

Dark Z boson and the W boson mass anomaly

Kazuki Enomoto
(KAIST)



Based on

- Hooman Davoudiasl¹, KE², Hye-Sung Lee², Jiheon Lee²,
William J. Marciano¹, [Phys. Rev. D108 \(2023\) 115018](#)
[\[arXiv:2309.04060\[hep-ph\]\]](#)

1. BNL, 2. KAIST

Extension of gauge symmetries

Problems in the Standard Model (SM)

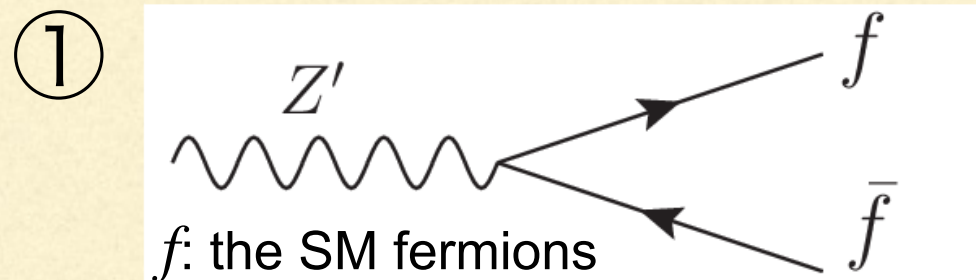
- **Unexplained phenomena** ν oscillation, dark matter, baryon asymmetry, ...
- **Theoretical problems** Unification of gauge interactions, gravity, ...
- **Experimental anomalies** Muon $g-2$, B anomaly, W boson mass anomaly, ...

We need new physics!

A new $U(1)$ gauge symmetry

$$SU(3)_C \times SU(2)_L \times U(1)_Y \times U(1)$$

New force!
New gauge boson Z'



f carries $U(1)$ charge
e.g.) $U(1)_{B-L}$ extension



f does NOT carry $U(1)$ charge
e.g.) dark photon model

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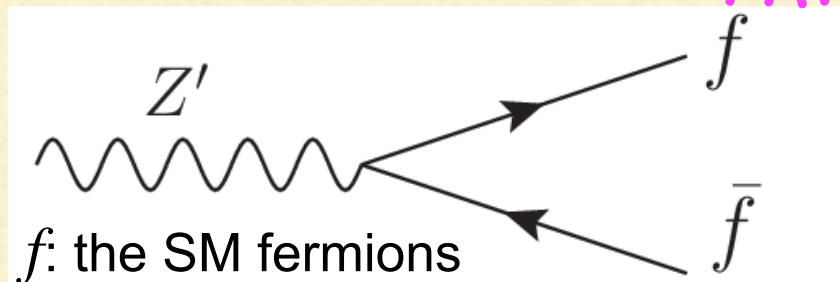
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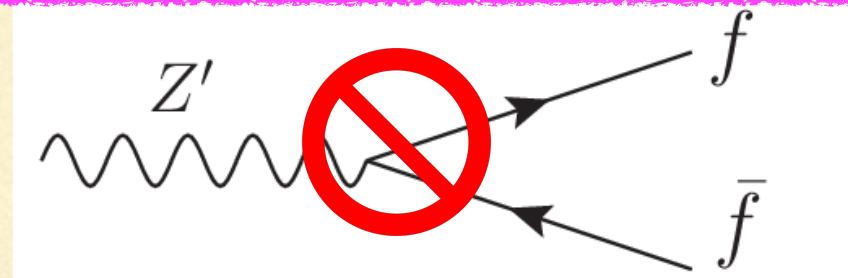
This talk

①



f carries $U(1)$ charge
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②



Dark photon model

Dark gauge symmetry: $U(1)_d$ (The SM fermions don't carry the dark charge Q_d)

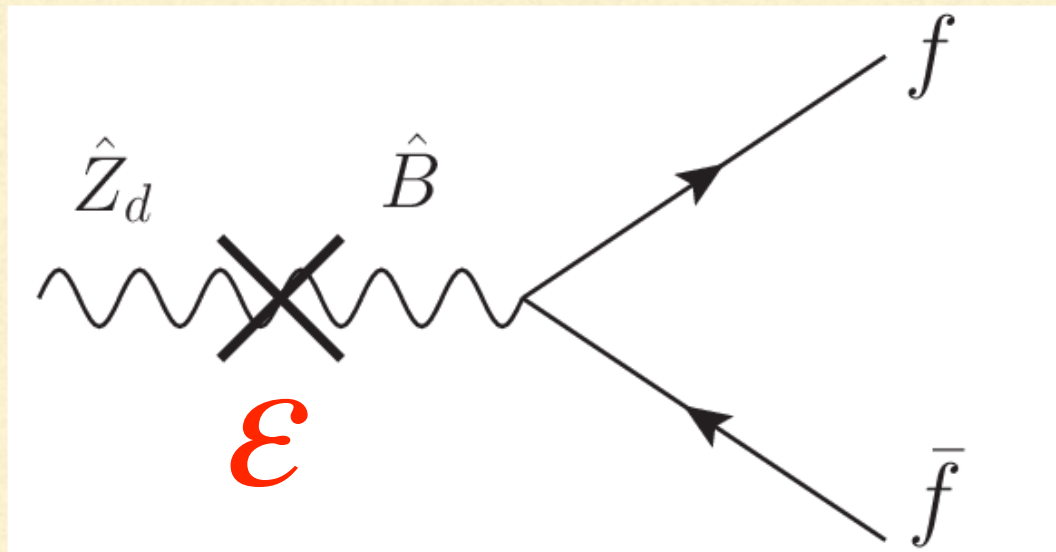
$$\mathcal{L} = -\frac{1}{4}\hat{B}_{\mu\nu}\hat{B}^{\mu\nu} + \frac{\varepsilon}{2c_W}\hat{B}_{\mu\nu}\hat{Z}_d^{\mu\nu} - \frac{1}{4}\hat{Z}_{d\mu\nu}\hat{Z}_d^{\mu\nu}$$

$c_W = \cos \theta_W$

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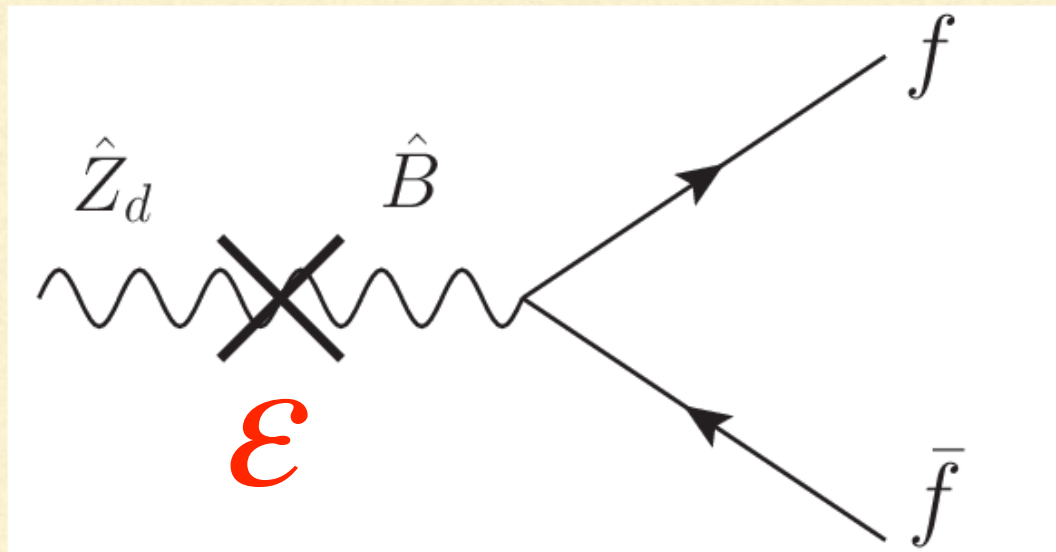
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The SM fermions interact with \hat{Z}_d
via kinetic mixing [Holdom, PLB \(1986\)](#)

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Kinetic mixing

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$U(1)_d$ symmetry breaking: \hat{Z}_d get the mass term by a **singlet VEV**

Mass eigenstates: γ , Z , and Z_d **New physical gauge boson**

$$\mathcal{L}_d \simeq -e\varepsilon J_{\text{em}}^\mu Z_{d\mu} \quad (m_{Z_d}^2 \ll m_Z^2) \quad Z_d \text{ couples } J_{\text{em}}^\mu \text{ (Dark photon)}$$

Dark Z model

[Davoudiasl, Lee, Marciano, 1203.2947](#)

Dark gauge symmetry: $U(1)_d$

Nature of gauge symmetry breaking is quite different

Higgs sector: $\Phi_1 : \left(\mathbf{1}, \mathbf{2}, \frac{1}{2}, 0 \right)$ $\Phi_2 : \left(\mathbf{1}, \mathbf{2}, \frac{1}{2}, 1 \right)$ $\Phi_d : \left(\mathbf{1}, \mathbf{1}, 0, 1 \right)$

$U(1)_d$ symmetry breaking: \hat{Z}_d get the mass term by the **singlet VEV** (v_d)
and the **doublet VEV** (v_2)

Mass matrix of neutral gauge bosons

$$\begin{pmatrix} \tilde{m}_Z^2 & -\tilde{m}_Z^2(\varepsilon_Z + \varepsilon t_W) \\ -\tilde{m}_Z^2(\varepsilon_Z + \varepsilon t_W) & \tilde{m}_{Z_d}^2 \end{pmatrix}$$

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New source of mixing!
Mass mixing independent of ε $\varepsilon_Z = \frac{2g_d v_2^2}{g_Z v^2}$

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$$\mathcal{L}_d \simeq - \left(e\varepsilon J_{\text{em}}^\mu + \frac{g}{2c_W} \varepsilon_Z J_{\text{NC}}^\mu \right) Z_{d\mu}$$

Z_d couples to J_{NC}^μ
Dark Z boson
($m_{Z_d}^2 \ll m_Z^2$)

Dark Z model

$$\mathcal{L}_d \simeq - \left(e \varepsilon J_{\text{em}}^\mu + \frac{g}{2c_W} \varepsilon_Z J_{\text{NC}}^\mu \right) Z_{d\mu}$$

Z_d predicts various distinctive phenomena

- Parity violation @ low energies [1203.2947](#) [1507.00352](#) [2309.04060](#)
- Rare meson decays [1203.2947](#) [2210.15662](#) [1402.3620](#)
- Higgs exotic decays [1304.4935](#)
- Collider signals [1401.2164](#) [2205.10304](#) [2209.03240](#)

In this talk,

The W boson mass anomaly in the dark Z boson

W boson mass (m_W) anomaly

PDG (2022)

W boson mass measurements

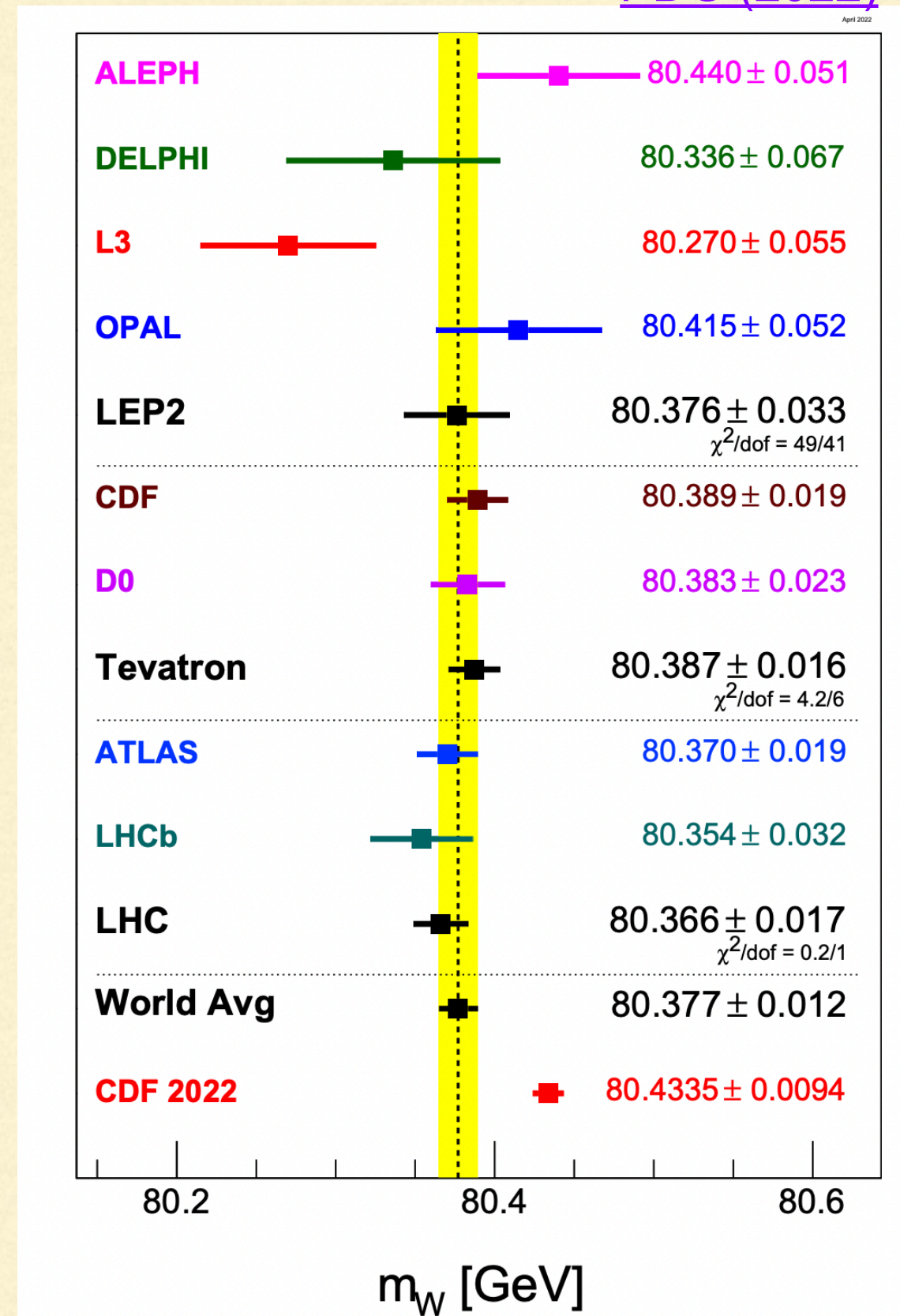
$$pp(p\bar{p}) \rightarrow W \rightarrow \ell\nu, \quad e^+e^- \rightarrow W^+W^-$$

