



Vassily Kandinsky, *Several Circles*, 1926



Flavour Tagging with Graph Neural Network at ATLAS

19th July 2024

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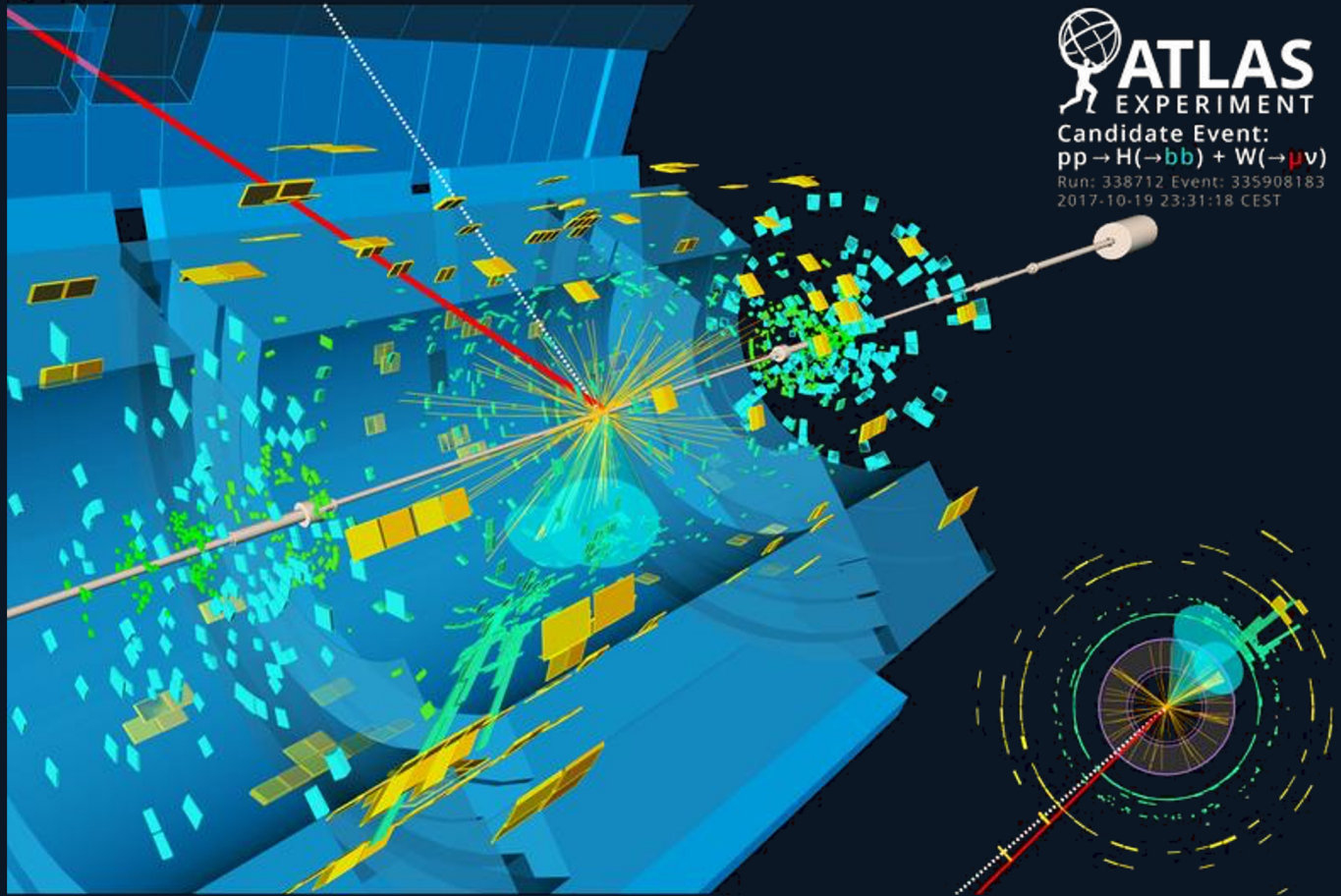
On behalf of the ATLAS Experiment

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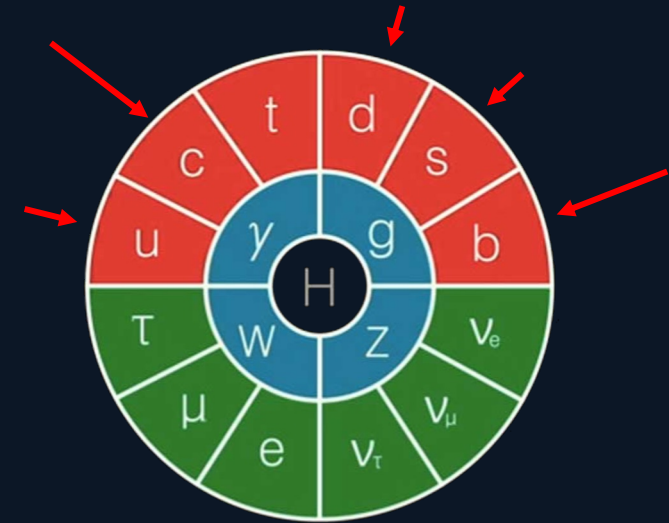


INTRODUCTION

ATLAS event display of a Higgs boson decaying to two b-quarks with an associated W boson decaying into a muon and a neutrino



ATLAS Collaboration relies on heavy-flavour jets classifiers



Used in many analyses:
 $H \rightarrow b\bar{b}$, $H \rightarrow c\bar{c}$, di-Higgs, ...

These classifiers are **ML TAGGERS**

Example: $VH \rightarrow b\bar{b} / c\bar{c}$ presented this morning

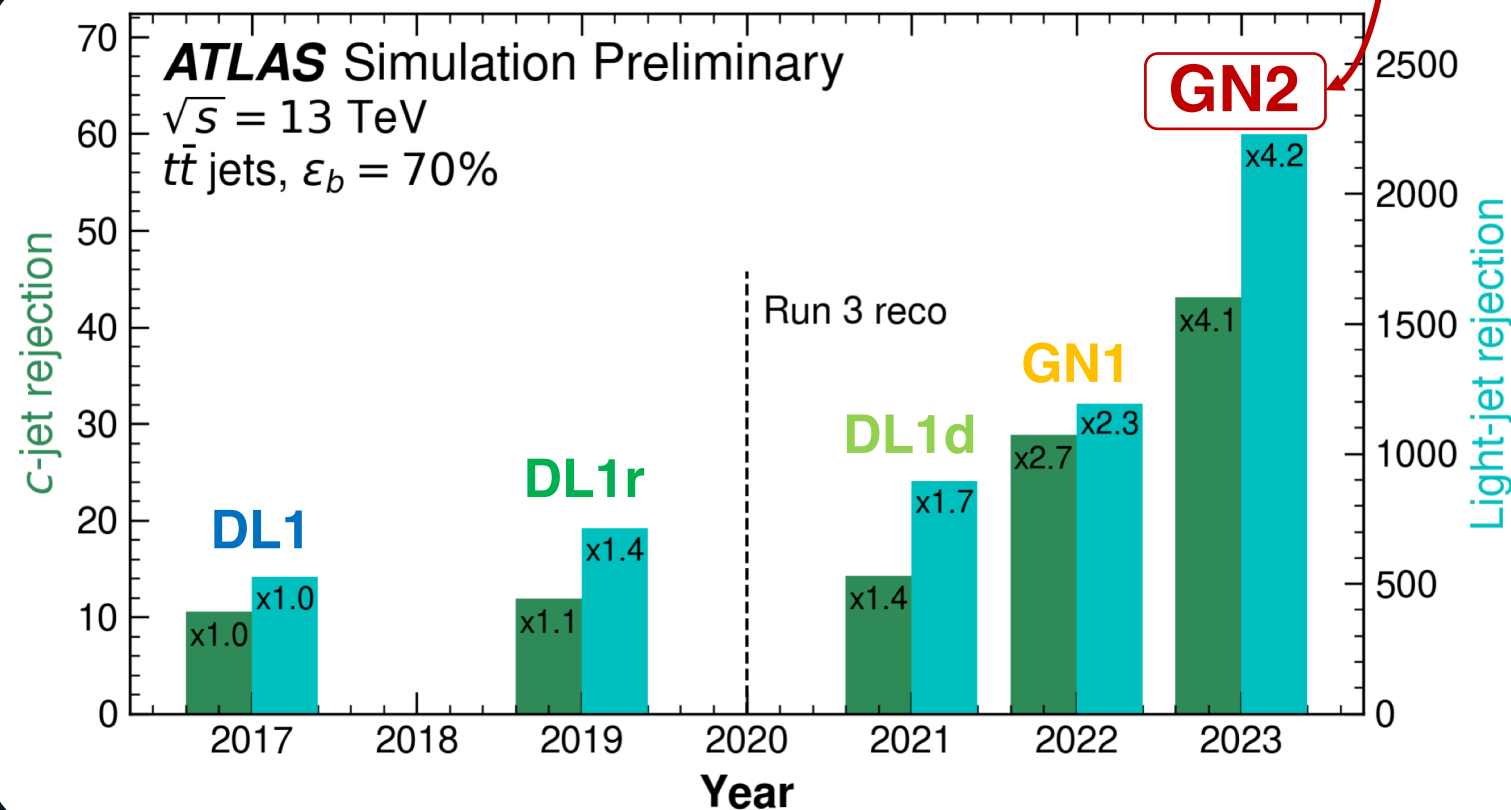
JET FLAVOUR TAGGING

CONTINUOUS EVOLUTION

→ BDT → Deep Network → RNN → DeepSet → Graph Attention → Transformer

Mission

Continuously improve the performance of the ATLAS tagger for $\{b, c, \text{light}^*, \tau^{**}\}$ jet discrimination



