

ESSNUSB AND THE PRECISE MEASUREMENT OF LEPTONIC CP VIOLATION AT THE SECOND NEUTRINO OSCILLATION MAXIMUM

ALESSIO GIARNETTI, ON BEHALF OF THE ESSNUSB+ PROJECT



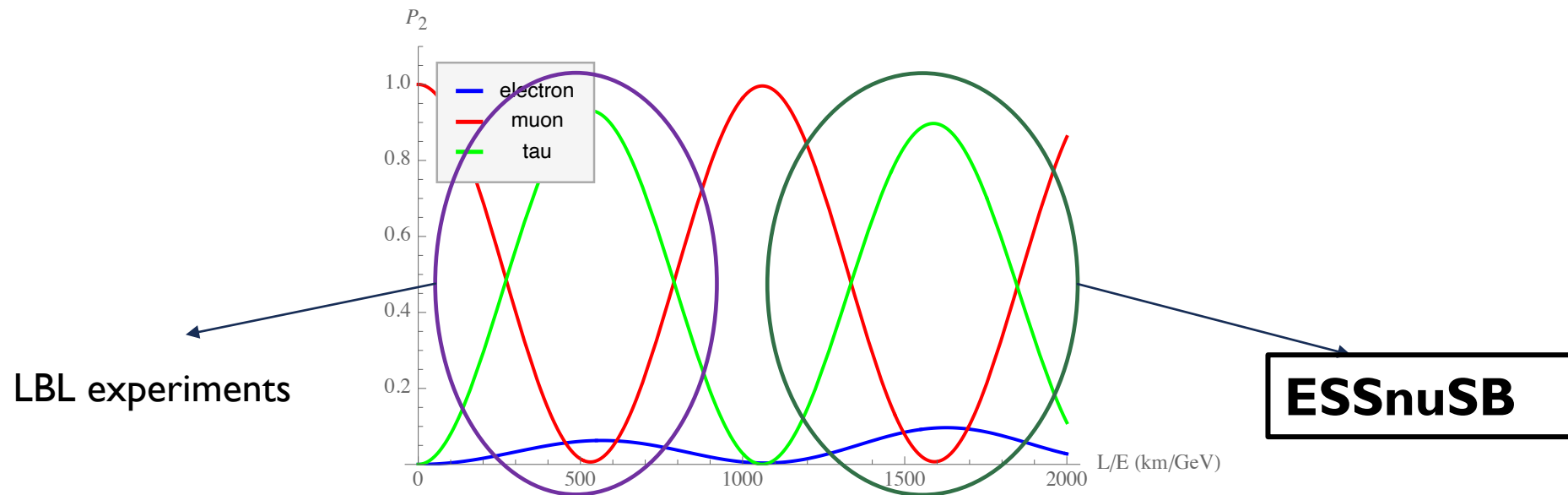
Co-funded by
the European Union

FPCP, BANGKOK, 30/05/2024



ESSnuSB: NEUTRINO OSCILLATION AT SECOND MAXIMUM

ESSnuSB is a design study for a next-to-next generation neutrino oscillation experiment which aims at the precise measurement of the CP violation in the leptonic sector looking at neutrino oscillation at the second atmospheric oscillation maximum.

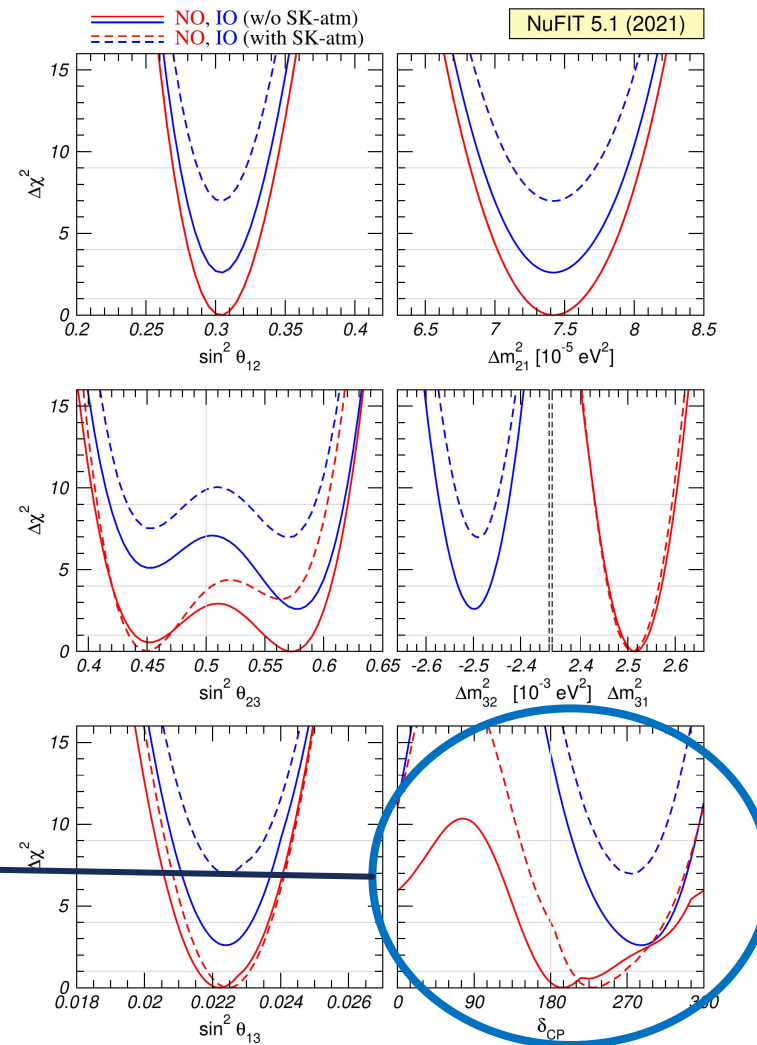


OSCILLATION PHYSICS AT THE SECOND MAXIMUM

In the precision era for the oscillation parameters measurements, we still do not know the amount of CP violation in the leptonic sector.

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{\text{CP}}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{\text{CP}}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{\text{CP}}} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta_{\text{CP}}} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta_{\text{CP}}} & c_{23}c_{13} \end{pmatrix}$$

Most of the possible values for the mixing matrix phase are allowed by current measurements, especially in Normal Ordering



OSCILLATION PHYSICS AT THE SECOND MAXIMUM

How to measure the phase?

$$\bar{J} \equiv \cos\theta_{13} \sin 2\theta_{12} \sin 2\theta_{23} \sin 2\theta_{13}$$

Electron neutrino appearance

$$P(\nu_\mu \rightarrow \nu_e) = \underbrace{\sin^2\theta_{23} \sin^2 2\theta_{13} \sin^2\left(\frac{\Delta m_{31}^2 L}{4E}\right)}_{\text{Atmospheric oscillations, leading term}} + \underbrace{\cos^2\theta_{23} \sin^2 2\theta_{12} \sin^2\left(\frac{\Delta m_{21}^2 L}{4E}\right)}_{\text{Solar subleading term}} + \underbrace{\bar{J} \cos(\delta_{\text{CP}} - \frac{\Delta m_{31}^2 L}{4E}) \sin\left(\frac{\Delta m_{21}^2 L}{4E}\right) \sin\left(\frac{\Delta m_{31}^2 L}{4E}\right)}_{\text{Interference term, depends on the phase!}}$$

CP VIOLATION



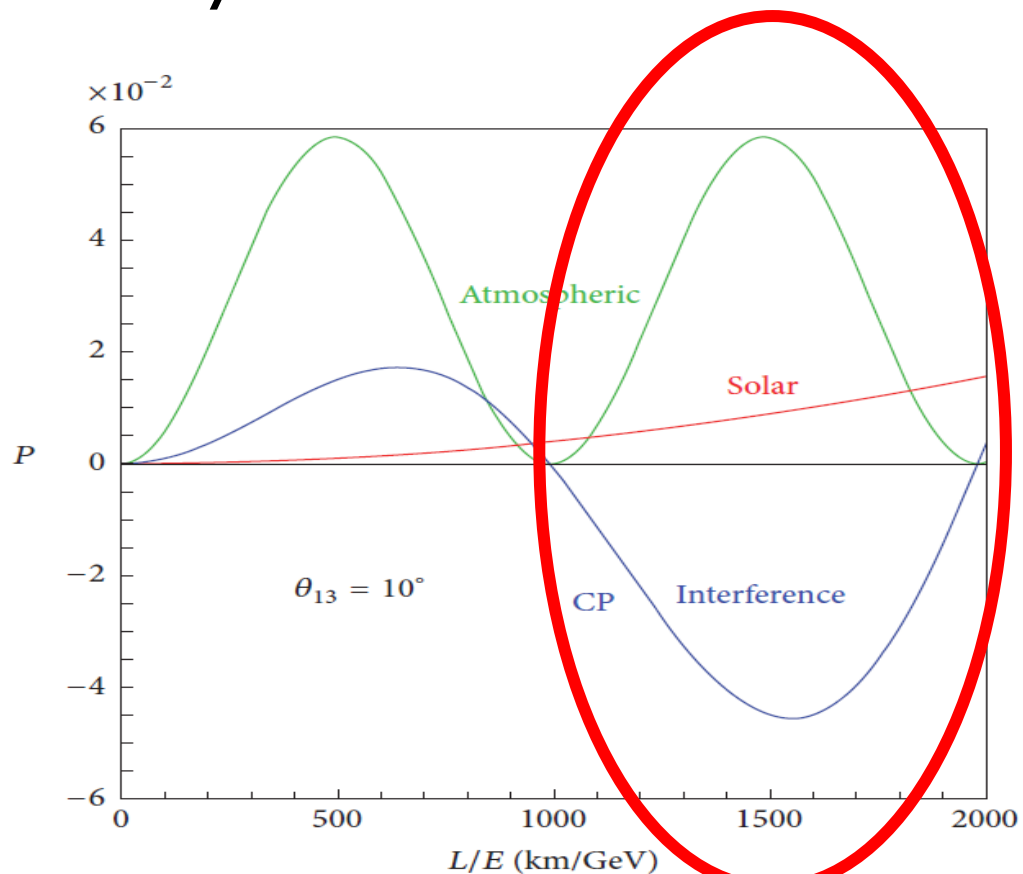
$$P_{\nu_\mu \rightarrow \nu_e} \neq P_{\bar{\nu}_\mu \rightarrow \bar{\nu}_e} \quad (\delta \rightarrow -\delta)$$

We want to look at both electron neutrino and antineutrino appearance starting with two different fluxes:

Muon neutrinos and Muon antineutrinos

OSCILLATION PHYSICS AT THE SECOND MAXIMUM

Why 2nd maximum?



At the second oscillation maximum the interference term is large!

$$\mathcal{A}_{\text{CP}}^{\alpha \rightarrow \beta} = P_{\nu_{\alpha} \rightarrow \nu_{\beta}} - P_{\bar{\nu}_{\alpha} \rightarrow \bar{\nu}_{\beta}}$$

$$\frac{\mathcal{A}_{\text{CP}}^{\mu \rightarrow e} \left(x_{\text{max}}^{(2)} \right)}{\mathcal{A}_{\text{CP}}^{\mu \rightarrow e} \left(x_{\text{max}}^{(1)} \right)} \approx 2.7$$

OSCILLATION PHYSICS AT THE SECOND MAXIMUM

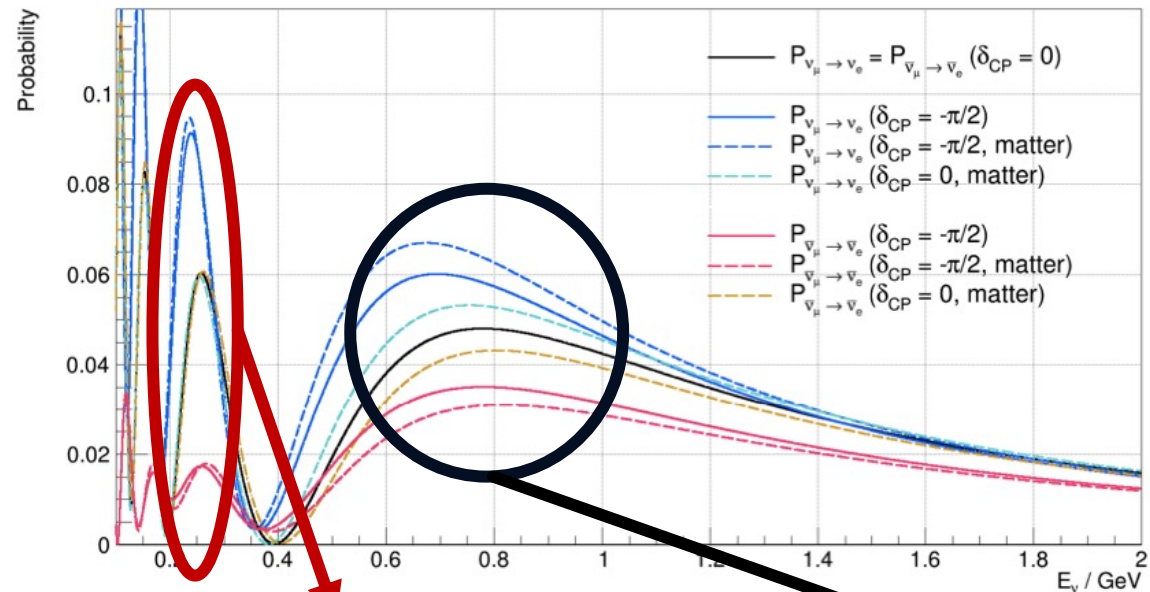
What about matter effects?

$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \left[\frac{1}{2E_\nu} U \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix} U^\dagger + A_{CC} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$$

Change sign for antineutrinos,
like the CP-violating phase

FAKE CP VIOLATION

(L = 360 km)



Second maximum, the
matter effects are not
important,
pure phase determination

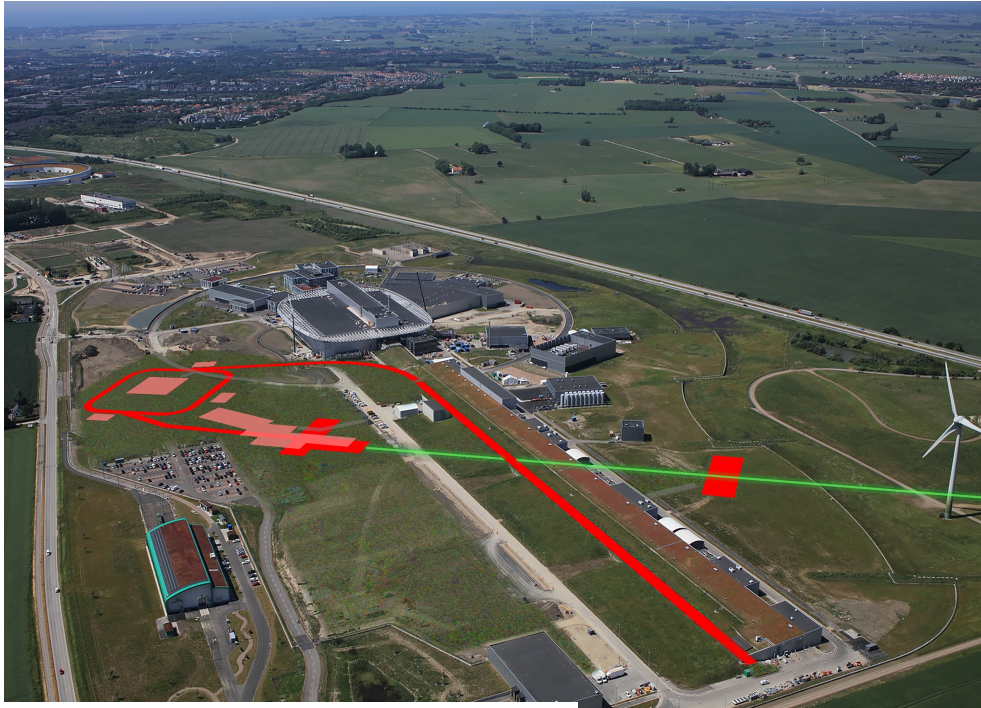
First maximum, matter and
CP phase have the same effect



THE ESSNUSB PROJECT (2017-2022)



ESS PROTON ACCELERATOR



- The ESS will be a copious source of spallation neutrons.

