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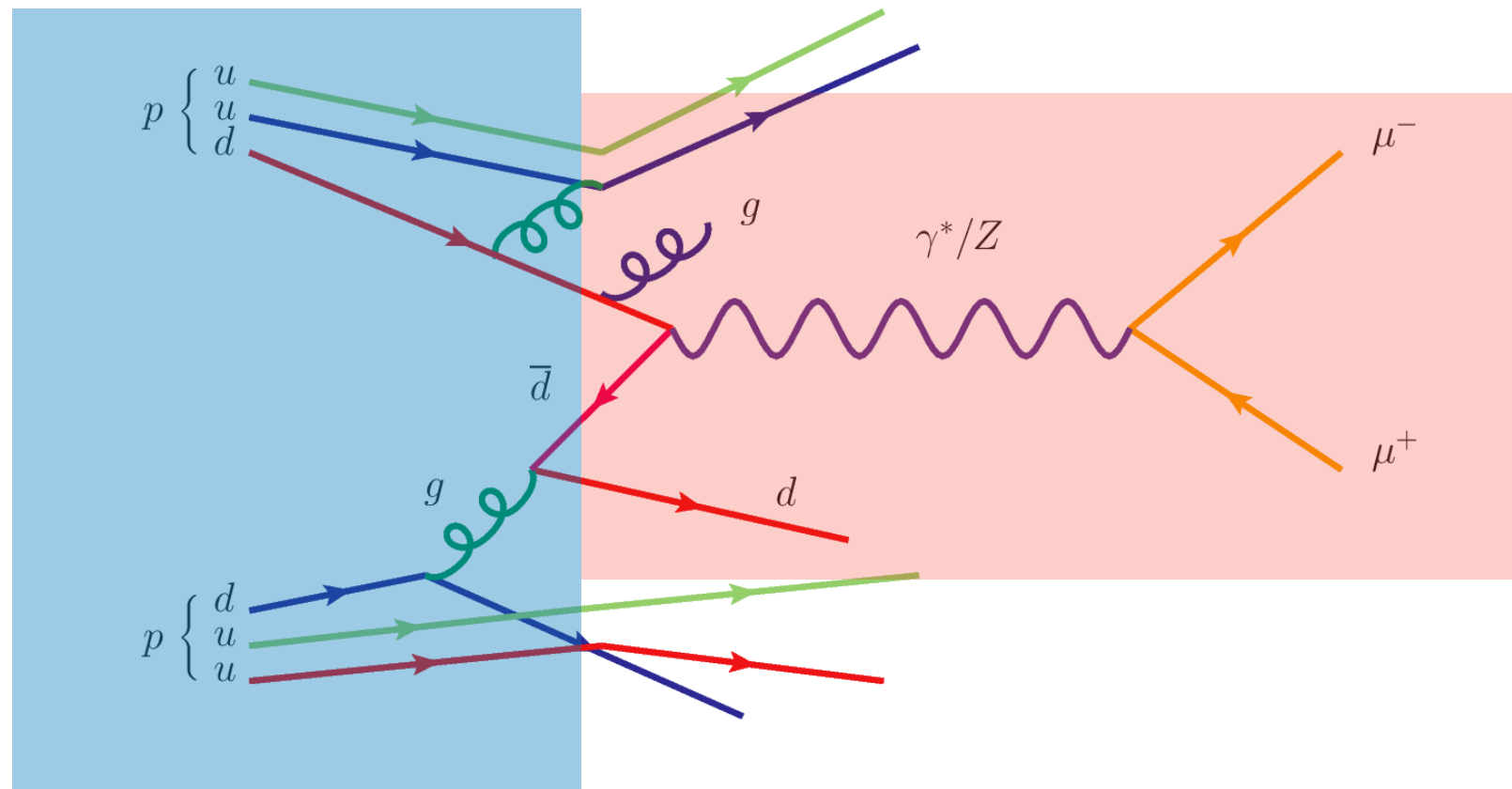


MARIA UBIALI  
UNIVERSITY OF CAMBRIDGE

# PARTON DISTRIBUTION FUNCTIONS

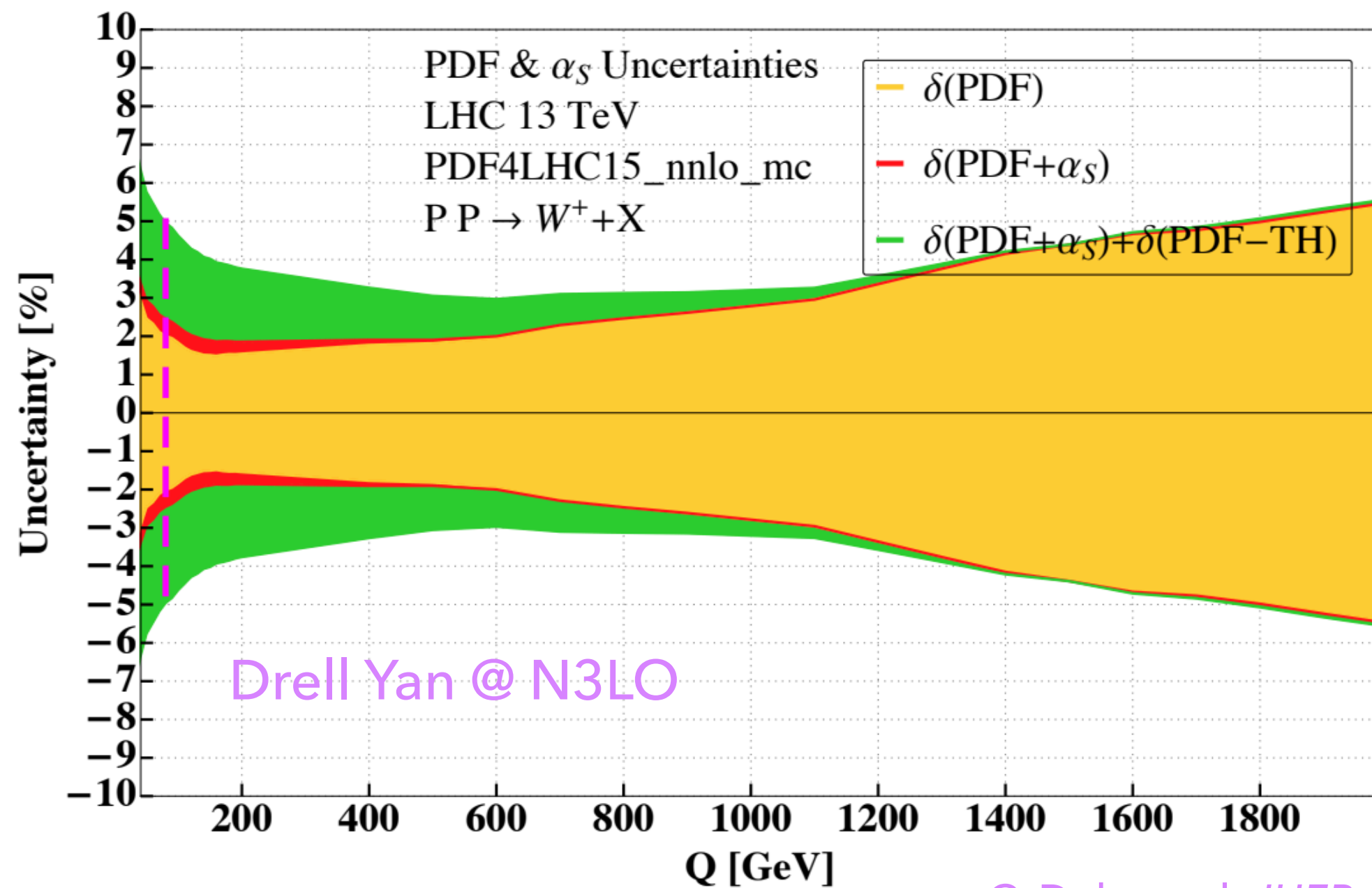
## AND THEIR IMPACT ON THE PRECISION OF CURRENT THEORY CALCULATIONS





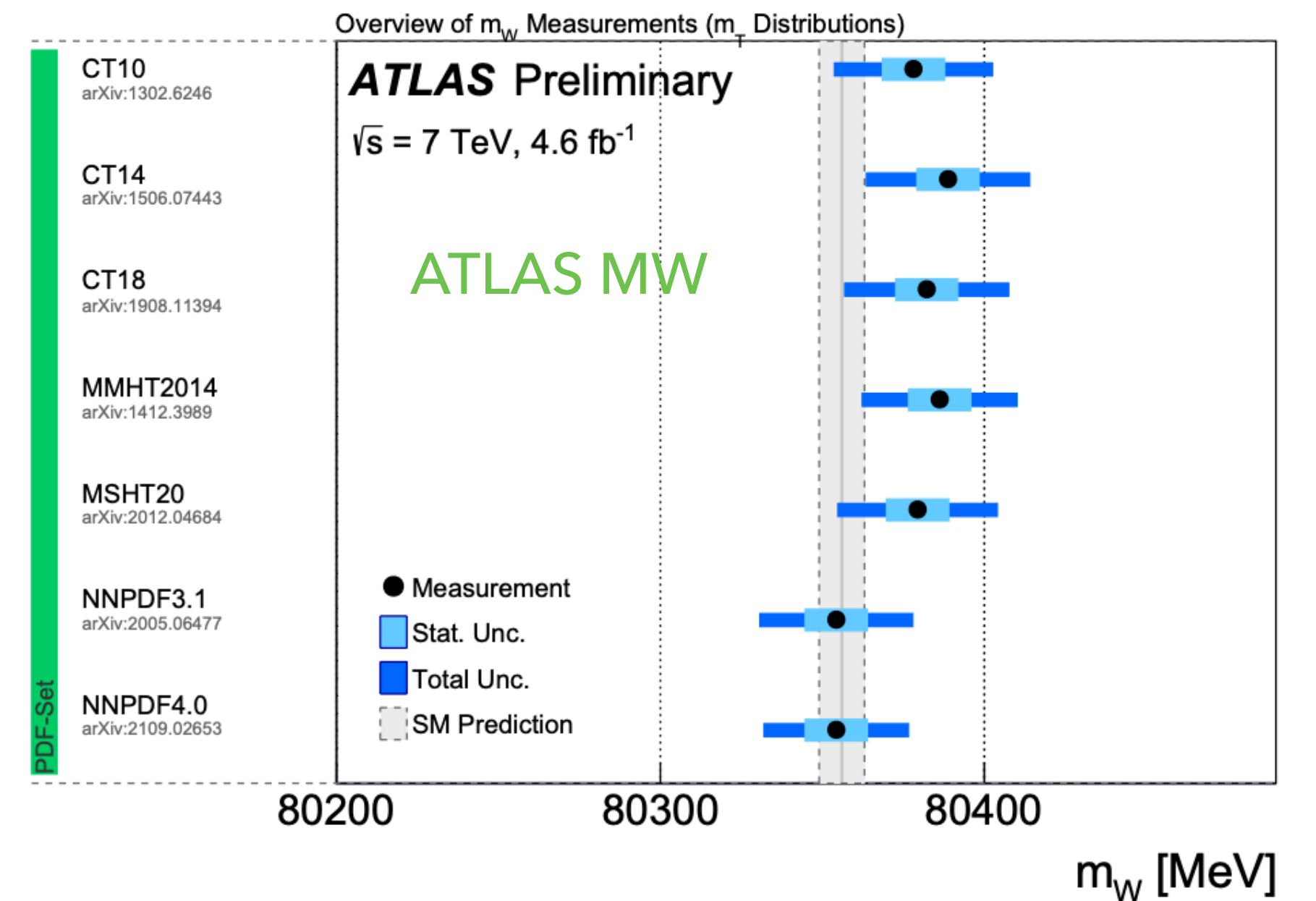
$$d\sigma^{pp \rightarrow ab} = \sum_{i,j} f_i \otimes f_j \otimes d\hat{\sigma}^{ij \rightarrow ab} + \dots$$

## #1: Theory uncertainty of SM predictions

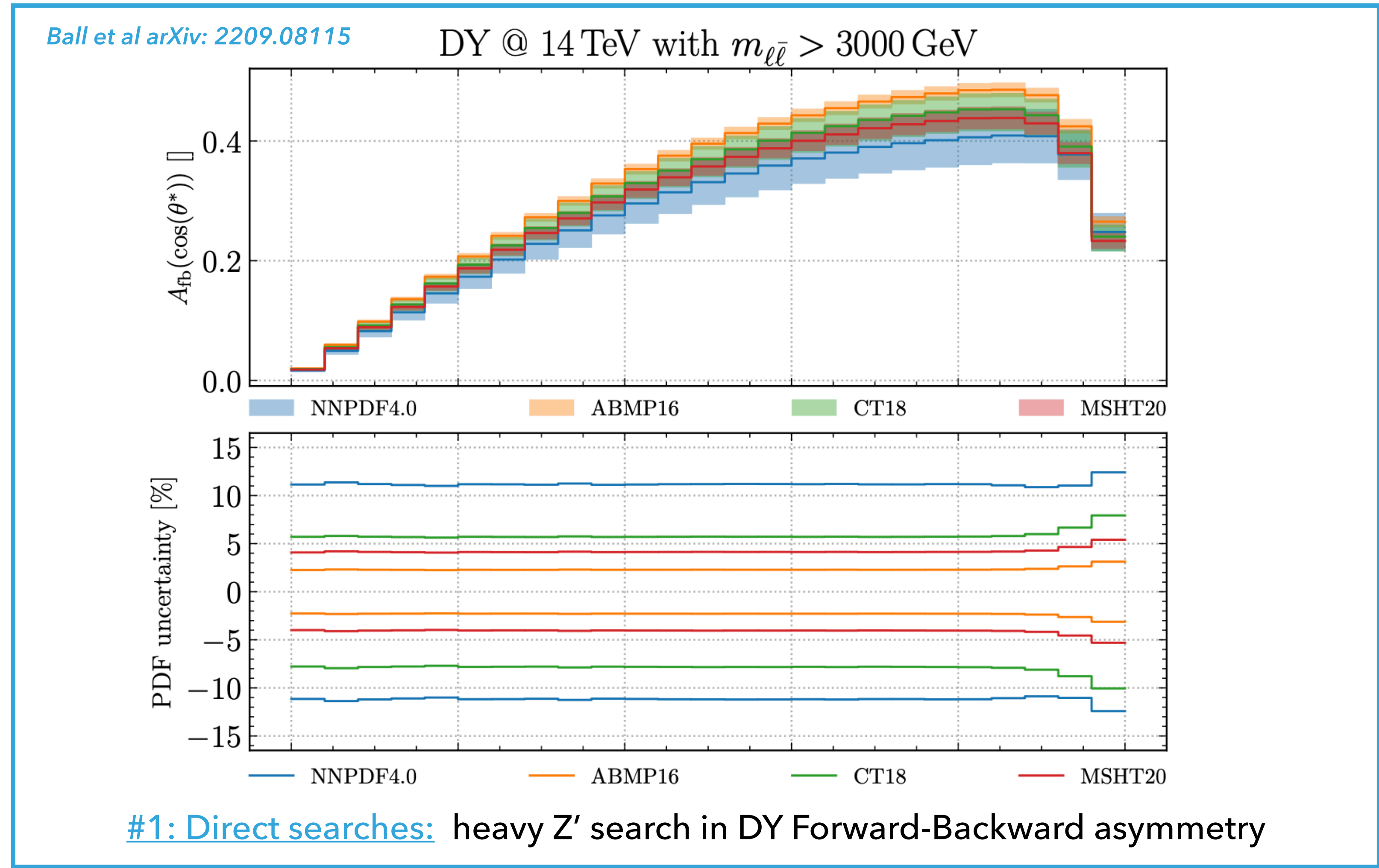
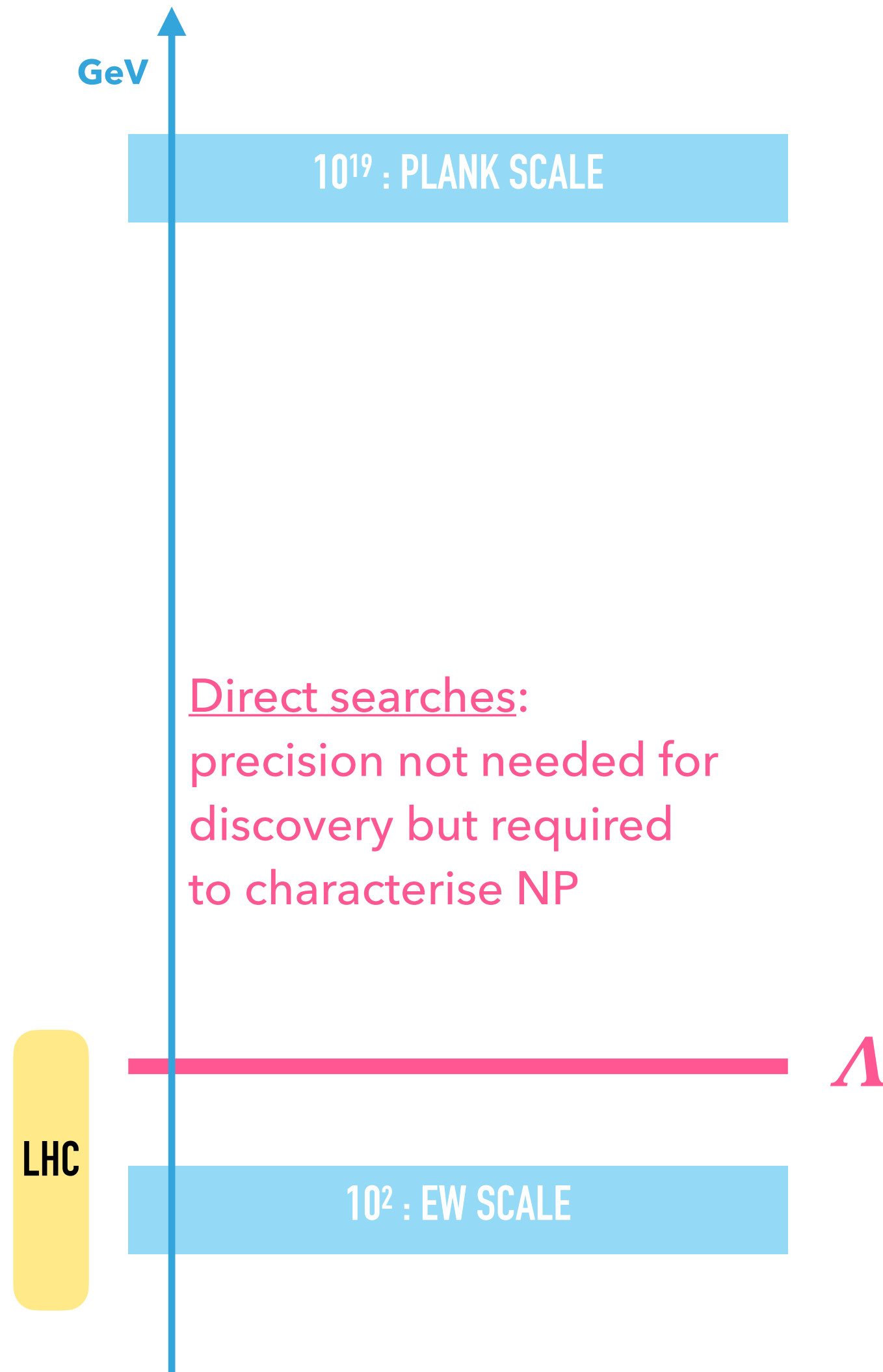


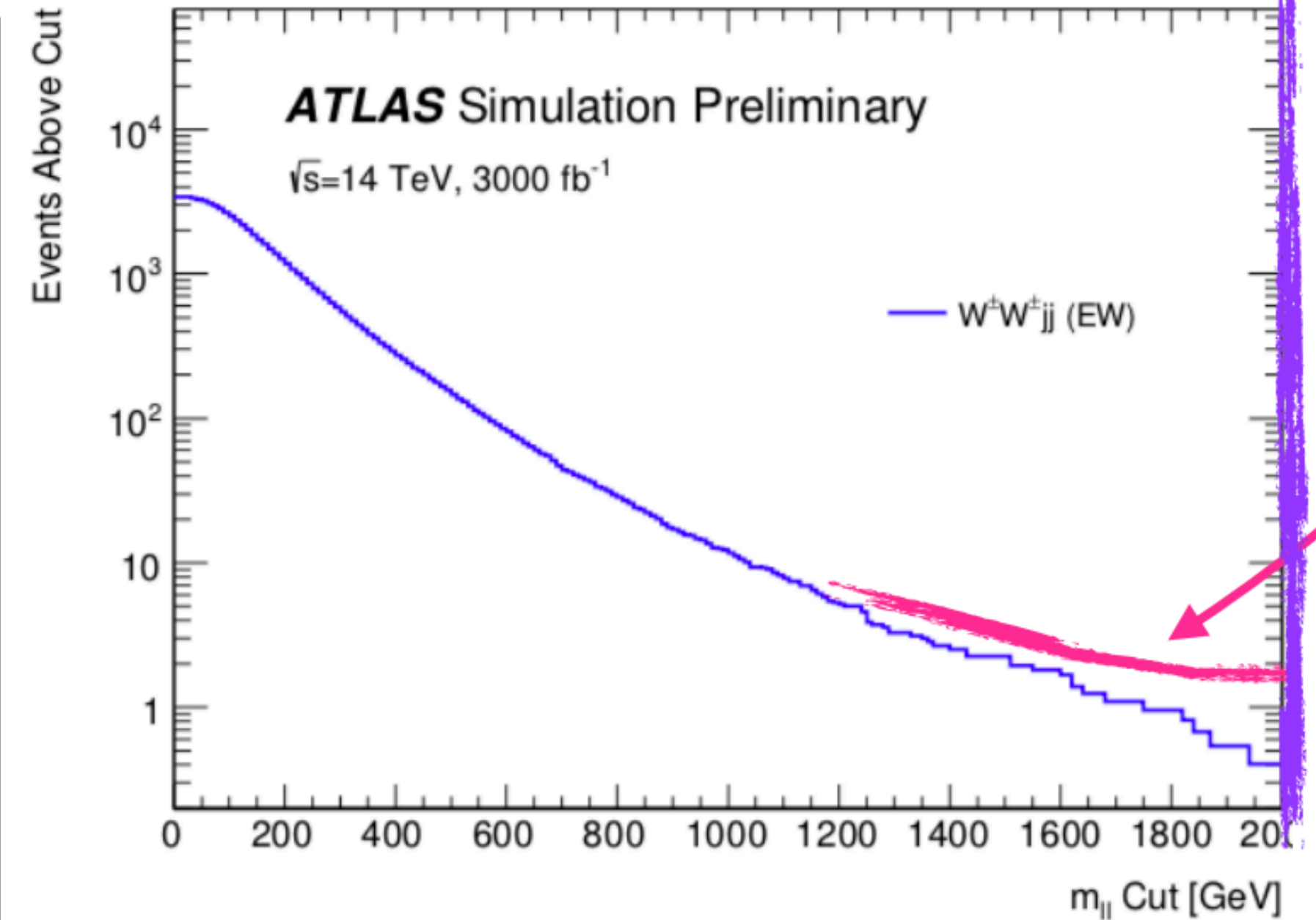
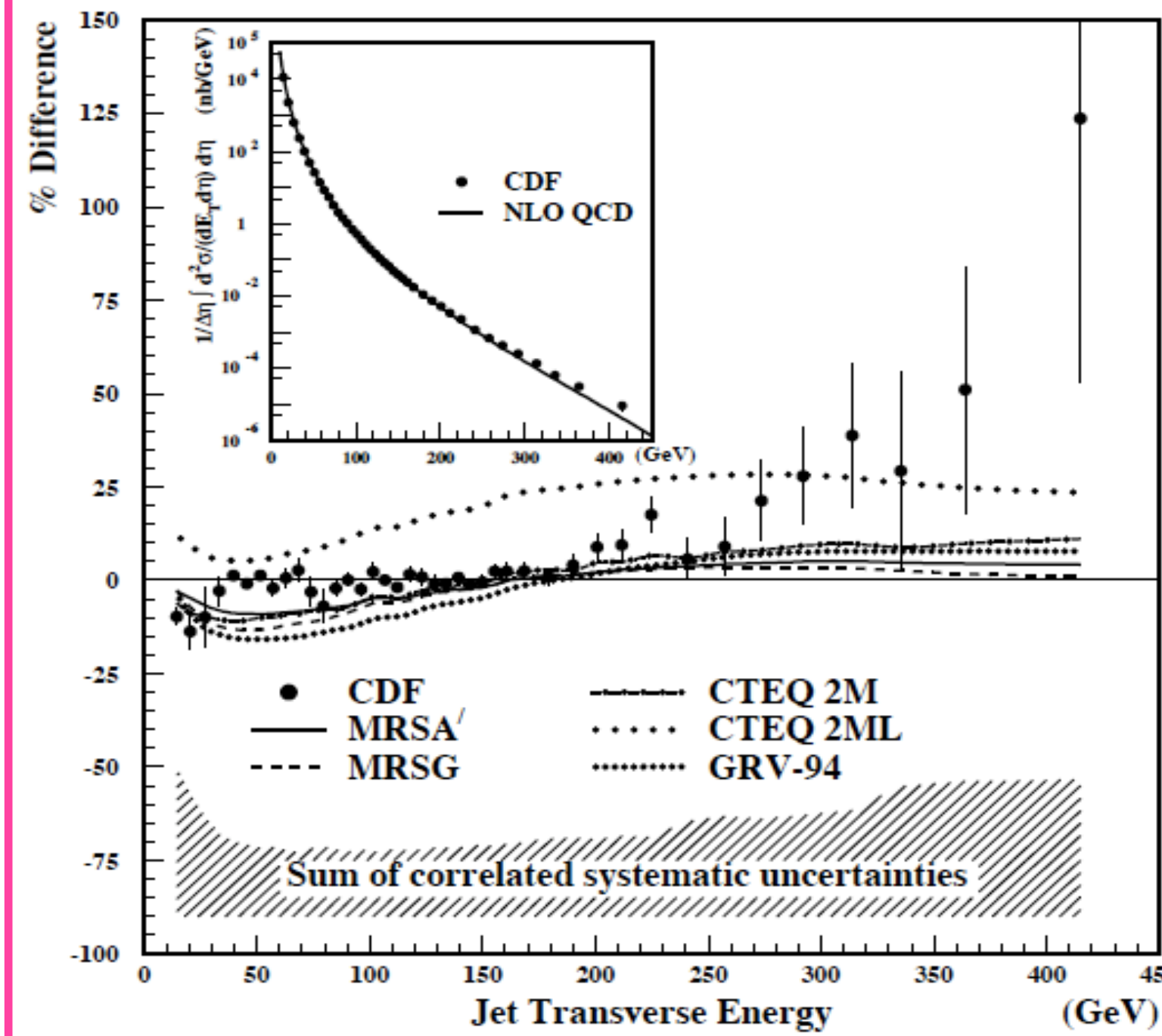
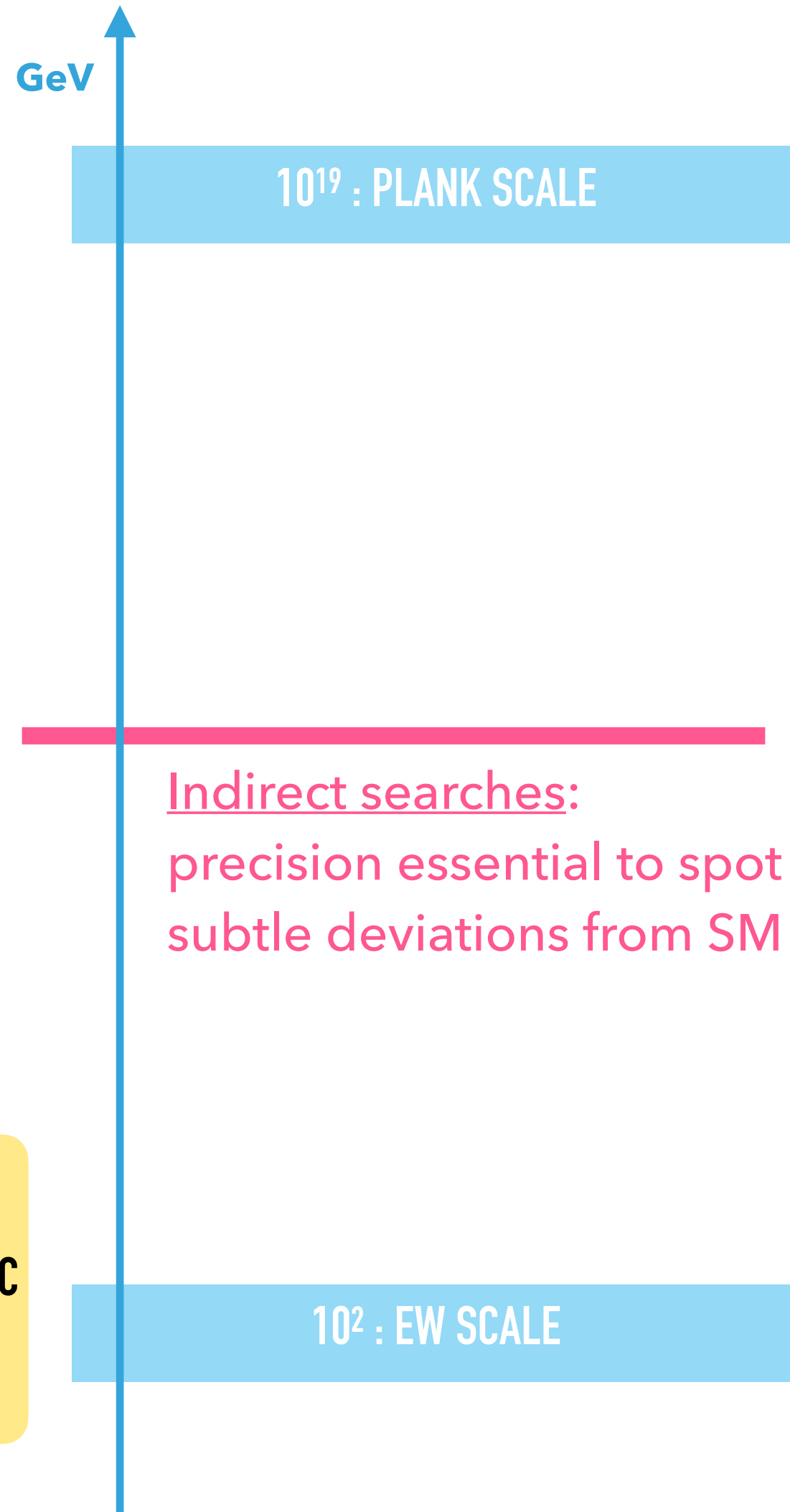
C. Duhr et al, *JHEP* 11 (2020) 143

## #2: Determination of SM parameters



ATLAS-CONF-2023-004





CA Lee, HL/HE-LHC Jamboree, 1 March 2019

### Discrepancy between QCD calculation and CDF jets data (1995)

At that time no information on PDF uncertainties and theory predictions strongly depended on gluon shape at  $x > 0.1$ . Once data included in the CTEQ fit, discrepancy disappeared.

