

# Physics Potential, Accelerator Options, and Experimental Challenges of a TeV-Scale Muon-Ion Collider

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O. Miguel Colin, M. Munyi, Y. Wang, D. Wood and X. Zuo



RICE



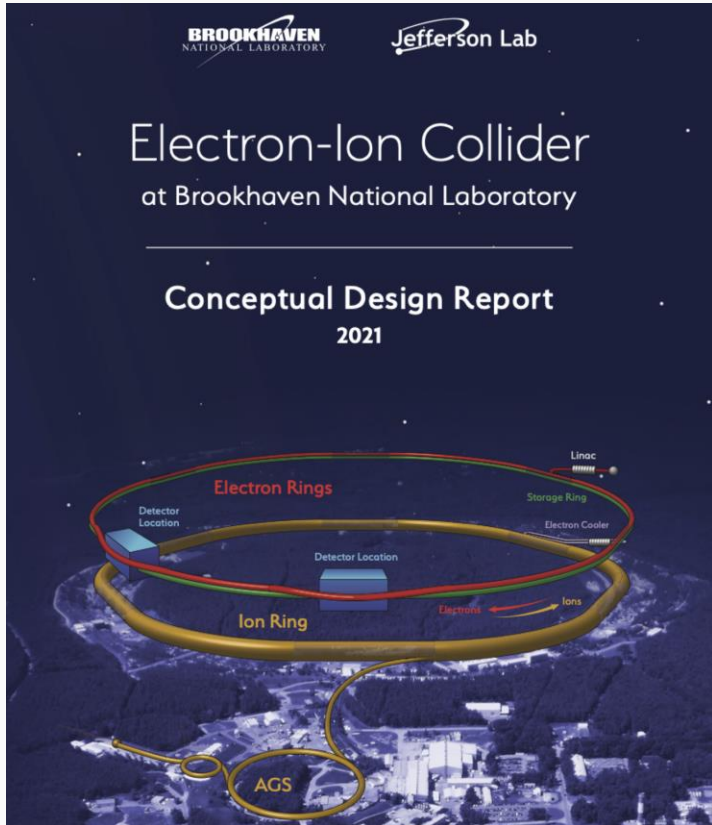
- The Muon-Ion Collider concept
- Deep Inelastic Scattering physics potential
- SM (and BSM) physics potential
- Interesting experimental challenges at a MuIC
- Summary

*Focus of this talk is on the creation and application of such a facility, not on the feasibility or details of a muon accelerator and collider design*

A first dedicated workshop on the concept held last December:

- <https://muic2023.rice.edu/>

# The DIS Frontier: The Electron-Ion Collider (EIC) at BNL



International facility already CD1 approved by the U.S. DOE  
**Nuclear Physics program.**

- Culmination of a 2 decade process
- Science to begin in the 2030s

[EIC Conceptual Design Report](#) recently released.

Salient points:

- Electron beam energy up to 18 GeV
- Hadron beam energy up to 275 GeV
- $\sqrt{s} = 20 -- 140$  GeV
- Luminosity  $10^{33} -- 10^{34}$  Hz/cm<sup>2</sup>
- Polarized electron, proton and ion beams (any species)

But what comes  
after 🤔

Physics goals:

- ep and eN deep inelastic scattering
- Nucleon spin structure
- Gluon saturation scale ( $Q_s$ )



- From the U.S. HEPAP P5 Committee 2023 report:

Exploring the Quantum Universe

## 2.3 The Path to a 10 TeV pCM

Realization of a future collider will require resources at a global scale and will be built through a world-wide collaborative effort where decisions will be taken collectively from the outset by the partners. This differs from current and past international projects in particle physics, where individual laboratories started projects that were later joined by other laboratories. The proposed program aligns with **the long-term ambition of hosting a major international collider facility in the US, leading the global effort** to understand the fundamental nature of the universe.

...

In particular, **a muon collider presents an attractive option** both for technological innovation and for bringing energy frontier colliders back to the US. The footprint of **a 10 TeV pCM muon collider is almost exactly the size of the Fermilab campus**. A muon collider would rely on a powerful multi-megawatt proton driver delivering very intense and short beam pulses to a target, resulting in the production of pions, which in turn decay into muons. This cloud of muons needs to be captured and cooled before the bulk of the muons have decayed. Once cooled into a beam, fast acceleration is required to further suppress decay losses.

...

Although **we do not know if a muon collider is ultimately feasible**, the road toward it leads from current Fermilab strengths and capabilities to **a series of proton beam improvements and neutrino beam facilities**, each producing world-class science while performing **critical R&D towards a muon collider**. At the end of the path is an unparalleled global facility on US soil. **This is our Muon Shot.**

Perhaps a MuIC could be a first science demonstrator

# Muon-Ion Collider Concept and Motivation



- The concept of a muon-proton collider has been discussed in the literature since ~25 years ago
- Our recent focused proposal offers an **upgrade successor to the EIC**
  - $E_{lep} \rightarrow 100X$  higher,  $\sqrt{s} \rightarrow 10X$  higher
- Leverage the Energy Frontier community interest for a muon collider and its associated technology, and apply toward a (first?) science demonstrator: **a muon-hadron collider**
  - Planning should start now, given the ~2 decade path to project approval...
- Basis of proposal for a MuIC at BNL:  
[Acosta and Li, NIM A1027 \(2022\)](#)
- MuIC science case further explored in Snowmass contribution:  
[Acosta et al., 2023 JINST 18 P09025](#)
  - + some further works in progress by students

# A Muon-Ion Collider – Who Ordered That?



Probe a **new energy scale** and nucleon momentum fraction in Deep Inelastic Scattering using a relatively compact machine (add new PDF data!)

- $\sqrt{s} \sim 1 \text{ TeV}$
- $Q^2$  up to  $10^6 \text{ GeV}^2$
- $x$  as low as  $10^{-6}$



**Well beyond the EIC**

i.e. extension of the EIC program and equivalent to the LHeC program, but with a muon accelerator

**Provides a science case for a TeV muon storage ring demonstrator** toward a multi-TeV  $\mu^+\mu^-$  collider:

- Precision PDFs in new regimes (incl. spin at BNL)
- QCD, including at extreme parton density
- Precision EWK and QCD measurements
- Higgs and other SM particle production
- BSM / LFUV sensitivity with an initial muon



**Luminosity depending**

Facilitate the **collaboration of the nuclear and particle physics communities** around an innovative and forward-looking machine

Broad science program helps share costs, and re-use helps economize

**Re-use existing facilities** (e.g. Upgrade the EIC at BNL, or FNAL? or CERN?)

# A Muon-Ion Collider at BNL

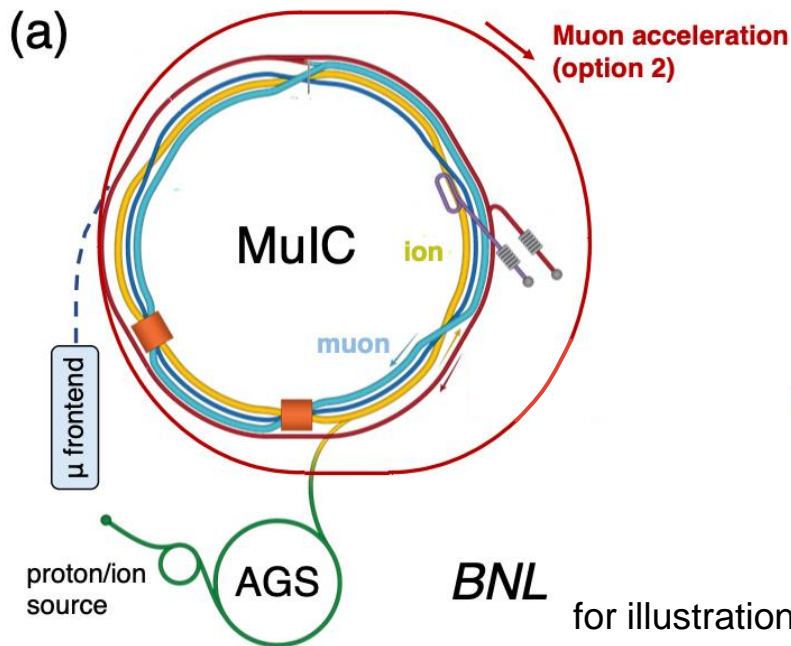


Acosta and Li, NIM A 1027 (2022) 166334

→ Replace e with  $\mu$  beam at EIC  
 [10 GeV → 1000 GeV]

Bending radius of RHIC tunnel:  $r = 290\text{m}$

Achievable muon beam energy:  $0.3Br$



Parameter	1 (aggressive)	2 (realistic)	$\beta$ (conservative)
Muon energy (TeV)	1.39	0.96	0.73
Muon bending magnets (T)	16 (FCC)	11 (HL-LHC)	8.4 (LHC)
Muon bending radius (m)		290	
Proton (Au) energy (TeV)		0.275 (0.11/nucleon)	
CoM energy (TeV)	1.24 (0.78)	1.03 (0.65)	0.9 (0.57)

$\sqrt{s} = 1 \text{ TeV}!$

7-8X increase over EIC energy

# A Muon-Ion Collider at BNL – Parameters



Acosta et al., JINST 18, P09025 (2023)

Parameter	BNL options → MuIC			
$\sqrt{s_{\mu p}}$ (TeV)	0.33	0.74	1.0	→ 2.0
$L_{\mu p}$ ( $10^{33}\text{cm}^{-2}\text{s}^{-1}$ )	0.07	2.1	4.7	
Int. Lumi. ( $\text{fb}^{-1}$ ) per 10 yrs	6	178	400	
	Muon			Proton
Beam energy (TeV)	0.1	0.5	0.96	0.275
$N_b$ ( $10^{11}$ )	40	20	20	3
$f_{\text{rep}}^{\mu}$ (Hz)	15	15	15	
Cycles per $\mu$ bunch, $N_{\text{cycle}}^{\mu}$	1134	1719	3300	
$\varepsilon_{x,y}^*$ ( $\mu\text{m}$ )	200	25	25	0.3
$\beta_{x,y}^*$ @IP (cm)	1.7	1	0.75	5
Trans. beam size, $\sigma_{x,y}$ ( $\mu\text{m}$ )	48	7.6	4.7	7.1

Staging: RLAs + RCS1 + RCS2

Taken from MuC parameters and BNL hadron ring

←  $\sqrt{s}$

← Luminosity likely overestimated 10–100X due to beam-beam effects (needs dedicated optimization)

← Beam energies

Staging options reduce number of acceleration stages required for muon beam

Muon Collider parameters + BNL/EIC and LHC proton beam parameters

→ Symmetric 1 TeV collider?



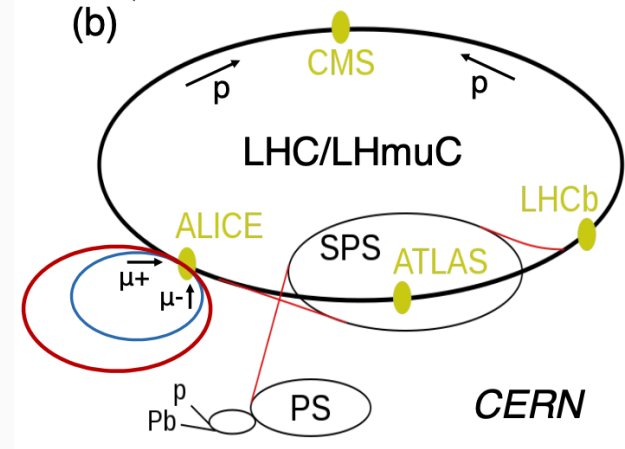
# A Muon-Ion Collider at CERN, "LHmuC"



Parameter	LHmuC	
$\sqrt{s_{\mu p}}$ (TeV)	6.5	
$L_{\mu p}$ ( $10^{33}\text{cm}^{-2}\text{s}^{-1}$ )	2.8	
Int. Lumi. ( $\text{fb}^{-1}$ ) per 10 yrs	237	
	Muon	Proton
Beam energy (TeV)	1.5	7
$N_b$ ( $10^{11}$ )	20	2.2
$f_{\text{rep}}^{\mu}$ (Hz)	12	
Cycles per $\mu$ bunch, $N_{\text{cycle}}^{\mu}$	3300	
$\epsilon_{x,y}^*$ ( $\mu\text{m}$ )	25	2.5
$\beta_{x,y}^*$ @IP (cm)	0.5	15
Trans. beam size, $\sigma_{x,y}$ ( $\mu\text{m}$ )	3	7.1

← Likely unrealistic

- Variation of the LHeC concept with a TeV muon beam replacing the 50 GeV electron beam
- Could accommodate a  $\mu p$  collider option if an initial **1.5+1.5 TeV  $\mu^+\mu^-$  collider** is sited at CERN (Intl. Muon Coll. Collab. design)

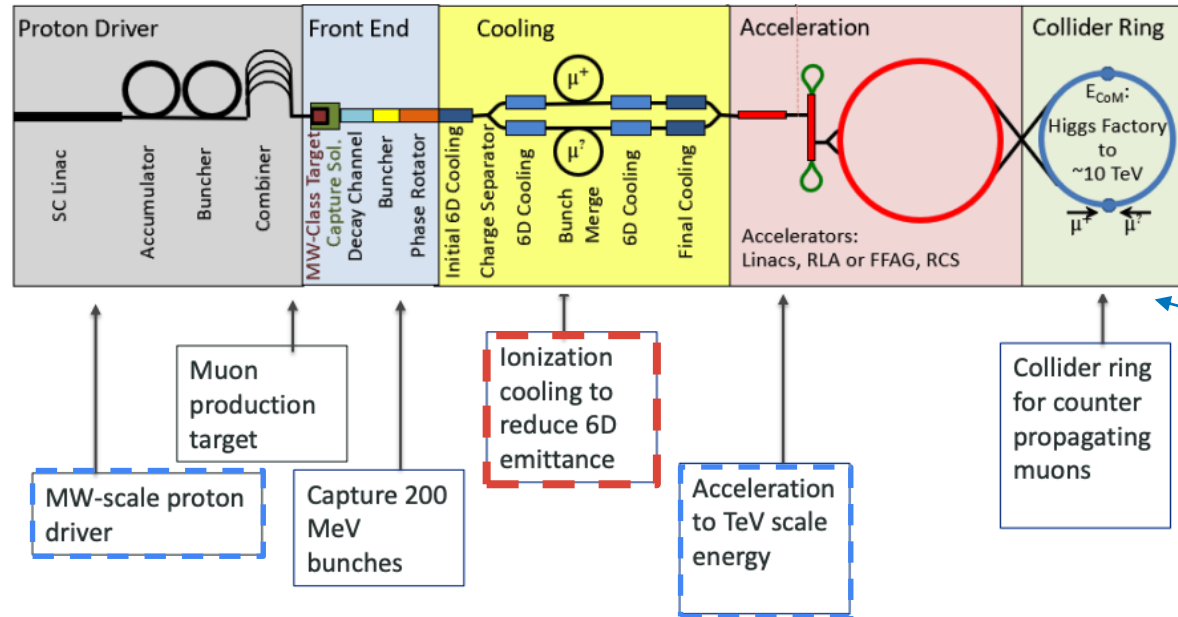


- Equivalent  $\sqrt{s}$  would actually exceed that of a 3 TeV  $\mu^+\mu^-$  collider

# A Muon Acceleration & Collider Complex

- From Diktys Stratakis, [link](#)

Recirculating Linacs,  
Rapid Cycling Synchrotrons  
(or FFAGs)



$\mu^+$  accelerators could also accelerate protons if no other existing hadron beam infrastructure



Extensive. In principle no show stoppers, but requires R&D and investment.  
Proton driver also synergistic with high intensity neutrino programs

# Alternative Cooling Idea for $\mu^+$ Only

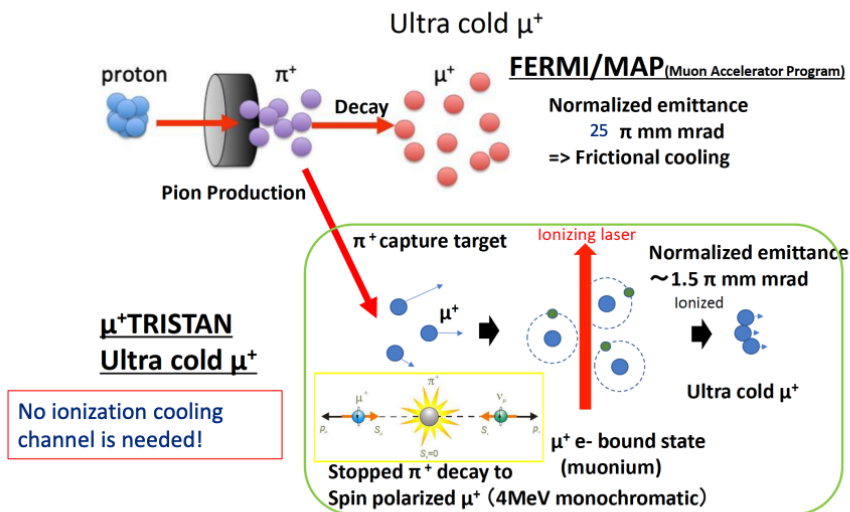


From Katsuya Yonehara, [link](#)

