

Lepton Flavour Universality tests and determination of V_{us} using the tau branching fractions fit

HFLAV
Tau

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Abstract

We describe the updated tau lepton averages performed by the Heavy Flavour Averaging Group (HFLAV) for the incoming edition of the Heavy Flavour measurements averages, and we use the results to update several Lepton Flavour Universality tests and the computation of $|V_{us}|$ with tau measurements.



Tau branching fraction fit inputs

inputs	examples
171 measurements of τ branching fractions & branching ratios	$B(\tau^- \rightarrow \pi^- \nu_\tau)$, $\frac{B(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau)}{B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)}$
1 nuisance fit parameter measurement (new feature)	$B(a_1^- \rightarrow \pi^- \gamma) = 0.0021 \pm 0.0008$ [Schael et al., 2005]
91 constraints	$B_{3/5} = \frac{B_3}{B_5}$ with $B_{3/5} = \frac{B(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau)}{B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)}$, $B_3 = B(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau)$, $B_5 = B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)$
1 uncertainty scale factor	5.44 scale factor applied to inconsistent BABAR and Belle $B(\tau^- \rightarrow K^- K^+ \nu_\tau)$

χ^2 minimization

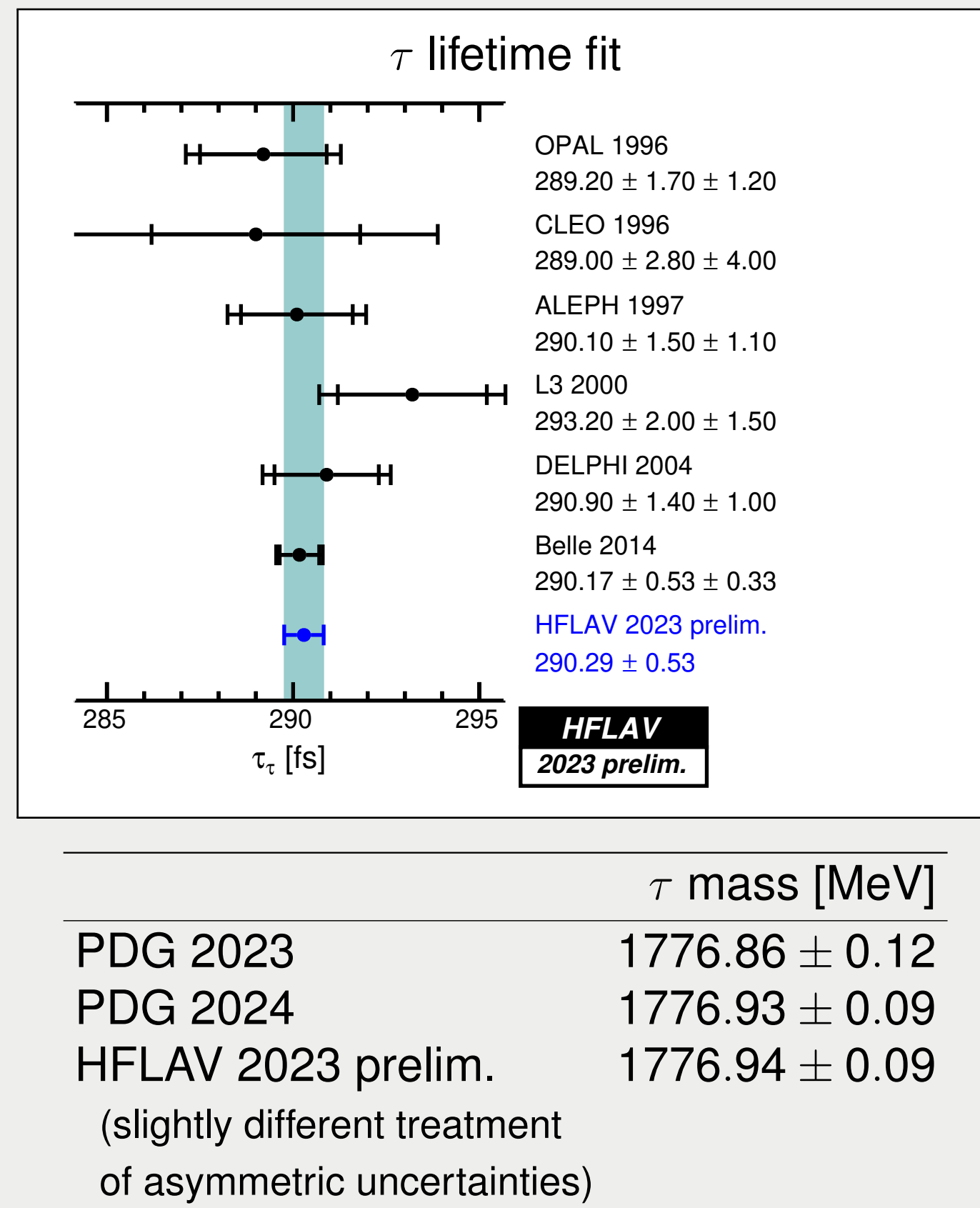
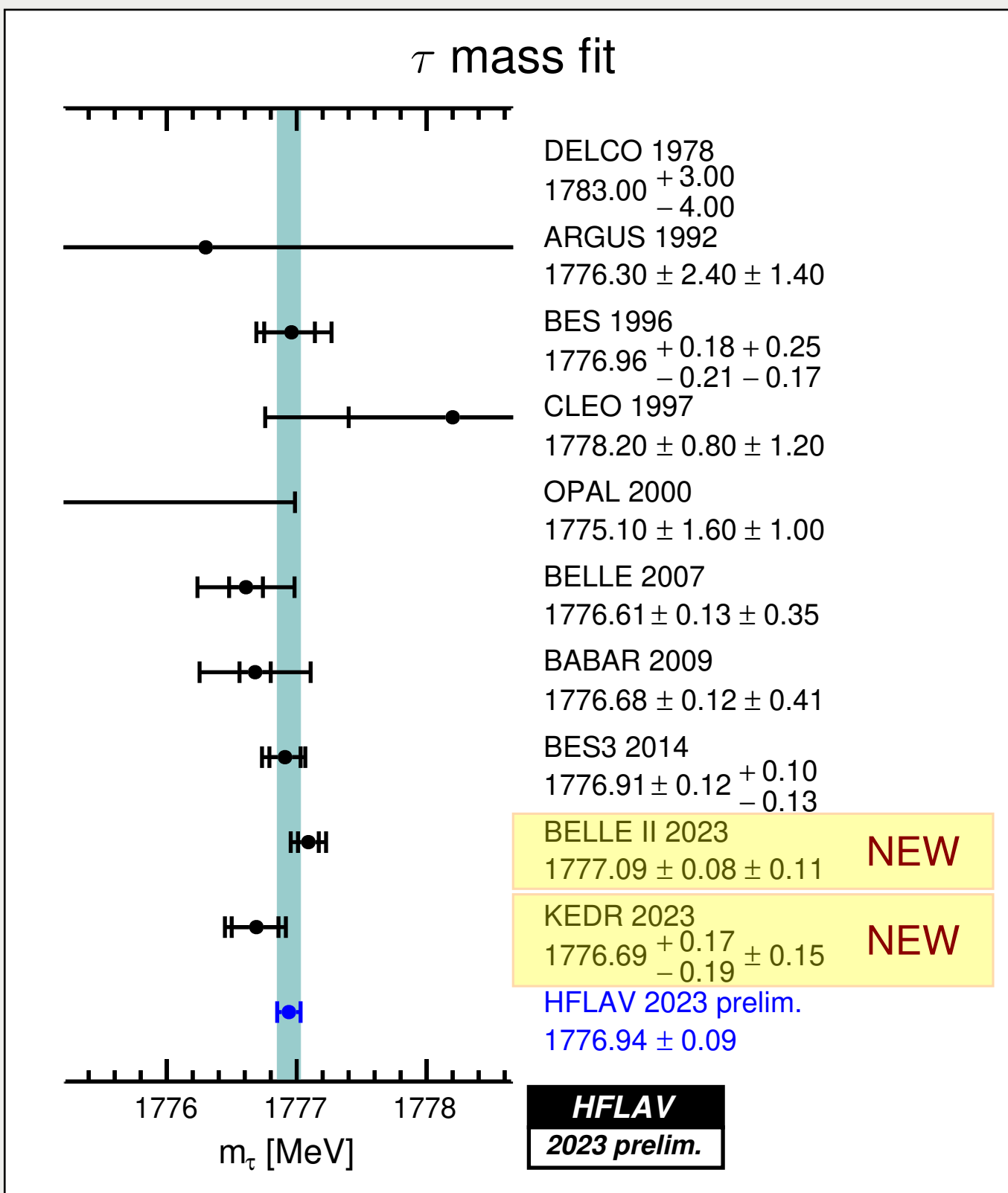
$$\chi^2 = \sum_{ijkl} (m_i - M_{ik} q_k) (V^{-1})_{ij} (m_j - M_{jl} q_l) + \sum_r \frac{(n_r - p_r)^2}{\sigma_{n_r}^2}$$

