

# Subleading Higgs effects in $e^+e^- \rightarrow \text{fermion} + \text{antifermion}$

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Prague  
Czech Republic



**NAWI Graz**  
Natural Sciences

**FWF** Österreichischer  
Wissenschaftsfonds



# What's up?

Review: 1712.04721  
Update: 2305.01960

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Subtle field theory creates new effects  
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See review for background!

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  - Peaks in (experimental) cross-sections

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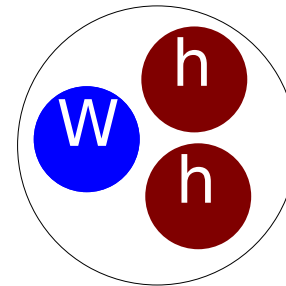
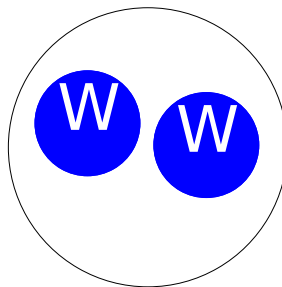
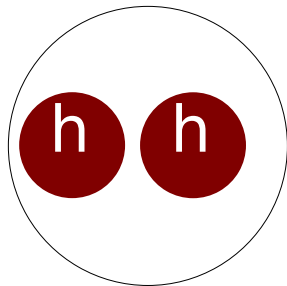
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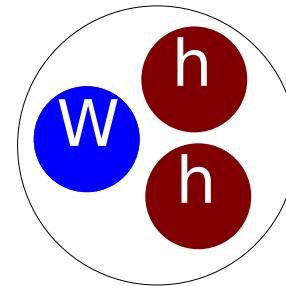
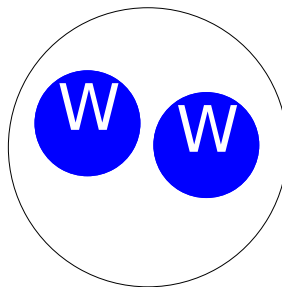
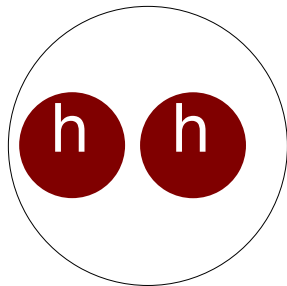


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- Why does perturbation theory work?
  - Fröhlich-Morchio-Strocchi mechanism



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[Fröhlich et al.'80,'81  
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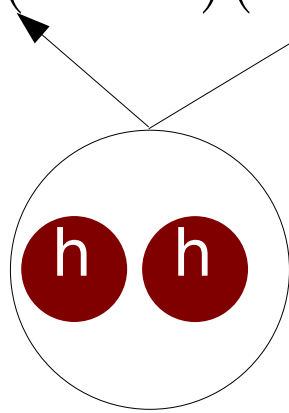


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Trivial two-particle state

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Standard  
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What about  
this? →

$$+v \langle \eta^\dagger \eta^2 + \eta^{\dagger 2} \eta \rangle + \langle \eta^{\dagger 2} \eta^2 \rangle$$

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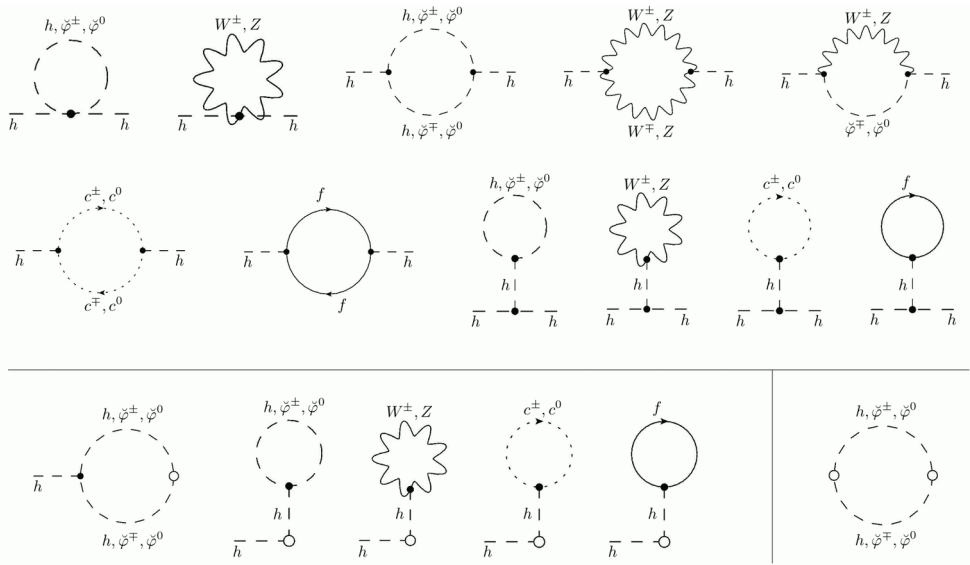
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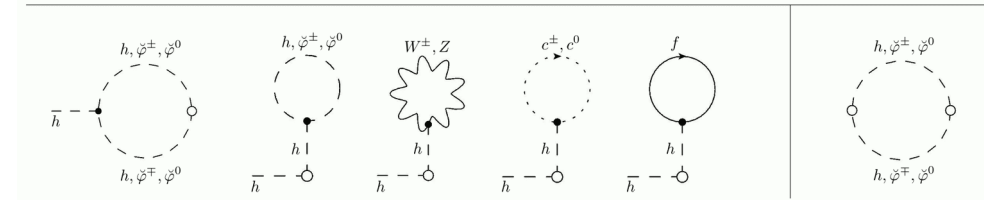
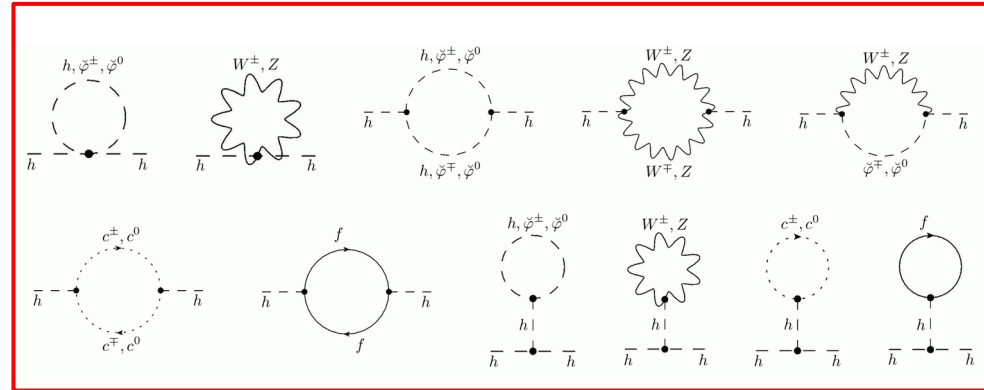
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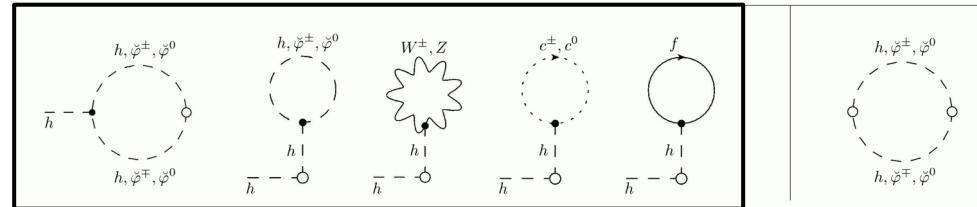
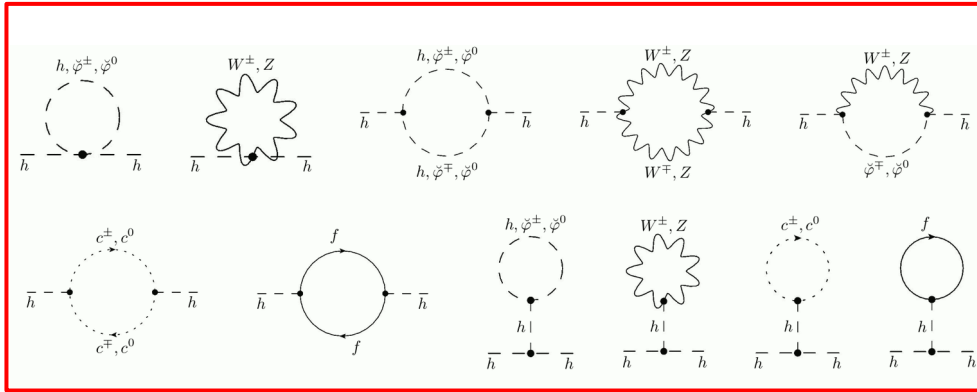
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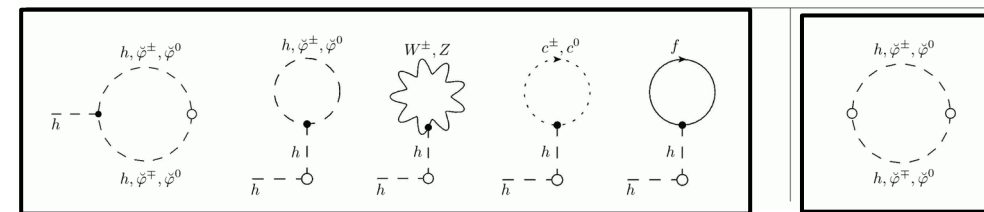
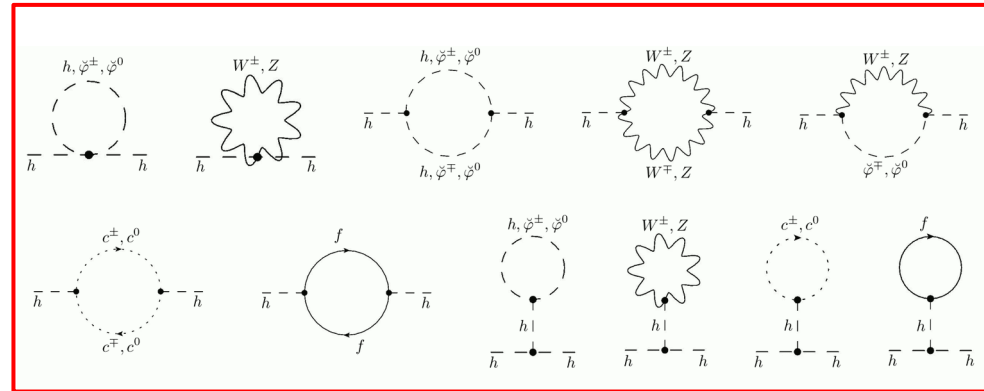
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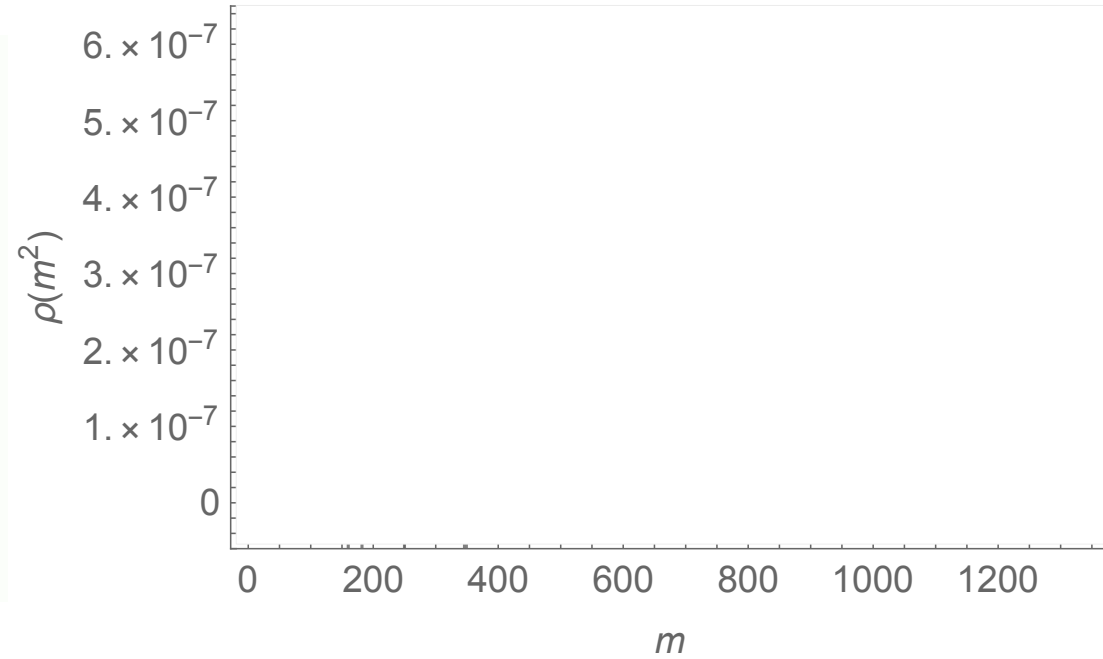
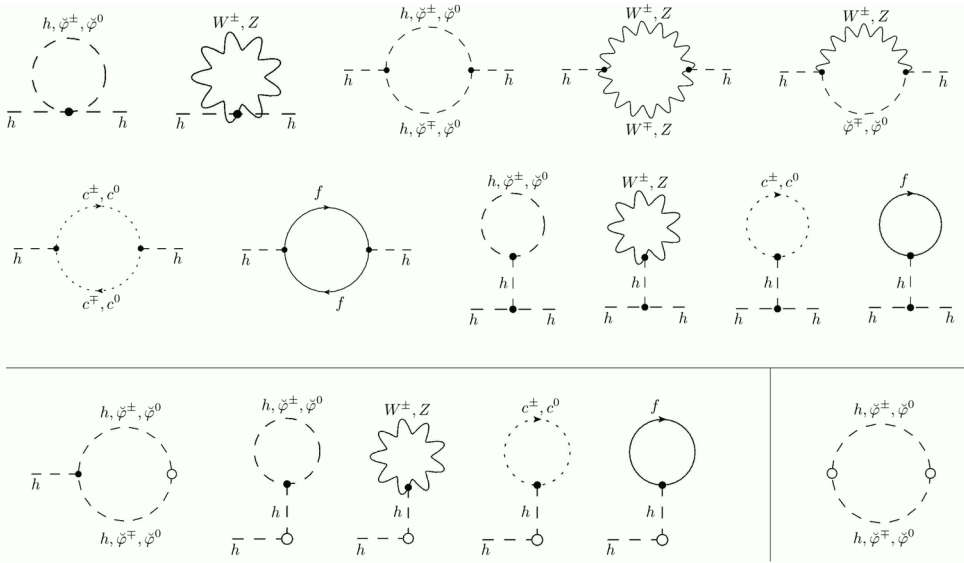