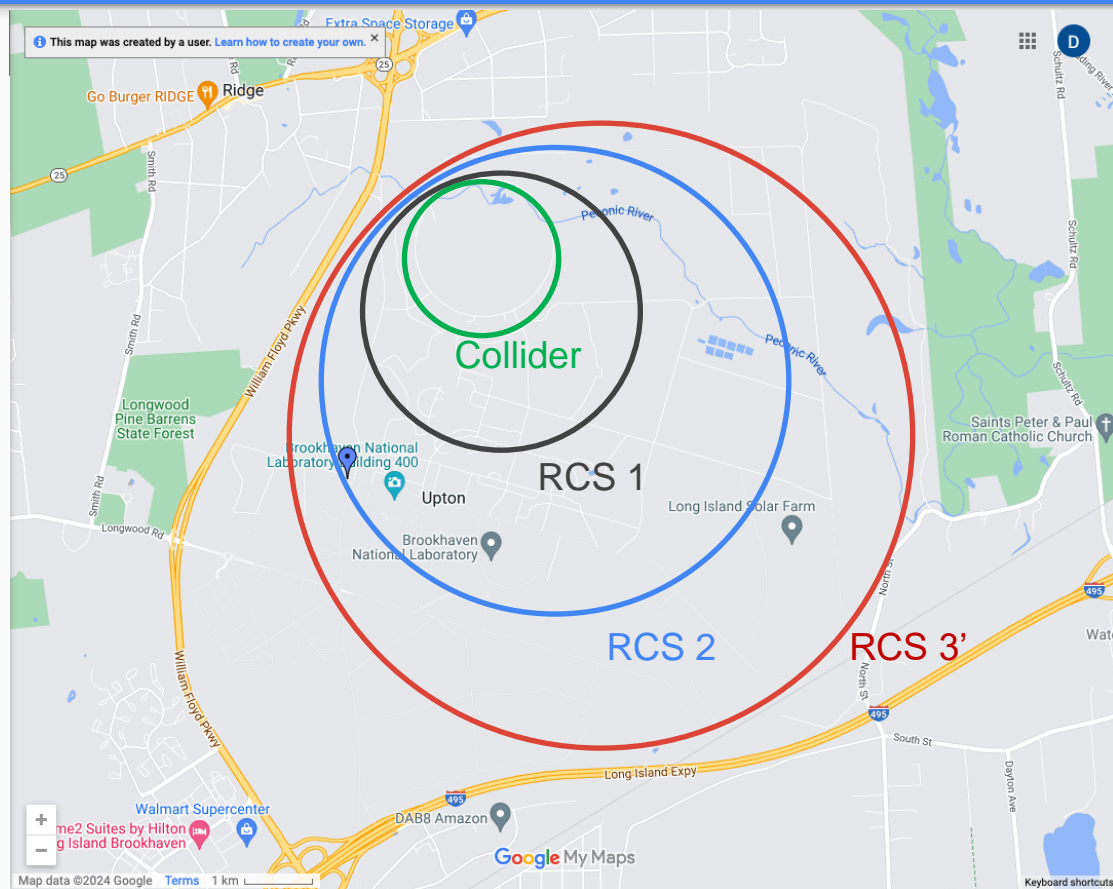
See: <https://cerncourier.com/a/muons-cooled-and-accelerated-in-japan/>

- Capture  $\mu^+$  with electrons in aerogel (so ultracold), and ionize with laser
- **No ionization cooling needed!**
- Development at KEK J-PARC for  $g-2$ /EDM experiment
  - [P.Bakule et al., arXiv:1306.3810](#)
  - [J.Beare et al, arXiv:2006.01947](#)
- Could create  $2 \times 10^{10}$   $\mu^+$ 
  - 100X less than initial Acosta/Wei numbers, but in direction of lowering neutrino bkg but still enabling novel DIS measurements
- Could also achieve up to 50% polarization!
- **Very small emittance,  $1.5 \mu\text{m}$**

## Alternative design: Cold muon beam from surface muon



# A BNL Site Filler – Max Size of Accelerating Rings



- Maximum accelerator size on BNL site:
  - $D \approx 4.45 \text{ km}$
  - Circumference: 14 km
- Following FNAL MuC plans, RCS 1 achieves  $\sqrt{s} = 0.7 \text{ TeV}$  and RCS 2  $\sqrt{s} > 1 \text{ TeV}$ 
  - Can fit RCS 2 at 10.5 km
- In principle could fit up to a RCS 3' to go to  $E_{\mu} \sim 3 \text{ TeV}$

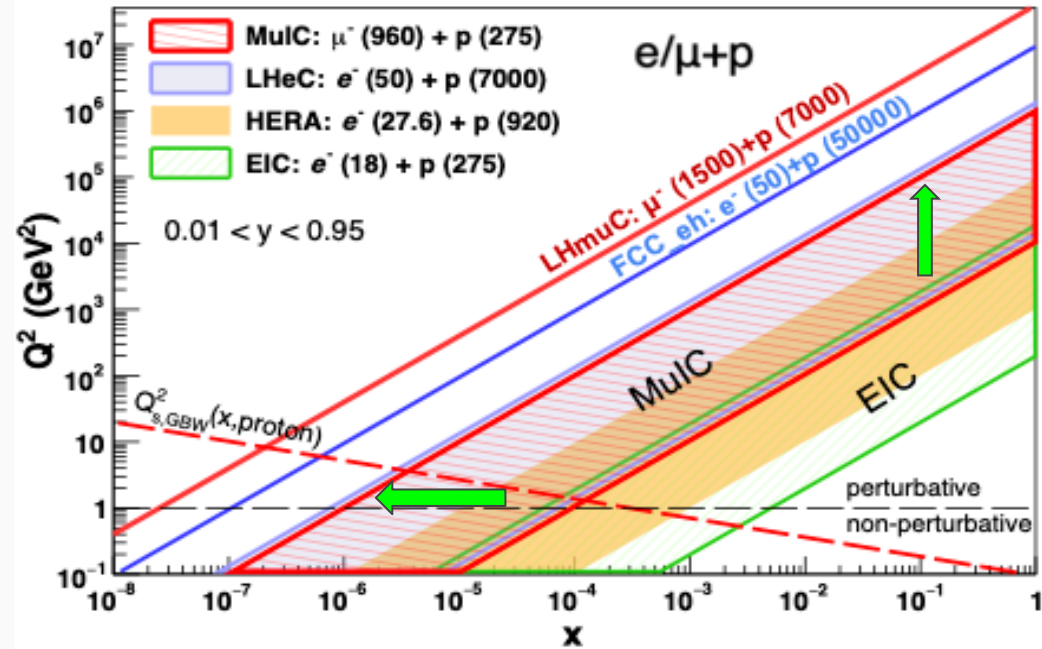
n.b. The accelerating rings are larger than the collider ring because of the need of rapid cycling magnets

# Physics Opportunities

# DIS Reach in $x$ and $Q^2$ for $\ell p$ Collisions



- MuIC expands DIS reach at high  $Q^2$  and low  $x$  by 1–3 orders of magnitude **beyond HERA and the EIC**
- Coverage of **MuIC at BNL** is nearly **identical** with that of the proposed **Large Hadron electron Collider** [1] (LHeC) at CERN with 50 GeV  $e^-$  beam
- Coverage of a **mu-LHC collider at CERN (LHmuC)** would **significantly exceed** even that of the **FCC-eh** option of a 50 TeV proton beam with 50 GeV  $e^-$  beam



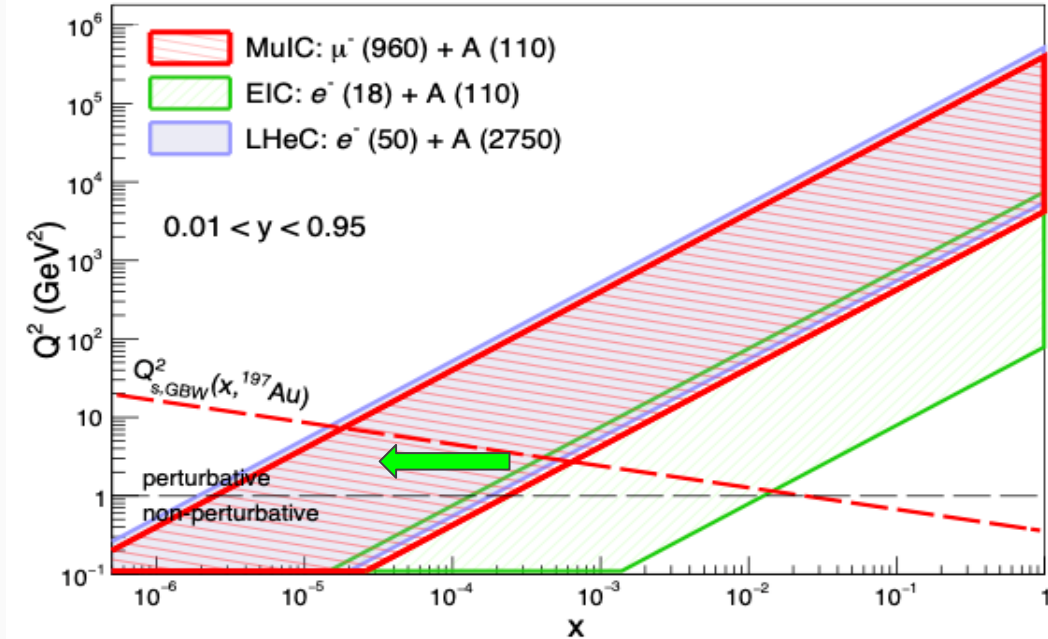
[1] LHeC: [2021 J. Phys. G: Nucl. Part. Phys. 48 110501](#)

[2] GBW model: [Phys. Rev. D 59, 014017 \(1998\)](#)

# DIS Reach in $x$ and $Q^2$ for $\ell A$ Collisions



- Can explore well the predicted **gluon saturation regime** in ions at low  $x$  in the GBW model [2]
- A MuIC at BNL also can scan a wide range of **ion species**, and with **beam polarization**

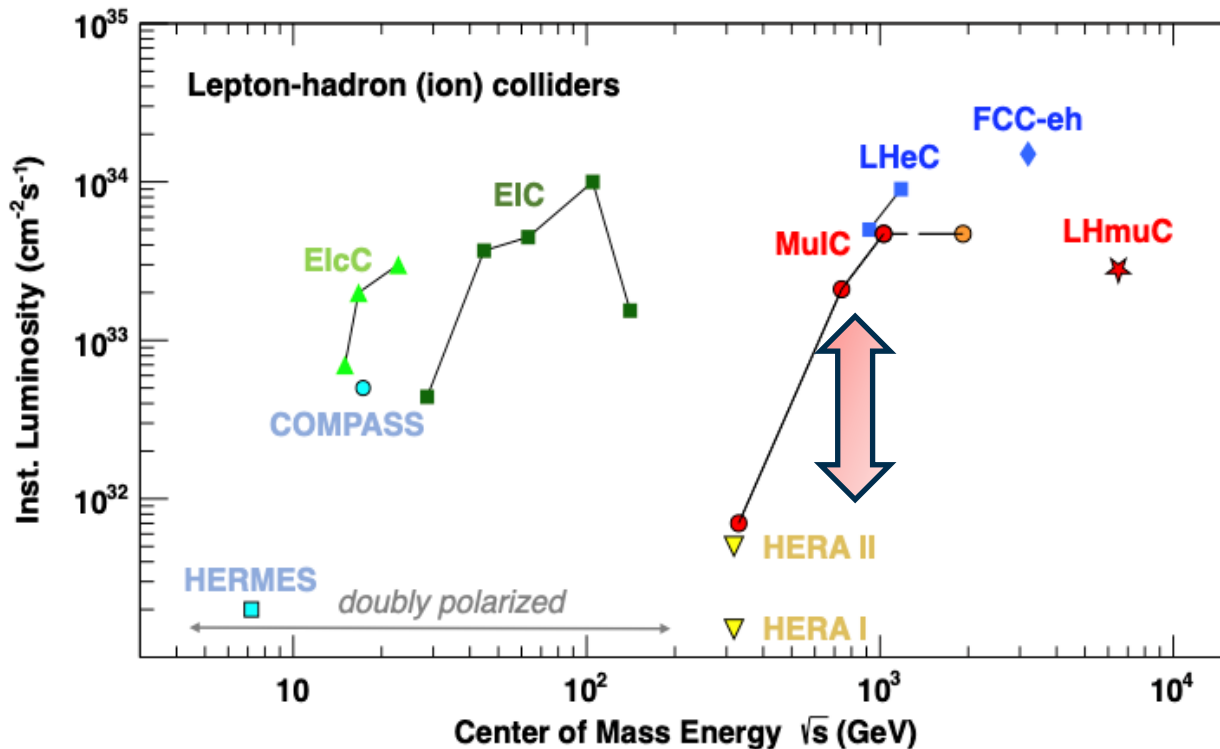


Saturation scale:

$$Q_s^2(A) = A^{1/3} Q_s^2(p)$$

[2] GBW model: [Phys. Rev. D 59, 014017 \(1998\)](#)

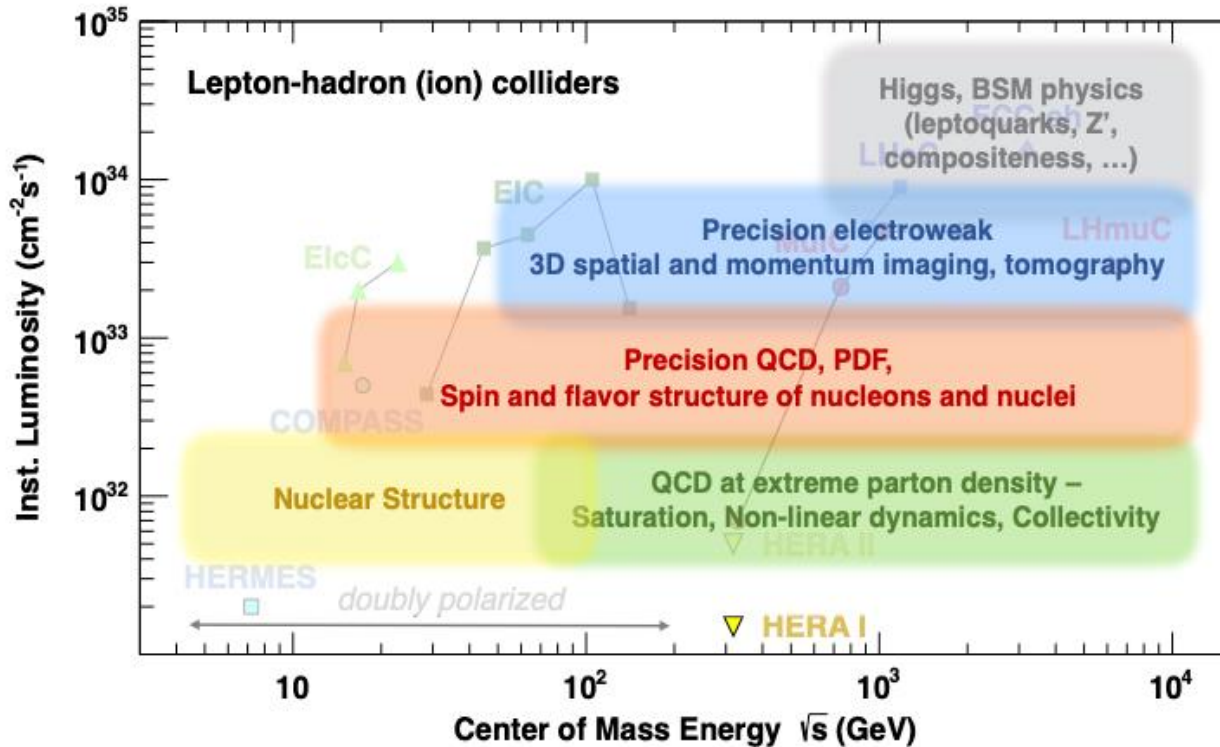
# DIS Evolution – Past and Proposed Machines