* *light* = u, d, s, gluon

** *hadronic τ decays resemble c -jets*

rejection = $1 / \text{miss-classification efficiency}$

JET FLAVOUR TAGGING

CONTINUOUS EVOLUTION

→ BDT → Deep Network → RNN → DeepSet → Graph Attention → **Transformer**

Inputs

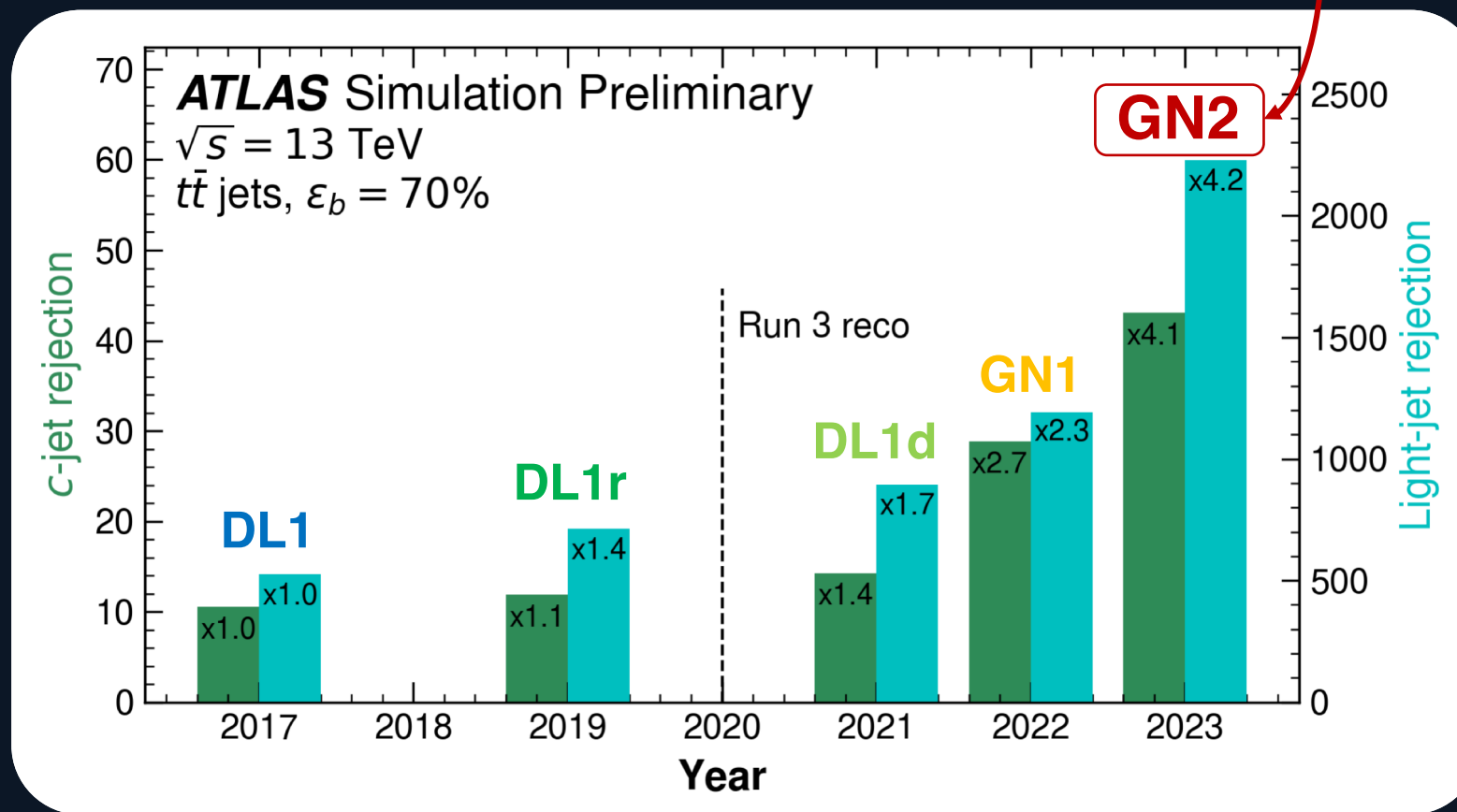
Tracks & jet

Outputs

Per-flavour*
probabilities
& discriminant

Trained on
simulated data
Calibrated on
real data

*{b, c, light, τ }



rejection = 1 / miss-classification efficiency

JET FLAVOUR TAGGING

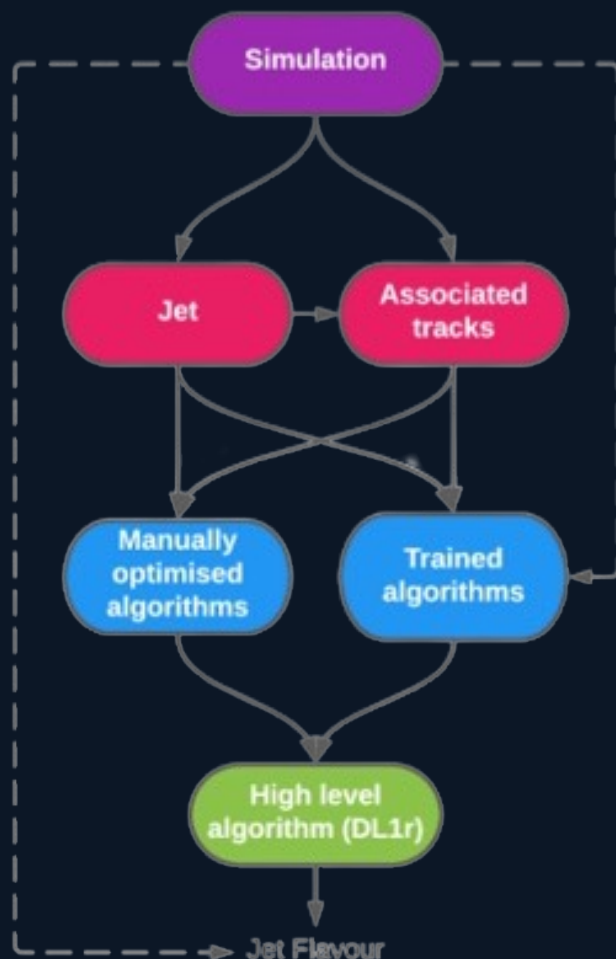
New design adopted by ATLAS for GN1 & GN2

DL1d

DL1r

Hierarchical

Many small submodels, cumbersome to maintain, limited use of Deep Learning

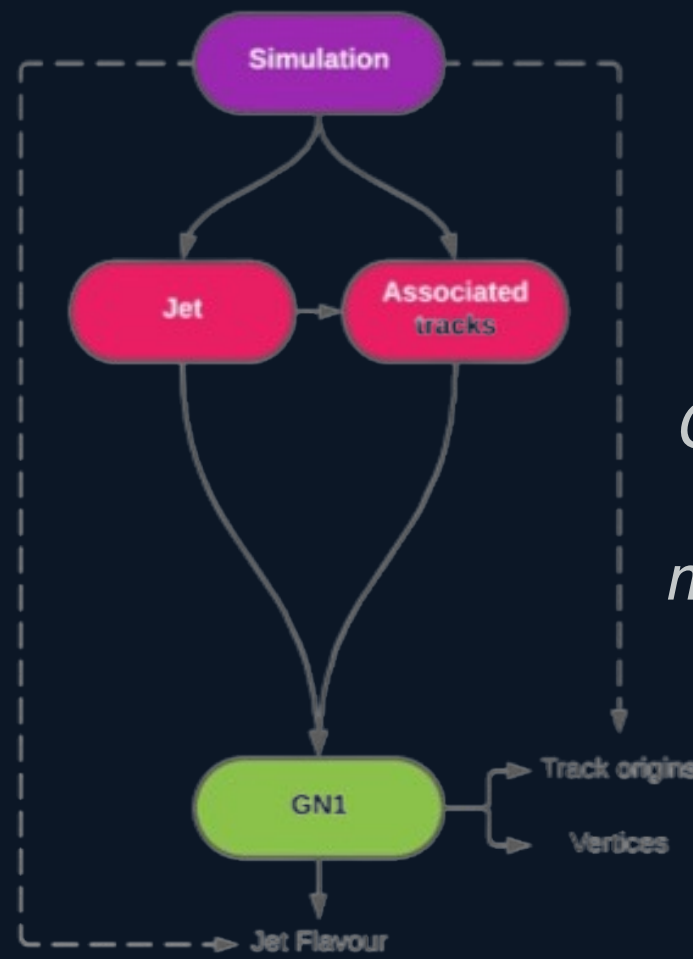


GN2

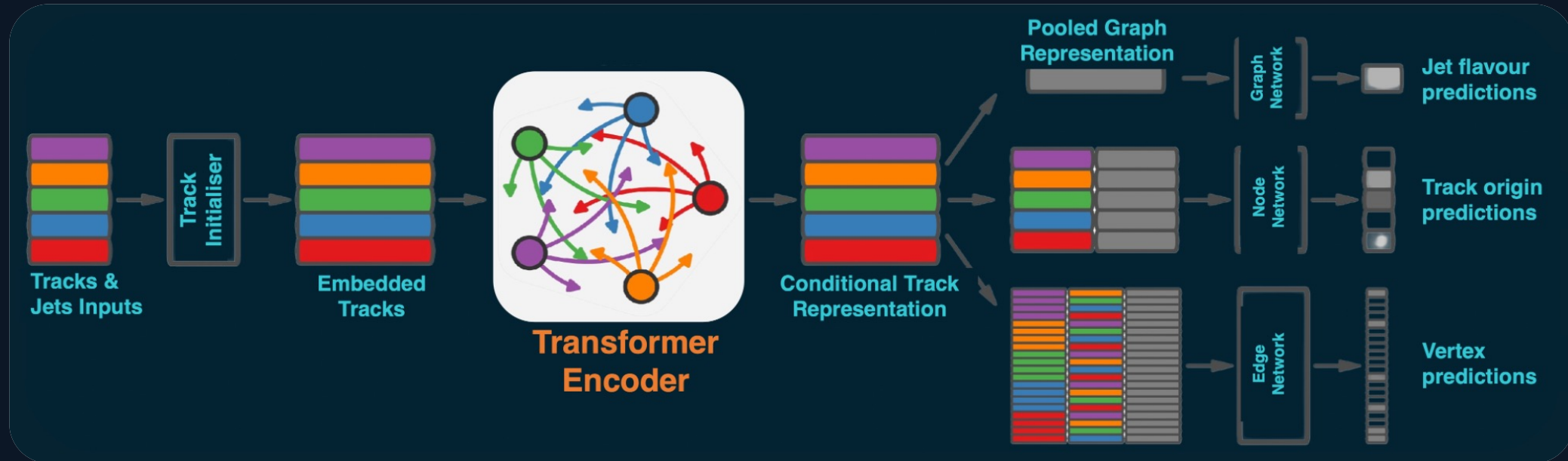
GN1

Integrated

One large network to rule them all, multitask, multimodal, agile and easy to update, fully leveraging Deep Learning



Large Multimodal Multitask Transformer Model



Multimodal

Combines **multiple** physics input types

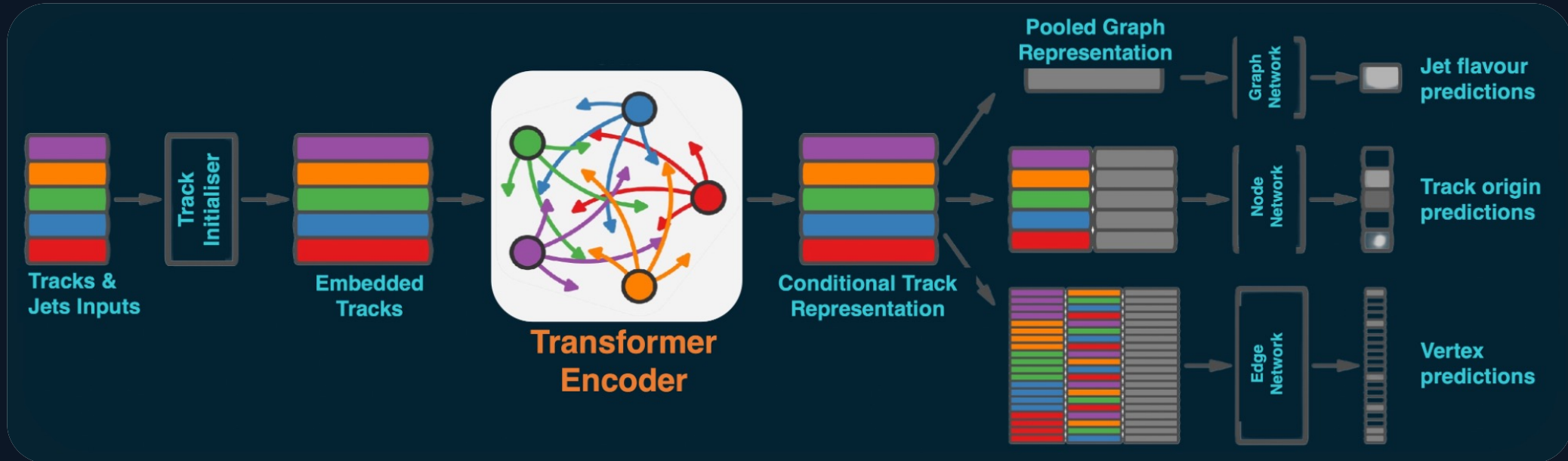
Architecture

Single network with **SOTA** performance

Multitask

Per-flavour probabilities + **auxiliary objectives**

Large Multimodal Multitask Transformer Model



DL1d — 130k parameters

“Large”

GN1 — 800k parameters

GN2 — 2600k parameters

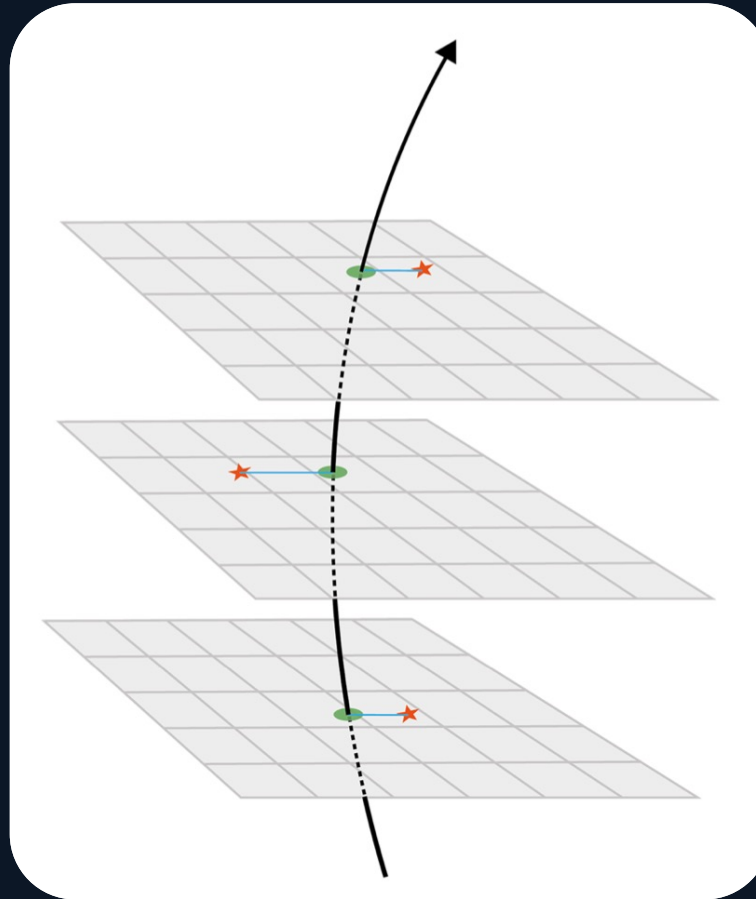
Multimodal Tracks + Jet Variables

Tracks

- Track parameters
- Uncertainties
- Impact parameters

Jet

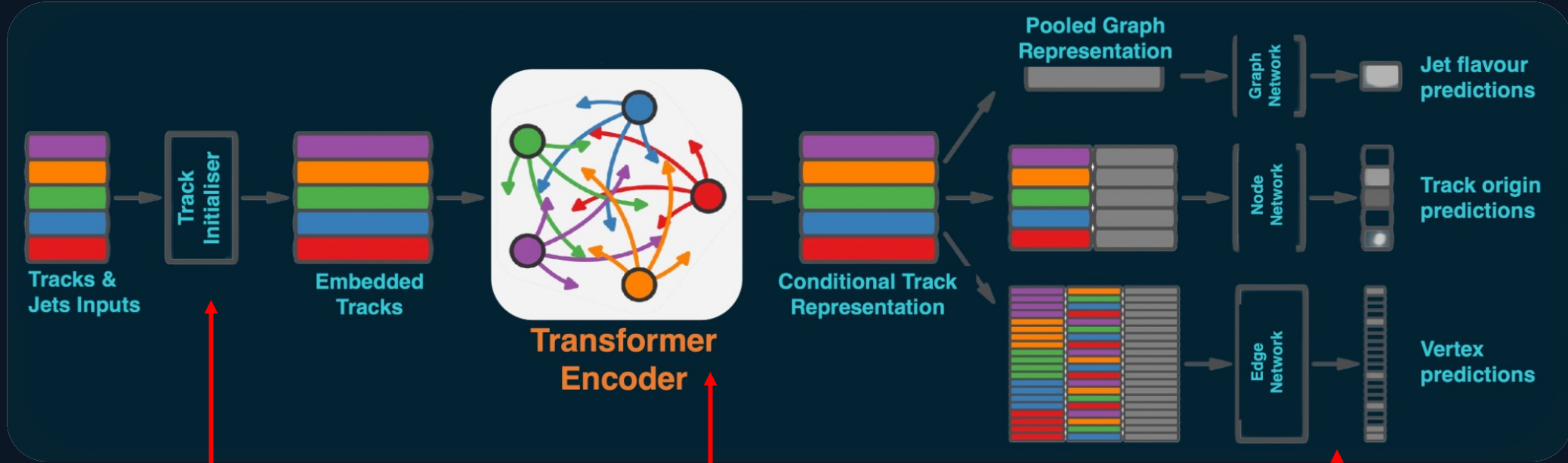
- p_T & η
- Resampled / flavour



192,000,000 simulated
jets for training

↑
Thanks to new pre-
processing software
+
Stabilising architecture
choices:
Layer Normalisation
Dropout

