

Quantum anomaly detection in the latent space of proton collision events at the LHC

Vasilis Belis¹ [[arXiv:2301.10780](https://arxiv.org/abs/2301.10780)]

K. Woźniak^{2,3}, E. Puljak^{2,4}, P. Barkoutsos^{5,*}, G. Dissertori¹, M. Grossi², M. Pierini², F. Reiter¹, I. Tavernelli⁵, S. Vallecorsa²

*currently Pasqal

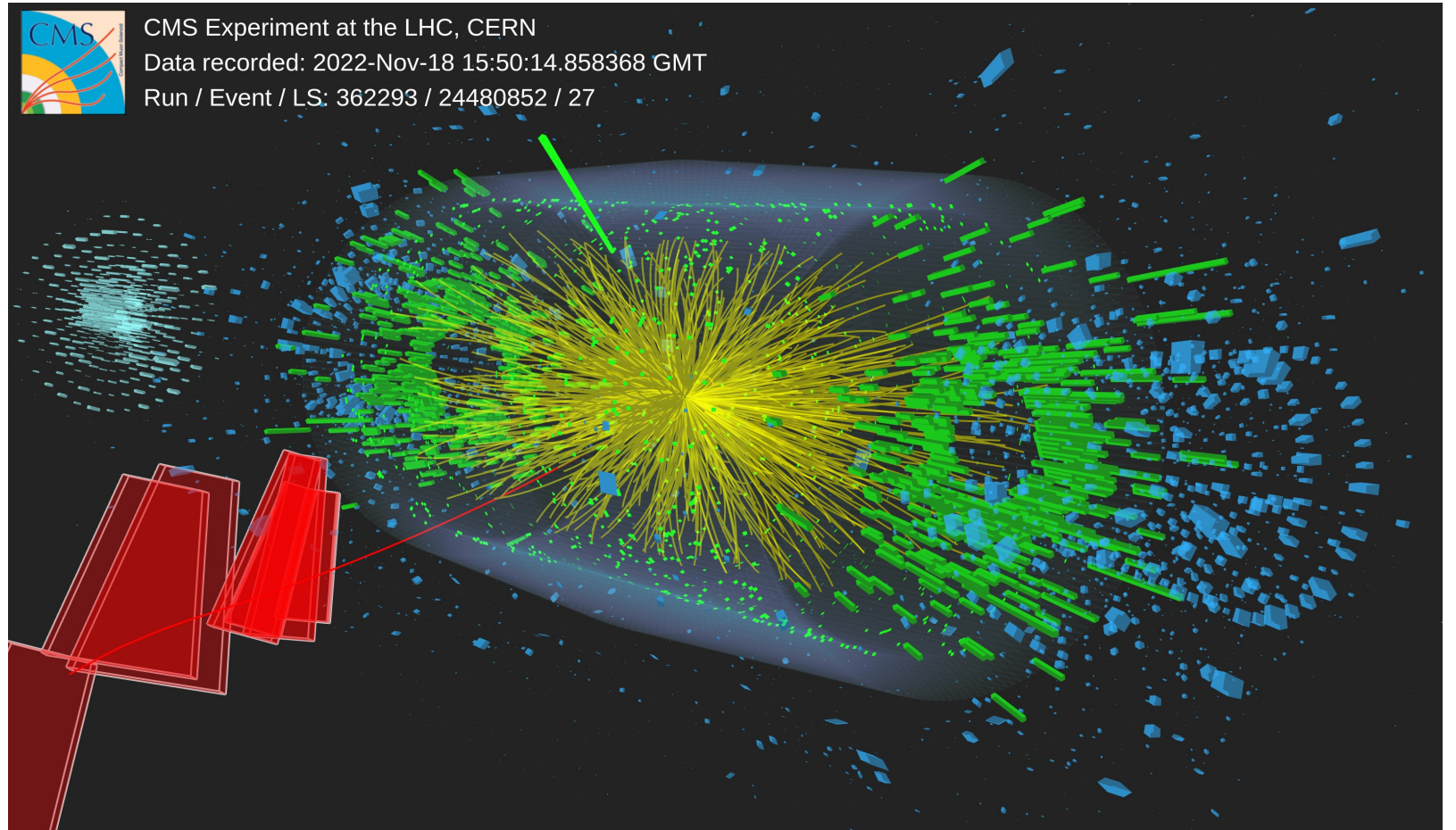
23 November, CERN

QTML 2023

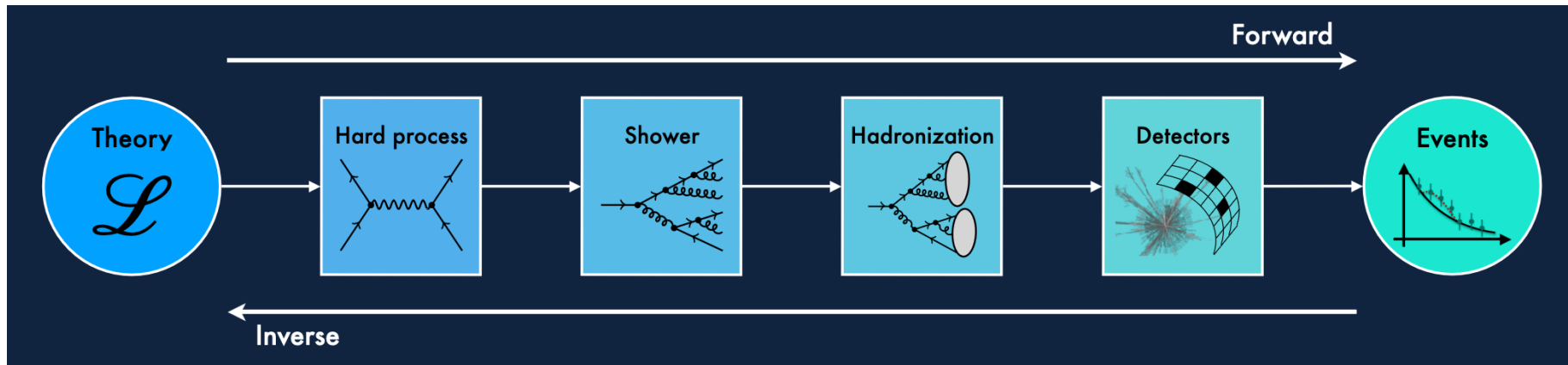
No cats and dogs exploited to explain this work



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Why QML for HEP?

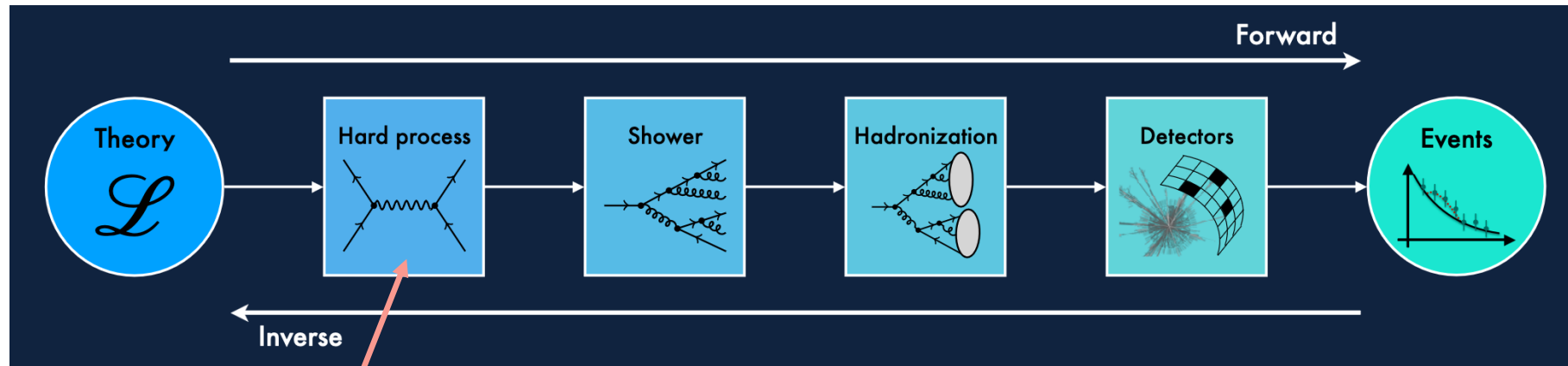


Fundamental motivation

Utilise information and correlations inherent in HEP data.

Exploit “quantum remnants” in data.

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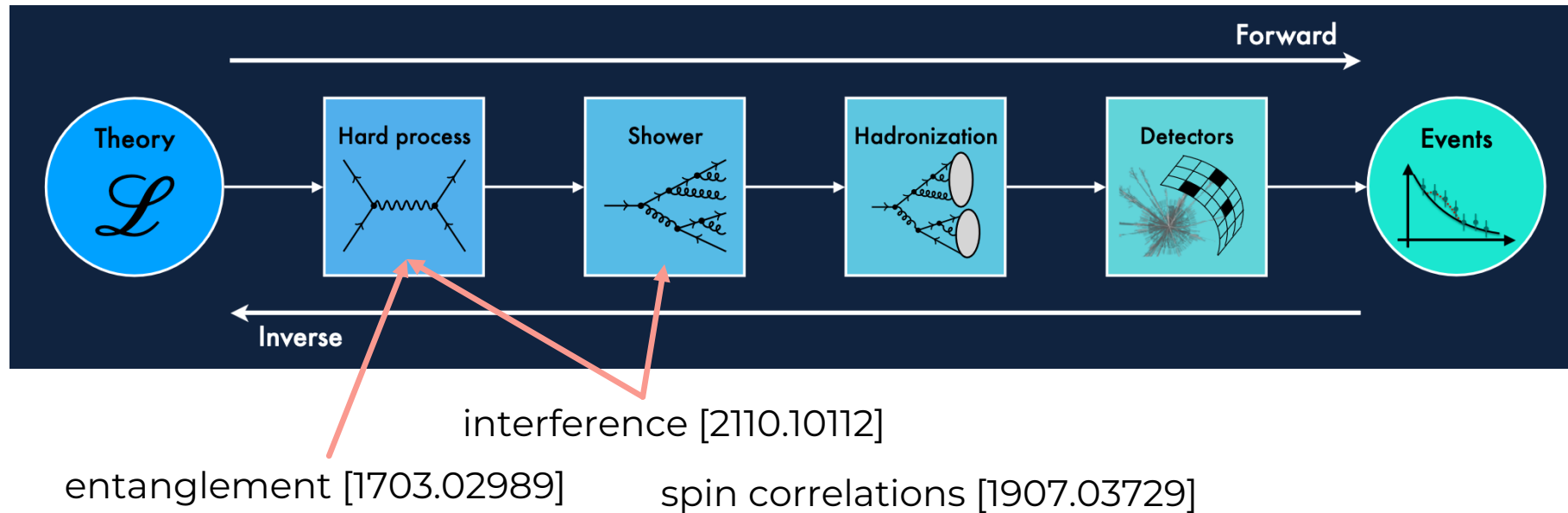
entanglement [1703.02989]

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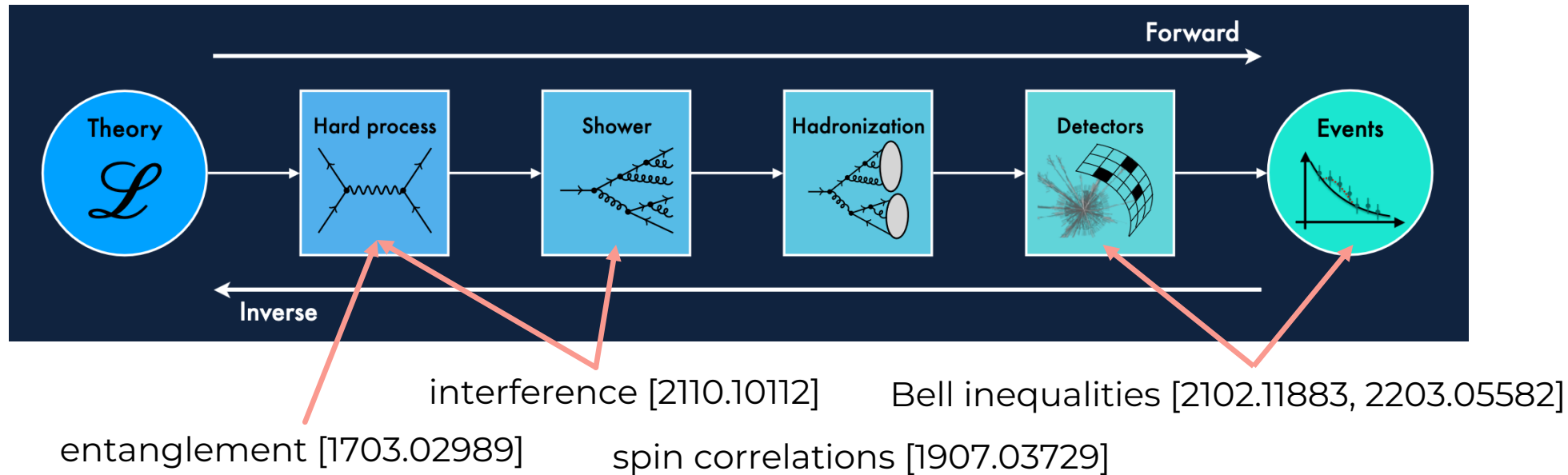


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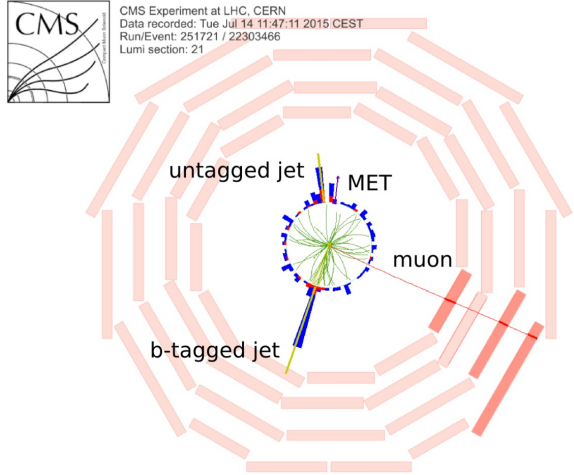


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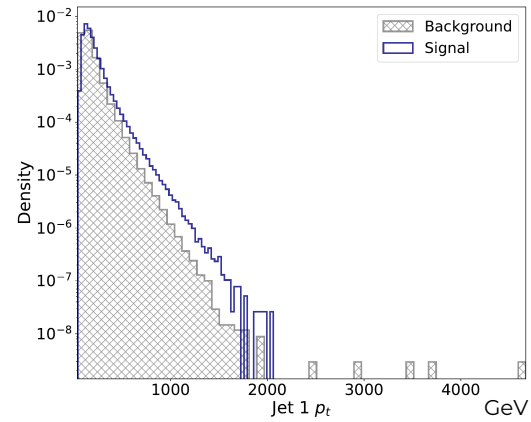
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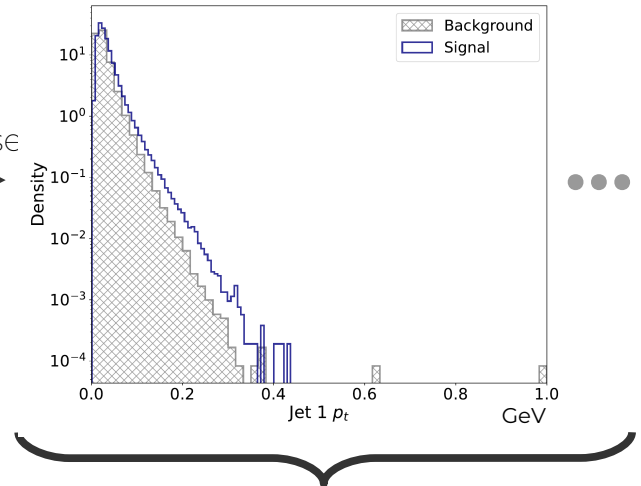
Typical workflow: Model-dependent searches



compute
prob.
distributions



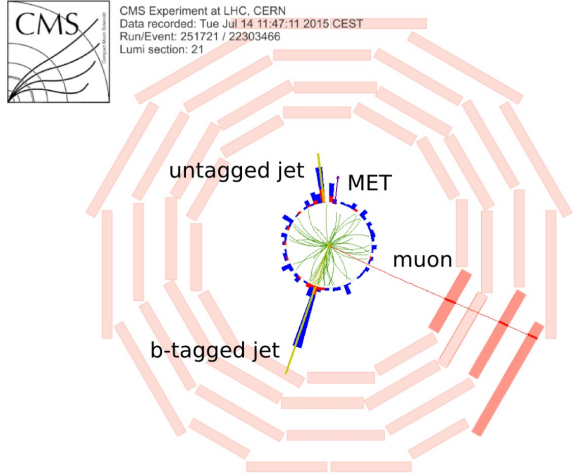
apply cuts
and normalise



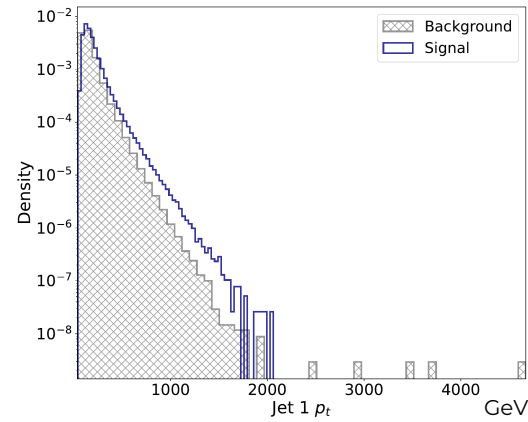
Theory + Simulation

**Input for classifiers
models**

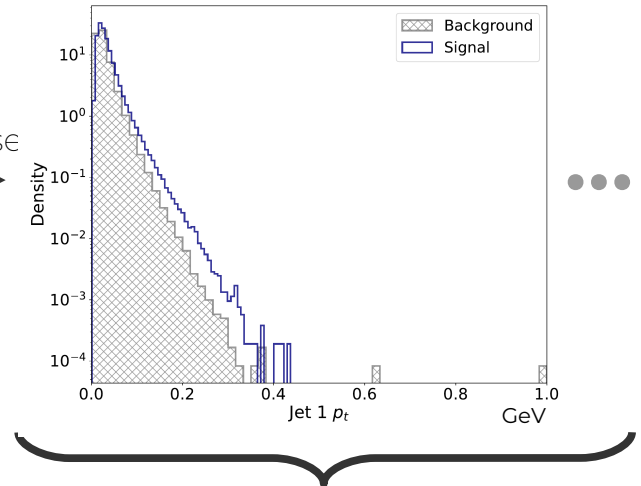
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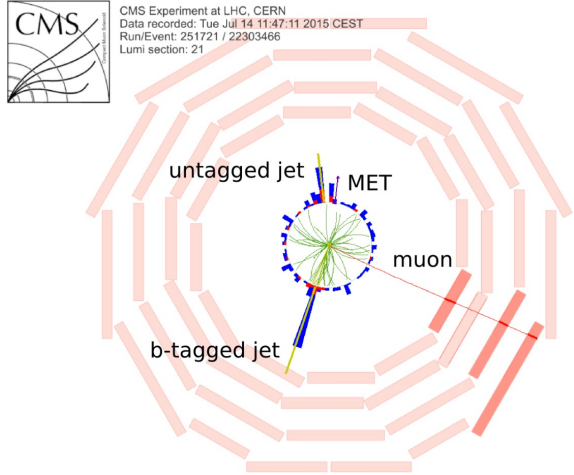
Classifier models

produce the *test statistic*

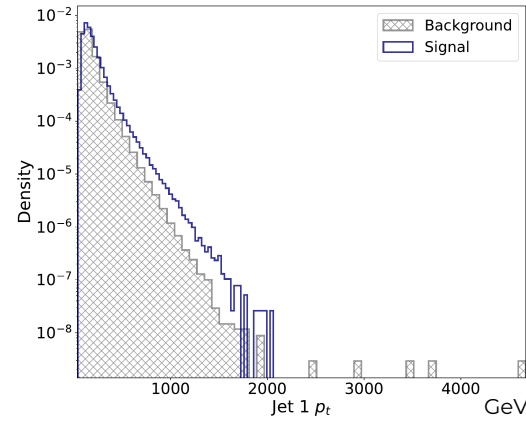
Likelihood ratio between
different hypotheses

