

// Nathan Killoran

# XANADU

Better than classical?  
The subtle art of benchmarking  
quantum ML models



QTM, November 2023

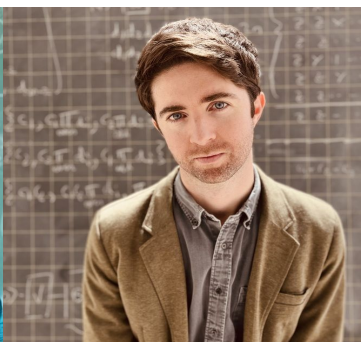
## Xanadu's quantum machine learning team



**Dr Maria Schuld**  
QML Team lead



**Dr Richard East**  
Researcher



**Dr Joseph Bowles**  
Researcher



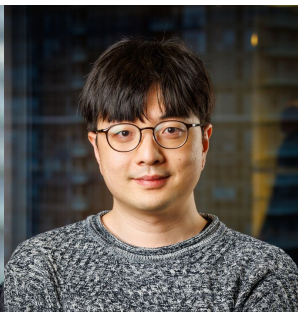
**Dr David Wakeham**  
Researcher



**Dr Shahnawaz Ahmed**  
Researcher



**Dr Nathan Killoran**  
CTO Software



**Dr Chae-Yeun Park**  
Researcher



**Dr David Wierichs**  
Researcher

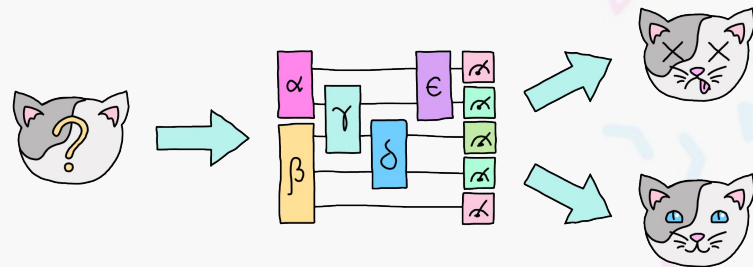
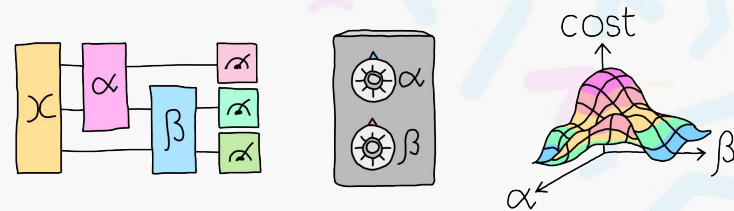


**Dr Korbinian Kottmann**  
Researcher

**We're hiring!**

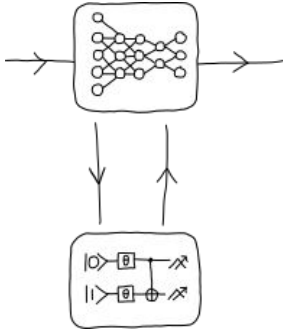
// The QML team objective

# Make quantum computers useful for machine learning



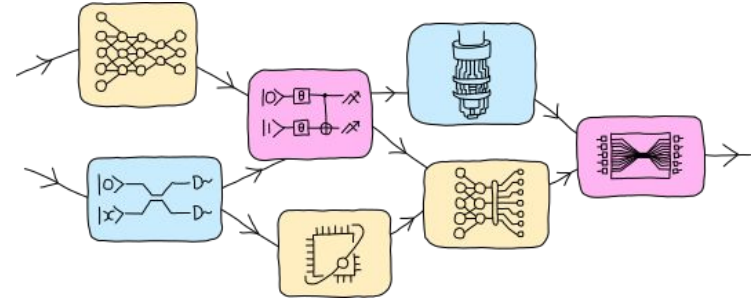
# Progress in quantum machine learning

## Pre-NISQ: Fault-tol. subroutines



Outsource parts of the computation to a quantum computer

## NISQ era: Variational circuits

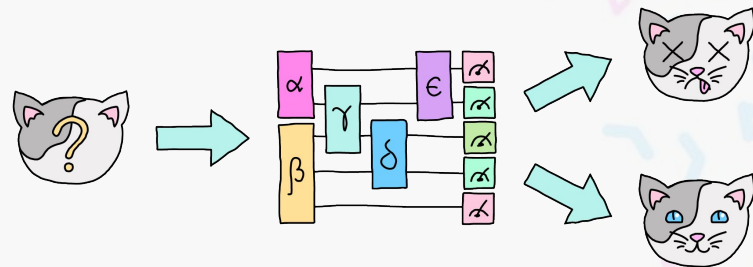
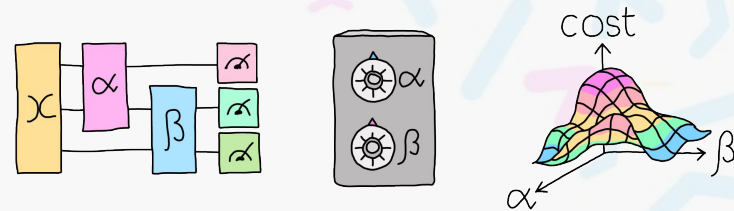


Use a model that is intrinsically quantum

// The QML team objective

# Make quantum computers useful for machine learning

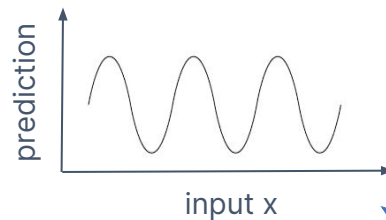
For this to happen we need to change some things in our approach to research



// Checking the compass: Model design

## “We use an ansatz of Pauli gates and entanglers...”

An impressive quantum circuit  
(of 10,000 qubits and 1 billion  
parameters with universal,  
classically intractable unitary  
evolutions imitating a deep learning  
technique)...



