

# Analytic electroweak corrections to di-Higgs and Higgs+jet production

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In collaboration with Joshua Davies, Kay Schönwald and Matthias Steinhauser

Based on [JHEP 08 (2022) 259] & [JHEP 10 (2023) 033]  
& [2407.05787] & [2407.12107]

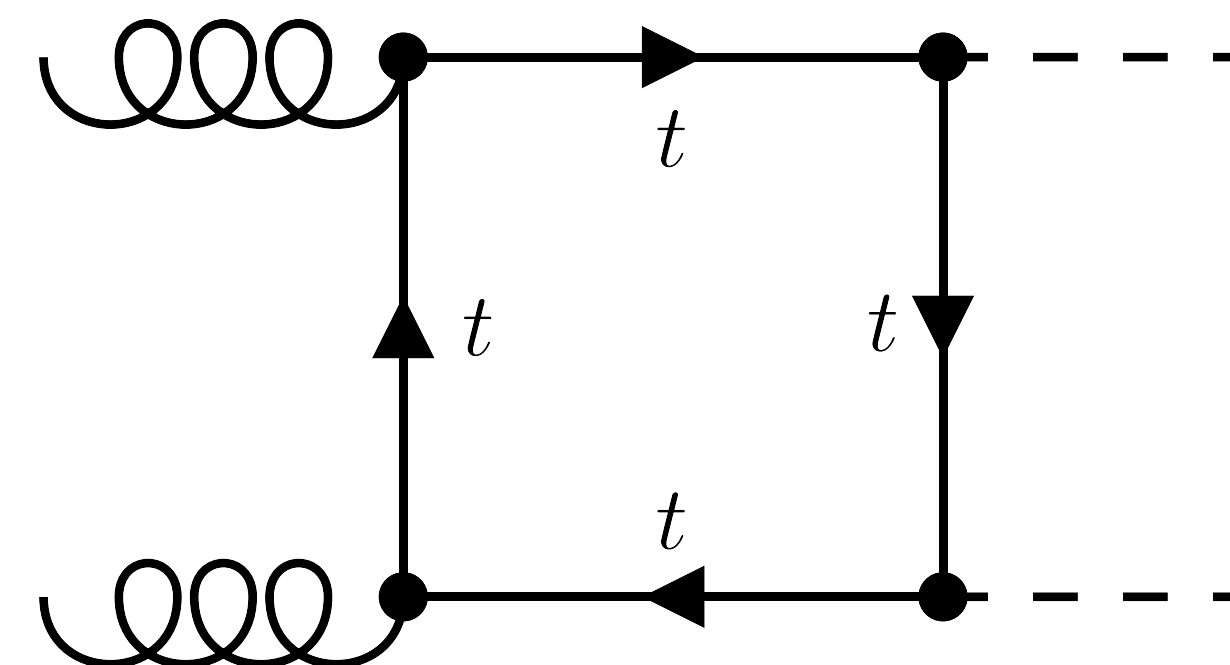
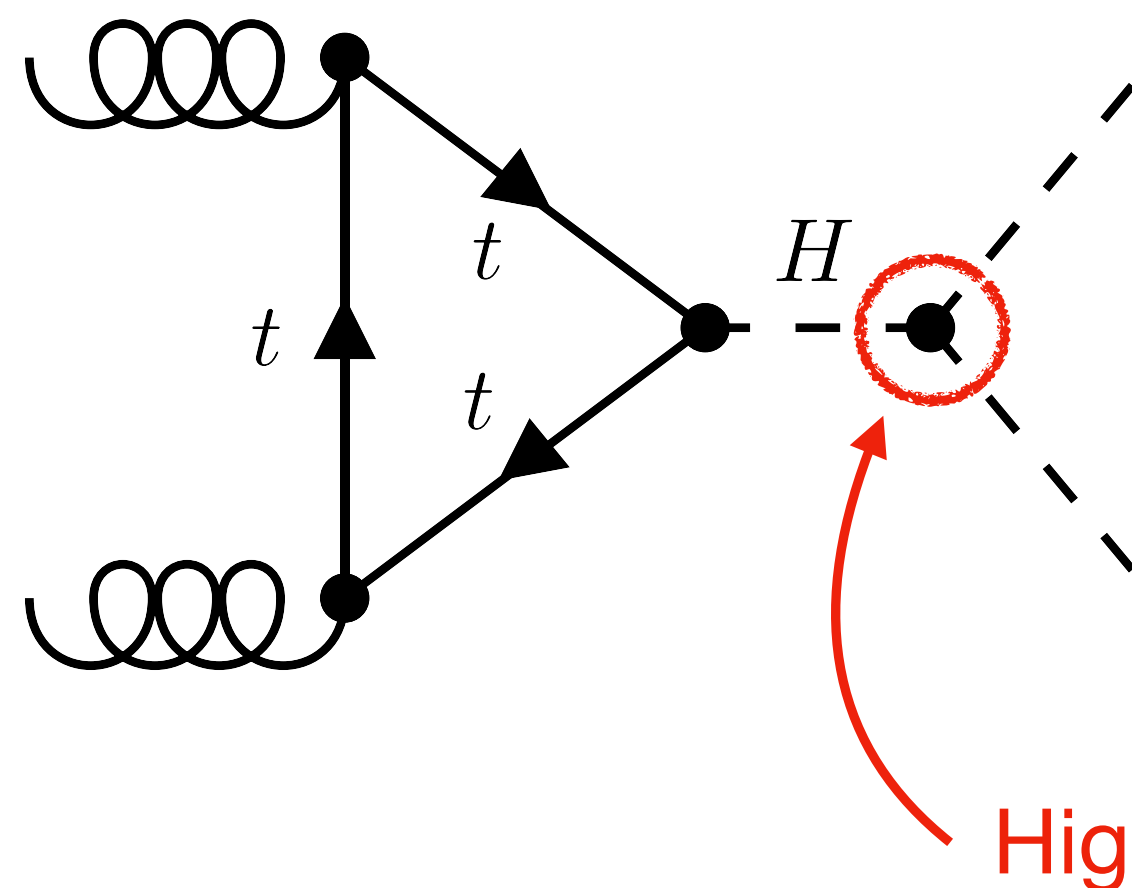
# Motivation: probe Higgs self-coupling

- Probe Higgs self-coupling in Higgs pair productions, and compare with the Standard Model value

$$\lambda = m_H^2/(2v^2) \approx 0.13 \text{ in the Higgs potential}$$

$$V(H) = \frac{1}{2} m_H^2 H^2 + \lambda v H^3 + \frac{\lambda}{4} H^4$$

- Gluon-fusion channel dominates Higgs boson pair production (key process at HL-LHC)

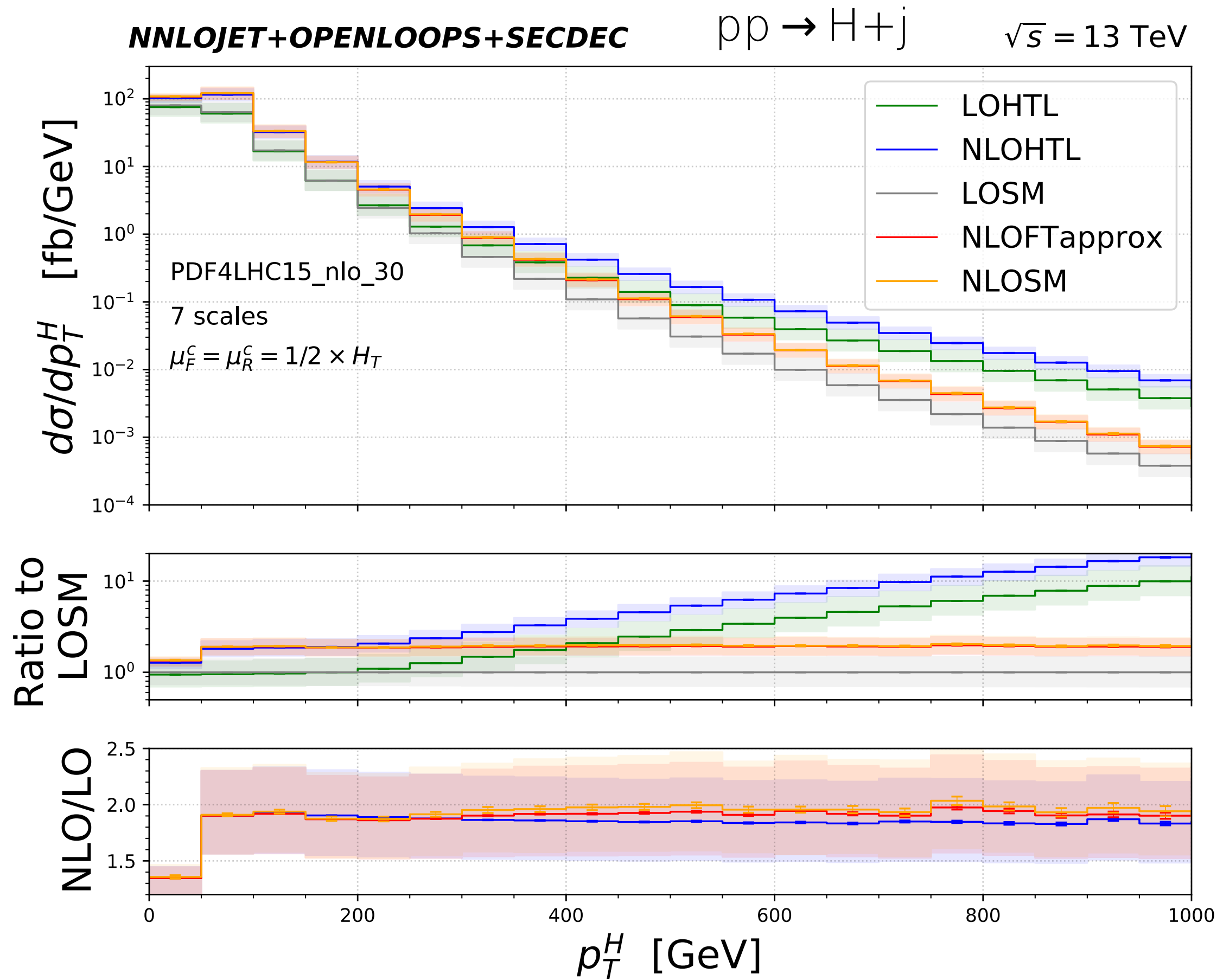
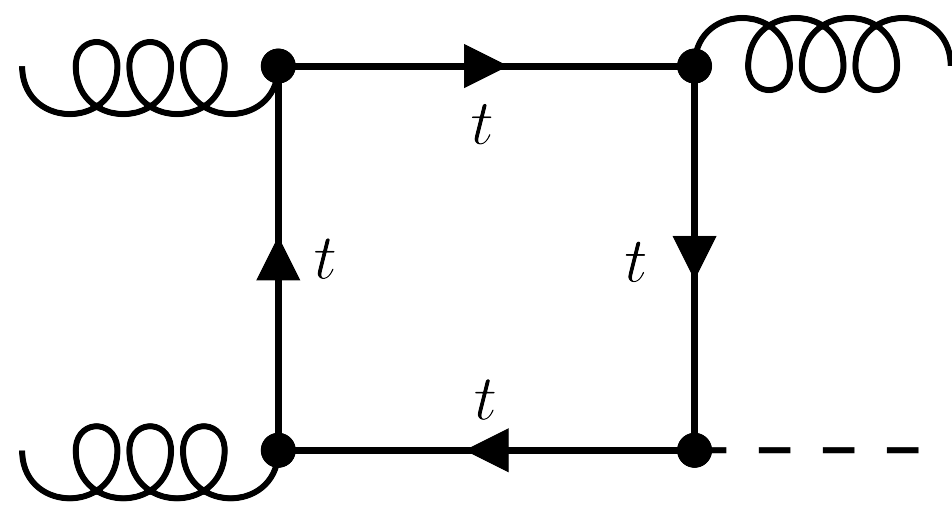
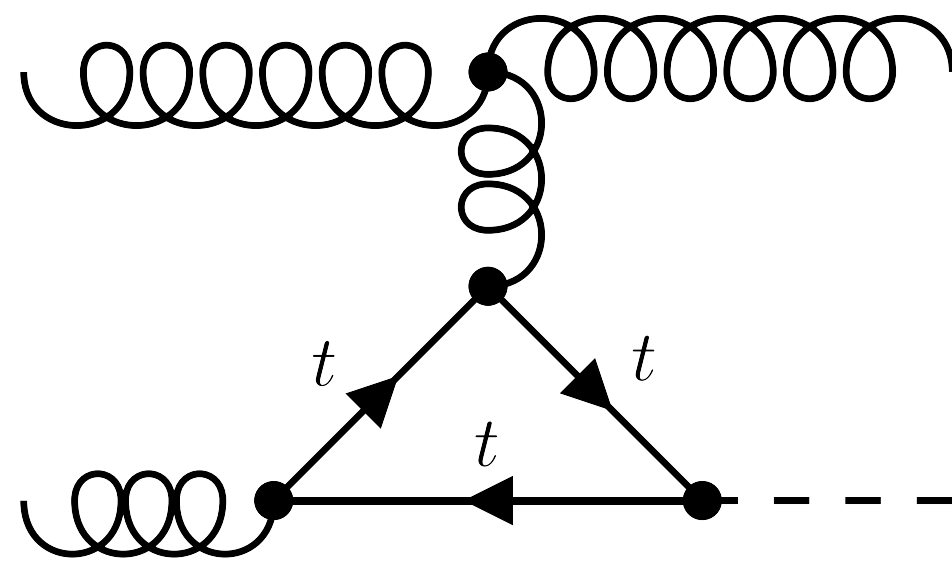


New Physics opportunity?

