Progress in the Unitarity Triangles (UTs) and in CP violation

Amarjit Soni
(BNL-HET)

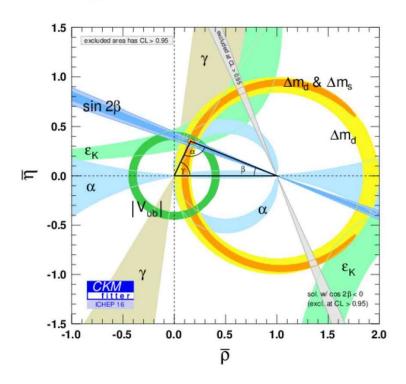
ICHEP-2024, Prague
07/18/24

Outline

- Motivation: It is exceedingly important to determine UTs as precisely as possible....
- Briefly recall special role of lattice BK in confirmation of KM theory of CPV
- Progress in lattice eps'....implications for both UTs though crucial for KUT
- K UT
- B UT: esp gamma
- Summary

Use exptal data + lattice WME to test KM picture of CPV

http://ckmfitter.in2p3.fr see also http://www.utfit.org



Neutral-Kaon Mixing from (2 + 1)-Flavor Domain-Wall QCD

D. J. Antonio, P. A. Boyle, T. Blum, P. A. H. Christ, S. D. Cohen, C. Dawson, T. Izubuchi, R. D. Kenway, C. Jung, S. Li, M. F. Lin, R. D. Mawhinney, J. Noaki, S. Ohta, P. S. Ohta, P. J. Pendleton, E. E. Scholz, A. Soni, R. J. Tweedie, and A. Yamaguchi

(RBC and UKQCD Collaborations)

¹SUPA, School of Physics, The University of Edinburgh, Edinburgh EH9 3JZ, United Kingdom
 ²RIKEN-BNL Research Center, Brookhaven National Laboratory, Upton, New York 11973, USA
 ³Physics Department, Columbia University, New York, New York 10027, USA
 ⁴Brookhaven National Laboratory, Upton, New York 11973, USA
 ⁵SUPA, Department of Physics & Astronomy, University of Glasgow, Glasgow G12 8QQ, United Kingdom
 ⁶Institute for Theoretical Physics, Kanazawa University, Kanazawa 920-1192, Japan
 ⁷School of Physics and Astronomy, University of Southampton, Southampton SO17 1BJ, United Kingdom
 ⁸Physics Department, University of Connecticut, Storrs, Connecticut 06269-3046, USA
 ⁹Institute of Particle and Nuclear Studies, KEK, Tsukuba, Ibaraki 305-0801, Japan
 ¹⁰Physics Department, SOKENDAI, Tsukuba, Ibaraki 305-0801, Japan
 (Received 9 February 2007; revised manuscript received 6 September 2007; published 22 January 2008)

We present the first results for neutral-kaon mixing using (2 + 1)-flavors of domain-wall fermions. A new approach is used to extrapolate to the physical up and down quark masses from our numerical studies with pion masses in the range 240-420 MeV; only $SU(2)_L \times SU(2)_R$ chiral symmetry is assumed and the kaon is not assumed to be light. Our main result is $B_K^{\overline{\text{MS}}}(2 \text{ GeV}) = 0.524(10)(28)$ where the first error is statistical and the second incorporates estimates for all systematic errors.

iviain points for 40+years on lattice eps' effort

- Calculational framework for K=> pi pi & eps'
- Obstacles aglore and major break-throughs

- Lattice chiral symmetry even for a finite non-vanishing lattice spacing! :
- Direct K=> pi pi w/o ChPT using finite vol correlation functions
- Non-perurbative renormalization
- 1st [prot-type] demonstration....~2015
- Difficulty therein: strong I=0 pi pi phase
- 1st complete result with GPBC, 2020
- 2nd independent method (PBC) developed, 2023
- Lattice applications to K and B-UTs

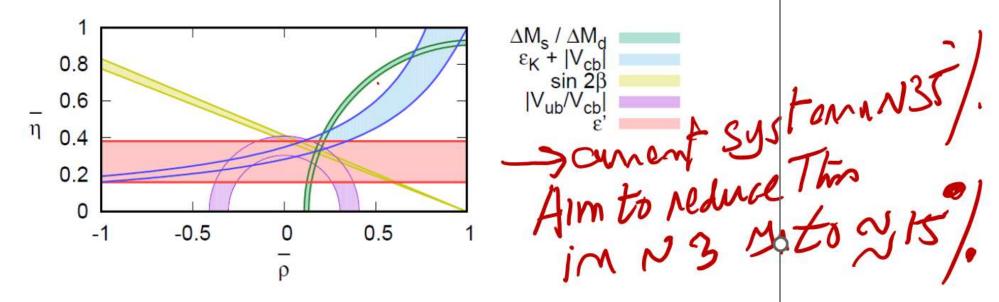


FIG. 12: The horizontal-band constraint on the CKM matrix unitarity triangle in the $\bar{\rho} - \bar{\eta}$ plane obtained from our calculation of ε' , along with constraints obtained from other inputs [6, 70, 71]. The error bands represent the statistical and systematic errors combined in quadrature. Note that the band labeled ε' is historically (e.g. in Ref. [72]) labeled as ε'/ε , where ε is taken from experiment.