- 5 MW average beam power.**

- 14 Hz repetition rate (2.86 ms pulse duration, 10^{15} protons).

- Duty cycle 4%.

- 2.0 GeV kinetic energy protons

- up to 3.5 GeV with linac upgrades

- > 2.7×10^{23} p.o.t./year.

From such a powerful accelerator, we can produce an intense neutrino beam!



The European Spallation Source neutrino Super Beam (ESSvSB)



EUROPEAN SPALLATION SOURCE

First beam on target expected in 2026.

Under construction in Lund, Sweden

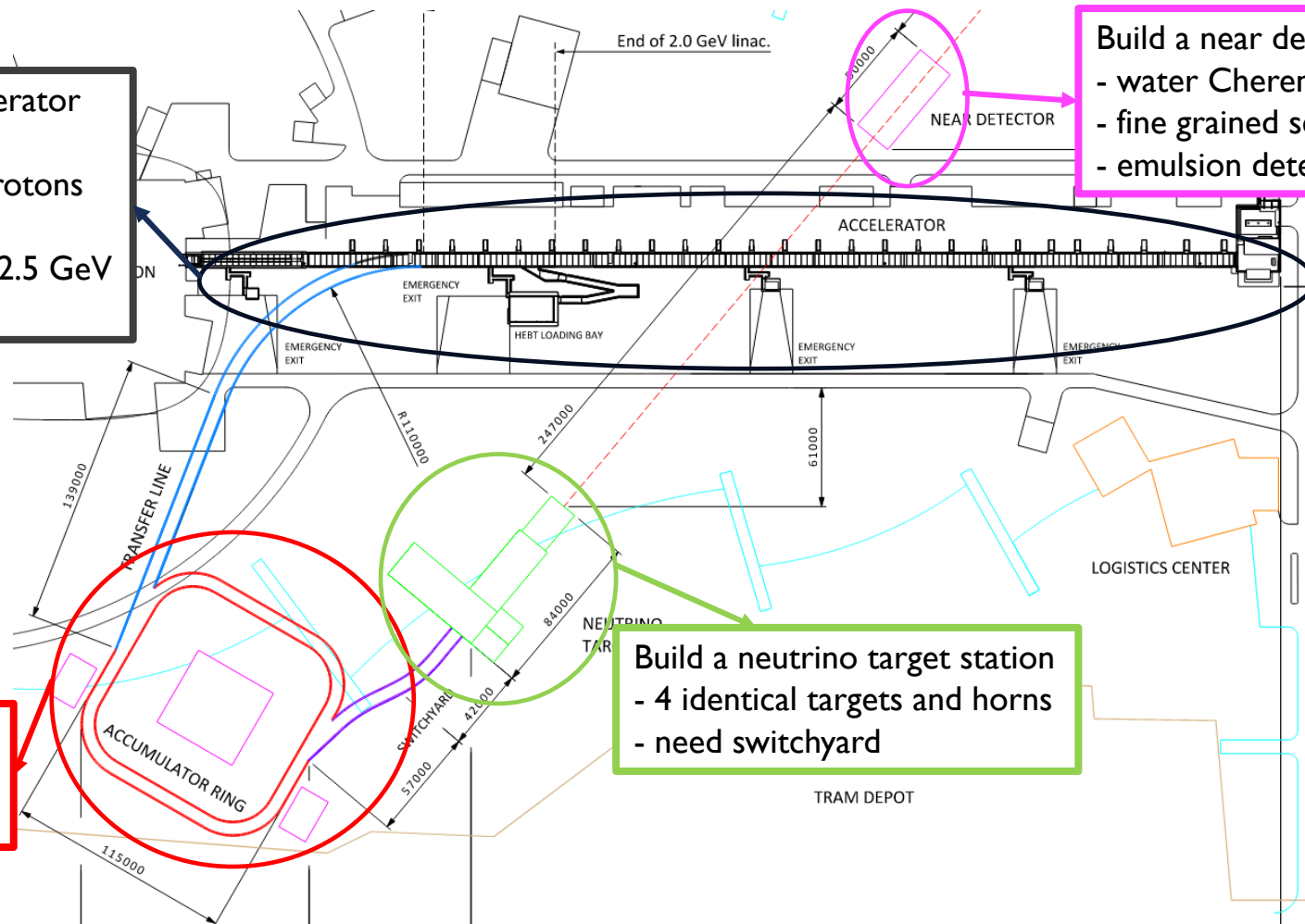
UPGRADE OF THE ESS SITE

Upgrade of the accelerator
- 14 Hz to 28 Hz
- use H^- instead of protons in ESSnuSB cycles
- increase energy to 2.5 GeV kinetic

Build a near detector site
- water Cherenkov detector
- fine grained scintillator
- emulsion detector

Build an accumulator ring
- shorten ESS pulses from 2.86 ms to $\approx 1 \mu s$

Build a neutrino target station
- 4 identical targets and horns
- need switchyard



NEUTRINO PRODUCTION: TARGET STATION

Hot Cell

- Able to manipulate/repair hadronic collector
- Work under Radioactive Environment



Decay tunnel

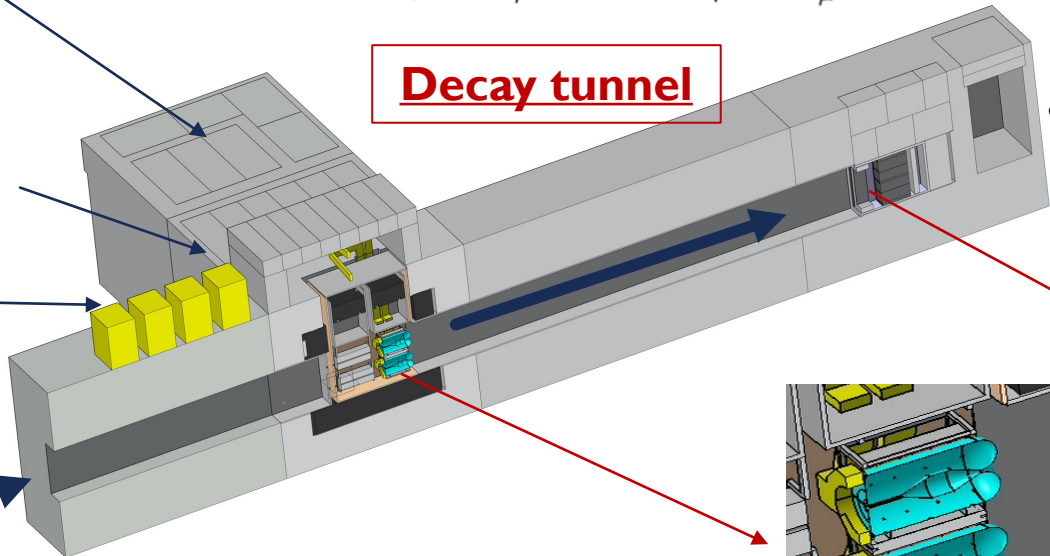
Neutrino beam

Power Supply Unit

- 16 modules (350 kA, 1.3 μ s)
- Located above the switchyard
- Outside of radioactive part of Facility

Morgue

To Store radioactive wastes



Proton Beam
($E_p=2.5$ GeV, 14 Hz)
4 x 1.25 MW

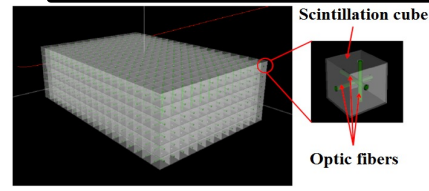
Beam dump

Hadronic Collector: Target + Horns

NEAR DETECTOR SITE

NINJA-like water-emulsion detector (1 t fiducial) ν IKING

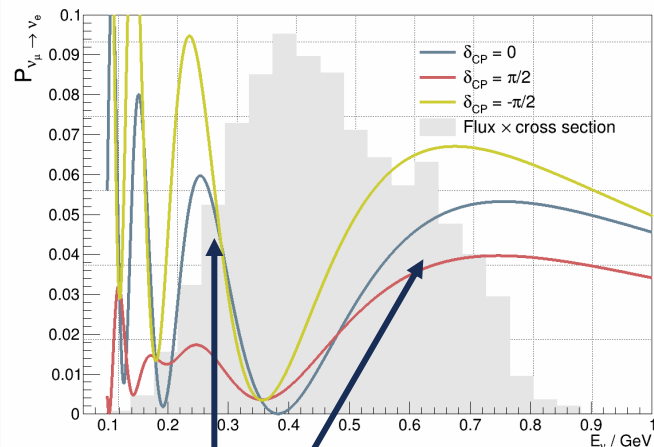
Super-FGD like detector (1 t fiducial)



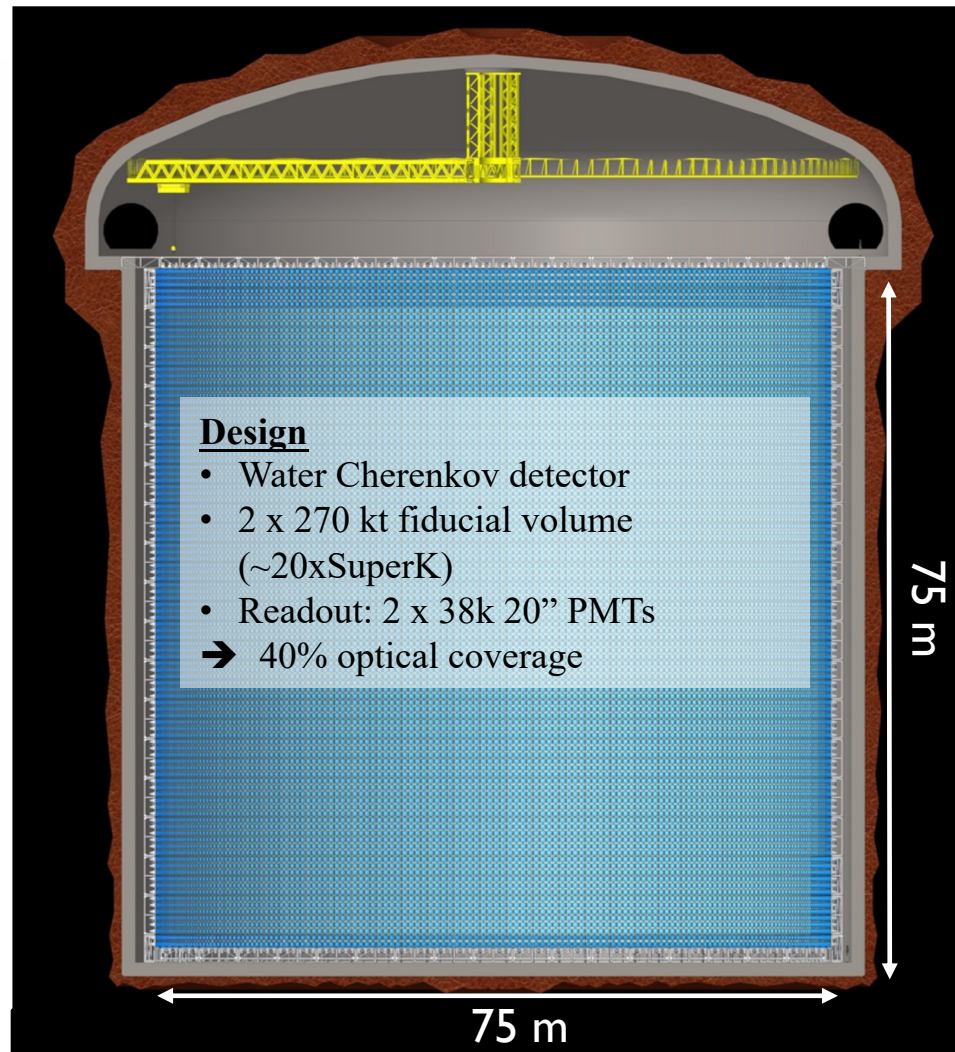
Near Water Cherenkov detector (0.77 kt fiducial)

- ν IKING: precise measurement of the final state topology of the neutrino–water interactions
- Super-FGD: magnetized, charge discrimination and neutrino energy reconstruction for the ND detectors
- WC detector: flux determination

THE FAR DETECTOR



*First and second
oscillation maxima
covered at 365 km
baseline!*



THE EVENT SPECTRA AT 360 KM

Table 29 Number of expected neutrino interactions in the detector per running year, per flavour and interaction type, and per each horn polarity

