

Flavour and τ physics at the FCC-ee

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The University of Manchester

Topics

- The FCC-ee and the IDEA detector
- Phenomenology and detector requirements

- Focusing on:

- V_{cb} & V_{ub}

- $b \rightarrow s\tau^+\tau^-$

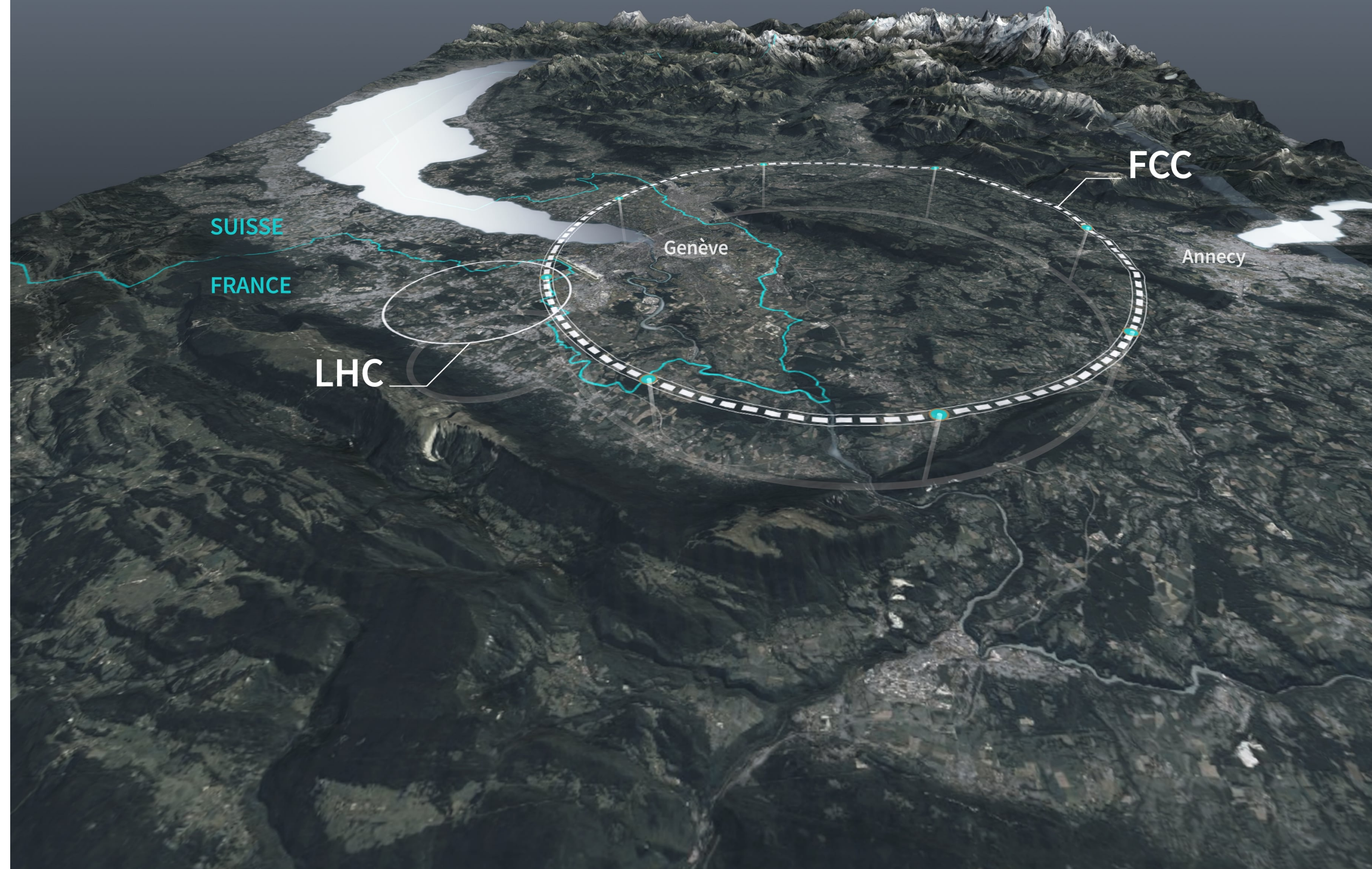
- $b \rightarrow s\nu\bar{\nu}$

- τ^\pm decays

} European Committee for Future Accelerators (ECFA) focus topics

The FCC-ee

- 91 km circumference
- 4 collision points
- 16 years operation
- Plan to operate at a number of energy levels; Z^0 -pole, W^+W^- , Z^0H , $t\bar{t}$
- I will primarily cover the latest Z^0 -pole prospects



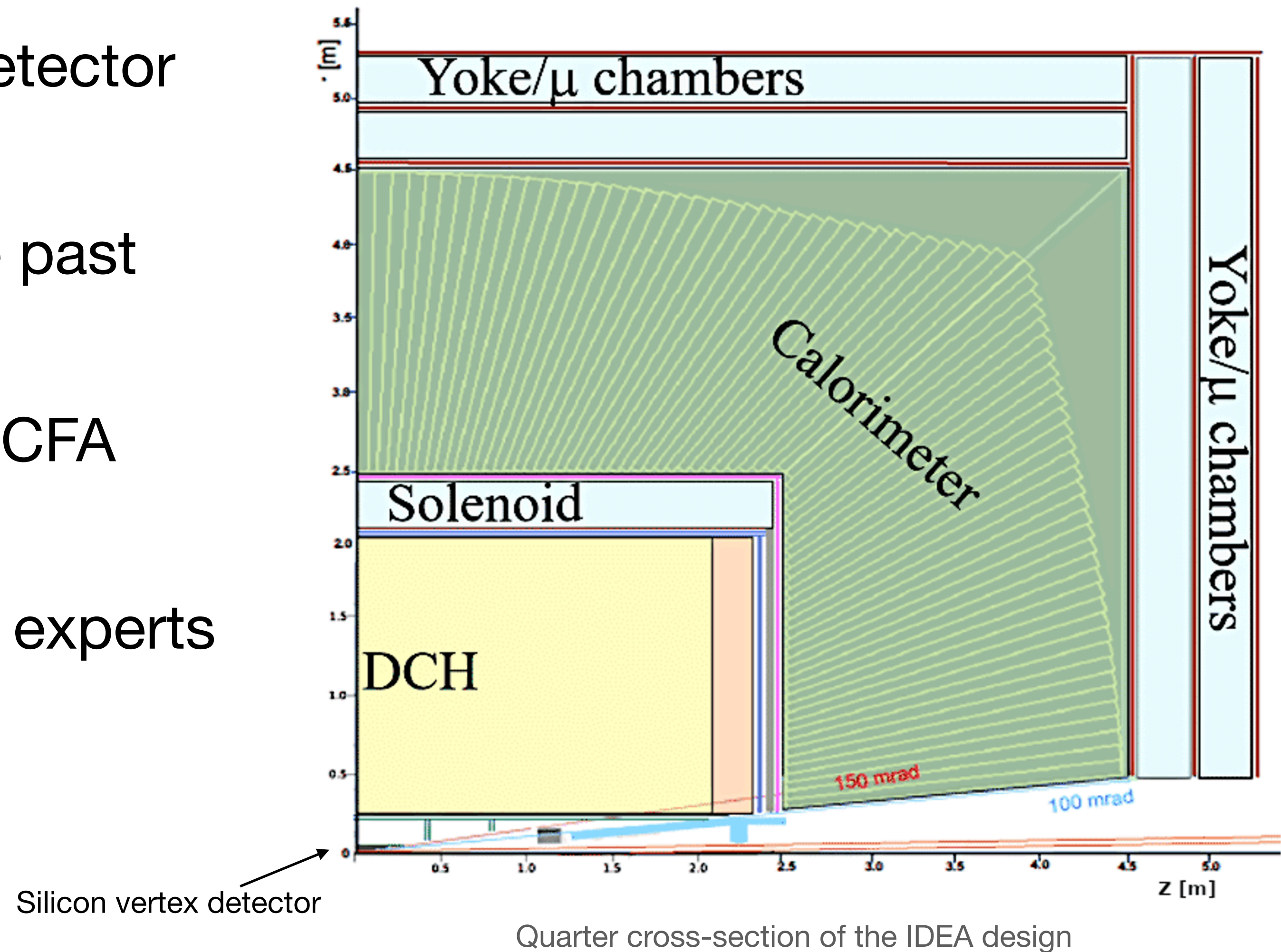
The FCC-ee

- Z^0 -pole run will deliver 6×10^{12} Z^0 s in total
 - “LEP in a minute”
- W^+W^- run will deliver 2.4×10^8 W^\pm pairs in total
- Almost a “best of both worlds” scenario compared to Belle II and LHCb
- We must determine what kind of detectors we need...

Attribute	$\Upsilon(4S)$	pp	Z^0
All hadron species		✓	✓
High boost		✓	✓
Enormous production cross-section		✓	
Negligible trigger losses	✓		✓
Low backgrounds	✓		✓
Initial energy constraint	✓		(✓)

Advantageous properties of Belle II ($\Upsilon(4S)$), LHC (pp) and FCC-ee (Z^0)
[arxiv:2106.01259]

- One of the candidates for a future detector design
- Plenty development activity over the past few years
 - See talks at the FCC weeks and ECFA meetings
- Need to marry this work by detector experts with the physics requirements



Crucial inputs for constraining **new physics** from rare meson decays and meson mixing - the largest source of uncertainty

Systematic uncertainties will eventually dominate the semileptonic V_{cb} measurements

Present Day
 $\sigma(V_{cb}) \sim 1.4 \%$
 $\sigma(V_{ub}) \sim 6.2 \%$



LHCb Upgrade II & Belle III
 $\sigma(V_{cb}) \sim 1.0 \%$
 $\sigma(V_{ub}) \sim 0.9 \%$

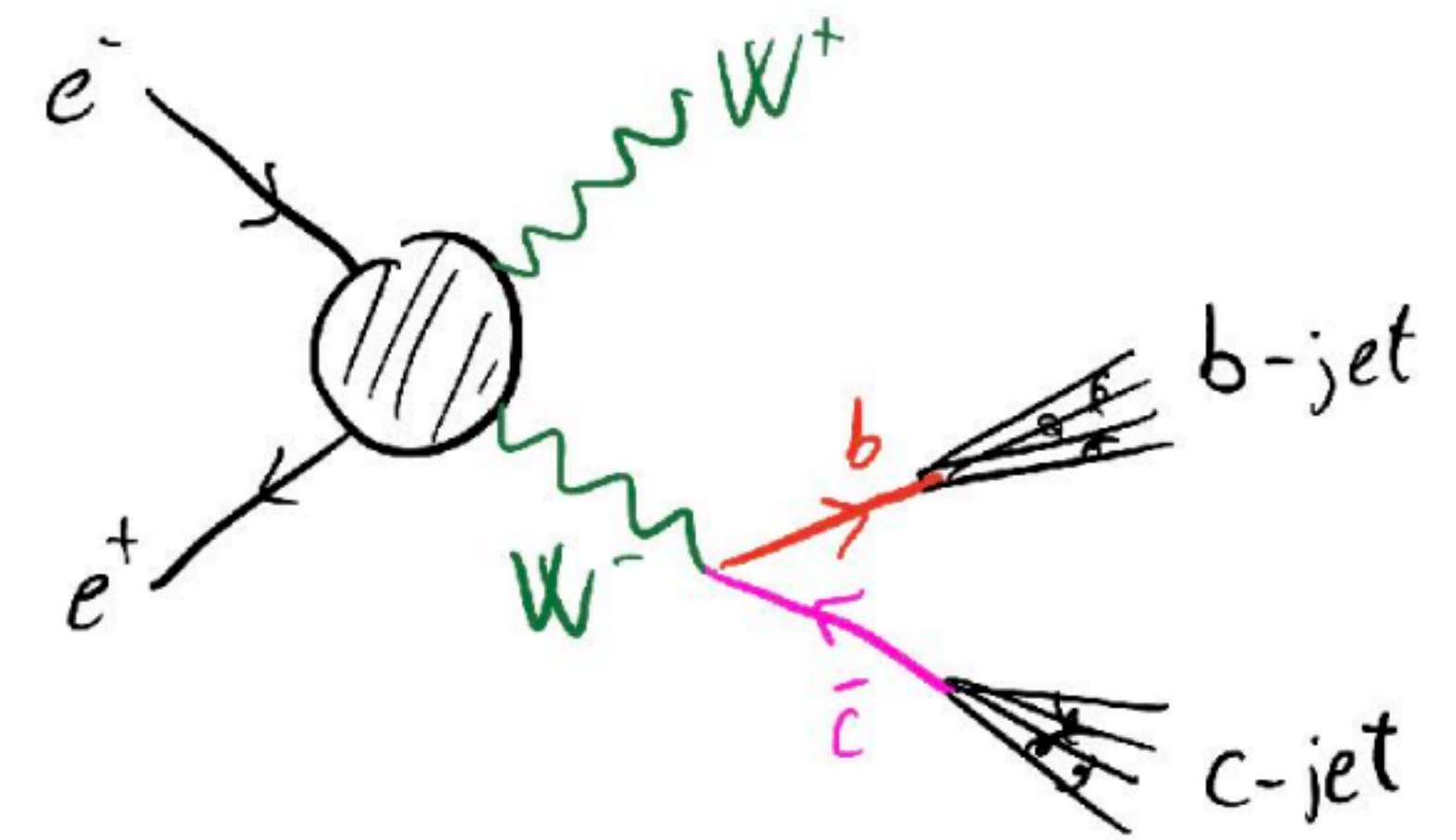
Can we improve on this?

