

# Model Independent Bounds on Left-Right Gauge Boson Masses from LHC Run 2 and Flavour Observables

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# Why LR Models?

- Mohapatra, Pati (1975)
- Senjanovic, Mohapatra (1975)
- Senjanovic (1979)

- New Physics: Dark Matter, Neutrino Masses,...
- The Laws of Physics are not invariant under **Parity**.

$$SU(3)_{\text{QCD}} \times SU(2)_L \times U(1)_Y$$



$$X = (B - L)/2$$

$$SU(3)_{\text{QCD}} \times SU(2)_L \times SU(2)_R \times U(1)_X$$

$g_S$

$g_L$

$g_R$

$g_X$

# General Results of LR Models

$$SU(3)_{\text{QCD}} \times SU(2)_L \times SU(2)_R \times U(1)_X$$

- Restoration of **Parity**:  $g_L = g_R$
- New Gauge Bosons:  $g, A, W_L^\pm, Z_L^0, W_R^\pm, Z_R^0$
- Right-Handed Neutrinos:  $\nu_R$
- Two **Energy Scales**:  $v_R \gg v_{EW}$
- New mixing matrices for fermions:  $V_L^{\text{CKM}}, V_L^{\text{PMNS}}, V_R^{\text{CKM}}, V_R^{\text{PMNS}}$



# SSB and Perturbativity

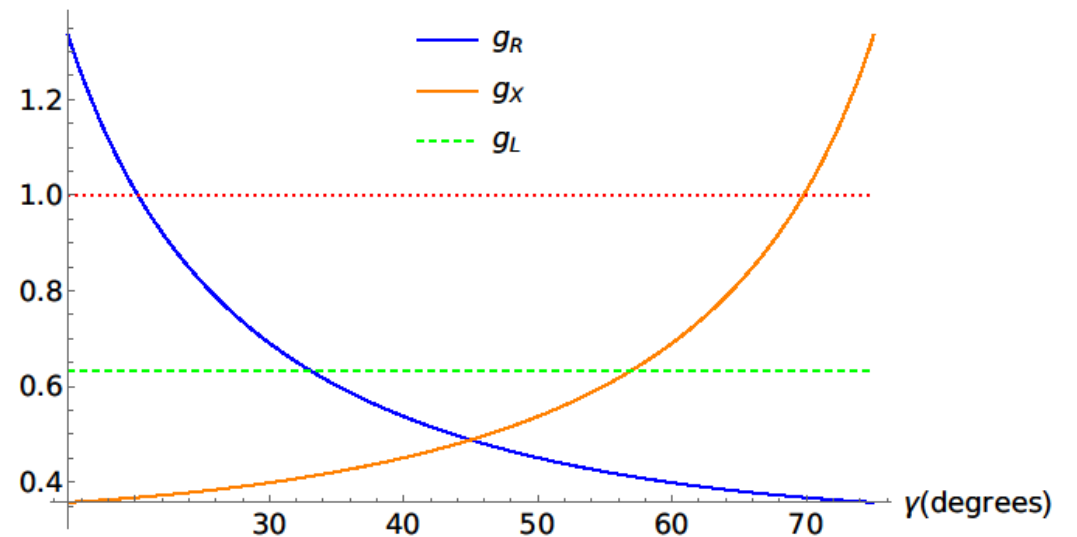
$$\begin{pmatrix} Z_L \\ Z_R \\ A \end{pmatrix} = \underbrace{\begin{pmatrix} \cos \alpha & -\sin \alpha & 0 \\ \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{Z_L - Z_R \text{ Mixing}} \begin{pmatrix} \cos \theta_W & 0 & -\sin \theta_W \\ 0 & 1 & 0 \\ \sin \theta_W & 0 & \cos \theta_W \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \gamma & -\sin \gamma \\ 0 & \sin \gamma & \cos \gamma \end{pmatrix} \begin{pmatrix} W_L^3 \\ W_R^3 \\ W_X \end{pmatrix}$$

$$Z_L - Z_R \text{ Mixing } \alpha \sim \left( \frac{v_{EW}}{v_R} \right)^2$$

- Perturbativity:  $g_R, g_X \leq 1$

$$e = g_R \cos \theta_W \sin \gamma = g_X \cos \theta_W \cos \gamma$$

$$70^\circ > \gamma > 20^\circ$$



# Scalar Fields

- **Bidoublet + Doublets (Dirac Neutrinos):**

$$\Phi := \begin{pmatrix} \phi_1^0 & \phi_1^+ \\ \phi_2^- & \phi_2^0 \end{pmatrix}, \quad \chi_L := \begin{pmatrix} \chi_L^+ \\ \chi_L^0 \end{pmatrix}, \quad \chi_R := \begin{pmatrix} \chi_R^+ \\ \chi_R^0 \end{pmatrix}.$$