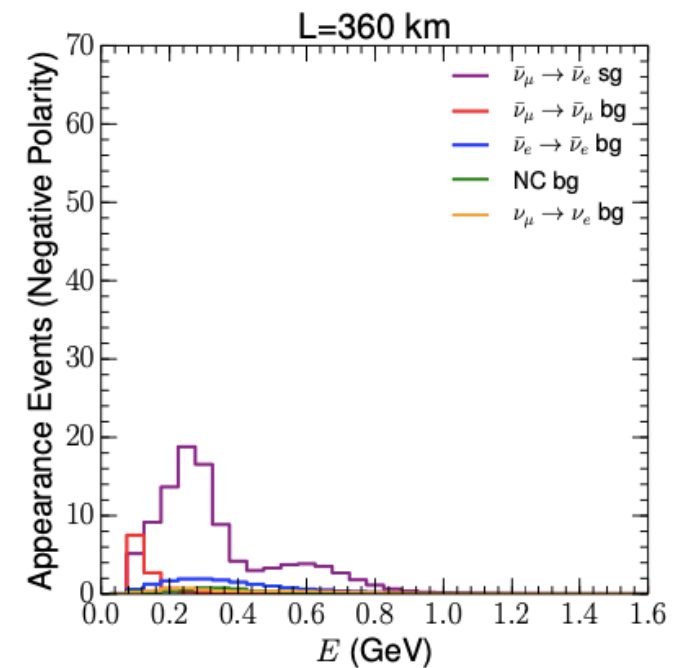
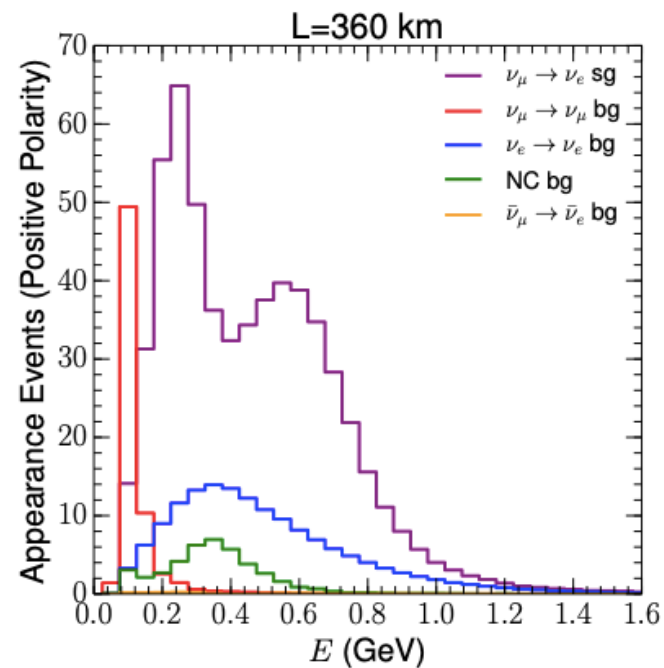
All interactions								
	ν_μ CC	ν_e CC	$\bar{\nu}_\mu$ CC	$\bar{\nu}_e$ CC	ν_μ NC	ν_e NC	$\bar{\nu}_\mu$ NC	$\bar{\nu}_e$ NC
Positive polarity	5.20×10^7	1.07×10^6	9.25×10^4	1.11×10^3	4.42×10^7	6.11×10^5	3.36×10^5	8.72×10^2
Negative polarity	1.06×10^6	8.90×10^3	9.74×10^6	1.89×10^5	8.81×10^5	1.11×10^4	9.65×10^6	1.36×10^5

Initial flux



- Almost pure ν_μ beam
- Small ν_e contamination \rightarrow ν_e cross-sections at the ND

At FD w oscillation





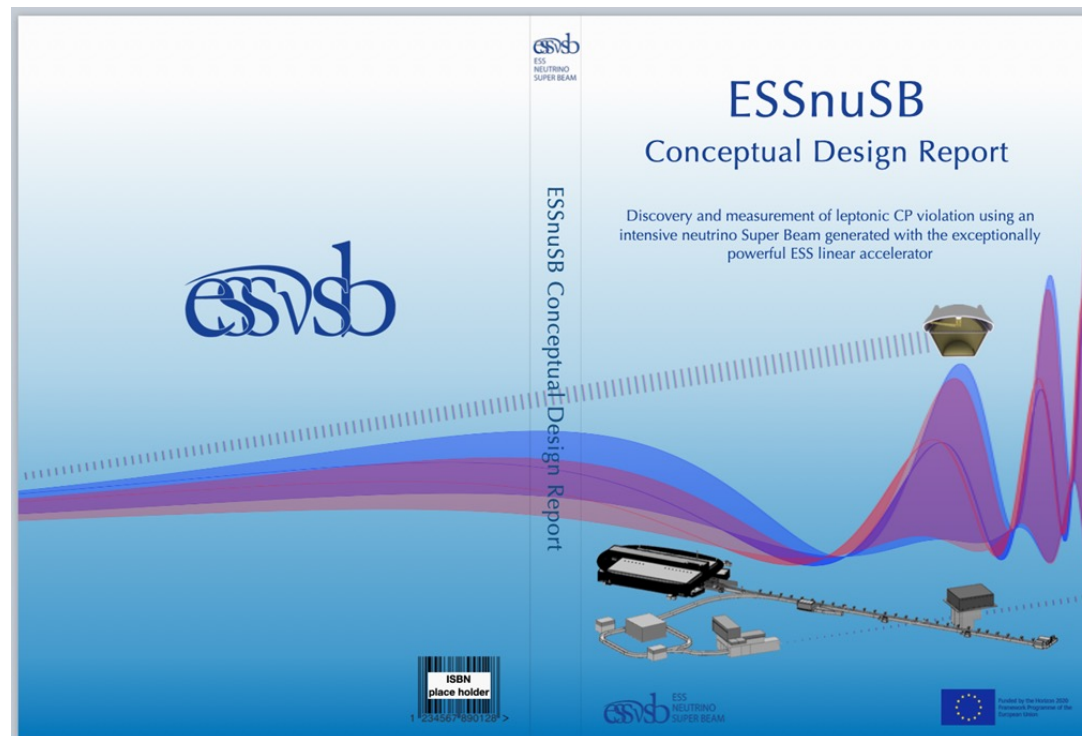
THE PHYSICS AT ESSNUSB



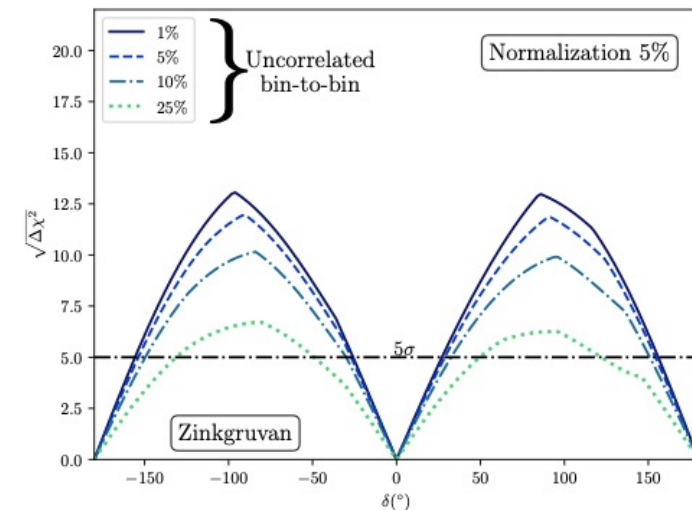
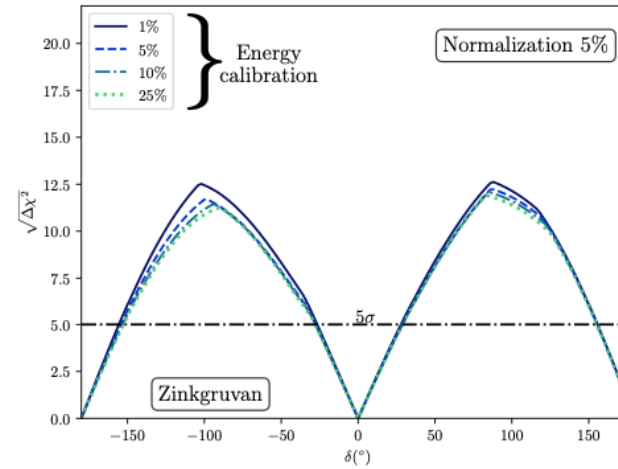
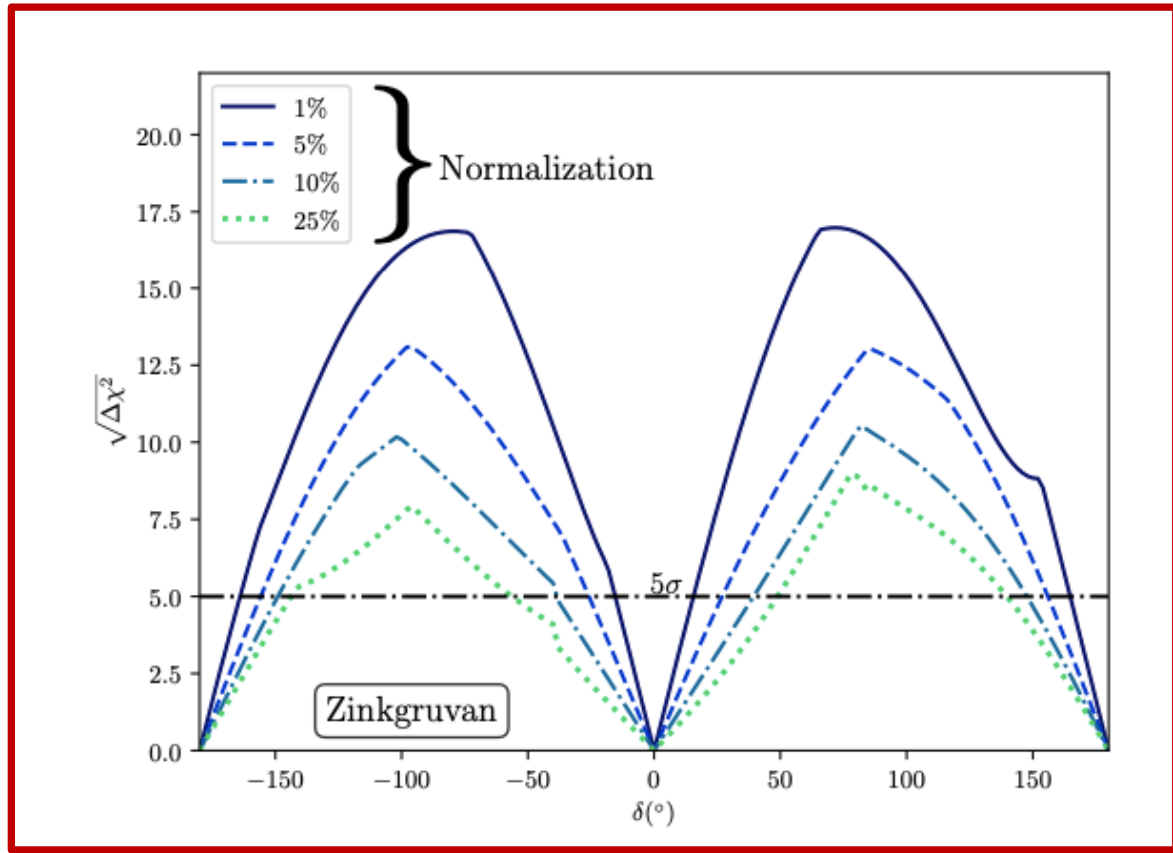
THE CDR (2022)

Conceptual Design Report

[Eur. Phys. J. ST. 231 \(21\), \(2022\) 3779](#)

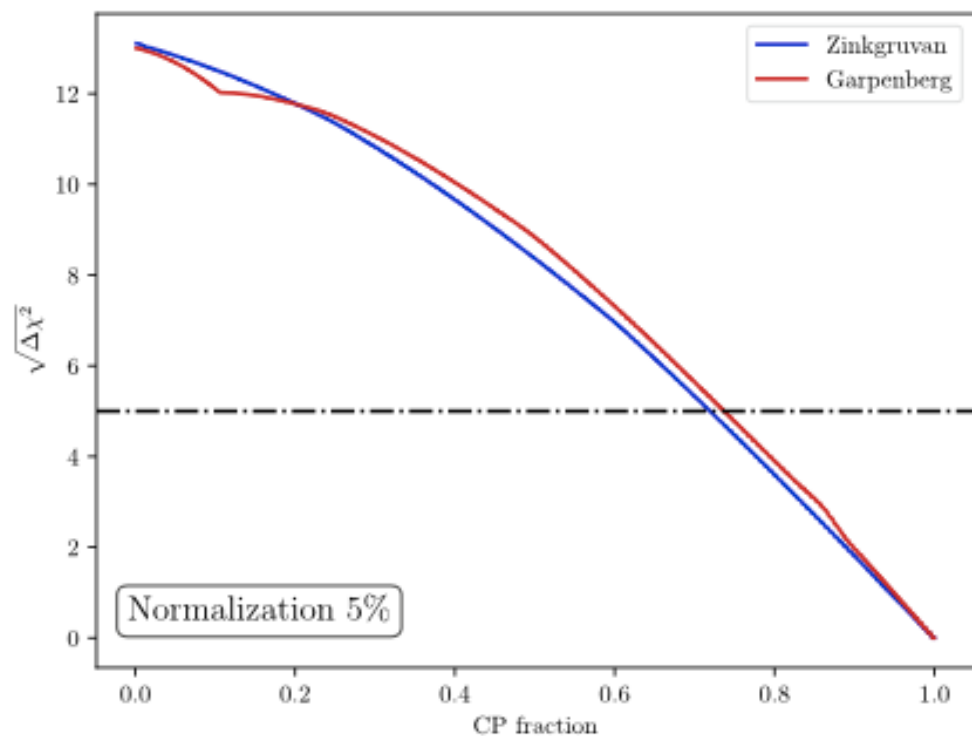


CP VIOLATION SENSITIVITY: EFFECT OF SYSTEMATICS

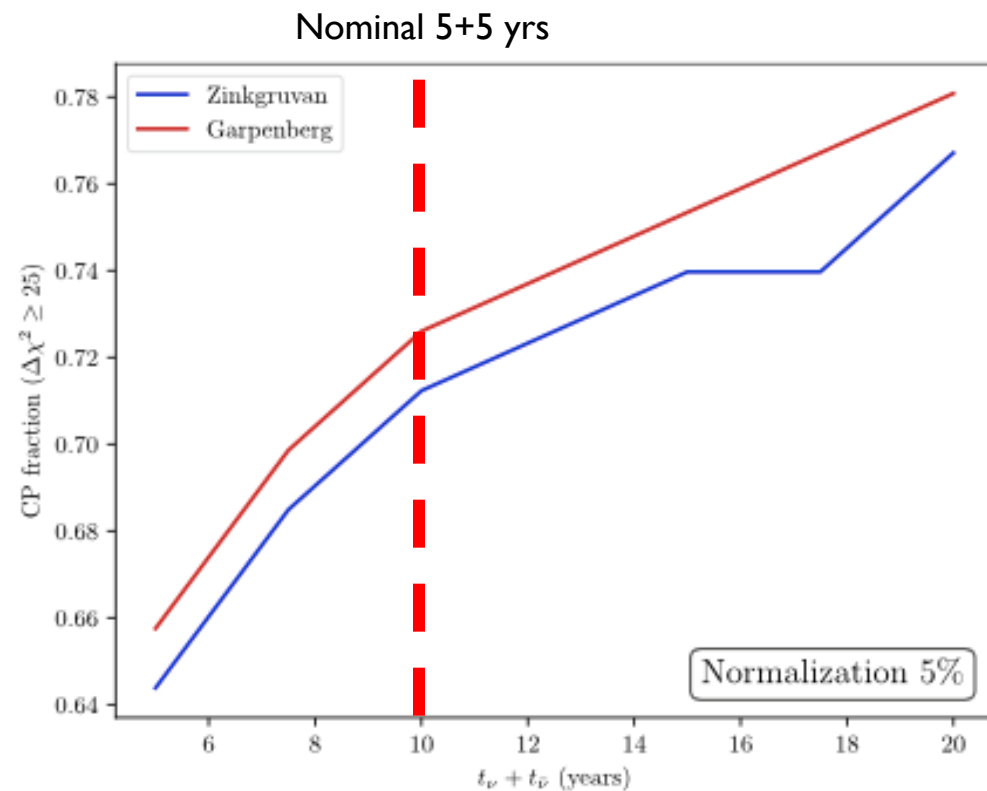


With 5% systematic uncertainty, up to 12.5 σ for maximum CPV!

