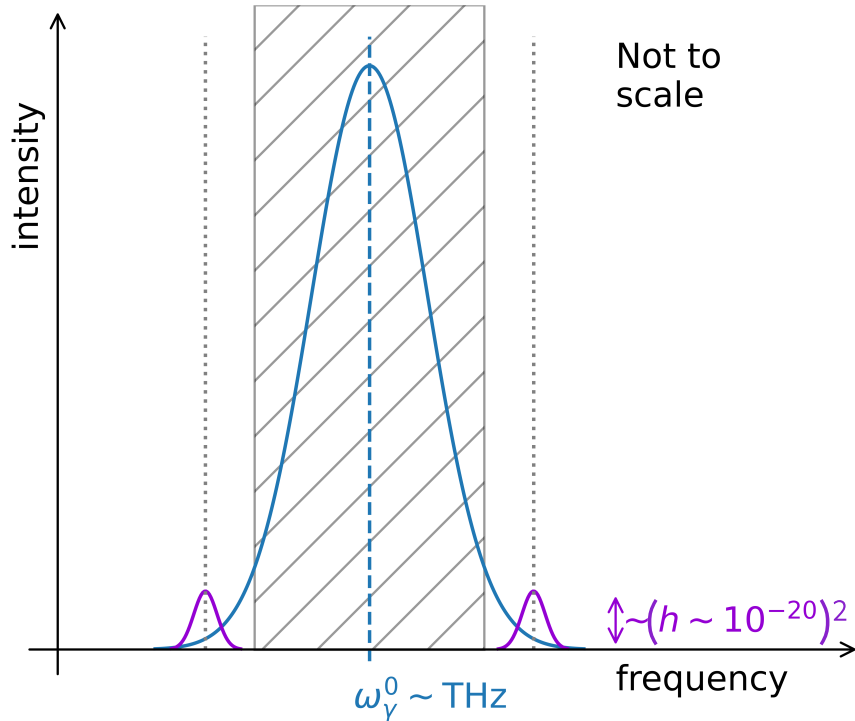
- Idea: design filter to cut out the intense carrier line  
→ direct detection of sidebands  
→ need to detect photons above background

# Detection: 1) Sidebands



- Idea: design filter to cut out the intense carrier line  
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→ need to detect photons above background
- Interference term “only” suppressed by  $h$ , but overwhelmed by background from carrier  
→ modulate carrier line? (further investigation)

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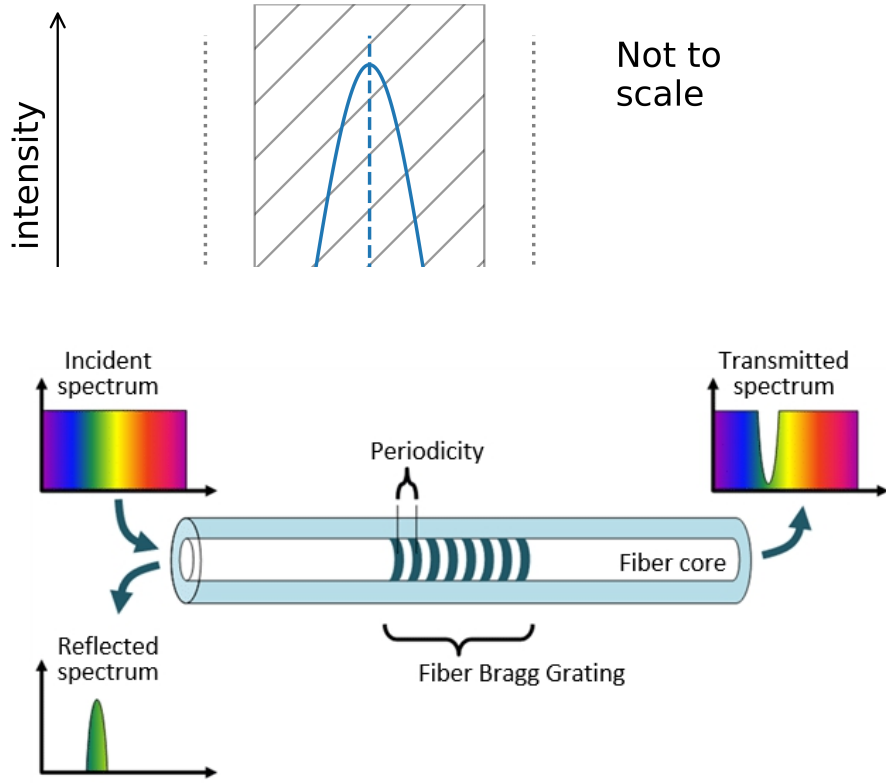


Idea: design filter to cut out the intense carrier line  
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- **Narrow filter** of bandwidth  $\Delta\lambda$  and suppression of carrier  $\alpha_T \ll 1$ 
  - Optical cavity tuned to sideband  
PTB: finesse 500,000,  $L=30\text{cm}$ ,  $\Delta\lambda = \text{kHz}$

# Detection: 1) Sidebands

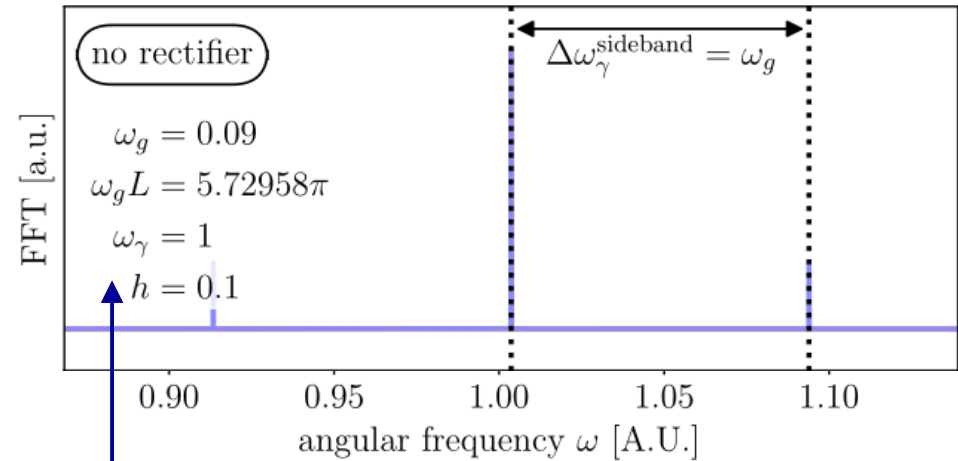
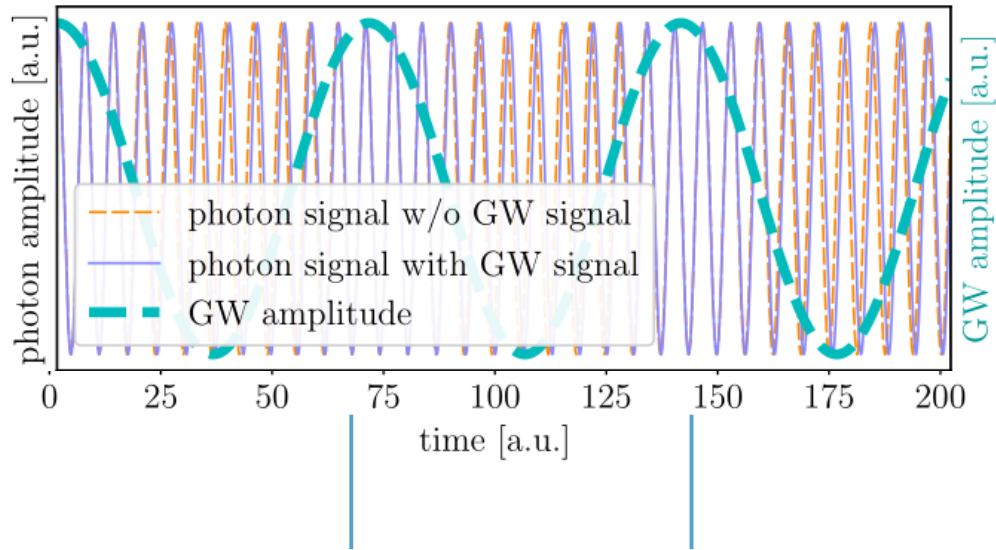


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  - Fiber Bragg Grating

# Detection: 2) Optical clocks

Original setup:



Parameters chosen for illustration purposes only

Phase modulation is averaged out during GW period



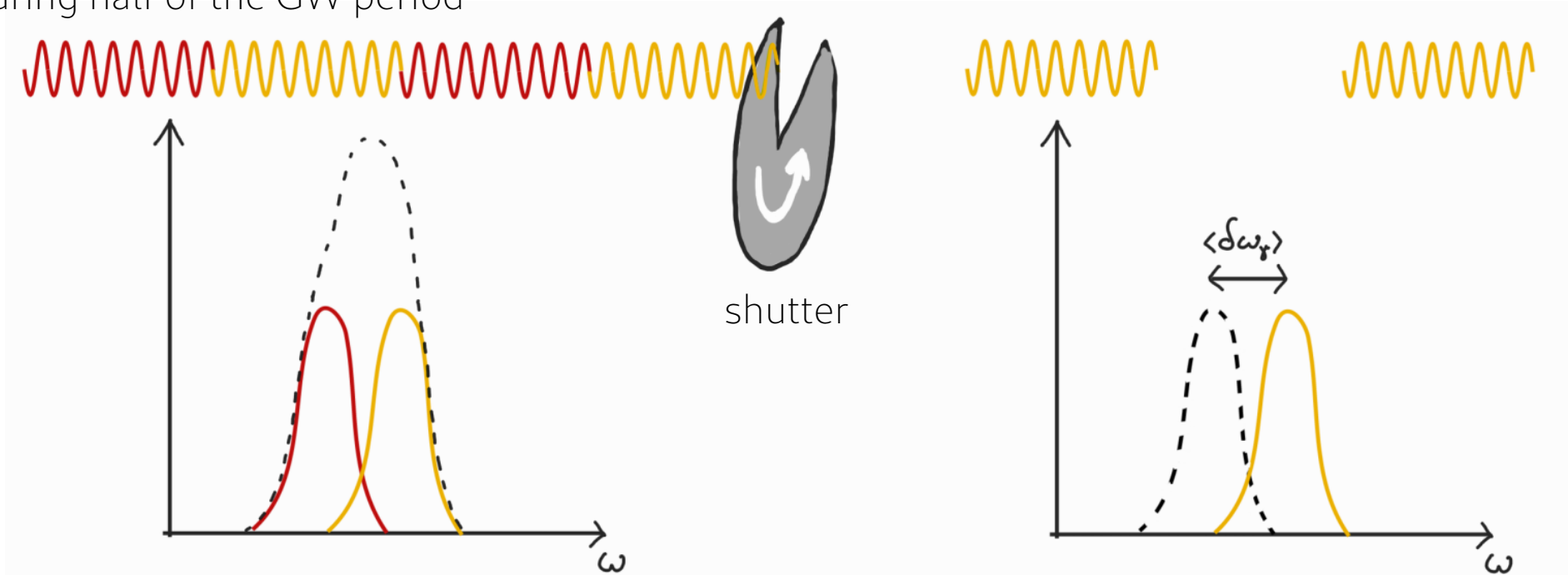
Only sidebands, no net frequency shift of  $\gamma$

# Detection: 2) Optical rectifier

Idea: block the photon propagation during half of the GW period



Shift does *not* average out

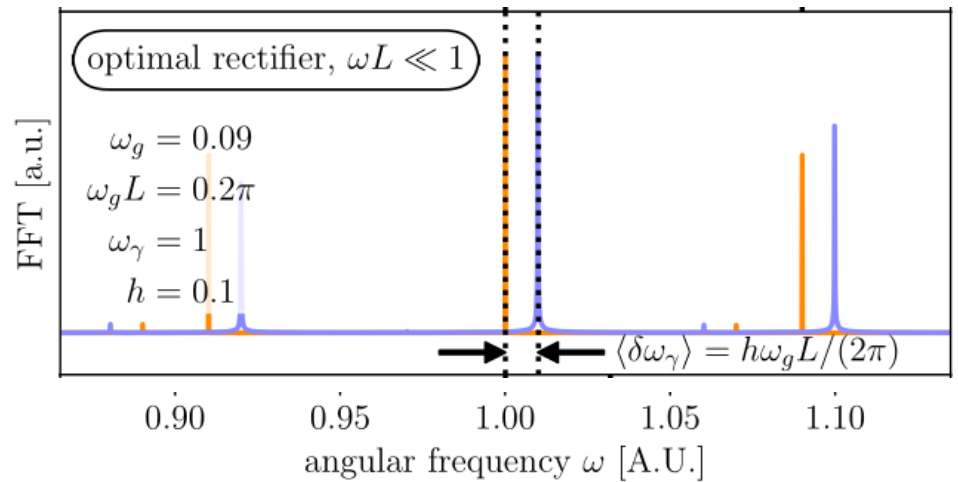
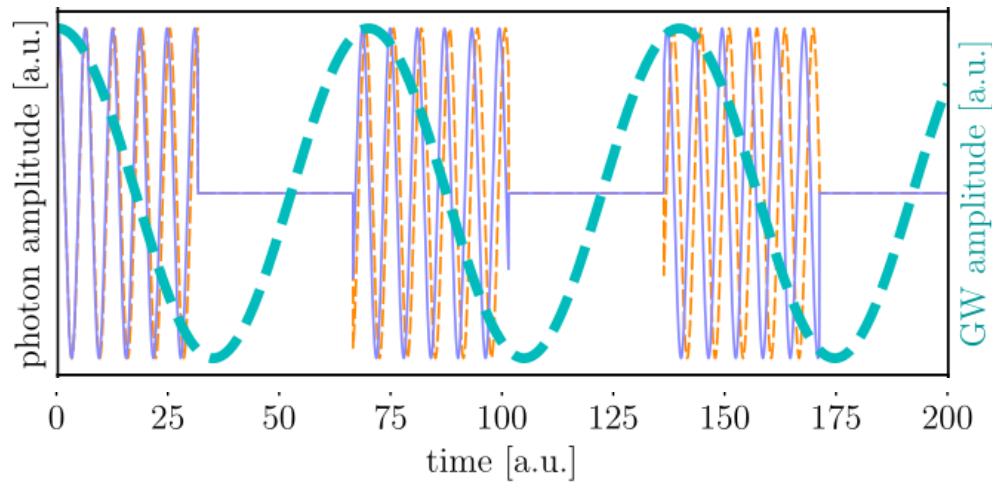


Photon net frequency shift detectable by Ramsey spectroscopy

# Rectifier: small $\omega L$

Pass if  $\sin \varphi_0 = \sin \omega_g t > 0$

$$\langle \delta\omega_\gamma \rangle = h\omega_g L / (2\pi) \quad (\theta = \pi/2)$$