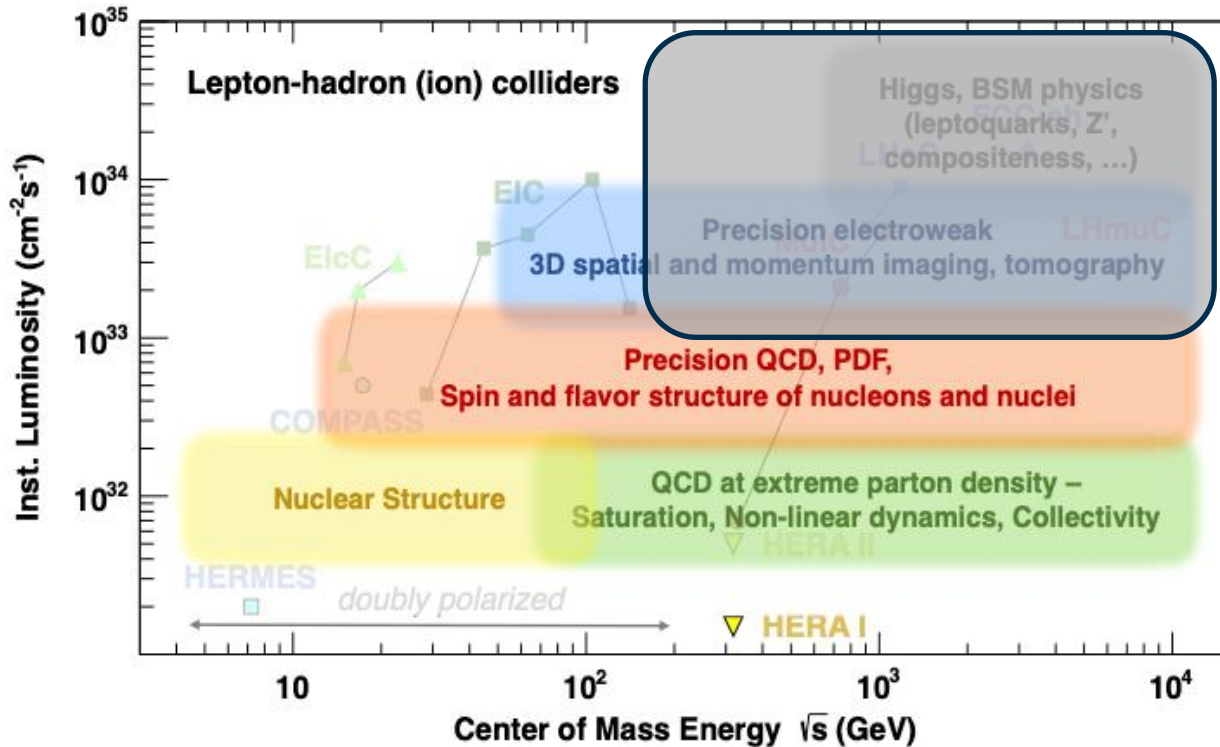
From Rice workshop discussion, beam-beam effects limit luminosity



# DIS Evolution and Physics Landscape



# DIS Evolution and Physics Landscape

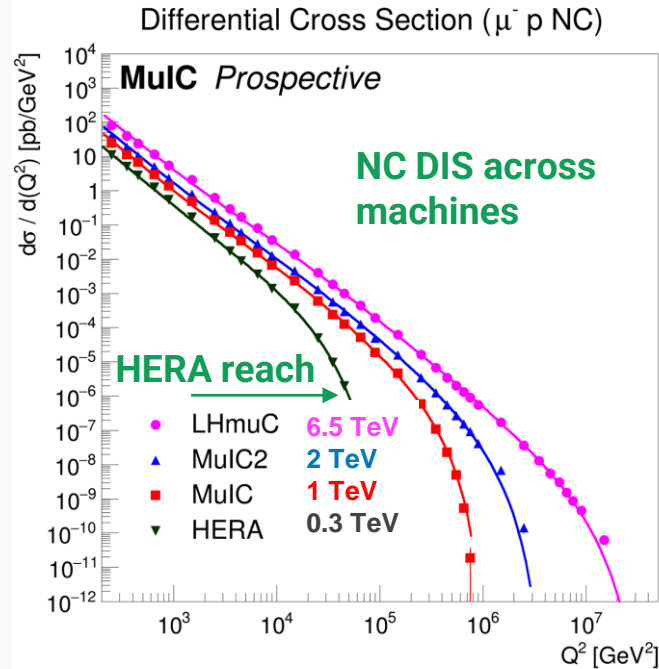


Precision electroweak, Higgs, and BSM physics would be limited if luminosity  $< 10^{32}$

# DIS Differential Cross Sections in $Q^2$ for Different Machines

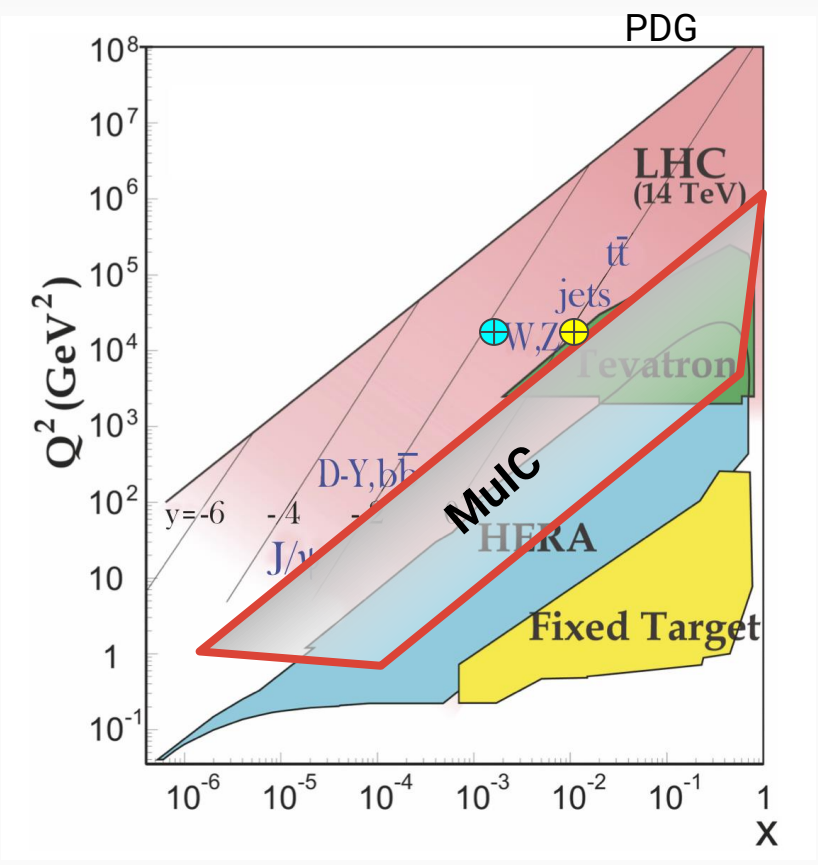


Computed with Pythia8  
and NNPDF2.3 PDF set,  
 $0.1 < y < 0.9$



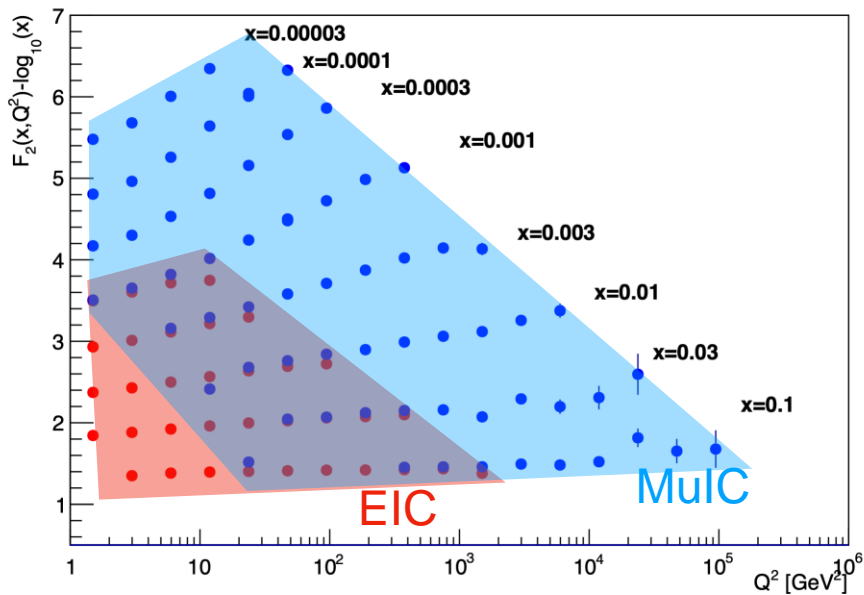
- MuIC can probe well beyond HERA and the electroweak scale
- Highest  $Q^2$  reach will require the largest luminosity ( $10^{33}$ – $10^{34}$  Hz/cm<sup>2</sup>)
  - But, measurements at lower  $Q^2$  and  $x$  can benefit from luminosity orders of magnitude smaller: ~HERA luminosity for the electroweak scale.

# Complementarity to (and input for) Hadron Colliders

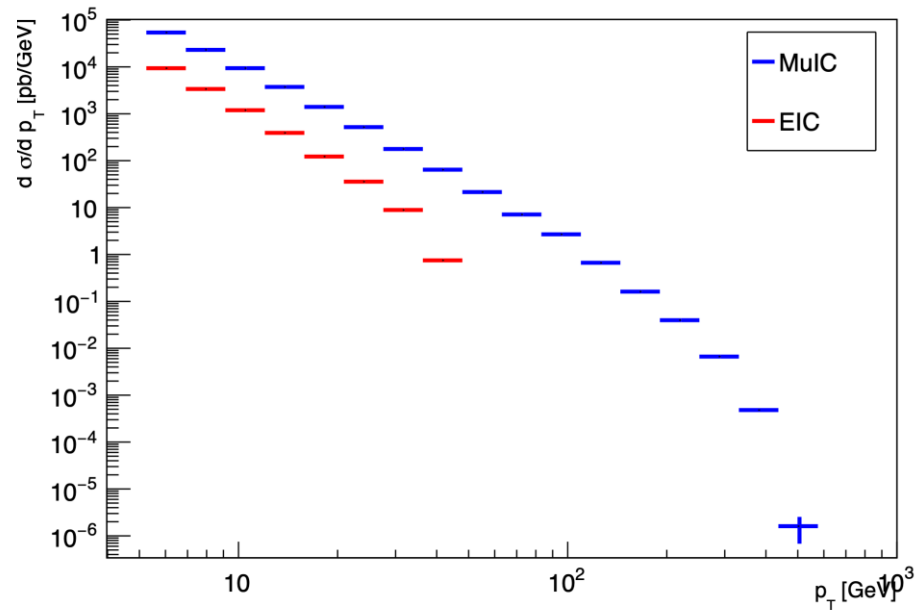


- DIS PDF measurements with an electroweak probe can more **cleanly decouple QCD and quark flavor** over hadron collider measurements
- The MuIC (or LHeC) can probe the parton densities directly at, or near, the scale for **Higgs production** at the **(HL)LHC**, and for a future **100 TeV FCCh**
  - PDF uncertainties are generally a limiting factor for calculation precision
  - **Reducing uncertainties** on pp cross sections **to ~1%** is critical for Higgs coupling tests
- **Useful (necessary?!)** input for a future **FCCh** program
  - **As HERA was for the LHC program**

# MuIC Potential for Structure Function & QCD Measurements



$F_2$  Structure function projection of EIC vs MuIC



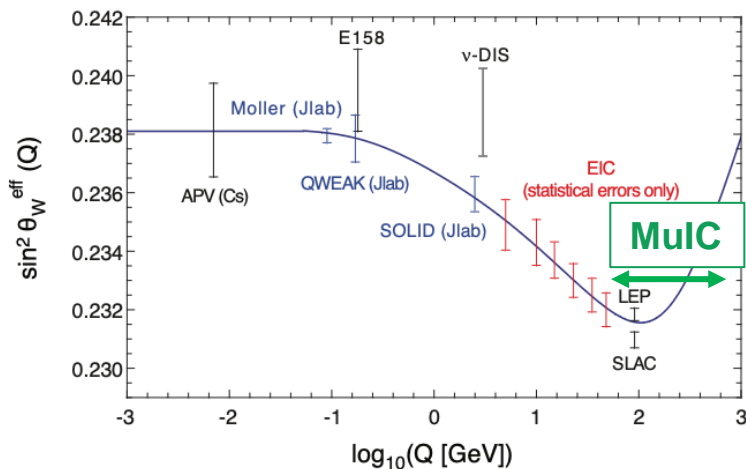
Single jet  $P_T$  spectra projection of EIC vs MuIC

Pseudo-data representing one year (at  $5 \times 10^{33}$  Hz/cm<sup>2</sup>) of running,  $\sim 40$  fb<sup>-1</sup>

# $\sin^2 \theta_W^{\text{eff}}$ Measurements



- Probe the effective **weak mixing angle** (and its running) over a wide scale range through combined fits of DIS data with PDFs and couplings
- **MuIC would extend the EIC scale coverage**, and is equivalent to that the LHeC would achieve
  - Beam polarization, and ability to change beam from  $^1\text{H} \rightarrow ^2\text{H}$  at BNL, will further help disentangle couplings from PDFs

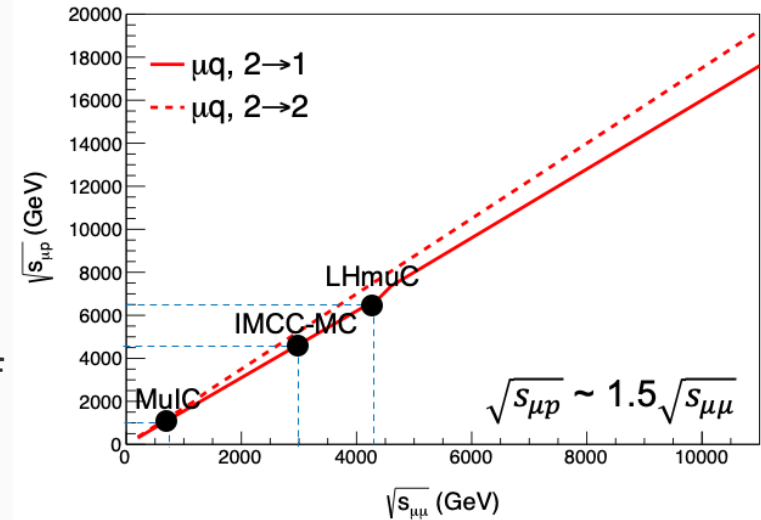


[EIC arXiv:1212.1701](https://arxiv.org/abs/1212.1701)

# Equivalent Reach for Particle Production, $\mu p$ vs. $\mu^+\mu^-$



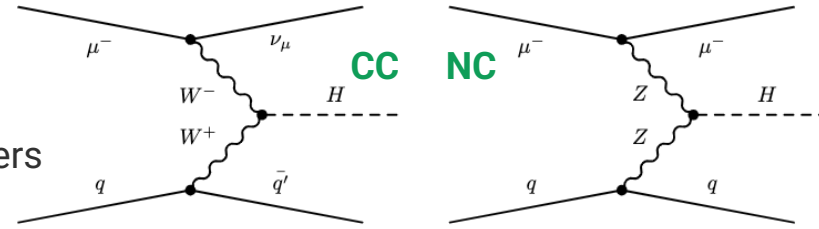
- Equivalent parton luminosity of a  $\mu p$  collider for  $2 \rightarrow 1$  and  $2 \rightarrow 2$  processes compared to a  $\mu^+\mu^-$  collider  $\rightarrow$
- We find that **a  $\mu^+\mu^-$  collider is equivalent to a  $\mu p$  collider of 50% higher  $\sqrt{s}$** , in terms of its discovery potential
  - **So with 50% higher  $\sqrt{s}$  you can probe much of the same particle physics with a  $\mu p$  collider**
- In terms of Higgs boson production, for example, **both are vector boson colliders** since VBF is the dominant cross section



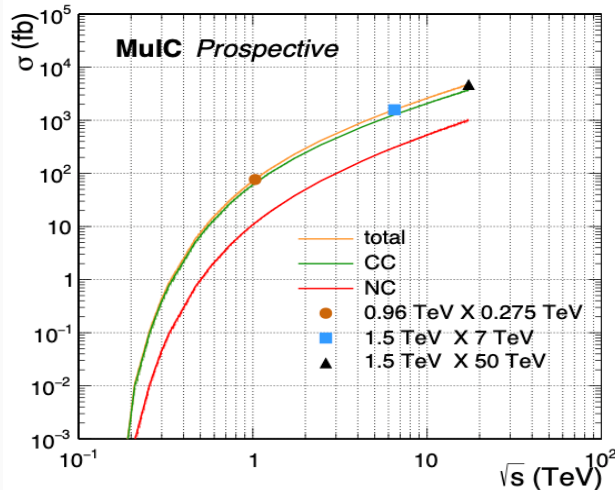
- A 1.5x7 TeV LHmuC has  $\sqrt{s} = 6.5$  TeV
- Equivalent to  $\sim 4.3$  TeV  $\mu^+\mu^-$
  - In turn equivalent to  $\sim 30$  TeV  $pp$