- Independent of the semileptonic measurements
- Independent of Lattice QCD inputs

⇒ improved precision

- For 10^8 W^\pm pairs $\sim 0.14\%$ relative uncertainty

with perfect jet flavour tagging



	b	c	uds
Eff b-jet tagger	25%		
Eff c-jet tagger	10%	50%	2%

Numbers inspired by:

ILD@ILC
 Tracking and Vertexing at Future Linear Colliders:
 Applications in Flavour Tagging
 Tomohiko Tanabe (U Tokyo)
 IAS Program on High Energy Physics 2017, HKUST



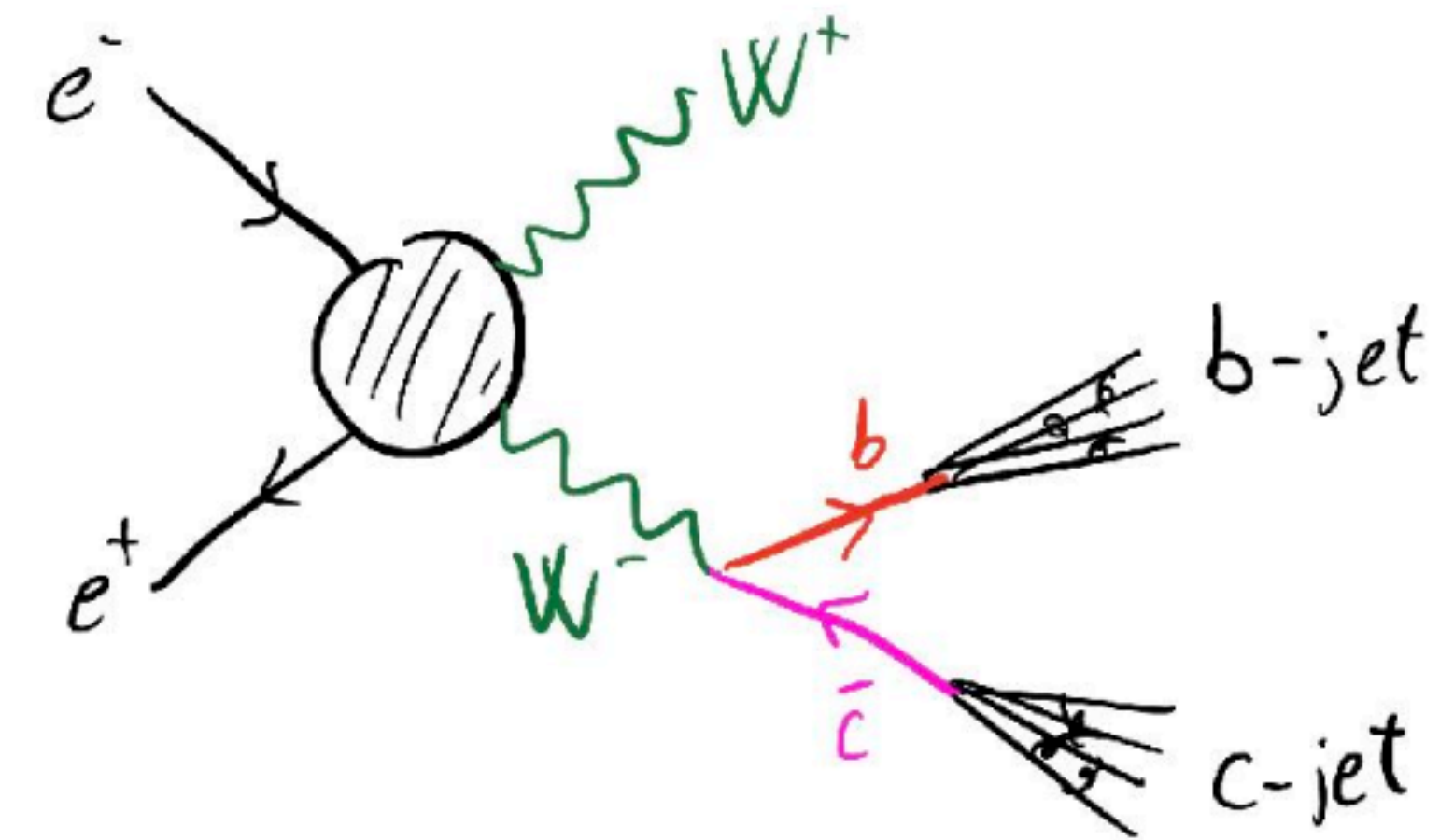
$\sim 0.4\%$
relative uncertainty

Marie-Hélène Schune: 3rd FCC Workshop 2020

Can even be slightly more optimistic given there may be twice as many W^\pm pairs in the nominal running plan

V_{cb} from on-shell W^\pm decays

- Independent of the semileptonic measurements
- Independent of Lattice QCD inputs
 \implies improved precision
- For 10^8 W^\pm pairs $\sim 0.14\%$ relative uncertainty
 with perfect jet flavour tagging
- Will need to calibrate with data - the main challenge


~~| | b | c | uds |
|------------------|-----|-----|-----|
| Eff b-jet tagger | 25% | | |
| Eff c-jet tagger | 10% | 50% | 2% |~~

	b	c	uds
Eff b-jet tagger	87%		
Eff c-jet tagger	100%	65%	0.01%



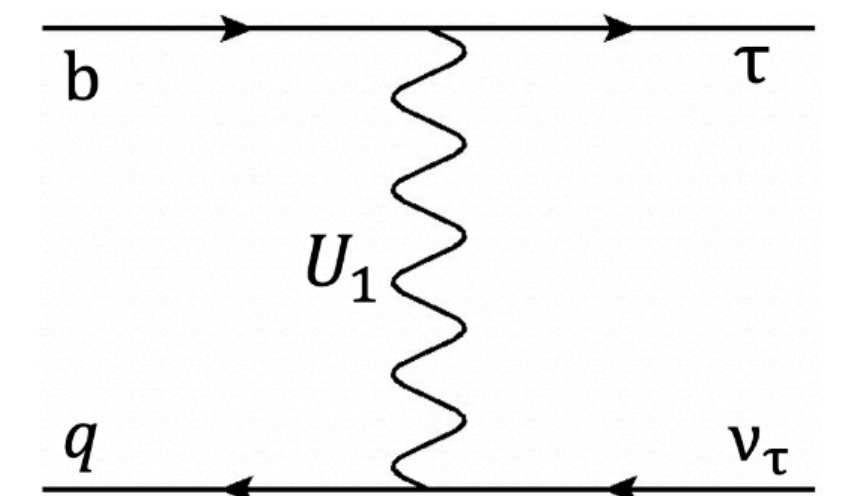
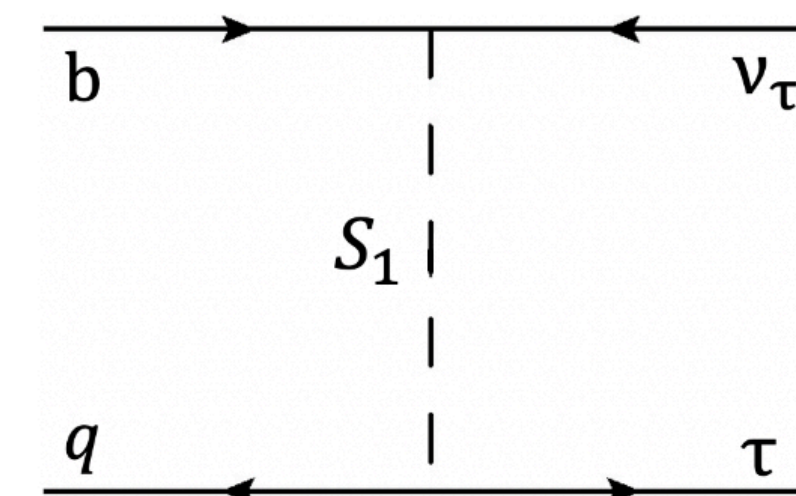
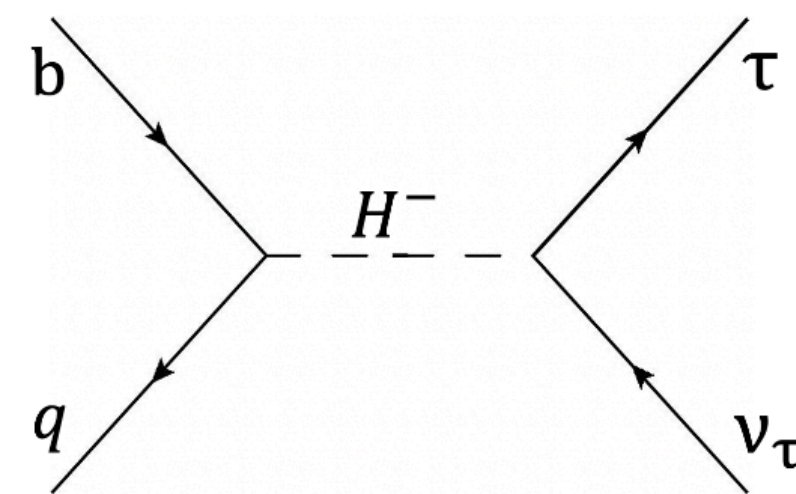
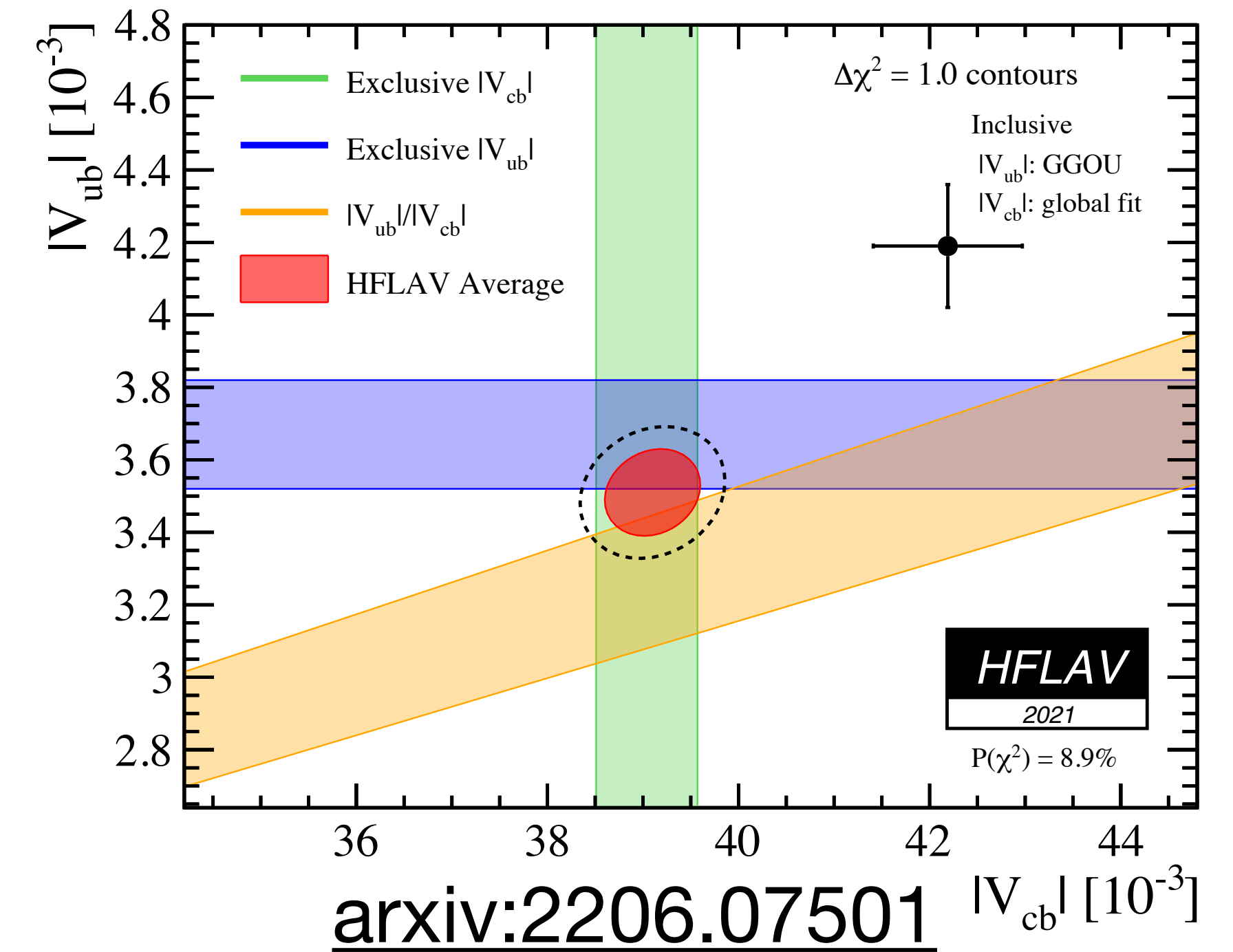
$\sim 0.15\%$
relative uncertainty