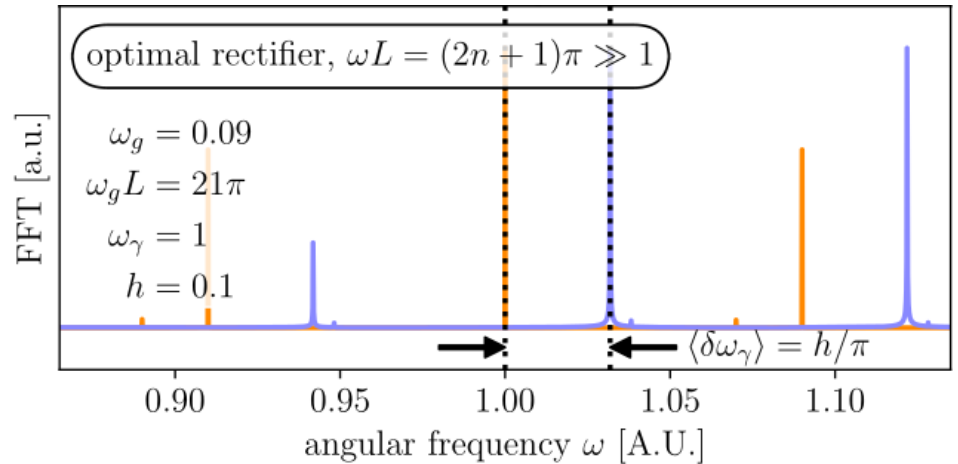
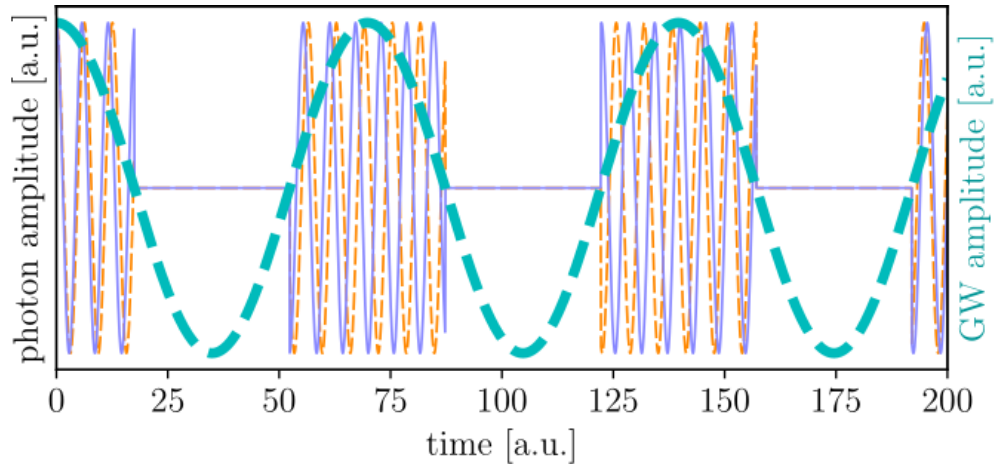
Orange sideband: effect of shutter

Not only sideband, but also frequency shift of photon carrier line

# Rectifier: large $\omega L$

Pass if  $\sin[\varphi_0 + \pi/2] > 0$

$$\langle \delta\omega_\gamma \rangle = h/\pi$$





# Sensitivity

Assumptions in the limits:

$$\tau = 1 \text{ s}, L = 1 \text{ m}, \omega_\gamma^S / 2\pi = 2 \times 10^{14} \text{ Hz}$$

Integration time

optical

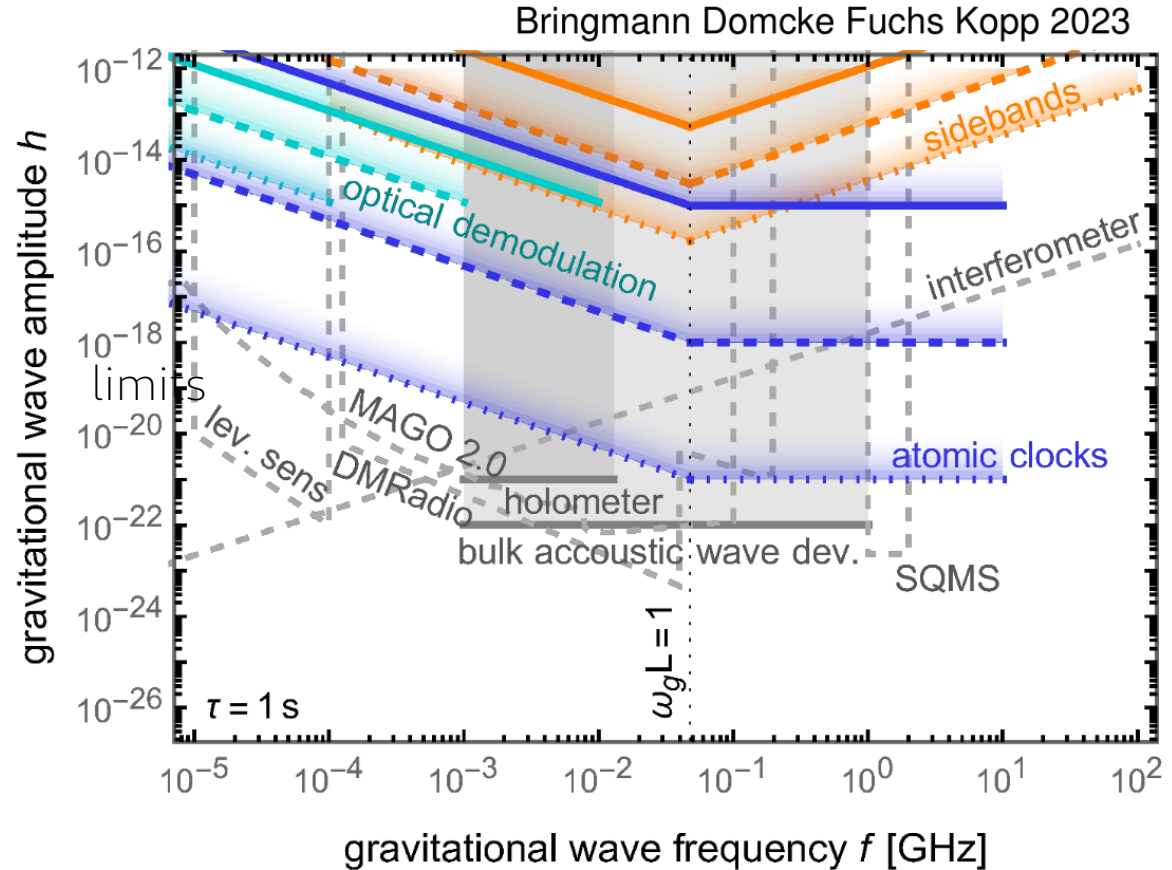
$$P = \text{mW} \quad \text{Laser power: need high \#photons}$$

transmission    Thermal noise

$$= \{ (\alpha_T, \alpha_{th}) \}$$

$(10^{-10}, 10^{-15})$	conservative
$(10^{-15}, 10^{-17})$	realistic
$(10^{-20}, 10^{-19})$	optimistic

Promising approach over broad frequency range



# Complementary: LHC, EDM, cosmo

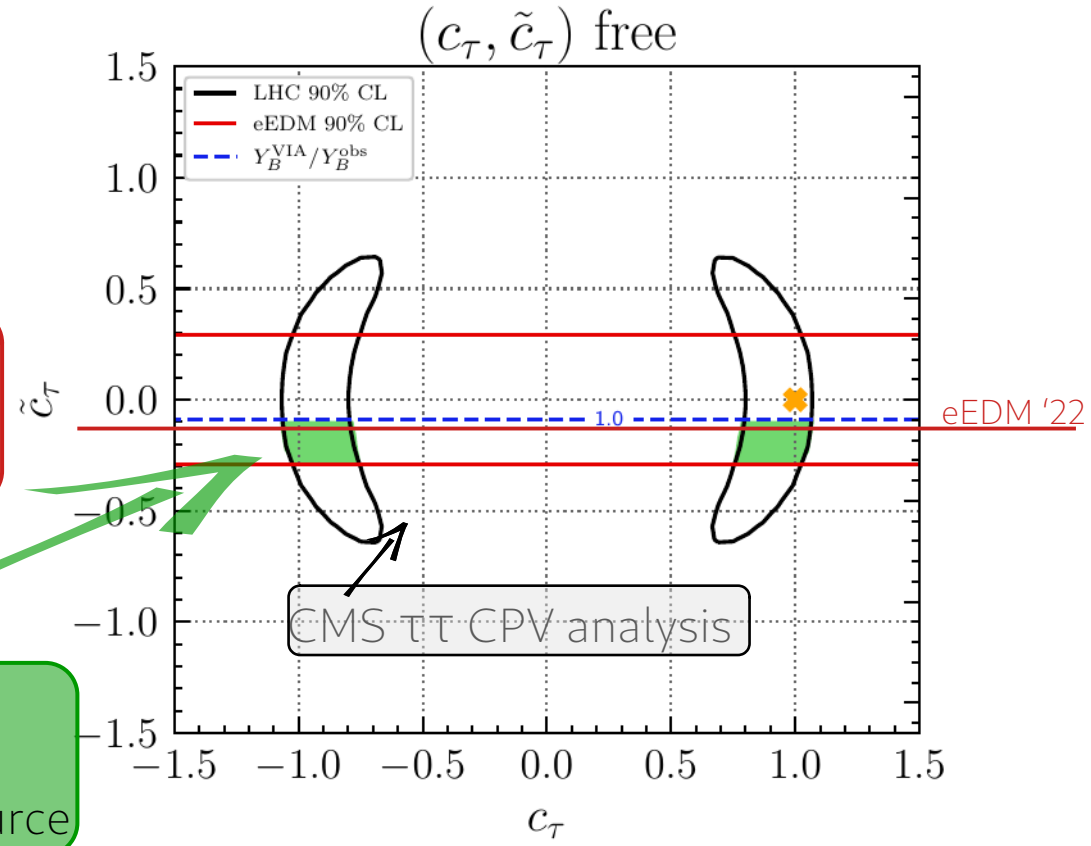
Bahl, EF, Heinemeyer, Katzy, Menen, Peters, Saimpert, Weiglein '22

*See also*  
 Brod, Haisch, Zupan '13  
 De Vries, Postma, van de Vis '18  
 EF, Losada, Nir, Viernik '19, '20, '20  
 Aharony-Shapira '21  
 Brod, Cornell, Skodras, Stamou '22

Electroweak  
 baryogenesis  
 $Y_B \propto \tilde{c}_f$

Caveat: "optimistic" scenario,  
 large uncertainty  
 (vev-insertion approximation)  
 → approx. **upper bound**

Basler, Mühlleitner, Müller '20  
 Cline, Kainulainen '20  
 Cline, Laurent '21, Postma '21  
 Kainulainen '21  
 Postma, van de Vis, White '22



Electron electric  
 dipole moment  
 $d_e \propto \tilde{c}_f$

Allowed by LHC, EDM,  
 EWBG (if VIA correct)  
 →  $\tau$  may be single source

# CERN Quantum Technology Initiative

CERN Accelerating science

QTI: <https://quantum.cern/> [Sign in](#) [Directory](#)



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Accelerating Quantum Technology Research and Applications

Head: Alberto di Meglio

<u>Branches:</u>	<u>Coordinators:</u>
Quantum Sensing	Michael Doser
Quantum Computing	Sofia Vallecorsa
Quantum Theory & Simulation	Elina Fuchs
Quantum Communication & Networks	Edoardo Martelli

Collaboration between CERN and universities/institutes in the member (&non-member) states → visitors!

Also collaboration with industry (e.g. IBM-Q)

Nov 2022: Quantum Technologies for High Energy Physics ([QT4HEP](#))

Next week: **QTI Phase 2** proposal in Council

01/2024 – 12/2028: planned QTI Phase 2 with e.g. cavities → axions, exotic atoms, quantum computing



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Stay tuned,  
get involved!

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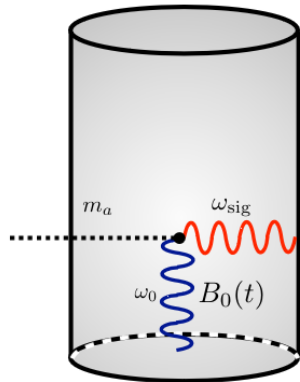
01/2024 – 12/2028: planned QTI Phase 2 with e.g. cavities → axions, exotic atoms, quantum computing



# Quantum sensing in Phase 2

Searches for **axions** and **GWs** with tuneable RF cavities Heterodyne Resonator:

$$\omega_{\text{sig}} \sim \omega_0 \pm m_a \sim V^{-1/3}$$



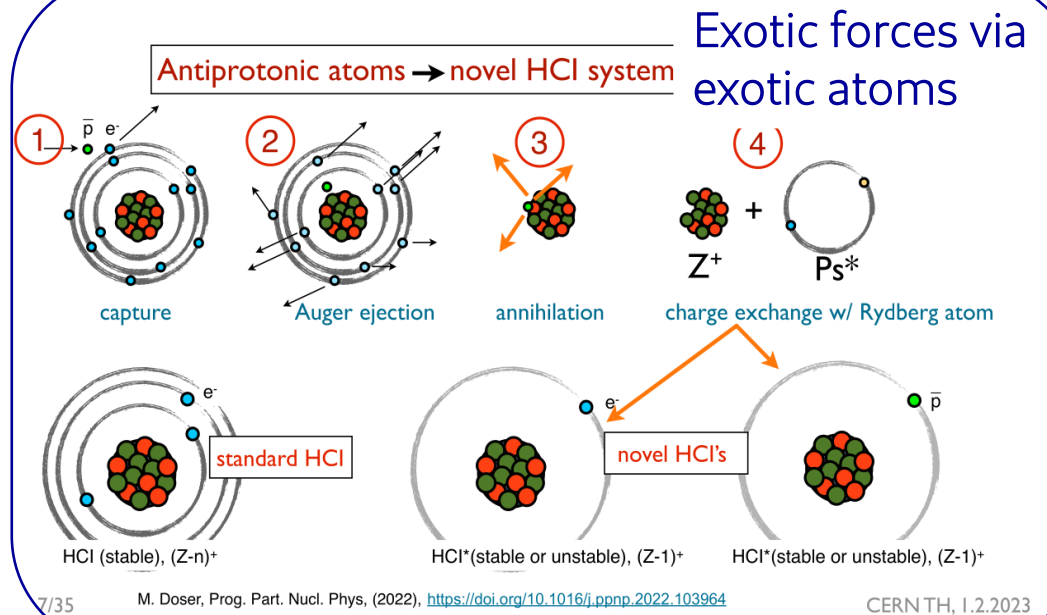
JHEP 07 (2020) 088, hep-ph/1912.11048  
 A. Berlin, R. T. D'Agnolo, SARE, P. Schuster, N. Toro,  
 C. Nantista, J. Neilson, S. Tantawi, K. Zhou