m_i	measurement result
q_k	fit parameter
M_{ik}	model matrix applied to fit parameters to predict measurements
V_{ij}	measurements covariance matrix
p_r	nuisance fit parameter
$n_r \pm \sigma_{n_r}$	measurement of nuisance fit parameter

Tau branching fractions fit results

137 fit parameters 1 nuisance fit parameter (new feature)
 covariance matrix of fit parameters and nuisance fit parameters
 $\chi^2/\text{d.o.f.} = 138/125$ $P(\chi^2) = 20.2\%$
 unitarity residual $B_{ur} = 1 - B_{all} = 0.0007 \pm 0.0011$

Tau mass and lifetime fits



Ratio of tau hadronic to leptonic branching fractions

$B_e^{\text{uni}} = (17.815 \pm 0.023)\%$, average of (see [Davier, Hocker, and Zhang, 2006])

- $B_e = B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau)$
- B_e from $B_\mu = B(\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau)$ assuming Lepton Flavour Universality
- B_e from τ lifetime assuming Lepton Flavour Universality

$$R_{\text{had}} = \frac{\Gamma(\tau \rightarrow \text{hadrons})}{\Gamma(\tau \rightarrow e \bar{\nu}_e \nu_\tau)} = \frac{B_{\text{had}}}{B_e^{\text{uni}}} = 3.634 \pm 0.008$$

Lepton Flavour Universality: coupling ratios

$$\left(\frac{g_\tau}{g_\mu}\right)_\pi = \sqrt{\frac{B(\tau \rightarrow \pi \nu_\tau) 2m_\pi m_\tau^2 R_\pi}{B(\pi \rightarrow \mu \bar{\nu}_\mu) (1 + \delta R_{\tau/\pi}) m_\pi^3 R_\tau}} \frac{1 - m_\mu^2/m_\pi^2}{1 - m_\pi^2/m_\tau^2} = 0.996 \pm 0.004$$

$$\left(\frac{g_\tau}{g_\mu}\right)_K = \sqrt{\frac{B(\tau \rightarrow K \nu_\tau) 2m_K m_\tau^2 R_K}{B(K \rightarrow \mu \bar{\nu}_\mu) (1 + \delta R_{\tau/K}) m_K^3 R_\tau}} \frac{1 - m_\mu^2/m_K^2}{1 - m_K^2/m_\tau^2} = 0.986 \pm 0.008$$

$$\left(\frac{g_\tau}{g_e}\right) = \sqrt{\frac{B(\tau \rightarrow \mu \bar{\nu}_\mu \nu_\tau) R_\tau}{B(\tau \rightarrow e \bar{\nu}_e \nu_\tau) R_e}} = 1.0002 \pm 0.0011$$

improved by Belle II recent prelim. measurement of $B_{\tau\mu}/B_{\tau e}$ [Adachi et al., 2024], was 1.0019 ± 0.0014

$$\left(\frac{m_\rho^2}{m_\lambda^2}\right) = 1 - 8x + 8x^3 - x^4 - 12x^2 \ln x$$

with $x = \frac{m_\rho^2}{m_\lambda^2}$, $\lambda, \rho = \text{lepton flavours}$