<	W	<u></u>			A
	Q2	R	12	26 JM	AO
A &		191	•0		

	F	$Re(A_0)$	Ir	$m(A_0)$
i	$(q,q) (\times 10^{-7} \text{ GeV})$	$(\gamma^{\mu}, \gamma^{\mu}) (\times 10^{-7} \text{ GeV})$	$(q,q) (\times 10^{-11} \text{ GeV})$	$(\gamma^{\mu}, \gamma^{\mu}) (\times 10^{-11} \text{ GeV})$
1	0.383(77)	0.335(64)	0	0
2	2.89(30)	2.81(28)	0	0
3	0.0081(58)	0.0050(42)	0.20(14)	0.12(10)
4	0.081(23)	0.088(17)	1.24(35)	1.34(27)
5	0.0380(68)	0.0339(53)	0.552(99)	0.492(77)
6	-0.410(28)	-0.398(27)	-8.78(60)	-8.54(57)
7	0.001863(56)	0.001900(56)	0.02491(75)	0.02540(75)
8	-0.00726(14)	-0.00708(13)	-0.2111(40)	-0.2060(39)
9	$-8.7(1.5) \times 10^{-5}$	$-8.5(1.4) \times 10^{-5}$	-0.133(22)	-0.128(21)
10	$2.37(38) \times 10^{-4}$	$2.13(32) \times 10^{-4}$	-0.0304(49)	-0.0273(41)
Total	2.99(32)	2.86(31)	-7.15(66)	-6.93(64)

TABLE XVIII: The contributions of each of the ten four-quark operators to $Re(A_0)$ and $Im(A_0)$ for the two different RI-SMOM intermediate schemes. The scheme and units are listed in the column headers. The errors are statistical, only.

Chriskoly et el PRO 2020

EXPT

Quantity	Value
$Re(A_0)$	$2.99(0.32)(0.59)\times10^{-7} \text{ GeV}$
$Im(A_0)$	$-6.98(0.62)(1.44)\times10^{-11} \text{ GeV}$
$Re(A_0)/Re(A_2)$	19.9(2.3)(4.4)
$\operatorname{Re}(\varepsilon'/\varepsilon)$	0.00217(26)(62)(50)
	$Re(A_0)$ $Im(A_0)$ $Re(A_0)/Re(A_2)$

TABLE I: A summary of the primary results of this work. The values in parentheses give the statistical and systematic errors, respectively. For the last entry the systematic error associated with electromagnetism and isospin breaking is listed separately as a third error contribution.

IB leased on libielianoctal THEN 2020

Motivations for independent calculation of eps' with PBC

- For the first time RBC-UKQCD calculated eps' from 1st principles with a modest accuracy of ~35%. Because of naturalness reasoning, continuing to search for a BSM-CP odd phase with eps' is important and therefore continuing to calculate eps' with better accuracy is highly desirable.
- With GPBC configs have to be specially created making it very expensive to use multiple lattice spacings for taking a continuum limit.
- With PBC no need for special configs and in fact two different lattice spacings with ~physical pions already exist, so taking the continuum limit seems a lot more viable
- Given the importance of the result on eps' and the complexity of the calculation, an independent calculation of K=> 2 pion and epsilon' with possibly using PBC seems highly desirable
- With GPBC a lattice calculation of corrections on eps' due to EM+isospin appears very difficult, with PBC this may be less problematic
- Driving force behind current RBC/UKQCD-PBC effort is Masaaki Tomii

Ensembles already generated for periodic BC

a² [GeV⁻²]

- ► 24³ x 64, $a^{-1} = 1.0$ GeV: measurements w 258 confs done \rightarrow soon 440 confs
- ► 32³ x 64, $a^{-1} = 1.4$ GeV: measurements w 107 confs done $\rightarrow \sim 250$ confs in a year
- ► $48^3 \times 96$, $a^{-1} = 1.7 \text{ GeV } \& 64^3 \times 128$, $a^{-1} = 2.4 \text{ GeV}$: future work

Precision performance

			32 ³ G-parity BC (previous work)	24 ³ Periodic BC	32 ³ Periodic BC (w/o AMA correction)
	70	# of configurations	741	258)	107
		$\Delta I = 1/2 \text{ ME via } Q_2^{\text{lat}}$	10%	14%	14%
Error % (statistical)		$\Delta I = 1/2 \text{ ME via } Q_6^{lat}$	6.5%	8.9%	11%
,		Re A ₀	11%	13%	14%
				Prelin	ninary