Also: R. Lasenby hep-ph/1912.11467

Dark Matter  
via Atom  
interferometer

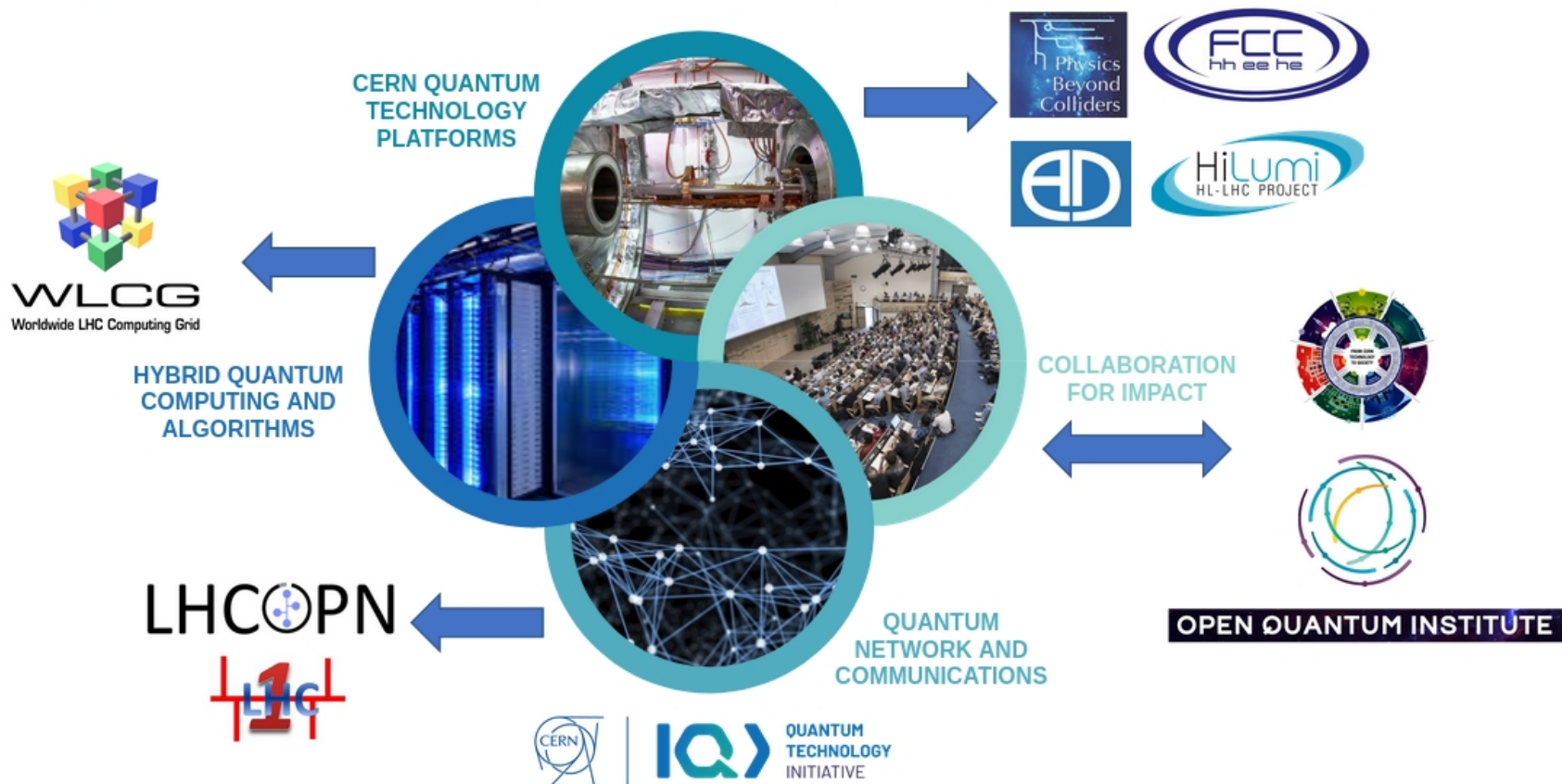
Dark Matter  
via nuclear  
clock

Millicharged particles via Transition Edge  
Sensor (low threshold)



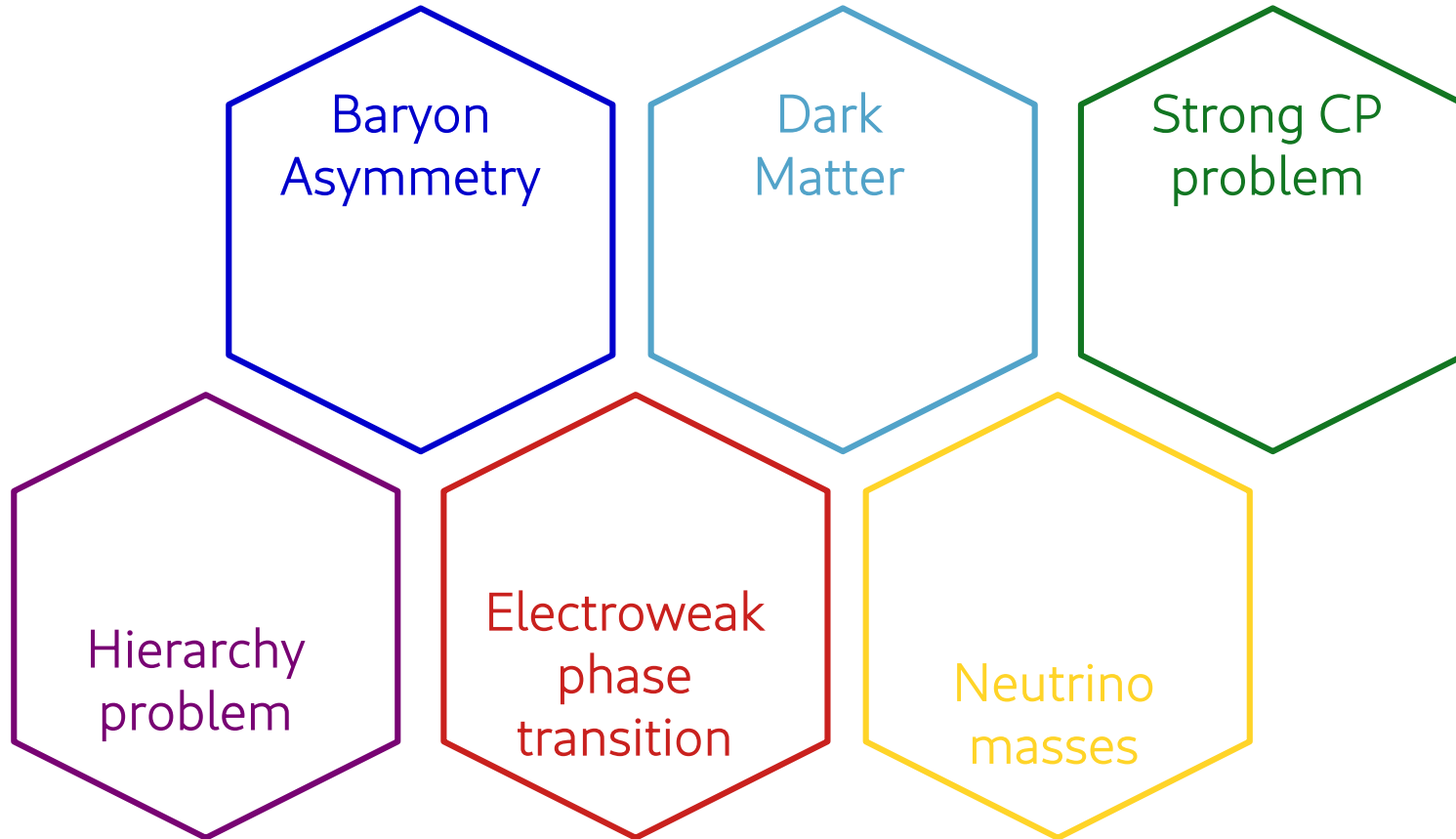


# QTI Phase 2 Vision



# Particle questions

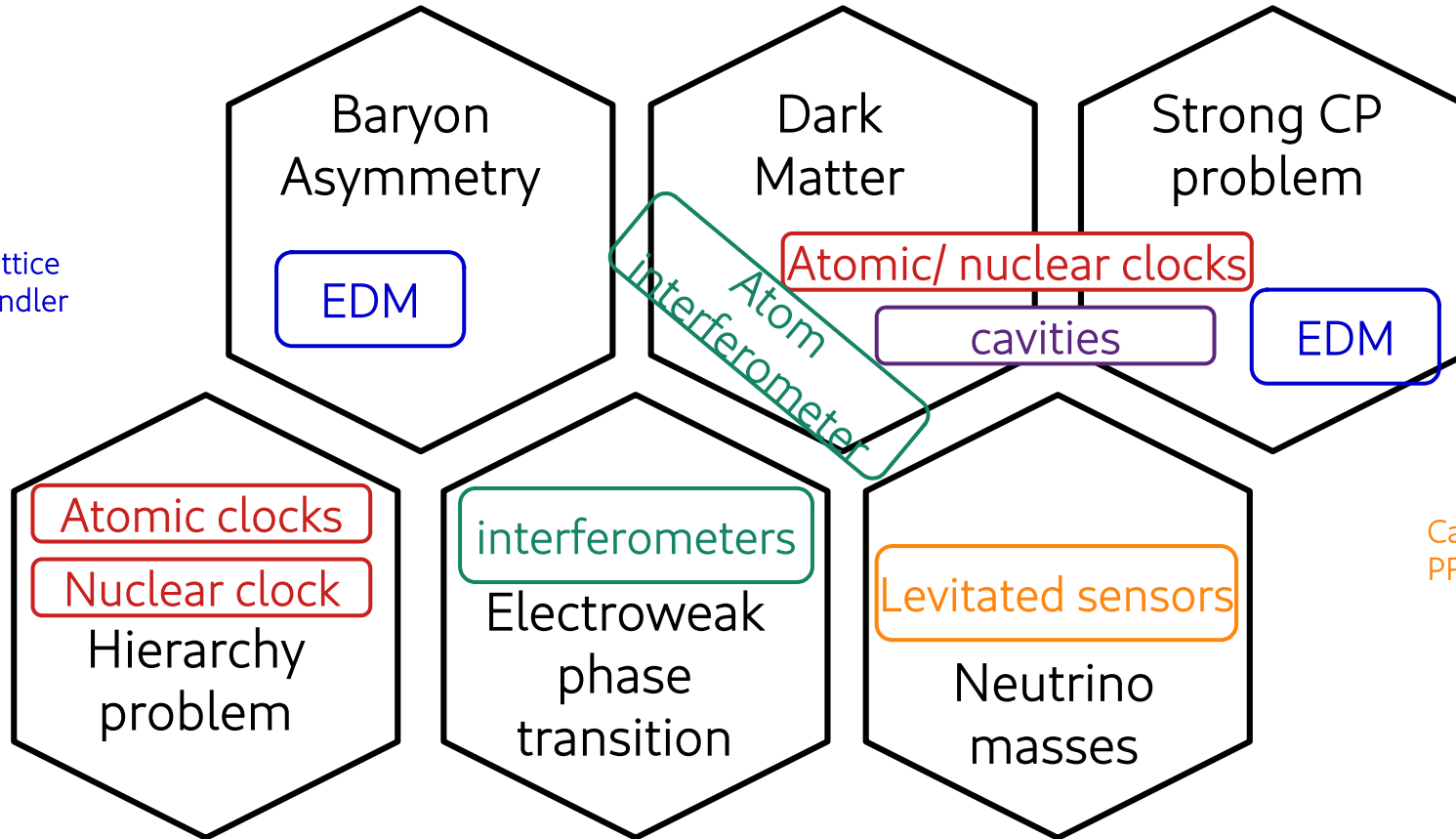
# Quantum sensing



# Particle questions

# Quantum sensing

→ yesterday's lattice coffee by A. Shindler



Engelhardt,  
Boonah, Liu  
2304.05863

Carney, Leach, Moore  
PRX Quantum '23



# Summary: Light NP vibrant



Well-motivated scenarios with light, feeble NP require novel searches



Quantum sensors can enable measurement & enhance the sensitivity



Isotope shifts of atomic clocks probe light new bosons



High-frequency GWs: proposal to look for sidebands and enable frequency shift

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Exciting developments across frontiers over past few years and expected in the very near future

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*CERN is an exciting place for QT4HEP with unique opportunities for breakthroughs*



*Exciting developments across frontiers over past few years and expected in the very near future*

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Thank  
you!



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---

# APPENDIX

# NP shifts of atomic spectra

Energy shift due to new long-range interaction

$$V_{\text{NP}} = \frac{y_e y_n}{4\pi r} e^{-m_\phi r}$$



$$m\nu_2 = F_{21}m\nu_1 + K_{21} - y_e y_n AA' (X_2 - X_1 F_{21})$$

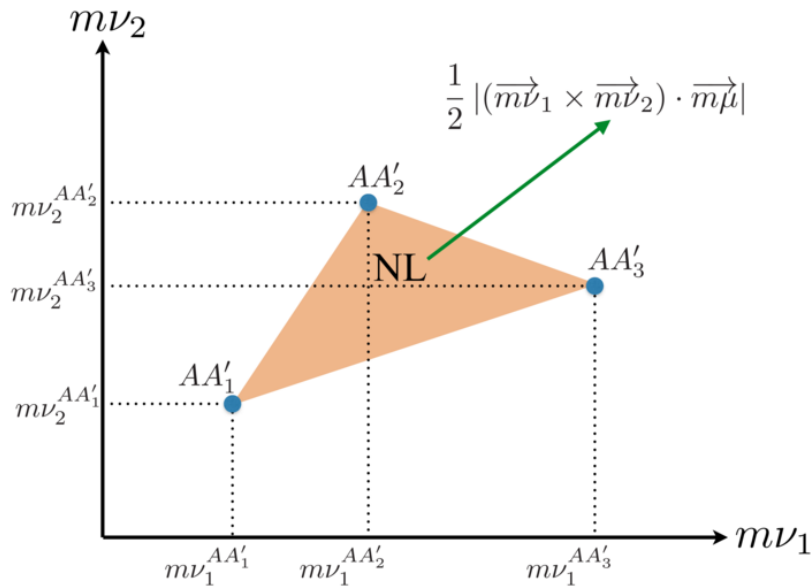
NP  $\phi$  coupling to electrons and neutrons

theory input: NP electronic coefficients  
 overlap of wavefunctions with NP potential  
 $X_i = X_i(m_\phi)$

Goal: bound on  $y_e y_n$  and  $m_\phi$  in data-driven approach

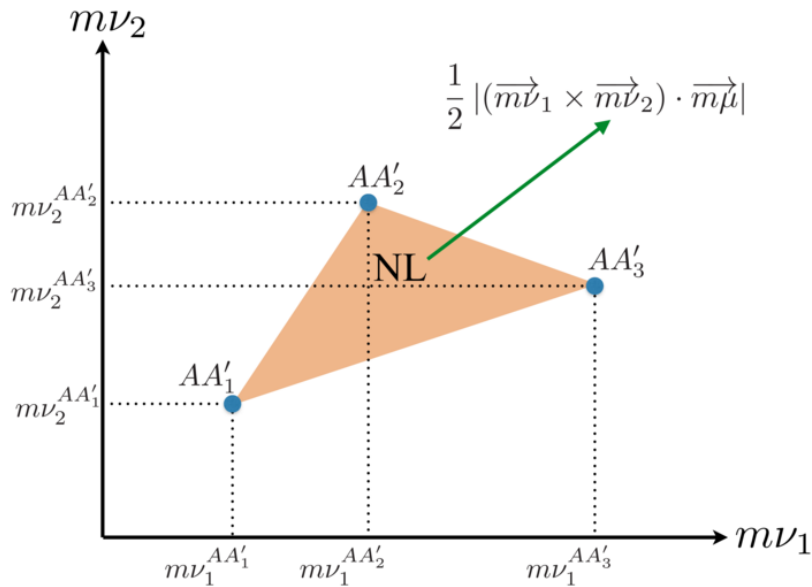
# Nonlinearity as data-driven NP measure