GN2 Architecture

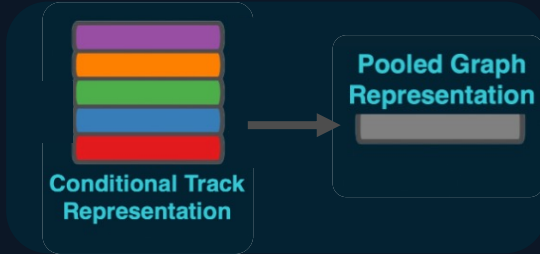


Neural network for combined representations embedding

Transformer Encoder for conditional track representation

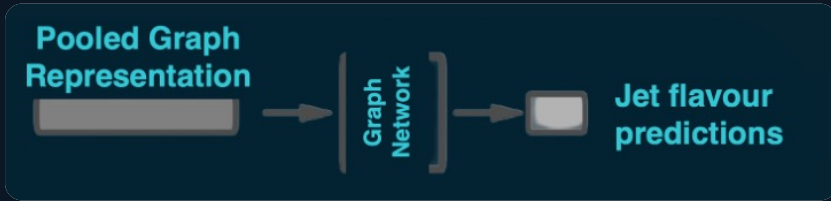
Auxiliary tasks for expert knowledge distillation

GN2 Loss



Global Attention Pooling

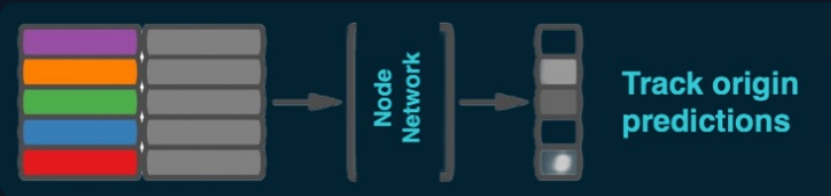
$$\mathcal{L}_{Total} = \mathcal{L}_{Jet} + \alpha \mathcal{L}_{Track} + \beta \mathcal{L}_{Vertex}$$



1 Predict jet flavour probabilities + tagging discriminant

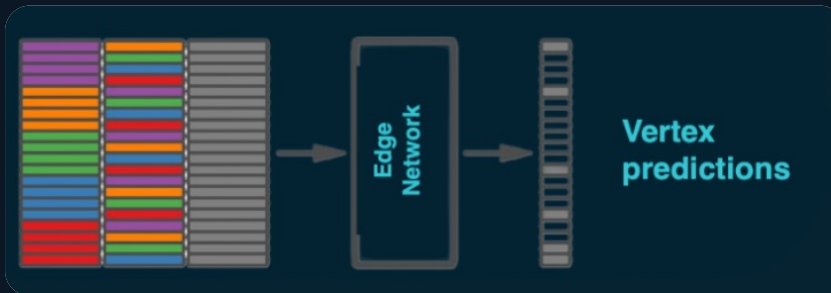
Model	f_c
DL1d	0.018
GN1	0.05
GN2	0.1

$$D_b = \frac{p_b}{f_c p_c + (1 - f_c) p_{light}}$$



2 Predict origin process of each track

Truth Origin	Description
Pileup	From a pp collision other than the primary interaction
Fake	Created from the hits of multiple particles
Primary	Does not originate from any secondary decay
fromB	From the decay of a b -hadron
fromBC	From a c -hadron decay, which itself is from the decay of a b -hadron
fromC	From the decay of a c -hadron
OtherSecondary	From other secondary interactions and decays



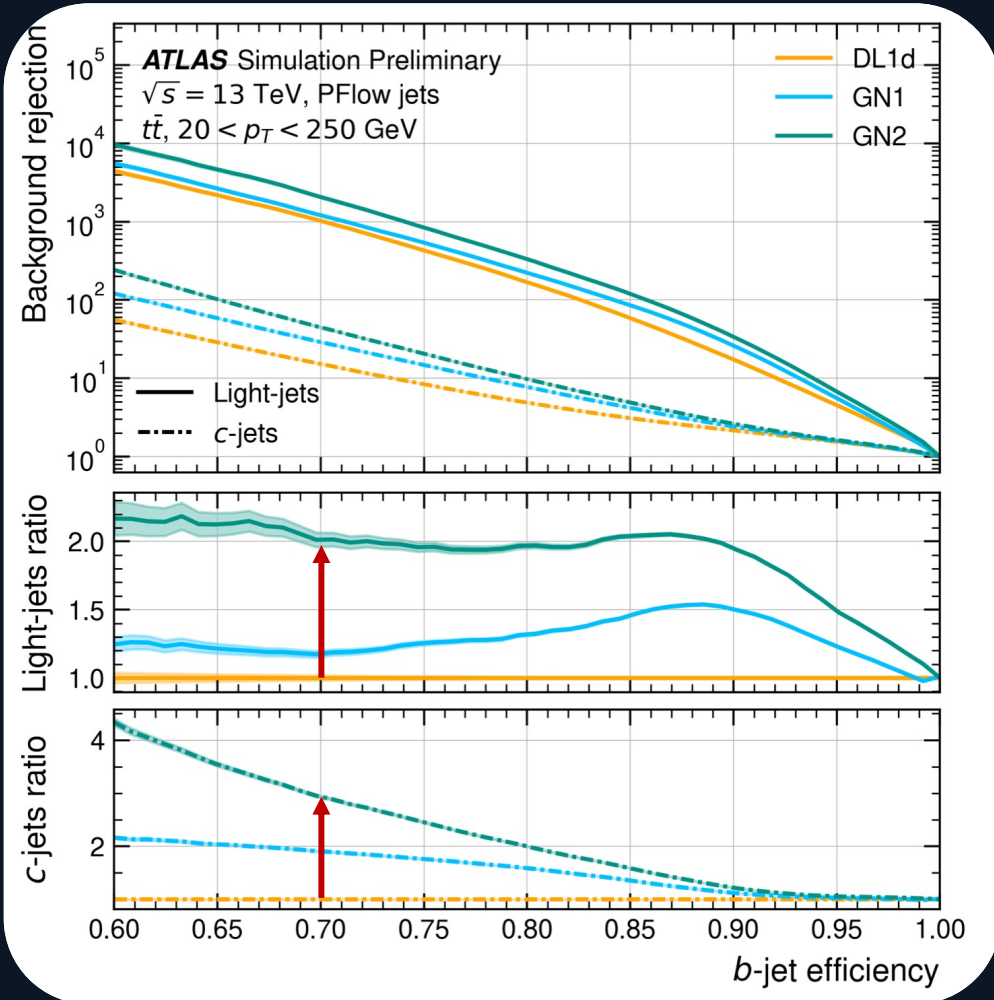
3 Predict track-pairs vertex compatibility

Significant improvement with GN2

Low p_T
($t\bar{t}$)
70* b-eff

Light-rej
x2

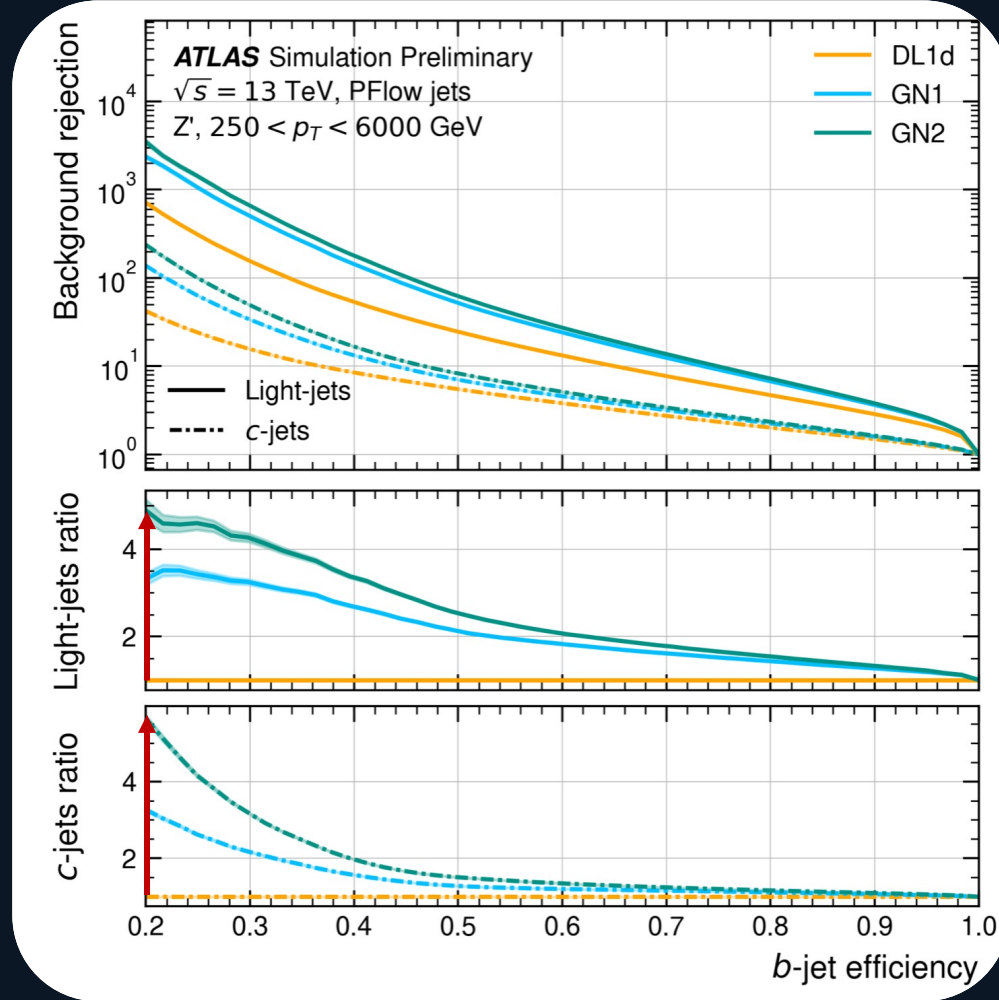
c-rej
x2.8



High p_T
(Z')
20* b-eff

Light-rej
x4.8

c-rej
x5.5



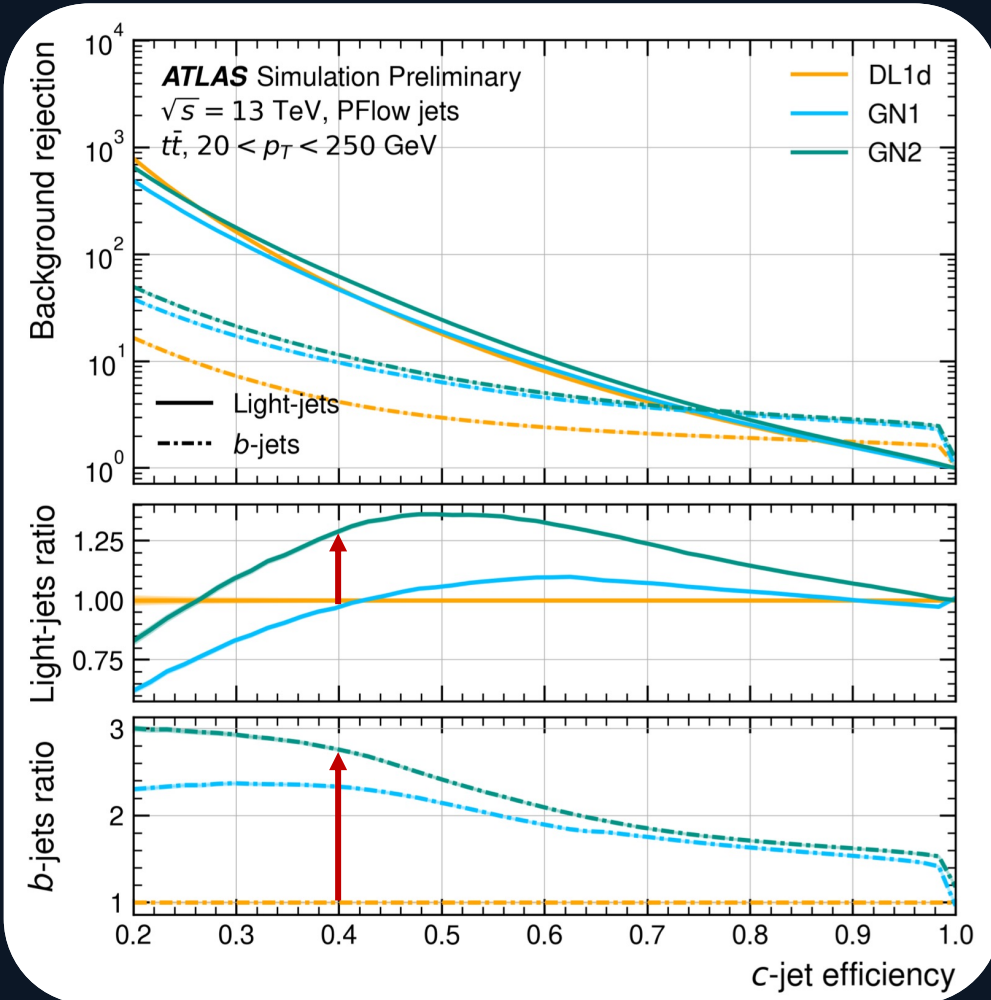
Left working point corresponds to right one