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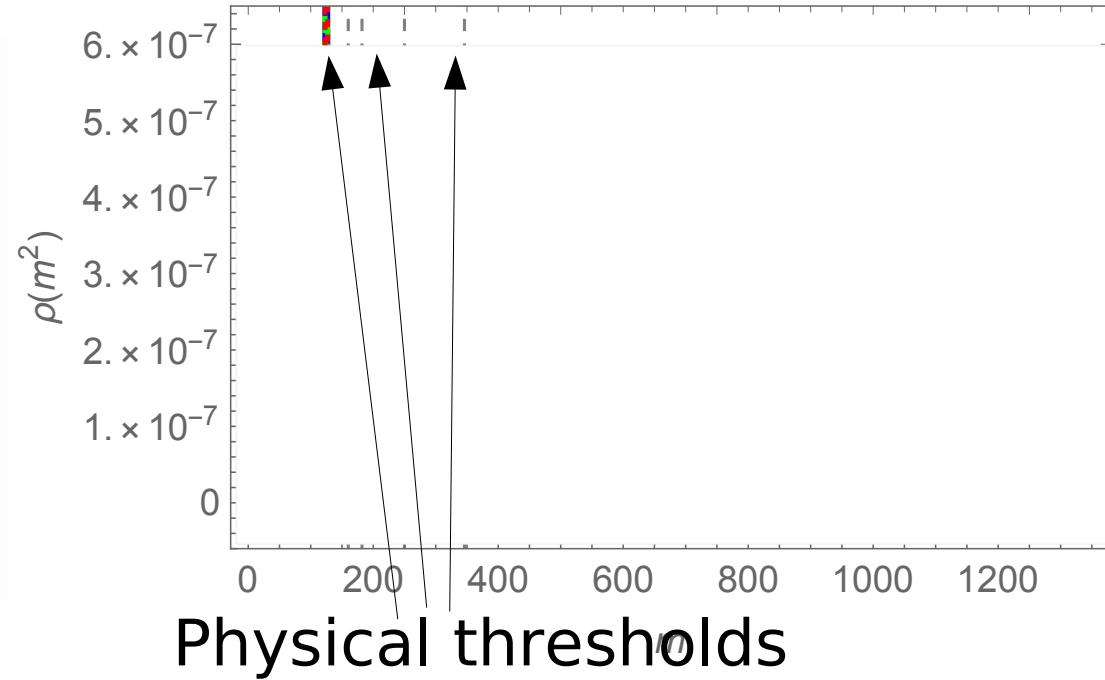
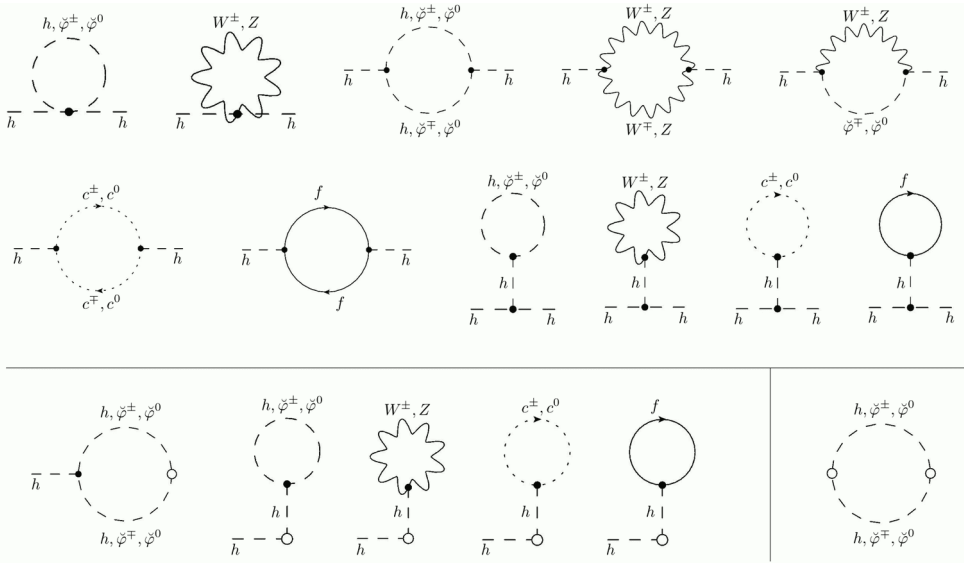


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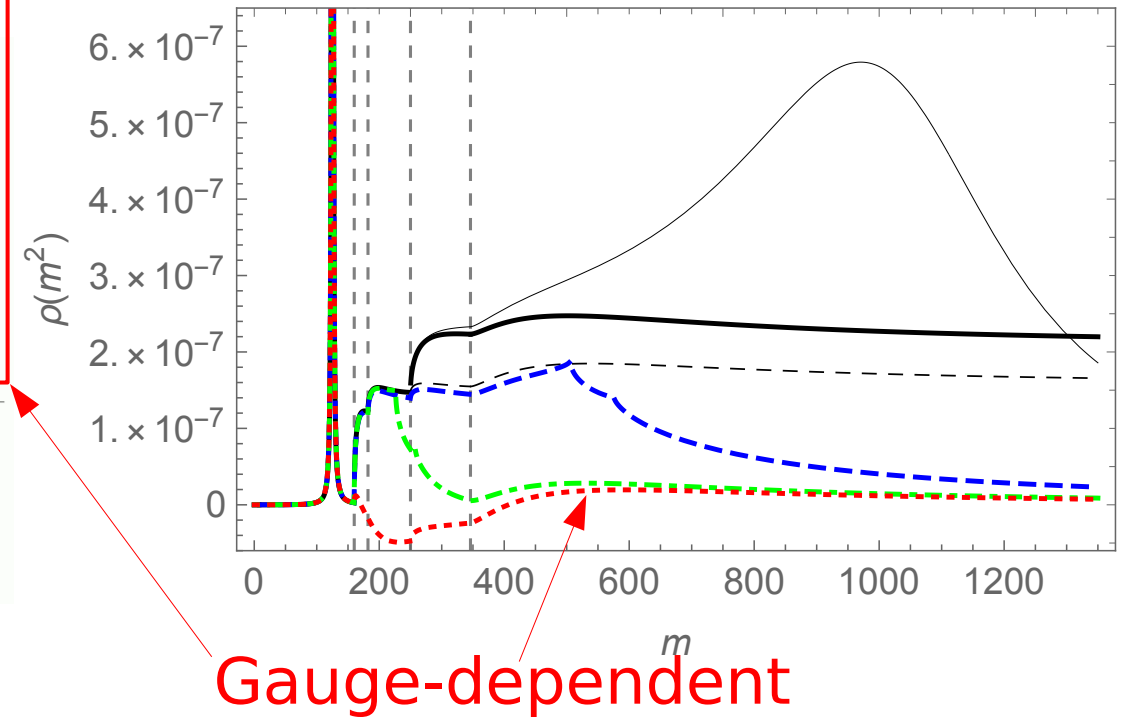
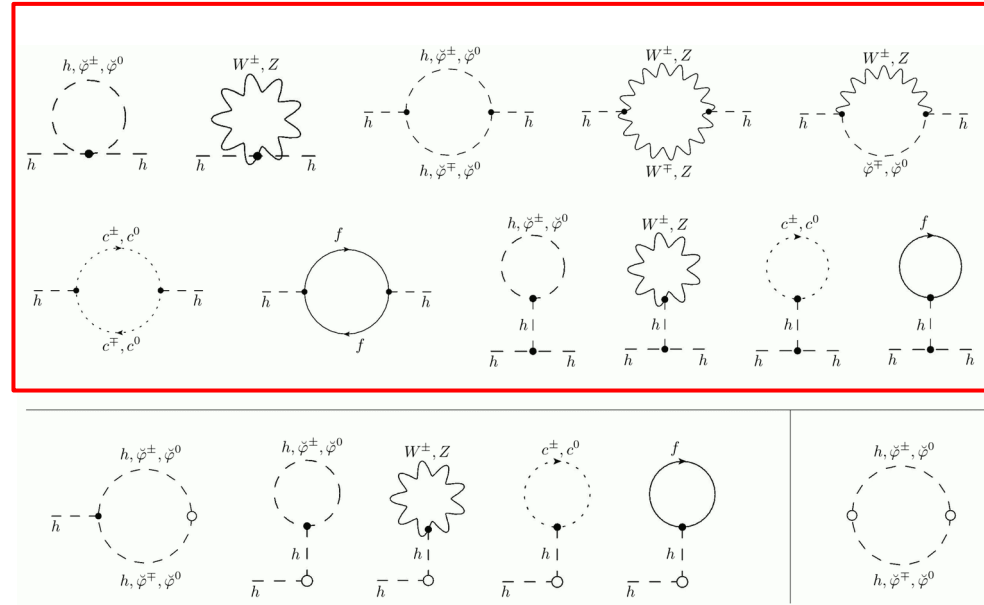
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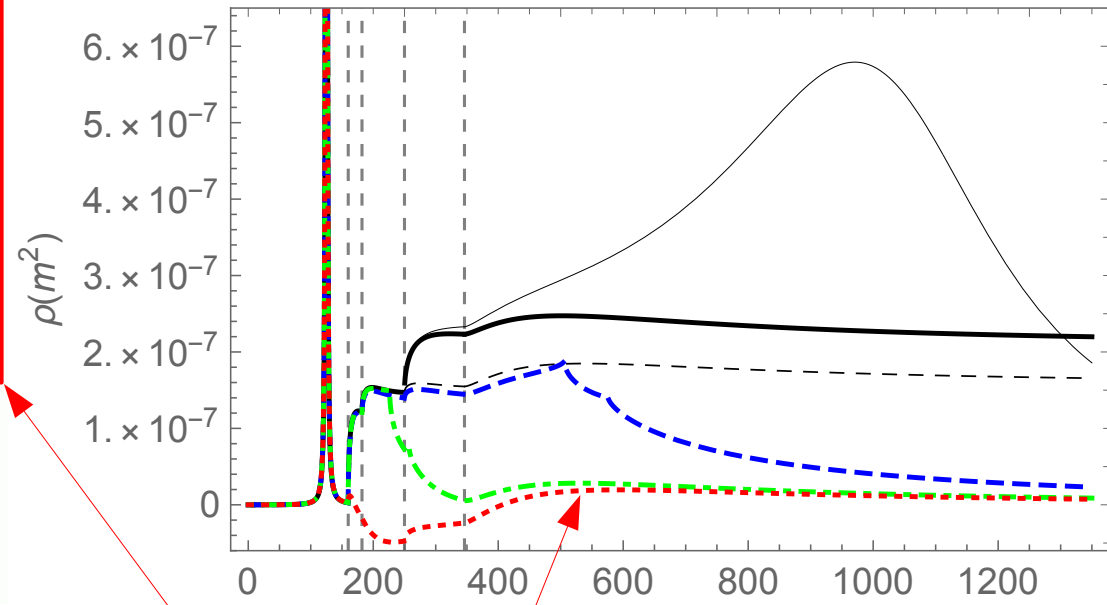
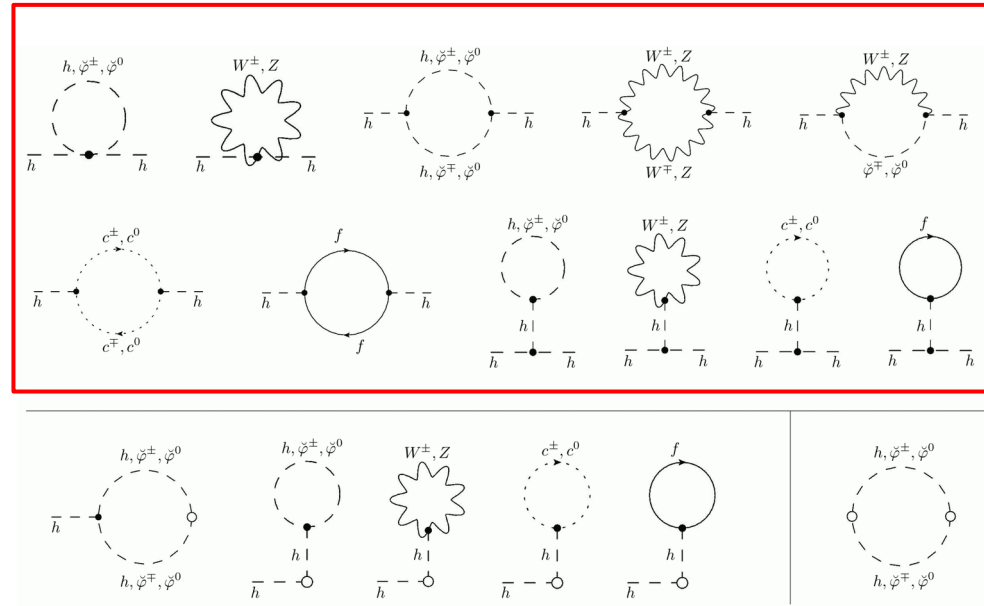
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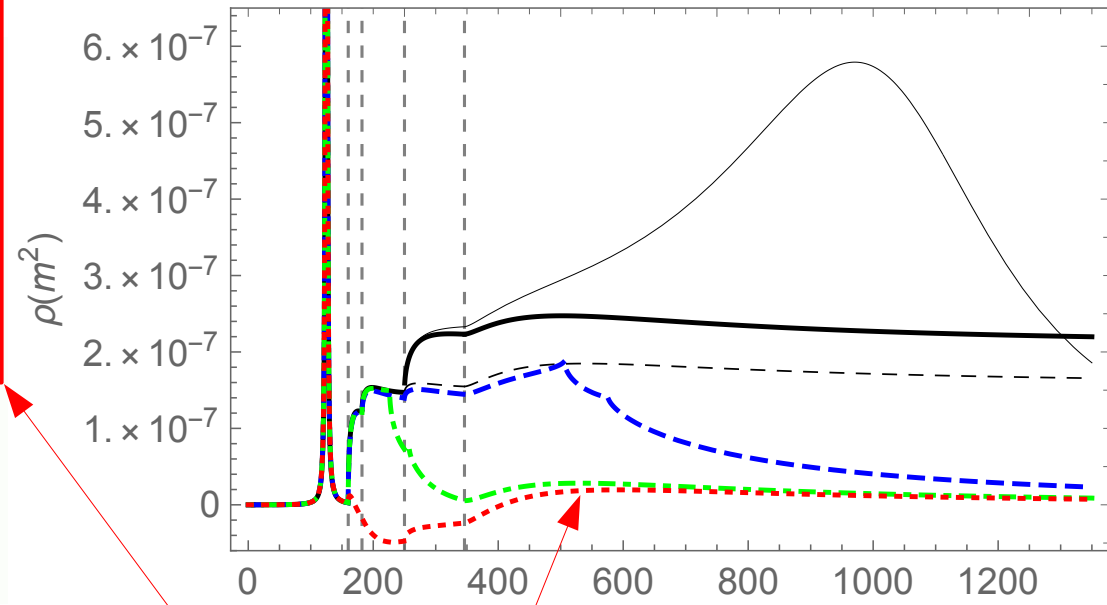
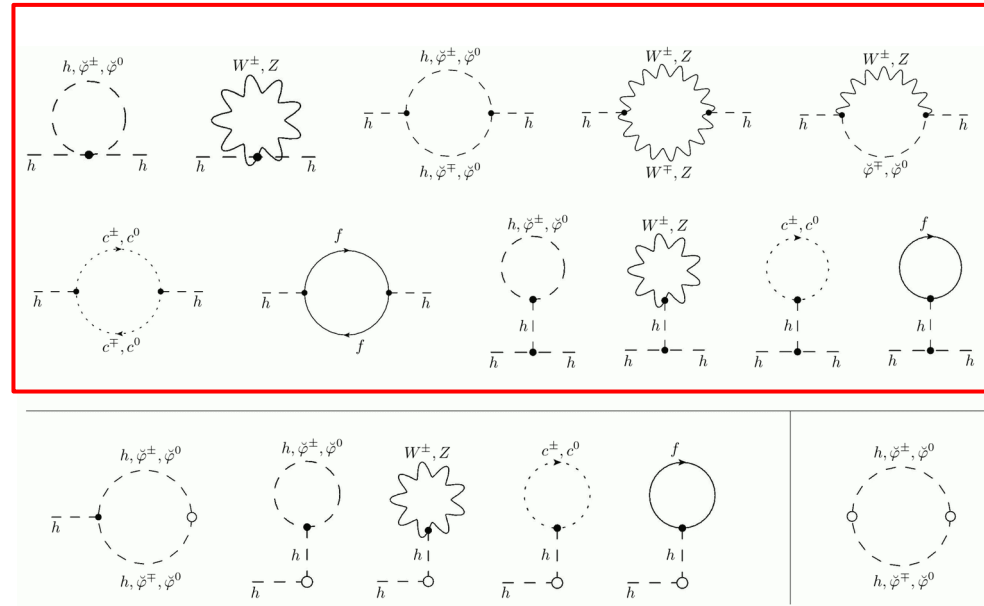


