

# Analyzing semileptonic $b \rightarrow u$ transitions with vector and scalar leptoquarks

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# Introduction and Motivation

# Flavor Changing Charged Current ( $b \rightarrow c$ )

- With no concrete direct evidence for New Physics (NP) in the experimental sector, indirect channels can be a prominent way to look for NP.
- $B$  sector anomalies have hinted at NP presence.
- Experimental values of  $R(D)$  and  $R(D^*)$  in  $b \rightarrow c l \bar{\nu}_\ell$  transitions exhibit discrepancies at  $1.5\sigma$  and  $2.5\sigma$ , respectively from Standard Model (SM) predictions<sup>1</sup>

	Experimental value	SM value
$R(D)$	$0.342 \pm 0.026$	$0.298 \pm 0.004$
$R(D^*)$	$0.287 \pm 0.012$	$0.254 \pm 0.005$

where

$$R(D^{(*)}) = \frac{Br(B \rightarrow D^{(*)}\tau\nu_\tau)}{Br(B \rightarrow D^{(*)}l\nu_l)}$$

- The  $b \rightarrow c$  sector is a well-explored sector.

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<sup>1</sup><https://hflav-eos.web.cern.ch/hflav-eos/semi/moriond24/html/RDsDsstar/RDRDs.html>

# Flavor Changing Charged Current ( $b \rightarrow u$ )

- $b \rightarrow u l \nu_\ell$  sector is not extensively probed for NP. We examine the decay channel  $B_c \rightarrow D l \nu_\ell$  in this work.
- LHCb future upgrade is expected to measure these modes with sufficient accuracy <sup>2</sup>.
- Lattice QCD calculations for form factors <sup>3</sup> pertaining to these modes are also available.
- For  $b \rightarrow u$  transitions, only two decay channels (for  $\ell = \tau$ ) are experimentally observed.

	Experimental value <sup>4</sup>	Calculated SM value
$B \rightarrow \tau \nu_\tau$	$1.09 \pm 0.24 \times 10^{-4}$	$0.89 \pm 0.14 \times 10^{-4}$
$B \rightarrow \pi \tau \nu_\tau$	$< 2.5 \times 10^{-4}$	$1.14 \pm 0.18 \times 10^{-4}$

- Does not have sufficient number of observables to constrain NP. Existing constraints are also not reliable.

<sup>2</sup>R. Aaij et al. (LHCb Collaboration), arXiv:1808.08865

<sup>3</sup>Cooper, Laurence J. and Davies, Christine T. H. and Wingate, Matthew, Phys. Rev. D 105, 014503 (2022)

<sup>4</sup>S. Navas et al. (Particle Data Group), to be published in Phys. Rev. D 110, 030001 (2024)

# Motivation to correlate

- Unreliability on existing constraints motivates us to correlate Wilson coefficients of  $b \rightarrow u$  to properly observed  $b \rightarrow c$  transitions.
- Model dependent approach can be used to correlate and analyze.
- Here, we explore  $B_c \rightarrow D\tau\nu_\tau$  channel within two Leptoquark Models ( $U_1$  and  $S_1$ ).

# Theoretical Framework

# Effective Hamiltonian

Including NP contributions, the effective Hamiltonian for  $b \rightarrow q\ell\nu_\ell$  transitions can be written as

$$\mathcal{H}_{\text{eff}} = \frac{4G_F}{\sqrt{2}} V_{qb} [(1 + C_{V_L}) \mathcal{O}_{V_L} + C_{V_R} \mathcal{O}_{V_R} + C_{S_L} \mathcal{O}_{S_L} + C_{S_R} \mathcal{O}_{S_R} + C_T \mathcal{O}_T],$$

where  $q = u$  or  $c$ ;  $C_{V_L}$ ,  $C_{V_R}$ ,  $C_{S_L}$ ,  $C_{S_R}$  and  $C_T$  are the vector, scalar and tensor Wilson coefficients, and

$$\begin{aligned}\mathcal{O}_{V_L} &= (\bar{q}_L \gamma^\mu b_L)(\bar{\tau}_L \gamma^\mu \nu_{\ell L}) \\ \mathcal{O}_{V_R} &= (\bar{q}_R \gamma^\mu b_R)(\bar{\tau}_L \gamma^\mu \nu_{\ell L}) \\ \mathcal{O}_{S_L} &= (\bar{q}_R b_L)(\bar{\tau}_R \nu_{\ell L}) \\ \mathcal{O}_{S_R} &= (\bar{q}_L b_R)(\bar{\tau}_R \nu_{\ell L}) \\ \mathcal{O}_T &= (\bar{q}_R \sigma^{\mu\nu} b_L)(\bar{\tau}_R \sigma^{\mu\nu} \nu_{\ell L})\end{aligned}$$

are the four-fermion operators.