Before Apr. 2022,

$$m_W^{\text{World-ave.}} = 80.377(12)$$

$$m_W^{\text{SM}} = 80.356(06) \quad \text{PDG (2022)}$$

Good agreement



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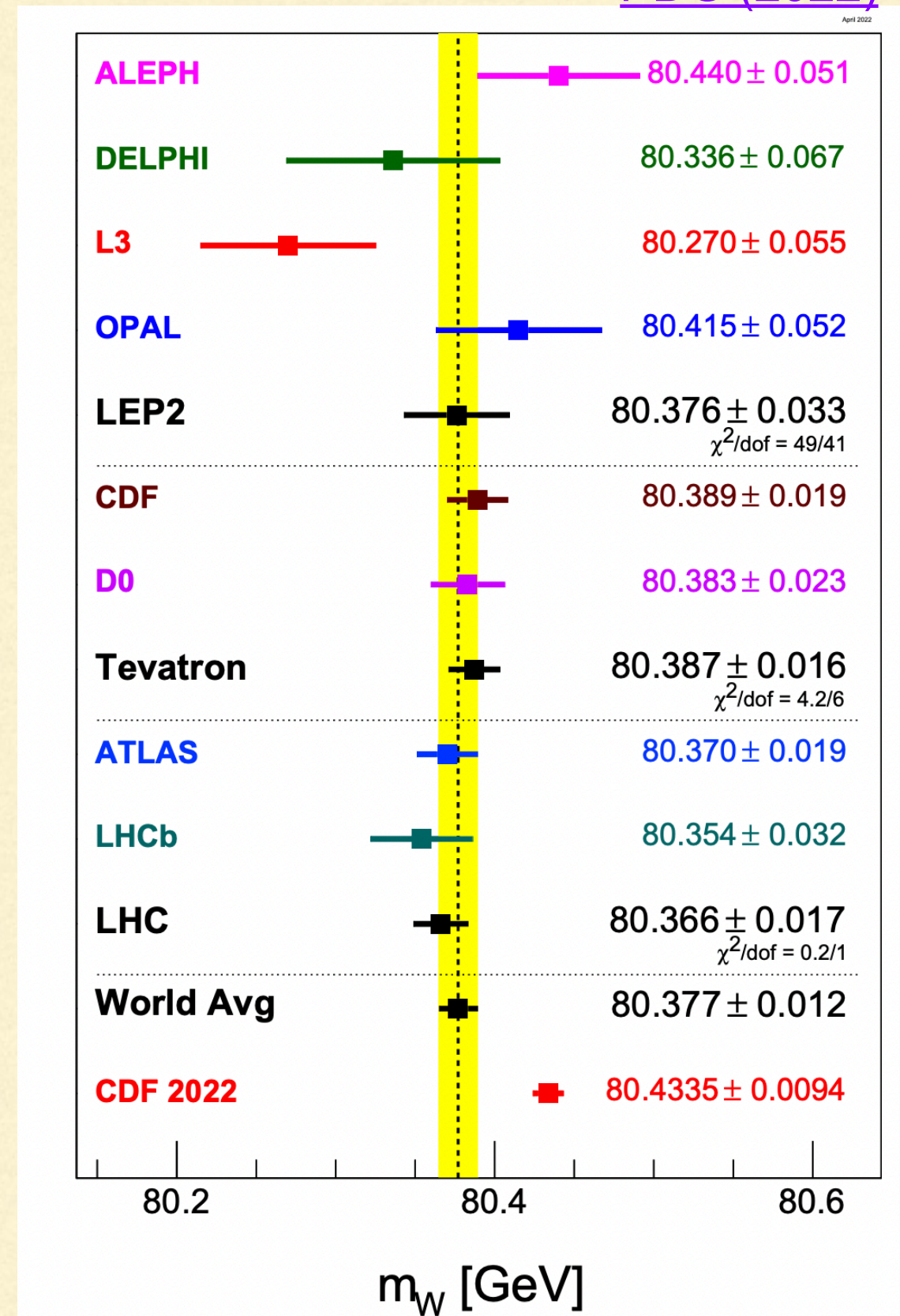
The CDF-II result [CDF, Science \(2022\)](#)

$$m_W^{\text{CDF-II}} = 80.4335(94)$$

7σ deviation!

New physics?

Need to **enhance** m_W



m_W anomaly and new physics

New physics effect: S, T, U parameters [Peskin, Takeuchi, PRL \(1990\)](#)

$$\Delta m_W^2 \equiv m_W^2 - (m_W^{\text{SM}})^2 = m_Z^2 c_W^2 \left(-\frac{\alpha S}{2(c_W^2 - s_W^2)} + \frac{\alpha T}{1 - t_W^2} + \frac{\alpha U}{4s_W^2} \right)$$

$$\Delta m_W^2 = (m_W^{\text{CDF-II}})^2 - (m_W^{\text{SM}})^2 \simeq \boxed{12.5 \text{ GeV}^2}$$

$$\longrightarrow -0.93S + 1.4T + 1.1U \simeq 0.25$$

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EW global fit (w/ the CDF-II result) [Lu et al, 2204.03796](#)

$$S = 0.06(10) \quad T = 0.11(12) \quad U = 0.14(09)$$

The dark photon model **CANNOT** explain the anomaly under this constraint. [Cheng et al, 2204.10156](#) [Thomas, Wang, 2205.01911](#)
[Asagi et al, 2204.05283](#)

Dark Z bosons and W boson mass anomaly

In the dark Z model, **couplings & mass of Z boson** deviates from the SM ones because of kinetic & mass mixing

$$\mathcal{L}_{\text{gauge}} = \frac{1}{2} \tilde{m}_Z^2 (1 + \Delta_1) Z^\mu Z_\mu - \frac{g}{2c_W} (1 + \Delta_2) J_{\text{NC}}^\mu Z_\mu - e \Delta_3 J_{\text{EM}}^\mu Z_\mu + \textcircled{\dots}$$

$$\tilde{m}_Z^2 = g^2 v^2 / (4c_W^2)$$

Other terms are
the same in the SM

Dark Z bosons and W boson mass anomaly

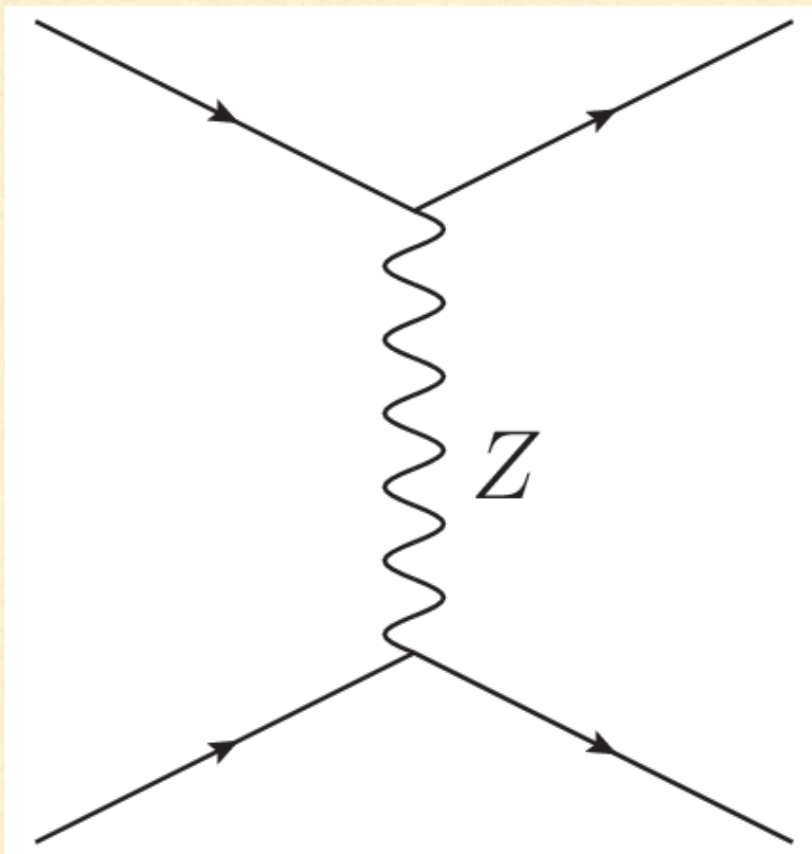
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New physics effect in 4 fermion processes



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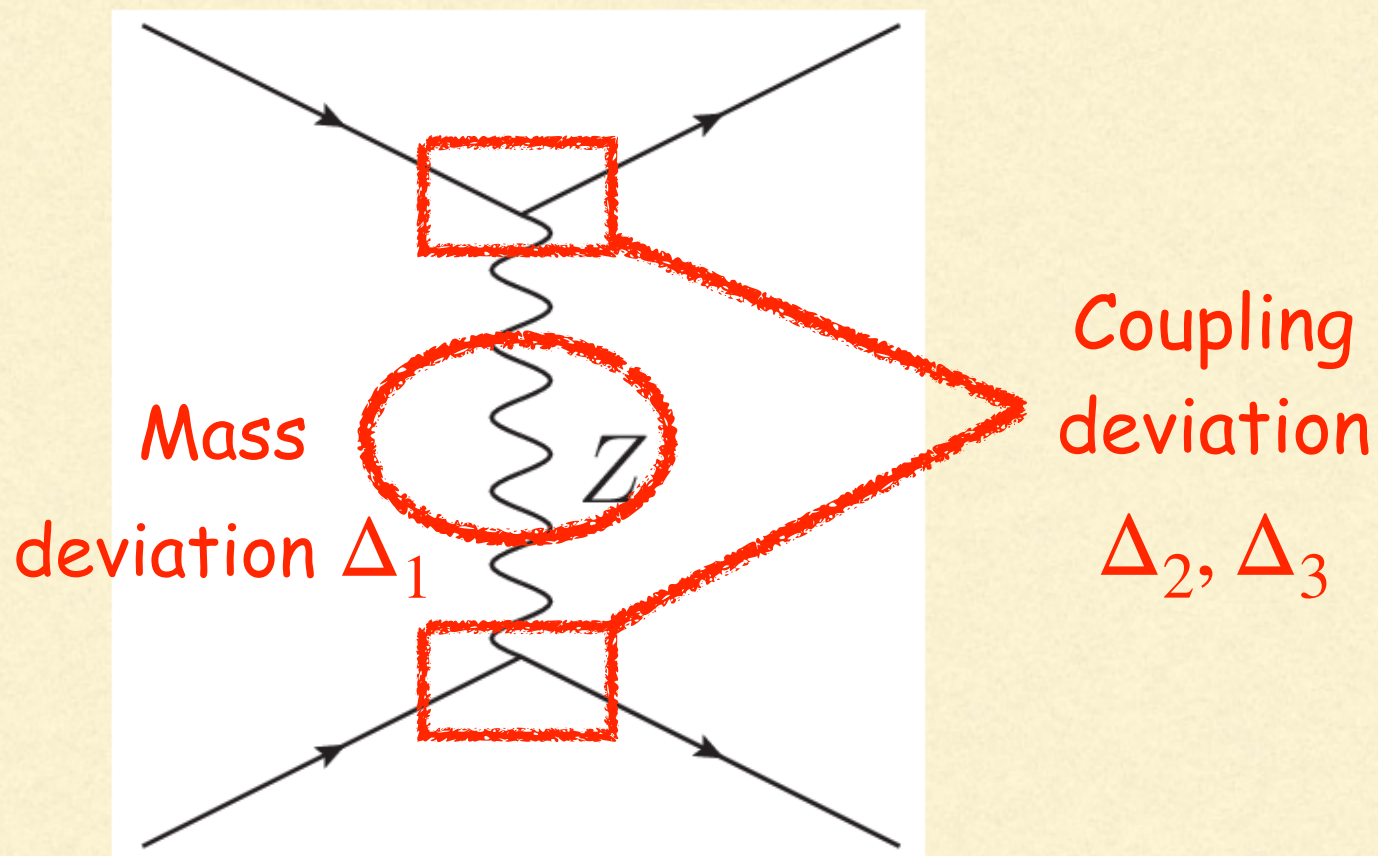
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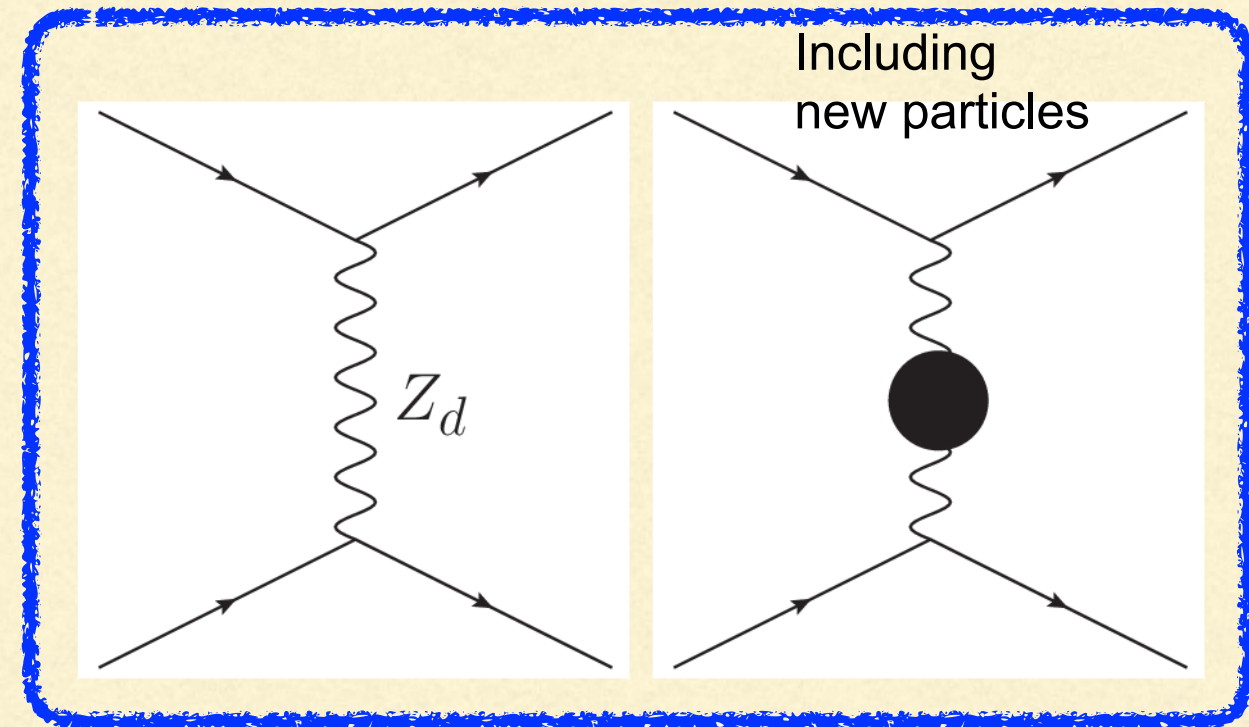
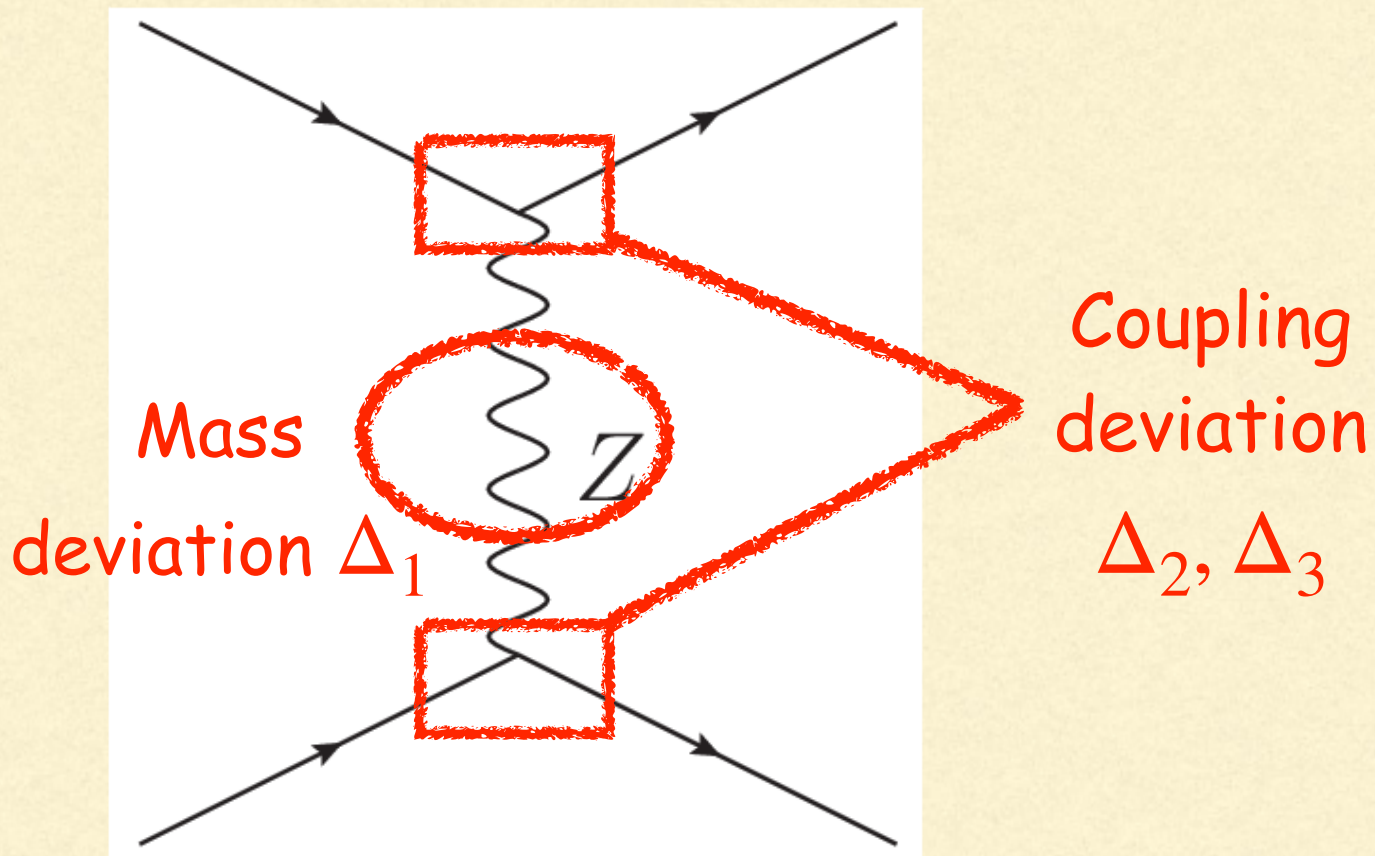
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Sub-leading @ Z pole
(unless $m_{Z_d} \simeq m_Z$)

