

# Measurement of the cross-section ratio $\sigma_{\psi(2S)}/\sigma_{J/\psi(1S)}$ in exclusive photoproduction at HERA

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(on behalf of the ZEUS collaboration)

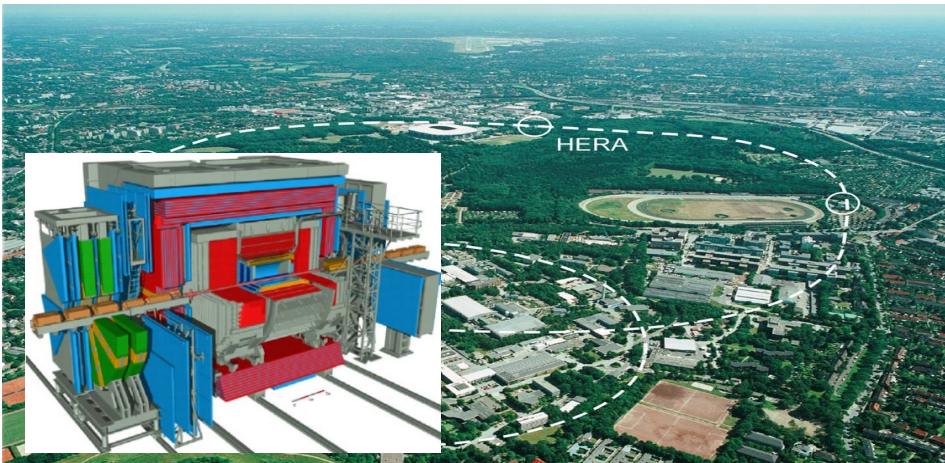
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*42<sup>nd</sup> International Conference on High Energy Physics, ICHEP-2024, 17 - 24 July 2024, Prague*

# HERA and ZEUS: 1992 – 2007, DESY, Hamburg

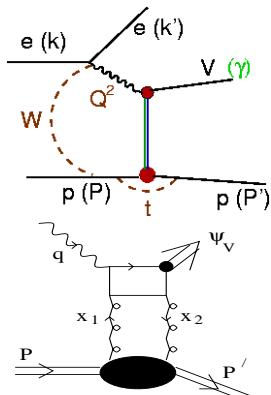
HERA: world's first and only  $e^\pm p$  collider,  $E_e = 27.5 \text{ GeV}$ ,  $E_p = 920 \text{ GeV}$  ( $\sqrt{s} = 318 \text{ GeV}$ )



ZEUS: multipurpose, hermetic detector (MVD, CTD, CAL, F/B/RMUON, BAC, ...)

Total luminosity:  $\int \mathcal{L} \sim 500 \text{ pb}^{-1}$  collected during HERA I + II running periods

# Production of Vector Mesons in Exclusive Diffraction in $ep$ Scattering



Exclusive process: proton stays intact  
 Proton dissociation also possible  $\rightarrow$   
 background

pQCD:  $M_V^2$  and  $Q^2$  - set the scale at which the  $W$  and  $|t|$  are probed  
 Process sensitive to the **gluon density** in the proton

Kinematics:  $M_V^2, Q^2, W, |t|$

$M_V^2$  - vector meson mass squared

$Q^2 (= -q^2 = -(k - k')^2)$  - the photon virtuality  
 (emitted by the incoming electron):

- $Q^2 \approx 0$  GeV<sup>2</sup> PHP (*Photoproduction*)
- larger  $Q^2$  for DIS (*Deep Inelastic Scattering*)

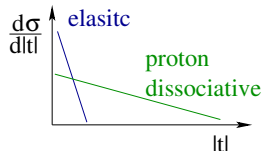
$W = (q + P)^2$  - invariant mass of the  $\gamma p$  system

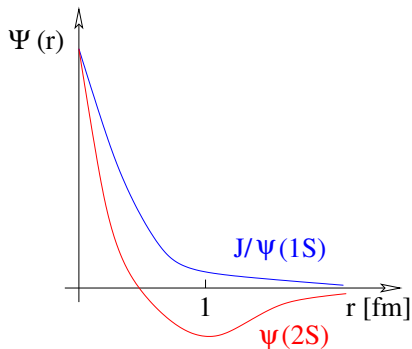
$$W \approx \sqrt{2E_P(E - p_Z)}_V$$

$|t|$  - 4-momentum transfer at the proton vertex

$$t = (P - P')^2$$

$$t \approx -p_{T,V}^2$$



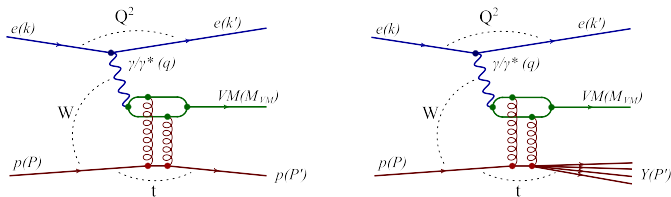


$$\text{Ratio } R = \frac{\sigma_{\gamma p \rightarrow \psi(2S)p}}{\sigma_{\gamma p \rightarrow J/\psi(1S)p}}$$

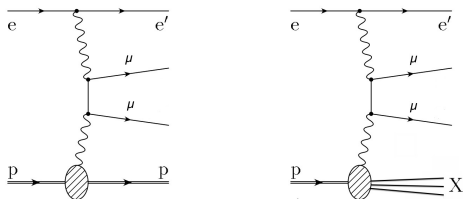
- sensitive to radial wave function of charmonium
- provides insight into the dynamics of the hard process

- $J/\psi(1S)$  and  $\psi(2S)$  have the same quark composition but distinctive wave functions
- $\psi(2S)$  has a node at  $\approx 0.4$  fm
- $\langle r_{\psi(2S)}^2 \rangle \approx 2 \langle r_{J/\psi(1S)}^2 \rangle$
- pQCD models predict  $R \sim 0.17$  in PHP and **rise of  $R$  with  $Q^2$  in DIS**
- $\psi(2S)$  cross section is expected to be suppressed w.r.t. the  $J/\psi$  production
- (Both Vector Mesons masses are much smaller than the  $\gamma p$  center-of-mass energy)

- **Signal MC: DIFFVM (VM production in  $ep$  scattering)**

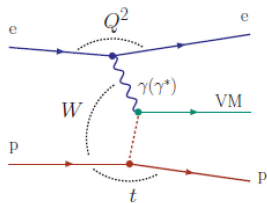
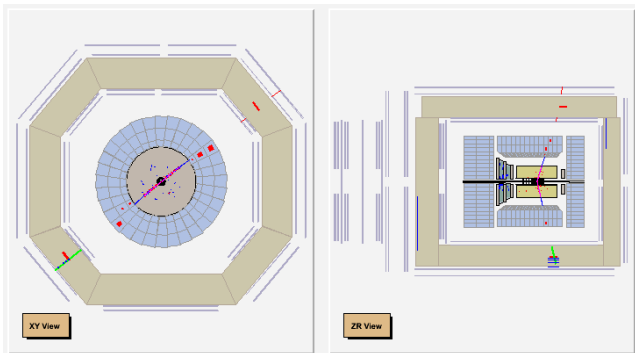


- **Background MC: GRAPE (Bethe-Heitler continuum  $\mu^+\mu^-$ )**



- **HERA II DATA:**  $\mathcal{L} = 373 \text{ pb}^{-1}$  (2003 - 2007)
- **Investigated decay channels:**
  - $\psi(2S) \rightarrow J/\psi + \pi^+\pi^-$ ,  $\psi(2S) \rightarrow \mu^+\mu^-$ ,  $J/\psi(1S) \rightarrow \mu^+\mu^-$
- **exclusive (elastic) photoproduction sample**

# Example of Final State Topology for $ep \rightarrow J/\psi p$ , $J/\psi \rightarrow \mu^+ \mu^-$



**Exclusive** process, reaction mediated by exchange of **colorless** object; **proton stays intact.**

$J/\psi$  and  $\psi(2S)$  are detected in the 2- or 4-prong final states ( $\mu^+ \mu^-$  or  $\mu^+ \mu^- \pi^+ \pi^-$ )  
**very clean final state topology:**

Photoproduction ( $Q^2 < 1 \text{ GeV}^2$ ): two or four charged particles and nothing else  
 $\implies$  **experimental challenge: triggering on soft muons**

