

# Investigating the Higgs self-couplings through HHH production

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**Panagiotis Stylianou**

based on 2312.04646

in collaboration with Georg Weiglein

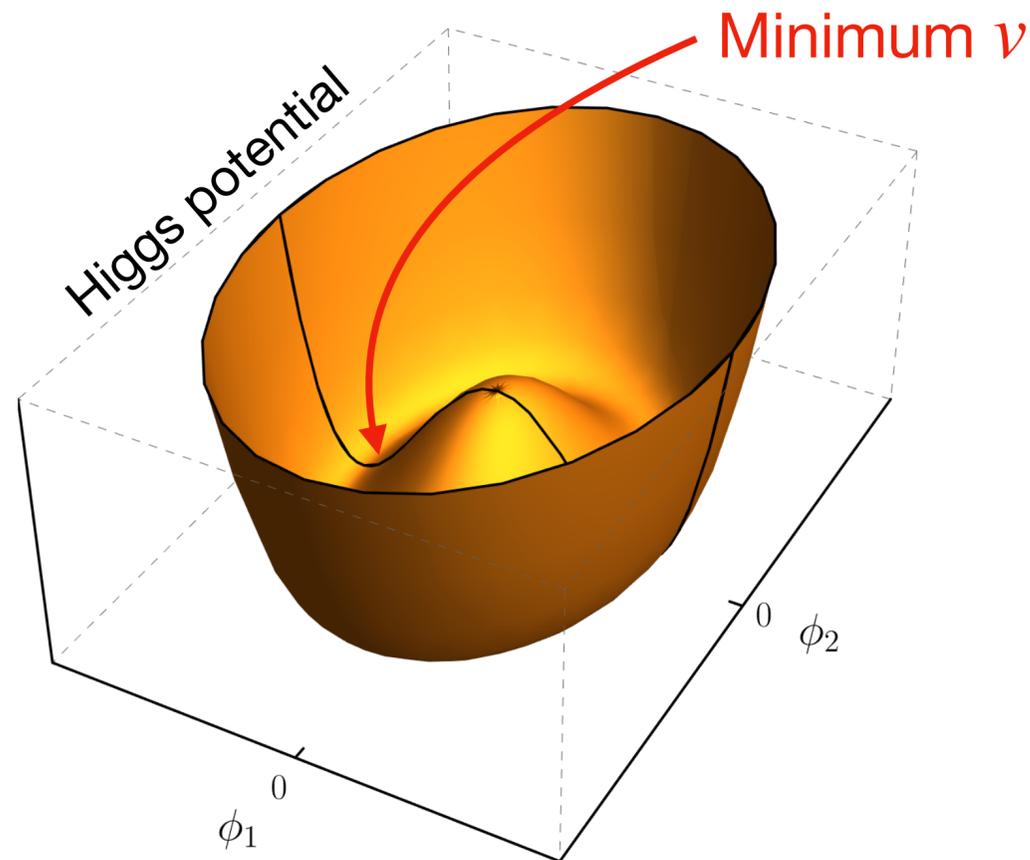


**ICHEP 2024 - Prague**

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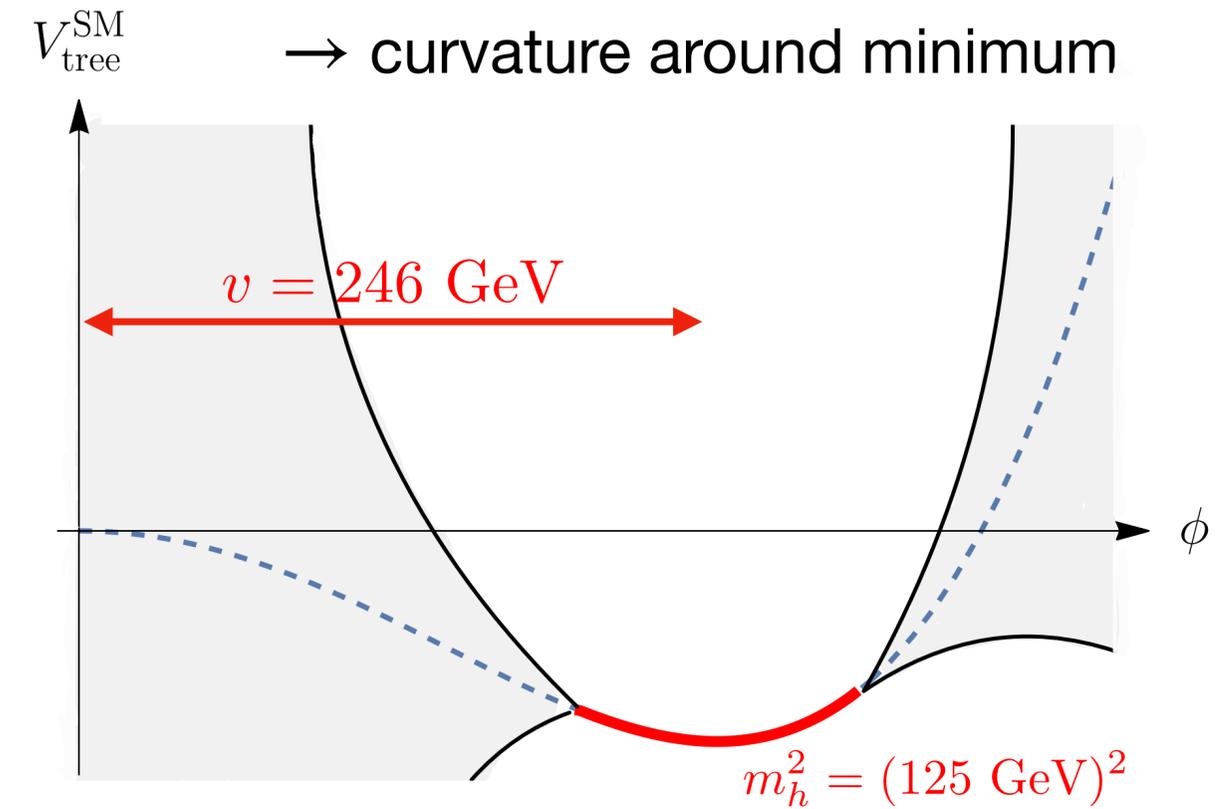
# Introduction: the Higgs potential

- Crucial questions about Electroweak Symmetry Breaking: What is the form of the Higgs potential?



So far we know:

- location of minimum
- curvature around minimum



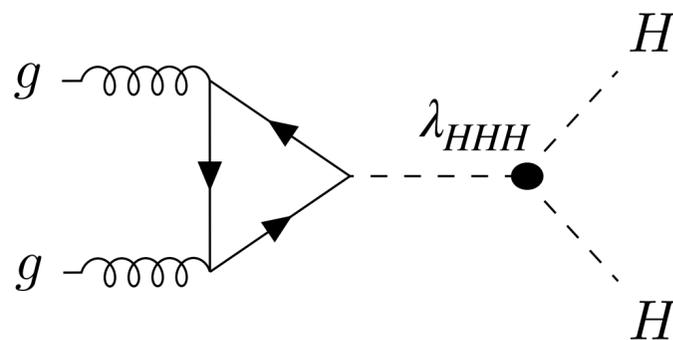
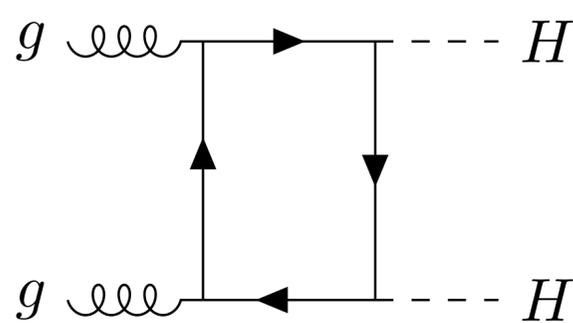
SM Potential:  $V(\Phi) = \lambda(\Phi^\dagger\Phi)^2 - \mu^2\Phi^\dagger\Phi$   
 $\supset -\lambda v H^3 - \frac{\lambda}{4} H^4$

BSM theories → more complicated shapes

Very challenging experimentally  
 requires **trilinear** and **quartic** Higgs self-couplings

# Trilinear Higgs coupling: experimental status

- Experimental bounds on signal strength from HH production:  $\mu_{HH} < 2.4$  (ATLAS)



$\lambda_{HHH}$  enters at LO order  
→ most direct probe

- Signal strength translated to limit on

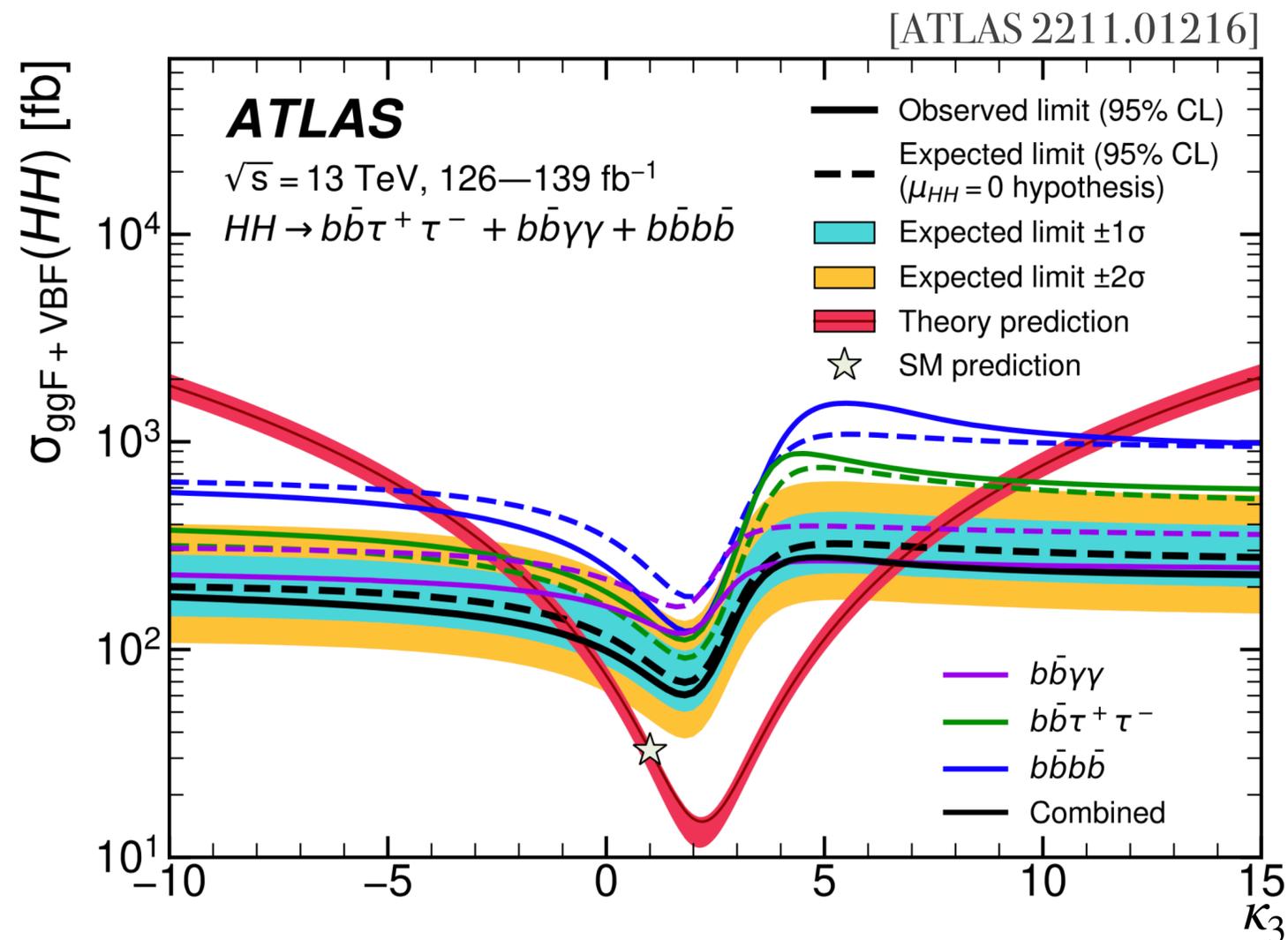
$$\kappa_3 = \frac{\lambda_{HHH}}{\lambda_{HHH}^{SM,(0)}}$$

Fixing other couplings to SM values:

**CMS:**  $[-1.2, 6.5]$   
**ATLAS:**  $[-0.4, 6.3]$  } @ 95% CL

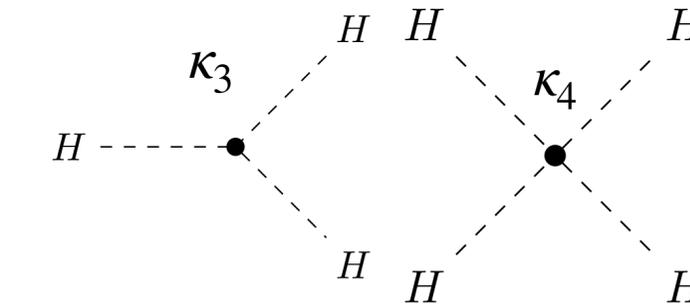
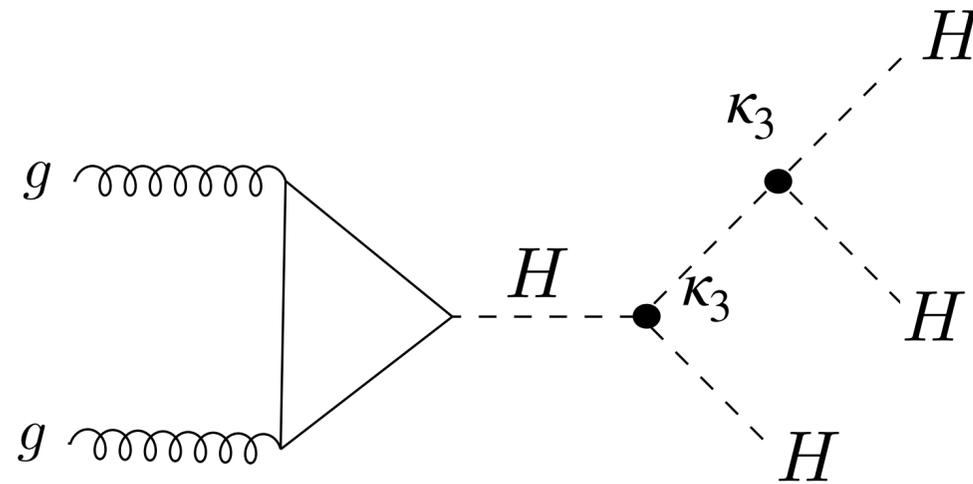
[CMS 2207.00043]  
 [ATLAS 2211.01216]

Including  
single Higgs

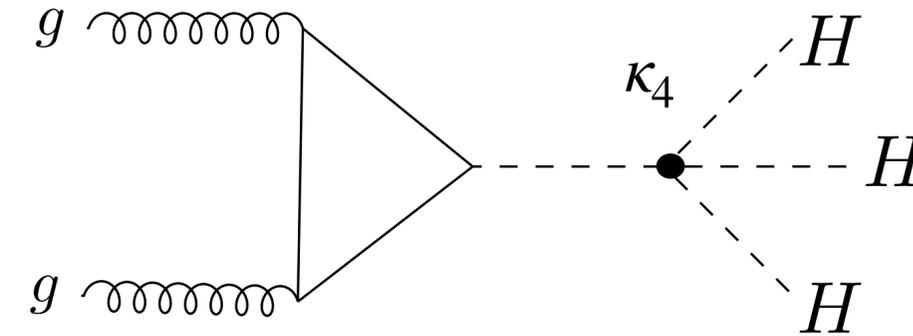


# Triple Higgs production

- Additional source of information  $\rightarrow$  HHH production
- Dependence on both trilinear  $\kappa_3$  and quartic  $\kappa_4$



early works: [Plehn, Rauch, '05]  
[Binoth, Karg, Kauer, Rückl, '06]



- Is it possible to obtain bounds on  $\kappa_3$  and  $\kappa_4$  from HHH production beyond theoretical bounds from perturbative unitarity?
- How big can deviations in  $\kappa_4$  be in BSM theories from the SM value ( $= 1$ )
- Is there potential to improve  $\kappa_3$  constraints from HH production?