$$q = -2 \log \frac{\mathcal{L}(x|S)}{\mathcal{L}(x|B)}$$

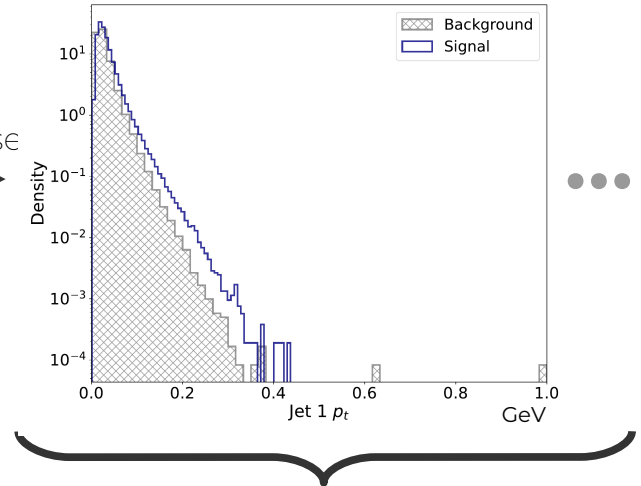
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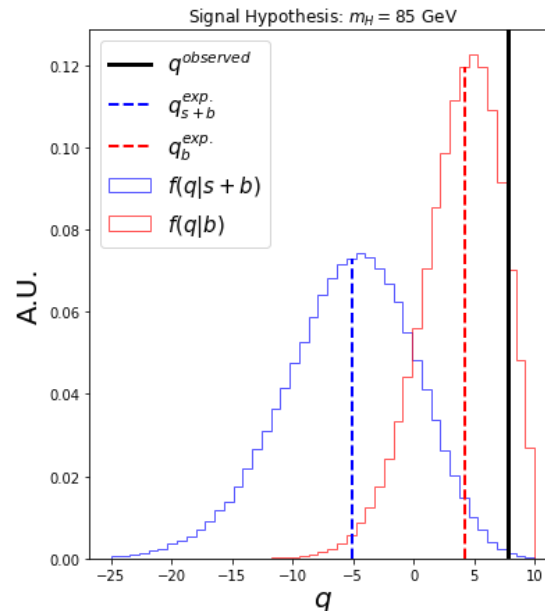
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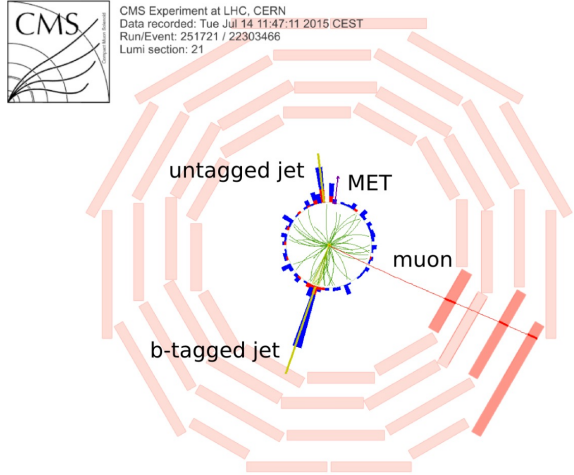
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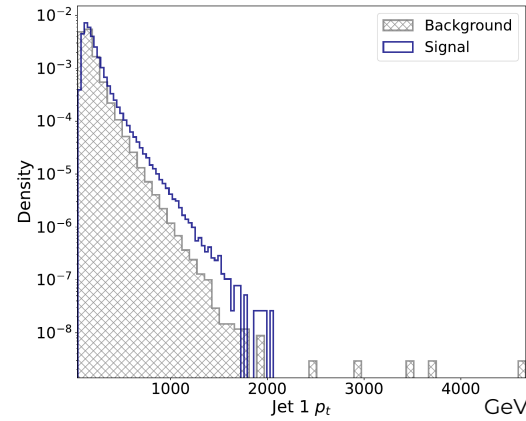
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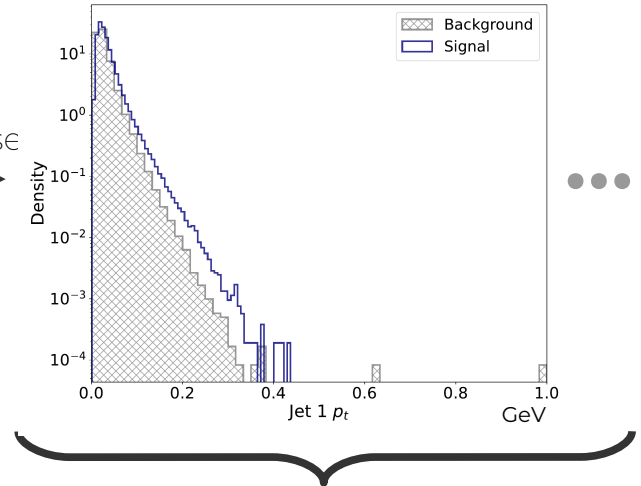
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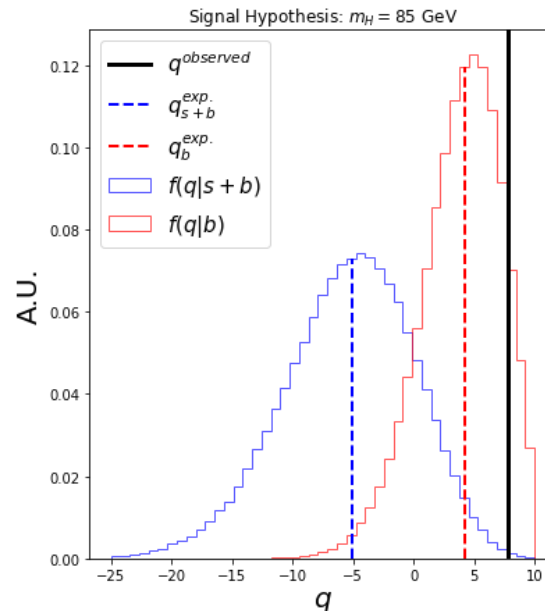
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What if you do not know the signal?

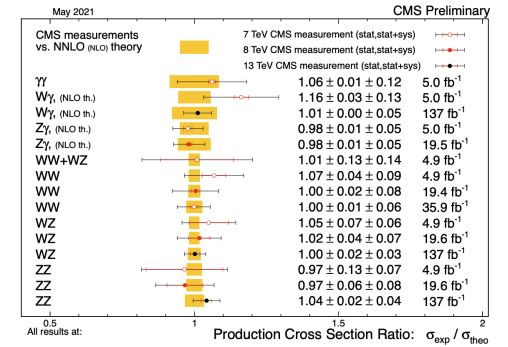
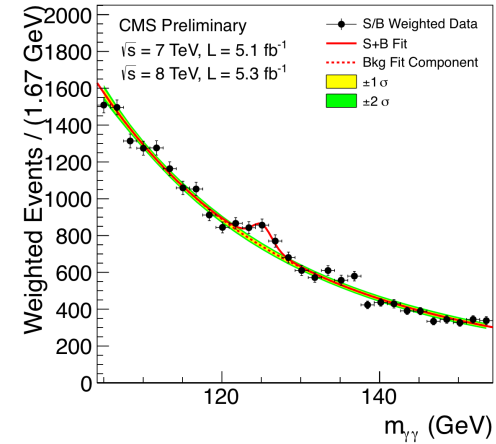
Motivating model-independent searches

Bias is **not necessarily bad**. It can be **great!**

Higher bias \longrightarrow lower variance of the statistical model

[Cramér–Rao bound]

[10.1016/j.physletb.2012.08.02]



Summary SM measurements @ CMS [\[link\]](#)

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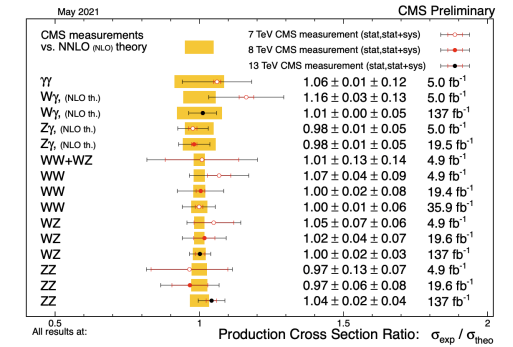
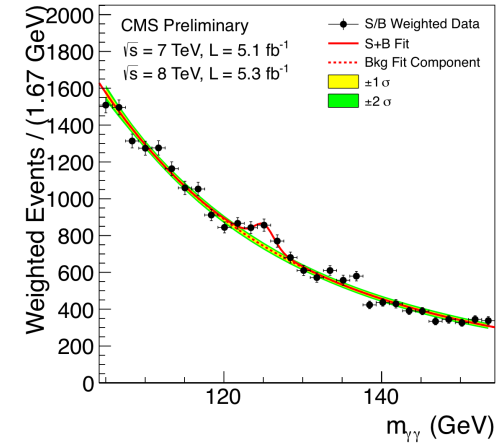
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So far, new-physics searches at the LHC:

assume SM + choose to test a signal hypothesis....

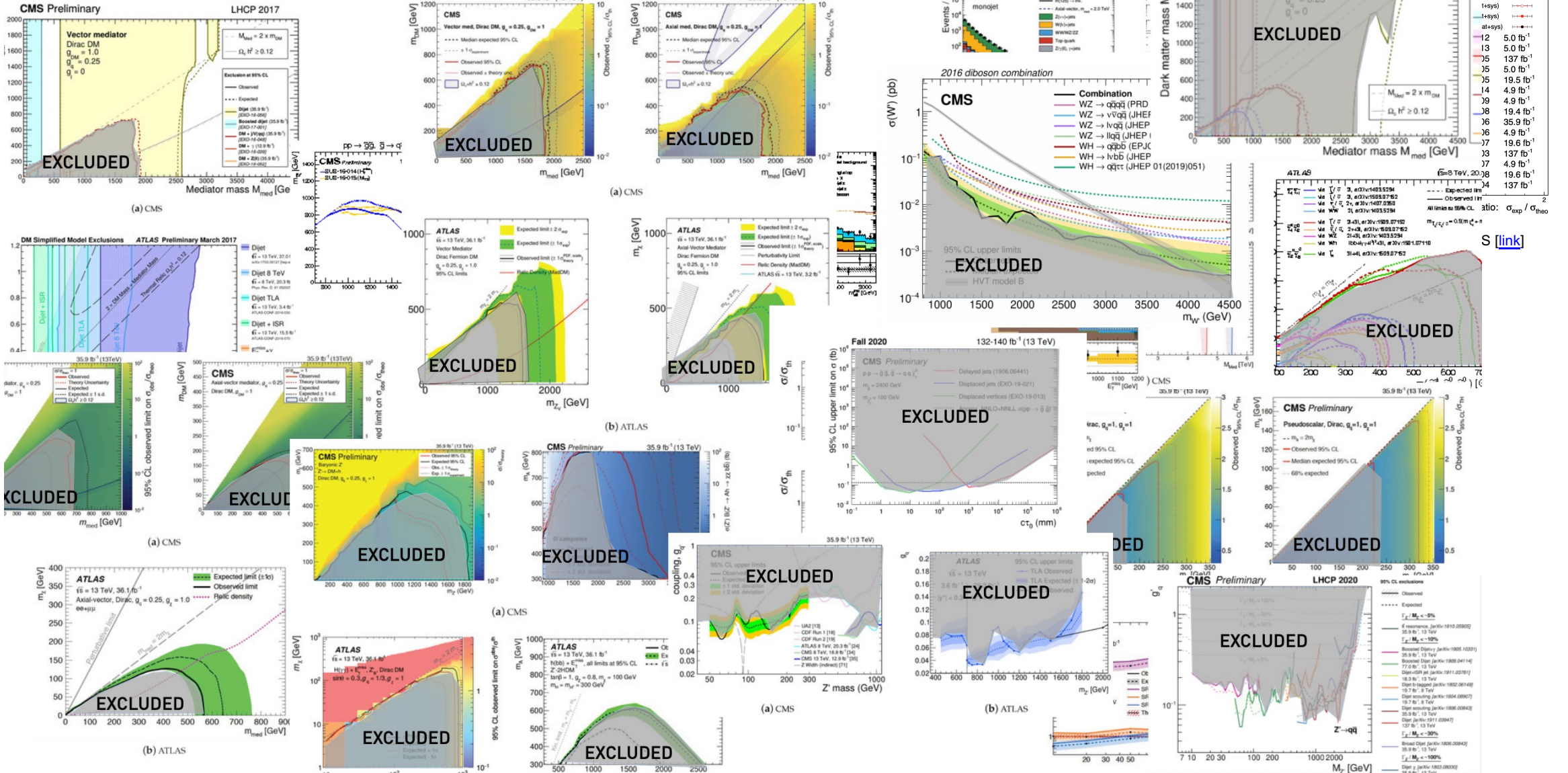
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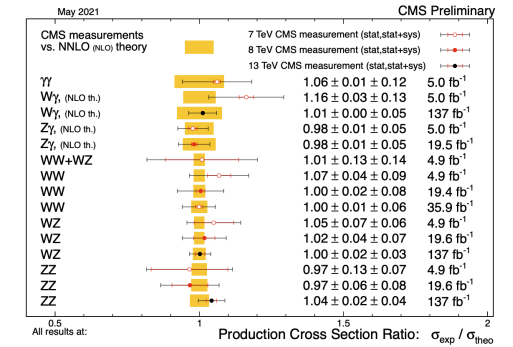
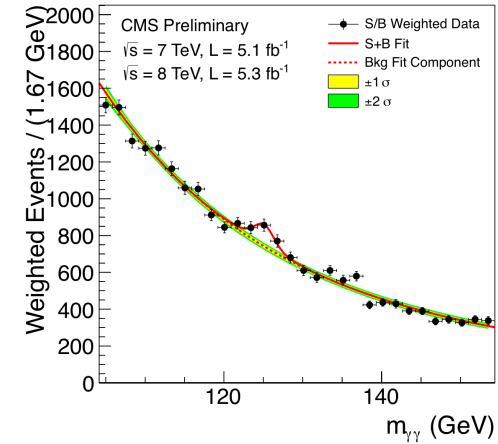
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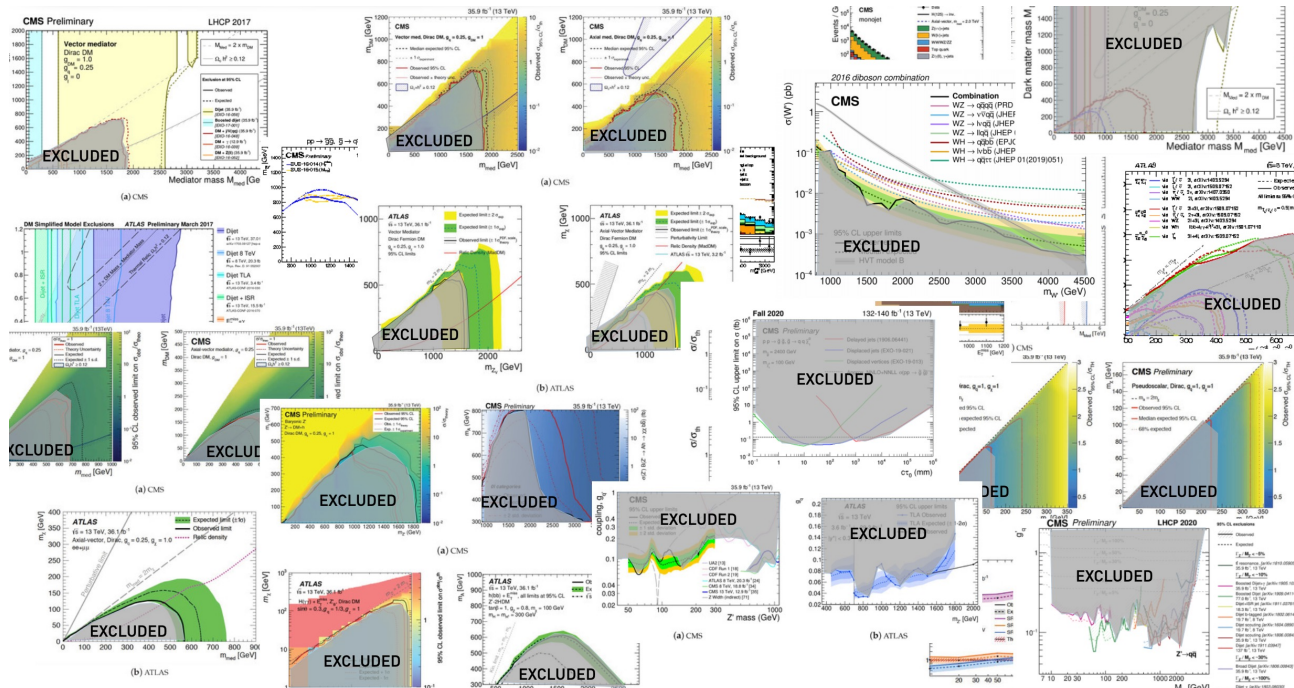
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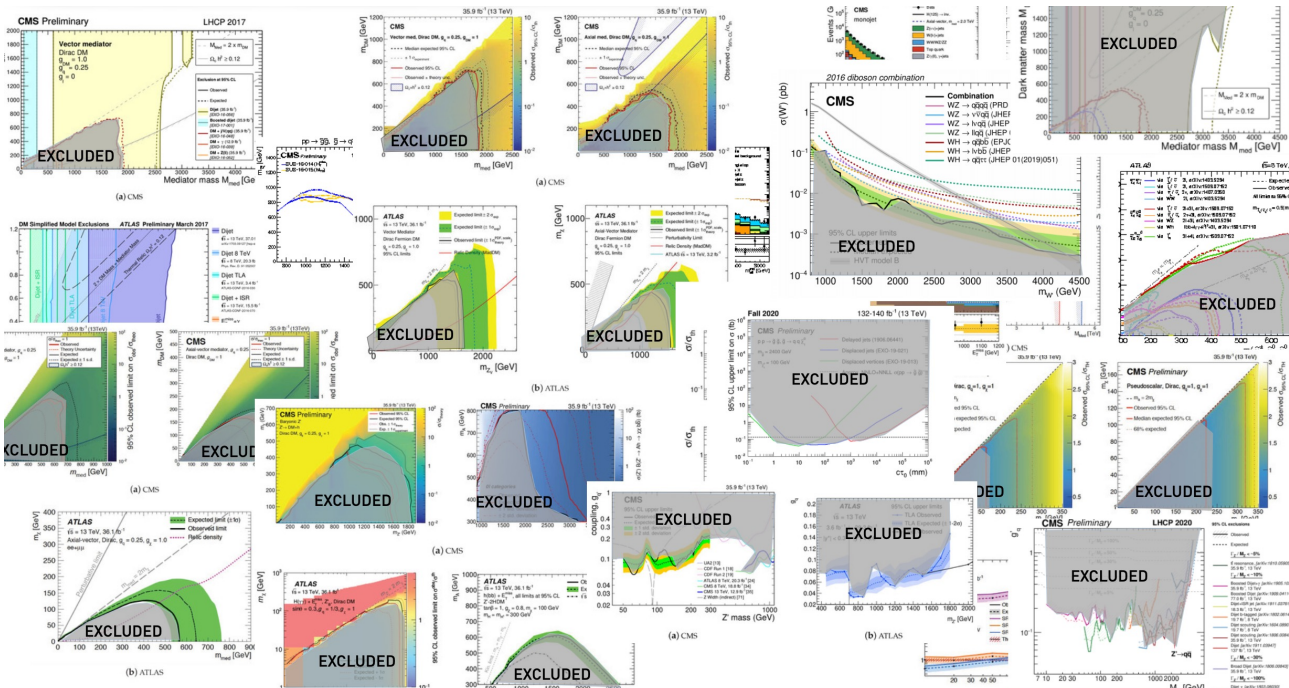
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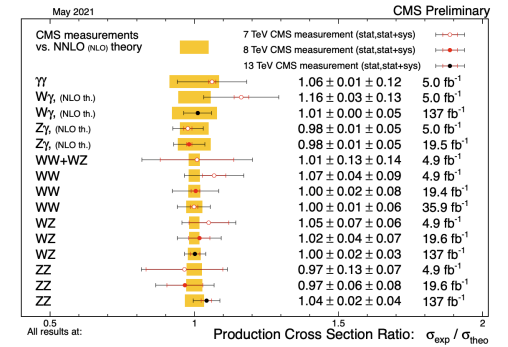
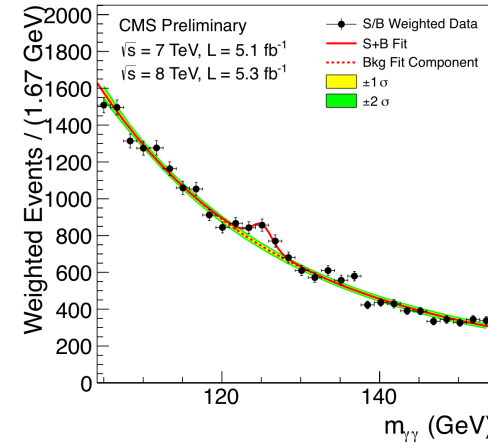
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What if you don't know where to look for new-physics?

Look at nature with minimal bias.

