

Generic tests of CP-violation for high- p_T multi-leptons

ICHEP 2024

BSM session
19/7/2024

Based on:

- "Generic tests of CP-violation in high- p_T multi-lepton signals at the LHC and beyond"
PRL (2023), [arxiv: 2212.09433](#), Afik(CERN), SBS(Technion), Pal(UCR), Soni(BNL), Wudka(UCR)
- "CP-Violation at the High-energy Frontier; guiding principles"
SBS, Soni, Wudka, [arxiv: 2407.XXXXX](#)

CPV @ the high-energy frontier

guiding principles

- SM_0 : SM has a $G_0 = U(3)^5$ flavor symmetry when all fermion masses are set to zero (SM_0 is CP-conserving !)
- SM_+ : the SM_0 with a massive top-quark has a reduced symmetry $G_+ = U(3)^4 \times U(2) \times U(1) \subset G_0$:

$$\mathcal{L}_{SM_t} = \mathcal{L}_{SM_0} + \left(y_t \bar{q}_3 t \tilde{\phi} + \text{H.c.} \right)$$

- NP that underlies the SM can be parameterized in general by higher dimensional, gauge-invariant effective operators:

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{n=5}^{\infty} \frac{1}{\Lambda^{n-4}} \sum_i \alpha_i Q_i^{(n)}$$

use the SMEFT framework (basis)

- SMEFT can likewise be segregated into the sectors that possess the G_0 & G_t global symmetries of the SM_0 and SM_t ; then

$$\begin{aligned}\mathcal{L}_{G_0} &= \mathcal{L}_{SM_0} + \mathcal{L}_{SMEFT_0} , \\ \mathcal{L}_{G_t} &= \mathcal{L}_{SM_t} + \mathcal{L}_{SMEFT_0} + \mathcal{L}_{SMEFT_t}\end{aligned}$$

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{n=5}^{\infty} \frac{1}{\Lambda^{n-4}} \sum_i \alpha_i Q_i^{(n)}$$

$$\mathcal{L}_{\mathcal{G}_0} = \mathcal{L}_{SM_0} + \mathcal{L}_{SMEFT_0} ,$$

$$\mathcal{L}_{\mathcal{G}_t} = \mathcal{L}_{SM_t} + \mathcal{L}_{SMEFT_0} + \mathcal{L}_{SMEFT_t}$$

- CPV parts of SMEFT₀ & SMEFT_t:

$\mathcal{L}_{SMEFT_0}^{CPV}$	$\mathcal{L}_{SMEFT_t}^{CPV}$
$Q_{\tilde{G}} = f^{ABC} \tilde{G}_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$	$Q_{tG} = (\bar{q}_3 \sigma^{\mu\nu} T^A t) \tilde{\phi} G_{\mu\nu}^A$
$Q_{\tilde{W}} = f^{IJK} \tilde{G}_{\mu}^{I\nu} W_{\nu}^{J\rho} W_{\rho}^{K\mu}$	$Q_{tW} = (\bar{q}_3 \sigma^{\mu\nu} t) \tau^I \tilde{\phi} W_{\mu\nu}^I$
$Q_{\phi\tilde{G}} = \phi^{\dagger} \phi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{tB} = (\bar{q}_3 \sigma^{\mu\nu} t) \tilde{\phi} B_{\mu\nu}$
$Q_{\phi\tilde{W}} = \phi^{\dagger} \phi \tilde{W}_{\mu\nu}^I G^{I\mu\nu}$	$Q_{t\phi} = \phi^{\dagger} \phi (\bar{q}_3 t) \tilde{\phi}$
$Q_{\phi\tilde{B}} = \phi^{\dagger} \phi \tilde{B}_{\mu\nu} B^{\mu\nu}$	
$Q_{\phi\tilde{W}B} = \phi^{\dagger} \tau^I \phi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	

$O(1/\Lambda^2)$ interference effects (CPV) only from:

SMEFT₀ × SM₀ & SMEFT_t × SM_t

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{n=5}^{\infty} \frac{1}{\Lambda^{n-4}} \sum_i \alpha_i Q_i^{(n)}$$

$$\mathcal{L}_{\mathcal{G}_0} = \mathcal{L}_{SM_0} + \mathcal{L}_{SMEFT_0} ,$$

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- CPV parts of $SMEFT_0$ & $SMEFT_t$:

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$\mathcal{L} Q_{\phi\tilde{W}B} = \phi^{\dagger} \tau^I \phi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	

- these opts are Loop Generated (LG) in the underlying theory

\mathcal{L} expect corresponding Wilson coef: $\alpha_i \sim 1/(4\pi)^2$

Arzt, Einhorn, Wudka, NPB(1995), hep-ph/9405214 & Einhorn, Wudka, NPB(2013), arxiv:1307.0478

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{n=5}^{\infty} \frac{1}{\Lambda^{n-4}} \sum_i \alpha_i Q_i^{(n)}$$

$$\mathcal{L}_{g_0} = \mathcal{L}_{SM_0} + \mathcal{L}_{SMEFT_0},$$

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- CPV parts of SMEFT₀ & SMEFT_t:

$\mathcal{L}_{SMEFT_0}^{CPV}$	$\mathcal{L}_{SMEFT_t}^{CPV}$
$\Rightarrow Q_{\tilde{G}} = f^{ABC} \tilde{G}_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$	$Q_{tG} = (\bar{q}_3 \sigma^{\mu\nu} T^A t) \tilde{\phi} G_{\mu\nu}^A$
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$\Rightarrow Q_{\phi\tilde{W}B} = \phi^{\dagger} \tau^I \phi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	

Also: these opts are tightly constrained by lepton and neutron EDMs
 Kley, Theil, Venturini, Weiler, EPJC(2022), arxiv:2109.15085

- these opts are Loop Generated (LC) from underlying theory

\Rightarrow expect corresponding coefficients: $\alpha_i \sim 1/(4\pi)^2$

Arzt, Einhorn, Wudka, hep-ph/9405214 & Einhorn, Wudka, NPB(2013), arxiv:1307.0478

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	$\mathcal{L}_{t\phi} = \phi^{\dagger} \phi (\bar{q}_3 t) \tilde{\phi}$

- the only opt. that is Potentially Tree-Level Generated (PTG) in the underlying theory

expect (naturalness) corresponding Wilson coef: $\alpha_i = O(1)$

Arzt, Einhorn, Wudka, NPB(1995), hep-ph/9405214 & Einhorn, Wudka, NPB(2013), arxiv:1307.0478

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$$Q_{t\phi} = \phi^\dagger \phi (\bar{q}_3 t) \tilde{\phi}$$

- Only $Q_{t\phi}$ can potentially generate leading CPV effects @ high-energy colliders - **in top-quark systems ...**

$$Q_{t\phi} = \phi^\dagger \phi (\bar{q}_3 t) \tilde{\phi} \implies \mathcal{L}_{tth} = -h\bar{t}(a + ib\gamma_5)t$$

- Best bet: CPV from interference of tree-level diagrams **e.g., in $e^+e^- \rightarrow tth$, $pp \rightarrow tth$, $pp \rightarrow th + X$**

$$Q_{t\phi} = \phi^\dagger \phi (\bar{q}_{3t}) \tilde{\phi}$$

- However: CP asymmetry behaves as:

$$\mathcal{A}_{CP} \propto \frac{d\sigma_{CPV}}{d\sigma_{CPC}}$$

$$\text{Im} \left(M_{SM} M_{NP}^\dagger \right) \propto \frac{v^2}{\Lambda^2}$$

$$|M_{SM}|^2$$

CPV @ the high-energy frontier: guiding principles

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$$|M_{SM}|^2$$

$$\mathcal{A}_{CP} \sim O \left(\frac{v^2}{\Lambda^2} \right) \sim O(1\%)$$

- Such CP effects are, unfortunately, too small to be detected !