# Augmented perturbation theory



**Gauge-dependent**  
 Unphysical features:  
 Positivity violation  
 Additional thresholds

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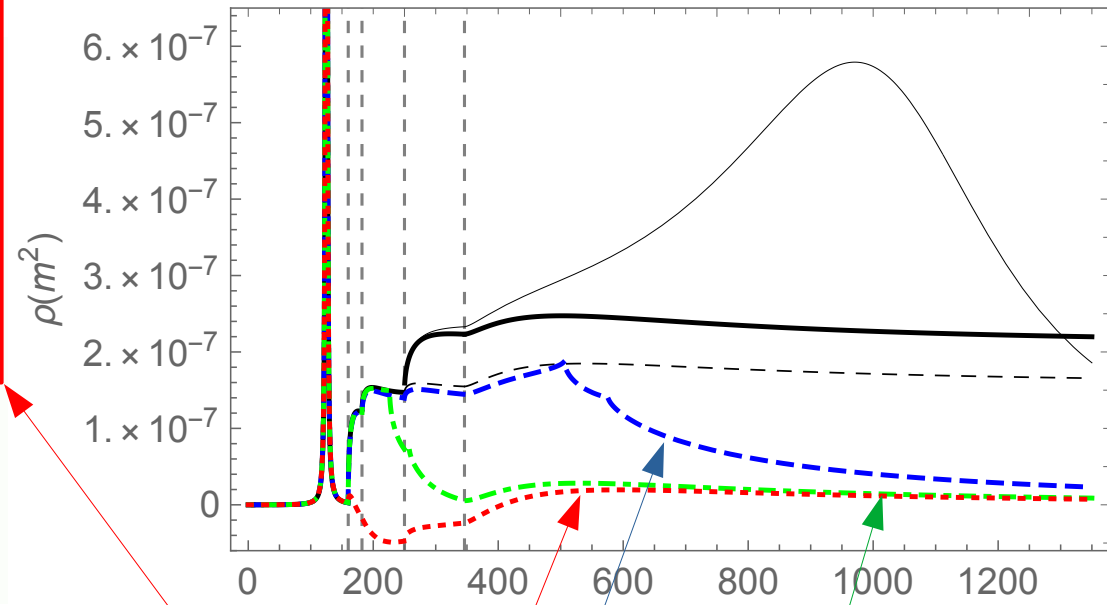
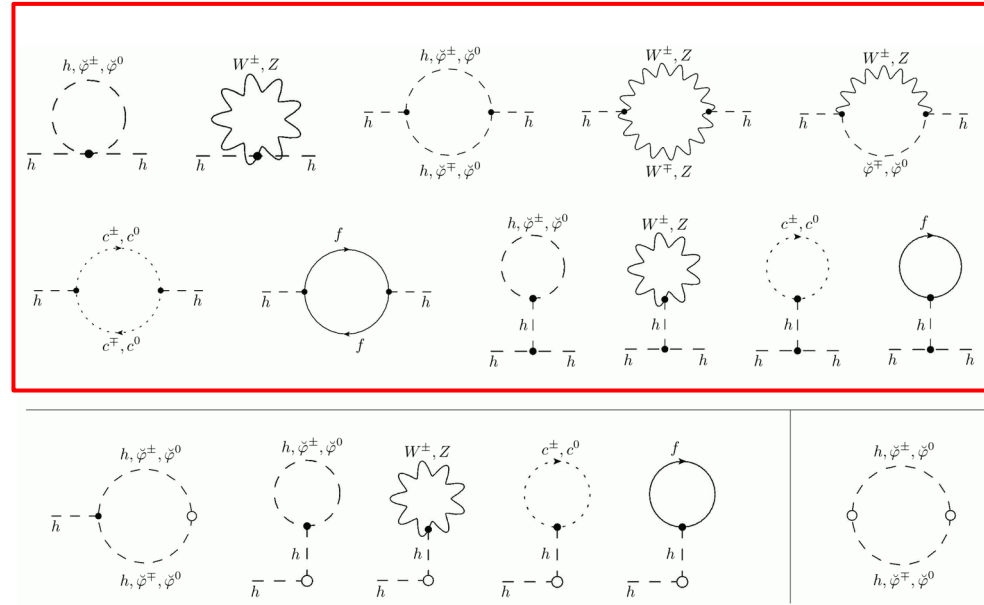


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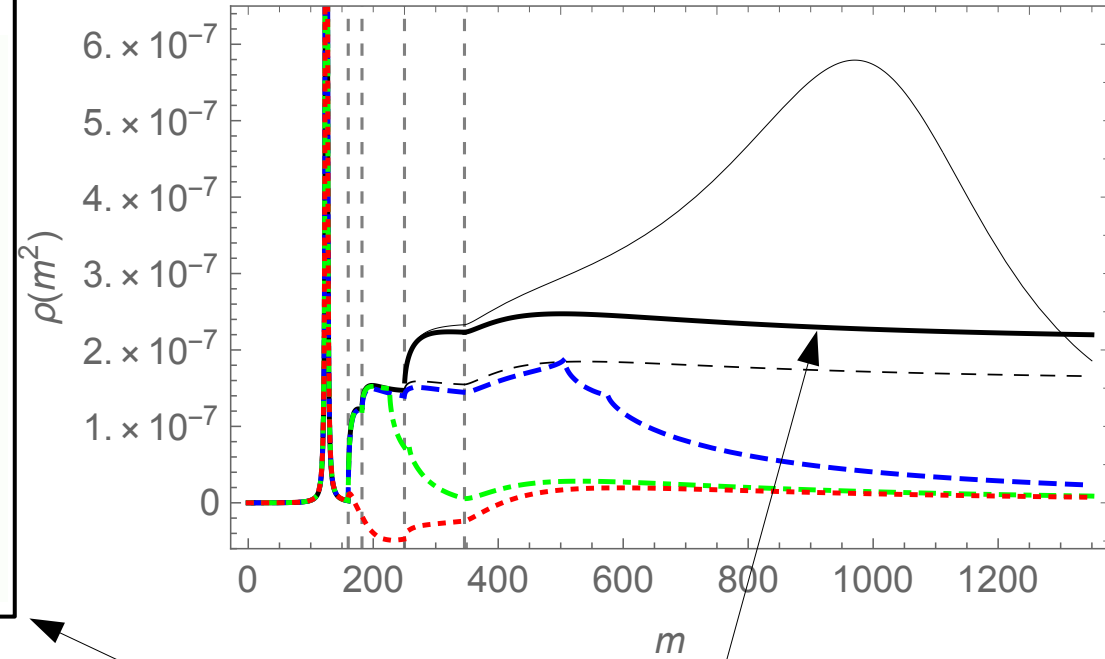
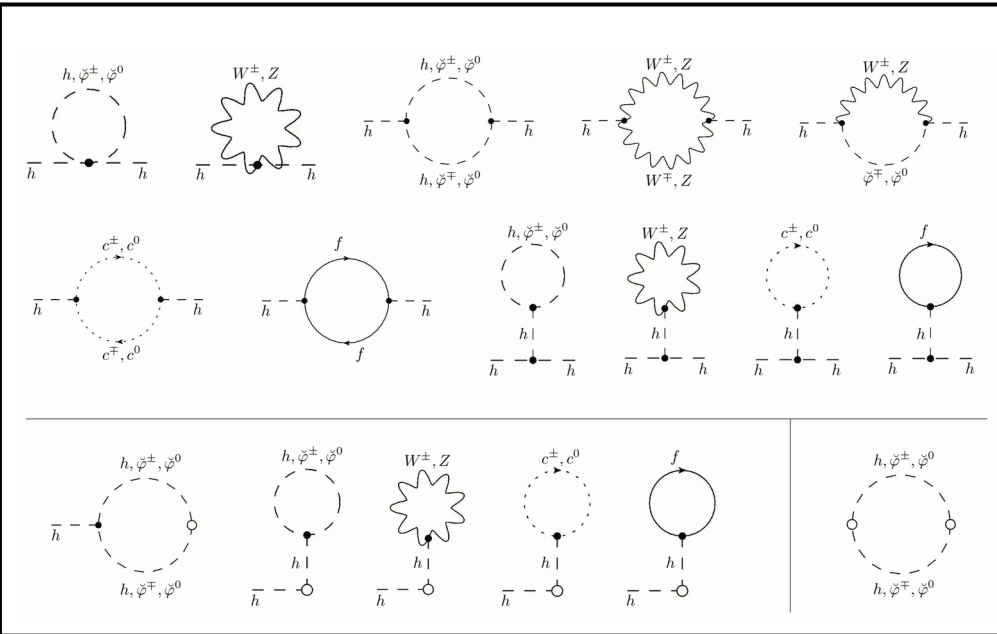
Not a consequence  
of instability: Occurs even  
for an asymptotically stable  
Higgs in a toy theory