# Perturbative unitarity and Higgs couplings

- Process relevant for perturbative unitarity bounds on  $\kappa_3, \kappa_4$  is  $HH \rightarrow HH$  scattering (see also [Liu et al `18])
- Jacob-Wick expansion allows to extract the zeroth partial wave:

$$a_{ii}^0 = \frac{3M_H^2 \sqrt{s^2 - 4M_H^2} s}{32\pi s(s - M_H^2)v^2} \left[ \kappa_4(s - M_H^2) - 3\kappa_3^2 M_H^2 + \frac{6\kappa_3^2 M_H^2 (s - M_H^2)}{s - 4M_H^2} \log\left(\frac{s}{M_H^2} - 3\right) \right]$$

- Tree level unitarity:

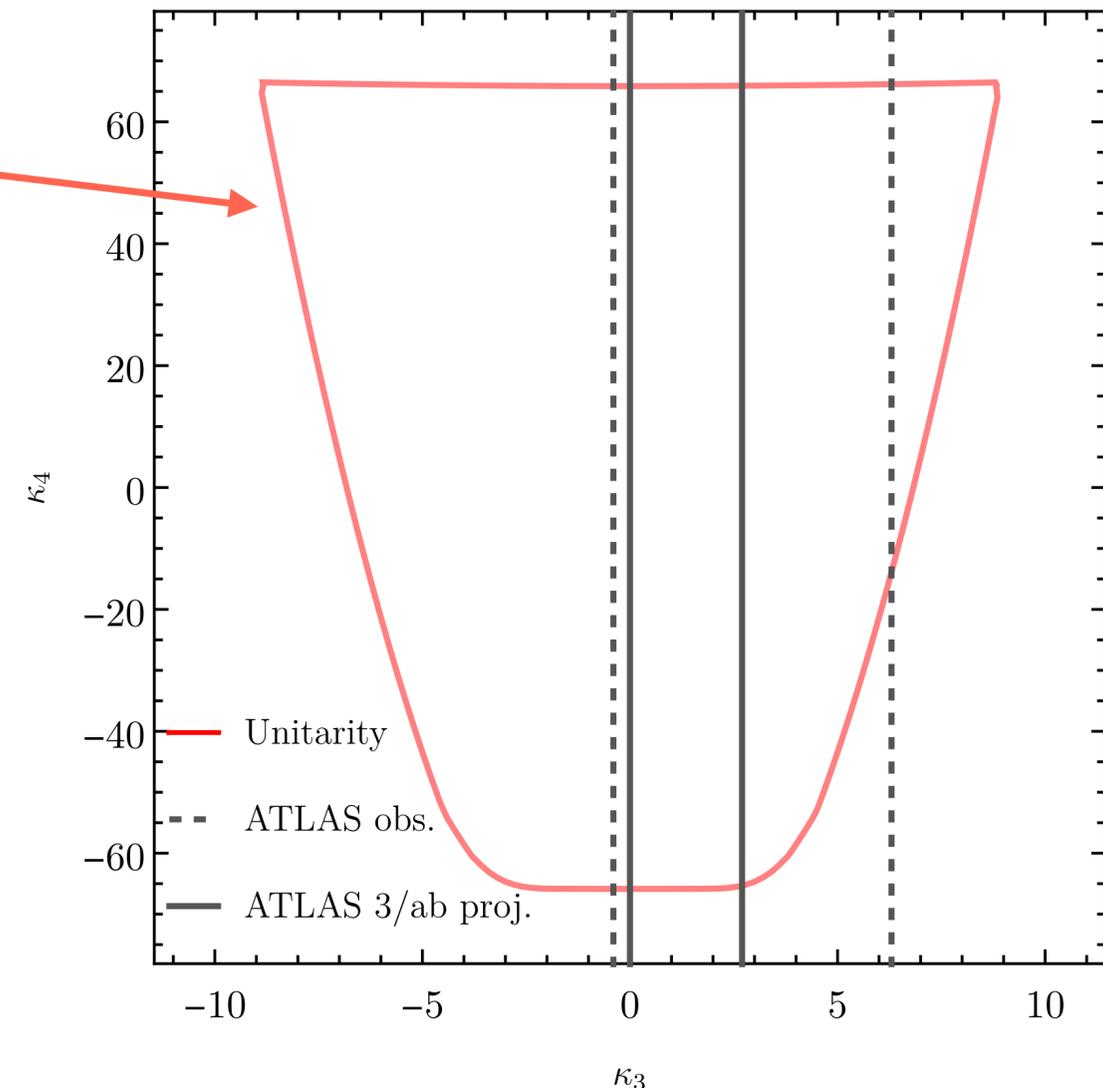
$$\text{Im} a_{ii}^0 \geq |a_{ii}^0|^2 \implies |\text{Re} a_{ii}^0| \leq \frac{1}{2}$$

95 % CL

**ATLAS current bounds:**  $[-0.4, 6.3]$

**CMS & ATLAS HH projections:**  $[0.1, 2.3]$

[ATLAS 2211.01216]  
[CERN Yellow Rep. 1902.00134]



# Extension of SM potential by operators

Linear power expansion for higher order terms in  $\Lambda^{-1}$  orders:

[Boudjema, Chopin '96]  
[Maltoni, Pagani, Zhao '18]

$$V_{\text{BSM}} = \frac{C_6}{\Lambda^2} \left( \Phi^\dagger \Phi - \frac{v^2}{2} \right)^3 + \frac{C_8}{\Lambda^4} \left( \Phi^\dagger \Phi - \frac{v^2}{2} \right)^4 + \dots$$

Contributions to  $\kappa_3, \kappa_4$ :

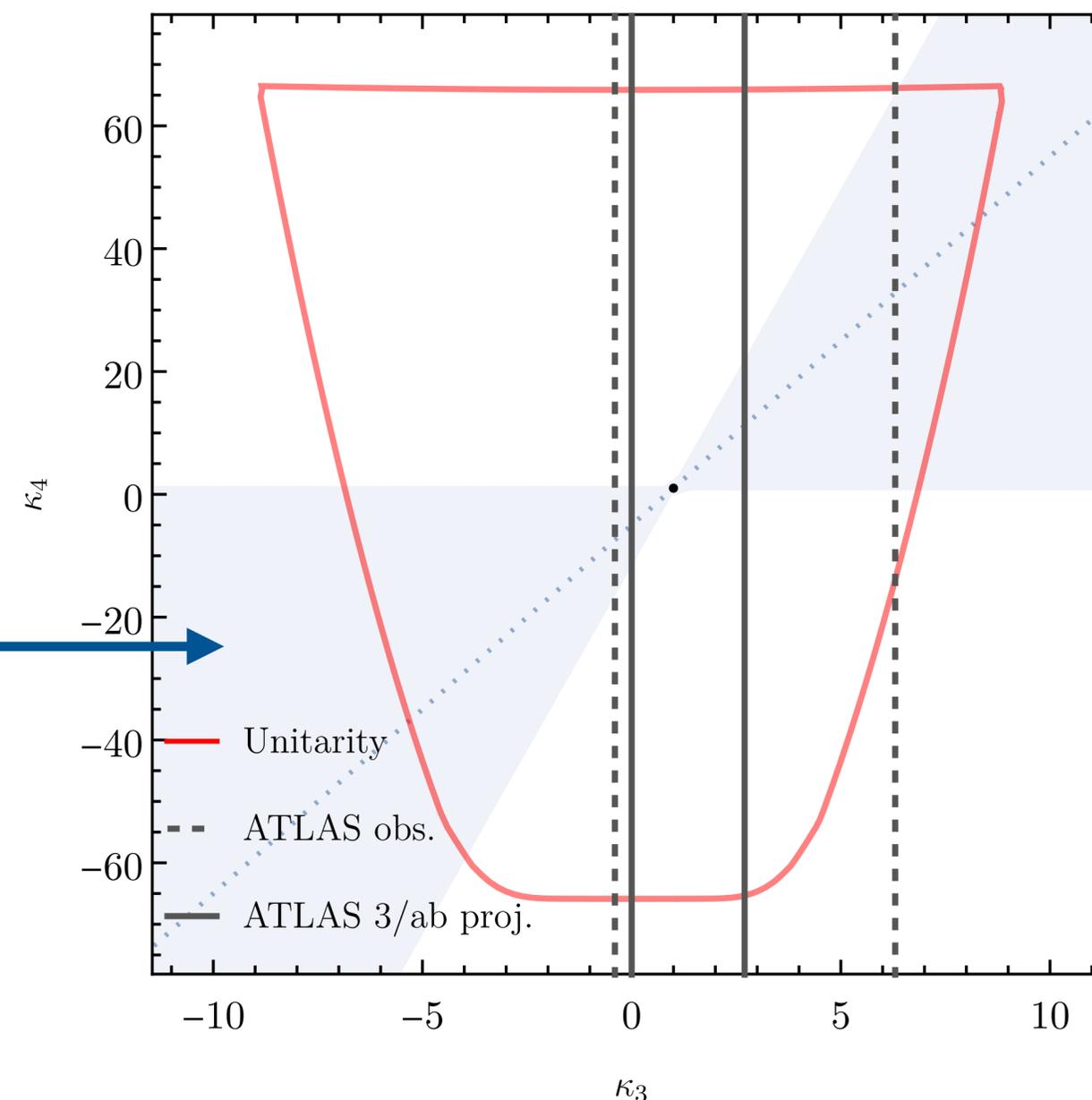
$$(\kappa_3 - 1) = \frac{C_6 v^2}{\lambda \Lambda^2},$$

$$(\kappa_4 - 1) = \frac{6C_6 v^2}{\lambda \Lambda^2} + \frac{4C_8 v^4}{\lambda \Lambda^4}$$

vanishing dimension-8  $\longrightarrow \simeq 6(\kappa_3 - 1) + \mathcal{O}\left(\frac{1}{\Lambda^4}\right)$

Shaded region:  $\frac{4C_8 v^4}{\lambda \Lambda^4} < \frac{6C_6 v^2}{\lambda \Lambda^2}$

Electroweak Chiral Lagrangian (HEFT):  
Higgs introduced as singlet and  $\kappa_3$  and  $\kappa_4$  are **free parameters**  $\rightarrow$  probes **non-linearity**



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Contributi

$$(\kappa_3 - 1) = \frac{C_6 v^2}{\lambda \Lambda^2},$$

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$$\simeq 6(\kappa_3 - 1) + \mathcal{O}\left(\frac{1}{\Lambda^4}\right)$$

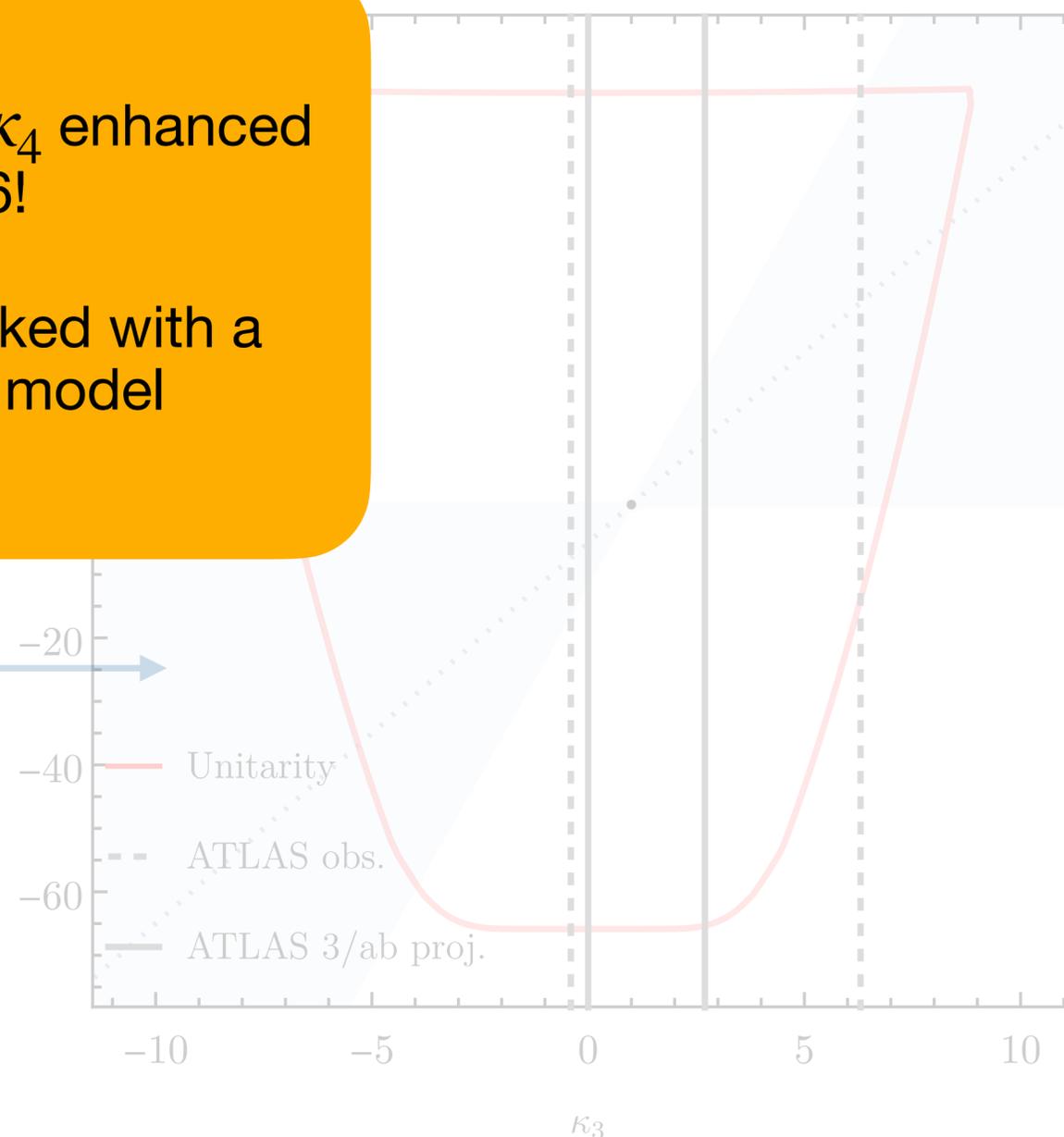
- Deviation in  $\kappa_4$  enhanced by factor of 6!
- Can be checked with a concrete UV model

vanishing dimension-8

Shaded region:

$$\frac{4C_8 v^4}{\lambda \Lambda^4} < \frac{6C_6 v^2}{\lambda \Lambda^2}$$

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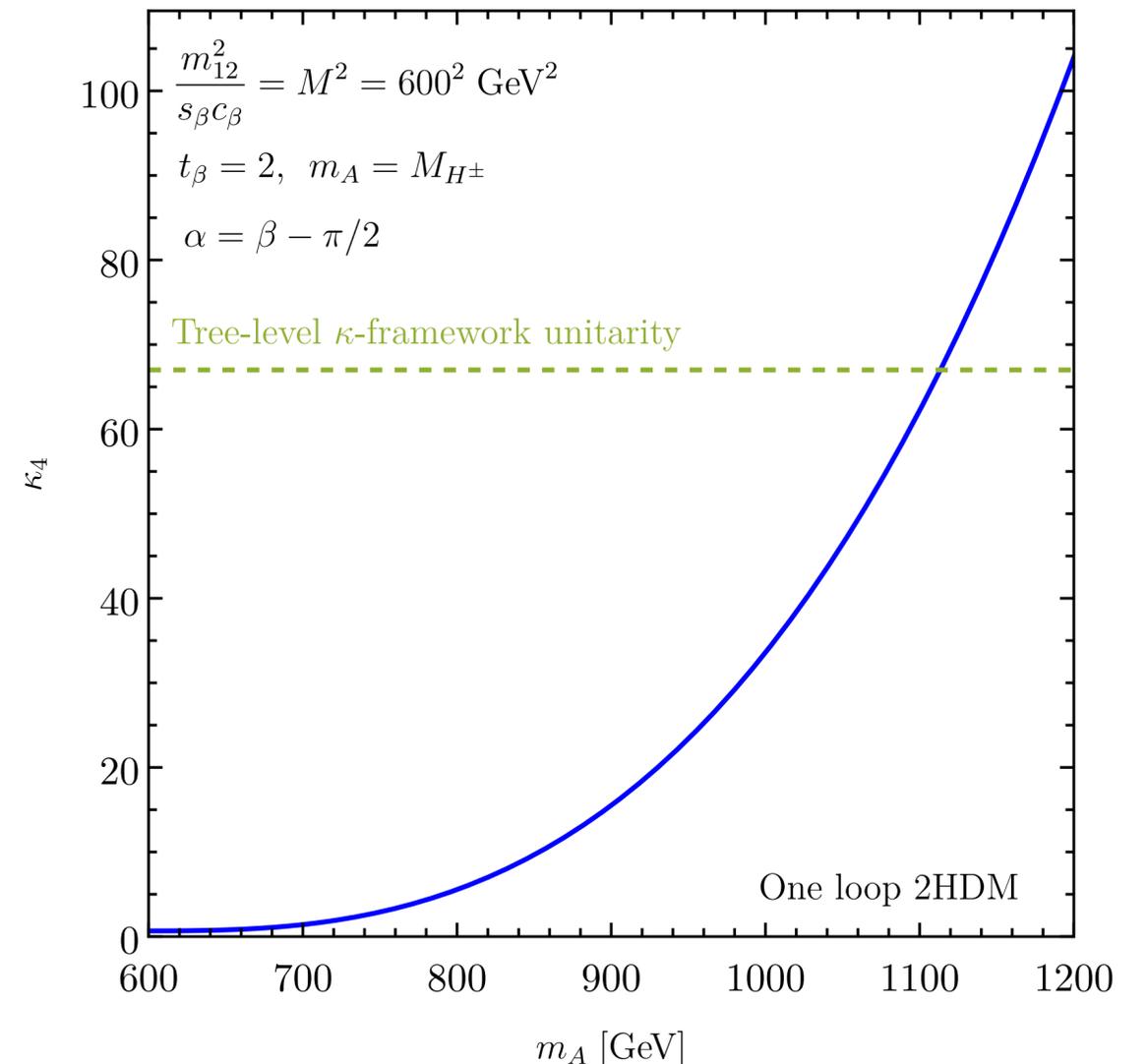
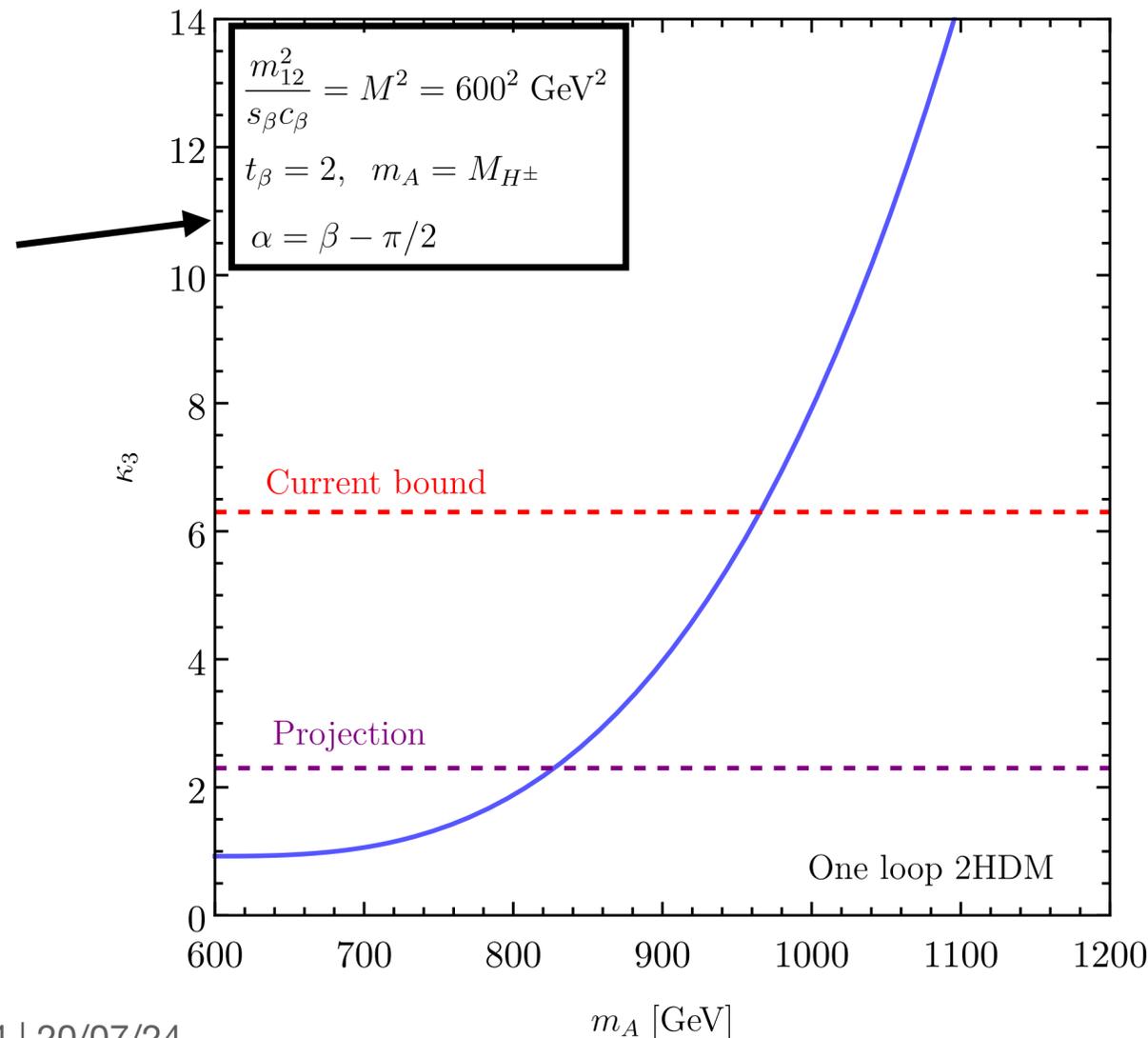
# Model example: 2HDM - trilinear vs quartic