[Iguro, Kitahara, Omura, Zhang, *Phys.Rev.D* 107 (2023) 7, 075017]

# Motivation of Higgs+jet: study $p_T^H$ spectrum

- Dominant channel for Higgs boson production with large transversal momentum  $p_T^H$  at LHC



$p_T^H$  spectrum:  
crucial for studying  
Higgs boson properties

NLOSM  $\Rightarrow$  NLO QCD with  
top-mass dependence

Precise Higgs + 2 jets @ NLO QCD also available  $\longrightarrow$  [Chen, Huss, Jones, Kerner, Lang, Lindert, Zhang, *JHEP* 03 (2022) 096]

# Overview of EW calculations

## Analytical approach

$gg \rightarrow HH$

- Yukawa-top corrections in high-energy expansion [Davies, Mishima, Schönwald, Steinhauser, **Zhang**, 22']
- Yukawa-top corrections in large- $m_t$  limit [Mühlleitner, Schlenk, Spira, 22']
- Full top-induced EW corrections in large- $m_t$  expansion [Davies, Schönwald, Steinhauser, **Zhang**, 23']
- Factorizable EW corrections [Davies, Schönwald, Steinhauser, **Zhang**, 24']

## Numerical approach

- Higgs self-coupling corrections with SecDec [Borowka, Duhr, Maltoni, Pagani, Shivaji, Zhao, 19']
- Full EW corrections with AMFlow [Bi, Huang, Huang, Ma, Yu, 24']
- Yukawa and Higgs self-coupling corrections with SecDec [Heinrich, Jones, Kerner, Stone, Vestner, 24]

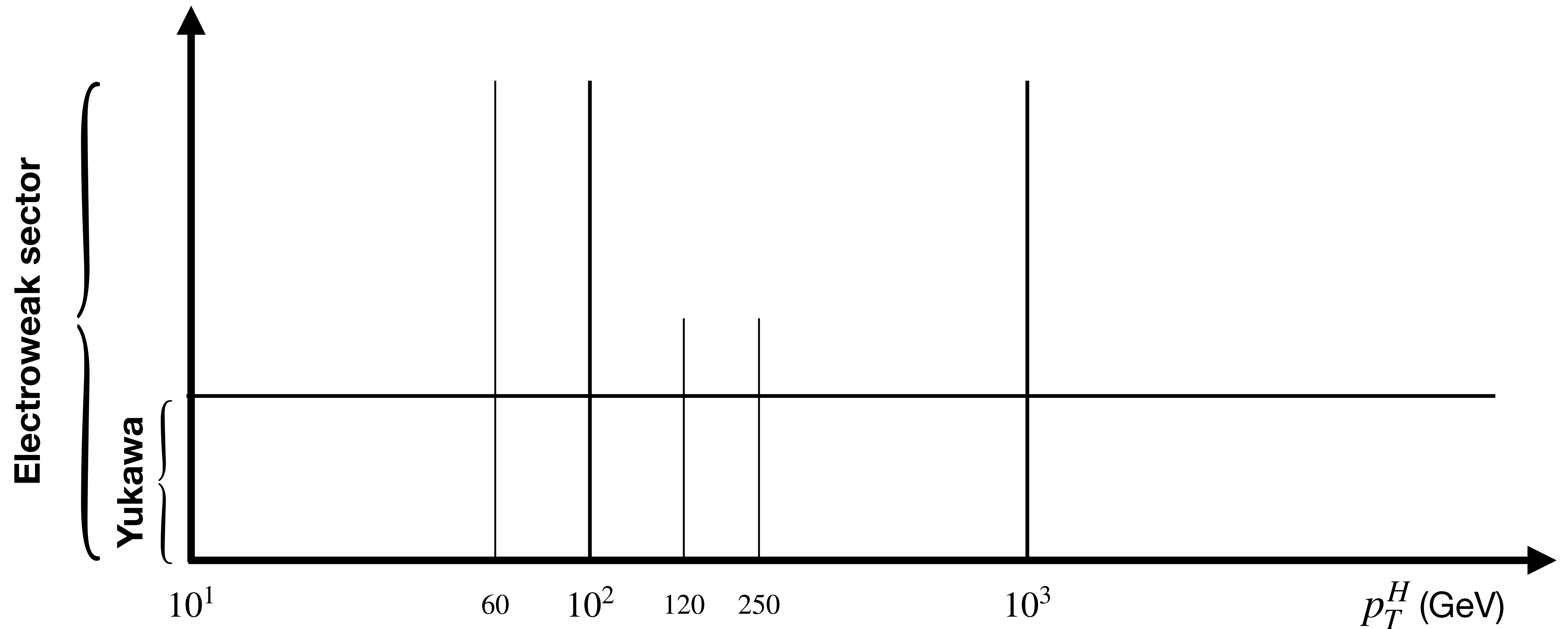
$gg \rightarrow Hg$

- Mixed QCD-EW correction (fully analytic) [Bonetti, Panzer, Smirnov, Tancredi, 20']
- Higgs self-coupling corrections in large- $m_t$  expansion [Gao, Shen, Wang, Yang, Zhou, 23']
- Full top-induced EW corrections in large- $m_t$  expansion [Davies, Schönwald, Steinhauser, **Zhang**, 23']

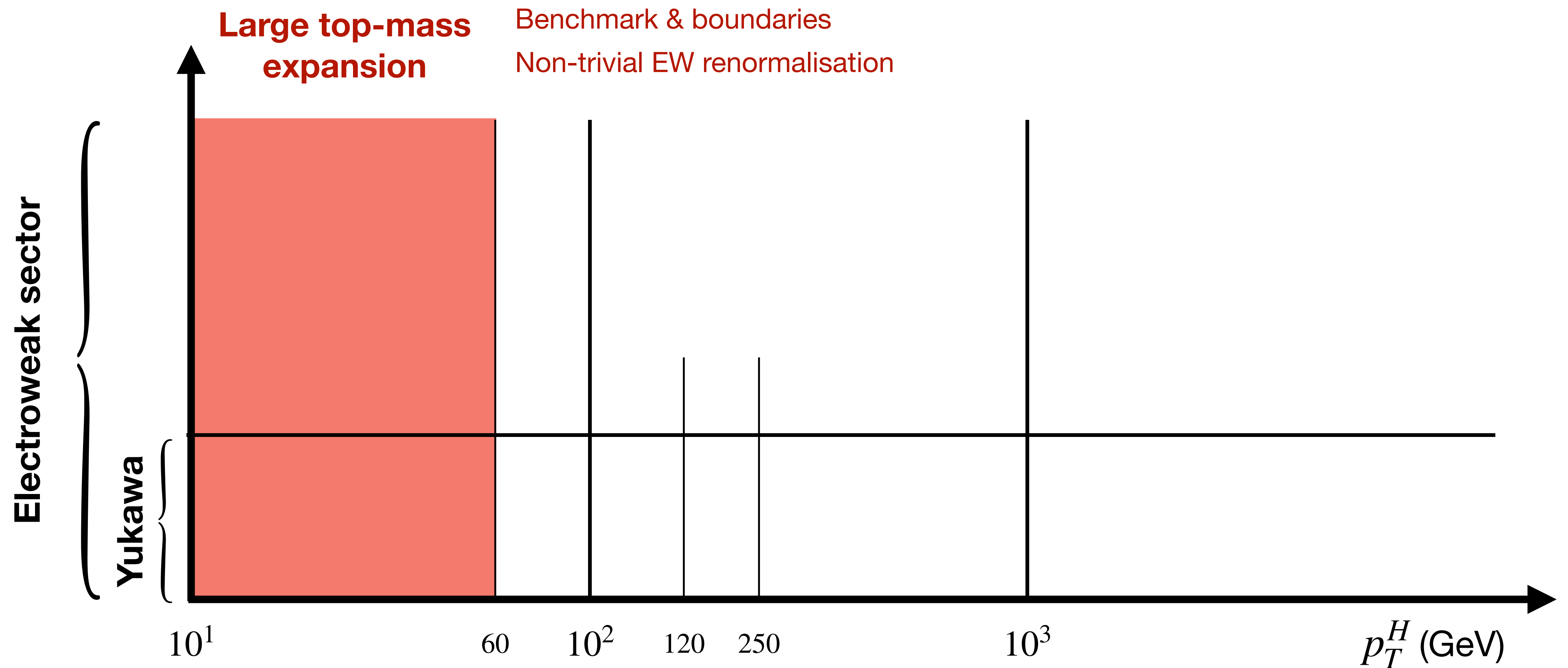
[ See talk by Matthias Steinhauser for QCD corrections to di-Higgs ]