- Deviations from straight line  $\rightarrow$  triangle
- Area = measure of NL

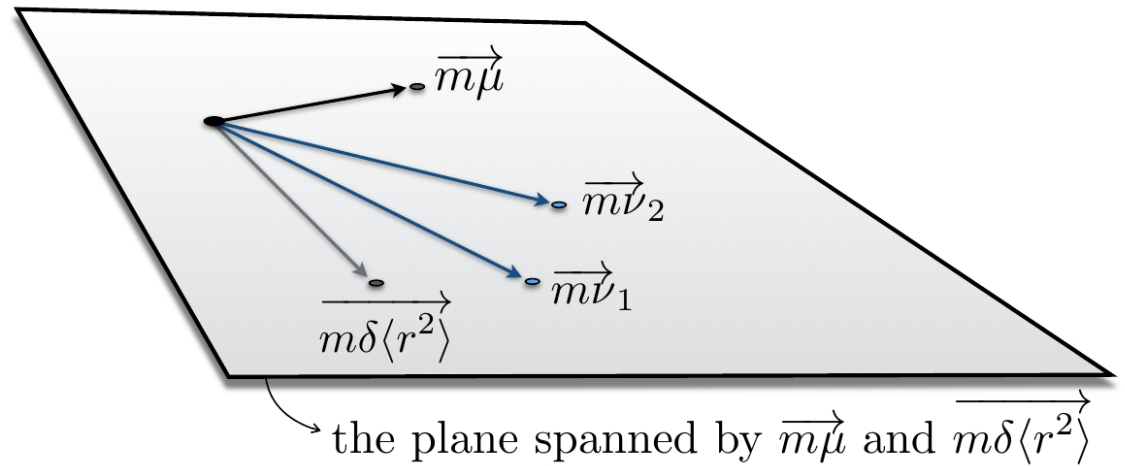


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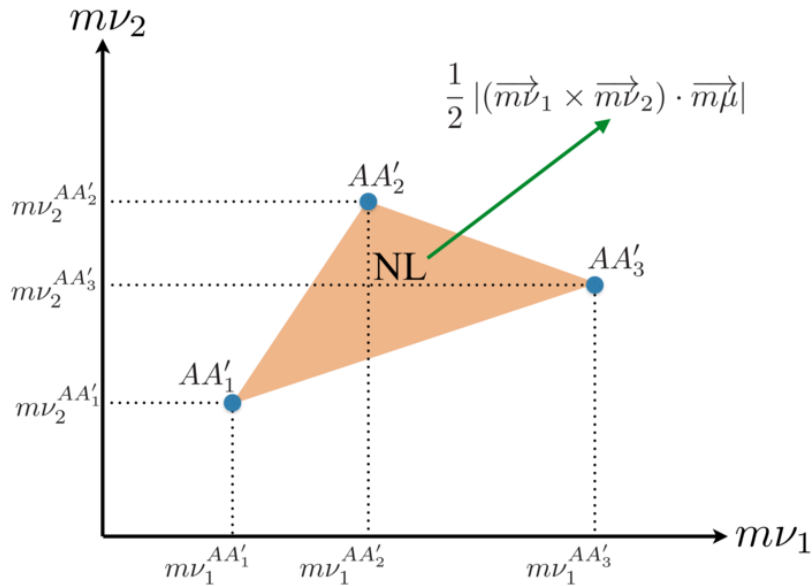
- Linearity plane: linear combinations of FS+MS
- Volume of parallelepiped = measure of NL



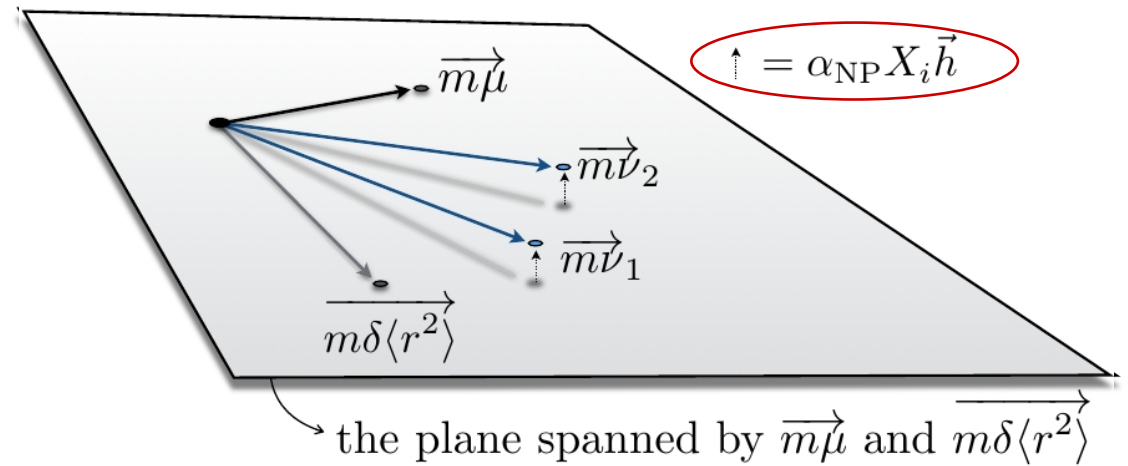


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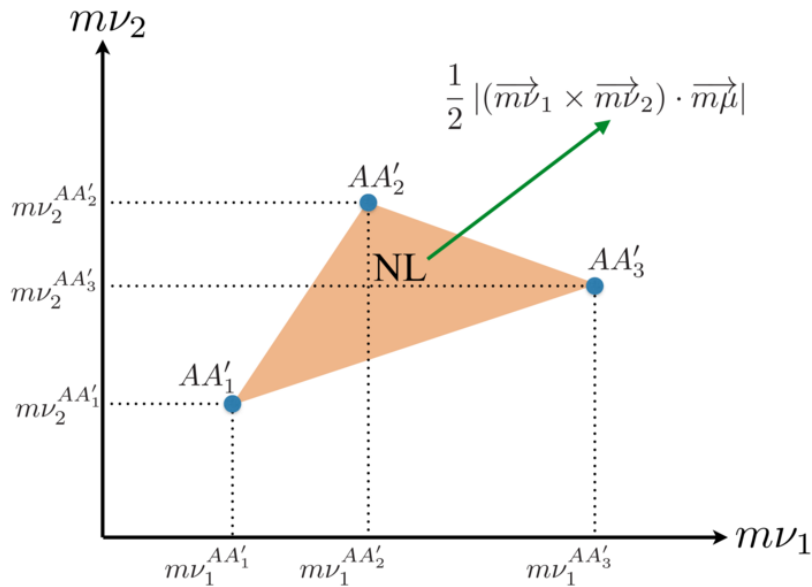


- Linearity plane: linear combinations of FS+MS
- Volume of parallelepiped = measure of NL

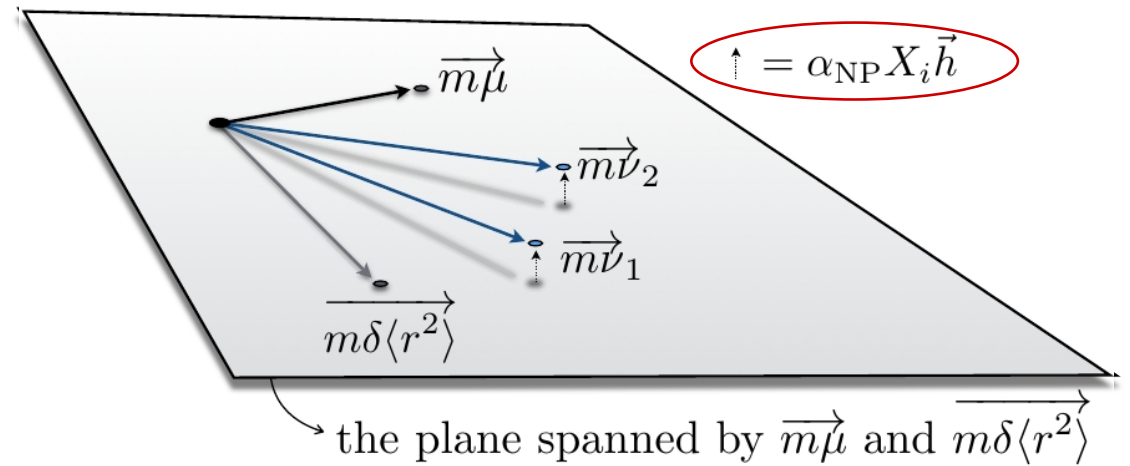


# Nonlinearity as data-driven NP measure

- Deviations from straight line  $\rightarrow$  triangle
- Area = measure of NL



- Linearity plane: linear combinations of FS+MS
- Volume of parallelepiped = measure of NL



quantify NL

if within uncertainty

bound NP

# NP King linearity violation (KLV)

- ▶ NP isotope dependence:  $\vec{h} \simeq -A\vec{A}'$  amu (for linear  $\phi - N$  coupling)

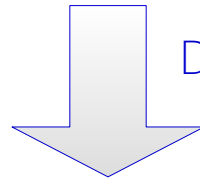
new term in King relation

[Berengut, Budker, Delaunay, Flambaum, Frugiuele, EF, Grojean, Harnik, Ozeri, Perez, Soreq, PRL 2018]

# NP King linearity violation (KLV)

- ▶ NP isotope dependence:  $\vec{h} \simeq -A\vec{A}' \text{ amu}$  (for linear  $\phi - N$  coupling)

new term in King relation



Developed isotope vector space

**NP can break linearity: non-linearity measure  $NL_{NP}$**

$$NL_{NP} = [\overrightarrow{m\mu} \times (X_2 - F_{21}X_1) \overrightarrow{m\nu}_1] \cdot \vec{h}$$

$NL_{NP} = 0$  if

(i)  $X_i \propto F_i$  (heavy  $m_\phi$ )

(ii)  $\vec{h} \parallel \overrightarrow{m\mu}$  or  $\overrightarrow{m\delta\langle r^2 \rangle}$   
MS FS

[Berengut, Budker, Delaunay, Flambaum, Frugiuele, EF, Grojean, Harnik, Ozeri, Perez, Soreq, PRL 2018]

# Constraint on mass and couplings

[Berengut, Budker, Delaunay, Flambaum, Frugiuuele, EF, Grojean, Harnik, Ozeri, Perez, Soreq] PRL 120 (2018) 091801

Data-driven  
bound:

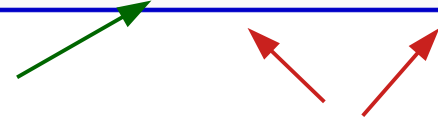
data



$$y_e y_n = \frac{(\vec{m}\vec{\nu}_1 \times \vec{m}\vec{\nu}_2) \cdot \vec{m}\vec{\mu}}{(\vec{m}\vec{\mu} \times \vec{h}) \cdot (X_1 \vec{m}\vec{\nu}_2 - X_2 \vec{m}\vec{\nu}_1)}$$

Mild NP  
assumption:  $\phi$   
couples linearly to  
nucleus

Theory input



# Constraint on mass and couplings

[Berengut, Budker, Delaunay, Flambaum, Frugiuuele, EF, Grojean, Harnik, Ozeri, Perez, Soreq] PRL 120 (2018) 091801

Data-driven  
bound:

data



$$y_e y_n = \frac{(\vec{m}\nu_1 \times \vec{m}\nu_2) \cdot \vec{m}\dot{\mu}}{(\vec{m}\dot{\mu} \times \vec{h}) \cdot (X_1 \vec{m}\nu_2 - X_2 \vec{m}\nu_1)}$$

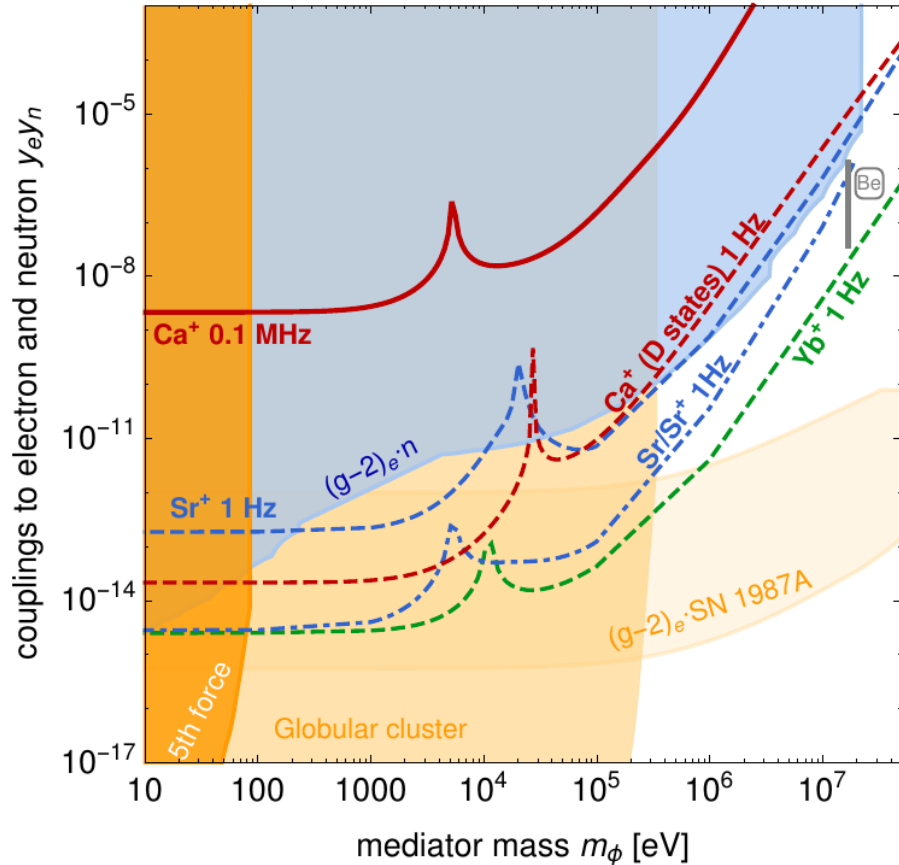
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+ uncertainty propagation of frequencies and masses

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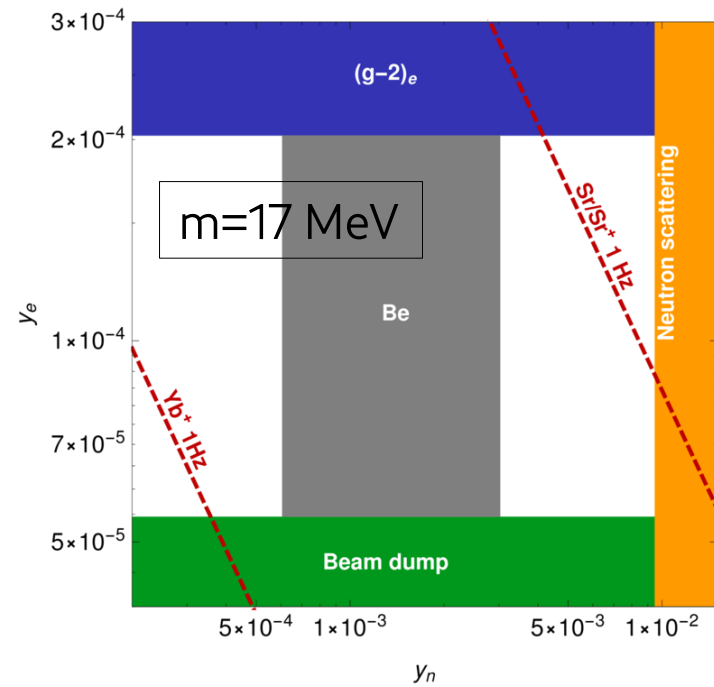
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Theory input