 Good precision performance of PBC (ME with excited-state ππ) compared to G-parity BC calculation (ME with ground-state ππ) my 1 : 2306 06781 (x bl on try 258 g.c

Massak, Tetal

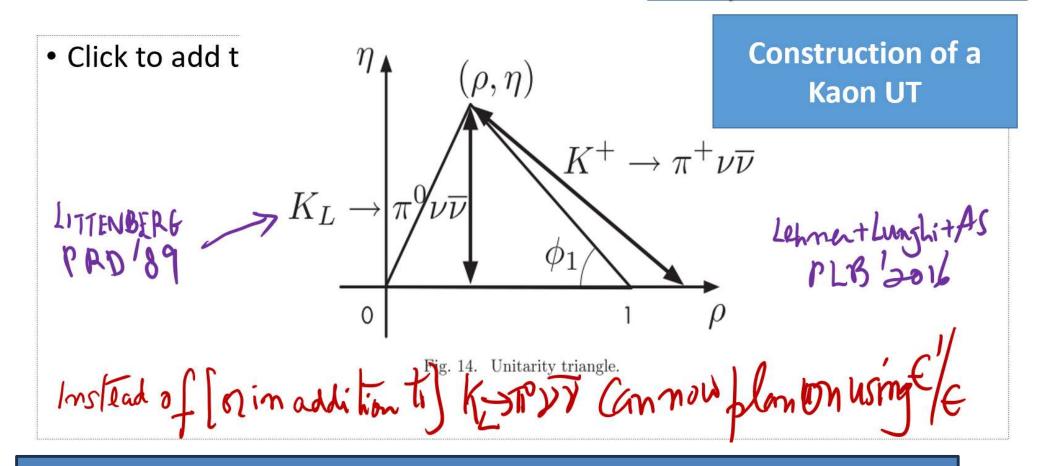
Quantity	This work	Experiment	
$Re(A_2)$	$1.74(15)(48) \times 10^{-8} \text{ GeV}$	$1.479(4) \times 10^{-8} \text{ GeV}$	
$\operatorname{Im}(A_2)$	$-5.91(13)(1.75) \times 10^{-13} \text{ GeV}$		
$\operatorname{Re}(A_0)$	$3.13(69)(95) \times 10^{-7} \text{ GeV}$	$3.3201(18) \times 10^{-7} \text{ GeV}$	
$\operatorname{Im}(A_0)$	$-9.3(1.5)(2.8)\times 10^{-11}~{\rm GeV}$		SXI
$\operatorname{Re}(A_0)/\operatorname{Re}(A_2)$	18.0(4.4)(7.4)	22.45(6)	
$\omega = \operatorname{Re}(A_2)/\operatorname{Re}(A_0)$	0.056(14)(23)	0.04454(12)	
$\operatorname{Re}(\varepsilon'/\varepsilon)$	$31.8(6.3)(11.8)(5.0) \times 10^{-4}$	$16.6(2.3) \times 10^{-4}$	

TABLE I. A summary of the primary results of this work shown in the middle column. The values in parentheses give the statistical and systematic errors, respectively. For the last entry the systematic error associated with electromagnetic and isospin breaking effects is listed separately as the third error, which we inherit from the estimation in Ref. [2] based on the large- N_c expansion of QCD and ChPT [49]. The corresponding experimental values are shown in the right column if applicable.

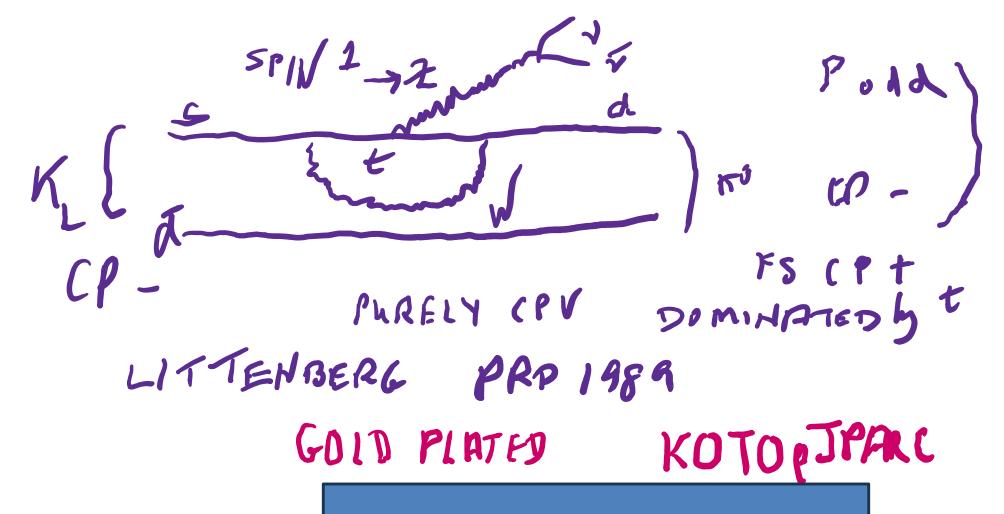
K-UT..MANY REASONS TO GO FOR IT E.G. LONG-STANDING ISSUES INCLUSIVE VERSUS EXCLUSIVE TENSION IN VXB