**This talk:** analytic expansion in large-mass, forward scattering, and high-energy kinematics

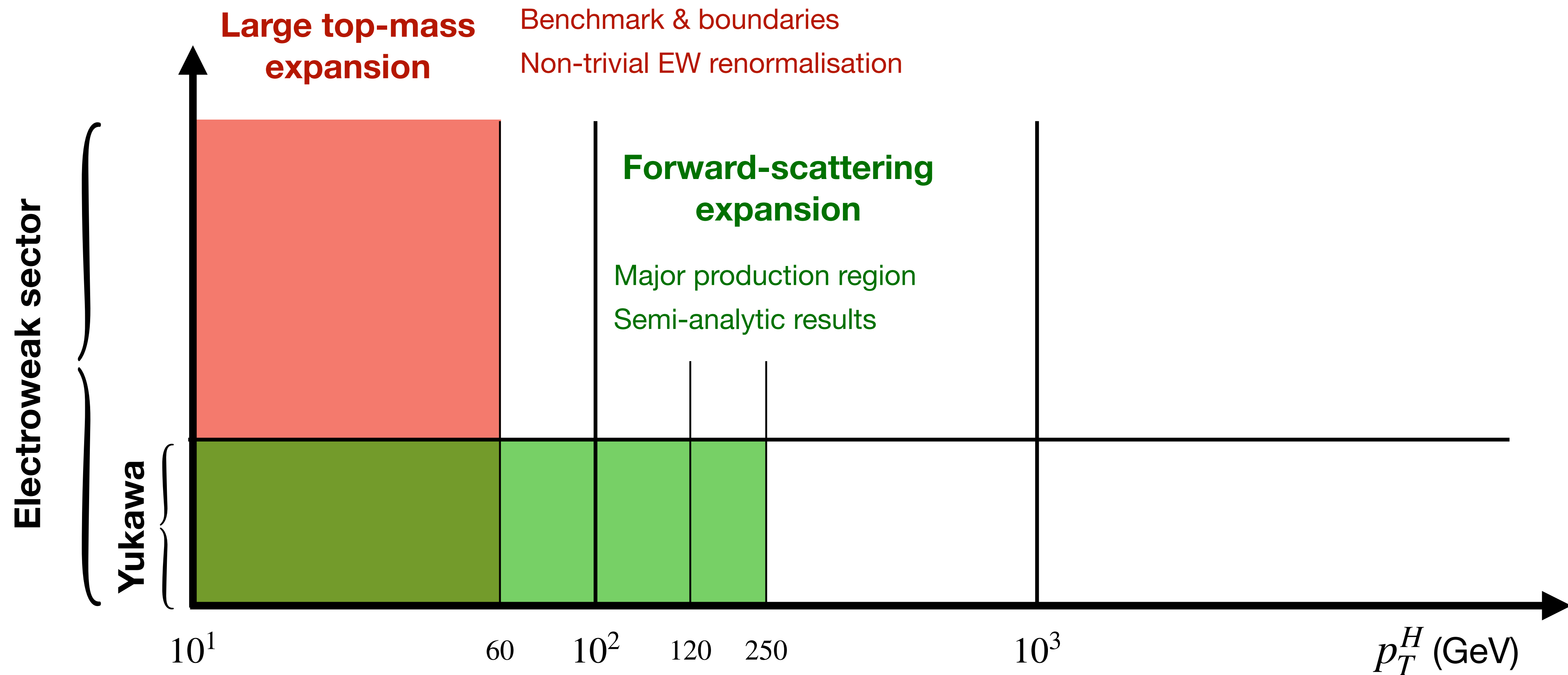
# Expansions of two-loop EW corrections



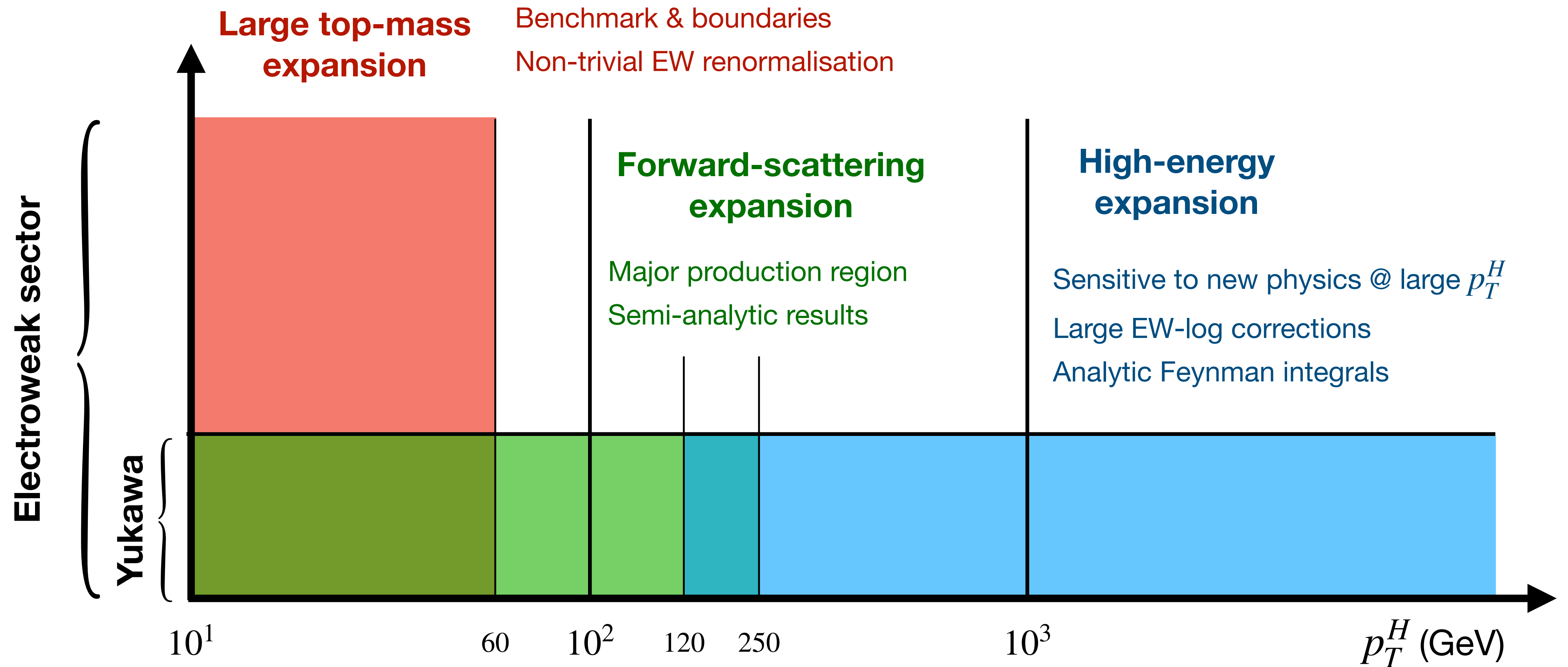
# Expansions of two-loop EW corrections



# Expansions of two-loop EW corrections



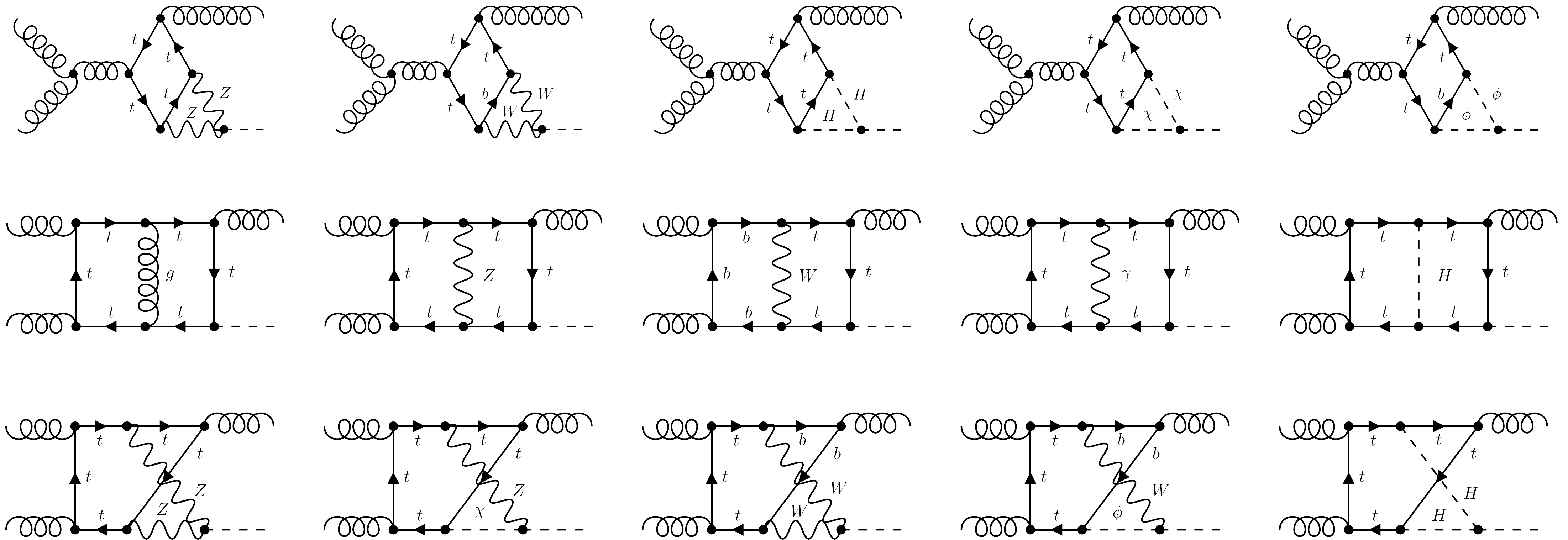
# Expansions of two-loop EW corrections





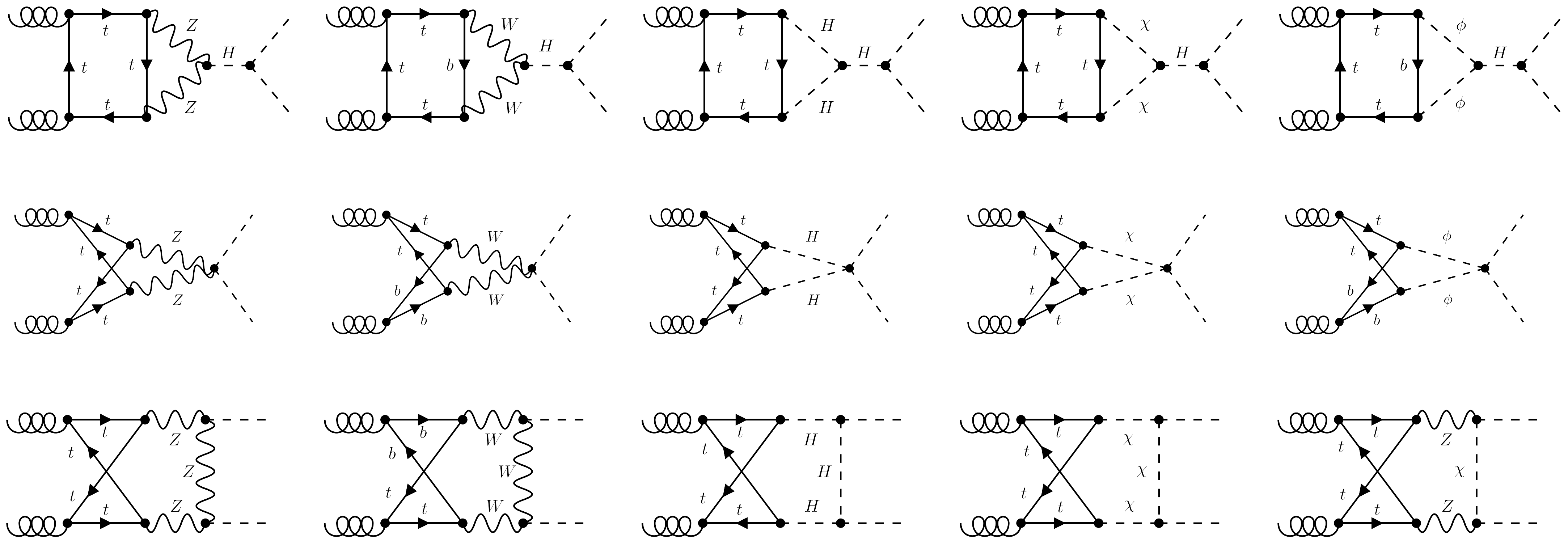
# Two-loop EW diagrams with top-quark (H+jet)

- Sample two-loop diagrams involving SM fields:  $\{t, b, H, \gamma, Z, W^\pm, \chi, \phi^\pm\}$  and ghosts:  $\{u^\gamma, u^Z, u^\pm\}$



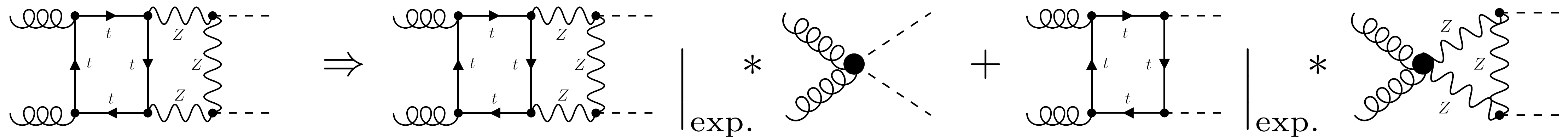
# Two-loop EW diagrams with top-quark (HH)

- Sample two-loop diagrams involving SM fields:  $\{t, b, H, \gamma, Z, W^\pm, \chi, \phi^\pm\}$  and ghosts:  $\{u^\gamma, u^Z, u^\pm\}$



# Large- $m_t$ expansion and EW renormalisation

- Expansion hierarchy:  $m_t^2 \gg s, t, m_H^2, m_W^2, m_Z^2$
- Expand and calculate in **general  $R_\xi$  gauge** with large gauge fixing parameters  $\xi_Z, \xi_W \gg 1$



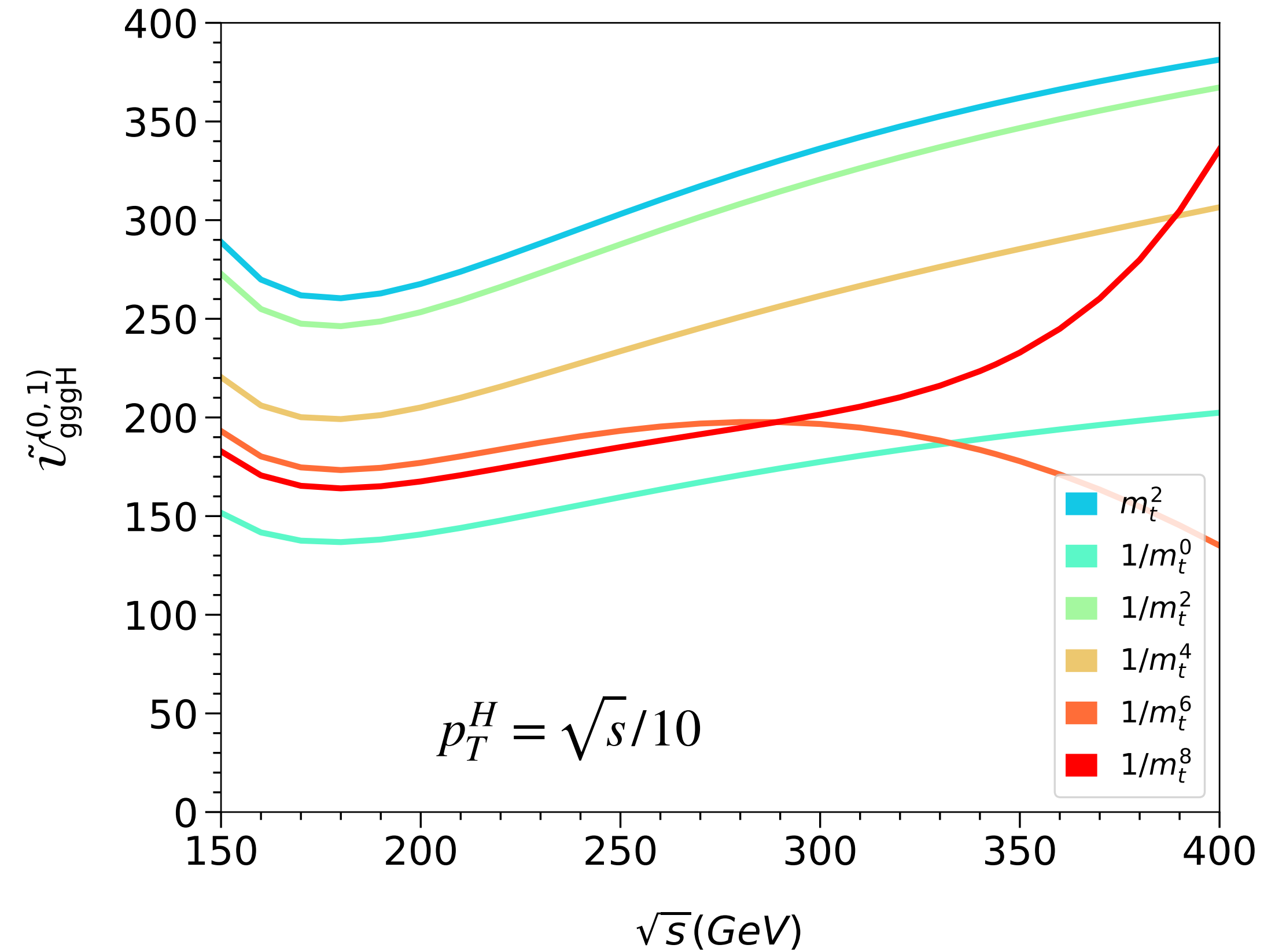
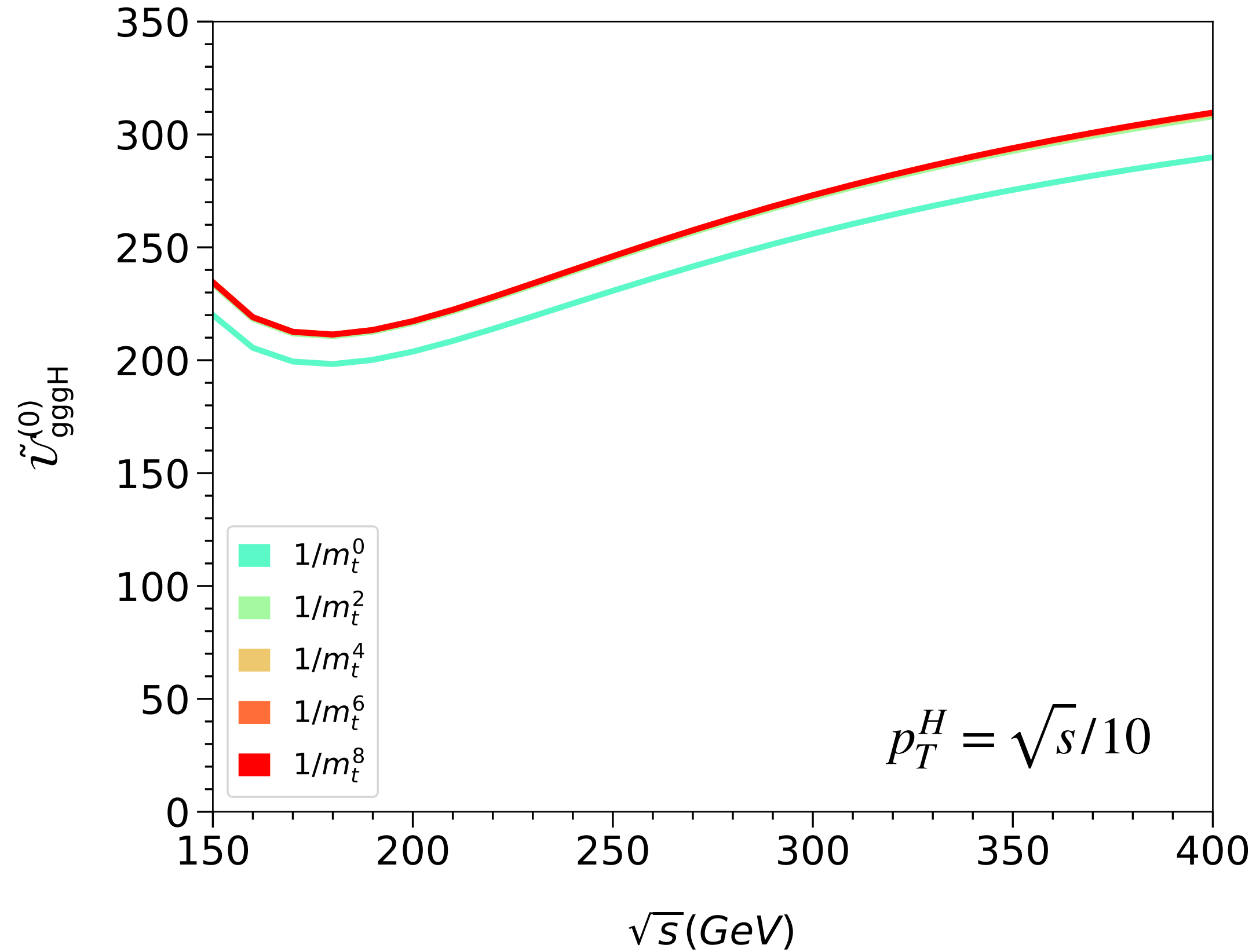
- **On-Shell renormalise** input parameters  $\{e, m_W, m_Z, m_t, m_H\}$  in  $G_\mu$  scheme
- $\xi_W, \xi_Z$  **cancel** after external Higgs **fields OS renormalisation**