Motivating model-independent searches

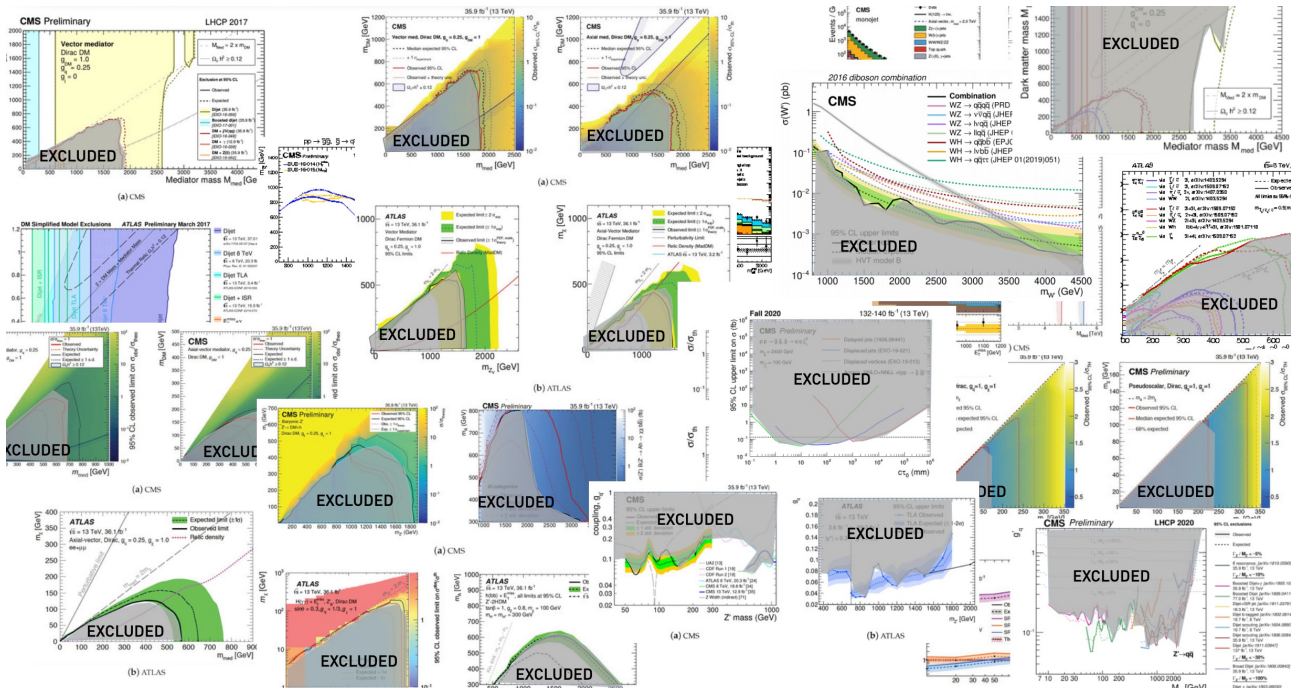
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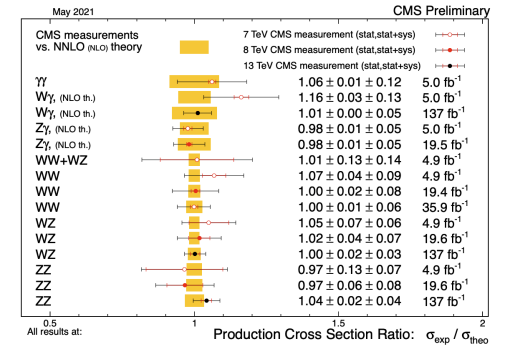
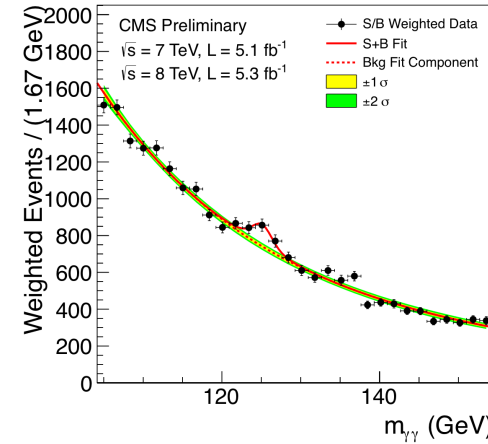
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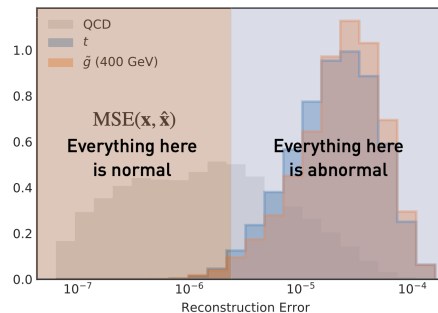


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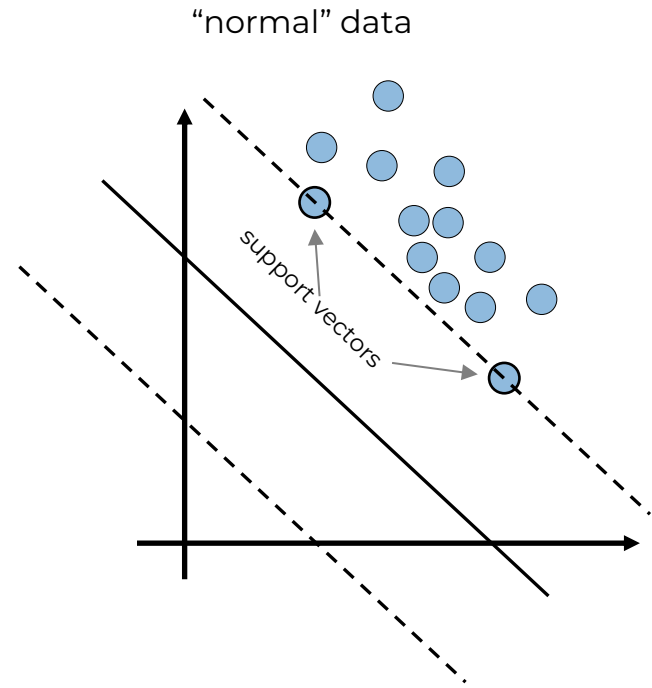
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One possible solution:
Anomaly detection



Unsupervised ML models

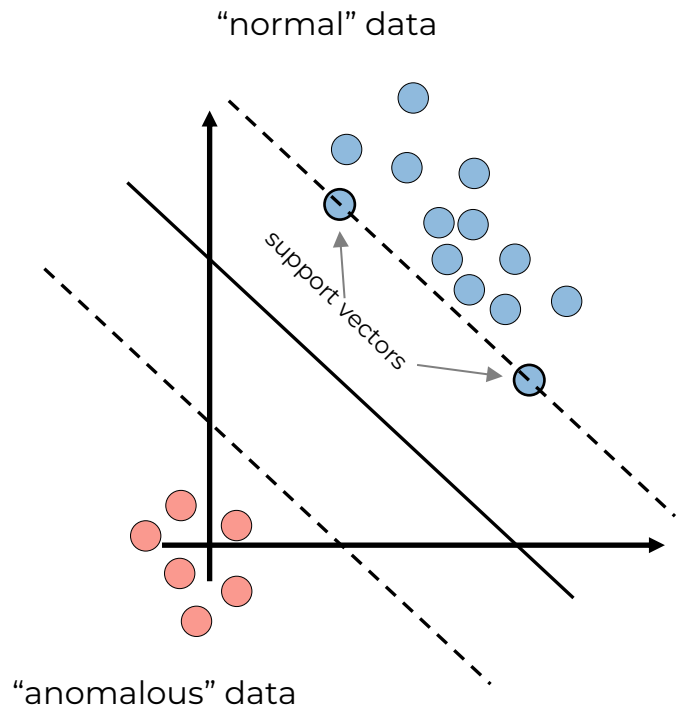
Unsupervised quantum kernel machines



$$\min_{w \in \mathcal{H}, \xi \in \mathbb{R}^N, \rho \in \mathbb{R}} \frac{1}{2} \|w\|^2 + \frac{1}{\nu N} \sum_i \xi_i - \rho$$

subject to $w \cdot \phi(x_i) \geq \rho - \xi_i, \xi_i \geq 0, \forall i$

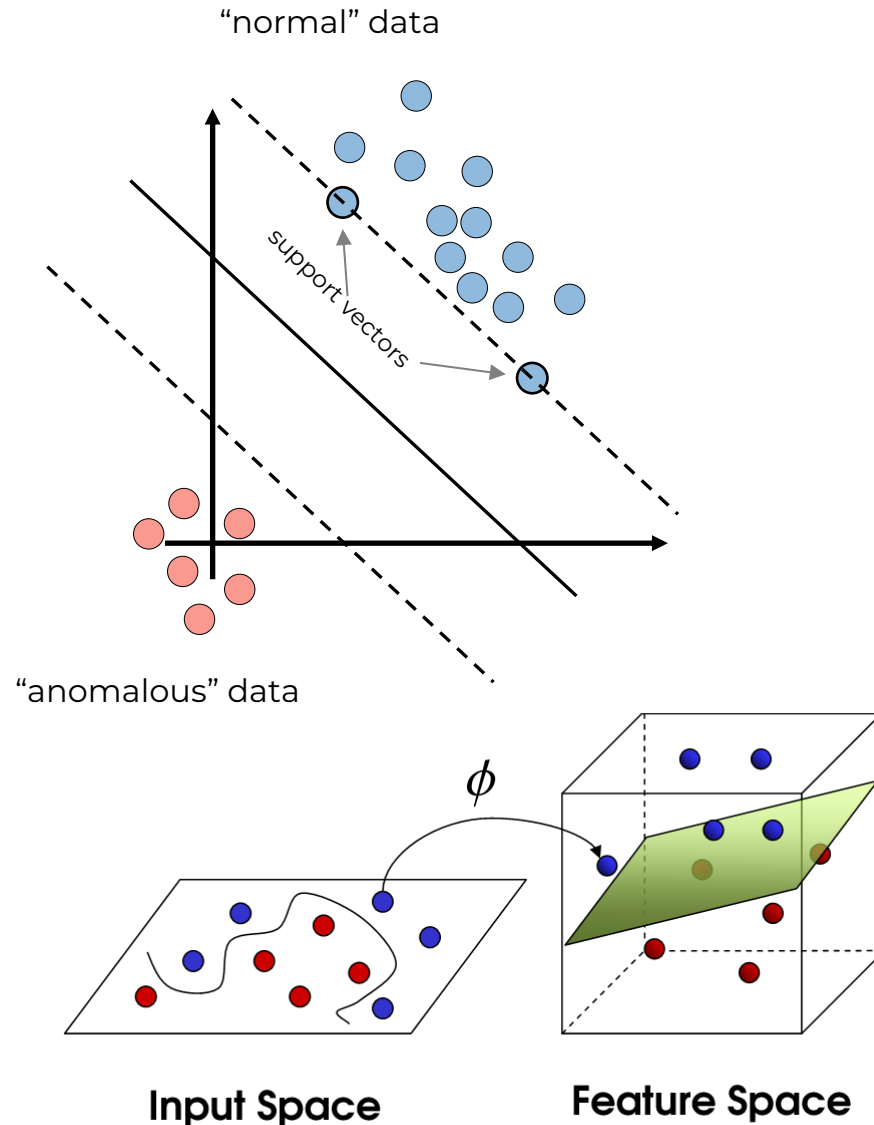
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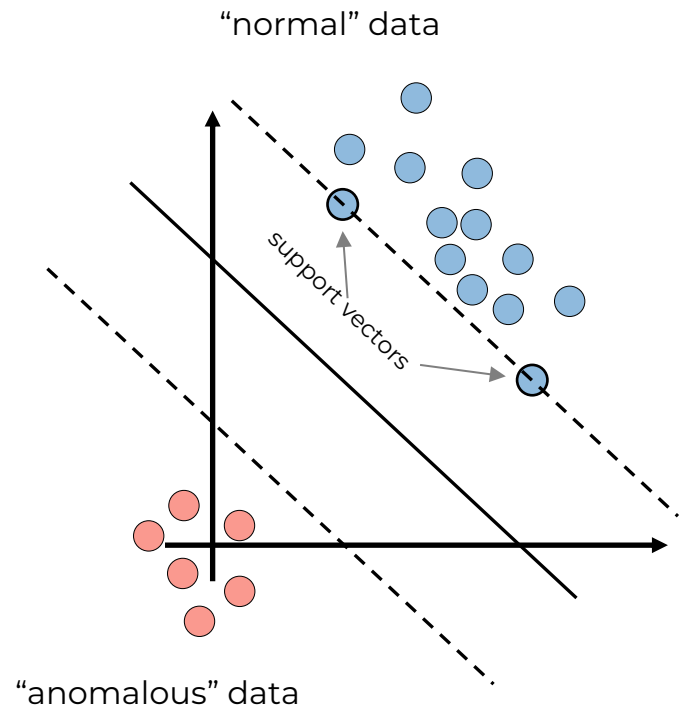
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Kernel trick:

$$(\vec{x}_i \cdot \vec{x}_j) \mapsto k(\vec{x}_i \cdot \vec{x}_j) = \phi(\vec{x}_i) \cdot \phi(\vec{x}_j)$$

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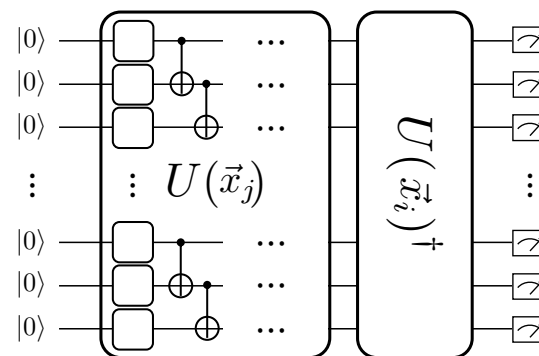
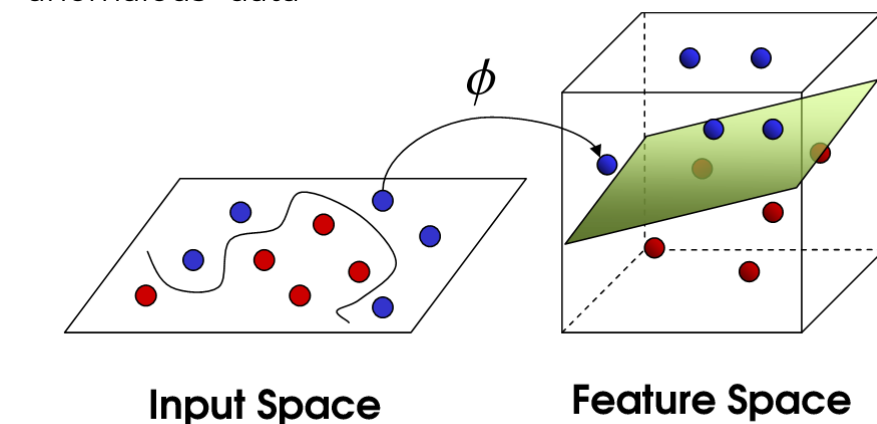


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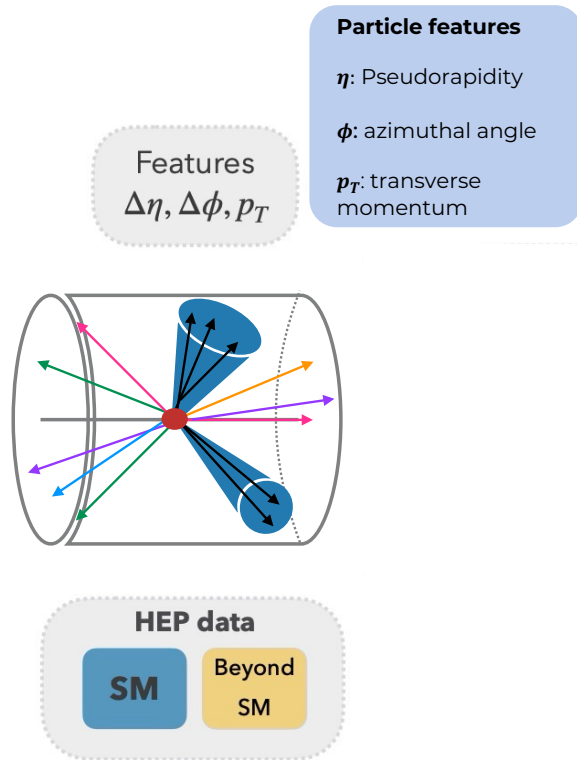


$$\Rightarrow K_{ij} = |\langle 0 | U^\dagger(\vec{x}_i) U(\vec{x}_j) | 0 \rangle|^2$$

Results

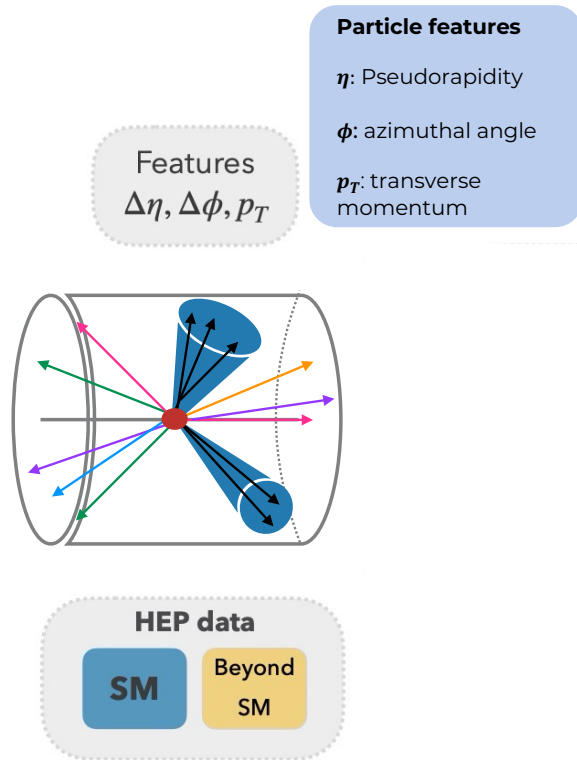
Finding new-physics in dijet events with QML

Anomaly detection with quantum machine learning



Background: QCD dijet events. 600 features per event

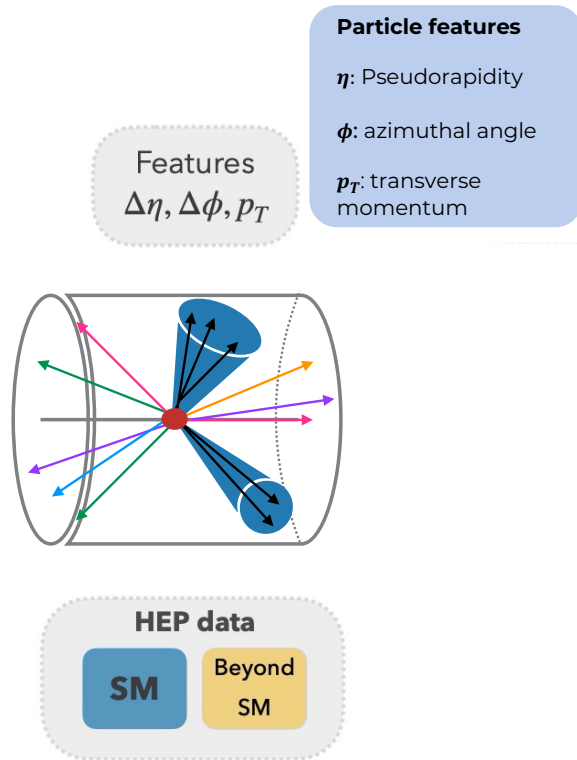
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 $G \rightarrow W^-W^+$ $A \rightarrow HZ \rightarrow ZZZ$