K-UT: A dream for some

Blucher, Winstein and Yamanaka '09; see also Buras



Also constrain KL=>pi0 nu nu via K0=>pi0 mu+mu- (c AS in Lat23)



BUT EXPERIMENTALLY extremely challenging

"NOTHING TO NOTHING"

4,0 74 WITH ENPICO LUNGI Try Reduce LD unjustainty WIP

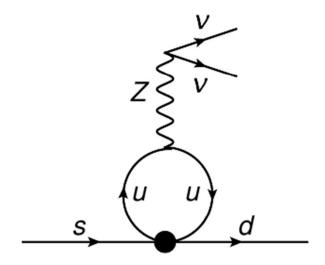


Figure 1. Long distance contributions to $K^+ \to \pi^+ \nu \bar{\nu}$ at the quark level.

CECCUCCI Rev.

$$B(K^+ \to \pi^+ \nu \bar{\nu}) = (8.39 \pm 0.30) \times 10^{-11} \left[\frac{|V_{cb}|}{40.7 \times 10^{-3}} \right]^{2.8} \left[\frac{\gamma}{73.2^{\circ}} \right]^{0.74}.$$

In the above formula, the explicit numerical uncertainty is the theoretical one originating from QCD and electroweak uncertainties, which amounts to 3.6%. Taking the latest values (28) for $|V_{cb}|_{avg} = (41.0 \pm 1.4) \times 10^{-3}$ and $\gamma = (72.1^{+4.1}_{-4.5})^{\circ}$, one finds the following:

$$B(K^+ \to \pi^+ \nu \bar{\nu})_{SM} = (8.5 \pm 1.0) \times 10^{-11}$$
.

The predictions are currently dominated by the parametric uncertainty that will plausibly be reduced by new measurements of $|V_{cb}|$ and γ by LHCb and Belle II.

cannot be detected. A long series of decay-at-rest searches for $K^+ \to \pi^+ \nu \bar{\nu}$ have culminated with the final results of the BNL E787/E949 experiments, which found the following (50):

$$B(K^+ \to \pi^+ \nu \bar{\nu})_{E787/E949} = (17.3^{+11.5}_{-10.5}) \times 10^{-11}.$$

From these analyses, the best upper limit, at 90% confidence level (CL), has been obtained:

$$B(K^+ \to \pi^+ \nu \bar{\nu})_{\text{NA62(2016-2017)}} \le 17.8 \times 10^{-11}.$$

The 2016–2017 data also allow one to set a 68% CL mean value for the branching ratio:

$$B(K^+ \to \pi^+ \nu \bar{\nu})_{\text{NA62(2016-2017)}} = (4.8^{+7.2}_{-4.8}) \times 10^{-11}$$
.

CECCUCCI Rev.

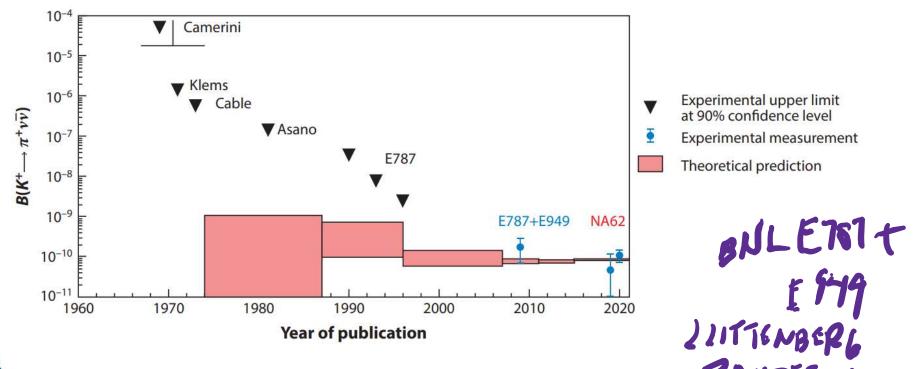


Figure 4

Timeline of theoretical predictions and experimental results for $K^+ \to \pi^+ \nu \bar{\nu}$ (10, 51, 57–64). Figure adapted with permission from Reference 58; copyright 2020 CERN for the benefit of the NA62 Collaboration.