### Deviations from SM predictions in high energy tails (>2023)

New physics or limited understanding of proton structure?



# OUTLINE

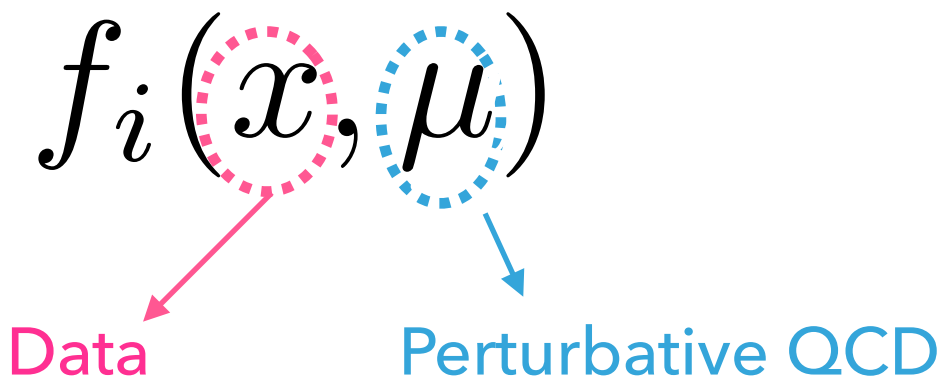
- Where we stand
  - ➔ Updates on PDF determination
  - ➔ The precision vs accuracy challenge
- New frontiers and challenges
  - ➔ Approximate N3LO PDFs
  - ➔ Missing Higher Order Uncertainties
  - ➔ PDF and new physics interplay
- Conclusions and outlook

# PART I: WHERE WE STAND

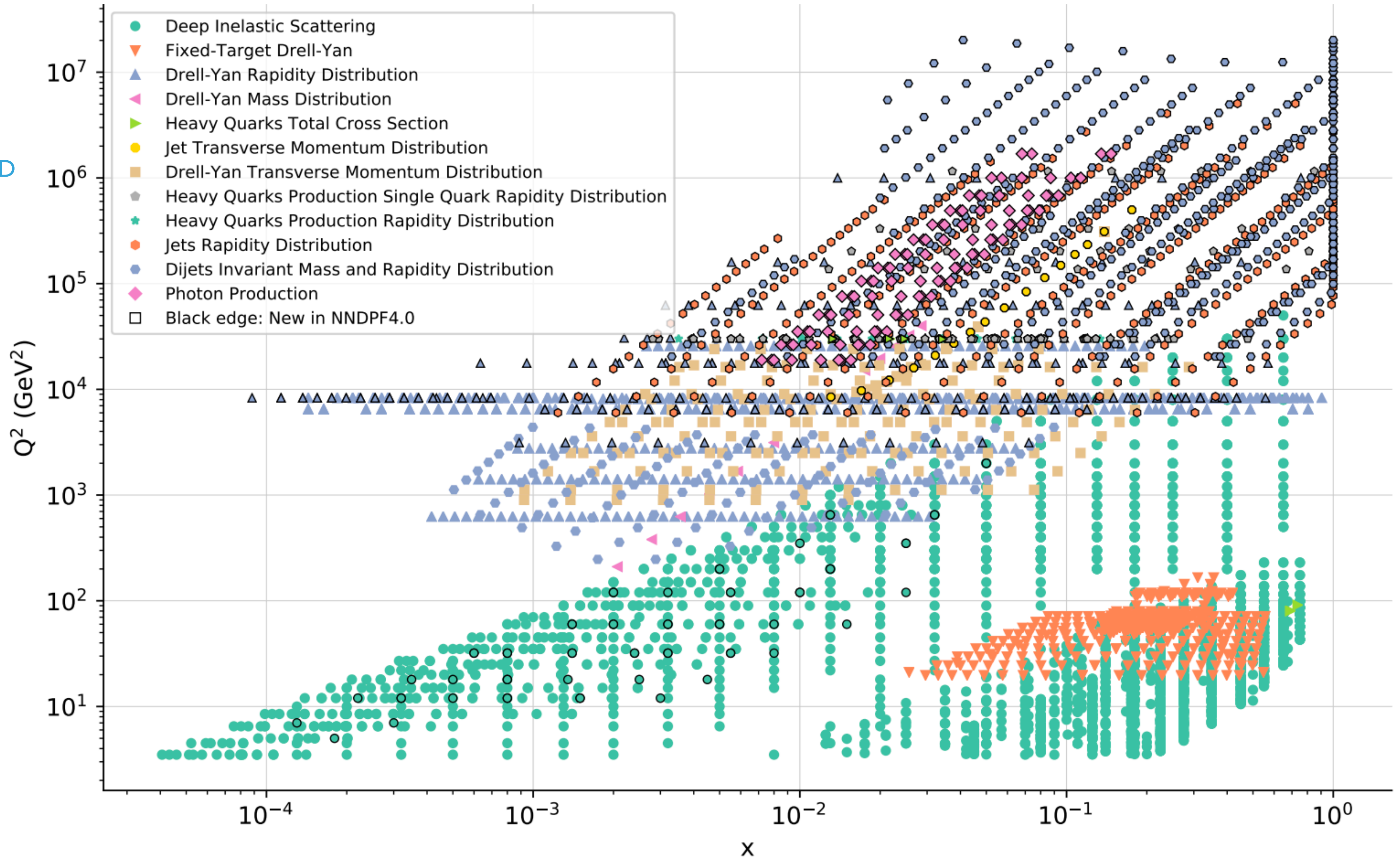
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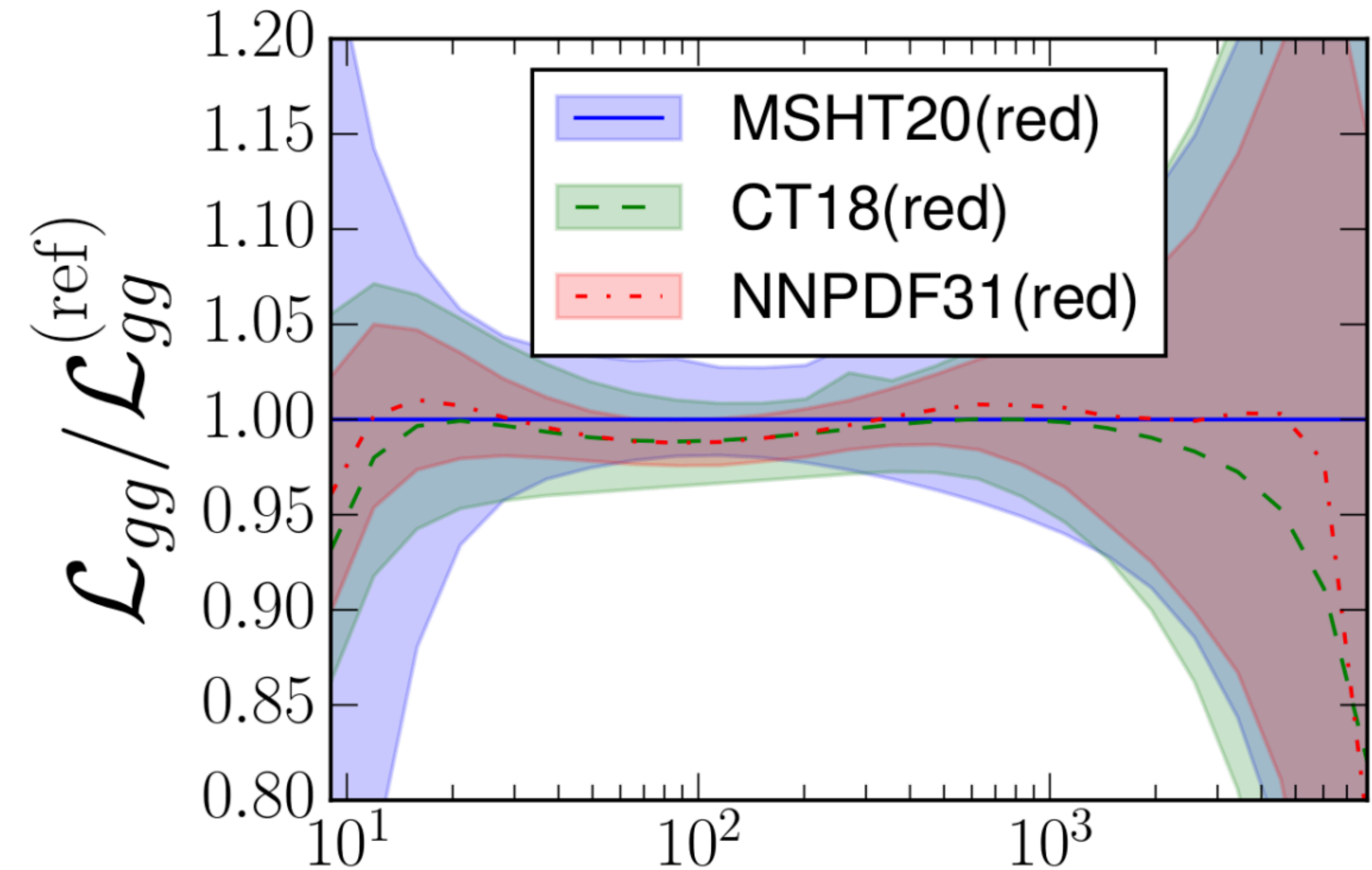
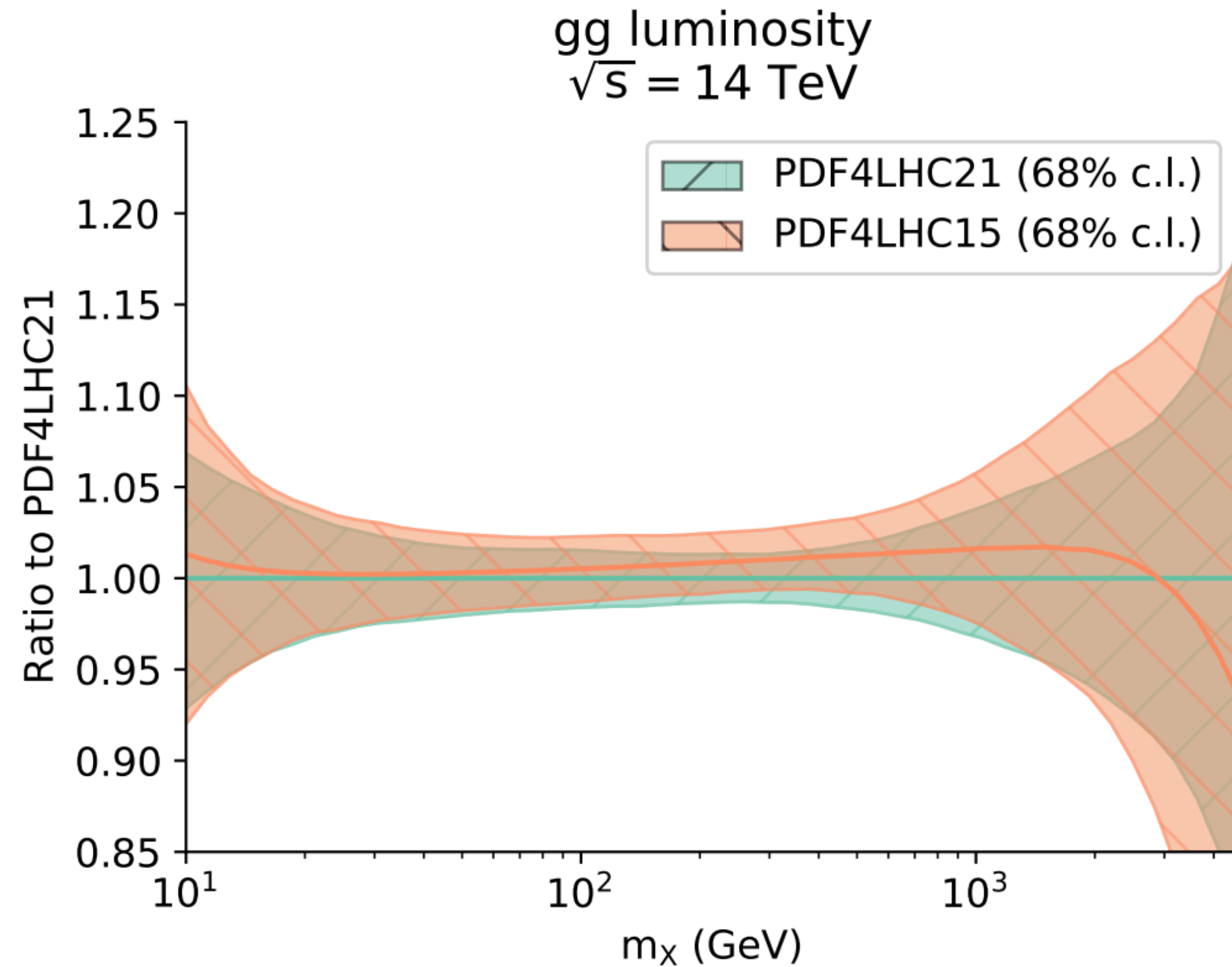
# DETERMINATION OF PDFS



- DGLAP evolution equations fully known up to NNLO and partially at N<sup>3</sup>LO
- Most theory predictions for processes in PDF fits known at NNLO (some at N<sup>3</sup>LO)
- Precision of most data of order few %
- Mostly from correlated systematic uncertainties



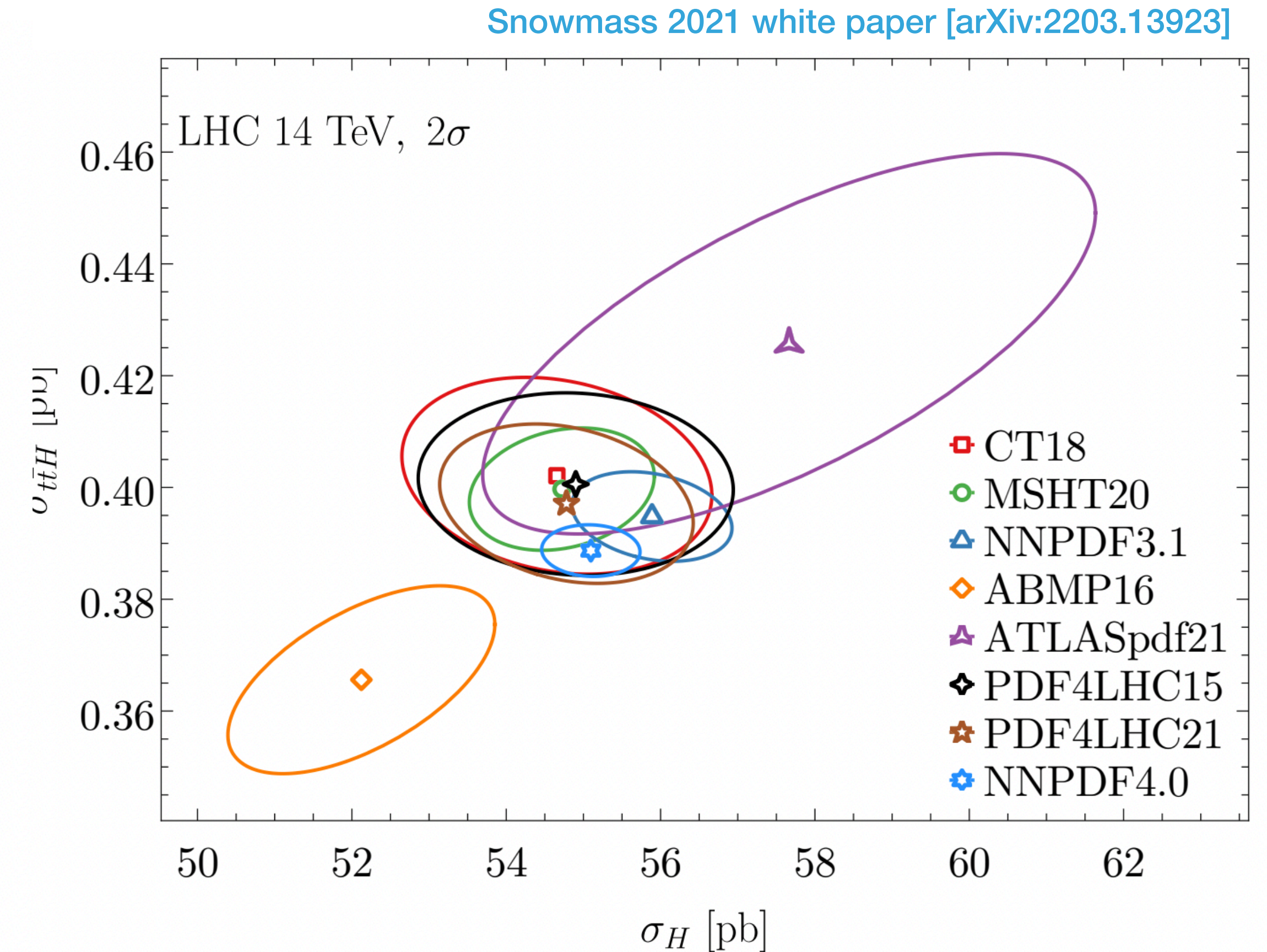
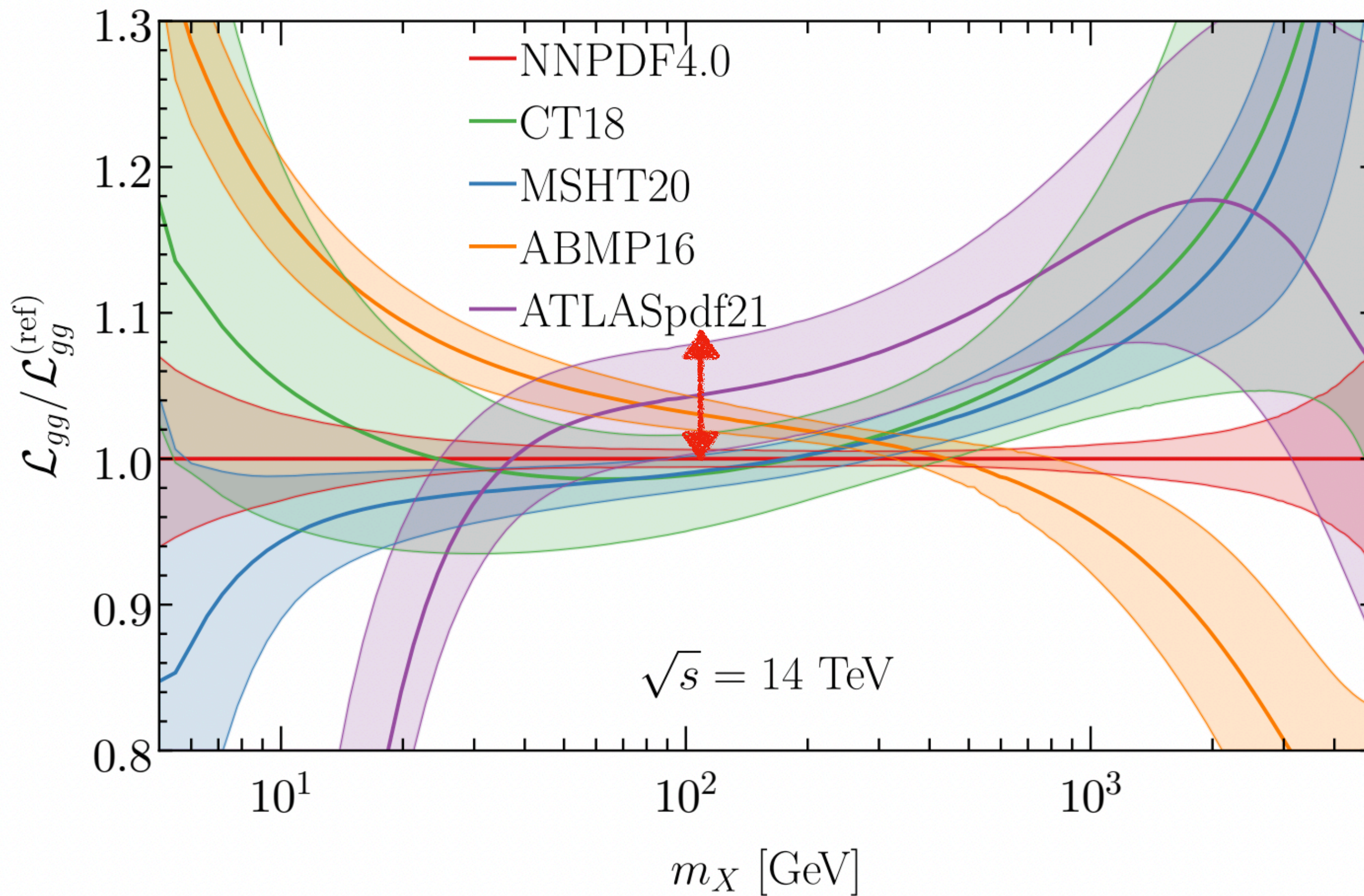




- In recent updates from global PDF fitting collaborations (NNPDF3.1, CT18, MSHT20, ABMP16) effect of LHC data driving PDF uncertainties down → PDF4LHC21 combination of NNPDF31', CT18' and MSHT20' smaller uncertainties than PDF4LHC15
- The increased precision of the data and their strong correlation demands methodological improvements (e. g. more flexible parametrisation that shifts PDFs outside nominal error band - MSHT) and shows some tension among (CT18 vs CT18Z)
- Benchmark among NNPDF3.1, MSHT20 and CT18: overall agreement, which improves once common dataset is used, differences in uncertainties with  $\Delta\text{CT18} \approx \Delta\text{MSHT20} \approx \Delta\text{NNPDF31}$
- NNPDF4.0 [arXiv:2109.02653], MSHT20aN3LO [arXiv:2207.04739] state-of-the-art post PDF4LHC21 sets



# WHERE WE STAND NOW



- **NNLO sets:** overall agreement around Higgs mass between global PDF sets with some shifts and differences in PDF uncertainties due to differences in methodologies and datasets included.
- NNPDF4.0 has the smallest uncertainty in the data region, towards 1% precision.
- **aN3LO sets:** see second part of this talk



# NNPDF4.0: THE ROLE OF LHC DATA

Data set	NNPDF3.1	NNPDF4.0	ABMP16	CT18	MSHT20
CMS $W$ asym. 7 TeV ( $\mathcal{L} = 36 \text{ pb}^{-1}$ )	✗	✗	✗	✗	✓
CMS $Z$ 7 TeV ( $\mathcal{L} = 36 \text{ pb}^{-1}$ )	✗	✗	✗	✗	✓
CMS $W$ electron asymmetry 7 TeV	✓	✓	✗	✓	✓
CMS $W$ muon asymmetry 7 TeV	✓	✓	✓	✓	✗
CMS Drell-Yan 2D 7 TeV	✓	✓	✗	(✓)	✓
CMS Drell-Yan 2D 8 TeV	(✓)	✗	✗	✗	✗
CMS $W$ rapidity 8 TeV	✓	✓	✓	✓	✓
CMS $W, Z$ $p_T$ 8 TeV ( $\mathcal{L} = 18.4 \text{ fb}^{-1}$ )	✗	✗	✗	(✓)	✗
CMS $Z$ $p_T$ 8 TeV	✓	✓	✗	(✓)	✗
CMS $W + c$ 7 TeV	✓	✓	✗	(✓)	✓
CMS $W + c$ 13 TeV	✗	✓	✗	✗	(✓)
CMS single-inclusive jets 2.76 TeV	✓	✗	✗	✗	✓
CMS single-inclusive jets 7 TeV	✓	(✓)	✗	✓	✓
CMS dijets 7 TeV	✗	✓	✗	✗	✗
CMS single-inclusive jets 8 TeV	✗	✓	✗	✓	✓
CMS 3D dijets 8 TeV	✗	(✓)	✗	✗	✗
CMS $\sigma_{tt}^{\text{tot}}$ 5 TeV	✗	✓	✗	✗	✗
CMS $\sigma_{tt}^{\text{tot}}$ 7, 8 TeV	✓	✓	✗	✗	✗
CMS $\sigma_{tt}^{\text{tot}}$ 8 TeV	✗	✗	✗	✗	✓
CMS $\sigma_{tt}^{\text{tot}}$ 5, 7, 8, 13 TeV	✗	✗	✓	✗	✗
CMS $\sigma_{tt}^{\text{tot}}$ 13 TeV	✓	✓	✓	✗	✗
CMS $t\bar{t}$ lepton+jets 8 TeV	✓	✓	✗	✗	✓
CMS $t\bar{t}$ 2D dilepton 8 TeV	✗	✓	✗	✓	✓
CMS $t\bar{t}$ lepton+jet 13 TeV	✗	✓	✗	✗	✗
CMS $t\bar{t}$ dilepton 13 TeV	✗	✓	✗	✗	✗
CMS single top $\sigma_t + \sigma_{\bar{t}}$ 7 TeV	✗	✓	✓	✗	✗
CMS single top $R_t$ 8, 13 TeV	✗	✓	✓	✗	✗
CMS single top 13 TeV	✗	✗	✗	✗	(✓)

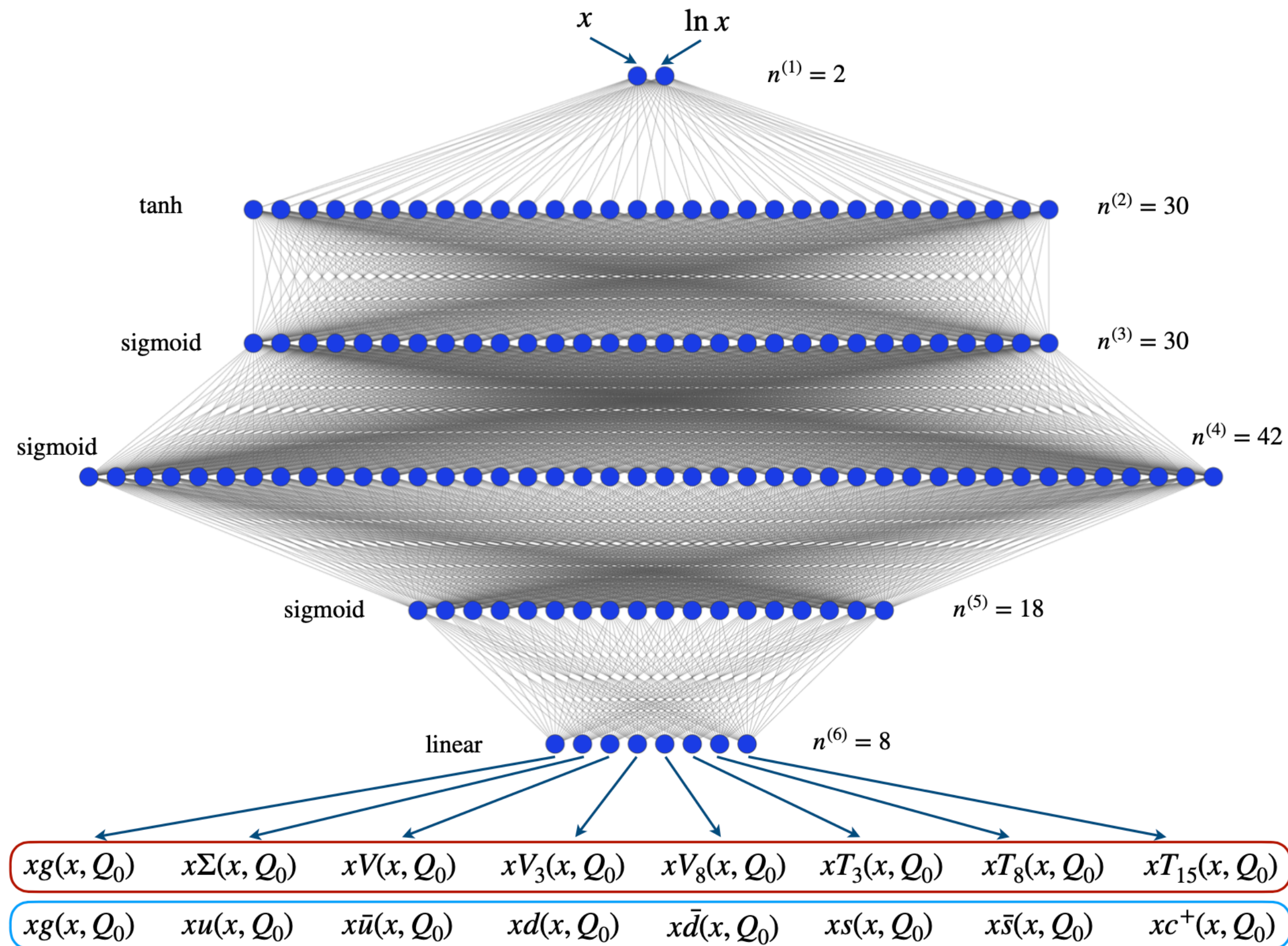
Data set	NNPDF3.1	NNPDF4.0	ABMP16	CT18	MSHT20
ATLAS $W, Z$ 7 TeV ( $\mathcal{L} = 35 \text{ pb}^{-1}$ )	✓	✓	✓	✓	✓
ATLAS $W, Z$ 7 TeV ( $\mathcal{L} = 4.6 \text{ fb}^{-1}$ )	✓	✓	✗	(✓)	✓
ATLAS low-mass DY 7 TeV	✓	✓	✗	(✓)	✗
ATLAS high-mass DY 7 TeV	✓	✓	✗	(✓)	✓
ATLAS $W$ 8 TeV	✗	(✓)	✗	✗	✓
ATLAS DY 2D 8 TeV	✗	✓	✗	✗	✓
ATLAS high-mass DY 2D 8 TeV	✗	✓	✗	(✓)	✓
ATLAS $\sigma_{W,Z}$ 13 TeV	✗	✓	✓	✗	✗
ATLAS $W$ +jet 8 TeV	✗	✓	✗	✗	✓
ATLAS $Z$ $p_T$ 7 TeV	(✓)	✗	✗	(✓)	✗
ATLAS $Z$ $p_T$ 8 TeV	✓	✓	✗	✓	✓
ATLAS $W + c$ 7 TeV	✗	✓	✗	(✓)	✗
ATLAS $\sigma_{tt}^{\text{tot}}$ 7, 8 TeV	✓	✓	✓	✗	✗
ATLAS $\sigma_{tt}^{\text{tot}}$ 7, 8 TeV	✗	✗	✓	✗	✗
ATLAS $\sigma_{tt}^{\text{tot}}$ 13 TeV ( $\mathcal{L} = 3.2 \text{ fb}^{-1}$ )	✓	✗	✓	✗	✗
ATLAS $\sigma_{tt}^{\text{tot}}$ 13 TeV ( $\mathcal{L} = 139 \text{ fb}^{-1}$ )	✗	✓	✗	✗	✗
ATLAS $\sigma_{tt}^{\text{tot}}$ and $Z$ ratios	✗	✗	✗	✗	(✓)
ATLAS $t\bar{t}$ lepton+jets 8 TeV	✓	✓	✗	✓	✓
ATLAS $t\bar{t}$ dilepton 8 TeV	✗	✓	✗	✗	✓
ATLAS single-inclusive jets 7 TeV, R=0.6	✓	(✓)	✗	✓	✓
ATLAS single-inclusive jets 8 TeV, R=0.6	✗	✓	✗	✗	✗
ATLAS dijets 7 TeV, R=0.6	✗	✓	✗	✗	✗
ATLAS direct photon production 8 TeV	✗	(✓)	✗	✗	✗
ATLAS direct photon production 13 TeV	✗	✓	✗	✗	✗
ATLAS single top $R_t$ 7, 8, 13 TeV	✗	✓	✓	✗	✗
ATLAS single top diff. 7 TeV	✗	✓	✗	✗	✗
ATLAS single top diff. 8 TeV	✗	✓	✗	✗	✗