# Observables I

- Differential Branching Fraction

$$\frac{dBr}{dq^2}(B \rightarrow P\ell\nu_\ell) = \tau_B \frac{G_F^2 |V_{ub}|^2}{192\pi^3 M_B^3} q^2 \sqrt{\lambda_P(q^2)} \left(1 - \frac{m_\ell^2}{q^2}\right)^2 \times$$

$$\left\{ |1 + C_{V_L} + C_{V_R}|^2 \left[ \left(1 + \frac{m_\ell^2}{2q^2}\right) H_{V,0}^2 + \frac{3}{2} \frac{m_\ell^2}{q^2} H_{V,t}^2 \right] \right.$$

$$+ \frac{3}{2} |C_{S_L} + C_{S_R}|^2 H_S^2 + 8 |C_T|^2 \left(1 + \frac{2m_\ell^2}{q^2}\right) H_T^2$$

$$+ 3 \text{Re}[(1 + C_{V_L} + C_{V_R})(C_{S_L}^* + C_{S_R}^*)] \frac{m_\ell}{\sqrt{q^2}} H_S H_{V,t}$$

$$\left. - 12 \text{Re}[(1 + C_{V_L} + C_{V_R}) C_T^*] \frac{m_\ell}{\sqrt{q^2}} H_T H_{V,0} \right\},$$

# Observables II

where

$$\begin{aligned}
 H_{V,0}(q^2) &= \sqrt{\frac{\lambda_P(q^2)}{q^2}} f_+(q^2), \\
 H_{V,t}(q^2) &= \frac{M_B^2 - M_P^2}{\sqrt{q^2}} f_0(q^2) \\
 H_S(q^2) &= \frac{M_B^2 - M_P^2}{m_b - m_u} f_0(q^2) \\
 H_T(q^2) &= \frac{\sqrt{\lambda_P(q^2)}}{M_B + M_P} f_T(q^2)
 \end{aligned}$$

are helicity amplitudes and  $f_0(q^2)$ ,  $f_+(q^2)$  and  $f_T(q^2)$  are the scalar, vector and tensor form factors.

Also,  $\lambda_P(q^2) = ((M_B - M_P)^2 - q^2)((M_B + M_P)^2 - q^2)$ .

# Observables III

- **Lepton Flavor Universality (LFU) Ratio**

$$R = \frac{Br(B_c \rightarrow D\tau\nu_\tau)}{Br(B_c \rightarrow Dl\nu_l)}$$

- **Forward-Backward Asymmetry ( $A_{FB}$ )**

$$A_{FB} = \frac{\int_0^1 \frac{d^2\Gamma}{dq^2 d\cos\theta} d\cos\theta - \int_{-1}^0 \frac{d^2\Gamma}{dq^2 d\cos\theta} d\cos\theta}{d\Gamma/dq^2} = \frac{b_\theta(q^2)}{d\Gamma/dq^2}$$

where the angular decay distribution with respect to  $q^2$  and  $\theta$  is given by

$$\frac{d^2\Gamma}{dq^2 d\cos\theta}(B \rightarrow P\ell\nu_\ell) = a_\theta(q^2) + b_\theta(q^2) \cos\theta + c_\theta(q^2) \cos^2\theta,$$

and  $b_\theta$  determines the lepton forward-backward asymmetry.