Significant improvement with GN2

Low p_T
($t\bar{t}$)
40* c-eff

Light-rej
x1.3

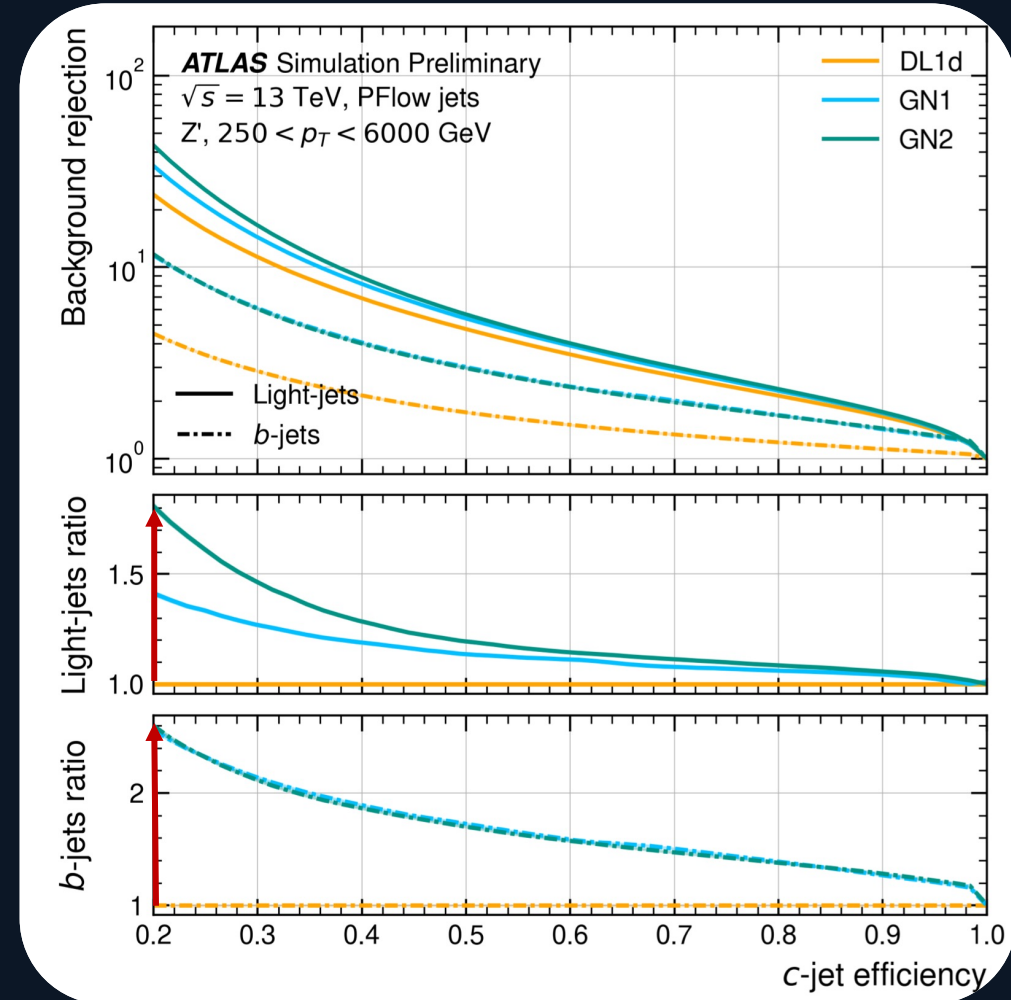
c-rej
x2.7



High p_T
(Z')
20* c-eff

Light-rej
x1.8

c-rej
x2.6



Left working point corresponds to right one

GN2 *Aftermath*

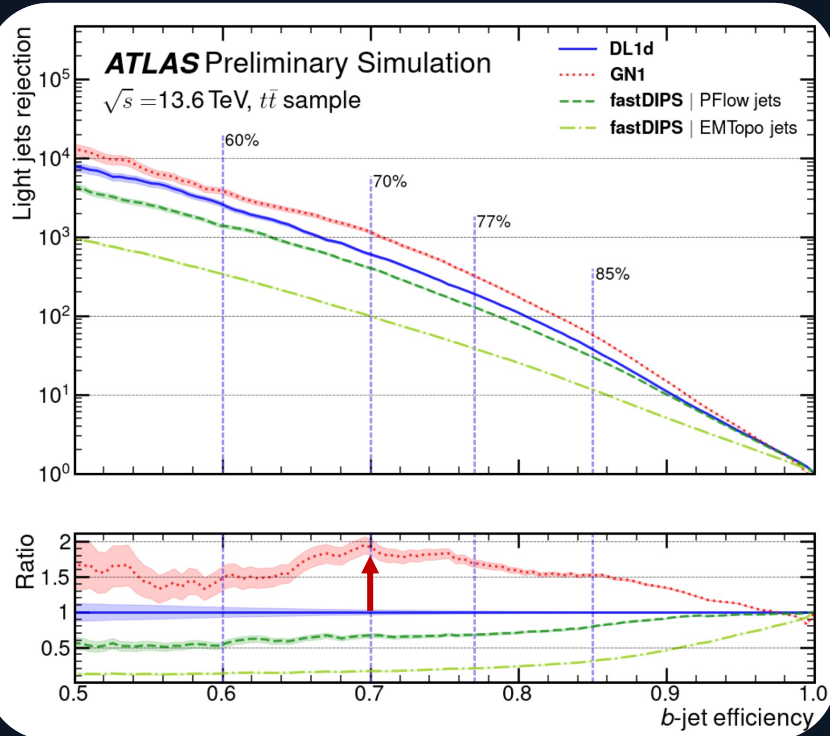
GN models bring a remarkable improvement to ATLAS

Quickly Proliferating

Boosted $X \rightarrow b\bar{b} / c\bar{c}$

Inference time (ms)