- NNPDF4.0 based on larger set of data from LHC Run I and Run II
- Open-source public code [\[arXiv:2109.02671\]](https://arxiv.org/abs/2109.02671)
- O(4500) data points and first time inclusion of di-jets preferred over inclusive jets based on perturbative stability [\[Khalek et al, 2005.11327\]](https://arxiv.org/abs/2005.11327)

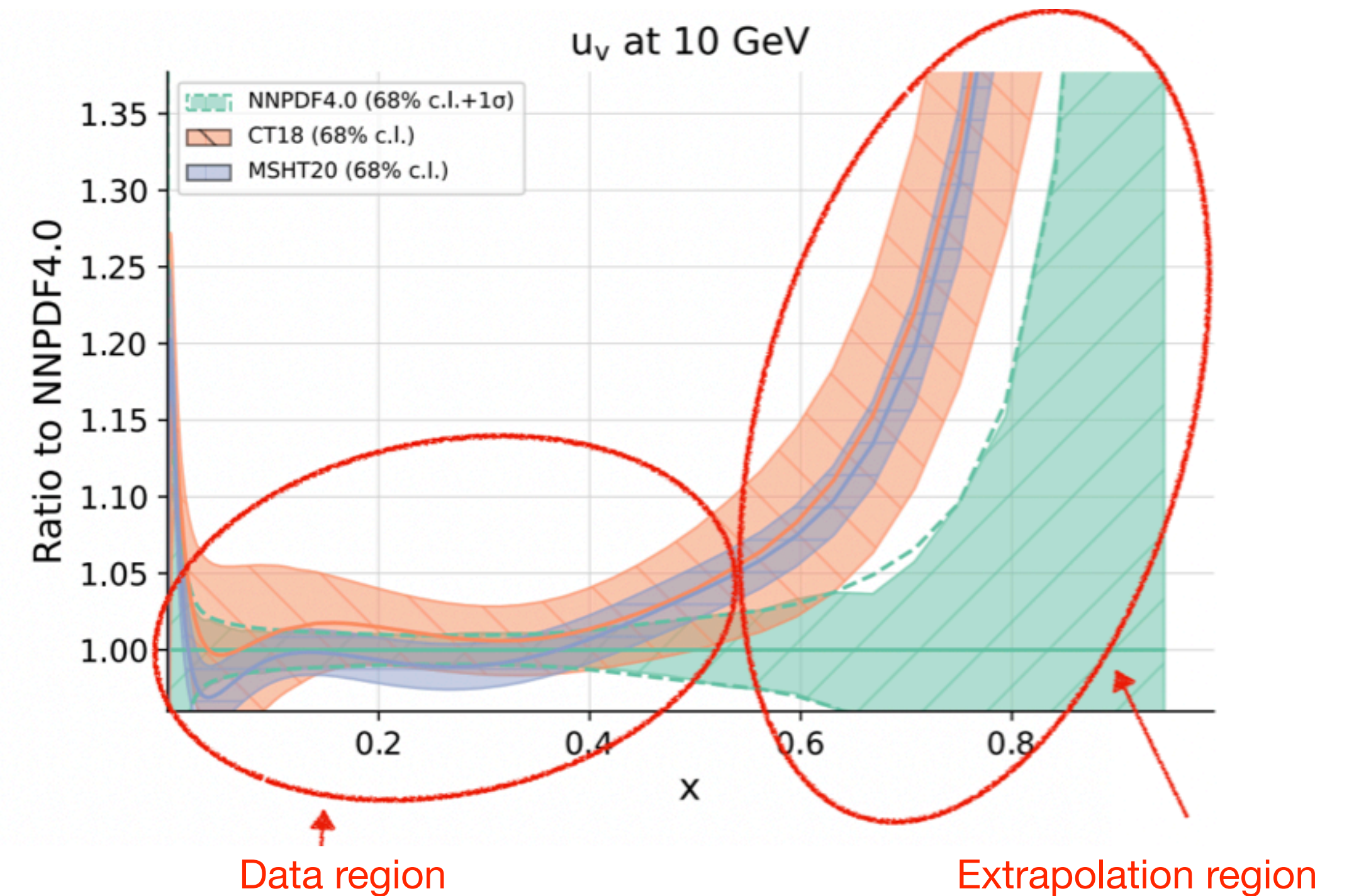


# NNPDF4.0: THE ROLE OF METHODOLOGY

- Single neural network to parametrise 8 independent PDF combinations ( $g, u, d, s, u\bar{,} d\bar{,} s\bar{,} c=c\bar{}$ )
- Optimisation strategy based on gradient descent rather than genetic algorithm (NNPDF3.1)
- Hyper-optimised methodology: scan of the hyper parameter space to find optimal minimisation settings (optimiser, initialiser, stopping patience, number of layers, learning rate, epochs, activation function) by minimising  $\chi^2_{\text{val}}$  [Carrazza et al, arXiv:1907.05075]

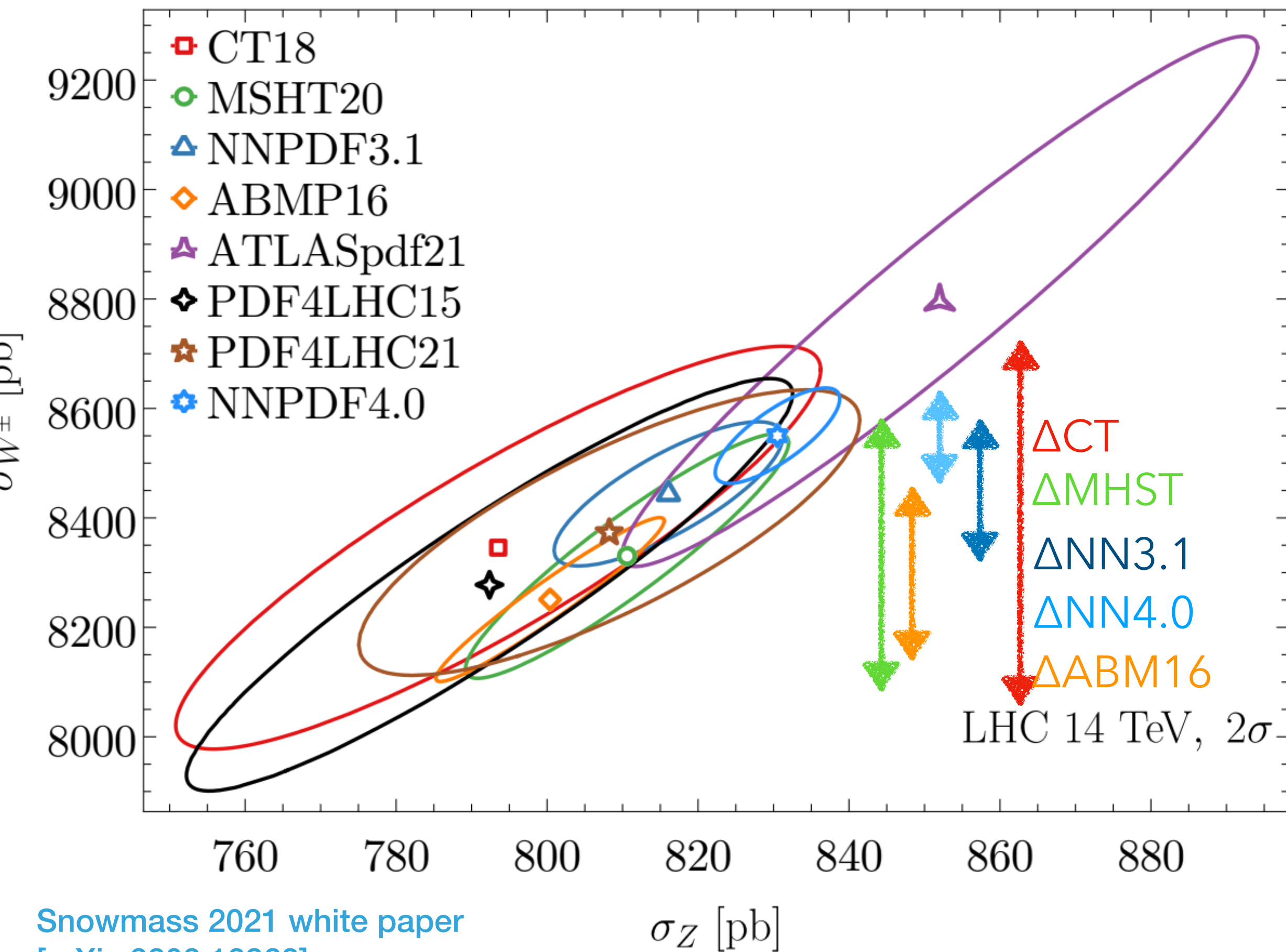


Thanks to superior methodology NN40 displays smaller uncertainty than NN3.1, O(500) extra LHC data further decrease uncertainties and shift PDFs.

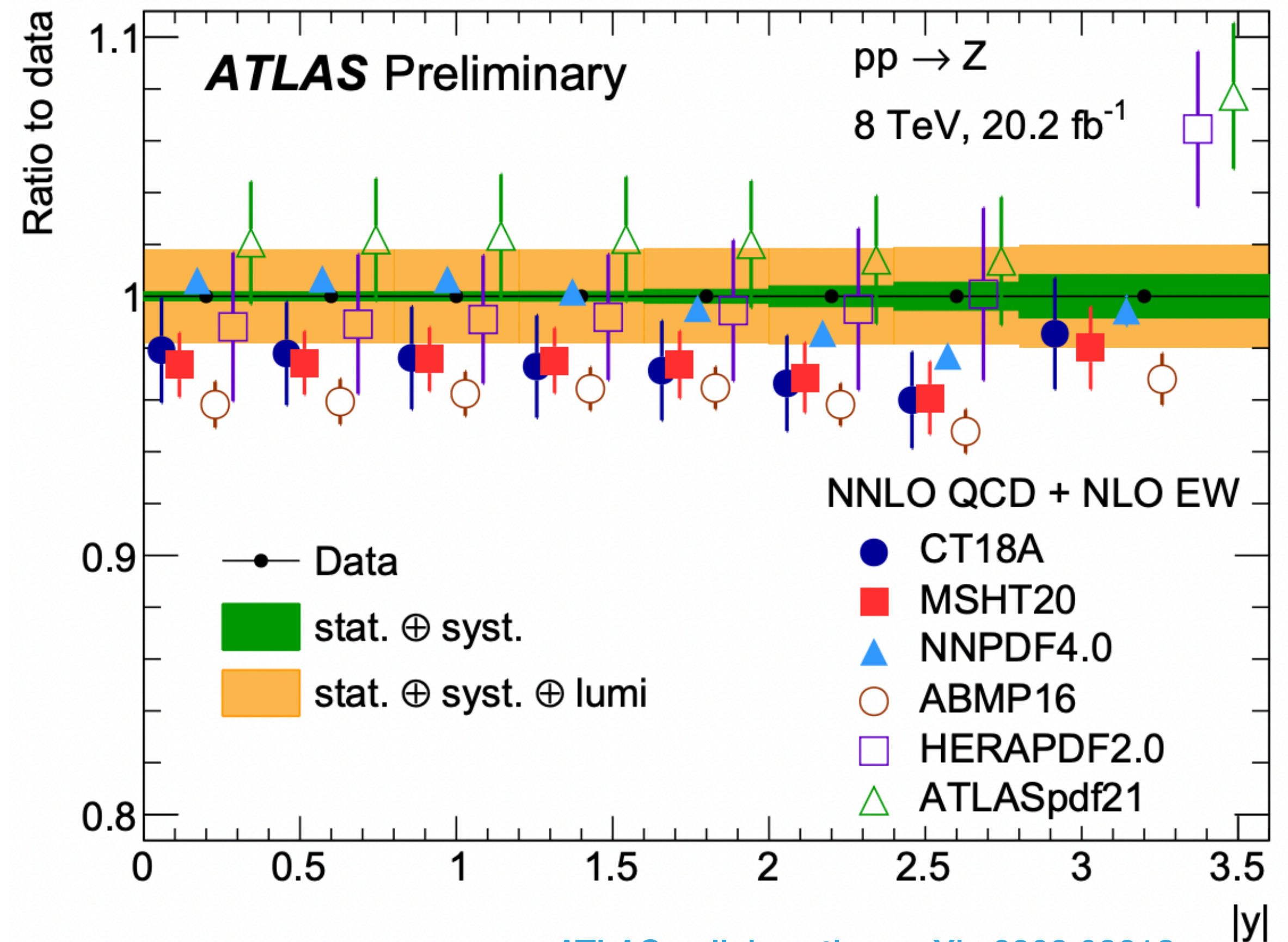




# PHENOMENOLOGICAL IMPLICATIONS



Snowmass 2021 white paper  
[arXiv:2203.13923]



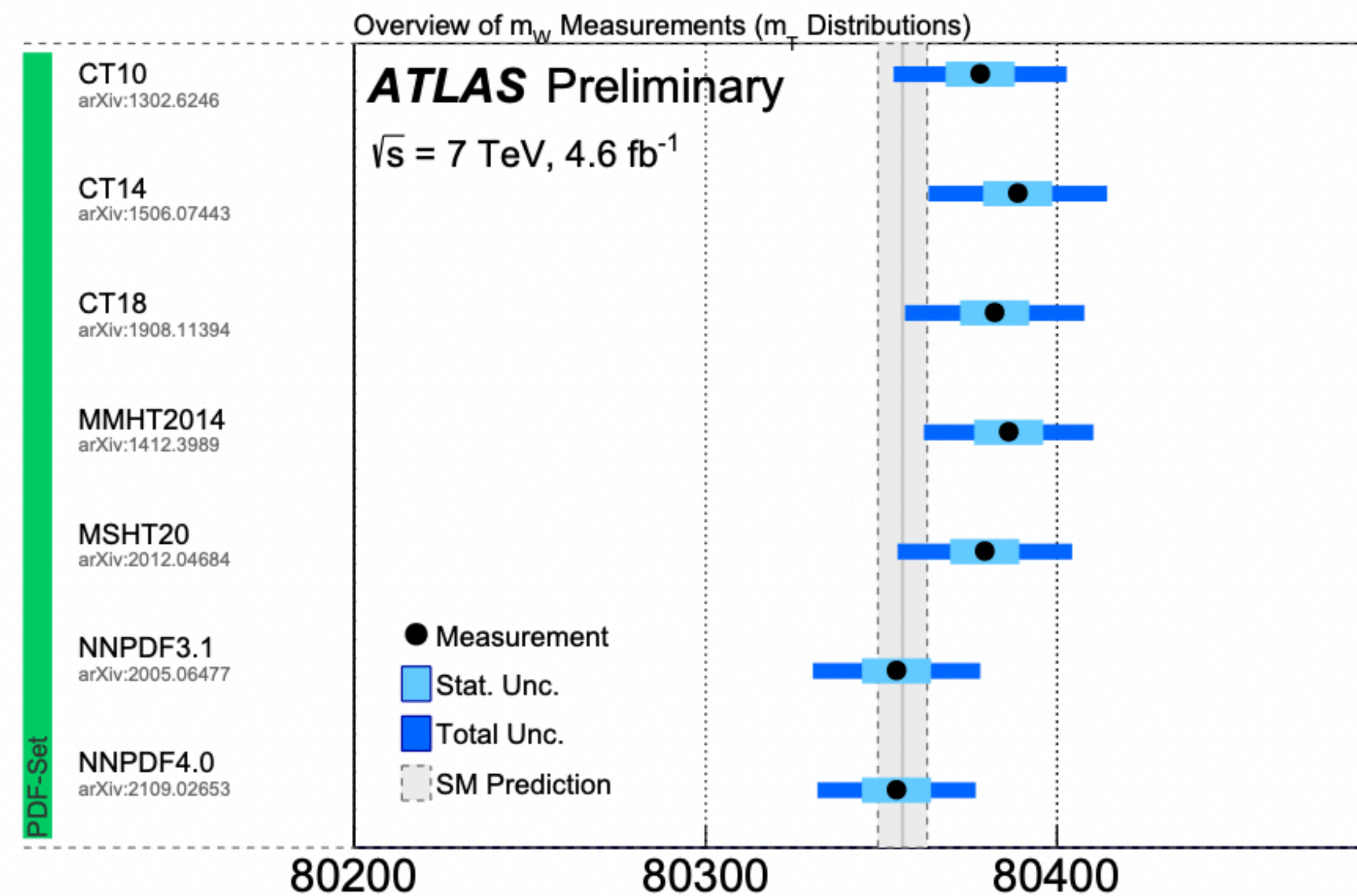
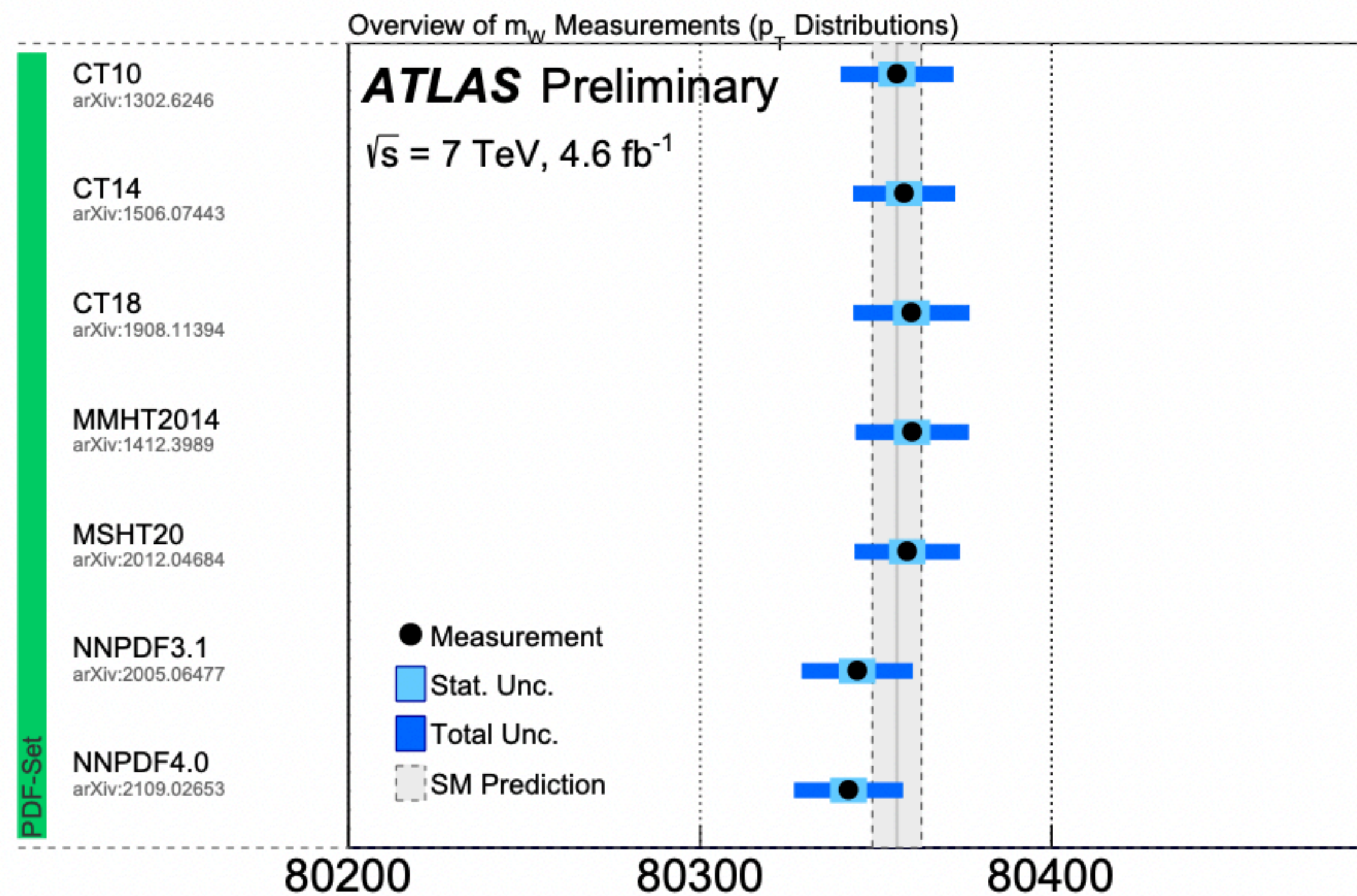
ATLAS collaboration, arXiv:2309.09318

- Extremely precise predictions and small PDF uncertainties for electroweak observables: implications for extraction of SM precision parameters, like  $\alpha_s$  from Z pT distribution and  $M_W$  from W mT distributions



# PHENOMENOLOGICAL IMPLICATIONS

ATLAS-CONF-2023-004



PDF-Set	$p_T^\ell$ [MeV]	$m_T$ [MeV]	combined [MeV]
CT10	$80355.6^{+15.8}_{-15.7}$	$80378.1^{+24.4}_{-24.8}$	$80355.8^{+15.7}_{-15.7}$
CT14	$80358.0^{+16.3}_{-16.3}$	$80388.8^{+25.2}_{-25.5}$	$80358.4^{+16.3}_{-16.3}$
CT18	$80360.1^{+16.3}_{-16.3}$	$80382.2^{+25.3}_{-25.3}$	$80360.4^{+16.3}_{-16.3}$
MMHT2014	$80360.3^{+15.9}_{-15.9}$	$80386.2^{+23.9}_{-24.4}$	$80361.0^{+15.9}_{-15.9}$
MSHT20	$80358.9^{+13.0}_{-16.3}$	$80379.4^{+24.6}_{-25.1}$	$80356.3^{+14.6}_{-14.6}$
NNPDF3.1	$80344.7^{+15.6}_{-15.5}$	$80354.3^{+23.6}_{-23.7}$	$80345.0^{+15.5}_{-15.5}$
NNPDF4.0	$80342.2^{+15.3}_{-15.3}$	$80354.3^{+22.3}_{-22.4}$	$80342.9^{+15.3}_{-15.3}$

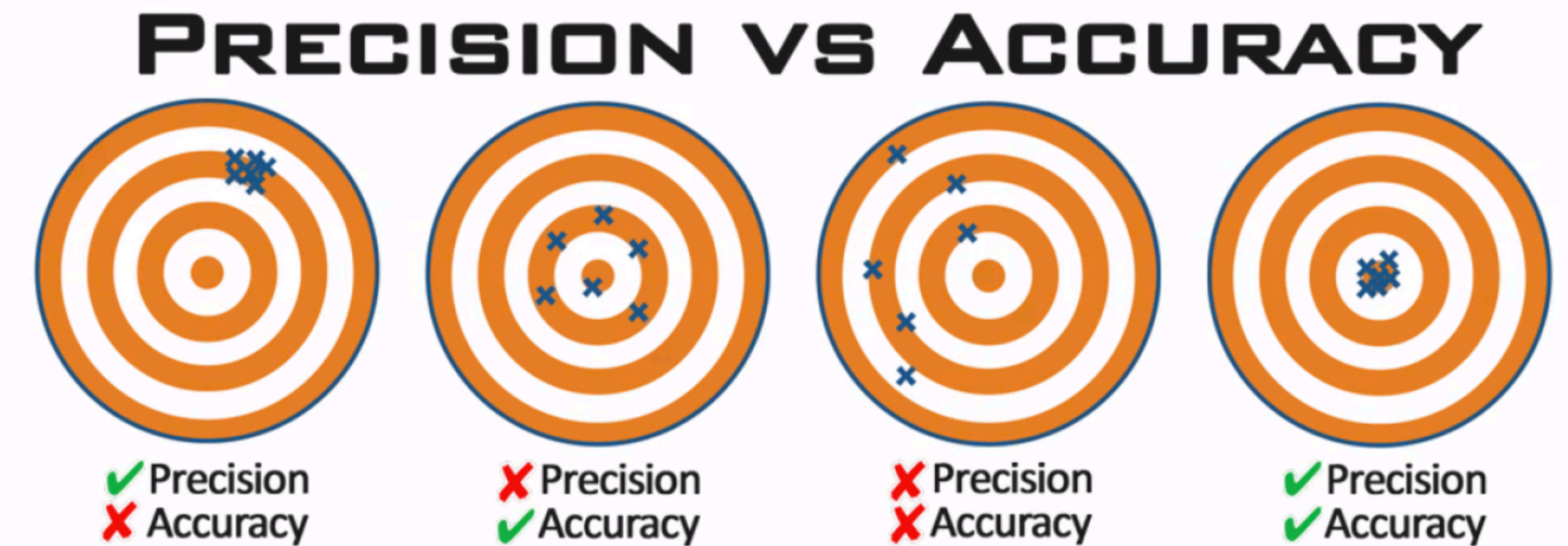
 $m_W$  [MeV] $m_W$  [MeV]

- Different PDF uncertainties yield slightly different total uncertainties.
- Differences of  $\sim 18$  MeV between central values obtained with NNP4.0 and CT18 comparable (larger) than measurement uncertainty
- Important to confirm results and understand the reason behind the differences



# THE PRECISION VERSUS ACCURACY CHALLENGE

- ▶ Inconsistency or tension in data
- ▶ Data-driven parametrisation change
- ▶ Changes in fitting methodology
- ▶ Theoretical framework
  - ➔ Missing higher order uncertainties
  - ➔ Other corrections (nuclear, non-perturbative effects...)
  - ➔ BSM effects



Methodology  
robustness

- Closure tests for data region: imagine we knew the law of Nature, is our fitting methodology able to reproduce it? Is the uncertainty faithful? Statistical validation of PDF uncertainties via closure tests  
 [Del Debbio et al, *Eur.Phys.J.C* 82 (2022) 4, 330]  
 [Barontini et al - in progress]

Generalisation/  
extrapolation

- Future tests: how well do PDF describe data that are not included in the fit (either in data or extrapolation region)? Help to discriminate among PDF sets  
 [J. Cruz-Martinez et al, *Acta Phys.Polon.B* 52 (2021) 243]  
 [NNPDF collaboration - in progress]