- Consider 2HDM as an example to investigate size of  $\kappa_4$  at one-loop
- Known sizeable loop predictions for  $\kappa_3$ : [Bahl, Braathen, Weiglein '22] (up to two-loops)  
 → reproduce the one-loop result for  $\kappa_3$  but also calculate  $\kappa_4$
- Expectedly much larger deviations in  $\kappa_4$  than  $\kappa_3$

$$\kappa_i = \frac{\Gamma_i^{(0)} + \hat{\Gamma}_i^{(1)}}{\Gamma_{\text{SM},i}^{(0)}}$$

$i \in \{3H, 4H\}$

Benchmark point from [Bahl, Braathen, Weiglein '22]



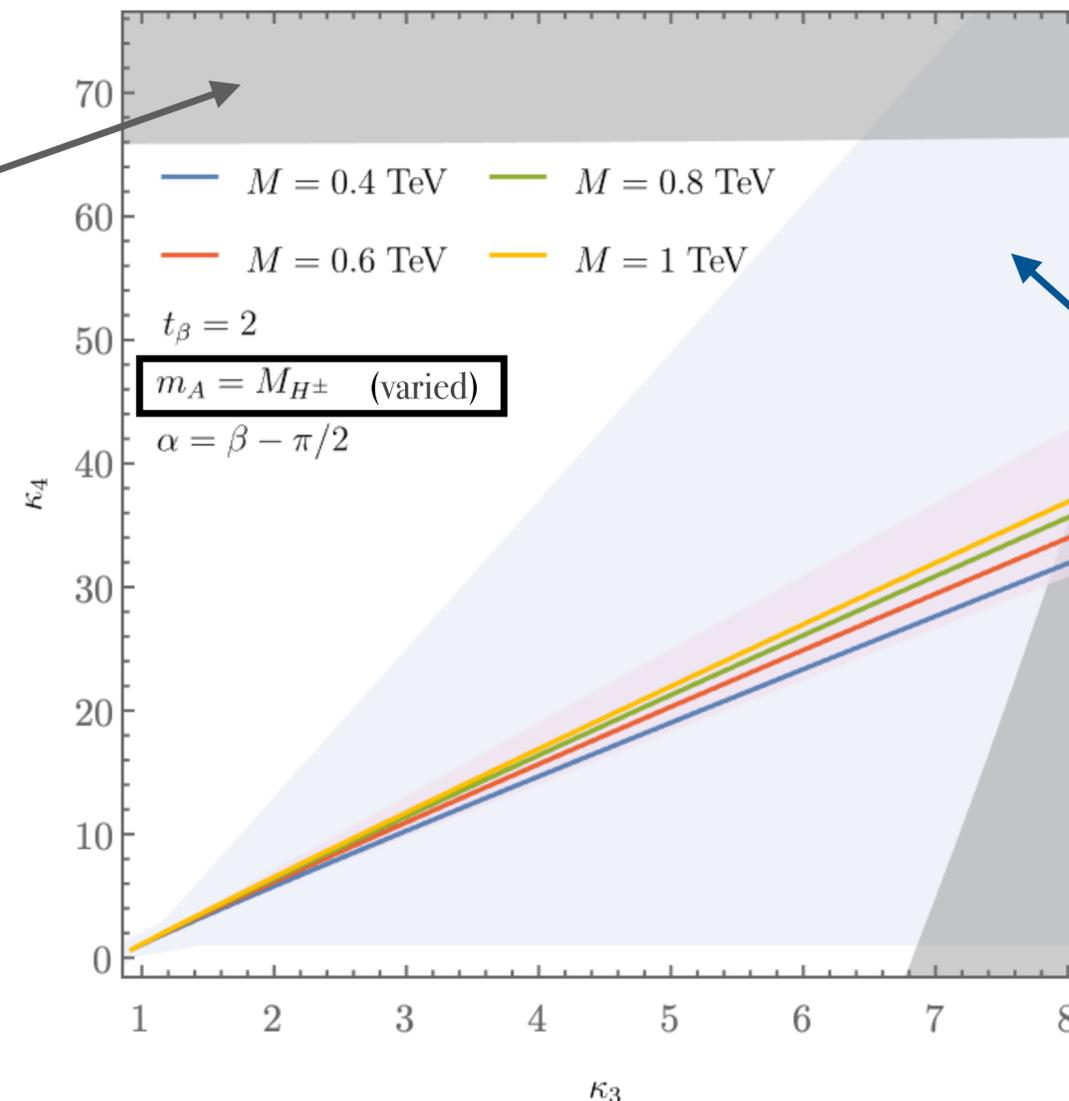
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$$\kappa_i = \frac{\Gamma_i^{(0)} + \hat{\Gamma}_i^{(1)}}{\Gamma_{\text{SM},i}^{(0)}}$$

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tree-level  $\kappa$ -framework  
perturbative unitarity



well-behaved  
perturbative  
expansion  
from before

# Prospects for the HL-LHC

- Triple Higgs production suffers from small cross sections at LHC → but potential deviations of  $\kappa_3, \kappa_4$  from SM values could yield larger rates



## Need to use dominant production & decays

- ▶ gluon fusion

- ▶ BRs:

$$\text{BR}(H \rightarrow b\bar{b}) = 0.584$$

$$\text{BR}(H \rightarrow \tau^+\tau^-) = 6.627 \times 10^{-2}$$

- Focus on  $6b$  and  $4b2\tau$  final states  $\left\{ \begin{array}{l} \text{studies at FCC energies: [Fuks, Kim, Lee `17] [Papaefstathiou, Xolocotzi, Zaro `19]} \\ 6b \text{ study going beyond self-couplings [Papaefstathiou, Xolocotzi `23]} \end{array} \right.$
- Assume at least 5 and 3 tagged  $b$ -quarks, respectively

## Included Backgrounds:

$6b$ : dominant QCD contributions (see also [Papaefstathiou, Robens, Xolocotzi `21])

$4b2\tau$ :  $W^+W^-b\bar{b}b\bar{b}$ ,  $Zb\bar{b}b\bar{b}$ ,

$t\bar{t}(H \rightarrow \tau\tau)$ ,  $t\bar{t}(H \rightarrow b\bar{b})$ ,

$t\bar{t}(Z \rightarrow \tau\tau)$ ,  $t\bar{t}(Z \rightarrow b\bar{b})$ ,  $t\bar{t}t\bar{t}$

# Event generation

- Signal and background events generated with MadGraph5\_aMC@NLO

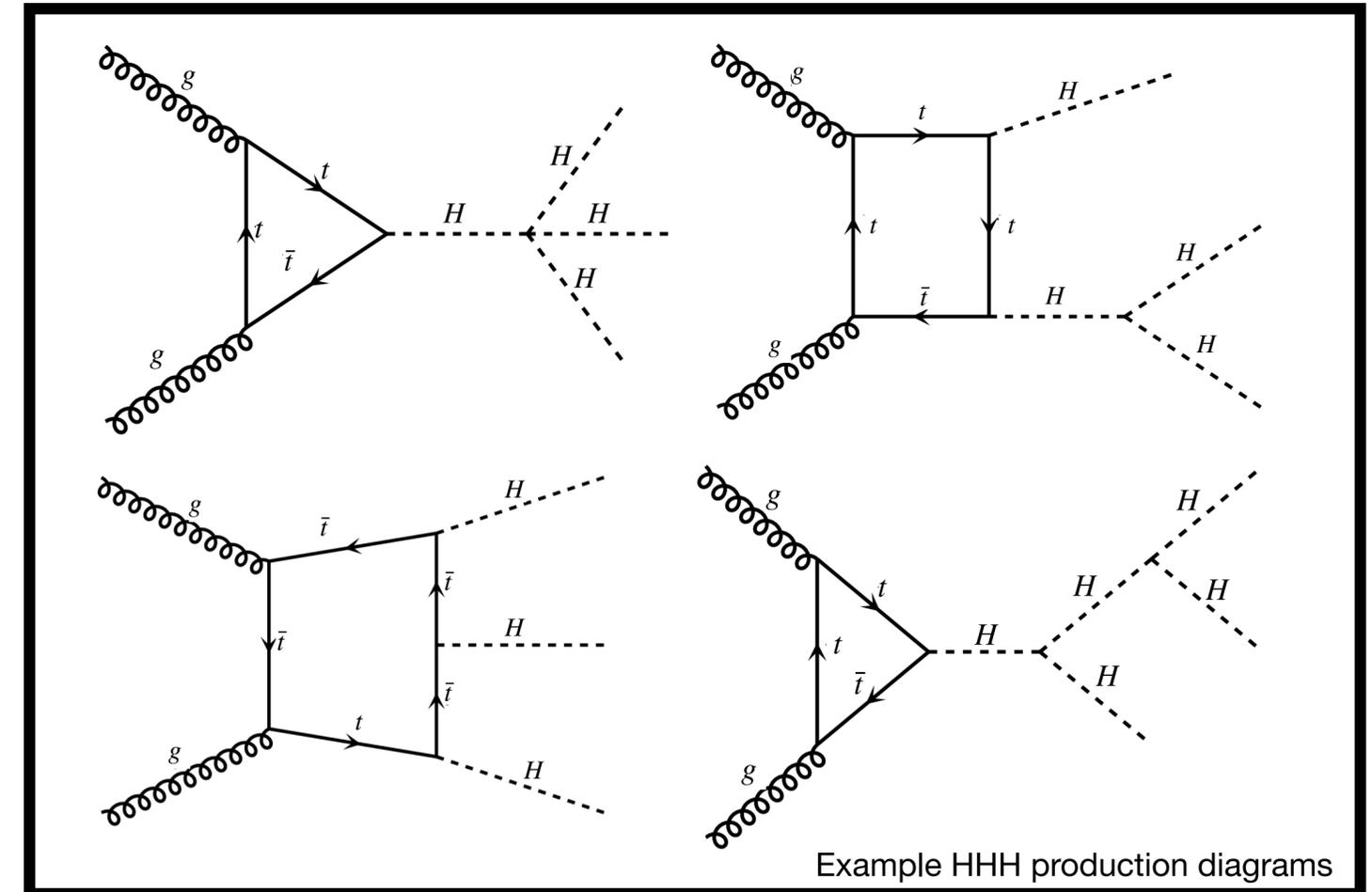
- Higgs states decayed with MadSpin

- K-factors:

- (conservative) background K-factor of 2
- signal K-factor of 1.7 [Florian, Fabre, Mazzitelli` 20]

- Utilise Graph Neural Networks (GNNs) to enhance efficiencies

- Assume flat 80% b-tagging and  $\tau$ -tagging efficiency



## Pre-selection cuts:

Invariant mass of final states:  $\gtrsim 350$  GeV

At least one pair of tagged states with

$$m_{ij} \in [110, 140]$$

$$p_T(b) > 30 \text{ GeV}$$

$$p_T(\tau) > 10 \text{ GeV}$$

$$|\eta(\tau)| < 2.5$$

$$|\eta(b)| < 2.5$$

# Signal Selection

- GNN trained on  $(\kappa_3, \kappa_4) = (1, 1)$  sample  $\longrightarrow$  Assume efficiencies same for other values of  $(\kappa_3, \kappa_4)$

- Binary classification for  $5b$  with signal region selected with cut on background score  $P[QCD] \lesssim 0.5\%$

- Multi-class classification for  $3b2\tau$ , trained on backgrounds:

$$W^+W^-b\bar{b}b\bar{b}, Zb\bar{b}b\bar{b}, t\bar{t}(H \rightarrow \tau^+\tau^-)$$

- Impose cuts on NN scores to define signal region for  $3b2\tau$ :

$$P[W^+W^-b\bar{b}b\bar{b}] < 0.03, \quad P[Zb\bar{b}b\bar{b}] < 0.1, \quad P[t\bar{t}(H \rightarrow b\bar{b})] < 0.3$$

**Significance:** 
$$Z = \sqrt{2 \left( (S + B) \ln \left( 1 + \frac{S}{B} \right) - S \right)}$$
  
from [Cowan, Cranmer, Gross, Vitells '10]