# $U_1 = (3, 1)_{2/3}$ leptoquark model I

- Lagrangian<sup>5</sup>  $\implies \mathcal{L} \supset x_{ij}^{LL} \bar{Q}^i \gamma_\mu U_1^\mu P_L L^j + x_{ij}^{RR} \bar{d}_R^i \gamma_\mu U_1^\mu P_R l_R^j$
- Couplings in matrix form

$$x_{ij}^{LL(RR)} = \begin{matrix} u \\ c \\ t \end{matrix} \begin{pmatrix} e & \mu & \tau \\ \lambda_{11}^{L(R)} & \lambda_{12}^{L(R)} & \lambda_{13}^{L(R)} \\ \lambda_{21}^{L(R)} & \lambda_{22}^{L(R)} & \lambda_{23}^{L(R)} \\ \lambda_{31}^{L(R)} & \lambda_{32}^{L(R)} & \lambda_{33}^{L(R)} \end{pmatrix}$$

- Expanding in the mass basis and assuming rotation in the up-type quark sector, we have

$$\mathcal{L} = [(\lambda_{13}^L V_{ud} + \lambda_{23}^L V_{us} + \lambda_{33}^L V_{ub}) \bar{u} \gamma_\mu \nu_\tau + (\lambda_{13}^L V_{cd} + \lambda_{23}^L V_{cs} + \lambda_{33}^L V_{cb}) \bar{c} \gamma_\mu \nu_\tau + \lambda_{33}^L \bar{b}_L \gamma_\mu \tau_L + \lambda_{33}^R \bar{b}_R \gamma_\mu \tau_R] U_1^\mu$$

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<sup>5</sup>Arvind Bhaskar, Diganta Das, Tanumoy Mandal, Subhadip Mitra, and Cyrin Neeraj Phys. Rev. D 104, 035016 (2022)

# $U_1 = (3, 1)_{2/3}$ leptoquark model I

- Only  $C_{V_L}$  and  $C_{S_R}$  can be generated in  $U_1$  leptoquark model

$$C_{V_L}(\mu_{LQ}) = \frac{1}{2\sqrt{2}G_F V_{qb}} \frac{\lambda_{q\nu}^L (\lambda_{b\tau}^L)^*}{M_{U_1}^2}$$

$$C_{S_R}(\mu_{LQ}) = -\frac{1}{\sqrt{2}G_F V_{qb}} \frac{\lambda_{q\nu}^L (\lambda_{b\tau}^R)^*}{M_{U_1}^2}$$

# $U_1 = (3, 1)_{2/3}$ leptoquark model I

For  $b \rightarrow u$  transition

$$C_{V_L}(\mu_{LQ}) = \frac{1}{2\sqrt{2}G_F V_{13}} \frac{\sum_{i=1}^3 V_{1i} \lambda_{i3}^L \lambda_{33}^L}{M_{U_1}^2}$$

$$C_{S_R}(\mu_{LQ}) = -\frac{1}{\sqrt{2}G_F V_{13}} \frac{\sum_{i=1}^3 V_{1i} \lambda_{i3}^L \lambda_{33}^R}{M_{U_1}^2}$$

For  $b \rightarrow c$  transition

$$C_{V_L}(\mu_{LQ}) = \frac{1}{2\sqrt{2}G_F V_{23}} \frac{\sum_{i=1}^3 V_{2i} \lambda_{i3}^L \lambda_{33}^L}{M_{U_1}^2}$$

$$C_{S_R}(\mu_{LQ}) = -\frac{1}{\sqrt{2}G_F V_{23}} \frac{\sum_{i=1}^3 V_{2i} \lambda_{i3}^L \lambda_{33}^R}{M_{U_1}^2}$$

# $S_1 = (\bar{3}, 1)_{1/3}$ leptoquark model

- Lagrangian<sup>6</sup>  $\implies \mathcal{L} \supset [g_{ij}^L \bar{Q}_i^c(i\tau_2)L_j + g_{ij}^R \bar{u}_i^c \ell_{R_j}] S_1^\dagger$
- Couplings in matrix form

$$g_{ij}^{L(R)} = \begin{matrix} u \\ c \\ t \end{matrix} \begin{pmatrix} e & \mu & \tau \\ g_{11}^{L(R)} & g_{12}^{L(R)} & g_{13}^{L(R)} \\ g_{21}^{L(R)} & g_{22}^{L(R)} & g_{23}^{L(R)} \\ g_{31}^{L(R)} & g_{32}^{L(R)} & g_{33}^{L(R)} \end{pmatrix}$$