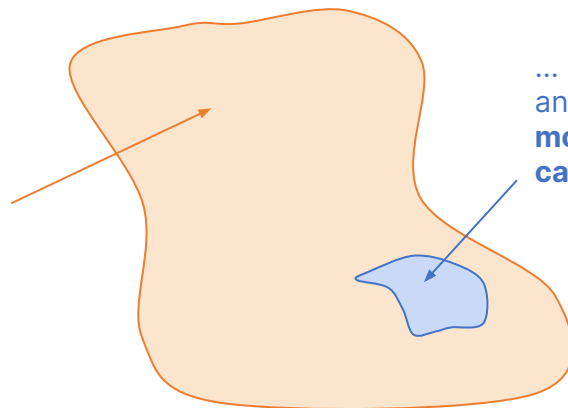
...can be a **useless ML model**.

Our circuit designs should be motivated better.

// Checking the compass: Model design

## “Quantum models generalise/train better/worse...”

**Theorems** about a very large class of models...



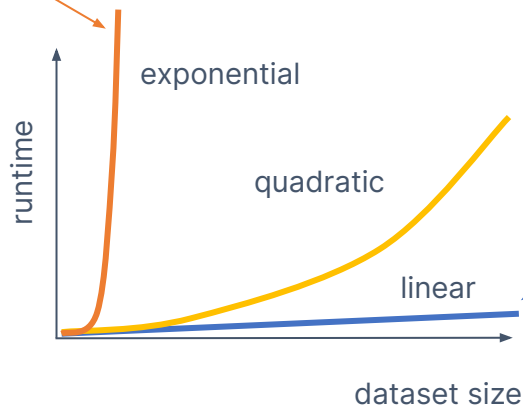
... may not tell us anything about the **models we eventually care about.**

We don't know if our theory targets relevant questions.

// Checking the compass: Performance

## “We prove an exponential speedup for QML...”

The problem that neural networks solve is **exponentially hard in theory...**



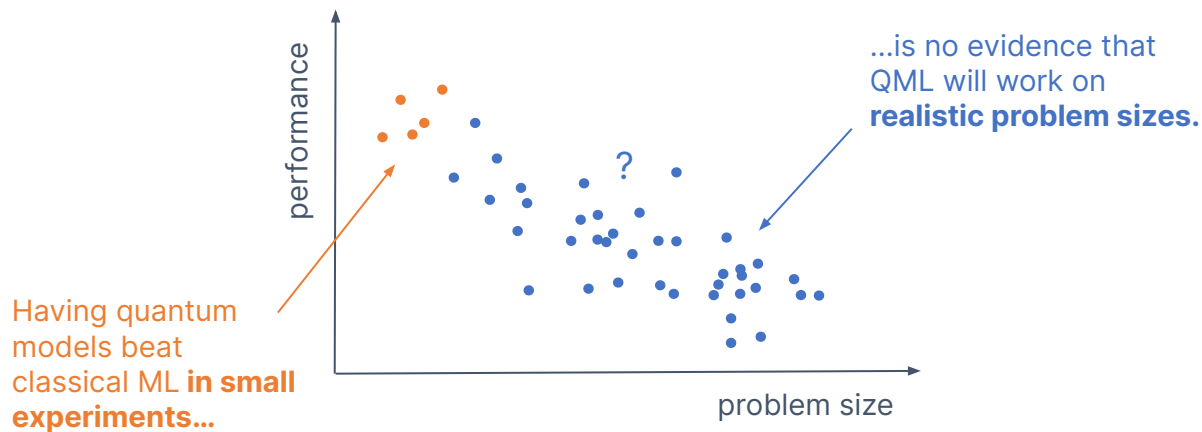
...but in practice neural nets run in **linear time.**

Our performance measures are not meaningful for (mainstream) ML.



// Checking the compass: Performance

## “Our quantum model does better on MNIST...”



Our experiments do not probe the right regimes yet.

# The subtle art of benchmarking

*[Note: work in progress!]*

// Assess how good quantum models really are

## What is the best benchmark design we can come up with?

### Model selection

- Arxiv papers >2018 with keywords “classif”, “learn”, “supervised”, “MNIST” [3500 papers]
- >=30 Google Scholar citations [561 papers]
- New NISQ quantum model for classification on conventional classical data [29 papers]
- In random subset of 15 papers
- Found implementable [11 papers]

→ Coded up 12 models

Pérez-Salinas et al. "Data re-uploading for a universal quantum classifier." 1907.02085v3

Mari et al. "Transfer learning in hybrid classical-quantum neural networks." 1912.08278v2

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QKernel

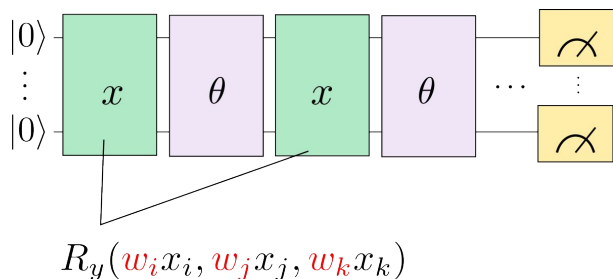
Henderson et al. "Quantum convolutional neural networks: powering image recognition.." 1904.04767v1