the NA62 Collaboration reported the following:

$$B(K^+ \to \pi^+ \nu \bar{\nu})_{\text{NA62(2016-2018)}} = (11.0^{+4.0}_{-3.5 \text{ stat}} \pm 0.3_{\text{syst}}) \times 10^{-11},$$

CECCUCCI Rev.

$$B(K_L^0 \to \pi^0 \nu \bar{\nu}) = (3.36 \pm 0.05) \times 10^{-11} \left[\frac{|V_{ub}|}{3.88 \times 10^{-3}} \right]^2 \left[\frac{|V_{cb}|}{40.7 \times 10^{-3}} \right]^2 \left[\frac{\sin \gamma}{\sin 73.2^{\circ}} \right]^2,$$

which, taking the latest values (28) for $|V_{cb}|_{avg} = (41.0 \pm 1.4) \times 10^{-3}$, $|V_{ub}|_{avg} = (3.82 \pm 0.24) \times 10^{-3}$, and $\gamma = (72.1^{+4.1}_{-4.5})^{\circ}$, leads to the following numerical prediction:

$$B(K_L^0 \to \pi^0 \nu \bar{\nu}) = (3.2 \pm 0.6) \times 10^{-11}$$
.

While the experimental situation for $K^+ \to \pi^+ \nu \bar{\nu}$ shows that we have two independent experimental techniques that can reach SM sensitivities, with the NA62 experiment on the way to making a precise measurement, the situation for the neutral mode is more complex. Progress has been hampered by the lack of a clean experimental signature because no redundancy is available once the π^0 mass is used as a constraint to reconstruct the decay vertex. The KOTO experiment at J-PARC builds on the experience of the predecessor experiment E391a (67), which was performed at KEK. It is based on the technique of letting a well-collimated "pencil" beam enter the decay region surrounded by high-performance photon vetoes. By vetoing extra photons and applying a transverse momentum cut (150 MeV/c) to eliminate residual $\Lambda \to n\pi^0$ decays, KOTO is expected to reach SM sensitivities by the mid-2020s. The KOTO experiment has published the best upper limit (68):

n sbut

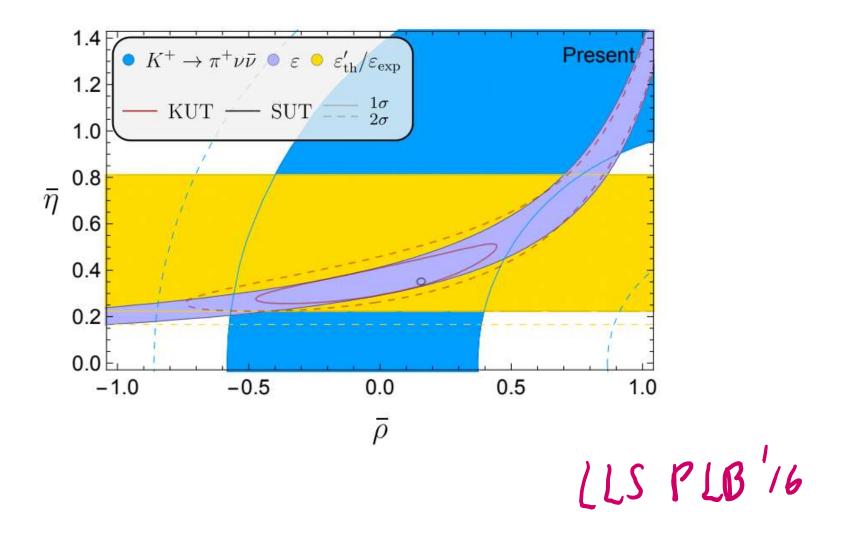
$$B(K_L^0 \to \pi^0 \nu \bar{\nu})_{\text{KOTO}} < 3.0 \times 10^{-9} \, (90\% \, \text{CL}).$$

2 orders of magnitude togo

- LHCb: Ks
- JPARC:KL
- Pheno: Isidori et al...;D'Ambrosio et al;Schact + AS (WIP)
- Lattice: RBC+UKQCD many papers on closely related rare K-decays