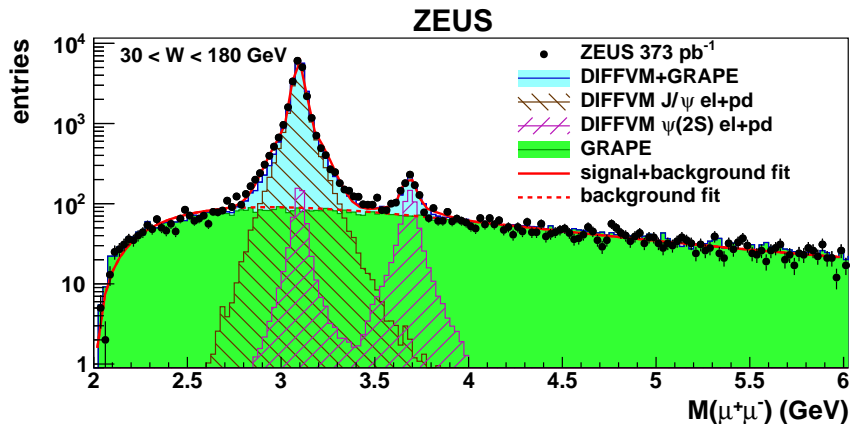
(Electroproduction ( $Q^2 > 1 \text{ GeV}^2$ ): scattered electron also visible in the detector)

**NOTE THE OPENING ANGLE OF THE DECAY PRODUCTS**

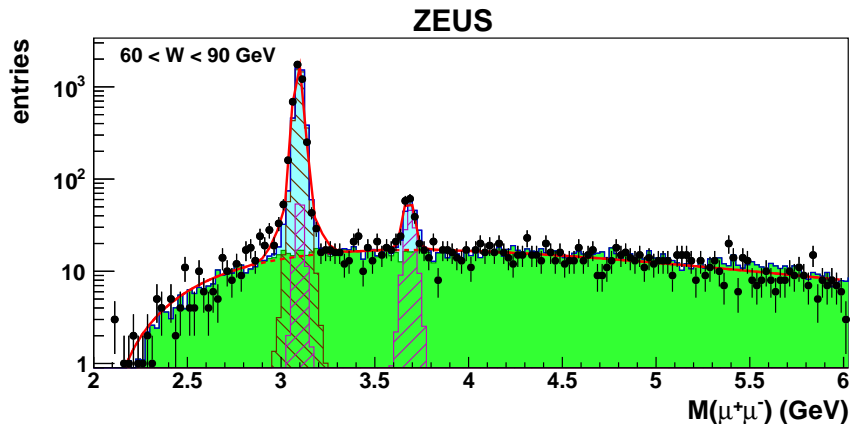
- **Exclusive Muon Triggers** (F/B/R/MUON or BAC)
- **Tracking and Vertex**
  - $N_{track} = 2$ , oppositely charged tracks matched to the primary vertex ( $\eta \in (-1.9, 1.9)$ )
  - **both tracks identified as a muon in CAL, at least one in F/B/RMUON or BAC**
  - $p_T > 1.0$  GeV of each track
  - anti-COSMIC cuts (CAL timing, acolinearity:  $\cos(\mu^+, \mu^-) < -0.985$ )
- **Elasticity/Exclusivity and Photoproduction cuts** (on CAL Energy)
  - no scattered electron found in CAL
  - $E_{clu} < 0.5$  GeV for clusters not matched to muons (or pions)  
(corresponds to an effective cut on  $Q^2 < 1$  GeV<sup>2</sup>)
  - $E(\theta < 0.12rad) < 1$  GeV  
the sum of the energy in the FCAL cone around the beam-pipe;  
**to suppress proton-dissociative events,  $ep \rightarrow e + VM + Y$**   
(corresponds to a requirement for  $M_Y \lesssim 5$  GeV)
- **Kinematic range (analysis phase space):**
  - $30 < W < 180$  GeV
  - $|t| < 1.0$  GeV<sup>2</sup>
  - $Q^2 < 1$  GeV<sup>2</sup> (median  $Q^2 \approx 3 \times 10^{-5}$  GeV<sup>2</sup>)
- (for 4-prongs selection see backup plots)



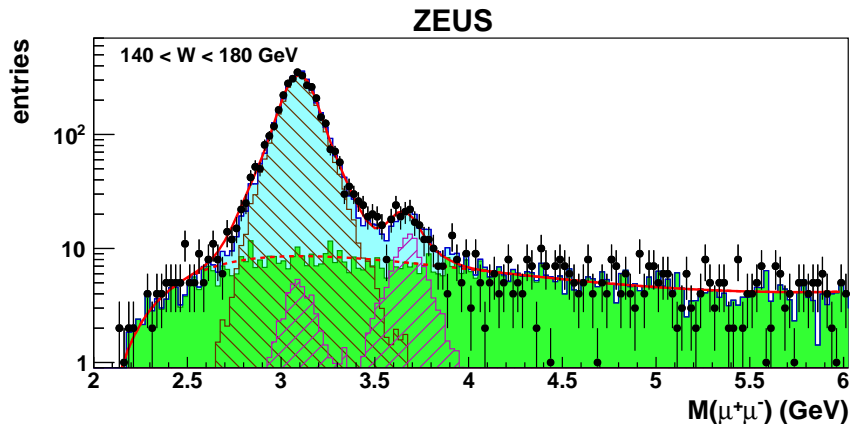
- **Signal Extraction, Mass spectra**

$M(\mu^+\mu^-)$ 

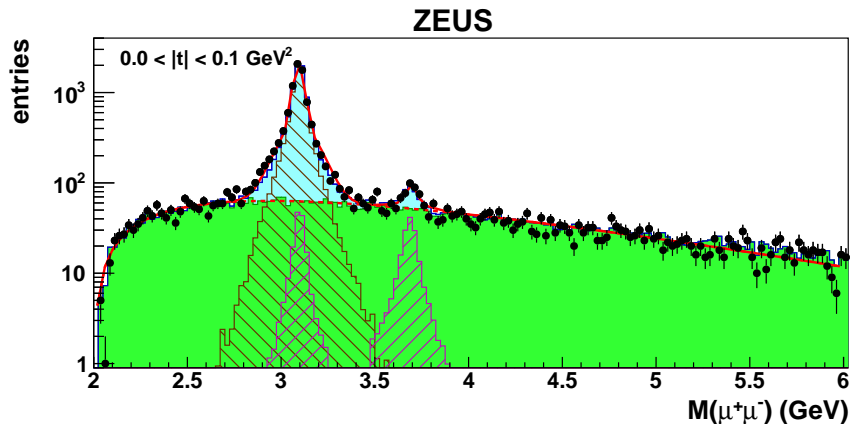
- full phase space:  $30 < W < 180 \text{ GeV}$ ,  $|t| < 1.0 \text{ GeV}^2$
- events yield:  $\sim 23\,000 J/\psi$  and  $\sim 700 \psi(2S)$  (from double Gaussian fit)
- resonant background under  $J/\psi$  peak

$M(\mu^+\mu^-)$ 

- **W2 bin:**  $60 < W < 90$  GeV,  $|t| < 1.0$  GeV<sup>2</sup>
- central rapidity region, long tracks, mass resolution:  $\sigma_M(\mu\mu) \sim 22$  MeV

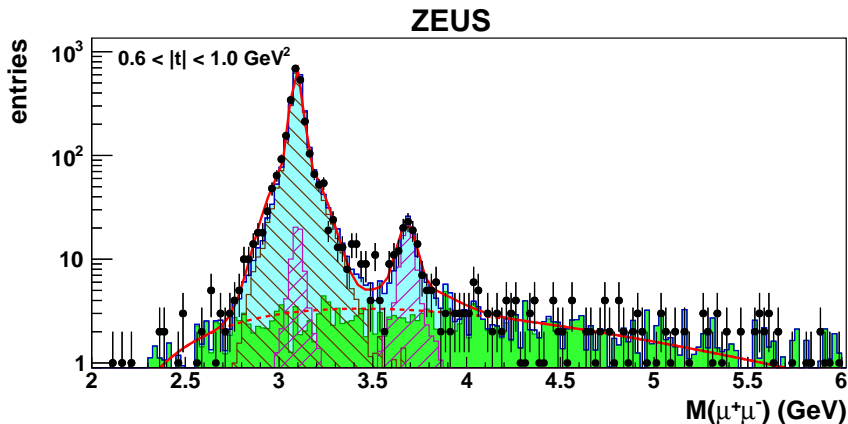
$M(\mu^+\mu^-)$ 

- **W5 bin:**  $140 < W < 180$  GeV,  $|t| < 1.0$  GeV<sup>2</sup>
- high  $W$ , backward short tracks, mass resolution:  $\sigma_M(\mu\mu) \sim 73$  MeV