- Expanding in the mass basis and assuming rotation in the up-type quark sector, we have

$$\begin{aligned} \mathcal{L} = & \{ [g_{13}^L (V_{ud}^* \bar{u}^c + V_{cd}^* \bar{c}^c) + g_{23}^L (V_{us}^* \bar{u}^c + V_{cs}^* \bar{c}^c) + g_{33}^L (V_{ub}^* \bar{u}^c + V_{cb}^* \bar{c}^c)] \tau_L \\ & - g_{33}^L \bar{b}^c \nu_L + [g_{13}^R (V_{ud}^* \bar{u}^c + V_{cd}^* \bar{c}^c) + g_{23}^R (V_{us}^* \bar{u}^c + V_{cs}^* \bar{c}^c) \\ & + g_{33}^R (V_{ub}^* \bar{u}^c + V_{cb}^* \bar{c}^c)] \tau_R \} S_1^\dagger \end{aligned}$$

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<sup>6</sup>Ufuk Aydemir, Tanumoy Mandal and Subhadip Mitra, Phys. Rev. D 101, 015011 (2020)

# $S_1 = (\bar{3}, 1)_{1/3}$ leptoquark model

- Only  $C_{V_L}$ ,  $C_{S_L}$  and  $C_T$  can be generated in the  $S_1$  leptoquark model

For  $b \rightarrow u$  transition

$$C_{V_L}(\mu_{LQ}) = \frac{1}{2\sqrt{2}G_F V_{13}} \frac{\sum_{i=1}^3 V_{1i} g_{i3}^L g_{33}^L}{2M_{S_1}^2}$$

$$C_{S_L}(\mu_{LQ}) = -\frac{1}{2\sqrt{2}G_F V_{13}} \frac{\sum_{i=1}^3 V_{1i} g_{i3}^R g_{33}^L}{2M_{S_1}^2}$$

$$C_T(\mu_{LQ}) = -\frac{1}{4} C_{S_L}(\mu_{LQ})$$

For  $b \rightarrow c$  transition

$$C_{V_L}(\mu_{LQ}) = \frac{1}{2\sqrt{2}G_F V_{23}} \frac{\sum_{i=1}^3 V_{1i} g_{i3}^L g_{33}^L}{2M_{S_1}^2}$$

$$C_{S_L}(\mu_{LQ}) = -\frac{1}{2\sqrt{2}G_F V_{23}} \frac{\sum_{i=1}^3 V_{1i} g_{i3}^L g_{33}^L}{2M_{S_1}^2}$$

$$C_T(\mu_{LQ}) = -\frac{1}{4} C_{S_L}(\mu_{LQ})$$

# Renormalization-Group Equations (RGE)

Wilson coefficients at the Leptoquark scale ( $\mu_{LQ}$ ) scale are evolved to the  $\mu_b$  using RGE <sup>7</sup>

$$\begin{pmatrix} C_{V_L}(\mu_b) \\ C_{V_R}(\mu_b) \\ C_{S_L}(\mu_b) \\ C_{S_R}(\mu_b) \\ C_T(\mu_b) \end{pmatrix} \equiv \begin{pmatrix} 1.12 & 0 & 0 & 0 & 0 \\ 0 & 1.07 & 0 & 0 & 0 \\ 0 & 0 & 1.91 & 0 & -0.38 \\ 0 & 0 & 0 & 2.00 & 0 \\ 0 & 0 & 0 & 0 & 0.89 \end{pmatrix} \begin{pmatrix} C_{V_L}(\mu_{LQ}) \\ C_{V_R}(\mu_{LQ}) \\ C_{S_L}(\mu_{LQ}) \\ C_{S_R}(\mu_{LQ}) \\ C_T(\mu_{LQ}) \end{pmatrix}$$

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<sup>7</sup>Syuhei Iguro, Teppei Kitahara, Ryoutaro Watanabe, arXiv:2210.10751

# Analysis

# Constraints for the new couplings $C_i$

We use the following observables to constrain the new couplings :

- $b \rightarrow c$  sector

$\implies R(D), R(D^*), P_\tau^{D^*}$  and  $Br(B_c \rightarrow \tau \nu_\tau)$

- $b \rightarrow u$  sector

$\implies Br(B \rightarrow \tau \nu_\tau), Br(B \rightarrow \pi \tau \nu_\tau)$  and  $R_\pi^l$

where

$$R_\pi^l = \frac{Br(B \rightarrow \tau \nu_\tau)}{Br(B \rightarrow \pi l \nu_l)}$$