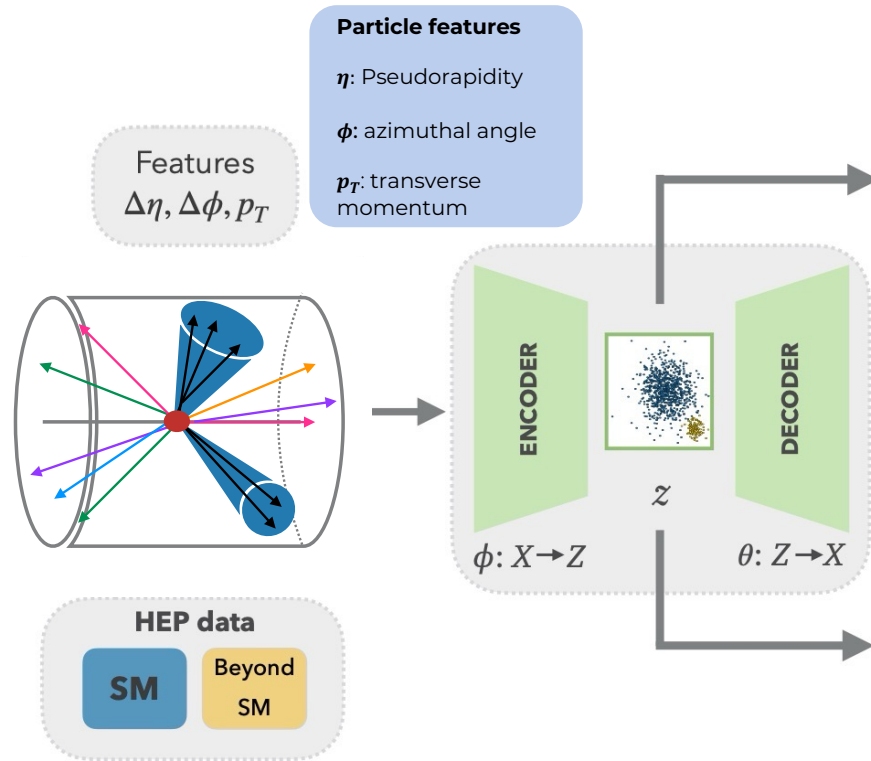
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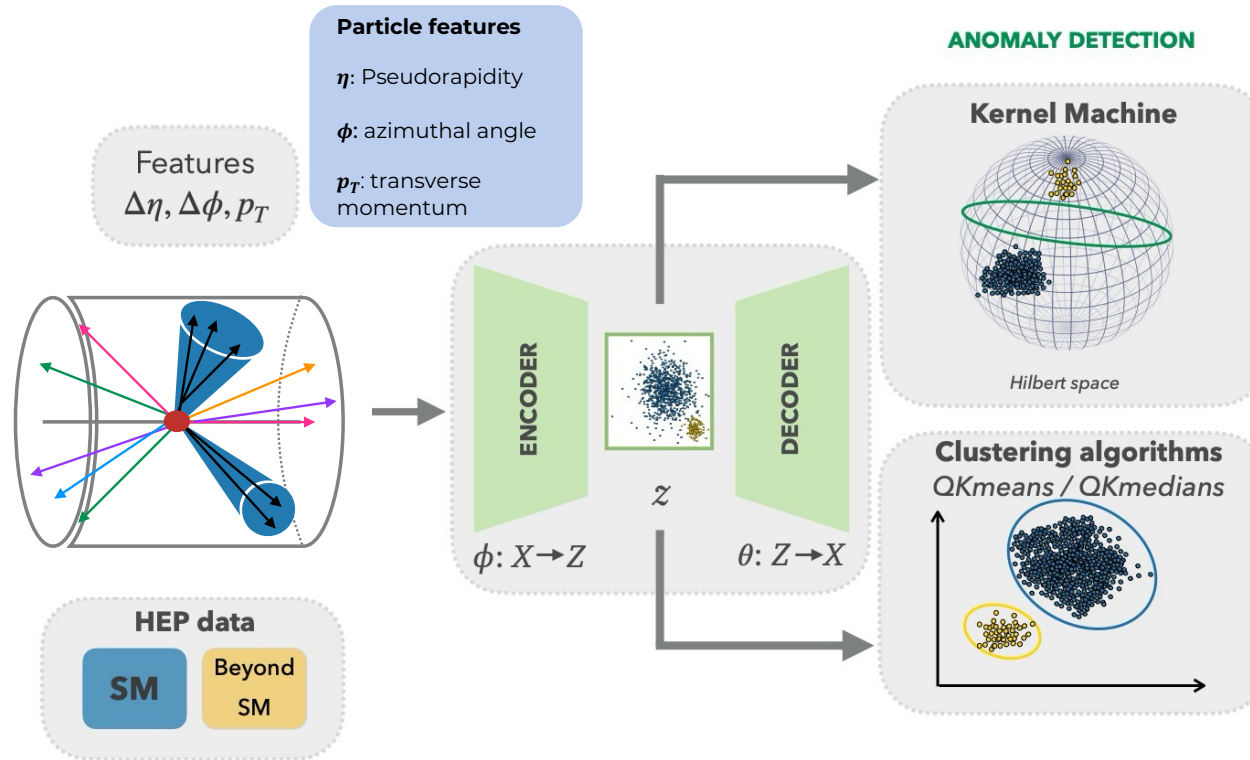
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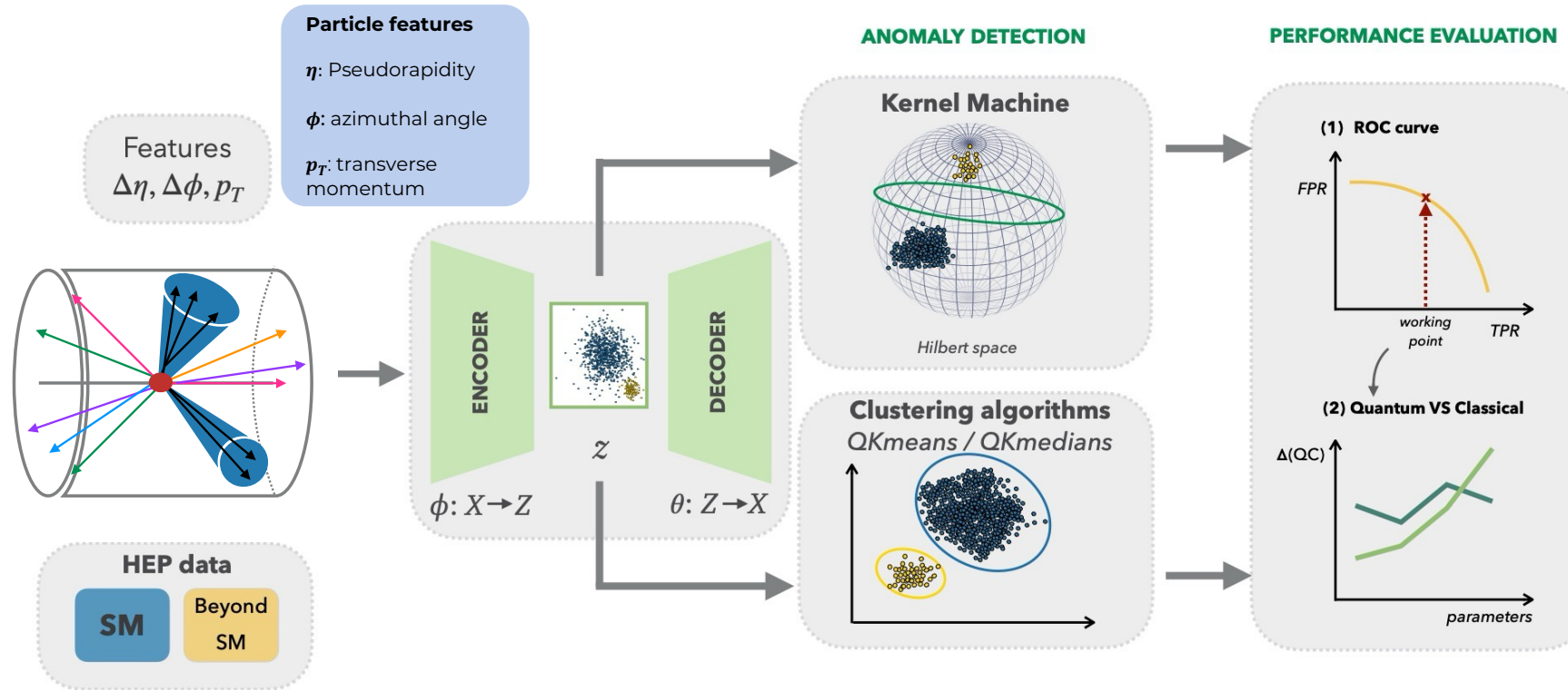
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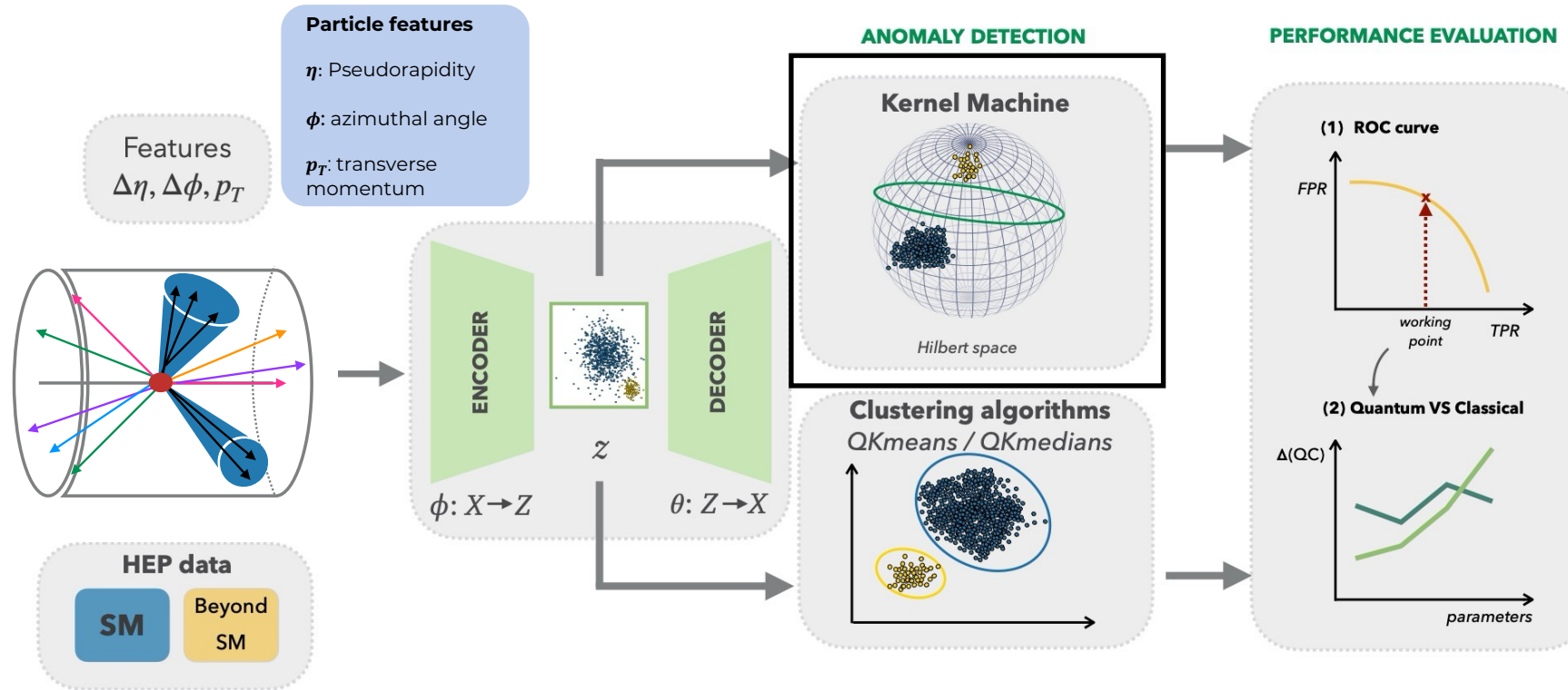
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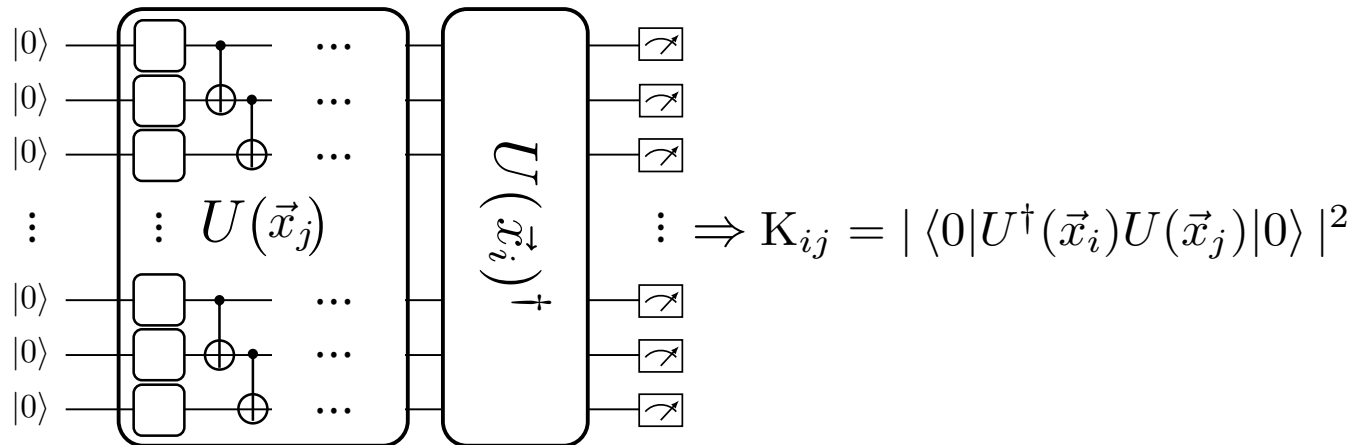
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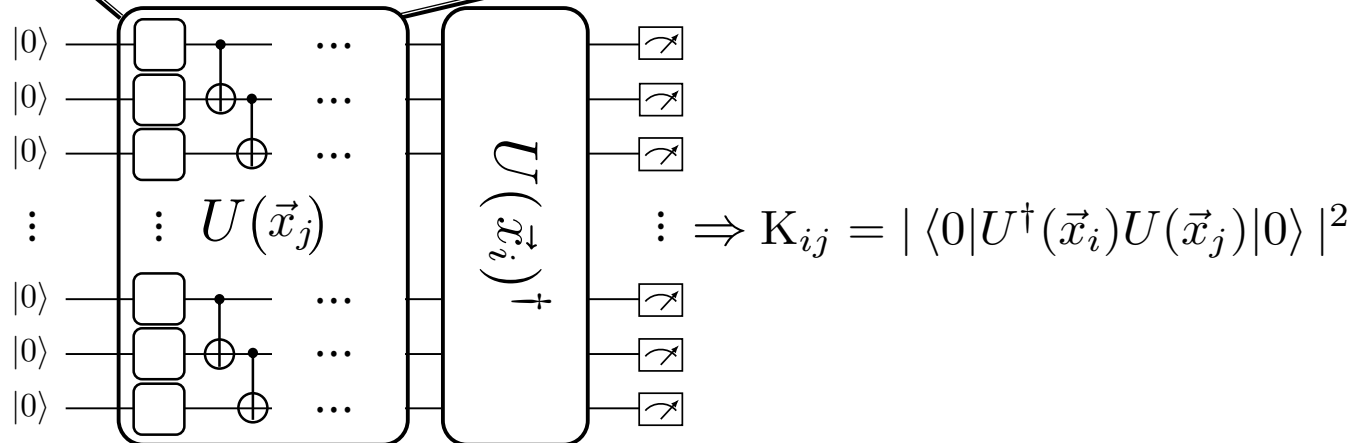
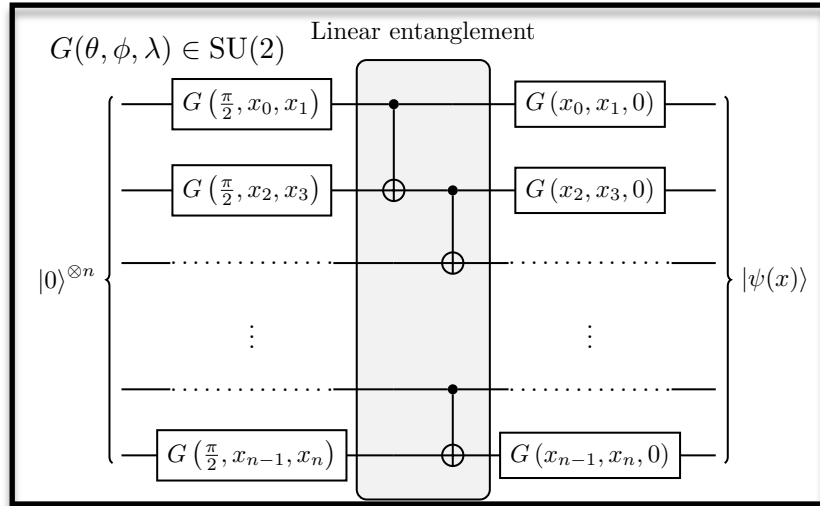
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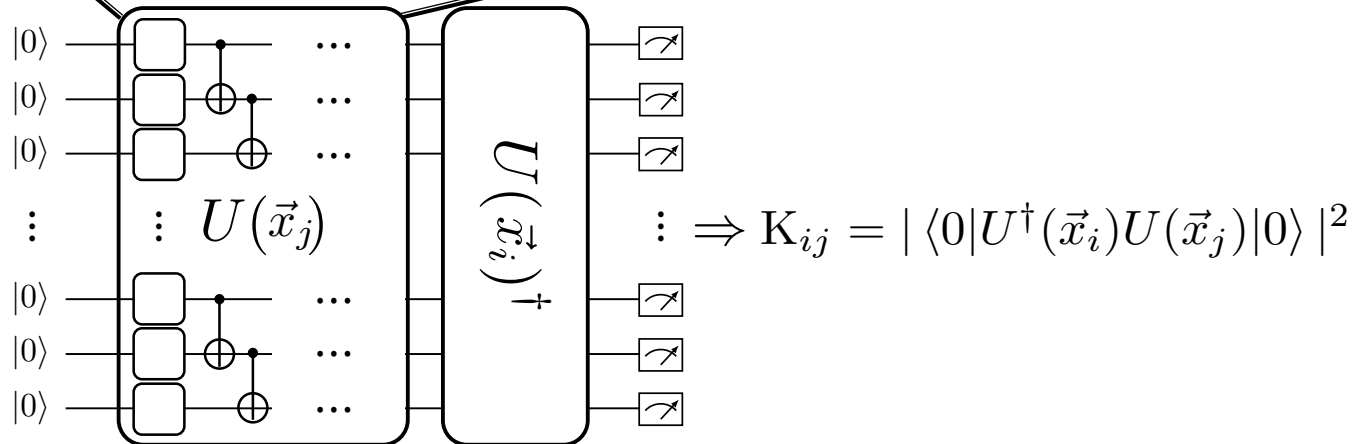
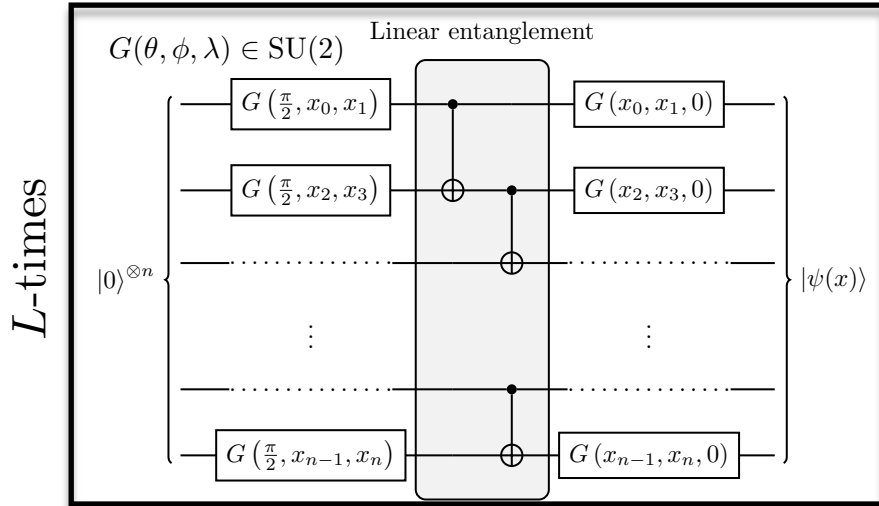
Unsupervised quantum kernel machine