$M(\mu^+\mu^-)$ 

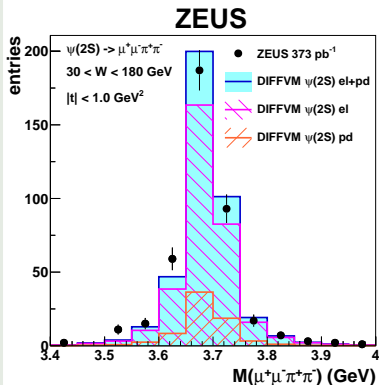
- **t1 bin:**  $30 < W < 180 \text{ GeV}$ ,  $|t| < 0.1 \text{ GeV}^2$
- low  $|t|$ , dominated by Bethe-Heitler continuum  $\mu^+\mu^-$  background

$M(\mu^+\mu^-)$

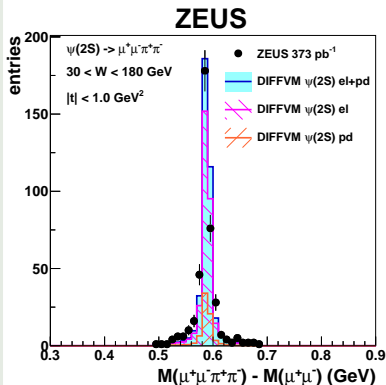


- **t5 bin:**  $30 < W < 180$  GeV,  $0.6 < |t| < 1.0$  GeV<sup>2</sup>
- higher  $|t|$ , small Bethe-Heitler continuum  $\mu^+\mu^-$  contribution
- **BUT:** high contamination proton dissociative events  $\rightarrow$   $t$ -spectra

$$M(\mu^+ \mu^- \pi^+ \pi^-)$$



$$M(\mu^+ \mu^- \pi^+ \pi^-) - M(\mu^+ \mu^-)$$



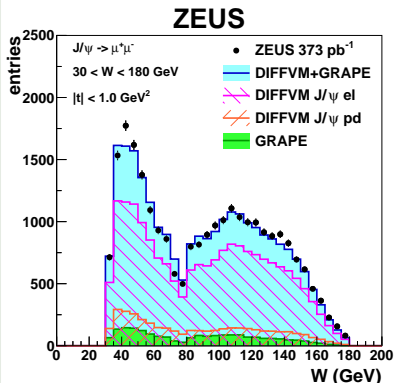
- events yield:  $\sim 400 \psi(2S)$  (background free)
- better resolution on mass difference  $\rightarrow$  cascade decay of  $\psi(2S)$
- proton dissociative fraction:  $f_{p,diss} = 0.16 \pm 0.01$  from  $t$ -spectra fit

- $W$  and  $|t|$  distributions: 2-prongs

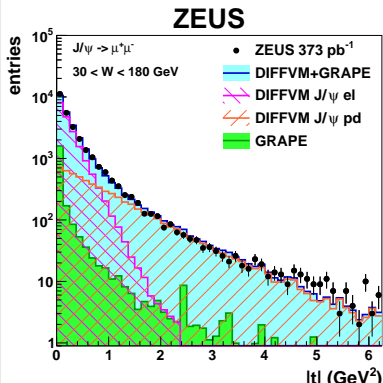


## 2-prongs: $W$ and $|t|$ distributions: $J/\psi$ mass window

$W$ :  $2.8 < M(\mu^+\mu^-) < 3.4$  GeV



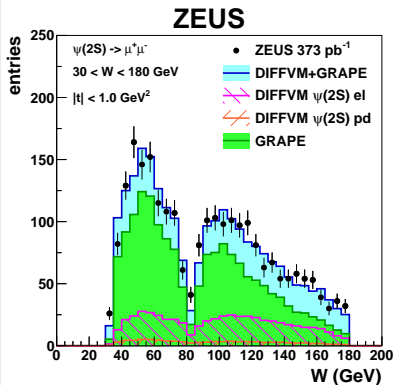
$|t|$ :  $2.8 < M(\mu^+\mu^-) < 3.4$  GeV



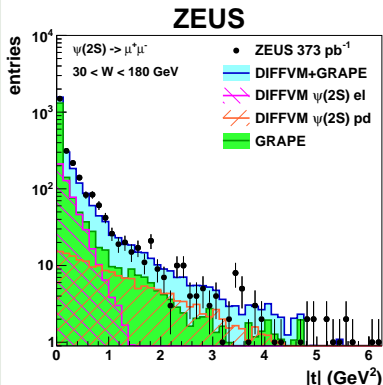
- dip in  $W$  distribution due to the anti-COSMIC cut:  $\cos(\mu^+, \mu^-) < -0.985$
- proton dissociation dominates for  $|t| > 1.0$  GeV<sup>2</sup>
- proton dissociative fraction:  $f_{p,diss} = 0.17 \pm 0.01$  ( $|t| < 1.0$  GeV<sup>2</sup>) from  $t$ -spectra fit

## 2-prongs: $W$ and $|t|$ distributions: $\psi(2S)$ mass window

$W$ :  $3.4 < M(\mu^+\mu^-) < 4.0$  GeV



$|t|$ :  $3.4 < M(\mu^+\mu^-) < 4.0$  GeV



- dip in  $W$  distribution due to the anti-COSMIC cut:  $\cos(\mu^+, \mu^-) < -0.985$
- proton dissociation dominates for  $|t| > 1.0$  GeV<sup>2</sup>
- channel dominated by Bethe-Heitler continuum  $\mu^+\mu^-$  background

- **Cross section ratio**

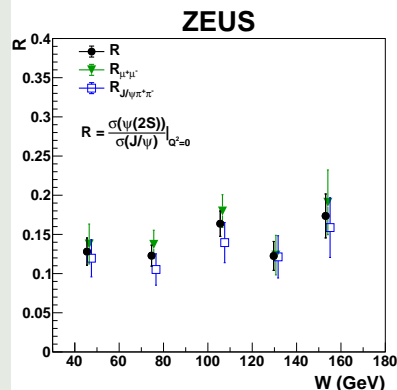
# Cross section ratio $R = \frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$ , full kinematic range

$30 < W < 180$  GeV,  $|t| < 1.0$  GeV<sup>2</sup>,  $Q^2 < 1.0$  GeV<sup>2</sup>

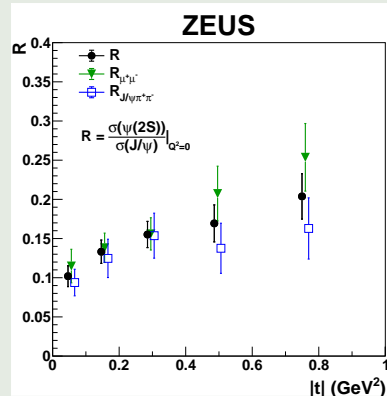
$\psi(2S)$ decay mode	$R = \frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$
$\mu^+ \mu^-$	$0.154 \pm 0.012$
$J/\psi(\rightarrow \mu^+ \mu^-) \pi^+ \pi^-$	$0.125 \pm 0.019$
combined	$0.146 \pm 0.010^{+0.016}_{-0.020}$

- $$R_{J/\psi\pi\pi} = \frac{N_{\psi(2S)}}{N_{J/\psi(1S)}} \cdot \frac{Acc_{J/\psi(1S) \rightarrow \mu^+ \mu^-}}{Acc_{\psi(2S) \rightarrow J/\psi\pi^+\pi^-}} \cdot \frac{1}{BR_{\psi(2S) \rightarrow J/\psi\pi^+\pi^-}} \cdot \frac{1 - f_{p.diss}^{\psi(2S)}}{1 - f_{p.diss}^{J/\psi(1S)}}$$
- $$R_{\mu\mu} = \frac{N_{\psi(2S)}}{N_{J/\psi(1S)}} \cdot \frac{Acc_{J/\psi(1S) \rightarrow \mu^+ \mu^-}}{Acc_{\psi(2S) \rightarrow \mu^+ \mu^-}} \cdot \frac{BR_{J/\psi(1S) \rightarrow \mu^+ \mu^-}}{BR_{\psi(2S) \rightarrow \mu^+ \mu^-}} \cdot \frac{1 - f_{p.diss}^{\psi(2S)}}{1 - f_{p.diss}^{J/\psi(1S)}}$$
- $Acc_i = \frac{N_i^{reco}}{N_i^{true}}, f_{p.diss}^i$  - fraction of proton dissociative events
- $BR(\psi(2S) \rightarrow J/\psi\pi^+\pi^-) = (34.68 \pm 0.3)\%$ ,  $BR(\psi(2S) \rightarrow \mu^+\mu^-) = (0.80 \pm 0.06)\%$ ,  
 $BR(J/\psi \rightarrow \mu^+\mu^-) = (5.961 \pm 0.033)\%$ ,  $BR(\psi(2S) \rightarrow \mu^+\mu^-\pi^+\pi^-) = (2.07 \pm 0.02)\%$  (PDG 2020)
- both channels have similar precision and provide consistent results**