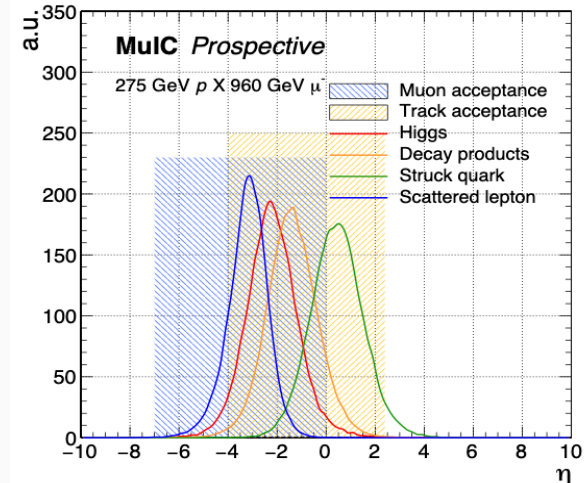
- Vector Boson Fusion mode
  - $\sigma$  grows with  $\sqrt{s}$ , with CC exchange larger than NC
  - Cross section comparable to LHeC and  $\mu^+\mu^-$  colliders
  - Polarization can increase cross section



- Acceptance
  - All final state objects, other than the muon, are in central region of detector (in contrast to LHeC: +3 units of  $\eta$  higher)



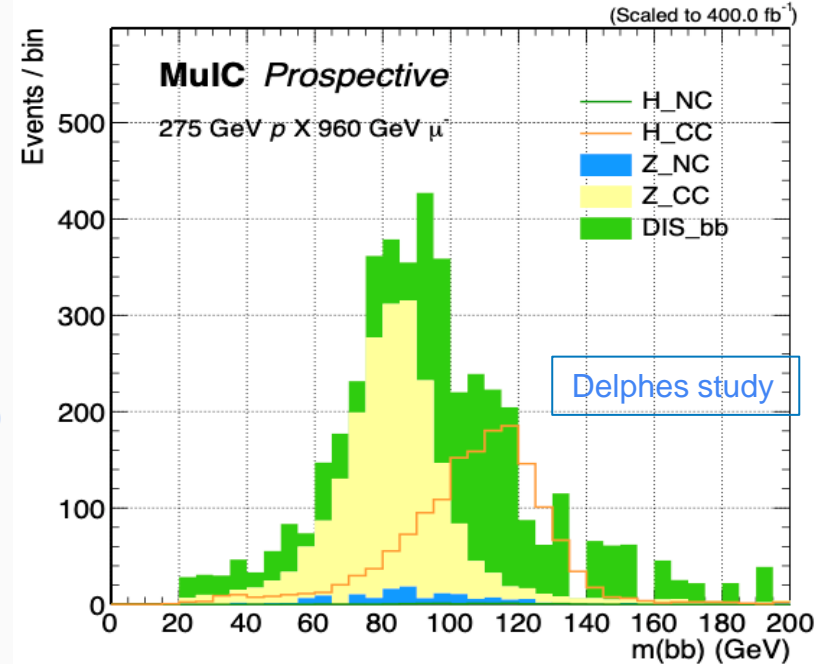
Computed with MadGraph







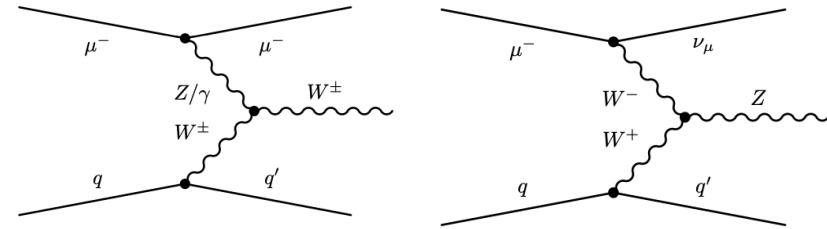
- A pseudo-analysis for  $H \rightarrow bb$ 
  - Requirements that enhance CC VBF process over NC DIS bb background:
    - 3 jets in final state (2 b-tagged)
    - muon veto, MET
    - Higgs  $p_T$
  - **S/B  $\sim 1$  for  $H \rightarrow bb$**
  - **Expect  $\sim 900$  selected  $H \rightarrow bb$  in  $400 \text{ fb}^{-1}$  (10 years\*) @ 1 TeV MuIC**
    - Increases by factor 10 at LHmuC



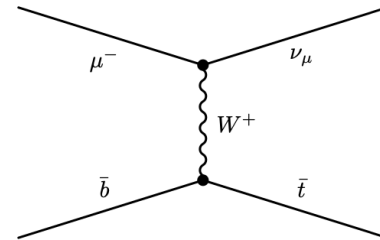
\* at  $L=5 \times 10^{33} \text{ Hz/cm}^2$



- Vector boson production, e.g.
  - Sensitive to **triple gauge couplings**
  - $\sigma(W) = 19 \text{ pb}$  for 1 TeV MuIC
    - $2.1 \times 10^4$  leptonic  $W \rightarrow l\nu$  decays into each lepton flavor for  $10 \text{ fb}^{-1}$

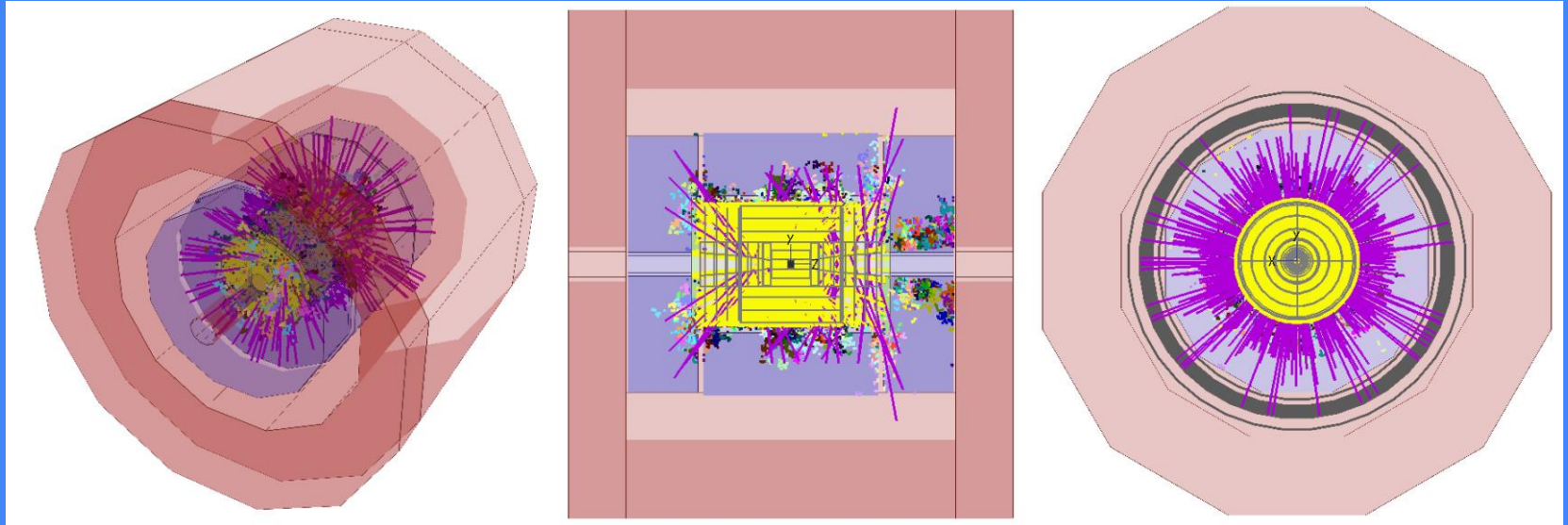


- Single top production
  - **Direct measurement of  $|V_{tb}|$**
  - $\sigma(t) = 1.0 \text{ pb}$  for 1 TeV MuIC



Potential for precision coupling measurements (and maybe mass measurements) with larger  $\sigma$  at higher  $\sqrt{s}$  and higher luminosity)

# Detector Considerations & Challenges

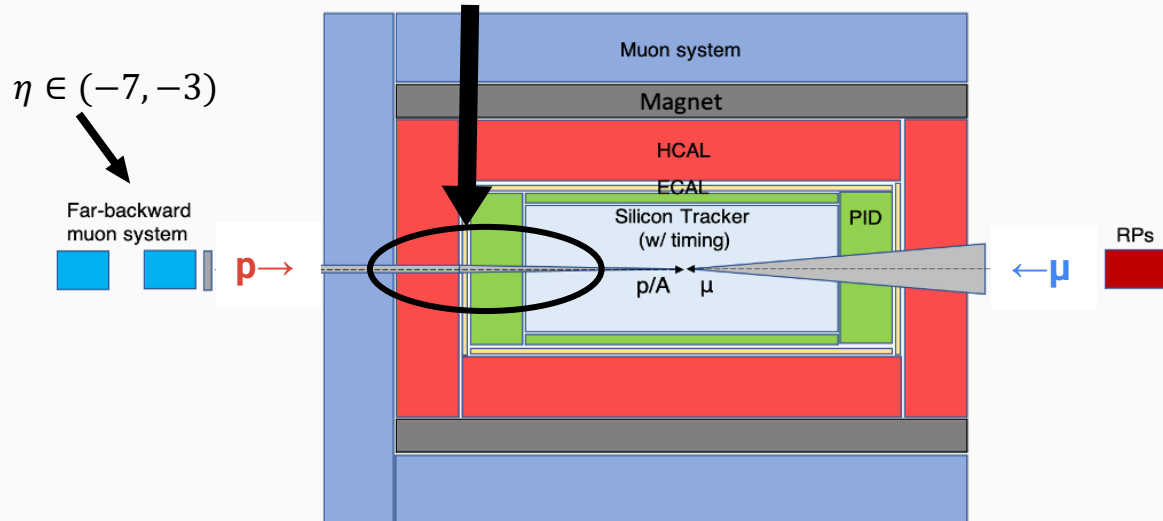


Simulation with beam induced backgrounds (BIB)

# Detector Considerations and Challenges



- Starting point: **Modified  $\mu^+\mu^-$  conceptual detector design**
- Hadron PID over a wide phase space, with **good timing measurements** to reduce BIB
- Measurement of scattered muons at high  $\eta \rightarrow 7$  (far-backward) up to TeV scale
  - Useful also for an experiment at a  $\mu^+\mu^-$  collider to tag/veto NC VBF processes (see backup), and perhaps measure luminosity from Bhabha scattering
- For MuIC ideally remove one shielding nozzle, **keep only on incoming muon side**



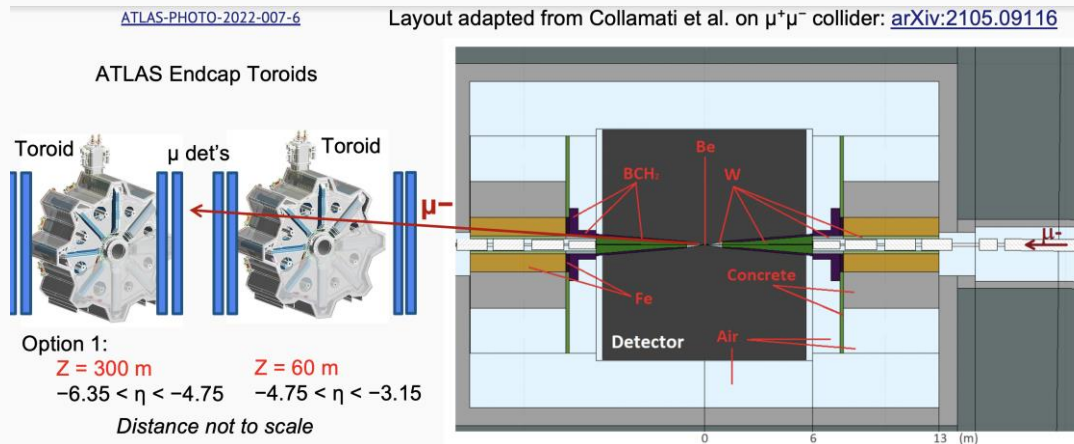
	Main requirements
<b>Muons</b>	<b><math>-7 &lt; \eta &lt; 0</math>, <math>\sigma(p)/p &lt; 5\%</math></b>
Tracking	$-5 < \eta < 2.4$
<b>PID (<math>\pi/k/p</math>)</b>	<b><math>-4 &lt; \eta &lt; 2.4</math>, <math>p &lt; 100</math> GeV</b>
Calorimetry (jets, photons)	$-5 < \eta < 2.4$

# A Far Backward Muon Spectrometer Design Study



Work in progress: DA,  
O.Miguel Colin, M.Munyi

- To begin to address some of the feasibility questions for a MuIC experiment, we initiated a GEANT-4 study of a muon spectrometer
  - Studied TeV muon scattering and energy loss in the tungsten shielding cone (covers  $|\eta| > 3$ )
    - In case we cannot entirely remove it,  
or want to apply the design also for a Muon Coll. experiment to tag NC VBF processes
- Exploring using an (ATLAS) toroidal magnet design for bending as a strawman design
  - Will study the necessary detector resolution for precision momentum measurements
  - Determined impact of shielding cone

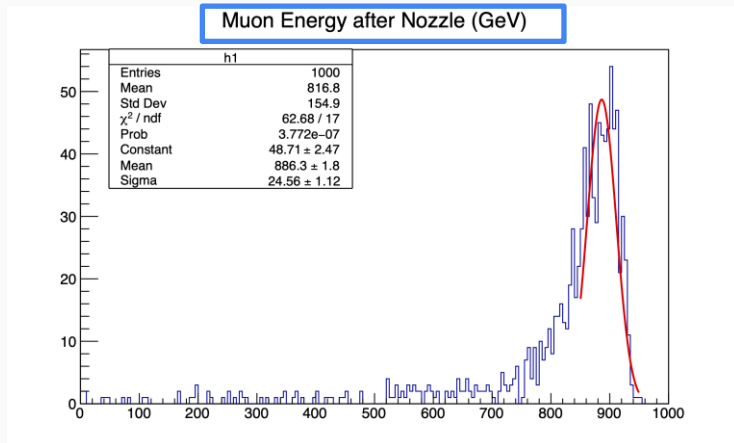


# Example of Shielding Impact on Muon Measurements



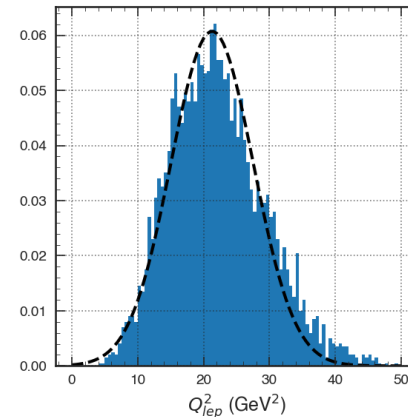
Work in progress: DA,  
O.Miguel Colin, M.Munyi

- A 1 TeV muon loses  $\sim 20\%$  of its energy going through the 6m tungsten cone, with a long tail
- Also, multiple scattering smears the outgoing angle (larger impact on measurements)



- This affects measurements:
  - e.g. 30% smearing for  $Q^2 = 20 \text{ GeV}^2 \rightarrow$  from reconstructed muon quantities
  - So ideally we would like to remove the shielding cone in the backward direction for MuIC (but we will study if ML can recover performance)

900 GeV Muon,  $\eta=6$ , 6m Tungsten w MS;  $Q^2 (\text{true}) = 22.120451$ , mean = 22.124750,  $\mu = 21.294892$ ,  $\sigma = 6.246940$



# Summary and Conclusions



- Collisions of a TeV-scale muon beam with a high-energy proton/ion beam provides a novel way to explore a new regime in DIS at high  $Q^2$  and at low  $x$ 
  - Options include BNL ( $\sqrt{s} = 1\text{-}2$  TeV) as an EIC upgrade, CERN/LHC ( $\sqrt{s} = 6.5$  TeV), or at FNAL depending on how the US muon program develops!
- High luminosity could be a challenge, and needs dedicated accelerator study
  - However, there is much to study at lower luminosity
- Science includes PDFs ( $\mu p$  and  $\mu N$ ) and QCD in novel regimes, but also electroweak and BSM with sufficient luminosity
  - Improved PDFs are also necessary input to future (and current!) hadron colliders
- Time could be running out (or long...) for an LHeC collider at HL-LHC, or an FCC-eh collider, to similarly reach the TeV scale in DIS
  - Worth considering other DIS options !
- Many synergies with muon collider development, and between nuclear, particle, and intensity frontier neutrino physics programs

# Acknowledgements



- This work is in part supported by the Department of Energy, United States grant numbers DE-SC0010103, DE-SC0023351 (D.A.), DE-SC0005131 (W.L.)