Update based on FCC performance study [Michele Selvaggi: FCC Week June 2023]

Can even be slightly more optimistic given there may be twice as many W^\pm pairs in the nominal running plan

$$B_{(c)}^+ \rightarrow \tau^+ \nu_\tau$$

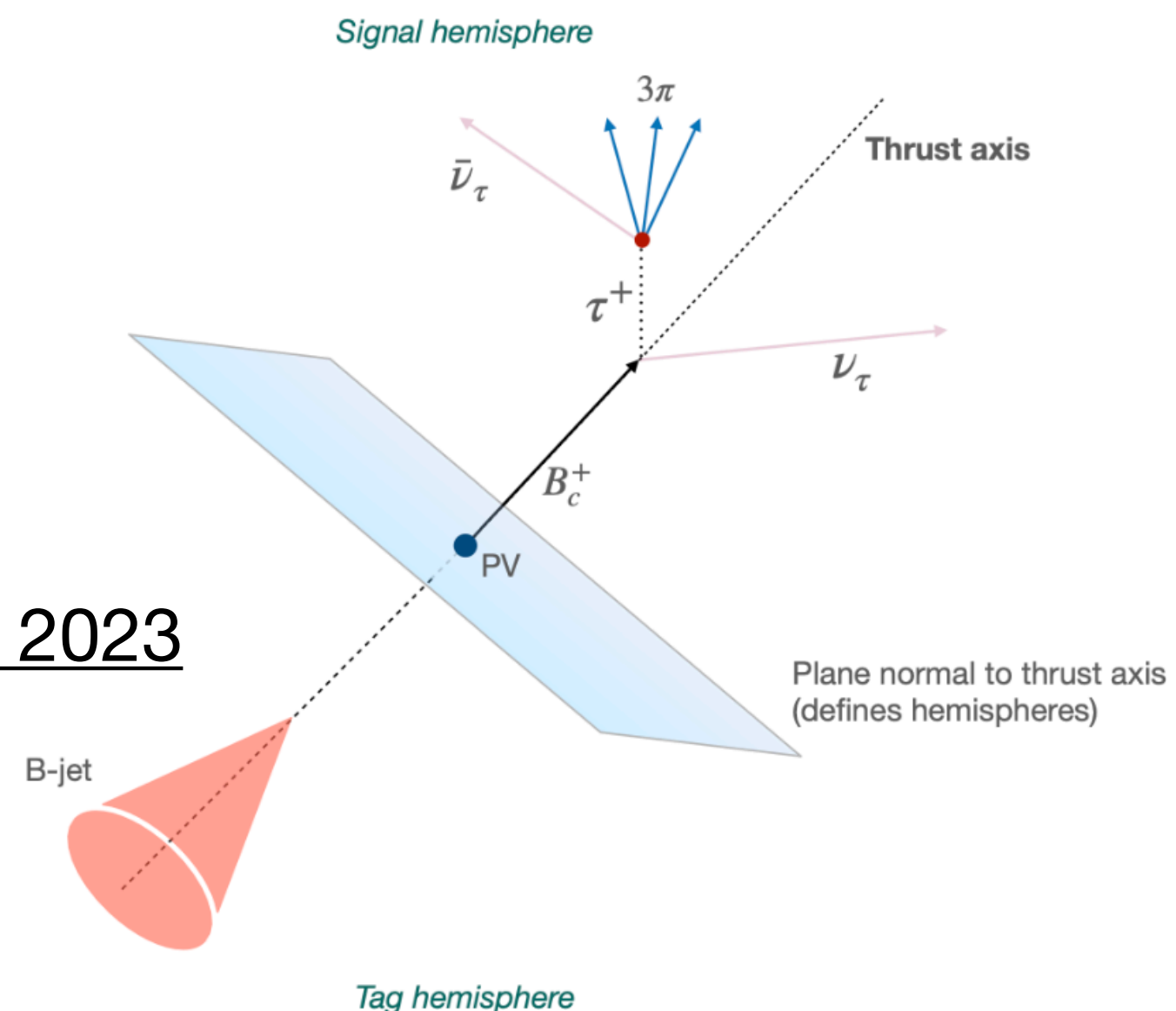
- Independent clean probes of V_{ub} and V_{cb}
- May help resolve the tension between exclusive and inclusive measurements
- Can also probe various NP models
 - Charged Higgs
 - Scalar leptoquarks
 - Vector leptoquarks



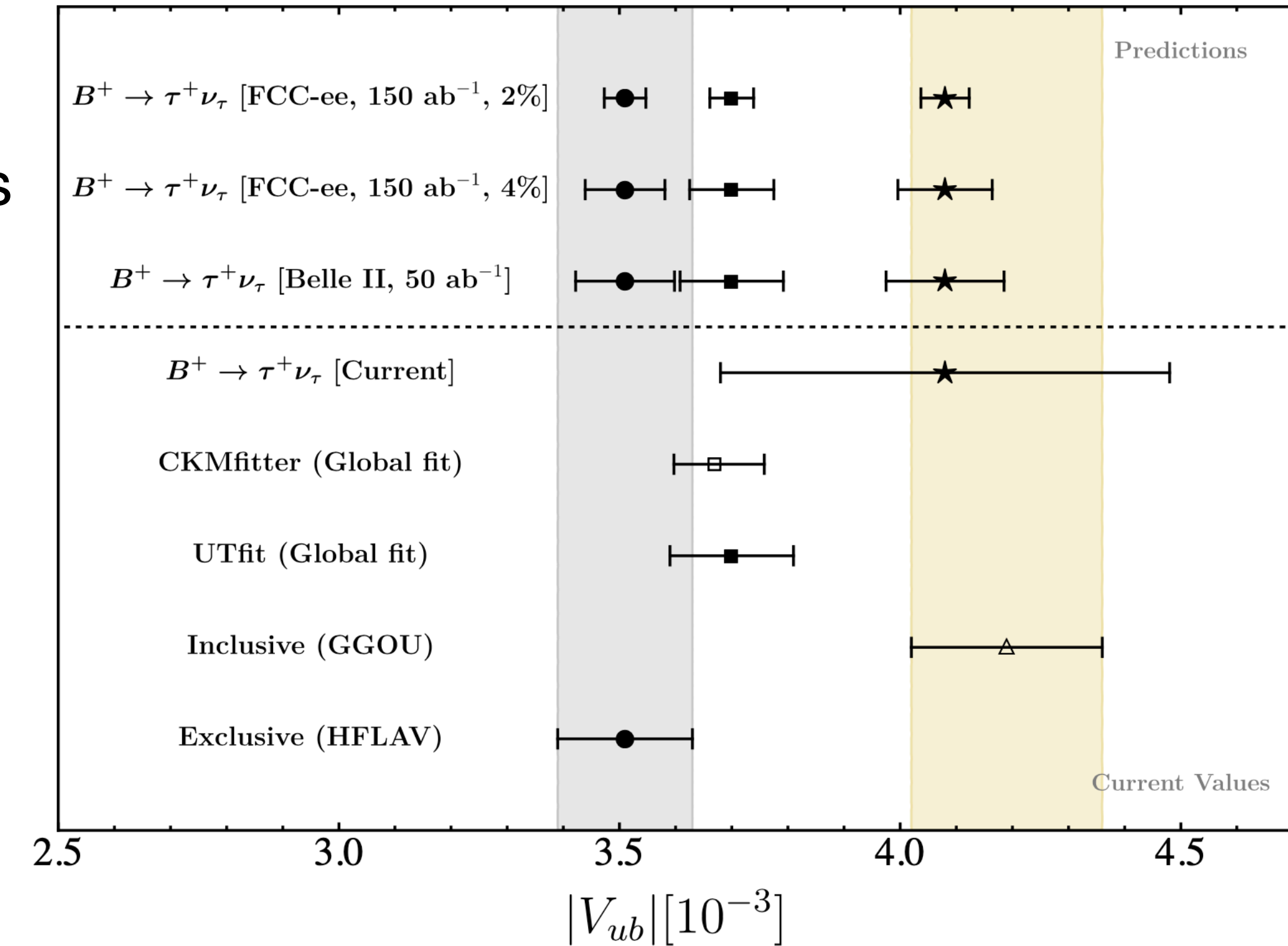
Feynman diagrams for tree-level contributions from: charged Higgs (left), scalar leptoquarks (middle) and vector leptoquarks (right)

$$B_{(c)}^+ \rightarrow \tau^+ \nu_\tau$$

- Reconstruct $\tau^+ \rightarrow \pi^+ \pi^- \pi^+ \bar{\nu}_\tau$ decay
- Decay topology split into high- and low-energy hemispheres
- 2-stage BDT selection: Hemisphere properties followed by candidate properties
- Determine ideal and pessimistic BF uncertainties
 - 2% and 4% respectively



