

# Taming Mass Gap with Anti-de Sitter Space

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CERN, 4 June 2024

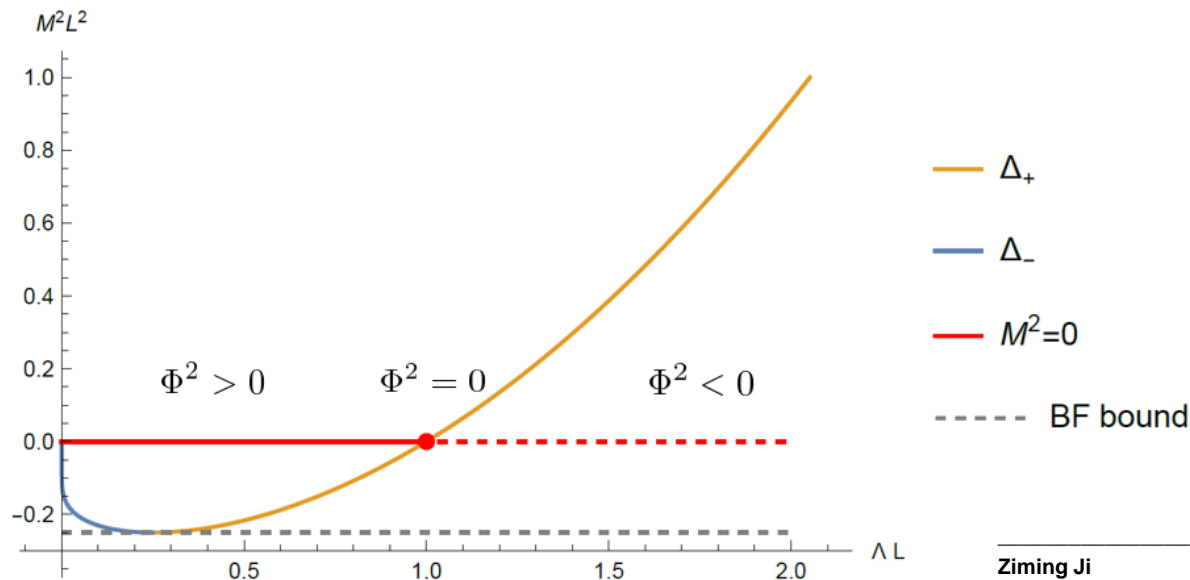
# The Focus:

## Boundary Diagnostic of the Mass Gap

- Asymptotic free theories with dynamically generated mass gaps in the IR in flat space.
- In AdS, by choosing different boundary conditions, we realize gapped and gapless phases.
- As we vary the AdS radius  $L$ , the theory interpolates between weak coupling and strong coupling.
- Consistency with flat space limit demands gapless phases to disappear at large enough  $L$ .
- Can we see this gapless-gapped transition from the boundary? How?