Observables	Experimental values
$R(D)^1$	$0.342 \pm 0.026$
$R(D^*)^1$	$0.287 \pm 0.012$
$P_\tau^{D^* 8}$	$0.38_{-0.55}^{+0.53}$
$Br(B_c \rightarrow \tau \nu_\tau)$	$< 30\%$
$Br(B \rightarrow \tau \nu_\tau)^4$	$1.09 \pm 0.24 \times 10^{-4}$
$Br(B \rightarrow \pi \tau \nu_\tau)^4$	$< 2.5 \times 10^{-4}$
$R_\pi^{l^4}$	$0.727 \pm 0.224$

Table: Numerical values of observables

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<sup>8</sup>S. Hirose et al. (Belle Collaboration) Phys. Rev. Lett. 118, 211801

- Predicted range for various couplings :

**Table:**  $U_1$  Leptoquark

Couplings	Range
$\lambda_{13}^L \lambda_{33}^L$	[-1.341 – 0.231]
$\lambda_{23}^L \lambda_{33}^L$	[0.271 – 0.833]
$\lambda_{33}^L \lambda_{33}^L$	[-1.991 – 1.642]
$\lambda_{13}^L \lambda_{33}^R$	[-0.011 – 0.089]
$\lambda_{23}^L \lambda_{33}^R$	[-0.261 – 0.059]
$\lambda_{33}^L \lambda_{33}^R$	[-0.321 – 1.972]
$C_{V_L}$	[-2.234 – 0.568]
$C_{S_R}$	[-0.131 – 0.039]

**Table:**  $S_1$  Leptoquark

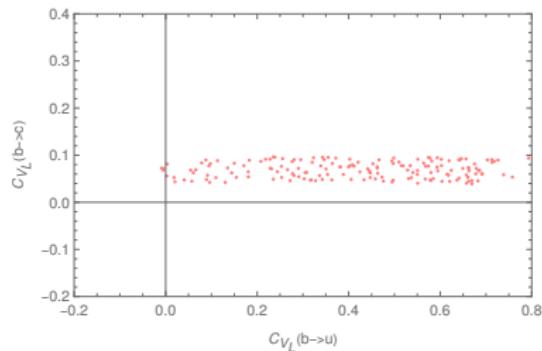
Couplings	Range
$g_{13}^L g_{33}^L$	[-0.193 – 0.083]
$g_{23}^L g_{33}^L$	[0.150 – 0.917]
$g_{33}^L g_{33}^L$	[-1.665 – 1.874]
$g_{13}^R g_{33}^L$	[-0.095 – 0.170]
$g_{23}^R g_{33}^L$	[-0.776 – 0.438]
$g_{33}^R g_{33}^L$	[-1.972 – 1.772]
$C_{V_L}$	[0.005 – 0.152]
$C_{S_L}$	[-0.011 – 0.046]
$C_T$	[-0.005 – 0.0012]

# SM and LQ predictions for Br. Ratio, $A_{FB}$ and LFU Ratio

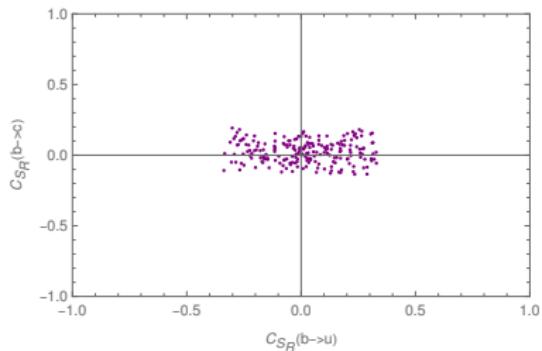
Observables	SM	$U_1$	$S_1$
$Br(B_c \rightarrow D\tau\nu_\tau)$	$(2.17 \pm 0.34) \times 10^{-5}$	$(2.21 - 4.93) \times 10^{-5}$	$(2.19 - 3.02) \times 10^{-5}$
$A_{FB}$	0.280	0.281 – 0.288	0.277 – 0.281
$R$	0.759	0.774 – 1.723	0.766 – 1.054