## **PART II: NEW FRONTIERS**

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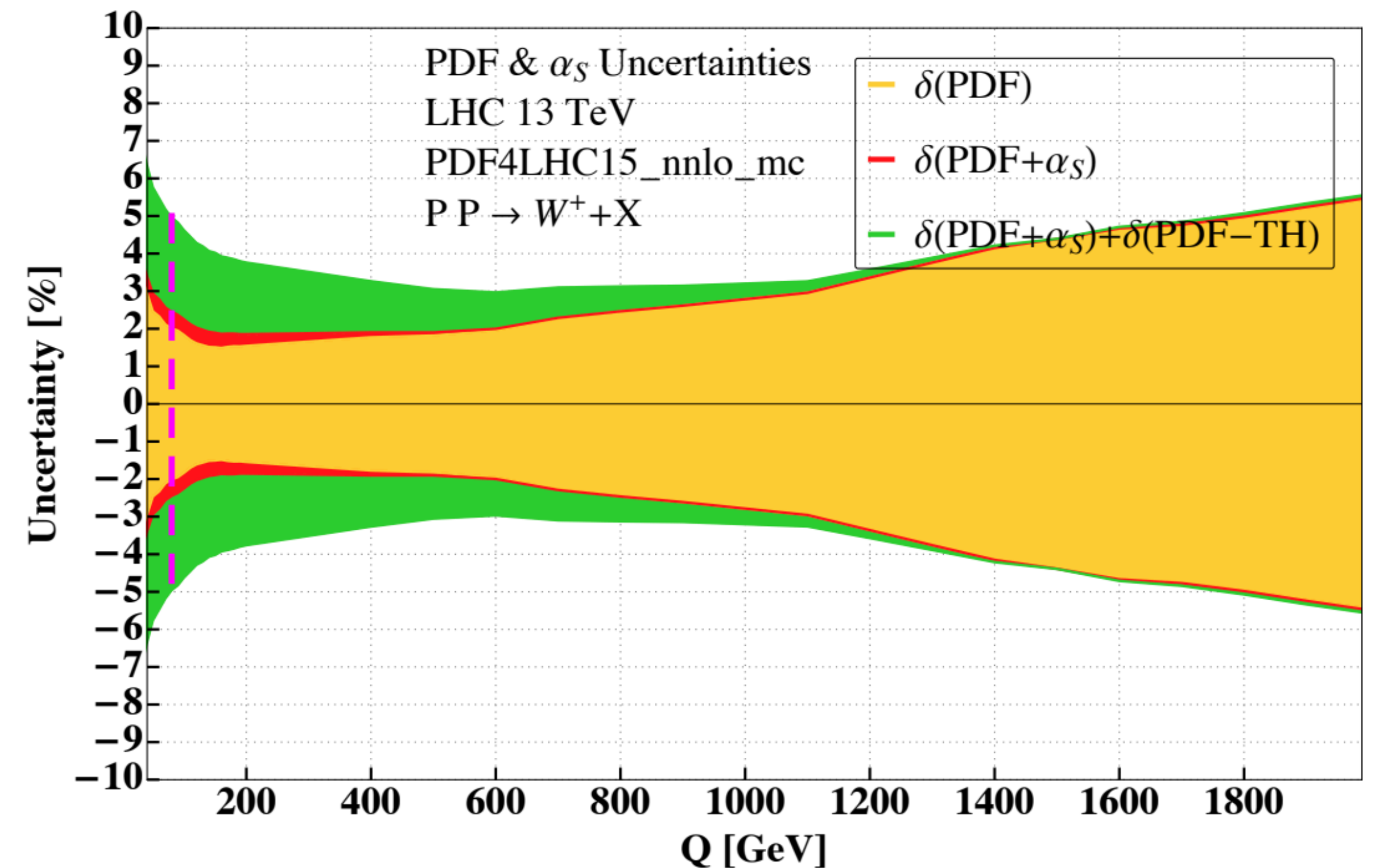
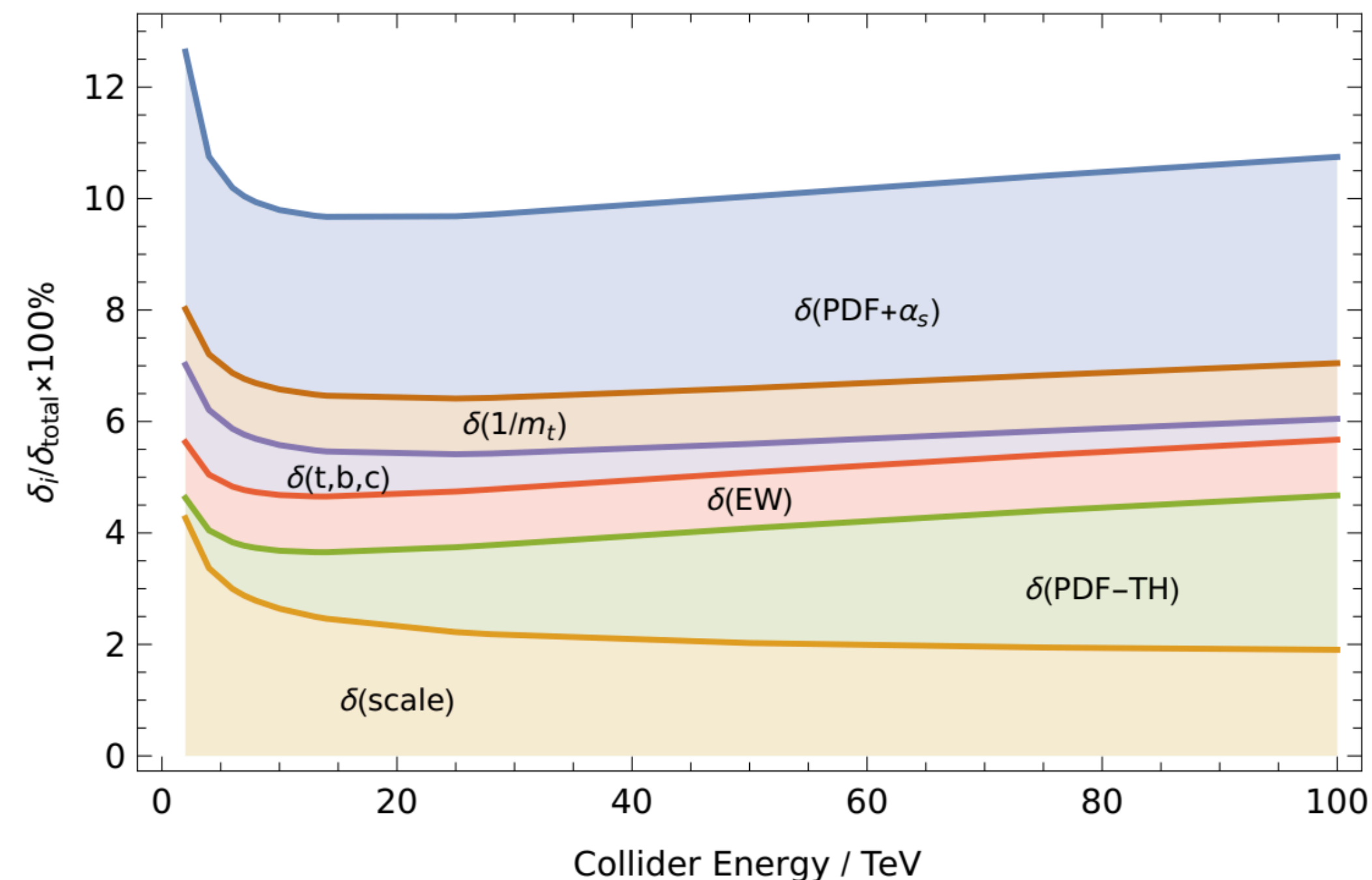
$$\sigma = \alpha_s^p \sigma_0 + \alpha_s^{p+1} \sigma_1 + \alpha_s^{p+2} \sigma_2 + \mathcal{O}(\alpha_s^{p+3})$$

- ▶ Standard global PDF fits based on fixed-order NNLO QCD calculations (using fast interpolation grid for NLO predictions accompanied by local K-factors for NNLO). PDF uncertainty reflects experimental uncertainty.
- ▶ N<sup>3</sup>LO is now the precision frontier for partonic cross sections (huge progress in N<sup>3</sup>LO splitting functions) [S. Moch's talk]
- ▶ Mismatch between perturbative order of partonic cross section and PDFs significant source of uncertainty

$$\delta(\text{PDF} - \text{TH}) = \frac{1}{2} \left| \frac{\sigma_{\text{NNLO-PDFs}}^{(2)} - \sigma_{\text{NLO-PDFs}}^{(2)}}{\sigma_{\text{NNLO-PDFs}}^{(2)}} \right|$$

## Gluon-gluon fusion into Higgs

## Drell-Yan





- ➔ Several ingredients required to perform N<sup>3</sup>LO PDF fits, many available some missing [[S. Moch's talk](#)]
- ➔ Only publicly available aN<sup>3</sup>LO PDF determination is from the MSHT collaboration [[McGowan et al, arXiv:2207.04739](#)]
- ➔ NNPDF has presented preliminary aN<sup>3</sup>LO results and paper is to appear soon

## MSHT

- All available theory input at the time of publication included (impact of new ingredients being explored)
- Incomplete N<sup>3</sup>LO terms added as variation in the prior and estimated by fitting nuisance parameters to the data (hence **posterior determined by fitting data**)
- No MHOU associated with NNLO contributions

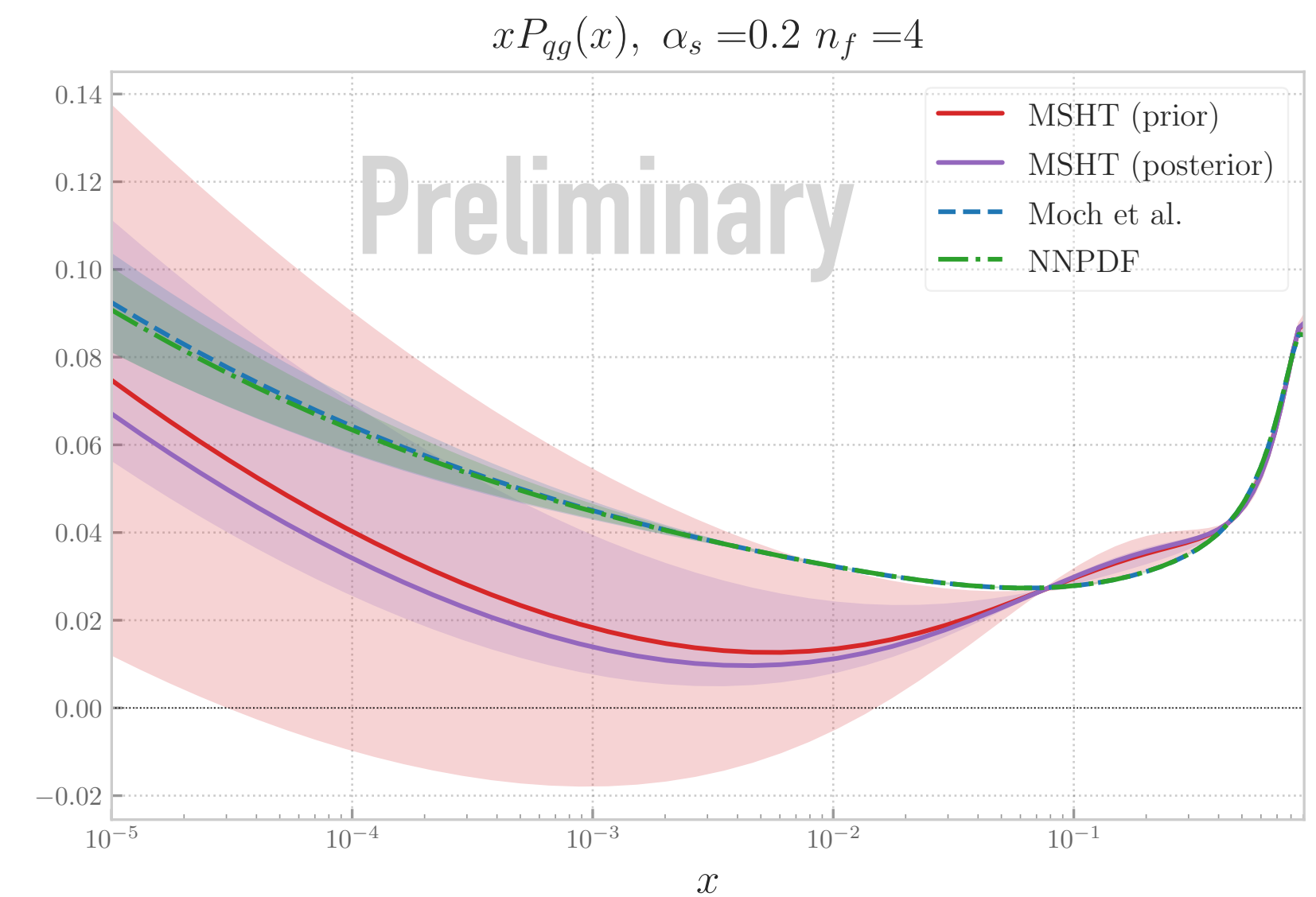
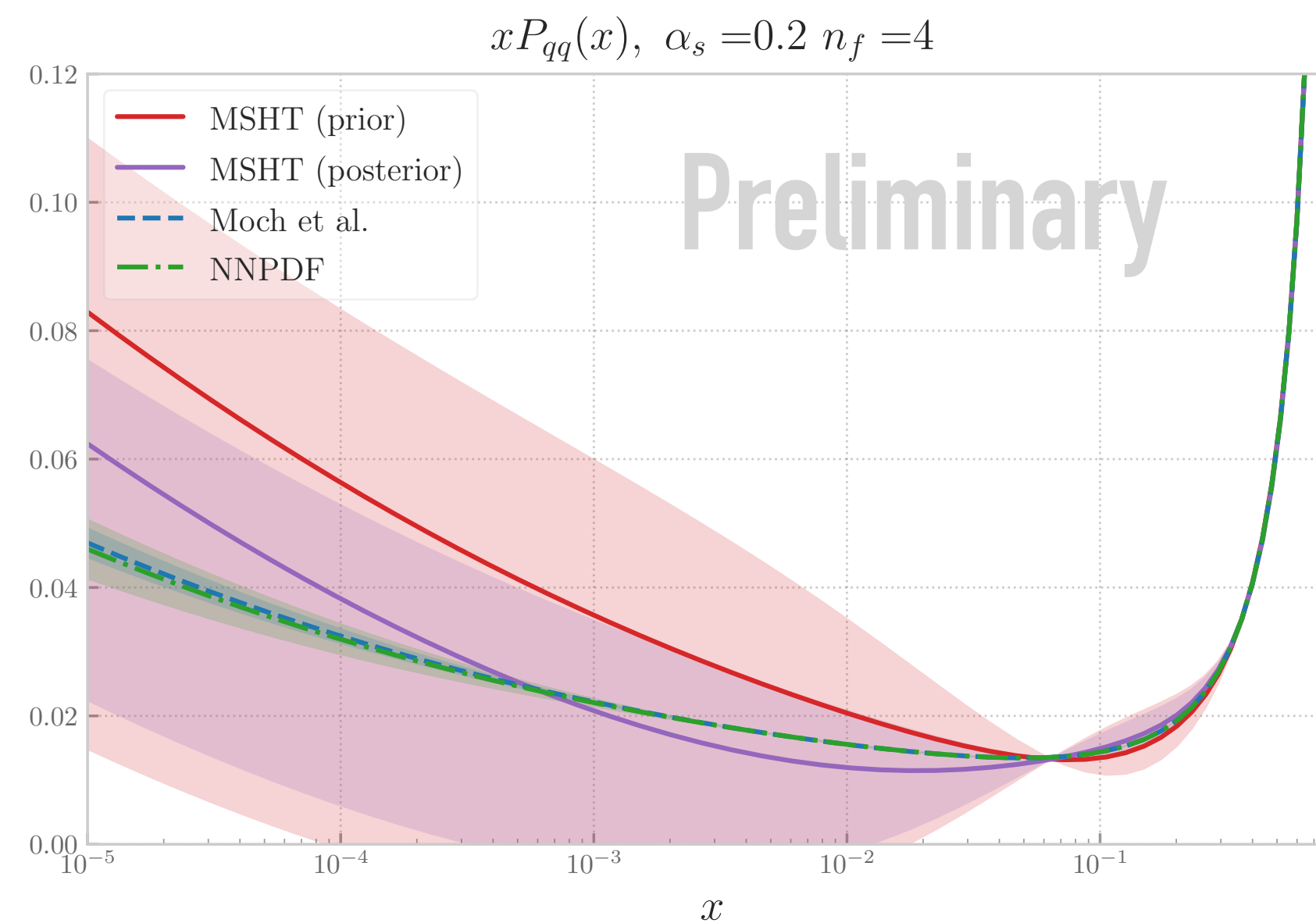
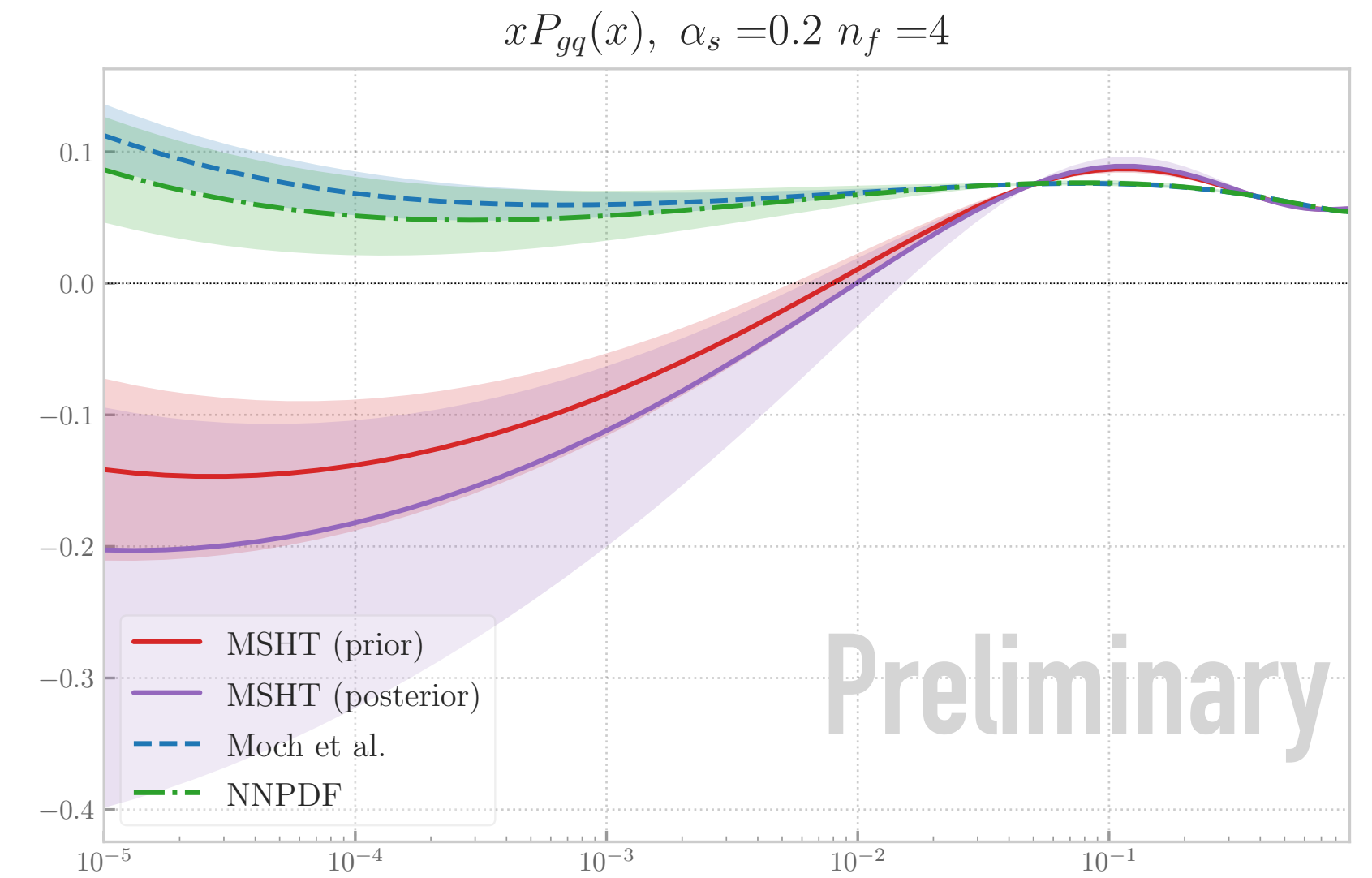
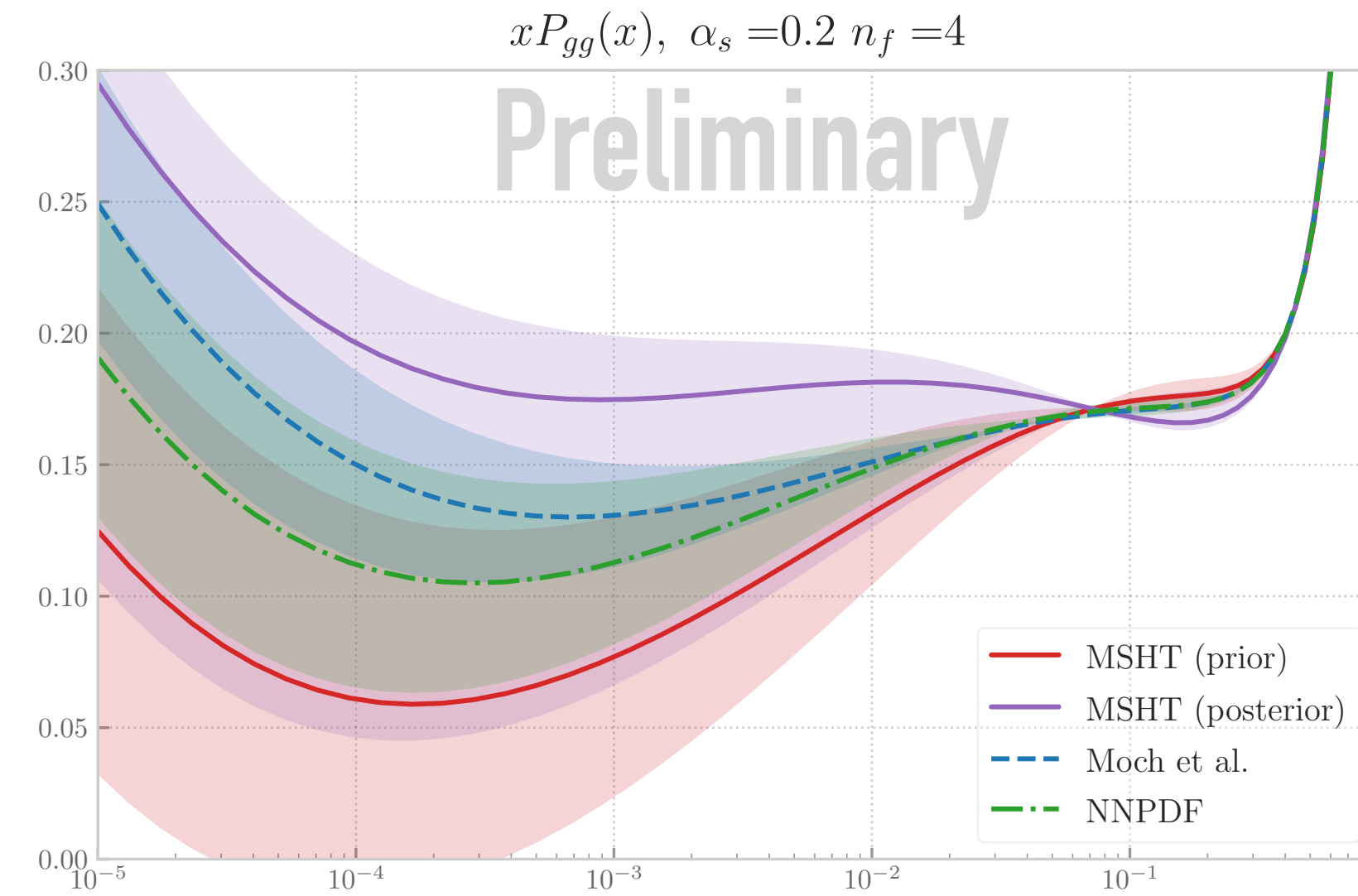
## NNPDF

- More theory inputs published in between and included, in particular 6(1) extra momentum for  $P_{qg}$ ,  $P_{qq}$  ( $P_{gq}$ ,  $P_{gg}$ ), some terms in the large  $n_f$  limit, sub-leading small- $x$  and large- $x$  terms.
- **Only theory inputs** and their variations added to an additional theory covariance matrix associated with incomplete missing higher orders (IHOU)
- MHOU associated with NNLO included via theory covariance matrix



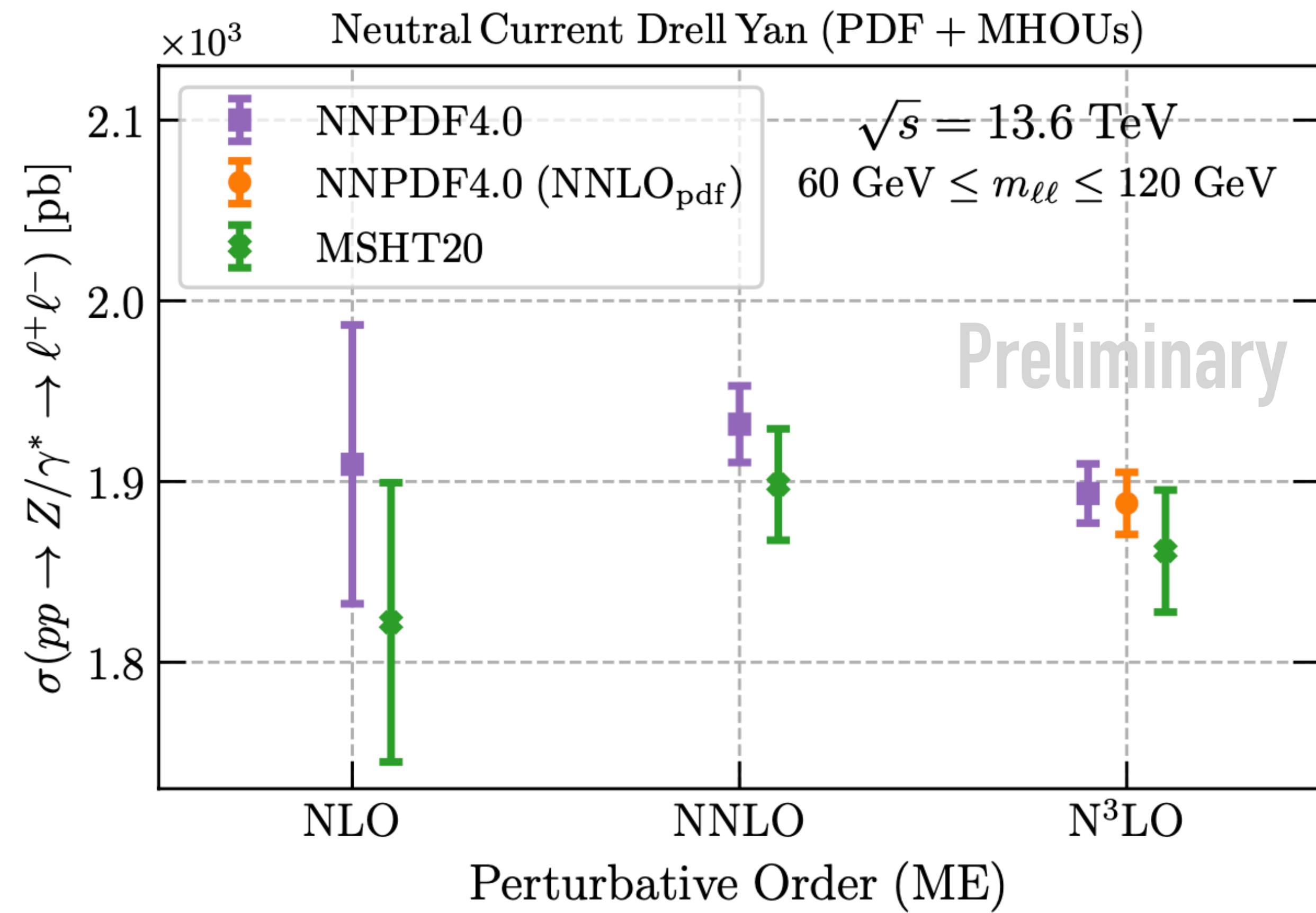
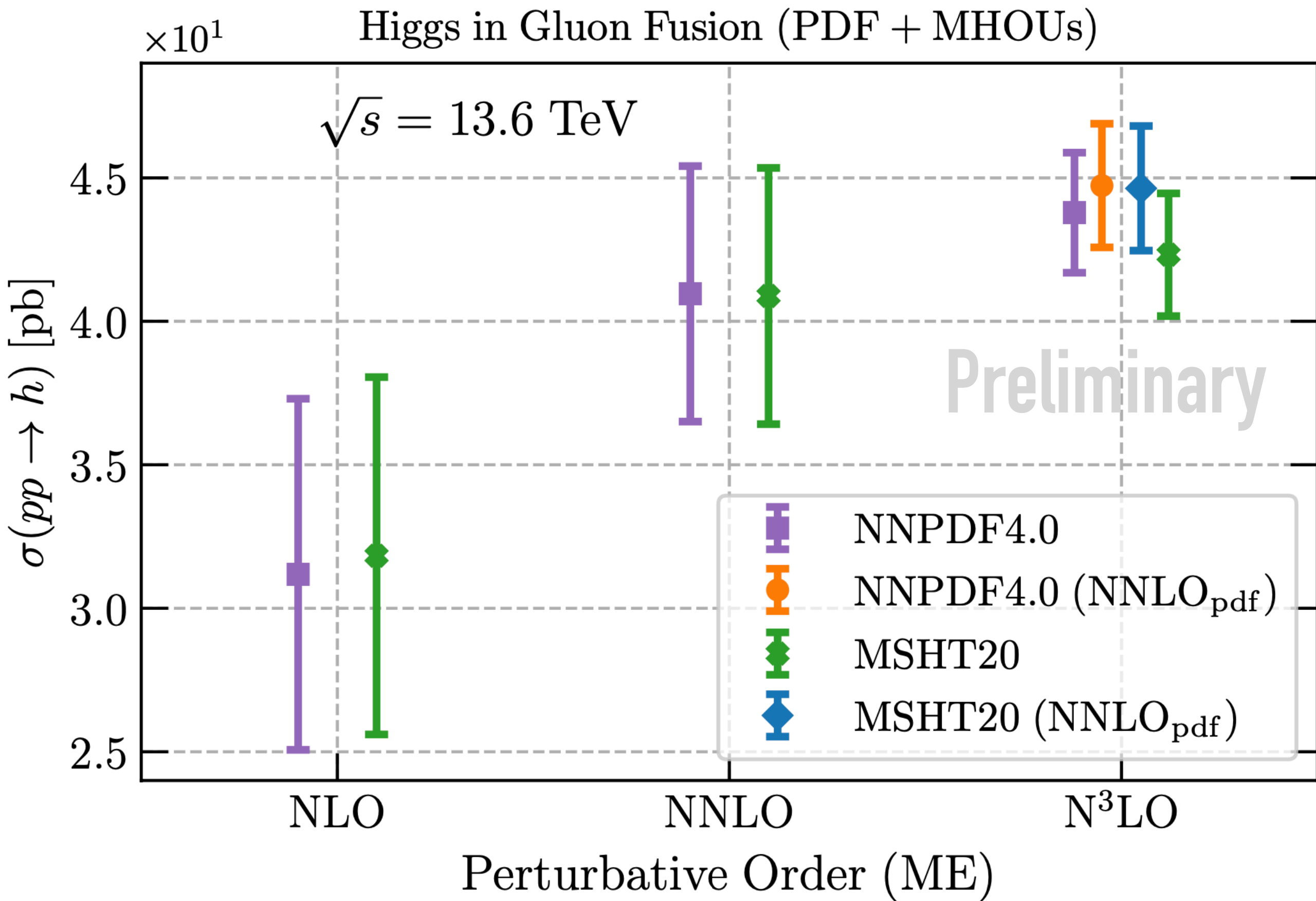
**MSHT prior** = pre-fit variation  
**MSHT posterior** = MSHTaN3LO  
**NNPDF** = NNPDF40aN3LO  
**Moch et al** = theory papers