Signal & background events embedded in graphs



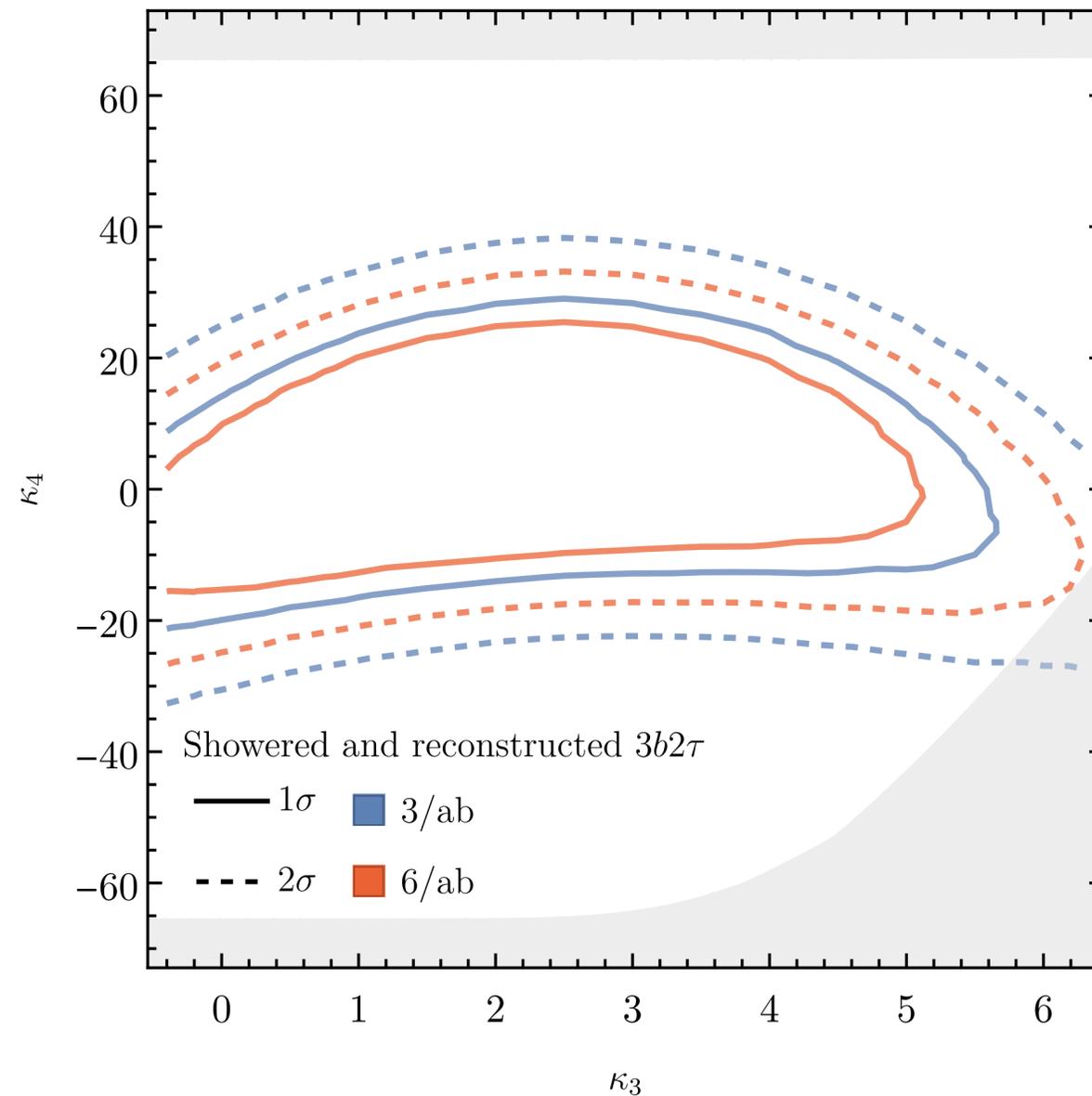
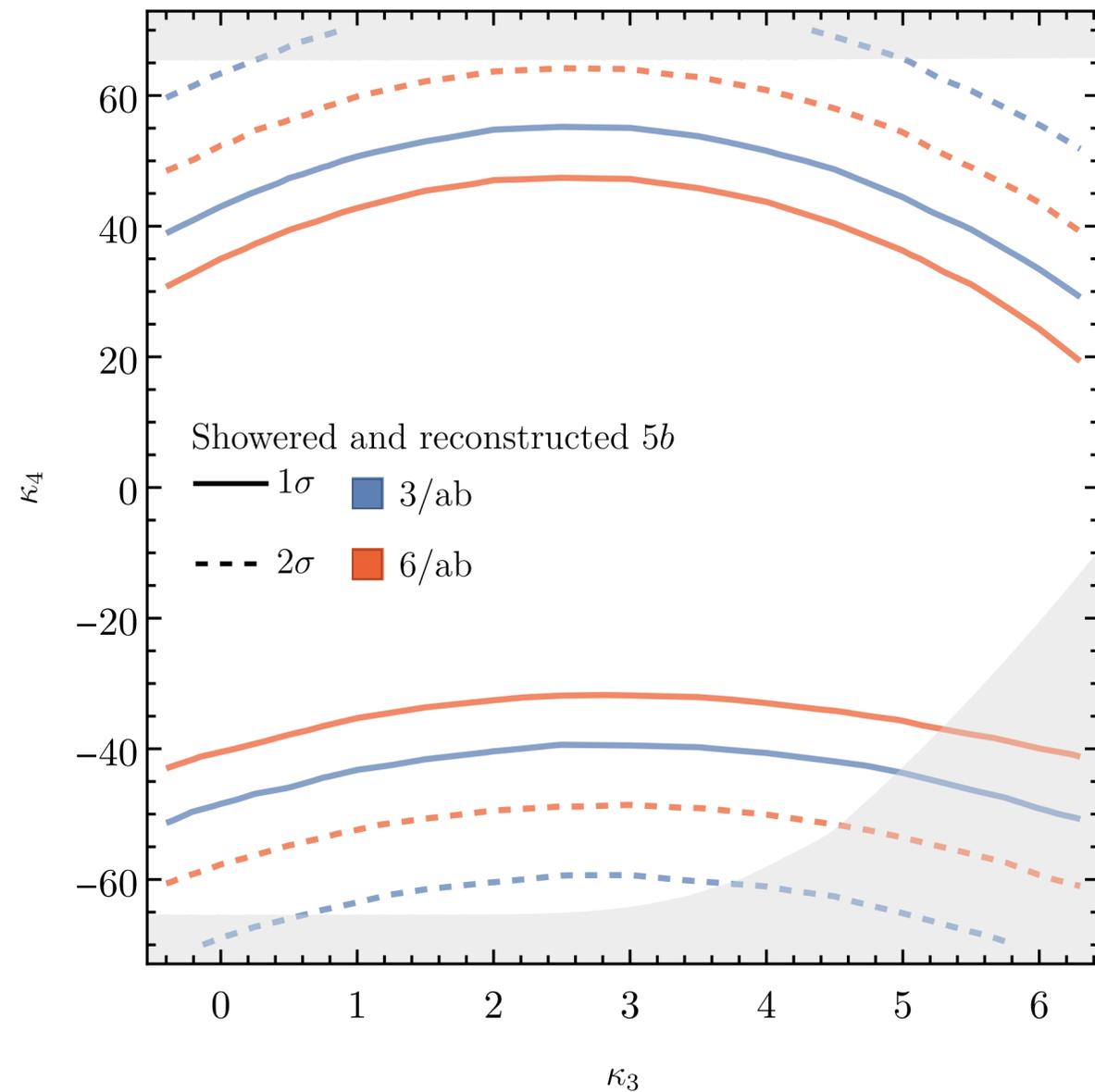
**GNN**  
2 EdgeConv layers + linear



$$\left\{ P(\mathbf{S}), P(\mathbf{B}_1), \dots, P(\mathbf{B}_N) \right\}$$

# Results

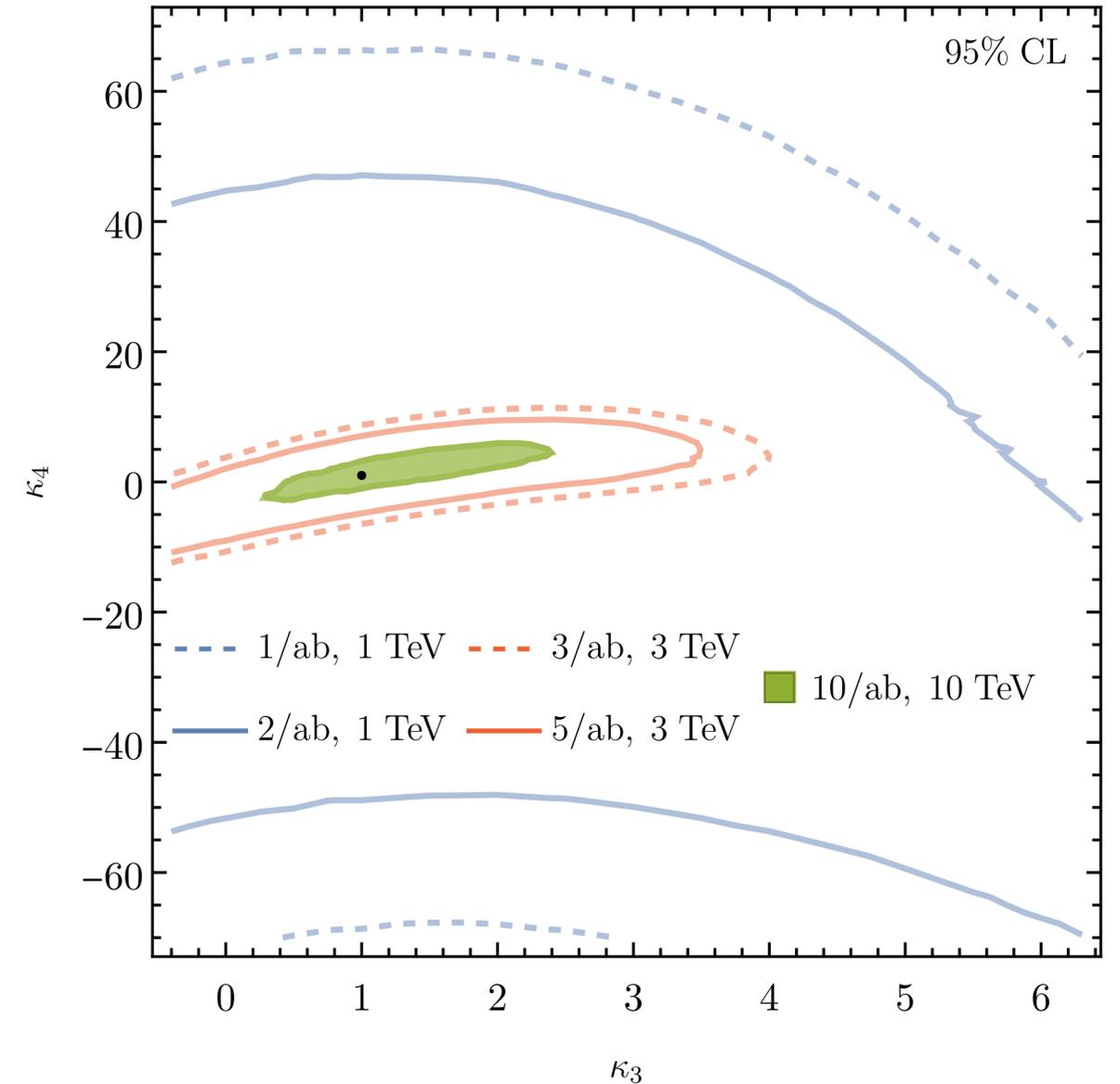
- Consider HL-LHC luminosity of  $3/\text{ab}$  and ATLAS-CMS combined luminosity of  $6/\text{ab}$
- Improved bounds on  $\kappa_4$  compared to perturbative unitarity are possible at HL-LHC



# Lepton Colliders

- How does HL-LHC perform when compared to other colliders?
- Inclusive  $\ell\ell \rightarrow HHH + X$  analysis with  $H \rightarrow b\bar{b}$
- Poissonian analysis:  $\mu_{\text{up}} = \frac{1}{2} F_{\chi^2}^{-1} \left[ 2(n + 1); \text{CL} \right]$  **Assumes no backgrounds!**
- See also previous analyses: [Maltoni, Pagani, Zhao `18]  
[Gonzalez-Lopez, Herrero, Martinez-Suarez `20] [Chiesa et al `20]

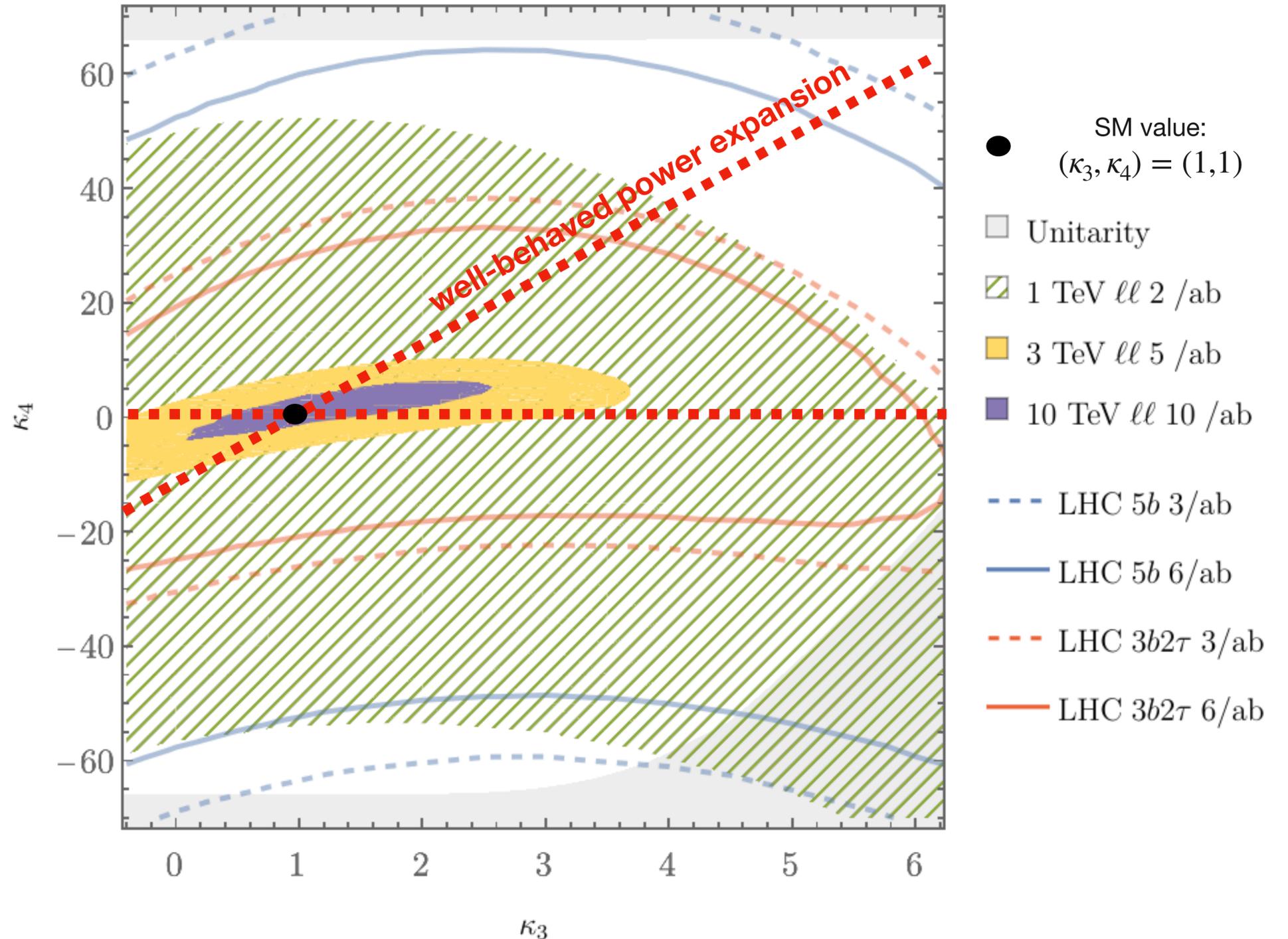
- ▶ At least 5 tagged  $b$ -quarks with  $p_T(b) > 30$  GeV
- ▶ Tagging efficiency: 80 %
- For high energies  $b$ -quarks are not only in the central part of detector  $\rightarrow$  assume extended tagging capabilities:  $|\eta| < 4$



# HL-LHC vs. future lepton colliders

- HL-LHC can provide competitive results compared to 1 TeV collider
- High energy lepton collisions way more sensitive

**BUT** such machines more comparable to FCC



# Conclusions

- Perturbative unitarity bounds for  $\kappa_4$  allow significantly larger values than  $\kappa_3$
- If there is a sizeable deviation in  $\kappa_3$ , an even larger deviation in  $\kappa_4$  is not unreasonable

- **GNNs** provide enhanced results at HL-LHC

- ▶ HL-LHC should be able to probe regions allowed by unitarity
- ▶ HHH not powerful enough to constrain  $\kappa_3$  as well as di-Higgs bounds

**BUT** can provide complementary information and be used in combination with di-Higgs

- techniques for di-Higgs can be used for triple-Higgs production
- additional channels (e.g. 4b+jets) could also be explored

- HL-LHC competitive with 1 TeV lepton colliders but higher energies more sensitive

*Thank you!*

# Backup

# Experimental constraints on $\kappa_3$

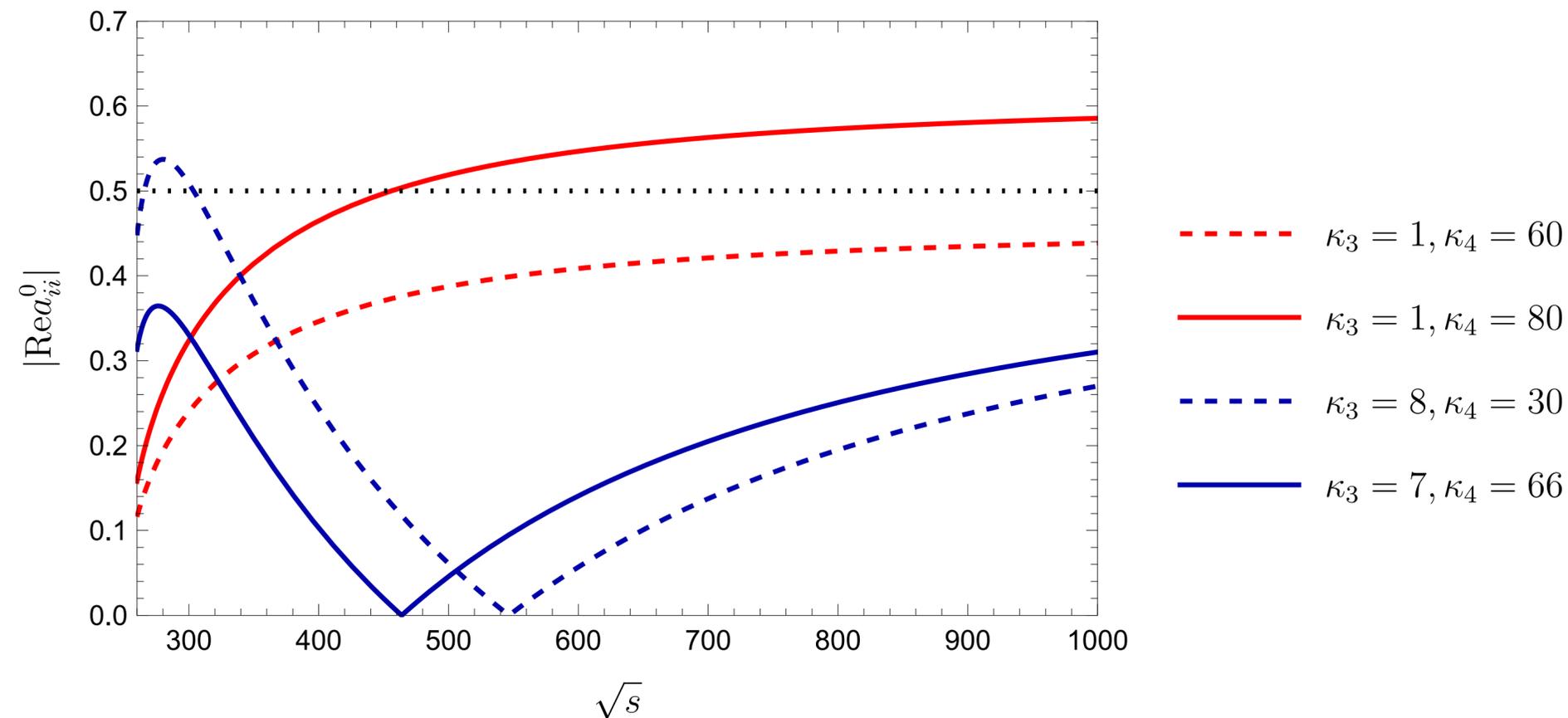
[ATLAS 2211.01216]

