

# Transport Simulations of Pion Production in Low Energy Au+Au Collisions

Master's Thesis  
by  
Christian Kummer



**AQTIVATE**

# Outline

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- Motivation
- GiBUU Transport Code
- Proton Rapidity Distributions
- Pion Spectra
- Dileptons
- Conclusions

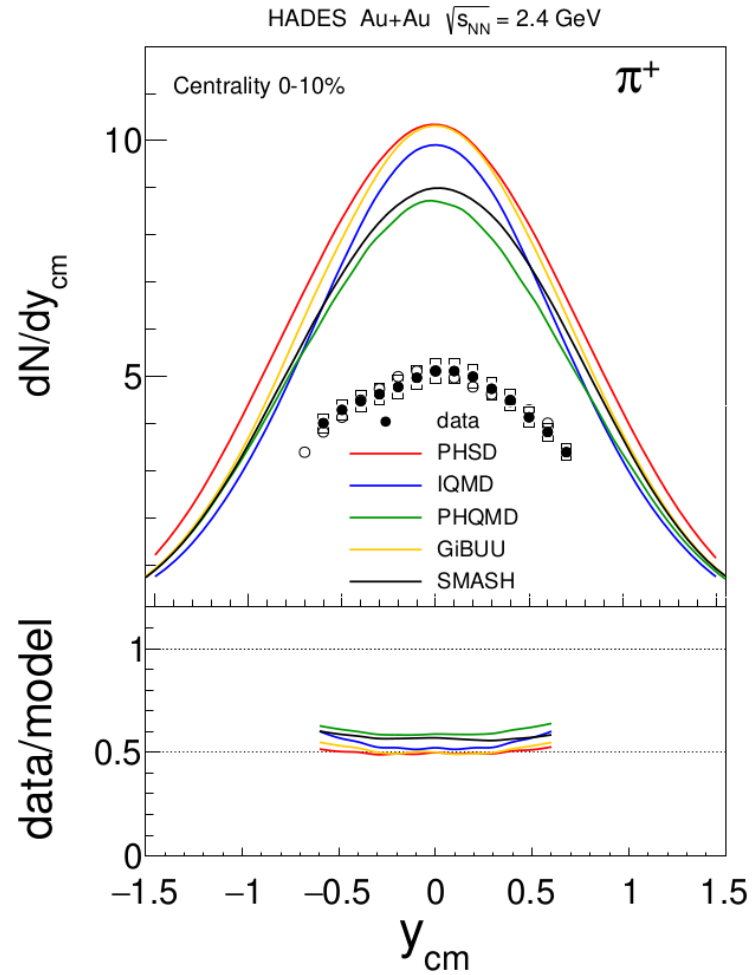
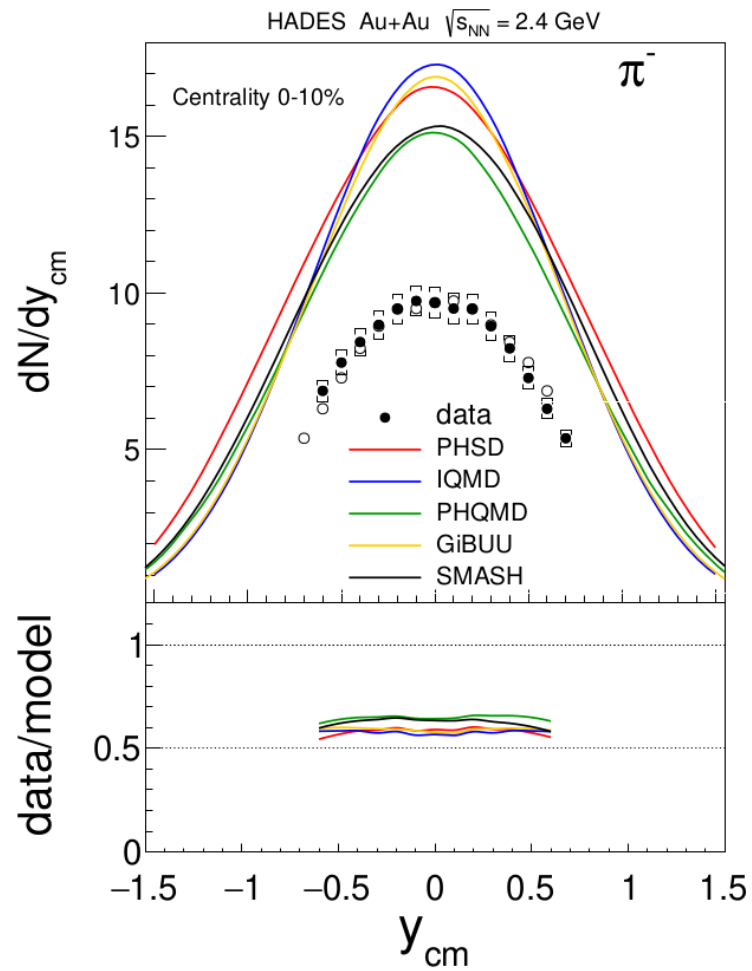
Based on: C. Kummer *et al.*, <http://arxiv.org/abs/2309.09042>

# Motivation

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- Strong nuclear force can be studied by Heavy-ion collisions (HIC)
- Transport models simulate HICs
- New experimental data from HADES [1] shows that transport theories produce an excess of pions

# Motivation



$$y = \frac{1}{2} \ln\left(\frac{E + p_z}{E - p_z}\right)$$

# GiBUU Transport Code

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- Giessen Boltzmann-Uehling-Uhlenbeck Transport Code [2] combines two concepts
- Inclusion of Mean-Field
- Cascade Model

$$\frac{\partial f}{\partial t} + \mathbf{v} \cdot \nabla_r f - \nabla_r U \cdot \nabla_p f = I_{\text{coll}}$$