Heavy dark Z bosons and W boson mass anomaly

$$\mathcal{L}_{\text{gauge}} = \frac{1}{2} \tilde{m}_Z^2 (1 + \Delta_1) Z^\mu Z_\mu - \frac{g}{2c_W} (1 + \Delta_2) J_{\text{NC}}^\mu Z_\mu - e \Delta_3 J_{\text{EM}}^\mu Z_\mu + \dots$$

The effect of the deviations Δ_1 , Δ_2 , and Δ_3 can be described by

S , T , and U parameters [Holdom, PLB \(1991\)](#)

$$\alpha S = 8s_W^2 c_W^2 \Delta_2 - 4s_W c_W (c_W^2 - s_W^2) \Delta_3$$

$$\simeq -4s_W c_W \left(\frac{\varepsilon_Z + \varepsilon t_W}{1 - r^2} \right) \left\{ s_W c_W \frac{\varepsilon_Z + \varepsilon t_W}{1 - r^2} - \varepsilon \right\}$$

$$r = m_{Z_d} / m_Z$$

$$s_W = \sin \theta_W$$

$$c_W = \cos \theta_W$$

$$\alpha T = -\Delta_1 + 2\Delta_2$$

$$\simeq -\left(\frac{\varepsilon_Z + \varepsilon t_W}{1 - r^2} \right) \left(\frac{(2 - r^2)\varepsilon_Z + r^2 \varepsilon t_W}{1 - r^2} \right)$$

EW global fit
(w/ CDF-II result)

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$$\alpha U = -8s_W^2 c_W (c_W \Delta_2 + s_W \Delta_3)$$

$$\simeq 4s_W^2 c_W^2 \left(\frac{\varepsilon_Z + \varepsilon t_W}{1 - r^2} \right)^2$$

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Heavy dark Z bosons and W boson mass anomaly

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Heavy dark Z bosons and W boson mass anomaly

Using S , T , and U parameters,

$$\Delta m_W^2 = m_Z^2 c_W^2 \left(-\frac{\alpha S}{2(c_W^2 - s_W^2)} + \frac{\alpha T}{1 - t_W^2} + \frac{\alpha U}{4s_W^2} \right) \text{Peskin, Takeuchi, PRL (1990); PRD (1992)}$$
$$= -m_Z^2 \left(\frac{c_W^2}{c_W^2 - s_W^2} \right) \left(\frac{1}{1 - r^2} \right) \left(\varepsilon_Z + \varepsilon t_W \right)^2$$

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$$r^2 < 1 \quad \longrightarrow \quad \Delta m_W^2 < 0$$

$$r^2 > 1 \quad \longrightarrow \quad \Delta m_W^2 > 0$$

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Favored by the CDF-II result

$$m_{Z_d} > m_Z$$

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CDF-II: $\Delta m_W^2 \simeq 12.5 \text{ GeV}^2$

$$(\varepsilon_Z - 0.55\varepsilon)^2 \simeq (1.6 \times 10^{-3}) \times \left(\left(\frac{m_{Z_d}}{100 \text{ GeV}} \right)^2 - 0.83 \right)$$

S, T, U parameters in the dark photon limit

In the dark photon (DP) limit ($\varepsilon_Z = 0$),

$$\alpha S_{\text{DP}} = 4s_W^2(c_W^2 - r^2) \left(\frac{\varepsilon}{1 - r^2} \right)^2$$

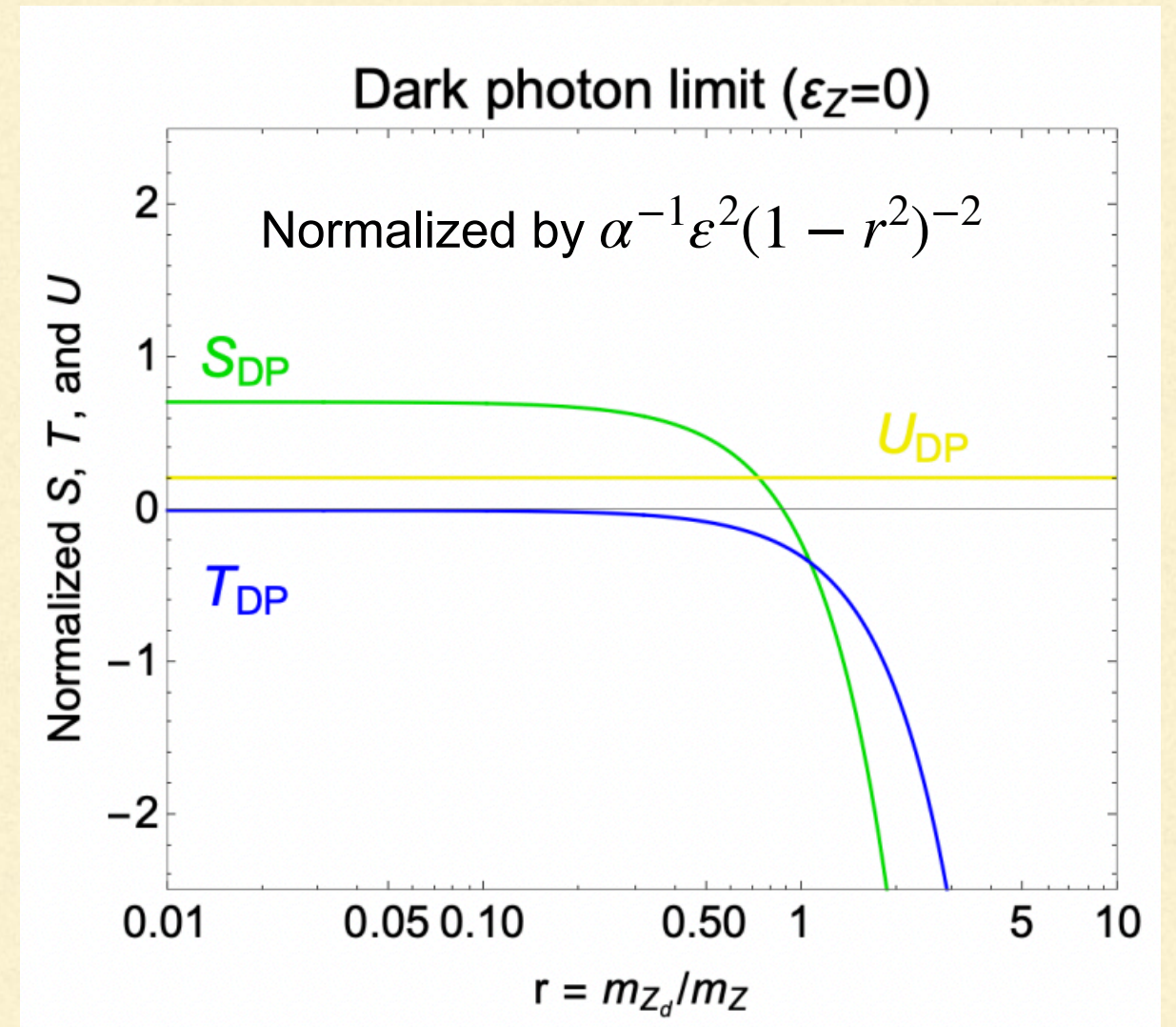
$$\alpha T_{\text{DP}} = -t_W^2 r^2 \left(\frac{\varepsilon}{1 - r^2} \right)^2$$

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When $r \gg 1$,

$$|S_{\text{DP}}|, |T_{\text{DP}}| \gg |U_{\text{DP}}|,$$

$$\text{and } S_{\text{DP}} = (4/c_W^2)T_{\text{DP}} \simeq 3.0T_{\text{DP}}$$



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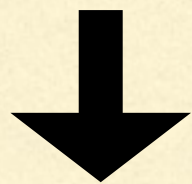
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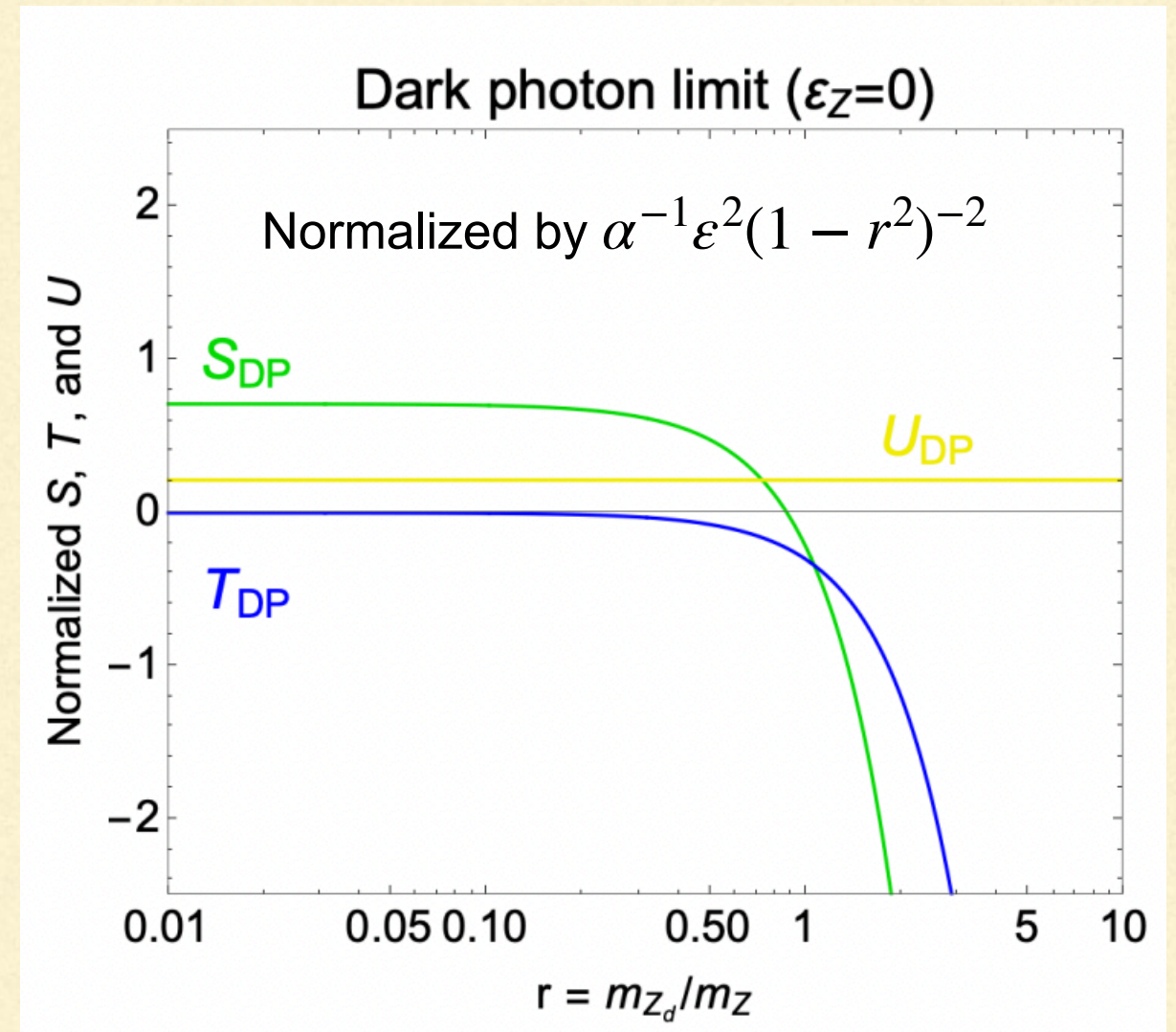
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$$\Delta m_W^2 \simeq -S_{\text{DP}} \times (35 \text{GeV}^2)$$