Combination assumption	Obs. 95% CL	Exp. 95% CL	Obs. value $^{+1\sigma}_{-1\sigma}$
<i>HH</i> combination	$-0.6 < \kappa_\lambda < 6.6$	$-2.1 < \kappa_\lambda < 7.8$	$\kappa_\lambda = 3.1^{+1.9}_{-2.0}$
Single- <i>H</i> combination	$-4.0 < \kappa_\lambda < 10.3$	$-5.2 < \kappa_\lambda < 11.5$	$\kappa_\lambda = 2.5^{+4.6}_{-3.9}$
<i>HH+H</i> combination	$-0.4 < \kappa_\lambda < 6.3$	$-1.9 < \kappa_\lambda < 7.5$	$\kappa_\lambda = 3.0^{+1.8}_{-1.9}$
<i>HH+H</i> combination, $\kappa_t$ floating	$-0.4 < \kappa_\lambda < 6.3$	$-1.9 < \kappa_\lambda < 7.6$	$\kappa_\lambda = 3.0^{+1.8}_{-1.9}$
<i>HH+H</i> combination, $\kappa_t, \kappa_V, \kappa_b, \kappa_\tau$ floating	$-1.3 < \kappa_\lambda < 6.1$	$-2.1 < \kappa_\lambda < 7.6$	$\kappa_\lambda = 2.3^{+2.1}_{-2.0}$

# Perturbative unitarity and Higgs couplings

- Process relevant for  $\kappa_3, \kappa_4$  is  $HH \rightarrow HH$  scattering (see also [Liu et al `18])
- Jacob-Wick expansion allows to extract zeroth partial wave:

$$a_{ii}^0 = \frac{3M_H^2 \sqrt{s^2 - 4M_H^2} s}{32\pi s (s - M_H^2) v^2} \left[ \kappa_4 (s - M_H^2) - 3\kappa_3^2 M_H^2 + \frac{6\kappa_3^2 M_H^2 (s - M_H^2)}{s - 4M_H^2} \log \left( \frac{s}{M_H^2} - 3 \right) \right]$$



# Two-Higgs Doublet Model (2HDM)

- Two-Higgs Doublet Model (2HDM) → a second doublet:  $\Phi_1 = \begin{pmatrix} \phi_1^+ \\ \frac{1}{\sqrt{2}}(v_1 + \rho_1 + i\eta_1) \end{pmatrix}, \Phi_2 = \begin{pmatrix} \phi_2^+ \\ \frac{1}{\sqrt{2}}(v_2 + \rho_2 + i\eta_2) \end{pmatrix}$

$$V_{2\text{HDM}} = m_{11}^2(\Phi_1^\dagger\Phi_1) + m_{22}^2(\Phi_2^\dagger\Phi_2) - m_{12}^2(\Phi_1^\dagger\Phi_2 + \Phi_2^\dagger\Phi_1) + \frac{\lambda_1}{2}(\Phi_1^\dagger\Phi_1)^2 + \frac{\lambda_2}{2}(\Phi_2^\dagger\Phi_2)^2 + \lambda_3(\Phi_1^\dagger\Phi_1)(\Phi_2^\dagger\Phi_2) + \lambda_4(\Phi_1^\dagger\Phi_2)(\Phi_2^\dagger\Phi_1) + \frac{\lambda_5}{2} \left( (\Phi_1^\dagger\Phi_2)^2 + (\Phi_2^\dagger\Phi_1)^2 \right)$$

- Free parameters:  $m_H, m_{H'}, m_A, m_{H^\pm}, m_{12}^2, v, \cos(\beta - \alpha), \tan \beta$

Scalar Particle content:

Neutral scalars:  $H', H(m_H = 125 \text{ GeV})$

Neutral pseudoscalars:  $A$

Charged scalars:  $H^\pm$

Alignment limit → couplings of light Higgs same as SM  
 $\cos(\beta - \alpha) = 0$

# Model example: 2HDM - calculation

- 1-loop calculation for  $\kappa_3, \kappa_4$  with FeynArts, FormCalc, LoopTools in alignment limit

$$\hat{\Gamma}_{3H}^{(1)} = \left[ \begin{array}{c} H \text{---} \text{---} H \\ \text{---} \text{---} H \\ \text{---} \text{---} H \end{array} \text{ (loop) } + \begin{array}{c} H \text{---} \text{---} H \\ \text{---} \text{---} H \\ \text{---} \text{---} H \end{array} \text{ (loop) } \right] \text{zero momenta}$$

- 2HDM renormalisation constants calculated with on-shell conditions
- divergence cancellation checked analytically

$$\Gamma_{3H}^{\text{CT}} = -\frac{3}{v} \left[ \delta M_H^2 + \frac{\delta T_H}{v} + M_H^2 \left( \delta Z_e + \frac{3}{2} \delta Z_H - \frac{\delta M_W^2}{2M_W^2} - \frac{\delta s_W}{s_W} \right) \right]$$

$$\Gamma_{4H}^{\text{CT}} = -\frac{3}{v^2} \left[ \delta M_H^2 + \frac{\delta T_H}{v} + 2M_H^2 \left( \delta Z_e + \delta Z_H - \frac{\delta M_W^2}{2M_W^2} - \frac{\delta s_W}{s_W} \right) \right]$$

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# Edge Convolution

Input features:  $\vec{x}_i^{(0)}$  → update iteratively with **Edge Convolution** operation:

## Edge Convolution operation

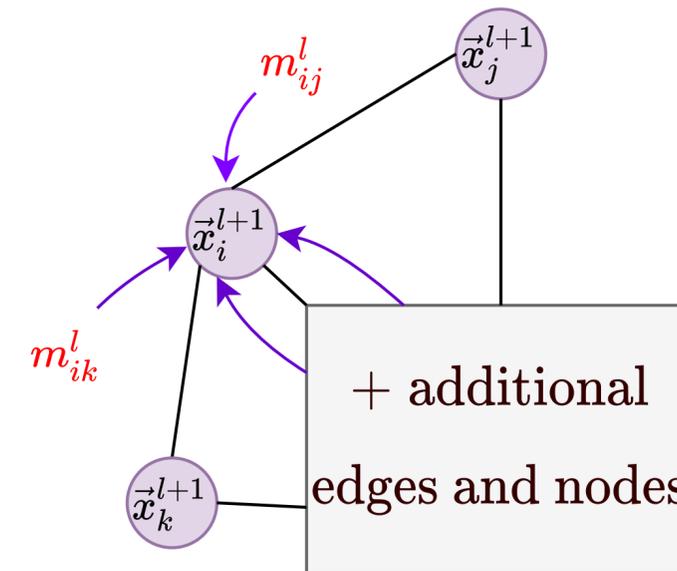
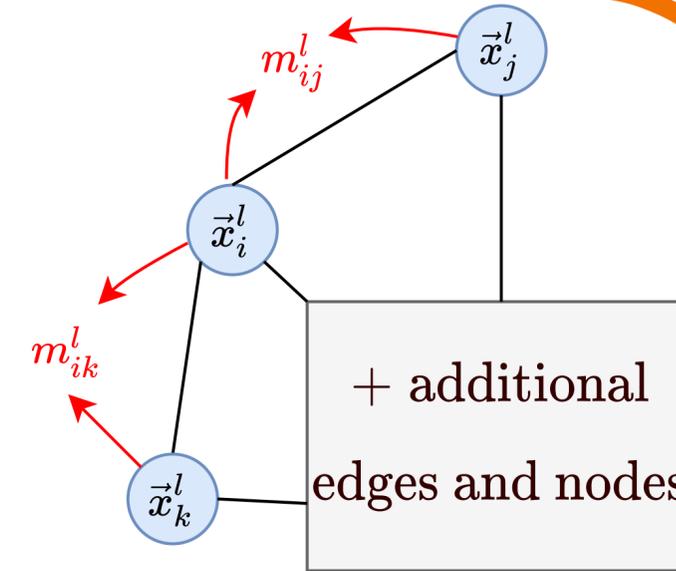
'Message' calculation:

$$m_{ij}^{(l)} = \text{RELU} \left( \Theta(\vec{x}_j^{(l)} - \vec{x}_i^{(l)}) + \Phi(\vec{x}_i^{(l)}) \right)$$

linear layers

Aggregation: update node features

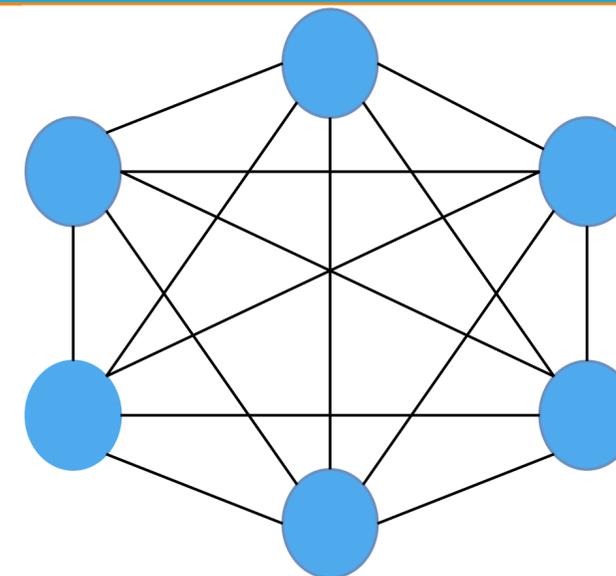
$$\vec{x}_i^{(l+1)} = \frac{1}{|\mathcal{N}(i)|} \sum_{j \in \mathcal{N}(i)} m_{ij}^{(l)}$$



# Graph Embedding

1.

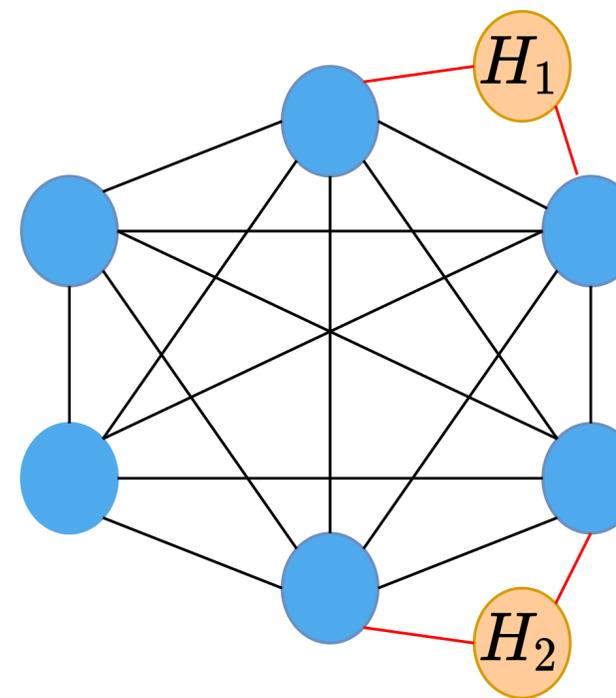
- Fully-connected nodes for  $b$  and  $\tau$  final states
- **Input features:**  $[p_T, \eta, \phi, E, m, \text{PDGID}]$
- Additional node for Missing Transverse Momentum (MTM) in showered & reconstructed events



FC: Fully-Connected

2.

- Consider combinations of  $b$ -quarks and  $\tau$  with reconstructed four-momentum  $(p_i + p_j)$
- If  $m_{ij} \in [100, 150]$  (GeV) add extra node  $H_i$

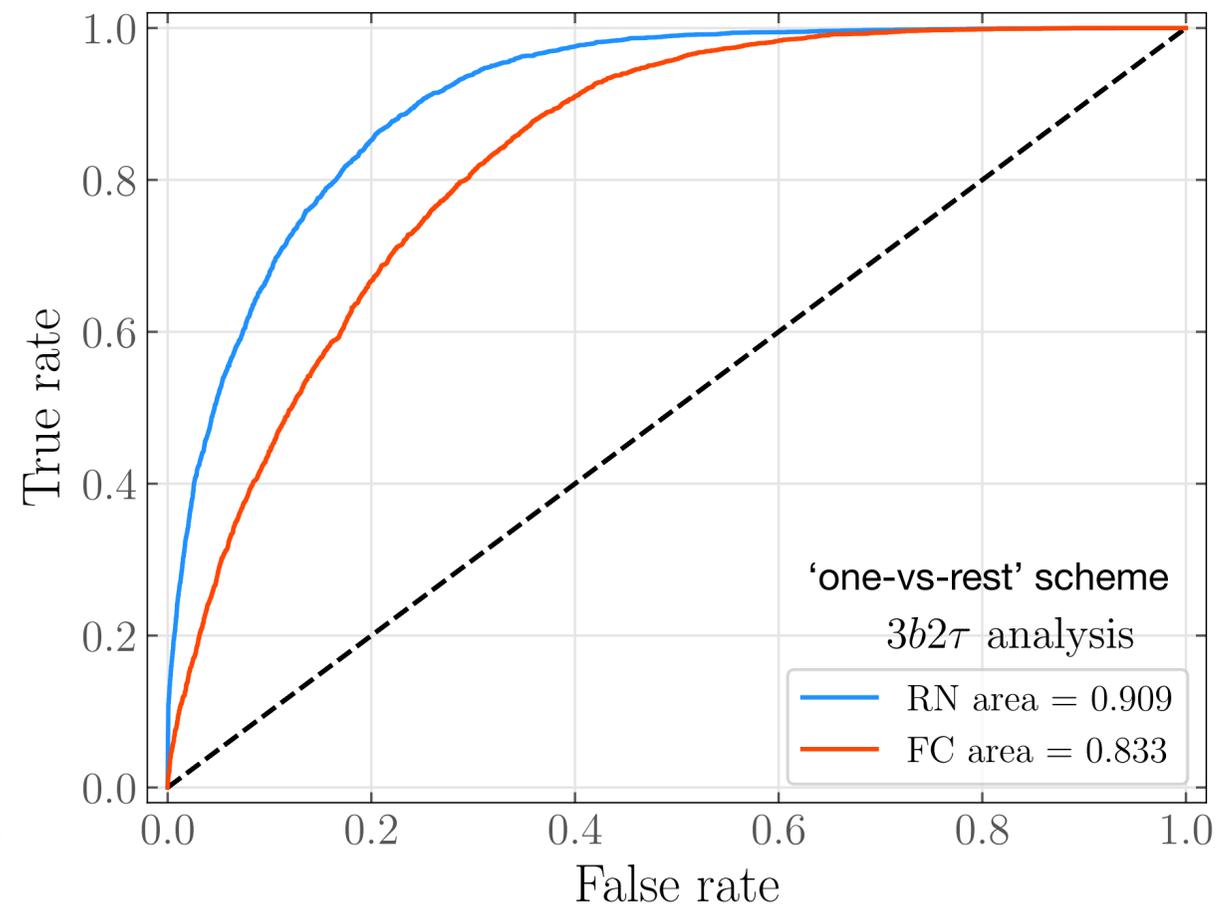
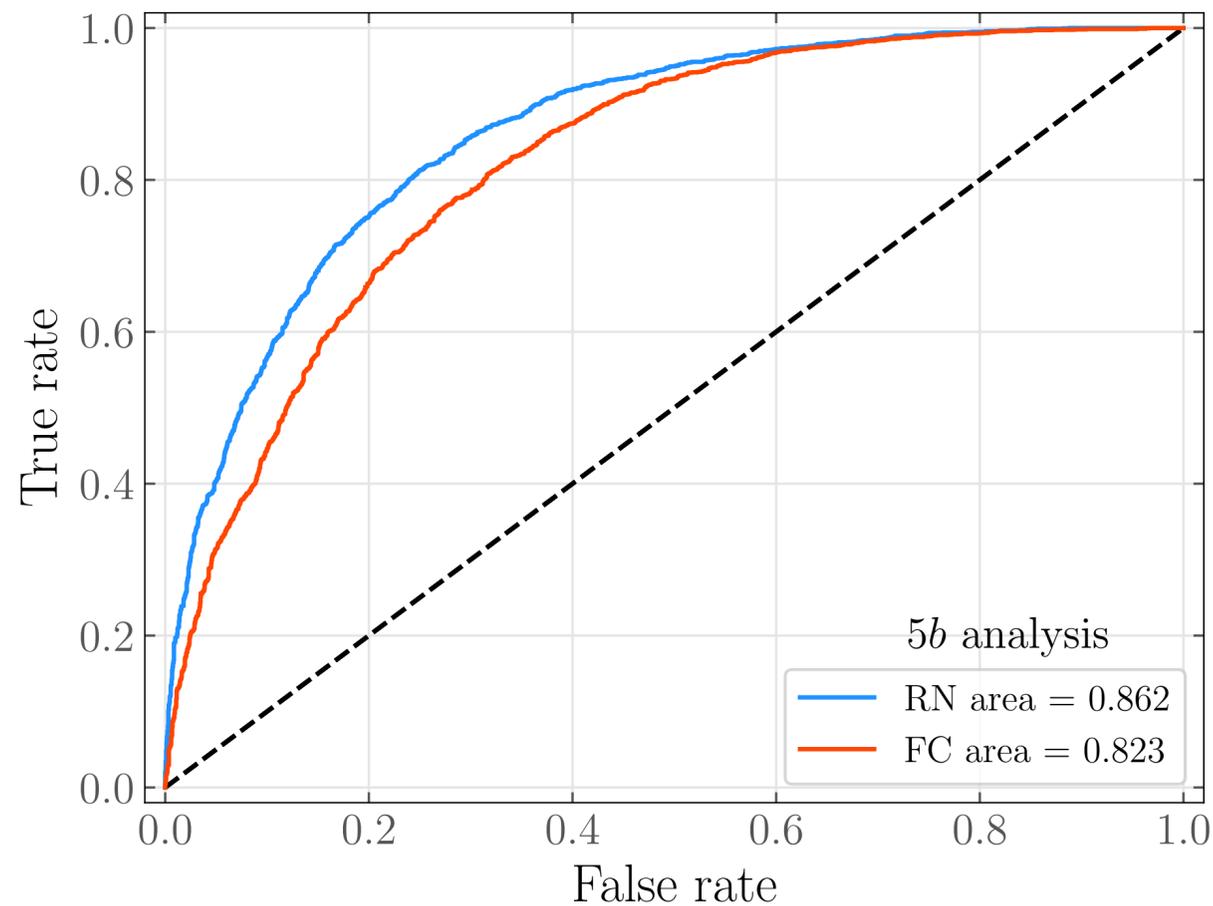