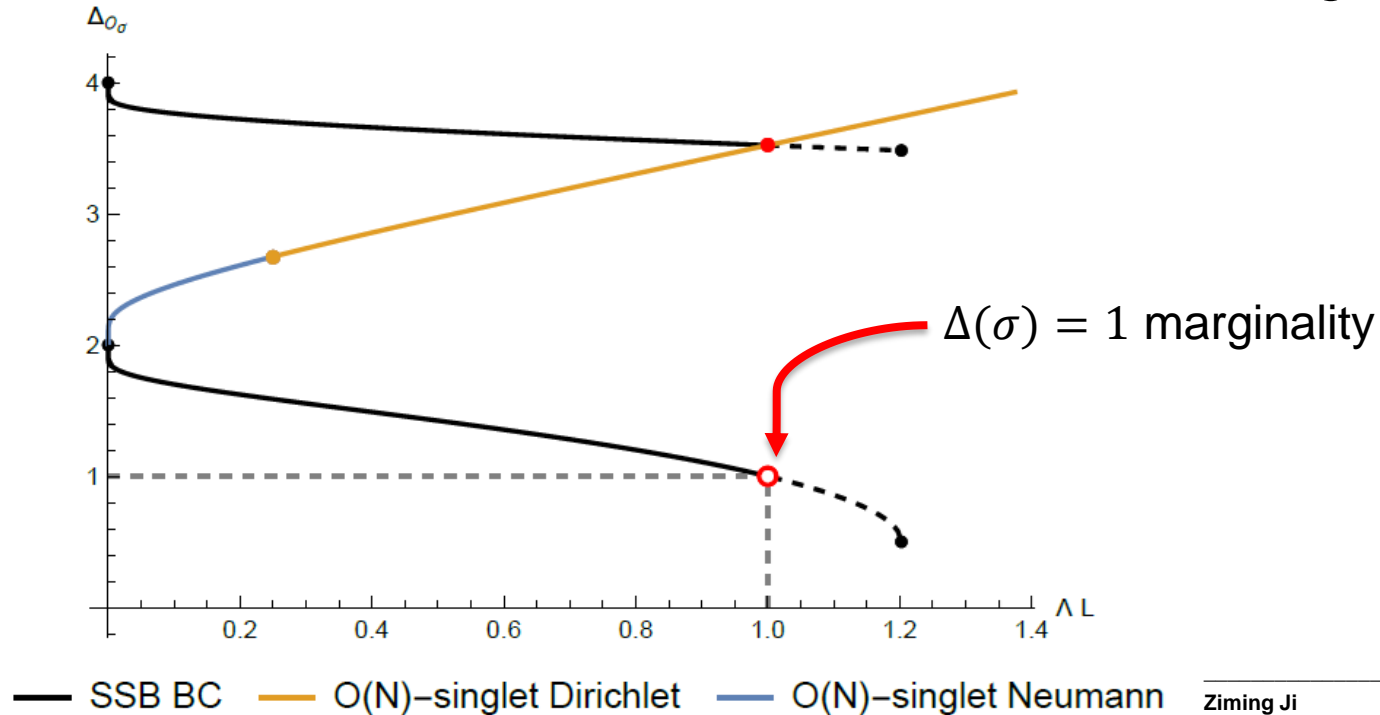
# $O(N)$ NLSM at large $N$

- In flat space,  $O(N)$  symmetric gap  $M \sim \Lambda$ . No SSB in 2d.
- In AdS, analog of SSB can happen due to IR regularity.
- At large  $N$ , bulk phases at all values of  $\Lambda L$  can be found by solving the gap equations.



# $O(N)$ NLSM at large $N$

- What is the boundary signal?
- Look at the lightest operator in the boundary spectrum of the Hubbard–Stratonovich field  $\sigma$  which is a singlet.

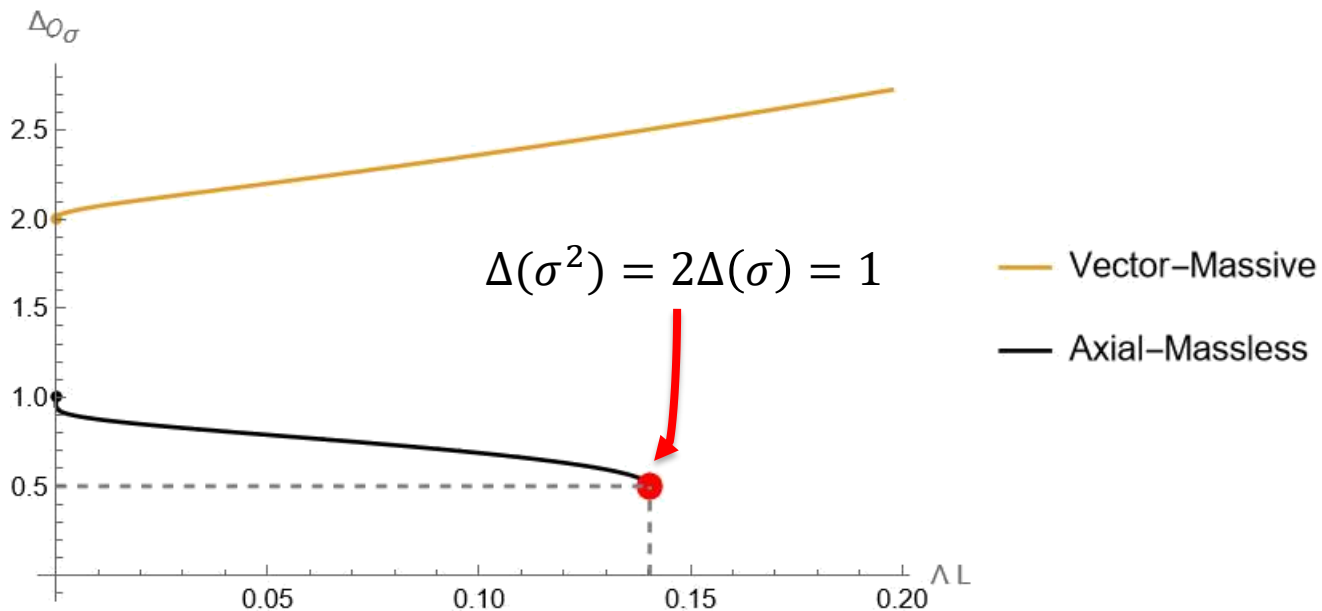


# Gross-Neveu at large $N$

- In flat space, vector symmetric gap  $M \sim \Lambda$ . The discrete axial symmetry is spontaneously broken.
- In AdS, we define massive vector boundary conditions and massless axial preserving boundary conditions.
- At large  $N$ , bulk phases at all values of  $\Lambda L$  can be found by solving the gap equations.
- No signal of gapless-gapped transition from the bulk gap equations.
- However, the gapless axial preserving boundary condition should disappear at large enough  $\Lambda L$ .

# Gross-Neveu at large $N$

- Try to look at the boundary data!
- Look at the lightest operator in the boundary spectrum of the Hubbard–Stratonovich field  $\sigma$ .  $\sigma^2$  is axial singlet.



# The conjecture:

## Boundary Singlet Marginal Gaps!

- Yang-Mills in four-dimensional Anti-de Sitter Space.
- Dirichlet boundary condition with boundary global symmetry and boundary conserved currents dual to gluons should disappear before the flat space limit.
- We conjecture that some singlet operator on the boundary will become marginal at some  $\Lambda L$  and destabilize this Dirichlet boundary condition, mediating a quantum phase transition to confinement.

**Thank you!**