CDF-II result ($\Delta m_W^2 \simeq 12.5 \text{GeV}^2$) requires

$$S_{\text{DP}} \simeq -0.54$$

$S = 0.06(10)$ out of 2σ region
($\sim 6.0\sigma$)

S, T, U parameters in the pure dark Z limit

In the pure dark Z (DZ) limit ($\varepsilon = 0$),

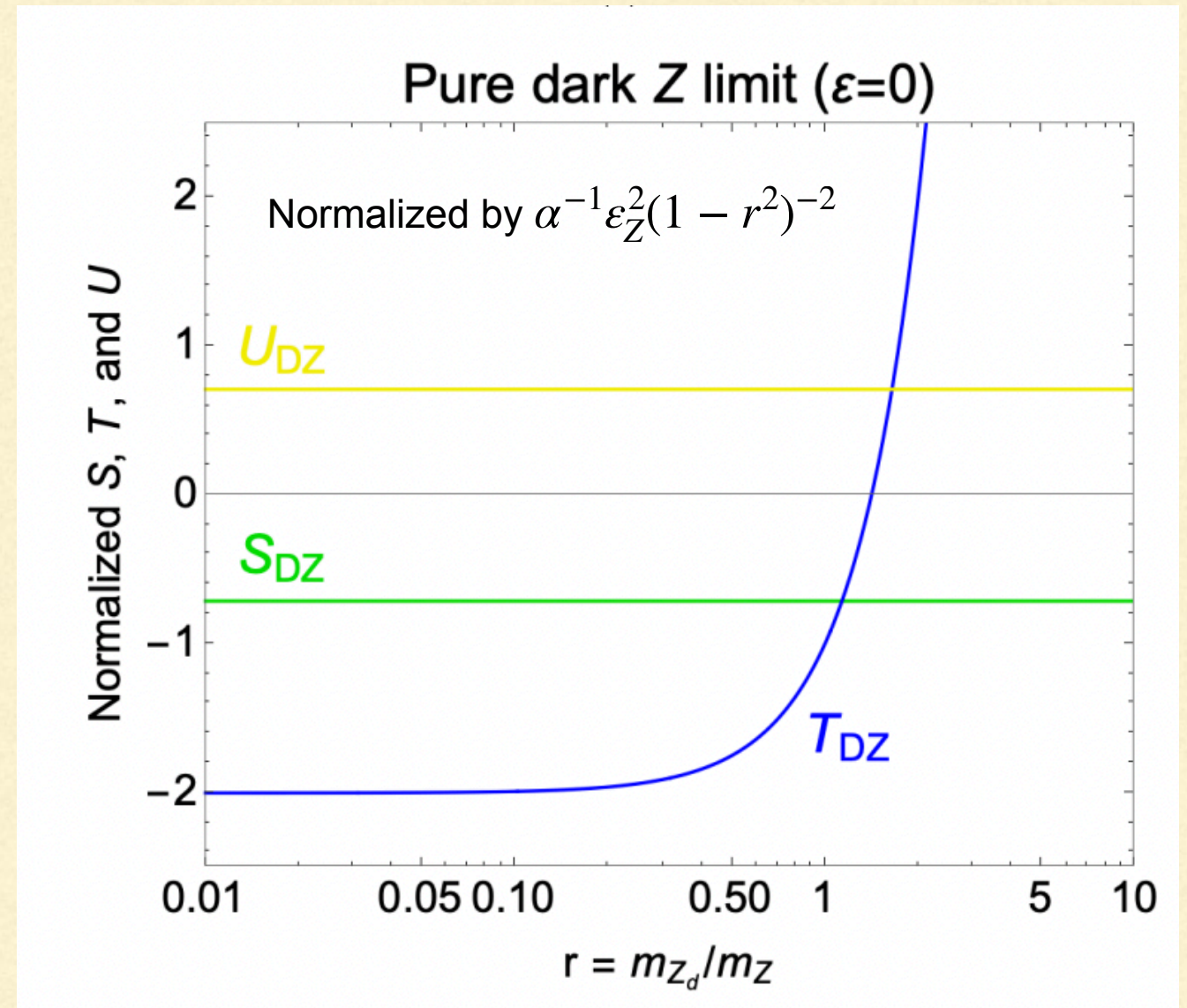
$$\alpha S_{\text{DZ}} = -4s_W^2 c_W^2 \left(\frac{\varepsilon_Z}{1-r^2} \right)^2$$

$$\alpha T_{\text{DZ}} = (r^2 - 2) \left(\frac{\varepsilon_Z}{1-r^2} \right)^2$$

$$\alpha U_{\text{DZ}} = 4s_W^2 c_W^2 \left(\frac{\varepsilon_Z}{1-r^2} \right)^2$$

$S_{\text{DZ}} = -U_{\text{DZ}}$ for all ε_Z and r

When $r \gg 1$, $|T_{\text{DZ}}| \gg |S_{\text{DZ}}| = |U_{\text{DZ}}|$



S, T, U parameters in the pure dark Z limit

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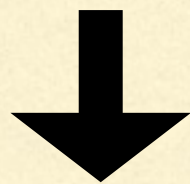
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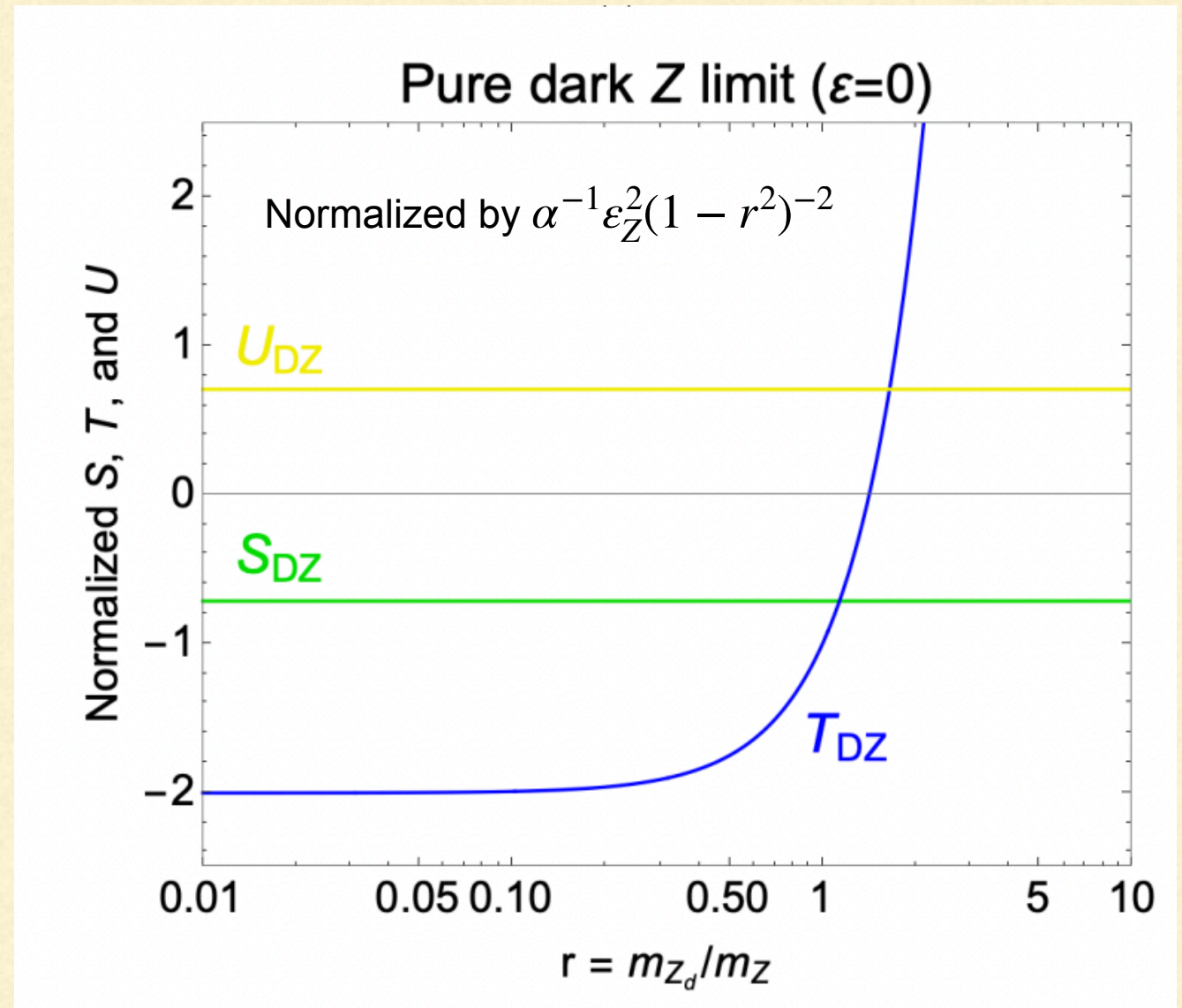
$$\alpha U_{\text{DZ}} = 4s_W^2 c_W^2 \left(\frac{\varepsilon_Z}{1-r^2} \right)^2$$

$$S_{\text{DZ}} = -U_{\text{DZ}} \text{ for all } \varepsilon_Z \text{ and } r$$

When $r \gg 1$, $|T_{\text{DZ}}| \gg |S_{\text{DZ}}| = |U_{\text{DZ}}|$



$$\Delta m_W^2 \simeq T_{\text{DZ}} \times (35 \text{ GeV}^2)$$



CDF-II result ($\Delta m_W^2 \simeq 12.5 \text{ GeV}^2$) requires

$$T_{\text{DZ}} \simeq 0.18$$

$$T = 0.11(12)$$

Within 2σ region
($\sim 0.6\sigma$)

The relation $S_{DZ} = -U_{DZ}$

$$\Delta\mathcal{L}_{\text{gauge}} = \frac{1}{2}\tilde{m}_Z^2\Delta_1 Z^\mu Z_\mu - \frac{g}{2c_W}\Delta_2 J_{\text{NC}}^\mu Z_\mu - e\Delta_3 J_{\text{EM}}^\mu Z_\mu$$

In the pure dark Z limit ($\varepsilon = 0$), $\Delta_3 = -\eta\varepsilon \sin\xi = 0$ $\eta = 1/\sqrt{1 - \varepsilon^2/c_W^2}$

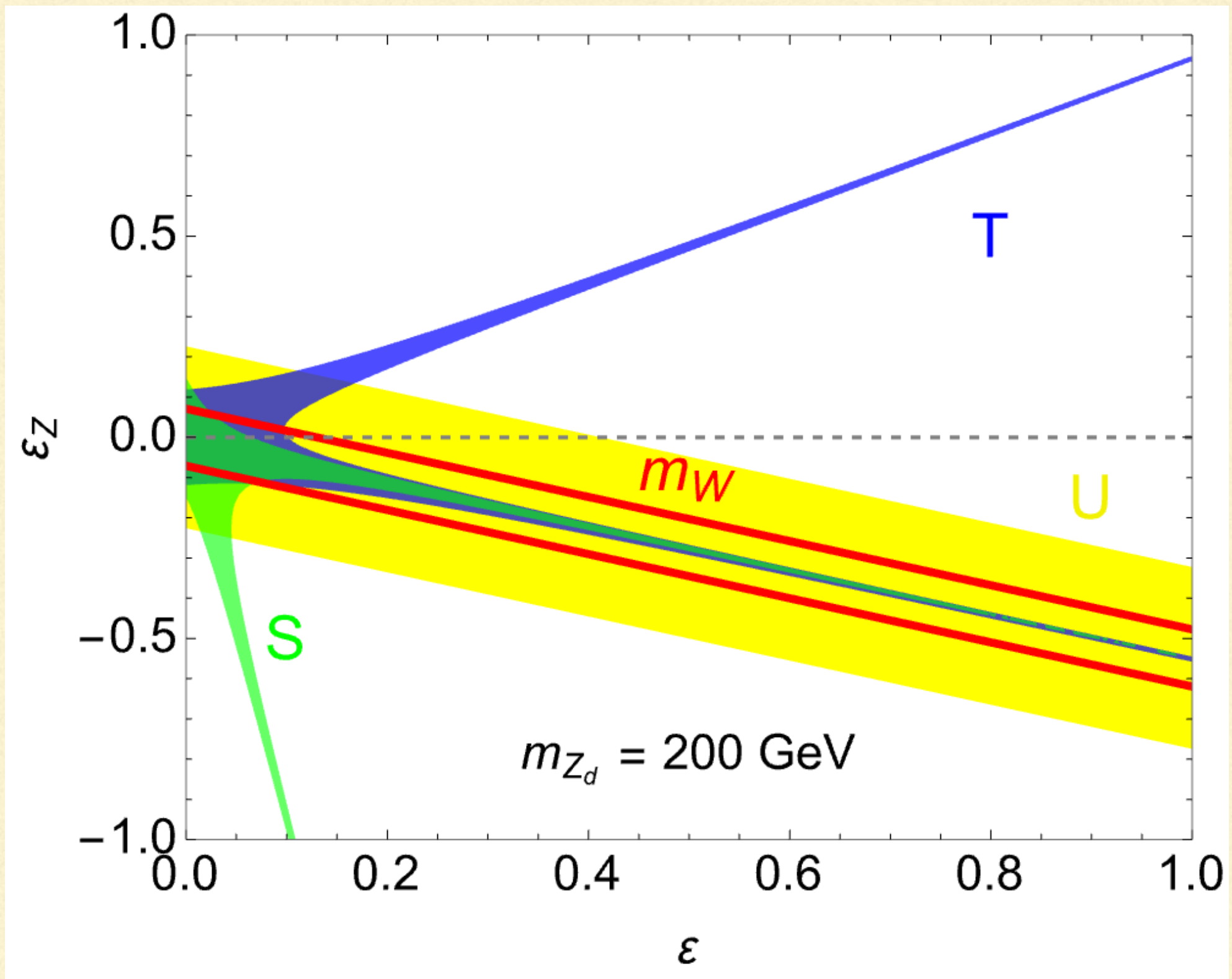
$$\Delta_1, \Delta_2 \neq 0$$

$$\alpha S = 8s_W^2 c_W^2 \Delta_2 - 4s_W c_W (c_W^2 - s_W^2) \Delta_3 = 8s_W^2 c_W^2 \Delta_2$$

$$\alpha U = -8s_W^2 c_W (c_W \Delta_2 + s_W \Delta_3) = -8s_W^2 c_W^2 \Delta_2$$