CP VIOLATION COVERAGE

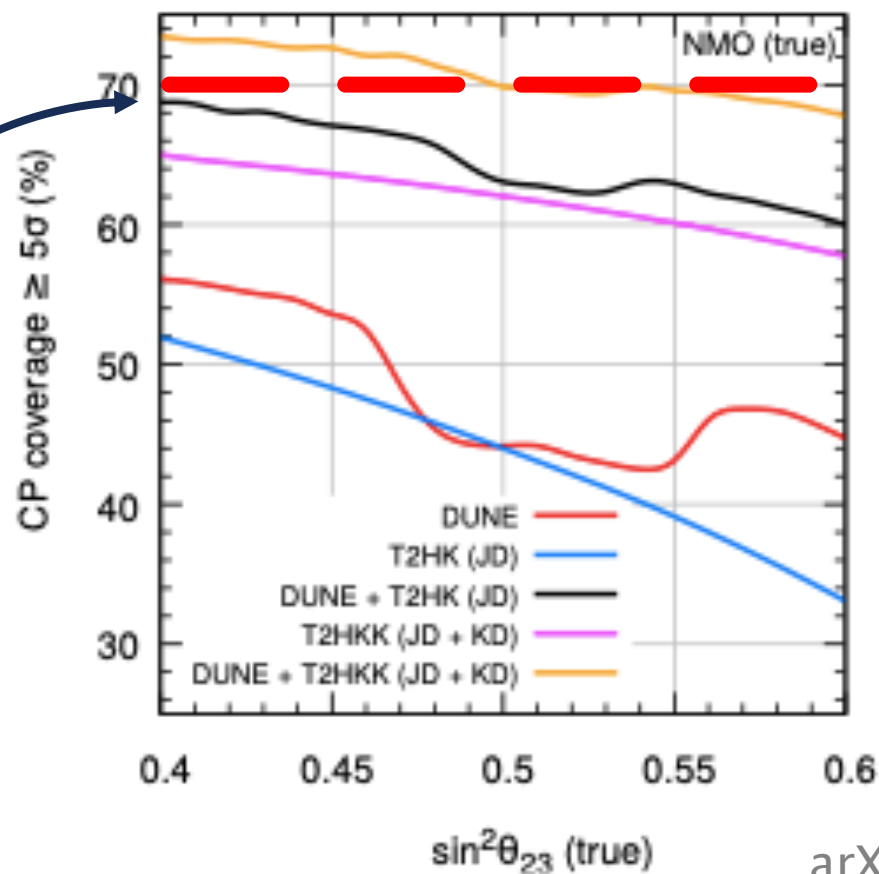
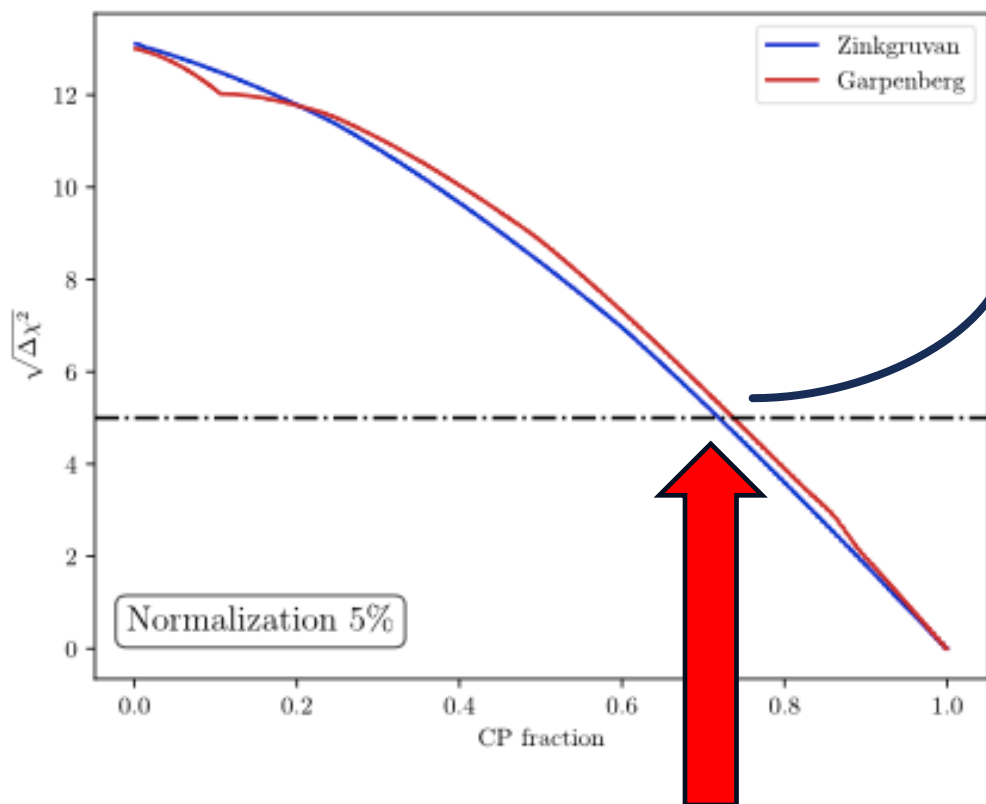


70% CP coverage at 5σ



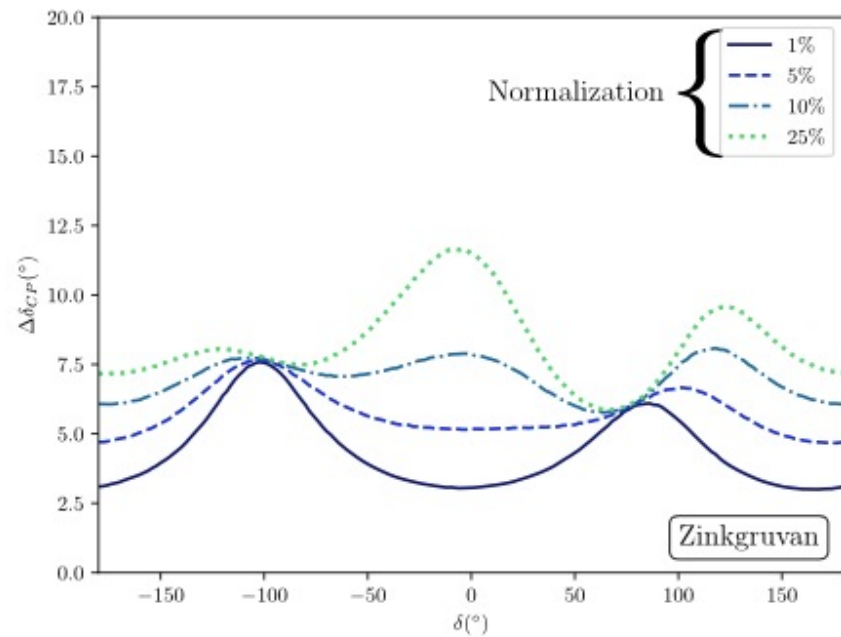
Results gets better with more running time

COMPARISON WITH NEXT-GEN LBL

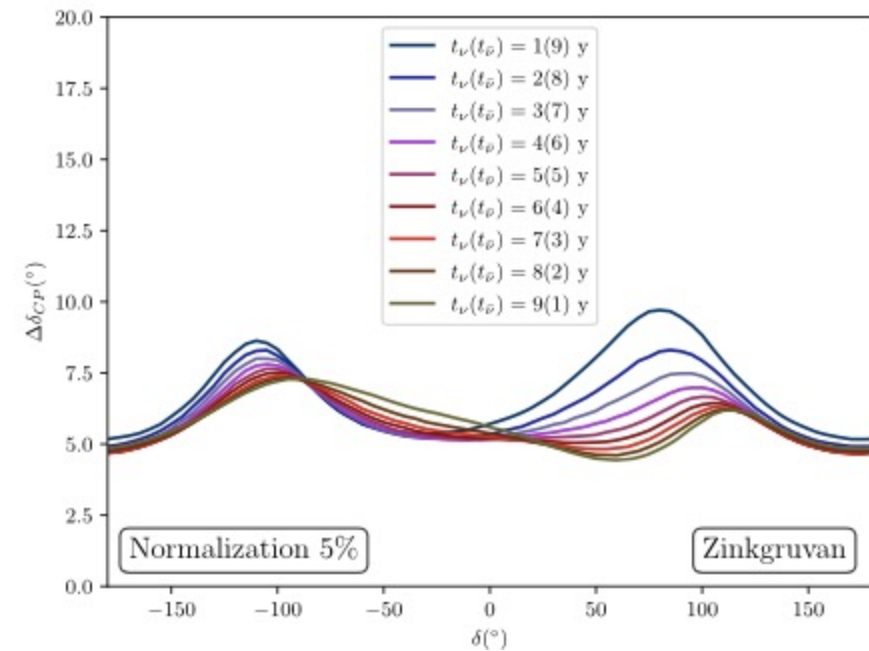


The same coverage might be reached only by DUNE+T2HKK (also, next-to-next gen proposed upgrade of T2HK) for LO values of θ_{23}

UNCERTAINTY ON CP VIOLATING PHASE

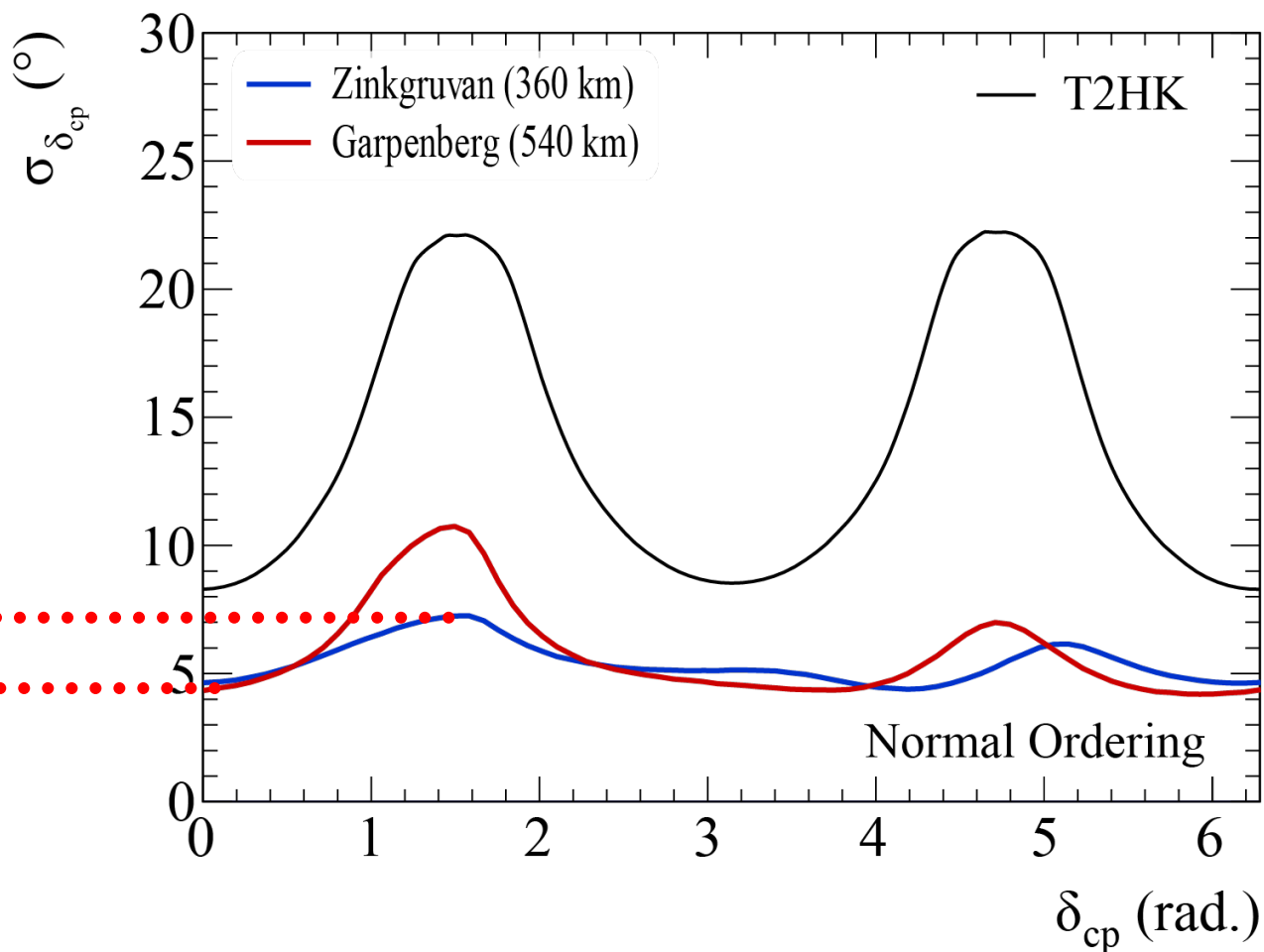
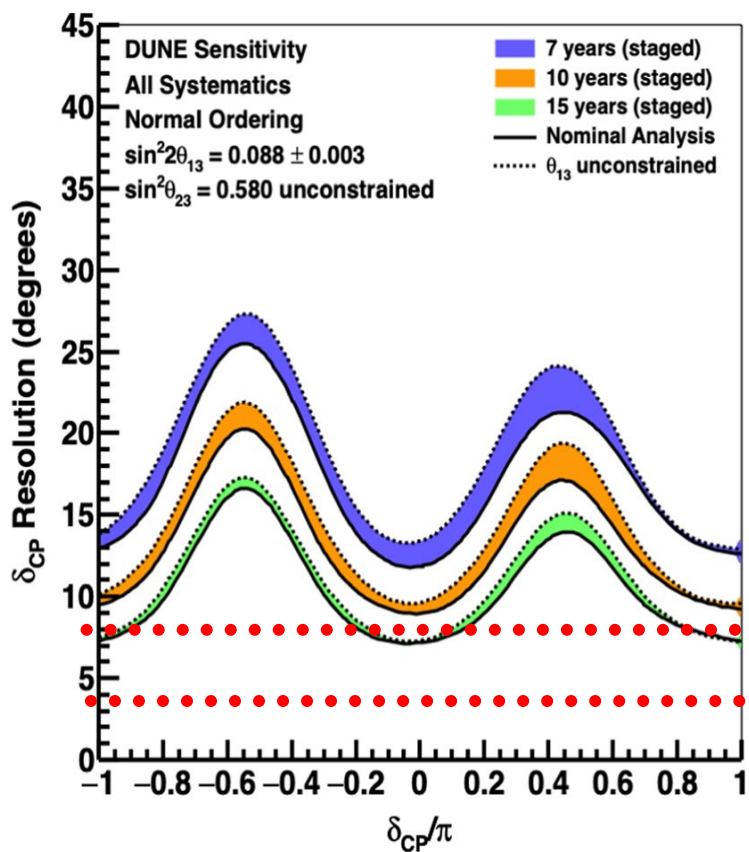