# Matrix elements for $gg \rightarrow gH$ @ NLO EW

[Davies, Schönwald, Steinhauser, Zhang, *JHEP* 10 (2023) 033]

$$\mathcal{M} = \frac{1}{8^2 2^2} \sum_{\text{col}} \sum_{\text{pol}} |\mathcal{A}|^2 = \frac{3}{32} (X_0^{\text{gggH}})^2 s \tilde{\mathcal{U}}_{\text{gggH}}$$

$$\tilde{\mathcal{U}}_{\text{gggH}} = \tilde{\mathcal{U}}_{\text{gggH}}^{(0)} + \frac{\alpha_s(\mu)}{\pi} \tilde{\mathcal{U}}_{\text{gggH}}^{(1,0)} + \frac{\alpha}{\pi} \tilde{\mathcal{U}}_{\text{gggH}}^{(0,1)}$$



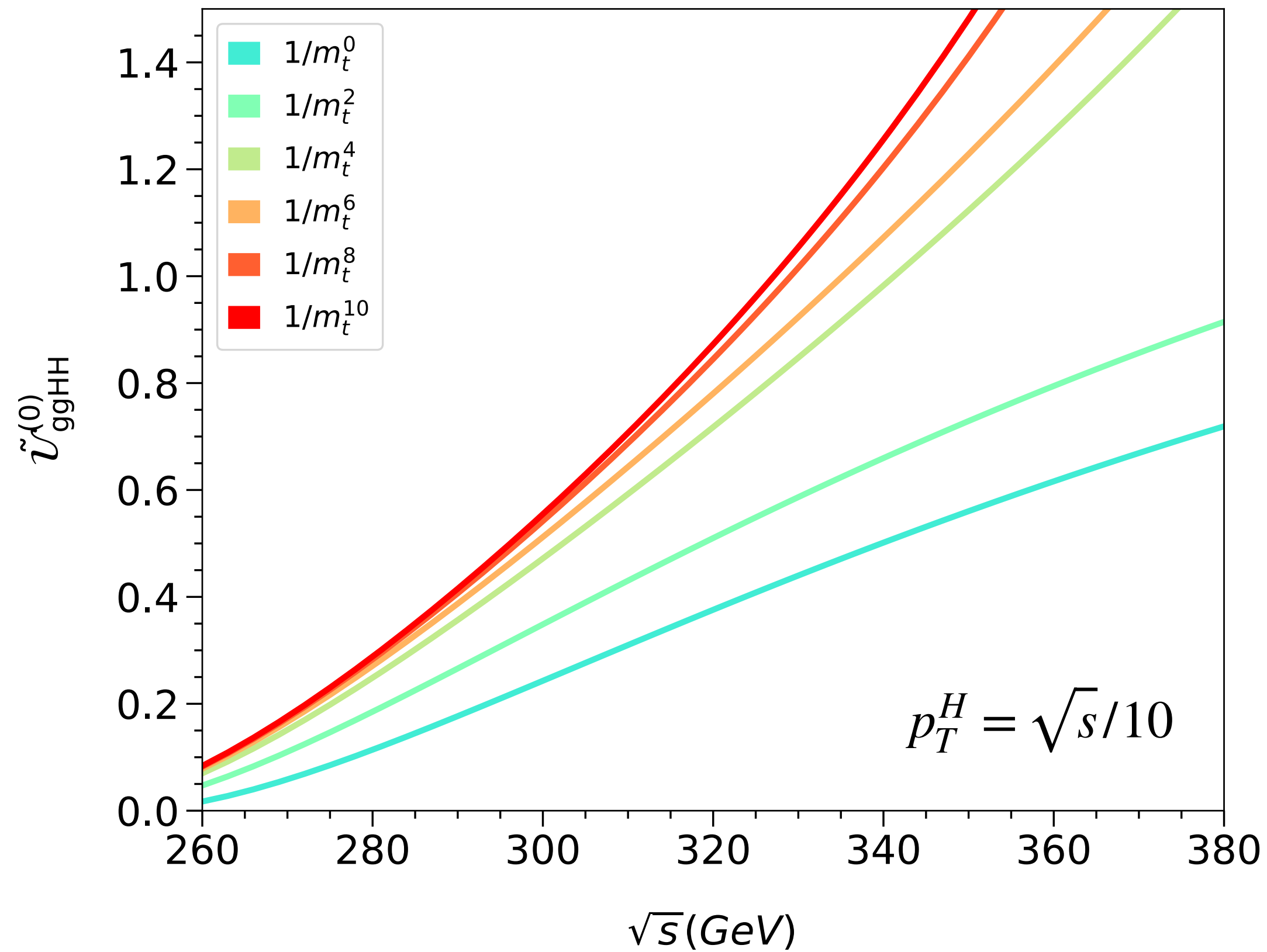
Good convergence observed, corrections are small  $\lesssim \mathcal{O}(1\%)$

# Matrix elements for $gg \rightarrow HH$ @ NLO EW

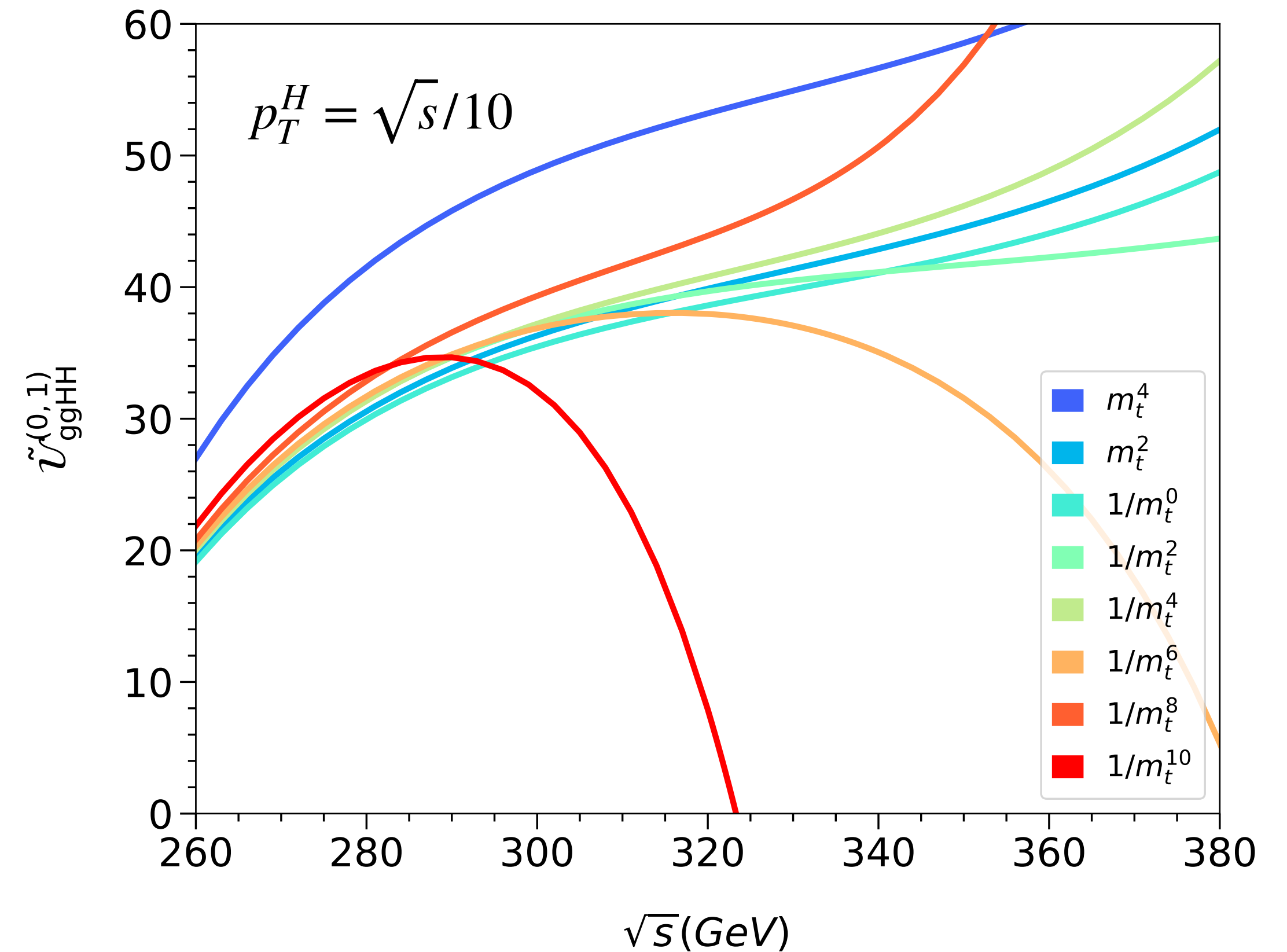
[Davies, Schönwald, Steinhauser, Zhang, *JHEP* 10 (2023) 033]

$$\mathcal{M} = \frac{1}{8^2 2^2} \sum_{\text{col}} \sum_{\text{pol}} |\mathcal{A}|^2 = \frac{1}{16} (X_0^{\text{ggHH}} s)^2 \tilde{\mathcal{U}}_{\text{ggHH}}$$

$$\tilde{\mathcal{U}}_{\text{ggHH}} = \tilde{\mathcal{U}}_{\text{ggHH}}^{(0)} + \frac{\alpha}{\pi} \tilde{\mathcal{U}}_{\text{ggHH}}^{(0,1)}$$



$\tilde{\mathcal{U}}_{\text{ggHH}}^{(0)}$  @ LO



$\tilde{\mathcal{U}}_{\text{ggHH}}^{(0,1)}$  plot up @ NLO EW

Not very good convergence at NLO, but serve as boundaries to forward scattering expansion

# Matrix elements for $gg \rightarrow HH$ @ NLO EW

[Davies, Schönwald, Steinhauser, Zhang, *JHEP* 10 (2023) 033]

$$\mathcal{M} = \frac{1}{8^2 2^2} \sum_{\text{col}} \sum_{\text{pol}} |\mathcal{A}|^2 = \frac{1}{16} (X_0^{\text{ggHH}} s)^2 \tilde{\mathcal{U}}_{\text{ggHH}}$$

$$\tilde{\mathcal{U}}_{\text{ggHH}} = \tilde{\mathcal{U}}_{\text{ggHH}}^{(0)} + \frac{\alpha}{\pi} \tilde{\mathcal{U}}_{\text{ggHH}}^{(0,1)}$$