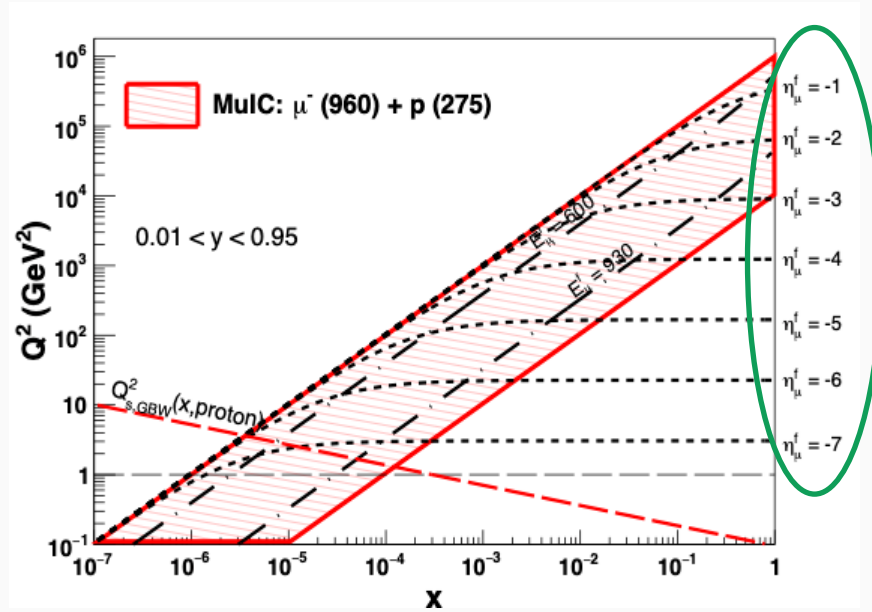


# Backup

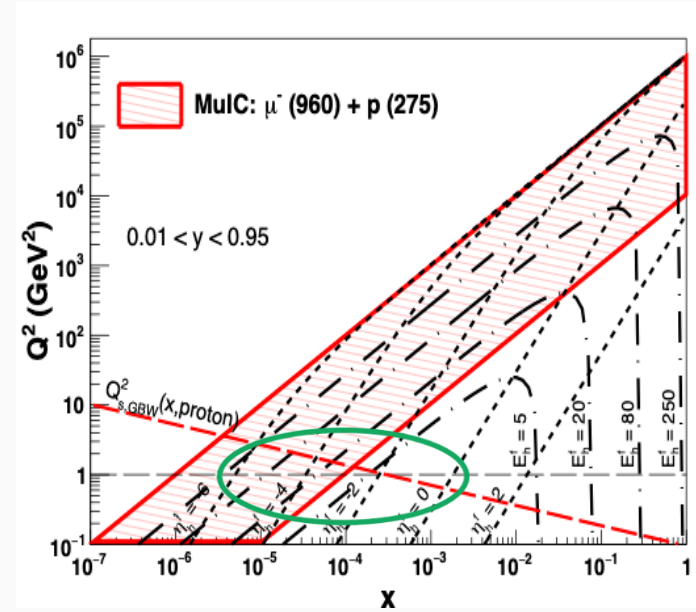
# MuIC Kinematics ( $E, \eta$ in $Q^2$ - $x$ plane)



- Scattered muon



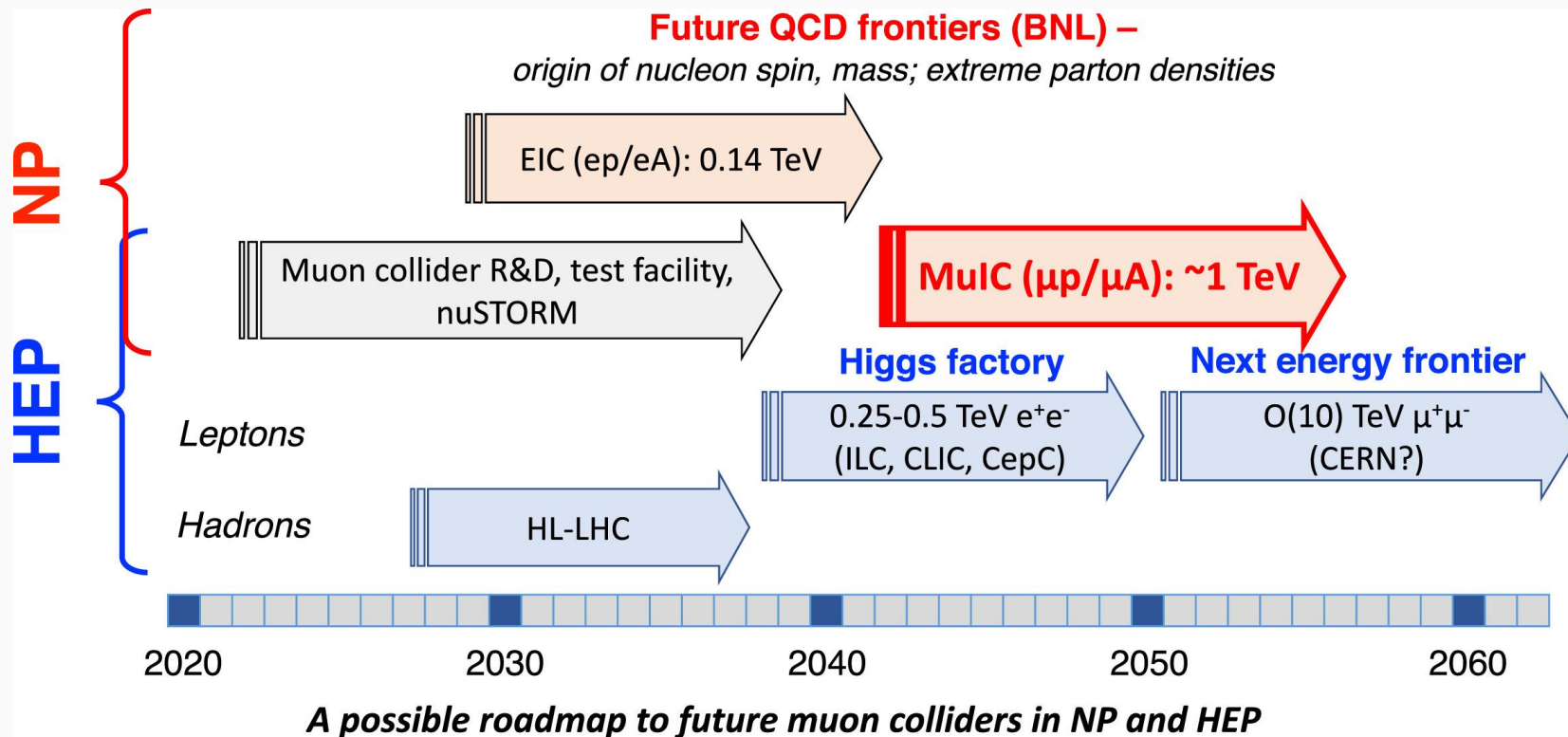
- Scattered jet



- Backward tagging of muons to  $\eta = -7$  (2 mrad) Hadronic system  $-5 < \eta < 2.4$

Quite different from EIC and LHeC kinematics

# Possible Timeline



# A 10 TeV Muon Collider at Fermilab (Site Filler)



- From Diktys Stratakis → [link](#)

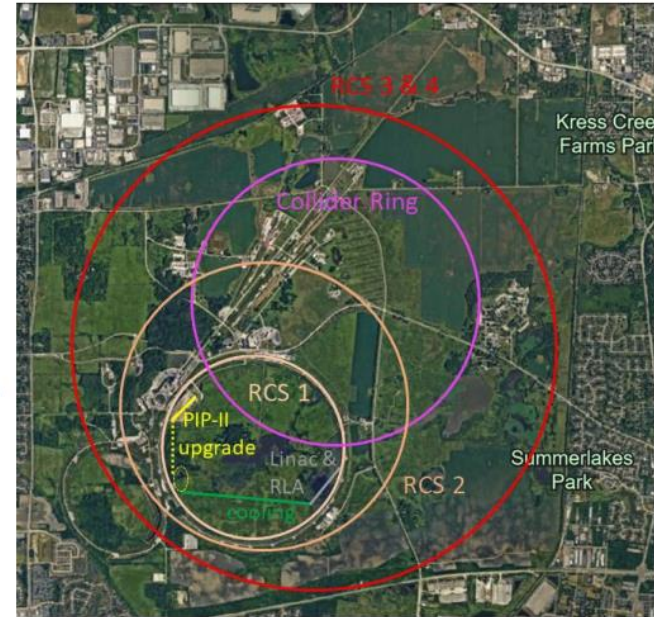
- Linac + RLAs get to 63 –173 GeV
- + RCS 1 gets to 0.45 TeV
- + RCS 2 gets to 1.7 TeV
- + RCS 3 + 4 gets to 5 TeV

Could become MuIC staging options

The accelerating rings are larger than the collider ring because of the need of rapid cycling magnets

## Muon Collider at Fermilab

- 10 TeV MuC concept is in place
- Proton source
  - Post-ACE driver -> Target
- Ionization cooling channel
- Acceleration (4 stages)
  - Linac + RLA → 173 GeV
  - RCS #1 → 450 GeV (Tevatron size)
  - RCS #2 → 1.7 TeV (col. ring size)
  - RCS #3, 4 → 5 TeV (site fillers)
- Collider ring, 10.5 km long
  - Could be combined with RCS #2
- We like to have a baseline design including a neutrino flux mitigation system



# A 10 TeV Muon Collider at Fermilab (Site Filler)



- From Diktys Stratakis → [link](#)

## MuC at Fermilab: Detailed parameters (D. Neuffer)

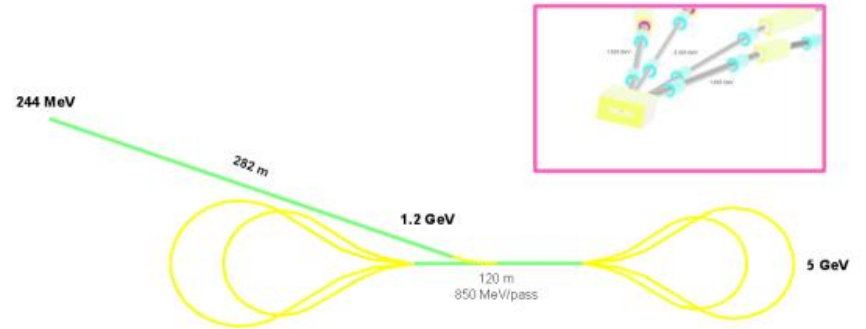
- Just Linac + RLAs would allow
  - $E_\mu = 63 \text{ GeV} \Rightarrow \text{MuIC } \sqrt{s} = 0.25 \text{ TeV} (< \text{HERA})$
  - $E_\mu = 173 \text{ GeV} \Rightarrow \text{MuIC } \sqrt{s} = 0.4 \text{ TeV} (> \text{HERA})$ 
    - Extension for FNAL MuC design
- Diameter of RCS 1 is 6.3 km
  - $E_\mu = 0.45 \text{ TeV} \Rightarrow \text{MuIC } \sqrt{s} = 0.7 \text{ TeV} (2 \times \text{HERA})$
- Diameter of RCS 2 is 10.5 km
  - $E_\mu = 1.7 \text{ TeV} \Rightarrow \text{MuIC } \sqrt{s} > 1 \text{ TeV} (\text{in principle})$
- Do these fit on BNL site?

Parameter	Symbol	Unit	RCS1	RCS2	RCS3	RCS4
Hybrid RCS			No	Yes	Yes	Yes
Repetition rate	$f_{ref}$	Hz	5	5	5	5
Circumference	$C$	m	6280	10500	16500	16500
Injection energy	$E_{inj}$	GeV	173	450	1725	3560
Ejection energy	$E_{ej}$	GeV	450	1725	3560	5000
Energy ratio	$E_{ej}/E_{inj}$		2.60	3.83	2.06	1.40
Decay survival rate	$N_{ej}/N_{in}$		0.85	0.83	0.85	0.89
Acceleration time	$T_{acc}$	ms	0.97	3.71	8.80	9.90
Revolution period	$T_{rev}$	$\mu\text{s}$	21	35	55	55
Number of turns	$N_{turn}$		46	106	160	180
Required energy gain per turn	$\Delta E$	GeV	6	12	11.5	8.0
Average accel. Gradient	$G_{avg}$	MV/m	0.96	1.15	0.70	0.48
Bunch population at injection	$N_{in}$	$10^{12}$	3.3	2.83	2.35	2.0
Bunch population at ejection	$N_{ej}$	$10^{12}$	2.83	2.35	2.0	1.8
Vertical norm. emittance	$\epsilon_{v,N}$	mm-mrad	25	25	25	25
Horiz. norm. emittance	$\epsilon_{h,N}$	mm-mrad	25	25	25	25
Long, norm. emittance	$\epsilon_{z,N}$	eV-s	0.025	0.025	0.025	0.025
Total straight length	$L_{str}$	m	1068	1155	2145	2145
Total NC dipole length	$L_{NC}$	m	5233	7448	10670	8383
Total SC dipole length	$L_{SC}$	m		1897	3689	5972
Max. NC dipole field	$B_{NC}$	T	1.80	1.80	1.80	1.80
Max. SC dipole field	$B_{SC}$	T		12	15	15
Ramp rate	$B'$	T/s	1134	970	440	363
Main RF frequency	$f_{rf}$	MHz	1300	1300	1300	1300
Total RF voltage	$V_{rf}$	MV	6930	13860	13280	9238

# Recirculating Linear Accelerators



- Linac + RLA 1
  - 0.25 → 1.2 GeV
  - 1.2 → 5 GeV (5 passes)



- RLA 2
  - 5 GeV → 63 GeV (4.5 passes)
  - Up to 173 GeV for FNAL MuC

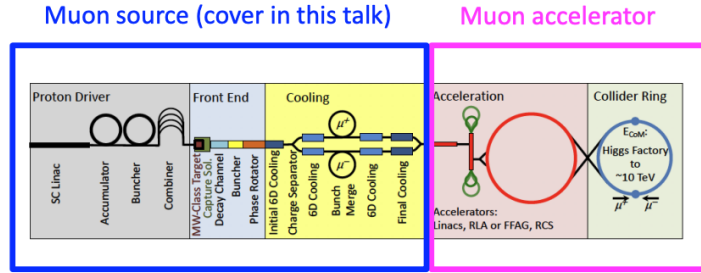


# Muon Cooling



- From Katsuya Yonehara, [link](#)

## Layout of muon accelerator complex for collider



MAP baseline design muon source parameter (based on simulation study)

- Proton driver:**  $10^{14}$ - $10^{15}$  protons per bunch, 3 ns bunch length, 5-15 Hz rep rate, 5-20 GeV
- Front end:** 2-4 MW class target,  $\pi/\mu$  capture section ( $\mu/p$  efficiency 10-15 % for each sign)
- Cooling:** Shrink 6D phase space volume by  $10^6$  (achieved transmission efficiency 5-10 %)

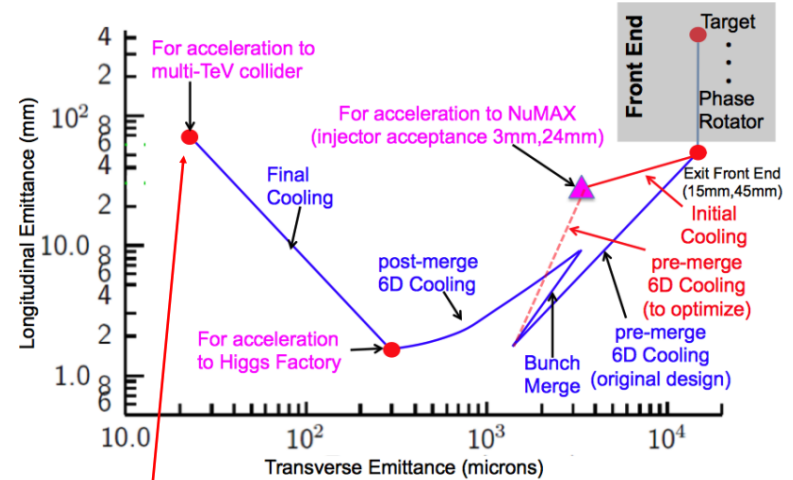
The design parameter is beyond the present accelerator technology.