▷ No CPV signal is expected from SMxEFT interreference if underlying NP obeys SM symmetries (G_0 & G_+)!

arxiv:2407.xxxxx, SBS, Soni, Wudka

- If flavor is violated in the underlying heavy theory
then:
all SMEFT opts containing flavor-violating
combinations of fermion fields can violate CP !

CPV from flavor violating NP

- Leading CPV effects in this case from **NPxNP' @ tree-level**
- **No SM contribution @ tree-level !**

$$\text{Im} \left(M'_{NP} M_{NP}^\dagger \right) \propto \frac{v_E^4}{\Lambda^4}$$

$$d\sigma \equiv d\sigma_{\text{CPC}} + d\sigma_{\text{CPV}}$$

$$|M_{NP}|^2 \propto \frac{v_E^4}{\Lambda^4}$$

$$v_E = v \text{ or } v_E = E \dots$$

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$$v_E = v \text{ or } v_E = E \dots$$

- **CP asymmetry expected in this case:**

$$\mathcal{A}_{\text{CP}} \propto \frac{d\sigma_{\text{CPV}}}{d\sigma_{\text{CPC}}} \sim \mathcal{O}(1)$$

CPV from flavor violating NP

Best bet: top-quark FV interactions (least constrained, heavy top ...)

Interesting example: **tull/tcII 4-Fermi contact terms**

$$Q_S = (\bar{\ell}_R \ell_R) (\bar{t}_R u_R) \quad , \quad Q_T = (\bar{\ell}_R \sigma_{\mu\nu} \ell_R) (\bar{t}_R \sigma_{\mu\nu} u_R) ; \quad \ell = e, \mu$$

Scalar

$$Q_{lequ}^{(1)} = (\bar{\ell}^j e) \epsilon_{jk} (\bar{q}^k u)$$

SMEFT 

Tensor

$$Q_{lequ}^{(3)} = (\bar{\ell}^j \sigma_{\mu\nu} e) \epsilon_{jk} (\bar{q}^k \sigma^{\mu\nu} u)$$



$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{\Lambda^2} [(\alpha_S Q_S + \alpha_T Q_T) + \text{H.c.}]$$

$$Q_S = (\bar{\ell}_R \ell_R) (\bar{t}_R u_R) \quad , \quad Q_T = (\bar{\ell}_R \sigma_{\mu\nu} \ell_R) (\bar{t}_R \sigma_{\mu\nu} u_R) ; \quad \ell = e, \mu$$

Scalar

Tensor

$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{\Lambda^2} [(\alpha_S Q_S + \alpha_T Q_T) + \text{H.c.}]$$

- *Current sensitivities (bounds):*

$$\Lambda(\text{t}\mu\mu) , \Lambda(\text{t}ee) > \sim \text{O}(0.5 \text{ TeV}) , \text{ Scalar} \\ > \sim \text{O}(1 \text{ TeV}) , \text{ Tensor}$$

$$Q_S = (\bar{\ell}_R \ell_R) (\bar{t}_R u_R) \quad , \quad Q_T = (\bar{\ell}_R \sigma_{\mu\nu} \ell_R) (\bar{t}_R \sigma_{\mu\nu} u_R) ; \quad \ell = e, \mu$$

Scalar

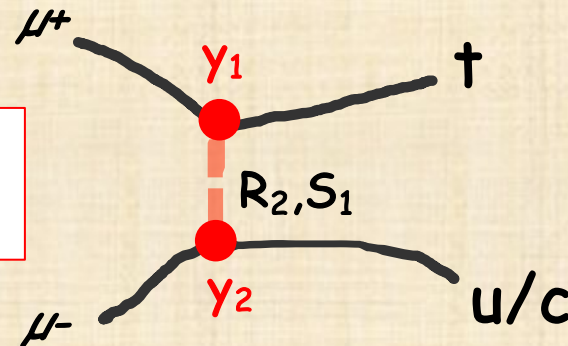
Tensor

$$\mathcal{L} = \mathcal{L}_{SM} + \frac{1}{\Lambda^2} [(\alpha_S Q_S + \alpha_T Q_T) + \text{H.c.}]$$

- Matching to possible underlying BSM scenarios:

Tree-level exchanges of the heavy R_2, S_1 LQ's

$$\alpha_S = 4\alpha_T = \frac{y_1 y_2^*}{2M_{LQ}^2}$$



Specific proportion of Wilson coefficients used as benchmark from underlying UV physics

$$\text{Im}(\alpha_S \cdot \alpha_T^*) = 0.25$$

CP test in high- p_T multi-leptons events

- Constructing generic tests of CPV (BSM) in multi-lepton processes: **focus on tri-lepton events**
(applies also to 4-leptons events ...)

$$\begin{aligned} pp &\rightarrow l'^- l^+ l^- + X_3 \\ pp &\rightarrow l'^+ l^- l^+ + \bar{X}_3, \\ pp &\rightarrow l'^+ l'^- l^+ l^- + X_4 \end{aligned}$$

e.g., $l'^- l^+ l^- = e^\pm \mu^+ \mu^-, \mu^\pm e^+ e^-$

- $l, l' = e, \mu, \tau$ (preferably $l \neq l'$)
- X_3, \bar{X}_3 and X_4 : jets and missing energy

CPV multi-leptons events

PRL2023, Afik, SBS, Pal, Soni, Wudka (arxiv: 2212.09433)

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- $l, l' = e, \mu, \tau$ (preferably $l \neq l'$)
- X_3, \bar{X}_3 and X_4 : jets and missing energy

- Note: sizeable, say $O(\text{few}\%)$, manifestation of CPV in multi-leptons events of the type considered will be an unambiguous indication of NP, since the CP-odd CKM-phase of the SM is expected to yield negligible CP-violating effects in these processes

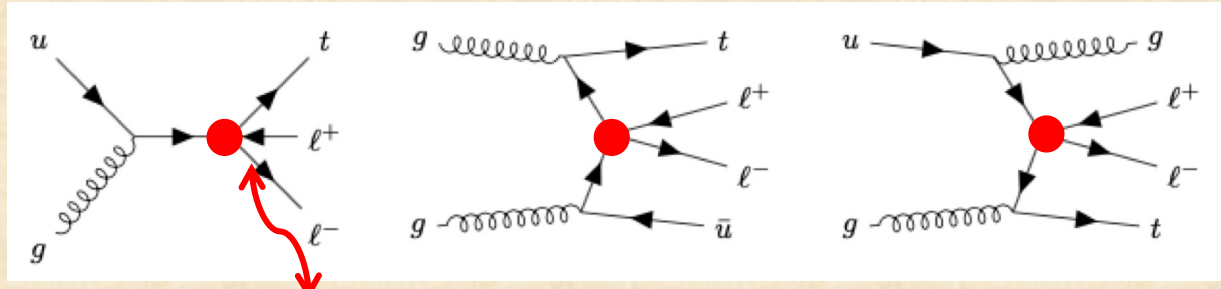
(CPV@SM in multi-lepton signals can only arise from EW processes at higher loop orders)

CPV in tri-lepton events from single top production

tull 4-Fermi is "injected" as an EFT toy model

$$pp \rightarrow l^+ l^- + t ,$$

$$pp \rightarrow l^+ l^- + t + j$$



tull/tcII 4-Fermi

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_{n=5}^{\infty} \frac{1}{\Lambda^{n-4}} \sum_i f_i \mathcal{O}_i^{(n)}$$

dim.6 scalar : $\mathcal{O}_S = (\bar{l}^j e) \epsilon_{jk} (\bar{q}^k u)$
 dim.6 tensor : $\mathcal{O}_T = (\bar{l}^j \sigma_{\mu\nu} e) \epsilon_{jk} (\bar{q}^k \sigma^{\mu\nu} u)$