Xunwu Zuo: EPS-HEP 2023

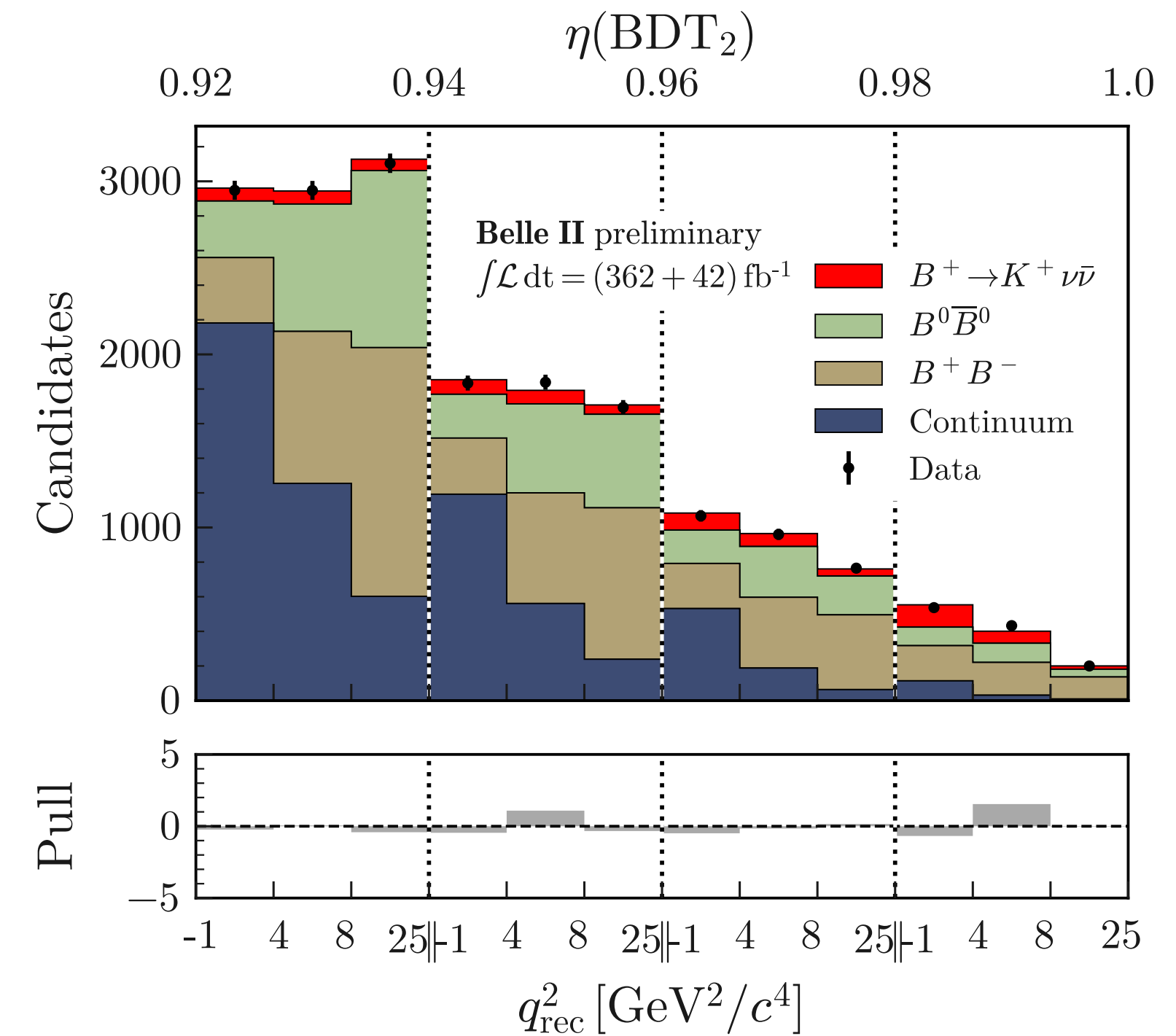


Comparison between current determinations of $|V_{ub}|$ and predicted determinations from Belle II and FCC-ee, where the FCC-ee values correspond to 2% and 4% uncertainty on $\mathcal{B}(B^+ \rightarrow \tau^+ \nu_\tau)$. Different central values are taken from the current Exclusive, Global and $B^+ \rightarrow \tau^+ \nu_\tau$ values.

This study assumes 5×10^{12} Z^0 s so we could actually push it a little further!

$b \rightarrow s\nu\bar{\nu}$ motivation

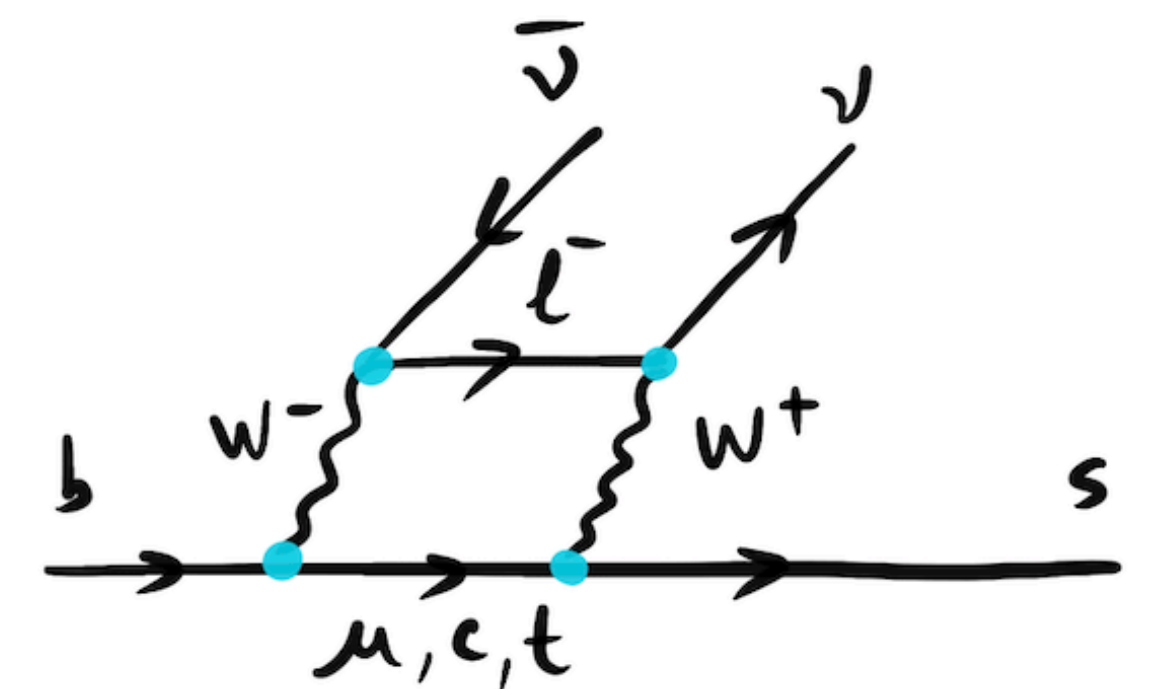
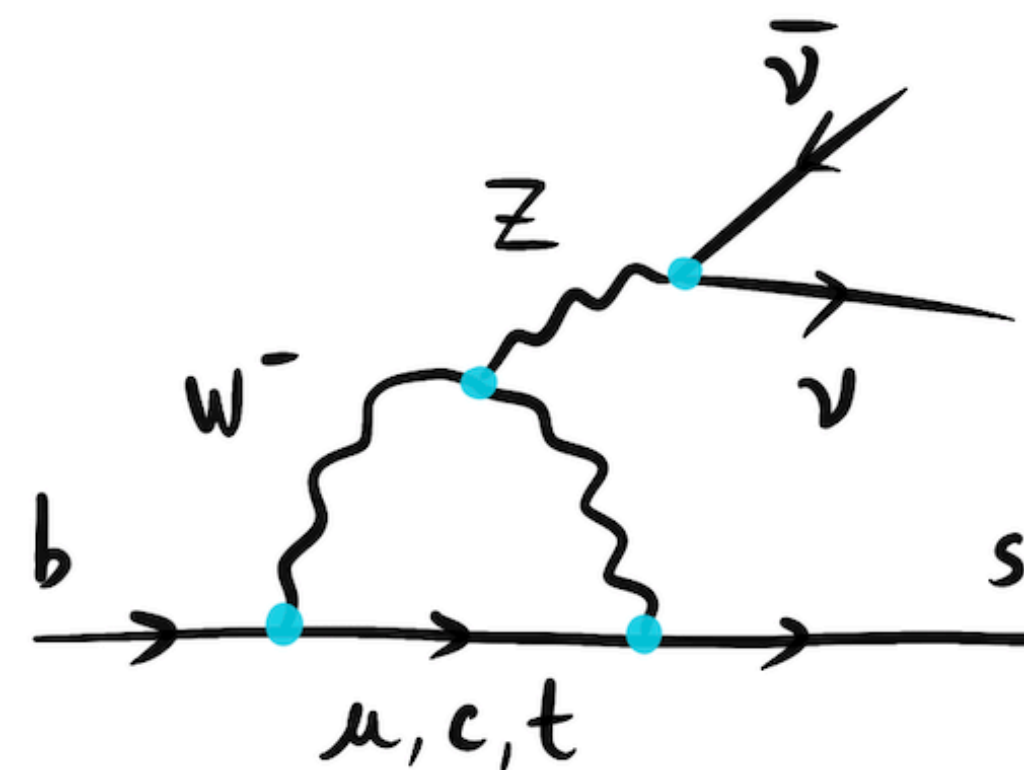
- Impossible at LHCb
- Belle II cannot do *all* B flavours
- Yet to be observed, besides evidence for $B^+ \rightarrow K^+\nu\bar{\nu}$
 - 2.7σ tension with SM [arxiv:2311.14647]
- Theoretically cleaner than the corresponding $b \rightarrow sl^+l^-$
 - No long-distance charm loops!
- Can be used to extract the CKM factor and hadronic form factors, and constrain Wilson coefficients
- Novel probes of CPV from new physics [arxiv:2208.10880]



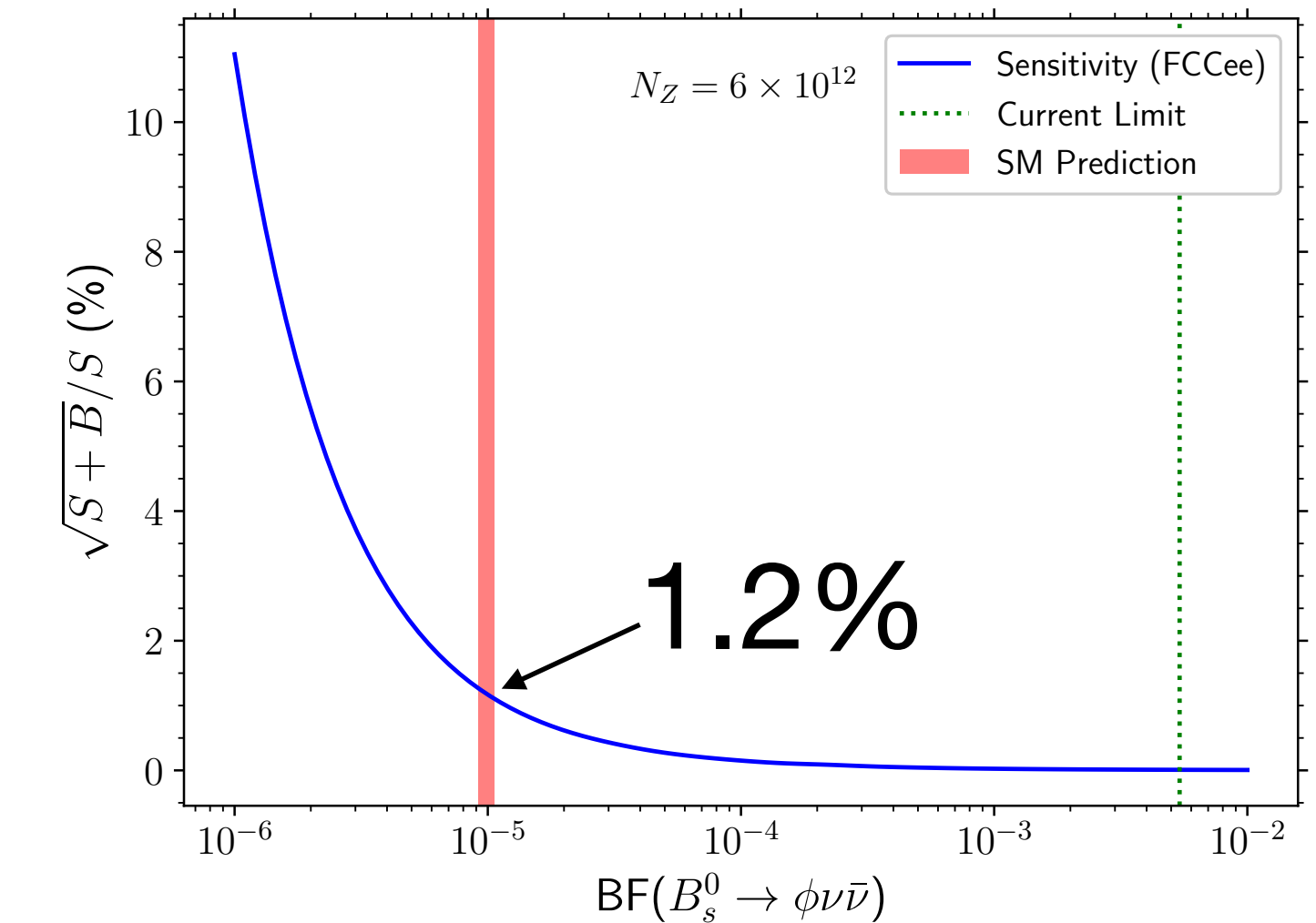
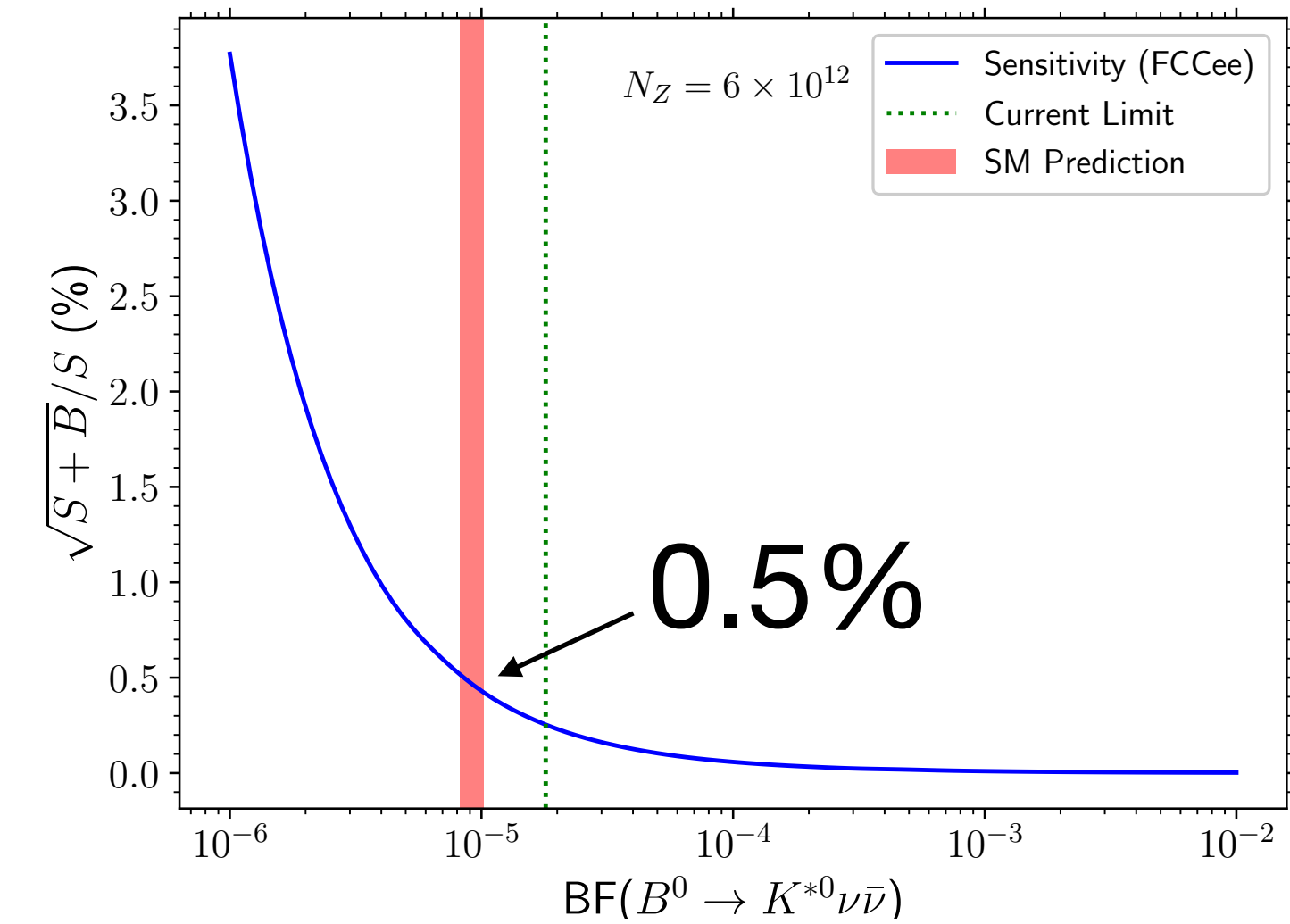
Plot of the maximum likelihood fit for $B^+ \rightarrow K^+\nu\bar{\nu}$ from inclusive tagging