$\Phi \sim (1, 2, \bar{2}, 0)$   
 $\chi_L \sim (1, 2, 1, 1/2)$   
 $\chi_R \sim (1, 1, 2, 1/2)$

- **Bidoublet + Triplets (Majorana Neutrinos):**

$$\Phi, \Delta_L := \begin{pmatrix} \delta_L^+/\sqrt{2} & \delta_L^{++} \\ \delta_L^0 & -\delta_L^+/\sqrt{2} \end{pmatrix}, \quad \Delta_R := \begin{pmatrix} \delta_R^+/\sqrt{2} & \delta_R^{++} \\ \delta_R^0 & -\delta_R^+/\sqrt{2} \end{pmatrix}.$$

$\Delta_L \sim (1, 3, 1, 1)$   
 $\Delta_R \sim (1, 1, 3, 1)$

- **$\chi_L + \chi_R$  Effective LR Model.**

- Babu, Dutta, Mohapatra (2019)
- Babu, He, Su, Thapa (2022)

# The $\chi_L + \chi_R$ Effective LR Model

- The scalar sector is very simple. We only have two physical degrees of freedom:

$$\chi_{L,R} := \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ v_{L,R} + \chi_{L,R}^{0r} \end{pmatrix}$$

(Unitary Gauge)

$$\begin{pmatrix} H \\ h \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \chi_R^{0r} \\ \chi_L^{0r} \end{pmatrix}$$

$$v_R \gg v_L = v_{EW}$$

- Only 5 free parameters in the scalar potential:

$$M_H^2 \approx 2\lambda_R v_R^2, \quad M_h^2 \approx \frac{4\lambda_L \lambda_R - \lambda_{LR}^2}{2\lambda_R} v_L^2$$

$$V = -\mu_L^2 \chi_L^\dagger \chi_L - \mu_R^2 \chi_R^\dagger \chi_R + \lambda_L (\chi_L^\dagger \chi_L)^2 + \lambda_R (\chi_R^\dagger \chi_R)^2 + \lambda_{LR} (\chi_L^\dagger \chi_L) (\chi_R^\dagger \chi_R).$$

$$\tan \theta = \frac{\lambda_{LR} v_L v_R}{\lambda_L v_L^2 - \lambda_R v_R^2}$$

# The $\chi_L + \chi_R$ Effective LR Model

- No  $W_L - W_R$  Mixing.

$$M_{W_L} = \frac{1}{2} g_L v_L, \quad M_{W_R} = \frac{1}{2} g_R v_R, \quad M_{Z_L} \approx \frac{M_{W_L}}{\cos \theta_W}, \quad M_{Z_R} \approx \frac{M_{W_R}}{\cos \gamma}$$

- We need Effective Operators to produce Fermion Masses:

$$\mathcal{L}_Y = -\frac{1}{\Lambda} \left\{ \begin{array}{l} C_d^{ij} \bar{q}_L^i \chi_L \chi_R^\dagger q_R^j + C_u^{ij} \bar{q}_L^i \tilde{\chi}_L \tilde{\chi}_R^\dagger q_R^j + C_e^{ij} \bar{l}_L^i \chi_L \chi_R^\dagger l_R^j + C_{\nu_D}^{ij} \bar{l}_L^i \tilde{\chi}_L \tilde{\chi}_R^\dagger l_R^j \\ + C_{\nu_{L,M}}^{ij} \bar{l}_L^i \tilde{\chi}_L \tilde{\chi}_L^T l_L^j + C_{\nu_{R,M}}^{ij} \bar{l}_R^i \tilde{\chi}_R \tilde{\chi}_R^\dagger l_R^j \end{array} \right\}$$

(Dirac Masses)

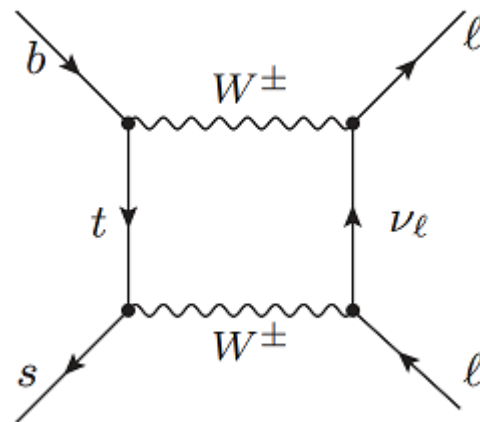
(Majorana Masses)

$$\tilde{\chi}_{L,R} := i\sigma^2 \chi_{L,R}^*$$



# Bounds from Flavour Physics

- We want to put a **Bound** on the **LR Scale** that **Does Not Depend** on other **Parameters of the Model**.
- Doing this using **Flavour Observables** for the **Effective Model** is **Highly Non-Trivial** because the complete calculations will require the **Addition of  $D = 6$  Operators**.