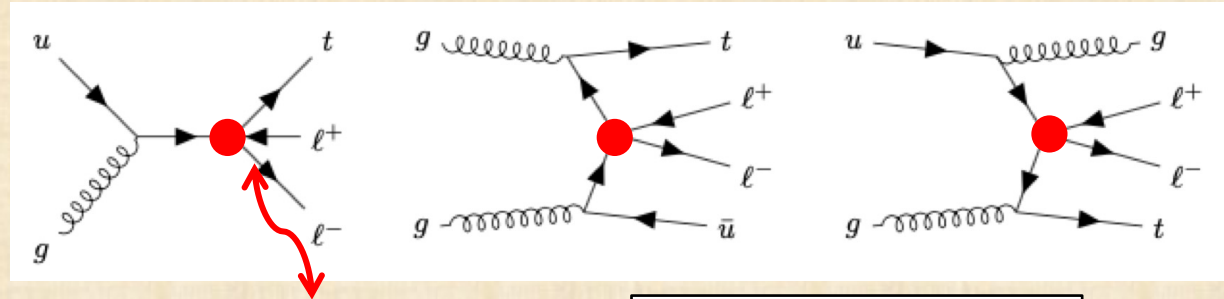
e.g.,

$$pp \rightarrow t \mu^+ \mu^- \rightarrow e^+ \mu^+ \mu^- + X \quad (\& \text{CC channel})$$

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e.g.,

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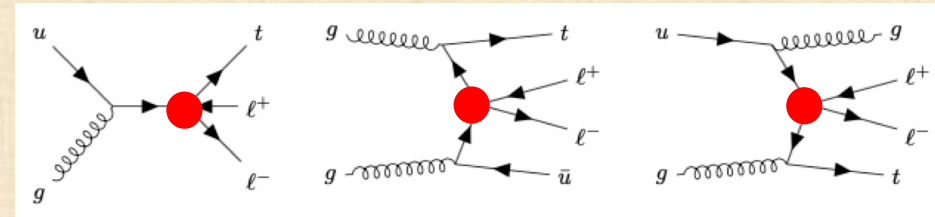
This channel has interesting implications also for generic BSM searches of new heavy states around the TeV-scale which generate top-leptons 4-Fermi

Dominant SM backg.

NP signals

$pp \rightarrow WZ + X$
followed by W & Z decays ...

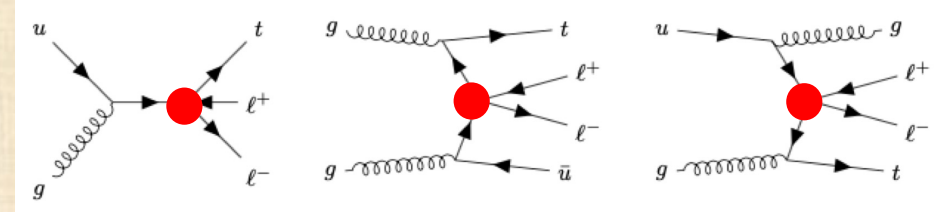
much smaller contribution from:
 $pp \rightarrow ttW, ttZ, tVV, tt, Z+\text{jets}$
followed by t and V decays ...



Dominant SM backg.

NP signals

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much smaller contribution from:
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followed by t and V decays ...

$$d\hat{\sigma}(CPV) \propto \epsilon(p_{u_i}, p_{\ell^+}, p_{\ell^+}, p_{\ell^-}) \cdot \text{Im}(f_S f_T^*)$$

CPV

No interference with SM:

$$\sigma(m_{\ell\ell}^{\min}) = \sigma^{\text{SM}}(m_{\ell\ell}^{\min}) + \frac{f^2}{\Lambda^4} \cdot \sigma^{\text{NP}}(m_{\ell\ell}^{\min})$$

$$\sigma(m_{\ell\ell}^{\min}) \equiv \sigma(m_{\ell\ell} \geq m_{\ell\ell}^{\min}) = \int_{m_{\ell\ell} \geq m_{\ell\ell}^{\min}} dm_{\ell\ell} \frac{d\sigma}{dm_{\ell\ell}}$$

$m_{\ell\ell}^{\min}$ - useful discriminating parameter

Constructing CP-asym. for tree-level CPV

$$\mathcal{M}_{ab \rightarrow \ell'^- \ell^+ \ell^-} = M_1 e^{i(\phi_1 + \delta_1)} + M_2 e^{i(\phi_2 + \delta_2)}$$

$\phi_{1,2}$ are CP-odd phases & $\delta_{1,2}$ are CP-even phases (from FSI, loops ...)

CPV @ tree-level (no FSI phases: $\delta=0$)!

- To probe tree-level CPV one needs T_N -odd observables ($T_N: \dagger \rightarrow -\dagger$)
=> T_N -odd observables do not vanish when FSI phases are zero ($\delta = 0$)

T_N - odd

asymmetries based on triple-products (TP)

$$\begin{aligned} \mathcal{O}_{\text{CP}} &= \vec{p}_{\ell'^-} \cdot (\vec{p}_{\ell^+} \times \vec{p}_{\ell^-}) \\ \overline{\mathcal{O}_{\text{CP}}} &= \vec{p}_{\ell'^+} \cdot (\vec{p}_{\ell^-} \times \vec{p}_{\ell^+}) \end{aligned}$$

CPV \rightarrow multi-leptons events: Constructing CP-asym from TP's

- Divide into 2 "hemispheres" in \mathcal{O}_{CP} space and define the **P-violating & T_N -odd** observables (odd under $t \rightarrow -t$):

Recall:

$pp \rightarrow t \mu^+ \mu^- \rightarrow e^+ \mu^+ \mu^- + X$ & CC channel

($l' = e, l = \mu$)

$$\begin{aligned}\mathcal{O}_{\text{CP}} &= \vec{p}_{l'-} \cdot (\vec{p}_{l'+} \times \vec{p}_{l-}) \\ \overline{\mathcal{O}_{\text{CP}}} &= \vec{p}_{l'+} \cdot (\vec{p}_{l-} \times \vec{p}_{l'+})\end{aligned}$$

$$\begin{aligned}A_T &\equiv \frac{N(\mathcal{O}_{\text{CP}} > 0) - N(\mathcal{O}_{\text{CP}} < 0)}{N(\mathcal{O}_{\text{CP}} > 0) + N(\mathcal{O}_{\text{CP}} < 0)}, \\ \bar{A}_T &\equiv \frac{N(-\overline{\mathcal{O}_{\text{CP}}} > 0) - N(-\overline{\mathcal{O}_{\text{CP}}} < 0)}{N(-\overline{\mathcal{O}_{\text{CP}}} > 0) + N(-\overline{\mathcal{O}_{\text{CP}}} < 0)}\end{aligned}$$

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In general: $A_T \neq 0$ & $\bar{A}_T \neq 0$ may also be a signal of some strong or generic CP-even phase (FSI...) even if the underlying dynamics are CP-conserving !

- Isolating the pure CPV effect:

$$A_{CP} = \frac{1}{2} (A_T - \bar{A}_T)$$

$$pp \rightarrow t \mu \mu \rightarrow \mu \mu e + X$$

$$A_{CP} = \frac{1}{2} (A_T - \bar{A}_T)$$

$$A_T \equiv \frac{N(\mathcal{O}_{CP} > 0) - N(\mathcal{O}_{CP} < 0)}{N(\mathcal{O}_{CP} > 0) + N(\mathcal{O}_{CP} < 0)},$$

$$\bar{A}_T \equiv \frac{N(-\overline{\mathcal{O}_{CP}} > 0) - N(-\overline{\mathcal{O}_{CP}} < 0)}{N(-\overline{\mathcal{O}_{CP}} > 0) + N(-\overline{\mathcal{O}_{CP}} < 0)}$$

NP (CPV)

$$Q_S = (\bar{l}_R l_R) (\bar{t}_R u_R), \quad Q_T = (\bar{l}_R \sigma_{\mu\nu} l_R) (\bar{t}_R \sigma_{\mu\nu} u_R); \quad l = e, \mu$$

$$\mathcal{O}_{CP} = \vec{p}_{e^-} \cdot (\vec{p}_{\mu^+} \times \vec{p}_{\mu^-})$$

$$\overline{\mathcal{O}_{CP}} = \vec{p}_{e^+} \cdot (\vec{p}_{\mu^-} \times \vec{p}_{\mu^+})$$