$R$  vs.  $W$



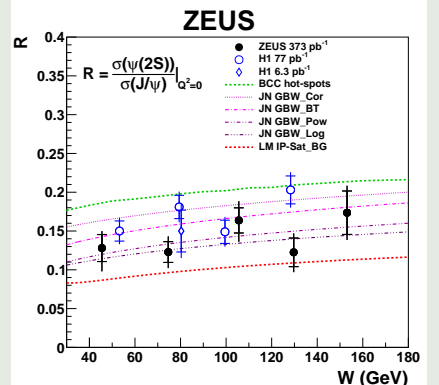
$R$  vs.  $|t|$



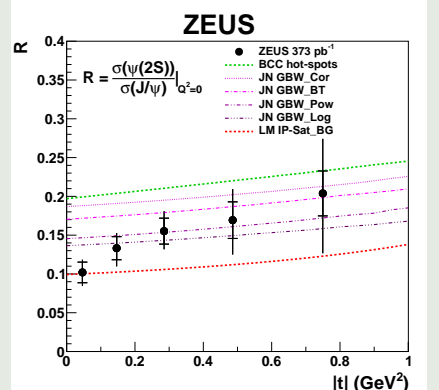
- $R_{\mu\mu}$  (2-prongs channel),  $R_{J/\psi\pi\pi}$  (4-prongs channel) and combined  $R$  (full dots)
- statistical errors only
- **good agreement between two channels**

# cross section ratio $R = \sigma_{\psi(2S)}/\sigma_{J/\psi(1S)}$ : Final Results

$R$  vs.  $W$



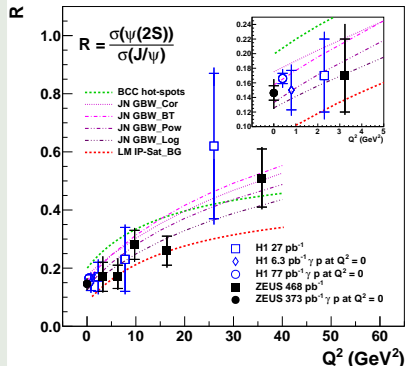
$R$  vs.  $|t|$



- for  $R$  vs.  $W$  ZEUS (full dots) and H1 (open markers) results are compared
- **no  $W$  dependence observed, moderate increase with  $|t|$**
- good agreement between data and theoretical models (see next page)
- errors at high- $|t|$  points dominated by systematics ( $\rightarrow$  proton dissociative fraction)

$R$  vs.  $Q^2$

**ZEUS**



theoretical models:

- Bendova, Cepila and Contreras (BCC hot-spots):
  - Phys. Rev. D **99**, 034025 (2019).
- Jan Nemchik et al. (JN):
  - Eur. Phys. J. C **79**, 154 (2019).
  - Eur. Phys. J. C **79**, 495 (2019).
  - Phys. Rev. D **103**, 094027 (2021).
- Lappi and Mäntysaari (LM IP-Sat):
  - Phys. Rev. C **83**, 065202 (2011).
  - Phys. Rev. D **87**, 034002 (2013).
  - PoS (DIS2014), 069 (2014).

- ZEUS (full dot) and H1 (open markers) photoproduction results plotted at  $Q^2 \sim 0$
- DIS results are also presented vs.  $Q^2$ : ZEUS (full squares) and H1 (open squares)
- good agreement between data and theoretical models ( $\rightarrow$  backup plots, page 30)
- **better precision of photoproduction points**

- **Cross section ratio  $R = \frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$**  in photoproduction using HERA II data was measured by ZEUS in the kinematic range:  $30 < W < 180$  GeV,  $|t| < 1.0$  GeV<sup>2</sup>
- first ZEUS measurement of  $R$  in photoproduction (at  $Q^2 = 0$ ):  
 $R = 0.146 \pm 0.01(\text{stat.})_{-0.022}^{+0.016}(\text{syst.})$
- first HERA result for  $R$  vs.  $|t|$  in photoproduction
- **moderate rise of cross section ratio as a function of  $|t|$**
- **no  $W$  dependence observed within experimental errors**
- consistent results for 2- and 4-prongs decay channels
- comparable precision in both decay channels
- **theoretical calculations of the ratio  $\frac{\sigma(\psi(2S))}{\sigma(J/\psi(1S))}$  for exclusive vector-meson production has been compared to the experimental data**
- **→ majority of the predictions are consistent with the data**
- **data start to exhibit constraining power**
- for more details see: [https://doi.org/10.1007/JHEP12\(2022\)164](https://doi.org/10.1007/JHEP12(2022)164)



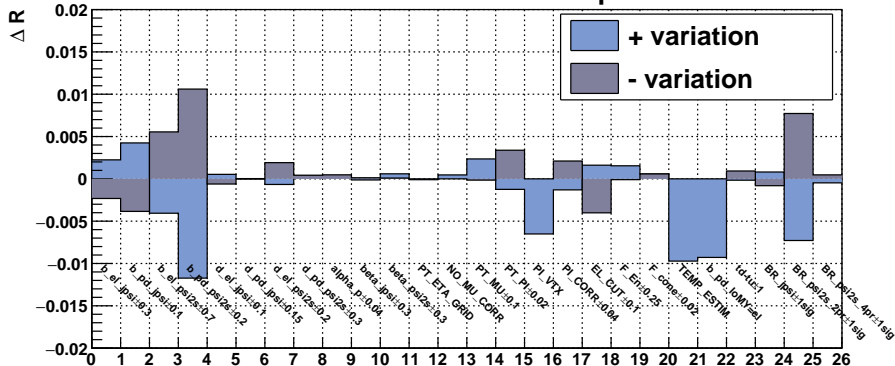
Thank You For Your Attention

BACKUP PLOTS FOLLOWS...

- **Systematics**

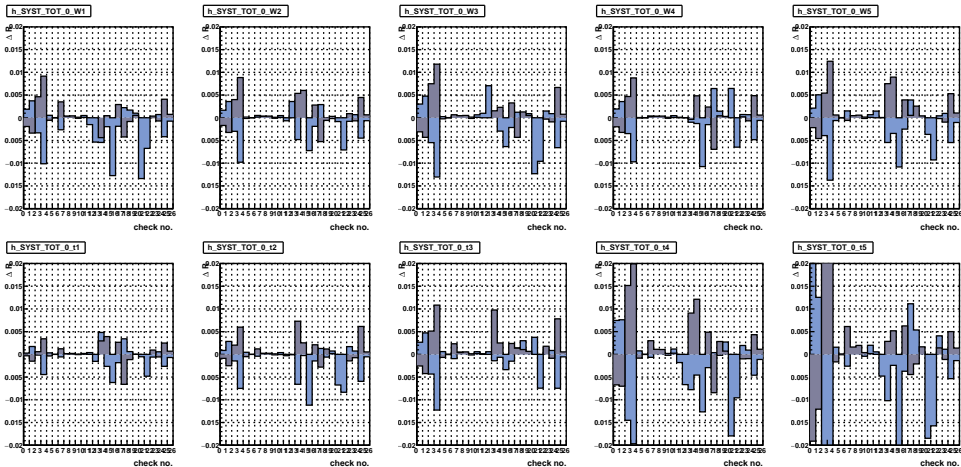
h\_SYST\_TOT\_0

### R GLOBAL: SYST error components



- biggest contributions from:
- $b$ -slope variation of  $t$ -dependence (esp. for  $b_{pd}$  of  $\psi(2S)$ )
- event number estimator (MC templates fit instead of Gaussian fit)
- slow pions vertexing
- $BR(\psi(2S) \rightarrow \mu^+ \mu^-)$

# R: components of SYST. error in $W$ and $|t|$ bins



- upper row: contributions in 5  $W$  bins
- bottom row: contributions in 5  $|t|$  bins
- bin order as on previous page

- **Theoretical Models**

- **Bendova, Cepila and Contreras (BCC hot-spots) :**
- Phys. Rev. D **99**, 034025 (2019).
- model with hot spots randomly sampled in the transverse plane bound by the size of the proton
- The slope parameter  $b$  is  $4.72 \text{ GeV}^{-2}$  and it is fixed by the combined H1 and ZEUS data from 2013 for JPsi photoproduction  $t$ -distribution.
- the same  $b$ -slope for both JPsi and Psi2s