CP precision always under 7.5° for 5% sys



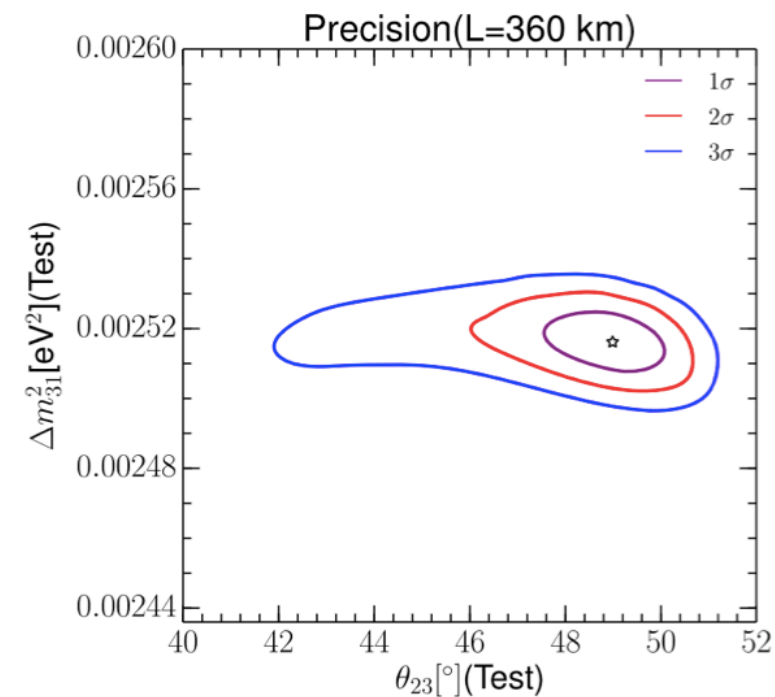
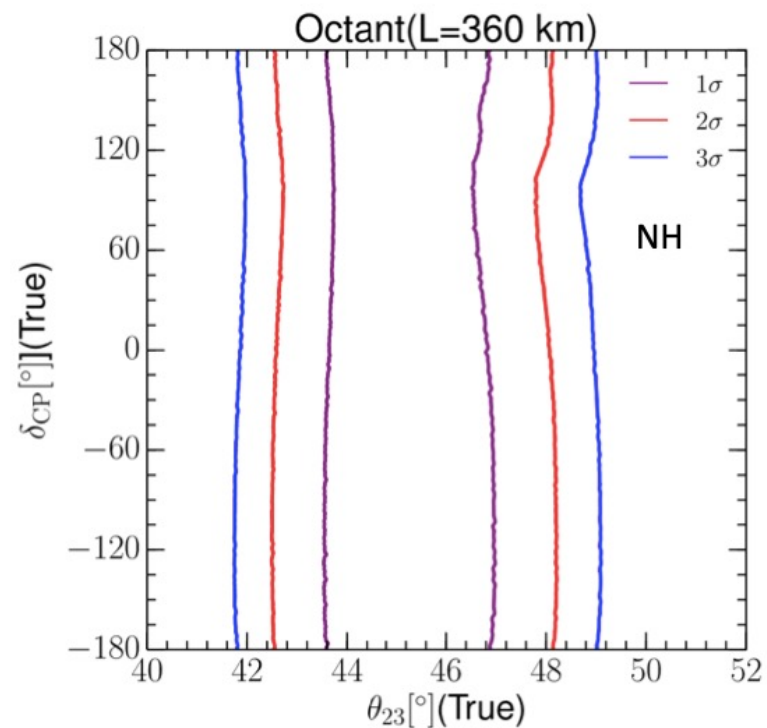
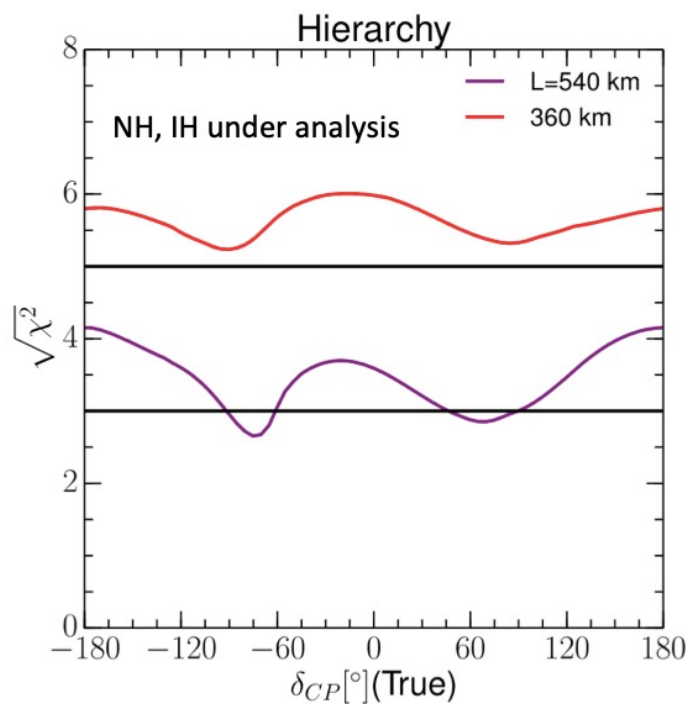
Precision optimized in a balanced run (5+5 yrs)

COMPARISON WITH NEXT-GEN LBL



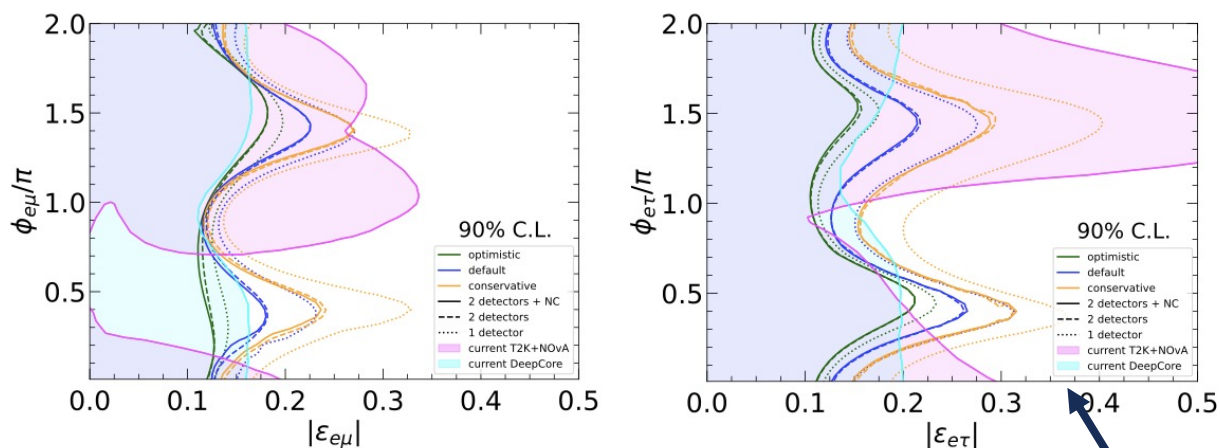
Great improvement with respect to DUNE and T2HK!!

OSCILLATION BEYOND CPV

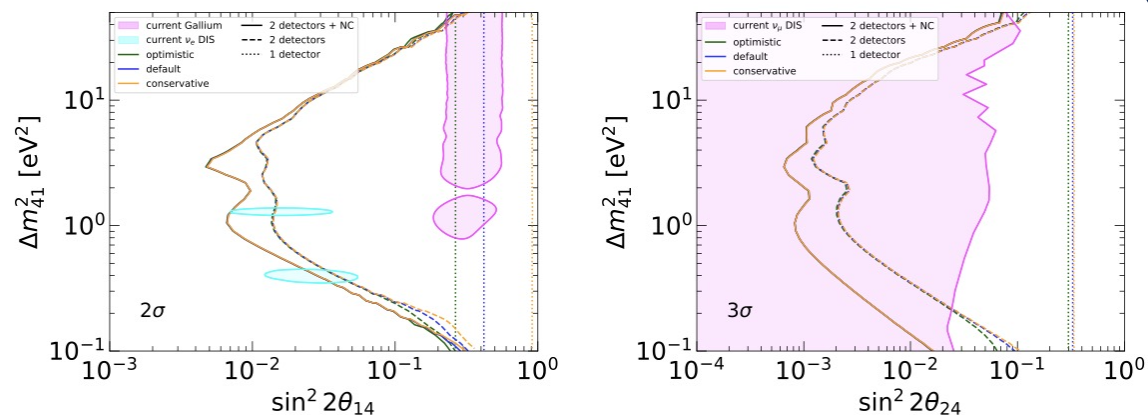


WHAT ABOUT BSM?

Non-Standard Interactions

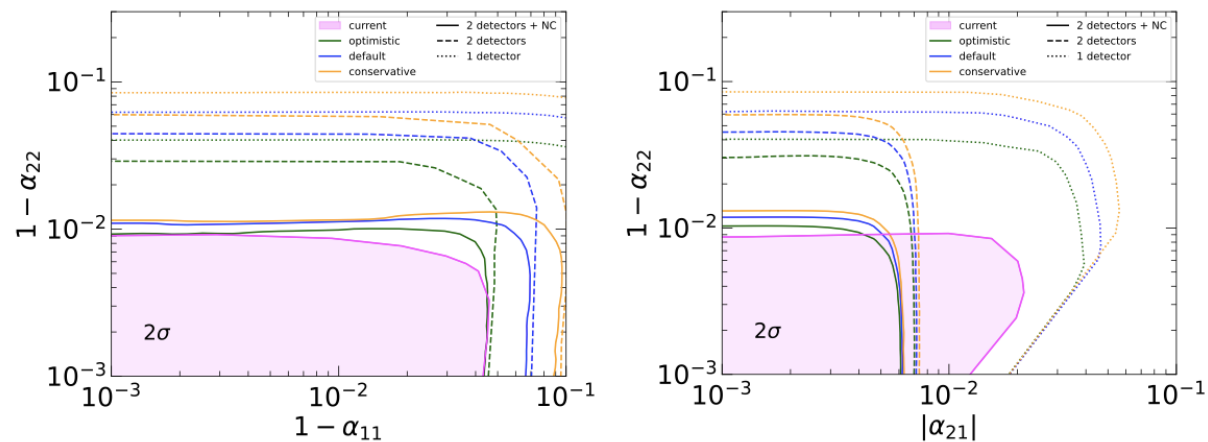


Steriles



[https://doi.org/10.1007/JHEP04\(2023\)130](https://doi.org/10.1007/JHEP04(2023)130)

Non-Unitarity of PMNS matrix



Possible new
sources of CPV:
Great sensitivity!

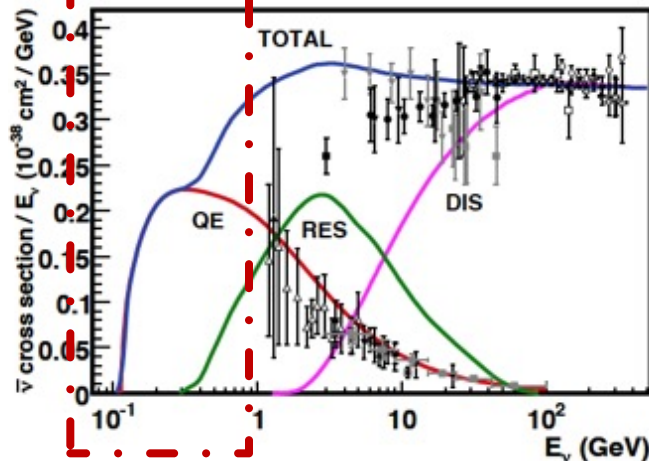
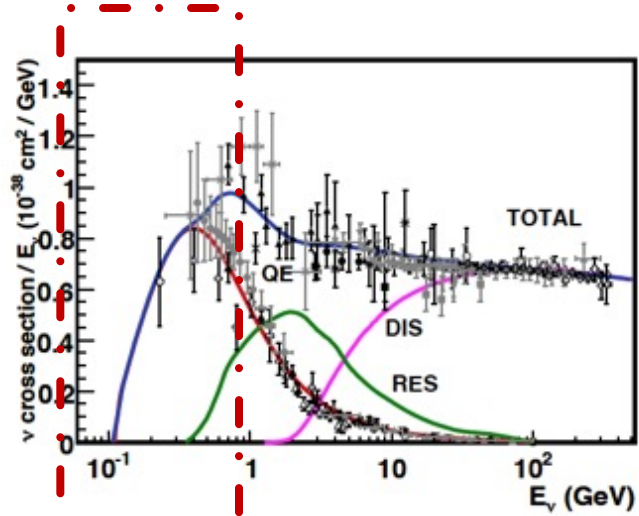
See also: -[https://doi.org/10.1007/JHEP03\(2020\)026](https://doi.org/10.1007/JHEP03(2020)026)
 -[https://doi.org/10.1007/JHEP05\(2021\)133](https://doi.org/10.1007/JHEP05(2021)133)
 -<https://doi.org/10.48550/arXiv.2305.16234>
 -<https://doi.org/10.1103/PhysRevD.106.075016>
 -<https://doi.org/10.1103/PhysRevD.107.075023>
 -



THE FUTURE: ESSNUSB+



THE LOW ENERGY NEUTRINO CROSS SECTION



Lack of neutrino cross section measurements in the low energy region fundamental for ESSnuSB!