	$t\bar{t}$	Z'
DL1d	0.07	0.08
GN1	0.40	0.78

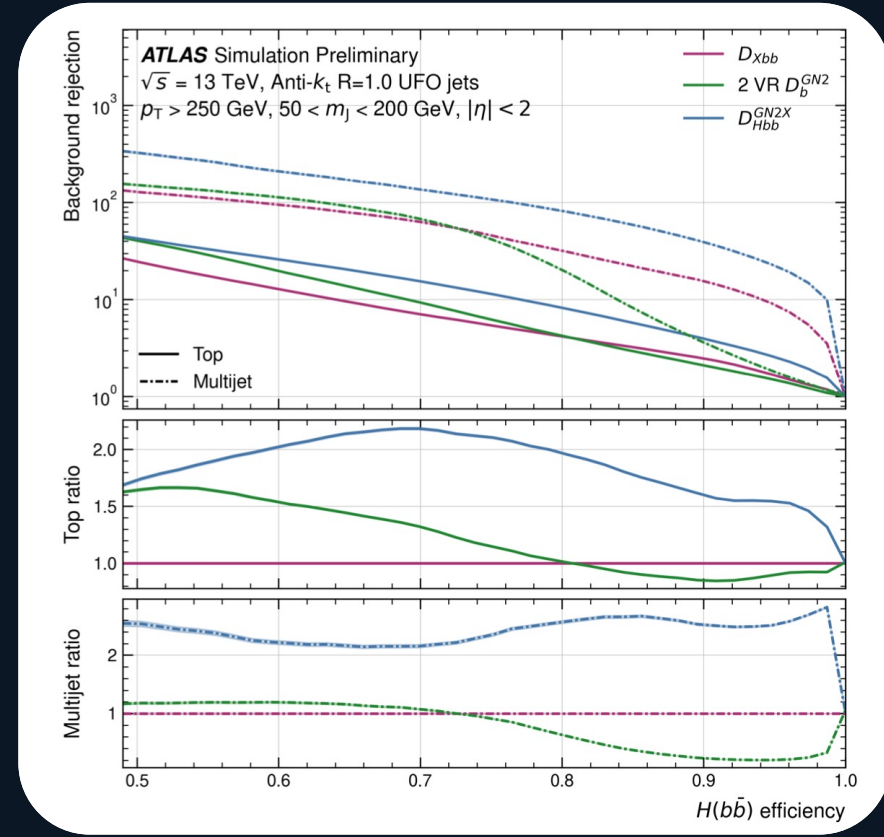


TRIGGERS

For Higgs tagging

Top-rej

Multi-jet-rej

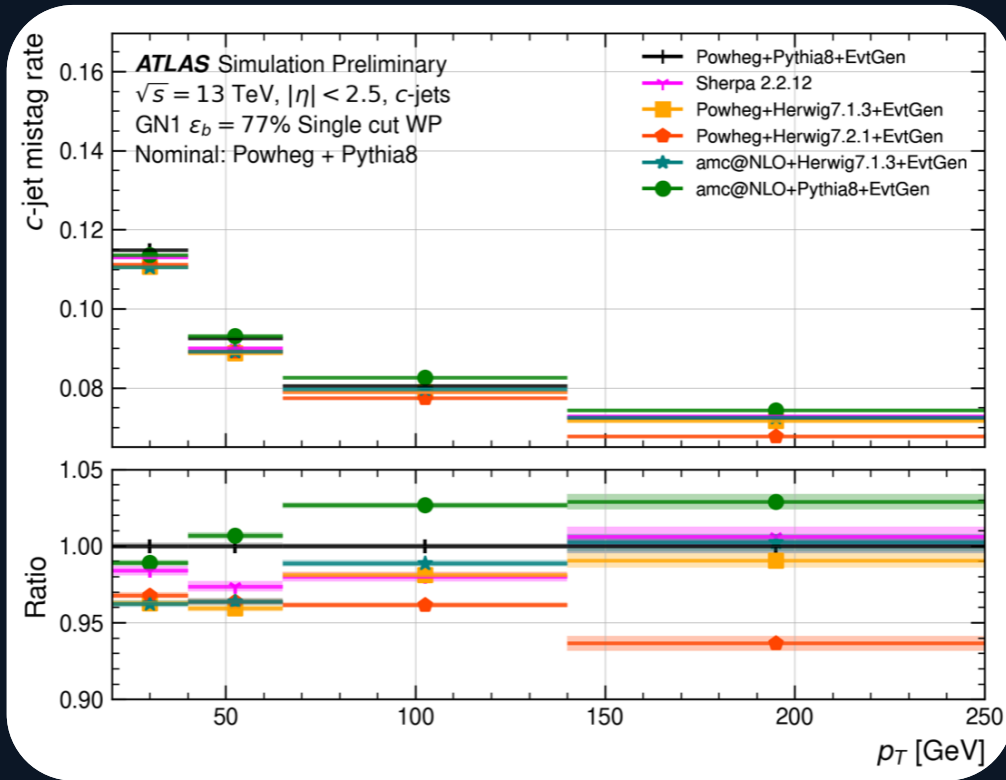


GN2X



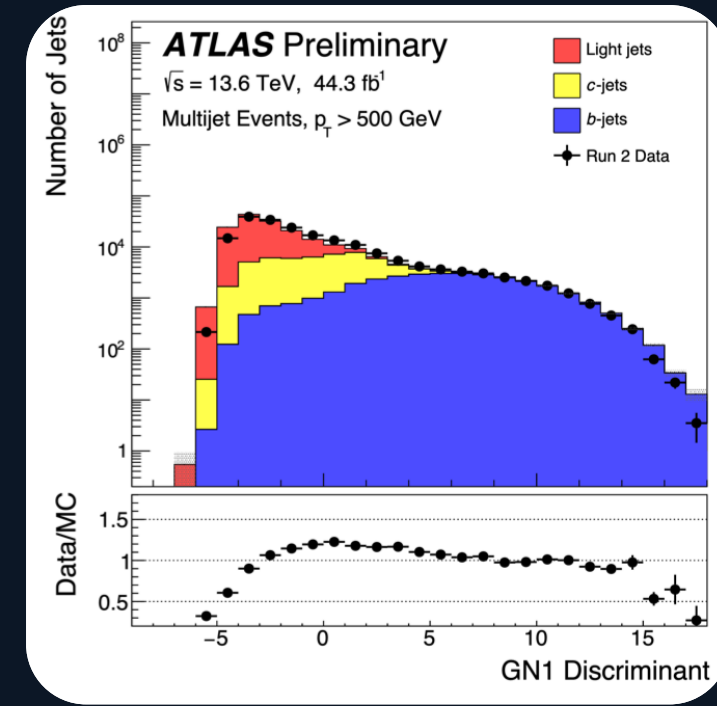
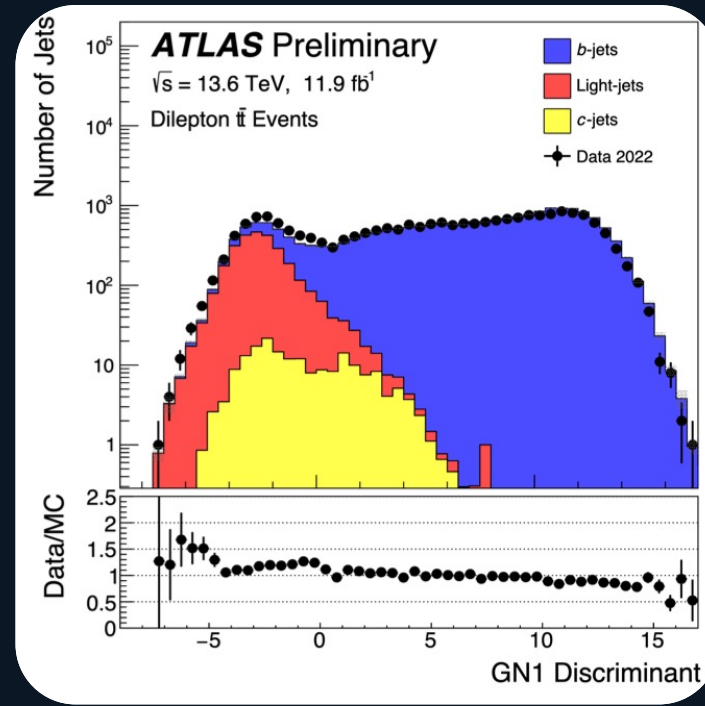
+ HL-LHC forecast, application to other part of the Collaboration, ...

MC Dependence



✓ Overall generator dependence $\sim O(3-6\%)$

Data / MC Agreement



✓ Good agreement in the bulk

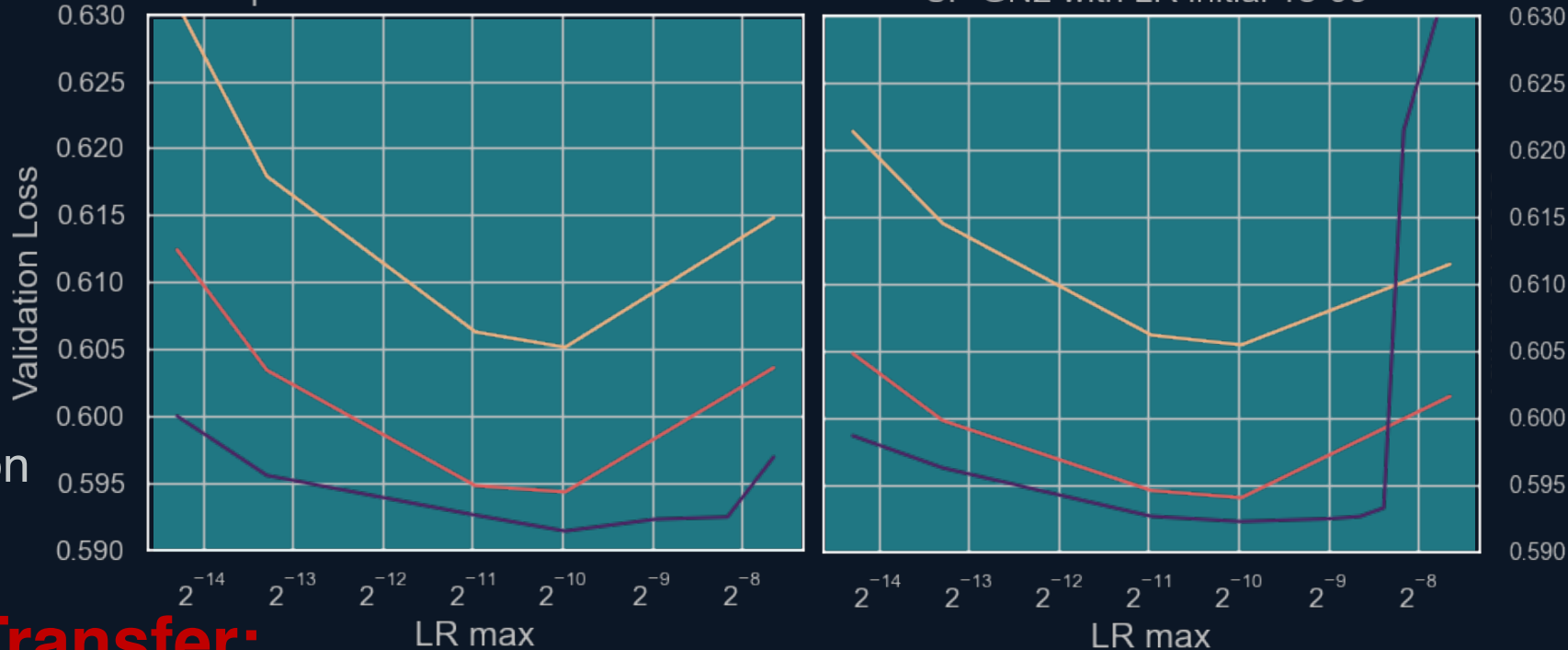
GN models bring a remarkable improvement to ATLAS Ongoing Hyperparameters Tuning

Embedding Width

- 64
- 128
- 256

ATLAS Simulation Preliminary,
μP GN2 with LR initial 1e-05

ATLAS Simulation Preliminary,
SP GN2 with LR initial 1e-05



μP
Maximal Update Parametrisation

SP
Standard Parametrisation (LeCun)

μTransfer:

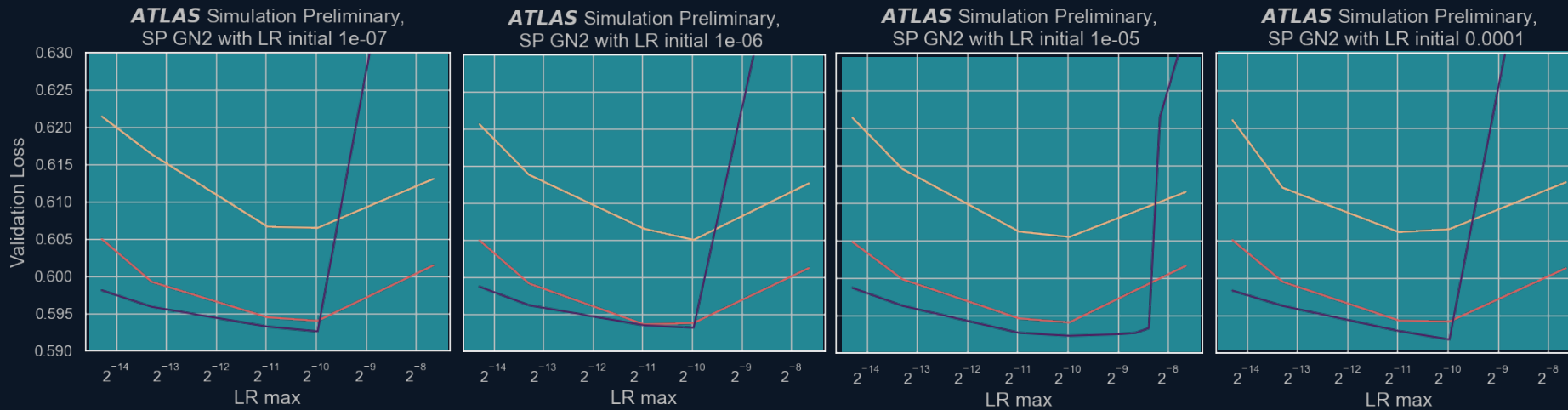
- HPO on the smaller model → faster training → better coverage
- Zero-shot transfer: best HP small model = best HP large model



Real Deployment

LR Scheduler Optimisation: LR Max per LR Initial

SP

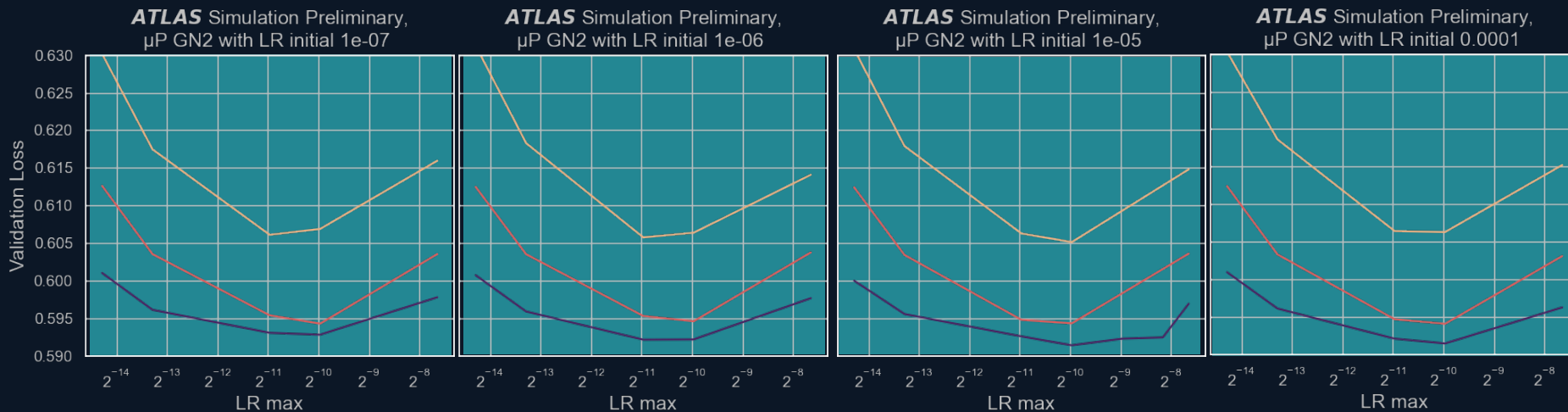


Embedding Width

- 64
- 128
- 256

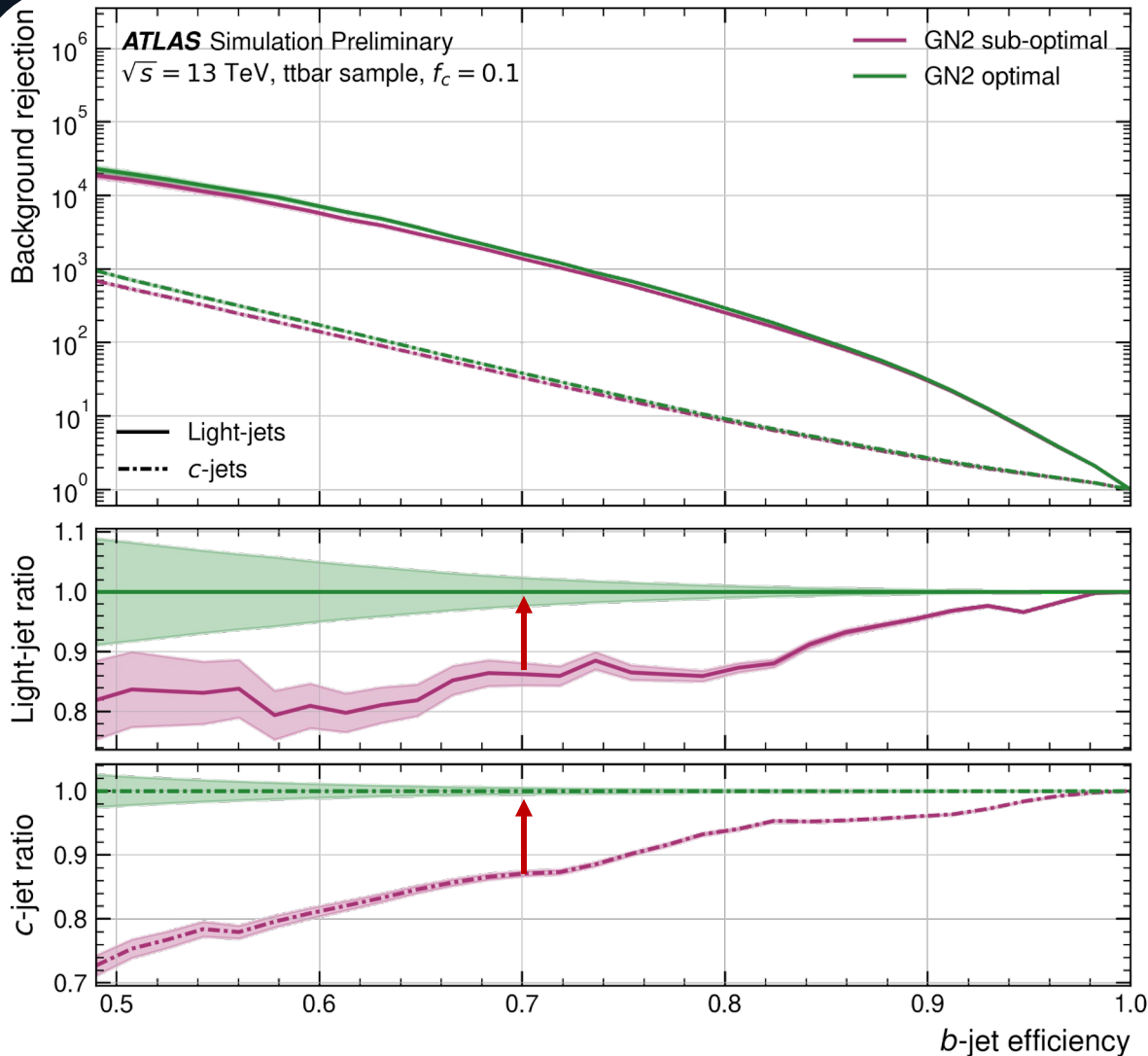
- ❖ Some SP trainings unstable
- ❖ No guarantee optimum shared across width