## Theory predictions: models (2)

- **Jan Nemchik (JN) et al. :**
- Eur. Phys. J. C **79**, no.6, 495 (2019).
- Eur. Phys. J. C **79**, no.2, 154 (2019).
- calculations have been performed for various combinations of quarkonium wave functions:
  - **Cor** (Cornell potential)
  - **BT** (Buchmüller-Tye)
  - **Pow** (Power-law potential)
  - **Log** (Logarithmic potential)
- and models for the dipole cross sections:
  - BGBK, **GBW** ← **used on the plots**
  - for each combinations calculations are performed with and w/o skewness in the gluon density
- the same  $b$ -slope parameters for both quarkonium states



- **Lappi and Mäntysaari (LM IP-Sat):**
  - the BFKL evolution plus the IP-Sat model to predict vector-meson production in ep and electronion collisions in the dipole picture
  - 2S parameters from arXiv:1406.2877 (PoS DIS2014 (2014) 069)
  - 1S parameters from hep-ph/0606272 (Phys.Rev. **D74** (2006) 074016)
  - Calculation described in (Phys.Rev. **C83** (2011) 065202)
  - **IP-Sat** dipole from fit (Phys.Rev. **D87** (2013) no.3, 034002)
  - Wave function: Boosted Gaussian (**BG**),  $Q^2 = 0 \text{ GeV}^2$
  - Skewedness and real part corrections included
- 
- predictions of all models were calculated within the phase space of this analysis:
    - $30 < W < 180 \text{ GeV}$
    - $|t| < 1.0 \text{ GeV}^2$
    - $Q^2 \sim 0$  (photoproduction points)

- **Signal extraction, cuts, control plots, ...**

## 2-prongs: Signal extraction: fit parameterization

- **Double Gaussian** shape:  $G(x)$  or  $g(x) = N \cdot \Delta \cdot \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{(x-m)^2}{2\sigma^2}\right)$   
where:  $N$  – number of events,  $\Delta$  – mass bin width,  
 $m$  – mean value,  $\sigma$  – RMS

- for  $J/\psi$ :  $N_1 \cdot G_1(x) + N_2 \cdot G_2(x)$

- for  $\psi'$ :  $N'_1 \cdot g_1(x) + N'_2 \cdot g_2(x)$

- introducing:  $N = N_1 + N_2$ ,  $N' = N'_1 + N'_2$ ,  $R = \frac{N'}{N}$

- **with additional constraints**:  $m_1 = m_2$ ,  $m'_1 = m'_2$ ,  
 $\frac{\sigma'_1}{\sigma_1} = \frac{\sigma'_2}{\sigma_2} = \alpha$ ,  $\xi = \frac{N_1}{N} = \frac{N'_1}{N'}$  (**scaling of the mass resolution**)

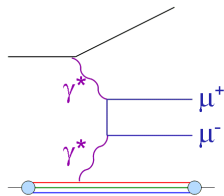
- final formulae:

$$F(x) = N \cdot ((\xi \cdot G_1(x) + (1 - \xi) \cdot G_2(x)) + R \cdot (\xi \cdot g_1(x) + (1 - \xi) \cdot g_2(x))) + BG(x)$$

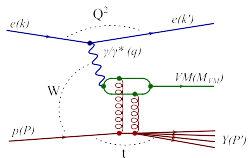
- **background function**:  $BG(x) = A \cdot (x - B)^C \cdot \exp(-D(x - B) - E(x - B)^2)$   
where  $A, B, C, D, E$  are fit parameters,  $B$  fixed ( $= 2p_{t,min}^\mu$ )

- (only differences w.r.t. the 2-prong channel)
- $N_{track} = 4$ , (two oppositely charged pairs, sorted by  $p_T$ )
- **highest momentum pair: muon candidates**  
lowest momentum pair: pion candidates
- no anti-COSMIC cuts
- transverse momentum of pion candidates:  $p_T^\pi > 0.12$  GeV;
- $2.8 < M(\mu^+ \mu^-) < 3.4$  GeV ( $J/\psi$  window)
- $M(\mu^+ \mu^- \pi^+ \pi^-) - M(\mu^+ \mu^-)$  in (0.5 – 0.7) GeV window (cascade decay of  $\psi(2S)$ )

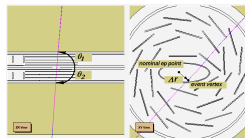
- QED di-muons (like  $\gamma^* \gamma^* \rightarrow \mu^+ \mu^-$ ) from the Bethe-Heitler process



- $J/\psi$  and  $\psi(2S)$  mesons production with the dissociation of the proton

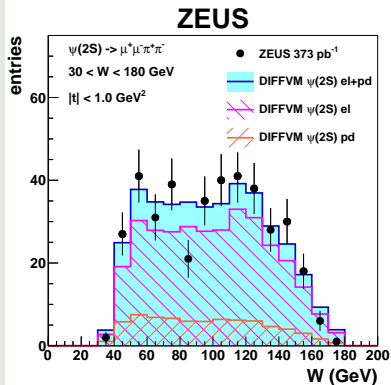


- Cosmic muons can mimic  $\mu^+ \mu^-$  pairs when passing close to the interaction point

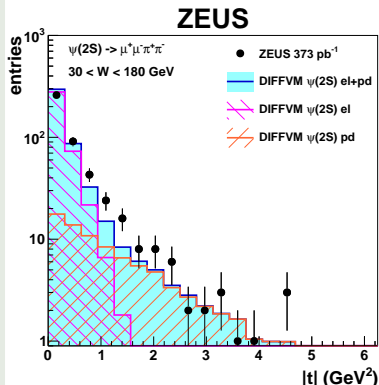


# 4-prongs: $W$ and $|t|$ distributions: $\psi(2S)$ mass window

$W$ :  $3.4 < M(\mu^+\mu^-\pi^+\pi^-) < 4.0$  GeV



$|t|$ :  $3.4 < M(\mu^+\mu^-\pi^+\pi^-) < 4.0$  GeV



- proton dissociation dominates for  $|t| > 1.0$  GeV<sup>2</sup>
- proton dissociative fraction:  $f_{p,diss} = 0.16 \pm 0.01$  ( $|t| < 1.0$  GeV<sup>2</sup>) from  $t$ -spectra fit

- **Monte Carlo**

# DIFFVM – A Monte Carlo Generator for Diffractive Processes in $ep$ Scattering.

B. List

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- soft diffractive processes in the Regge framework and Vector Dominance Model

- $\frac{d\sigma}{dQ^2} \propto \frac{1}{(1+Q^2/M_Y^2)^{1.5}}$

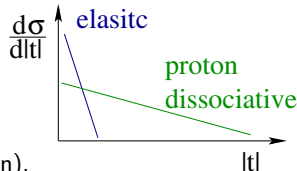
- $\frac{d\sigma}{d|t|} \propto W_{\gamma p}^{4\epsilon} e^{-b|t|}$  ( $4\epsilon = \delta$ ) (elastic)

- $\frac{d^2\sigma}{d|t|dM_Y^2} \propto W_{\gamma p}^{4\epsilon} e^{-b'|t|} M_Y^{-\beta}$  (p.diss)

- $\frac{d\sigma}{dM_Y^2} \sim \frac{f(M_Y^2)}{M_Y^{2(1+\epsilon)}}$  for  $M_Y^2 < 3.6 \text{ GeV}^2$  ( $p$  resonance region),

- $\frac{d\sigma}{dM_Y^2} \sim \frac{1}{M_Y^{2(1+\epsilon)}}$  for  $M_Y^2 \geq 3.6 \text{ GeV}^2$  (continuum region)

- assuming SCHC: s-channel helicity conservation





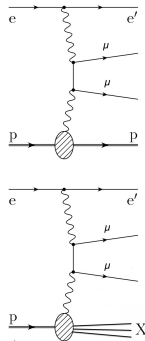
## GRAPE-Dilepton (Version 1.1)

A generator for dilepton production in  $ep$  collisions

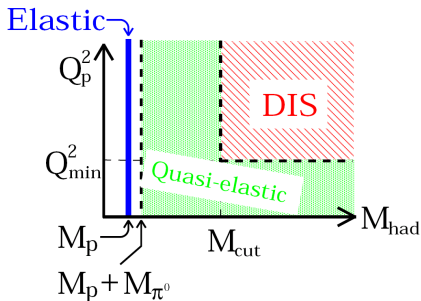
Tetsuo Abe

*Department of Physics, University of Tokyo, 7-3-1 Hongo, Bunkyo-ku, Tokyo 113-8654, Japan*