- Different known ingredients included and different ways of parametrising sub-leading contributions produces different candidates (IHOU)
- Benchmarking exercise started before Summer in Les Houches to check the impact of the aN3LO splitting functions
- Write-up in preparation for Les Houches proceedings





# #1 - APPROXIMATE N3LO PDFS



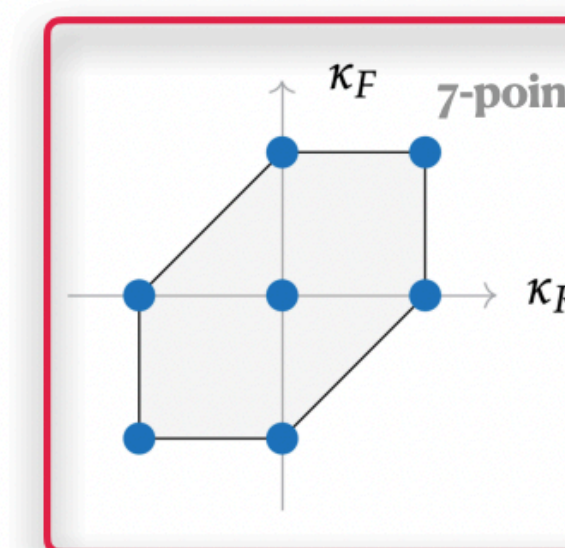
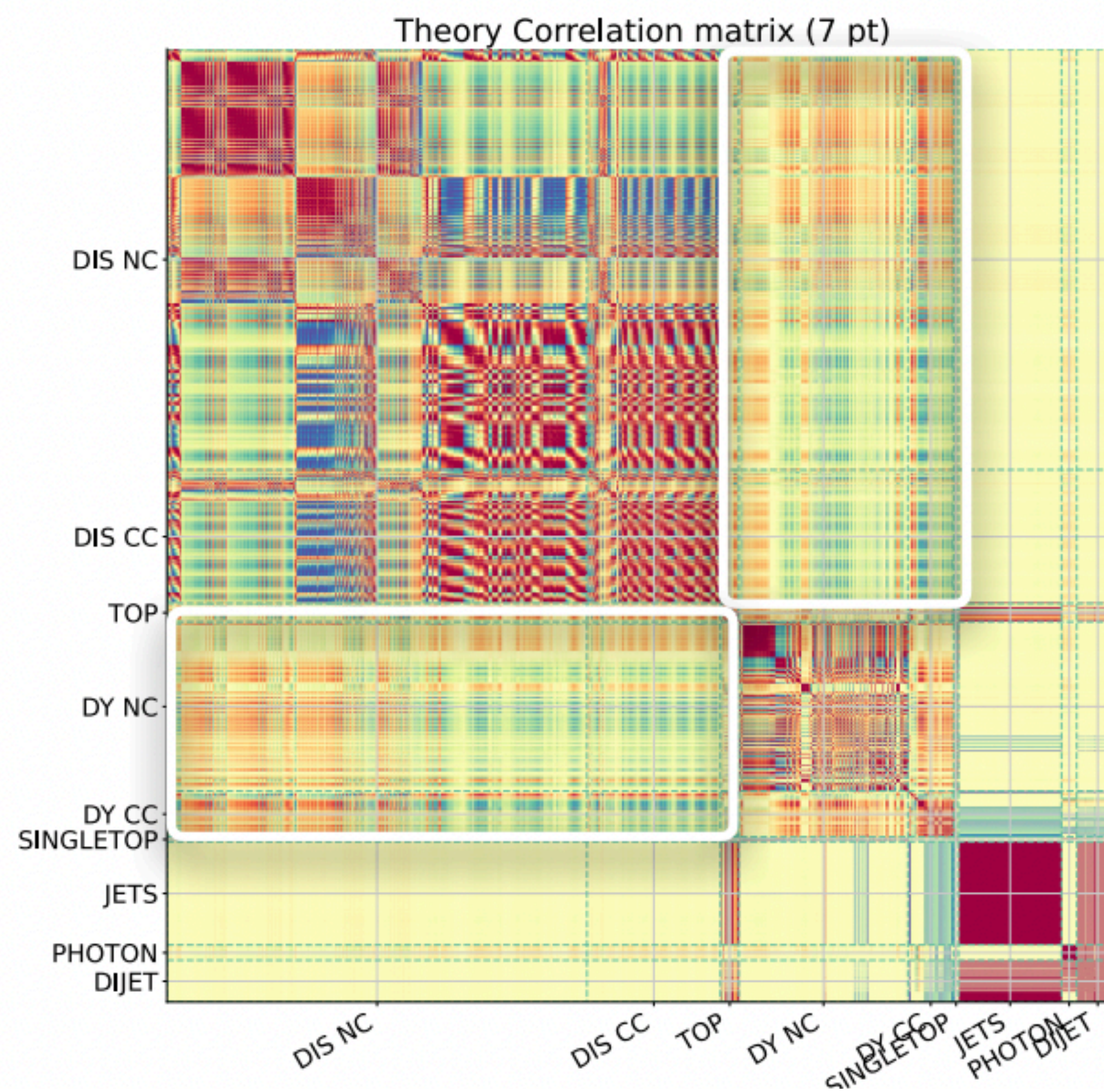
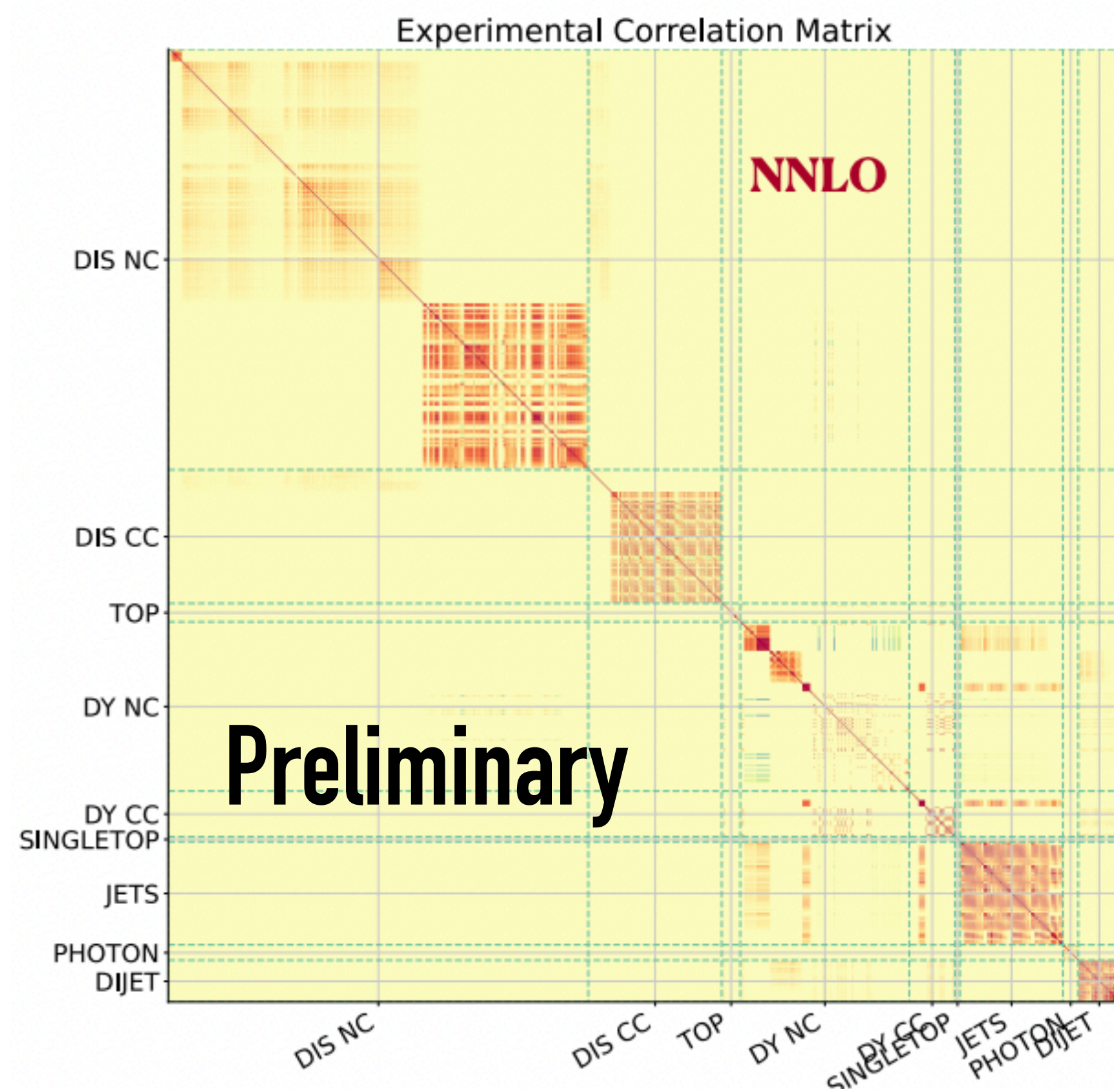


# #2 - MISSING HIGHER ORDER UNCERTAINTIES IN PDF FITS

- ➔ PDF uncertainties only include experimental component: how to include uncertainty associated to truncation of perturbative expansion in theoretical predictions used in PDF fits?
- ➔ One option is to construct a theory covariance matrix from scale-varied cross sections and combine it with the experimental covariance matrix

$$\chi^2 = \sum_{m,n=1}^N (d_m - t_m)(\text{cov}_{\text{exp}} + \text{cov}_{\text{th}})_{mn}^{-1} (d_n - t_n)$$

- Assumptions: experimental and theoretical errors independent and Gaussian



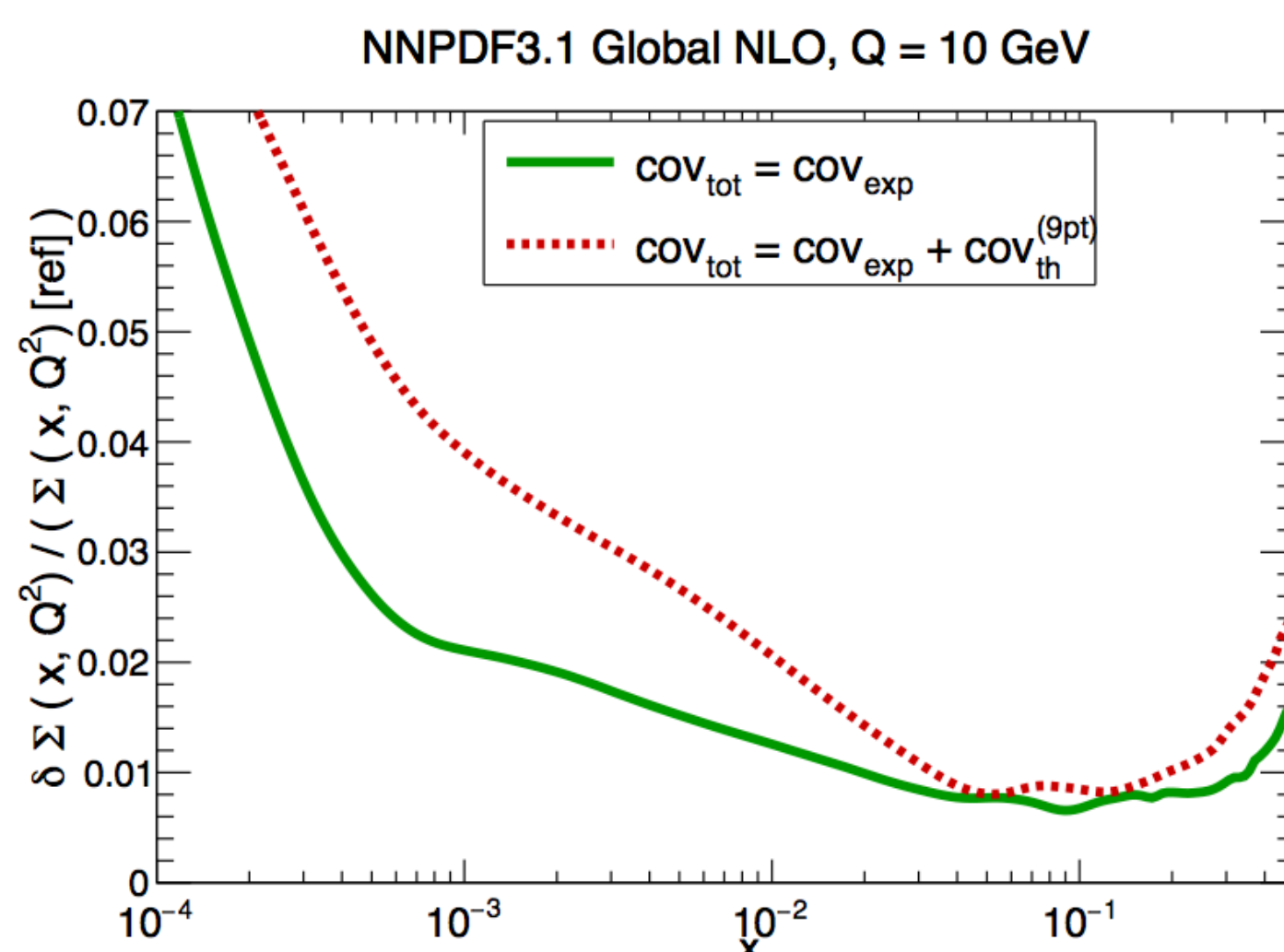
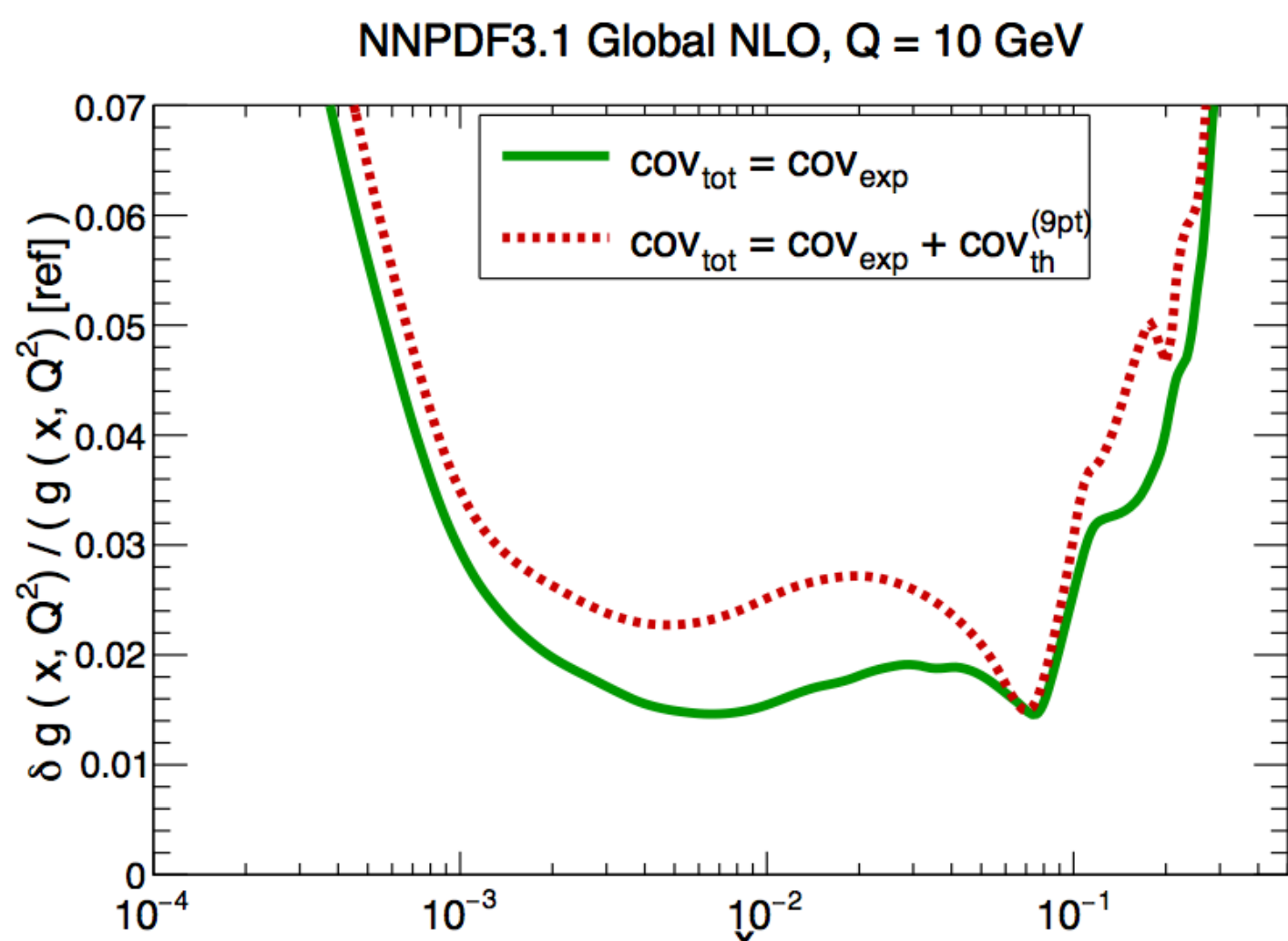
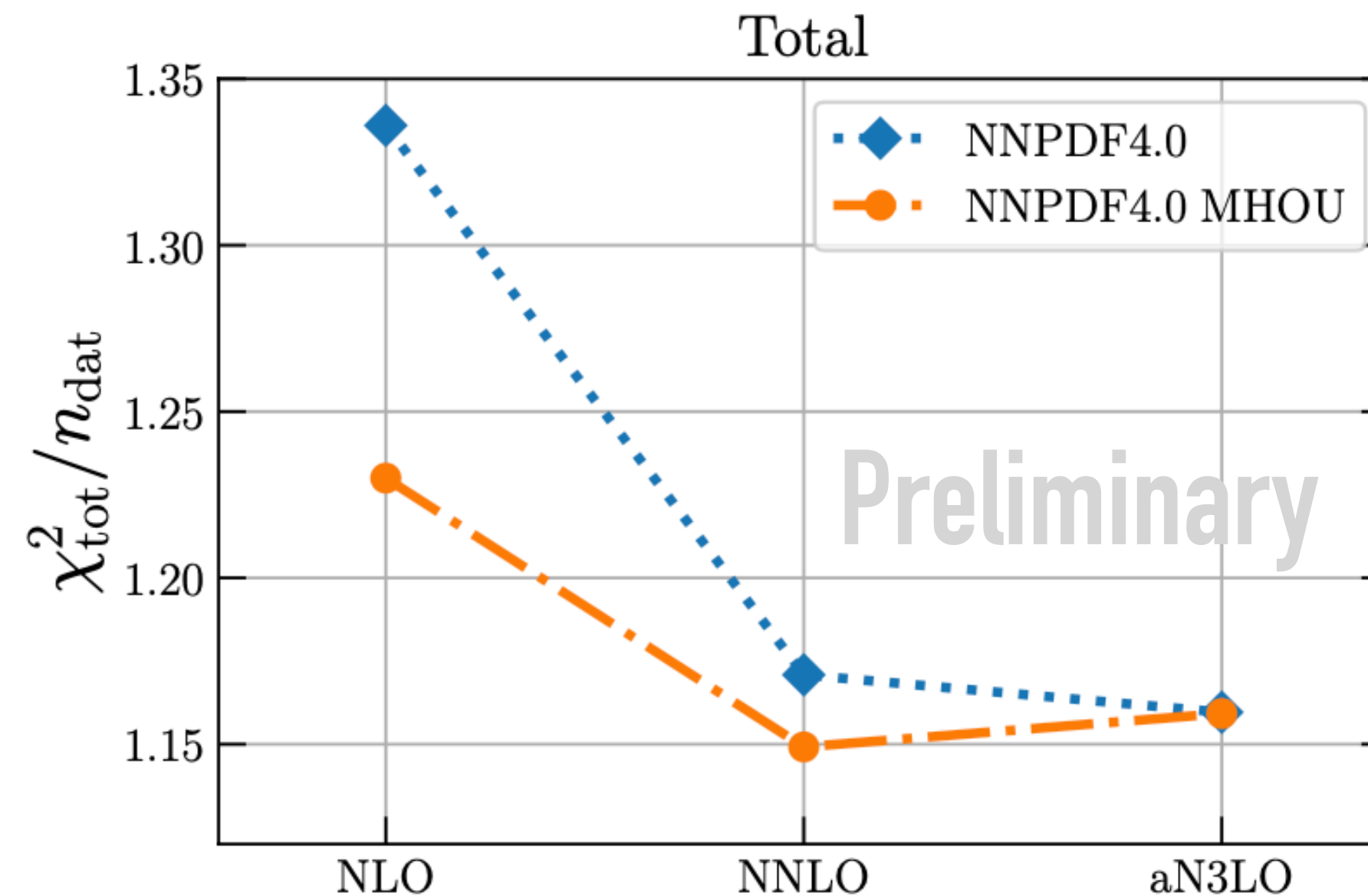
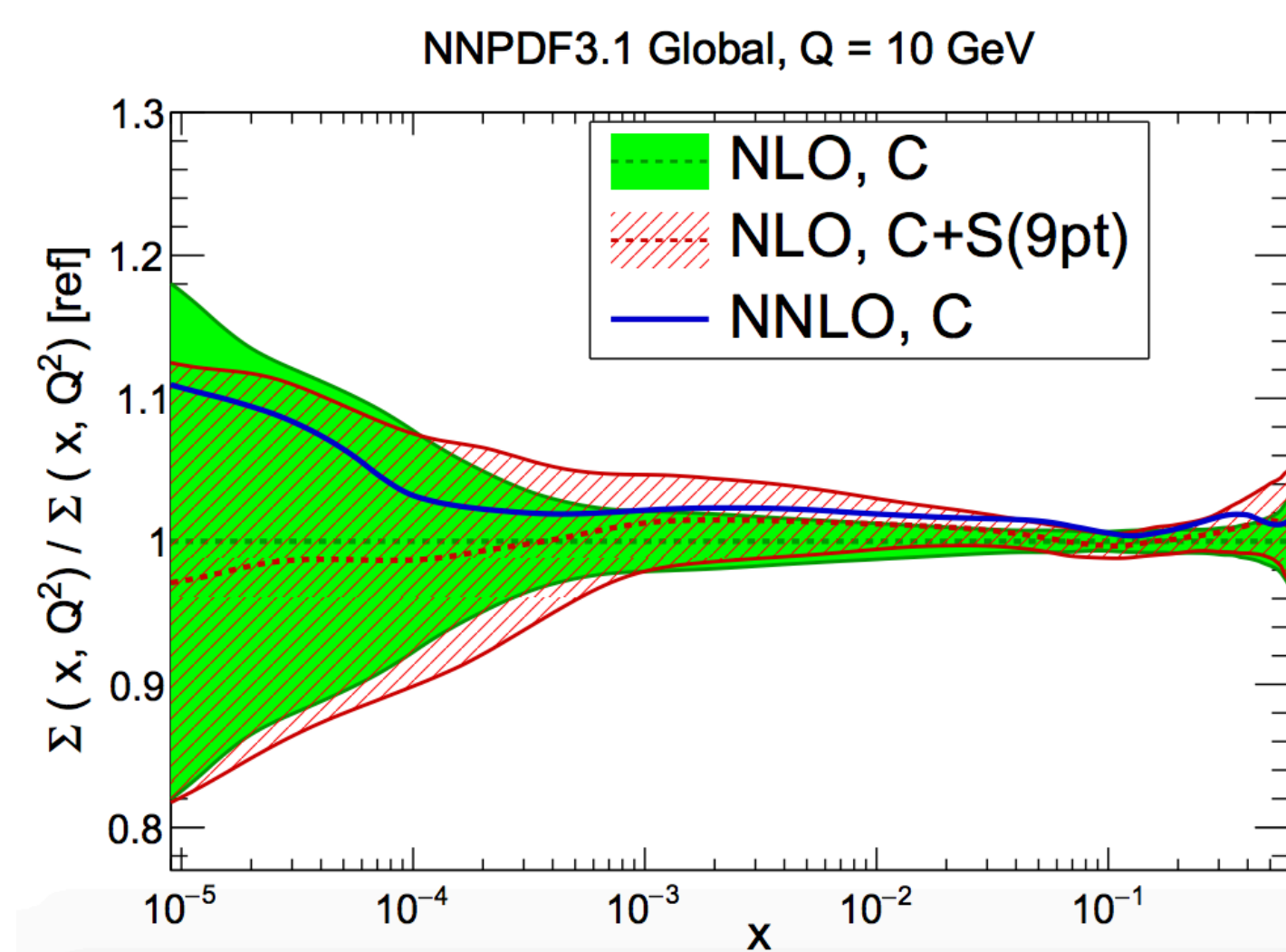
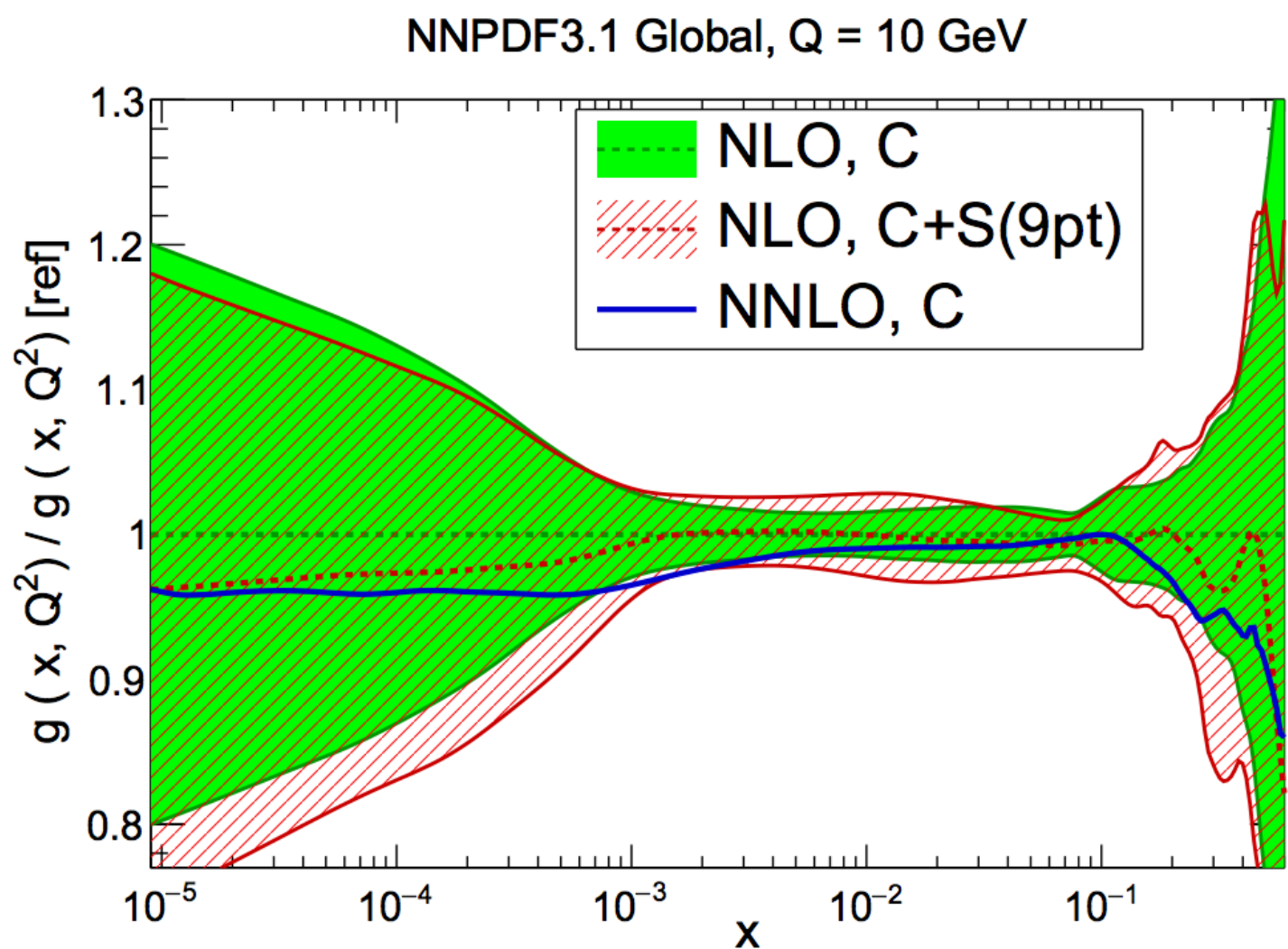
7-pts variation