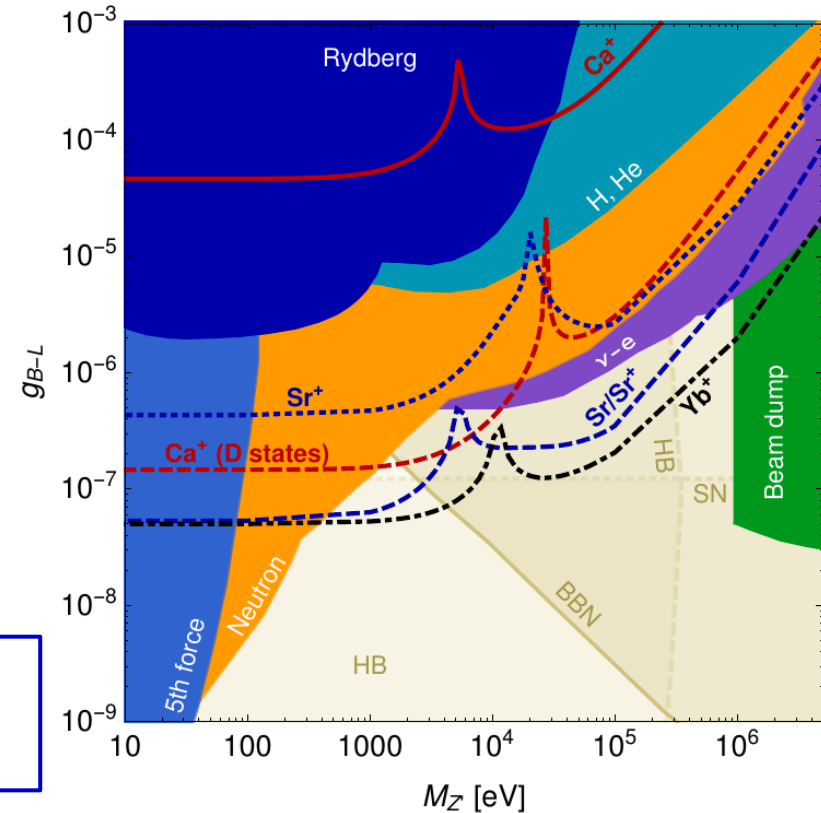
+ uncertainty propagation of frequencies and masses

# Implications for NP models

[Frugiuete, EF,  
Perez, Schlaffer '17]



$U(1)_{B-L}$   
New  $Z'$  boson





# Caveat: Linearity breaking in SM

- SM nonlinearity

- Mixing of degenerate energy levels

[Griffith, Isaak, New, Rall '81]

- NLO field shift

[Palmer, Stacey '81]

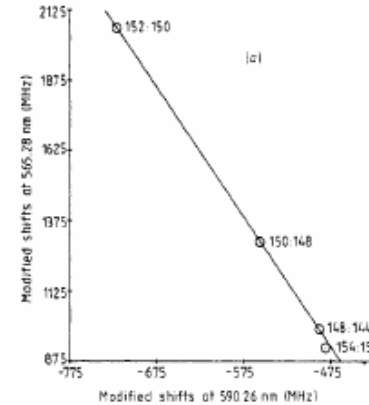
- Nuclear polarization

[Seltzer '69]

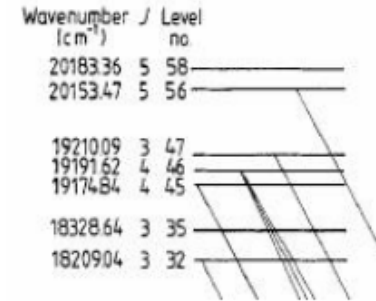
[Blundell, Baird, Palmer,  
Stacey, Woodgate '87]

- Nuclear deformation

[Flambaum, Samsonov,  
Tan, Viatkina '21]



Samarium (Sm)



- Standard Model contribution to King nonlinearity calculated: for some transitions [Flambaum, Geddes, Viatkina '18] in Ca<sup>+</sup>, Sr<sup>+</sup>, Ba<sup>+</sup>, Yb<sup>+</sup>, Hg<sup>+</sup>

- SM nonlinearities: dependence on nuclear radii [Müller, Yerokhin, Artemyev, Surzhykov '21]

- Few-electron ions [Debierre, Oreshkina, Valuev, Harman, Keitel '22]

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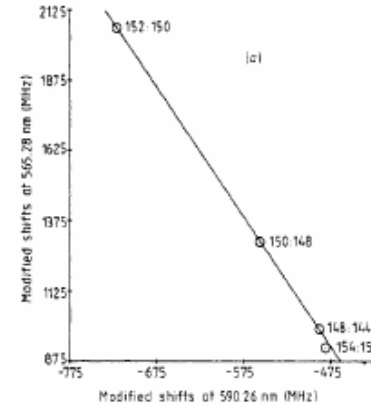
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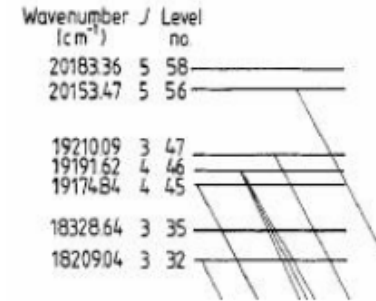
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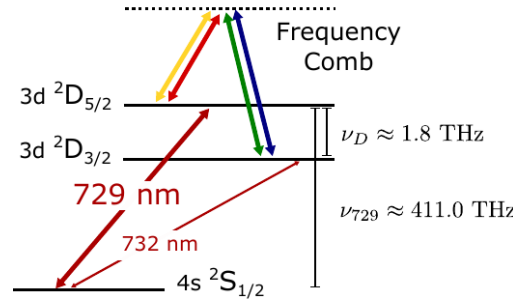
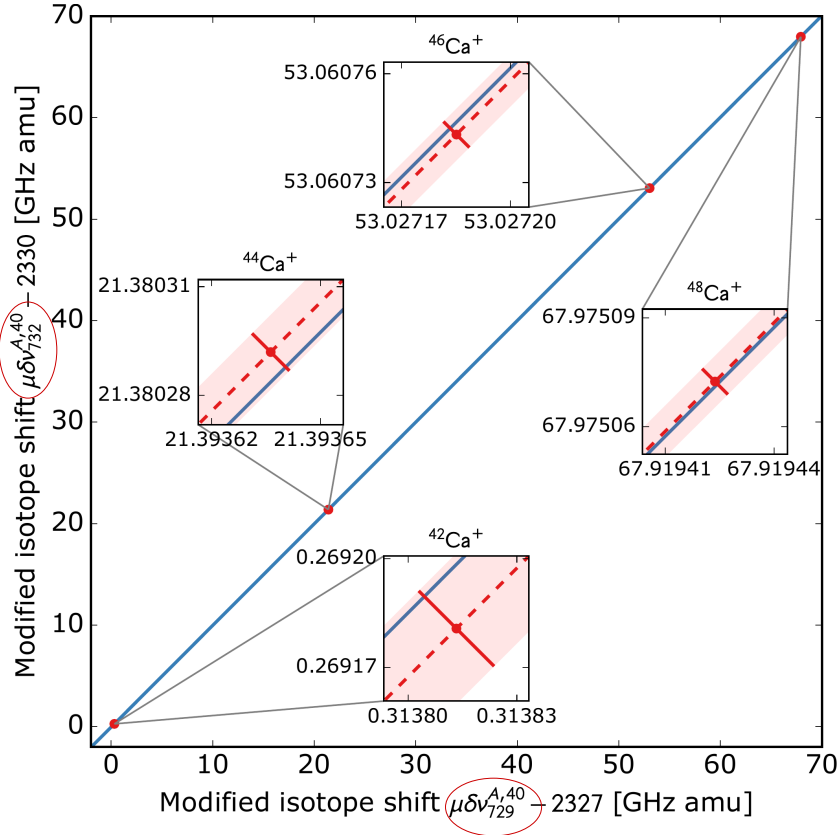


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**Strategy:** consider predicted SM NL and constrain residual NL

# Very precise Ca<sup>+</sup> King Plot

[Solaro, Meyer, Fisher, Berengut, EF, Drewsen, PRL 125, 123003 (2020)]



[Solaro, Meyer, Fisher, DePalatis, Drewsen, PRL.120.253601]

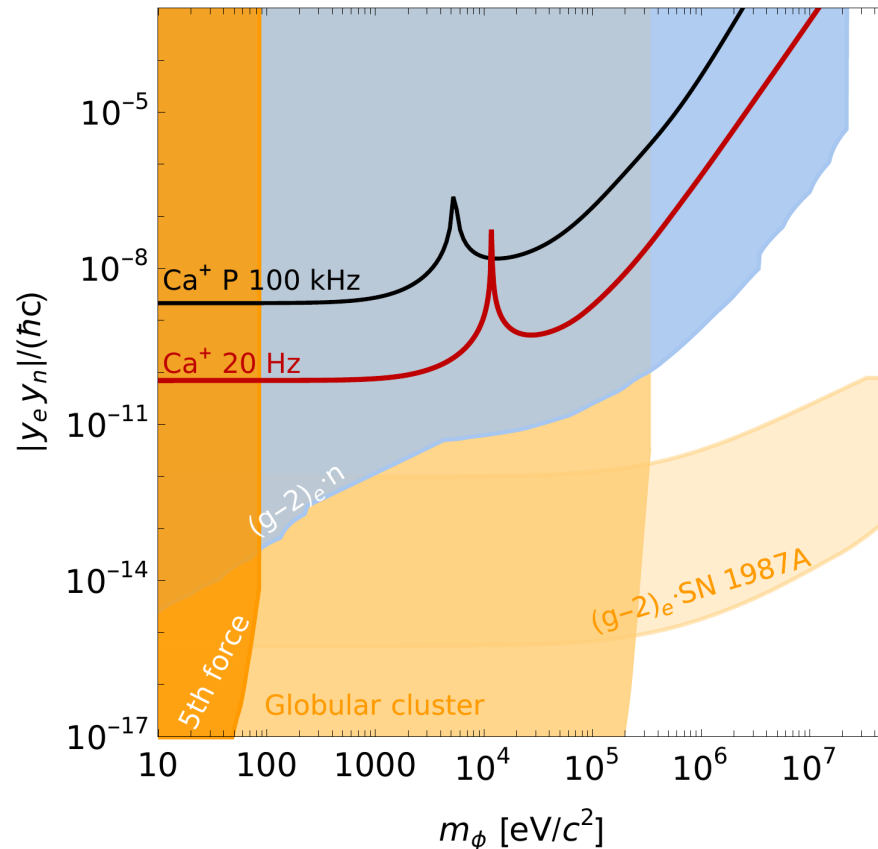
Aarhus:  $D_{3/2} - D_{5/2}$  at 20 Hz

Ca 40, 42, 44, 46, 48

King plot linear at  $\sim 1\sigma$ ,  $\chi^2=0.9$

# New $\text{Ca}^+$ Isotope Shift Bounds on $\Phi$

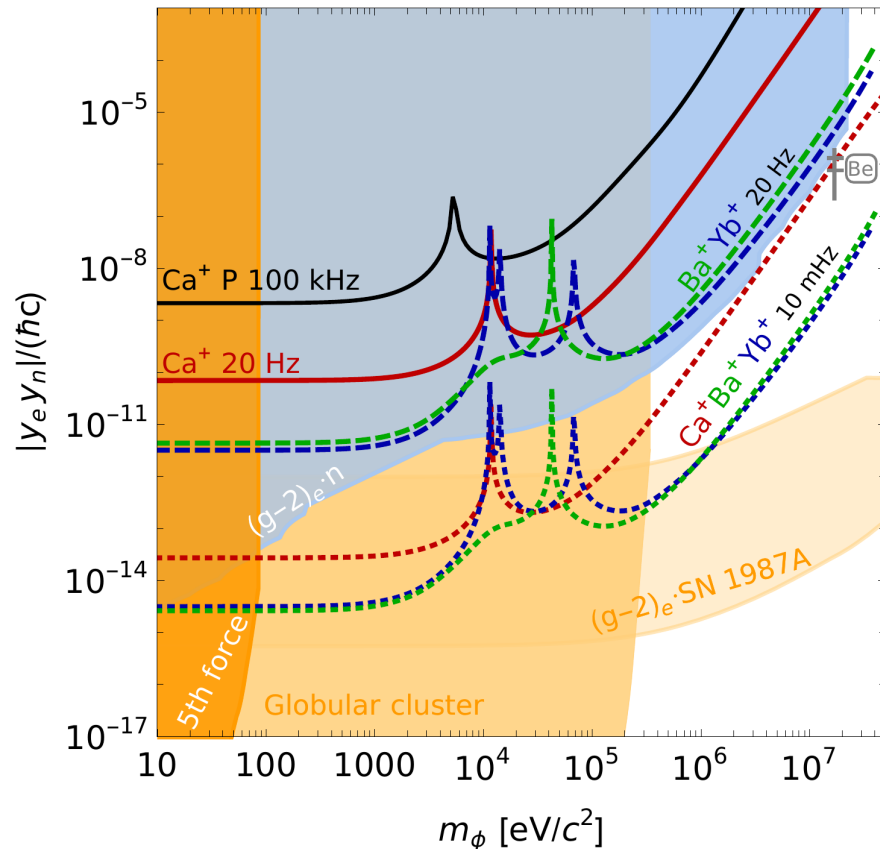
[Solaro, Meyer, Fisher, Berengut, EF, Drewsen, PRL 125, 123003 (2020)]



- **New 4D** projection method for 4 isotope pairs
- **Improvement** of former Ca bound by factor 30
- Limited by D-fine precision
- Same transitions in Ba, Yb with 20 Hz comparable to  $(g-2)_e \cdot n$ -scatt
- Anticipated precision: **10 mHz**
  - Ca, Ba, Yb can probe untested parameter space

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# Scrutinizing the Yb anomaly

Figueroa, Berengut, Dzuba, Flambaum, Budker, Antypas, PRL 2022

New Yb/Yb<sup>+</sup> King plot: reduced nonlinearity could be explained by **nuclear deformation**

Hur, Craik, Counts, Berengut, Vuletic et al, '22

S → F octupole transition of Yb<sup>+</sup> combined with previous Yb<sup>+</sup> and Yb IS:

- 4.3 sigma for **2<sup>nd</sup> source**
- future: 4 orders improvement of exp. uncertainty to sub-Hz level as in simultaneously trapped Sr<sup>+</sup>

Flambaum, Samsonov, Tan, Viatkina '21

**Nuclear polarization** effects in atoms and ions

Fürst, Zeh, Dreissen, Kulosa, Kalincev, Lange, Benkler, Huntemann, Peik, Mehlstäubler PRL 2020

- **Improved measurement** of 411nm (E2) and 467nm (E3) transitions in <sup>172</sup>Yb<sup>+</sup> at few Hz
- further with isotope shifts of S-D, S-F at sub-10-Hz precision → update coming soon

# Highly charged ion (HCI) King plot

[Rehbehn, Rosner, Bekker, Berengut, Schmidt, King, Micke, Gu, Müller, Suryzhkov, Crespo Lopez-Urrutia '21]