- based on the **exact matrix elements** in the electroweak theory at tree level via  $\gamma\gamma$ ,  $\gamma Z^0$ ,  $Z^0 Z^0$  and via photon internal conversion (QED Compton)
- **Feynman amplitudes** are generated by the automatic calculation system **GRACE**
- **proton vertex** covers the whole kinematical region
- interface to PYTHIA and SOPHIA  
→ complete hadronic final state
- covers **elastic, quasi-elastic and DIS processes**



**GRAPE** generator - simulate QED lepton pair (Bethe-Heitler)



Important for the **shape of the BH  $M_{\mu^+\mu^-}$  spectrum** (sidebands)  
 and for the **BH  $t$ -dependence**: low  $t$  - elastic BH, higher  $t$  - QEL BH

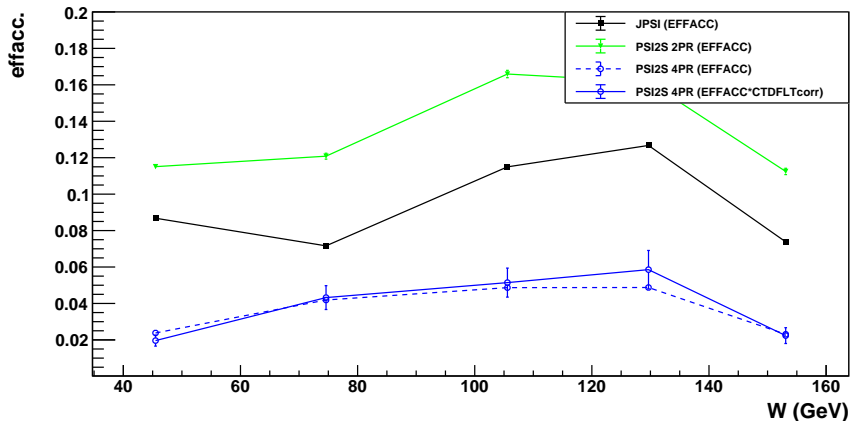
- **Tuning of DIFFVM Monte Carlo**

- Reweighting of MC sample at generator level
- **|t| dependence**:  $\sim \exp(-b|t|)$ , generated with  $b_{el} = 4.0$ ,  $b_{pd} = 1.0$   
reweighted to:  
 $b_{el} = 4.6 \pm 0.3$ ,  $b_{pd} = 1.0 \pm 0.1$  (JPSI)  
 $b_{el} = 4.3 \pm 0.7$ ,  $b_{pd} = 0.7 \pm 0.2$  (PSI2S)
- shrinkage added by reweighting:  $b = b_0 + 4.0\alpha' \log(W/W_0)$ ;  
 $\alpha' = 0.12 \pm 0.04 \text{ GeV}^{-2}$ ,  $W_0 = 90 \text{ GeV}$  (elastic only)
- **W dependence**:  $\sigma \sim W^\delta$ ,  
generated with  $\delta = 0.88$  for both elastic and p.diss  
reweighted to:  
 $\delta_{el} = 0.67 \pm 0.10$ ,  $\delta_{pd} = 0.42 \pm 0.15$  (JPSI)  
 $\delta_{el} = 1.10 \pm 0.20$ ,  $\delta_{pd} = 0.70 \pm 0.30$  (PSI2S)
- **$M_Y$  dependence**:  $\sim \frac{1}{M_Y^\beta}$ , generated with  $\beta = 2.5$   
reweighted to  $\beta = 2.4 \pm 0.3$  (both JPSI and PSI2S, p.diss only)
- **all parameters are subject to systematics checks**

- **selection efficiency**

# Acceptance\*efficiency in $W$ bins: elastic

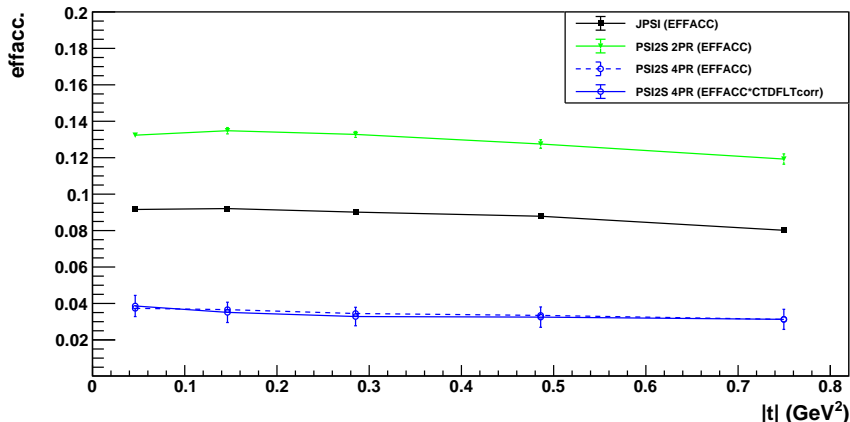
EFFACC (el) of JPSI, PSI2S-2PR, PSI2S-4PR vs.  $W$



- JPSI, PSI2S 2- and 4-prong ( $2 \div 16\%$ )
- Higher di-muon acceptance for higher mass state (PSI2S)
- different angular coverage for final state muons
- second  $W$  bin ( $W2$ ) is the “dip” for di-muon acceptance

# Acceptance\*efficiency in $|t|$ bins: elastic

EFFACC (el) of JPSI, PSI2S-2PR, PSI2S-4PR vs.  $|t|$

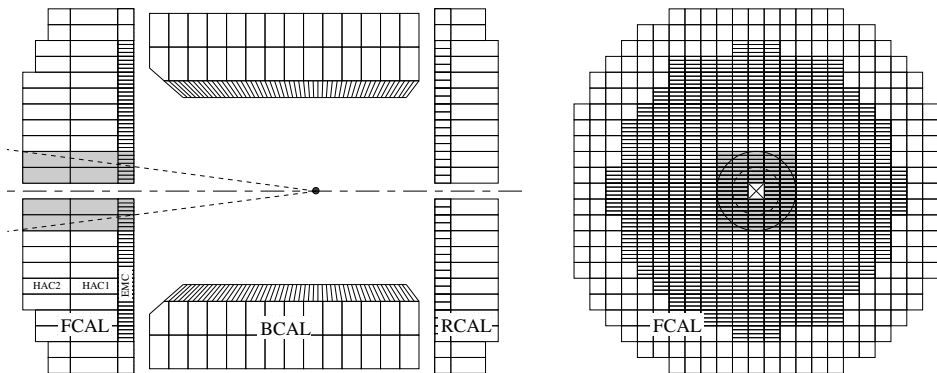


- JPSI, PSI2S 2- and 4-prong (**4 ÷ 12%**)
- Higher di-muon acceptance for higher mass state (**PSI2S**)
- **flat in  $|t|$  (no angular correlations to  $|t|$ )**
- **dashed line after CTD FLT corrections**

- **extracting fractions of proton dissociation**



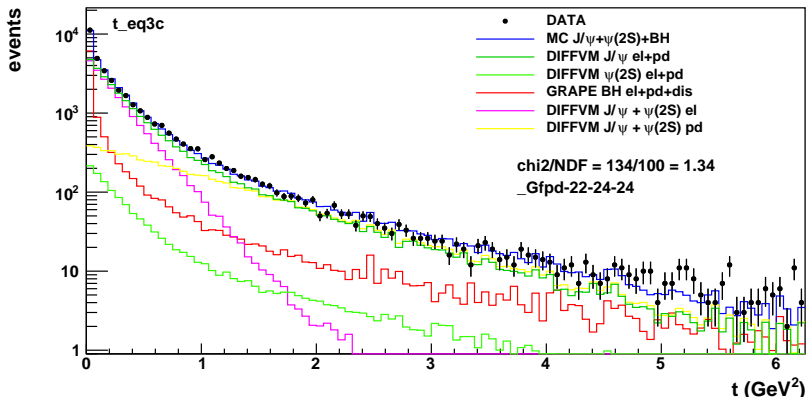
# Proton dissociation taggers



- Energy in forward cone to **suppress p.diss events**:  $\theta_{max} = 0.12 \text{ rad}$
- using EFO : “Energy Flow Objects” (trackers + CAL info):

$$\left( \sum_{EFOs} E(\theta_{EFO} < \theta_{max}) \right) < 1 \text{ GeV}$$

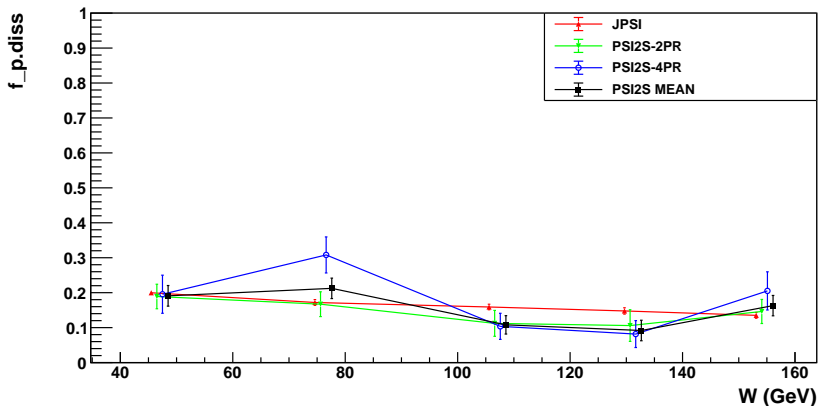
## 2-prongs: $|t|$ distribution: all 2-prong events