$R_\gamma^\lambda, R_W^{\lambda\rho}$ radiative corrections [Pich, 2014]

Lepton Flavour Universality, g_τ/g_μ coupling ratio

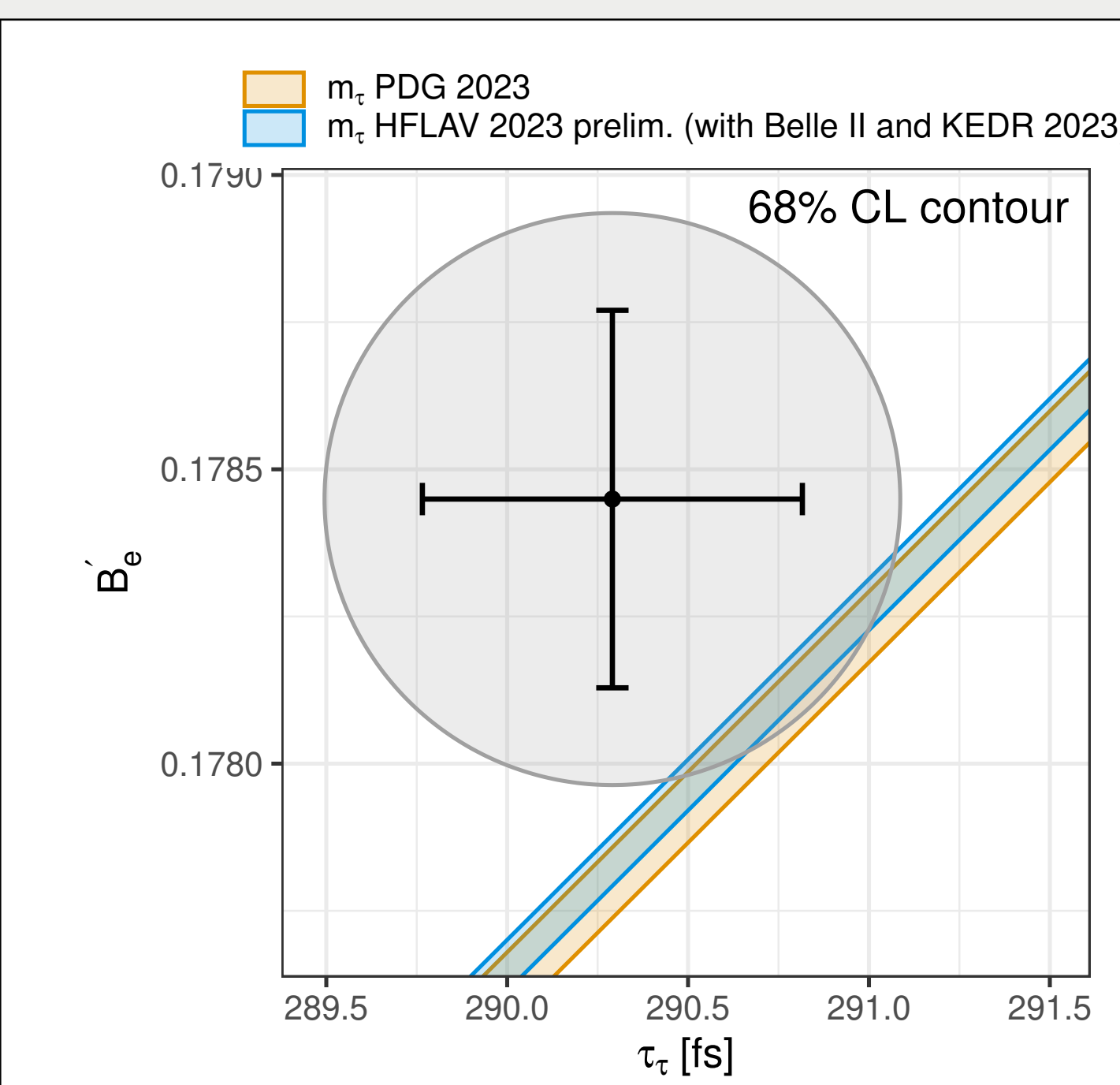
$$\left(\frac{g_\tau}{g_\mu}\right)_\pi = \sqrt{\frac{B(\tau \rightarrow \pi \nu_\tau) 2m_\pi m_\tau^2 R_\pi}{B(\pi \rightarrow \mu \bar{\nu}_\mu) (1 + \delta R_{\tau/\pi}) m_\pi^3 R_\tau}} \frac{1 - m_\mu^2/m_\pi^2}{1 - m_\pi^2/m_\tau^2} = 0.996 \pm 0.004$$