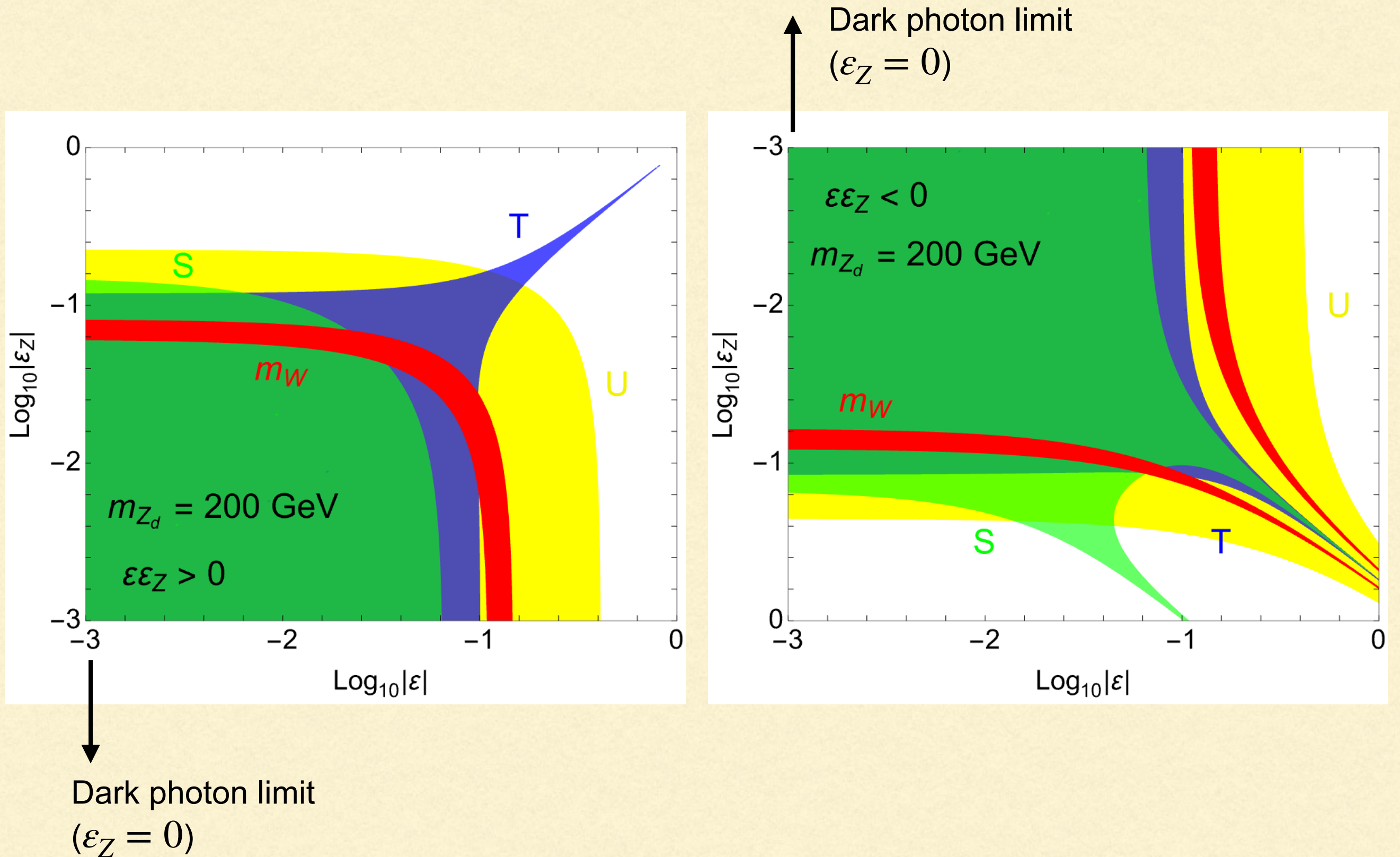
$$\longrightarrow S = -U$$

W boson mass anomaly & EW global fit



Colored regions = 2σ regions

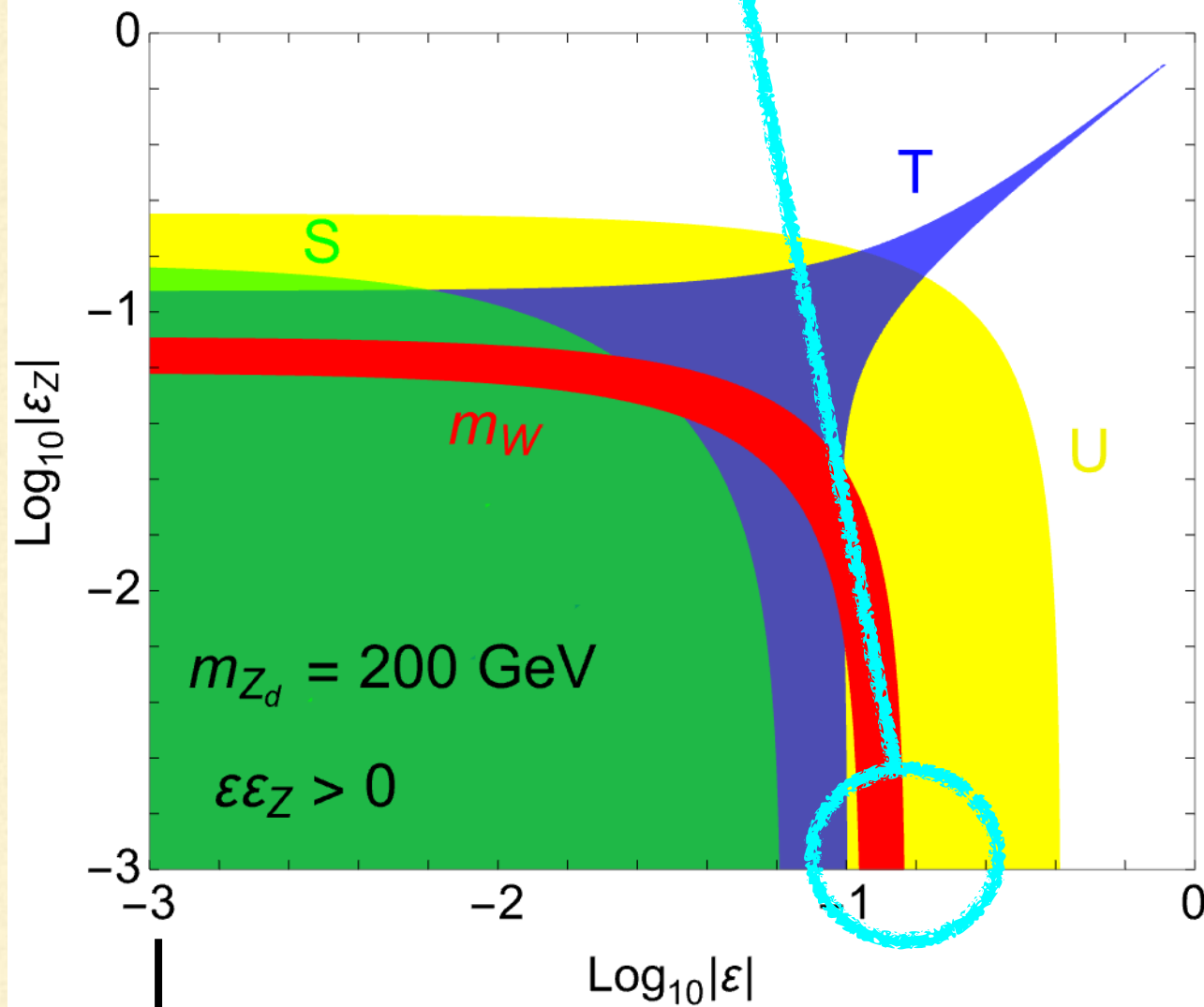
W boson mass anomaly & EW global fit



W boson mass anomaly & EW global fit

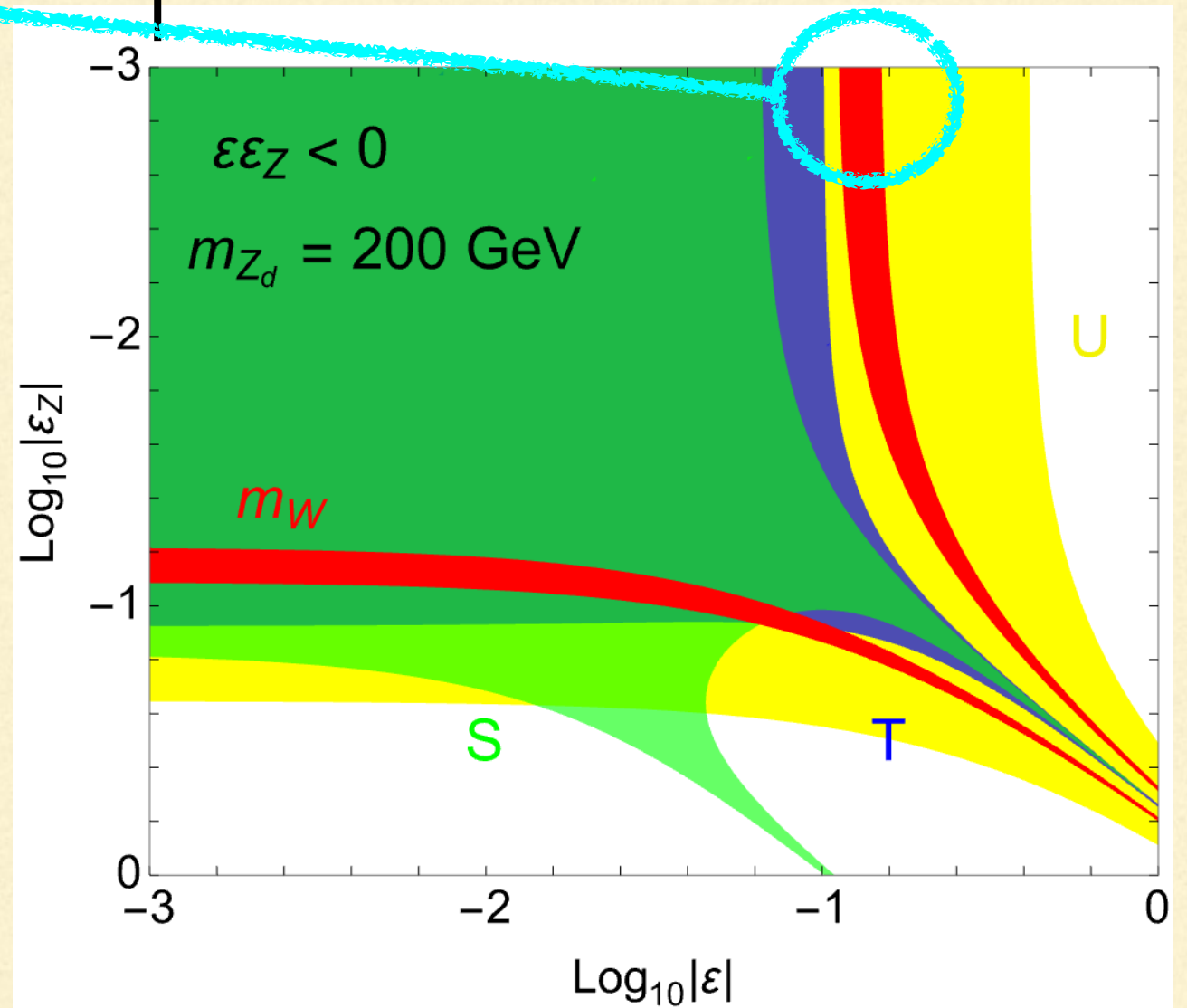
No overlap region
in dark photon limit

[Cheng et al, 2204.10156](#)
[Thomas, Wang, 2205.01911](#)
[Asagi et al, 2204.05283](#)



Dark photon limit
($\epsilon_Z = 0$)