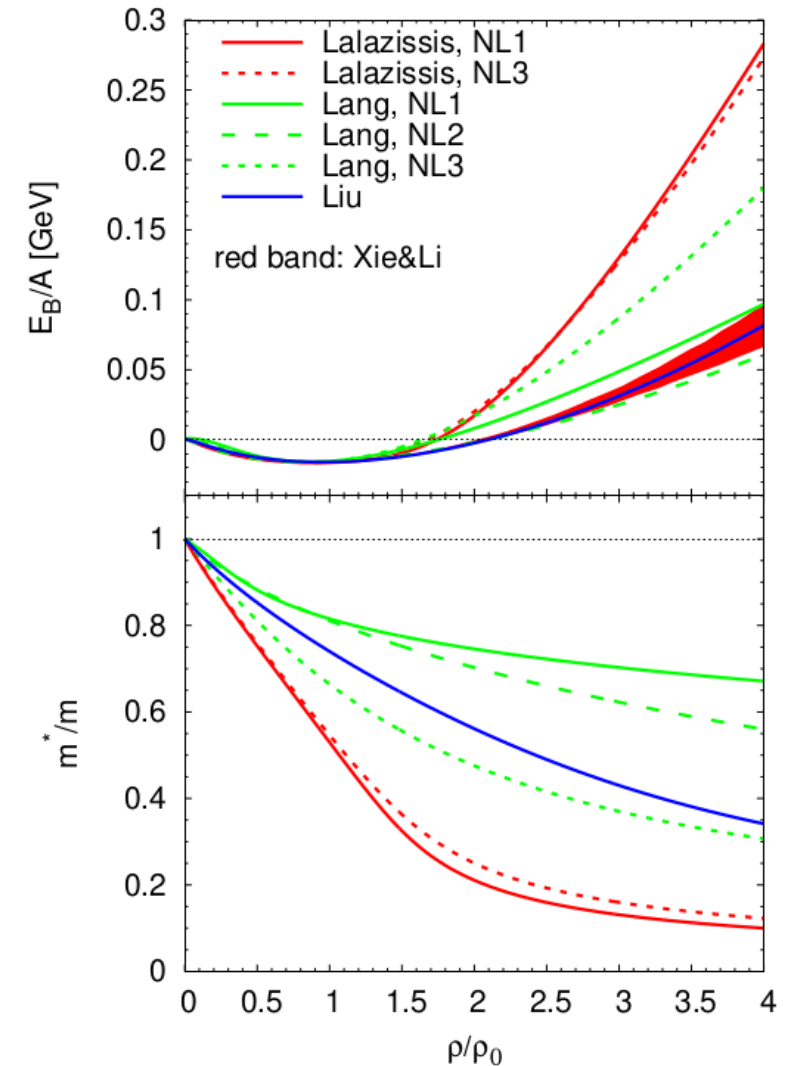
# GiBUU Transport Code: Mean Field

- Relativistic Mean Field (RMF)
- Gives equation of state (EOS)
- Meson fields are included

$$m_N^* = m_N + S \quad p^{*\mu} = p^\mu - V^\mu$$

$$(p^*)^2 - (m_N^*)^2 = 0$$

[3-6]



# GiBUU Transport Code: Cascade Model

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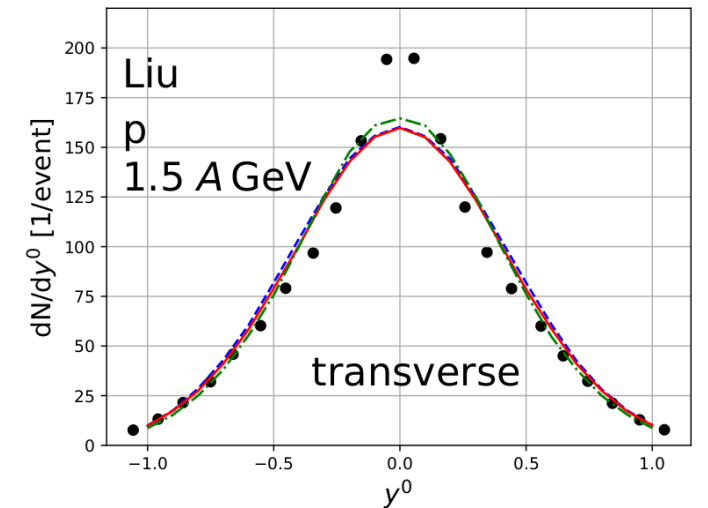
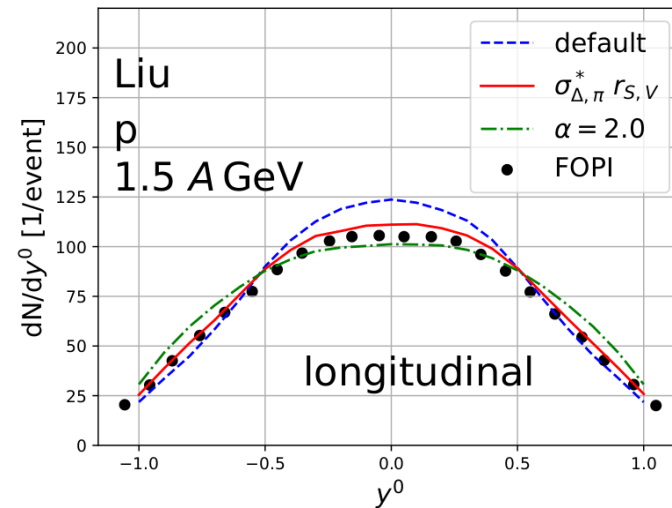
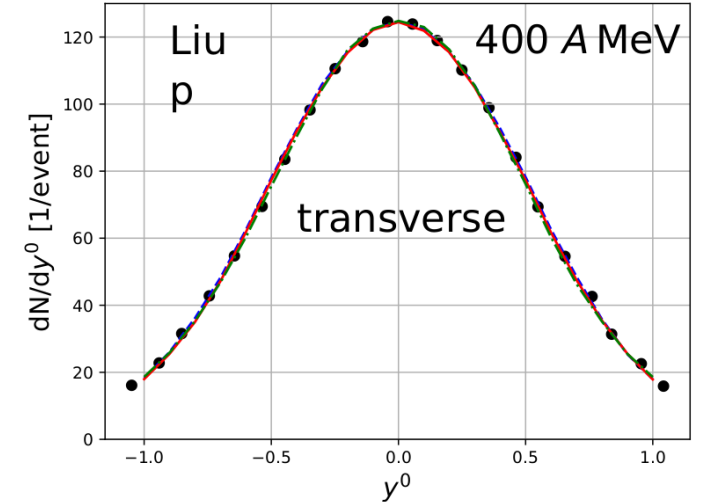
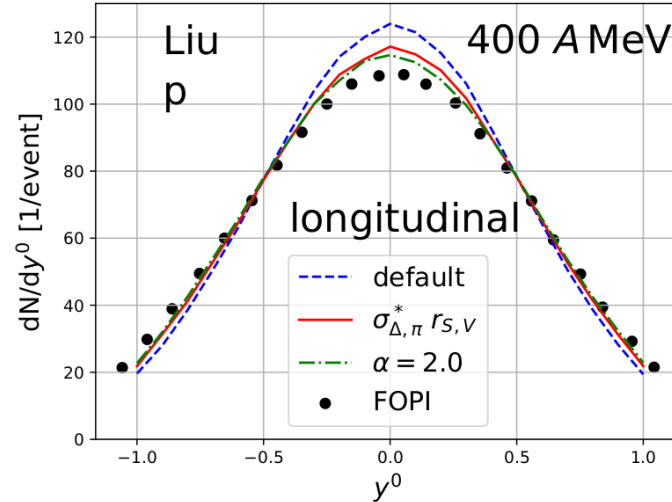
- Checks for Collisions
- Decides on the reaction channel by Monte Carlo (MC)
- Cross sections can be altered by
  - Effective Mass
  - Delta potential modifications
  - Exponential Suppression