$$\left(\frac{g_\tau}{g_\mu}\right)_K = \sqrt{\frac{B(\tau \rightarrow K \nu_\tau) 2m_K m_\tau^2 R_K}{B(K \rightarrow \mu \bar{\nu}_\mu) (1 + \delta R_{\tau/K}) m_K^3 R_\tau}} \frac{1 - m_\mu^2/m_K^2}{1 - m_K^2/m_\tau^2} = 0.986 \pm 0.008$$

$\delta R_{\tau/\pi}, \delta R_{\tau/K}$ radiative corrections [Arroyo-Ureña et al., 2021; Amhis et al., 2023]

$$\left(\frac{g_\tau}{g_\mu}\right)_{\tau+\pi+K} = 1.0011 \pm 0.0014$$

“Canonical” tau Lepton Flavour Universality plot



$B_e' = \text{average of } B_e = B(\tau^- \rightarrow e^- \bar{\nu}_e \nu_\tau) \text{ and } B_e \text{ prediction from } B_\mu, B_\mu \frac{f(m_e^2/m_\tau^2) R_W^e R_\tau^e}{f(m_\mu^2/m_\tau^2) R_W^\mu R_\tau^\mu}$ proportional to g_e, g_μ

B_e' Standard Model prediction from tau lifetime

$$B(\mu \rightarrow e \bar{\nu}_e \nu_\mu) \frac{R_\tau^e m_\tau^5 f(m_e^2/m_\tau^2) R_W^e R_\tau^e}{R_\tau^\mu m_\tau^5 f(m_e^2/m_\tau^2) R_W^\mu R_\tau^\mu}$$

represented by oblique bands, whose widths are determined primarily by the tau mass precision (improved by recent Belle II [Adachi et al., 2023] & KEDR [Anashin et al., 2023] results)

$|V_{us}|$ from $B(\tau \rightarrow \text{“strange hadronic system”} + \nu)$, – “inclusive”

$$|V_{us}|_{\tau S} = \sqrt{R_S / \left[\frac{R_{VA}}{|V_{ud}|^2} - \delta R_{\tau-SU(3)\text{-break}} \right]}$$
 [Gámiz et al., 2003]

$\delta R_{\tau-SU(3)\text{-break}}$ accounts for SU(3)-breaking effects

$R_S = B(\tau \rightarrow \text{strange hadronic})/B_e^{\text{uni}}$, $R_{VA} = B(\tau \rightarrow \text{non-strange hadronic})/B_e^{\text{uni}}$

$|V_{us}|$ from $B(\tau \rightarrow \pi \nu)/B(\tau \rightarrow K \nu)$ and $B(\tau \rightarrow \pi \nu)$ – “exclusive”