RN: Reconstructed Nodes

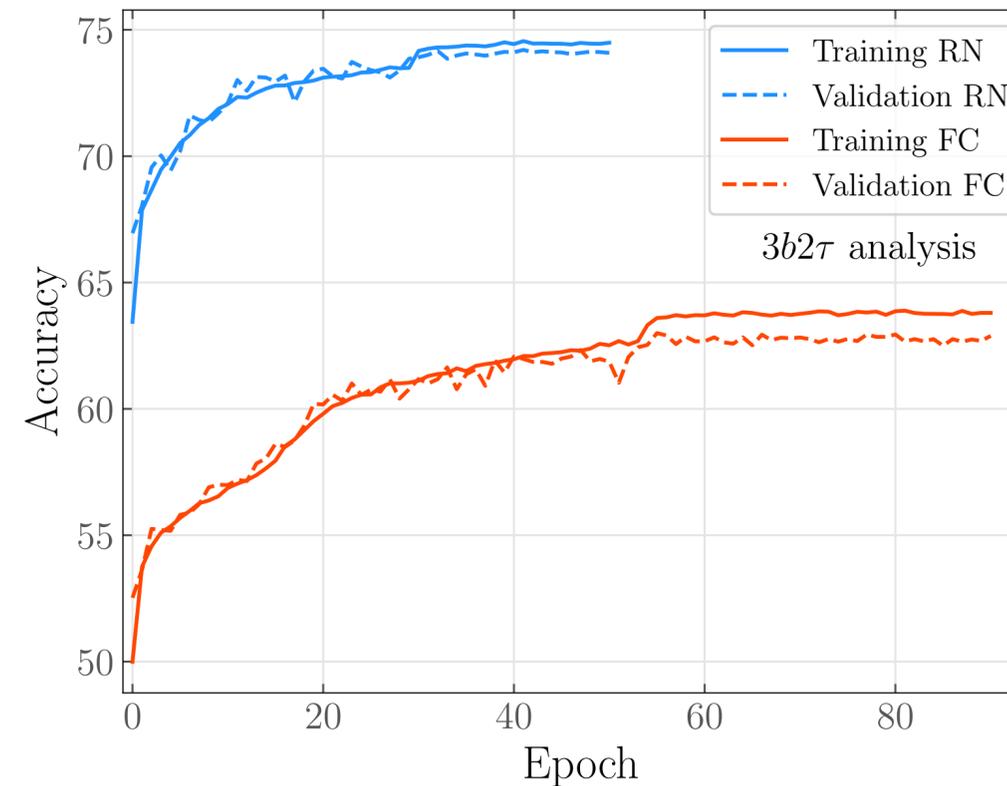
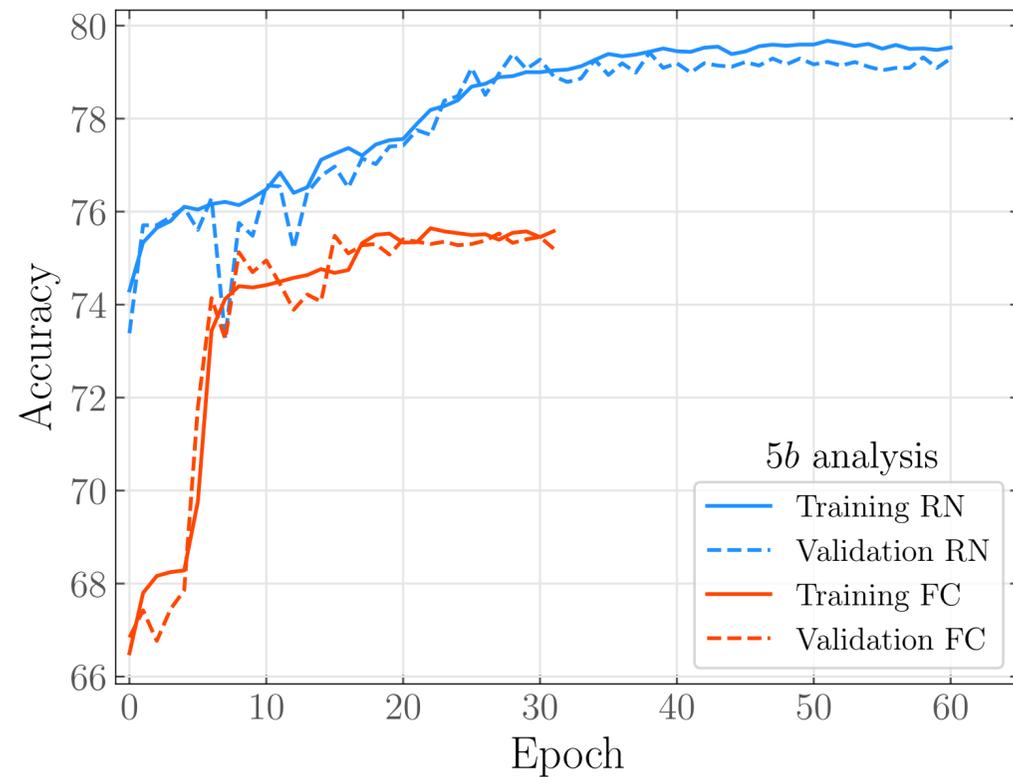
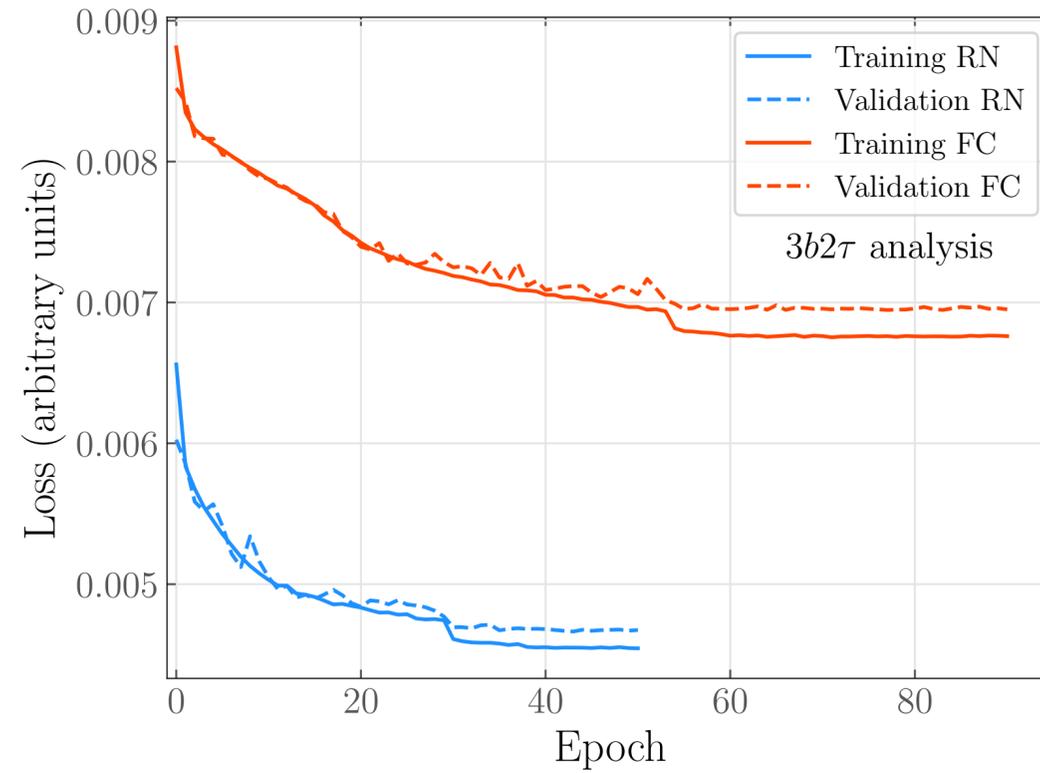
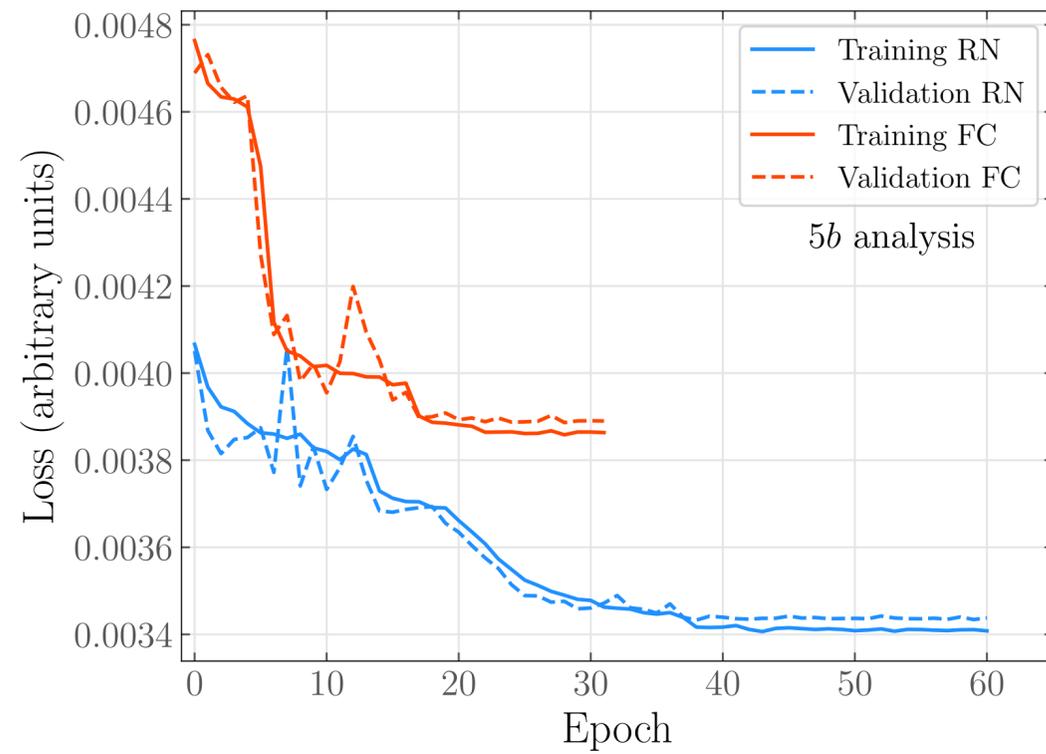
# Embedding performance