- spectra like this are used to evaluate the p.diss fractions (use longer “lever arm” then integrate it up to  $|t| = 1.0 \text{ GeV}^2$ )
- using root package TFractionalFitter (TFF)
- fitted  $f_{p.diss} = 0.17$  and  $= 0.16$  (JPSI and PSI2S, BH subtracted)
- p.diss take over elastic around  $\sim 1 \text{ GeV}^2$  (yellow and magenta histos)

# $f_{p,diss}$ fractions in $W$ bins (TFF estimator)

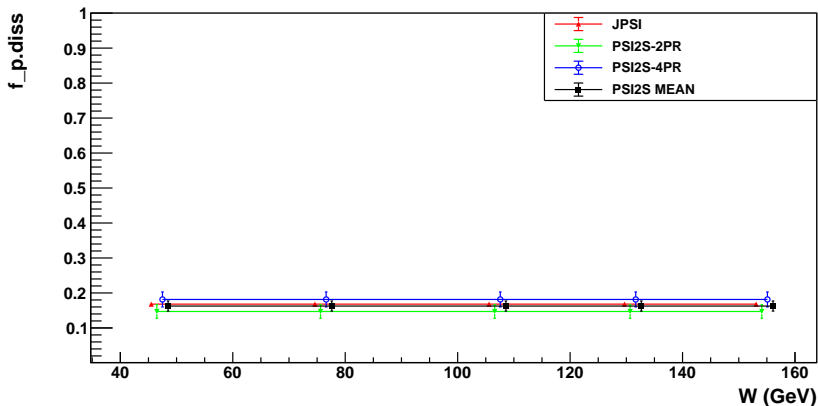
fraction  $f_{p,diss}$ : JPSI and PSI2S 2PR, 4PR vs.  $W$



- average value  $\sim 17\%$  JPSI and  $\sim 16\%$  PSI2S (mean)
- compatible results for 2- and 4-prong channels, no  $W$  dependence
- **black**: weighted mean for PSI2S 2- and 4-prong
- bigger fluctuations for PSI2S 2- and 4-prongs

# $f_{p,diss}$ fractions in $W$ bins (TFF estimator)

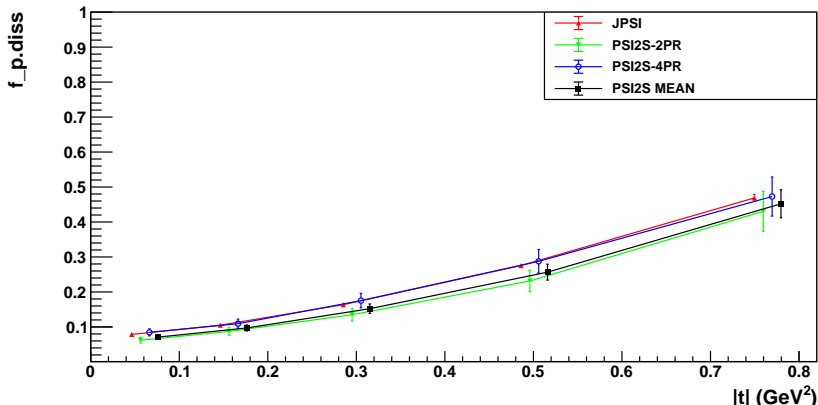
fraction  $f_{p,diss}$ : JPSI and PSI2S 2PR, 4PR vs.  $W$



- average value  $\sim 17\%$  JPSI and  $\sim 16\%$  PSI2S (mean)
- **black**: weighted mean for PSI2S 2- and 4-prong (used in analysis)
- **for R analysis: the same mean value is used for all  $W$  bins**
- no significant impact on final ratio  $R$  ( $f_{p,diss}$  fractions cancels out)

# $f_{p.diss}$ fractions in $|t|$ bins (TFF estimator)

fraction  $f_{p.diss}$ : JPSI and PSI2S 2PR, 4PR vs.  $|t|$



- compatible results for 2- and 4-prong channels
- **black**: weighted mean for PSI2S 2- and 4-prong (used in analysis)
- negligible effect on final R analysis ( $f_{p.diss}$  fractions cancels out)
- bigger impact on systematics for large  $|t|$  due to the  $b$ -slope variation !

- **Modeling of nucleon resonance states**
- (low  $M_Y$  proton dissociation)

- $\frac{d\sigma}{dM_Y^2} \sim \frac{1}{M_Y^{2(1+\epsilon)}}$  for  $M_Y^2 \geq 3.6 \text{ GeV}^2$  (continuum region)
- $\frac{d\sigma}{dM_Y^2} \sim \frac{f(M_Y^2)}{M_Y^{2(1+\epsilon)}}$  for  $M_Y^2 < 3.6 \text{ GeV}^2$  ( $p$  resonance region)
- $f(M_Y^2)$  from the **fit the the p.diss cross section on deuterium**:  
 $pD \rightarrow YD$  (Phys. Rep. **101** (3) (1983), 169)
- for  $M_Y < 1.9 \text{ GeV}$  several resonances are included  
(Pomeron carries quantum numbers of the vacuum ( $l=0, G = P = C = +$ )  
only  $N^{*+}$  states with  $J^P = \frac{1}{2}^+, \frac{3}{2}^-, \frac{5}{2}^-, \dots$ )
- $N^{*+} = N(1440), N(1520), N(1680), N(1700)$
- $N^{*+}$  decays into:  $N\pi, \Delta\pi, N\rho, N\pi\pi$  included (BR from PGD 1992)
- $N^{*+}$  decays isotropically in their rest frame
- dissociation in the continuum state carried by JETSET  
(splitting proton into  $q - qq$  system,  $q$  couples to  $\mathbb{P}$ , leaving  $qq$  spectator)

- $d\sigma \sim L_{\mu\nu} W^{\mu\nu}$

- hadron tensor:

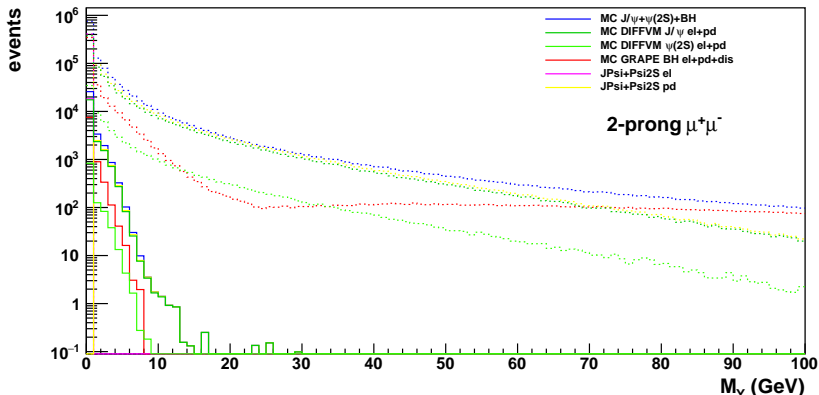
$$W^{\mu\nu} = W_1 \left( -g^{\mu\nu} + \frac{q^\mu q^\nu}{q^2} \right) + W_2 \frac{1}{M_p^2} \left( p_P^\mu - \frac{p_P \cdot q}{q^2} q^\mu \right) \left( p_P^\nu - \frac{p_P \cdot q}{q^2} q^\nu \right)$$

- $W_{1,2}(Q_p^2, M_{had})$  are proton electromagnetic structure functions
- for  $M_{had} < 2$  GeV  $W_{1,2}$  parameterized by Brasse at al. (Nucl. Phys. **B 110** (1976) 413.) (resonance region)
- for  $M_{had} > 2$  GeV  $W_{1,2}$  parameterized by ALLM97 (hep-ph/9712415) (continuum)
- both parameterizations from **fits to experimental total  $\gamma^* p$  cross sections**
- exclusive hadronic final state generated by SOPHIA
- (plus DIS di-leptons diagrams, in the framework of QPM, using PDF's)