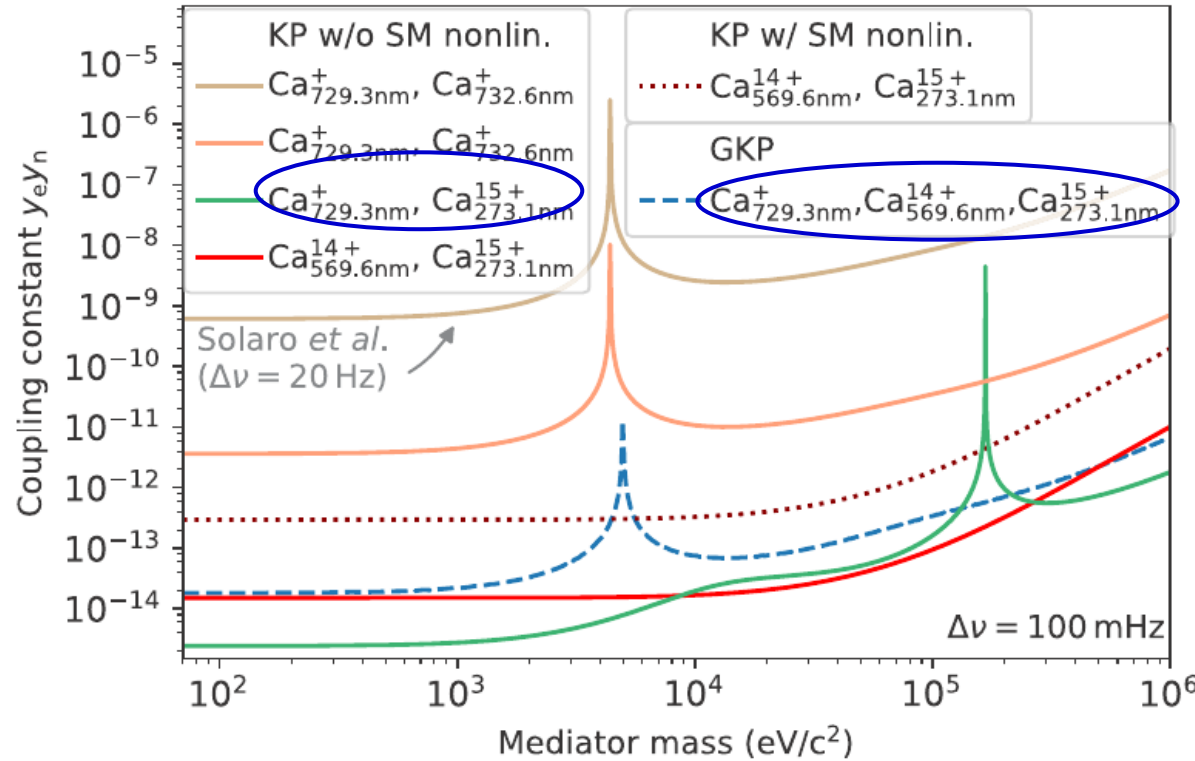
[King, Spieß, Micke, Wilzewski, Leopold, Benkler, Lange, Huntemann, Suryzhkov, Zerokhin, Crespo, Schmidt; Nature 611 (2022)]

- HCIs: less electrons
- Generalized King plot
- Projected bounds assuming no isotope mass uncertainties

Very promising combination of singly and highly charged Ca ions

- find optimal combination
- ongoing: replacement of isotope masses AND higher-order mass shift

[Berengut, EF, Mariotti, Richter, Surzhykov, Viatkina; work in progress]



See also Hydrogen-like ions [Debierre, Keitel, Harman '22]

# Direct comparison of theory and data

## Few-electron systems

- Data *and* theory very precise
- Need only  $\geq 1$  transition,  $\geq 1$  isotope
  - Isotope shifts: need p-radius
  - Direct frequency: combine with (g-2), Rydberg or 2<sup>nd</sup> transition

cf [Karshenboim '01, '10]

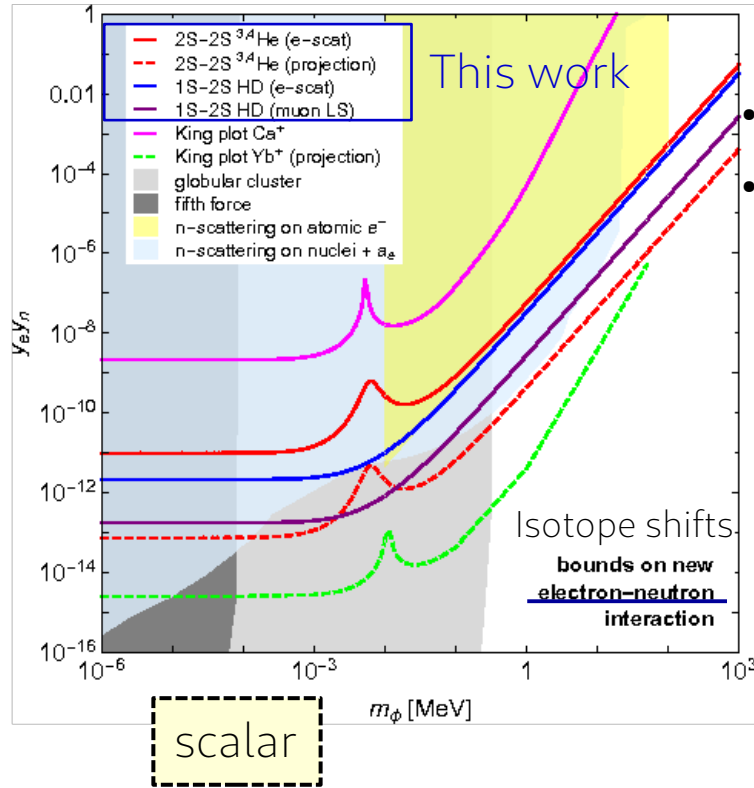
[Jaeckel, Roy '10]

[Pachucki, Patkos, Yerokhin '17]



# Direct comparison of theory and data

[Delaunay, Frugiuiele, EF, Soreq '17]

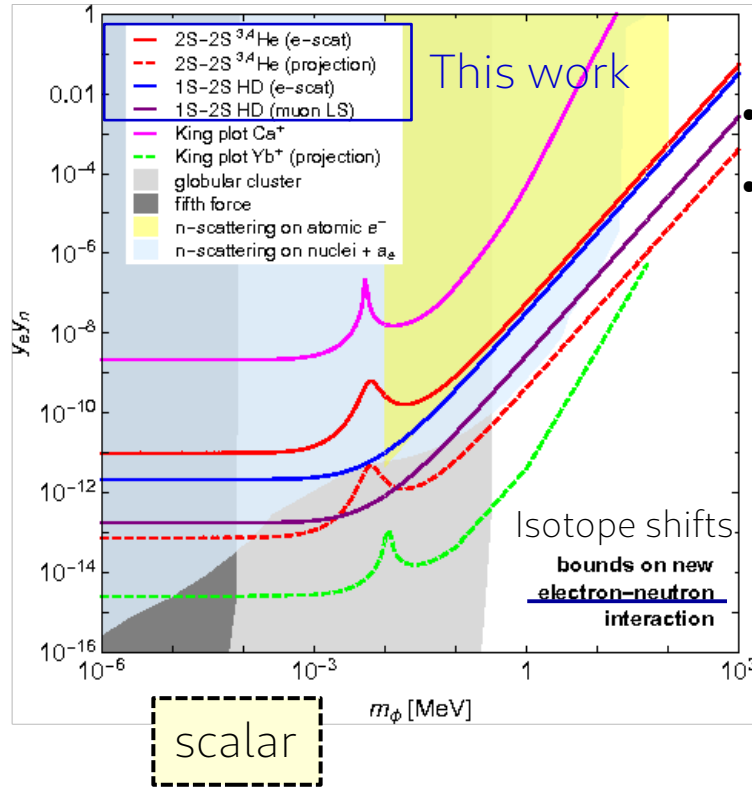


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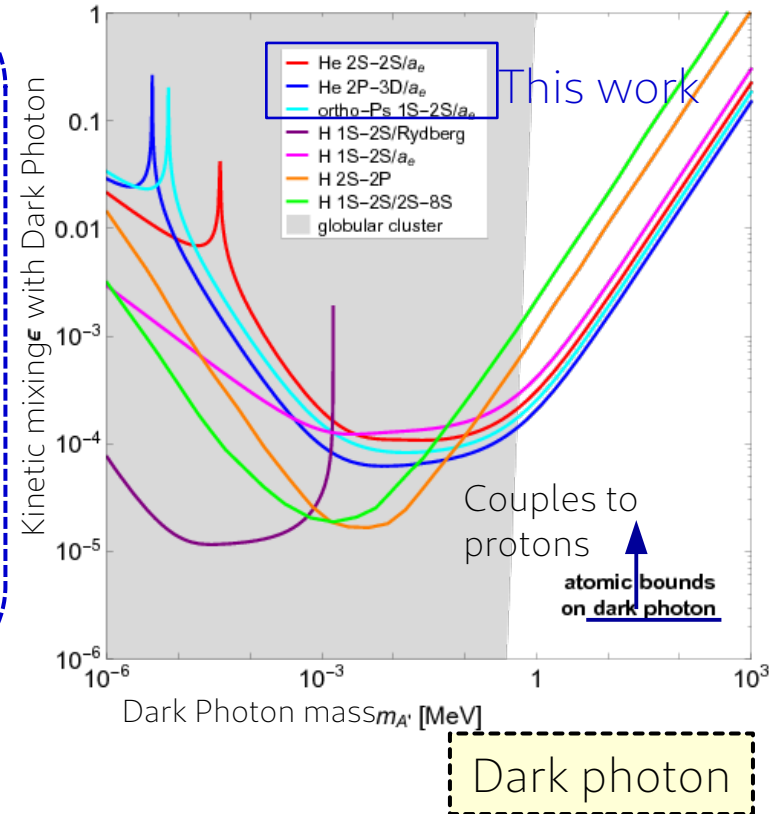
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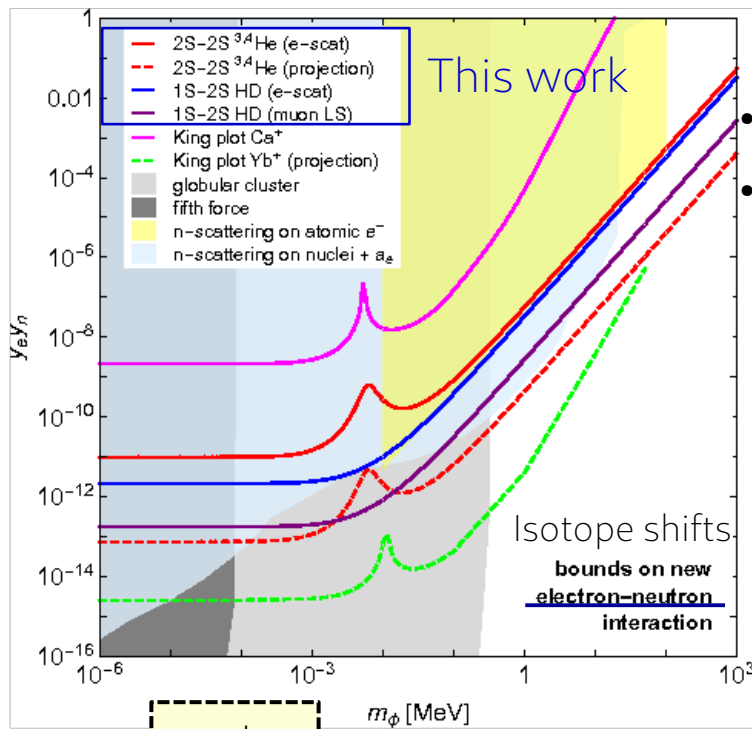
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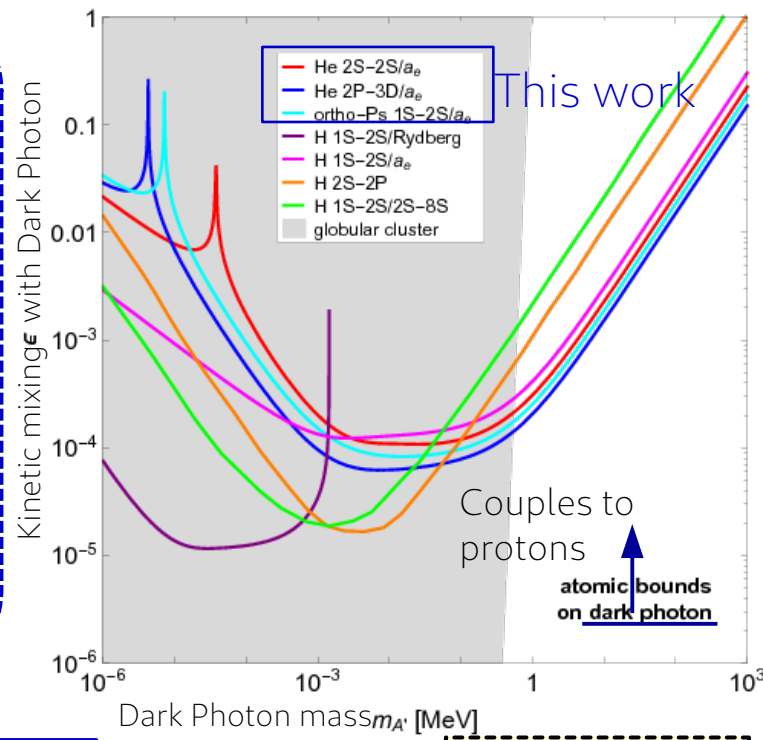


scalar

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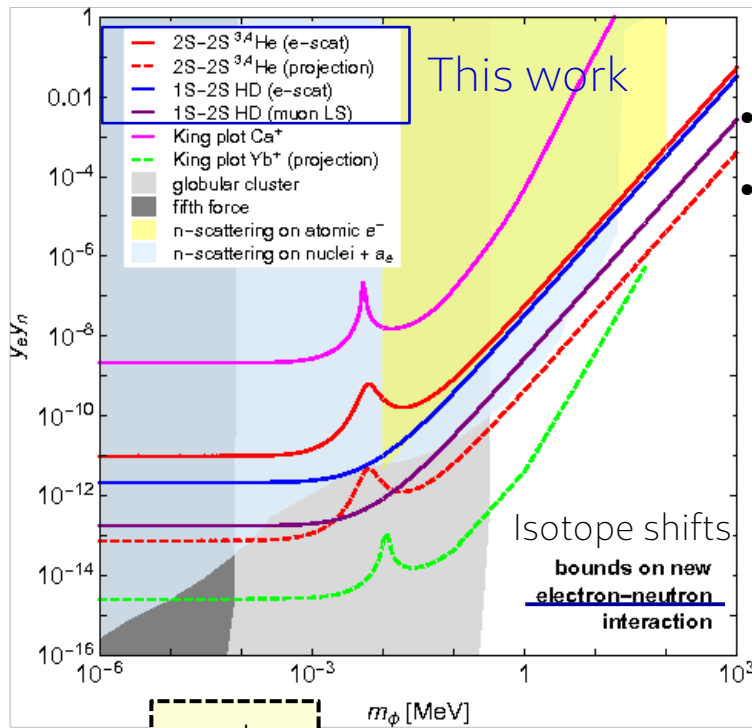
Precise frequencies and isotope shifts  
 → complementary to King plot



Dark photon

# Direct comparison of theory and data

[Delaunay, Frugiuiele, EF, Soreq '17]