# Wilson coefficients correlation ( $U_1$ )

Figure: Correlation between Wilson coefficients of  $b \rightarrow u$  and  $b \rightarrow c$  for  $U_1$  leptoquark



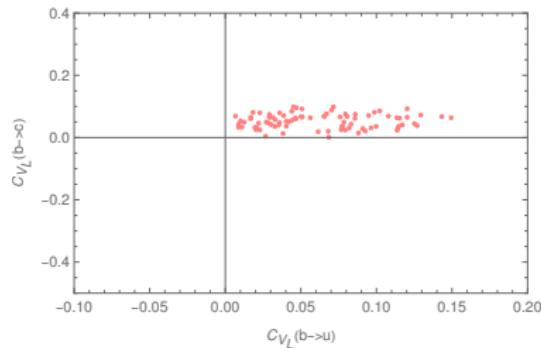
(a)  $C_{V_L}$



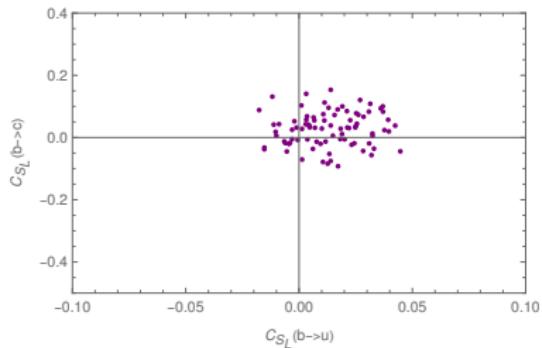
(b)  $C_{S_R}$

# Wilson coefficients correlation $S_1$

Figure: Correlation between Wilson coefficients of  $b \rightarrow u$  and  $b \rightarrow c$  for  $S_1$  leptoquark



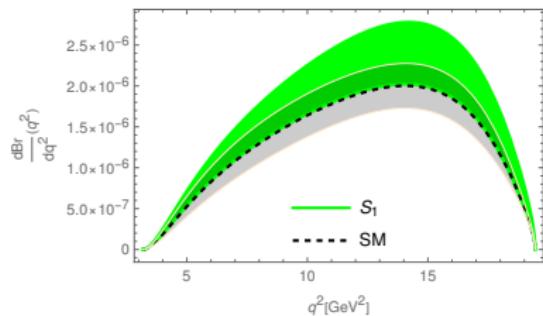
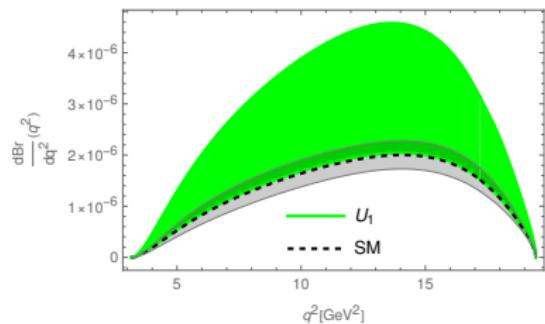
(a)  $C_{V_L}$