$$\sim m_{f_1} m_{f_2} \sim \frac{1}{\Lambda^2}$$

# $b \rightarrow s\gamma$ and $b \rightarrow sll$ Preliminary Work

- For the **Other Models** we can calculate the contributions for these processes assuming that the **Masses of the Scalars are much Bigger than the ones of the Gauge Bosons (FCNC) and Light RH Neutrinos.**

$$C_7|_{\text{NP}} = \frac{1}{\sqrt{2}} 4em_b G_F \sum_{i=u,c,t} \frac{g_R}{g_L} \frac{m_i}{m_b} \sin \xi_W e^{-i\lambda} (V_L^{\text{CKM}})^*_{is} (V_R^{\text{CKM}})_{ib} \tilde{F}(x_{W_L}^{f_i}) \quad C_9^l|_{\text{NP}} \sim \mathcal{O}(v_R^{-4})$$

$$C_7^l|_{\text{NP}} = \frac{1}{\sqrt{2}} 4em_b G_F \sum_{i=u,c,t} \frac{g_R}{g_L} \frac{m_i}{m_b} \sin \xi_W e^{i\lambda} (V_R^{\text{CKM}})^*_{is} (V_L^{\text{CKM}})_{ib} \underbrace{\tilde{F}(x_{W_L}^{f_i})}_{\text{Loop Function}} \quad C_{10}^l|_{\text{NP}} \sim \mathcal{O}(v_R^{-4})$$

$$C_9^l = \frac{4}{9} \left( \frac{eg_R}{M_{W_R}} \right)^2 \sum_{i=u,c,t} (V_R^{\text{CKM}})^*_{is} (V_R^{\text{CKM}})_{ib} \ln \left( \frac{m_i}{m_0} \right) \quad C_{10}^l \sim \mathcal{O}(v_R^{-4})$$

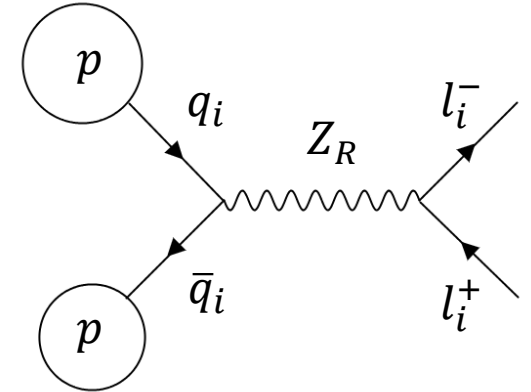
Bishara et al. (2104.10930)

- Assuming a **Diagonal Structure** of  $V_R^{\text{CKM}}$ ,  $g_L = g_R$  and a **Mixing Equal** to  $(v_{EW}/v_R)^2$  between the  $W_L$  and the  $W_R$  we get from  $C_7|_{\text{NP}}$ :

$$v_R \sim 7 \text{ TeV}$$

LHCb Collaboration (2111.10194)

# $Z_R$ Physics in Colliders



- Narrow Resonance Approximation  $\sqrt{s} = 13 \text{ TeV}$

$$\sigma(pp \rightarrow Z_R X \rightarrow f \bar{f} X) \approx \frac{\pi}{6s} \sum_q c_q^f \cdot \omega_q(s, M_{Z_R}^2)$$

Ellis, Stirling, Webber (2011)

- The  $\omega_q(s, M_{Z_R}^2)$  depend on the Parton Distribution Functions

- $c_q^f := \frac{1}{2} (g_V^{q^2}(\gamma) + g_A^{q^2}(\gamma)) \text{Br}(Z_R \rightarrow f \bar{f}) \quad \mathcal{L}_{Z_R}^{ff} = \frac{1}{2} Z_R^\mu \bar{f} \gamma_\mu (g_V^f - g_A^f \gamma_5) f$

No Dependence on the Mixing Matrices

# $Z_R$ Decay to Charged Leptons

- We only need to compute

(Assuming  $M_{Z_R} \gg m_f$ )

$$\text{Br}(Z_R \rightarrow l^+ l^-) := \Gamma(Z_R \rightarrow l^+ l^-) / \Gamma_{Z_R} \quad \Gamma(Z_R \rightarrow f \bar{f}) \approx N_C^f \frac{M_{Z_R}}{48\pi} \left[ g_V^{f^2}(\gamma) + g_A^{f^2}(\gamma) \right]$$