Wei "A quantum convolutional neural network on NISQ devices." 2104.06918v3

QConv

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DataReuploadingClassifier

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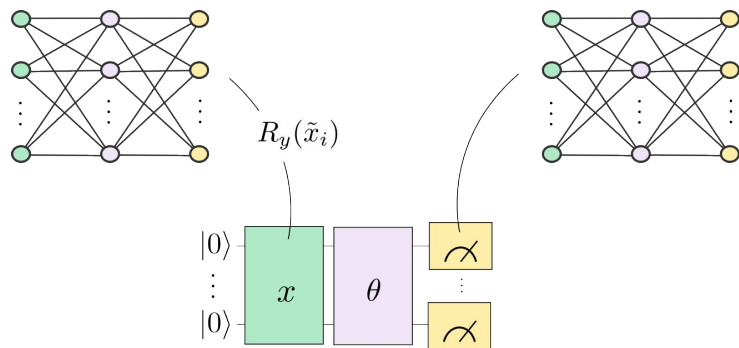
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DressedQuantumCircuitClassifier

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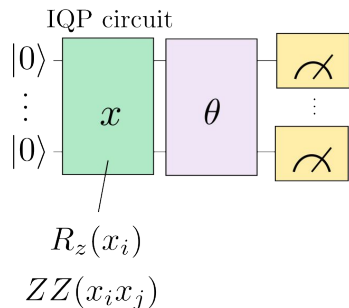
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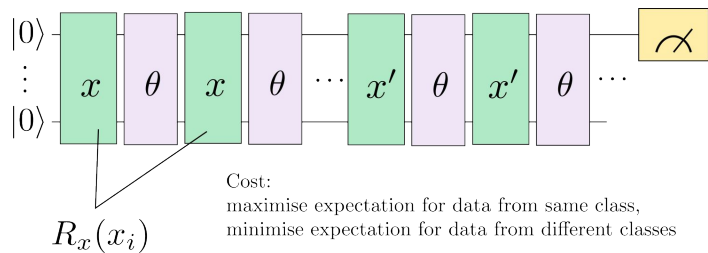
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QuantumMetricLearner

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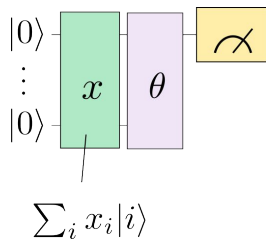
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CircuitCentricClassifier

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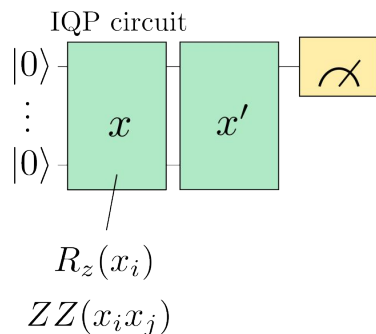
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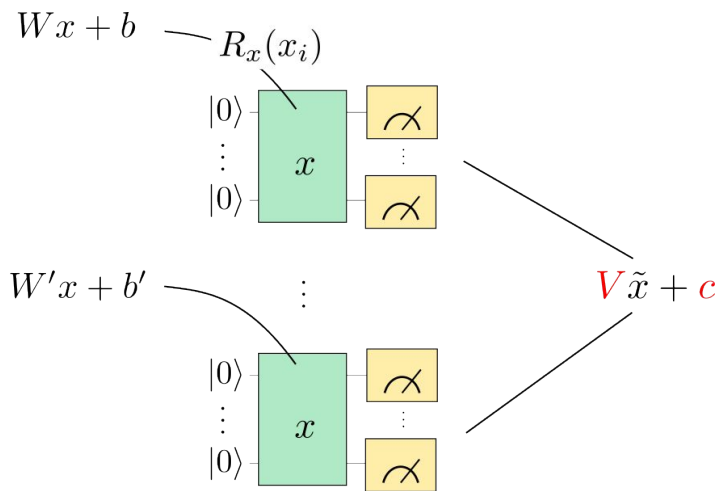
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QuantumKitchenSinks

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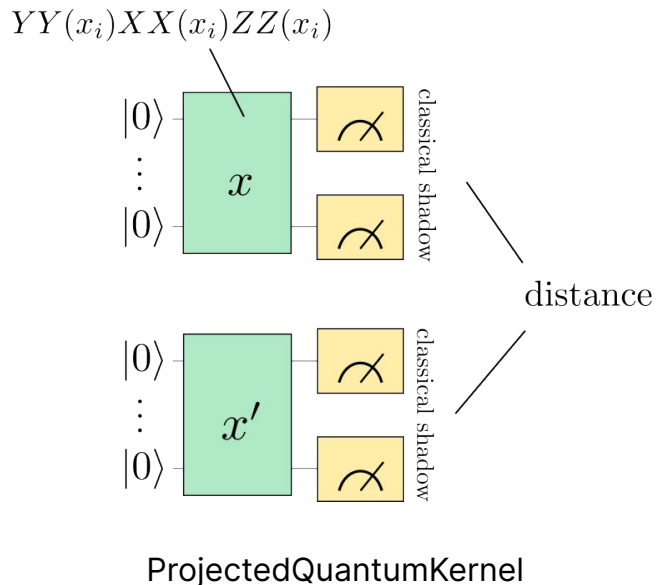
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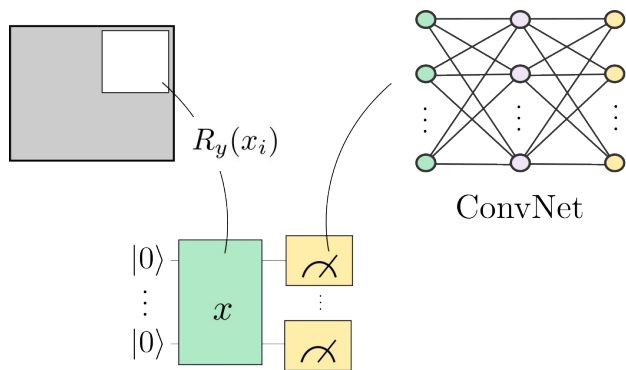
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Quantum Convolutional Neural Network