[NNPDF: 1906.10698]

NNLO paper in preparation



# #2 - MISSING HIGHER ORDER UNCERTAINTIES IN PDF FITS



➔ NNPDF40NNLO with MHOU and NNPDF40aN3LO will be published soon

$$Cov_{ij} = Cov_{ij,EXP} + Cov_{ij,MHOU} + Cov_{ij,IHOU}$$

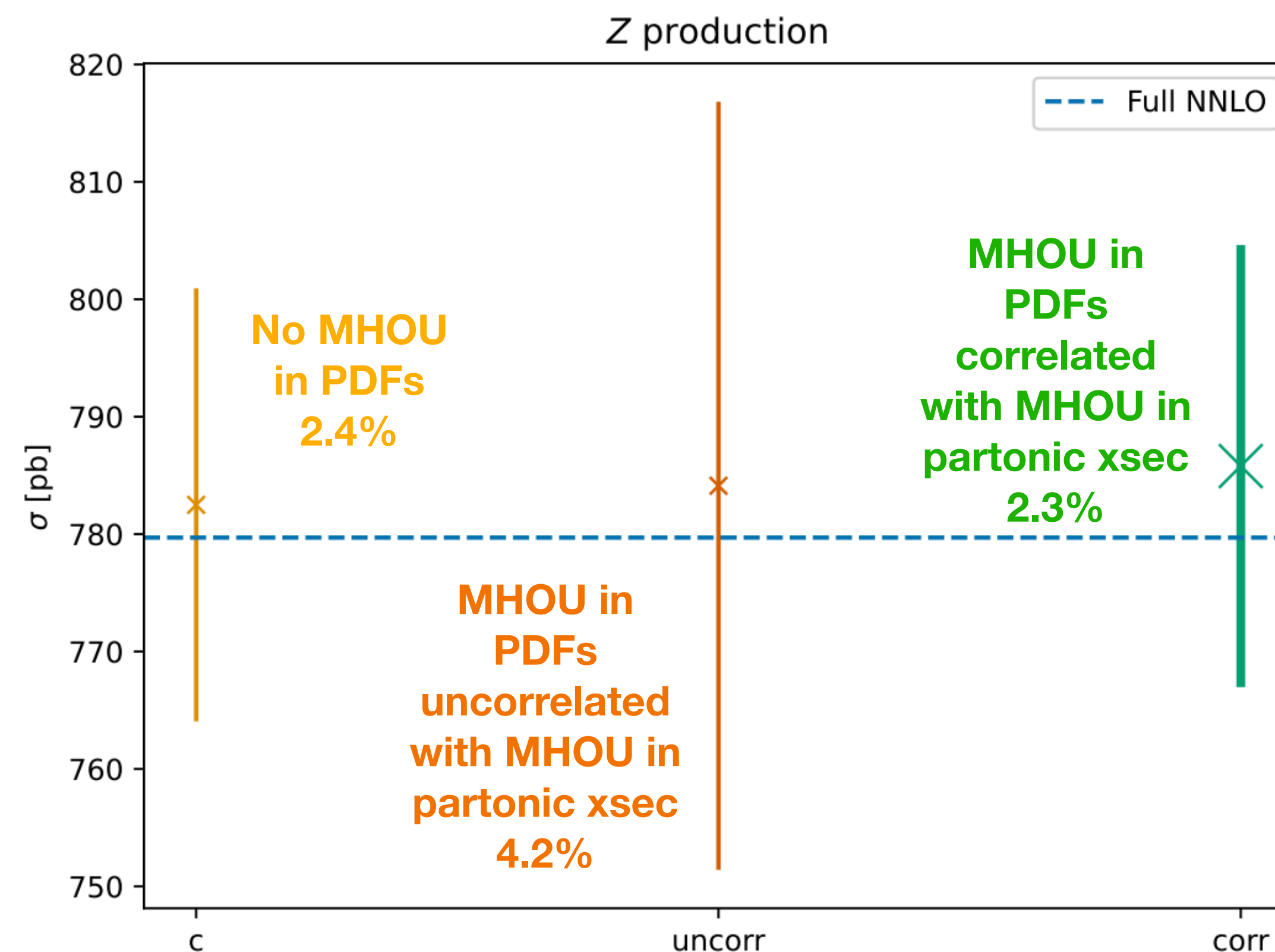
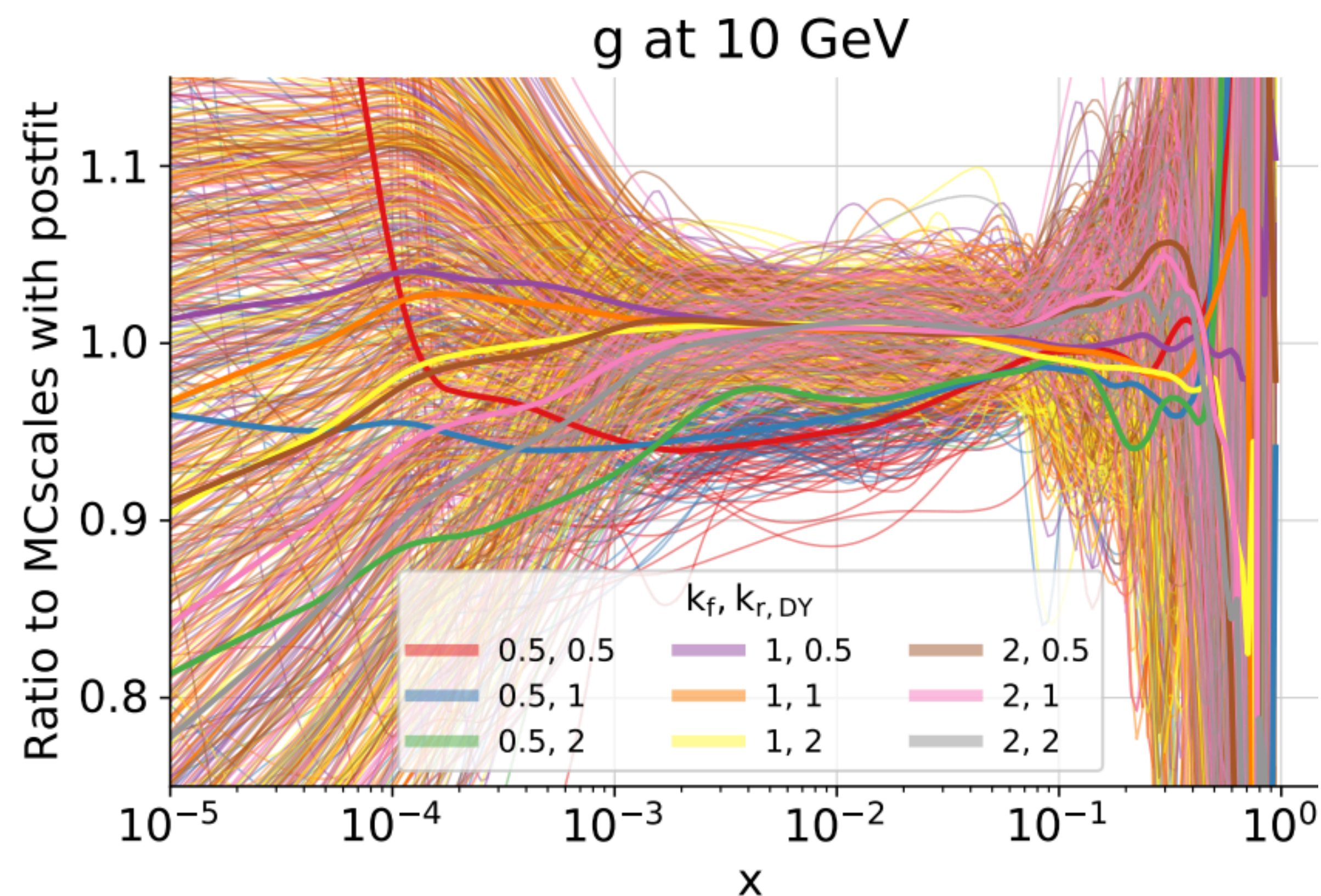
➔ Missing correlation between scale variation in PDF fits and hard cross sections [Harland-Lang, Thorne Eur.Phys.J.C 79 (2019) 3, 225] [Ball, Pearson arXiv:2105.05114]



# #2 - MISSING HIGHER ORDER UNCERTAINTIES IN PDF FITS

- ➔ Alternatively, MCscales [Kassabov et al, 2207.07616]: renormalisation and factorisation scales treated as free parameters of the fixed-order theory, that induce an uncertainty on the theory predictions included in a PDF fit & need to be propagated.
- ➔ Joint sampling of experimental uncertainty (propagated to PDF uncertainty by MC sampling) by specifying a suitable prior probability distribution of all possible scale choices & a-posteriori criterion based on agreement with the data.
- ➔ Can compute full PDF+SCALE uncertainty in cross sections by matching the scales in the hard cross section computation with the scales in the MCscale PDF set: correlation fully taken into account

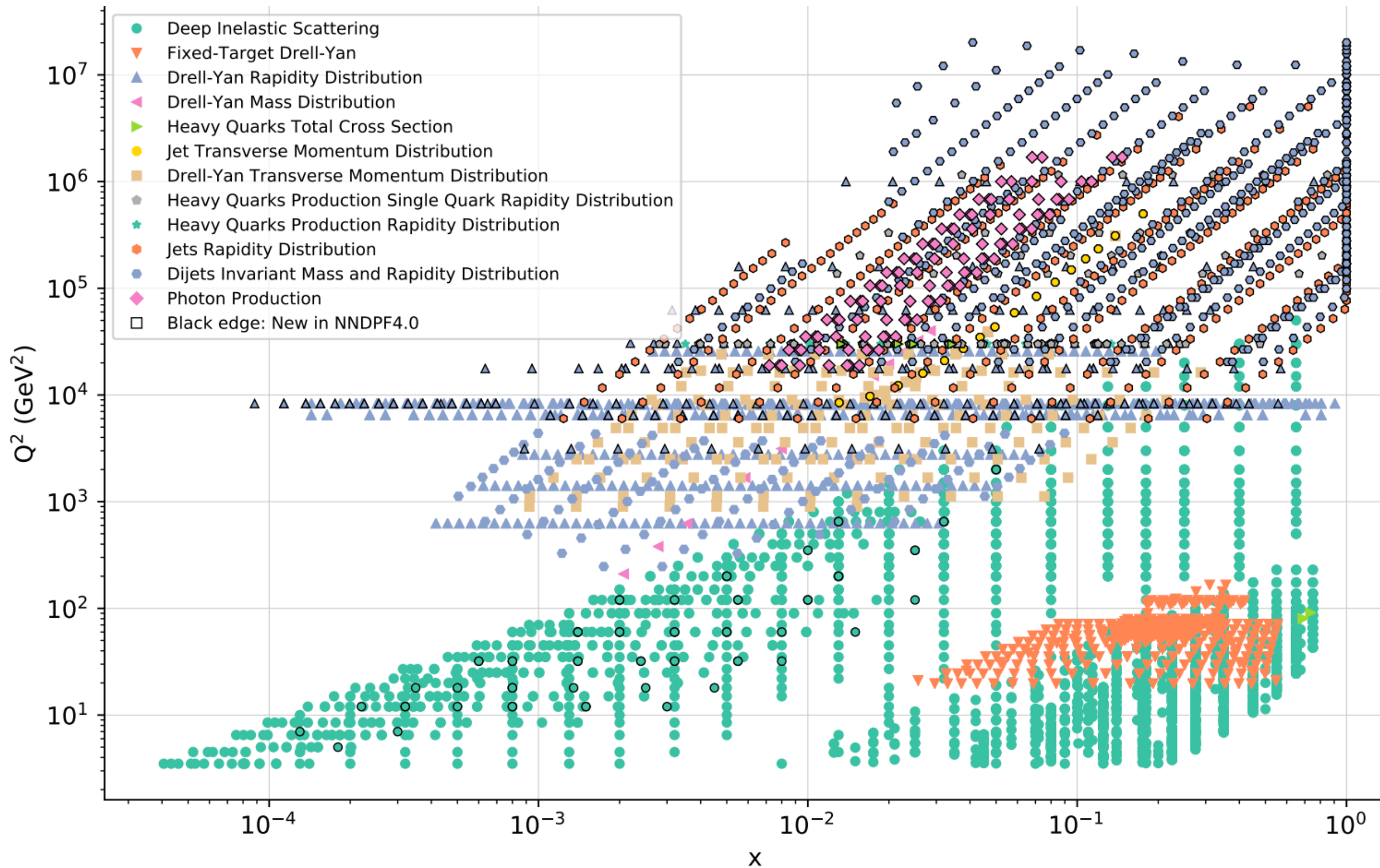
Kassabov et al: 2207.07616]





# #3 – PDF AND NEW PHYSICS INTERPLAY

$$\chi^2 = \frac{1}{N_{\text{dat}}} \sum_{i=1}^{N_{\text{dat}}} (T_i(\{\theta\}, \{c\}) - D_i) \text{cov}_{ij}^{-1} (T_j(\{\theta\}, \{c\}) - D_j)$$



$$T_i(\{\theta\}, \{c\}) = \text{PDFs}(\{\theta\}, \{c\}) \otimes \hat{\sigma}_i(\{c\})$$



(B)SM parameters:  $\alpha_s(M_Z), M_W, \theta_W, \text{SMEFT WCs} \dots$

Parameters determining PDFs at initial scale

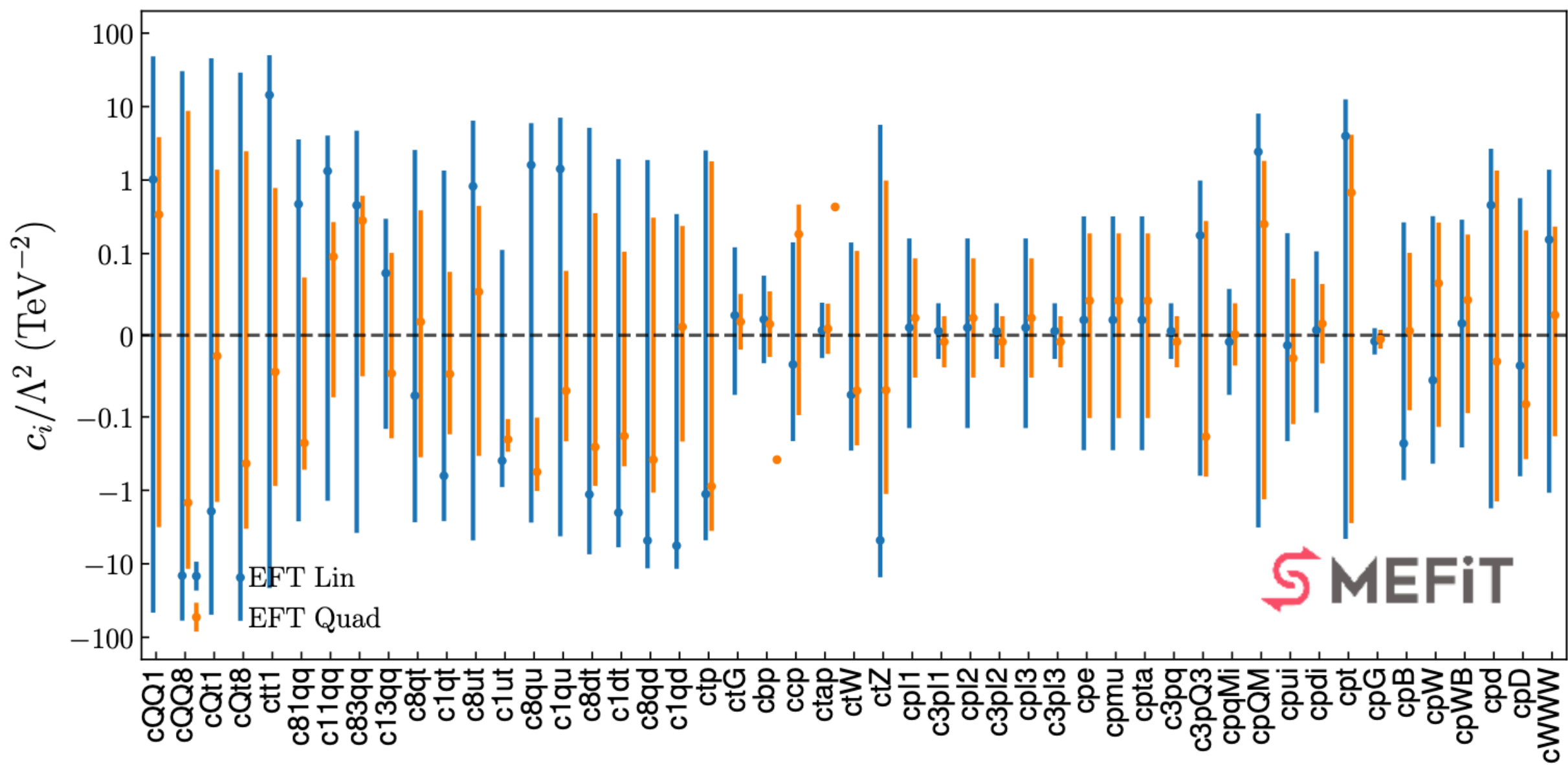
✓ In a PDF fit typically

$$T_i(\{\theta\}) = \text{PDFs}(\{\theta\}, \{c = \bar{c}\}) \otimes \hat{\sigma}_i(\{c = \bar{c}\})$$



$$\chi^2 = \frac{1}{N_{\text{dat}}} \sum_{i=1}^{N_{\text{dat}}} (T_i(\{\theta\}, \{c\}) - D_i) \text{cov}_{ij}^{-1} (T_j(\{\theta\}, \{c\}) - D_j)$$

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i}{\Lambda^2} \mathcal{O}_i^{(6)} + \dots$$



$$T_i(\{\theta\}, \{c\}) = \text{PDFs}(\{\theta\}, \{c\}) \otimes \hat{\sigma}_i(\{c\})$$



(B)SM parameters:  $\alpha_s(M_Z), M_W, \theta_W, \text{SMEFT WCs} \dots$

Parameters determining PDFs at initial scale

✓ In a PDF fit typically

$$T_i(\{\theta\}) = \text{PDFs}(\{\theta\}, \{c = \bar{c}\}) \otimes \hat{\sigma}_i(\{c = \bar{c}\})$$

✓ In a fit of (B)SM parameters

$$T_i(\{c\}) = \text{PDFs}(\{\bar{\theta}\}, \{\bar{c}\}) \otimes \hat{\sigma}_i(\{c\})$$

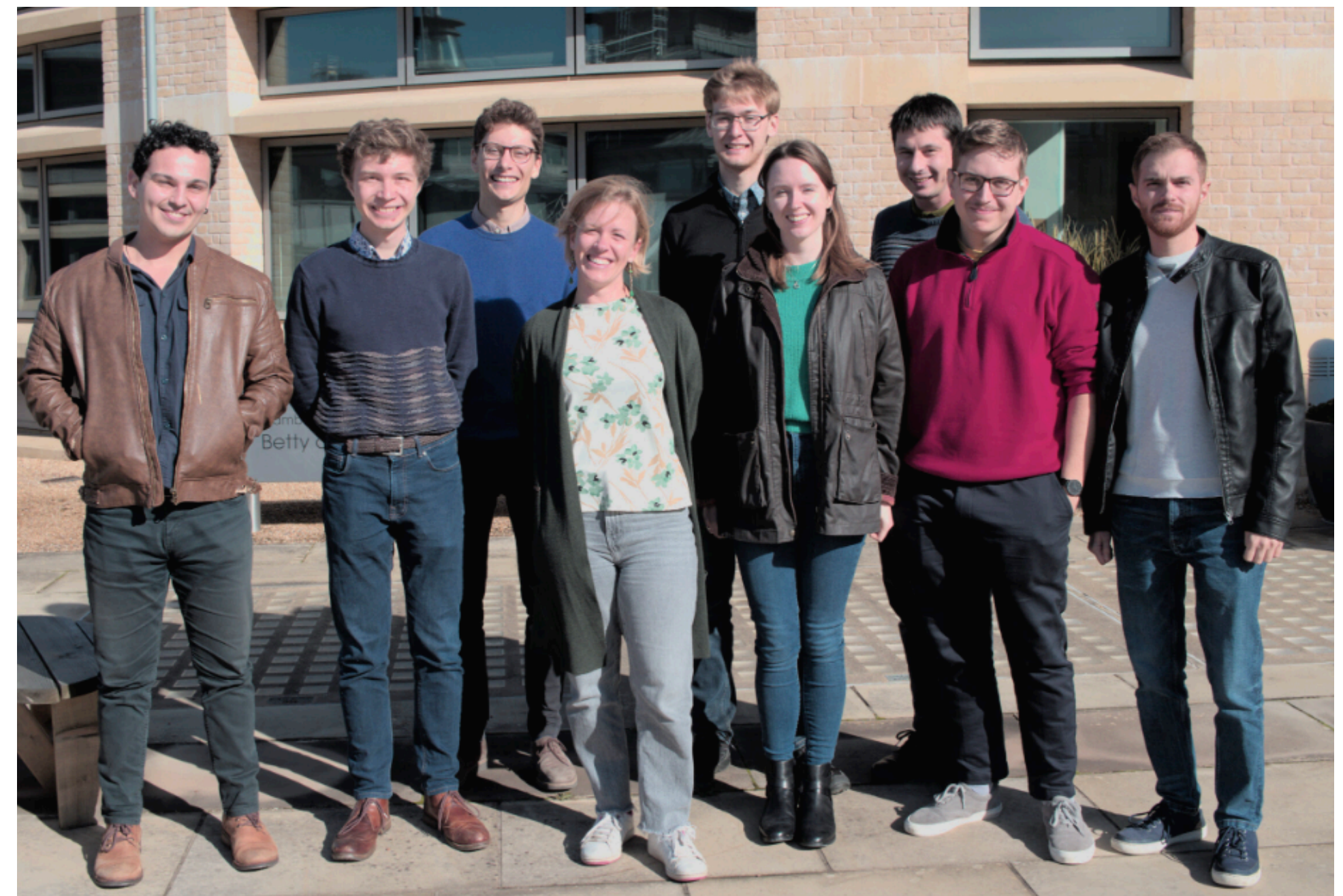


# #3 – PDF AND NEW PHYSICS INTERPLAY

- From the point of view of PDF fits:
  - ➔ How to make sure that new physics effects are not inadvertently fitted away in a PDF fit?
- From the point of view of SMEFT fits:
  - ➔ Should I make sure I am using a clean set of PDFs in a SMEFT analysis? How to define it? Is it enough?
  - ➔ How would the bounds change if I was consistently using PDFs that include in the fit the same operators that I am fitting?

PBSP 

MU + Z. Kassabov, M. Madigan,  
L. Mantani, J. Moore, M.  
Morales Alvarado, E. Hammou,  
M. Costantini






# #3 – PDF AND NEW PHYSICS INTERPLAY

- From the point of view of PDF fits:

➔ How to make sure that new physics effects are not inadvertently fitted away in a PDF fit?

- ◆ With current experiments, at the HL-LHC found a model involving a new heavy  $W'$  that would affect high energy Drell-Yan tails. If there was a new heavy  $W'$  PDF fits would have same quality but PDFs (hence theory predictions at LHC) would be significantly different. Large- $x$  PDFs would absorb New Physics in this case!
- ◆ Need orthogonal input from low-energy experiments!



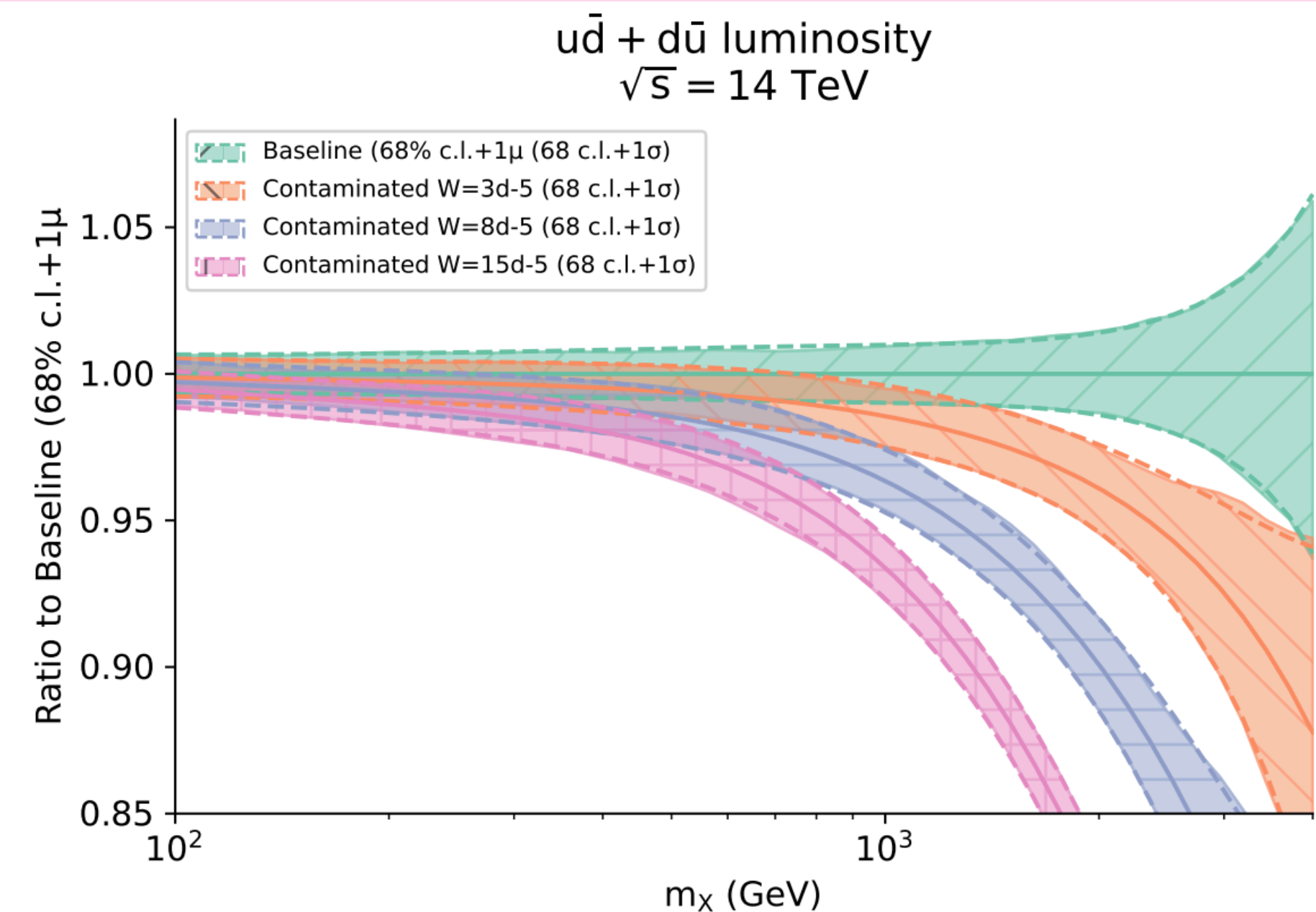
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 PUBLISHED: November 16, 2023

## Hide and seek: how PDFs can conceal new physics

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Elie Hammou,<sup>a</sup> Zahari Kassabov,<sup>a</sup> Maeve Madigan,<sup>b</sup> Michelangelo L. Mangano,<sup>c</sup>  
 Luca Mantani,<sup>a</sup> James Moore,<sup>a</sup> Manuel Morales Alvarado<sup>a</sup> and Maria Ubiali<sup>a</sup>





# #3 – PDF AND NEW PHYSICS INTERPLAY

- From the point of view of PDF fits:
  - ➔ How to make sure that new physics effects are not inadvertently fitted away in a PDF fit?
- From the point of view of SMEFT fits:
  - ➔ Should I make sure I am using a clean set of PDFs in a SMEFT analysis? How to define it? Is it enough?
  - ➔ How would the bounds change if I was consistently using PDFs that include in the fit the same operators that I am fitting?

$$d\sigma^{pp \rightarrow ab} = \sum_{i,j} \boxed{f_i \otimes f_j \otimes d\hat{\sigma}^{ij \rightarrow ab}} + \dots$$

↑  $f(\{\theta_k\})$       ↑  $\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i}{\Lambda^2} \mathcal{O}_i^{(6)} + \dots$

➔ Simultaneous fits of SMEFT and PDFs

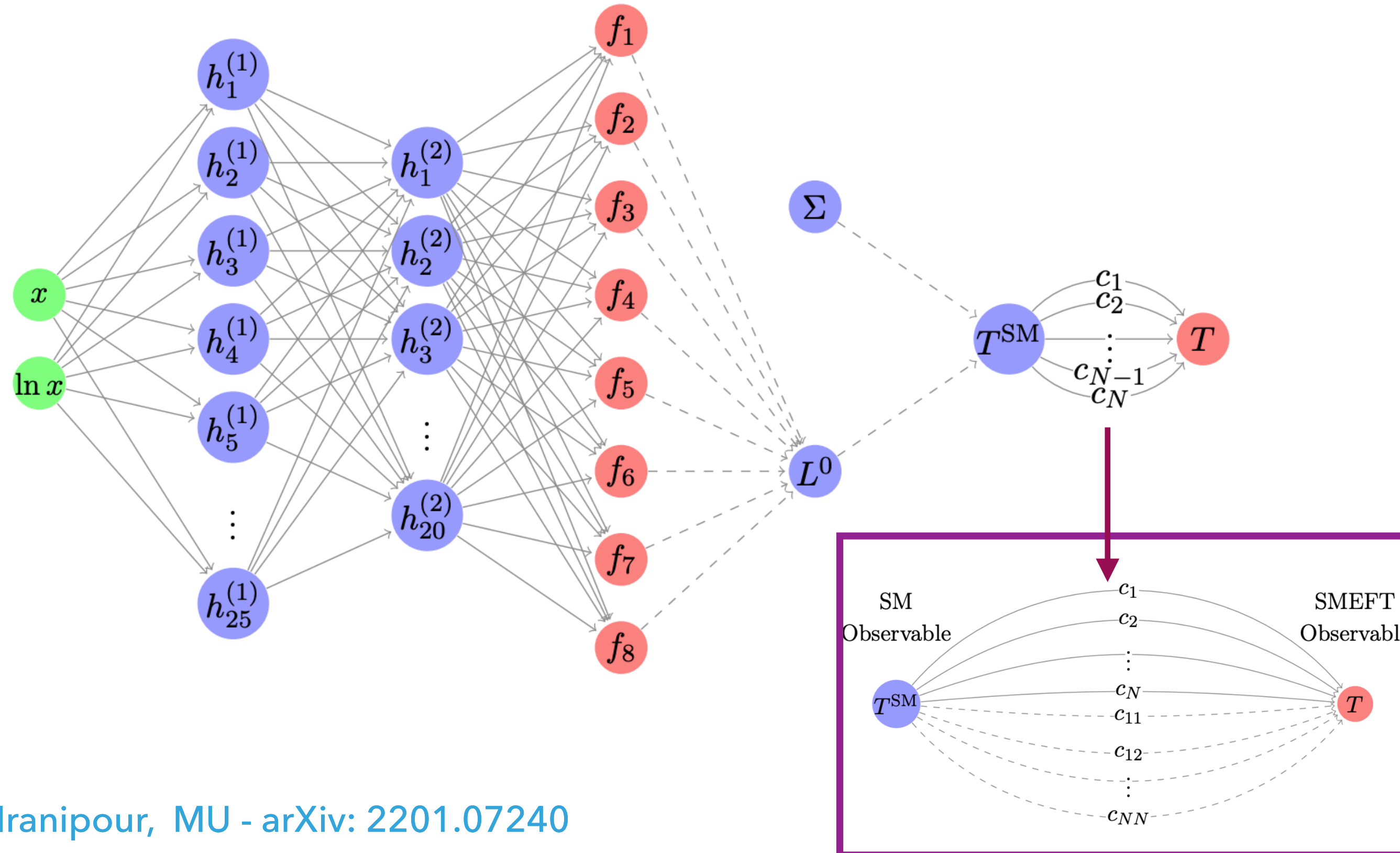
$T(\{\theta_k\}, \{c_i\})$



# #3 – PDF AND NEW PHYSICS INTERPLAY

- How to perform simultaneous fits?
- SimuNET [soon available open-source] yields simultaneous fit of PDFs and SMEFT coefficients, it does not have limit in number of parameters that can be fitted alongside PDFs at the initial scale!