- The processes that contribute to the total width of the  $Z_R$  at leading order in  $e$  are

$$Z_R \rightarrow f \bar{f}, W_L^+ W_L^-, Z_L h^0, Z_L H^0, W_L^\pm H^\mp, h^0 H^0, W_L^\pm W_R^\mp, H_1 H_2, W_R^\pm H^\mp \text{ and } W_R^\pm W_R^\mp$$

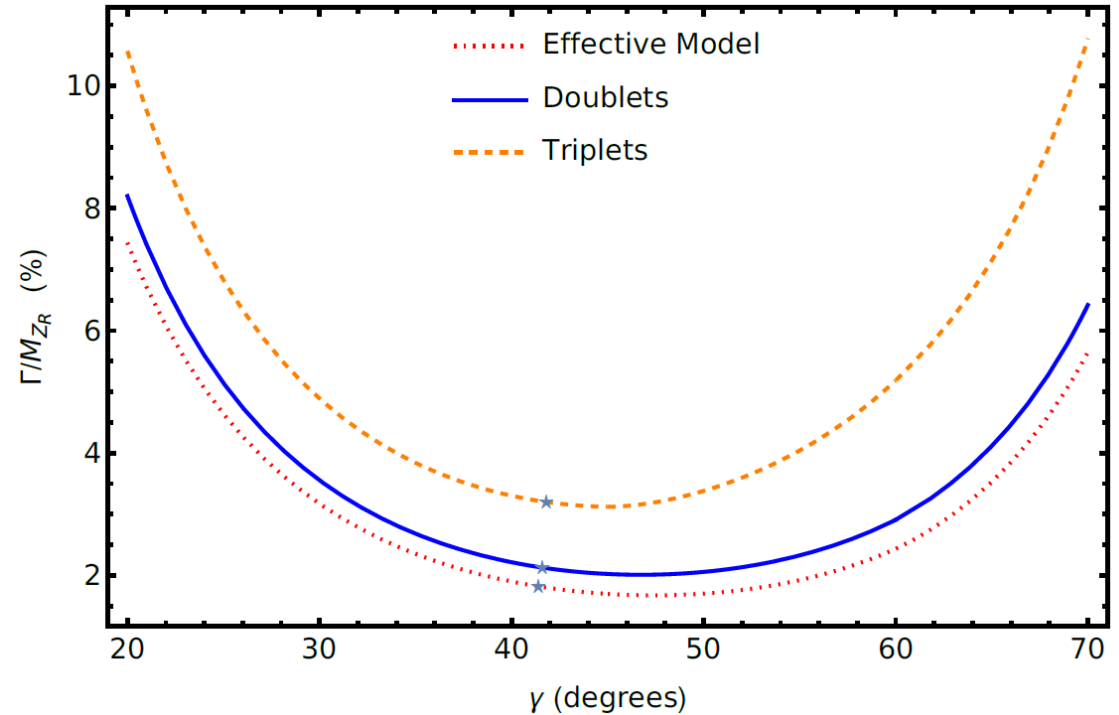
- Since the **Diagonalization of the Scalar Potentials** is highly non-trivial we will only put an **Upper Bound on  $\Gamma_{Z_R}$** . Consequently, we will get the **Less Constraining Lower Bound on  $M_{Z_R}$** .

# The Total Width of the $Z_R$

$$Z_R \rightarrow W_L^+ W_L^-, Z_L h^0, Z_L H^0, W_L^\pm H^\mp, h^0 H^0, H_1 H_2$$

**2 Scalars**

(Using the Equivalence Theorem)