71910-10644 1866-11520 1701.08258

KOTO Ipple



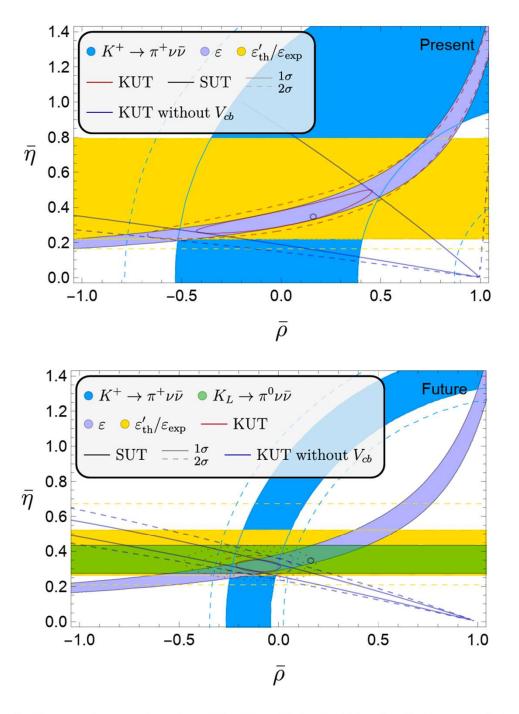


Figure 5. Top panel: current status of the Kaon Unitarity Triangle. Bottom panel: impact of improved calculations of $\text{Im}A_{0,2}$ from lattice QCD and of expected measurements of charged (NA62) and neutral (KOTO) $K \to \pi \nu \bar{\nu}$ branching ratios on the Kaon Unitarity Triangle. The two dotted contours are the 3σ and 4σ KUT contours, respectively.

UT ANGLE GAMMA = 0 = - arg (- Var Vul)

Dalitz analysis: Giri, Grossman, Soffer & Zupan PRD '03; Atwood, Dunietz + AS, PRD'01

ADS also PRL'97

- Both emphasize model independent (diff approaches) analysis
- via the Dalitz plot
- Following the then existing experimental data from F 637 Collab It should be realized that three body states $K^+\rho^-$, $K_s\rho^0$? analysis $U_{and}^*K^{*+}\pi^-$ can all lead to the common final state (though it $d_{\mathfrak{C}}K_s\pi^+\pi^-$. If one examines the distribution in phase space,
 - 1.Briefly ADS uses local regions of DP to look for minimum values of gamma; followed by searches globally
 - 2. The crucial point is that it then uses A+S method of "optimized observables" (PRD92) and demonstrates that

solution to gamma thus obtained are just as good as the optimal construction gives

VERY HOPEFUL THAT BELLE-II (MAY BE EVEN LHCB?) WILL BE ABLE TO HANDLE FS WITH 1 PIO

Optimised observables (Atwood+AS, PRD 45,'92); see esp sec III

7 you are asing crypts hate to determine

expand the total differential cross section in terms of λ we have

$$\Sigma = \Sigma_0 + \lambda \Sigma_1$$

(6)

Construction is used extensively these days in ML applications

$$f = f_{\text{opt}} = \frac{\Sigma_1}{\Sigma_0} .$$

The ultimate theoretical error on γ from $B \to DK$ decays

Secana Miss wholy ministed higher order

CORNECTION Y ISTRIBUTED

In the SM-KM

bearedign of

CPV

Joachim Brod and Jure Zupan

Department of Physics, University of Cincinnati, Cincinnati, Ohio 45221, U.S.A.

E-mail: brodjm@ucmail.uc.edu, zupanje@ucmail.uc.edu

ABSTRACT: The angle γ of the standard CKM unitarity triangle can be determined from $B \to DK$ decays with a very small irreducible theoretical error, which is only due to second-order electroweak corrections. We study these contributions and estimate that their impact on the γ determination is to introduce a shift $|\delta\gamma| \lesssim \mathcal{O}(10^{-7})$, well below any present or planned future experiment.

III Indirect CP violation BNL 1964 Fitch, Cromin, Christensen+ Tundang To CPV in state mixing, 15=2 Heff