Input layer    Hidden layer 1    Hidden layer 2    PDF flavours    Convolution step    SM Observable    SMEFT Observable



Linear dim-6 operator

$$T(\hat{\theta}) = \Sigma(\{c_n\}) \cdot L^0(\theta) = T^{\text{SM}}(\theta) \cdot \left( 1 + \sum_{n=1}^N c_n R_{\text{SMEFT}}^{(n)} \right)$$

$$T^{\text{SM}}(\theta) = \Sigma^{\text{SM}} \cdot L^0(\theta)$$

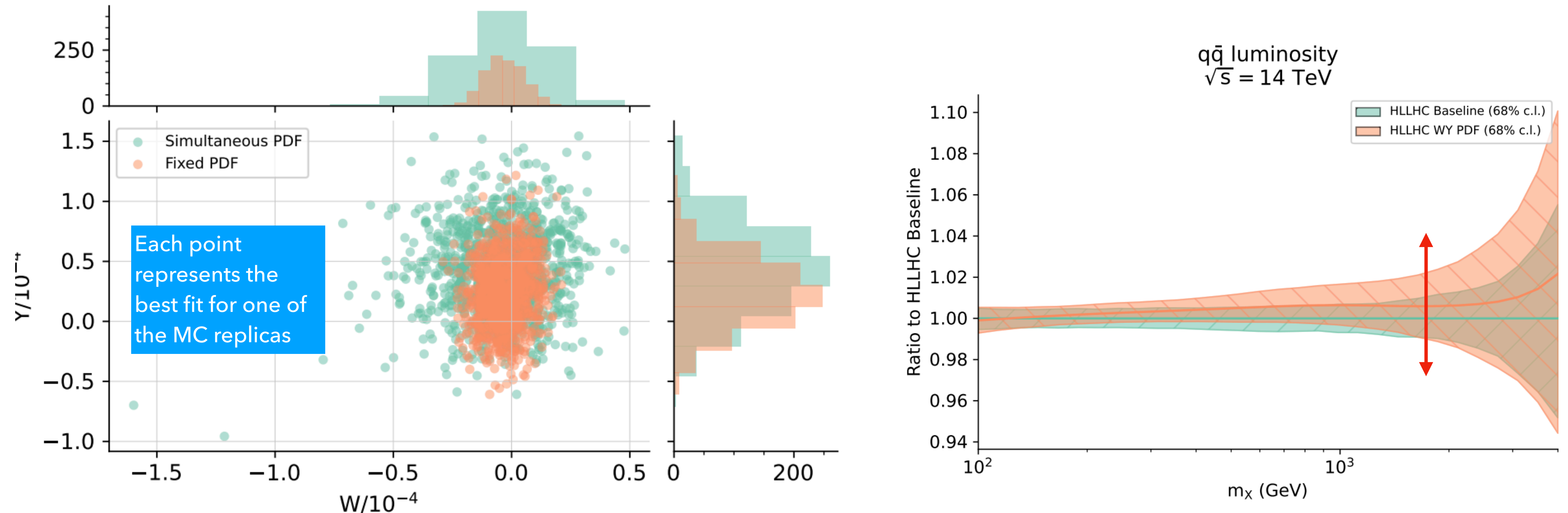
Quadratic dim-6 operator

$$T(\hat{\theta}) = T^{\text{SM}}(\theta) \cdot \left( 1 + \sum_{n=1}^N c_n R_{\text{SMEFT}}^{(n)} + \sum_{1 \leq n \leq m \leq N} c_{nm} R_{\text{SMEFT}}^{(n,m)} \right)$$

$c_n c_m$



# #3 – PDF AND NEW PHYSICS INTERPLAY

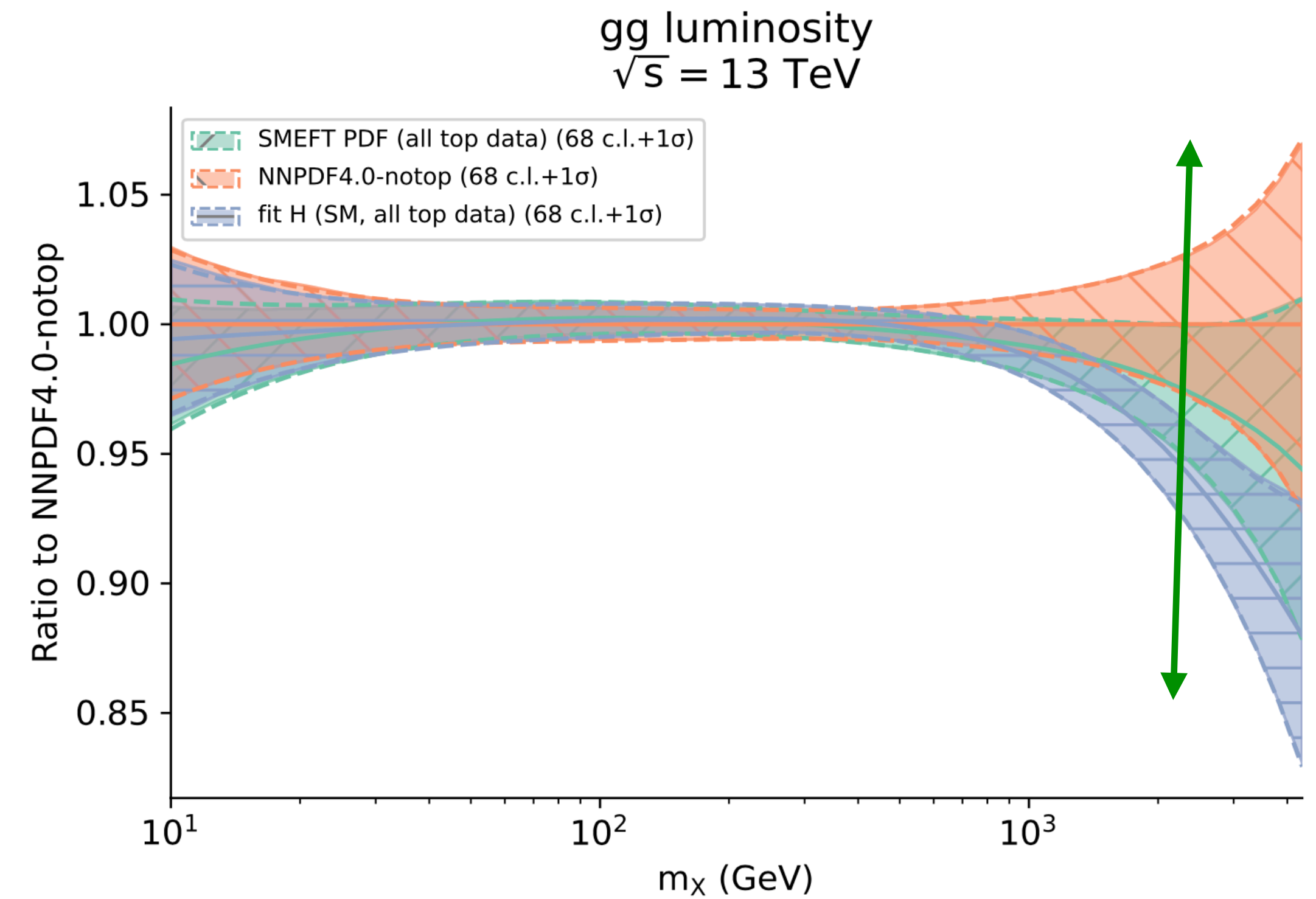
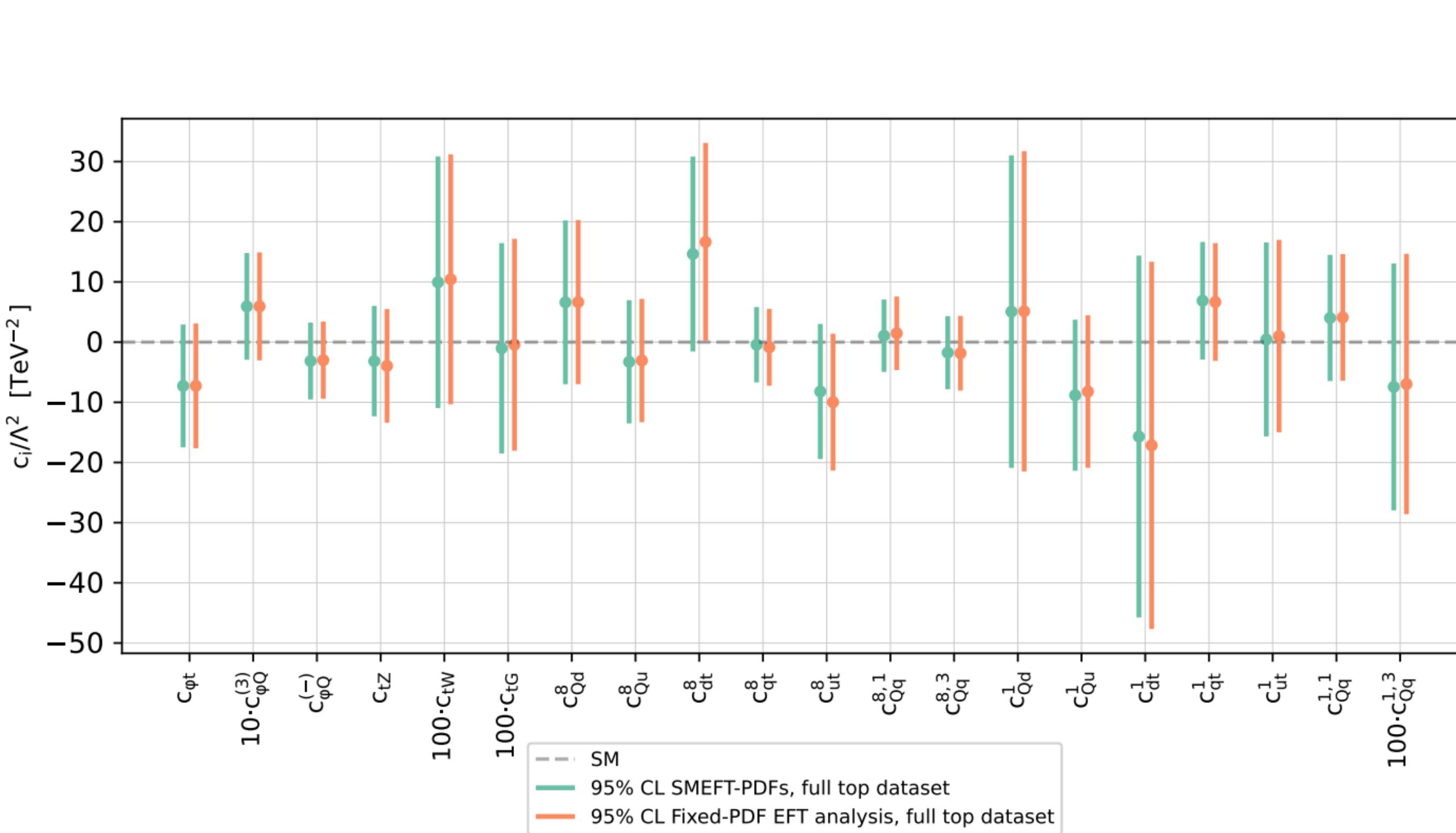


S. Iranipour, MU - arXiv: 2201.07240

- ✓ Simultaneous analysis of PDFs and **Drell-Yan sector** Wilson coefficient of DIS + DY (including HL-LHC projections) using simuNET method shows that at HL-LHC the effect of interplay becomes important as WCs bounds broaden and PDF uncertainties change significantly once SMEFT effects allowed in theory predictions entering PDF fit



# #3 – PDF AND NEW PHYSICS INTERPLAY



Z. Kassabov, M. Madigan, L. Mantani, J. Moore, M. Morales, J. Rojo, MU - arXiv: 2303.06159

✓ Simultaneous analysis of PDFs and more than 20 operators in the **top sector** using simuNET method shows that WCs are stable, while PDF uncertainties broaden and PDF fitted simultaneously alongside WCs sit nicely between PDF-only fit without top data and PDF fit including all top data



# CONCLUSIONS AND OUTLOOK

- In an era of precision, need precise and accurate PDFs
- Lots of progress in theoretical framework: aN3LO PDFs, inclusion of MHOUs in PDF error bands
- No time to mention QED sets and intrinsic charm studies
- New exciting avenues being explored, for example interplay between new Physics and PDFs, hinting to complementarity of low-energy experiments/lattice to determine large- $x$  PDFs (EIC, FFP)

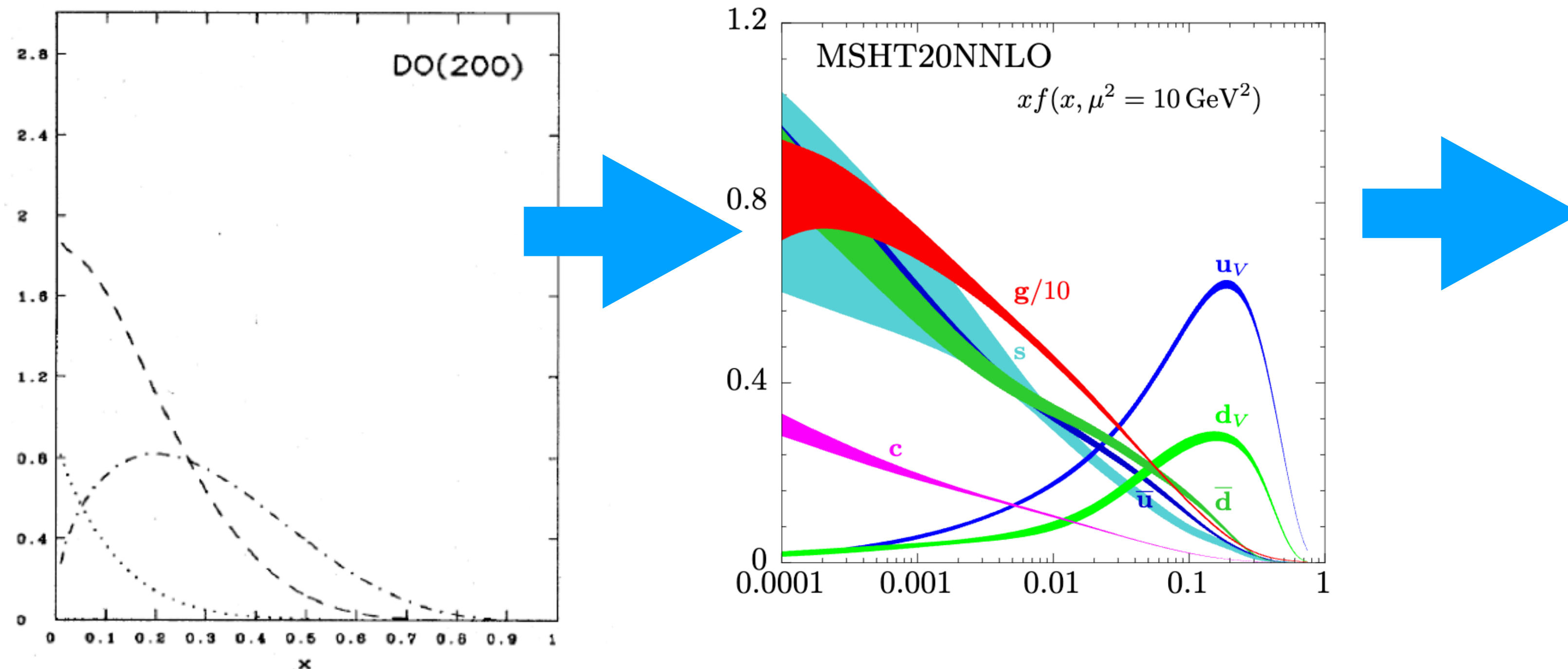


FIG. 27. “Soft-gluon” ( $\Lambda = 200 \text{ MeV}$ ) parton distributions of Duke and Owens (1984) at  $Q^2 = 5 \text{ GeV}^2$ : valence quark distribution  $x[u_v(x) + d_v(x)]$  (dotted-dashed line),  $xG(x)$  (dashed line), and  $q_v(x)$  (dotted line).



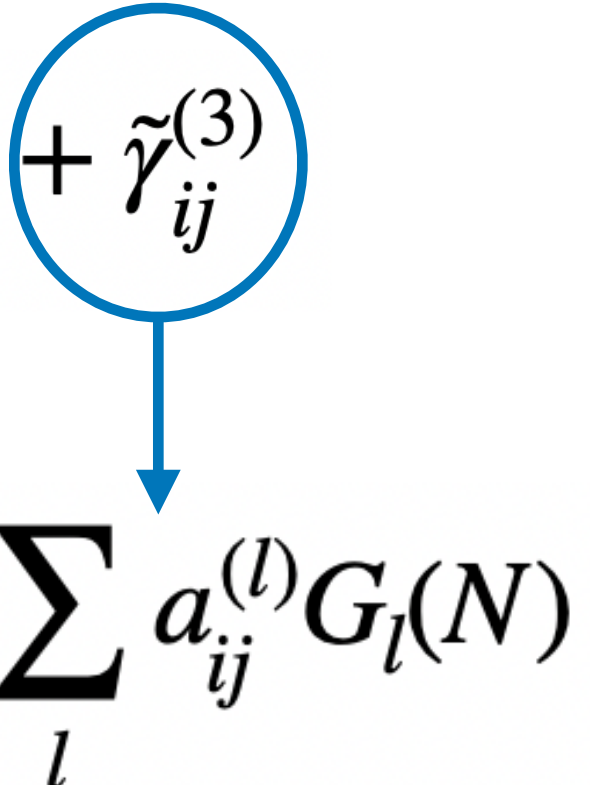
**EXTRA MATERIAL**

---



- How to combine the known existing limits?

In Mellin space, for each power of  $n_f$

$$\gamma_{ij}^{(3)} = \gamma_{ij,n_f^3}^{(3)} + \gamma_{ij,N \rightarrow \infty}^{(3)} + \gamma_{ij,N \rightarrow 0}^{(3)} + \tilde{\gamma}_{ij}^{(3)}$$


$$\tilde{\gamma}_{ij} = \sum_l a_{ij}^{(l)} G_l(N)$$

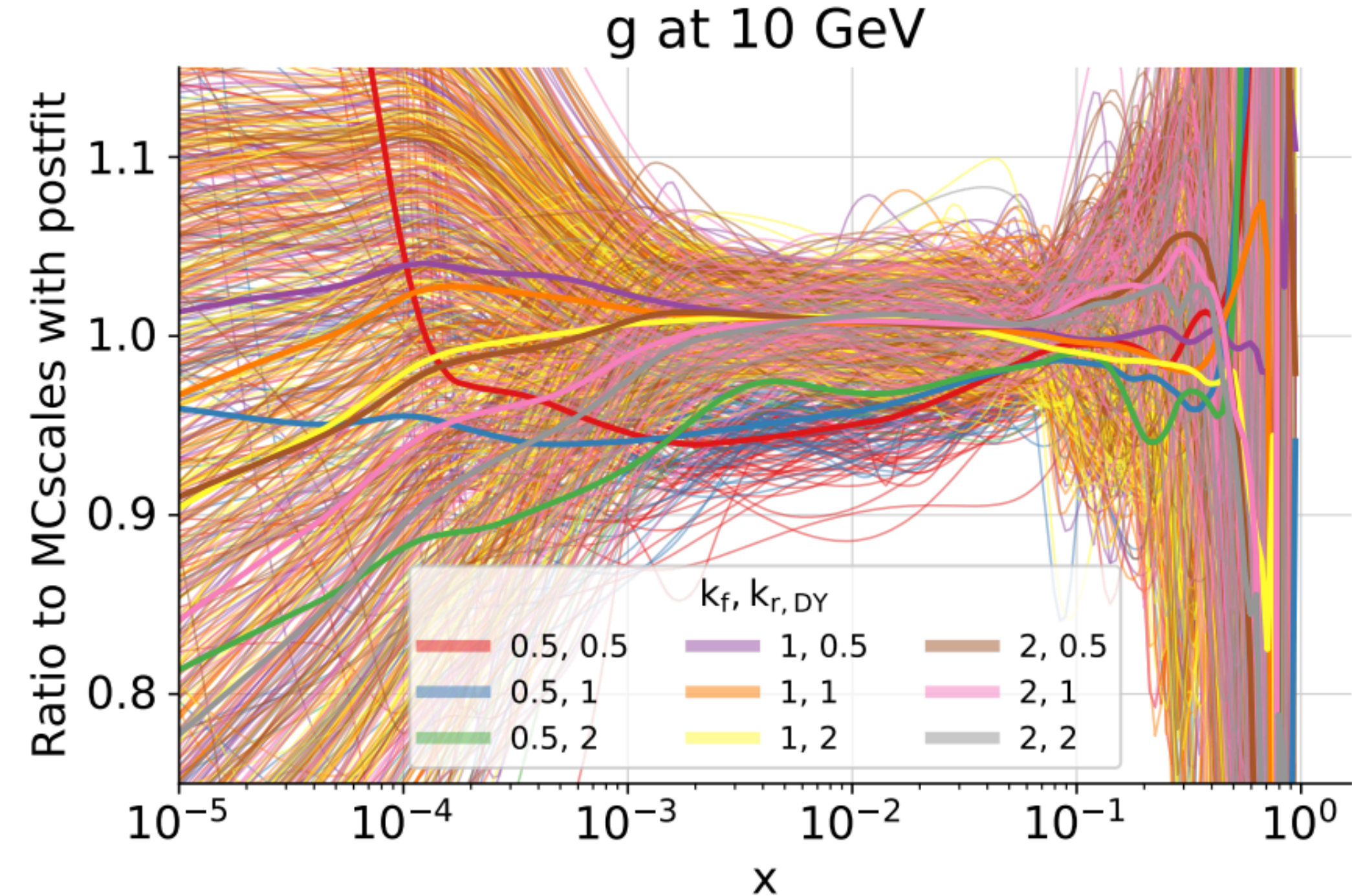
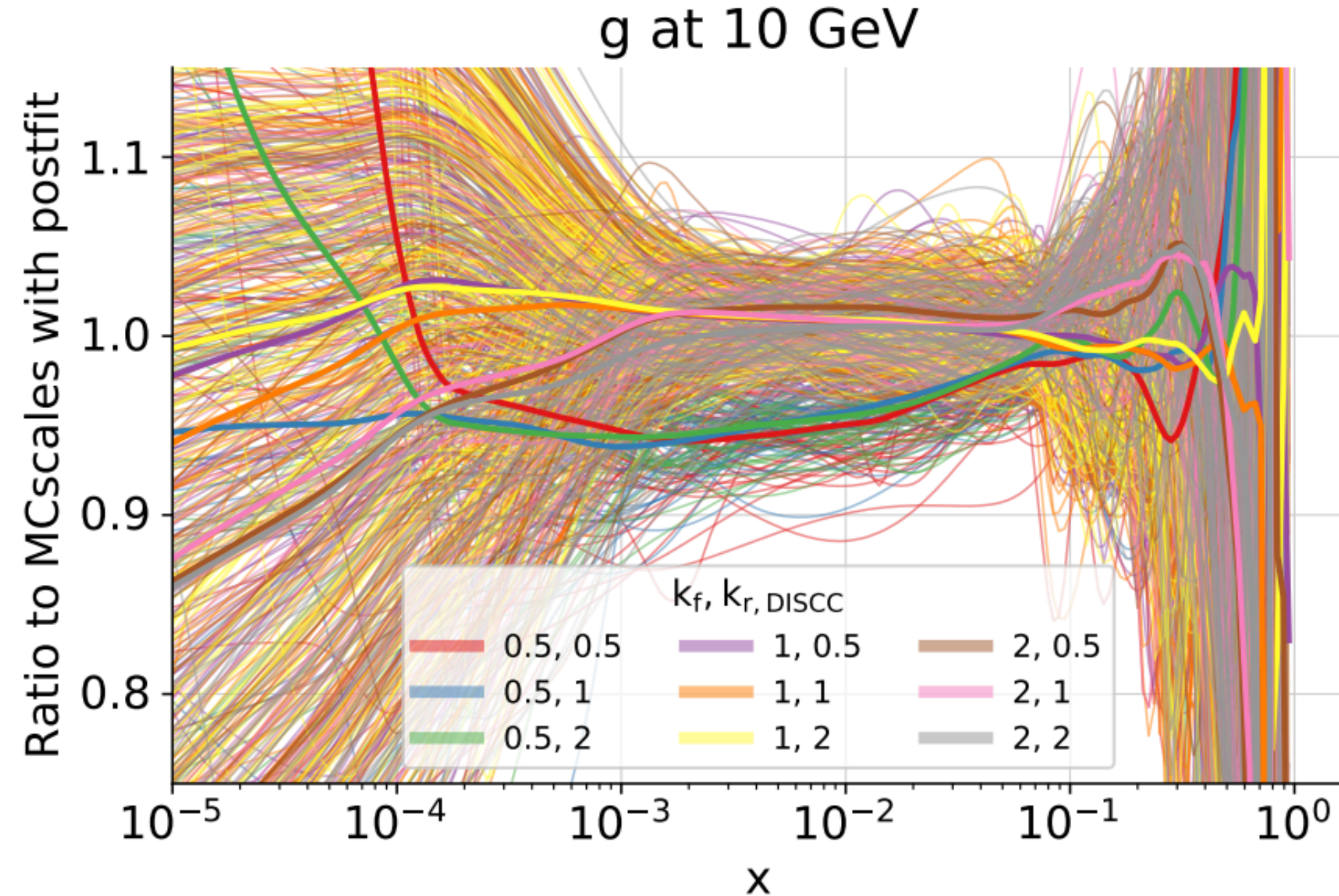
$$\gamma_{ij}(N) = - \int_0^1 dx x^{N-1} P_{ij}(x)$$

- For example, in NNPDF fit, for the  $P_{qq}$  splitting function

$G_1(N)$	$\mathcal{M}[(1-x) \ln^2(1-x)]$	➔ Large-N contribution
$G_2(N)$	$-\frac{1}{(N-1)^2} + \frac{1}{N^2}$	➔ Small-N contribution
$\gamma_{qq,ps}^{(3)}(N)$	$\frac{1}{N^4}, \frac{1}{N^3}, \mathcal{M}[(1-x) \ln(1-x)]$	➔ Sub-leading small-N and large-N contributions
$\{G_{3,\dots,8}(N)\}$	$\mathcal{M}[(1-x)^2 \ln(1-x)^2], \frac{1}{N-1} - \frac{1}{N}, \mathcal{M}[(1-x) \ln(x)]$	
$\{G_9(N), G_{10}(N)\}$	$\mathcal{M}[(1-x)(1+2x)], \mathcal{M}[(1-x)x^2],$ $\mathcal{M}[(1-x)x(1+x)], \mathcal{M}[(1-x)]$	➔ Sub-leading

- Varying the sub-leading basis produces different candidates ➔ Incomplete Higher Order Uncertainty (IHOU)
- Different choice of basis and approaches in varying basis between NNPDF and MSHT and playing it the fit





- ✓ Main idea of MCscales: the renormalisation and factorisation scales are free parameters of the fixed-order theory, that induce an uncertainty on the theory predictions included in a PDF fit & need to be propagated
- ✓ Joint sampling of experimental uncertainty (propagated to PDF uncertainty by MC sampling) by specifying a suitable prior probability distribution of all possible scale choices & a-posteriori criterion based on agreement with the data.