Decay	B-factories	FCC-ee
$B^+ \rightarrow K^+\nu\bar{\nu}$	✓	✓
$B^+ \rightarrow K^{*+}\nu\bar{\nu}$	✓	✓
$B^0 \rightarrow K_S^0\nu\bar{\nu}$	✓	✓
$B^0 \rightarrow K^{*0}\nu\bar{\nu}$	✓	✓
$B_s^0 \rightarrow \phi\nu\bar{\nu}$	✗	✓
$\Lambda_b^0 \rightarrow \Lambda^{(*)0}\nu\bar{\nu}$	✗	✓

B decays accessible by B-factories and FCC-ee



- Belle II expects $\mathcal{O}(10\%)$ uncertainty on $\mathcal{B}(B \rightarrow K^{(*)}\nu\bar{\nu})$ with 50 ab^{-1}
 - Let's see where they go with $B^+ \rightarrow K^+\nu\bar{\nu} \dots$
- Follow a similar analysis procedure to $B_{(c)} \rightarrow \tau^+\nu_\tau$
- FCC-ee assuming perfect vertex seeding and PID:
 - $\mathcal{O}(1\%)$ uncertainty for $B^0 \rightarrow K^{*0}\nu\bar{\nu}$ & $B_s^0 \rightarrow \phi\nu\bar{\nu}$
 - $\mathcal{O}(3\%)$ uncertainty for $B^0 \rightarrow K_S^0\nu\bar{\nu}$
 - $\mathcal{O}(10\%)$ uncertainty for $\Lambda_b^0 \rightarrow \Lambda^0\nu\bar{\nu}$



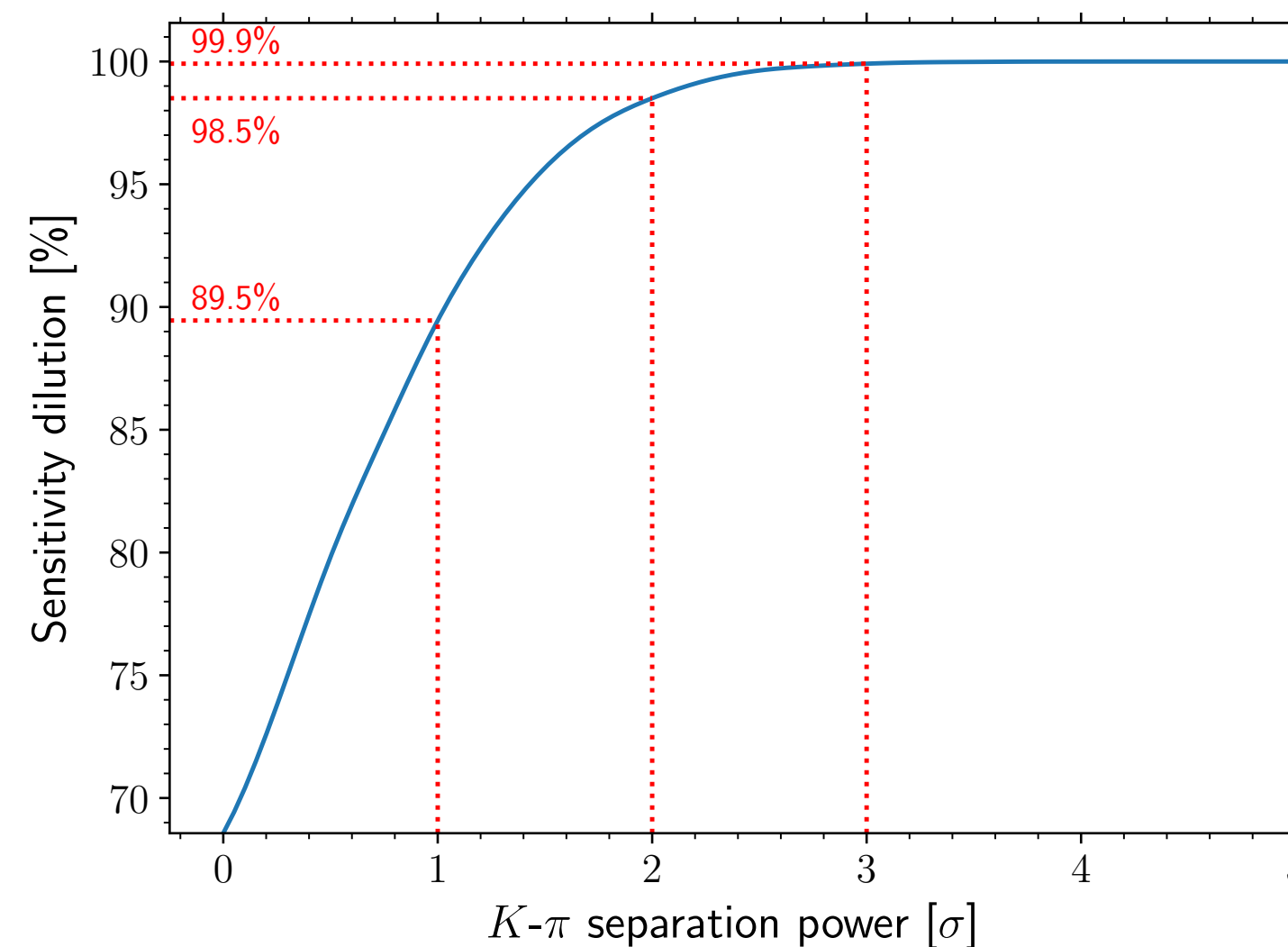
Sensitivity estimate plots for a range of BFs of $B^0 \rightarrow K^{*0}\nu\bar{\nu}$ (top) & $B_s^0 \rightarrow \phi\nu\bar{\nu}$ (bottom)