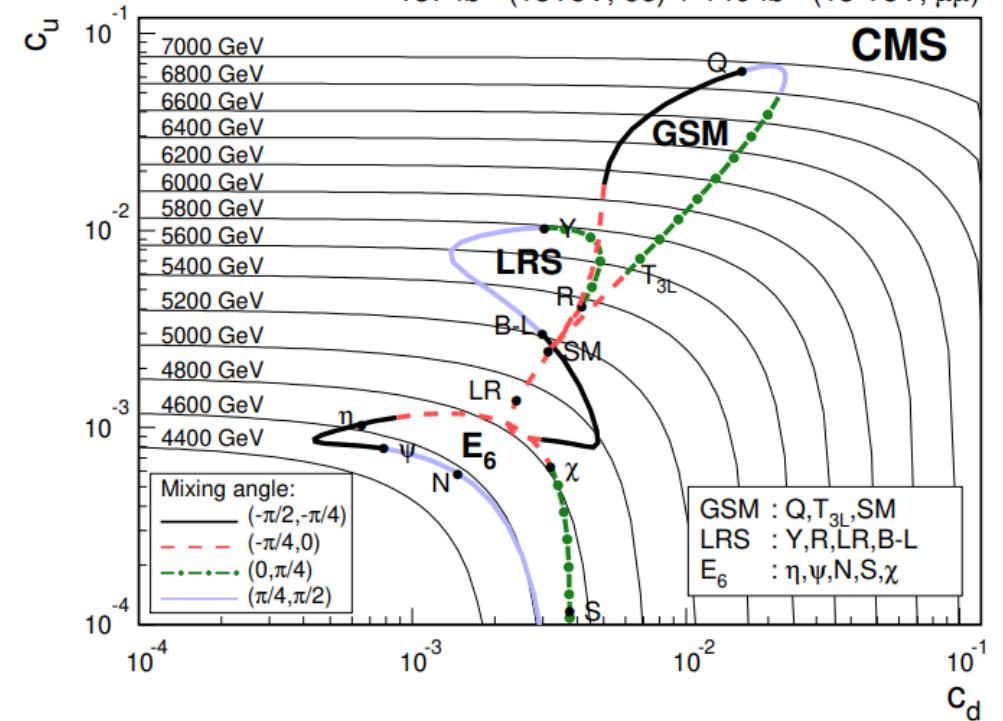
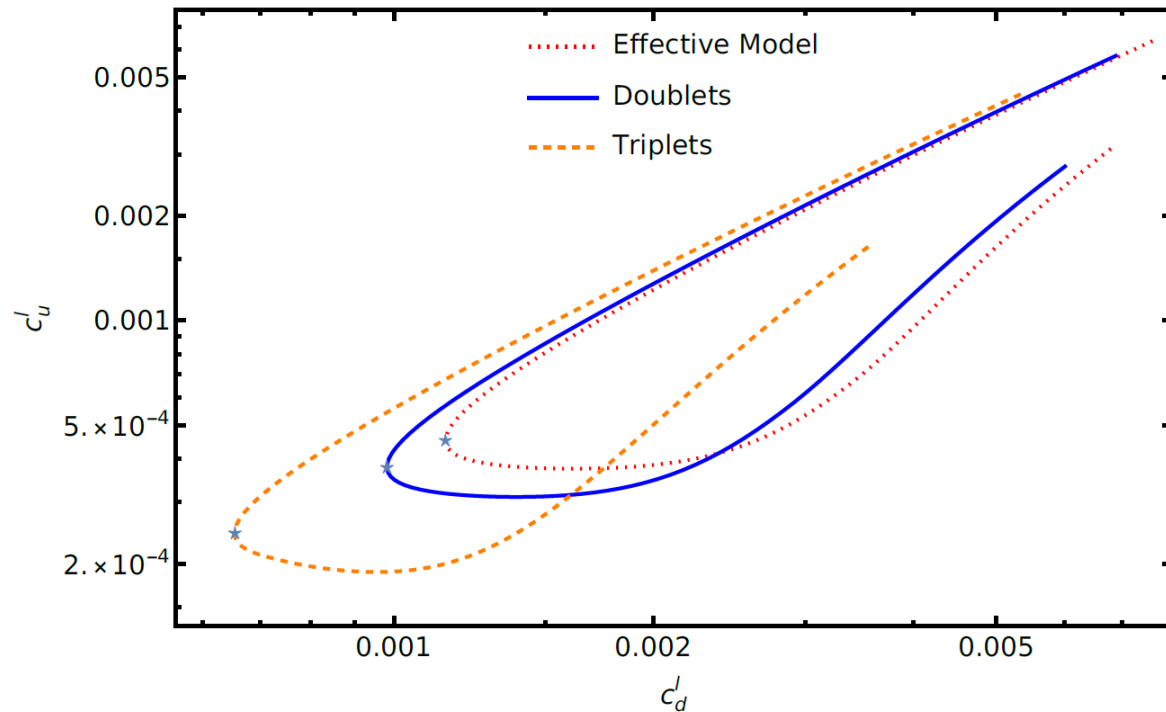


$$\Gamma(Z_R \rightarrow \mathbf{2\ Scalars}) \leq \Gamma(Z_R \rightarrow \mathbf{2\ Scalars}) \Big|_{m_S=0} = \frac{M_{Z_R} e^2}{96\pi \cos^2 \theta_W} \{2 \tan^2 \gamma + 3 \cot^2 \gamma\}$$