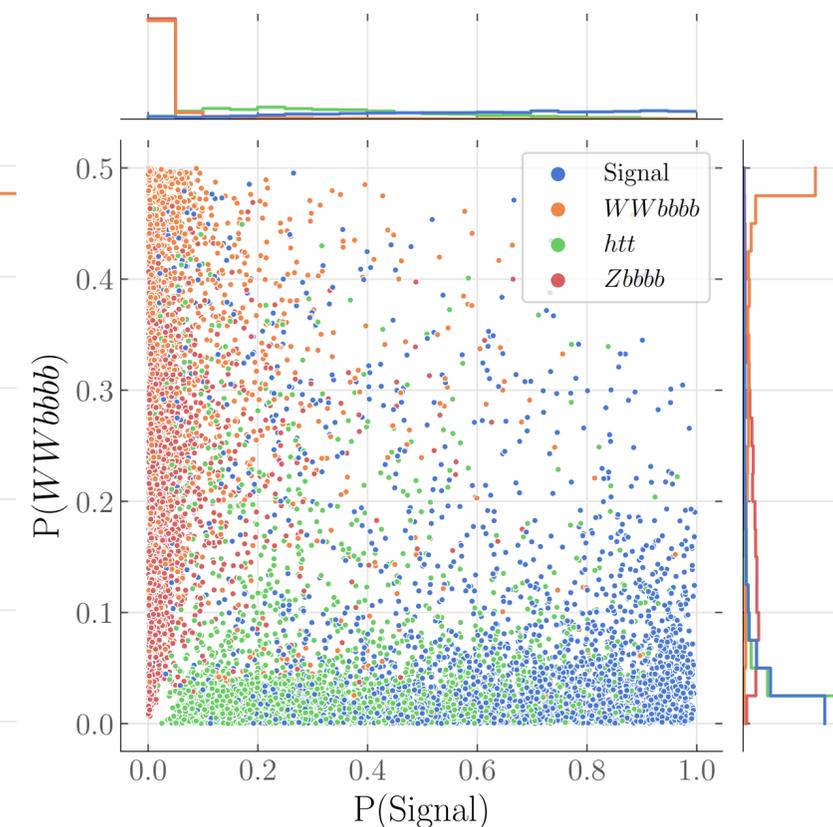
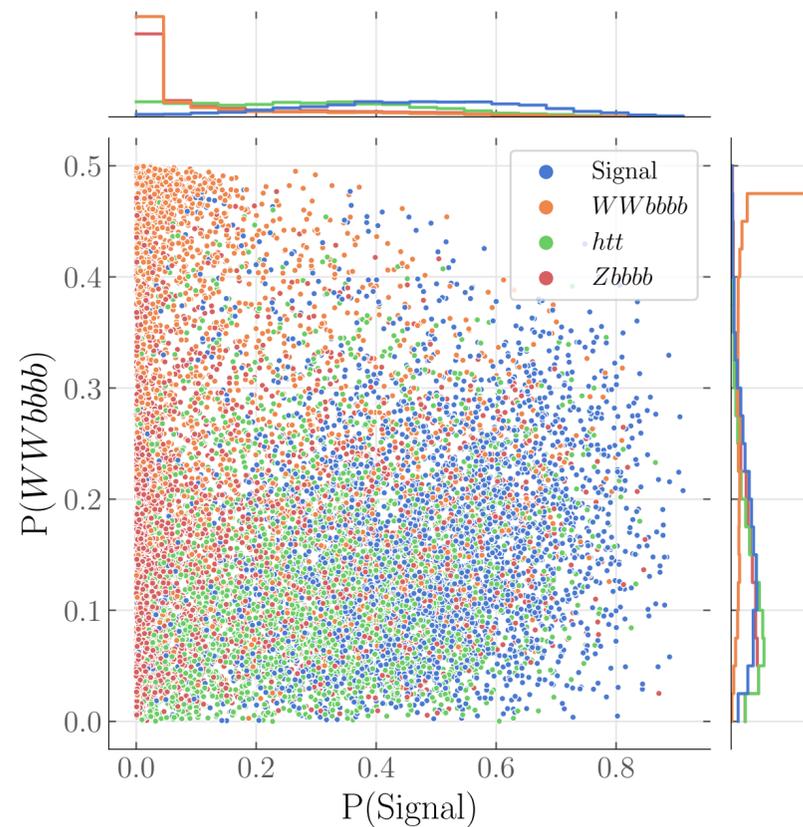
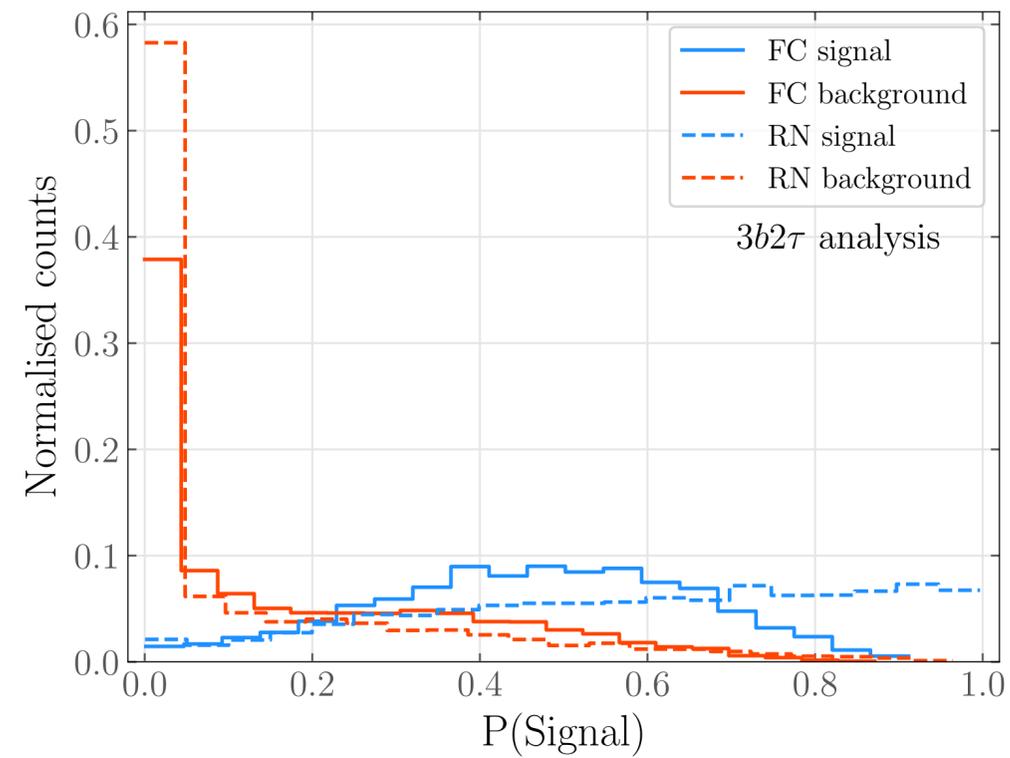
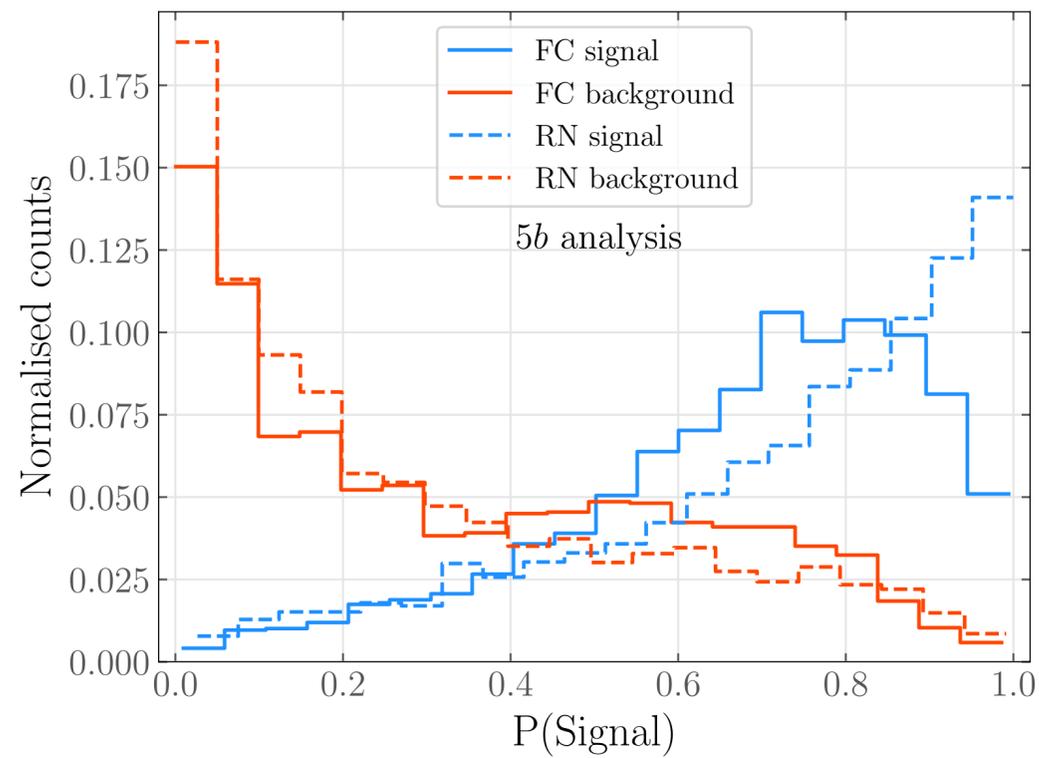
- GNN trained on  $(\kappa_3, \kappa_4) = (1,1)$  sample
- Evaluate performance with Receiver Operating Characteristic (ROC) curves



# Training loss and accuracy



# Score distributions



# Cutflow $3b2\tau$

- Binary classification for  $5b$  with signal region selected with cut on background score  $P[QCD] \lesssim 0.5\%$

- Multi-class classification for  $3b2\tau$ , trained on backgrounds:

$$W^+W^-b\bar{b}b\bar{b}, Zb\bar{b}b\bar{b}, t\bar{t}(H \rightarrow \tau^+\tau^-)$$

- Impose cuts on NN scores to define signal region:

$$P[W^+W^-b\bar{b}b\bar{b}] < 0.03, \quad P[Zb\bar{b}b\bar{b}] < 0.1, \quad P[t\bar{t}(H \rightarrow b\bar{b})] < 0.3$$

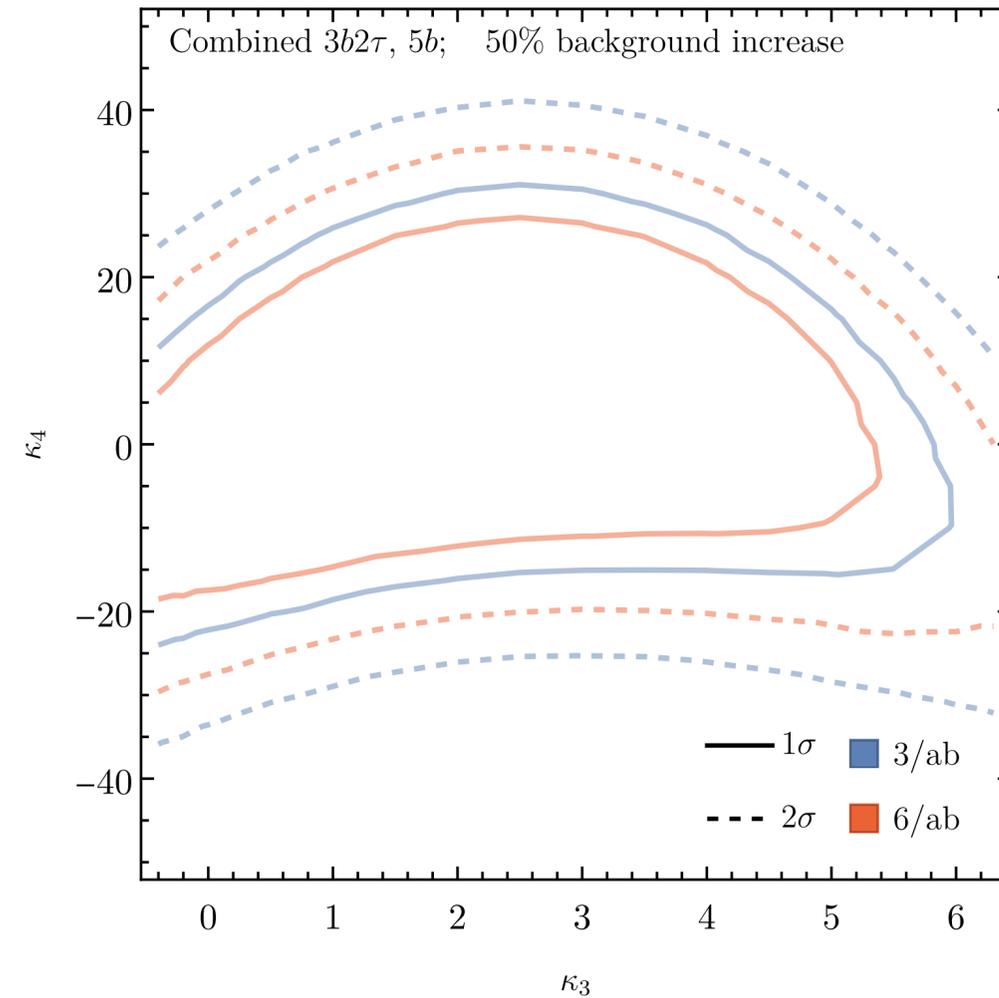
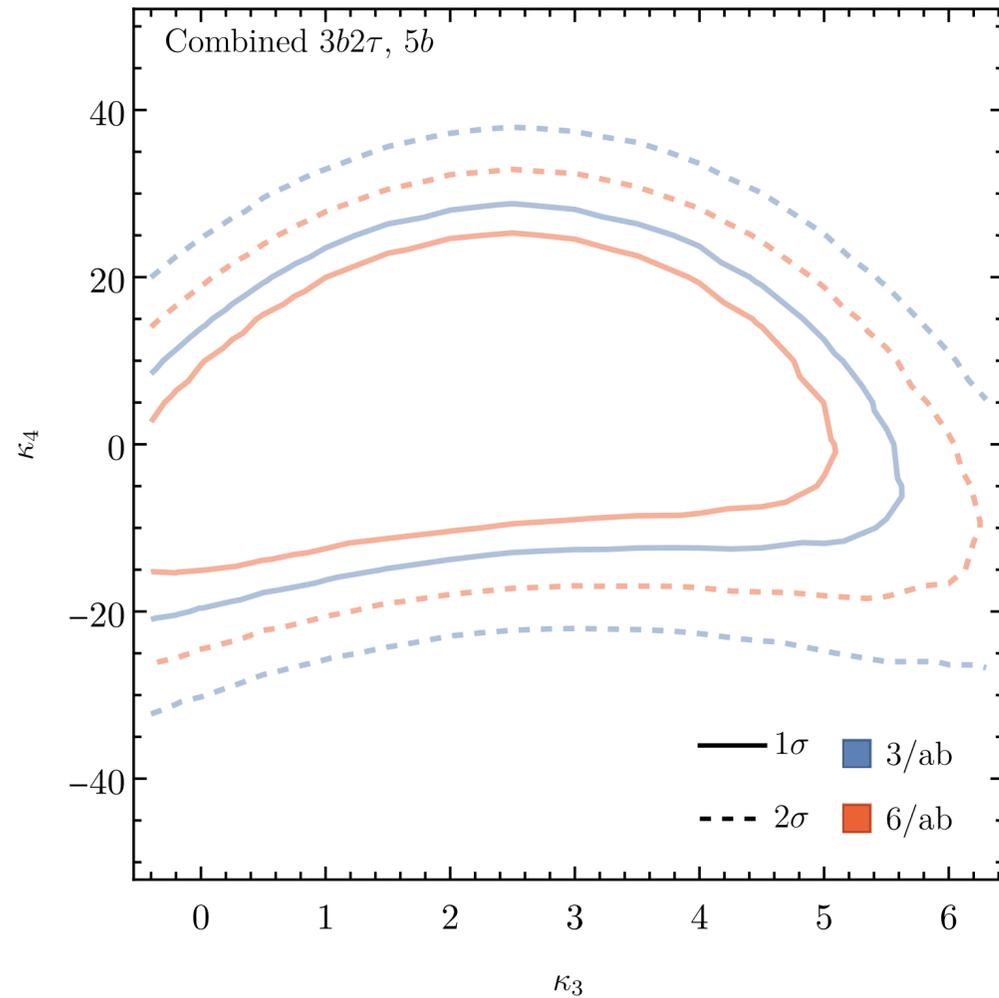
## $3b2\tau$ backgrounds:

	$\sigma(\text{gen.})(\text{fb})$	$\sigma(\text{sel.})(\text{fb})$	$\sigma(\text{NN})(\text{fb})$
$t\bar{t}(H \rightarrow \tau\tau)$	3.8	0.17	0.011
$WWb\bar{b}b\bar{b}$	31	4.6	$8.1 \times 10^{-3}$
$t\bar{t}(H \rightarrow b\bar{b})$	3.5	0.89	$3.8 \times 10^{-3}$
$Zb\bar{b}b\bar{b}$	4.3	0.45	$3.3 \times 10^{-4}$
$t\bar{t}(Z \rightarrow b\bar{b})$	0.77	0.15	$3.1 \times 10^{-4}$
$t\bar{t}(Z \rightarrow \tau\tau)$	4.7	0.080	$2.2 \times 10^{-4}$
$t\bar{t}t\bar{t}$	0.38	0.091	$2.1 \times 10^{-4}$

# Combined Results

- **Assumption:** No correlations  $\rightarrow$  combine significances

$$Z_{\text{comb}} = \sqrt{Z_{3b2\tau}^2 + Z_{5b}^2}$$



**Combination** of further channels and improvements of **tagging/ reconstruction** methods could enhance results further

# Integrated Gradients

→ **Integrated Gradients:** [Sundararajan, Taly, Yan 1703.01365]

- ▶ axiomatic method
- ▶ uses Neural Network gradients → **fast!**
- ▶ **requires a differentiable model**

**suitable for  
Neural Networks!**

• Definition:

$$I_i(x) = (x_i - x'_i) \int_0^1 d\alpha \frac{\partial F(x' + \alpha(x - x'))}{\partial x_i}$$

input ↑ ↑ baseline

Attribution scores  
→ importance of feature

Gradient of Neural Network  $F$

• Easy to implement for Graph Neural Networks as well

- ▶ Does **not** take into account graph structures → work in progress in Deep Learning community
- ▶ Viable to understand important features → expect mass of reconstructed Higgs to be important

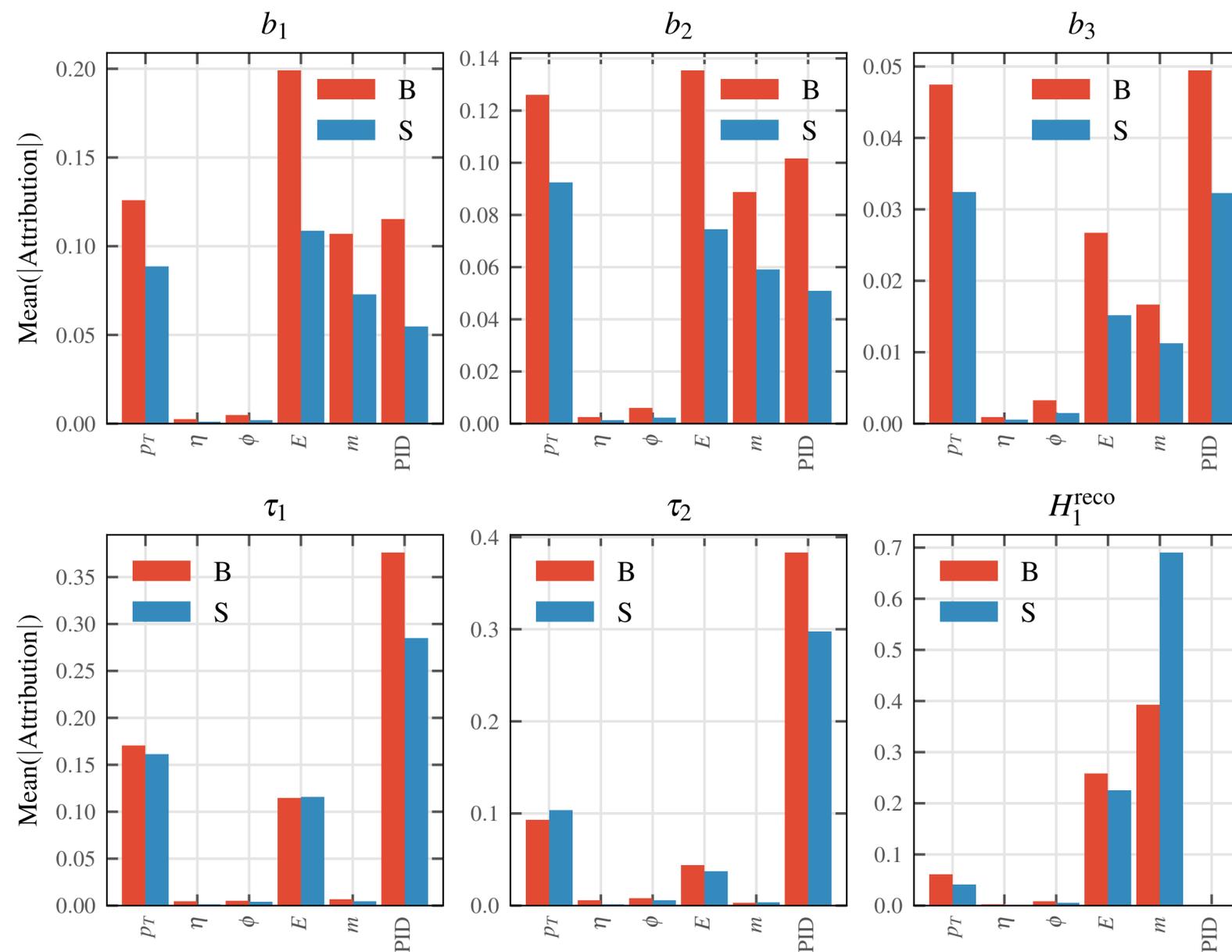
# NN Interpretation axioms

- **Integrated Gradients Axioms:**
  - **Completeness:** sum of attributions equal to difference of network output for input and baseline values
  - **Sensitivity:** when baseline and input have different values and different NN outputs, attributions should also be different
  - **Dummy:** A zero input should yield no attribution
  - **Implementation Invariance:** If two methods are equivalent (i.e. yield same scores for all inputs despite being different) then attributions should be identical
  - **Linearity:** Attributions should be linear for linear combinations of networks  $aF_1 + bF_2$
  - **Symmetry:** For a network symmetric for two variables  $F(x, y) = F(y, x)$ , the attributions should be the same