$b \rightarrow s\nu\bar{\nu}$ detector requirements

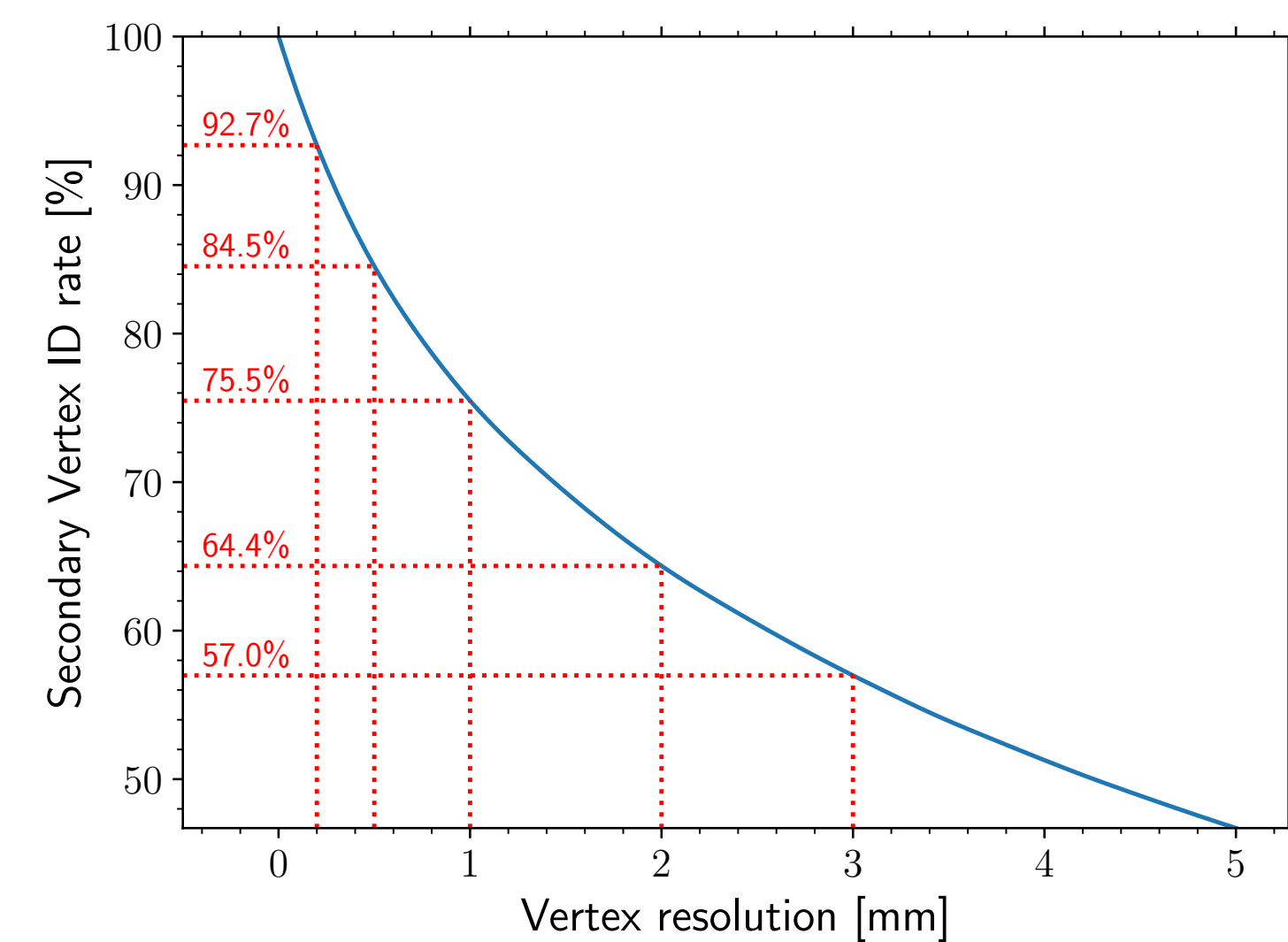
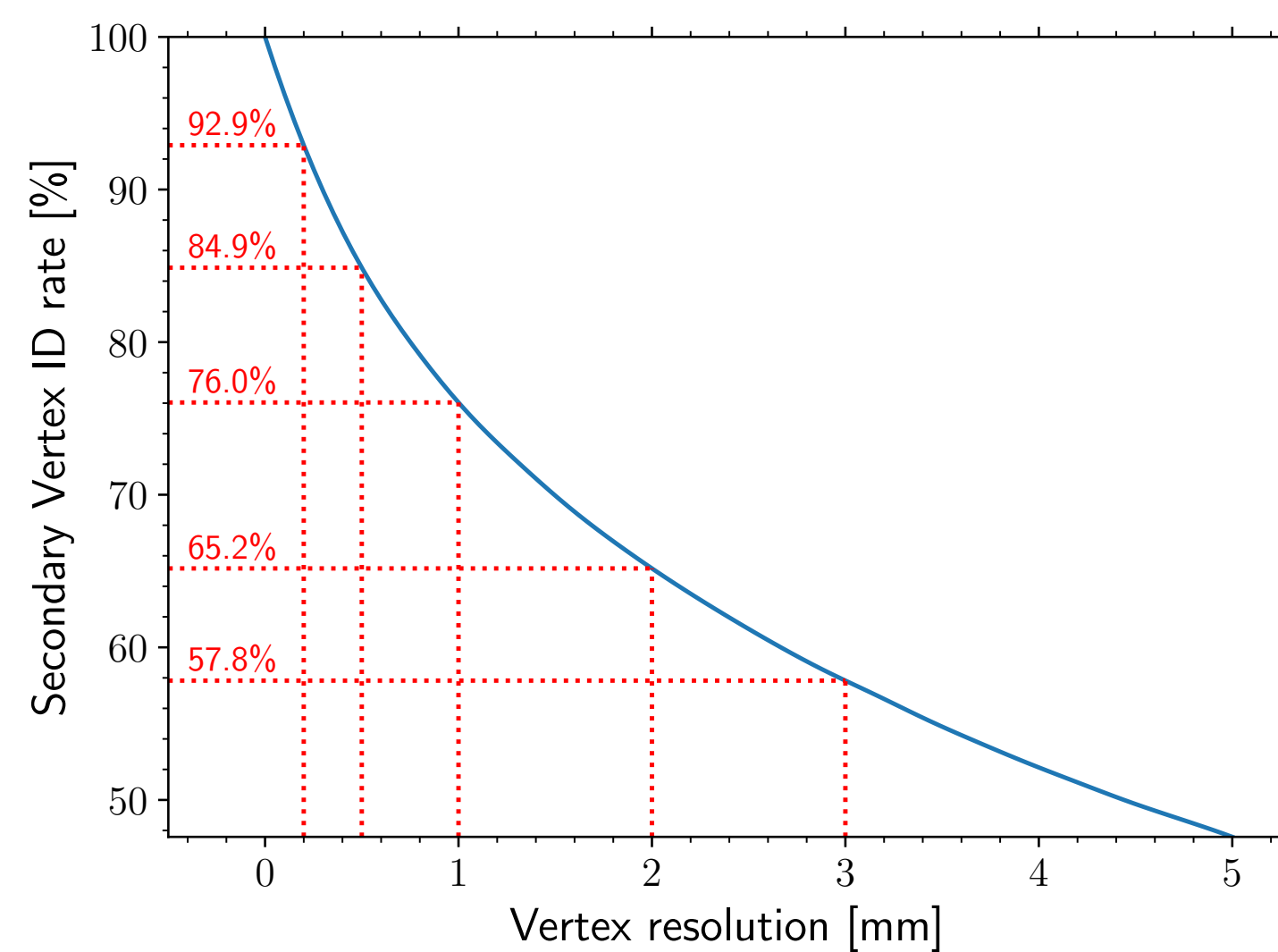
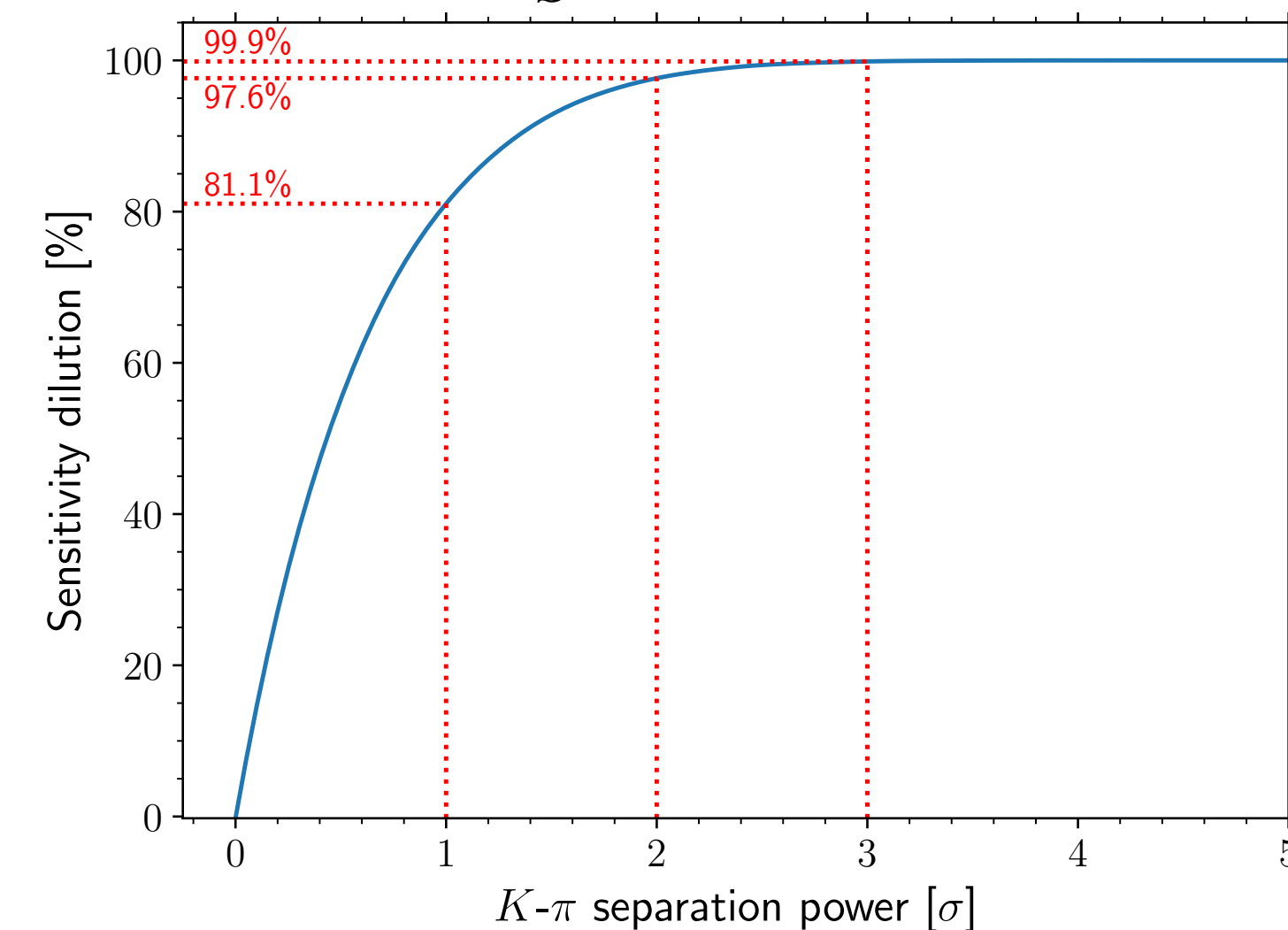
[arxiv:2309.11353]

- Robust against $\pi - K$ mis-ID with at least $\sim 2\sigma$ separation
- Require $\leq 0.2\text{mm}$ vertex resolution
 - Well above the expected resolution $\mathcal{O}(10\mu\text{m})$
- More detailed studies in the future to evaluate the full detector requirements