3 12/14/23 muIC 2023, Target and Cooling, Yonehara



- Ionization cooling + acceleration
- RF cavities
- High field solenoids (10's of T)

## Muon Phase Space Evolution in cooling channels



$$\varepsilon_{N\perp,final} = 25 \mu\text{m rad}, \varepsilon_{NL,final} = 600 \text{ mm}, N_{\mu} \sim 10^{12} \mu/\text{spill}$$



### Key design parameter in ionization cooling

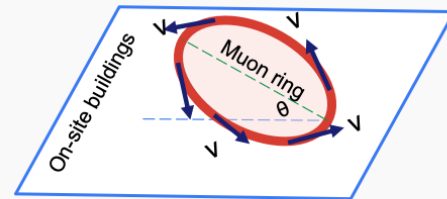
- **Low Z ionization absorber:** Longer radiation length is better for cooling
- **RF cavity as energy loss compensation:** Higher gradient is better for cooling
- **Magnet to make low beta function at absorber:** Stronger field is better for cooling

Heated by multiple sources

# Beam Induced Background, and Neutrino Radiation



- Muon colliders entail a significant beam induced background from  $\mu$  decays and subsequent interactions with materials
  - Experiment requires shielding, high granularity, and excellent time resolution
  - **But this challenge has much in common with hadron collider experiments with high pileup**
- The abundant neutrinos pose a radiation risk from the highly collimated beam just before it exits the ground, particularly from any long straight sections
  - Dose depends inversely on the square of the opening angle ( $\sim 1/\gamma$ ) and on the energy:  $\propto E^3$
  - Thus the radiation at 1 TeV is only 1% of that at 5 TeV, for example
  - **And at low luminosity and energy, collider may be perfectly fine on the surface**
- Otherwise situate deep underground, or on a “remote island”
  - With a small tilt, BNL might be considered such an island! 😊



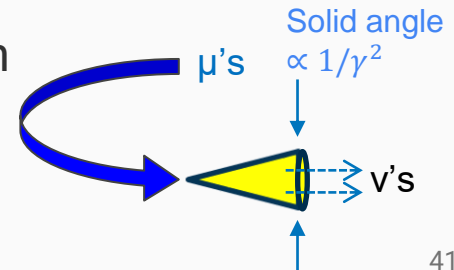
**Tilt the disk plane at a small angle to direct straight sectors toward land/sea and sky?**



# Neutrino Radiation Background



- Collimated beams of neutrinos from muon decays exist along beam line
- For neutrinos near surface, those that interact just before exiting ground can pose a long-term radiation dose for stationary objects
- Long straight sections further intensify this radiation
- The radiation grows with  $E$ , and the collimation effect as  $E^2$ 
  - Hence studies to place ring deep underground for wider spread of radiation at surface
- For a 1 TeV MuIC with a single muon beam compared to a 10 TeV muon collider, the **overall radiation hazard is reduced** by a factor:
  - $2$  (one beam)  $\times 5^3$  (energy dependence)  $\times 10$ -100 (bunch charge reduction)  $\approx 2.5 \times 10^4$
- Radiation hazard is much less of a concern in comparison
- But is it negligible?

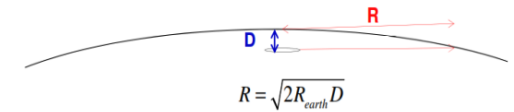
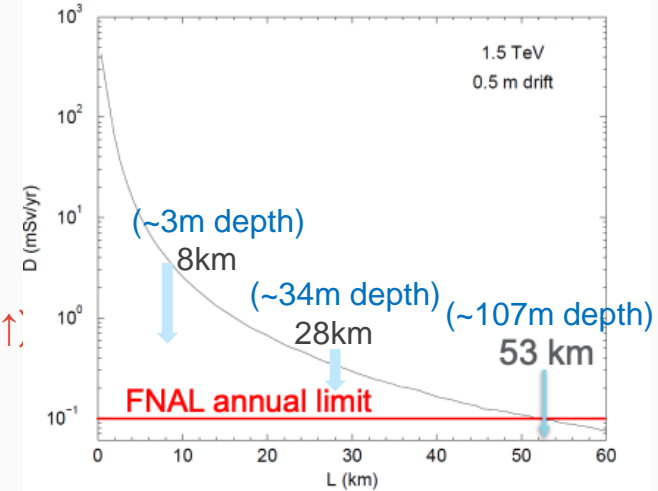


# Neutrino Radiation Background



N.Mohkov, [Snowmass MC Workshop 2022](#)

- Dose vs distance traveled in soil for 1.5 TeV MC to meet 0.1 mSv/yr from just 0.5m straight section →
- **MuIC at BNL might need ~50m straight section at IR? (100X longer!)**
- Bunch intensity reduction for MuIC: 10 – **100X** (cancels↑)
- Energy reduction factor for 1 TeV:  $(1.5)^3 = 3.4X$
- ⇒ **Still need significant depth: ~34 m**
- Lower beam energy to ~0.5 TeV ( $0.5^3 \rightarrow 10X$ )
  - ⇒ **Depth ~3m (i.e. near surface)**
- Or lower beam energy to 0.7 TeV ( $0.7^3 \rightarrow 3X$ ), and reduce straight sections to < 15 m (3.3X) [10X overall]



	$\sqrt{s}$ (TeV)	0.5	1	2	3	4
	$N \times 10^{21}$	0.2	0.2	1.2	1.2	1.2
1 mSv	$R$ (km)	0.4	1.1	6.5	12	18
	$D$ (m)	$\leq 1$	$\leq 1$	3.3	11	25
0.1 mSv	$R$ (km)	1.2	3.2	21	37	57
	$D$ (m)	$\leq 1$	$\leq 1$	34	107	254



# Flip side of neutrino background



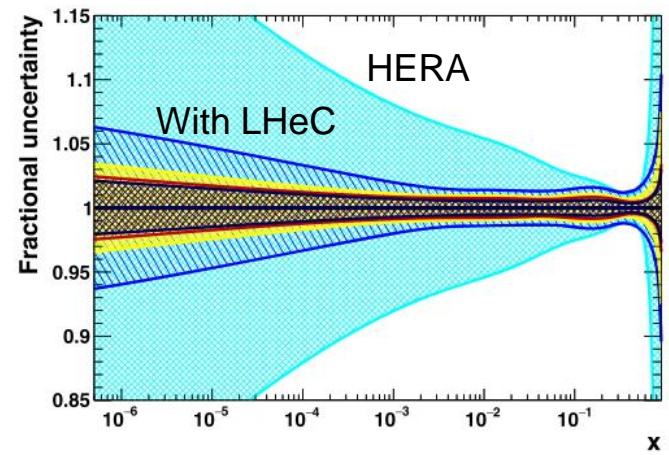
- Turning the radiation argument around, **can a highly collimated neutrino beam be useful for a high-energy neutrino DIS experiment?**
  - Perhaps with more data than collected in the past, if not in energy, for **fixed target?**
- Also makes for a “**neutrino-hadron collider**” in principle, but with very much lower luminosity
  - Blow-up of transverse beam size area in 50m section ( $\sim 10^6$  X)
  - Rate of muon decays ( $\sim 1000$ X less  $\nu$  per muon for 1000 turns per  $\mu$  lifetime)
  - Fraction of decays in straight section ( $\sim 100$ X less for 50m/4000m)
  - $\Rightarrow$  Luminosity  $\sim 11$  orders of magnitude smaller:  $L \sim 10^{20}$  (?)
  - Also how to disentangle from muon-hadron DIS?



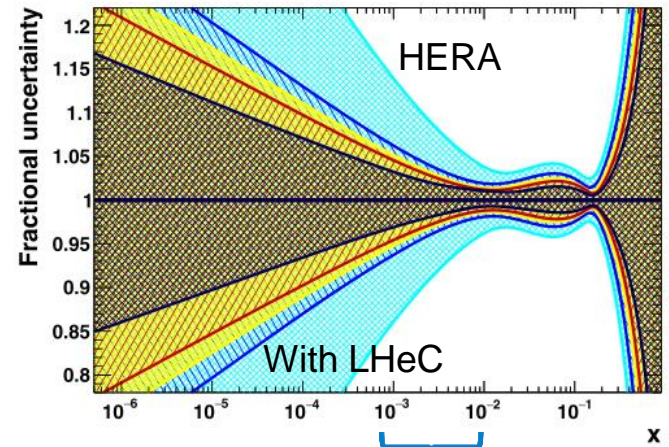
- Luminosity measurement via the  $\mu p \rightarrow \mu p \gamma$  process (analog to HERA and EIC measurement) would be challenging at a MuIC with the large BIB
  - May already have a large  $\gamma$  flux even if all other charged particles are swept away
  - This also may plague roman pot measurements for scattered protons (?)
- Find another normalization process?

# Potential Expected PDF Uncertainties

- From LHeC CDR:
  - [2021 J. Phys. G: Nucl. Part. Phys. 48 110501](#)
  - $Q^2 = 1.9 \text{ GeV}^2$
  - $L = 5, 50, 1000 \text{ fb}^{-1}$
- Greatly improves precision at mid- to low- $x$



Sea quark distribution ( $\log_{10} x$  scale).



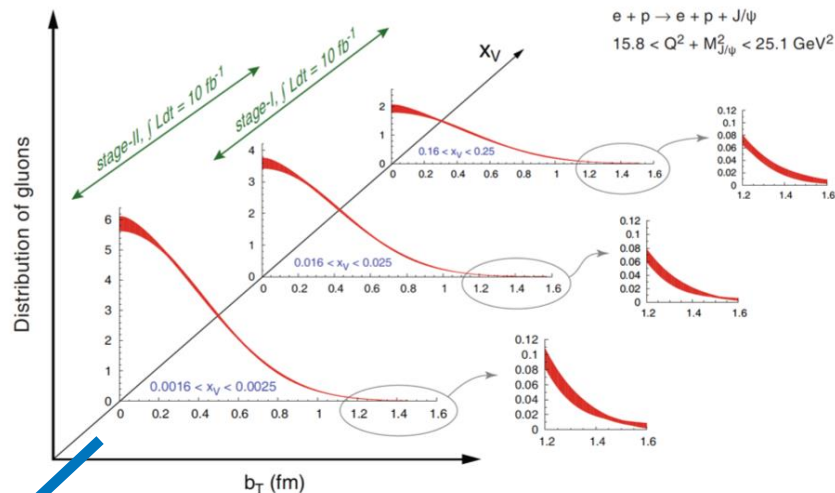
Gluon distribution ( $\log_{10} x$  scale).



# Nuclear Structure and Spin at the MuIC



- Transverse Spatial Distributions of Partons
  - Generalized parton distributions (GPDs)



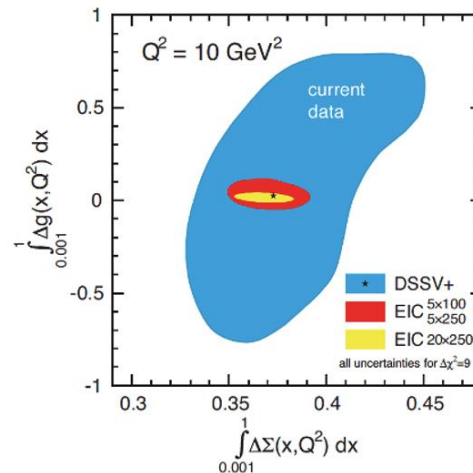
From [EIC Yellow Report](#)

MuIC can extend EIC measurements to  $x \approx 10^{-5}$ , and nucleon polarization is possible at BNL

- Spin Structure and the Nucleon Spin Puzzle

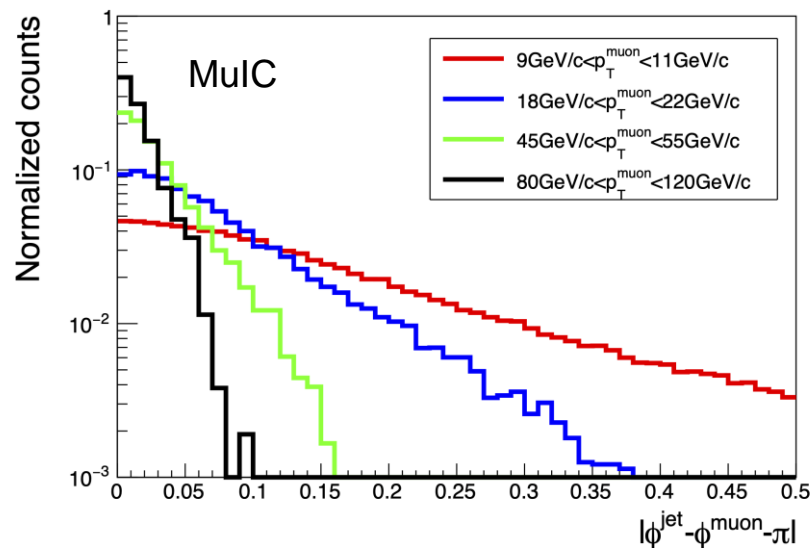
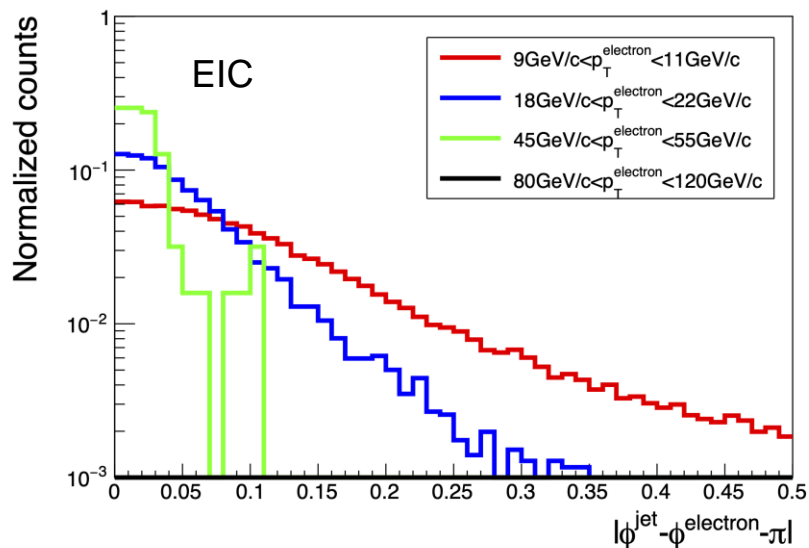
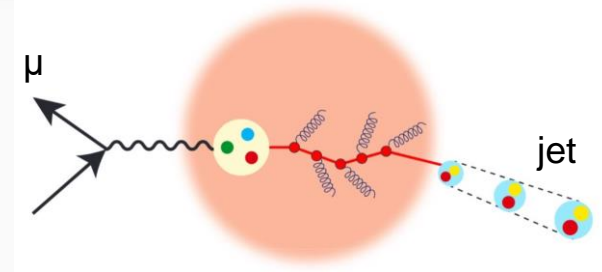
“Helicity sum rule”

$$\frac{1}{2}\hbar = \underbrace{\frac{1}{2}\Delta\Sigma}_{\text{quark contribution}} + \underbrace{\Delta G}_{\text{gluon contribution}} + \underbrace{\sum_q L_q^z + L_g^z}_{\text{orbital angular momentum}}$$



# A lab for QCD and Nuclei at the MuIC

- A promising observable to probe the dense gluonic medium inside a heavy nucleus is the **decorrelation in azimuth from back-to-back of the muon-jet system**



(28 weeks at 50% duty cycle  $\rightarrow \sim 40 \text{fb}^{-1}$ )

# QCD and the Running of $\alpha_s$



- Measurements can span a broad range to measure  $\alpha_s(Q^2)$  in a **single experiment**

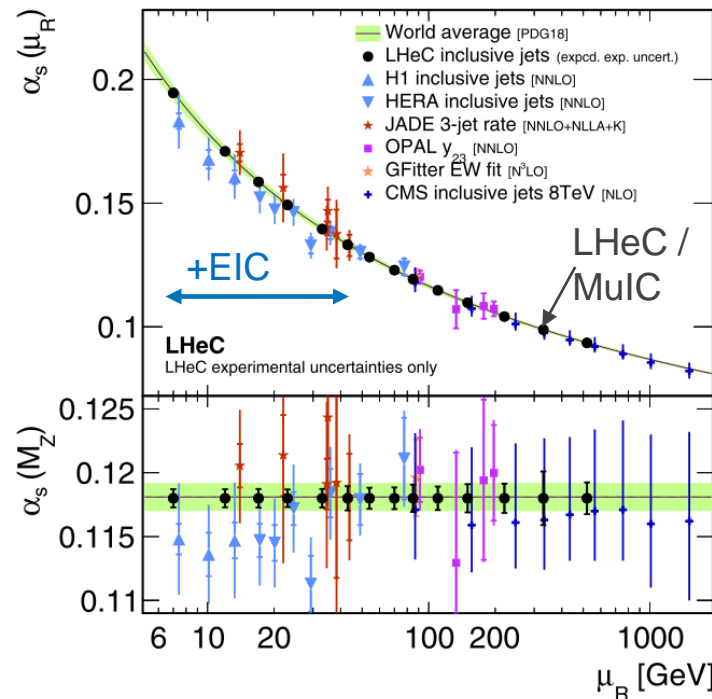
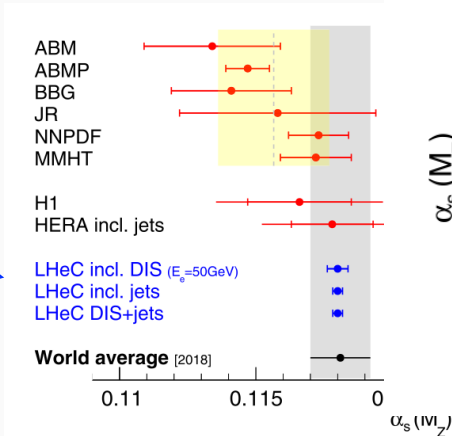
- From DIS inclusive jet cross section measurements,  $F_L$  measurements, and from QCD evolution fits to structure function data
- Removes some inter-experiment systematics

- From the LHeC CDR:

- Inclusive jets with expected uncertainties for  $1 \text{ ab}^{-1} \rightarrow$ 
  - (JES uncertainty: 0.5%)