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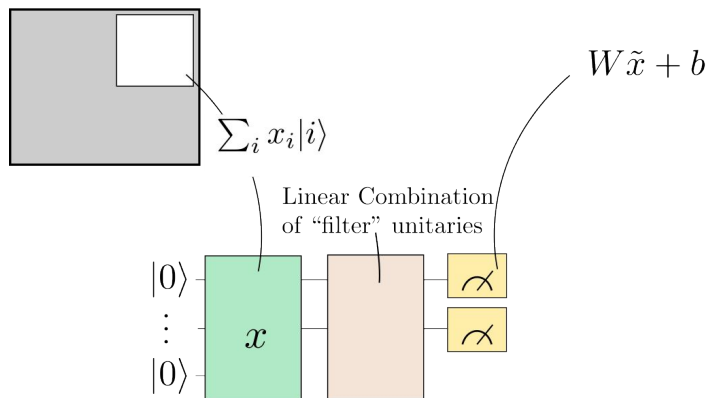
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WeiNet

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### Tasks

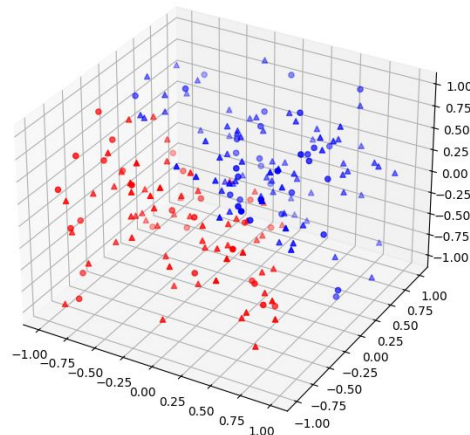
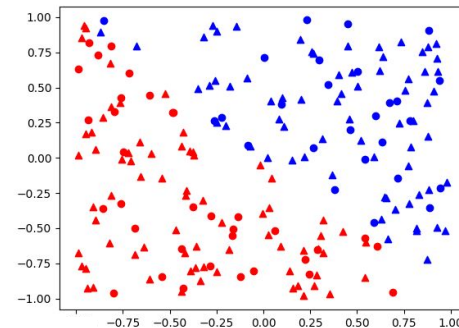
- Binary classification
- Figure of merit: accuracy
- 4 datasets of variable dimension:

// Assess how good quantum models really are

## What is the best benchmark design we can come up with?

### Tasks

- Binary classification
- Figure of merit: accuracy
- 4 datasets of variable dimension:
  - **SIMPLE:** Linearly separated points in hypercube

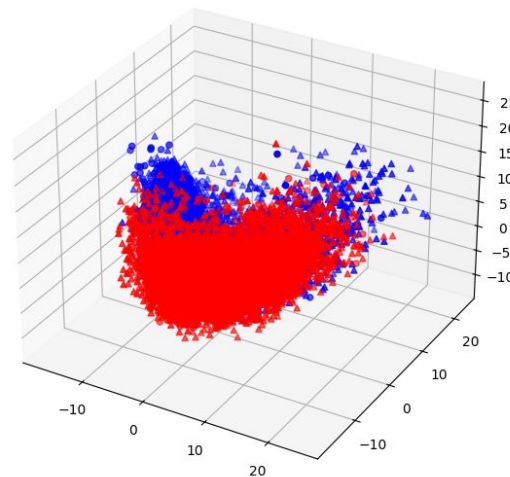
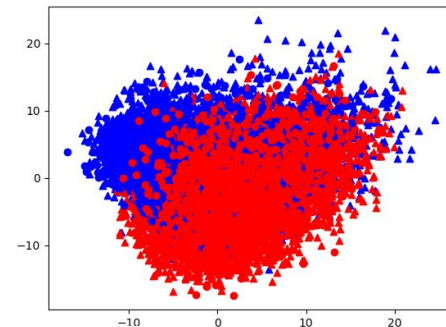


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## What is the best benchmark design we can come up with?

### Tasks

- Binary classification
- Figure of merit: accuracy
- 4 datasets of variable dimension:
  - **SIMPLE:** Linearly separated points in hypercube
  - **WIDELY USED:** Pre-processed MNIST



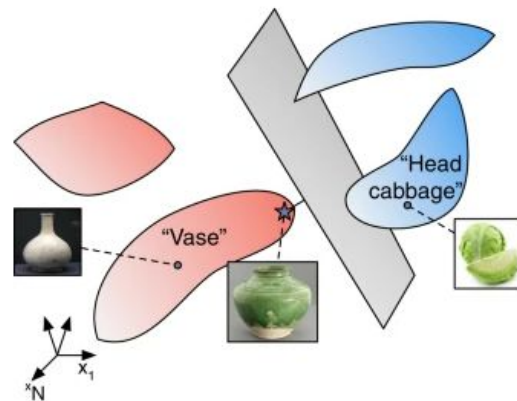


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## What is the best benchmark design we can come up with?

### Tasks

- Binary classification
- Figure of merit: accuracy
- 4 datasets of variable dimension:
  - **SIMPLE:** Linearly separated points in hypercube
  - **WIDELY USED:** Pre-processed MNIST
  - **[REALISTIC:** Low-dimensional manifolds (Goldt 2019, Buchanan 2020)]
  - **[TAILORMADE:** Multi-dimensional Fourier series]



<https://www.nature.com/articles/s41467-020-14578-5>



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## What is the best benchmark design we can come up with?