Recup:

$$pp \rightarrow t \mu \mu \rightarrow \mu \mu e + X$$

$$A_{CP} = \frac{1}{2} (A_T - \bar{A}_T)$$

$$A_T \equiv \frac{N(\mathcal{O}_{CP} > 0) - N(\mathcal{O}_{CP} < 0)}{N(\mathcal{O}_{CP} > 0) + N(\mathcal{O}_{CP} < 0)},$$
$$\bar{A}_T \equiv \frac{N(-\overline{\mathcal{O}}_{CP} > 0) - N(-\overline{\mathcal{O}}_{CP} < 0)}{N(-\overline{\mathcal{O}}_{CP} > 0) + N(-\overline{\mathcal{O}}_{CP} < 0)}$$

NP (CPV)

$$Q_S = (\bar{\ell}_R \ell_R) (\bar{t}_R u_R), \quad Q_T = (\bar{\ell}_R \sigma_{\mu\nu} \ell_R) (\bar{t}_R \sigma_{\mu\nu} u_R); \quad \ell = e, \mu$$

$$\mathcal{O}_{CP} = \vec{p}_{e^-} \cdot (\vec{p}_{\mu^+} \times \vec{p}_{\mu^-})$$

$$\overline{\mathcal{O}}_{CP} = \vec{p}_{e^+} \cdot (\vec{p}_{\mu^-} \times \vec{p}_{\mu^+})$$

SM contributes to the denominators **while** NP(CPV) contributes to numerators !



Asymmetries sensitive to di-leptons invariant mass:

SM \in low m_{ll}

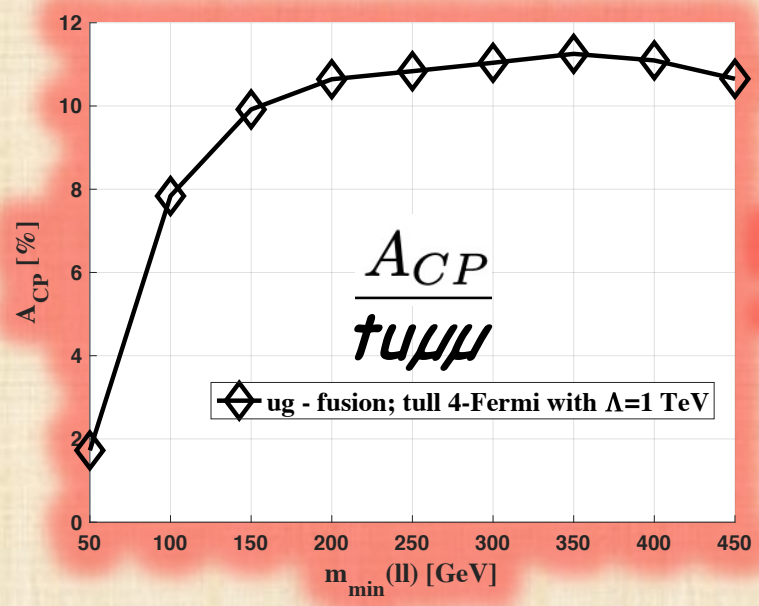
NP \in high m_{ll}

Results:

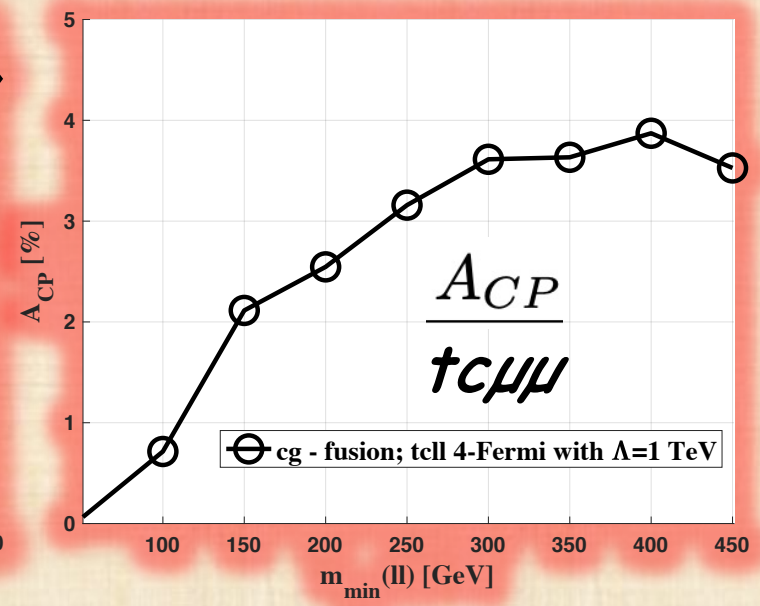
$u g \rightarrow t \mu \mu \rightarrow \mu \mu e$
($\tau u \mu \mu$ 4-Fermi)

$c g \rightarrow t \mu \mu \rightarrow \mu \mu e$
($\tau c \mu \mu$ 4-Fermi)

	$u g$ -fusion: $\Lambda = 1(2)$ TeV	$c g$ -fusion: $\Lambda = 1(2)$ TeV
A_{CP}	11.1(7.9)%	3.9(0.7)%
A_T	16.4(13.5)%	3.1(0.5)%
\bar{A}_T	-5.8(-2.3)%	-4.7(-1.0)%



**$O(10\%)$ asymmetry at high m_{\parallel} !
 (di-lepton inv-mass > 150 GeV)**



**2-4% asymmetry at high m_{\parallel} !
 (di-lepton inv-mass > 150 GeV)**

SUMMARY



CONCLUSION

- Under naturalness arguments of the underlying heavy NP & in the absence of flavor-changing interactions,

only a single operator $Q_{t\phi} = \phi^\dagger \phi (\bar{q}_3 t) \tilde{\phi}$ can generate non-vanishing CPV from SMxNP interference !

- $Q_{t\phi}$ modifies the top-Yukawa coupling:

$$Q_{t\phi} = \phi^\dagger \phi (\bar{q}_3 t) \tilde{\phi} \implies \mathcal{L}_{tth} = -h\bar{t}(a + ib\gamma_5) t$$

- Unfortunately, CPV effects in top-quark systems, from $Q_{t\phi}$, are too small ... !



- If flavor is violated @ TeV-scale in the top-quark sector, then large CPV effects might be manifested in multi-leptons signals at the LHC
 - Besides: multi-leptons signals provide an excellent & rich testing ground of NP:
flavor physics, lepton flavor universality, **CP-Violation ...**

“Tri- and four-lepton events as a probe for new physics in ttll contact interactions”
NPB980 (2022), 115849 [arxiv: 2111.13711](#), Afik(CERN), SBS(Technion), Pal(UCR), Soni(BNL), Wudka(UCR)

“New flavor physics in di- and trilepton events from single-top production at the LHC and beyond”,
PRD103 (2021), 075031, [arxiv: 2101.05286](#), Afik, SBS, Soni, Wudka

“High pT correlated tests of lepton universality in lepton(s) + jet(s) processes; An EFT analysis”,
PLB811 (2020), 135908, [arxiv: 2005.06457](#), Afik, SBS, Cohen(Technion), Soni, Wudka

“Searching for New Physics with blll contact interactions”,
PLB807 (2020), 135541, [arxiv: 1912.00425](#), Afik, SBS, Cohen, Rozen(Technion)

- We have constructed useful CP asymmetries for measuring CP-violation in multi-lepton events
- These asymmetries have several new & unique features, that make them particularly useful for searching for CP-violation at high-energy colliders

SUMMARY



CONCLUSION

- Our CP tests use multi-lepton final states as probes, which makes them experimentally highly distinctive
- They are based on simple kinematic observables that only require the reconstruction of the relatively easily-identifiable charged-lepton momenta
- They can be generated by tree-level CP -violating underlying physics, making them very sensitive to new physics
- They are generic, meaning they can probe a wide range of underlying new physics
- They include a new modification to the classic formula for CP -violation in scattering and decay processes, which takes into account the effect of an asymmetric initial state on the measurement of CP -violation



- Resulting CP asymmetries:

$O(10\%)$ with new CPV TeV-scale NP

- SM backg. For CPV in multi-lepton events is at the sub-% level ...
- Expect $O(10000)$ high- p_T tri-lepton events

with $L \sim O(1000) \text{ fb}^{-1}$ & TeV scale NP (generating a full 4-Fermi)

Thank you!