Famous di-Higgs destructive interference  
(vanishing ME at production threshold in HTL)

is **lifted**

3-loop QCD corrections also **lifts** this  
destructive interference

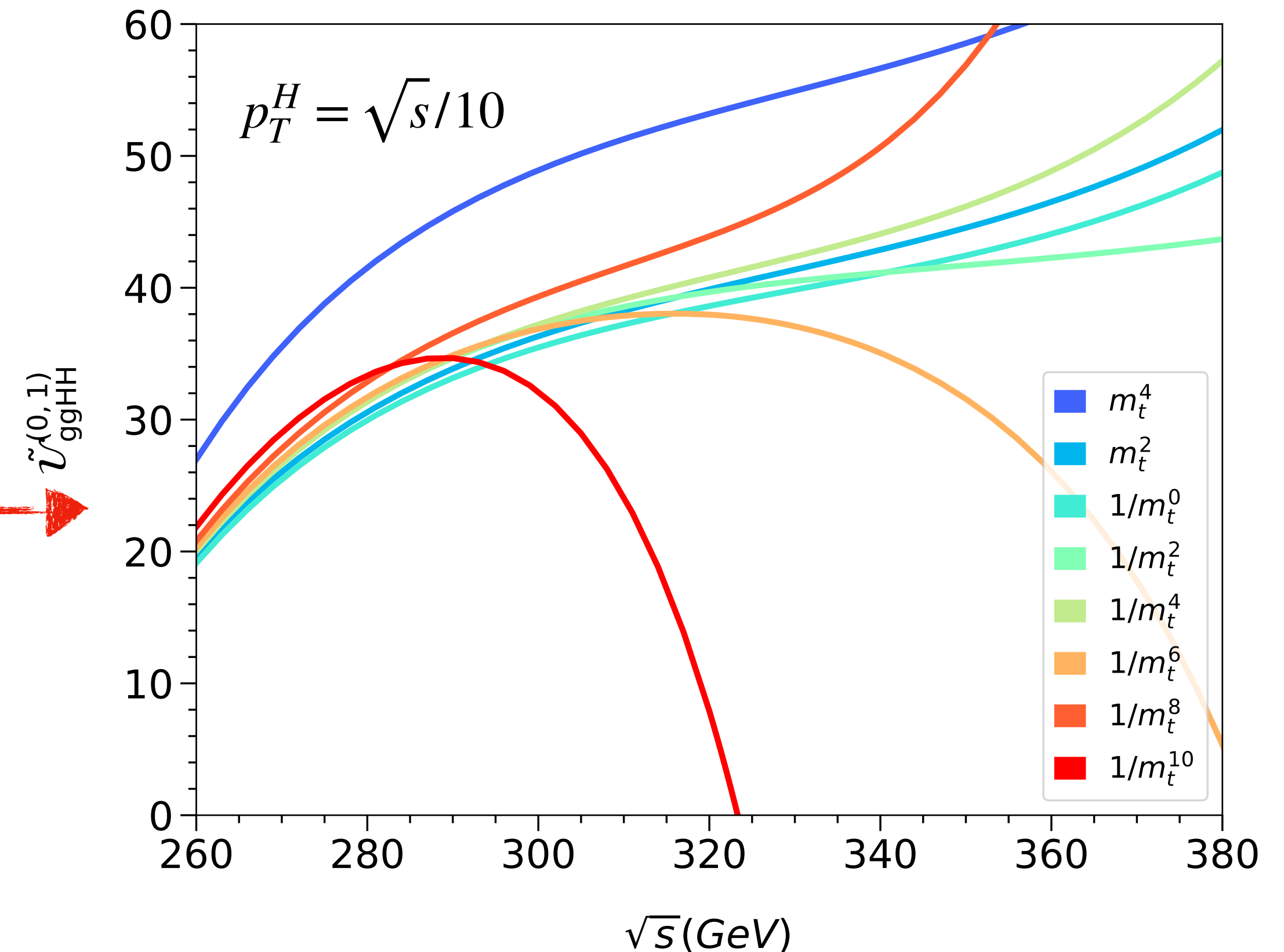
[Grigo, Melnikov, Steinhauser, 14']

Large EW (Yukawa) corrections found near  
production threshold by several groups

[Mühlleitner, Schlenk, Spira, 22']

[Bi, Huang, Huang, Ma, Yu, 24']

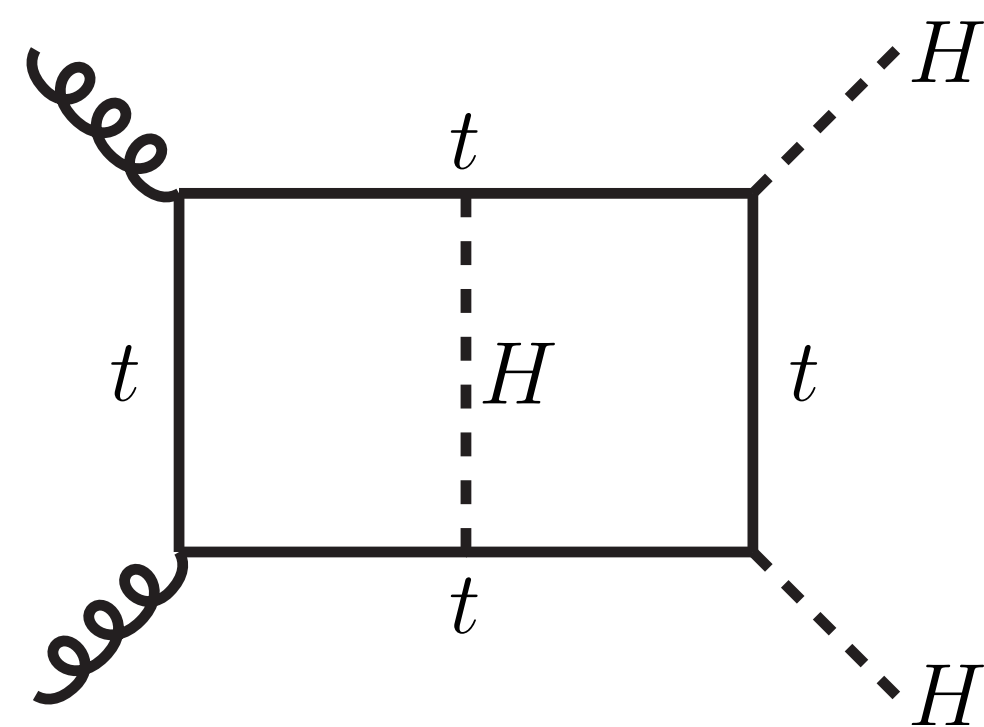
[Heinrich, Jones, Kerner, Stone, Vestner, 24]



$\tilde{\mathcal{U}}_{\text{ggHH}}^{(0,1)}$  plot up @ **NLO EW**

# Beyond large- $m_t$ expansion @ NLO Yukawa $\mathcal{O}(\alpha_s y_t^4)$

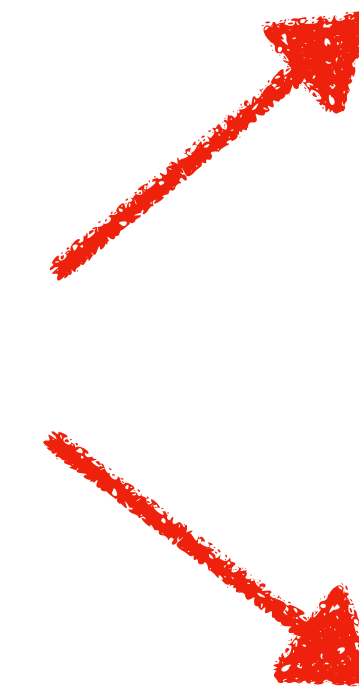
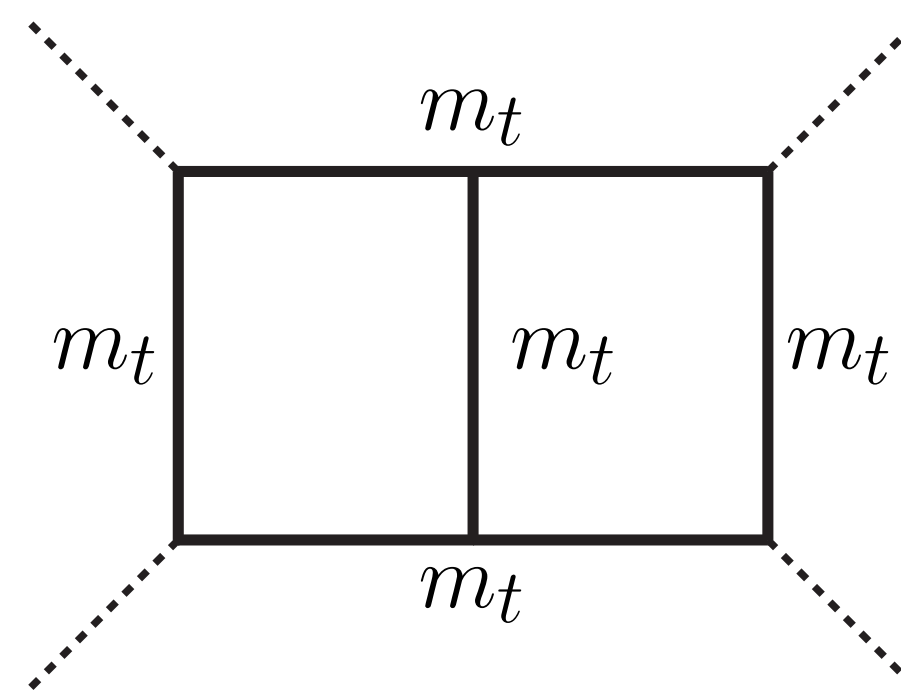
- Sample two-loop diagrams and expansion strategy



**Taylor expansion** in internal mass difference  
and external Higgs mass



scalar master integral



Use boundary conditions  
from large- $m_t$  limit



$$s, m_t^2 \gg t \text{ or } u$$

**Forward scattering  
expansion**

[See talk by M. Steinhauser]

$$s, t, u \gg m_t^2$$

**High-energy expansion**

# High energy expansion @ NLO Yukawa

1. **Asymptotic expansion:**  $s, t \gg m_t^2$
2. **System of differential equations for 140 Master Integrals** from IBP reduction [Kira]

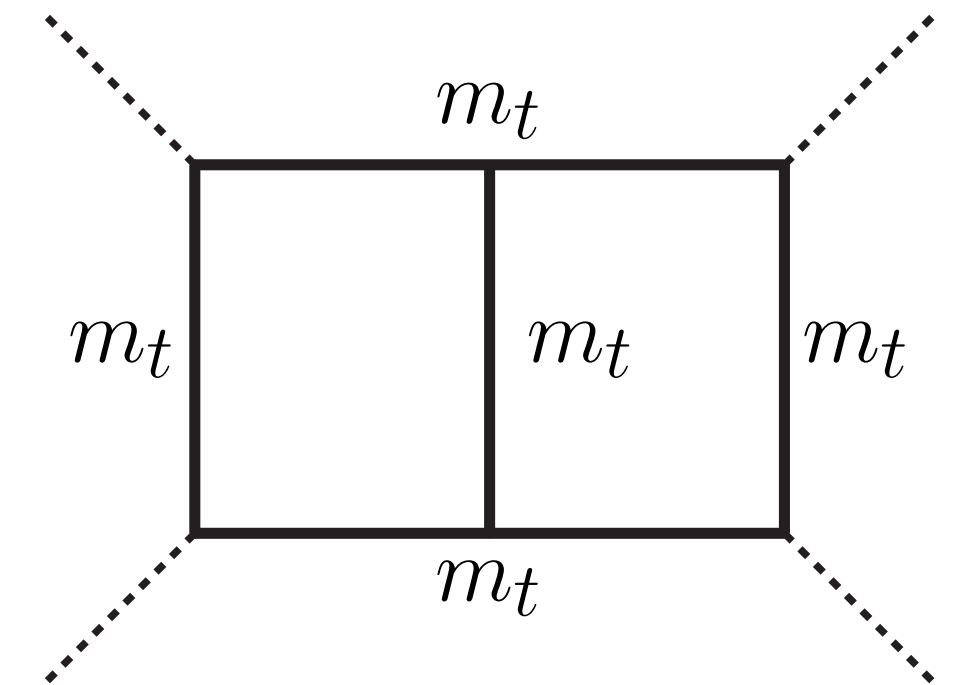
$$\frac{\partial}{\partial(m_t^2)} \mathbf{I} = M(s, t, m_t^2, \epsilon) \mathbf{I} \quad \text{with} \quad \mathbf{I} = (\mathcal{I}_1, \dots, \mathcal{I}_{140})^T$$

3. Plug in **power-log ansatz** for each master integral

$$\mathcal{I}_n = \sum C_{(n)}^{ijk}(s, t) \epsilon^i [m_t^2]^j [\log(m_t^2)]^k$$

4. Solve **boundary master integrals in  $m_t^2/s \rightarrow 0$  to higher orders** with Mellin-Barnes method by AsyInt [Zhang]  
with help of `asy.m` [Smirnov], `MB.m` [Czakon], `HarmonicSums.m` and `Sigma.m` [Ablinger, Schneider]

5. Apply **Padé approximations** to  $\mathcal{O}(m_t^{120})$  expansion terms at the level of form factors as a **precision tool**