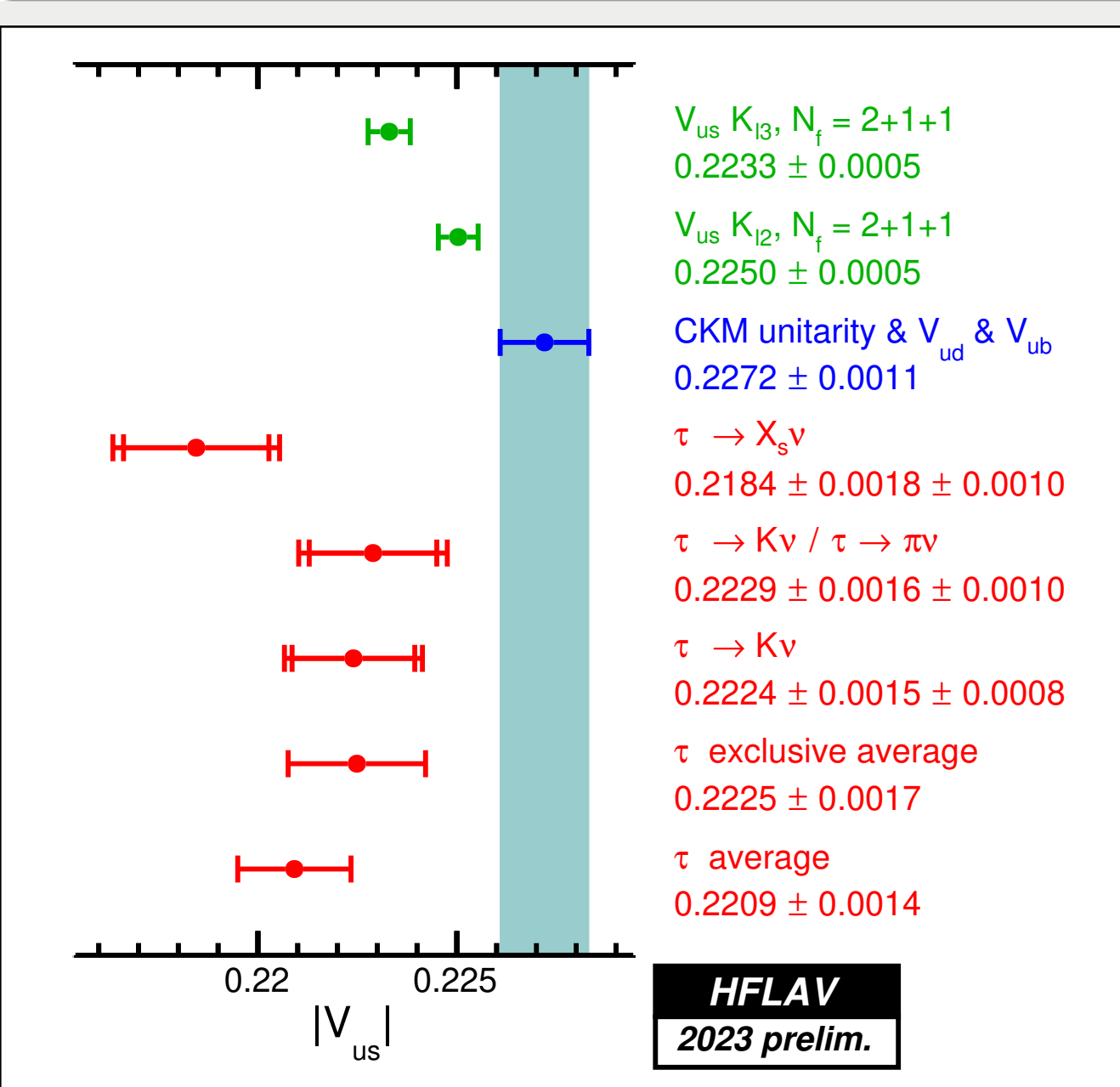
$$|V_{us}| = |V_{ud}| \sqrt{\frac{B(\tau^- \rightarrow K^- \nu_\tau) f_{K^\pm}^2 (m_\tau^2 - m_\pi^2)^2}{B(\tau^- \rightarrow \pi^- \nu_\tau) f_{K^\pm}^2 (m_\tau^2 - m_K^2)^2} \frac{1}{1 + \delta_{\tau K/\tau \pi}}}$$

$$|V_{us}| = \frac{1}{G_F f_{K^\pm}} \sqrt{\frac{16\pi \hbar B(\tau^- \rightarrow K^- \nu_\tau)}{\tau_\tau m_\tau^3 S_{EW}^2 (1 + \delta_{\tau K})}}$$

calculations require decay constants (obtained from lattice QCD averages) and radiative corrections

details in incoming HFLAV report (updated from previous HFLAV report)

$|V_{us}|$ from tau measurements



$|V_{us}|$ computed using tau measurements (red) compared with the determinations based on kaon measurements (green) [Cirigliano et al., 2023] and $|V_{us}|$ prediction assuming unitarity of first row of CKM matrix and the measured value of $|V_{ud}|$ [Cirigliano et al., 2023]

details in incoming HFLAV report

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