Backups

- CPV may be the key to a deeper understanding of particle physics and the evolution of the universe; it has far-reaching implications for cosmology ...
 - CPV is needed to explain the observed baryon asymmetry of the universe (BAU)
 - CPV@SM is insufficient to explain the BAU
 - CP is not a symmetry of nature
 - ▶ on general grounds, one expects any generic new physics to entail BSM CP-odd phase(s)
- Examples:
SUSY, Mutli-Higgs models, Leptoquarks, Vector-like fermions ...

multi-leptons signals - a window to NP

$$\begin{aligned}(1\ell) &: pp \rightarrow \ell^\pm + n \cdot j_b + m \cdot j + \cancel{E}_T + X , \\(2\ell) &: pp \rightarrow \ell'^+ \ell''^- + n \cdot j_b + m \cdot j + \cancel{E}_T + X , \\(3\ell) &: pp \rightarrow \ell'^\pm \ell^+ \ell^- + n \cdot j_b + m \cdot j + \cancel{E}_T + X , \\(4\ell) &: pp \rightarrow \ell'^\pm \ell''^\mp \ell^+ \ell^- + n \cdot j_b + m \cdot j + \cancel{E}_T + X\end{aligned}$$

- Rich & clean signals in the hadronic environment of the LHC
- Excellent test ground for NP (e.g., in $pp \rightarrow ttV, ttH, tV, tttt \dots$):
 - Sensitive to many types of underlying NP

(lepton-flavor violation, lepton universality violation,
lepton-number violation - same sign leptons, CP violation ...)

- easy to construct observables with charged leptons
- High- E/p_T (TeV energies ...) leptons still relatively unexplored
- Correlated multi-lepton channels due to common underlying NP !

“Tri- and four-lepton events as a probe for new physics in $t\bar{t}ll$ contact interactions”
NPB980 (2022), 115849 [arxiv: 2111.13711](#), Afik(CERN), SBS(Technion), Pal(UCR), Soni(BNL), Wudka(UCR)

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“Searching for New Physics with $b\bar{b}ll$ contact interactions”,
PLB807 (2020), 135541, [arxiv: 1912.00425](#), Afik, SBS, Cohen, Rozen(Technion)

CPV multi-leptons events


- Consider the underlying hard processes for tri-leptons production:

$$ab \rightarrow \ell'^- \ell^+ \ell^- \quad \text{and} \quad \bar{a}\bar{b} \rightarrow \ell'^+ \ell^- \ell^+$$

- CPV requires at least 2 amplitudes with different CP-odd phases:

$$\mathcal{M}_{ab \rightarrow \ell'^- \ell^+ \ell^-} = M_1 e^{i(\phi_1 + \delta_1)} + M_2 e^{i(\phi_2 + \delta_2)}$$

$\phi_{1,2}$ are CP-odd phases & $\delta_{1,2}$ are CP-even phases


$$\bar{\mathcal{M}}_{\bar{a}\bar{b} \rightarrow \ell'^+ \ell^- \ell^+} = M_1 e^{i(-\phi_1 + \delta_1)} + M_2 e^{i(-\phi_2 + \delta_2)}$$

CC channel

CPV \Rightarrow multi-leptons events

- Classification of CP according to T_N transformation properties ($T_N: \dagger \rightarrow -\dagger$)

$$\mathcal{M}_{ab \rightarrow \ell' - \ell + \ell -} = M_1 e^{i(\phi_1 + \delta_1)} + M_2 e^{i(\phi_2 + \delta_2)}$$

- type: T_N - odd T_N - even

- CP asymmetry: $A_{CP} \propto \cos \Delta\delta \sin \Delta\phi$ $A_{CP} \propto \sin \Delta\delta \sin \Delta\phi$

$$\Delta\phi = \phi_1 - \phi_2, \Delta\delta = \delta_1 - \delta_2$$

- phases: Only CP-odd Both CP-odd & CP-even (strong phase)

- Sensitivity: tree-level CPV strong phase from FSI typically higher order effect ...

- Expected size: $O(10\%)$ $O(0.1\%)$

CPV \rightarrow multi-leptons events

- Classification of CP according to T_N transformation properties ($T_N: \dagger \rightarrow -\dagger$)

$$\mathcal{M}_{ab \rightarrow \ell' - \ell + \ell -} = M_1 e^{i(\phi_1 + \delta_1)} + M_2 e^{i(\phi_2 + \delta_2)}$$

- type:

T_N - odd

T_N - even

- CP asymmetry:

$$A_{CP} \propto \cos \Delta\delta \sin \Delta\phi$$

$$A_{CP} \propto \sin \Delta\delta \sin \Delta\phi$$

triple-products (TP) asymmetry

$$\begin{aligned} \mathcal{O}_{CP} &= \vec{p}_{\ell' -} \cdot (\vec{p}_{\ell +} \times \vec{p}_{\ell -}) \\ \overline{\mathcal{O}_{CP}} &= \vec{p}_{\ell' +} \cdot (\vec{p}_{\ell -} \times \vec{p}_{\ell +}) \end{aligned}$$

odd under P & under $T_N (\dagger \rightarrow -\dagger)$

and

$$\begin{aligned} C(\mathcal{O}_{CP}) &= +\overline{\mathcal{O}_{CP}}, & C(\overline{\mathcal{O}_{CP}}) &= +\mathcal{O}_{CP}, \\ CP(\mathcal{O}_{CP}) &= -\overline{\mathcal{O}_{CP}}, & CP(\overline{\mathcal{O}_{CP}}) &= -\mathcal{O}_{CP} \end{aligned}$$

Rate asymmetry

$$A_{CP} = \frac{N(\ell' - \ell + \ell -) - N(\ell' + \ell - \ell +)}{N(\ell' - \ell + \ell -) + N(\ell' + \ell - \ell +)}$$

A_{CP} function of $N(\text{sign}(\mathcal{O}_{CP}))$ & $N(\text{sign}(\overline{\mathcal{O}_{CP}}))$

Constructing CP-asym. For tree-level CPV

$$\mathcal{M}_{ab \rightarrow \ell' - \ell + \ell^-} = M_1 e^{i(\phi_1 + \delta_1)} + M_2 e^{i(\phi_2 + \delta_2)}$$

$\phi_{1,2}$ are CP-odd phases & $\delta_{1,2}$ are CP-even phases (from FSI, loops ...)

- Classification of CP according to T_N transformation properties ($T_N: \dagger \rightarrow -\dagger$)

- type:

T_N - odd

T_N - even

- CP asymmetry:

$$A_{CP} \propto \cos \Delta\delta \sin \Delta\phi$$

$$A_{CP} \propto \sin \Delta\delta \sin \Delta\phi$$

- requires:

Only CP-odd phase

Both CP-odd & CP-even phases

Constructing CP-asym. For tree-level CPV

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$$A_{CP} \propto \cos \Delta\delta \sin \Delta\phi$$

$$A_{CP} \propto \sin \Delta\delta \sin \Delta\phi$$

- requires:

Only CP-odd phase

Both CP-odd & CP-even phases

CPV @ tree-level (no FSI phases: $\Delta\delta=0$) !