# Proton Rapidity Distributions

- Data from FOPI [7]

$$y_z = \frac{1}{2} \log \left( \frac{E + p_z}{E - p_z} \right)$$

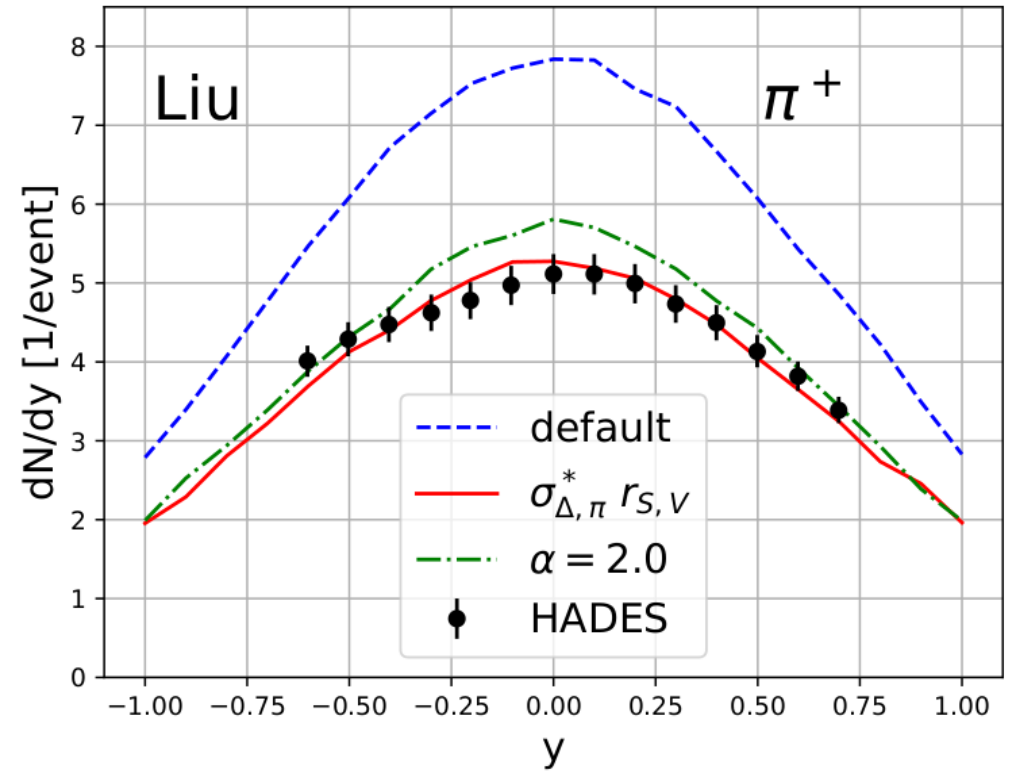
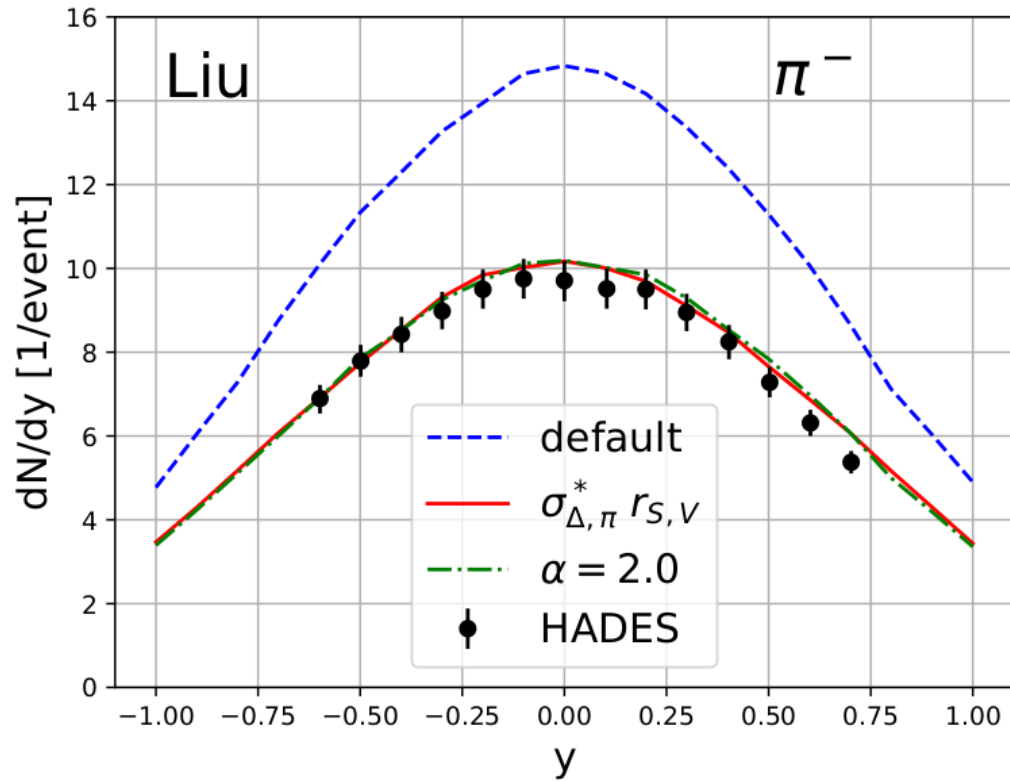
$$y_x = \frac{1}{2} \log \left( \frac{E + p_x}{E - p_x} \right)$$