### Crucial decisions

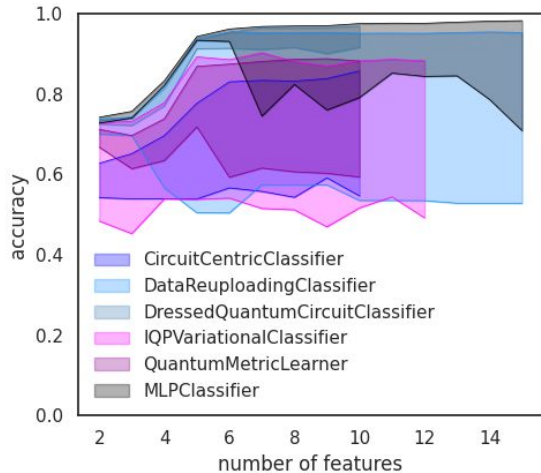
- **Faithful implementation**  
We carefully deduced the model design and training procedure from the paper
- **Convergence criteria**  
We compare averages over 2 loss intervals
- **Batches in SGD**  
We didn't optimize this hyperparameter, but adapted it to runtime needs
- **Data preprocessing**  
We always prescaled data to a meaningful interval (like  $[0, 2\pi]$ )
- **Hyperparameter optimisation grid**  
We balanced choices from paper, common sense and runtime considerations
- **Classical comparison**  
We pick matching box classical models with typical sizes: NN, SVM, CNN



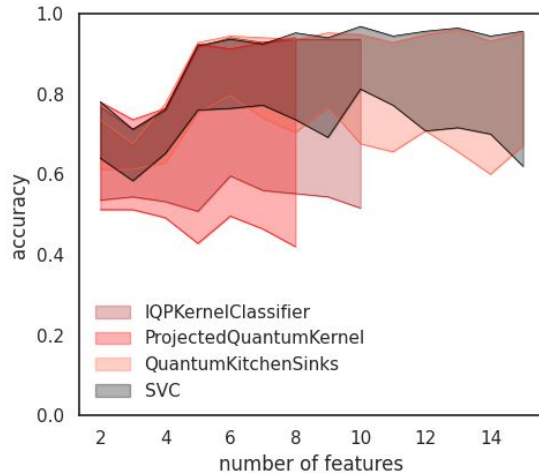
// Preliminary results

## Hyperparameters matter

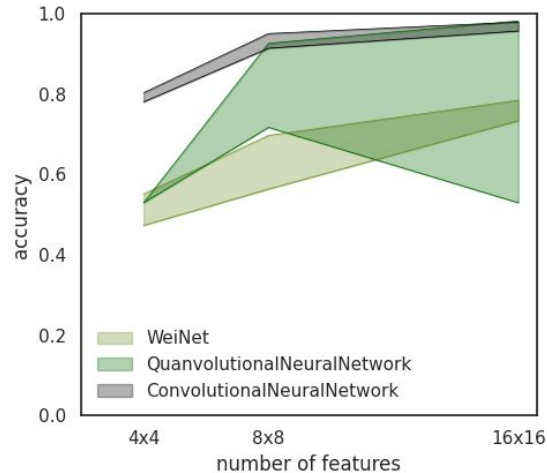
Test score range on PCA-reduced MNIST over all hyperparameters



Test score range on PCA-reduced+subs. MNIST over all hyperparameters

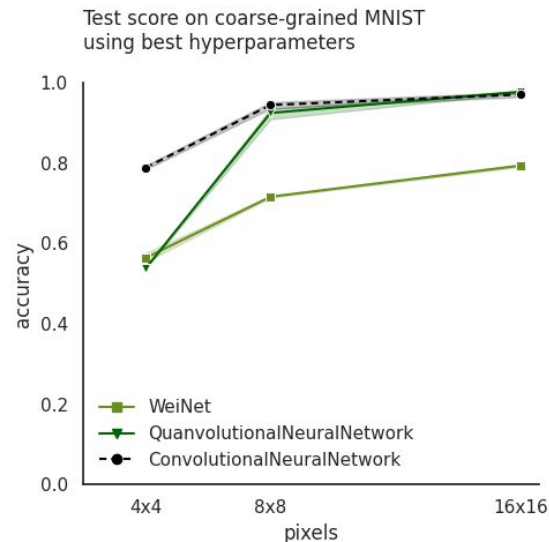
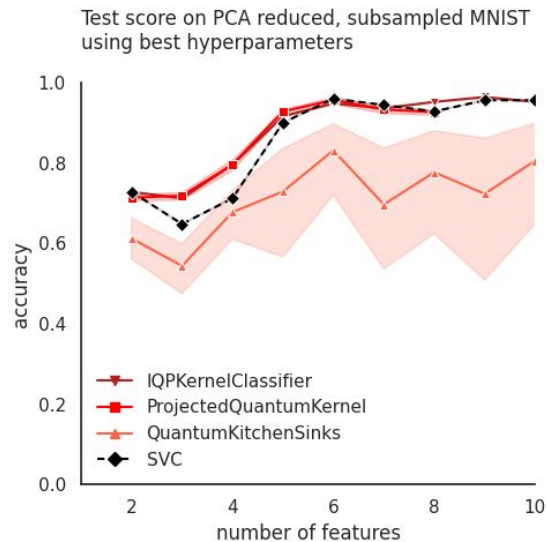
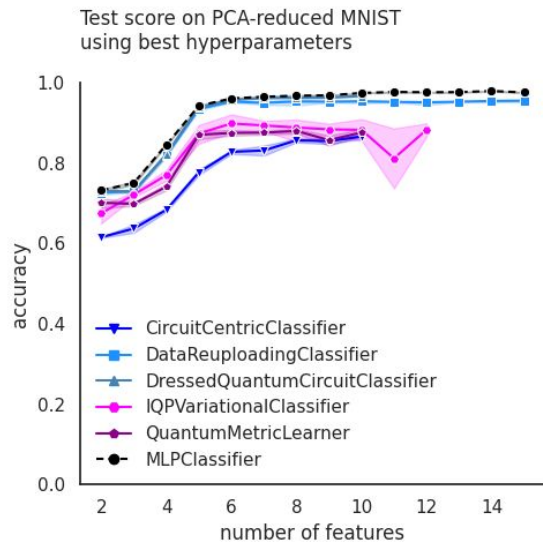