Current sensitivities (bounds ...)

what do we know about the FC dim.6 (tu)(2l) opts

LEP: ($ee \rightarrow tu,tc$):

$\Lambda(tuee) > 0.5 - 1.5 \text{ TeV}$

(depending on Lorentz structure)

SBS,Wudka PRD1999

PLB2002 (0210041) ; EPJC2011 (1102.4455)

LHC ($pp \rightarrow tt$ followed by $t \rightarrow \mu\mu + \text{jet}$):

$\Lambda(tu\mu\mu) \sim \Lambda(tuee) > \sim 0.4 - 1 \text{ TeV}$

(depending on Lorentz structure)

Chala,Santiago,Spannowsky JHEP2019 (1809.09624)

also studied in:

Davidson,Mangano,Perries,Sordini EPJC2015 (1507.07163)

Durieux,Maltoni,Zhang PRD2015 (1412.7166)

Aguilar-Saavedra NPB2011 (1008.3562)

Boughezal,Chen,Petriello,Wiegand PRD2019 (1907.00997)

TABLE I: The estimated cross-sections in [fb], for the NP tri-lepton signals and the SM tri-lepton background.

Numbers are given for the NP parameters

$\text{Im}(f_S f_T^*) = 0.25$, $\Lambda = 1$ TeV and for three values of $m_{min}(\ell\ell)$ as indicated. See also description in the paper.

$m_{min}(\ell\ell)[GeV] \Rightarrow$	200	300	400
$\sigma_{NP}(pp_{ug} \rightarrow \ell'^- \ell^+ \ell^- + X)$	12.43	11.65	10.84
$\sigma_{NP}(\bar{u}g \rightarrow \ell'^+ \ell^- \ell^+ + X)$	0.98	0.87	0.76
$\sigma_{NP}(pp_{cg} \rightarrow \ell'^- \ell^+ \ell^- + X)$	0.37	0.32	0.27
$\sigma_{NP}(pp_{\bar{c}g} \rightarrow \ell'^+ \ell^- \ell^+ + X)$	0.37	0.32	0.27
$\sigma_{SM}(pp \rightarrow \ell'^- \ell^+ \ell^- + X)$	0.33	0.11	0.05
$\sigma_{SM}(pp \rightarrow \ell'^+ \ell^- \ell^+ + X)$	0.56	0.21	0.10

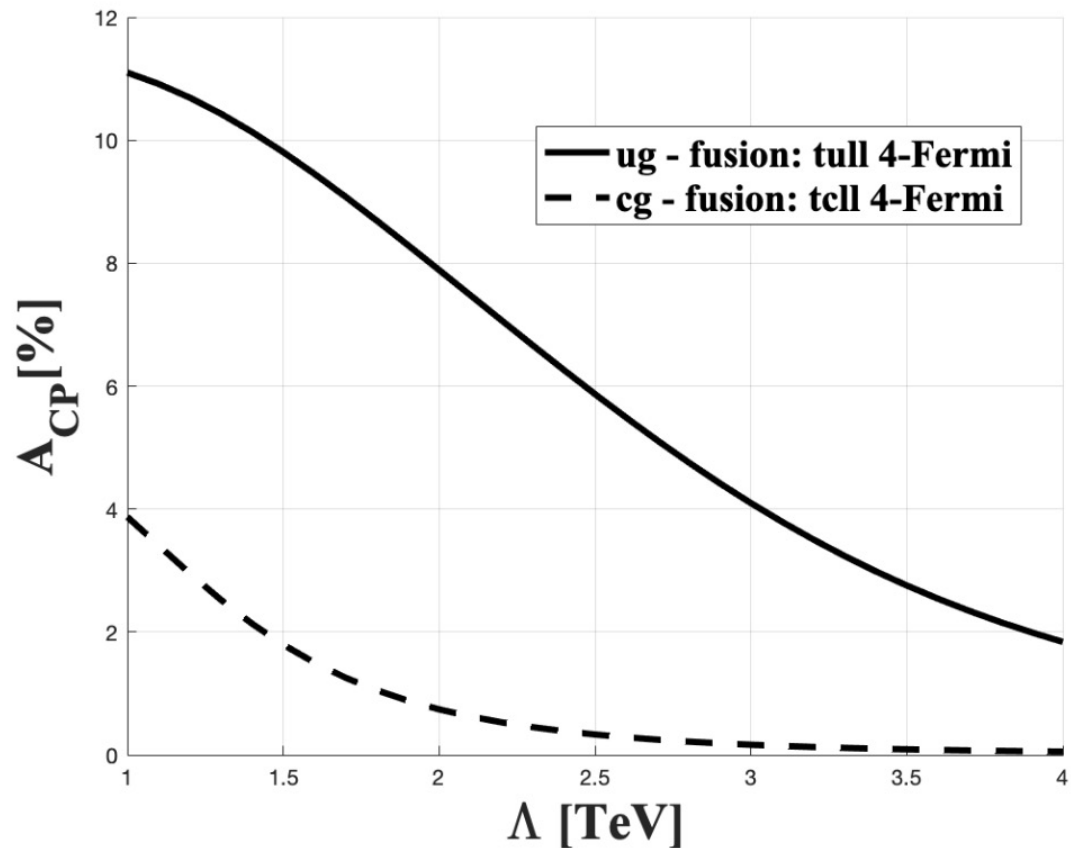


FIG. 1: The expected CP-asymmetry A_{CP} , as a function of the NP scale Λ , for $m_{min}(ll) = 400$ GeV and $\text{Im}(f_S f_T^*) = 0.25$. Results are shown for the cases of NP from ug and cg -fusion, which arise from the *tull* and *tcll* 4-Fermi operators, respectively. The SM background is calculated from $pp \rightarrow ZW^\pm + X$.

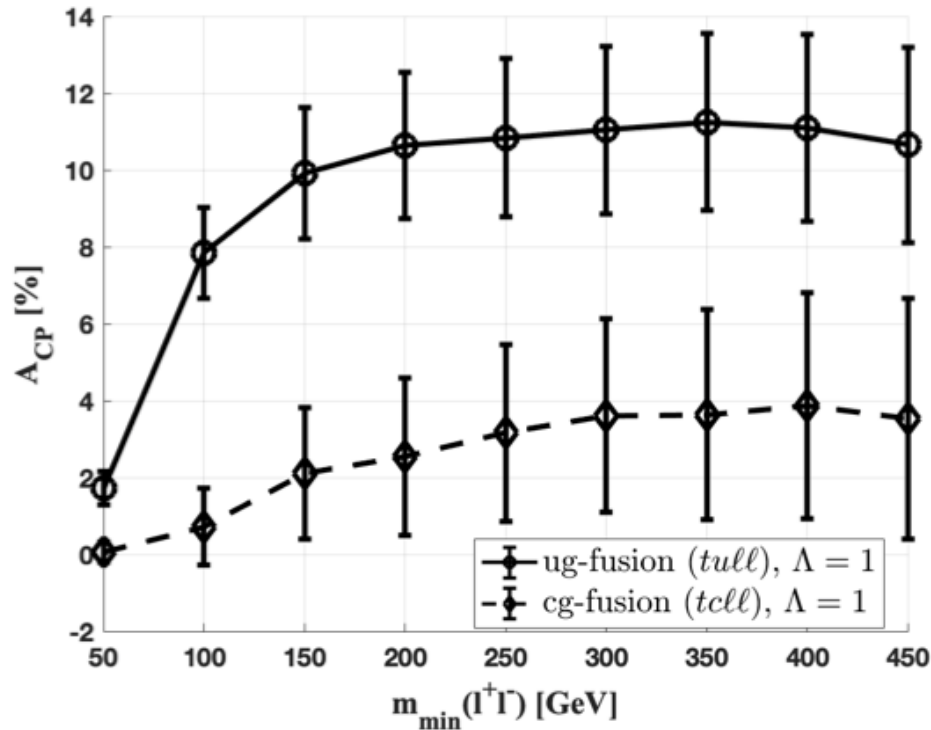


FIG. 2: A_{CP} as a function of $m_{\min}(\ell^+\ell^-)$, for $\Lambda = 1$ TeV, $\text{Im}(f_S f_T^*) = 0.25$ and including the SM background. The dependence of the asymmetry on Λ is given in Appendix B. The error bars represent the expected statistical uncertainty with an integrated luminosity of 1000(3000) fb^{-1} for the ug-fusion(cg-fusion) case.