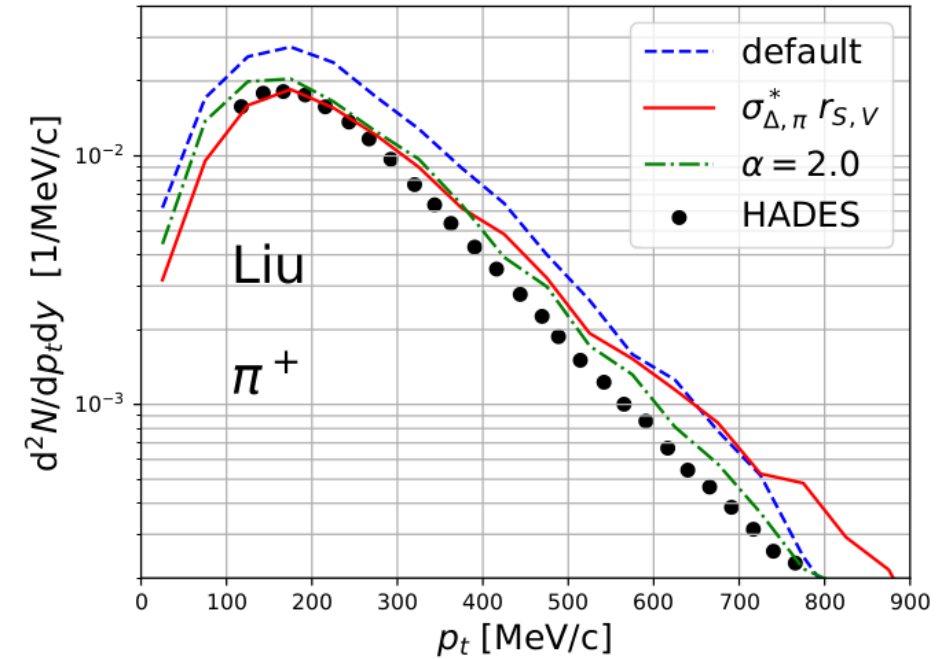
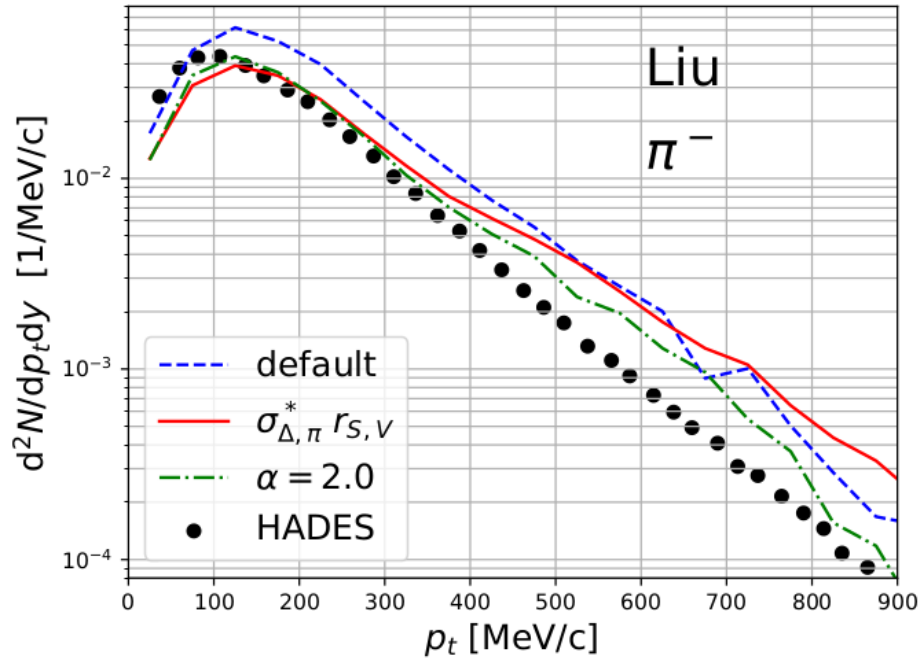


# Pion Spectra

- Data from HADES [1]