Even though the effect of systematics for the CP violation measurement is much less in ESSnuSB is crucial to obtain new precise results in this direction


From eV to EeV: Neutrino cross sections across energy scales,
Rev. Mod. Phys. 84, 1307 –
Published 24 September 2012

POSSIBLE STUDIES FOR THE CROSS SECTION MEASUREMENTS

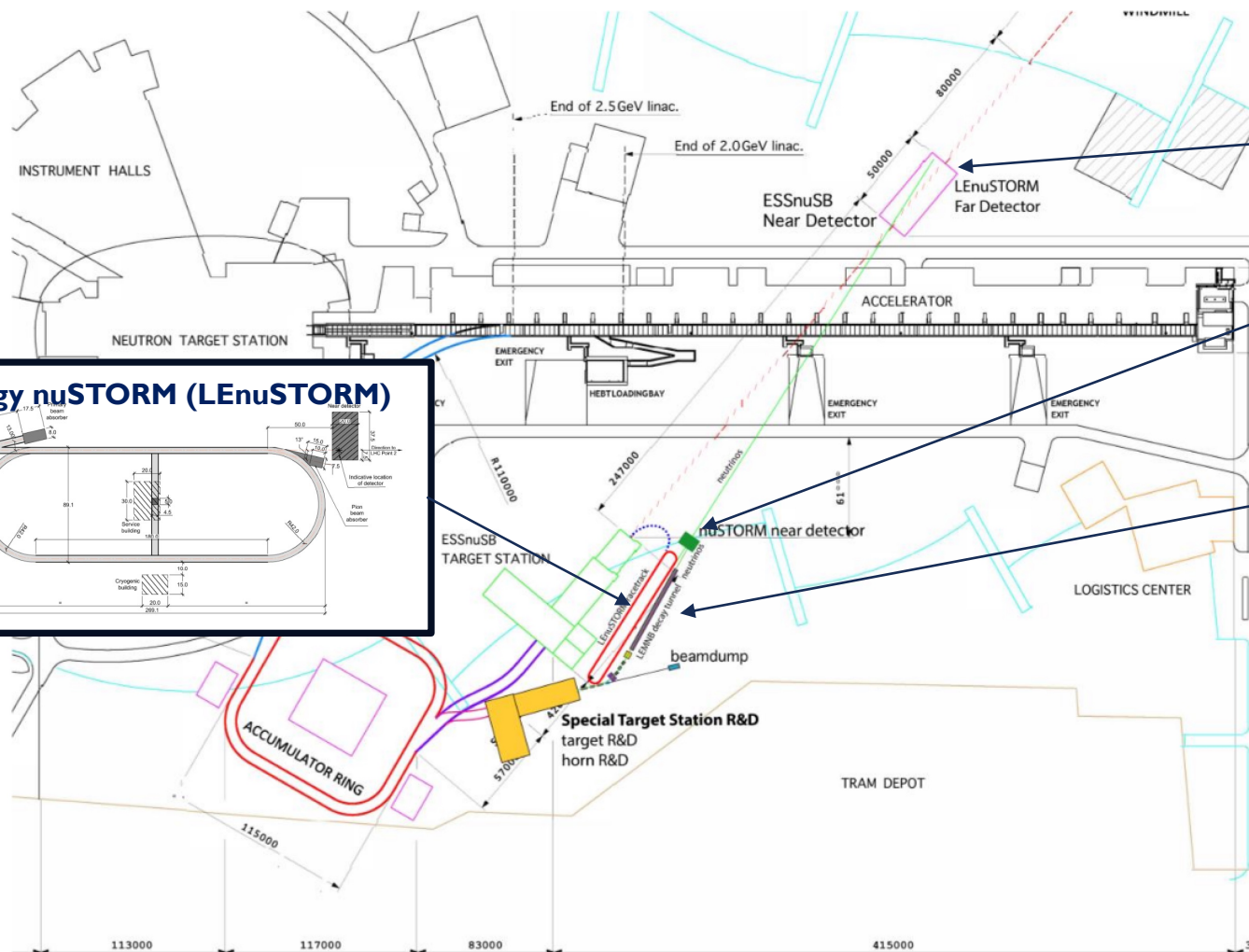
1. Design a **transfer line** from the ESSvSB accumulator ring to the target
2. Design a **special target facility** that depends on one horn-target system
3. Design a pion **extraction and deflection system**
4. Design an **injection scheme** for the extracted pions to the racetrack storage ring, where the pions will decay to muons
5. Design a **storage ring** for the low energy nuSTROM (for cross section measurements and sterile neutrino searches)
6. Design a **Monitored Neutrino Beam** (low energy ENUBET for cross section measurements)
7. **Optimize the performance** of the ESSvSB detectors



Cross-section measurements with:

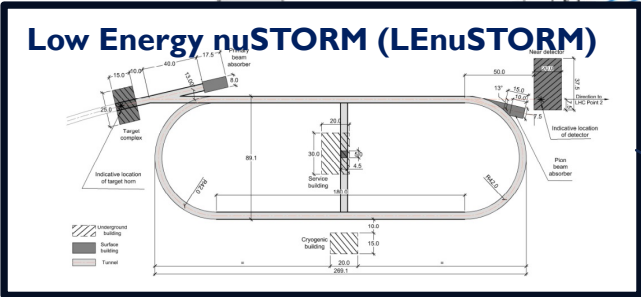
- Low Energy nuSTORM: $\pi \rightarrow \mu \rightarrow e + \nu_\mu + \nu_e$
 - Low Energy ENUBET: $\pi \rightarrow \mu + \nu_\mu$
- 

ESSNUSB+



Gd doping for WC detectors

New Near Detector



ESSNUSB+

Research and Innovation actions

Design Study

HORIZON-INFRA-2022-DEV-01



Title of Proposal:

Study of the use of the ESS facility to accurately measure the neutrino cross-sections for ESSvSB leptonic CP violation measurements and to perform sterile neutrino searches and astroparticle physics.

Acronym of Proposal: ESSvSB+



Marcos DRACOS
CENTRE NATIONAL DE LA RECHERCHE
SCIENTIFIQUE CNRS
RUE MICHEL ANGE 3
75794 PARIS
FRANCE

Subject: Horizon Europe (HORIZON)
Call: HORIZON-INFRA-2022-DEV-01
Project: 101094628 — ESSnuSBplus
GAP invitation letter

Dear Applicant,

I am writing in connection with your proposal for the above-mentioned call.

Having completed the evaluation, we are pleased to inform you that your proposal has passed this phase and that we would now like to start grant preparation.

Please find enclosed the evaluation summary report (ESR) for your proposal.

Invitation to grant preparation

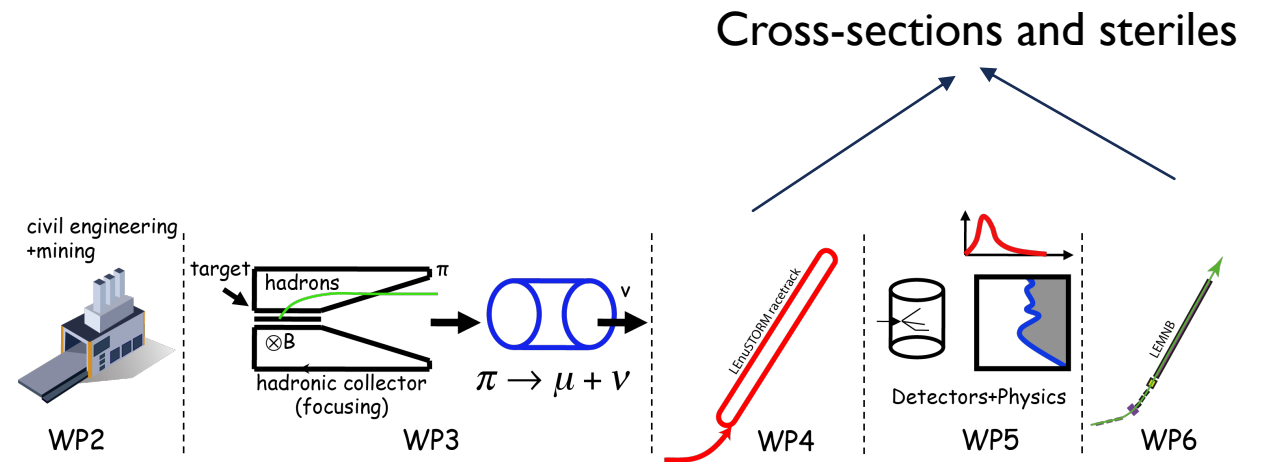
Approved! 26/07/2022

3 M €, 4 YEARS

ESSNUSB+

20 participant institutes

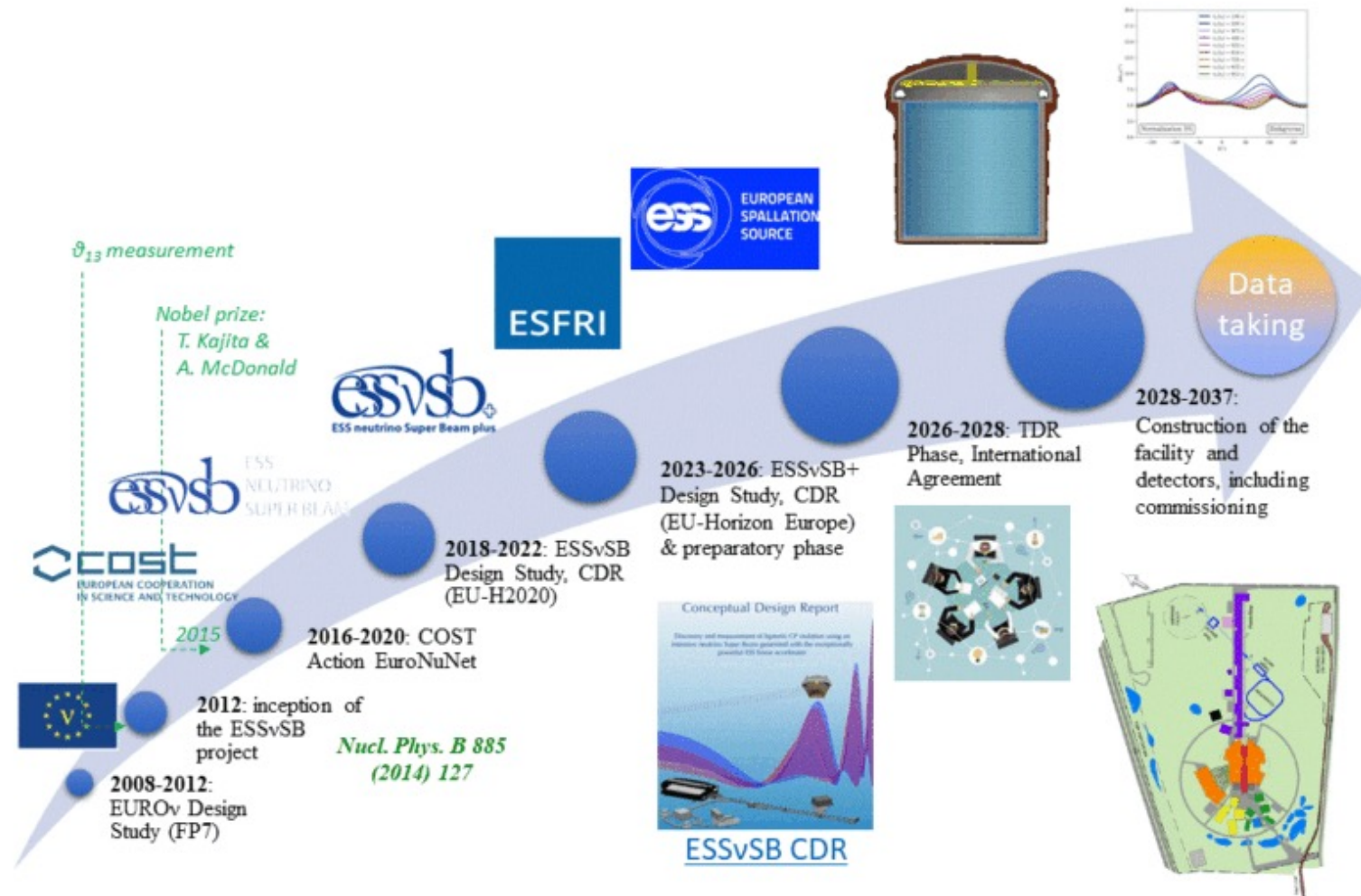
Participant no.	Participant organisation name	Part. short name	Country
1 (Coordinator)	Centre National de la Recherche Scientifique	CNRS	France
2	Université de Strasbourg	UNISTRA ¹	France
3	Rudjer Boskovic Institute	RBI	Croatia
4	Tokai National Higher Education and Research System, National University Corporation	NU ²	Japan
5	Uppsala Universitet	UU	Sweden
6	Lunds Universitet	ULUND	Sweden
7	European Spallation Source ERIC	ESS	Sweden
8	Kungliga Tekniska Hoegskolan	KTH	Sweden
9	Universitaet Hamburg	UHH	Germany
10	University of Cukurova	CU	Turkey
11	National Center for Scientific Research "Demokritos"	NCSR	Greece
12	Aristotelio Panepistimio Thessalonikis	AUTH ¹	Greece
13	Sofia University St. Kliment Ohridski	UniSofia	Bulgaria
14	Lulea Tekniska Universitet	LTU	Sweden
15	European Organisation for Nuclear Research	CERN	IEIO ³
16	Universita degli Studi Roma Tre	UNIROMA3	Italy
17	Universita degli Istudi di Milano-Bicocca	UNIMIB	Italy
18	Istituto Nazionale di Fisica Nucleare	INFN	Italy
19	Universita degli Istudi di Padova	UNIPD ¹	Italy
20	Consortio para la construccion, equipamiento y explotacion de la sede espanola de la fuente Europea de neutrones por espalacion	ESSB	Spain



Non Beam physics:

- Atmospheric
- Supernovae
- ...

TIMELINE



CONCLUSIONS

- ESSnuSB is a next-to-next generation neutrino oscillation experiment which aims to precisely measure CP violation looking at neutrino oscillations at the 2nd oscillation maximum
- This baseline choice allows to have a measurement less affected by systematic errors and matter effects
- We predict that in 10 years of data taking ESSnuSB will be able to reach a 70% coverage for the CP violating phase and a precision of less than 8°
- The accelerator complex will be based at the ESS linac, the most powerful proton accelerator in the world
- The large far detectors can also be used for rich astroparticle physics programme
- The ESSnuSB Design Study has been supported by EU-Horizon 2020 during the period 2018-2022 and the ESSnuSB+ Project which started this year has further enriched the great physics program of the experiment