(b)  $C_{S_L}$

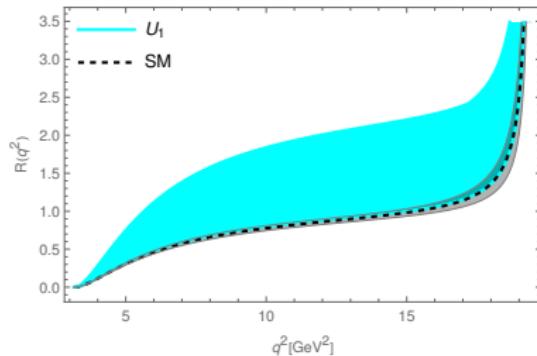
# Differential Branching Fraction

Figure:  $q^2$ -dependence of Differential Branching Fraction

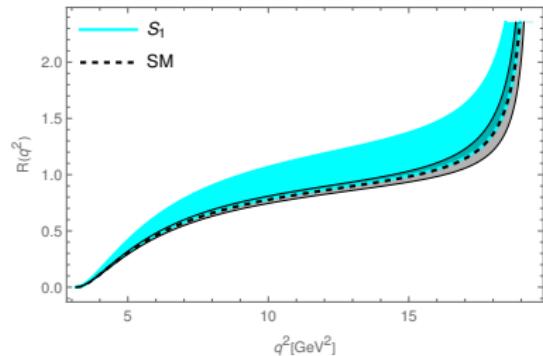


# Lepton Flavor Universality Ratio

Figure:  $q^2$ -dependence of LFU ratio  $R$



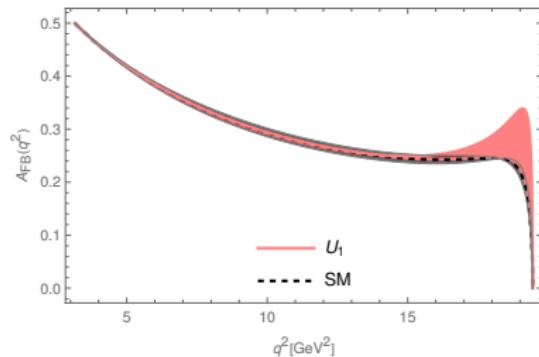
(a)  $U_1$  Leptoquark



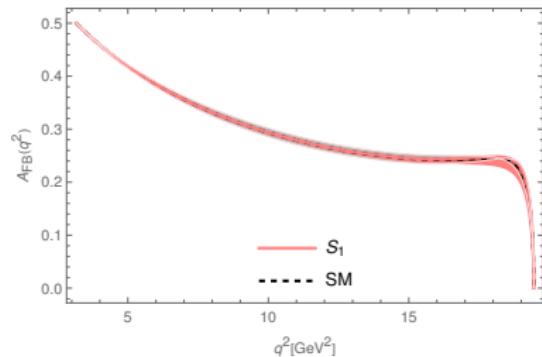
(b)  $S_1$  Leptoquark

# Forward-Backward Asymmetry

Figure:  $q^2$ -dependence of  $A_{FB}$



(a)  $U_1$  Leptoquark



(b)  $S_1$  Leptoquark

# Conclusion

# Conclusion

- $B_c \rightarrow D\tau\nu_\tau$  decay mode is analysed within the SM and in the  $U_1$  and  $S_1$  Leptoquark models.
- NP couplings are constrained using available experimental measurements in the  $b \rightarrow c$  and  $b \rightarrow u$  sectors.
- Predictions of various observables, such as  $dBr(B_c \rightarrow D\tau\nu_\tau)$ ,  $R$  and  $A_{FB}$  in SM as well as in  $U_1$  and  $S_1$  Leptoquark models are presented.
- The observables are found have more sensitivity in the presence of  $U_1$  leptoquark compared to  $S_1$  leptoquark.
- The LFU ratio can have large deviations from the SM and can be tested further to substantiate or rule out NP.
- $A_{FB}$  has less sensitivity to the leptoquarks.  $A_{FB}$  in presence of  $U_1$  leptoquark show deviations mainly at high  $q^2$ , where scalar coupling plays a dominating role.
- With future LHCb upgrade and precision measurements, these modes can be measured and tested for any NP sensitivity or constrain NP.

THANK YOU

BACK UP

# Form factor I

Form factors can be parametrized as

$$f(q^2) = P(q^2)^{-1} \sum_{n=0}^{N_n} c^{(n)} \hat{z}^{(n, N_n)}$$

where

$$z(q^2) = \frac{\sqrt{t_+ - q^2} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - q^2} + \sqrt{t_+ - t_0}}$$

and  $c^{(n)}$  is defined in reference. We use the Bourreley-Caprini-Lellouch (BCL) parametrization.

For  $f_0$

$$\hat{z}_0^{(n, N_n)} = z^n$$

For  $f_+$

$$\hat{z}_+^{(n, N_n)} = z^n - \frac{n(-1)^{N_n+1-n}}{N_n + 1} z_{N_n+1}$$

## Form factor II

$P(q^2)$  is given as

$$P(q^2) = 1 - \frac{q^2}{M_{res}^2}$$

and for  $f_0$  and  $f_+$  the value of  $M_{res}$  are

$m_{B(0^+)}$	5.627 GeV
$m_{B(1^-)}$	5.279 GeV

Results are derived from the Lattice QCD model. Details can be found in <sup>9</sup>