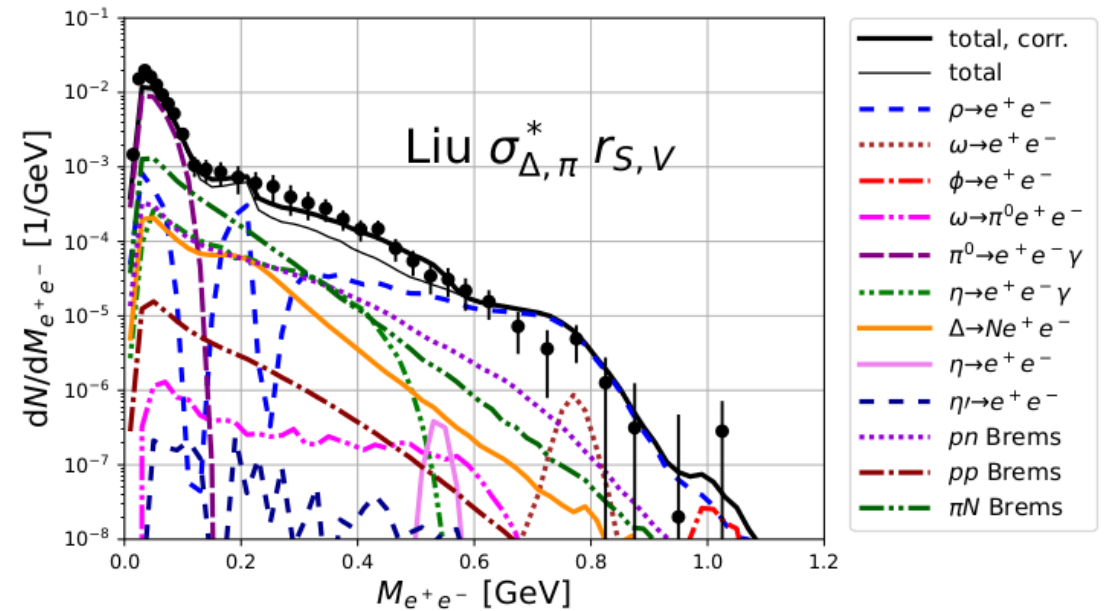
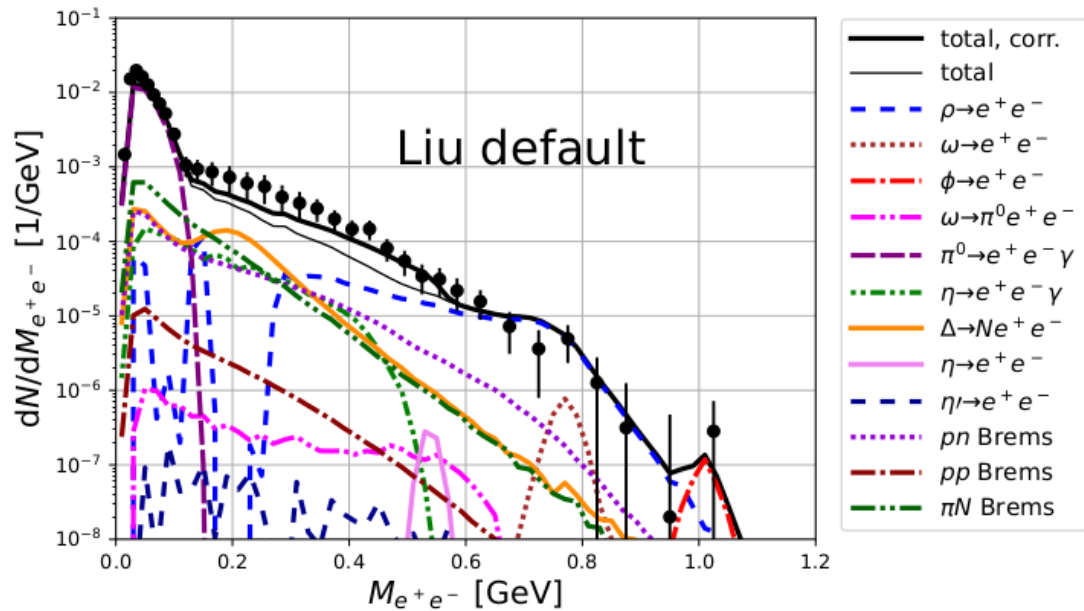
# Pion Spectra



	default	$\sigma_{\Delta, \pi}^* r_{S, V}$	$\alpha = 2.0$	HADES
$M(\pi^-)$	24.462	17.188	16.999	$17.1 \pm 1.8$
$M(\pi^+)$	13.577	9.2364	9.7266	$9.3 \pm 1.0$
$M(\pi^-)/M(\pi^+)$	1.8017	1.8609	1.7476	$1.83 \pm 0.17$

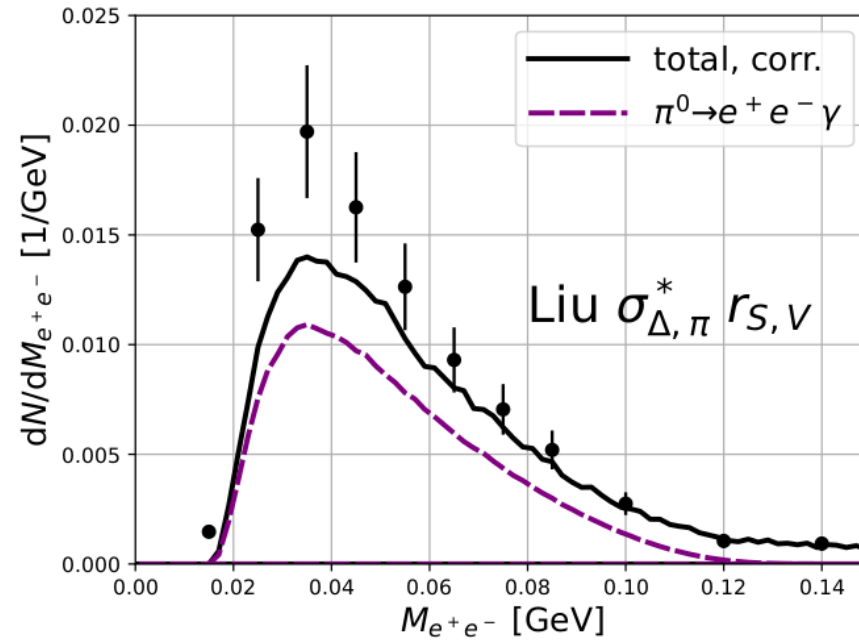
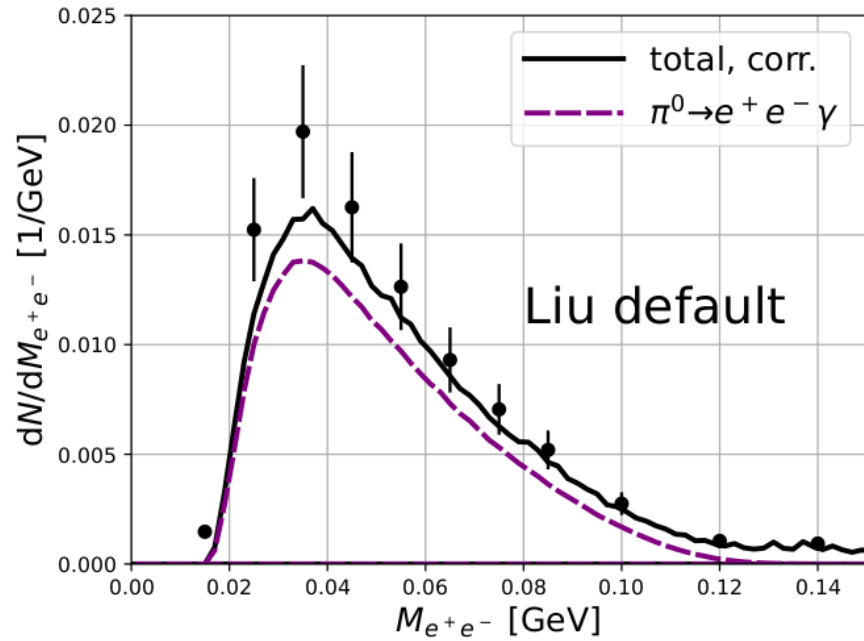
# Dileptons