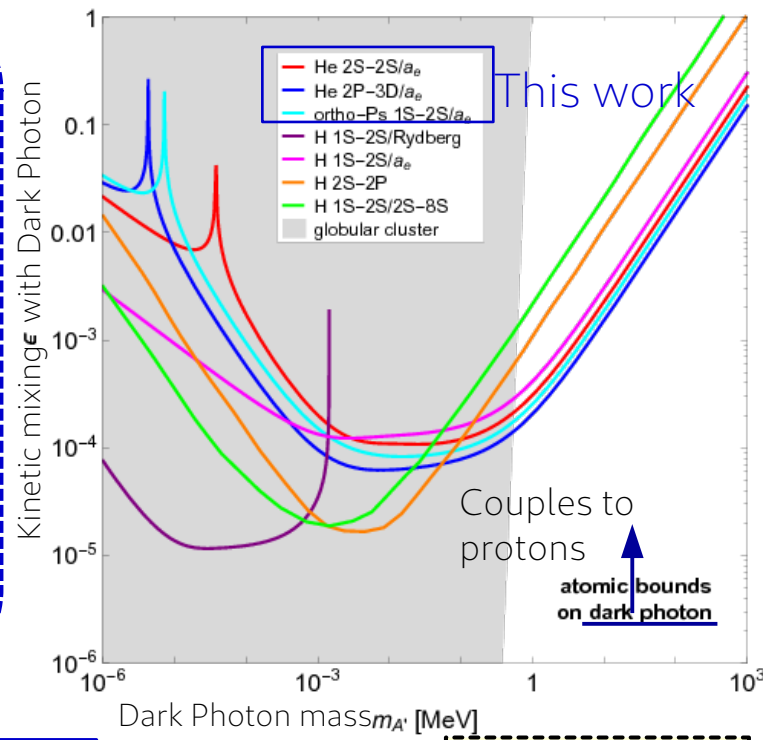


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Dark photon

# New Ca<sup>+</sup> Isotope Shift Measurements

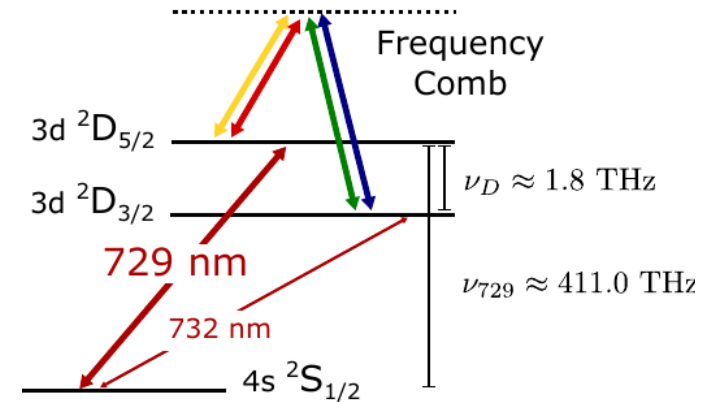
[Solaro, Meyer, Fisher, Berengut, EF, Drewsen, PRL 125, 123003 (2020)]

- Very precise measurement of **D-fine splitting** of Ca<sup>+</sup> at Aarhus (Denmark)

$D_{3/2} - D_{5/2}$  at 20 Hz → precision  $\sim 10^{-6}$

- S- $D_{5/2}$  at 2 kHz → precision  $\sim 10^{-7}$

[Knollmann, Patel, Doret, PRA 2019]  $\sim 10^{-9}$



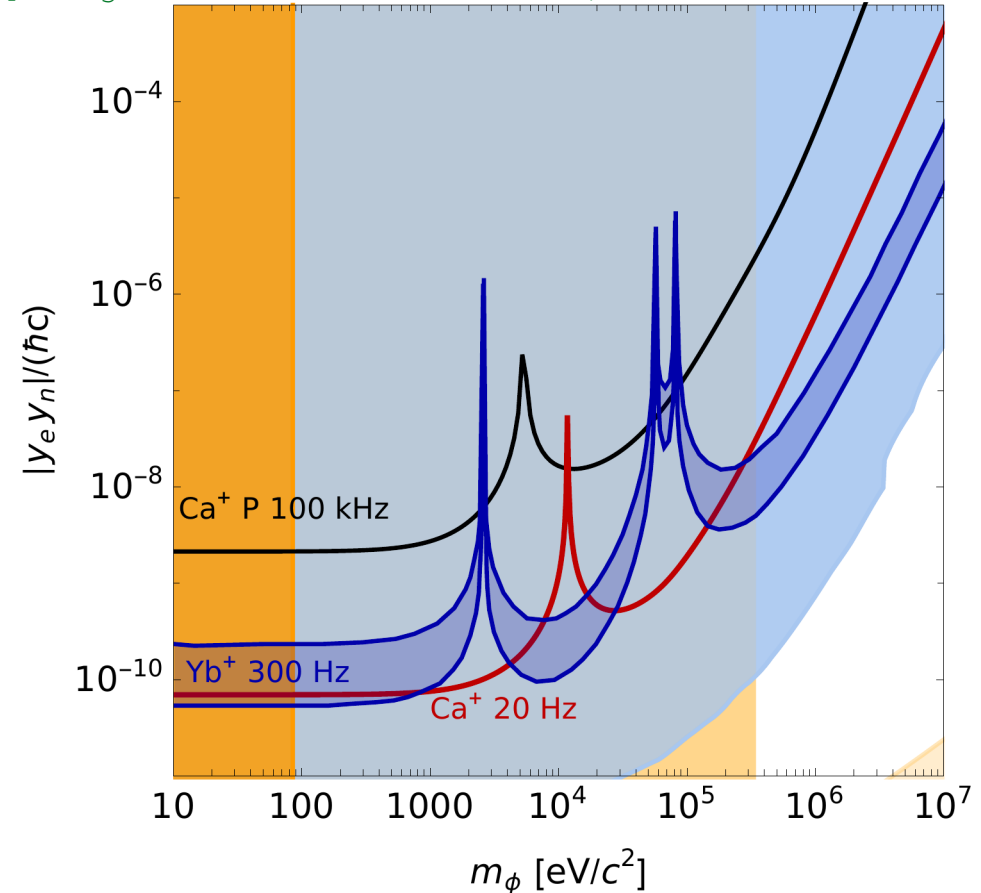
[Solaro, Meyer, Fisher, DePalatis, Drewsen (Aarhus University), PhysRevLett.120.253601]

5 isotopes measured: Ca 40, 42, 44, 46, 48  
→ 4 pairs, i.e. 1 more than required

# Ca vs Yb King plots - compatibility

- Reach same sensitivity
  - Yb 10x more susceptible to NP
  - Ca 10x more precisely measured
- non/linearity no contradiction
  - different nuclear physics

[Yb digitalized from Counts et al '20; Ca from Solaro et al '20]



# Ca vs Yb King plots - compatibility

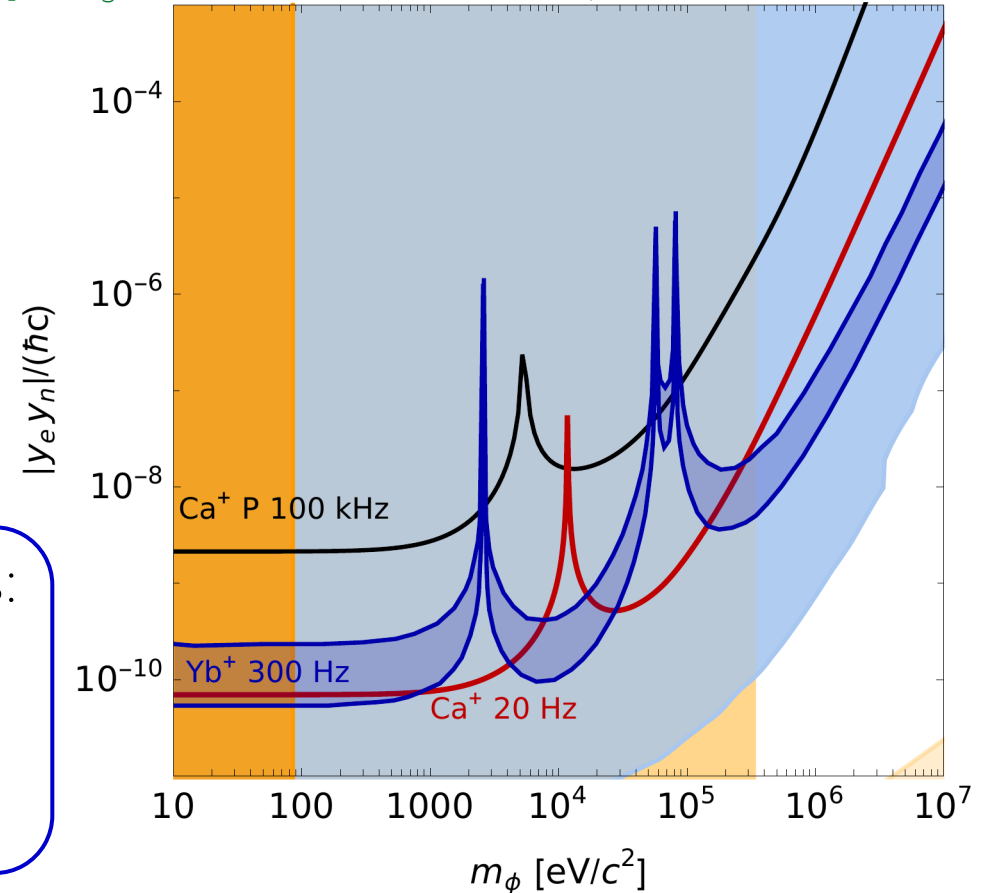
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*if Yb-NL assumed as purely New Physics:*

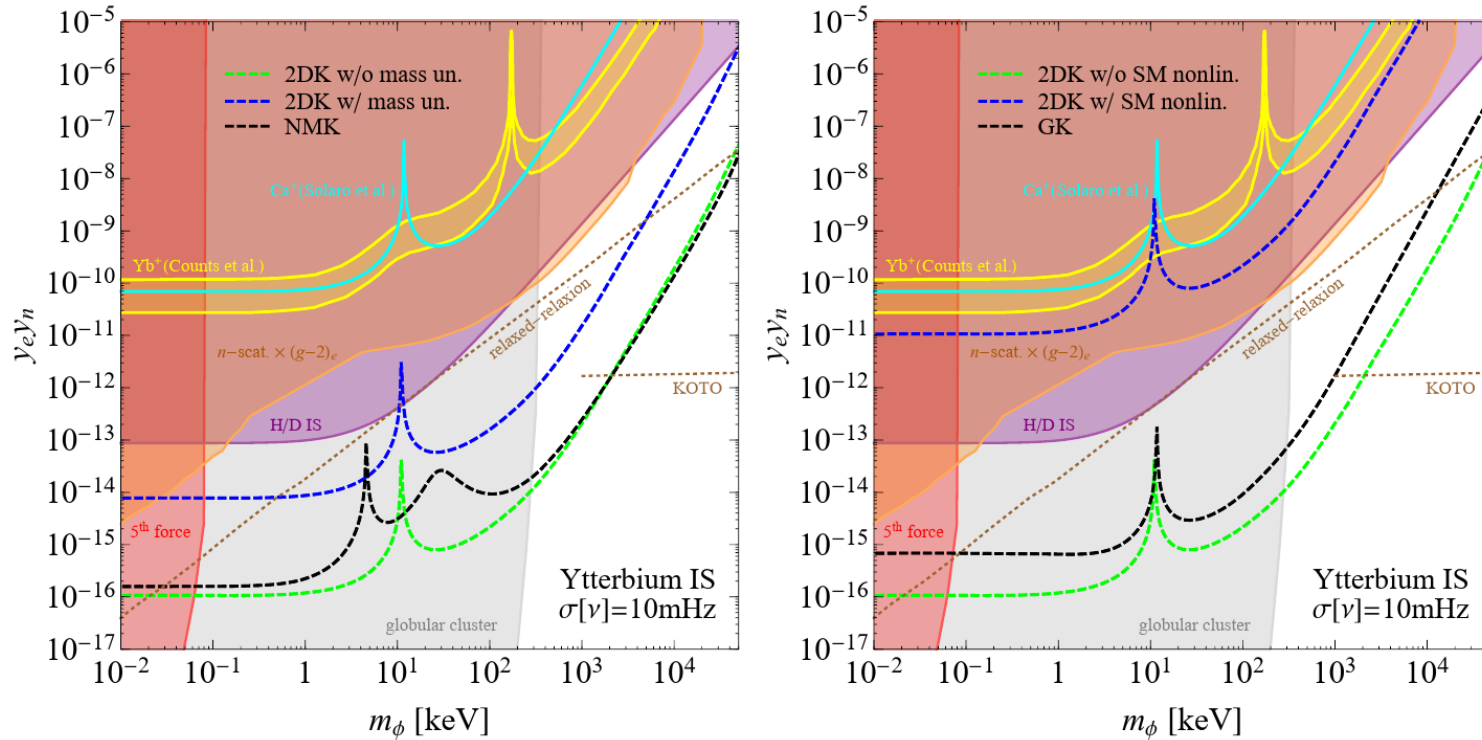
→ necessary coupling range is

- partly excluded by Ca
- excluded by  $(g-2)_e$  \* n-scattering

[Yb digitalized from Counts et al '20; Ca from Solaro et al '20]



# Generalised King Plot





# NP electronic overlap

Electronic NP coefficient: overlap of wavefunctions of initial and final states (a, b) with the NP (Yukawa) potential

Perturbative approximation:

$$X_i = \int d^3r \frac{e^{-m_\phi r}}{4\pi r} [|\Psi_b(r)|^2 - |\Psi_a(r)|^2]$$

Contact-Interaction + Multibody Perturbation Theory (CI+MBPT)

$$X_i = \frac{1}{A - Z} \left. \frac{d\epsilon_{ab}}{d\alpha_{\text{NP}}} \right|_{\alpha_{\text{NP}}=0}$$

Difference of energy levels as a function of  $\alpha_{\text{NP}}$

# Chameleon search with King plot



Dark Energy

Matter density

[Khoury, Weltman '04, '04]  
[Brax, Burrage '10, '11]  
[Frugiuuele, EF, Perez, Schlaffer '17]

$$V_{\text{eff}} = V(\phi) + \frac{\phi\rho}{M}$$

Energy scale/coupling

Chameleon mass is density dependent:  
→ Heavy in dense environment  
→ screening in test masses  
→ mediating a long-range interaction

$$\delta H|_n = -\frac{m_e m_N}{4\pi r M^2}$$

Change in Hamiltonian  
→ change in energy level of e

Match to  $V_{\text{NP}}$

$$M > \sqrt{\frac{m_e m_n}{y_e y_n|_{\text{min}}}} \approx 500 \text{ TeV} \approx 2.5 \cdot 10^{-13} M_{\text{Pl}}$$

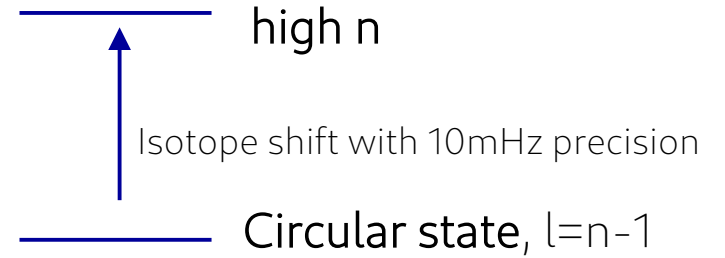
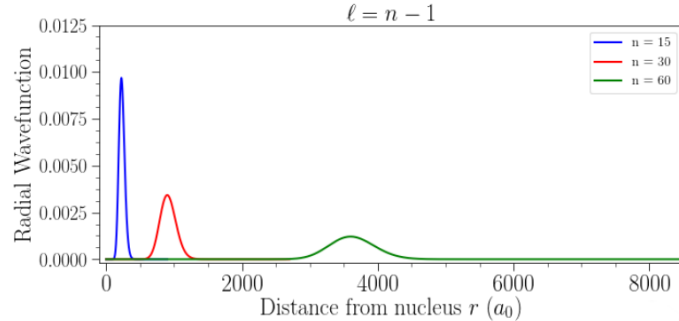
Sensitivity projection with future Yb<sup>+</sup> King plot with 1Hz precision