# Augmented perturbation theory



Gauge-dependent  
Other gauge choices

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Physical - same for all gauge choices



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  - Global  $SU(3)$  generation
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- Can this be true? Lattice test

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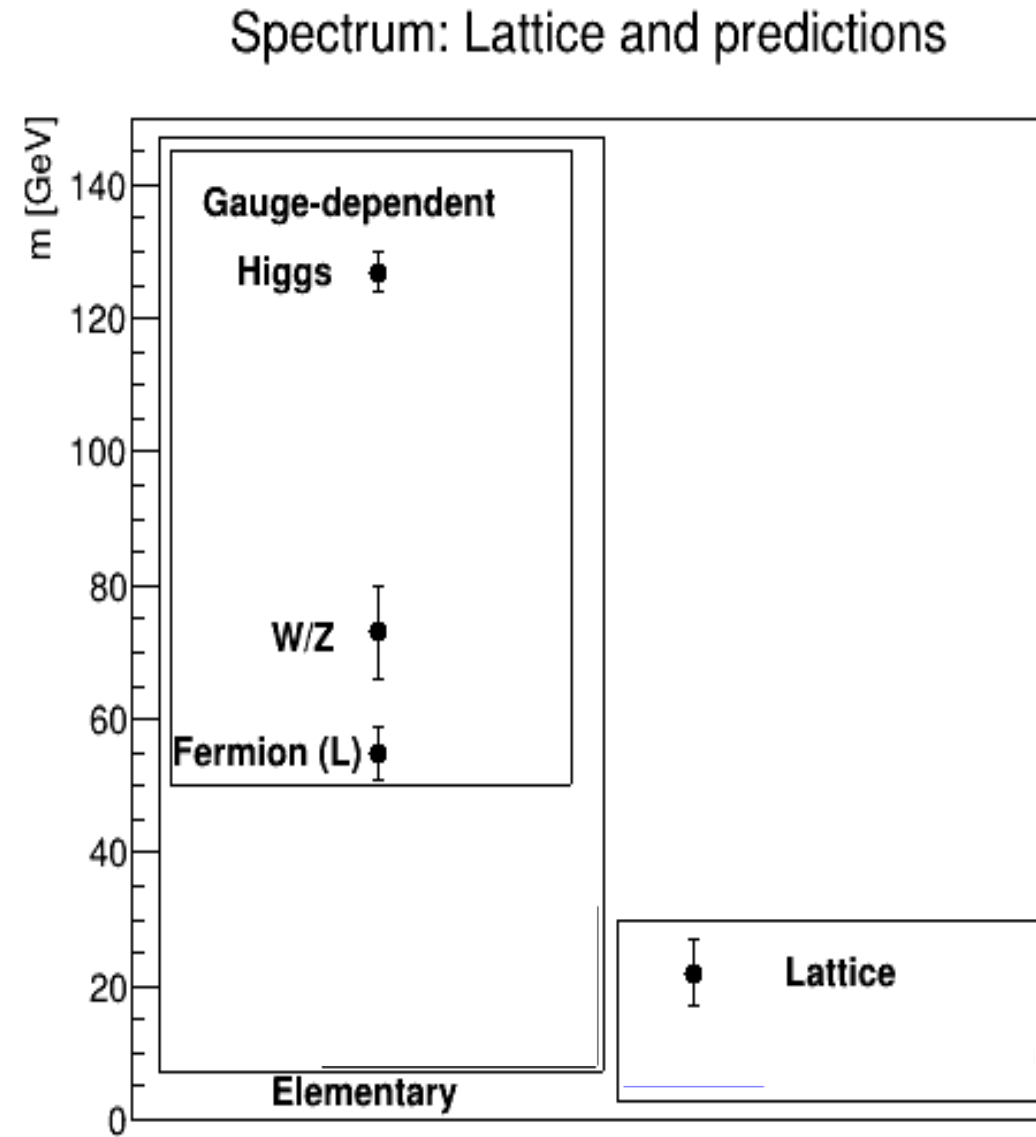
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- Same qualitative outcome
  - FMS construction
  - Mass defect
  - Flavor and custodial symmetry patterns

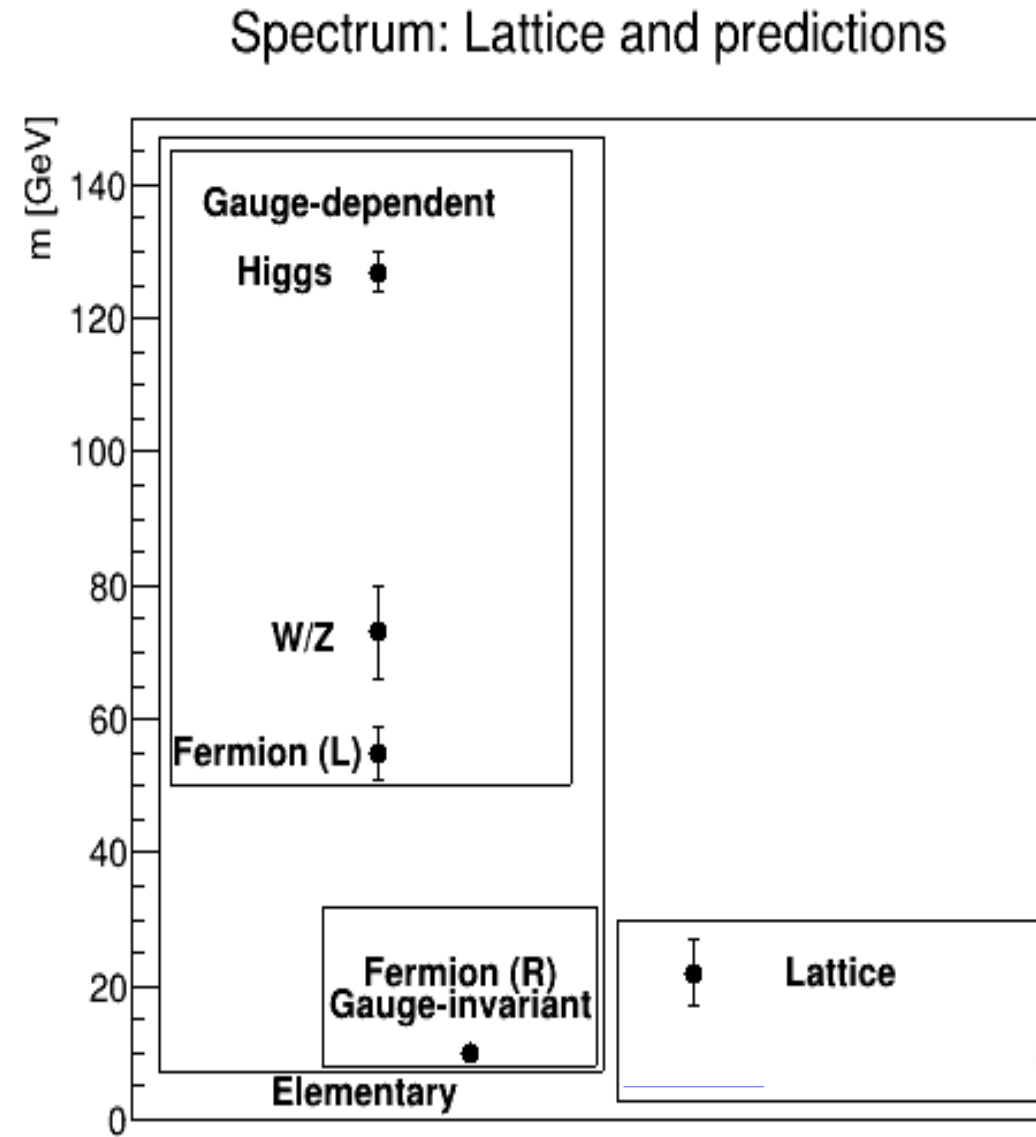
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  - Quenched
- Same qualitative outcome
  - FMS construction
  - Mass defect
  - Flavor and custodial symmetry patterns