- Data from HADES [8]



# Dileptons

- Data from HADES [8]



# Conclusions

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- Liu EOS describes the mean field well
- Modifications lower pion numbers drastically
- Modifications are not just motivated by phenomenology
- Some problems remain (transverse momentum spectra and dileptons)
- Overall: Significant improvement and excellent agreement with rapidity spectra

Thank you

# Bibliography

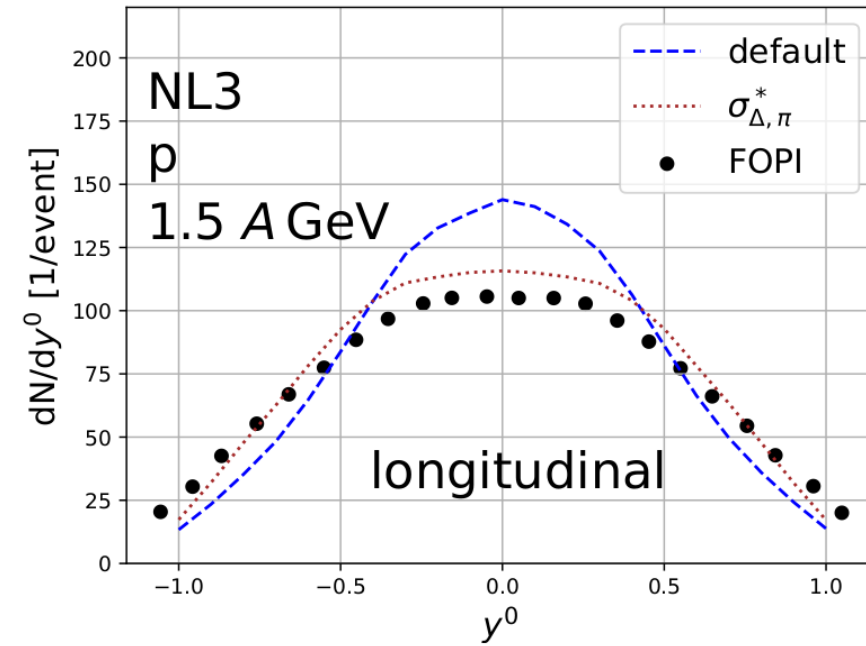
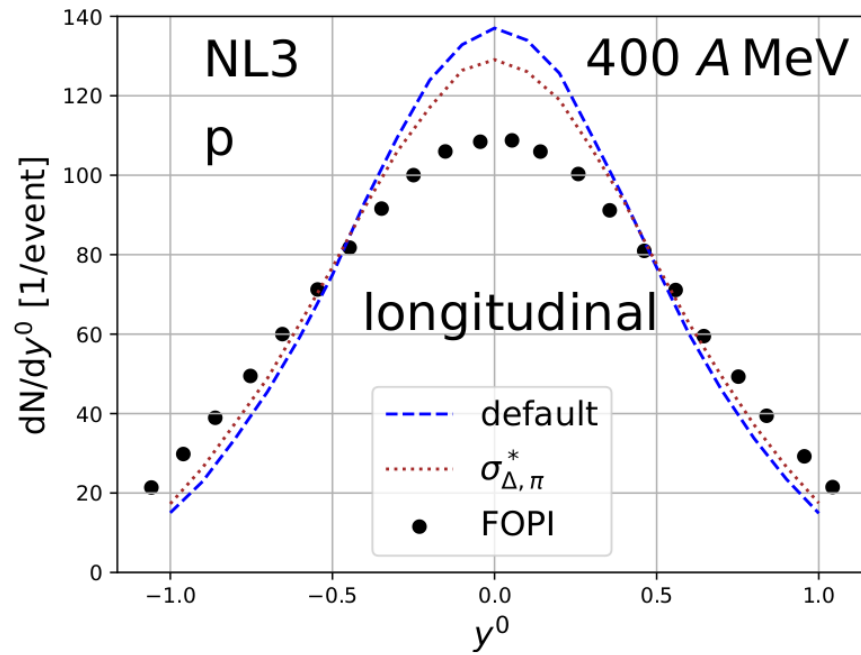
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- [1] J. Adamczewski-Musch *et al.*, EPJA 56, 259 (2020)
- [2] O. Buss *et al.*, PR 512, 1 (2012)
- [3] G.A. Lalazissis *et al.*, PRC 55, 540 (1997)
- [4] A. Lang *et al.*, NPA 541, 507 (1992)
- [5] B. Liu *et al.*, PRC 65, 045201 (2002)
- [6] W.J. Xie *et al.*, AJ 899.1, 4 (2020)
- [7] W. Reisdorf *et al.*, PRL 92, 232301 (2004)
- [8] J. Adamczewski-Musch *et al.*, Nature 15.10, 1040 (2019)