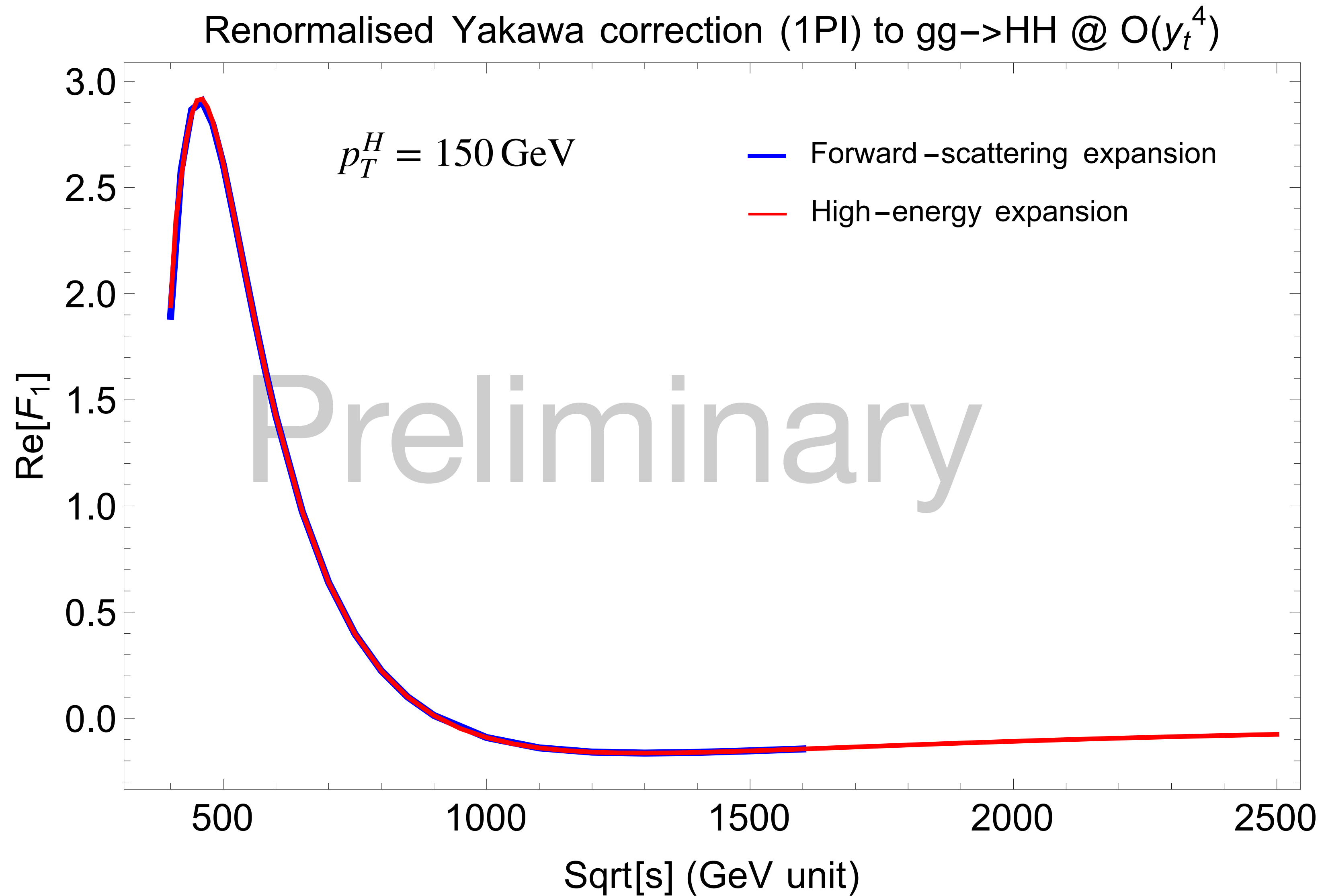


Released today in [2407.12107]





# Combination of F.S. and H.E. expansions @ NLO Yukawa



$$\mathcal{A}^{\mu\nu} = T_1^{\mu\nu} \mathcal{F}_1 + T_2^{\mu\nu} \mathcal{F}_2^{\mu\nu}$$

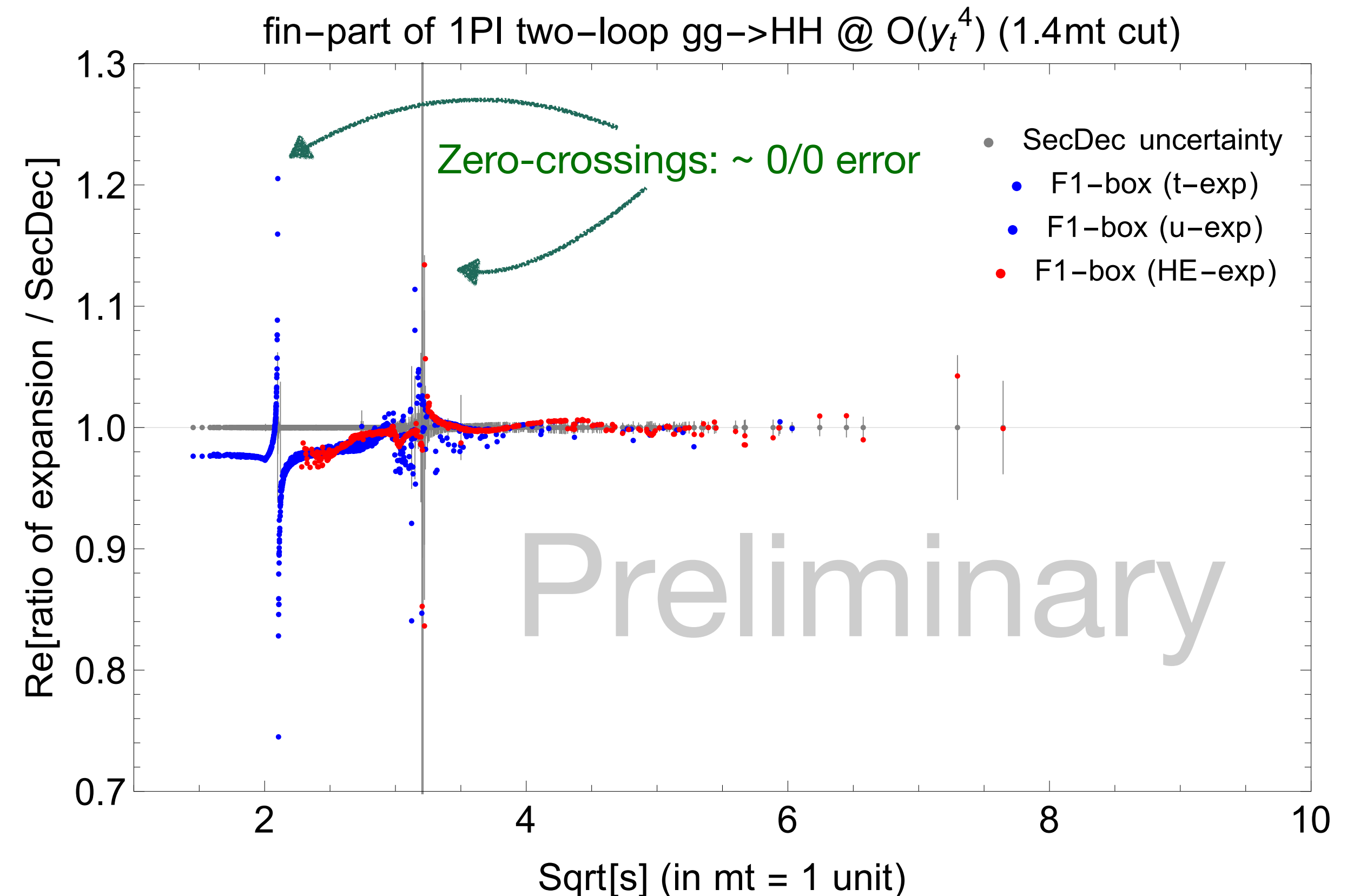
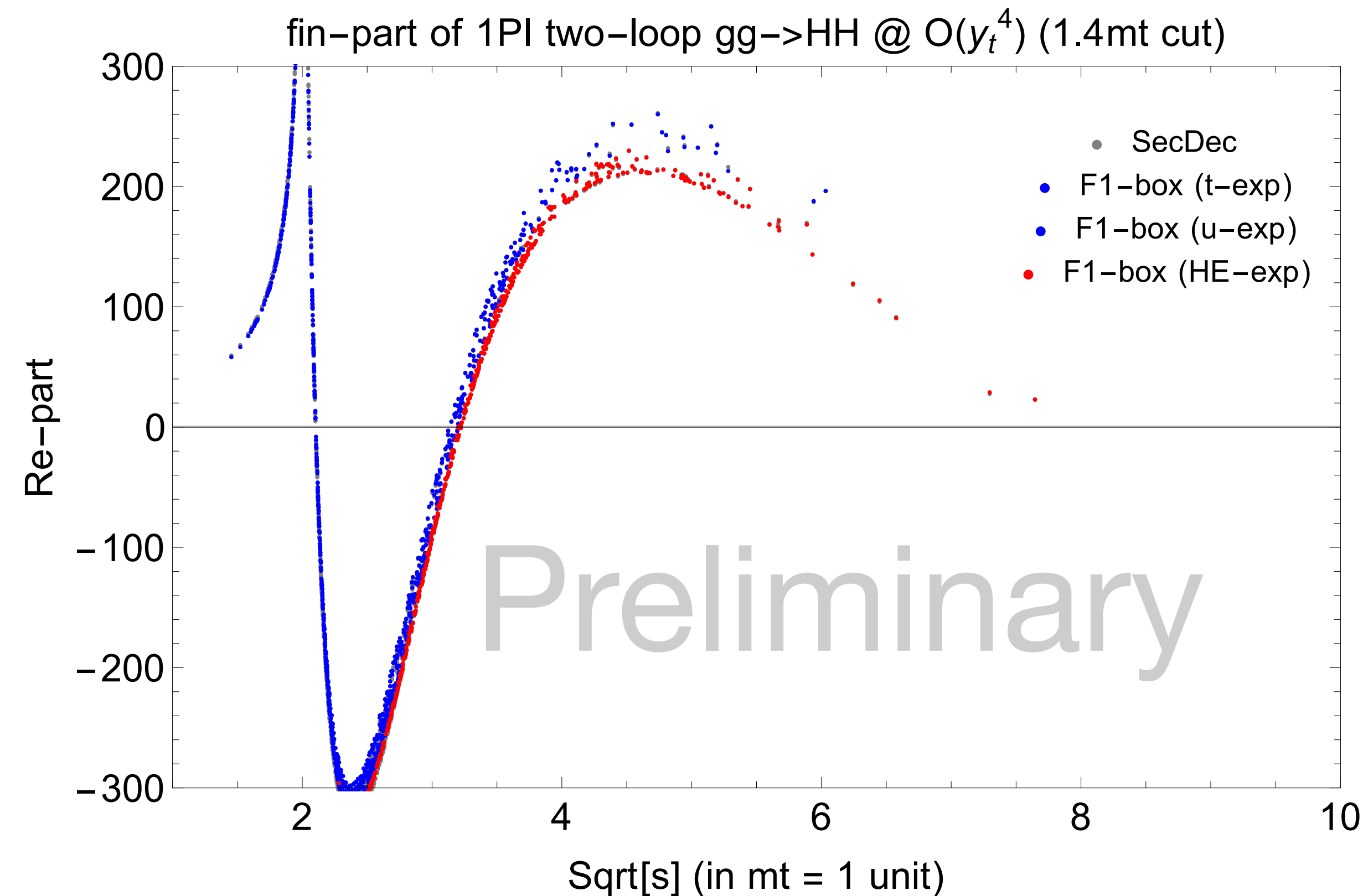
$$p_T^H = \sqrt{\frac{ut - m_H^4}{s}}$$

Highest available expansion terms are used

# Comparison to SecDec numerical results @ NLO Yukawa

Finite part of bare two-loop form factor comparison to SecDec group

[Heinrich, Jones, Kerne, Stone, Vestner, 2407.04653]



**High-energy expansion agree perfectly with SecDec results**

Forward-scattering expansion agree within 2% level with SecDec near production threshold  
(more expansion terms under computing)

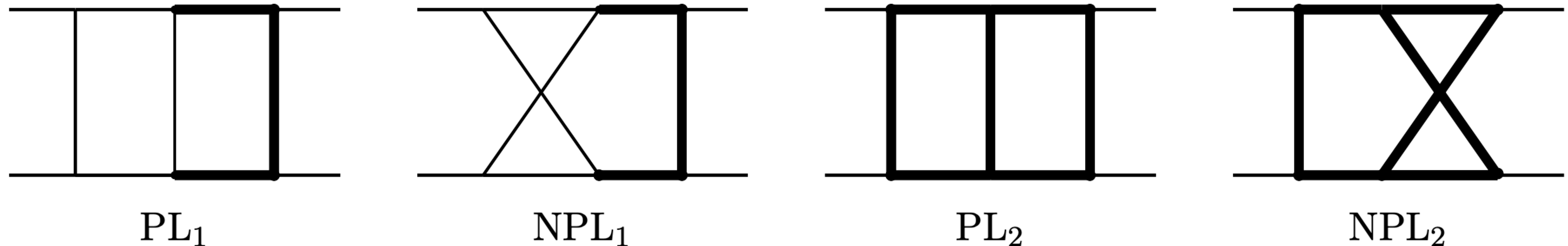
# AsyInt

by Hantian Zhang — *hep-ph [2407.12107]*

For analytic calculations of massive two-loop four-point integrals at high energies

Download at: <https://gitlab.com/asyint/asyint-public>

Sample Feynman diagrams calculated by AsyInt



Sample planar and non-planar diagrams. Thick lines denote massive propagators



leading H.E. terms to  $\epsilon$ -finite part  
@  $\mathcal{O}(1/m)$  and  $\mathcal{O}(m^0)$