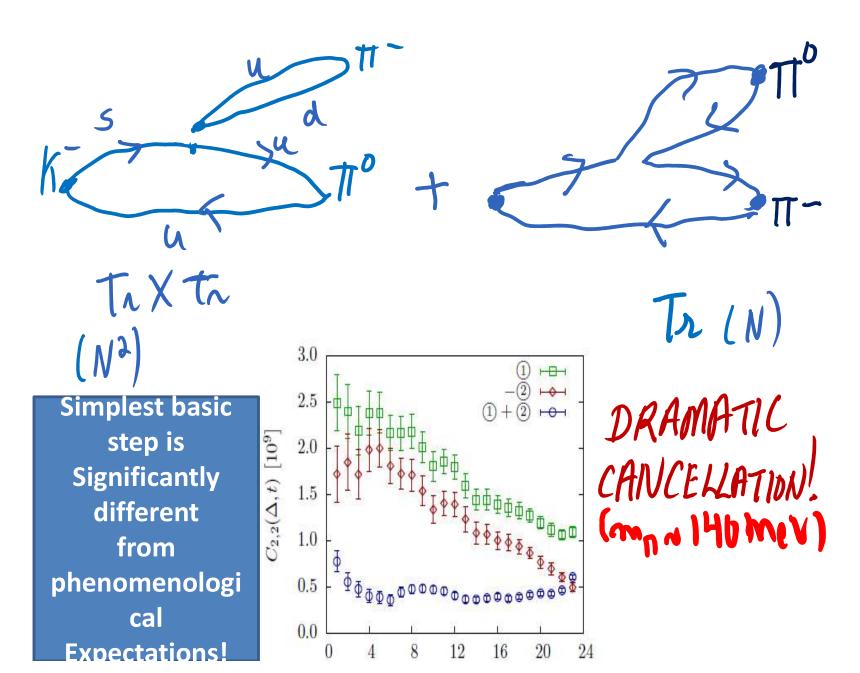
IN NATURALNESS WE TRUST

Summary + Outlook

- After decades of development and effort, using DWQ, and GPBC in 2020 completed the 1st calculation of eps' with a modest accuracy of 35% at a single of lattice spacing~1.38 GeV; resulting eps' is compatible with experiment within 1 sigma [also attained qualitative and quantitative understanding of the Delta I=1/2 Rule]
- We are well on our way to get eps' along with scattering phases again, in a completely independent set up using PBC. Driving force for this effort is MASAAKI TOMII. With this method we are hopeful to get eps' for the 1st time in the continuum limit
- Showed how using eps' + eps + Br (K+ => pi+ nu nu) can construct the K-UT
- Also K0=>pi0 mu+ mu- input from LHCb, JPARC, pheno and lattice should provide important constraints for the gold plated KL=>pi0 nu nu mode being pursued by the KOTO expt @ JPARC
- UT gamma: D0 Dalitz decays with 1 pi0 in FSBelle-II, LHCb
- UT gamma: ADS PRD method should also be used => v likely get improve results
- It is exceedingly important to determine/constrain UTs as precisely as possible as it is highly unlikely to be just a triangle

EXTRA'S

Dissecting (the much easier) $\Delta I=3/2$ [I=2 $\pi\pi$] Amp on the lattice: 2 contributing topologies only



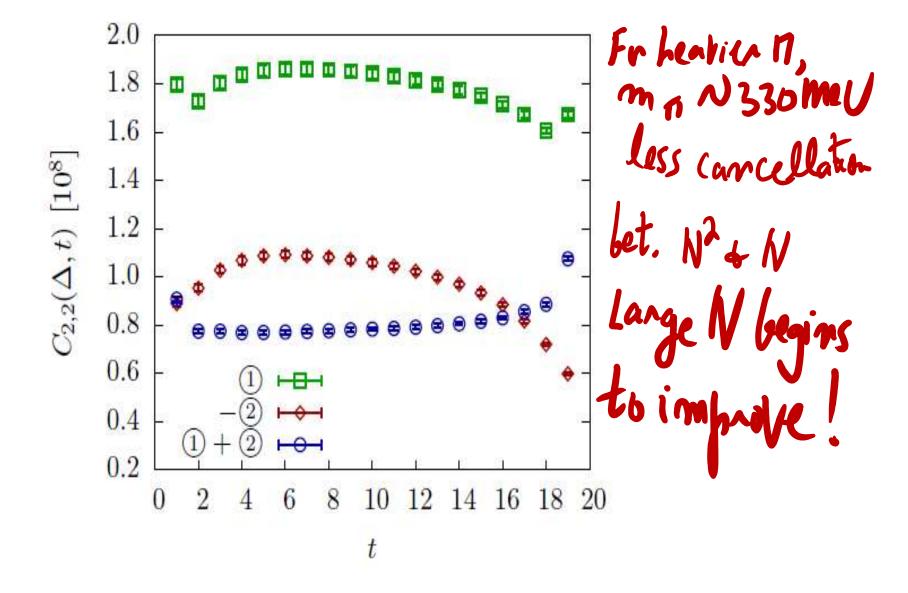


FIG. 3: Contractions ①, -② and ① + ② as functions of t from the simulation at threshold with $m_{\pi} \simeq 330 \,\text{MeV}$ and $\Delta = 20$.

USED for Ao <u>Ensemble</u>

• 32^3 x64 Mobius DWF ensemble with IDSDR gauge action at β =1.75. Coarse lattice spacing (a-1=1.378(7) GeV) but large, (4.6 fm)3 box.

machines at ANL and the STFC BG/O "DiRAC" machines at Edinburgh, UK.