# Flavor on the lattice

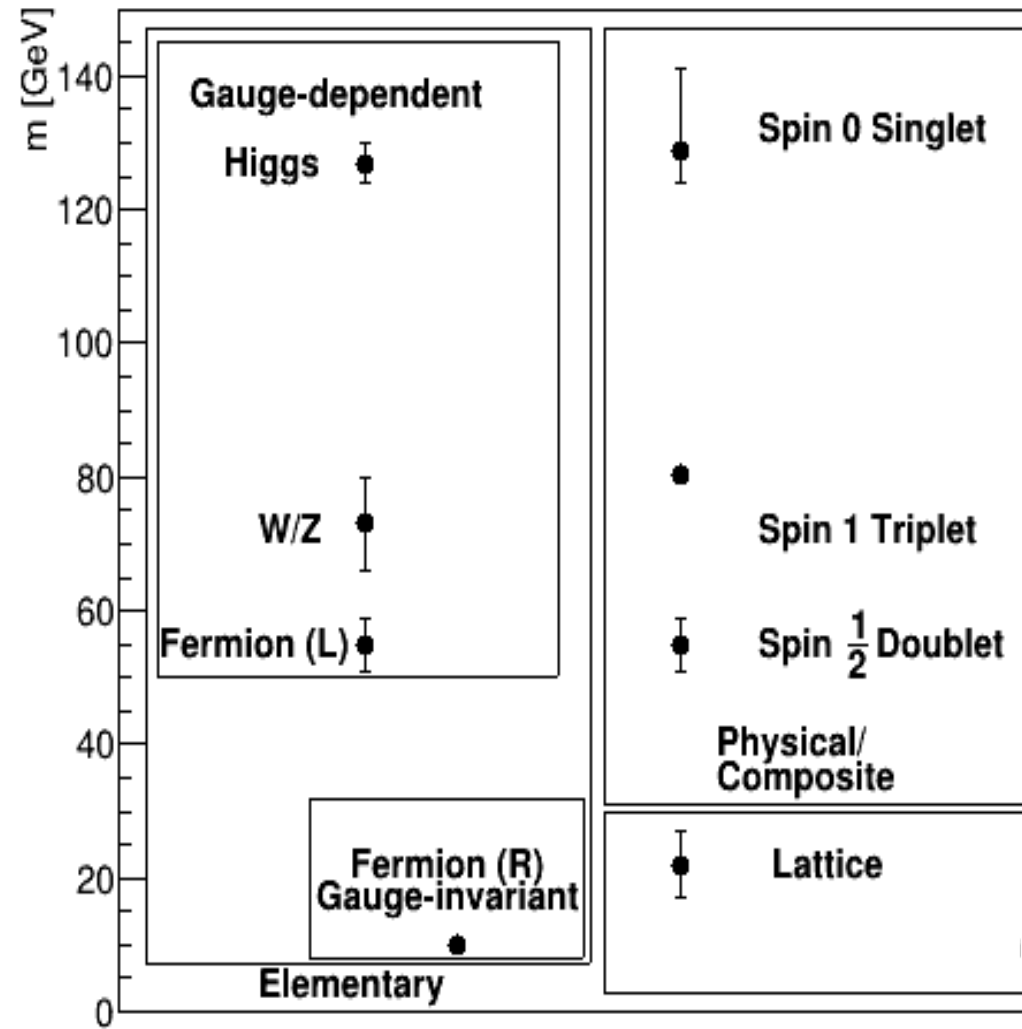
- Only mock-up standard model
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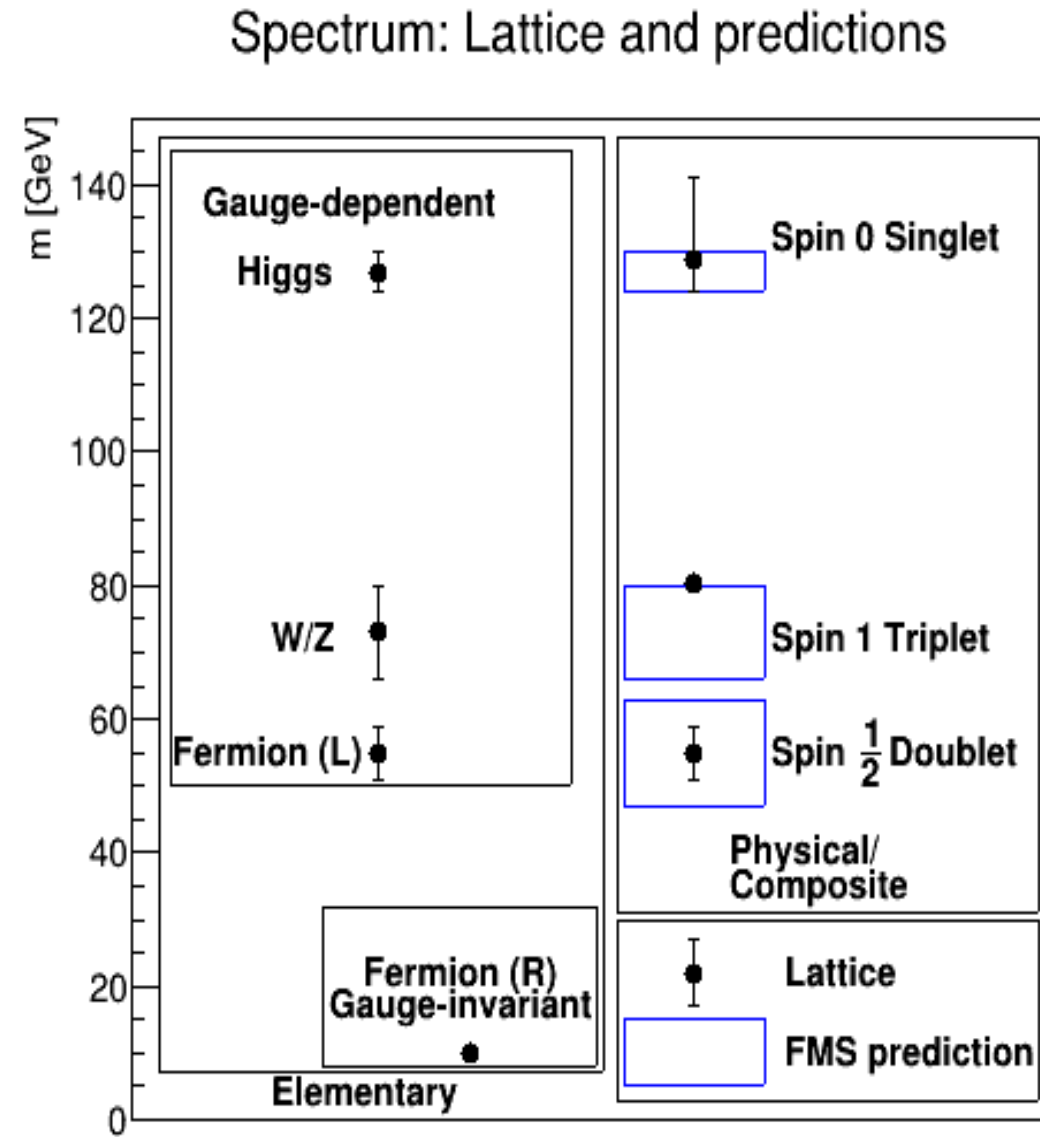
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Spectrum: Lattice and predictions



# Flavor on the lattice

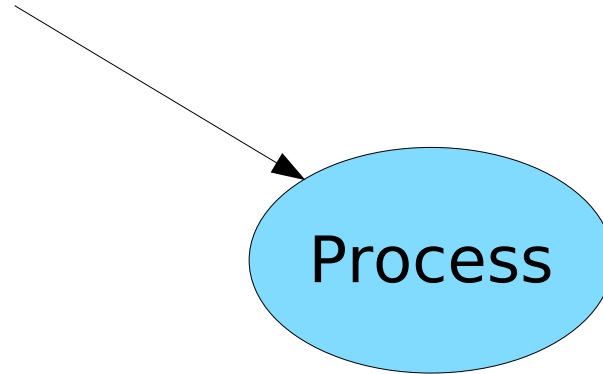
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# Scattering

[Maas et al.'17  
Maas & Reiner '22  
Maas, Plätzer et al.' unpublished]

Incoming (asymptotic) particle  
Standard LSZ: Elementary particle



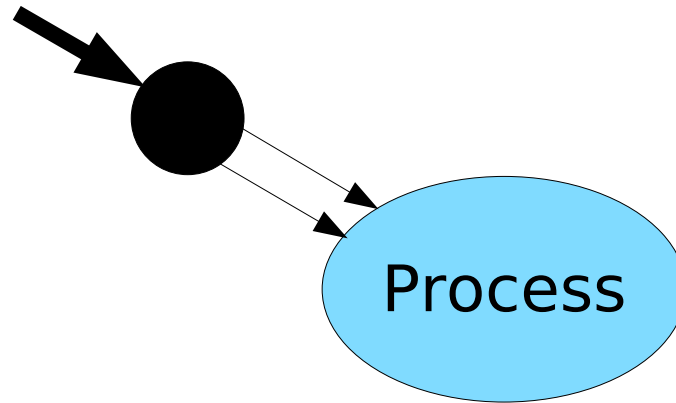
$$\langle f(p) \dots \rangle$$



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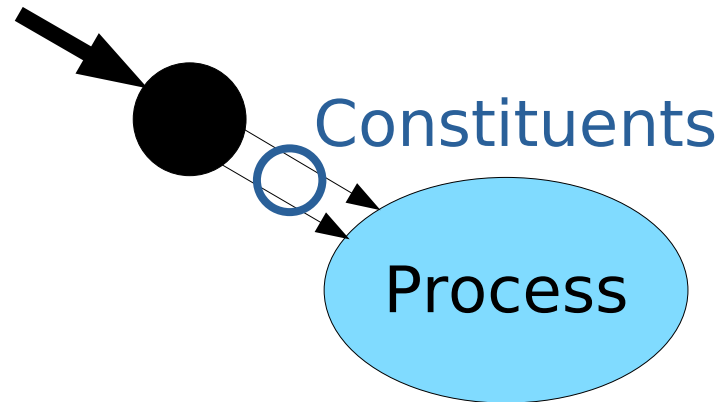


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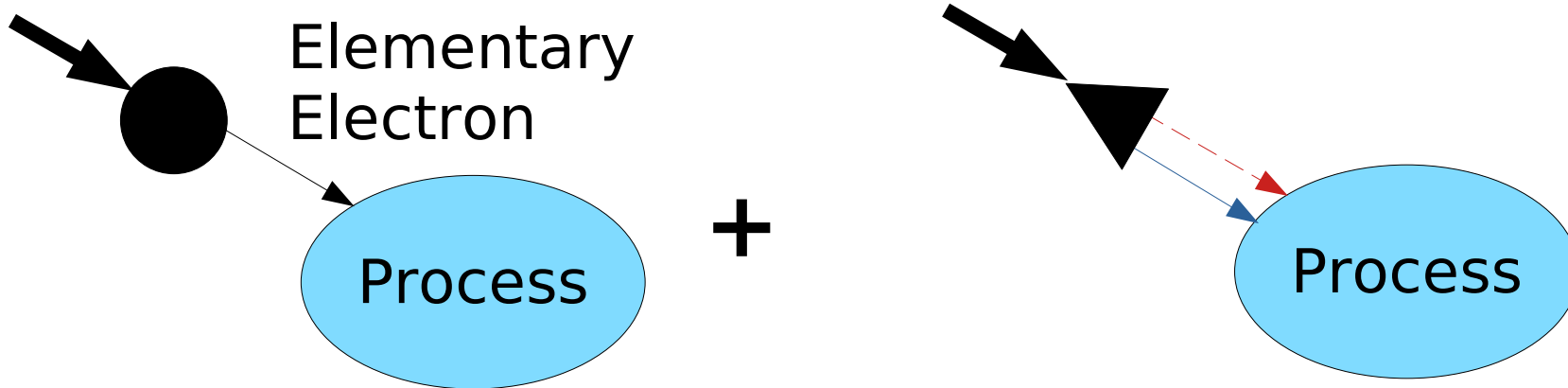


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FMS LSZ: Elementary and fluctuations

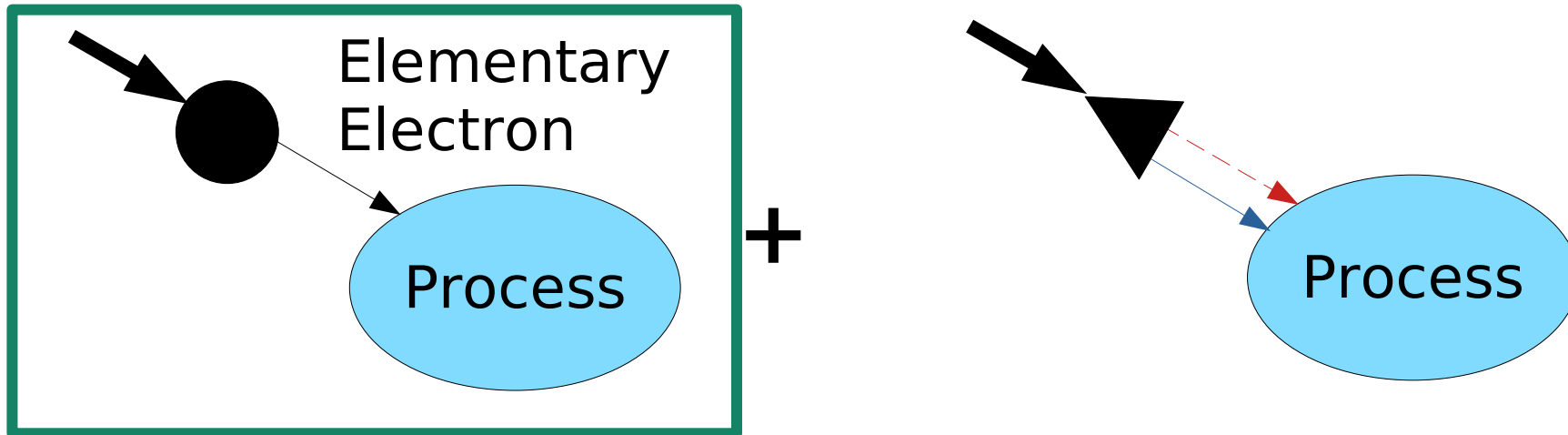


$$v \langle f(p) \dots \rangle + \int dq \Gamma(P, q) D_f(p-q) D_h(q) \langle h(q) f(P-q) \dots \rangle$$

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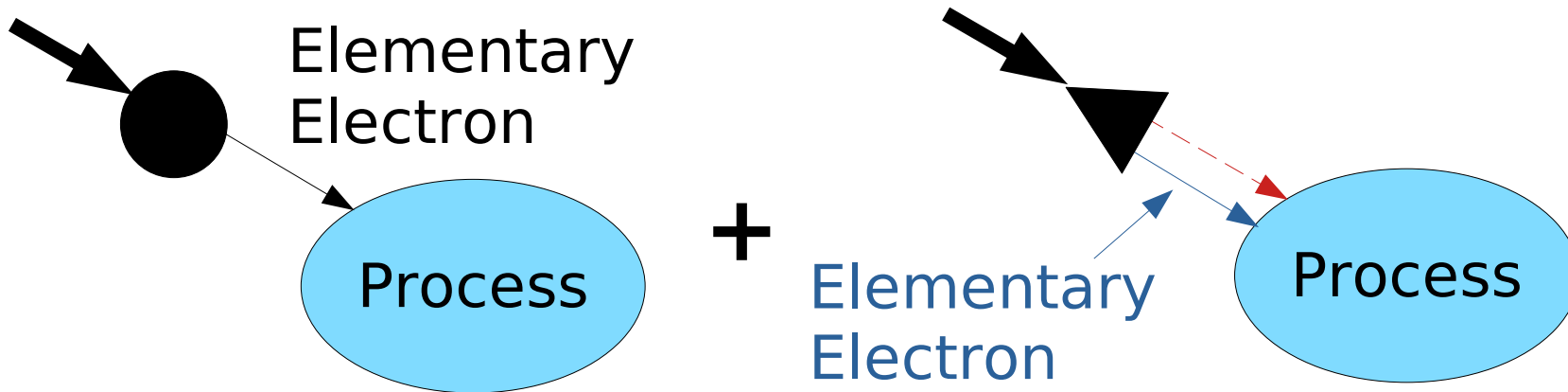
Standard perturbation theory