# MC generator level: $M_Y$ before and after selection cuts

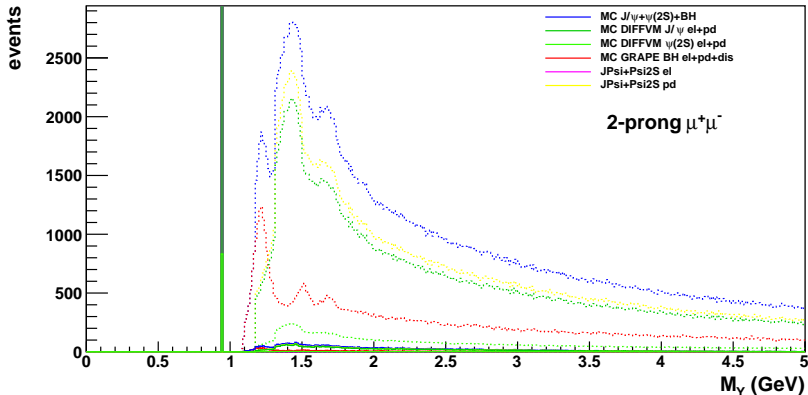
$M_Y$  gener before and after cuts



- $M_Y$  at generator level (not measured quantity !  $\rightarrow$  lost in beam-pipe)
- before and after selection cuts
- **GRAPE (BH) does include DIS scattering  $\rightarrow$  rise of xsec. for large  $M_Y$**
- DIFFVM in DIS mode generates only **electroproduction** (with proton dissociation, “rapidity gap events”)  $\rightarrow$  this is OK

# MC generator level: zoom at low $M_Y < 5$ GeV (lin scale)

$M_Y$  gener before and after cuts

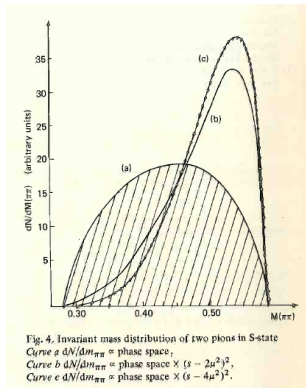


- different structure of nucleon resonances between GRAPE and DIFFVM (!?)
- which is right ?
- how much it is important for p.diss BG subtraction ?

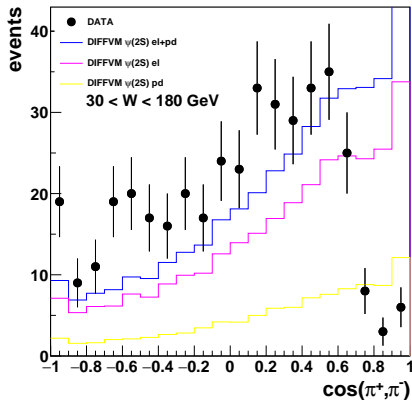
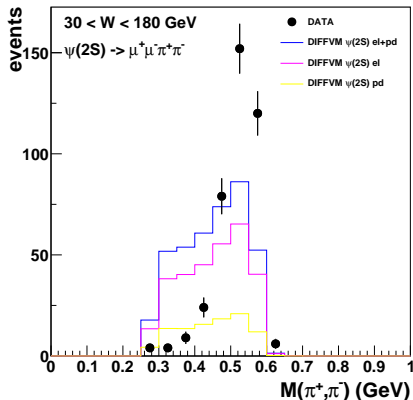
- **Pions phase space reweighting**

# Pions phase space reweighting (DIFFVM 4-prongs)

- $weight = (M(\pi^-, \pi^+)^2 - 4.0 * M_\pi^2)^2$
- ref: Phys\_Lett\_B61\_1976\_183.pdf
- final  $\pi^+\pi^-$  interaction is not in pure S-state
- → for the impact of this correction see next 2 pages

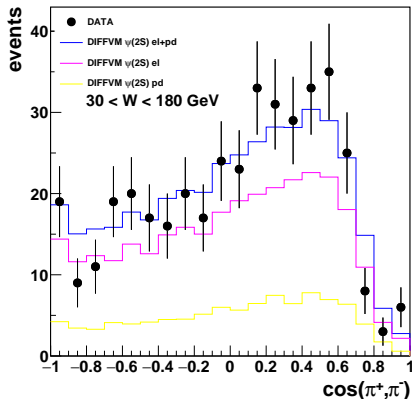
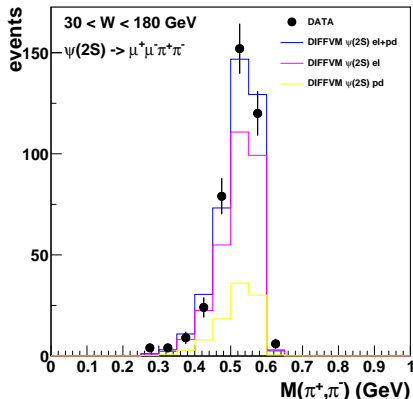


# 4-PRONGS: $M(\pi^-, \pi^+)$ , $\cos(\pi^-, \pi^+)$



- $\psi' \rightarrow J/\psi + \pi^+ \pi^-$
- $M(\pi^-, \pi^+)$ ,  $\cos(\pi^-, \pi^+)$
- DIFFVM MC **before** pions phase space reweighting

# 4-PRONGS: $M(\pi^-, \pi^+)$ , $\cos(\pi^-, \pi^+)$



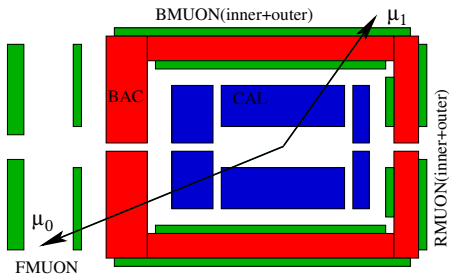
- $\psi' \rightarrow J/\psi + \pi^+ \pi^-$
- $M(\pi^-, \pi^+)$ ,  $\cos(\pi^-, \pi^+)$
- DIFFVM MC **after** pions phase space reweighting

- Muon effic. corrections

# Muon effic. corrections: TAG and PROBE

- TAG: “the triggering” muon
- PROBE: “the tested” muon
- effic in given  $(p_{t_{eff}}^j, \eta^j)$  bin:

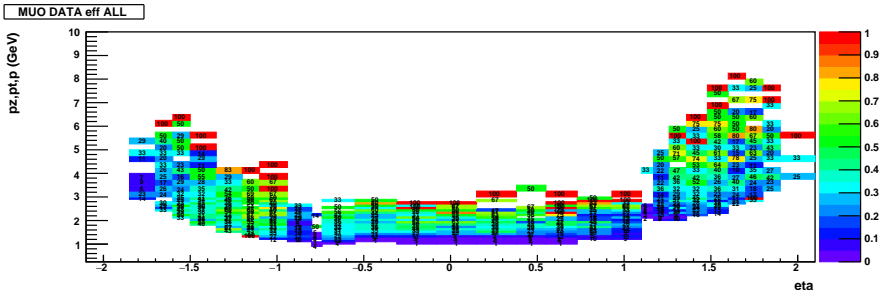
$$\epsilon = N_{PROBE}^j / N_{TAG}^i$$



- **one step correction** for (FLT and SLT and TLT and off-line REC)
- separate maps for F/B/R/MUO, BAC and CAL (off-line only)
- evaluated for single muon **in  $(p_{t_{eff}}, \eta)$  bins**, where as  $p_{t_{eff}}$  is used:  
(motivated by the CAL/BAC geometry and scaling of the muon path length)
  - $p$  in Forecap
  - $p_t$  in Barrel
  - $p_z$  in Rearcap
- proper identification of **the triggering muon** is crucial
- → the DATA/MC ratio delivers the correction weight:  $\epsilon_x = \frac{\epsilon_{DATA}}{\epsilon_{MC}}$



# Muon correction maps: ( $p_z, p_t, p$ vs. $\eta$ ) - DATA



- muon tomography
- probability (%) to fire FLT-SLT-TLT-REC chain by single muon on ( $p_z, p_t, p; \eta$ ) grid
- X-axis (along eta): Rear-MUO, Barrel-MUO, Forward-MUO detectors
- only events with  $M(\mu^+, \mu^-) < 6$  GeV  
(ie. in the phase space range of di-muon mass fits)
- current choice for  $p_z, p_t, p$  grid: 100 MeV per bin ( $p_{eff} < 3$  GeV), 250 MeV per bin ( $p_{eff} > 3$  GeV)
- size of the grid is subject to systematics