μP



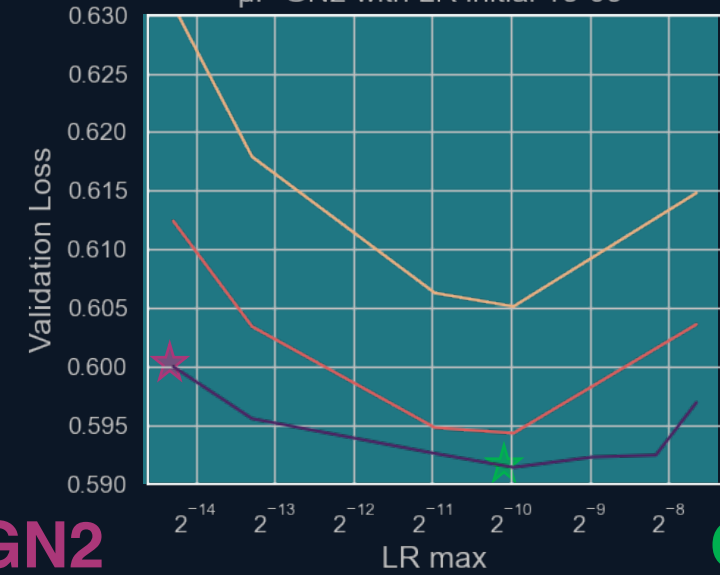
- ✓ μP trainings always stable
- ✓ Guaranteed shared optimum for sufficient width

HPO matters ...



ROC curves on $t\bar{t}$

ATLAS Simulation Preliminary,
 μ P GN2 with LR initial $1e-05$



GN2 Sub-optimal **GN2 Optimal**

Significant performance dependency on HP

$$D_b = \frac{p_b}{f_c p_c + (1 - f_c) p_{light}}$$



Vassily Kandinsky, *Several Circles*, 1926



**Thank you
for your attention!**

19th July 2024

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Vassily Kandinsky, *Several Circles*, 1926



René Magritte – *Le Retour*

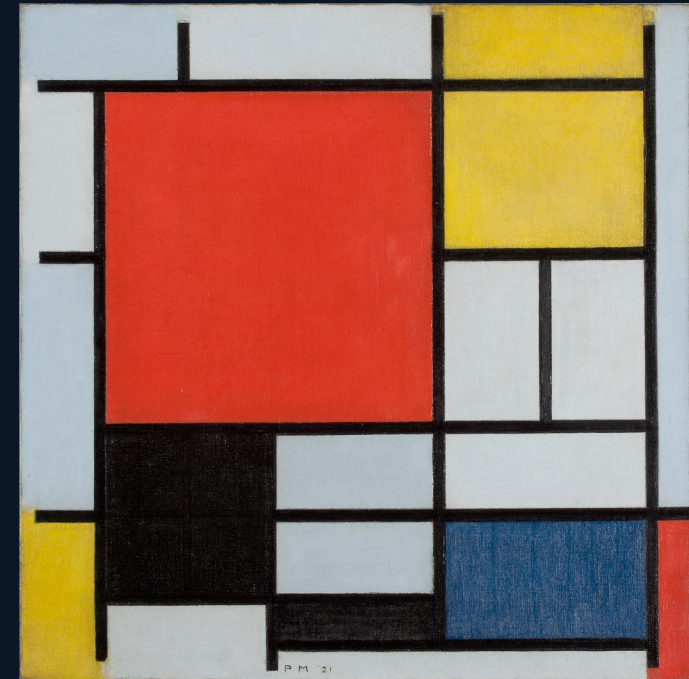


Monet – *Les Coquelicots*

B
A
C
K
U
P



René Magritte – *Souvenir de Voyage*



Piet Mondriaan
– *Composition with Red, Yellow, and Blue*

Jet Input	Description
p_T	Jet transverse momentum
η	Signed jet pseudorapidity
Track Input	Description
q/p	Track charge divided by momentum (measure of curvature)
$d\eta$	Pseudorapidity of the track, relative to the jet η
$d\phi$	Azimuthal angle of the track, relative to the jet ϕ
d_0	Closest distance from the track to the PV in the longitudinal plane
$z_0 \sin \theta$	Closest distance from the track to the PV in the transverse plane
$\sigma(q/p)$	Uncertainty on q/p
$\sigma(\theta)$	Uncertainty on track polar angle θ
$\sigma(\phi)$	Uncertainty on track azimuthal angle ϕ
$s(d_0)$	Lifetime signed transverse IP significance
$s(z_0)$	Lifetime signed longitudinal IP significance
nPixHits	Number of pixel hits
nSCTHits	Number of SCT hits
nIBLHits	Number of IBL hits
nBLHits	Number of B-layer hits
nIBLShared	Number of shared IBL hits
nIBLSplit	Number of split IBL hits
nPixShared	Number of shared pixel hits
nPixSplit	Number of split pixel hits
nSCTShared	Number of shared SCT hits
nPixHoles	Number of pixel holes
nSCTHoles	Number of SCT holes
leptonID	Indicates if track was used in the reconstruction of an electron or muon (only for GN1 Lep)

GN2 *Track Selection*

Parameter	Selection
p_T	> 500 MeV
$ d_0 $	< 3.5 mm
$ z_0 \sin \theta $	< 5 mm
Silicon hits	≥ 8
Shared silicon hits	< 2
Silicon holes	< 3
Pixel holes	< 2

“Quality selections applied to tracks, where d_0 is the transverse IP of the track, z_0 is the longitudinal IP with respect to the PV and θ is the track polar angle. Shared hits are hits used on multiple tracks which have not been classified as split by the cluster-splitting neural networks. Shared hits on pixel layers are given a weight of 1, while shared hits in the SCT are given a weight of 0.5. A hole is a missing hit, where one is expected, on a layer between two other hits on a track”.

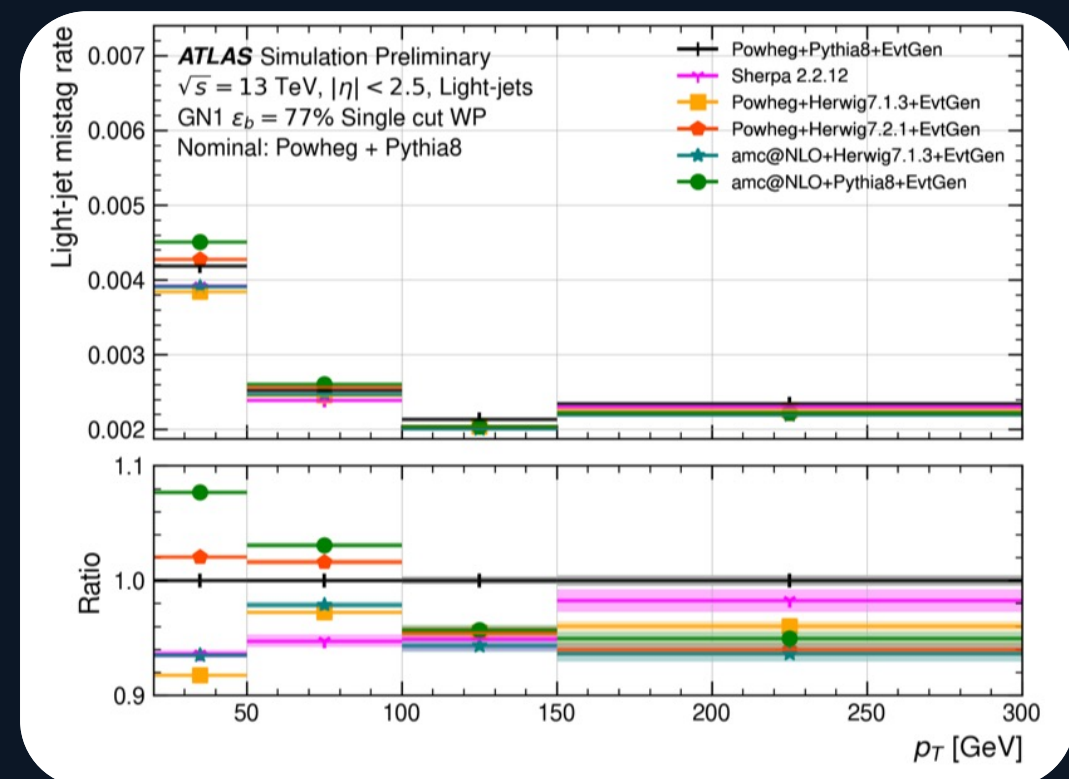
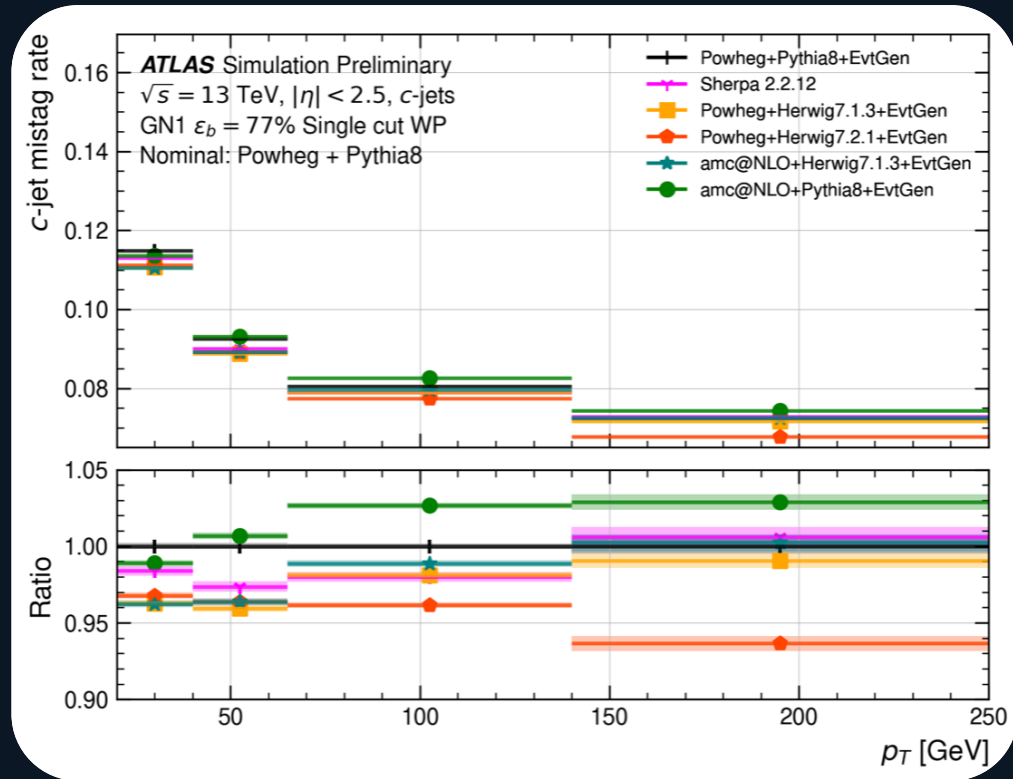
ATLAS GNN