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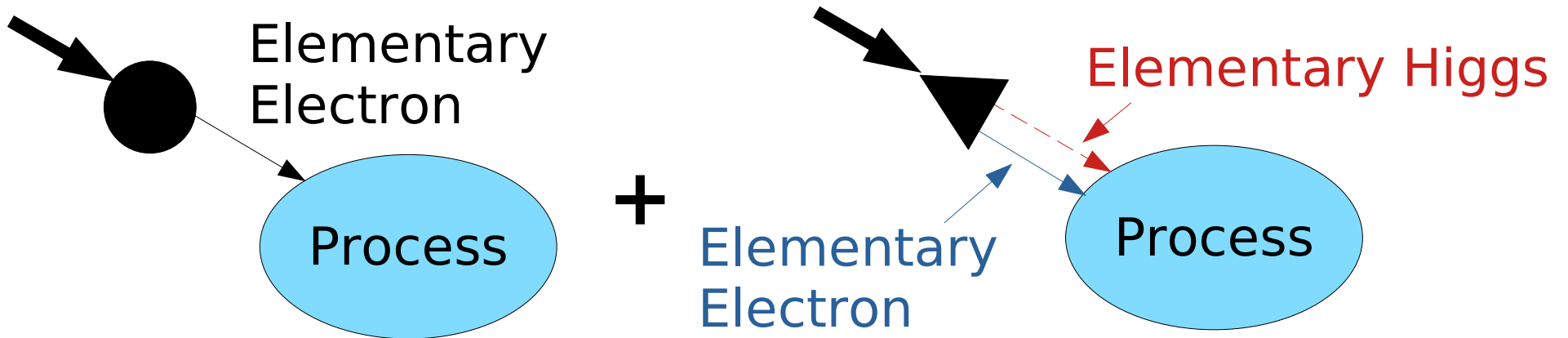


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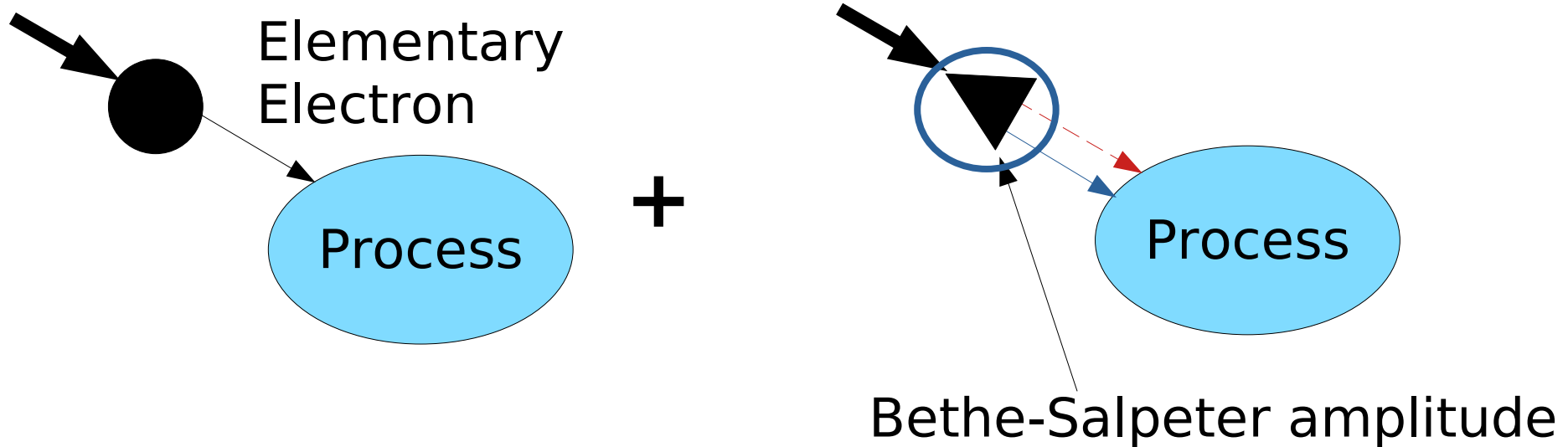


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[Maas, Plätzer et al. unpublished]



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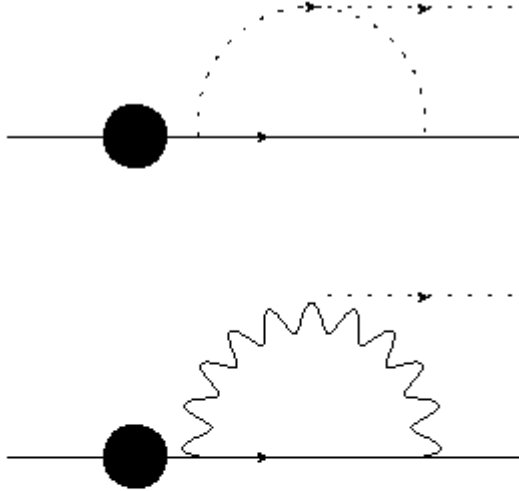
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Calculable itself in augmented perturbation theory

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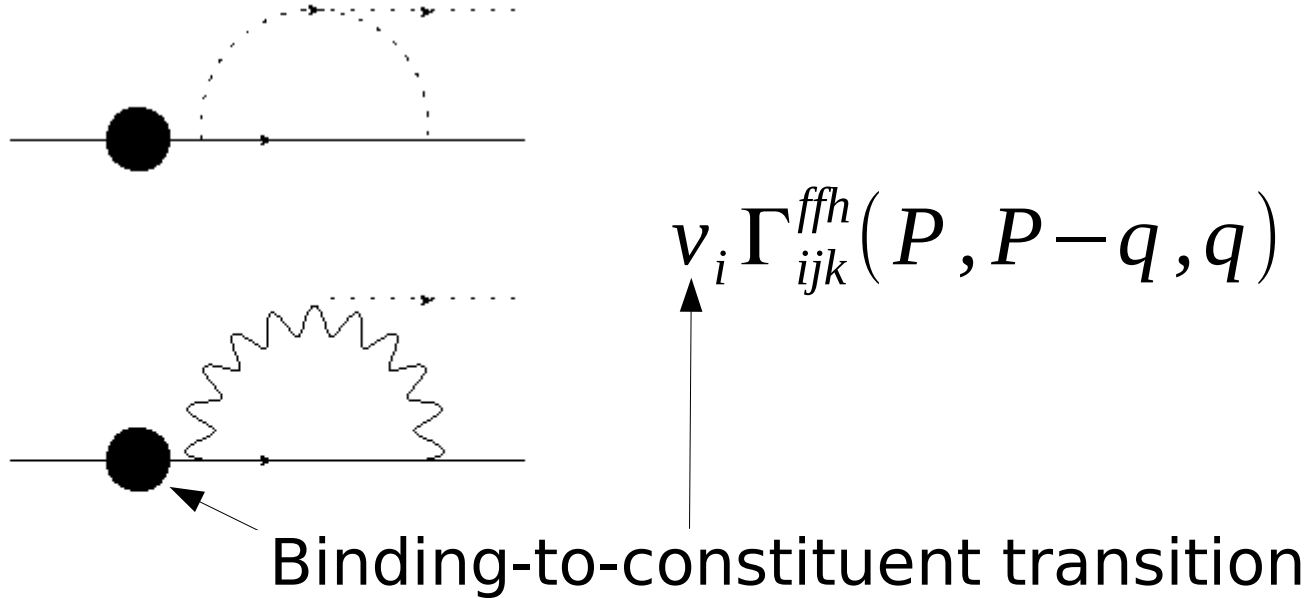


$$v_i \Gamma_{ijk}^{ffh}(P, P-q, q)$$

# Bethe-Salpeter Amplitude

[Maas, Plätzer et al. unpublished]

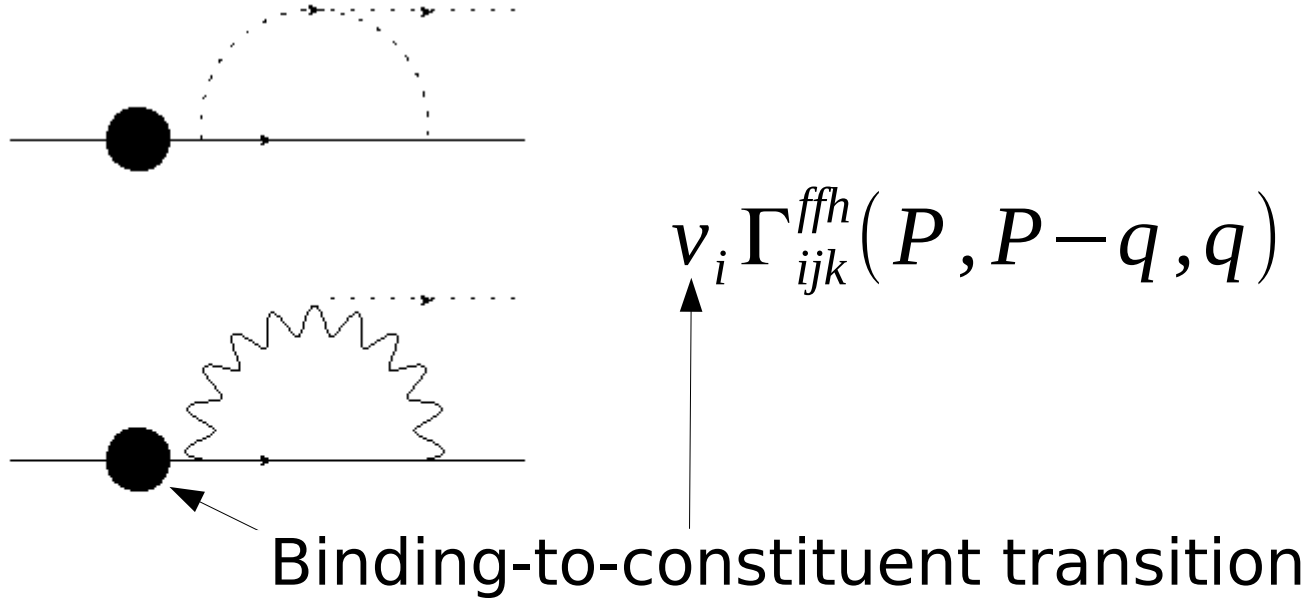
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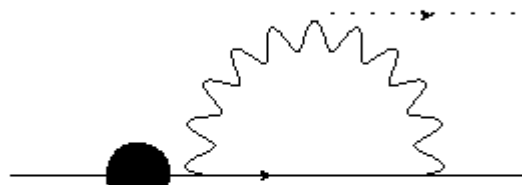
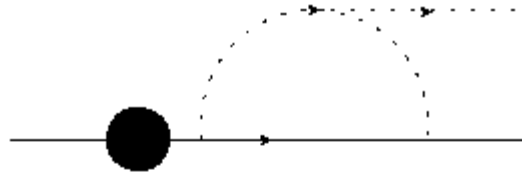


Reweights  
standard  
diagrams

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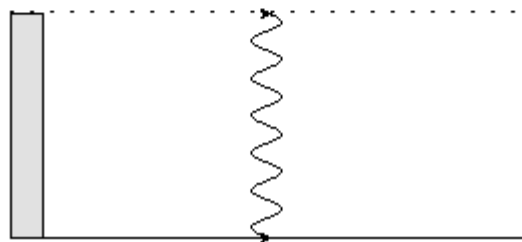
Calculable itself in augmented perturbation theory