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<sup>9</sup>Cooper, Laurence J. and Davies, Christine T. H. and Wingate, Matthew, Phys. Rev. D 105, 014503 (2022)

# Decay Frame

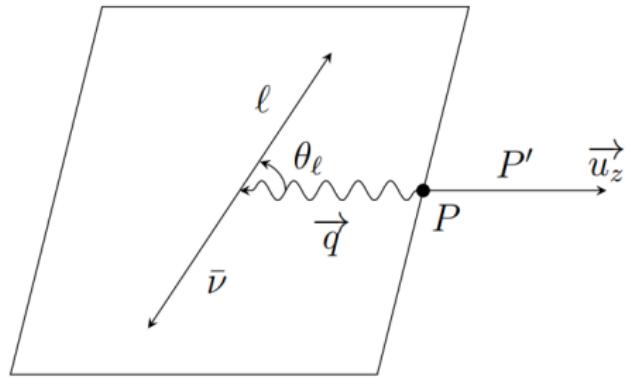
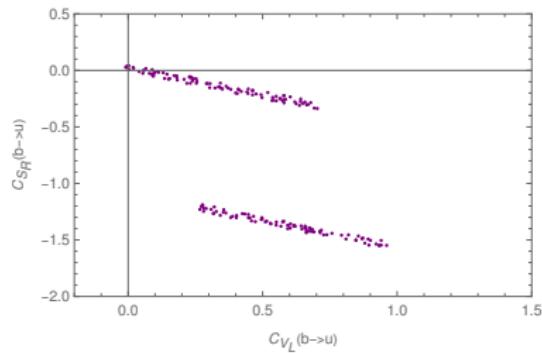


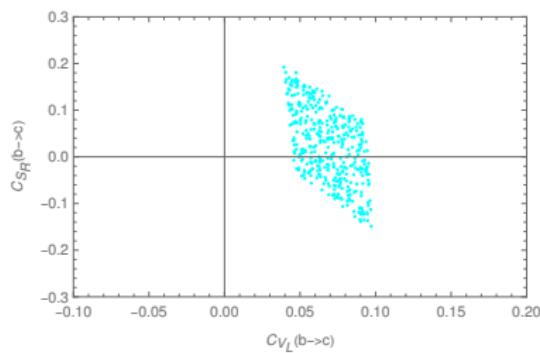
Figure: Angular convention for the process  $P \rightarrow P' \tau \bar{\nu}_\tau u \bar{d}$

$U_1$ 

**Figure:** Variation of Wilson coefficients  $C_{V_L}$  vs  $C_{S_R}$  for  $U_1$  leptoquark



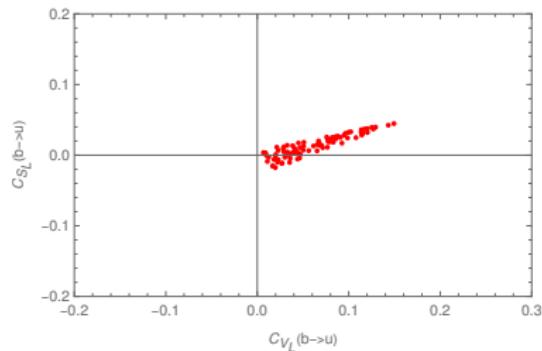
(a) For  $b \rightarrow u$  transition



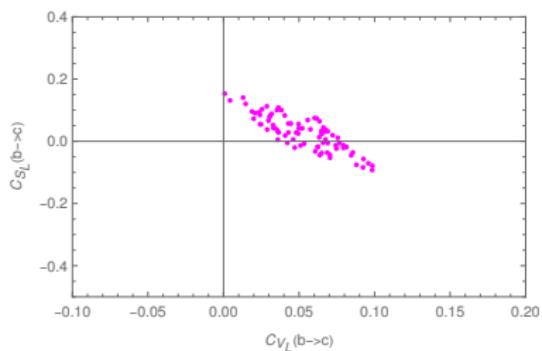
(b) For  $b \rightarrow c$  transition

$S_1$ 

**Figure:** Variation of Wilson coefficients  $C_{V_L}$  vs  $C_{S_R}$  for  $S_1$  leptoquark



(a) For  $b \rightarrow u$  transition



(b) For  $b \rightarrow c$  transition