# Bound on the Mass of the $Z_R$

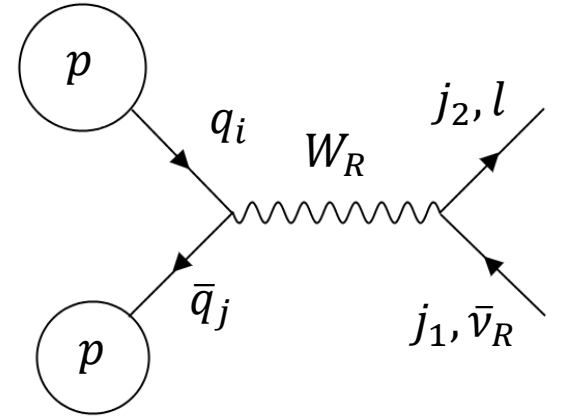
CMS (2103.02708)

137 fb<sup>-1</sup> (13TeV, ee) + 140 fb<sup>-1</sup> (13 TeV,  $\mu\mu$ )



$Z_R \rightarrow e^+e^-, \mu^+\mu^-$	$\Phi + \chi_{L,R}$	$\Phi + \Delta_{L,R}$	$\chi_L + \chi_R$
$M_{Z_R}$ (TeV)	4.3	4.2	4.3

# $W_R$ Physics in Colliders



- We will study the Decay of the  $W_R$  into **Two Jets** and  $l\nu_R$  (model dependent for Majorana neutrinos).
- Narrow Resonance Approximation.  $\sqrt{s} = 13 \text{ TeV}$

$$\sigma(pp \rightarrow W_R X \rightarrow jjX) \approx \sigma(pp \rightarrow W_R X) \text{Br}(W_R \rightarrow qq)$$

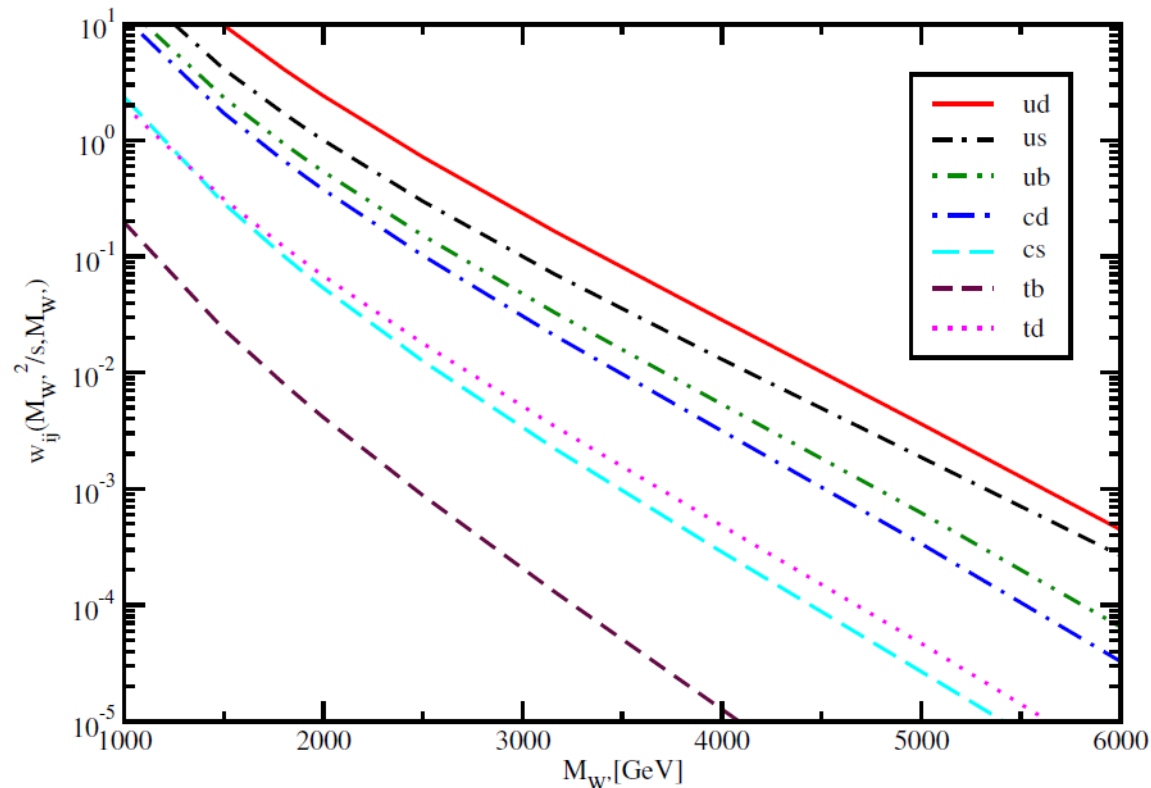
Ellis, Stirling, Webber (2011)

$$\sigma(pp \rightarrow W_R X \rightarrow l\nu_R X) \approx \sigma(pp \rightarrow W_R X) \text{Br}(W_R \rightarrow l\nu_R)$$

$$\sigma(pp \rightarrow W_R X) \approx \frac{2\pi^2}{3s} \alpha_R \sum_{ij} \left| (V_R^{\text{CKM}})_{ij} \right|^2 \omega_{ij} \left( \frac{M_{W_R}^2}{s}, M_{W_R} \right)$$