Designed data encoding circuit



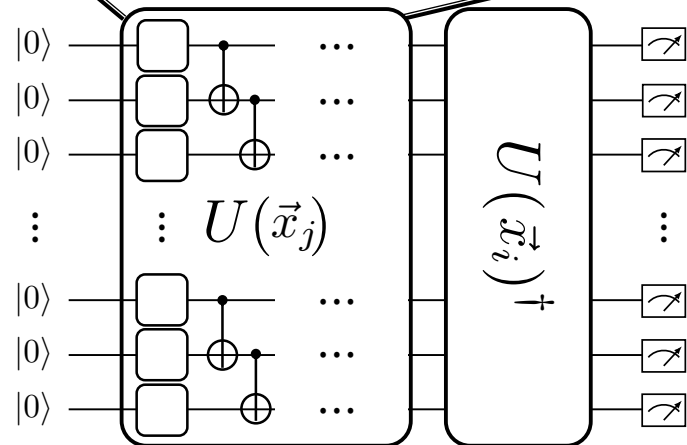
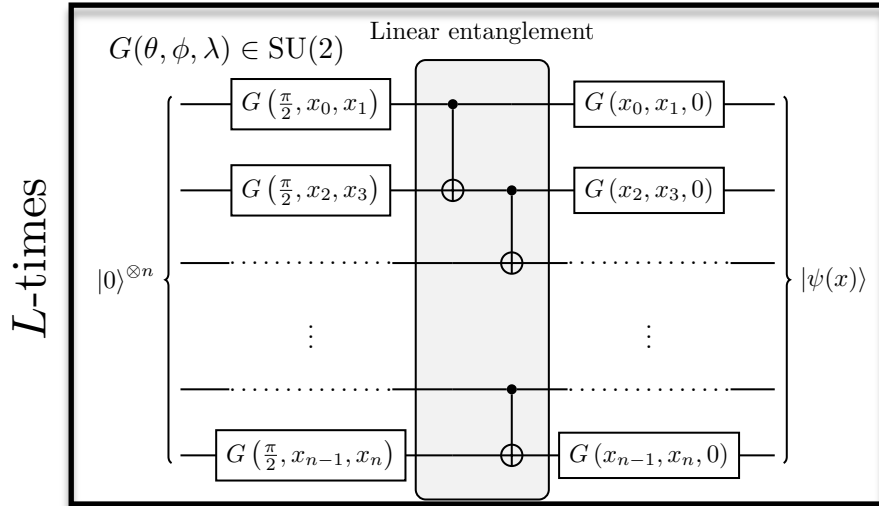
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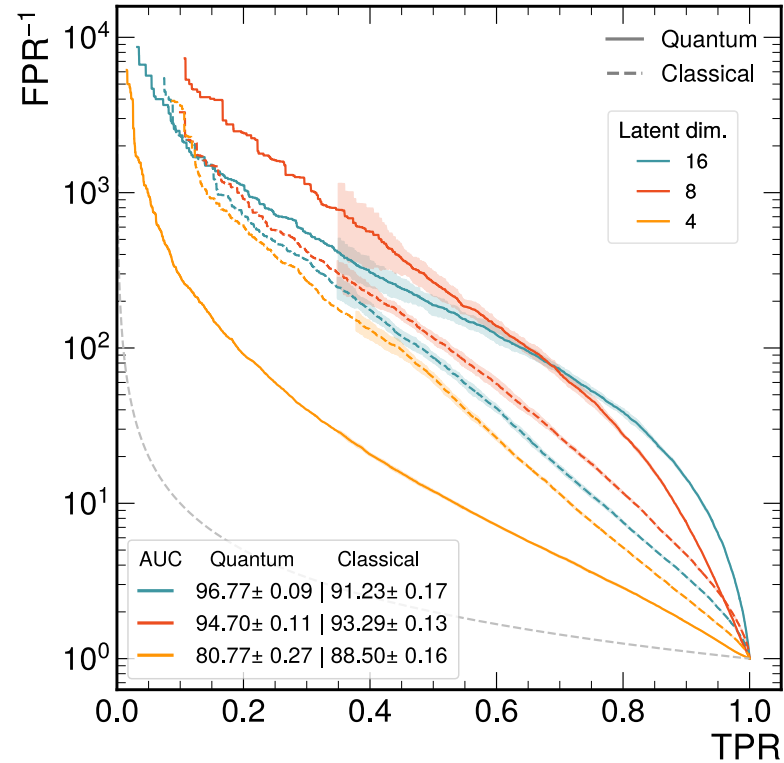


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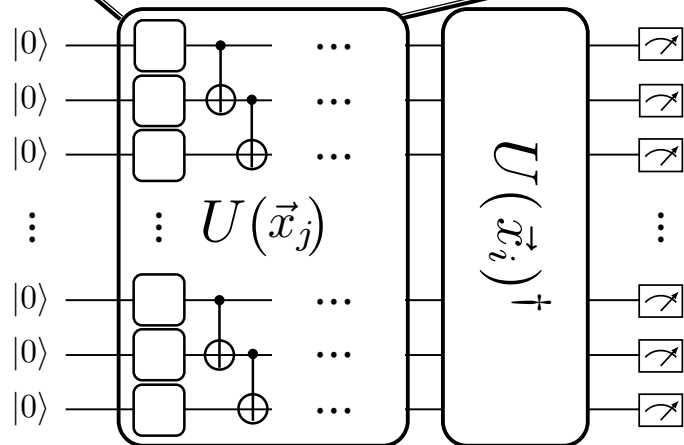
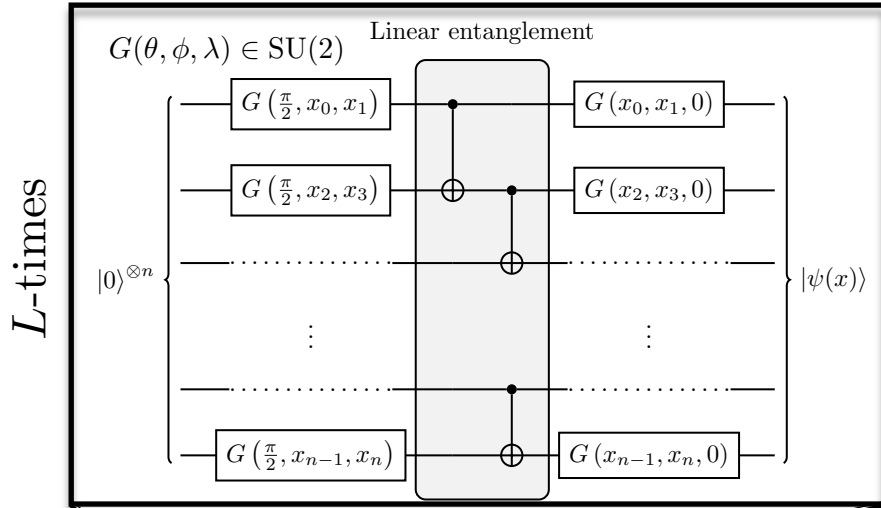


Different qubit number

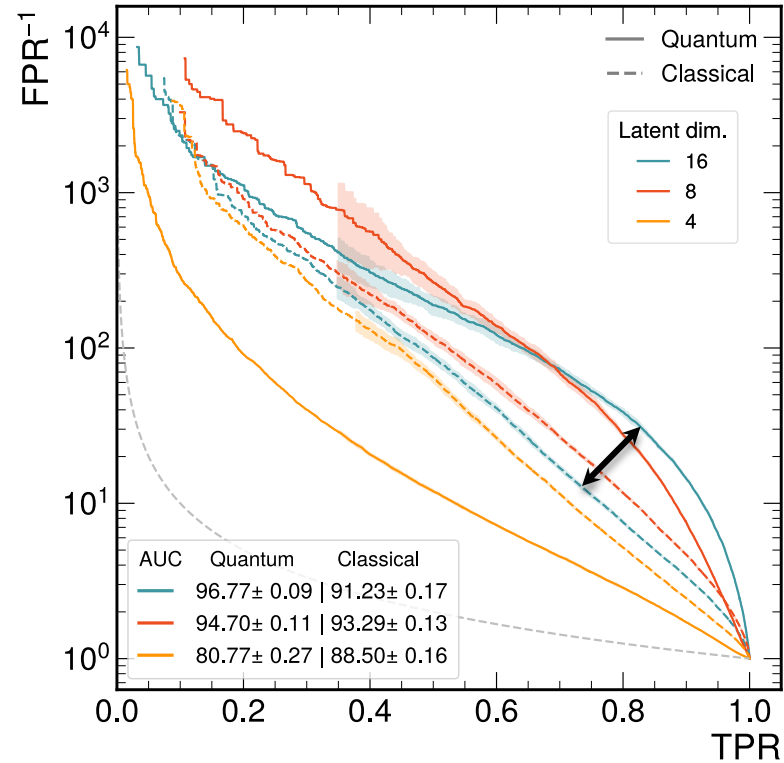


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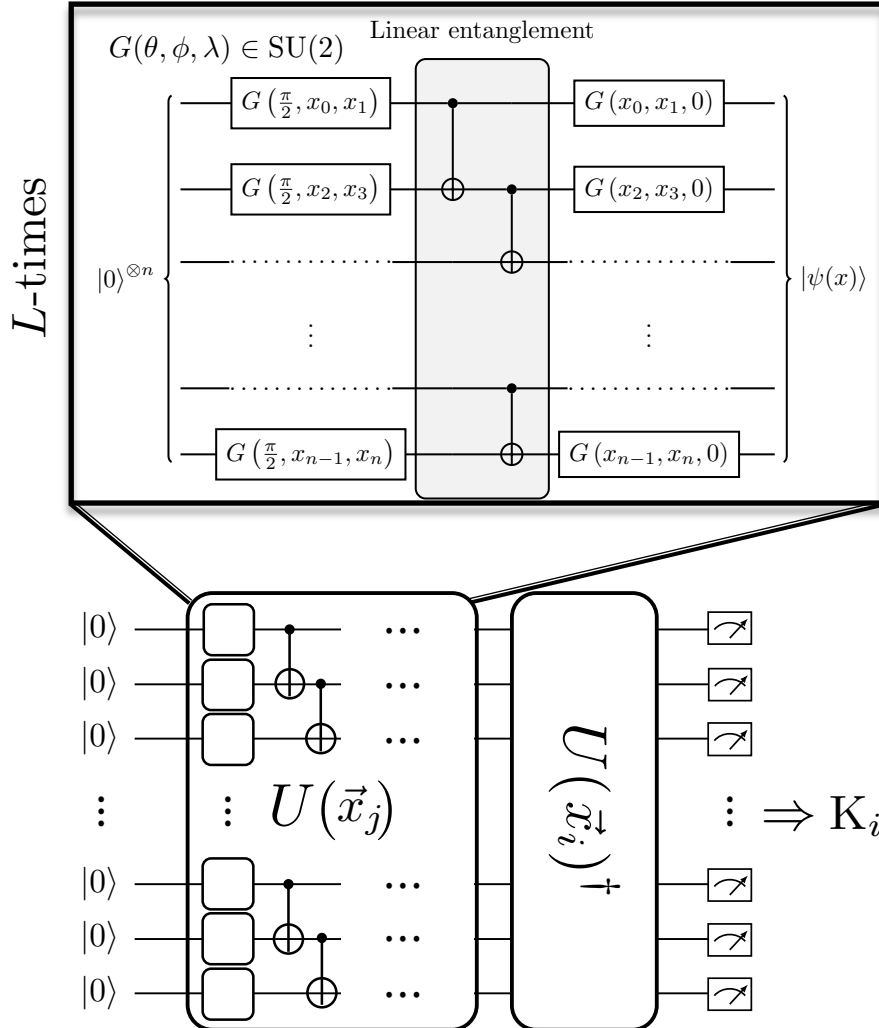


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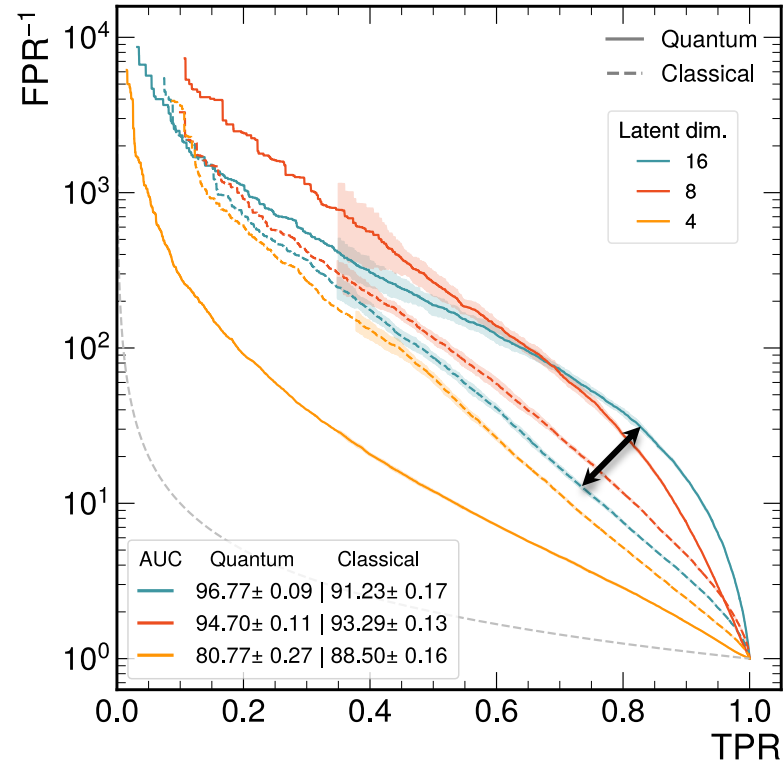


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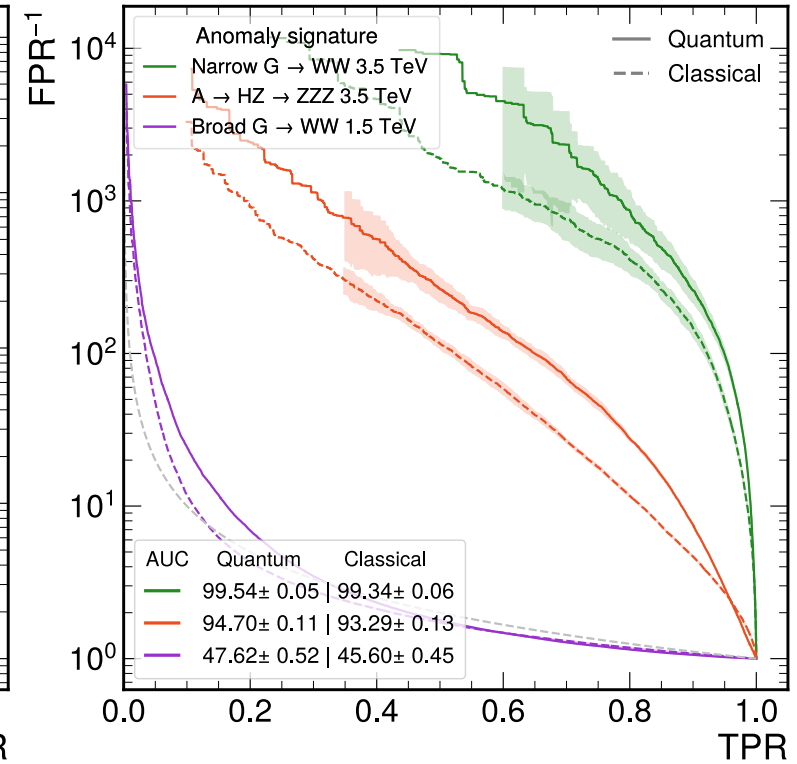
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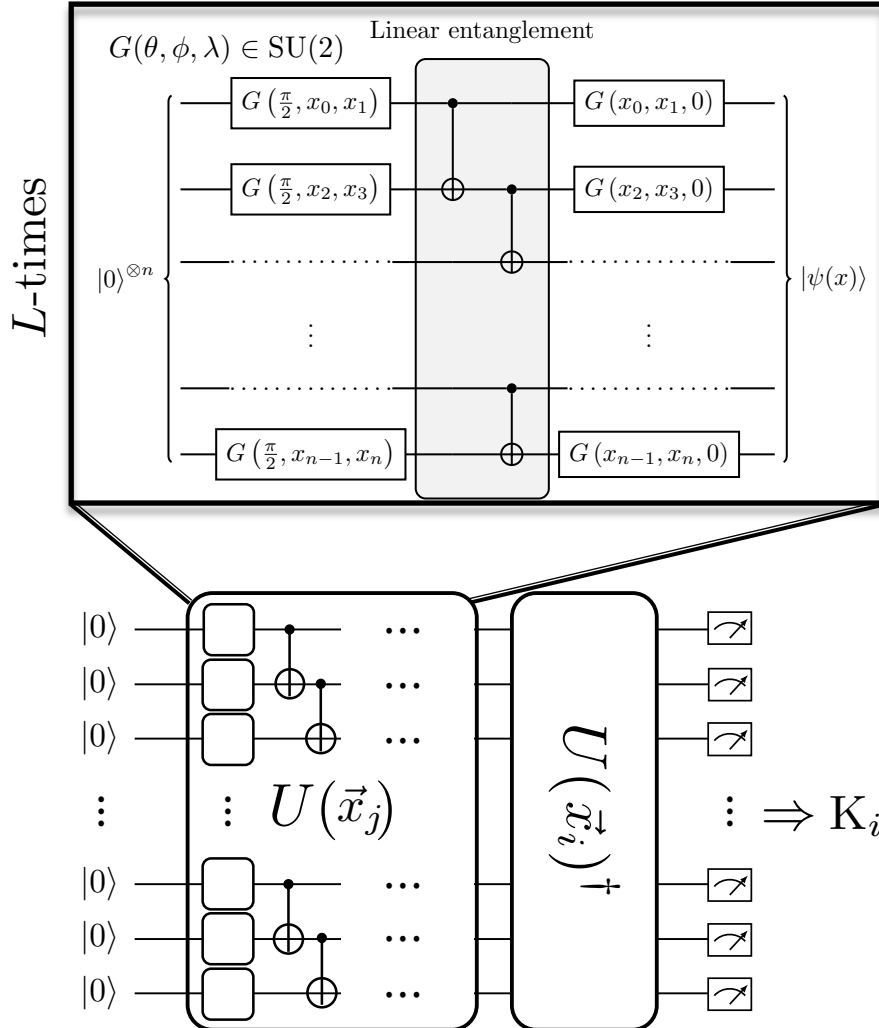