- Expected  $\alpha_s(M_Z)$  uncertainties

- $\pm 0.00038$
- Even  $50 \text{ fb}^{-1}$  ( $\sim 1$  year) is competitive



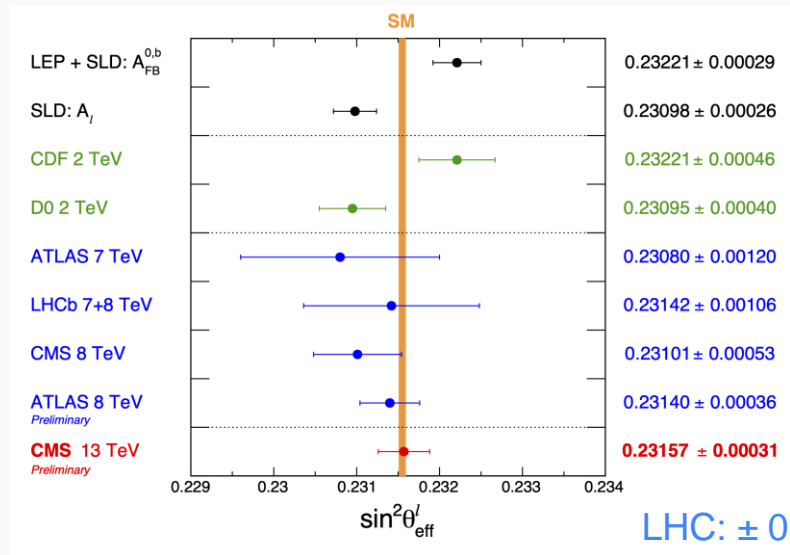


# $\sin^2 \theta_W^{\text{eff}}$ Measurements at $M_Z$

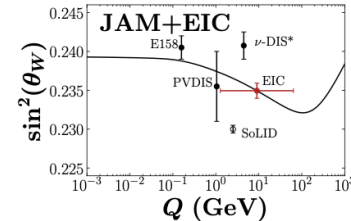


- Drell-Yan angular distribution at LHC

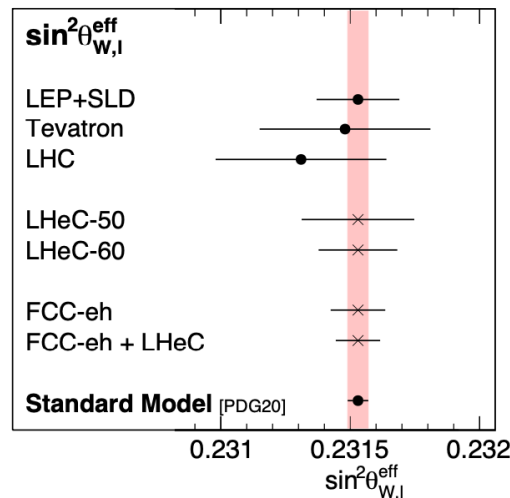
[CMS-PAS-SMP-22-010](#)



- Future DIS expts.



[PoS EPS-HEP2021 \(2022\) 485](#)



[Nucl.Phys.A1026\(2022\) 122447](#)

EIC:  $\pm 0.0001$

LHeC:  $\pm 0.00021$

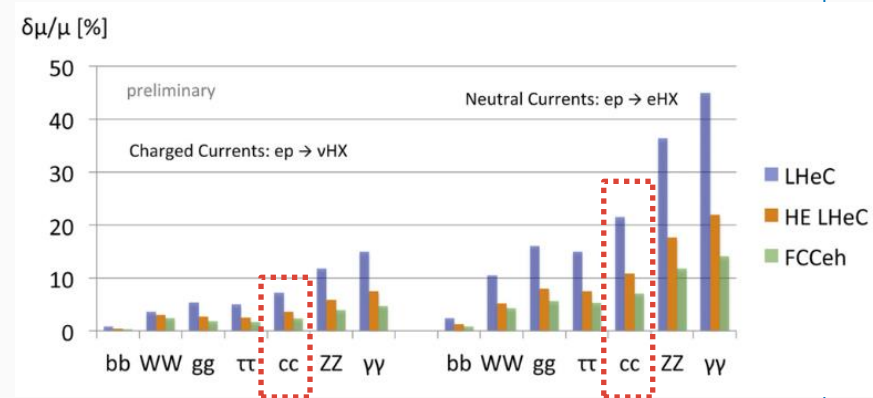
MuIC similar?

- Potentially comparable (or better) sensitivity than past measurements

# Higgs $\rightarrow$ cc ?



- Charm decay channel is difficult at the LHC, so it could be an opportunity
- However, it is also challenging for the MuIC:
  - 20X smaller Branching Ratio for  $H \rightarrow cc$  vs.  $H \rightarrow bb$
  - Smaller c-tagging efficiency
  - More DIS background
- Similar pseudo analysis by P.Ahluwalia, S.Sekula, et al.: [arXiv:2211.02615](https://arxiv.org/abs/2211.02615)
  - Yielded only a handful of events – **not so promising**
  - Did not yet include mis-tagged light dijet background
  - **However, there may be topological features to utilize to discriminate signal**
- Perhaps more optimism in LHeC CDR
  - Machine learning (BDT) analysis
  - $\sim 7\%$  (20%) precision on coupling for **CC** (NC) production with  $1 \text{ ab}^{-1}$
- So there may be potential at MuIC



# Probing Models Relevant to LFU Violations



- e.g. Consider **Z' models** and couplings discussed in M. Abdullah et al., [Phys. Rev. D 97, 075035](#), that couple via O9 operator mostly to 2<sup>nd</sup> generation leptons ( $\mu$ ) and 2<sup>nd</sup> and 3<sup>rd</sup> generation quarks (s, b) to explain anomalies in B meson decays.

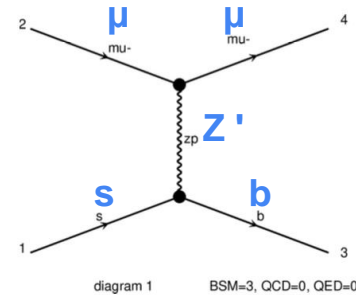
$$\mathcal{L} \supset Z'^{\mu} \left[ g_{\mu} \bar{\mu} \gamma^{\mu} \mu + g_{\mu} \bar{\nu}_{\mu} \gamma^{\mu} P_L \nu_{\mu} + g_b \sum_{q=t,b} \bar{q} \gamma^{\mu} P_L q + (g_b \delta_{bs} \bar{s} \gamma^{\mu} P_L b + \text{h.c.}) \right] \quad (6)$$

- $g_{\mu}$  and  $g_s$  are flavor conserving couplings
- $\delta_{bs}$  parameterizes non-flavor conserving couplings

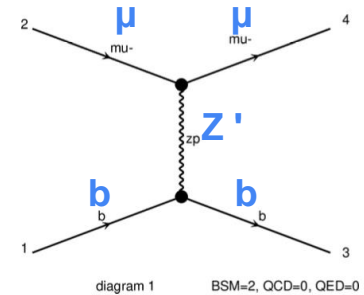
$$g_b \delta_{bs} g_{\mu} (100 \text{ GeV} / m_{Z'})^2 \simeq 1.3 \times 10^{-5} \quad (5)$$

to fit lepton flavor universality violations

Which admittedly are diminished with latest [LHCb measurement](#) that is compatible with the SM



(a)  $s \mu^- \rightarrow b \mu^-$



(b)  $b \mu^- \rightarrow b \mu^-$

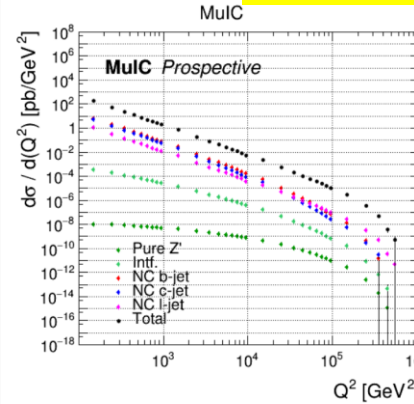
- Consider **interference** with NC DIS
  - so flavor conserving coupling dominates

# Probing Models Relevant to LFU Violations

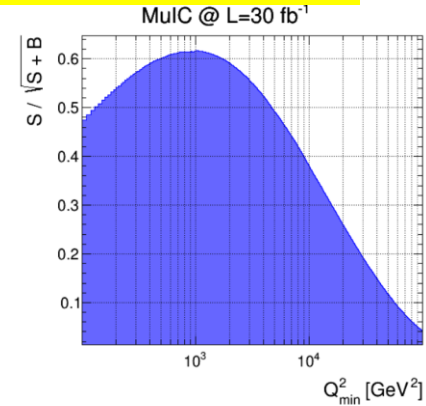


Work in progress: DA, O.Miguel Colin

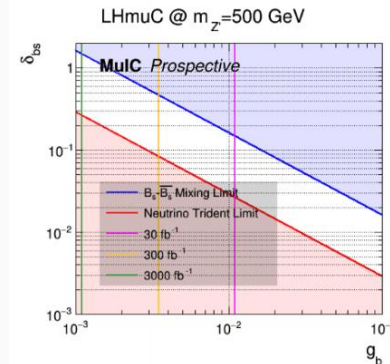
- Perform pseudo-analysis using a **cut-and-count** approach on the reconstructed  $Q^2$  from the muon, optimized for sensitivity
- Apply b-tagging and mis-tagging efficiencies to final state jet
  - b, c, light: 70%, 10%, 1%
- Derive expected limits
- **Conclusion: generally need LHmuC (120 fb<sup>-1</sup>) to be competitive with HL-LHC (3000 fb<sup>-1</sup>) for this model**



(a)  $m_{Z'} = 500$  GeV



(b)  $m_{Z'} = 500$  GeV



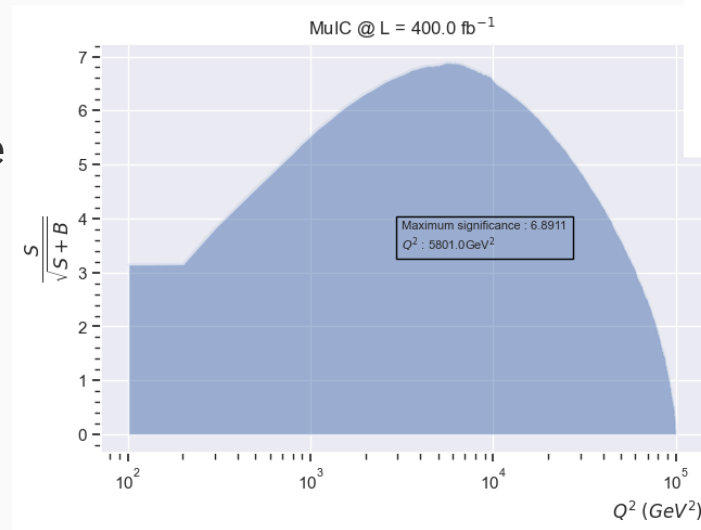
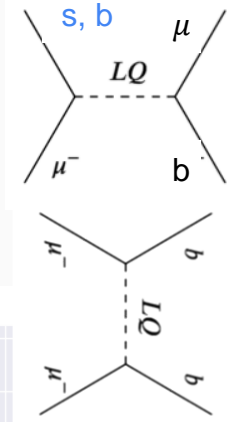
(a) LHmuC

# Probing Leptoquarks Relevant to LFU Violations



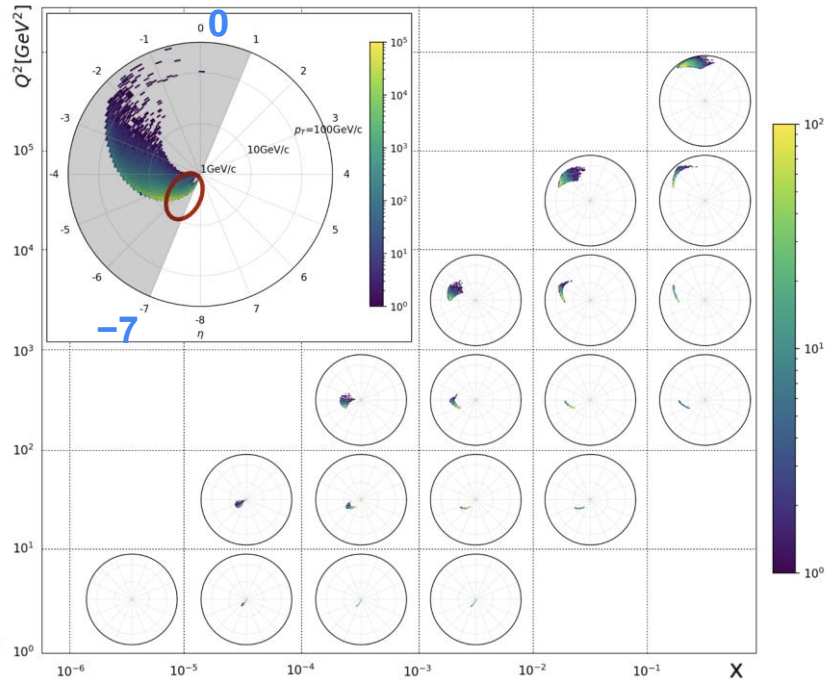
Work in Progress

- Studies focused on LQ models inspired by B and  $\mu$  anomalies
  - S3 type LQ (F=2, LL coupling,  $\mu b$ ),  $\lambda = 0.1$ ,  $M = 500$  GeV shown here
- Consider **interference** with SM DIS in both s- and t-channel
  - Negative interference term subtracts from SM DIS diff. xsec
- Try Z' **cut-and-count** method on reconstructed  $Q^2$  to estimate sensitivity
- **Conclusion: much more sensitive than Z' search**
  - Generally because final state muon is more central than for Z' interference
- On-shell mass reconstruction also to be studied

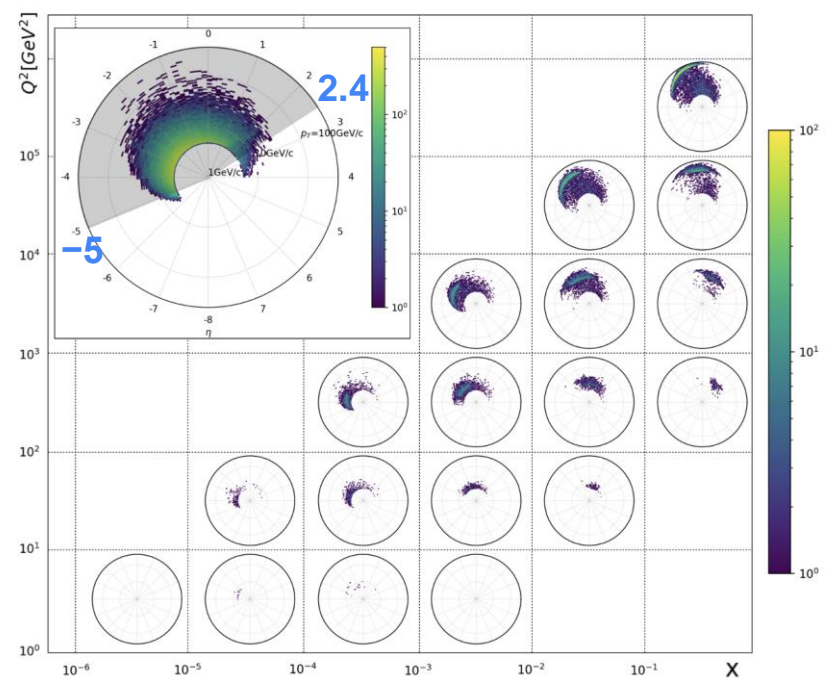


- Scattered muon (far backward  $\rightarrow$  central with  $Q^2$ )

- Scattered jet (More central)



Distribution of Scattering Muon



Distribution of Jets

- Backward tagging of muons to  $\eta = -7$

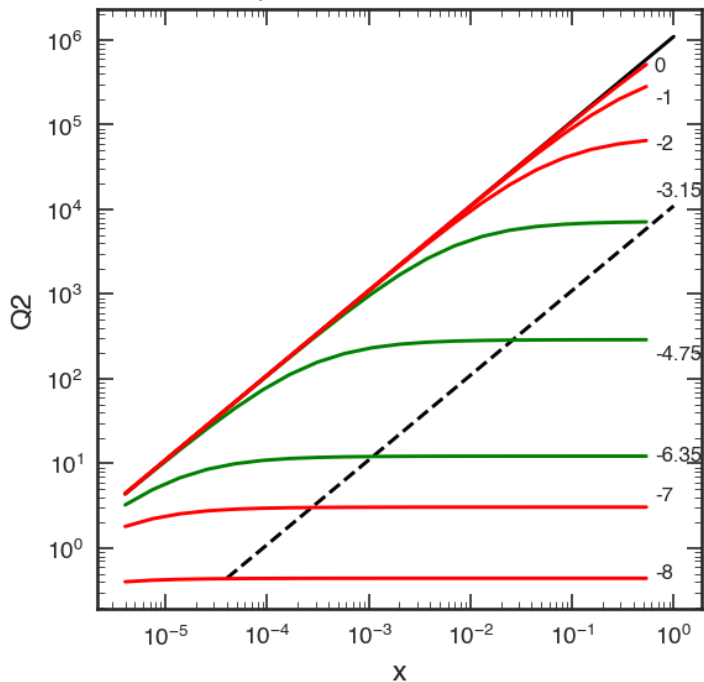
- Hadronic system  $-5 < \eta < 2.4$

# A Far Backward Muon Spectrometer Design Study



Work in progress: DA,  
O.Miguel Colin, M.Munyi

MuIC mu-p 1000 x 275 GeV, Constant Eta



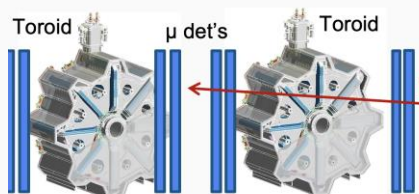
← Near Toroid coverage

← Far Toroid coverage

[ATLAS-PHOTO-2022-007-6](#)