BACKUP



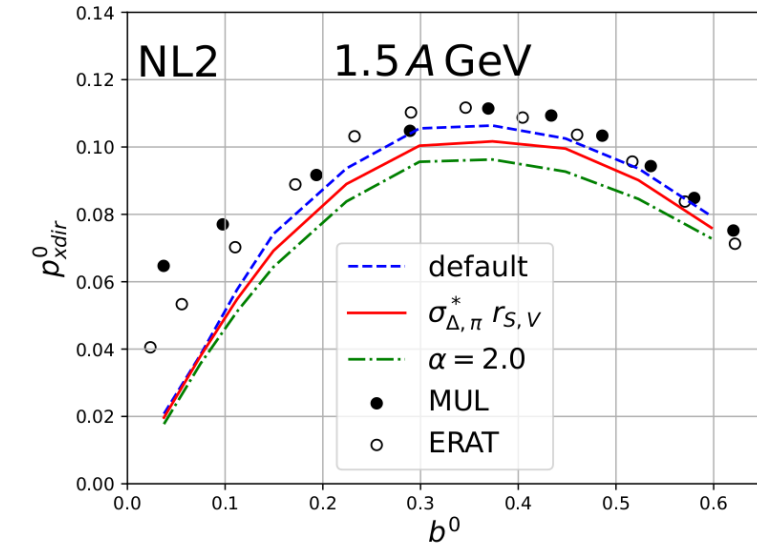
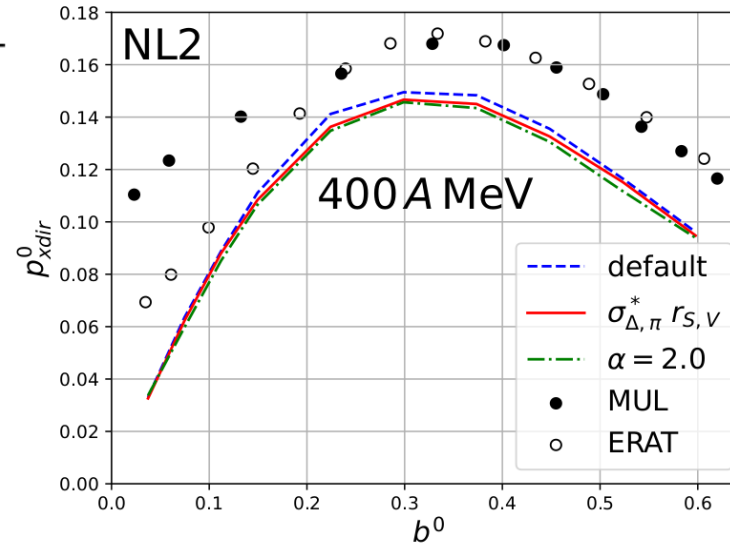
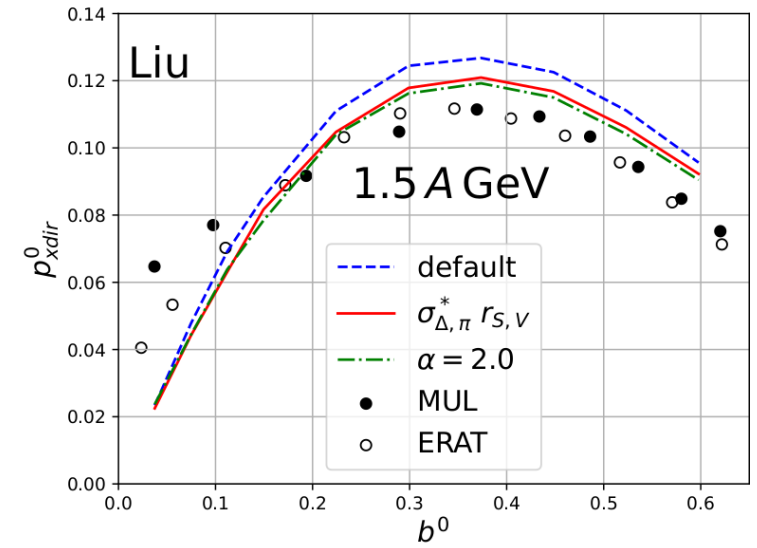
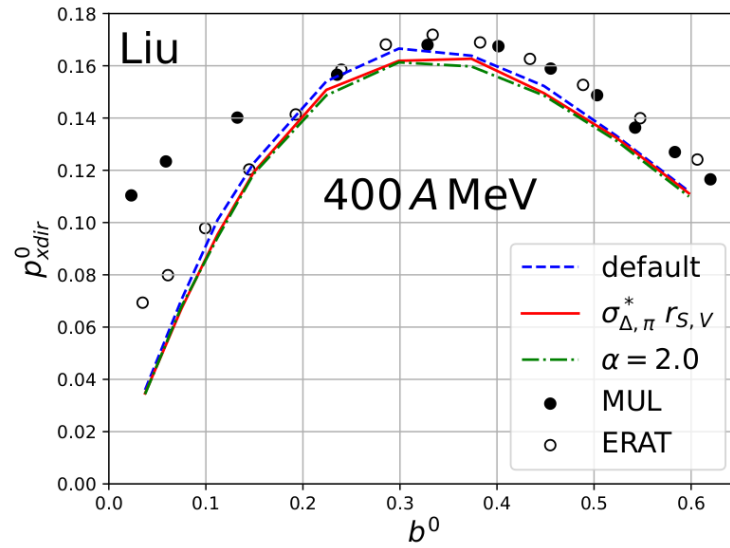
# Proton Rapidity Distribution, NL3 Lalazissis EOS