Co-funded by the European Union





THANK YOU FOR YOUR ATTENTION



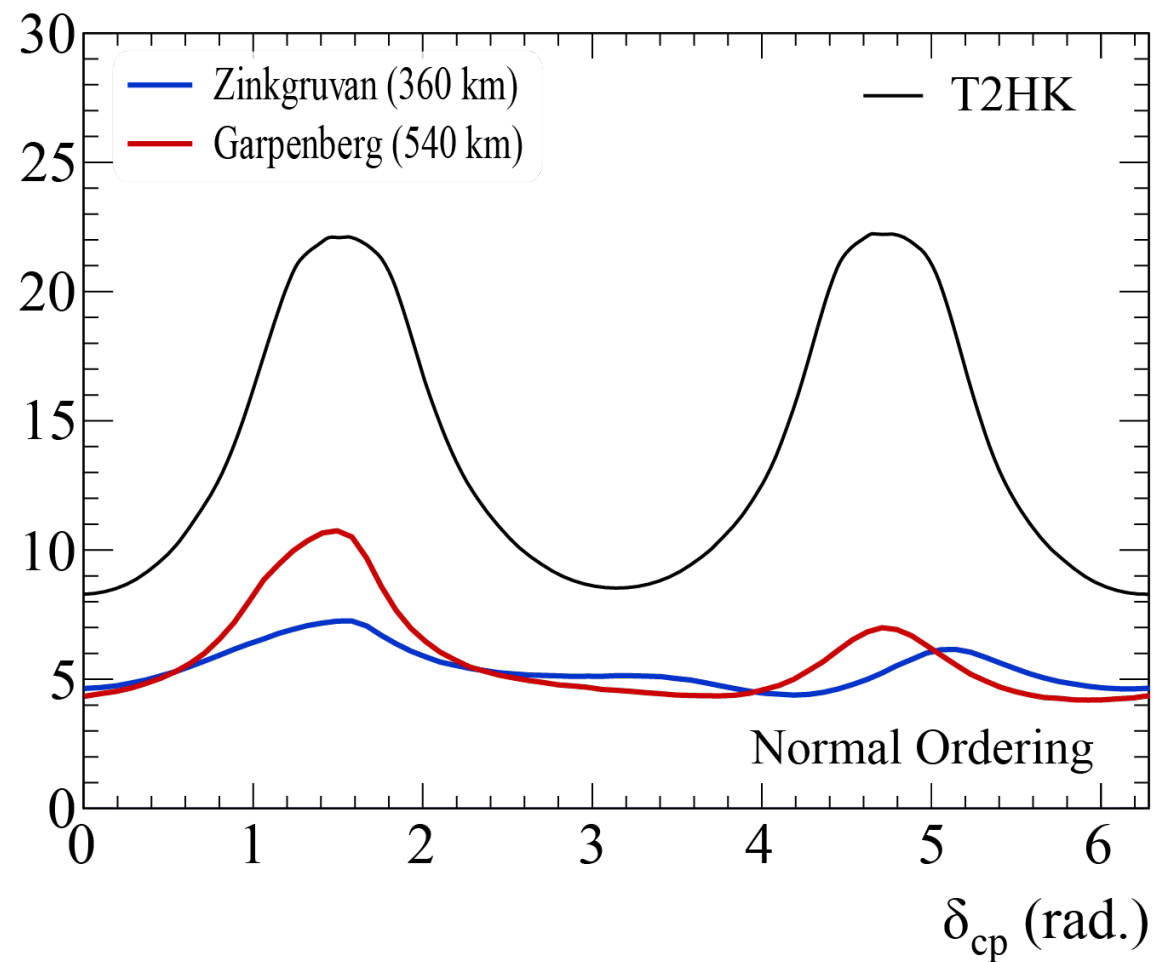
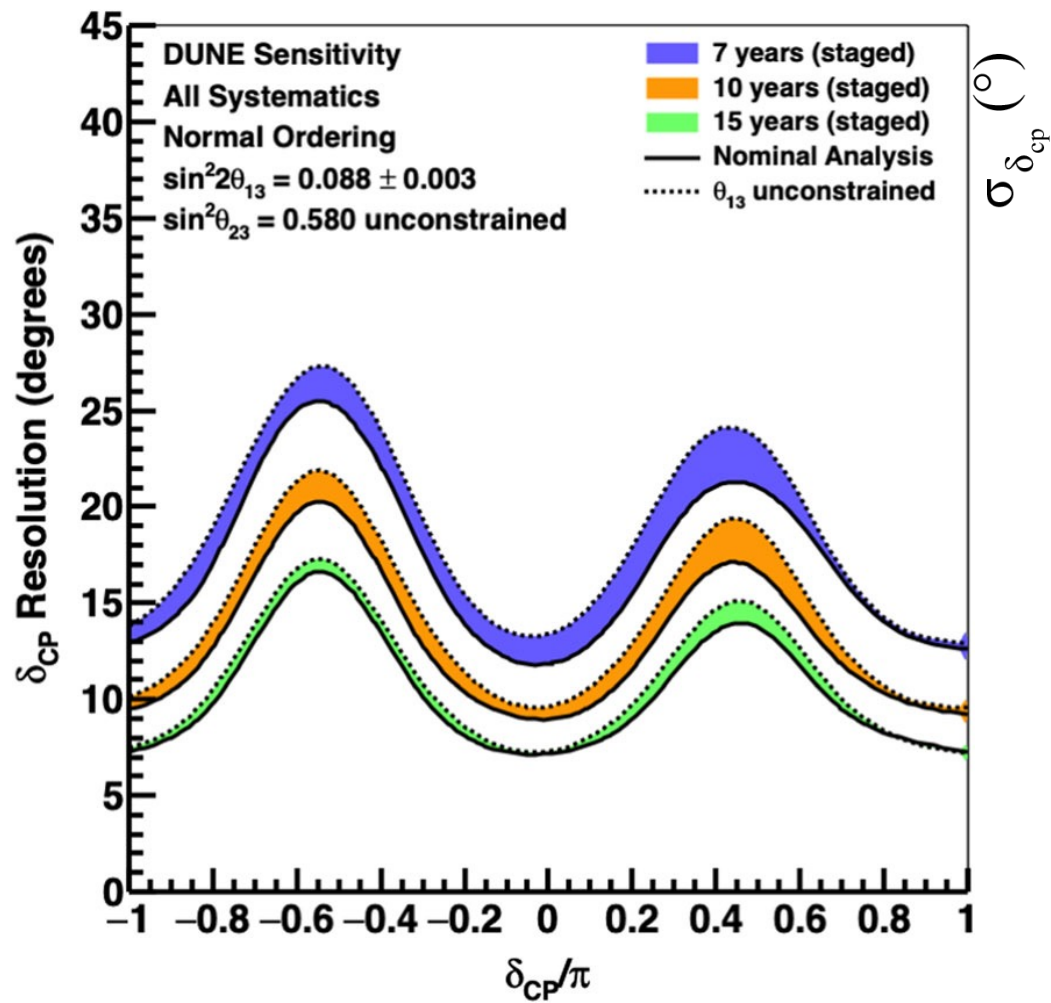
BACKUP



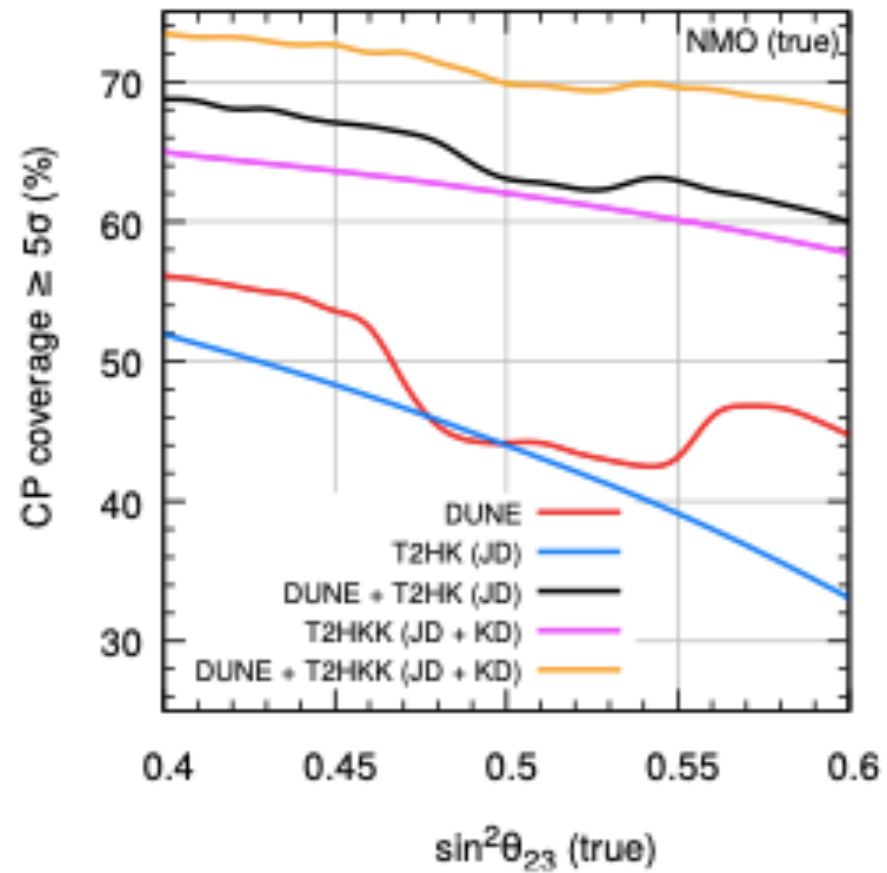
SYSTEMATICS

Systematics	SB			BB			NF		
	Opt.	Def.	Cons.	Opt.	Def.	Cons.	Opt.	Def.	Cons.
Fiducial volume ND	0.2%	0.5%	1%	0.2%	0.5%	1%	0.2%	0.5%	1%
Fiducial volume FD (incl. near-far extrap.)	1%	2.5%	5%	1%	2.5%	5%	1%	2.5%	5%
Flux error signal ν	5%	7.5%	10%	1%	2%	2.5%	0.1%	0.5%	1%
Flux error background ν	10%	15%	20%	correlated			correlated		
Flux error signal $\bar{\nu}$	10%	15%	20%	1%	2%	2.5%	0.1%	0.5%	1%
Flux error background $\bar{\nu}$	20%	30%	40%	correlated			correlated		
Background uncertainty	5%	7.5%	10%	5%	7.5%	10%	10%	15%	20%
Cross secs \times eff. QE [†]	10%	15%	20%	10%	15%	20%	10%	15%	20%
Cross secs \times eff. RES [†]	10%	15%	20%	10%	15%	20%	10%	15%	20%
Cross secs \times eff. DIS [†]	5%	7.5%	10%	5%	7.5%	10%	5%	7.5%	10%
Effec. ratio ν_e/ν_μ QE [*]	3.5%	11%	–	3.5%	11%	–	–	–	–
Effec. ratio ν_e/ν_μ RES [*]	2.7%	5.4%	–	2.7%	5.4%	–	–	–	–
Effec. ratio ν_e/ν_μ DIS [*]	2.5%	5.1%	–	2.5%	5.1%	–	–	–	–
Matter density	1%	2%	5%	1%	2%	5%	1%	2%	5%

COMPARISON WITH LBL



COMPARISON WITH LBL



EVENTS

Table 5.13: Expected number of neutrino interactions in 538 kt FD fiducial volume at a distance of 360 km (Zinkgruvan mine) in 200 days (one effective year). Shown for positive (negative) horn polarity.

	Channel	Non oscillated	Oscillated		
			$\delta_{CP} = 0$	$\delta_{CP} = \pi/2$	$\delta_{CP} = -\pi/2$
CC	$\nu_\mu \rightarrow \nu_\mu$	22 630.4 (231.0)	10 508.7 (101.6)	10 430.6 (5.8)	10 430.6 (100.9)
	$\nu_\mu \rightarrow \nu_e$	0 (0)	768.3 (8.6)	543.8 (5.8)	1 159.9 (12.8)
	$\nu_e \rightarrow \nu_e$	190.2 (1.2)	177.9 (1.1)	177.9 (1.1)	177.9 (1.1)
	$\nu_e \rightarrow \nu_\mu$	0 (0)	5.3 (3.3×10^{-2})	7.3 (4.5×10^{-2})	3.9 (2.4×10^{-2})
	$\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$	62.4 (3 640.3)	26.0 (1 896.8)	26.0 (1 898.9)	26.0 (1 898.9)
	$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$	0 (0)	2.6 (116.1)	3.5 (164.0)	1.4 (56.8)
	$\bar{\nu}_e \rightarrow \bar{\nu}_e$	1.3×10^{-1} (18.5)	1.3×10^{-1} (17.5)	1.3×10^{-1} (17.5)	1.2×10^{-1} (17.5)
	$\bar{\nu}_e \rightarrow \bar{\nu}_\mu$	0 (0)	3.0×10^{-3} (4.0×10^{-1})	1.5×10^{-3} (2.1×10^{-1})	4.1×10^{-3} (5.6×10^{-1})
NC	ν_μ			16 015.1 (179.3)	
	ν_e			103.7 (0.7)	
	$\bar{\nu}_\mu$			55.2 (3 265.5)	
	$\bar{\nu}_e$			1×10^{-1} (13.6)	

EVENTS

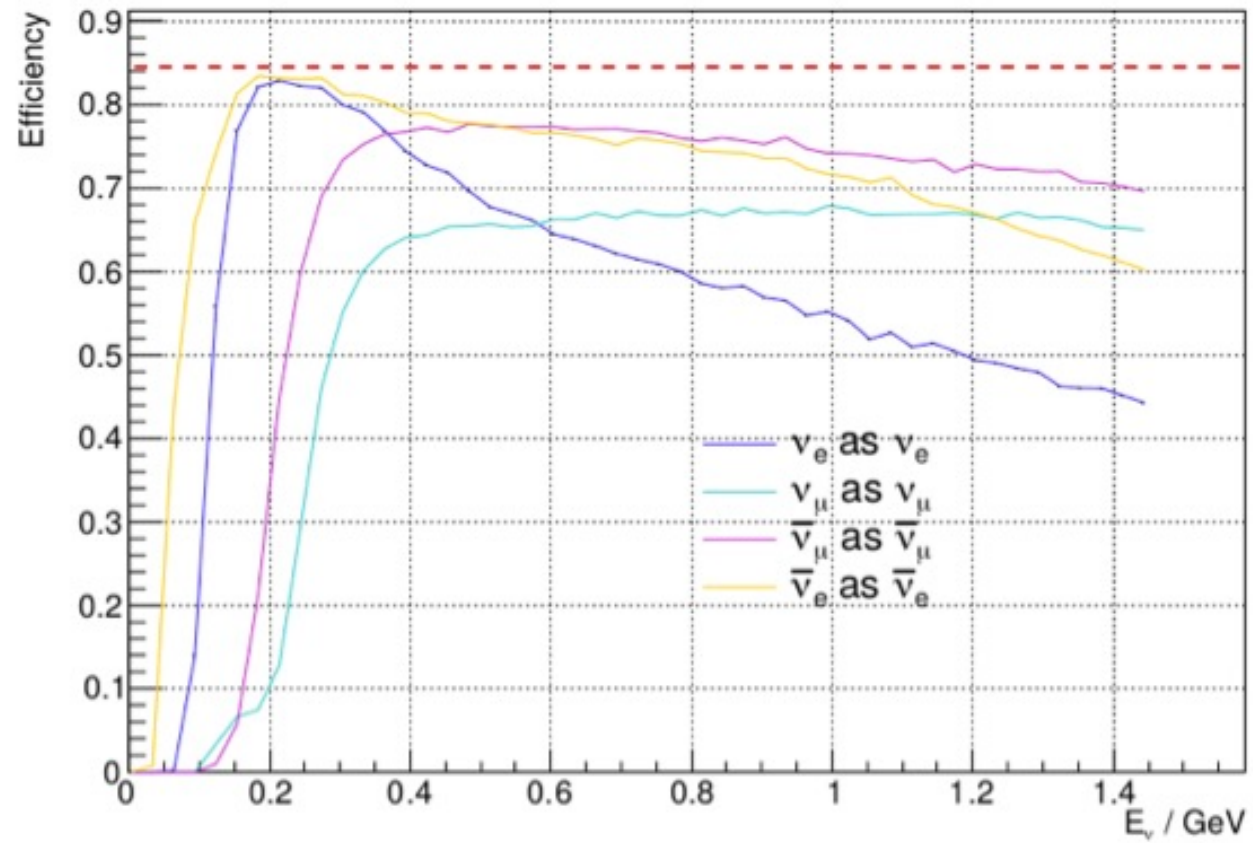
	Channel	$L = 540$ km	$L = 360$ km
Signal	$\nu_\mu \rightarrow \nu_e$ ($\bar{\nu}_\mu \rightarrow \bar{\nu}_e$)	272.22 (63.75)	578.62 (101.18)
Background	$\nu_\mu \rightarrow \nu_\mu$ ($\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$)	31.01 (3.73)	67.23 (11.51)
	$\nu_e \rightarrow \nu_e$ ($\bar{\nu}_e \rightarrow \bar{\nu}_e$)	67.49 (7.31)	151.12 (16.66)
	ν_μ NC ($\bar{\nu}_\mu$ NC)	18.57 (2.10)	41.78 (4.73)
	$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ ($\nu_\mu \rightarrow \nu_e$)	1.08 (3.08)	1.94 (6.47)

Table 1: Signal and major background events for the appearance channel corresponding to positive (negative) polarity per year for $\delta_{\text{CP}} = 0^\circ$.