Test score range on coarse-grained MNIST over all hyperparameters



// Preliminary results

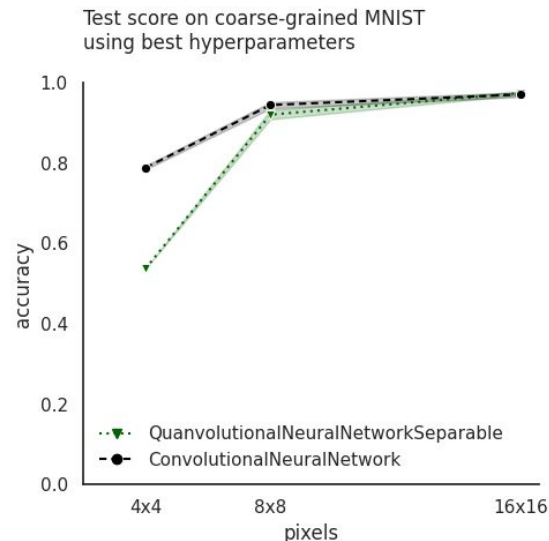
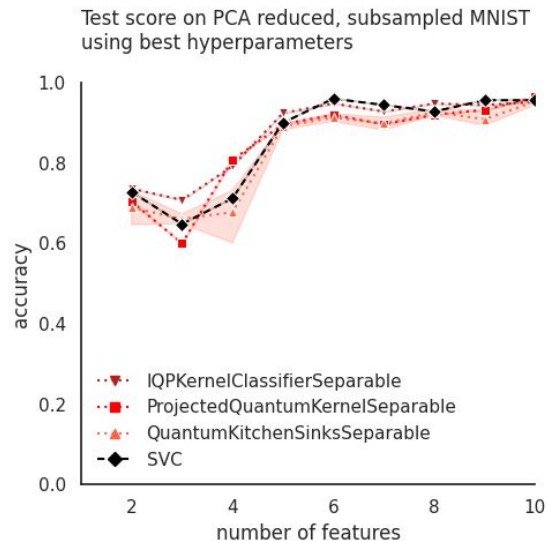
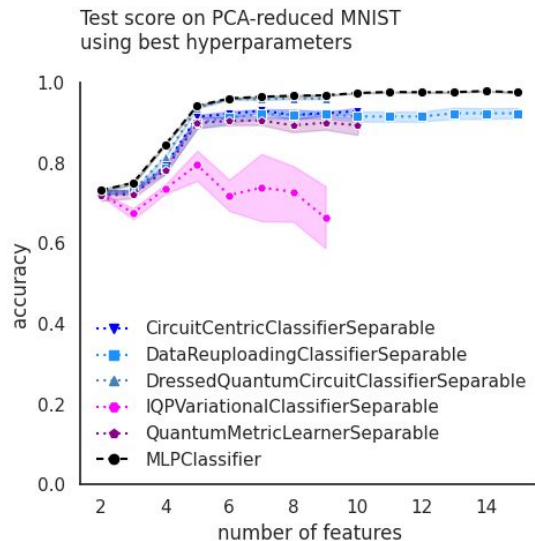
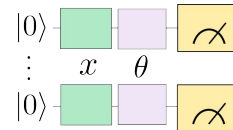
## Out-of-the box classical models are not easily beaten



// Preliminary results

## Separable circuits perform the same

This is (more or less) the basic circuit we replace all quantum circuits with!



// A possible explanation

## What “features” do our quantum models create?

Example for input  $x = [x_1, x_2]$

trigonometric

```
sin(x1)sin(x2)  
sin(x1)cos(x2)  
cos(x1)sin(x2)  
cos(x1)cos(x2)
```

Pérez-Salinas et al. "Data re-uploading for a universal quantum classifier." 1907.02085v3

Mari et al. "Transfer learning in hybrid classical-quantum neural networks." 1912.08278v2

\*Havlíček et al. "Supervised learning with quantum-enhanced feature spaces." 1804.11326v2

Lloyd et al. "Quantum embeddings for machine learning." 2001.03622

Schuld et al. "Circuit-centric quantum classifiers." 1804.00633v1

[Zhang et al. "Toward trainability of quantum neural networks." 2011.06258v2]

[Zoufal et al. "Variational quantum Boltzmann machines." 2006.06004v1]

QNN

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Wilson et al. "Quantum kitchen sinks: An algorithm for ML on near-term...." 1806.08321v2

Huang et al. "Power of data in quantum machine learning." 2011.01938v2

QKernel

Henderson et al. "Quantum convolutional neural networks: powering image recognition.." 1904.04767v1

Wei "A quantum convolutional neural network on NISQ devices." 2104.06918v3

QConv

// A possible explanation

## What “features” do our quantum models create?

Example for input  $x = [x_1, x_2]$

scaling + trigonometric

$$\begin{matrix} \sin(w_1 x_1) \sin(w_2 x_2) \\ \sin(w_1 x_1) \cos(w_2 x_2) \\ \cos(w_1 x_1) \sin(w_2 x_2) \\ \cos(w_1 x_1) \cos(w_2 x_2) \end{matrix}$$

Pérez-Salinas et al. "Data re-uploading for a universal quantum classifier." 1907.02085v3

Mari et al. "Transfer learning in hybrid classical-quantum neural networks." 1912.08278v2

\*Havlíček et al. "Supervised learning with quantum-enhanced feature spaces." 1804.11326v2

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QKernel

Henderson et al. "Quantum convolutional neural networks: powering image recognition.." 1904.04767v1