GN2 MC Dependency

C-jets

Light-jets

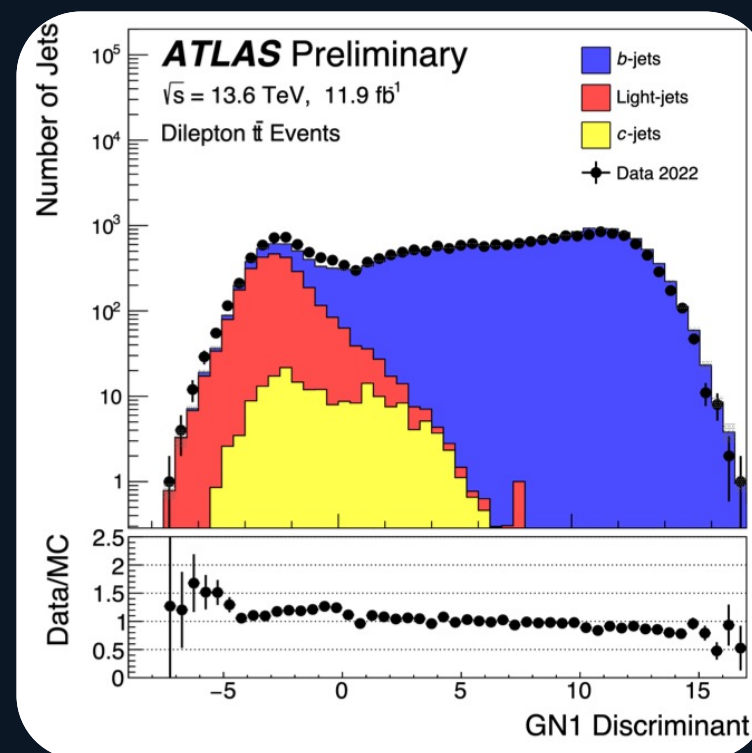
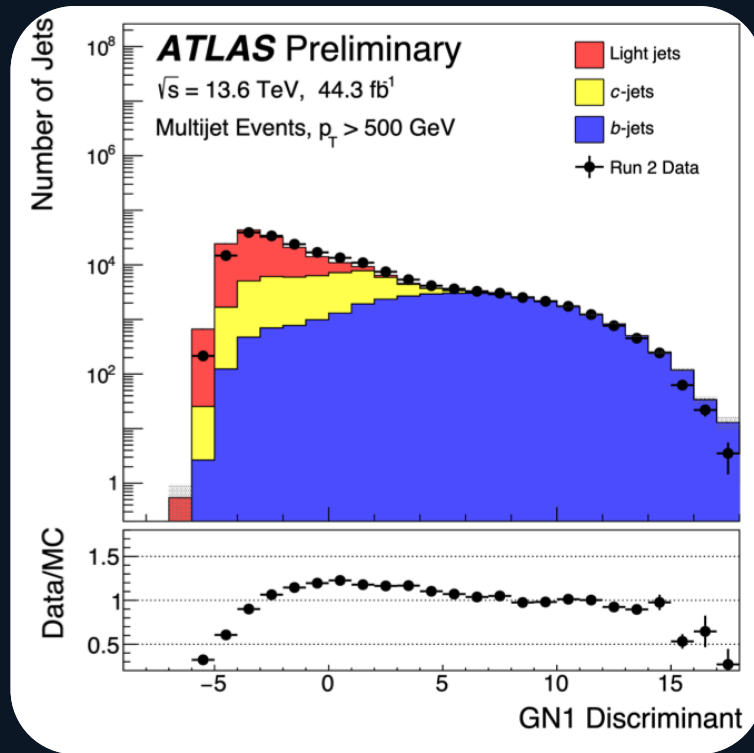


- “Tag and probe” event selection: tag jet must pass 85% b-eff
- Simulations are scaled to match the total yield in data

Tag jet pass
85% b-eff

$p_T > 200$
GeV

Event
 $p_T > 500$
GeV



- 2-lepton 2-jet selection, 1 lepton trigger
- Opposite sign electron and muon
- Invariant mass of each lepton-jet pair < 175 GeV
- Tagger discriminant for leading jet

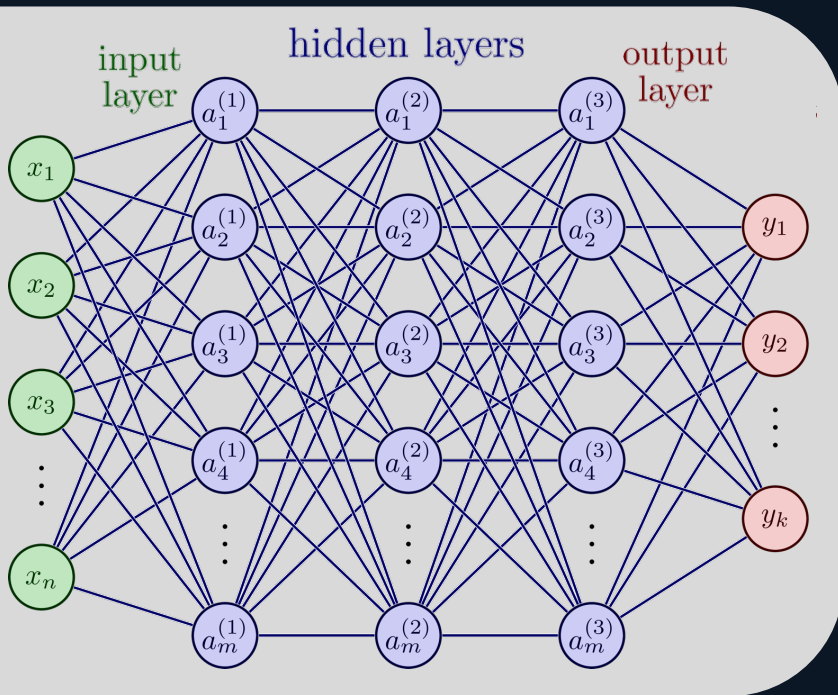
Maximal Update Parametrization

What if we could do HPO on a smaller model instead?

PARAMETRIZATION MATTERS!

➤ Standard Parametrization* (SP)

➤ Maximal Update Parametrization (μ P)



$$d_{L_{in}}^{in} = n \quad d_{L_{hid}}^{in} = m \quad d_{L_{out}}^{in} = m$$

$$w^{L_{in}} \sim \mathcal{N}\left(0, \frac{1}{d_{L_{in}}^{in}}\right)$$

$$w^{L_{hid}} \sim \mathcal{N}\left(0, \frac{1}{d_{L_{hid}}^{in}}\right)$$

$$w^{L_{out}} \sim \mathcal{N}\left(0, \frac{1}{d_{L_{out}}^{in}}\right)$$

$$b^{L_{...}} = 0$$

$$w^{L_{in}} \sim \mathcal{N}\left(0, \frac{1}{d_{L_{in}}^{in}}\right)$$

$$w^{L_{hid}} \sim \mathcal{N}\left(0, \frac{1}{d_{L_{hid}}^{in}}\right)$$

$$w^{L_{out}} \sim \mathcal{N}\left(0, \frac{1}{d_{L_{out}}^{in} \times d_{L_{out}}^{in}}\right)$$

$$b^{L_{...}} = 0$$

INITIALISATION

\forall weights η

$$\eta_{w_{L_{in}}} = \eta$$

$$\eta_{w_{L_{hid}}} = \eta / d_{L_{hid}}^{in}$$

$$\eta_{w_{L_{out}}} = \eta / d_{L_{out}}^{in}$$

LR
Adam

*LeCun et al; 1998

With attention scale $1 / d^{in}$ instead $1 / \sqrt{d^{in}}$

Maximal Update Parametrization

“Effect of **updates** on activations becomes roughly **independent of width**”

“Each **weight matrix** is **maximally updated** without blowing up”

μ Transfer



$$f(x) = V^T U x \text{ with } x \in \mathbb{R} \text{ \& } V^T, U \in \mathbb{R}^{n \times 1}$$

μ P



SP

$$V_i \sim \mathcal{N}\left(0, \frac{1}{n}\right) \quad U_i \sim \mathcal{N}(0, 1)$$

$$V' \leftarrow V + \theta U \quad U' \leftarrow U + \theta V$$

$$f(x) \leftarrow (V^T U + \theta U^T U + \theta V^T V + \theta^2 U^T V) x$$

By LLN* $\Theta(n)$... blows up

μ P

$$V_i \sim \mathcal{N}\left(0, \frac{1}{n^2}\right) \quad U_i \sim \mathcal{N}(0, 1)$$

$$V' \leftarrow V + \frac{\theta}{n} U \quad U' \leftarrow U + \theta V$$

$$f(x) \leftarrow (V^T U + \frac{\theta}{n} U^T U + \theta V^T V + \frac{\theta^2}{n} U^T V) x$$

$\Theta(x)$... stable ✓

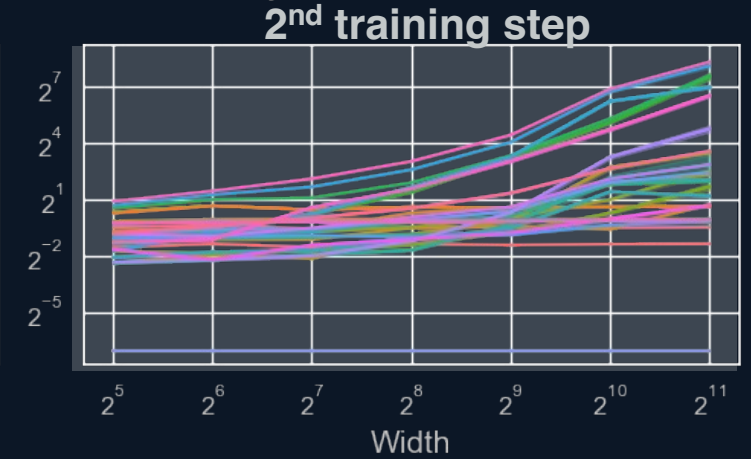
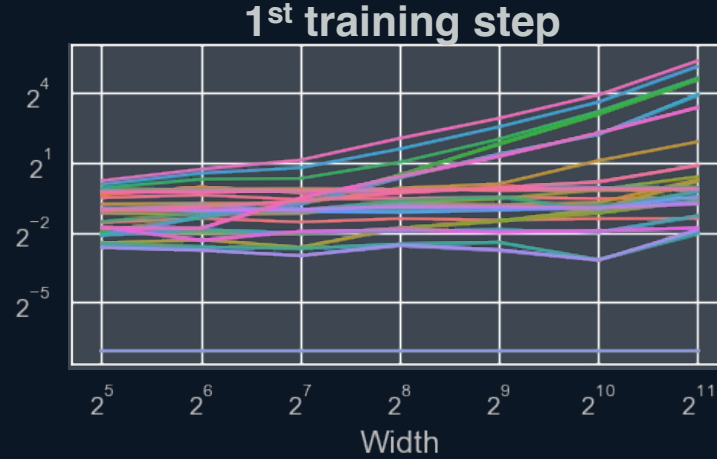
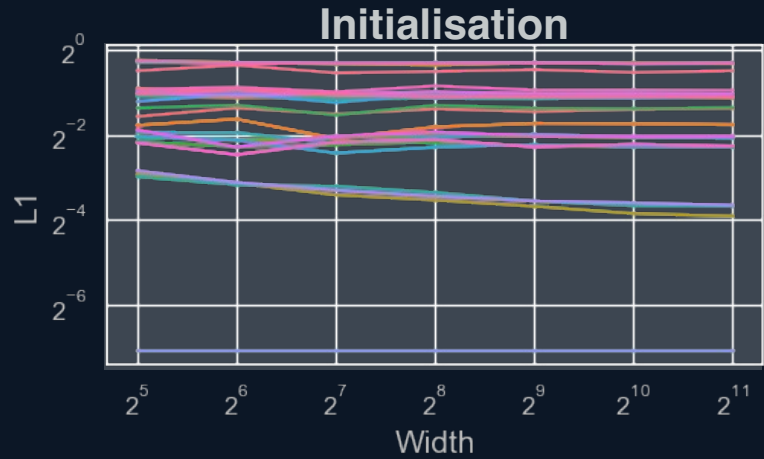
*Sum of n squared Gaussians of variance 1 is a Chi distribution of degree n