$$P(k_f = \xi_f, k_{r_1} = \xi_1, \dots, k_{r_{N_p}} = \xi_{N_p}) = P(\omega)$$

$$\text{with } \omega \in \Omega = \{(\xi_f, \xi_1, \dots, \xi_{N_p}) \mid \forall \xi_f, \xi_1, \dots, \xi_{N_p} \in \Xi\}$$

$3^{1+N_p}$  elements, with  $N_p = 5$ ,  $p = \text{DIS NC, DIS CC, DY, JET, TOP}$

Choose prior = choose  $P(\omega)$

Posterior

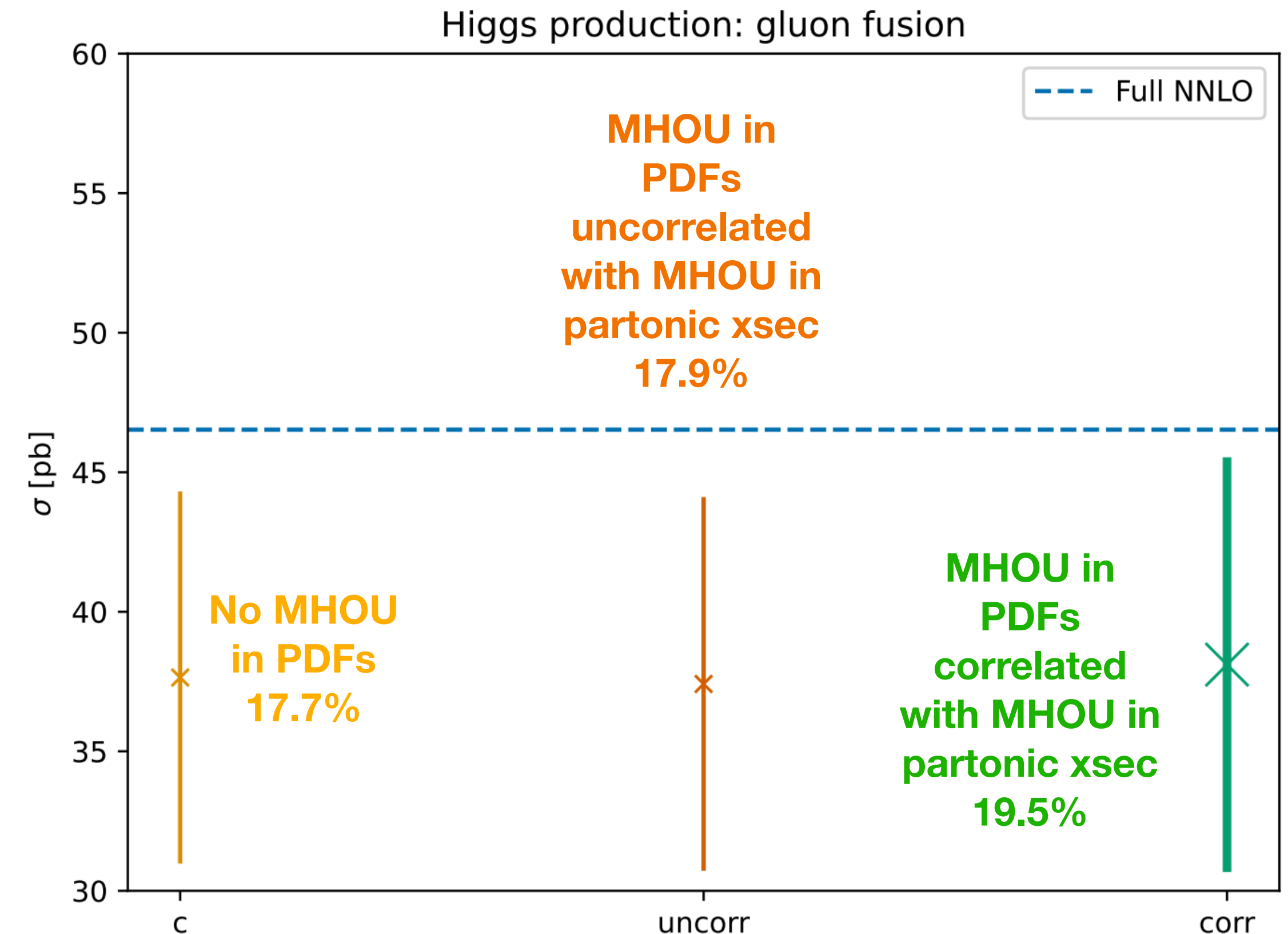
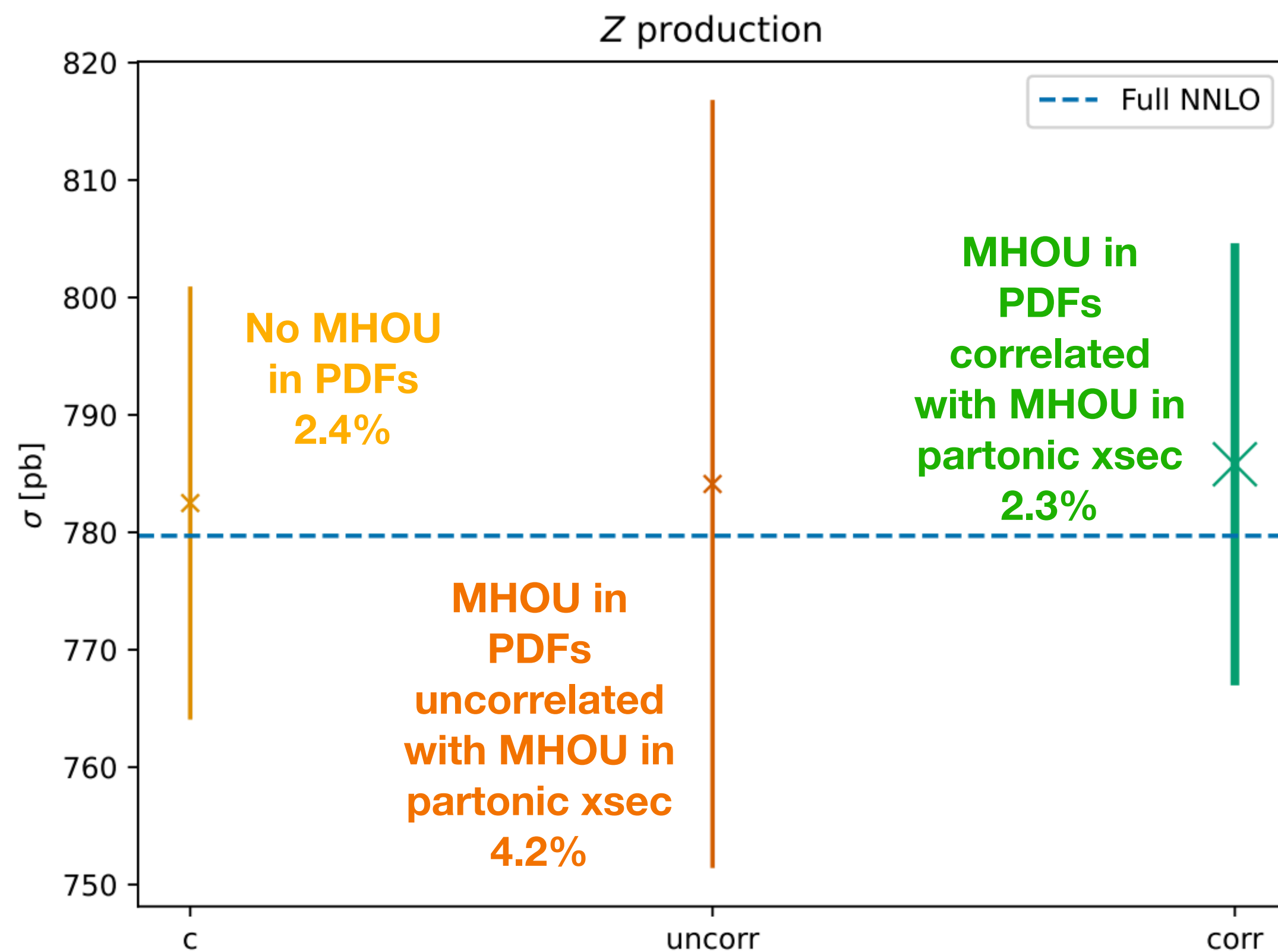
$$\chi_n^2 > \langle \chi^2 \rangle_n | \omega^{(n)} = \{1, \dots, 1\} + 4 \text{std}(\chi^2)_{n | \omega^{(n)} = \{1, \dots, 1\}}$$



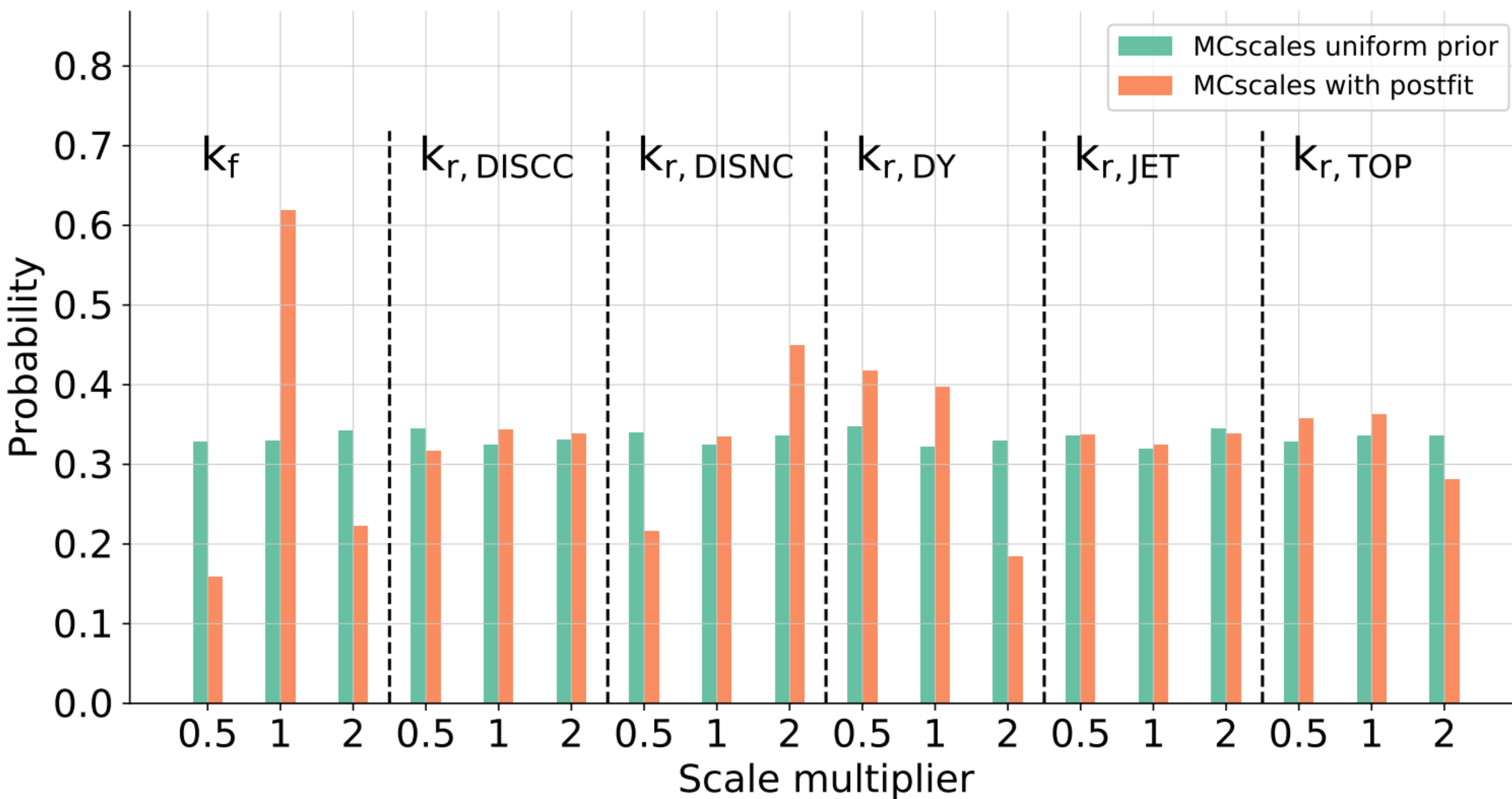
# THE MCSCALES APPROACH

✓ Can compute full PDF+SCALE uncertainty in cross sections at NLO by matching the scales in the hard cross section computation with the scales in the MCscale PDF set: correlation fully taken into account

$$\left\{ \sigma_n = \hat{\sigma}_p(k_f^{(n)}, k_{r_p}^{(n)}) \otimes f_n(k_f^{(n)}, k_{r_p}^{(n)}) \quad \forall n = 1, \dots, N \right\}$$



# THE MCSCALES APPROACH

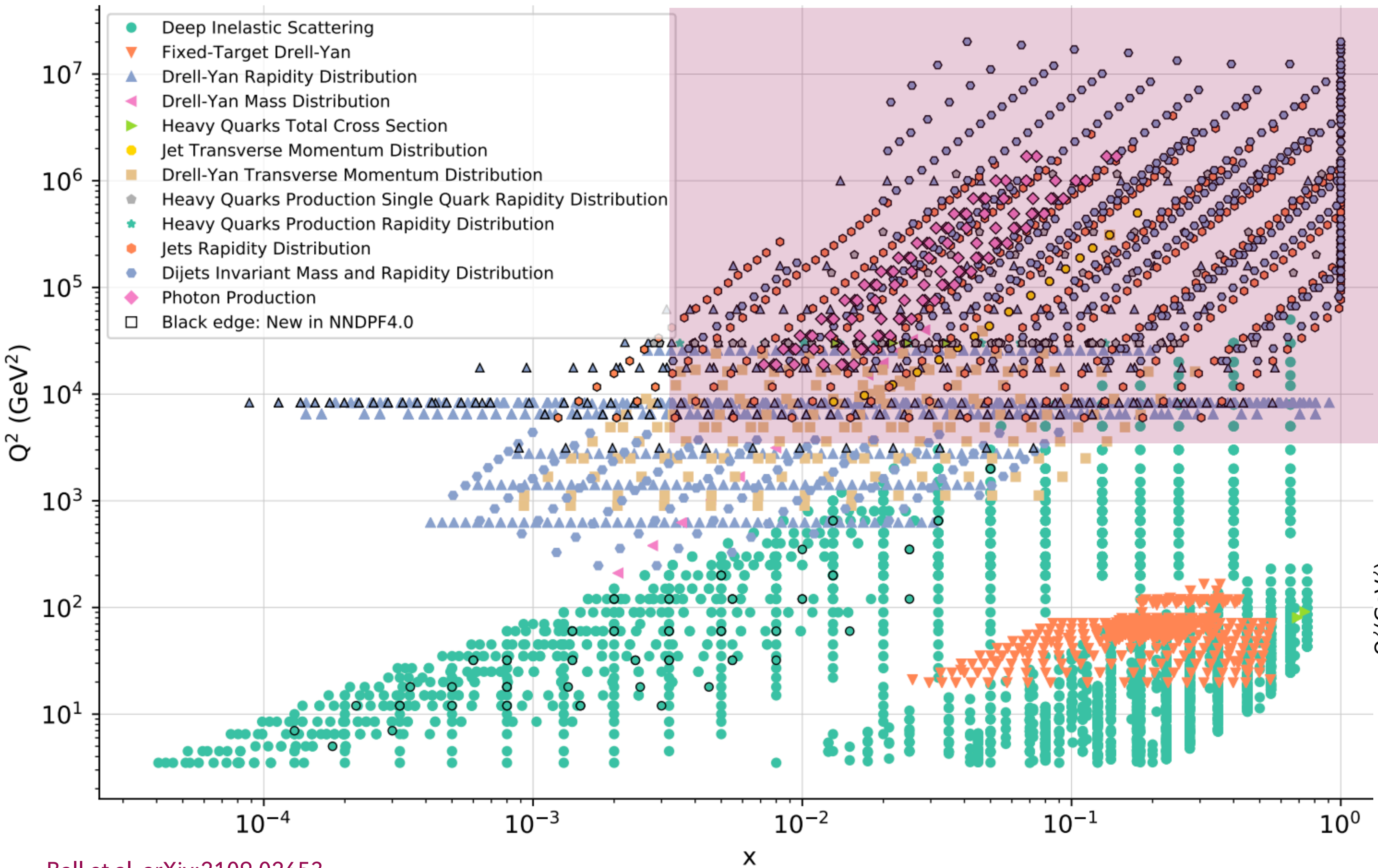


- ✓ Can look at the distribution of each of the scales over replicas.
- ✓ Flat distribution for the MCscales uniform prior.
- ✓ After applying postfit observe preference for central factorisation scale.
- ✓ Each process affected in a different way.

Scale multipliers	Process	Preferred values
$(k_f, k_r)$	DIS CC	(1, 1)
	DIS NC	(1, 2)
	DY	(1, 1)
	Jets	$(1, \frac{1}{2})$
	Top	(1, 1)



# OVERLAP BETWEEN DATA IN PDF AND SMEFT FITS



Ball et al, arXiv:2109.02653

➔ Top pair production and single top data included in SMEFT analysis

[Hartland et al 1901.05965] [Ellis et al 2012.02779]

➔ Dijets data in [Bordone et al 2103.10332]

[Alioli et al 1706.03068]

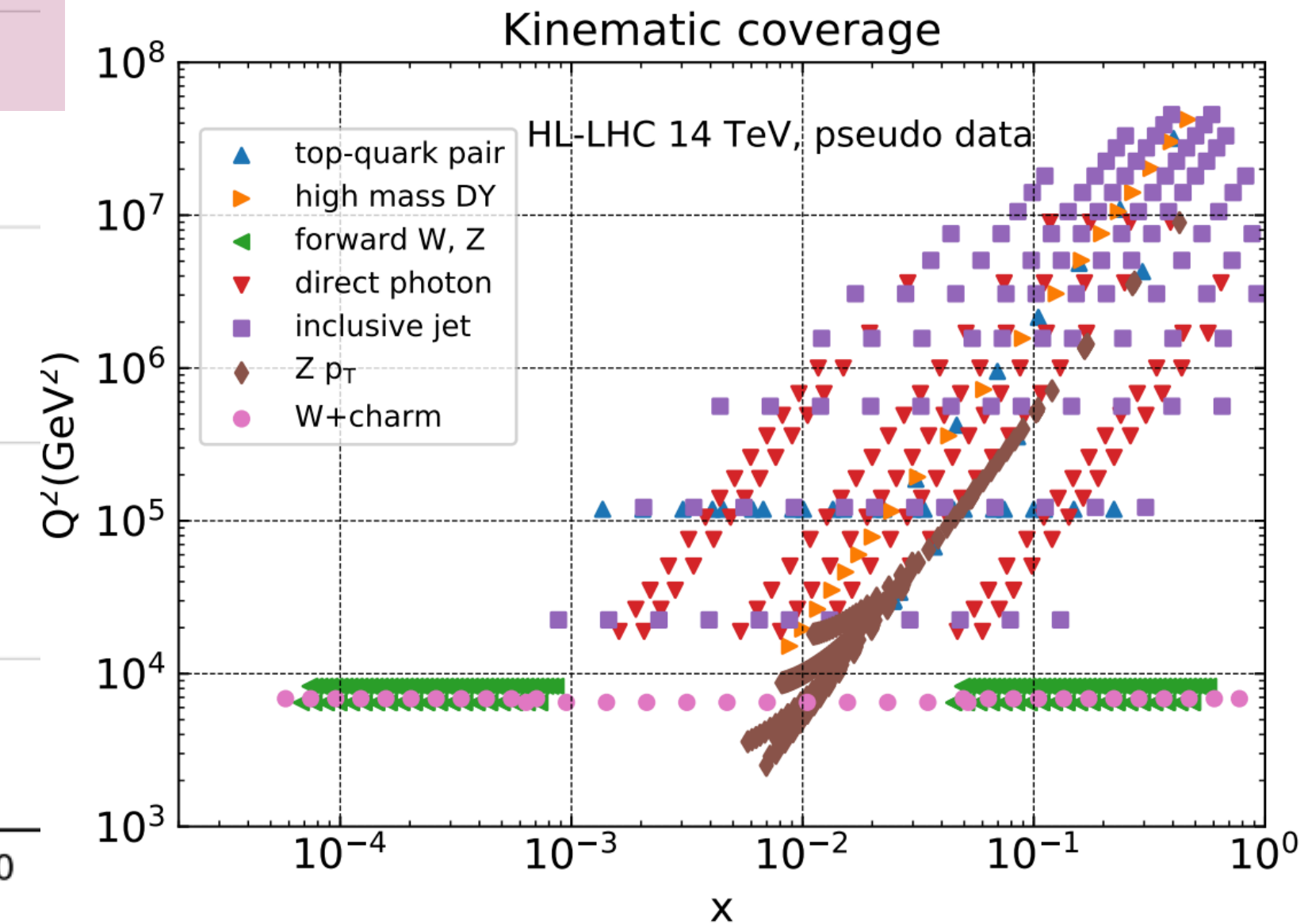
➔ Drell-Yan data in [Farina et al 1609.08157]

[Torre et al 2008.12978]

➔ Inclusive jets in [Alte et al 1711.07484]

➔ Overlap enhanced in HL-LHC

projections [Abdul Khalek et al, 1810.03639]

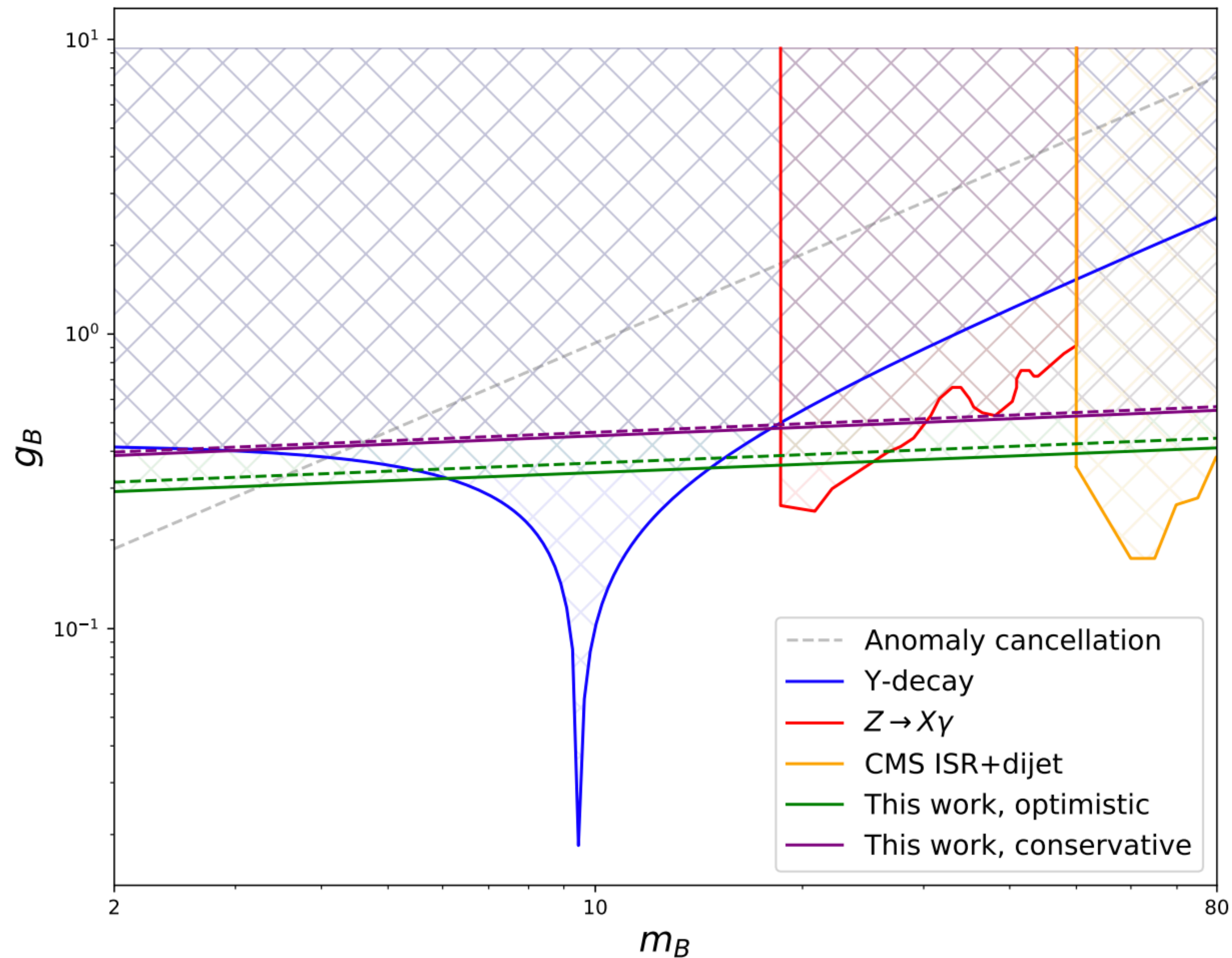


Abdul Khalek et al, arXiv:1810.03639



# DARK PHOTON

M. McCullough, J. Moore, MU, arXiv:2203.12628



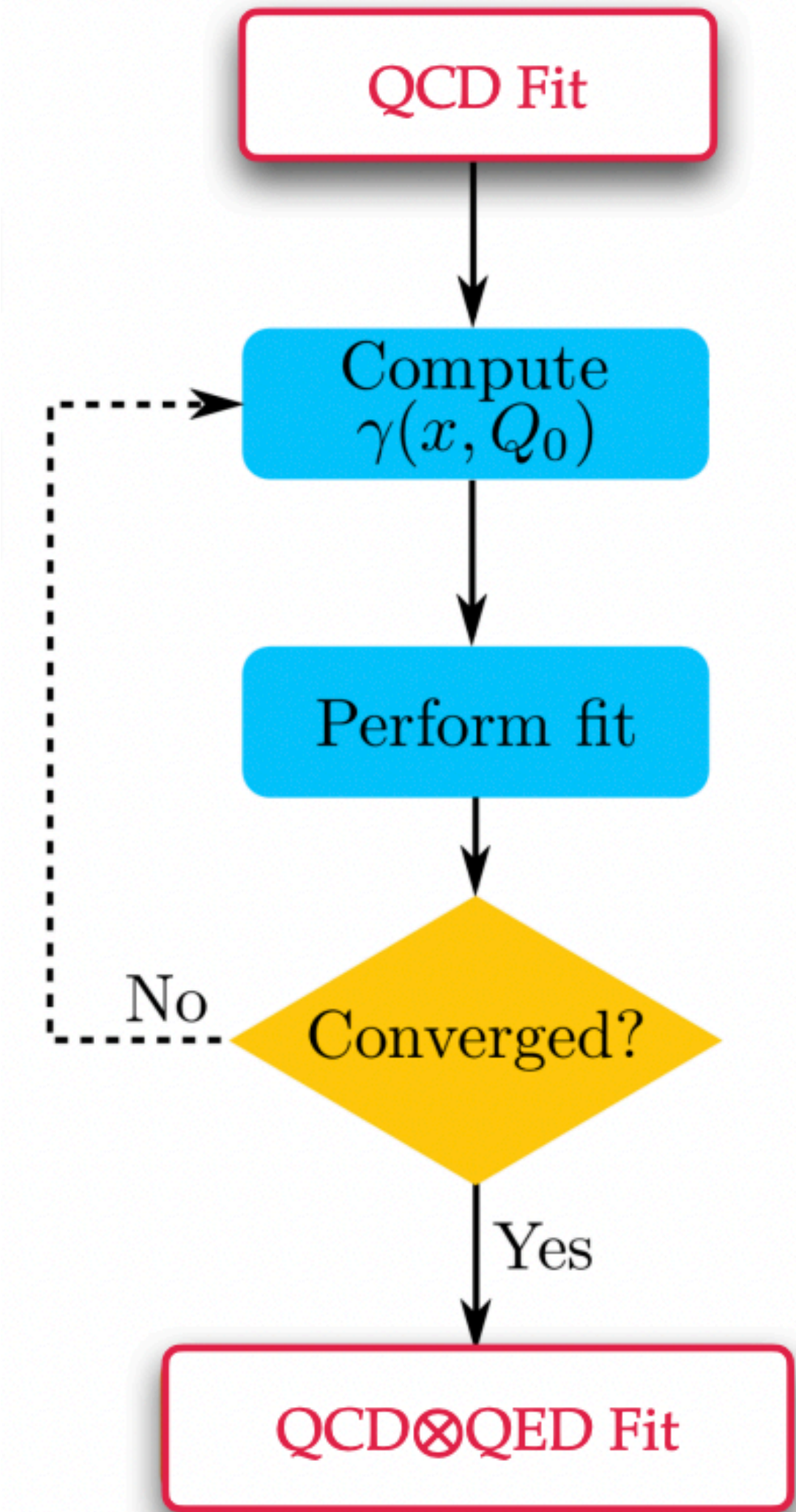
- If there was a lepto-phobic dark photon weakly coupled to quarks, it would appear among the partons of the proton.

$$\mathcal{L}_{\text{int}} = \frac{1}{3} g_B \bar{q} \not{B} q$$

- The presence of the dark Parton would modify the evolution of standard quarks and gluon.
- Precise LHC data can indirectly constrain parameter space of the dark photon in a competitive way compared to direct searches



- Two main changes required to account for QED effects in PDF fits: modified DGLAP equations including  $O(\alpha_s\alpha)$  and  $O(\alpha^2)$  terms and mixed QCDxQED sum rules implemented in new theory pipeline given by EKO [Candido, Hekhorn, Magni arXiv:2202.02338] and Yadism [Candido, Hekhorn in preparation]
- **NNPDF4.0QED:** PDFs and photon determined such that they satisfy sum rules
- Photon iteratively computed during the fit using structure function input a la LUXQED Manohar, Nason, Salam, Zanderighi [arXiv:1607.04266,1708.01256]



NNPDF [arXiv:1712.07053]

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