Wei "A quantum convolutional neural network on NISQ devices." 2104.06918v3

QConv

// A possible explanation

## What “features” do our quantum models create?

Example for input  $x = [x_1, x_2]$

linear + trigonometric

$$\begin{aligned} & \sin(\mathbf{v}\mathbf{x} + \mathbf{b}_1) \sin(\mathbf{w}\mathbf{x} + \mathbf{b}_2) \\ & \sin(\mathbf{v}\mathbf{x} + \mathbf{b}_1) \cos(\mathbf{w}\mathbf{x} + \mathbf{b}_2) \\ & \cos(\mathbf{v}\mathbf{x} + \mathbf{b}_1) \sin(\mathbf{w}\mathbf{x} + \mathbf{b}_2) \\ & \cos(\mathbf{v}\mathbf{x} + \mathbf{b}_1) \cos(\mathbf{w}\mathbf{x} + \mathbf{b}_2) \end{aligned}$$

Pérez-Salinas et al. "Data re-uploading for a universal quantum classifier." 1907.02085v3

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QConv



// A possible explanation

## What “features” do our quantum models create?

Example for input  $x = [x_1, x_2]$

NN + trigonometric

```
sin( $\phi(\mathbf{v}\mathbf{x})$ ) sin( $\phi(\mathbf{w}\mathbf{x})$ )  
sin( $\phi(\mathbf{v}\mathbf{x})$ ) cos( $\phi(\mathbf{w}\mathbf{x})$ )  
cos( $\phi(\mathbf{v}\mathbf{x})$ ) sin( $\phi(\mathbf{w}\mathbf{x})$ )  
cos( $\phi(\mathbf{v}\mathbf{x})$ ) cos( $\phi(\mathbf{w}\mathbf{x})$ )
```

Pérez-Salinas et al. "Data re-uploading for a universal quantum classifier." 1907.02085v3

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QKernel

Henderson et al. "Quantum convolutional neural networks: powering image recognition.." 1904.04767v1

Wei "A quantum convolutional neural network on NISQ devices." 2104.06918v3

QConv

// A possible explanation

## What “features” do our quantum models create?

Example for input  $x = [x_1, x_2]$

poly + trigonometric

```
sin(x1) sin(x2) sin(x1x2)
sin(x1) sin(x2) cos(x1x2)
...
cos(x1) cos(x2) cos(x1x2)
```

Pérez-Salinas et al. "Data re-uploading for a universal quantum classifier." 1907.02085v3

Mari et al. "Transfer learning in hybrid classical-quantum neural networks." 1912.08278v2

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Lloyd et al. "Quantum embeddings for machine learning." 2001.03622

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QKernel

Henderson et al. "Quantum convolutional neural networks: powering image recognition.." 1904.04767v1

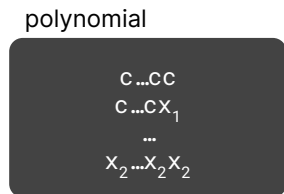
Wei "A quantum convolutional neural network on NISQ devices." 2104.06918v3

QConv

// A possible explanation

## What “features” do our quantum models create?

Example for input  $x = [x_1, x_2]$



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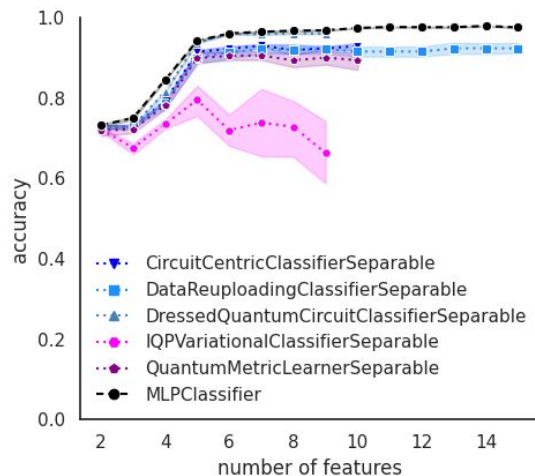
Wei "A quantum convolutional neural network on NISQ devices." 2104.06918v3

QConv

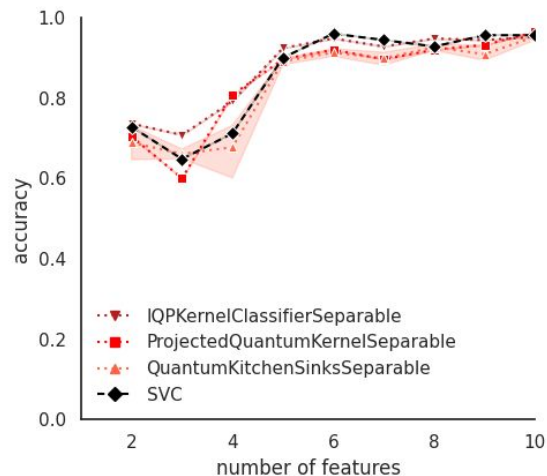
// Preliminary results

## Separable circuits perform the same

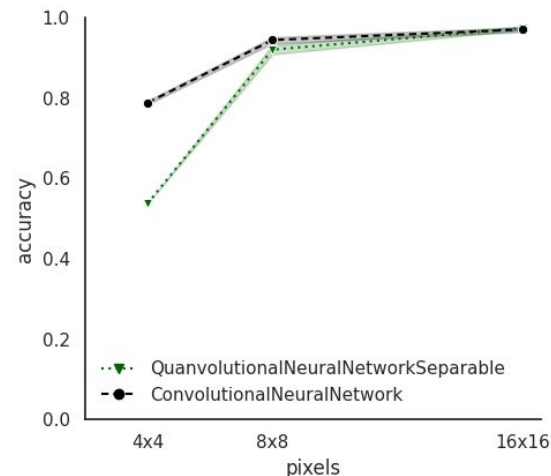
Test score on PCA-reduced MNIST using best hyperparameters