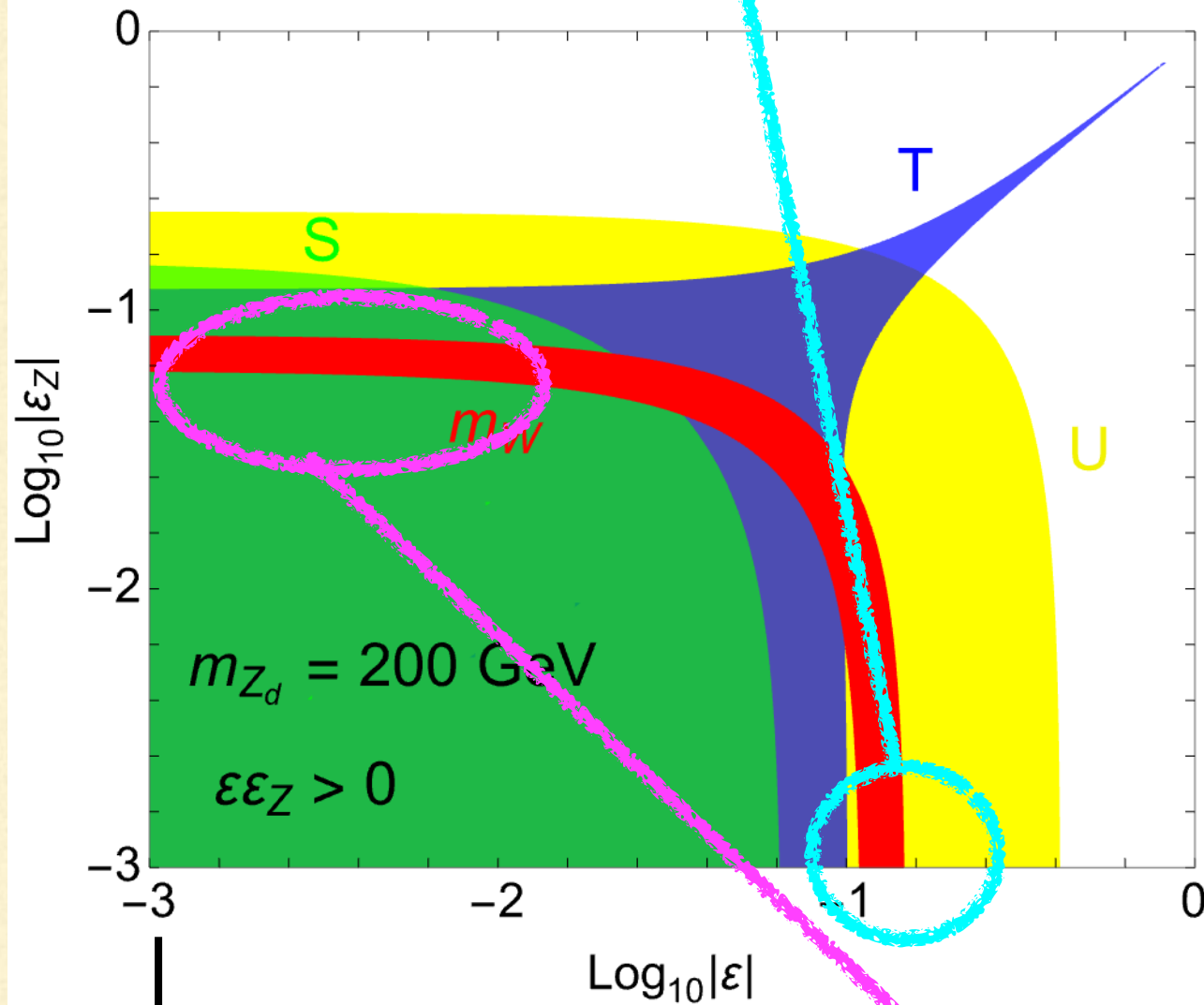
Dark photon limit
($\epsilon_Z = 0$)



W boson mass anomaly & EW global fit

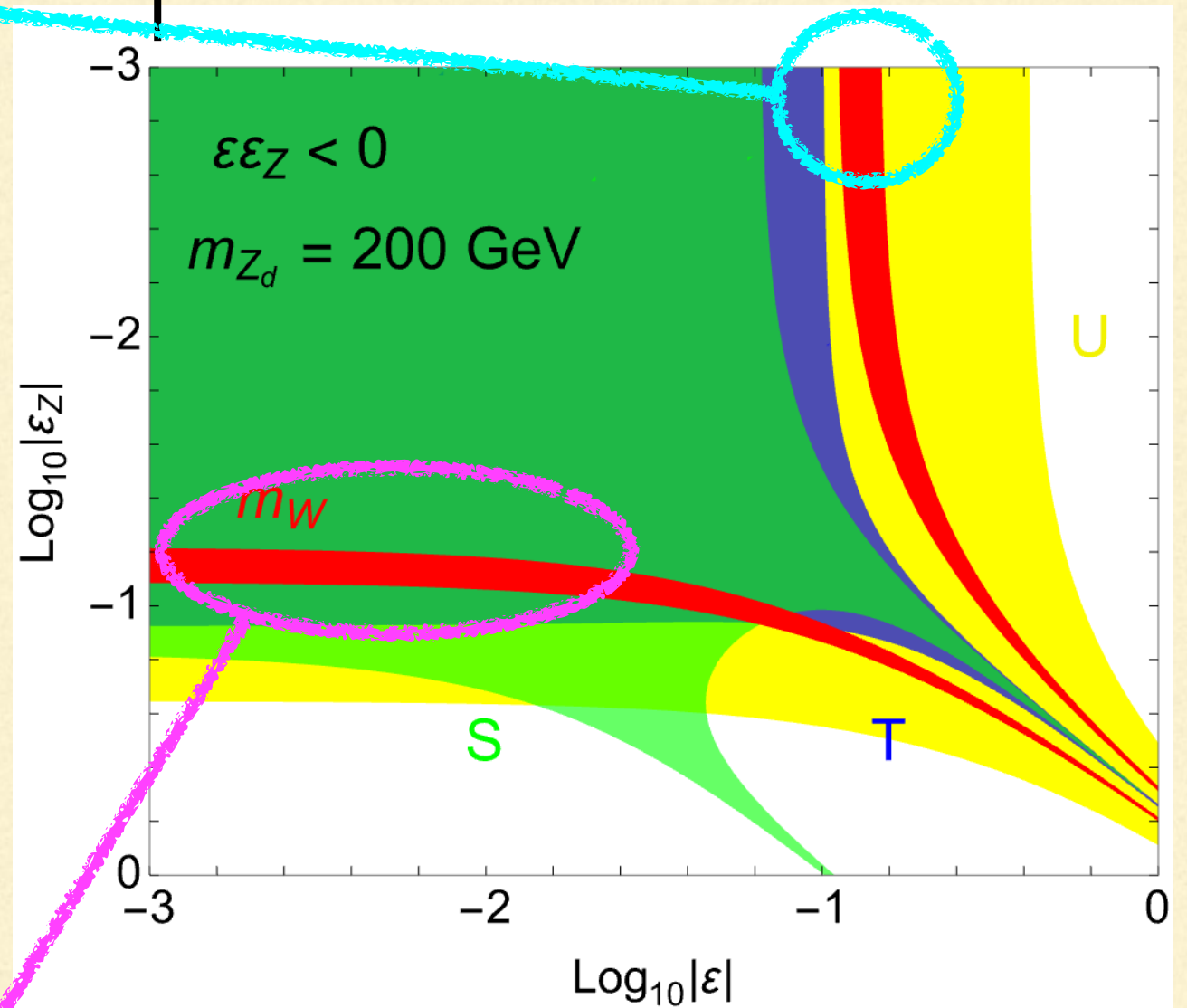
No overlap region
in dark photon limit

[Cheng et al, 2204.10156](#)
[Thomas, Wang, 2205.01911](#)
[Asagi et al, 2204.05283](#)



Dark photon limit
($\epsilon_Z = 0$)

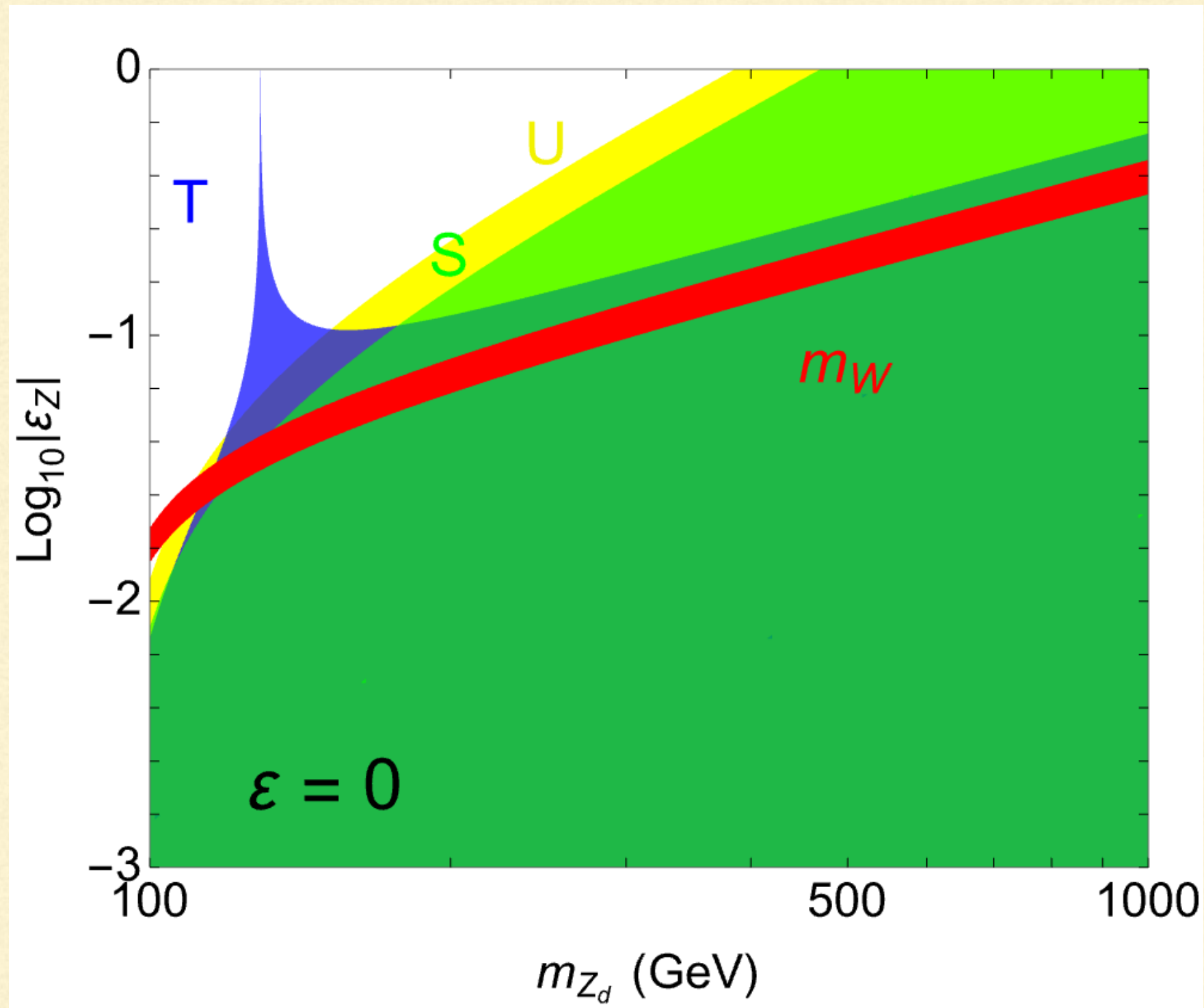
Dark photon limit
($\epsilon_Z = 0$)