$$B^0 \rightarrow K^{*0}\nu\bar{\nu}$$

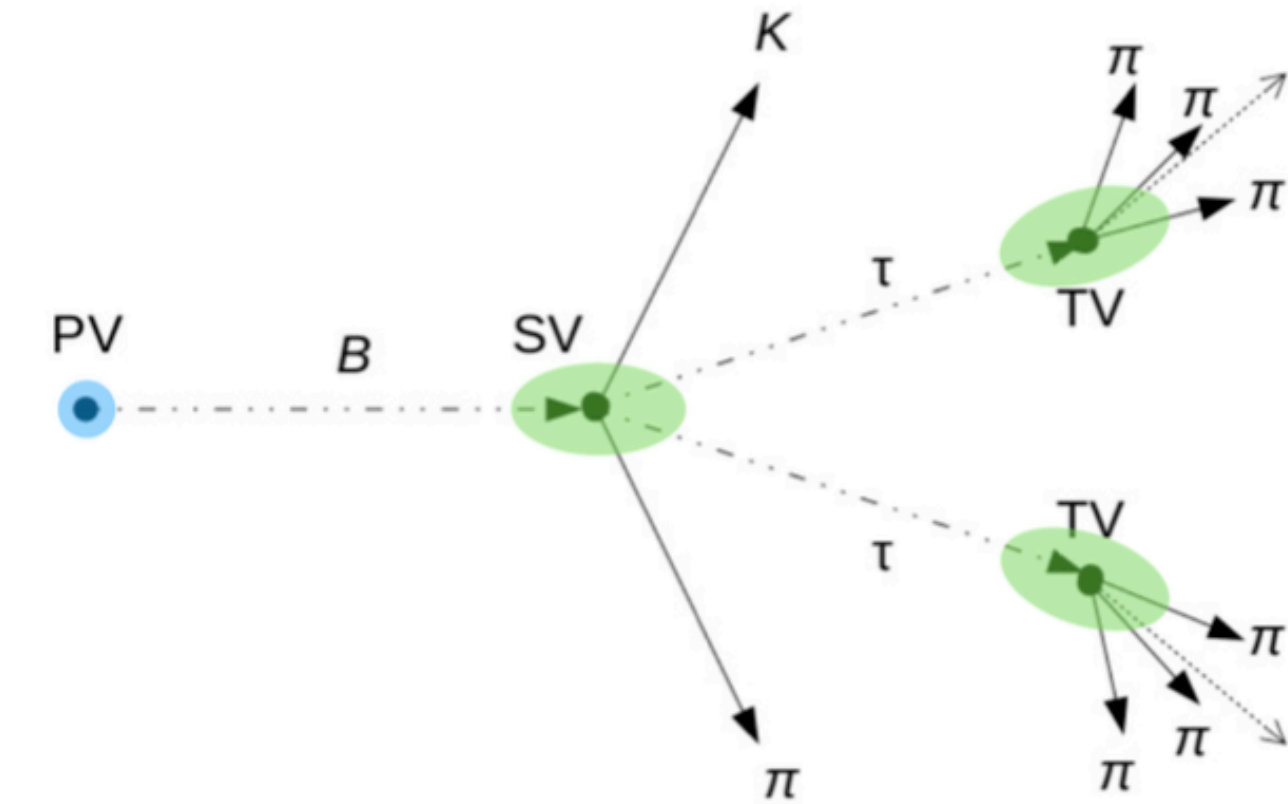


$$B_s^0 \rightarrow \phi\nu\bar{\nu}$$

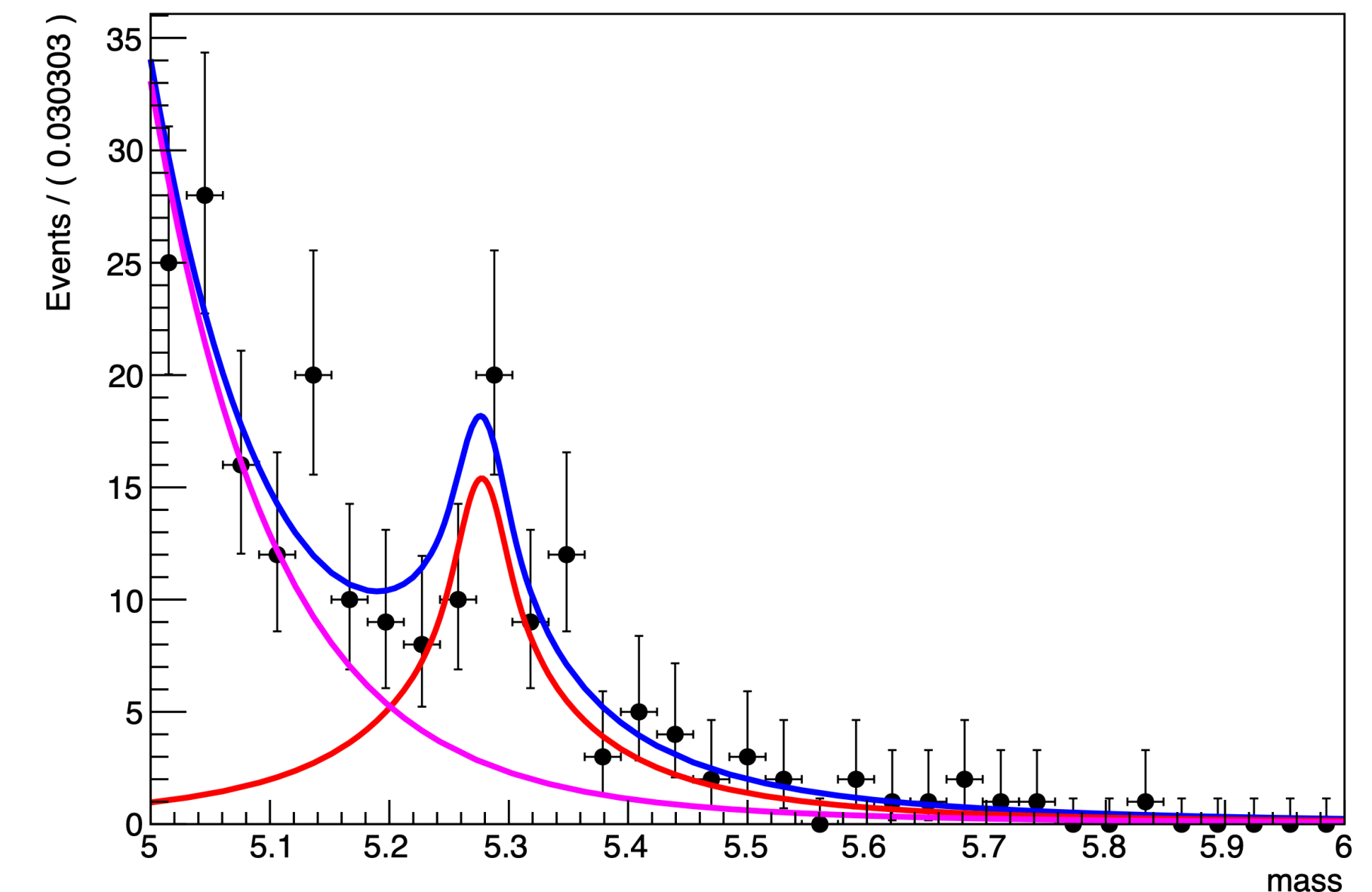


$$B^0 \rightarrow K^{*0} \tau^+ \tau^-$$

- Yet to be observed - $\mathcal{O}(10^{-7})$ BF
 - Current limit $\mathcal{O}(10^{-4}) - \mathcal{O}(10^{-3})$
- Many NP models expect NP to couple primarily to the Higgs and the third generation Ben Stefanek: 2nd ECFA Workshop 2023
- Focus again on the the 3-prong $\tau^+ \rightarrow \pi^+ \pi^- \pi^+ \bar{\nu}$ decay
- Use energy-momentum conservation to resolve ν kinematics
- BDT trained with candidate kinematics to reduce backgrounds
- Signal yield extracted with an unbinned ML fit to the candidate B mass

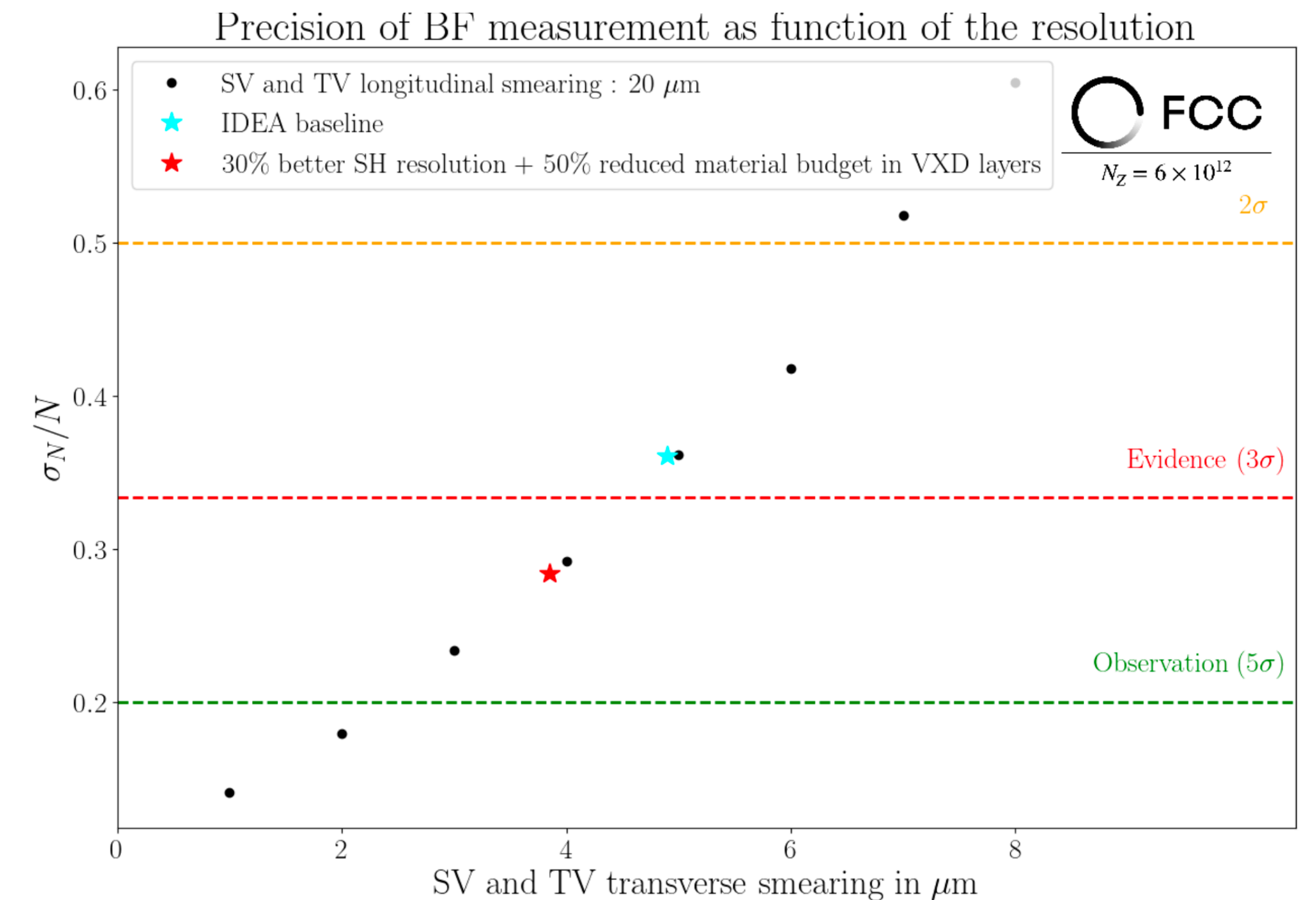


Schematic of the signal decay

 B^0 candidate invariant mass fit to rescaled signal and background MC

$B^0 \rightarrow K^{*0} \tau^+ \tau^-$ sensitivity

- Current FCC-ee and IDEA would not allow for discovery of this mode
 - Trying to play with detector performance
 - $\implies 3.5\sigma$
- Clearly some work to do!
 - Better vertexing?
 - Easier said than done
 - Higher luminosity/longer run period?
 - Difficult/competition with other runs
 - Consider other τ decays?
 - Leptonics harder to handle but would produce $\mathcal{O}(10)$ times the data



Dependence of the relative signal yield uncertainty on the vertex resolution of the IDEA detector

- $\sim 10^{11} Z \rightarrow \tau^+ \tau^-$ at the FCC-ee
- m_τ is a SM parameter - must push experimental sensitivity as far as possible
 - Required for many SM predictions
 - Charged weak currents
 - CKM elements
 - Enters LFU tests at the fifth power
 - LFV searches complement that of μ
- Can also directly measure lifetime and BFs (extract $\alpha_s(m_\tau)$)
- τ coupling $\implies \nu_\tau$ coupling - link to oscillations and LFV, probe orders of magnitude better than current experiments [[arXiv:1612.02728](https://arxiv.org/abs/1612.02728), [arXiv:2203.05502v2](https://arxiv.org/abs/2203.05502v2), [arXiv:2203.06520](https://arxiv.org/abs/2203.06520)]

- A recent Belle II analysis, [arxiv:2305.19116](https://arxiv.org/abs/2305.19116), gives the most precise measurement

$$m_\tau = 1777.09 \pm 0.08(\text{stat.}) \pm 0.11(\text{syst.}) \text{ MeV}/c^2$$

- Systematically limited
 - Knowledge of the beam energy
 - Momentum corrections due to scale factor dependence on p_T
- FCC-ee should be able to significantly reduce these effects
 - Beam energy should be known to within 1ppm
 - ~2ppm momentum scale calibration should be possible using $m_{j/\psi}$
- Baseline IDEA should be sufficient to obtain 14ppm measurement of $\sigma_{m_\tau} \sim 0.02 \text{ MeV}/c^2$