Different BSM scenarios

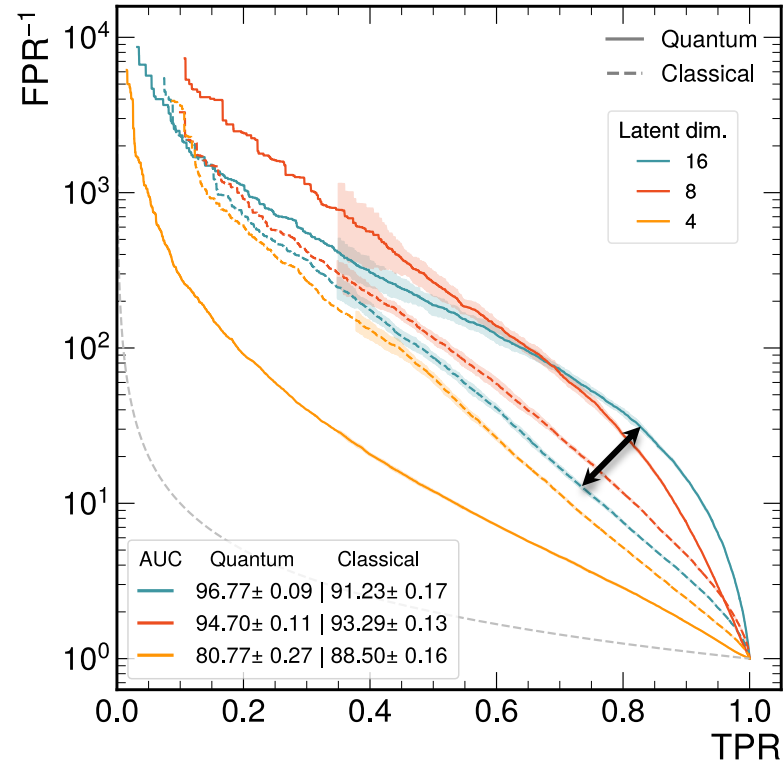


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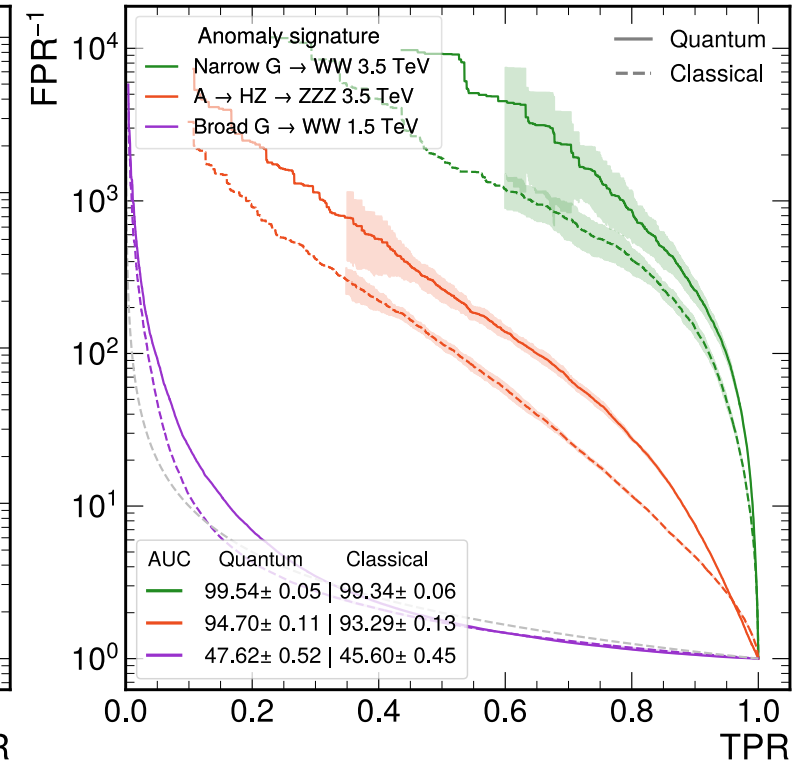
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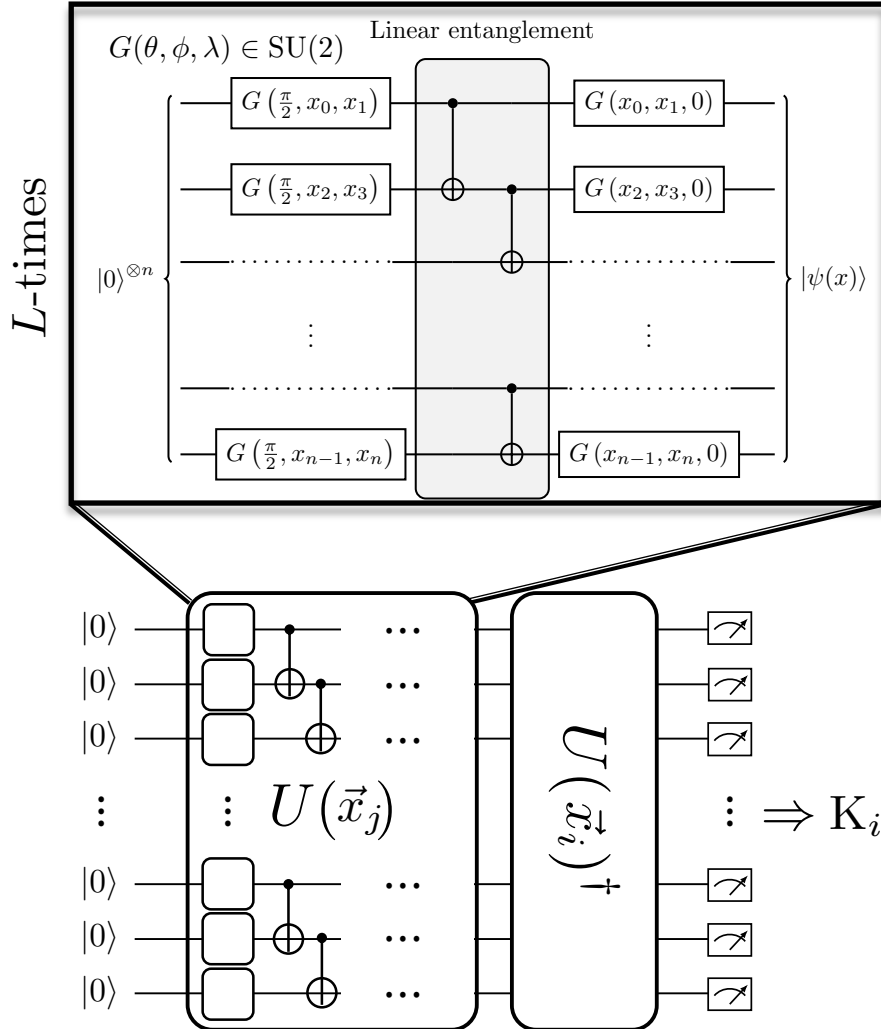
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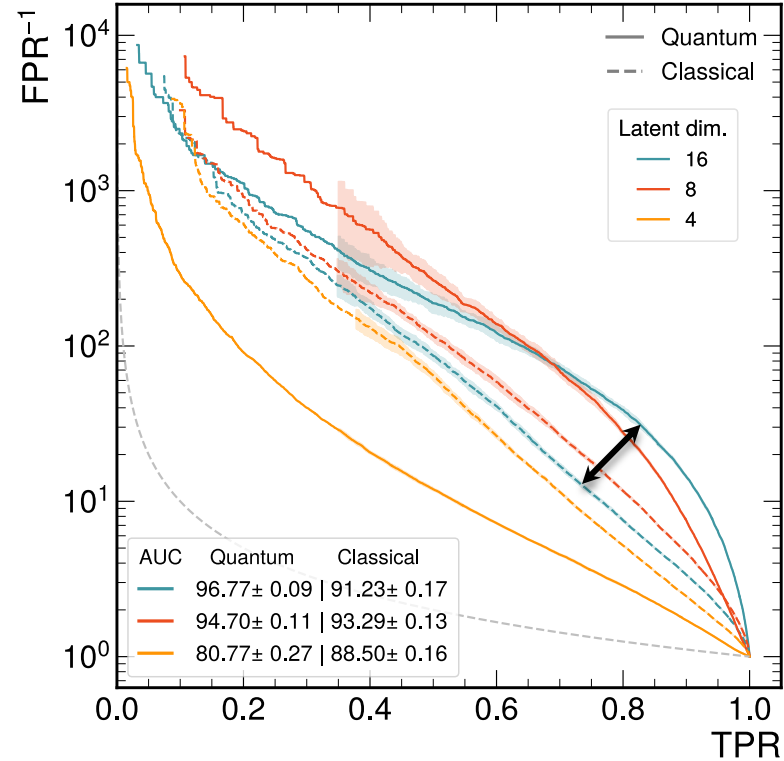
Are quantum effects utilized by the model?

Unsupervised quantum kernel machine

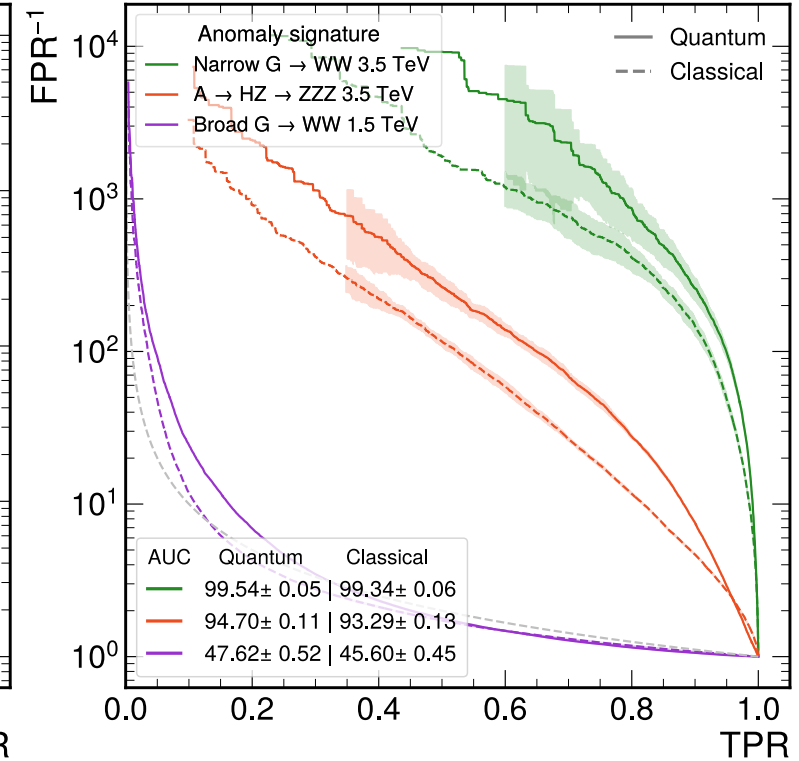
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Are quantum effects utilized by the model?

Yes!

Quantum circuit properties vs. performance

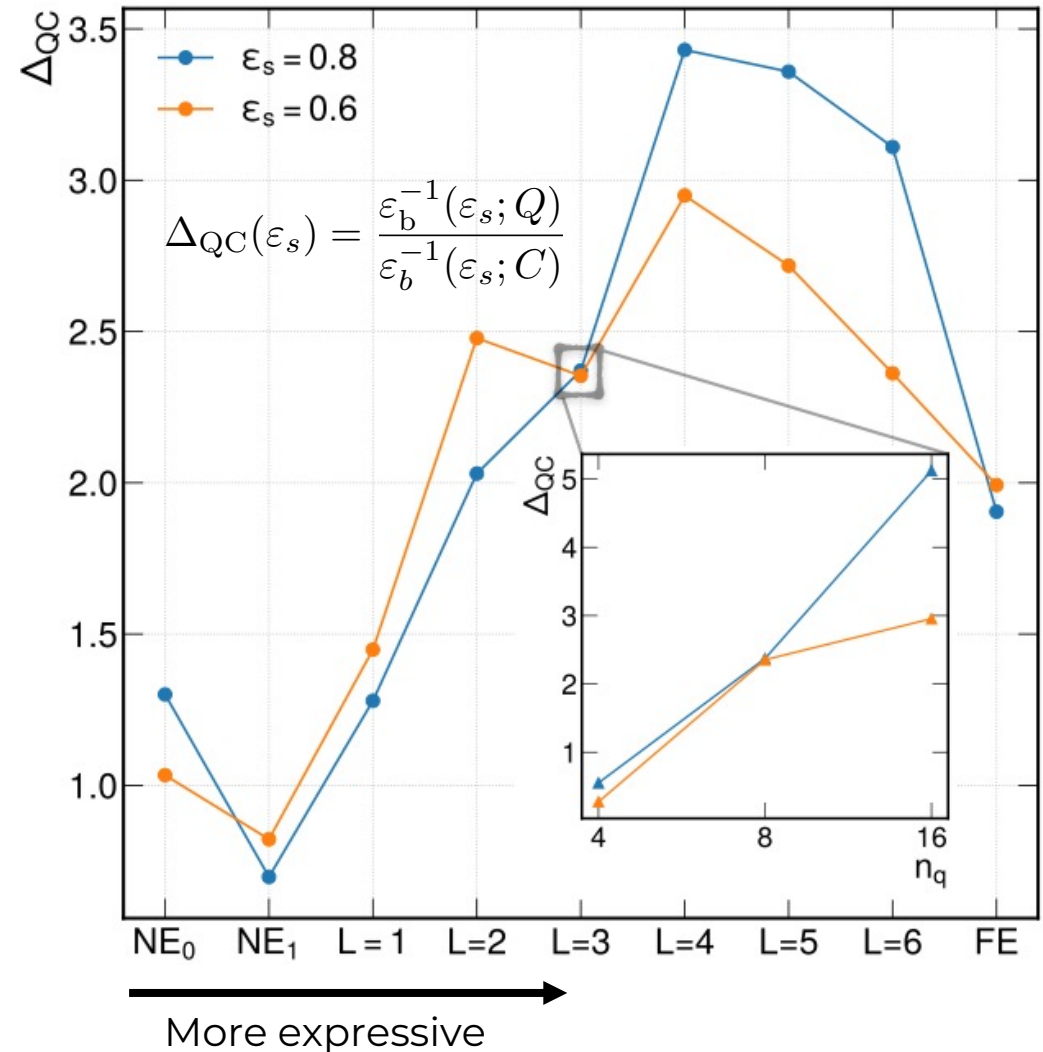
Importance of intrinsically quantum properties of the feature map.

Quantum circuit properties vs. performance

Importance of intrinsically quantum properties of the feature map.

ε_s Signal efficiency = True Positive Rate (TPR)

ε_b^{-1} Background Rejection = Inverse of False Positive Rate



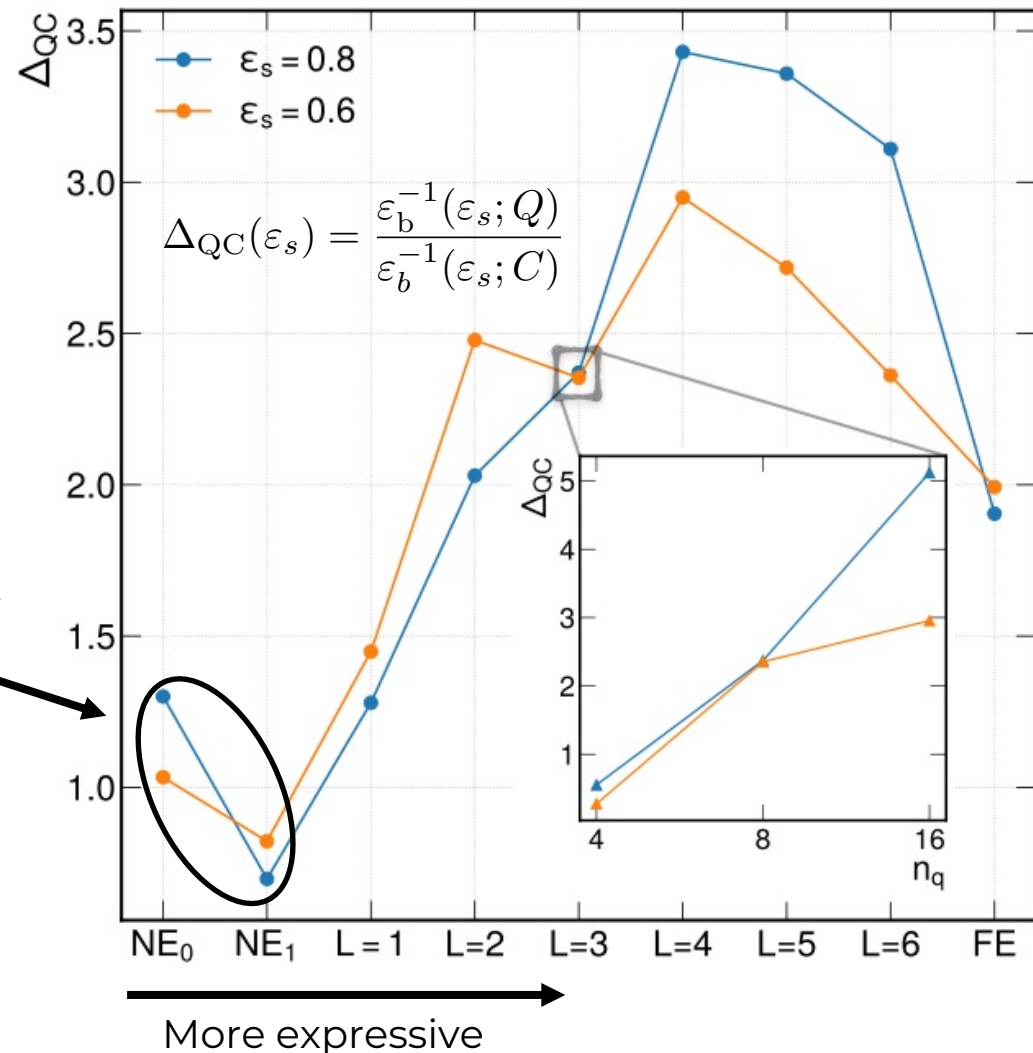
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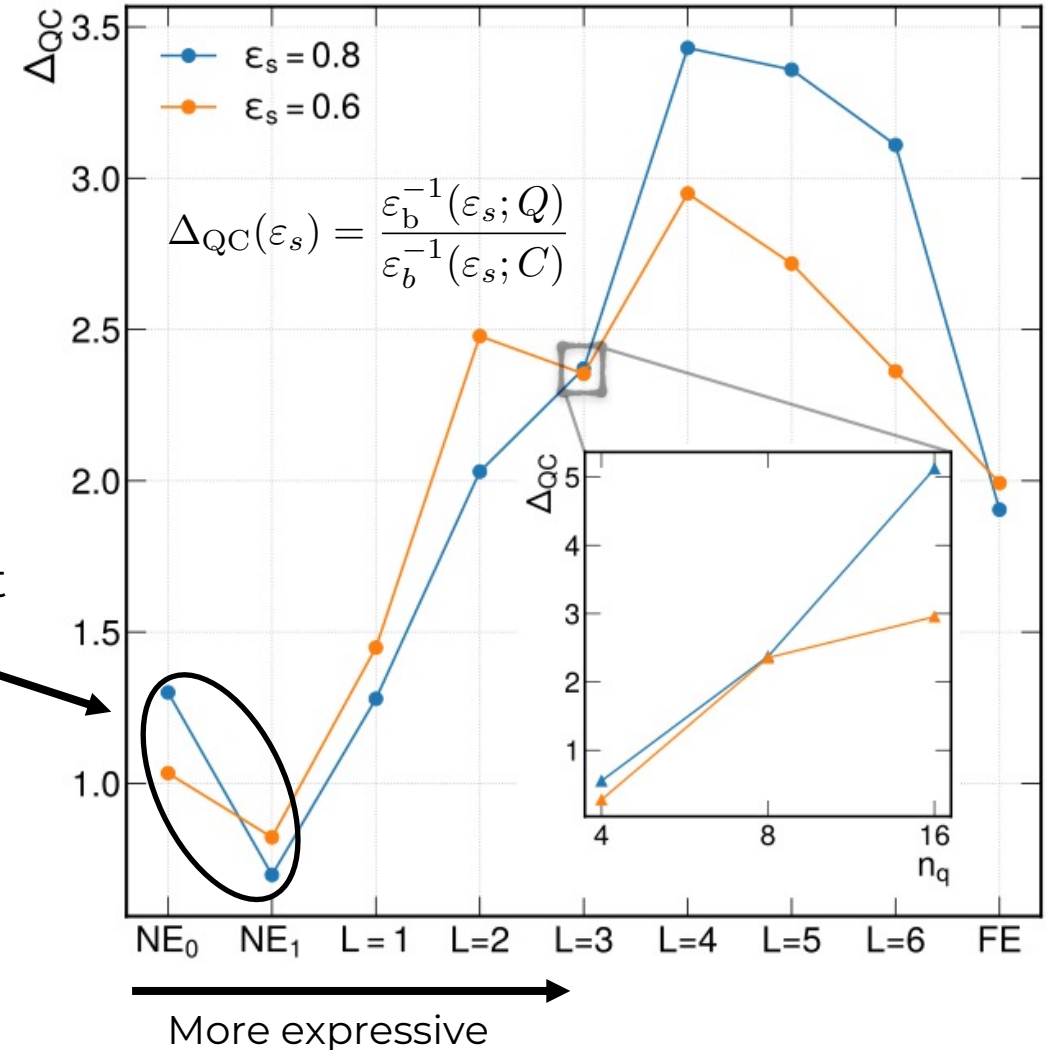
Importance of intrinsically quantum properties of the feature map.

Up to **five times** the performance of the classical benchmark for 16 qubits!

No entanglement

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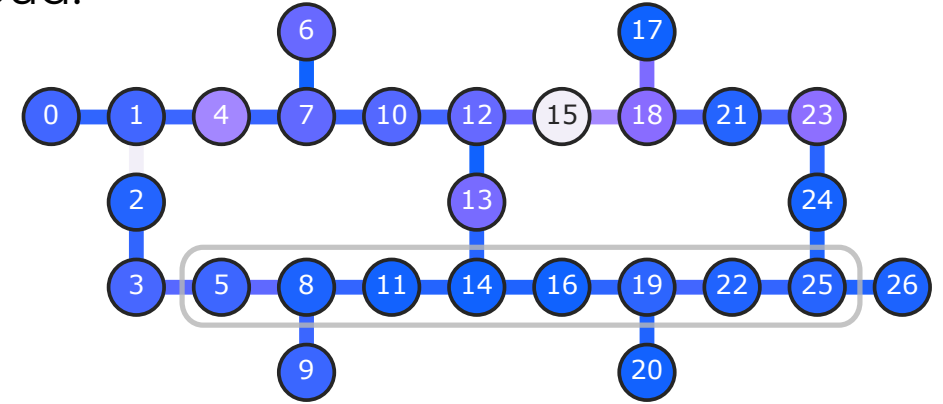
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Quantum hardware runs

Submit jobs to a real machine (ibm_toronto) using IBMQ cloud.

Minimal instance 100 + 100 (train + test) datapoints.