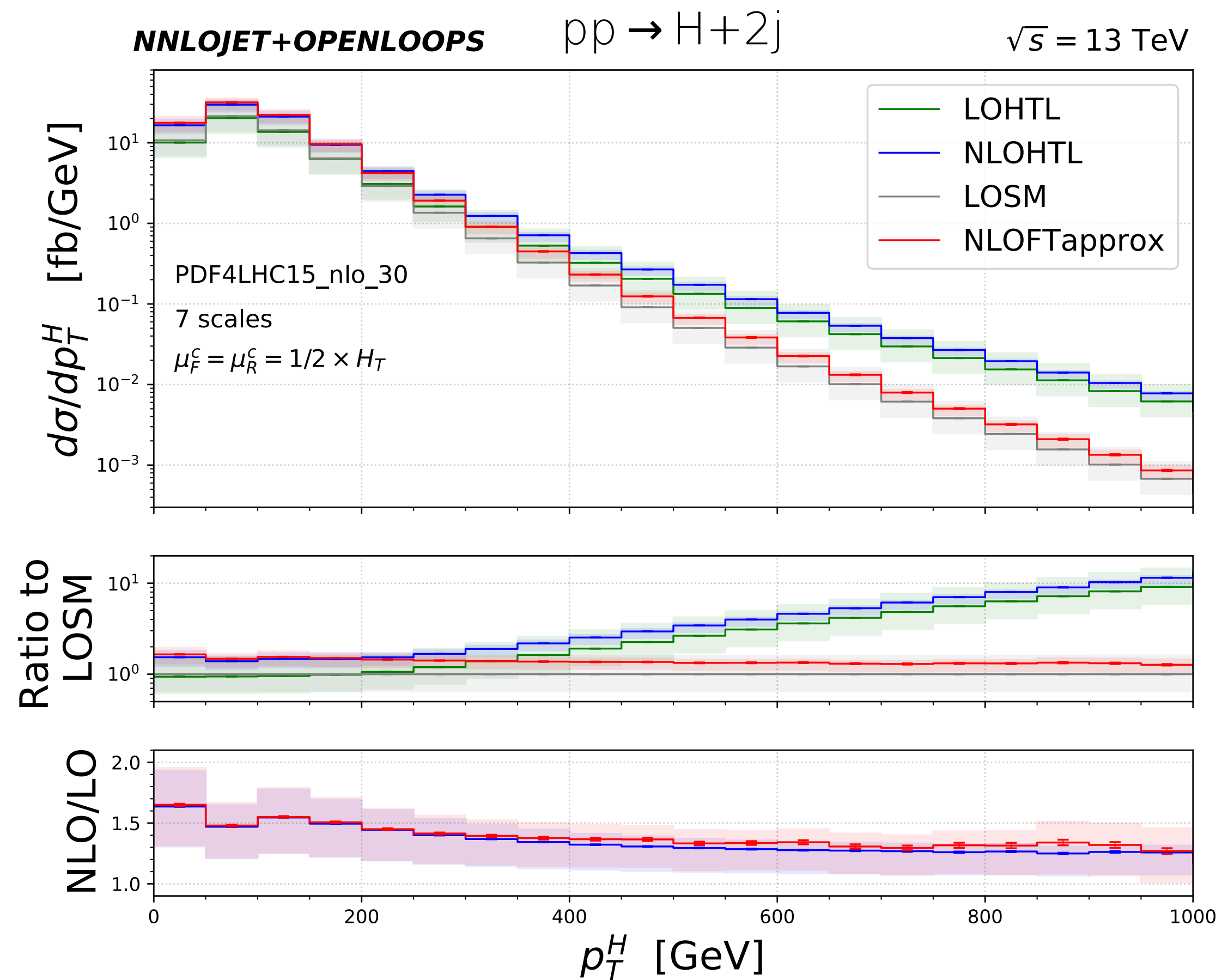
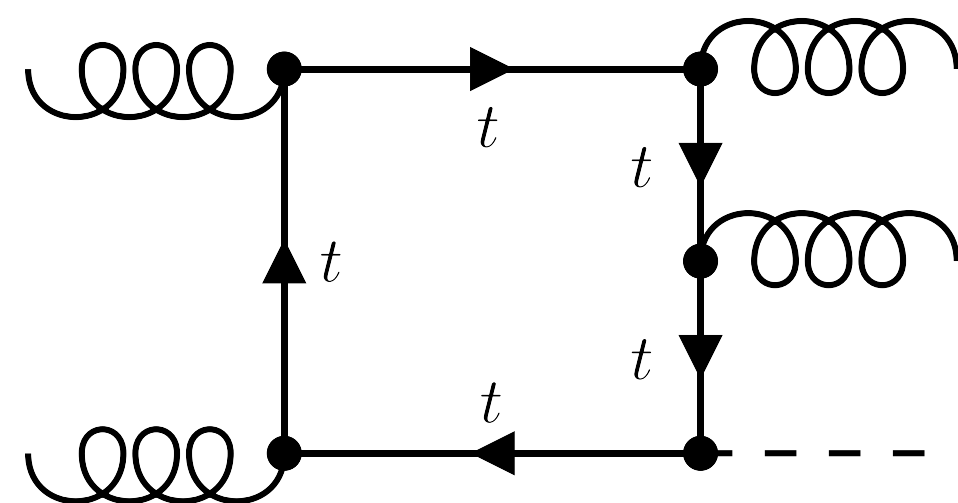
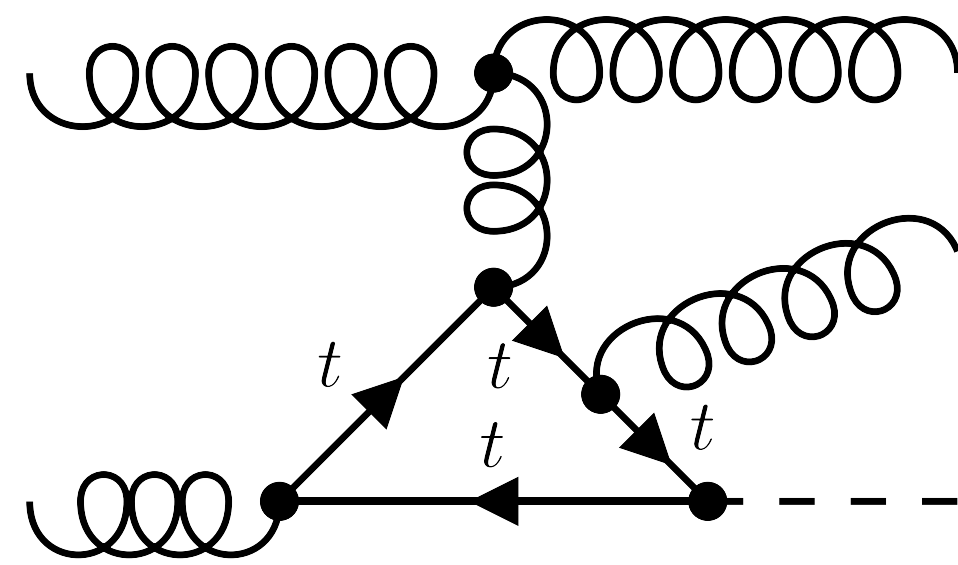
# Conclusions

- We compute **NLO leading Yukawa corrections** to  $gg \rightarrow HH$  in **forward-scattering expansion** and **high-energy expansion** [*JHEP 08 (2022) 259*]
  - Precise (semi)-analytic results for the whole phase space
  - Cross-checked with SecDec group's numerical results
- We compute **full top-induced NLO EW corrections** to  $gg \rightarrow HH$  and  $gg \rightarrow gH$  in large- $m_t$  expansion [*JHEP 10 (2023) 033*]
- We also compute factorisable EW corrections to  $gg \rightarrow HH$  analytically [*2407.05787*]
- **AsyInt** released in [*2407.12107*]
  - Toolbox for analytic calculations of massive two-loop four-point Feynman integrals at high energies

# Backup Slides

# Higgs+2 jets @ NLO QCD

- Dominant channel for Higgs boson production with large transversal momentum  $p_T^H$  at LHC



$p_T^H$  spectrum:  
crucial for studying  
Higgs boson properties

NLOSM  $\Rightarrow$  NLO QCD with  
top-mass dependence

First NLO Higgs + 2 jets calculation with top-mass dependence

[Chen, Huss, Jones, Kerner, Lang, Lindert, Zhang, *JHEP* 03 (2022) 096]

# Forward scattering expansion @ NLO Yukawa

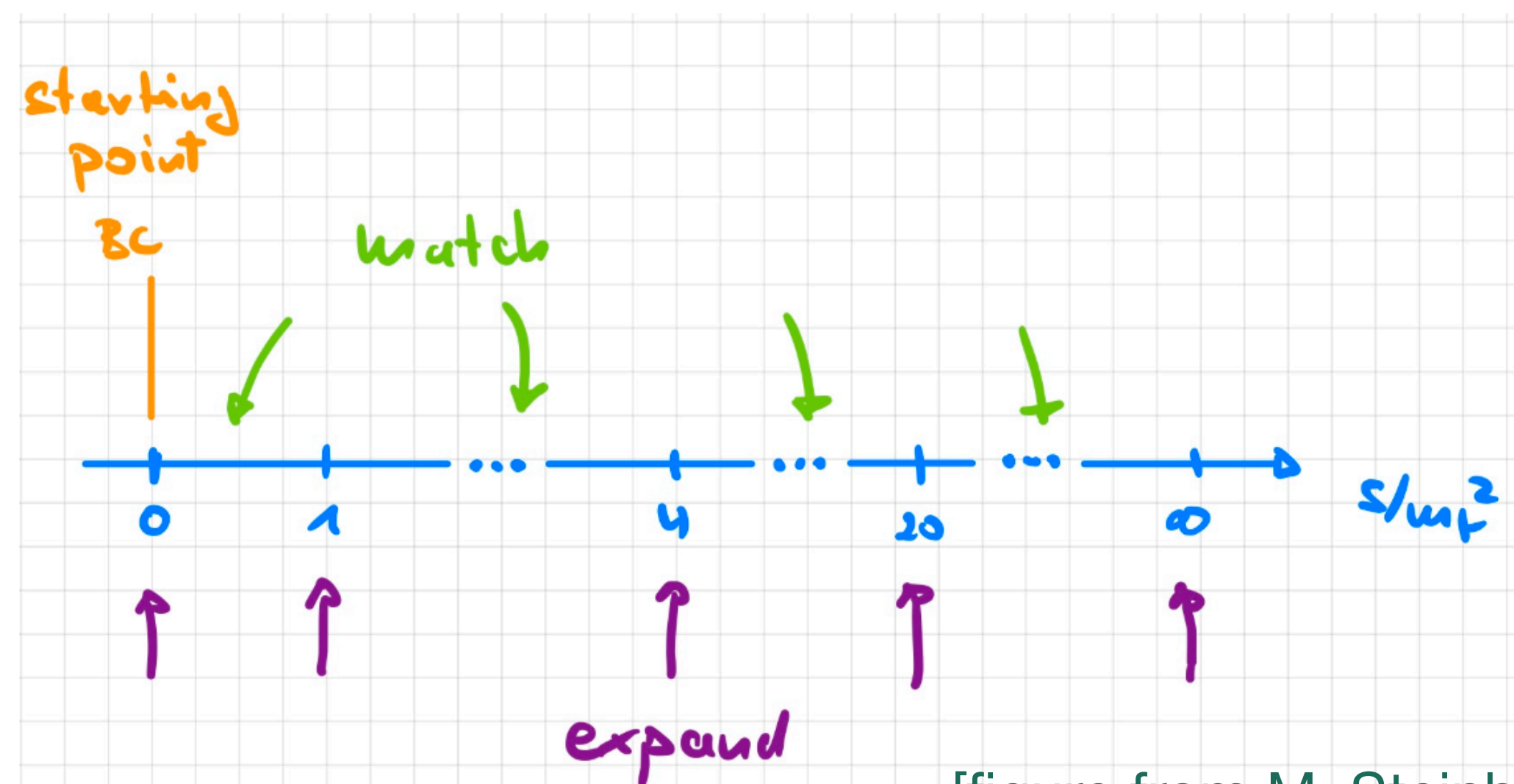
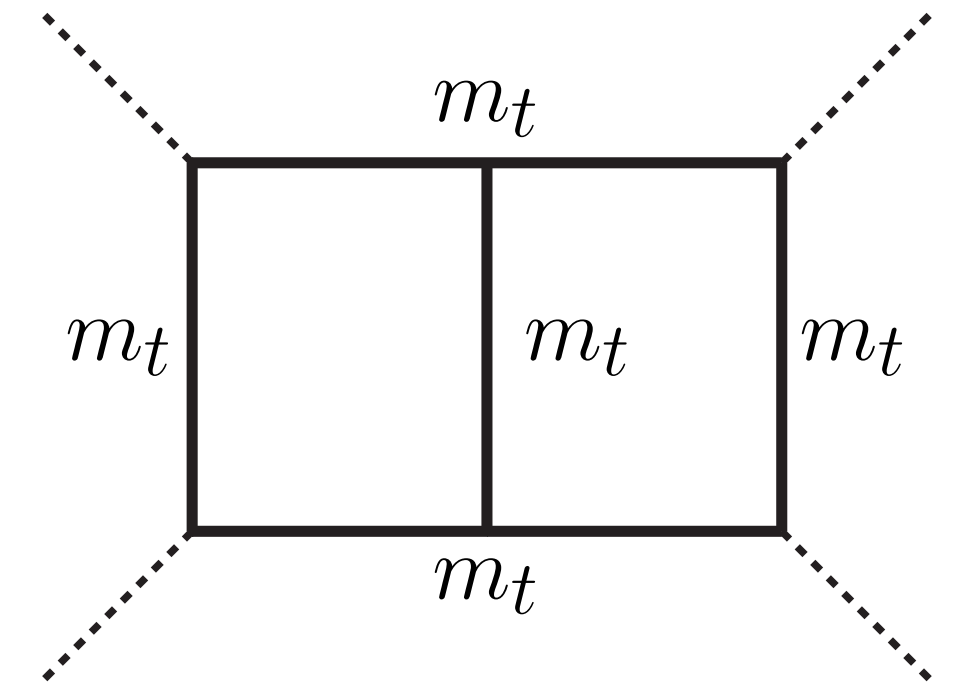
1. **Taylor expansion in  $t \rightarrow 0$** :  $t$ -series expressed in terms of MIs  $I(s, m_t^2)$