Test score on PCA reduced, subsampled MNIST using best hyperparameters

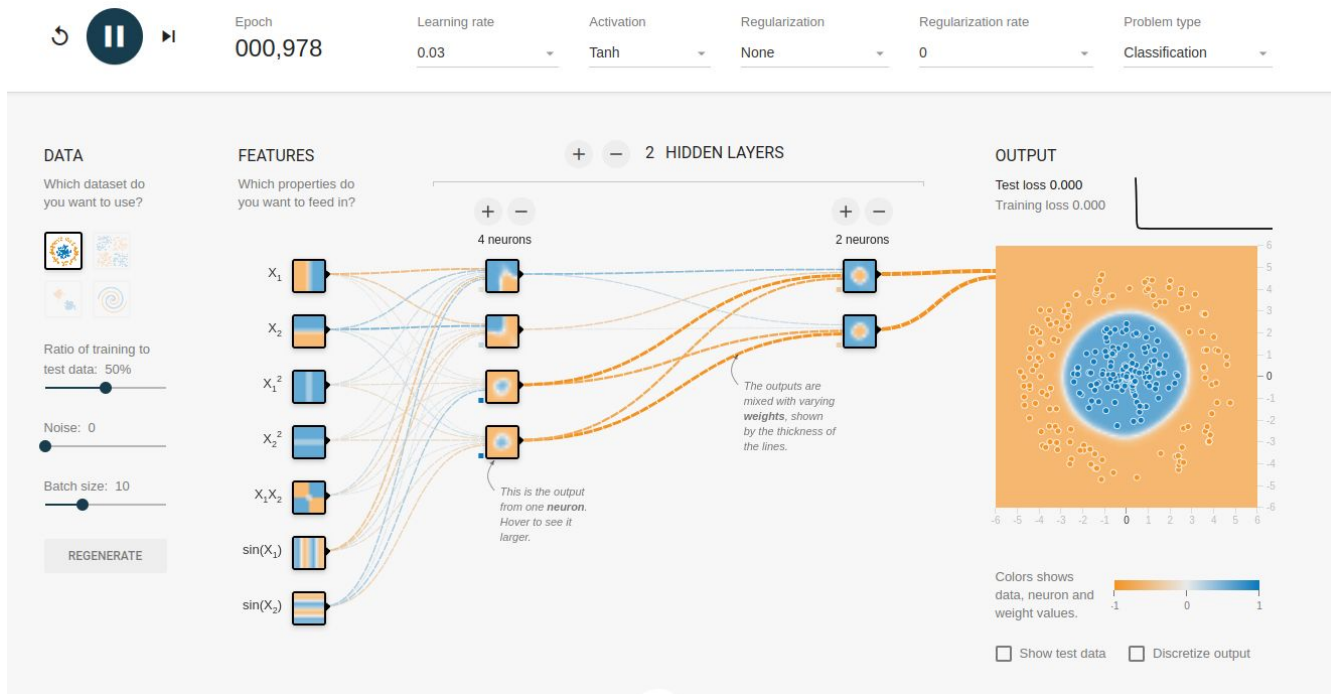


Test score on coarse-grained MNIST using best hyperparameters



// A possible explanation

# Are we “just” building trigonometric/polynomial feature extractors?



<https://playground.tensorflow.org/>

// More to come

## Here comes the $SU(N)$ : multivariate quantum gates and gradients

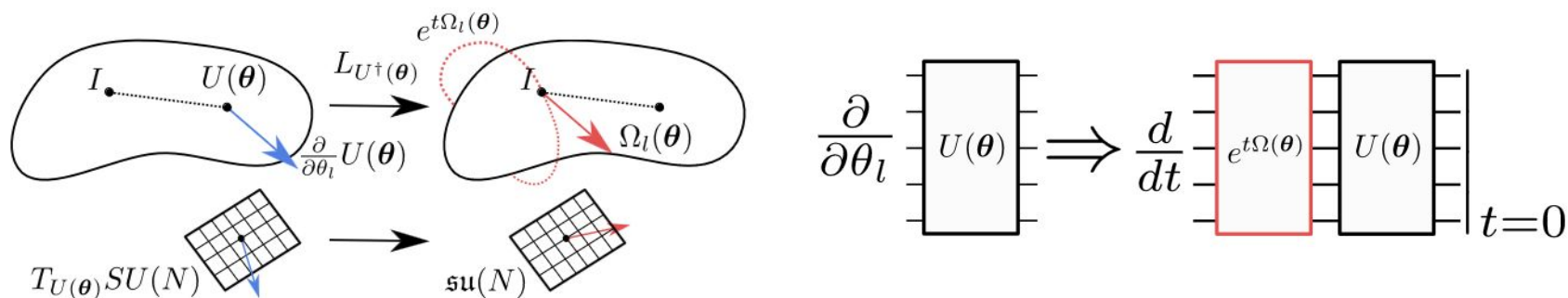
Roeland Wiersema,<sup>1,2</sup> Dylan Lewis,<sup>3</sup> David Wierichs,<sup>4</sup> Juan Carrasquilla,<sup>1,2</sup> and Nathan Killoran<sup>4</sup>

<sup>1</sup>Vector Institute, MaRS Centre, Toronto, Ontario, M5G 1M1, Canada

<sup>2</sup>Department of Physics and Astronomy, University of Waterloo, Ontario, N2L 3G1, Canada

<sup>3</sup>Department of Physics and Astronomy, University College London, London WC1E 6BT, United Kingdom

<sup>4</sup>Xanadu, Toronto, ON, M5G 2C8, Canada



**Tomorrow!**

21 Nov 2023, 16:45

Thank you



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