# Understanding the 'black box': NN interpretations

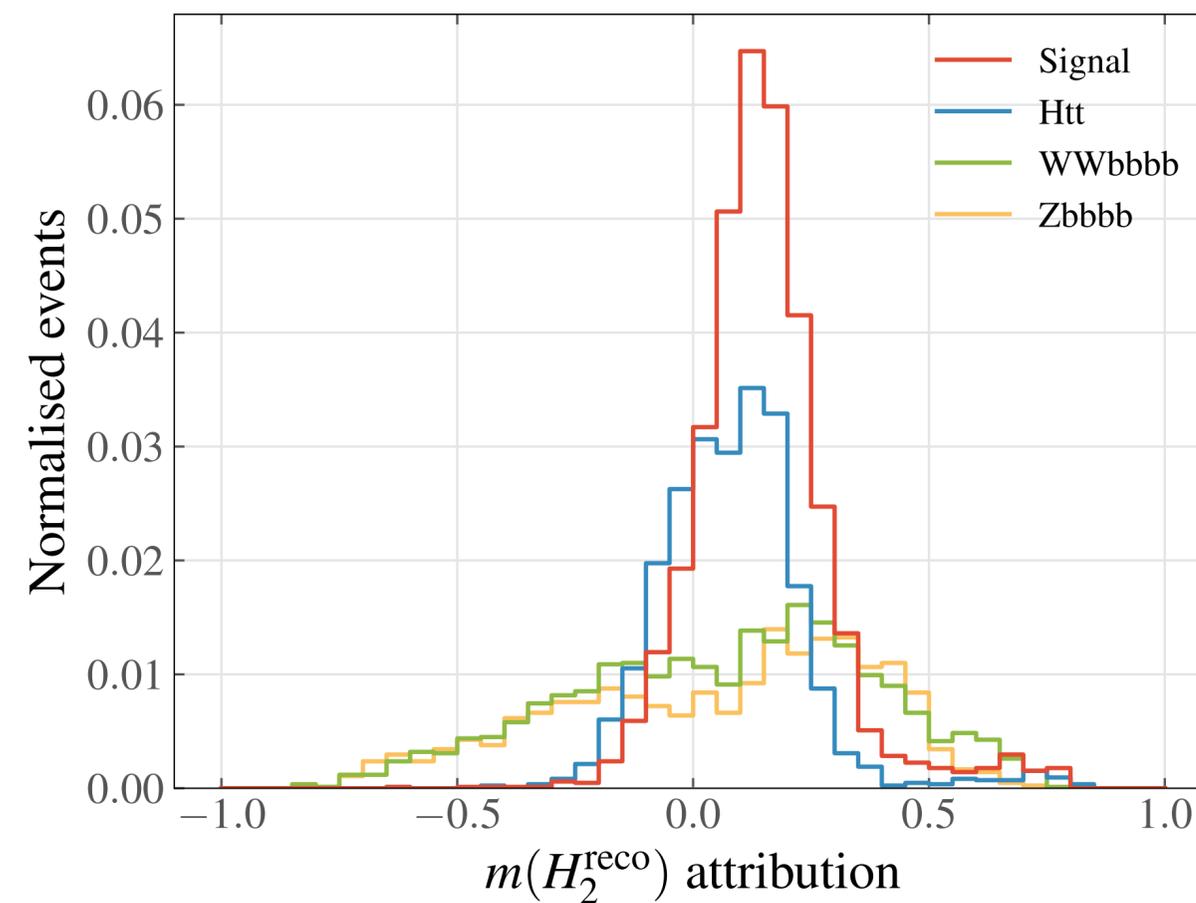
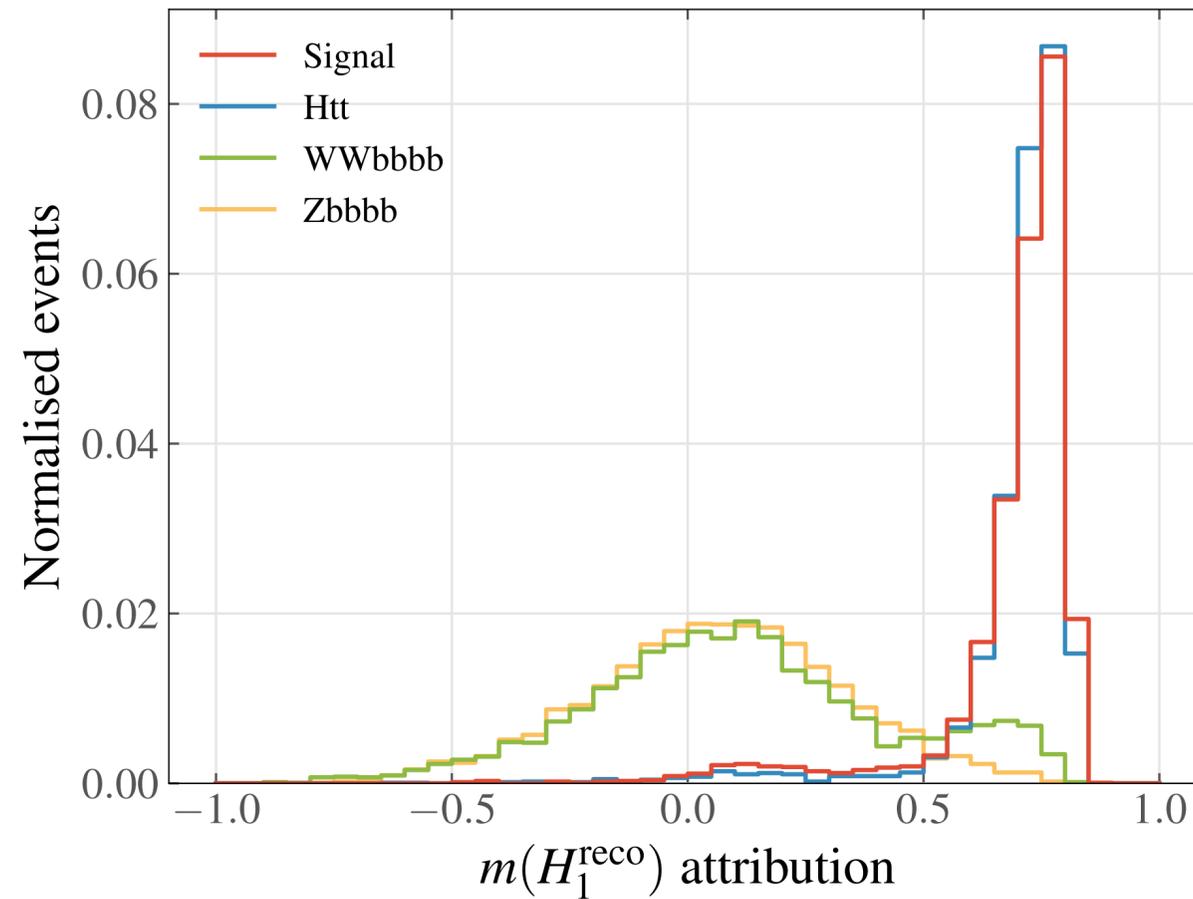
Which features are more important? Investigate with 'Integrated Gradients' method

- Tagged  $b$ -jets and  $\tau$  nodes ordered by  $p_T$
- 'Roughly' reconstructed Higgs nodes ordered by 'closeness' to 125 GeV
- $p_T$ ,  $E$  and PID more important than angular observables
- Higgs masses most important



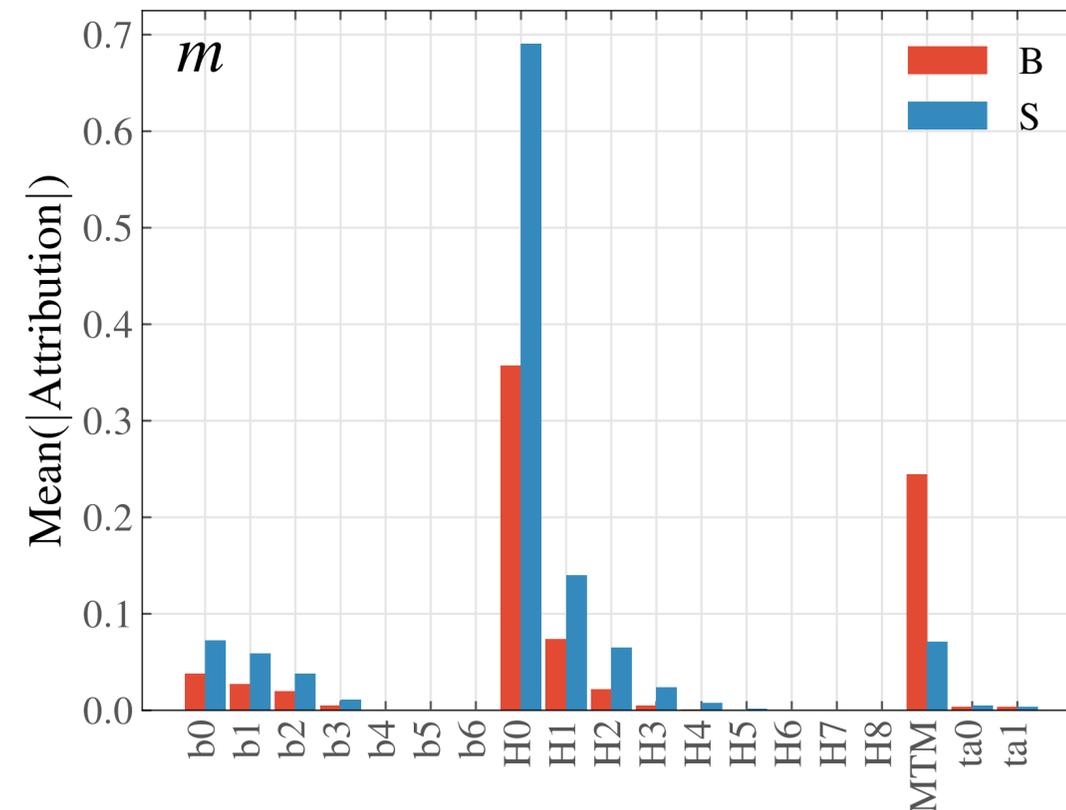
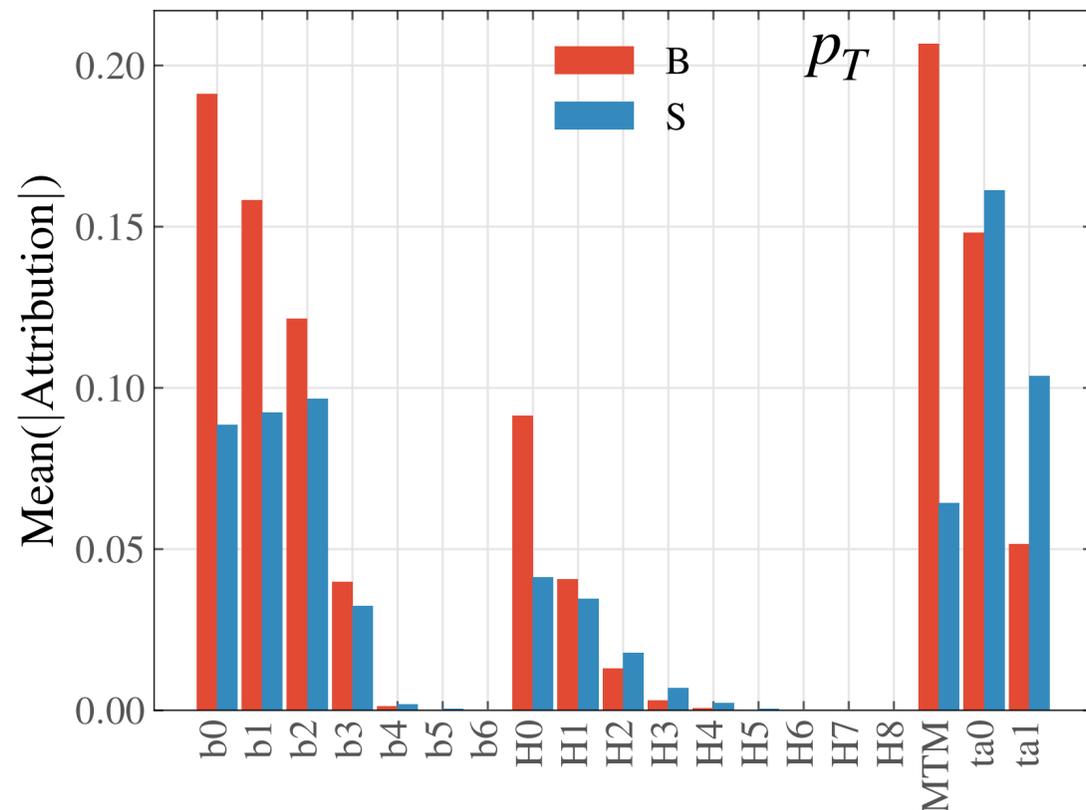
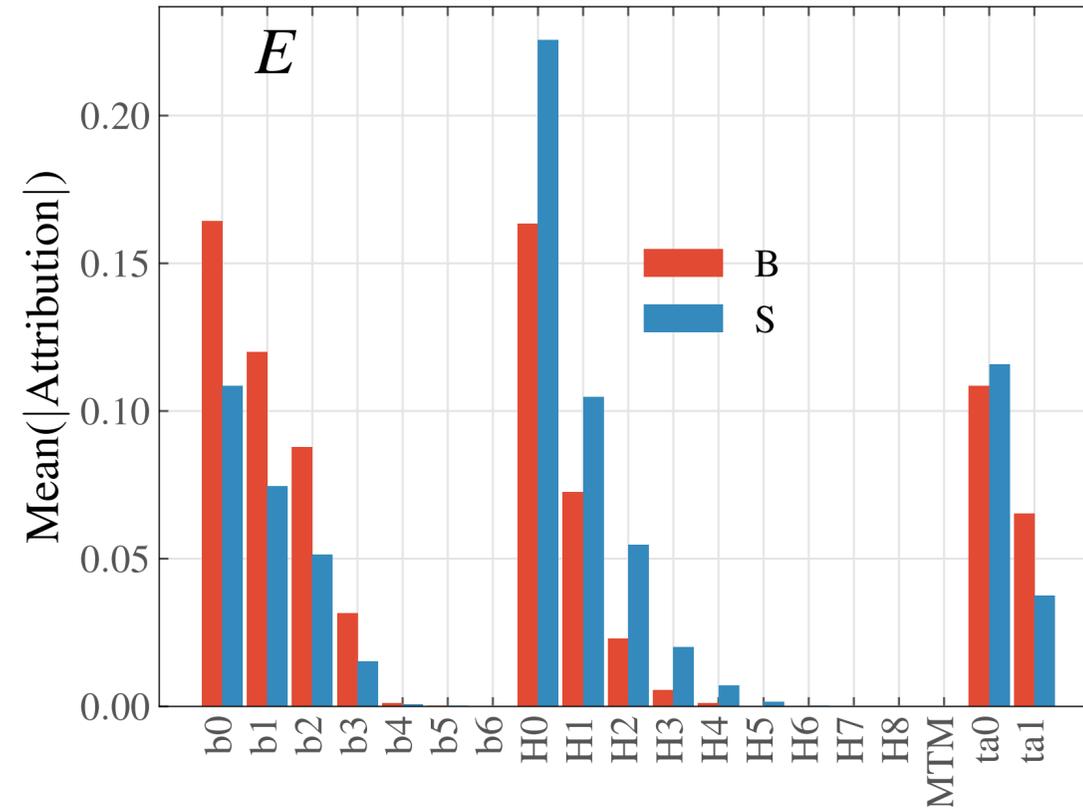
# Reconstructed Higgs Mass

- **Interpretation as expected:**  
If a Higgs close to 125 GeV can be found  $\implies$  signal
- Complete understanding would require to study correlations between observables  $\rightarrow$  **future work**



# Attribution vs. nodes

- $E$  and  $p_T$  from leading order particles is more important
- $m$  is more important for the reconstructed Higgs closest to the SM mass value



# Lepton collider cross sections

- Inclusive  $\ell\ell \rightarrow HHH + X$  analysis with  $H \rightarrow b\bar{b}$
- Cross sections small below 1 TeV
- **Note:**  $\mu^+\mu^-$  vs.  $e^+e^-$  collider at 10 TeV has difference of less than 5% on cross sections