Binding-to-constituent transition

$$v_i \Gamma_{ijk}^{ffh}(P, P-q, q)$$

Reweights  
standard  
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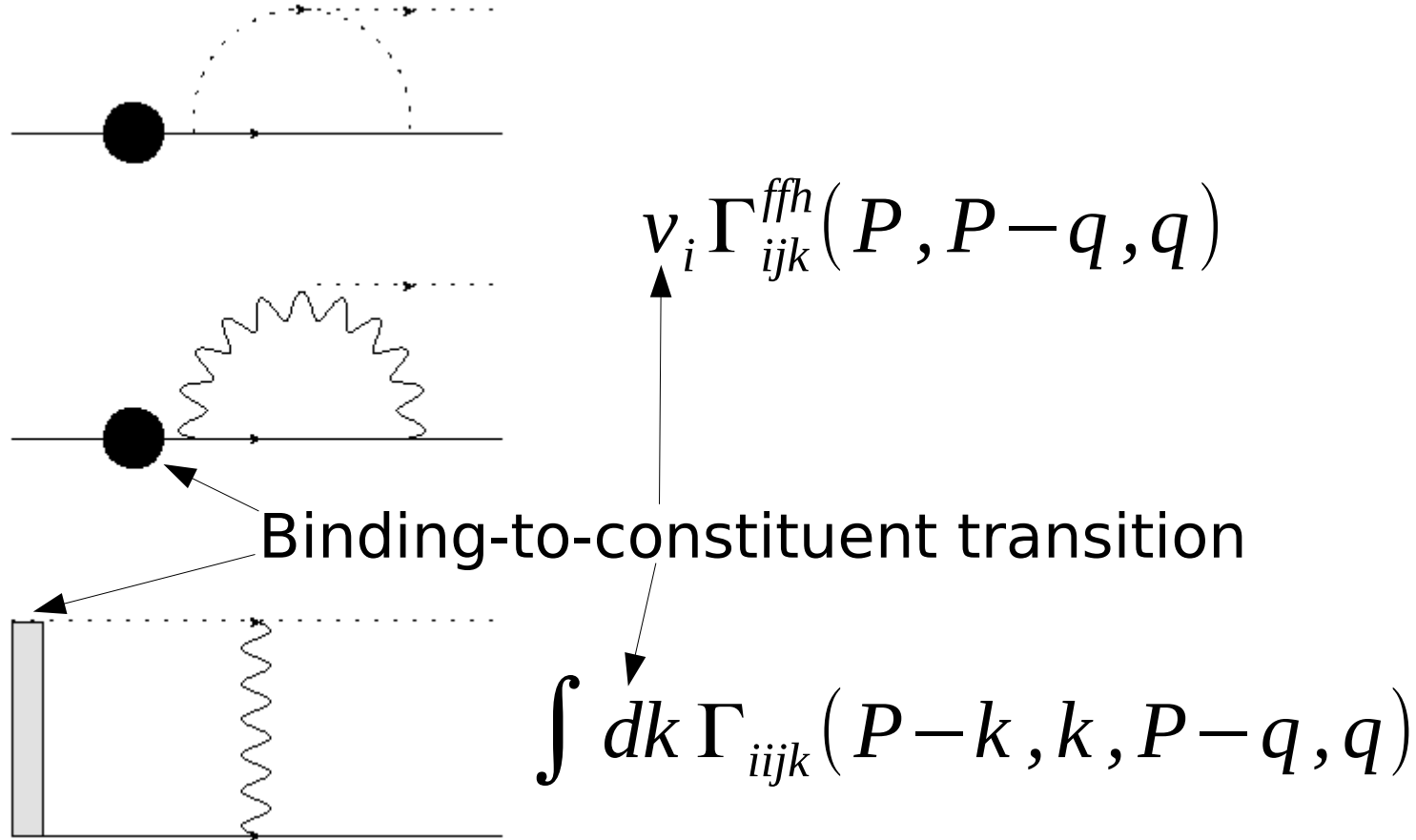


$$\int dk \Gamma_{ijk}(P-k, k, P-q, q)$$

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Calculable itself in augmented perturbation theory

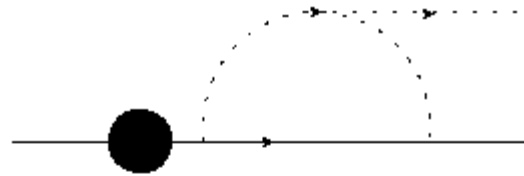


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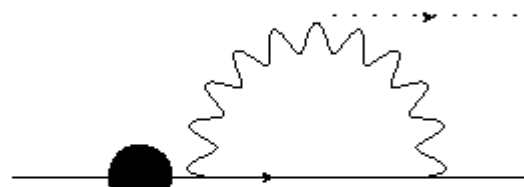
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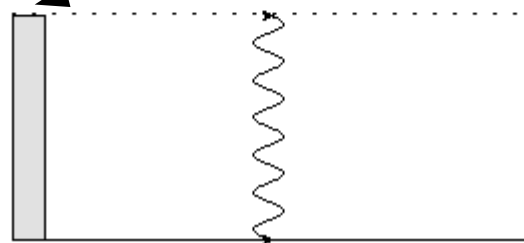
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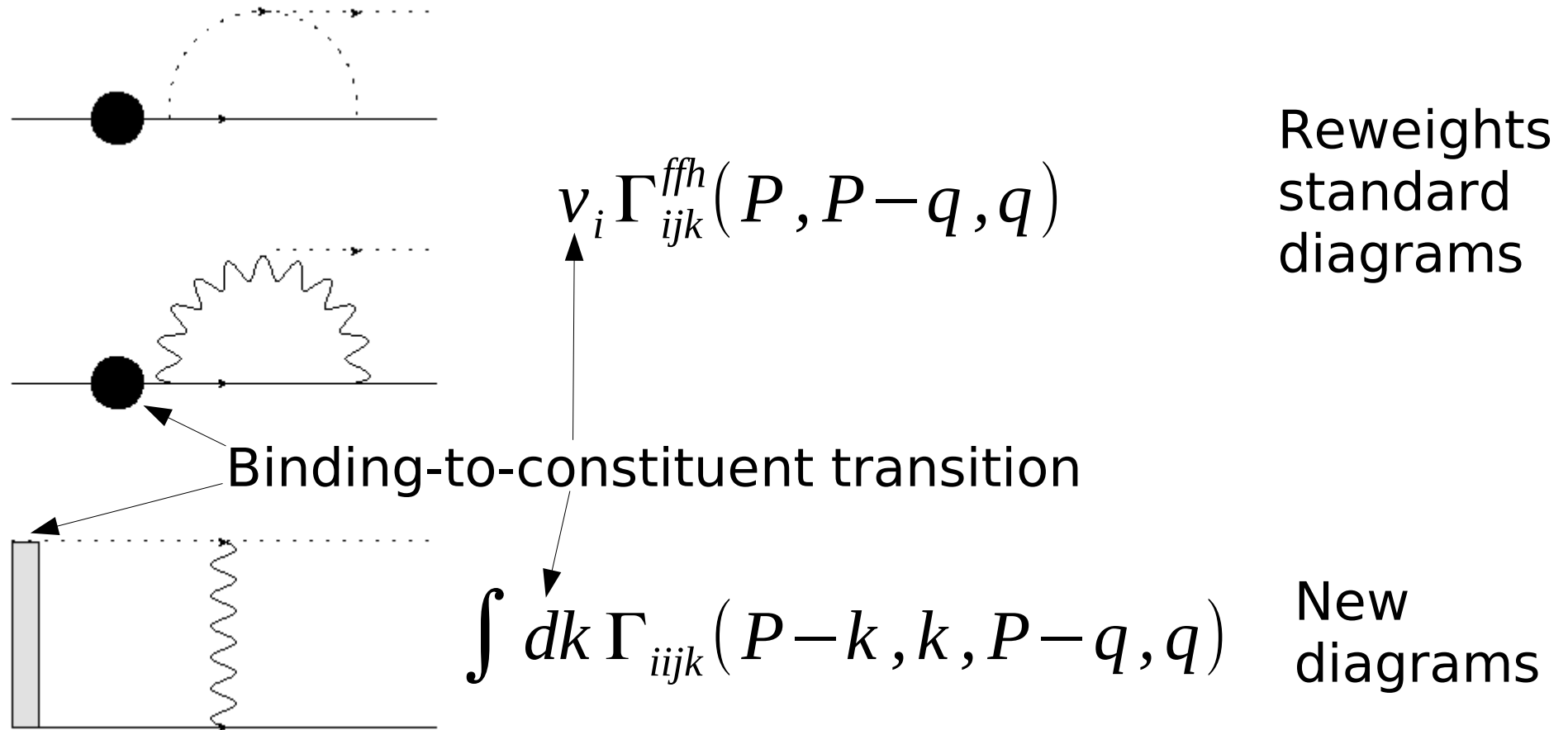
New  
diagrams

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[Maas, Plätzer et al. unpublished]

Calculable itself in augmented perturbation theory



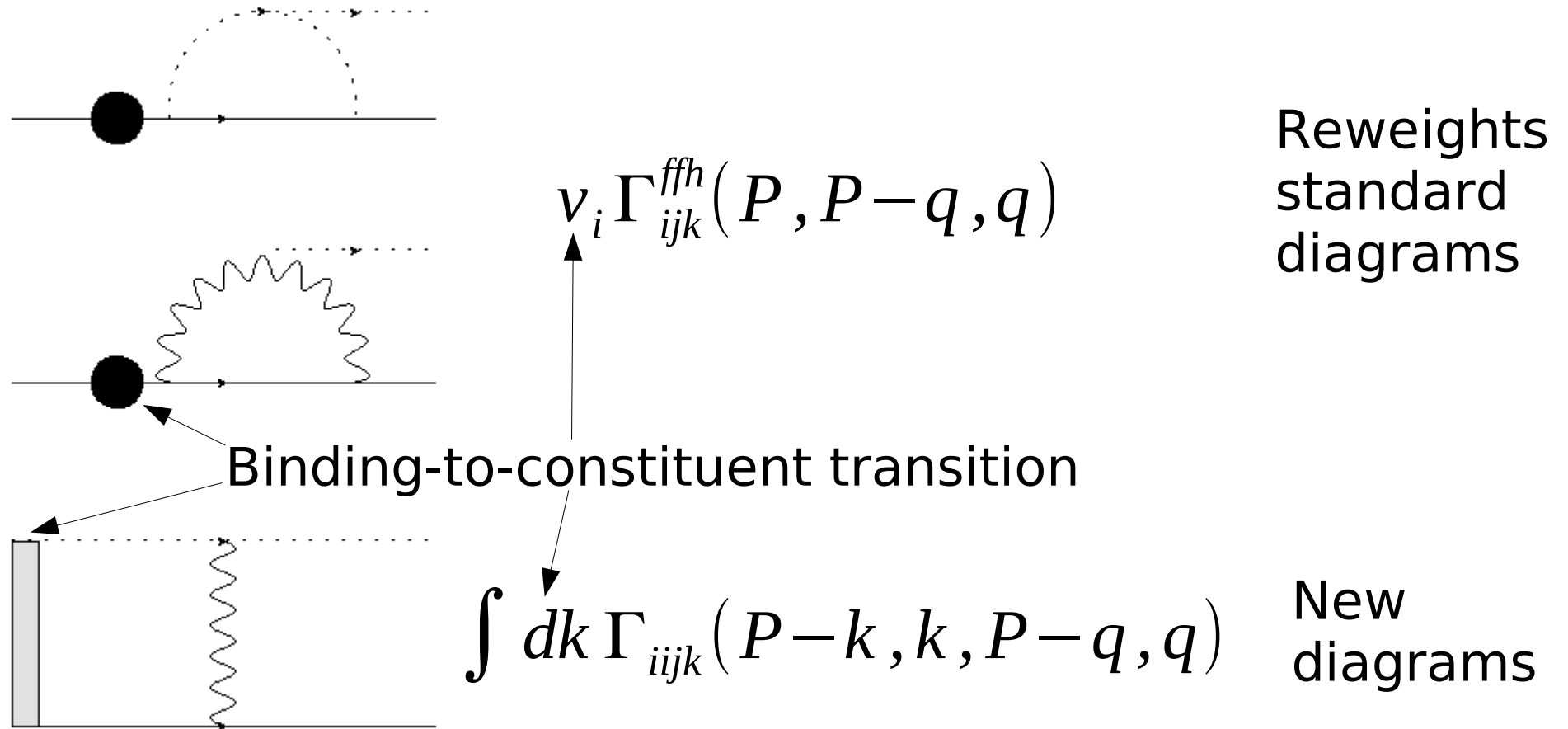
Both raise (in the standard model) the number of loops by 1



# Bethe-Salpeter Amplitude

[Maas, Plätzer et al. unpublished]

Calculable itself in augmented perturbation theory



Both raise (in the standard model) the number of loops by 1  
But neither are Yukawa suppressed

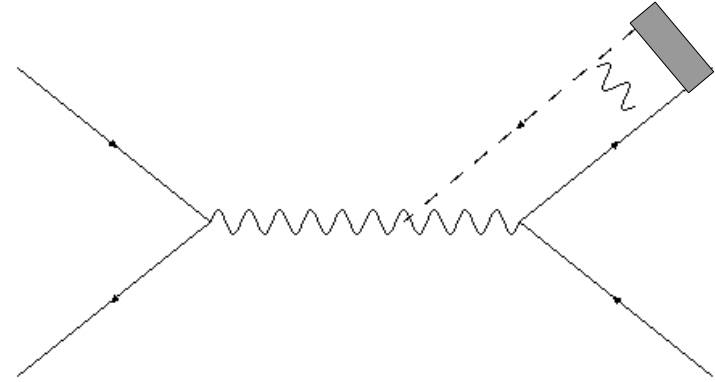
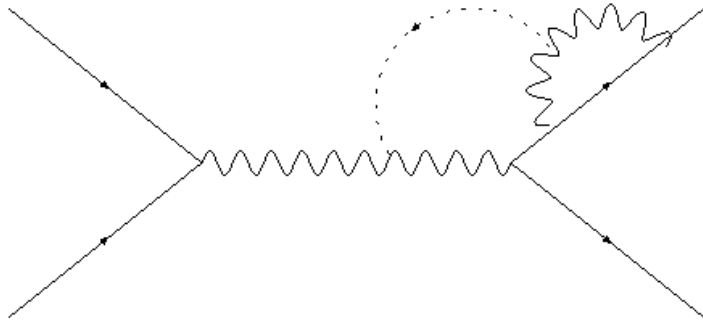
# Impact on processes