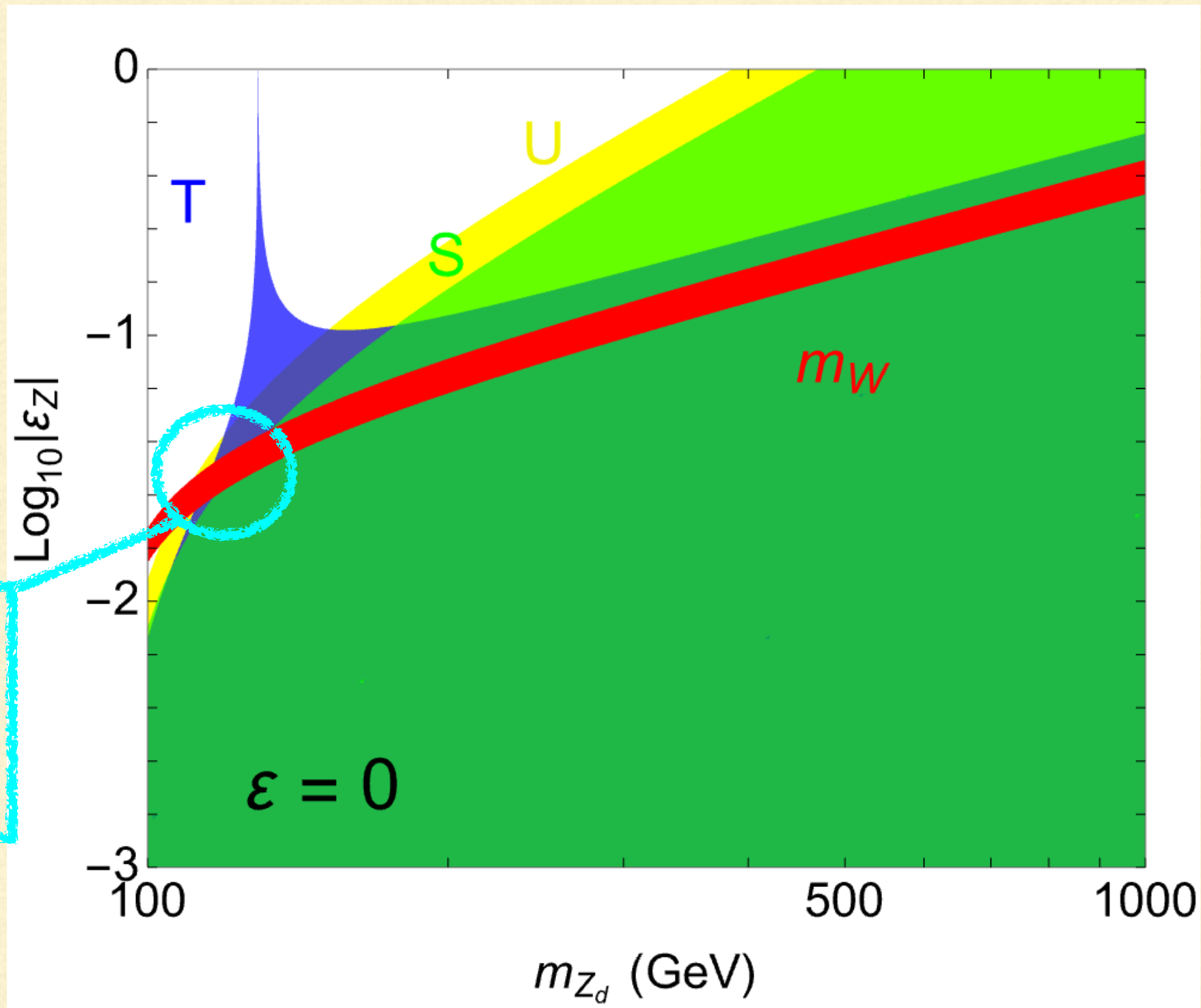
CDF-II result can be explained

with $|\epsilon_Z| = O(0.1)$ and small ϵ

W boson mass anomaly & EW global fit

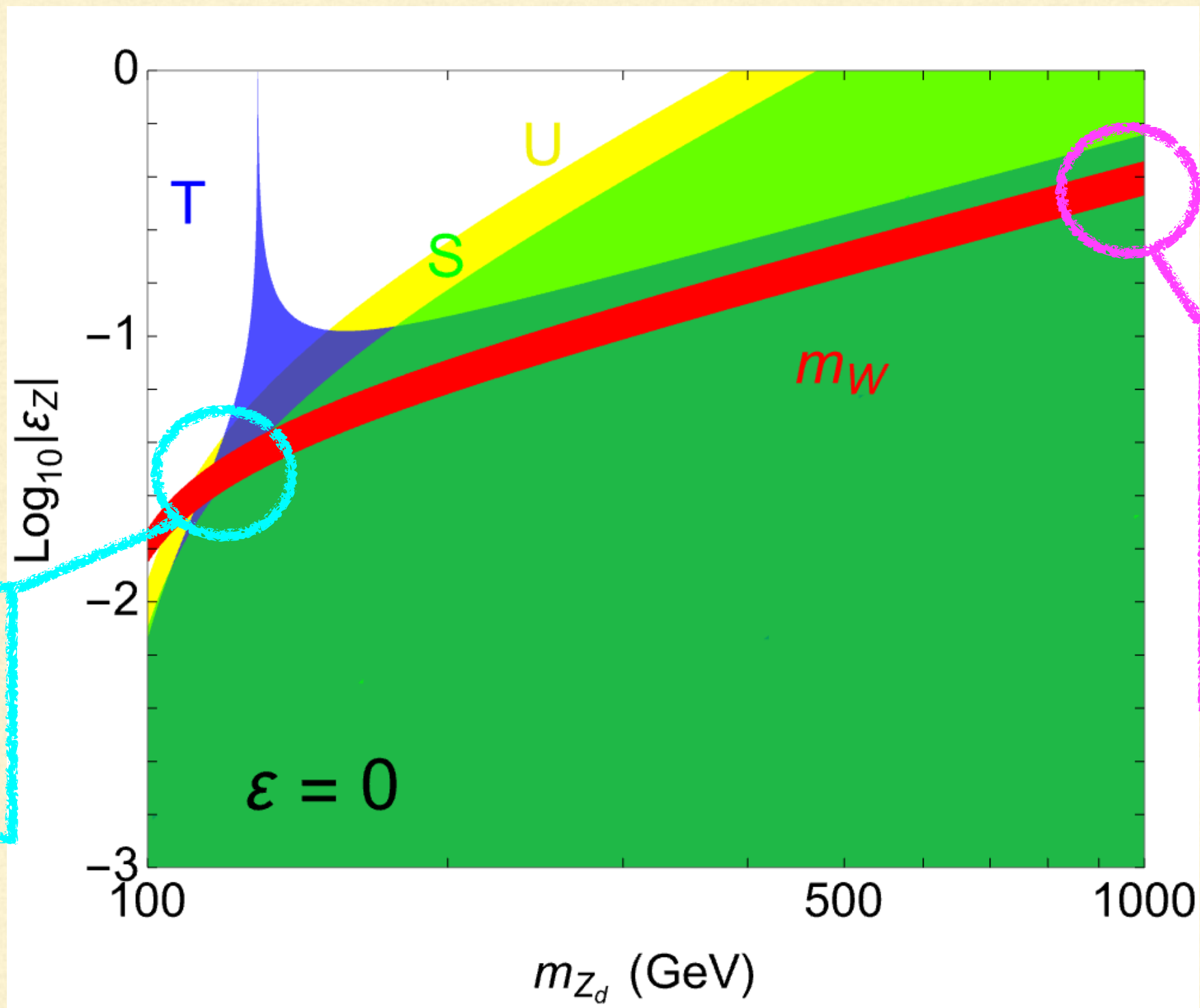


W boson mass anomaly & EW global fit



Minimum m_{Z_d}
 $m_{Z_d} \simeq 130$ GeV
($|\epsilon_Z| \simeq 0.03$)

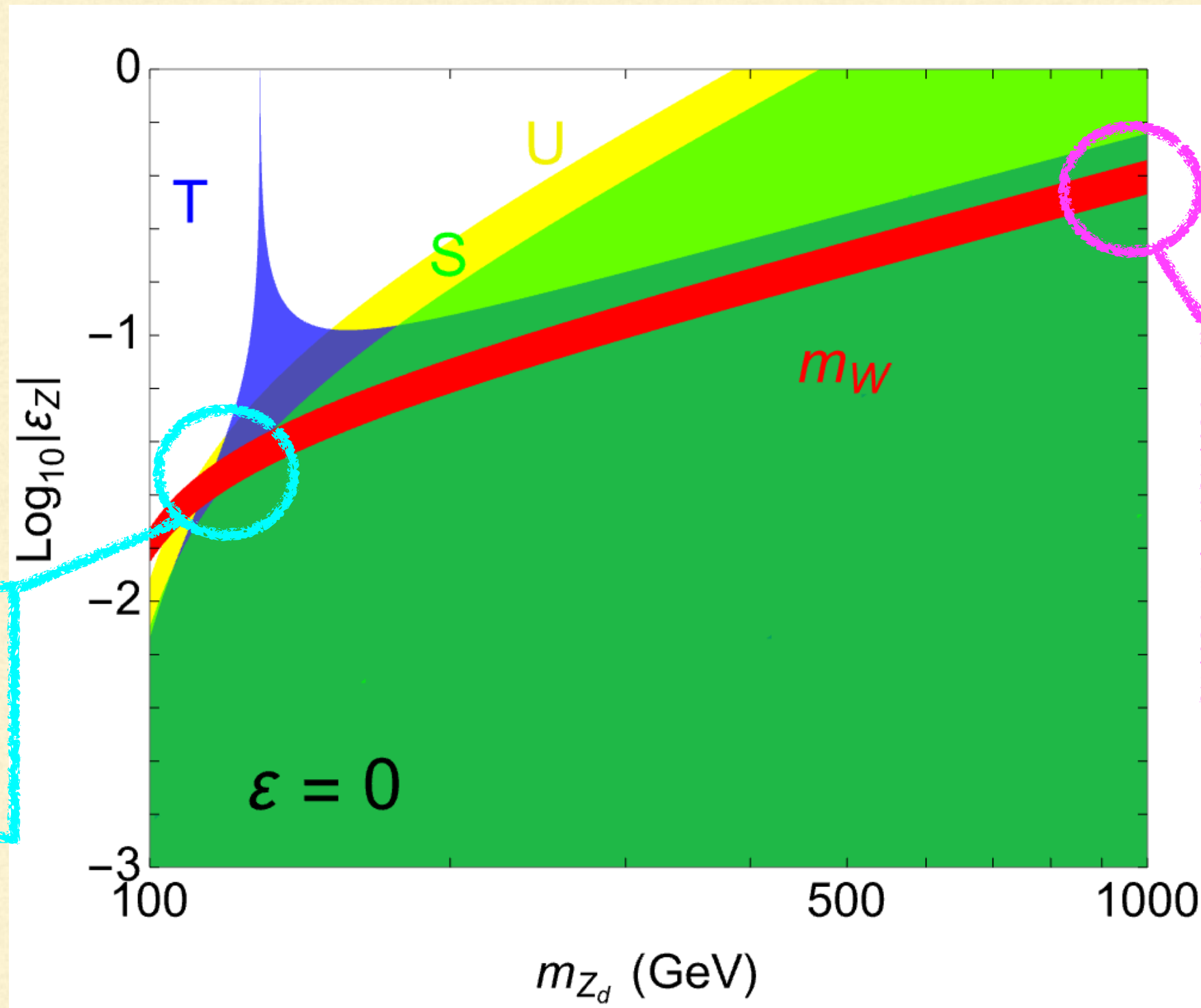
W boson mass anomaly & EW global fit



Minimum m_{Z_d}
 $m_{Z_d} \simeq 130$ GeV
($|\epsilon_Z| \simeq 0.03$)

Large ϵ_Z
for heavier Z_d
||
Perturbation
is not good

W boson mass anomaly & EW global fit



Minimum m_{Z_d}
 $m_{Z_d} \simeq 130$ GeV
 $(|\epsilon_Z| \simeq 0.03)$

Large ϵ_Z
 for heavier Z_d
 ||
 Perturbation
 is not good

Heavy Z_d ($m_{Z_d} = O(100)\text{GeV}$) and relatively large $|\epsilon_Z|$ ($\gtrsim 0.03$)

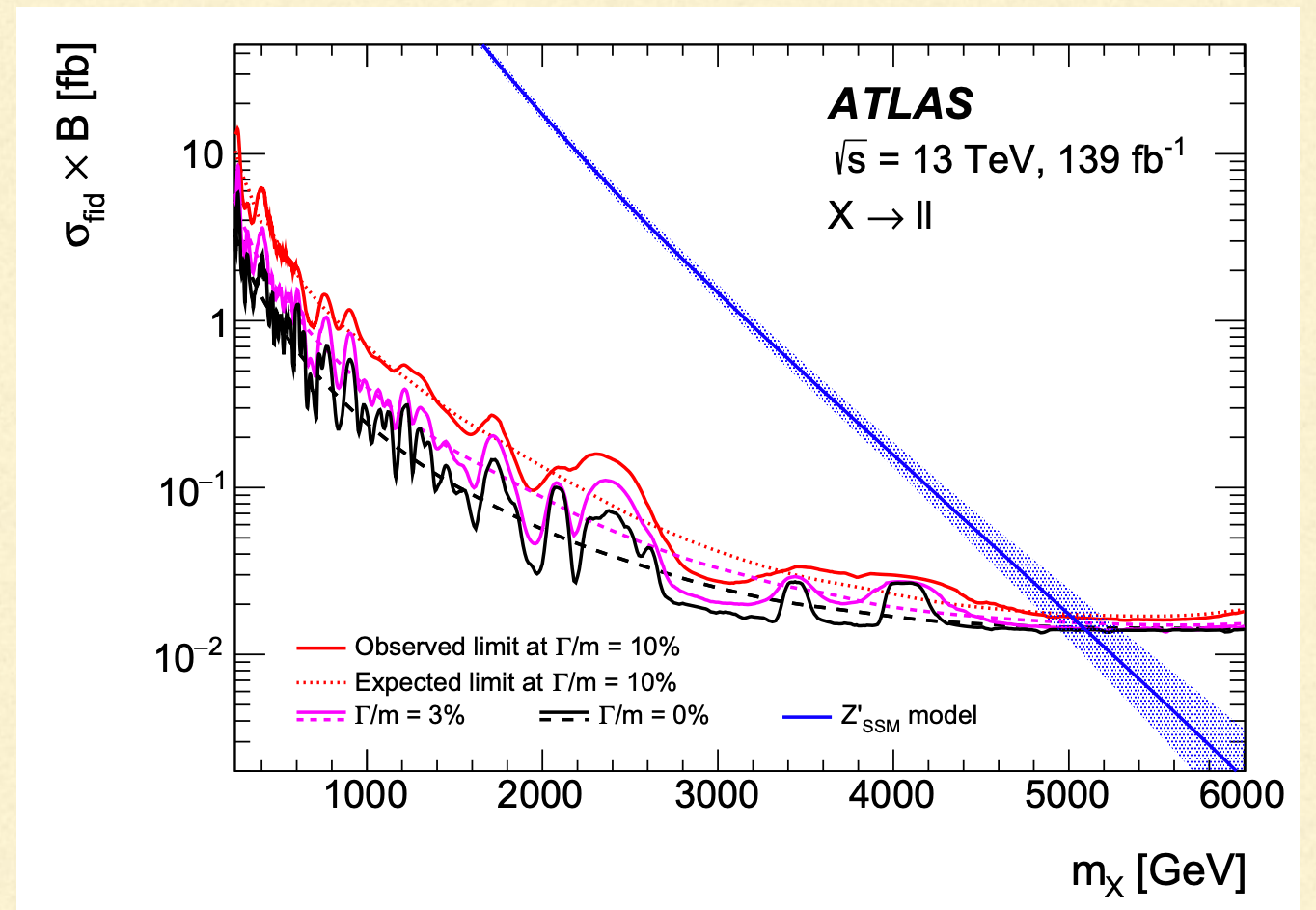
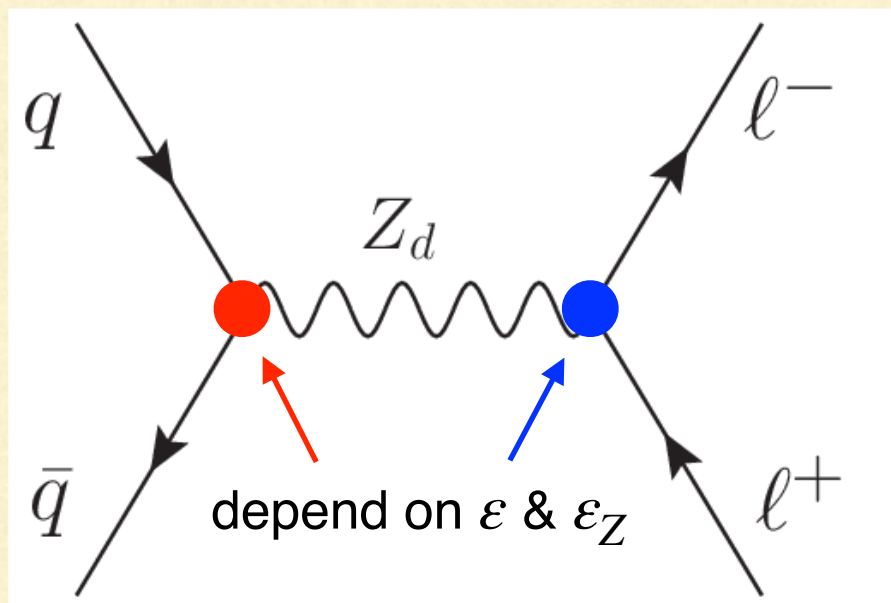
Constraint from direct searches

$$m_{Z_d} = O(100) \text{ GeV}$$

$$|\varepsilon_Z| = 0.03 - O(0.1)$$

Dilepton resonant search @ LHC [ATLAS, 1903.06248](#)

$$pp \rightarrow Z_d \rightarrow \ell^+ \ell^- \quad (225 \text{ GeV} \leq m_{Z_d} \leq 6000 \text{ GeV})$$



Dijet resonant search is not effective in the relevant mass range

[CMS, 1911.03947](#)