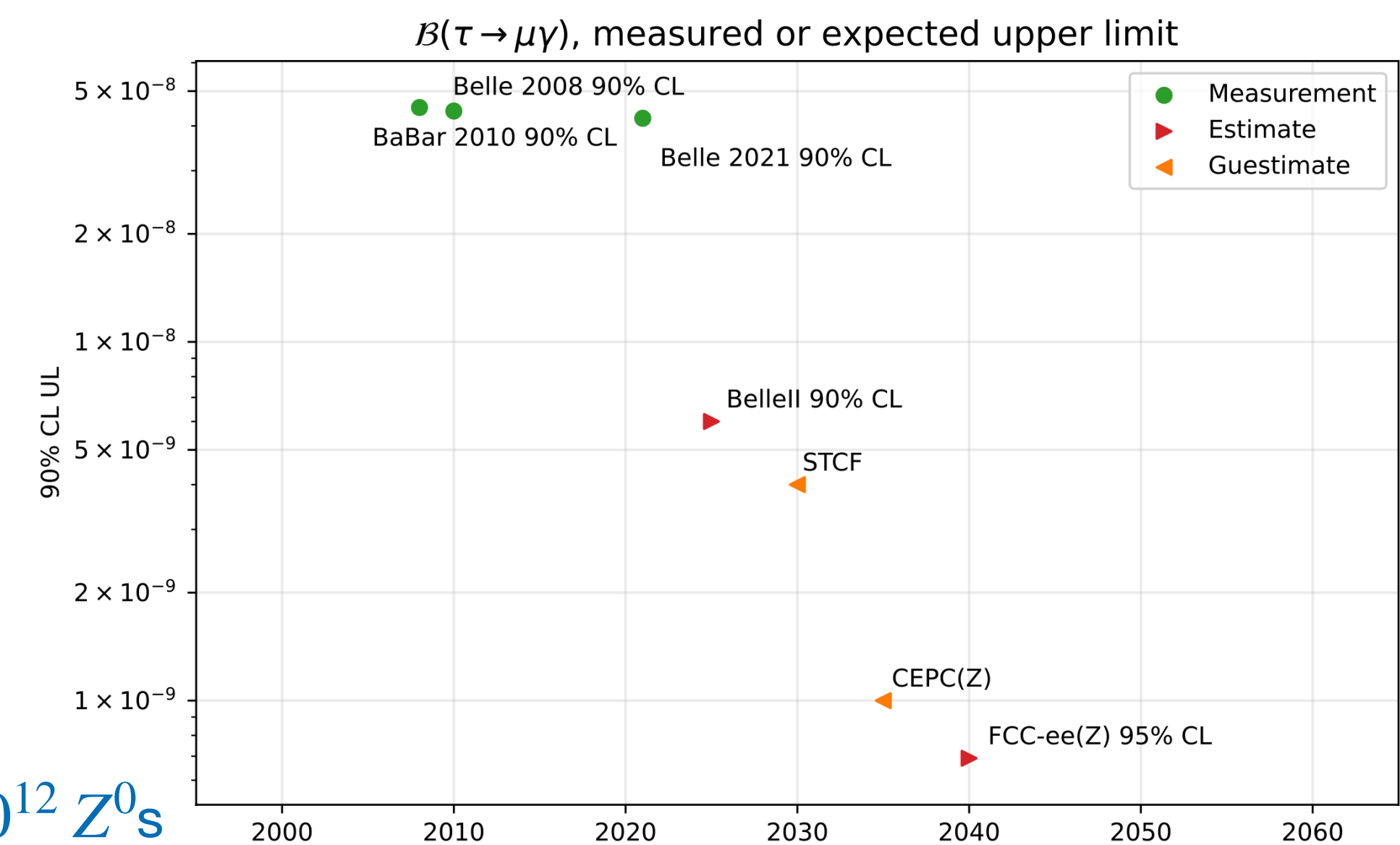
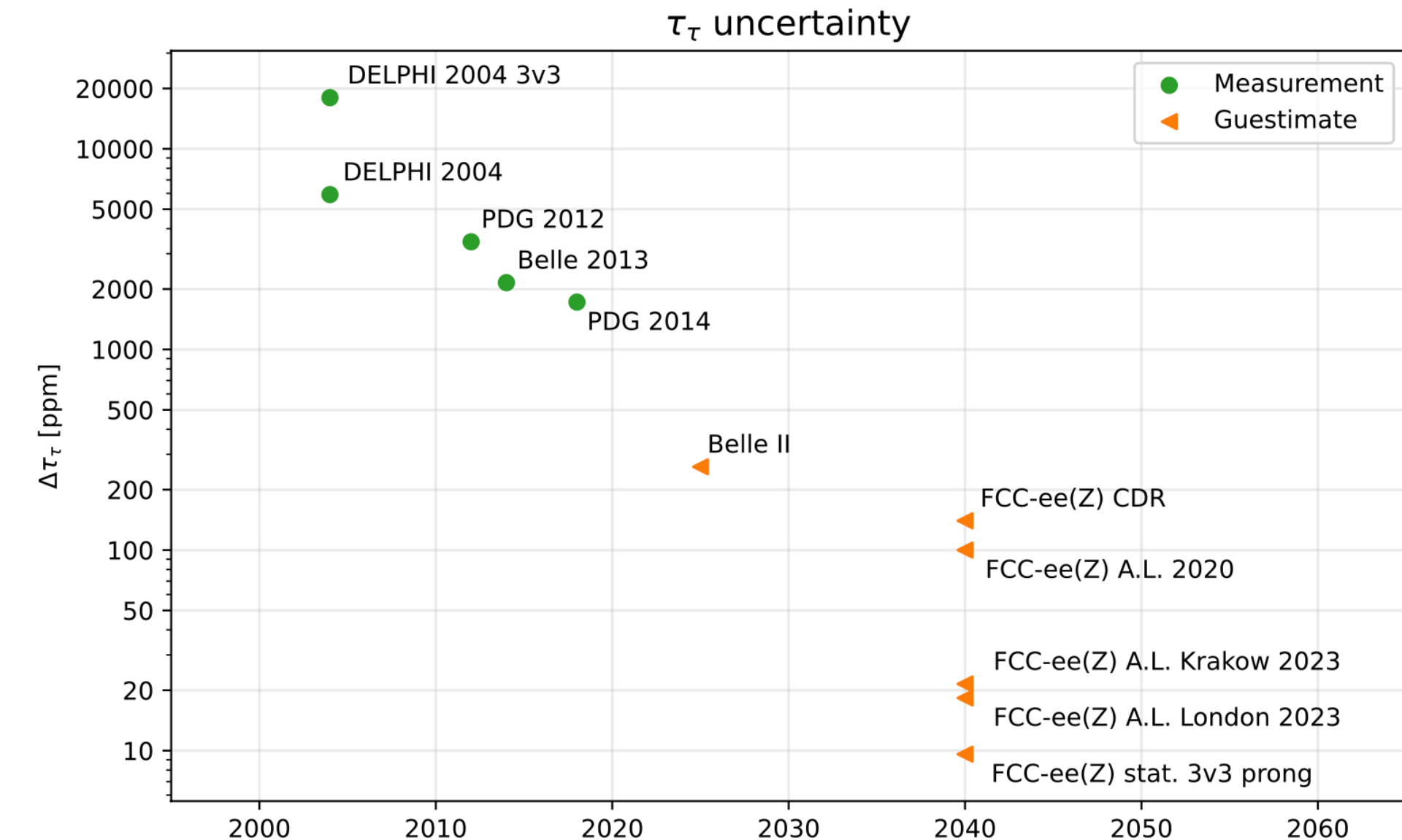
Source	Uncertainty [MeV/ c^2]
Knowledge of the colliding beams:	
Beam-energy correction	0.07
Boost vector	< 0.01
Reconstruction of charged particles:	
Charged-particle momentum correction	0.06
Detector misalignment	0.03
Fit model:	
Estimator bias	0.03
Choice of the fit function	0.02
Mass dependence of the bias	< 0.01
Imperfections of the simulation:	
Detector material density	0.03
Modeling of ISR, FSR and τ decay	0.02
Neutral particle reconstruction efficiency	≤ 0.01
Momentum resolution	< 0.01
Tracking efficiency correction	< 0.01
Trigger efficiency	< 0.01
Background processes	< 0.01
Total	0.11

Systematic uncertainties in the Belle II m_τ measurement
[arxiv:2305.19116](https://arxiv.org/abs/2305.19116)

τ^\pm lifetime and BFs

- FCC-ee should provide the most precise measurements of τ lifetimes and BFs
- For lifetime
 - Impact parameter is $\sim 70 \mu\text{m}$, much greater than the FCC IP resolution and beam spot size
 - Uncertainty on the average length scale of vertex detector elements $\leq 4.8 \text{ ppm}$
- For BFs
 - Good EM energy resolution, $< 20\% / \sqrt{E(\text{GeV})}$ (LEP)
 - Granular EM calorimeter $> 15 \times 15 \text{ mrad}^2$ (LEP)

Should temper expectations a little as these plots assume $8 \times 10^{12} Z^0\text{s}$



That's not all...

- Obviously there is much more flavour physics to explore in the future
 - CKM measurements - the “flattest” unitarity triangle [arxiv:2402.09987](#)
 - Lepton flavour violation, e.g. $e^+e^- \rightarrow \tau^\pm\mu^\mp$ [arxiv:2305.03869](#)
 - Lepton number violation and heavy neutral leptons [Stefan Antusch: 2nd ECFA Workshop 2023](#), [Jürgen Reuter: 2nd ECFA Workshop 2023](#)
 - t flavour changing neutral currents [arxiv:1904.10956](#)
- We need to do our best to ensure we build something that lets us do as much as possible — What would you want to do that current experiments cannot?
 - More ideas are welcome
 - And more people to do studies!

Summary

- CKM measurements far more precise than possible at current experiments
- Can perform extensive studies of (semi-)invisible final states
 - Impossible at LHCb due to missing energy
 - Possible at Belle II but limited to $\sigma_{\mathcal{B}} \sim \mathcal{O}(10\%)$ and B^0, B^+
 - FCC-ee should get $\sigma_{\mathcal{B}} \sim \mathcal{O}(1\%)$ BF measurements
- Can push τ^\pm measurements further
 - Difficult at LHCb
 - Limited at Belle II by sample size, species and systematics
 - $\sigma_{m_\tau} \sim 14\text{ppm}$, $\sigma_{\tau_\tau} \sim 12\text{ppm}$,
- More papers on the way - focus on detailed detector requirements increasing!
- More ideas and collaborators are welcome!

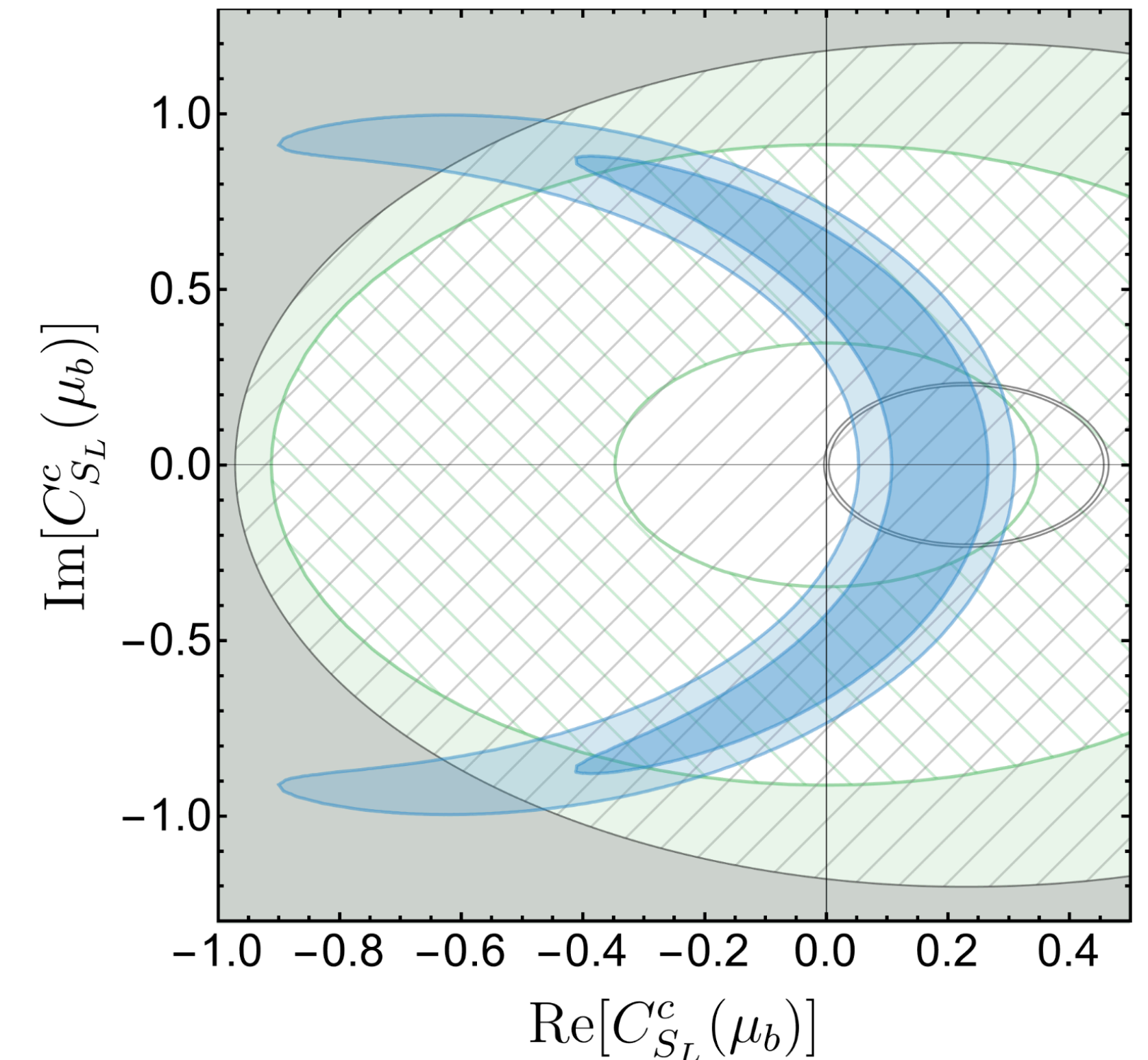
[GitHub: FCCeePhysicsPerformance](#)

Backup

$B_{(c)} \rightarrow \tau^+ \nu_\tau$: analysis and leptoquarks

[arxiv:2105.13330, arxiv:2305.02998]

- Subsequent $\tau^+ \rightarrow \pi^+ \pi^- \pi^+ \bar{\nu}_\tau$ decay
- Decay topology split into high- and low-energy hemispheres
- 2-stage BDT selection: Hemisphere properties followed by candidate properties
- First stage BDT trained with hemisphere properties of signal and inclusive background MC
 - Total energy, charged energy, neutral energy, multiplicities, number of tracks, etc...
- Second stage BDT trained with the candidate properties
 - Mass, vertex χ^2 , momentum, impact parameters...
- Signal yield determined by a fit to the maximum hemisphere energy



- Grey shade is the exclusion by current results
- Green hash is the exclusion expected for HL-LHC
- Grey hash is the exclusion by FCC-ee (the thin annulus survives)
- Blue shades are $1\sigma, 2\sigma, 3\sigma$ bands from current $b \rightarrow c$ anomalies