# $V_R^{\text{CKM}}$ Structures

- We can use a structure of the  $V_R^{\text{CKM}}$  matrix for which we get the less stringent bound on  $M_{W_R}$  (minimum Cross Section).



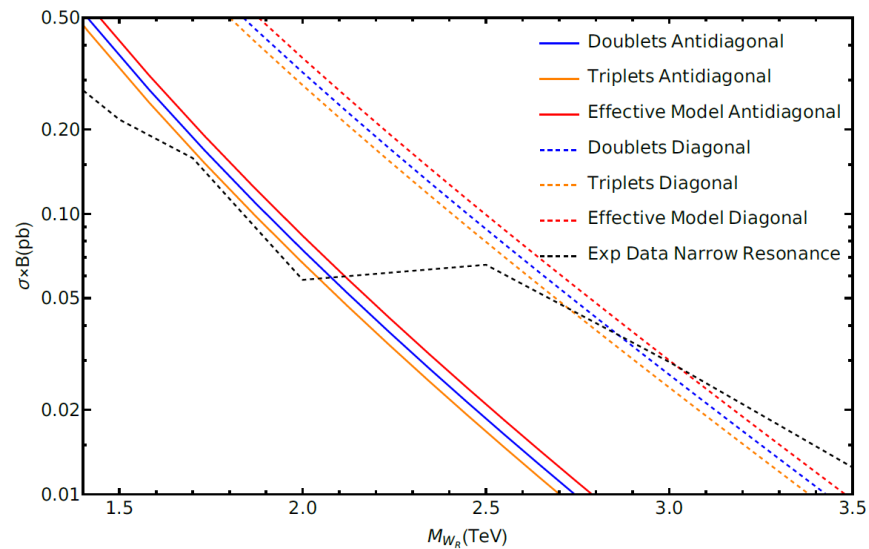
$$V_R^{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix} \quad (\text{Unitarity})$$

- We can also compare with the diagonal structure.
- Bernard, Descotes-Genon, Vale Silva (2001.00886)
- Ball et Al. (1207.1303)

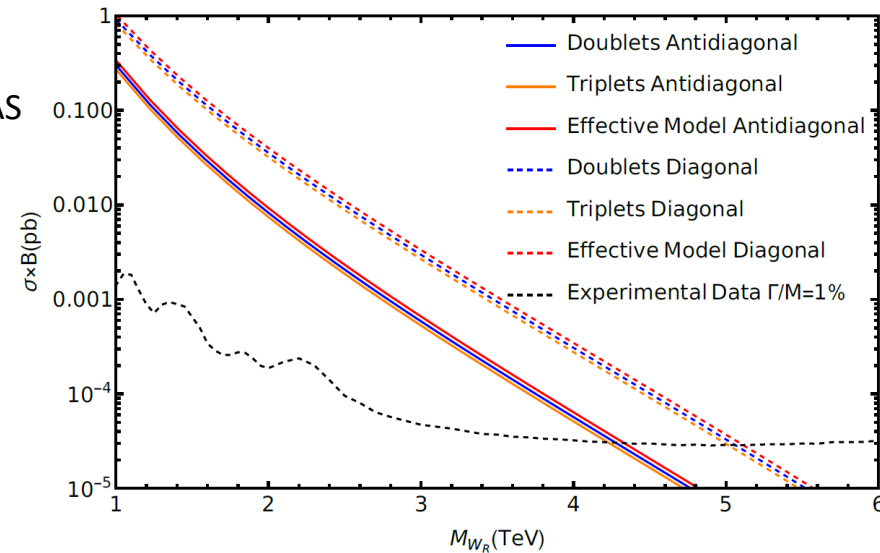


# Bound on the Mass of the $W_R$

- We take the minimum possible value of the cross section. It corresponds to the less constraining bound on  $M_{W_R}$  and  $\Gamma_{W_R} \approx 1\%$ .