	Channel	$L = 540$ km	$L = 360$ km
Signal	$\nu_\mu \rightarrow \nu_\mu$ ($\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$)	4419.69 (733.31)	7619.16 (1602.02)
Background	$\nu_e \rightarrow \nu_e$ ($\bar{\nu}_e \rightarrow \bar{\nu}_e$)	7.77 (0.02)	17.08 (0.05)
	ν_μ NC ($\bar{\nu}_\mu$ NC)	69.23 (8.24)	155.77 (18.54)
	$\nu_\mu \rightarrow \nu_e$ ($\bar{\nu}_\mu \rightarrow \bar{\nu}_e$)	14.68 (0.06)	61.30 (0.17)
	$\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$ ($\nu_\mu \rightarrow \nu_\mu$)	12.35 (41.00)	21.39 (72.59)

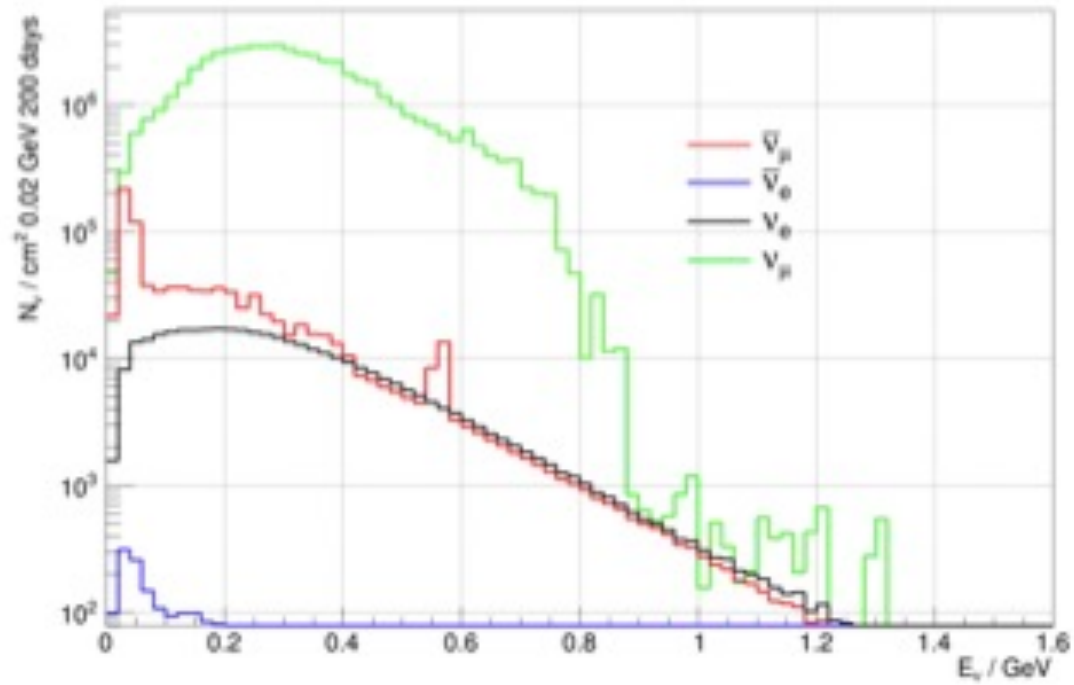
Table 2: Signal and major background events for the disappearance channel corresponding to positive (negative) polarity per year for $\delta_{\text{CP}} = 0^\circ$.

EFFICIENCY

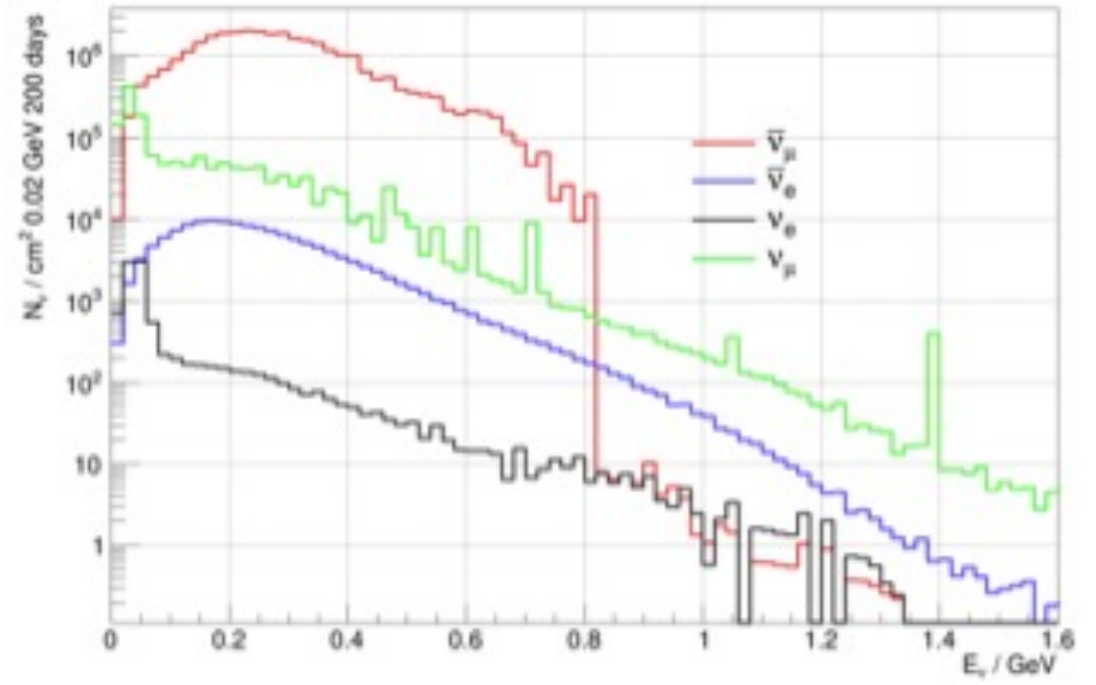


FLUXES

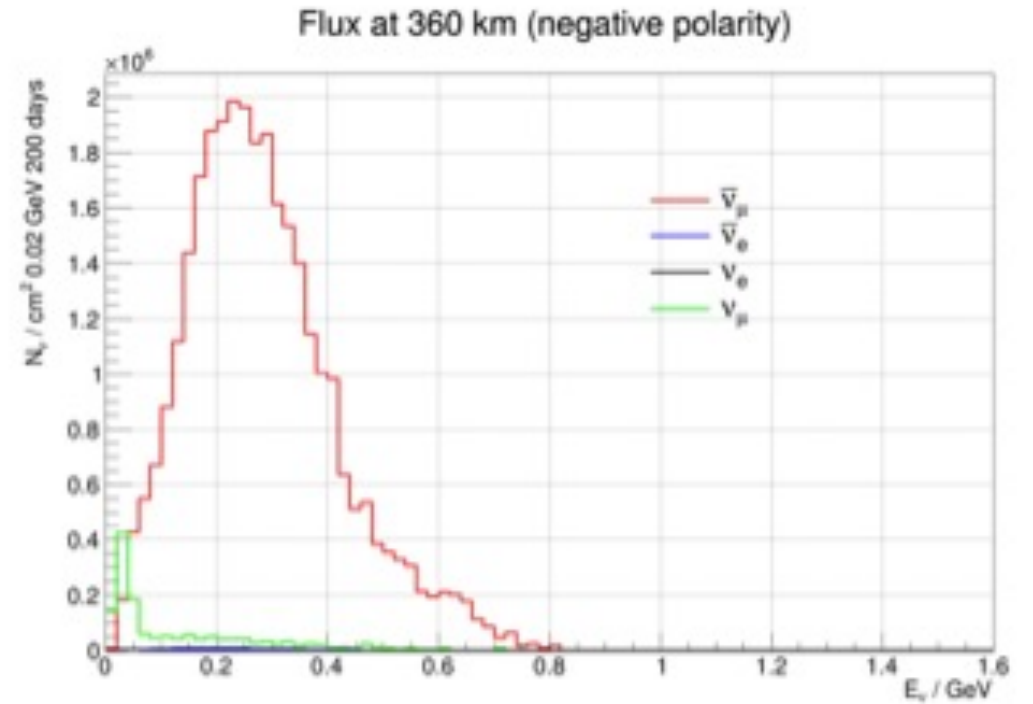
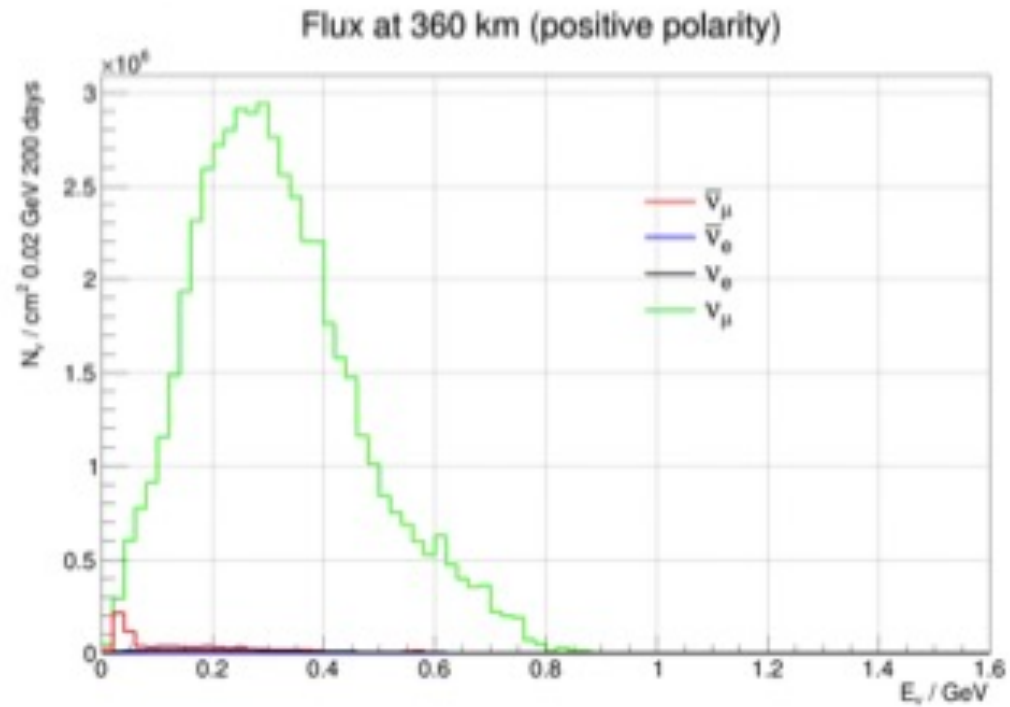
Flux at 360 km (positive polarity)



Flux at 360 km (negative polarity)



FLUXES



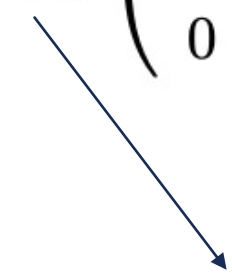
FLUXES

Flavour	ν Mode		$\bar{\nu}$ Mode	
	N_ν ($10^5/\text{cm}^2$)	%	N_ν ($10^5/\text{cm}^2$)	%
ν_μ	520.06	97.6	15.43	4.7
ν_e	3.67	0.67	0.10	0.03
$\bar{\nu}_\mu$	9.10	1.7	305.55	94.8
$\bar{\nu}_e$	0.023	0.03	1.43	0.43

Events at 360 km w/o oscillations

BSM: NSI

$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \left[\frac{1}{2E_\nu} U \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix} U^\dagger + A_{CC} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$$


$$\tilde{V}_{MSW} = a_{CC} \begin{pmatrix} 1 + \epsilon_{ee}^m & \epsilon_{e\mu}^m & \epsilon_{e\tau}^m \\ \epsilon_{e\mu}^{m*} & \epsilon_{\mu\mu}^m & \epsilon_{\mu\tau}^m \\ \epsilon_{e\tau}^{m*} & \epsilon_{\mu\tau}^{m*} & \epsilon_{\tau\tau}^m \end{pmatrix}$$

BSM: STERILE

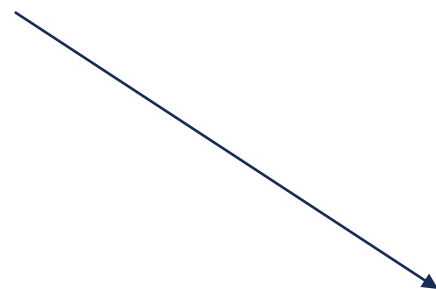
$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \\ \nu_s \end{pmatrix} = U = R(\theta_{34}) R(\theta_{24}) R(\theta_{23}, \delta_3) R(\theta_{14}) R(\theta_{13}, \delta_2) R(\theta_{12}, \delta_1)$$

New sources of CP violation!

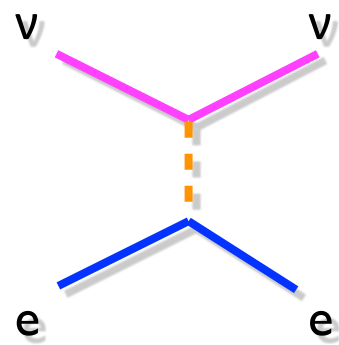
$$= \left[\frac{1}{2E_\nu} U \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 & 0 \\ 0 & 0 & \Delta m_{31}^2 & 0 \\ 0 & 0 & 0 & \Delta m_{41}^2 \end{pmatrix} U^\dagger + \begin{pmatrix} A_{CC} + A_{NC} & 0 & 0 & 0 \\ 0 & A_{NC} & 0 & 0 \\ 0 & 0 & A_{NC} & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \\ \nu_s \end{pmatrix}$$

BSM: NU

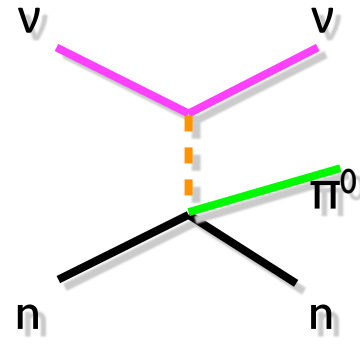
$$N = (1 + \alpha)U_{PMNS}.$$


$$\alpha = \begin{pmatrix} \alpha_{11} & 0 & 0 \\ |\alpha_{21}|e^{i\phi_{21}} & \alpha_{22} & 0 \\ |\alpha_{31}|e^{i\phi_{31}} & |\alpha_{32}|e^{i\phi_{32}} & \alpha_{33} \end{pmatrix}$$

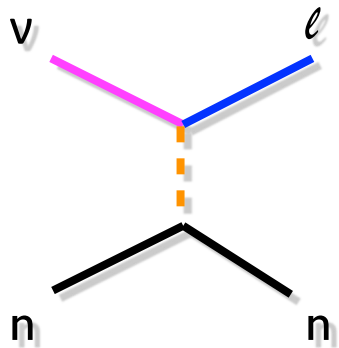
NEUTRINO INTERACTIONS



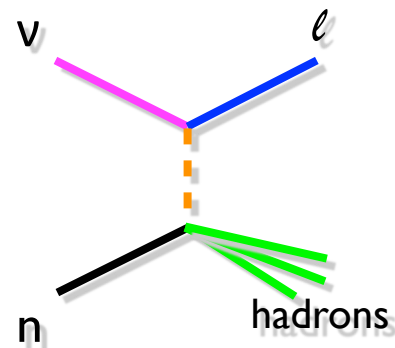
Elastic



Resonant (RES)



Quasi-Elastic (QE)



Deep inelastic (DIS)