Layout adapted from Collamati et al. on  $\mu^+\mu^-$  collider: [arXiv:2105.09116](#)

ATLAS Endcap Toroids



Option 1:

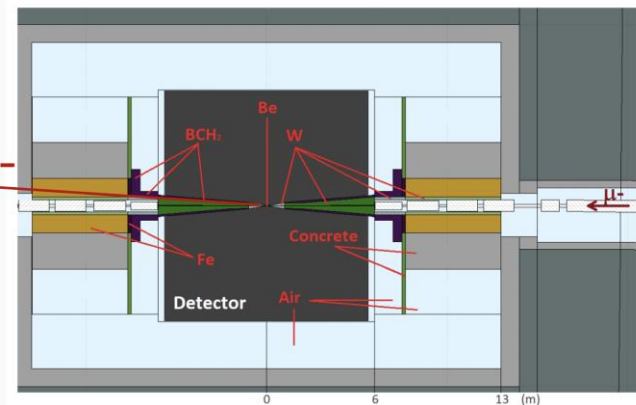
Z = 300 m

Z = 60 m

$-6.35 < \eta < -4.75$

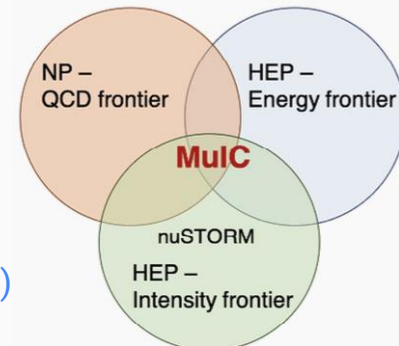
$-4.75 < \eta < -3.15$

Distance not to scale





- Siting a muon collider at a facility with a high energy hadron ring opens up a very interesting additional, complementary science program
  - Would be an exciting upgrade to the EIC
  - But siting at FNAL or CERN is also very interesting and synergistic
- Re-use of some existing hadron accelerator infrastructure may help allay some cost
  - And can still benefit from a lower initial muon beam energy if collided with TeV scale hadron beam
- A MuIC provides a science case for an **initial muon collider demonstrator**
  - Luminosity demands for proton/nuclear structure measurements at extreme parton density (low  $x$ ) are much less stringent than the ultimate needs for Higgs studies, etc.
- Similar detector needs to future  $\mu^+\mu^-$  and FCC-hh experiments
  - Good timing for background mitigation, high eta muon spectrometer(s)
- A MuIC would address particle physics, nuclear physics, and intensity frontier interests
  - Two communities to join in detector development and construction
  - Joint funding from particle and nuclear physics programs? (as for the LHC program)



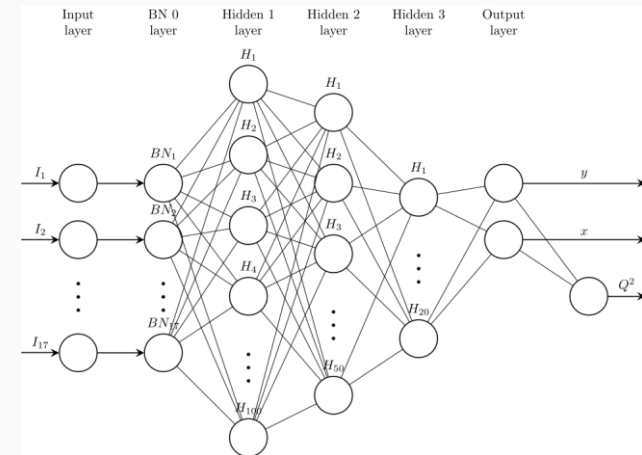


# Machine Learning Methods to Reconstruct DIS Variables



Work in progress:  
O.Miguel Colin, A.Amarilla

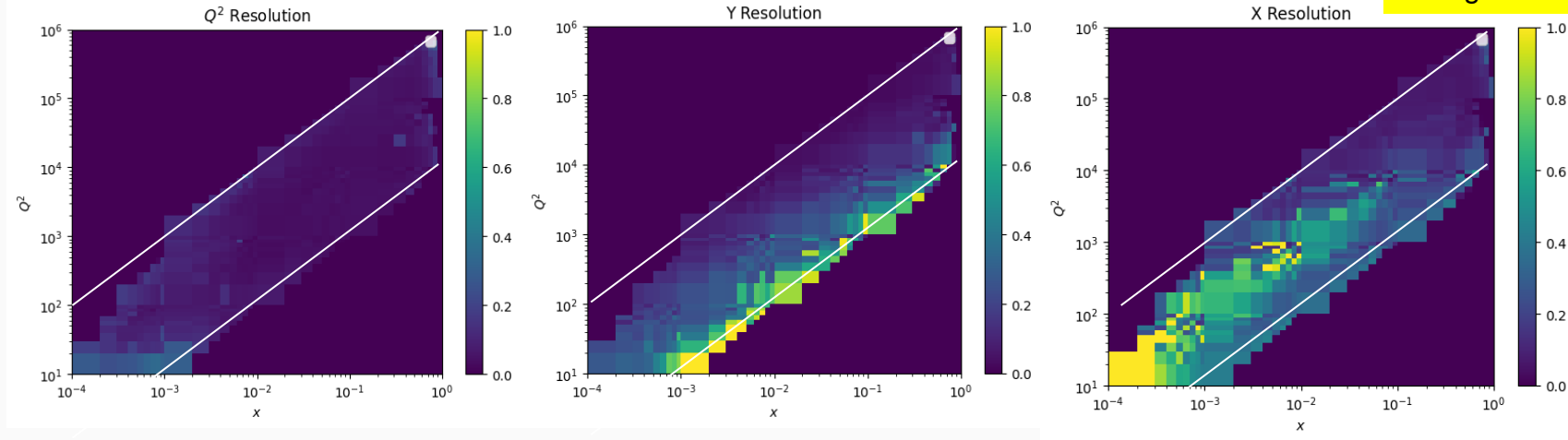
- The lepton method, or any of the other well-known DIS approaches (DA, JB) do not use all of the available scattering information, and have (different) regions of good and poor resolution
- We started using a machine-learning approach to reconstruct  $Q^2$ ,  $x$ , and  $y$  as a proxy for the best method we can use
- Applying this to gen level final state particles, smeared by detector resolutions
- Input variables:
  - muon energy (outgoing)
  - muon eta (outgoing)
  - Shower - Sum of energy deposited in calorimeter
  - Shower - Sum of momentum in x direction
  - Shower - Sum of momentum in y direction
  - Shower - Sum of momentum in z direction
  - Shower - Sum of (energy - momentum in z direction)
  - Reconstructed Jaquet-Blondel Angle (Direction of shower)
  - Reconstructed Lepton Method:  $Q^2$ ,  $x$ ,  $y$
  - Reconstructed Jaquet-Blondel Method:  $Q^2$ ,  $x$ ,  $y$
  - Reconstructed Double Angle Method:  $Q^2$ ,  $x$ ,  $y$



# Machine Learning Methods to Reconstruct DIS Variables



Work in progress:  
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- Uses detector variable smearing as in [Acosta and Li, NIM A 1027 \(2022\) 166334](#) , but not yet any smearing from a shielding cone
- Aiming to get better resolution than any single standard approach
- Still a work in progress (e.g. need to improve x resolution)
- Can be used to optimize necessary detector resolutions and coverage

# DIS Resolution Studies

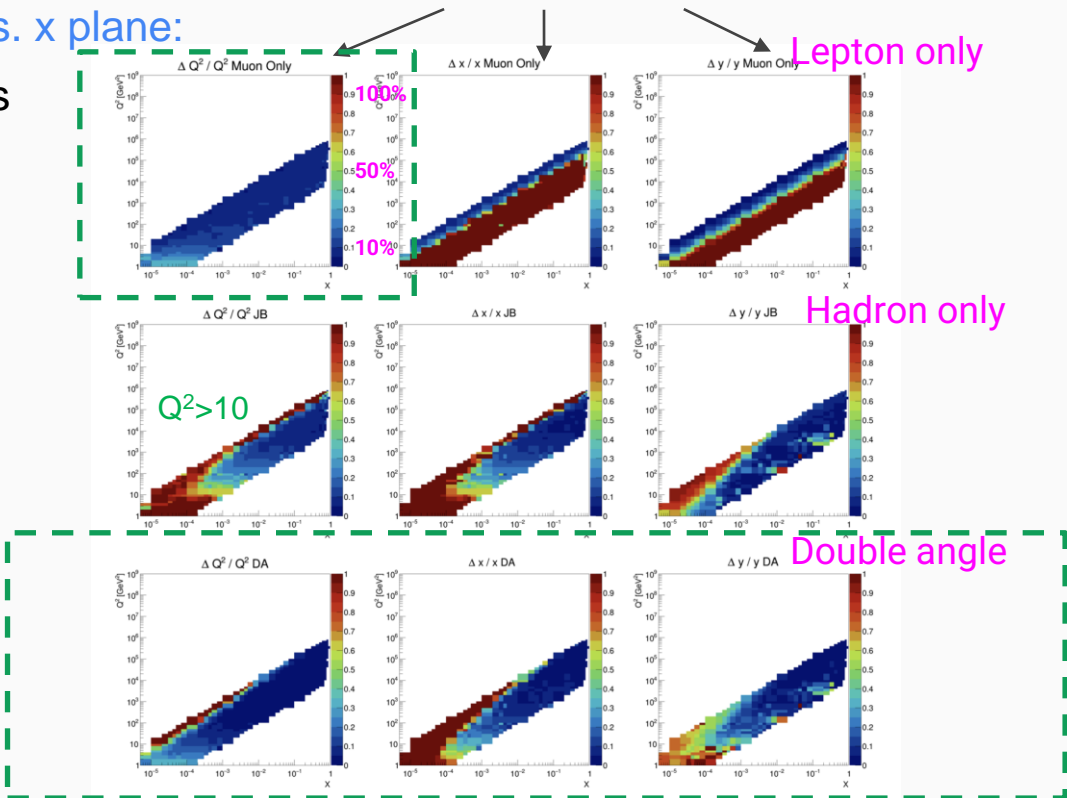


Resolutions of reconstructed  $Q^2$ ,  $x$  and  $y$  with 3 methods  
 $Q^2$  vs.  $x$  plane:

Simple assumptions of detector resolutions  
to smear particles from PYTHIA 8

Particle	Detector	Resolution	
		$\frac{\sigma(p)}{p}$ or $\frac{\sigma(E)}{E}$	$\sigma(\eta, \varphi)$
(Forward) Muons	e.g., MPGD	$0.01\% p \oplus 1\%$	$0.2 \times 10^{-3}$
Charged particles ( $\pi^\pm, K^\pm, p/\bar{p}, e^\pm$ )	Tracker + PID	$0.1\% p \oplus 1\%$	$\left(\frac{2}{p} \oplus 0.2\right) \times 10^{-3}$
Photons	EM Calorimeter	$\frac{10\%}{\sqrt{E}} \oplus 2\%$	$\frac{0.087}{\sqrt{12}}$
Neutral hadrons ( $n, K_L^0$ )	Hadronic Calorimeter	$\frac{50\%}{\sqrt{E}} \oplus 10\%$	$\frac{0.087}{\sqrt{12}}$

- Muons: 10% at 1 TeV,  $\eta > -7$
- Hadrons:  $-4 < \eta < 2.4$  (shielding)



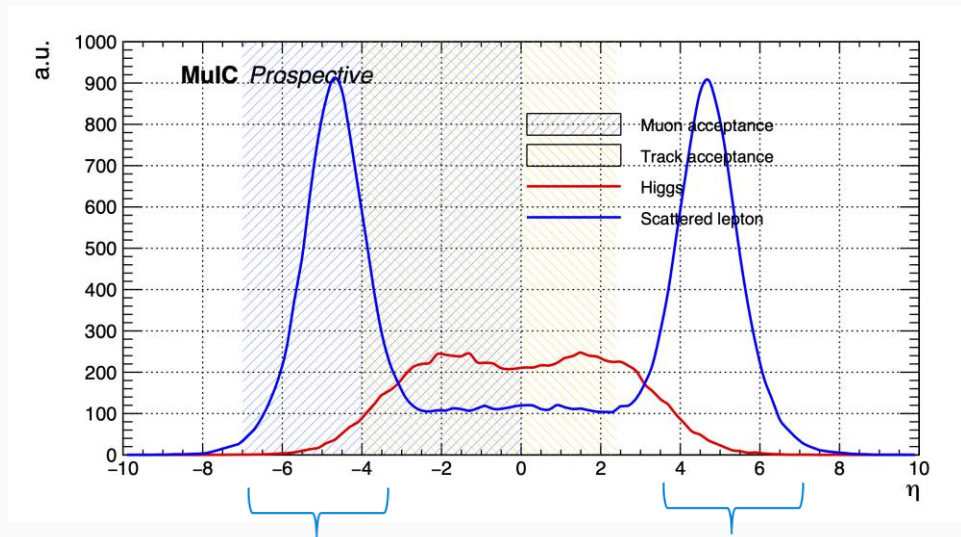


- Ketenoglu et al. ([Mod. Phys. Lett. A 37 \(2022\) 2230013](#)) discuss that previously listed MuIC beam-beam tune-shifts are too high, and obtain lower values by lowering  $N_\mu$  by factor 100 to get:  $L \approx 10^{31} - 10^{32} \text{ Hz/cm}^2$
- Christoph Montag at the [MuIC workshop](#) made similar remarks in his [talk](#)
  - Space charge effects, intrabeam scattering (down factor 240)
  - Beam-beam effects (reduce by factor 100, but could increase  $\mu$  bunches by 100)
  - Hadron beam emittance growth from muon replacement
  - **Suggests increasing beam emittances, lowering muon bunch charge by factor 7**, and using 1200 proton bunches (colliding with one at a time)
  - Luminosity reduced by factor 100:  $L \approx 5 \times 10^{31} \text{ Hz/cm}^2$
  - Larger beam sizes will lead to challenges for IR design and reduced detector acceptance
  - But effects improve at higher beam energy
  - Colliding with **multiple proton bunches at a time also could increase luminosity ( $\approx 10^{32}$ )**
- On the plus side:
  - Increasing emittance may relax cooling requirements
  - Lowering  $N_\mu$  decreases neutrino radiation background vs. MuC

# VBF Higgs Production for a 10 TeV $\mu^+\mu^-$ Collider



- Pseudorapidity distribution for scattered lepton in VBF Higgs production
- 5 x 5 TeV

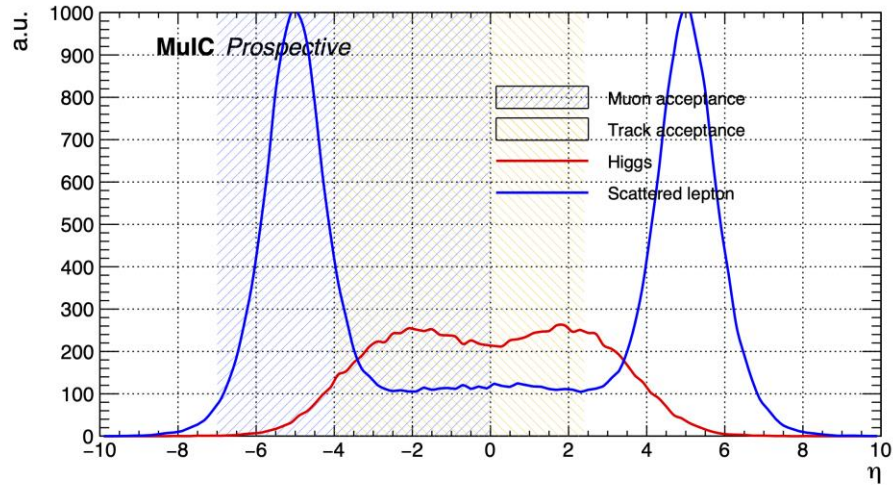


- Scattered muons in far backward and forward regions similar to MuIC

# VBF Higgs Production for $\mu^+\mu^-$ Collider



- Pseudorapidity distribution for scattered lepton in VBF Higgs production
- 7 x 7 TeV



- Scattered muons in far backward and forward regions