Hadronic: ATLAS  
(1910.08447)



Leptonic: ATLAS  
(1906.05609)

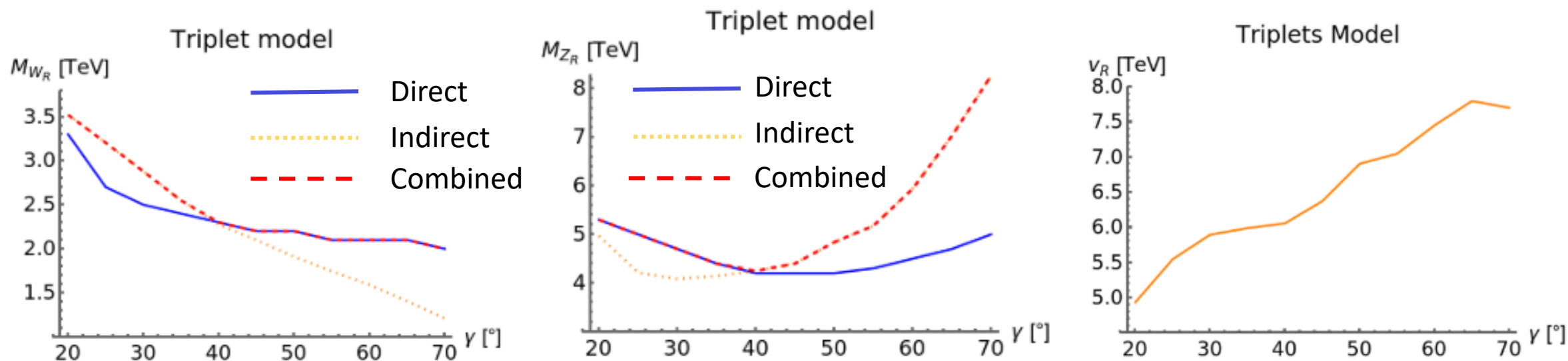
$W_R \rightarrow j_1 j_2$	$\Phi + \chi_{L,R}$	$\Phi + \Delta_{L,R}$	$\chi_L + \chi_R$
$M_{W_R}(\text{TeV})_{AD}$	2.1	2.0	2.1
$M_{W_R}(\text{TeV})_D$	2.9	2.7	3.0

$W_R \rightarrow e\nu_R, \mu\nu_R$	$\Phi + \chi_{L,R}$	$\Phi + \Delta_{L,R}$	$\chi_L + \chi_R$
$M_{W_R}(\text{TeV})_{AD}$	4.3	4.2	4.3
$M_{W_R}(\text{TeV})_D$	5.1	5.0	5.1

# Combination of Direct and Indirect Bounds

If we put a **Direct Bound** on the mass of **One Gauge Boson** for a certain value of  $\gamma$ , we can put an **Indirect Bound** on the mass of the **Other Gauge Boson** and  $v_R$  using:

$$M_{W_R} \approx M_{Z_R} \cos \gamma \approx \frac{e v_R}{2 \cos \theta_W \sin \gamma} \quad (\text{Doublets}) \quad M_{W_R} \approx \frac{1}{\sqrt{2}} M_{Z_R} \cos \gamma \approx \frac{e v_R}{\sqrt{2} \cos \theta_W \sin \gamma} \quad (\text{Triplets})$$



# Summary of Bounds

	$\Phi + \chi_{L,R}$	$\Phi + \Delta_{L,R}$	$\chi_L + \chi_R$
$M_{W_R}$ (TeV)	4.3	2.0	2.1
$M_{Z_R}$ (TeV)	5.4	4.2	4.3
$v_R$ (TeV)	10	4.9	10

	Origin of the Bound
$M_{W_R}$ Doublets	Direct $W_R \rightarrow l\nu_R$
$M_{Z_R}$ Doublets	Indirect $W_R \rightarrow l\nu_R$
$M_{W_R}$ Triplets	Direct $W_R \rightarrow qq$
$M_{Z_R}$ Triplets	Combination $Z_R \rightarrow ll$ $W_R \rightarrow qq$
$M_{W_R}$ Effective	Direct $W_R \rightarrow qq$
$M_{Z_R}$ Effective	Direct $Z_R \rightarrow ll$

# Results

- We have proposed a new way to study LR Models using **Effective Field Theory**.
- We have seen that achieving **Model Independent Bounds** with **Flavour Observables** requires a **Global Fit** allowing for **Any Possible Structure** of the RH Quark Mixing Matrix.
- We have been able to put a **General Bound** on the **Width** of the  $W_R$  and  $Z_R$  using the **Equivalence Theorem**.
- Assuming **Perturbativity**, we obtain from the LHC Run 2 data **Model Independent Bounds** on  $M_{W_R}$ ,  $M_{Z_R}$  and  $v_R$  for the different **SSB Mechanisms**.

# Backup Slide: Summary of Plots