[Davies, Mishima, Schönwald, Steinhauser, 23']

2. Compute boundary conditions at  $s/m_t^2 \rightarrow 0$  limit

3. Use **“Expand and match”** method evolve  $I(s, m_t^2)$  towards  $s/m_t^2 \rightarrow \infty$

through differential equations [Fael, Lange, Schönwald, Steinhauser, 21', 22']

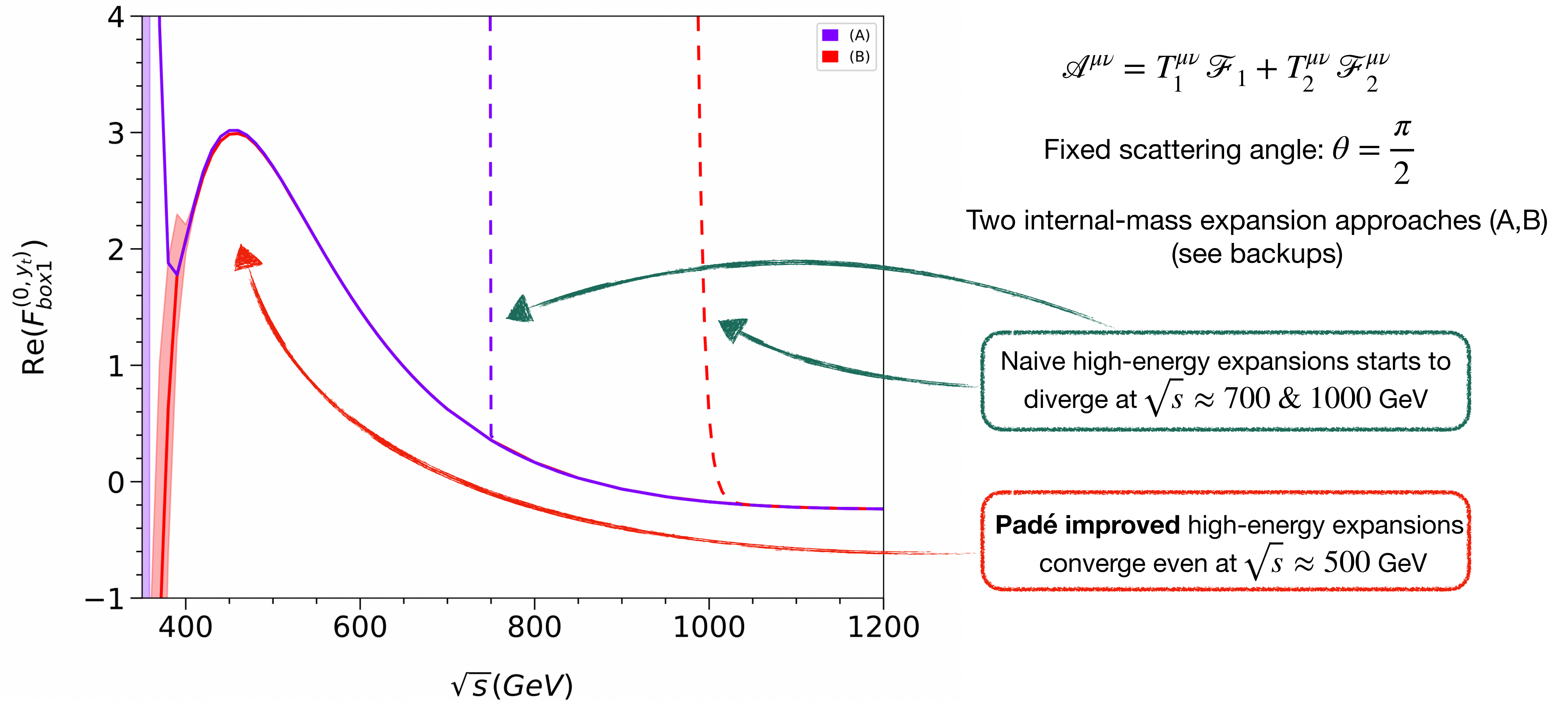


[figure from M. Steinhauser]

[See talk by M. Steinhauser for more details]

# High energy expansion @ NLO Yukawa

[Davies, Mishima, Schönwald, Steinhauser, Zhang, *JHEP* 08 (2022) 259]



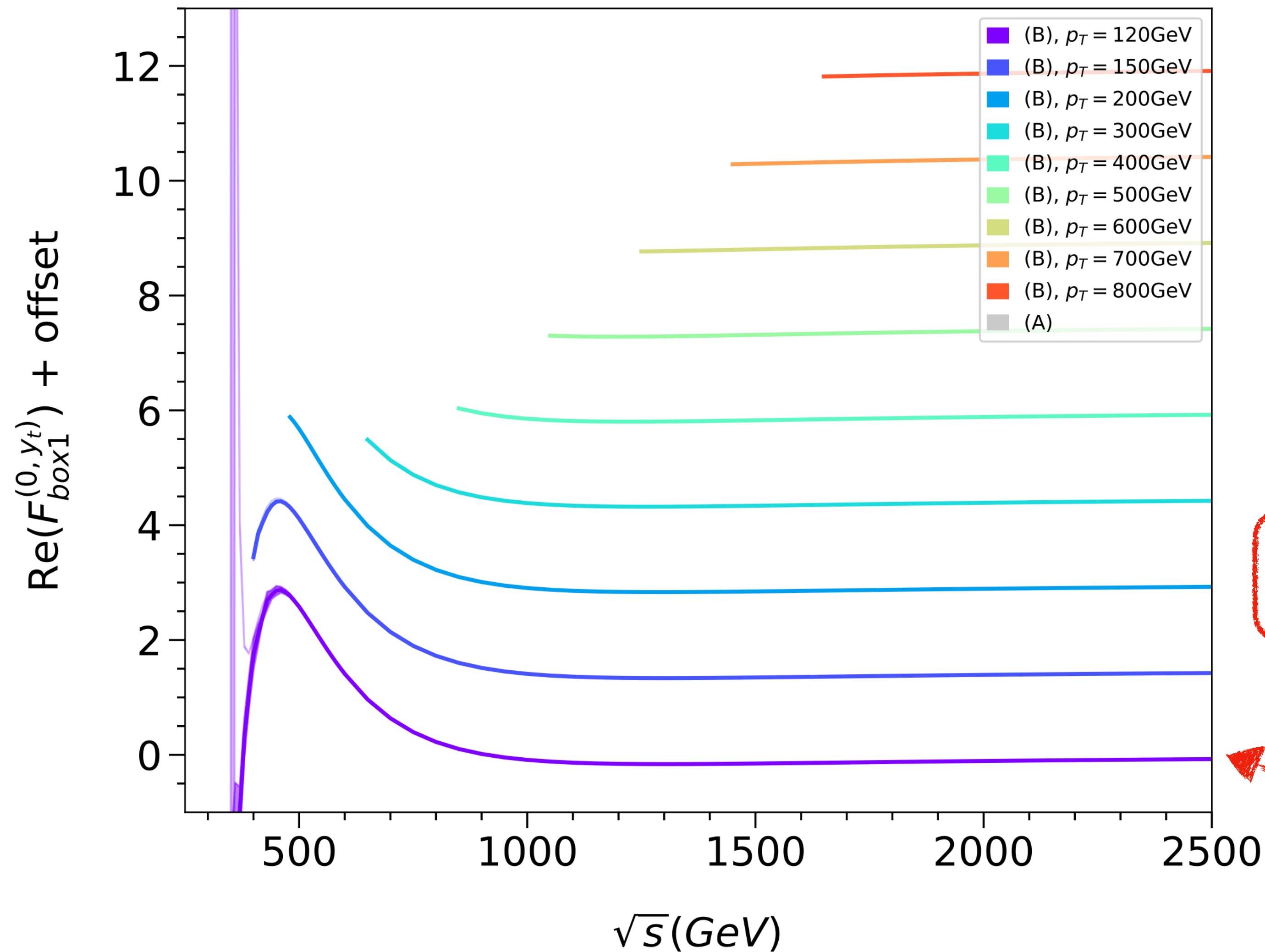
**Solid color lines:** Padé improved results using MIs from  $\mathcal{O}(m_t^{116})$  in two expansion approaches

**Dashed color lines:** Naive expansions at high energies to  $\mathcal{O}(m_t^{116})$



# High energy expansion @ NLO Yukawa

[Davies, Mishima, Schönwald, Steinhauser, Zhang, *JHEP* 08 (2022) 259]



$$\mathcal{A}^{\mu\nu} = T_1^{\mu\nu} \mathcal{F}_1 + T_2^{\mu\nu} \mathcal{F}_2$$

$$p_T^H = \sqrt{\frac{ut - m_H^4}{s}}$$

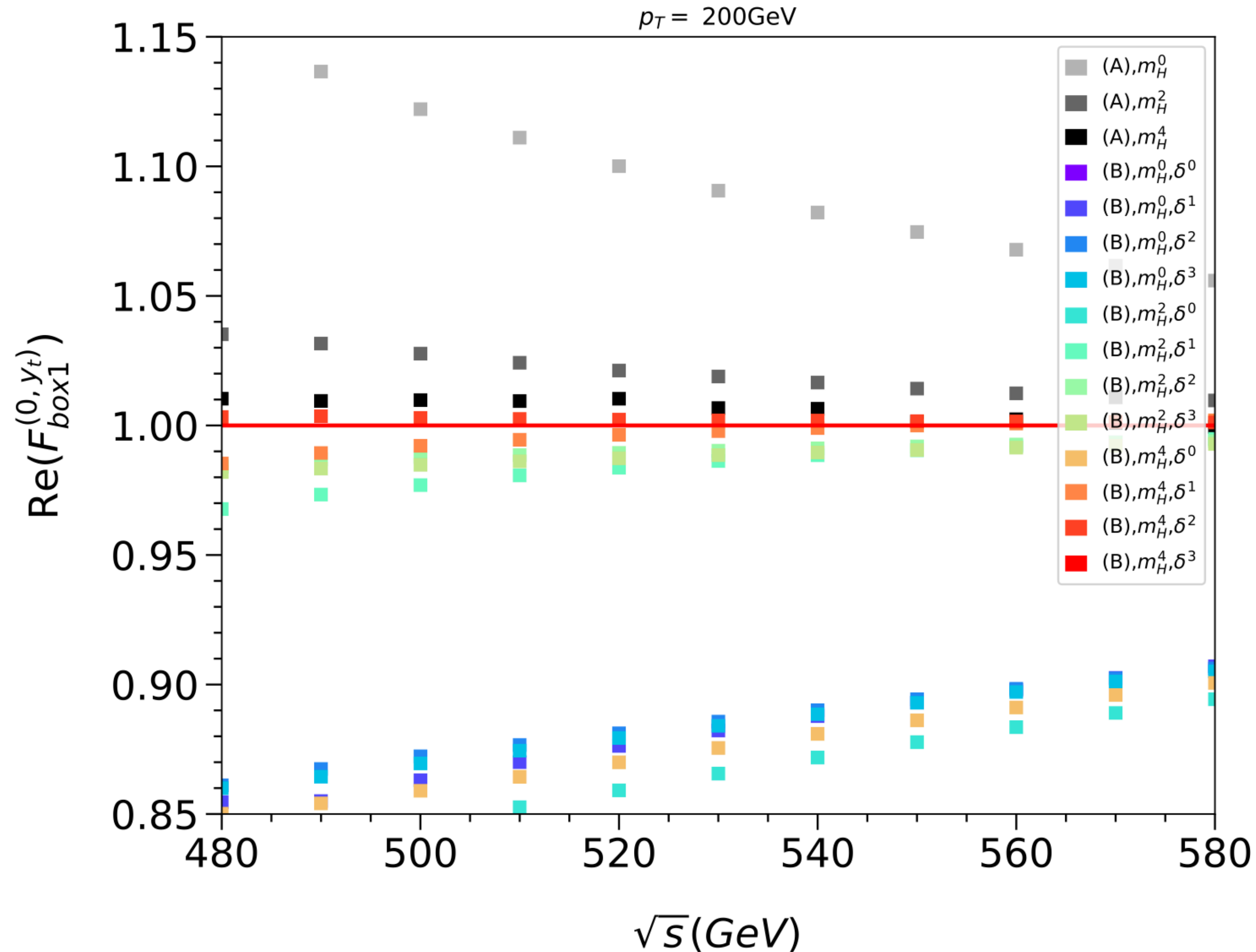
**Padé improved** high energy expansions converge even at  $p_T^H = 120$  GeV

**Color lines:** Padé improved equal-mass  $\delta$  expansions in  $m_t^2 \approx (m_H^{\text{int}})^2$  using MIs from  $\mathcal{O}(m_t^{116})$

**Grey lines:** Coincide with colourful lines (two approaches agree)

# Convergence of H.E. expansions for $gg \rightarrow HH$ form factors

[Davies, Mishima, Schönwald, Steinhauser, Zhang, *JHEP* 08 (2022) 259]



$$\mathcal{A}^{\mu\nu} = T_1^{\mu\nu} \mathcal{F}_{\text{box1}} + T_2^{\mu\nu} \mathcal{F}_{\text{box2}}$$

The benchmark is expansion at  $\mathcal{O}\left(m_{H(\text{ext})}^4, \delta^3, m_t^{116}\right)$ .

$$\delta = 1 - \frac{m_H^{(\text{int})}}{m_t}$$

**Color points:** Convergence plot of different expansion orders by ratios to the benchmark at fixed  $p_T^H = 200$  GeV.