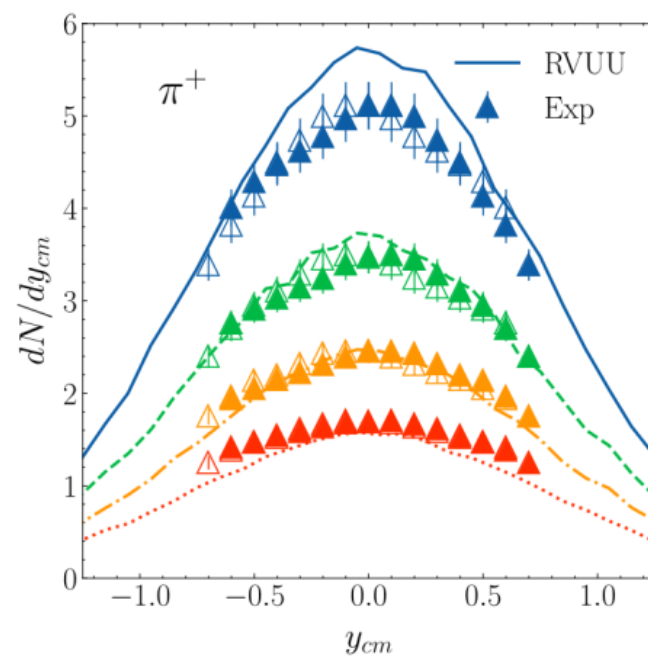
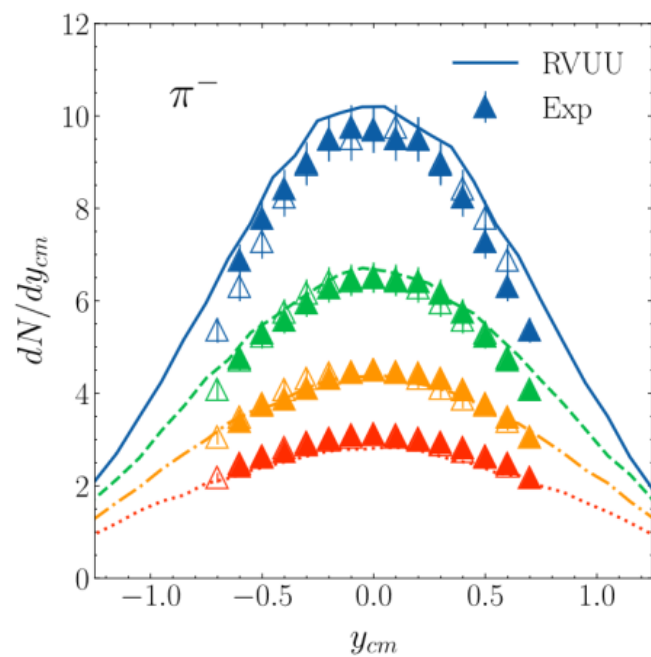
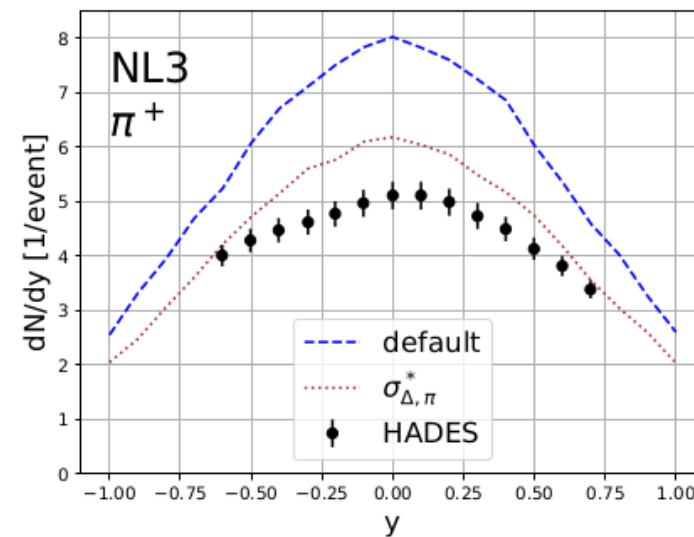
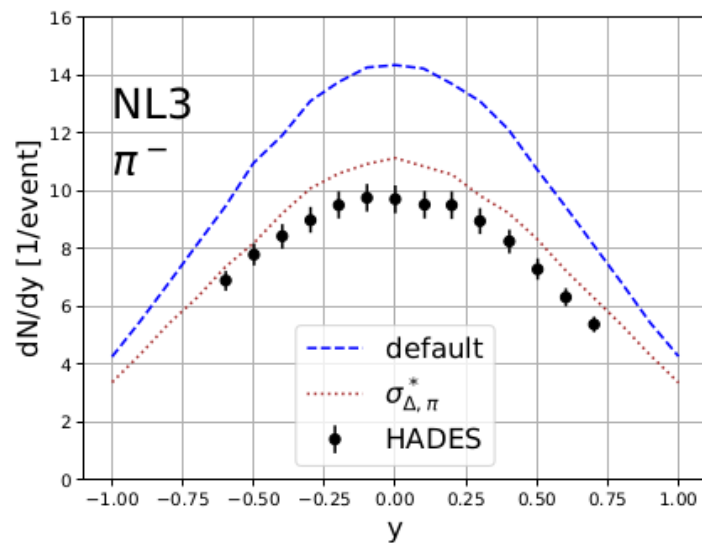
Sideflow

$$p_{xdir}^0 = \frac{p_{xdir}}{u_{1cm}}$$

$$p_{xdir} = \frac{\sum \text{sign}(y) Z u_x}{\sum Z}$$



# Pion rapidity spectra



$$\mathcal{L} = \bar{\psi} \left[ \gamma_{\mu} (i\partial^{\mu} - g_{\omega}\omega^{\mu} - g_{\rho}\boldsymbol{\tau}\boldsymbol{\rho}^{\mu} - \frac{e}{2}(1 + \tau^3)A^{\mu}) - m_N - g_{\sigma}\sigma \right] \psi$$

$$+ \frac{1}{2}\partial_{\mu}\sigma\partial^{\mu}\sigma - U(\sigma) + \frac{1}{2}m_{\omega}^2\omega^2 + \frac{1}{2}m_{\rho}^2\boldsymbol{\rho}^2 - \frac{1}{16\pi}F_{\mu\nu}F^{\mu\nu}$$

$$\left[ \gamma_{\mu} \left( i\partial^{\mu} - g_{\omega}\omega^{\mu} - g_{\rho}\boldsymbol{\tau}\boldsymbol{\rho}^{\mu} - \frac{e}{2}(1 + \tau^3)A^{\mu} \right) - m_N - g_{\sigma}\sigma \right] \psi = 0$$

$$V^{\nu} = g_{\omega}\omega^{\nu} + g_{\rho}\tau^3\rho^{3,\nu} + \frac{e}{2}(1 + \tau^3)A^{\nu}$$

$$S = g_{\sigma}\sigma .$$

$$f = \exp \left( - \alpha \left( \frac{\rho}{\rho_0} \right)^\beta \right)$$

$$\begin{aligned} d\sigma_{12 \rightarrow 1'2' \dots N'}^* &= (2\pi)^4 \delta^{(4)} \left( p_1 + p_2 - \sum_{i=1'}^{N'} p_i \right) \frac{n_1^* n_2^* \prod_{i=1'}^{N'} n_i^*}{4I_{12}^*} |\mathfrak{M}_{12 \rightarrow 1'2' \dots N'}|^2 \\ &\times \mathcal{S}_{1'2' \dots N'} \prod_{i=1'}^{N'} A_i(p_i) \frac{d^4 p_i}{(2\pi)^3 2p_i^{*0}} , \end{aligned}$$