[Maas, Plätzer et al. unpublished  
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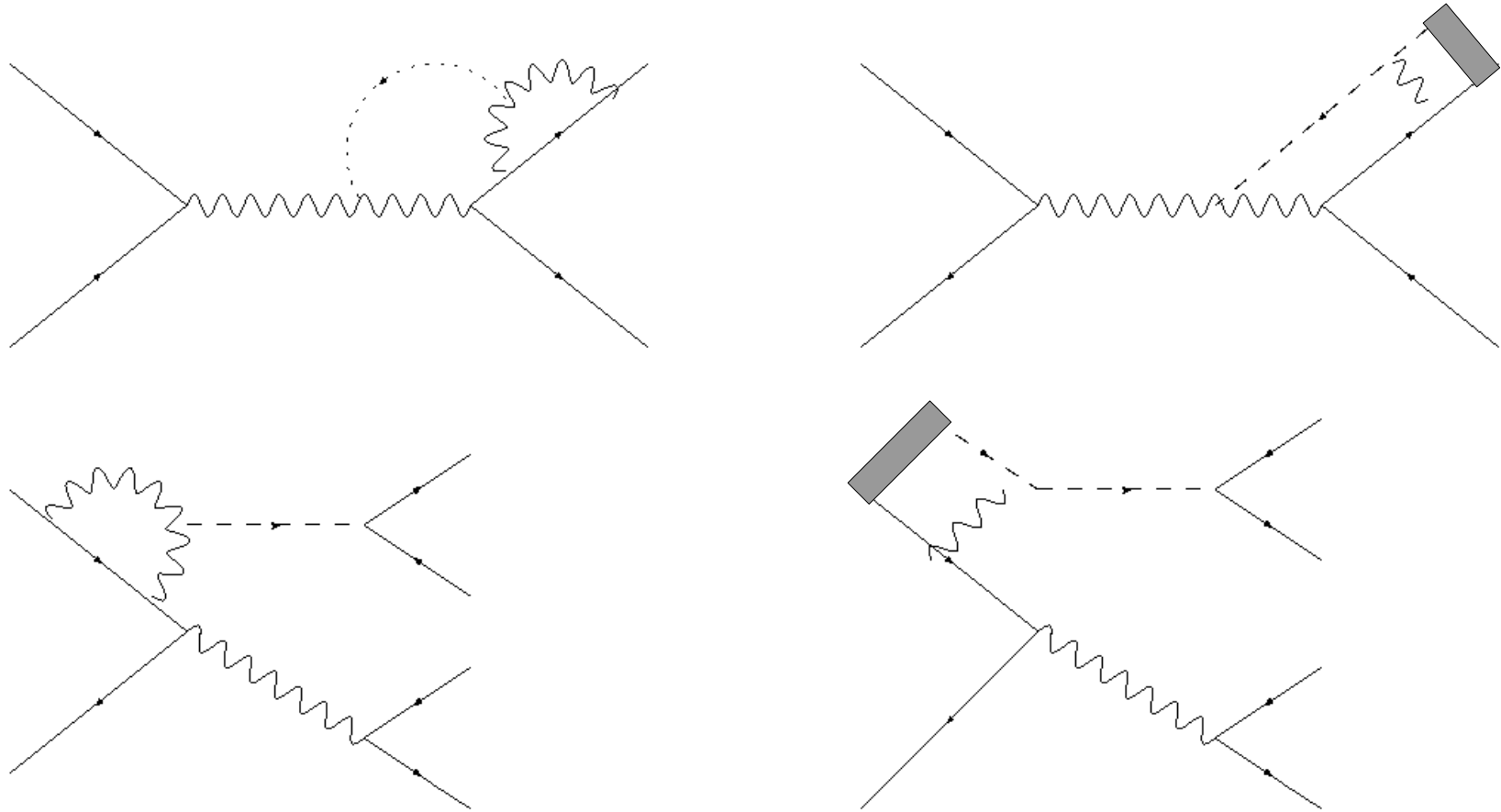
Process  $ff \rightarrow ff$ : 2-loop (in  $g_{\text{weak}}$ ) suppressed contribution



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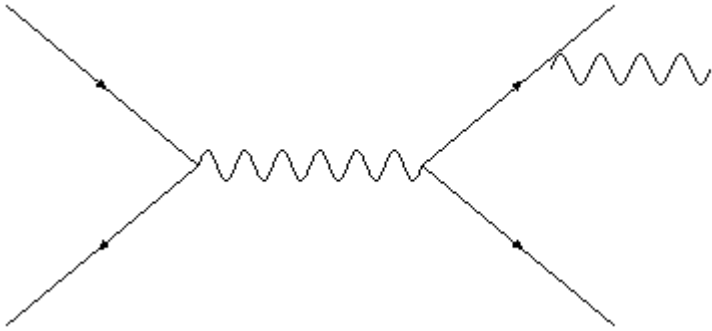


Process  $ff \rightarrow ffff$  1-loop ( $g_{\text{weak}} y$ ) suppressed contribution

# Resummation effects

[Ciafaloni et al. '00  
Maas et al.'22]

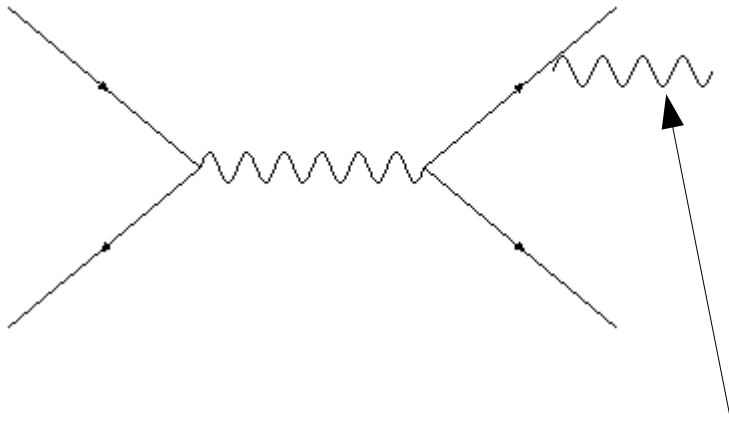
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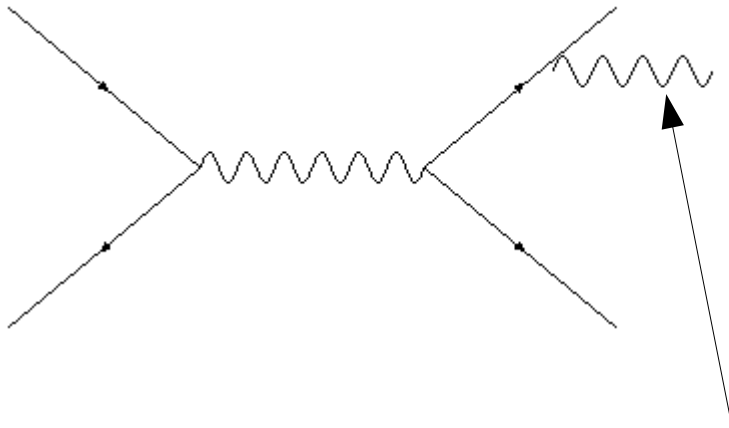


Resumming real emission

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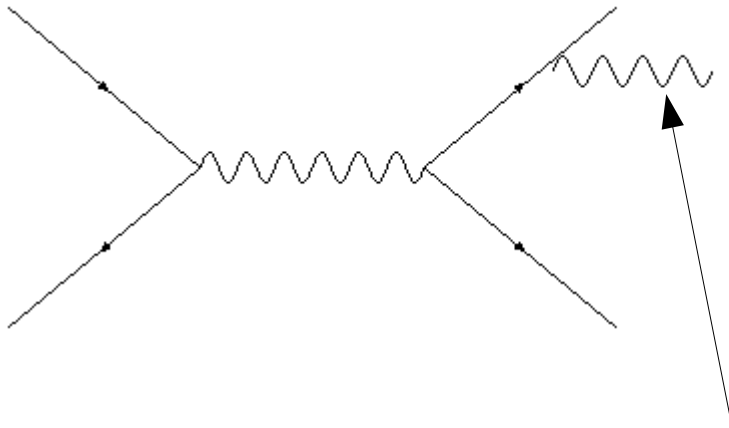
$$\sim \ln^2 \frac{S}{m_W^2}$$

at 1 TeV of the same  
order as strong  
corrections

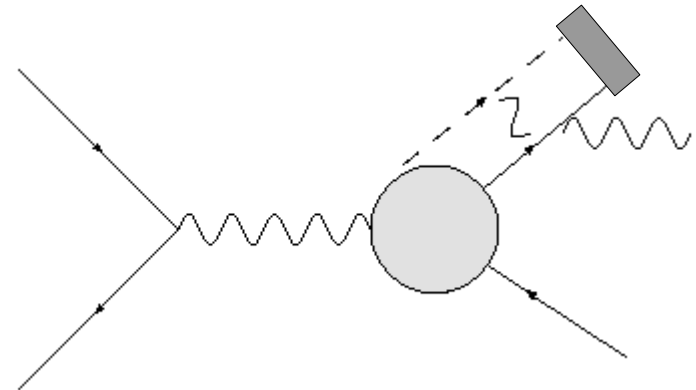
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Augmented by correct asymptotic state



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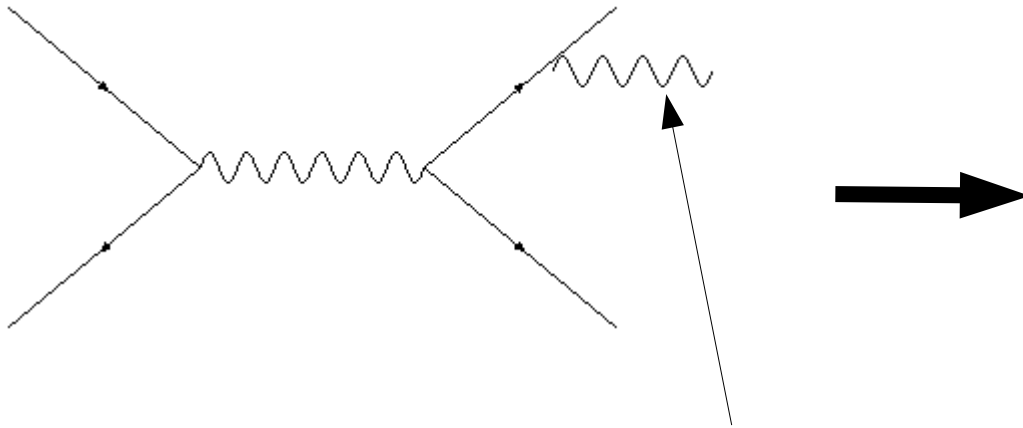
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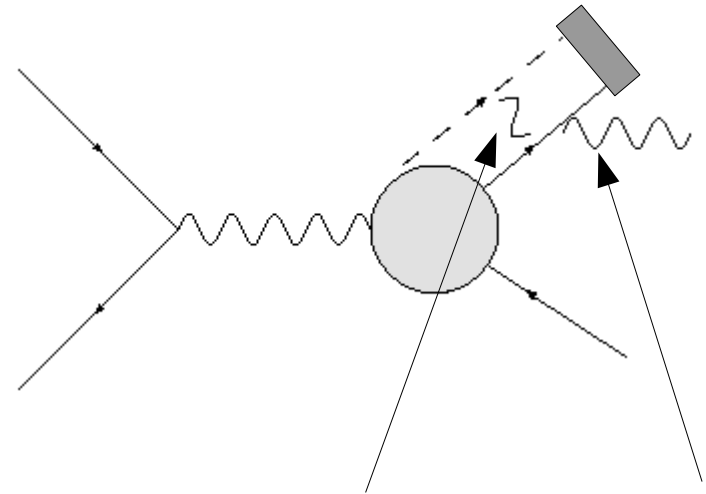


Resumming real emission

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at 1 TeV of the same  
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corrections

Augmented by correct  
asymptotic state



Virtual and real  
emissions compensate  
(BN/KLN theorems)  
- substantial change

# Summary

Review: 1712.04721

Update: 2305.01960

- Field theory requires change of asymptotic states
  - Can be treated using FMS-augmented perturbation theory
  - Changes in the SM at one or two loop orders

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