Axis dependent asymmetries

$$\mathcal{O}_{CP}^i = p_a^i \cdot (\vec{p}_b \times \vec{p}_c)^i$$



$$A_{CP}^{x,y,z} = \frac{1}{2} (A_T^{x,y,z} - \bar{A}_T^{x,y,z})$$

A measurement of the axis-dependent asymmetries can be used to distinguish between the different types of underlying NP: in our test case, between the $t\ell\ell$ and the $t\bar{c}\ell\ell$ CP-violating dynamics ...

TABLE II: The expected T_N -odd and CP asymmetries A_T , \bar{A}_T , A_{CP} and the corresponding axis-dependent asymmetries A_T^i , \bar{A}_T^i , A_{CP}^i ($i = x, y, z$), for the tri-lepton events $pp \rightarrow \ell'^{\pm}\ell^+\ell^- + X$ at the LHC with $m_{min}(\ell\ell) = 400$ GeV. Results are given for both the ug -fusion and cg -fusion production channels (and the CC ones). Numbers are presented for $\Lambda = 1$ TeV, $\text{Im}(f_S f_T^*) = 0.25$ and the dominant SM background from $pp \rightarrow ZW^{\pm} + X$ is included. The cases where an asymmetry is $\lesssim 0.5\%$ is marked by an X.

	A_{CP}	A_{CP}^x	A_{CP}^y	A_{CP}^z
ug -fusion:	11.1%	8.1%,	8.1%	X
cg -fusion:	3.9%	X	X	5.6%

	A_T	A_T^x	A_T^y	A_T^z
ug -fusion:	16.4%	11.3%,	10.7%	3.8%
cg -fusion:	3.1%	5.0	X	X

	\bar{A}_T	\bar{A}_T^x	\bar{A}_T^y	\bar{A}_T^z
ug -fusion:	-5.8%	-5.0%	-5.6%	3.1%
cg -fusion:	-4.7%	-6.3%	X	X

EFT-validity

Two "measures" to consider:

$$\sigma^{NP}(g, \Lambda, m_{\ell\ell}) = \frac{g^2}{\Lambda^2} \cdot \sigma^{SM \times NP}(m_{\ell\ell}) + \frac{g^4}{\Lambda^4} \cdot \sigma^{NP \times NP}(m_{\ell\ell})$$

$$\mathcal{R}_\Lambda \equiv \frac{\hat{s}}{\Lambda^2}$$

Addresses the validity of the specific calculation within the EFT framework - depends on the details of the underlying heavy physics and the process at hand

$$\mathcal{R}_{\Lambda/g} \equiv \frac{\hat{s}}{\Lambda^2/g^2}$$

The EFT expansion param - the expansion of the effective Lagrangian at leading order in g/Λ

EFT-validity

Two "measures" to consider:

$$\sigma^{NP}(g, \Lambda, m_{\ell\ell}) = \frac{g^2}{\Lambda^2} \cdot \sigma^{SM \times NP}(m_{\ell\ell}) + \frac{g^4}{\Lambda^4} \cdot \sigma^{NP \times NP}(m_{\ell\ell})$$

$$\mathcal{R}_\Lambda \equiv \frac{\hat{s}}{\Lambda^2}$$

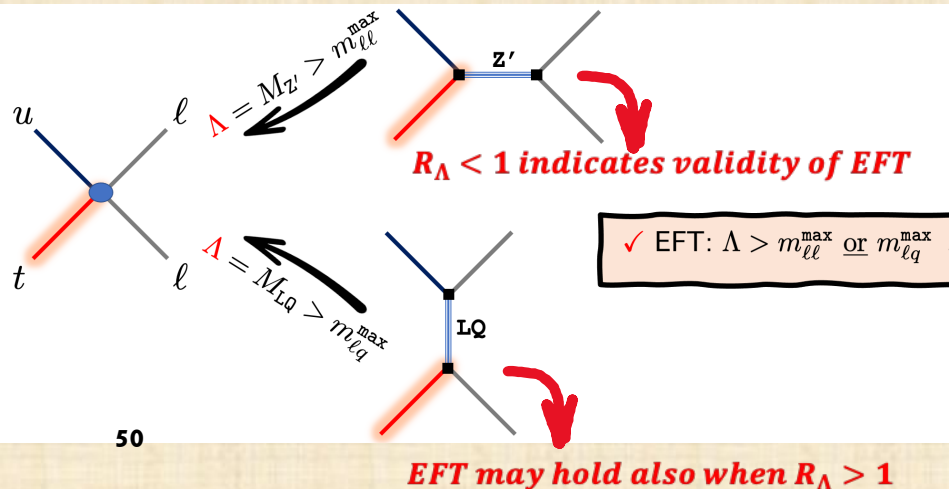
Addresses the validity of the specific calculation within the EFT framework - depends on the details of the underlying heavy physics and the process at hand

$$\mathcal{R}_{\Lambda/g} \equiv \frac{\hat{s}}{\Lambda^2/g^2}$$

The EFT expansion param - the expansion of the effective Lagrangian at leading order in g/Λ

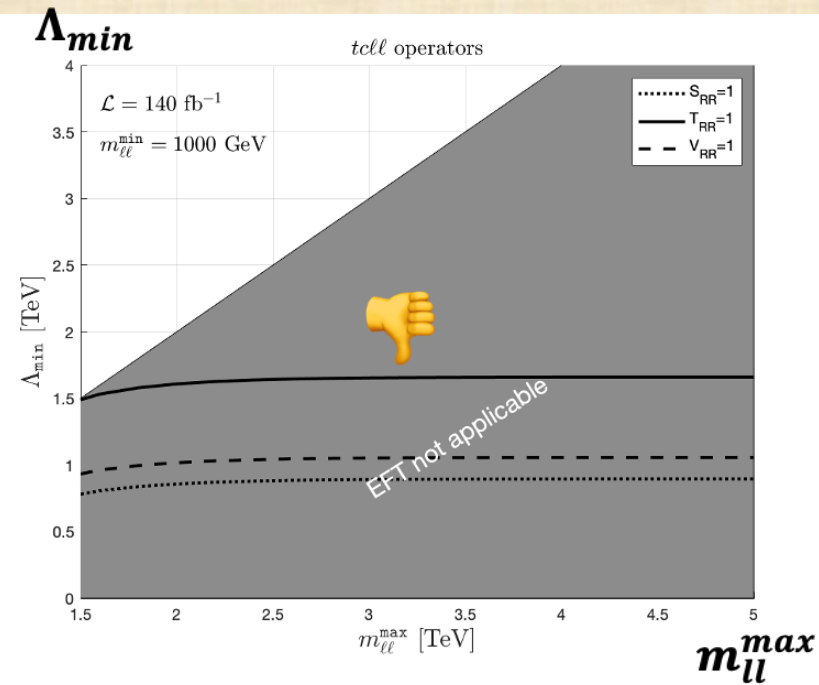
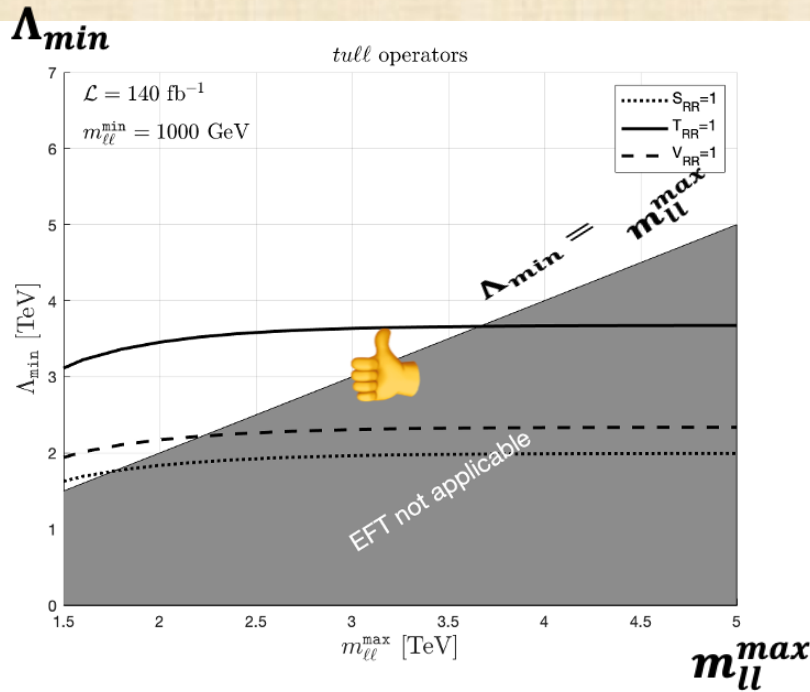
SMxNP interference term $\propto O(R_{\Lambda/g})$
NPxNP term $\propto O(R_{\Lambda/g}^2)$