# Rydberg states: reduce nucl. uncertainty

[Duque-Mesa, Firstenberg, EF, Geller, Ozeri, Perez, Shpilman; work in progress]

## Highly excited states

- less overlap with nucleus
- but also with NP

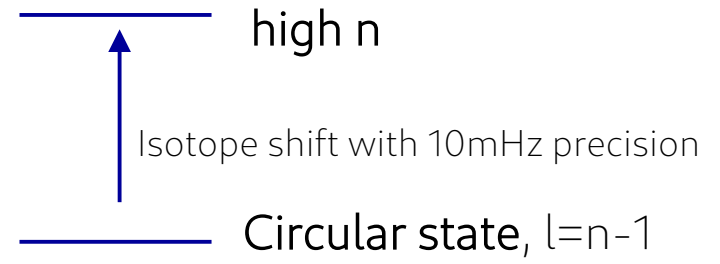
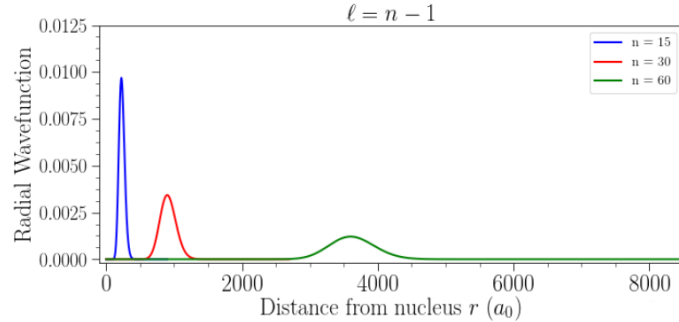


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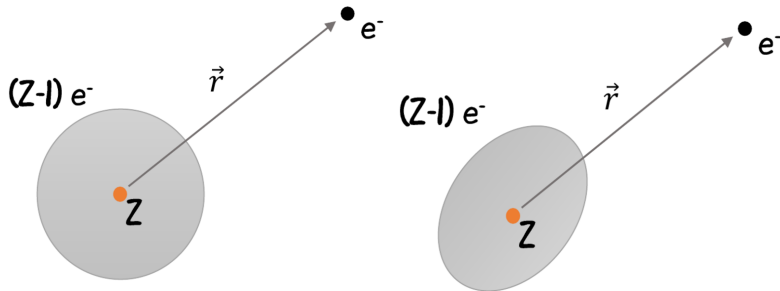
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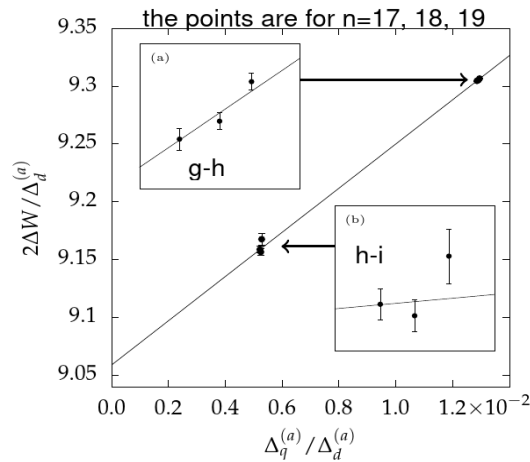
- less overlap with nucleus
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## Bottleneck: Core polarizability



[image: MSc thesis, S. Duque-Mesa]



Rb data in polarizability plot:  
[Berl, Sackett, Gallagher, Nunkaew '20]

Trick: Measure many transitions

# Rydberg states: reduce nucl. uncertainty

[Duque-Mesa, Firstenberg, EF, Geller, Ozeri, Perez, Shpilman; work in progress]

Expect points in plane

$$\frac{f_{AB}}{\delta_Y} = - \left( \alpha_A^d m_e \mu_{AB}^{-1} + \frac{1}{2} \Delta \alpha_{AB}^d \right) \frac{\delta_{r^{-4}}}{\delta_Y} - \left( 3\alpha_A^q m_e \mu_{AB}^{-1} + \frac{1}{2} \Delta \alpha_{AB}^q \right) \frac{\delta_{r^{-6}}}{\delta_Y} + 2\pi R_\infty m_e \mu_{AB}^{-1} \frac{\delta_{r^{-1}}}{\delta_Y} + \alpha_{NP}$$

dipole
quadrupole

$\vec{x}$ 
 $\vec{y}$

$$\delta_{r^q} = \langle r^q \rangle_{n_2 l_2} - \langle r^q \rangle_{n_1 l_1}$$

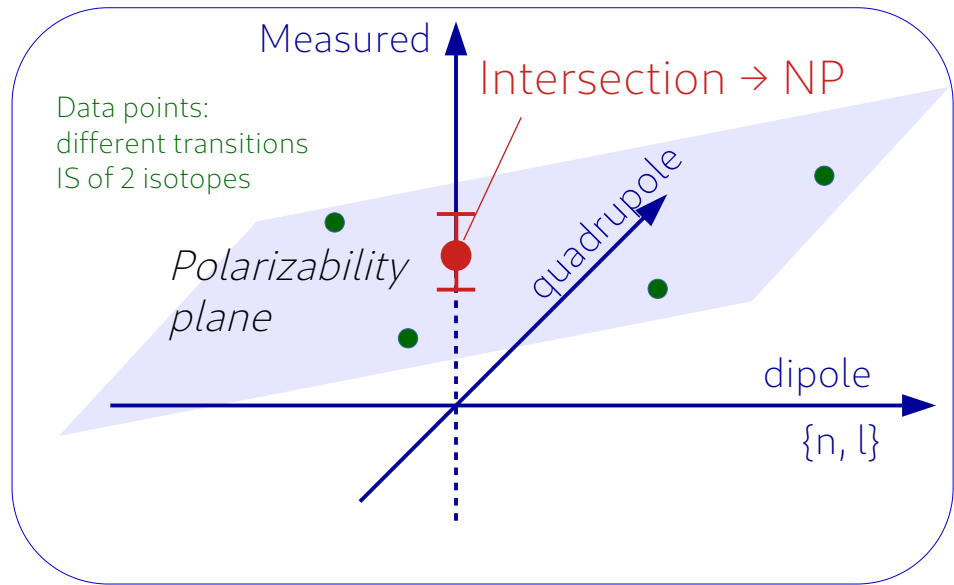
$$\delta_Y = \left\langle \frac{e^{-m_\phi r}}{r} \right\rangle_{n_2 l_2} - \left\langle \frac{e^{-m_\phi r}}{r} \right\rangle_{n_1 l_1}$$

..

Vector:  
Many n, l

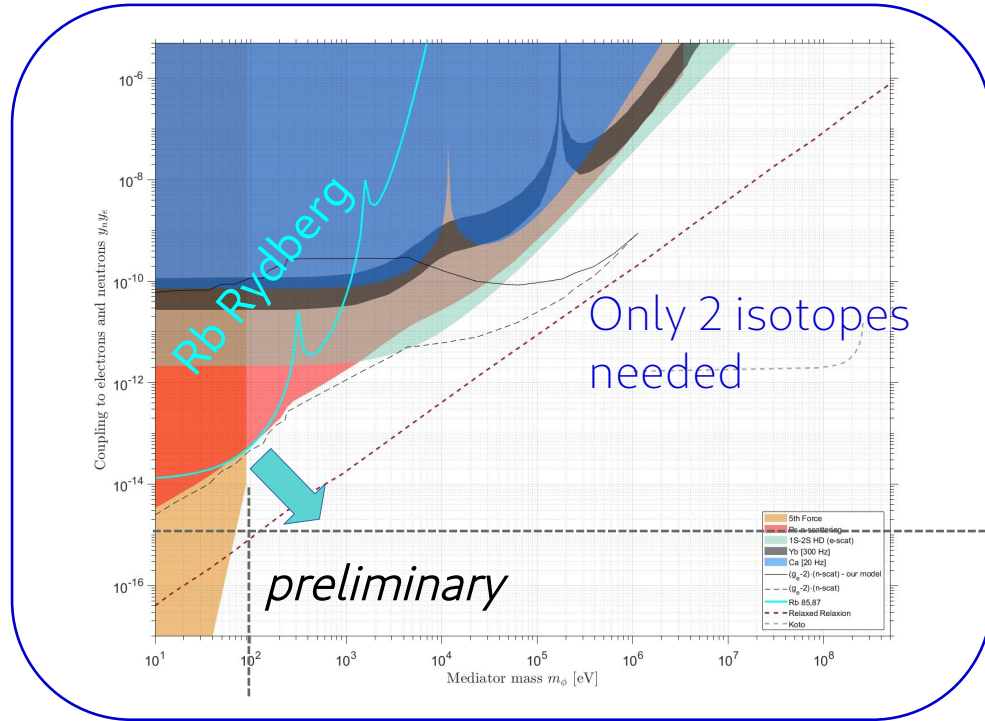
$$\vec{z} = C + A\vec{x} + B\vec{y}$$

$$C = \frac{(\vec{x} \times \vec{y}) \cdot \vec{z}}{(\vec{x} \times \vec{y}) \cdot \vec{1}} \rightarrow \alpha_{NP}$$

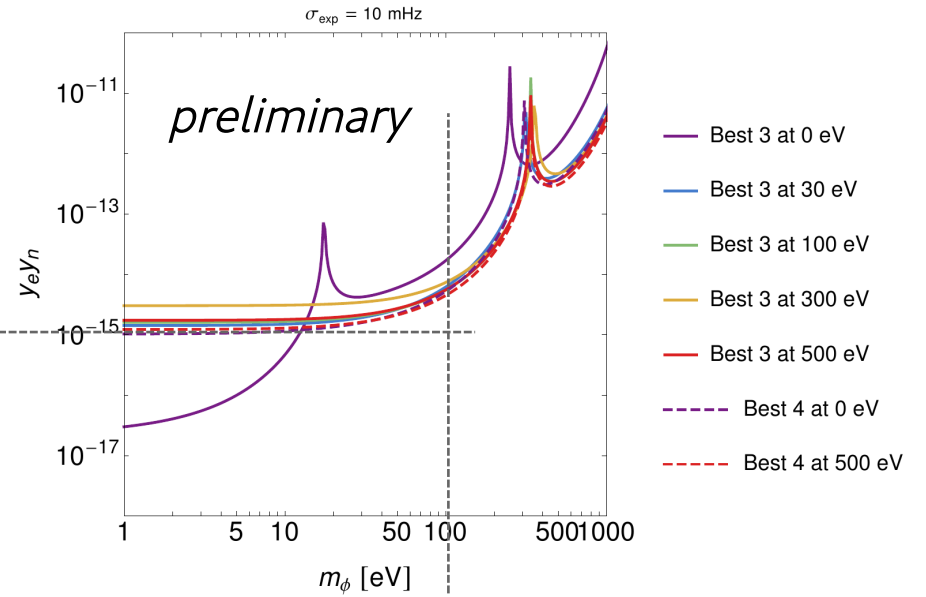


# Rydberg states: reduce nucl. uncertainty

[Duque-Mesa, Firstenberg, EF, Geller, Ozeri, Perez, Shpilman; work in progress]



Choose best transitions for a mass range  
4 or 3 transitions? only small improvement



See also Rydberg hydrogen [Jones, Potvliege, Spannowsky '19]

Possibly test new parameter space

# Further NP atomic precision probes

---

- Rydberg states
- Few-electron systems (H, He, D, Li,...)
- Tests of Local Lorentz invariance violation

# Atomic clock key figures

Characterize the performance of a clock by its relative frequency change

*Goals:* stable and accurate clock

$$f(t)/f_0 = 1 + \epsilon + y(t)$$

Accuracy

Stability

- Systematic uncertainty in clock frequency.
- Two types of shifts
  1. **Field shifts** e.g. Zeeman shift and black body shift
  2. **Motional shifts** e.g. Relativistic Doppler

- Average fractional frequency variations
- Typically characterized by the *Allan deviation*:

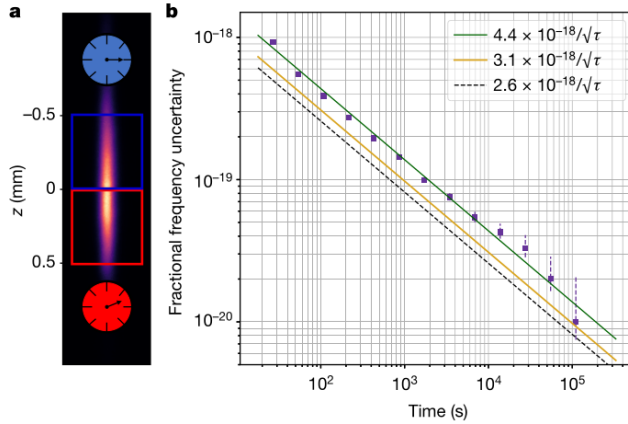
$$\frac{\Delta f}{f} = \frac{\langle \vec{v} \cdot \hat{k} \rangle}{c} - \frac{\langle v^2 \rangle}{2c^2} - \frac{\langle \vec{v} \cdot \hat{k} \rangle^2}{2c^2} + \dots$$

$$\sigma_y(\tau) \cong \frac{1}{Q} \frac{1}{SNR} \sqrt{\frac{T_C}{\tau}}$$

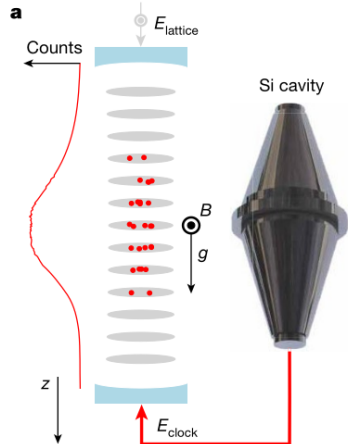
See D. Hume's [talk](#) at [ECFA](#) workshop '21



# Sr lattice clock



- 1-dimensional Sr optical lattice clock: measured linear frequency gradient inside a single atomic sample to a relative uncertainty of phenomenal  $7.6 \times 10^{-21}$
- 100,000 ultracold Sr atoms in an optical lattice
- narrow  $S_0 \rightarrow P_0$  transition
- magic trap depth  $\rightarrow$  suppress collisional shifts
- fundamental to achieve this precision: the record coherence time of 37s
- frequency comparison within one sample: 2 uncorrelated subregions separated by a mm
- Test gravitational time dilation at mm scale.



CERN TH, 14/06/2023

Elina Fuchs (CERN | LUHannover | PTB)



# Noise

- Quantum projection noise:

- Discrete measurement outcomes 0,1 with probabilities  $p$ ,  $(1-p)$

- Experiment repeated  $N$  times  $\rightarrow$

- Variance of binomial distribution

$$p = \frac{N_1}{N}$$
$$\sigma_{p,\text{quantum}}^2 = \frac{1}{N} p(1-p).$$

- Decoherence

- Decoherence & relaxation  $\rightarrow$  random transitions

- $\rightarrow$  reduced probability  $\delta p_{\text{obs}}(t) = \delta p(t)e^{-\chi(t)},$

$$\chi(t) = (\Gamma t)^a,$$

- Decoherence time/ decay rate  $\Gamma = T_{\chi}^{-1} \rightarrow$  max. sensing time