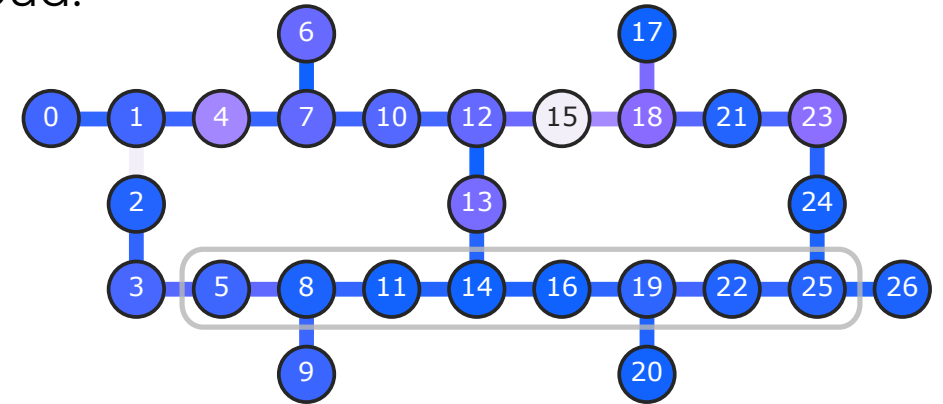


Superconducting qubits connectivity topology

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Superconducting qubits connectivity topology

Kernel Machine Run	AUC	$\langle \text{tr} \rho^2 \rangle$
Hardware $L = 1$	0.844	0.271(6)
Ideal $L = 1$	0.999	1
Hardware $L = 3$	0.997	0.15(2)
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Classical	0.998	-

Purity of fully mixed state: $1/2^{n_q} \approx 0.39 \times 10^{-2}$

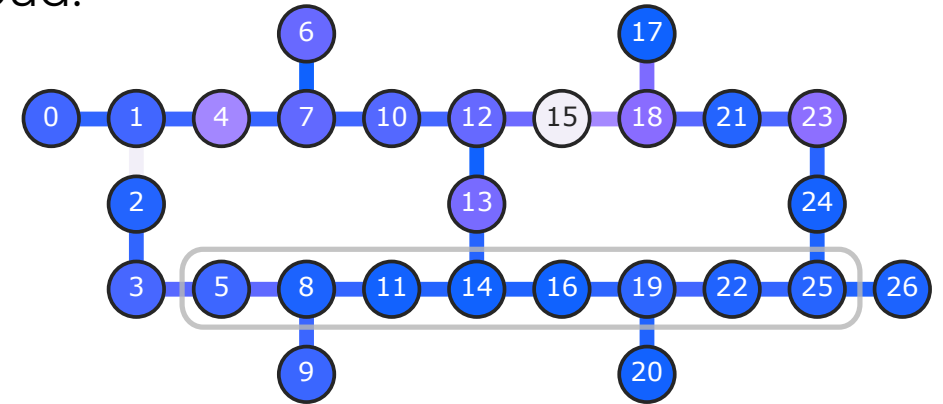
$$\langle \text{tr} \rho^2 \rangle = \langle K(x_i, x_i) \rangle$$

$$\rho(x_i) = U(x_i)|0\rangle\langle 0|U^\dagger(x_i)$$

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Proposed data encoding circuit realistic and suitable for current devices

Summary

QML + HEP : very promising results and interplay (sandbox).

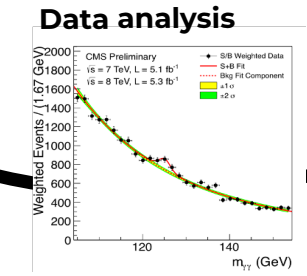
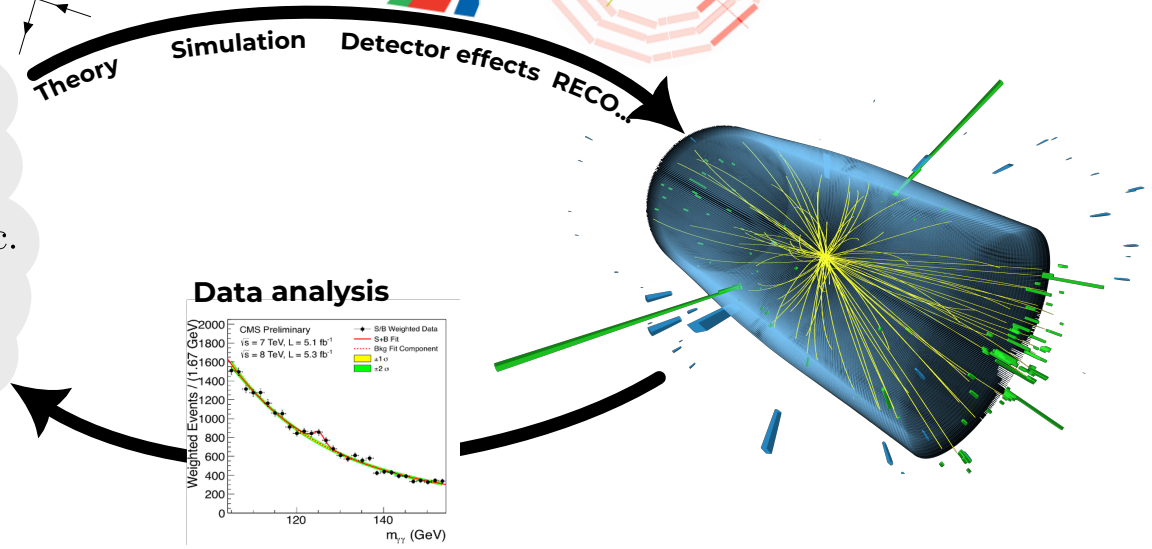
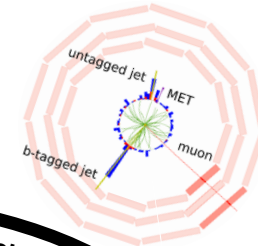
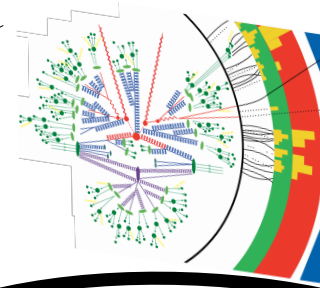
- Utilize data generated by a quantum process.
- New inductive biases?

$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}^a F^{a\mu\nu} + \sum_f \bar{\psi}_f (i\gamma^\mu D_\mu - m_f)\psi_f$$

$$+ (D_\mu \Phi)^\dagger (D^\mu \Phi) - V(\Phi) - \sum_f y_f \bar{\psi}_f \Phi \psi_f + \text{h.c.}$$

+ BSM?

$$\langle \Omega | T \{ \phi(x_1) \phi(x_2) \} | \Omega \rangle = \frac{\int \mathcal{D}\phi \phi(x_1) \phi(x_2) e^{iS[\phi]}}{\int \mathcal{D}\phi e^{iS[\phi]}}$$



Summary

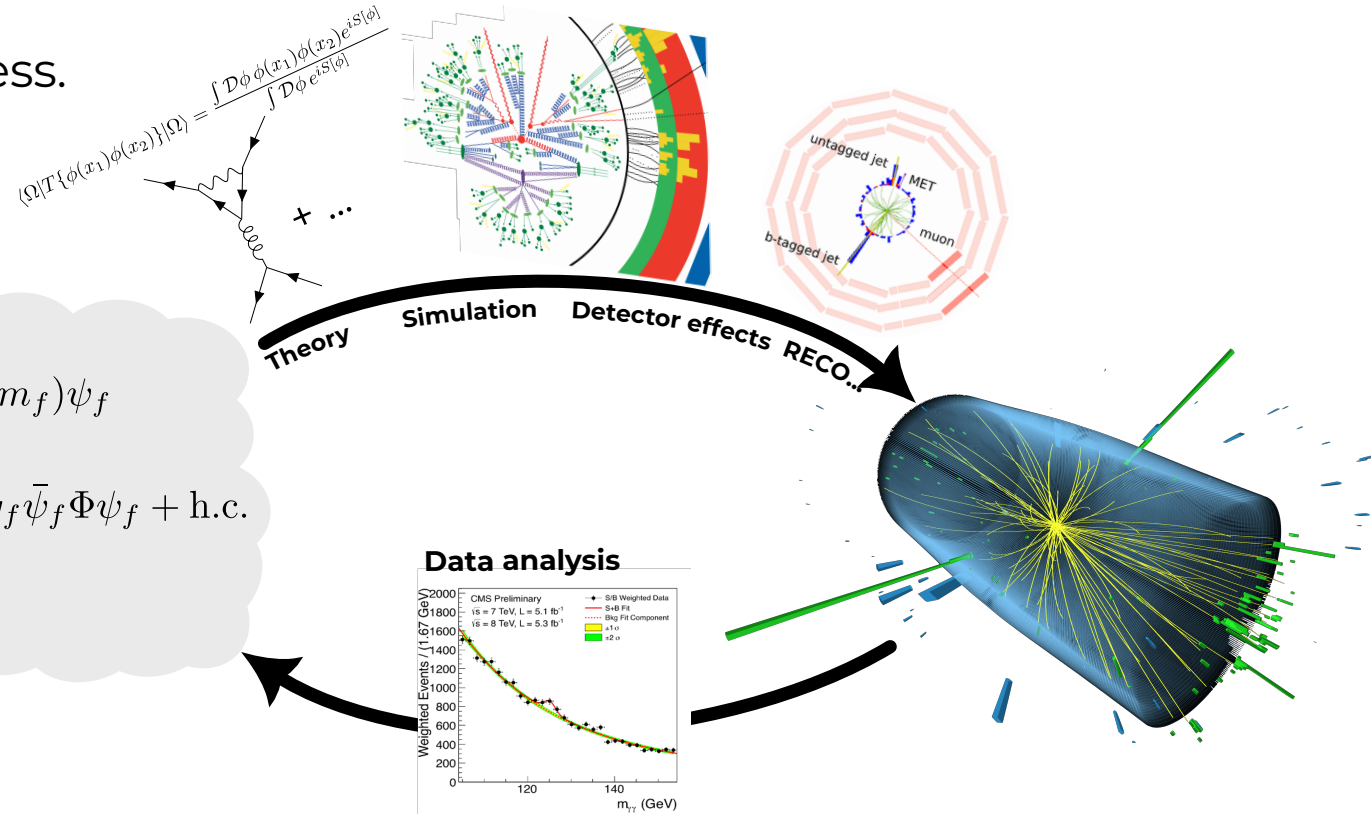
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For more details checkout:

[K.A. Wozniak*, VB*, E. Puljak* et al., 2301.10780]

[VB, S. González-Castillo, et al., 2104.07692]

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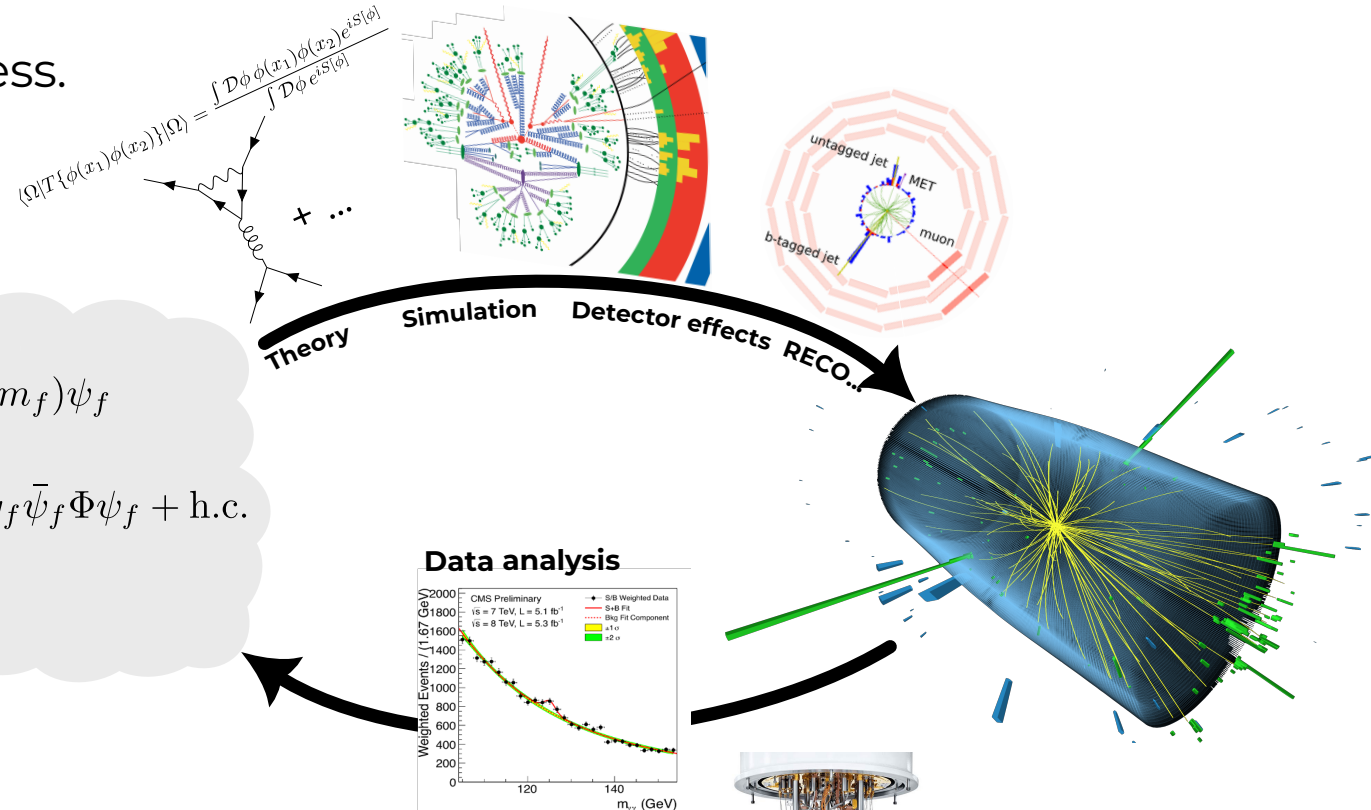
[T. Muser, E. Zapusek, VB, F. Reiter, 2309.14406]

Summary

QML + HEP : very promising results and interplay (sandbox).

- Utilize data generated by a quantum process.
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$$\mathcal{L} = -\frac{1}{4}F_{\mu\nu}^a F^{a\mu\nu} + \sum_f \bar{\psi}_f (i\gamma^\mu D_\mu - m_f)\psi_f + (D_\mu \Phi)^\dagger (D^\mu \Phi) - V(\Phi) - \sum_f y_f \bar{\psi}_f \Phi \psi_f + \text{h.c.} + \text{BSM?}$$



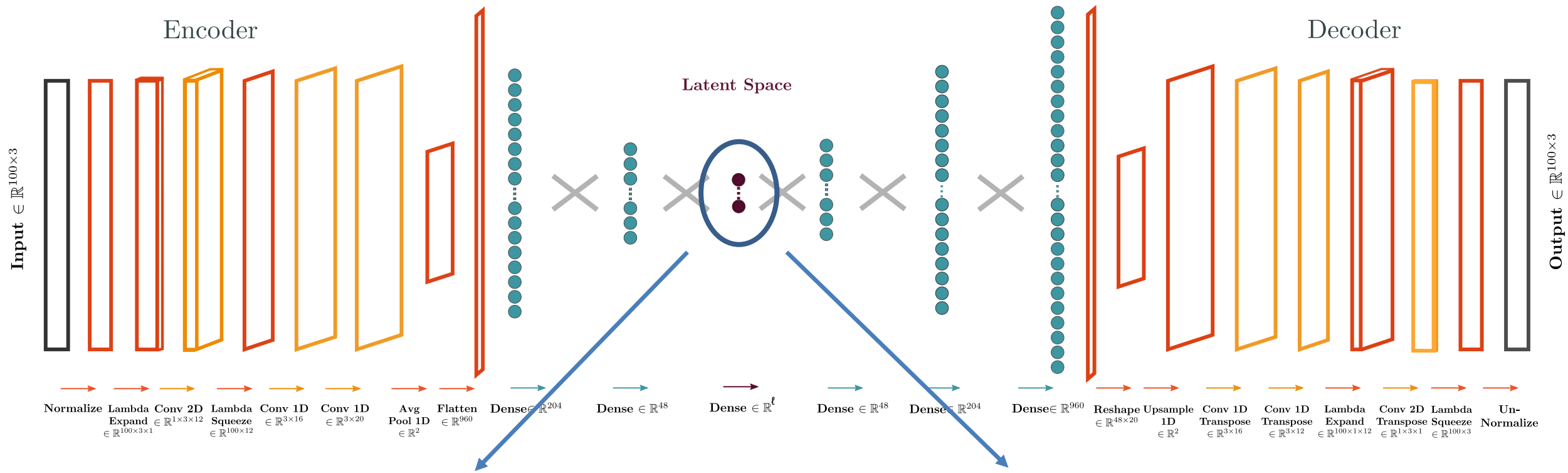
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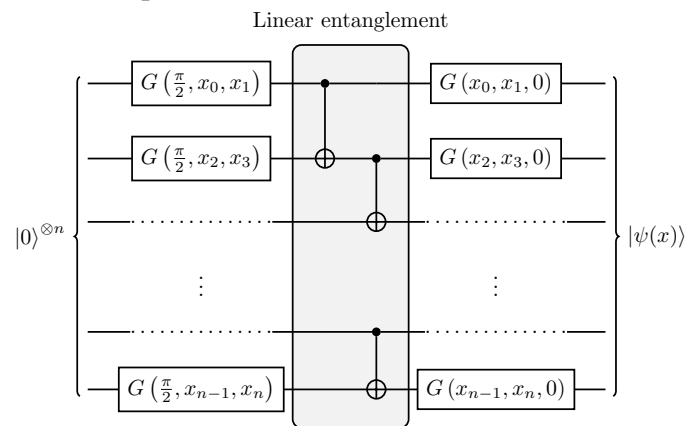
Any cool ideas?
 Questions?

Backup slides

Convolutional autoencoder architecture

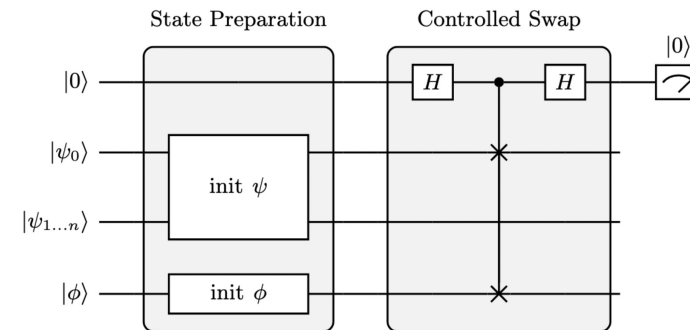


Unsupervised kernel machine



Training size:
 $\mathcal{O}(10^2) - \mathcal{O}(10^3)$

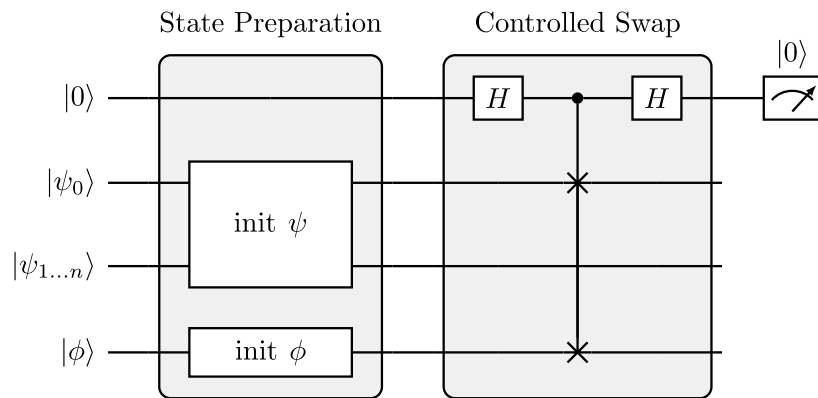
Quantum clustering algorithms



Quantum clustering for anomaly detection

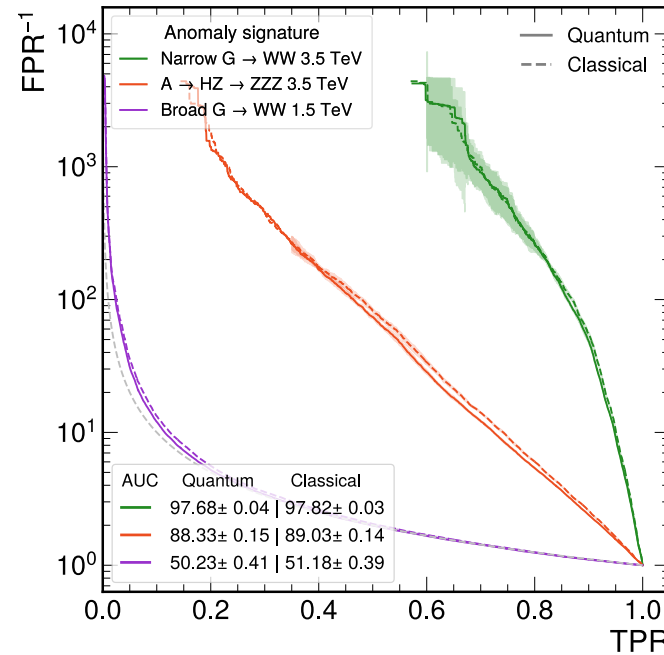
Construct clusters in the Hilbert space

Quantum distance calculation from clusters

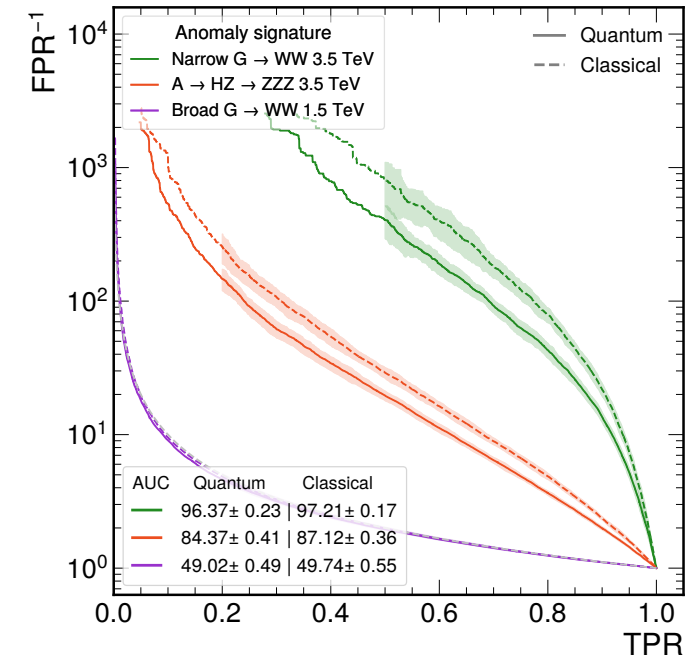


Minimise the distance with **quantum** (QK-means) or hybrid/**classical** (QK-medians) optimisation algorithms