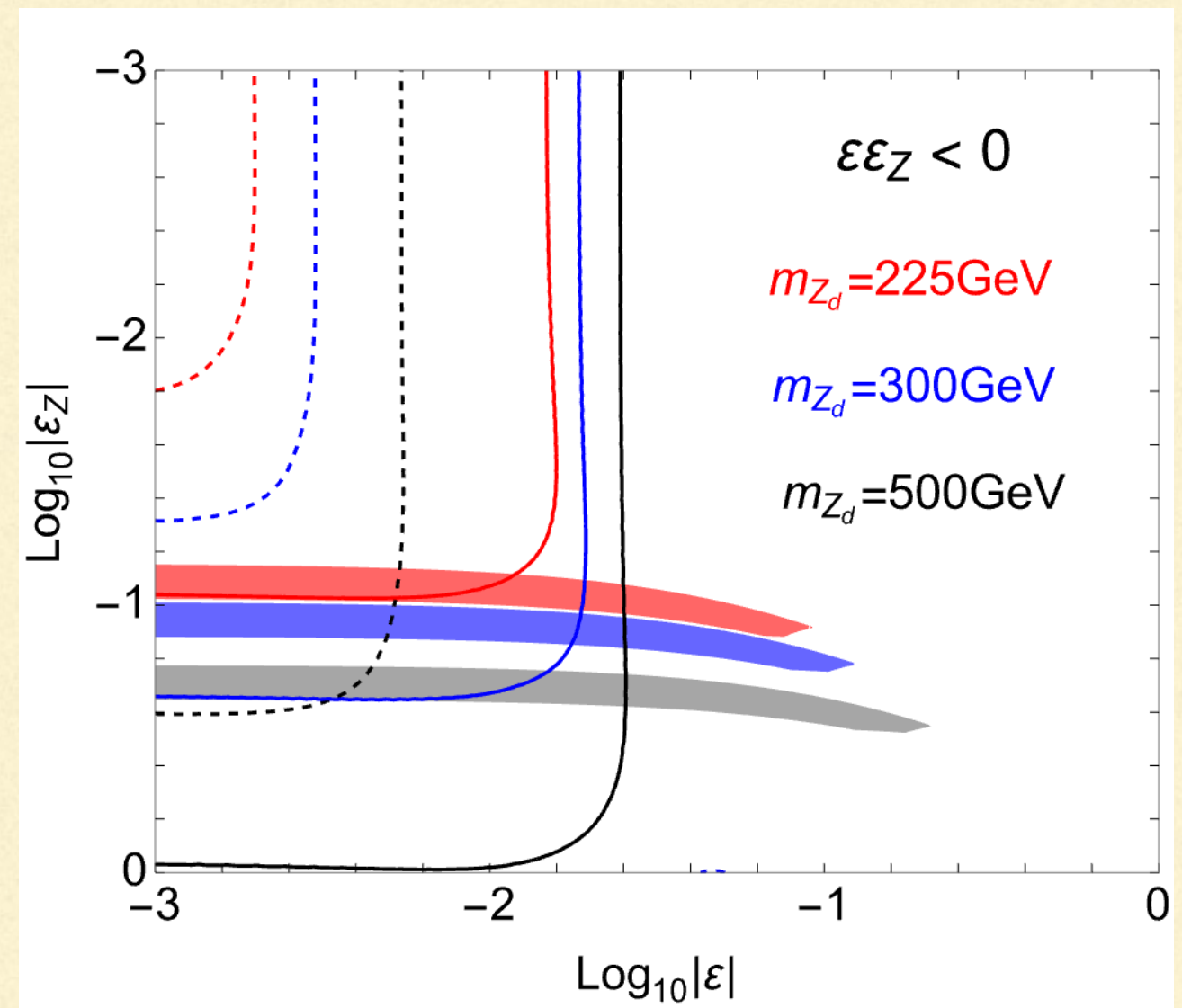
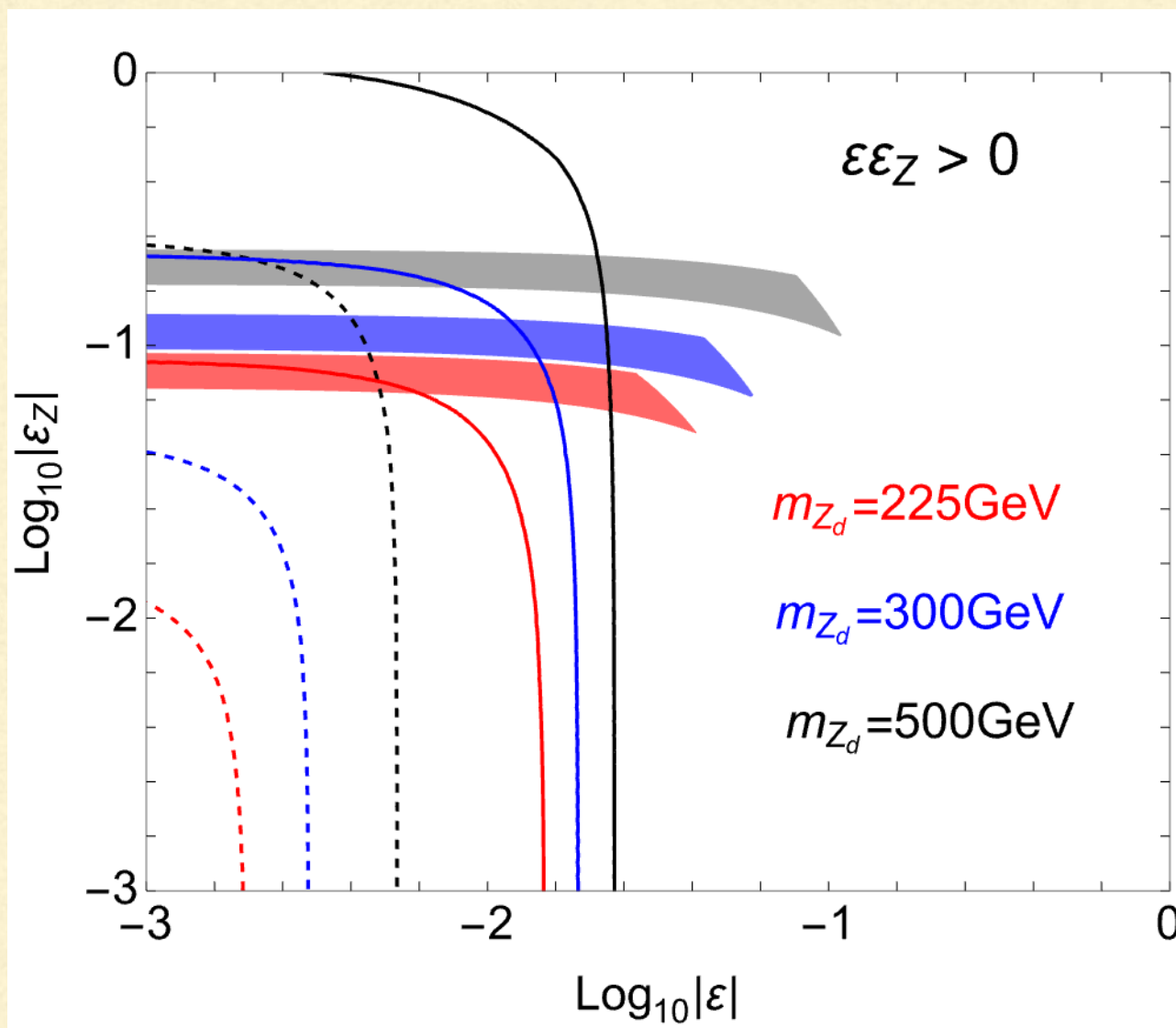
[ATLAS, 1903.06248](#)

Constraint from direct searches

The constraint depends on $\text{Br}[Z_d \rightarrow \ell^+ \ell^-]$

Case 1: Only the SM fermions (Dashed lines)

Case 2: Including a dark fermion [$m_\psi = 50$ GeV, $g_d = 0.1$] (Solid lines)



Colored regions: CDF-II result & EW global fit within 2σ

Summary

- **New $U(1)$ gauge symmetry** is an attractive candidate for new physics.
- The dark Z model includes **mass mixing ε_Z independent of kinetic mixing ε** and provides richer phenomenology.
- **Heavy dark Z bosons** with relatively **large ε_Z** can reproduce the CDF-II result of m_W and the result of EW global fit.

$$m_{Z_d} = \mathcal{O}(100) \text{ GeV} > m_Z, \quad \varepsilon_Z \geq 0.03$$

- Such a dark Z is constrained by the **dilepton resonant searches**.
Considering **dark decay channels**, this constraint is relaxed.

Thank you for listening!

Backup Slides

Mass eigenstate of neutral gauge bosons

$$\mathcal{L}_{\text{kin}} = -\frac{1}{4}\hat{B}^{\mu\nu}\hat{B}_{\mu\nu} + \frac{\varepsilon}{2\cos\theta_W}\hat{B}^{\mu\nu}\hat{Z}_{d\mu\nu} - \frac{1}{4}\hat{Z}_d^{\mu\nu}\hat{Z}_{d\mu\nu},$$

Digonalize the kinetic term

$$\begin{pmatrix} \tilde{B}_\mu \\ \tilde{Z}_{d\mu} \end{pmatrix} = \begin{pmatrix} 1 & -\varepsilon/c_W \\ 0 & \sqrt{1 - \varepsilon^2/c_W^2} \end{pmatrix} \begin{pmatrix} \hat{B}_\mu \\ \hat{Z}_{d\mu} \end{pmatrix}$$

Mass matrix for \tilde{B}_μ and $\tilde{Z}_{d\mu}$

$$\mathcal{L}_{\text{mass}} = m_W^2 W_\mu^+ W^{-\mu} + \frac{1}{2}(\tilde{Z}^\mu, \tilde{Z}_d^\mu) M_V^2 \begin{pmatrix} \tilde{Z}_\mu \\ \tilde{Z}_{d\mu} \end{pmatrix},$$

$$\tilde{Z}_\mu = -\sin\theta_W \tilde{B}_\mu + \cos\theta_W \hat{W}_\mu^3, \quad \tan\theta_W = g'/g$$

$$M_V^2 = \begin{pmatrix} \tilde{m}_Z^2 & -\tilde{m}_Z^2 \eta(\varepsilon_Z + \varepsilon t_W) \\ -\tilde{m}_Z^2 \eta(\varepsilon_Z + \varepsilon t_W) & \tilde{m}_{Z_d}^2 \end{pmatrix} \quad \eta = \frac{1}{\sqrt{1 - \varepsilon^2/c_W^2}}$$

Mass eigenstate of neutral gauge bosons

Mass eigenstates Z_μ and $Z_{d\mu}$

$$\begin{pmatrix} Z_\mu \\ Z_{d\mu} \end{pmatrix} = \begin{pmatrix} \cos \xi & -\sin \xi \\ \sin \xi & \cos \xi \end{pmatrix} \begin{pmatrix} \tilde{Z}_\mu \\ \tilde{Z}_{d\mu} \end{pmatrix}$$

Mixing matrix

$$\sin \xi \simeq \frac{\varepsilon_Z + \varepsilon t_W}{1 - r^2},$$

$$\cos \xi \simeq 1 - \frac{1}{2} \left(\frac{\varepsilon_Z + \varepsilon t_W}{1 - r^2} \right)^2,$$

$$r = m_{Z_d} / m_Z$$

Mass eigenvalues

$$m_Z^2 \simeq \tilde{m}_Z^2 \left(1 + \frac{(\varepsilon_Z + \varepsilon t_W)^2}{1 - \tilde{r}^2} \right),$$

$$m_{Z_d}^2 \simeq \tilde{m}_{Z_d}^2 \left(1 - \frac{\varepsilon_Z^2}{\tilde{r}^2(1 - \tilde{r}^2)} - \frac{\varepsilon^2 t_W^2 + 2\varepsilon_Z \varepsilon t_W}{1 - \tilde{r}^2} \right),$$

$$\tilde{r} = \tilde{m}_{Z_d} / \tilde{m}_Z$$

The covariant derivative in mass eigenstate basis

$$D_\mu = \partial_\mu + igT^a\hat{W}_\mu + ig'Y\hat{B}_\mu + ig_d\mathcal{Q}_d\hat{Z}_{d\mu} + (\text{QCD term})$$

After diagonalization of kinetic terms and mass terms,

$$\begin{aligned} D_\mu = & \dots + \frac{ig}{c_W}(c_\xi + \eta s_\xi \epsilon t_W)(T^3 - s_W^2 Q)Z_\mu - ie\eta s_\xi \epsilon Q Z_\mu - ig_d \eta s_\xi \mathcal{Q}_d Z_\mu \\ & + \frac{ig}{c_W}(s_\xi - \eta c_\xi \epsilon t_W)(T^3 - s_W^2 Q)Z_{d\mu} + ie\eta c_\xi \epsilon Z_{d\mu} + ig_d \eta c_\xi \mathcal{Q}_d Z_{d\mu} \\ \simeq & \dots + \frac{ig}{c_W}(T^3 - s_W^2 Q)Z_\mu - ig_d \mathcal{Q}_d \left(\frac{\epsilon_Z + \epsilon t_W}{1 - r^2} \right) Z_\mu \\ & + \frac{ig}{c_W(1 - r^2)} (r^2 \epsilon t_W + \epsilon_Z) Z_{d\mu} + ie\epsilon Q Z_{d\mu} + ig_d \mathcal{Q}_d Z_{d\mu} \\ & \rightarrow 0 \quad (m_{Z_d}/m_Z \rightarrow 0) \end{aligned}$$

$S_{\text{DZ}}, T_{\text{DZ}}, U_{\text{DZ}}$ parameters in the decoupling limit

In the decoupling limit of Z_d ($r \rightarrow \infty$),
the generated dimension-six operator is only

$$O_{\varphi}'^{(6)} = O_2^{\mu} O_{2\mu} \quad O_2^{\mu} = \Phi_2^{\dagger} D^{\mu} \Phi_2 - (D^{\mu} \Phi_2)^{\dagger} \Phi_2$$

This induces the deviation of $\mathcal{O}(m_{Z_d}^{-2})$

$$\Delta_1 = \varepsilon_Z^2 r^{-2}, \quad \Delta_2 = 0, \quad \Delta_3 = 0.$$

$$\rightarrow \alpha S = 8s_W^2 c_W^2 \Delta_2 - 4s_W c_W (c_W^2 - s_W^2) \Delta_3 = 0$$

S is not generated by the $d = 6$ operator.

$$S_{\text{DZ}} \text{ and } U_{\text{DZ}} \text{ is generated by } \mathcal{O}_{\varphi}'^{(8)} = \frac{1}{2} O_{2\mu\nu} O_2^{\mu\nu}$$

$d = 8$ operator $(O_2^{\mu\nu} = \partial^{\mu} O_2^{\nu} - \partial^{\nu} O_2^{\mu})$