$R_{\Lambda/g} < 1$ naively indicate the **regime of validity** of the EFT prescription & the potential effects from higher dim opts can be assessed from $R_{\Lambda/g}$



EFT-validity

Consider bounds (Λ_{min}) obtained on the scale Λ of an s -channel underlying NP $pp \rightarrow NP \rightarrow l^+ l^-$; $\hat{s} = m_{ll}$



CPV multi-leptons events: Constructing CP-asym from TP's

- Divide into 2 "hemispheres" in \mathcal{O}_{CP} space and define the **P-violating & T_N -odd** observables (odd under $\dagger \rightarrow -\dagger$):

$$ab \rightarrow \ell'^- \ell^+ \ell^- \quad \text{and} \quad \bar{a}\bar{b} \rightarrow \ell'^+ \ell^- \ell^+$$

$$\mathcal{M}_{ab \rightarrow \ell'^- \ell^+ \ell^-} = M_1 e^{i(\phi_1 + \delta_1)} + M_2 e^{i(\phi_2 + \delta_2)}$$

$$A_T \propto \sin(\Delta\delta + \Delta\phi)$$

$$\bar{A}_T \propto \sin(\Delta\delta - \Delta\phi)$$

$$\Delta\phi = \phi_1 - \phi_2, \quad \Delta\delta = \delta_1 - \delta_2$$

$$A_T \equiv \frac{N(\mathcal{O}_{\text{CP}} > 0) - N(\mathcal{O}_{\text{CP}} < 0)}{N(\mathcal{O}_{\text{CP}} > 0) + N(\mathcal{O}_{\text{CP}} < 0)},$$

$$\bar{A}_T \equiv \frac{N(-\overline{\mathcal{O}_{\text{CP}}} > 0) - N(-\overline{\mathcal{O}_{\text{CP}}} < 0)}{N(-\overline{\mathcal{O}_{\text{CP}}} > 0) + N(-\overline{\mathcal{O}_{\text{CP}}} < 0)}$$

A measurement of $A_T \neq 0$ and/or $\bar{A}_T \neq 0$ may indicate the presence of CP-violation (CP-odd phase), but may also be a signal of some strong or generic CP-even phase, e.g., from final state interaction (FSI), even if the underlying dynamics that drives the processes under consideration is CP-conserving.

- Isolating the pure CPV effect:

$$A_{\text{CP}} = \frac{1}{2} (A_T - \bar{A}_T)$$

CPV \Rightarrow multi-leptons events

- The resulting asymmetries:

$$\Delta\phi = \phi_1 - \phi_2, \quad \Delta\delta = \delta_1 - \delta_2$$

$$A_T = \mathcal{I}_{ab} \sin(\Delta\phi + \Delta\delta)$$

$$\bar{A}_T = \mathcal{I}_{\bar{a}\bar{b}} \sin(-\Delta\phi + \Delta\delta)$$

$$A_{CP} = \frac{1}{2} (A_T - \bar{A}_T)$$

"conventional" CPV term

initial state not self-conjugate

$$A_{CP} = \frac{\mathcal{I}_{ab} + \mathcal{I}_{\bar{a}\bar{b}}}{2} \cos \Delta\delta \sin \Delta\phi + \frac{\mathcal{I}_{ab} - \mathcal{I}_{\bar{a}\bar{b}}}{2} \sin \Delta\delta \cos \Delta\phi$$

$$V \propto \text{Im} (M_1 M_2^\dagger)$$

$$\mathcal{I}_{ab(\bar{a}\bar{b})} = \frac{\int_R d\Phi f_a(\bar{a}) f_b(\bar{b}) V \cdot \text{sign}(\mathcal{O}_{CP})}{\int_R d\Phi f_a(\bar{a}) f_b(\bar{b}) U}$$

PDF's

CPV \rightarrow multi-leptons events

- The resulting asymmetries:

$$A_T = \mathcal{I}_{ab} \sin(\Delta\phi + \Delta\delta)$$

$$\bar{A}_T = \mathcal{I}_{\bar{a}\bar{b}} \sin(-\Delta\phi + \Delta\delta)$$

$$\Delta\phi = \phi_1 - \phi_2, \Delta\delta = \delta_1 - \delta_2$$

$$A_{CP} = \frac{1}{2} (A_T - \bar{A}_T)$$

"conventional" CPV term

initial state not self-conjugate

$$A_{CP} = \frac{\mathcal{I}_{ab} + \mathcal{I}_{\bar{a}\bar{b}}}{2} \cos \Delta\delta \sin \Delta\phi + \frac{\mathcal{I}_{ab} - \mathcal{I}_{\bar{a}\bar{b}}}{2} \sin \Delta\delta \cos \Delta\phi$$

a modification to the classic formula for CP-violation in scattering and decay processes
takes into account the effect of an asymmetric initial state on the measurement of CP-violation

$$V \propto \text{Im} (M_1 M_2^\dagger)$$

$$\mathcal{I}_{ab(\bar{a}\bar{b})} = \frac{\int_R d\Phi f_{a(\bar{a})} f_{b(\bar{b})} V \cdot \text{sign}(\mathcal{O}_{CP})}{\int_R d\Phi f_{a(\bar{a})} f_{b(\bar{b})} U}$$

PDF's

Recap:

$$A_T = \mathcal{I}_{ab} \sin(\Delta\phi + \Delta\delta)$$

$$\bar{A}_T = \mathcal{I}_{\bar{a}\bar{b}} \sin(-\Delta\phi + \Delta\delta)$$

$$A_{CP} = \frac{\mathcal{I}_{ab} + \mathcal{I}_{\bar{a}\bar{b}}}{2} \cos \Delta\delta \sin \Delta\phi + \frac{\mathcal{I}_{ab} - \mathcal{I}_{\bar{a}\bar{b}}}{2} \sin \Delta\delta \cos \Delta\phi$$

- $A_T \neq 0$ and/or $\bar{A}_T \neq 0$ can be observed even in the absence of CP-violation (i.e., $\Delta\phi = 0$) due to the presence of CP-even phases $\Delta\delta \neq 0$...
- $|A_T| \neq |\bar{A}_T|$ is possible at the LHC even with $\Delta\delta = 0$ (if different PDF's are different: $f_a, f_b \neq f_{\bar{a}}, f_{\bar{b}}$) due to CP-asymmetric nature of the initial state at the LHC ...
- $A_{CP} \propto \sin \Delta\phi$ (maximal when $\Delta\delta \rightarrow 0$) if same PDF's of incoming particles ($f_a f_b = f_{\bar{a}} f_{\bar{b}}$)
- $A_{CP} \propto \sin \Delta\phi$ when $\Delta\delta \rightarrow 0$, even when $f_a f_b \neq f_{\bar{a}} f_{\bar{b}}$
- Thus, when $\Delta\delta \ll \Delta\phi$, A_{CP} is essentially probing the underlying CP-violating dynamics !

the case, in general, for the scattering processes at the LHC if there are no resonances involved, since then CP-even phases can only come from FSI, which occur at higher loop orders, whereas A_{CP} probes tree-level CPV effects !