Quantum K-medians



Quantum K-means

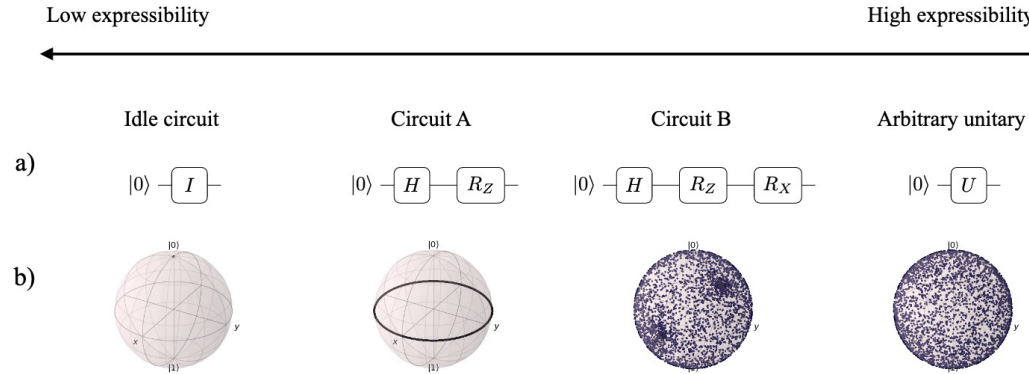


[K.A. Wozniak*, VB*, E. Puljak*, et al., arXiv: 2301.10780]

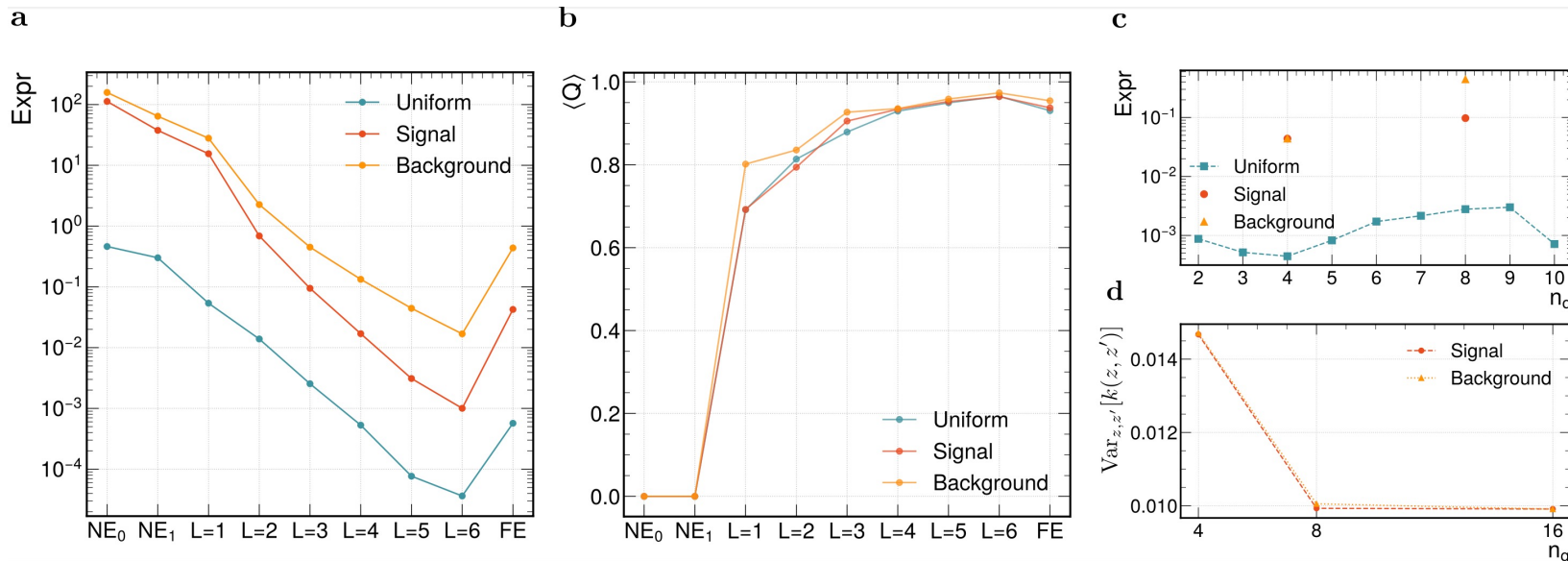
Quantum and classical anomaly detection has similar performance.

Expressibility and entanglement capability

Expressibility [S. Sim, et al., Adv. Quantum Technol. 2 (2019) 1900070]

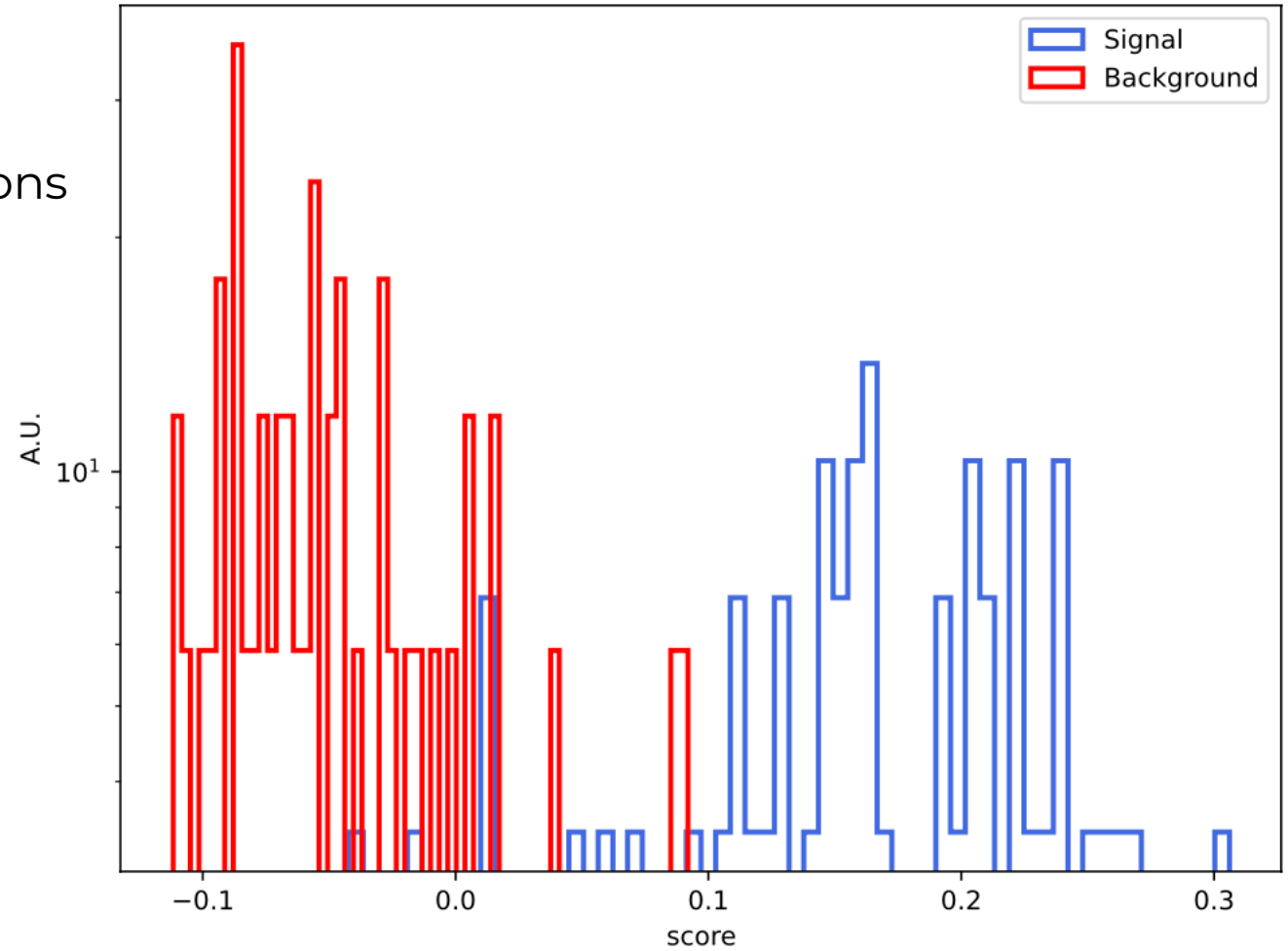


Expressibility & Entanglement capability of our data encoding circuit



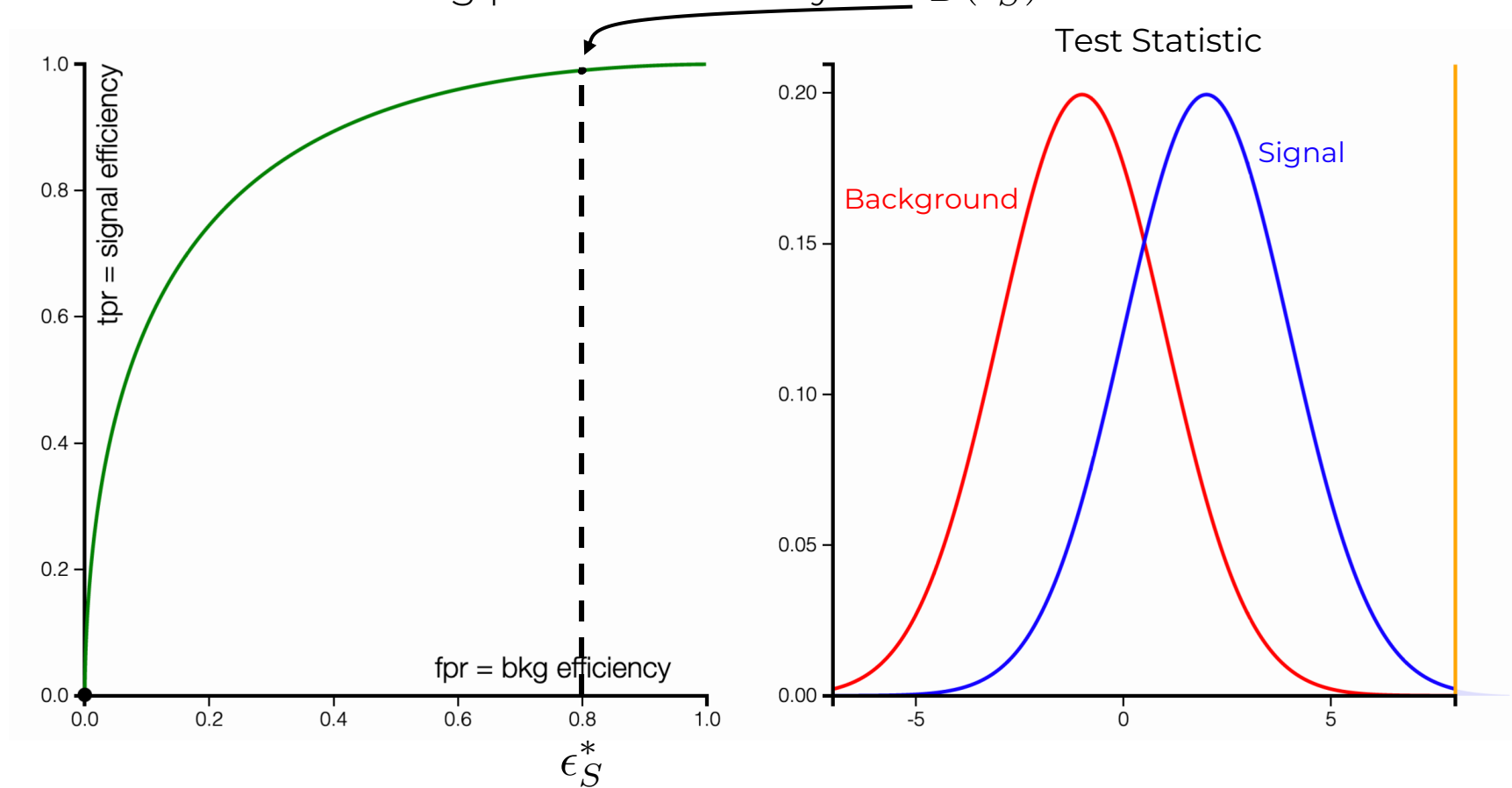
Sparsity of the distributions in hardware

All models have sparse output distributions when training size is low.



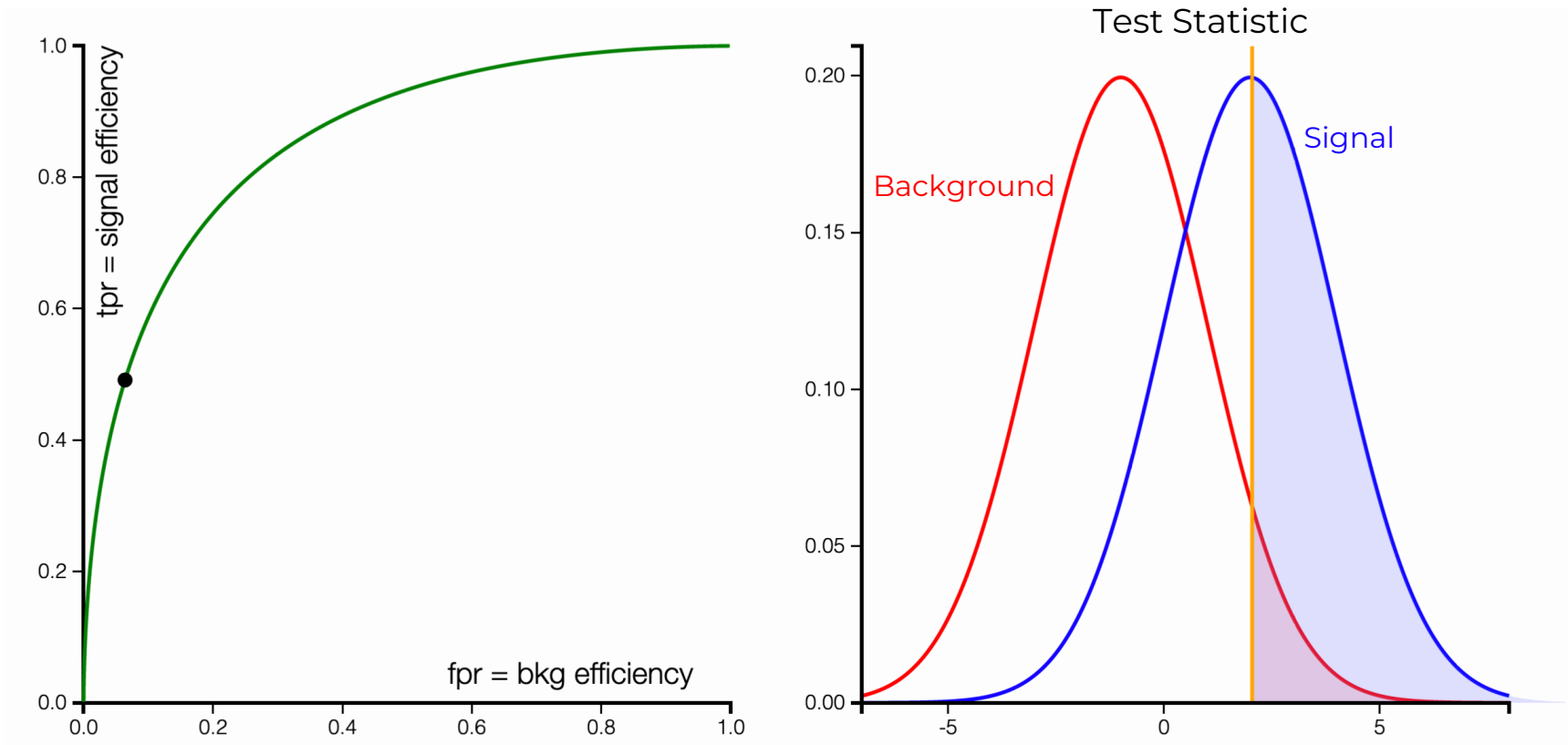
Performance Metric

- The normalised data samples are split into training, validation, and testing data sets.
- Classification power metric: Receiver Operating Characteristic (ROC) curve.
- More compact metric: Area Under Curve (AUC) of the ROC curve.
- More practical metric: working point of an analysis $\epsilon_B(\epsilon_S^*)$



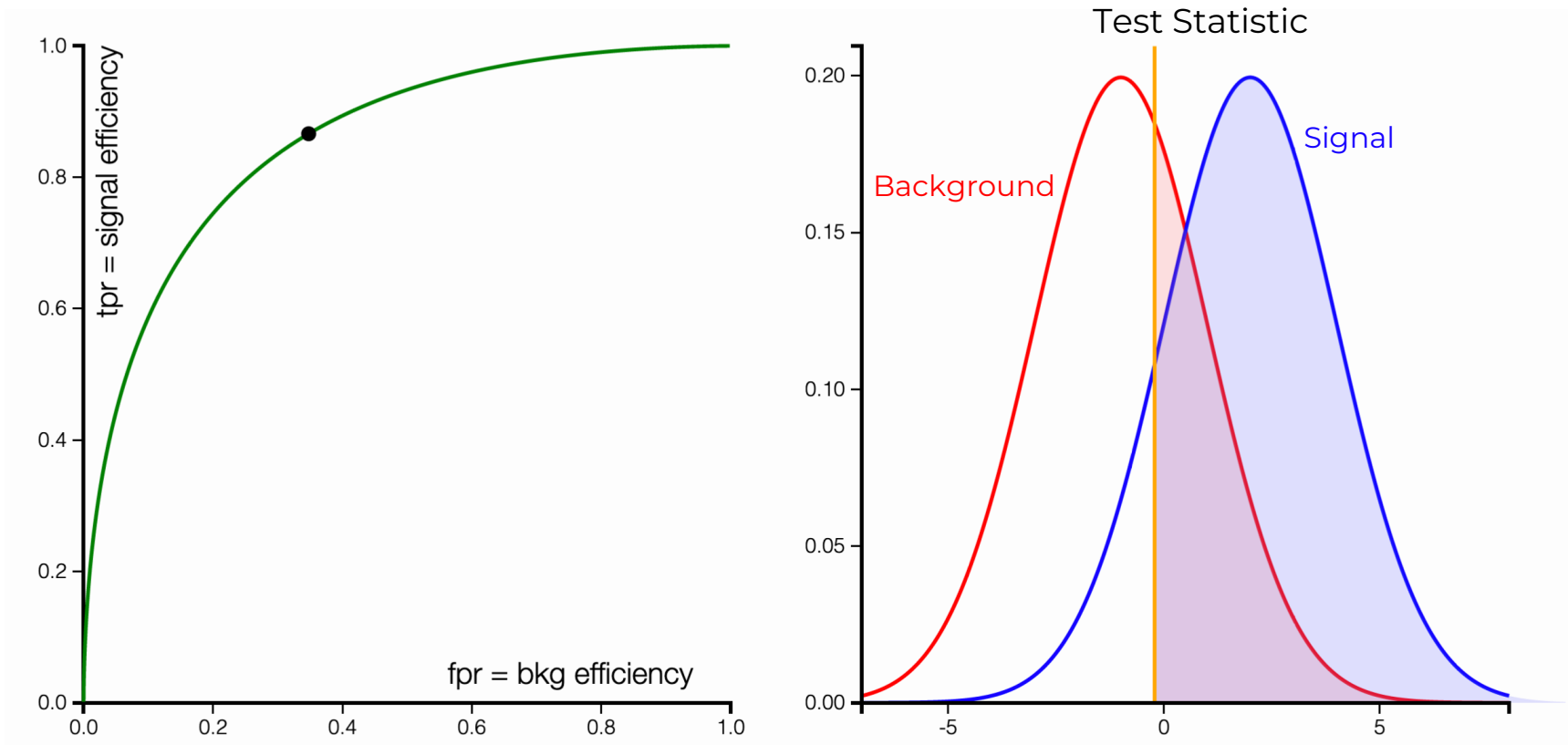
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