Maximal Update Parametrization

Pre-activation weights $L_1(m) = \sum |w_i^{(m)}|$

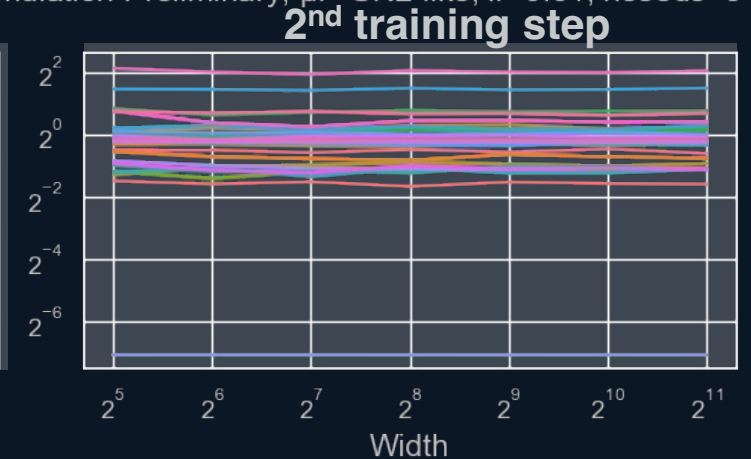
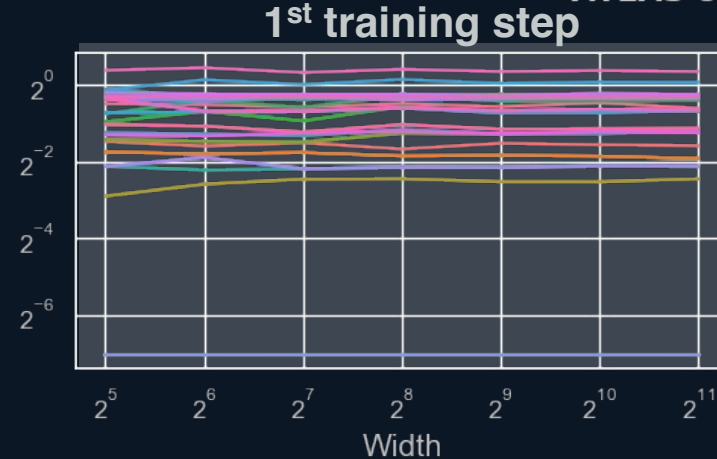
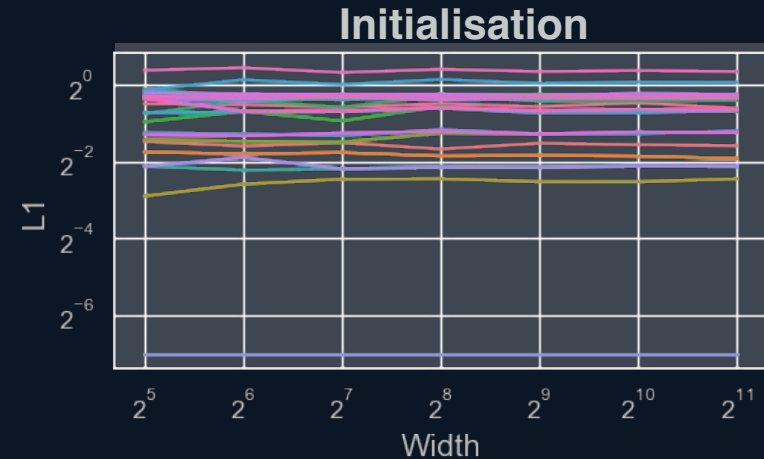
Blows up for SP, stable for μ P!

SP



ATLAS Simulation Preliminary, SP GN2-like, lr=0.01, nseeds=5

μ P



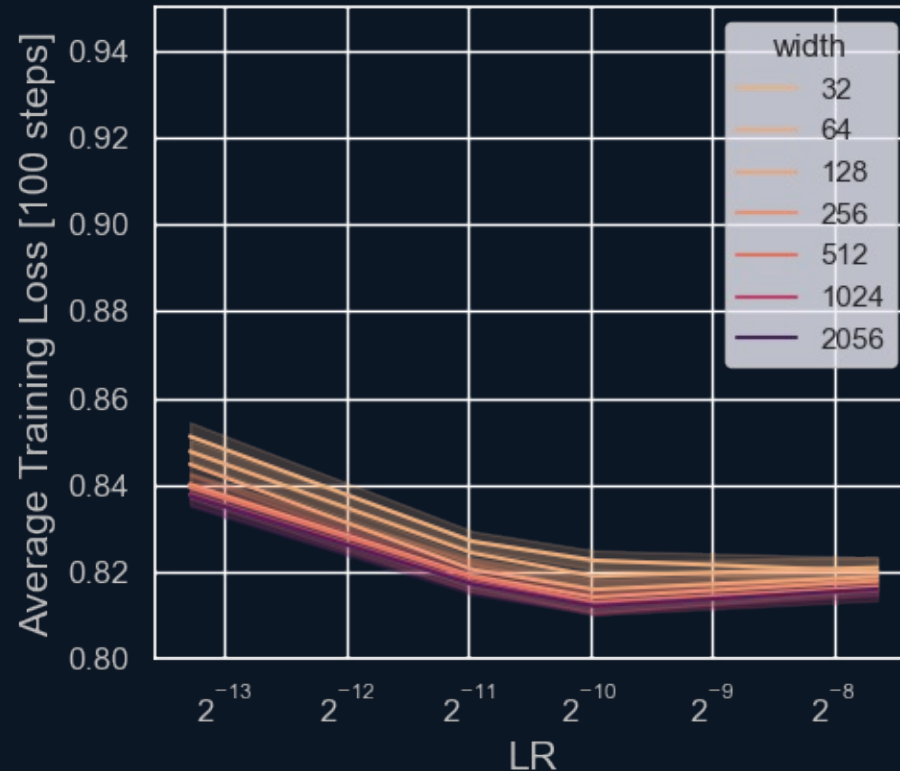
ATLAS Simulation Preliminary, μ P GN2-like, lr=0.01, nseeds=5

Pathologic Test Case

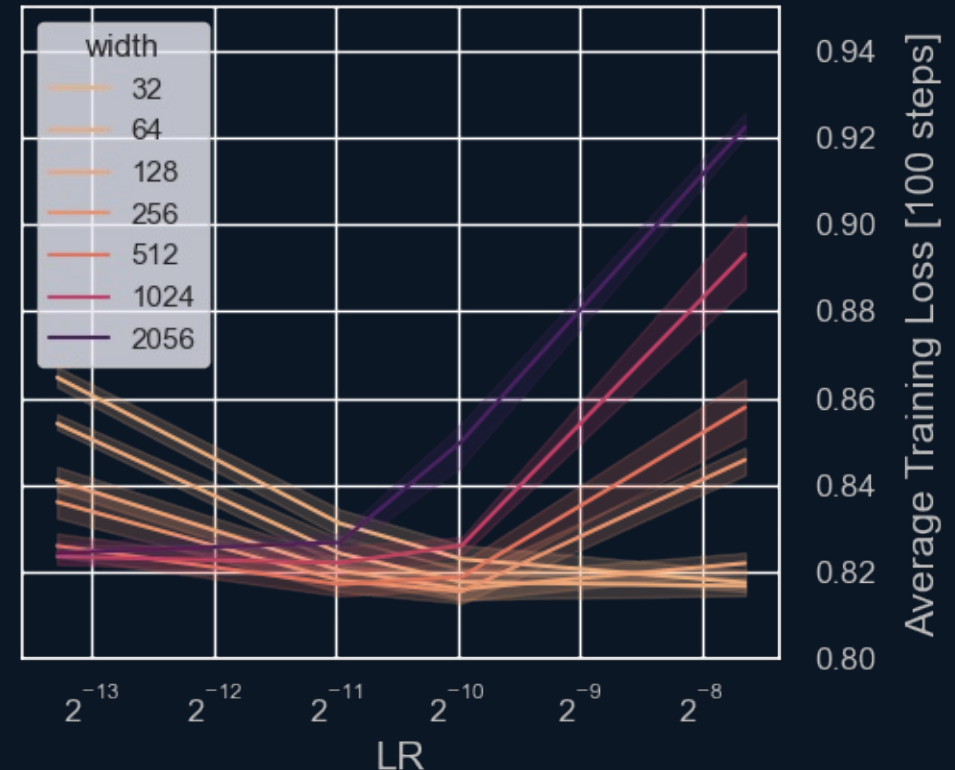
Fixed LR Value Optimisation on Simplified Architecture

ATLAS Simulation Preliminary, μ P GN2-like, nseeds=5 ATLAS Simulation Preliminary, SP GN2-like, nseeds=5

μ P



SP



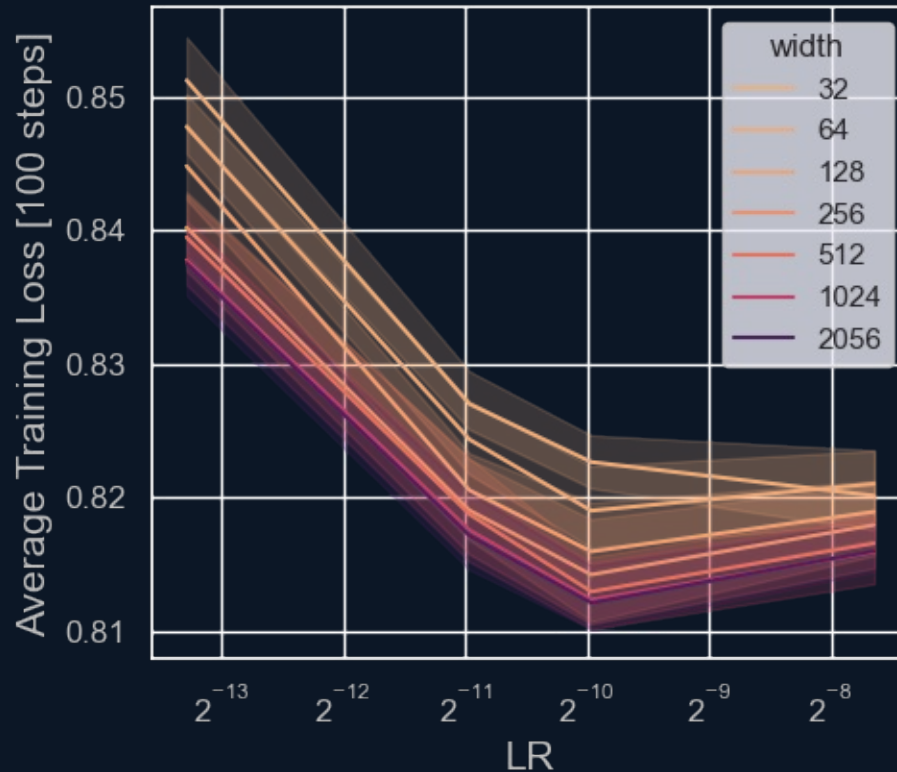
- ✓ μ P models share LR optimum across large widths differences
- ✓ Wider μ P models are better
- ✓ μ P models outperforms SP equivalent
- ✓ SP models do not share LR optimum at different widths

Pathologic Test Case

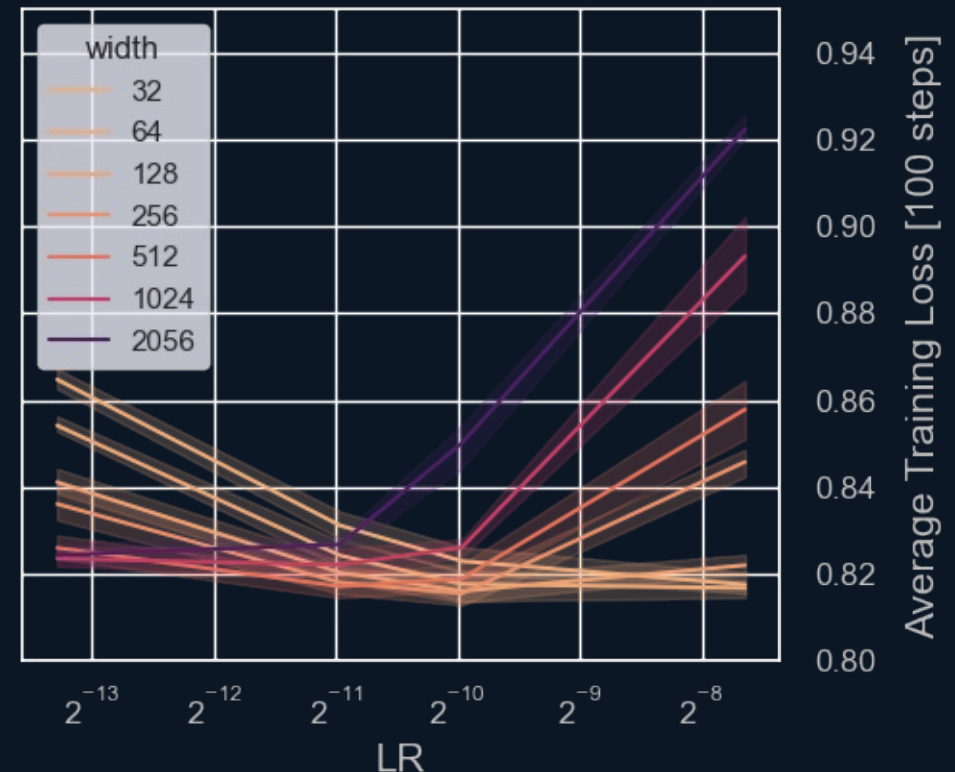
Fixed LR Value Optimisation on Simplified Architecture

ATLAS Simulation Preliminary, μ P GN2-like, nseeds=5 ATLAS Simulation Preliminary, SP GN2-like, nseeds=5

μ P



SP



- ✓ μ P models share LR optimum across large widths differences
- ✓ Wider μ P models are better
- ✓ μ P models outperforms SP equivalent
- ✓ SP models do not share LR optimum at different widths

- **Many variants under consideration (WIP):**
 - lepton,
 - more tracks,
 - hadronic taus,
 - neutral constituents
 - trackless b-tagging with hits
 - more output classes (taus, lep/had b, ...)
 - full vertex reconstruction,
 - mass / energy regression
- **Now training on combined MC data for Run3: ~ 300M jets**
- **Calibration & Trigger ongoing**
- **GN2X for boosted Higgs tagging (H(bb) & H(cc)) vs top and QCD**
- **Synergies with other groups: Tau tagging, emerging jet tagging, ...**