- Using Mobius params (b+c)=32/12 and L =12 obtain same explicit χSB as the L_s=32 Shamir DWF + IDSDR ens. used for ΔI =3/2 but at reduced cost. • Utilized USQCD 512-node BG/Q machine at BNL, the DOE "Mira" BG/Q
- Performed 216 independent measurements (4 MDTU sep.).
- Cost is ~1 BG/Q rack-day per complete measurement (4 configs generated + 1 set of contractions).
- G-parity BCs in 3 spatial directions results in close matching of kaon and $\pi\pi$ energies:

 $E_{\pi\pi}(I=0) = 498(11) \text{ MeV}$ $E_{\pi\pi}(I=2) = 573.0(2.9) \text{ MeV}$ $E_{\pi}=274.6(1.4) \text{ MeV} \qquad (m_{\pi} = 143.1(2.0) \text{ MeV})$

$$m_{\kappa} = 490.6(2.4) \text{ MeV}$$

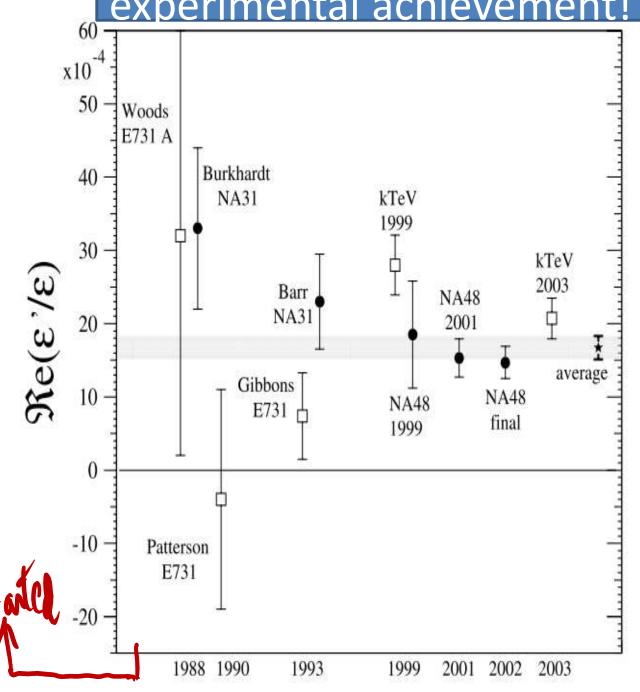
$$E_{\pi\pi}(I=0) = 498(11) \text{ MeV}$$

$$E_{\pi\pi}(I=2) = 573.0(2.9) \text{ MeV}$$

$$E_{\pi} = 274.6(1.4) \text{ MeV}$$
 $(m_{\pi} = 143.1(2.0) \text{ MeV})$

45

A monumental experimental achievement!



Kmad kleinknecht "UncabigCPV"

16.6(2.3) X10 PDG 2014

Error source	Value
Excited state	-
Unphysical kinematics	5%
Finite lattice spacing	12%
Lellouch-Lüscher factor	1.5%
Finite-volume corrections	7%
Missing G_1 operator	3%
Renormalization	4%
Total	15.7%

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Error source	Value	
	$Re(A_0)$	$Im(A_0)$
Matrix elements	15.7%	15.7%
Parametric errors	0.3%	6%
Wilson coefficients	12%	12%
Total	19.8%	20.7%

21/.

TABLE XXV: Relative systematic errors on the infinite-volume matrix elements of

 $\overline{\text{MS}}$ -renormalized four-quark operators Q'_i .

TABLE XXVI: Relative systematic errors on $Re(A_0)$ and $Im(A_0)$.

Numerical results will be Superseded by the higher Stations Adventure Re(A) and Re

Results for ϵ'

Using Re(A) and Re(A) from experiment (A and the phas shifts

and our lattic value for e s



RBC-UKQCD PRL'15 EDITOR'S CHOICE

$$\operatorname{Re}\left(\frac{\varepsilon'}{\varepsilon}\right) = \operatorname{Re}\left\{\frac{i\omega e^{i(\delta_2 - \delta_0)}}{\sqrt{2}\varepsilon} \left[\frac{\operatorname{Im} A_2}{\operatorname{Re} A_2} - \frac{\operatorname{Im} A_0}{\operatorname{Re} A_0}\right]\right\}$$

LARGE CANCELLATION!!

$$= 1.38(5.15)(4.43) \times 10^{-4},$$
$$16.6(2.3) \times 10^{-4}$$

216 gye Config

Bearing in mind the largish errors in this first calculation, we interpret that our result are consistent with experiment at $\sim 2\sigma$ level

W= ReAz NO.145
ReAs ICHEP-202

Of ompated neviz executing agreement v

Computed ReA0 good agreement with expt

Offered an "explanation" of the Delta I=1/2 enhancement

ICHEP-2024(Prague); A Soni (BNL-HET)

er

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Error source	Value
Excited state	-
Unphysical kinematics	5%
Finite lattice spacing	12%
Lellouch-Lüscher factor	1.5%
Finite-volume corrections	7%
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Systemata emos

le Ao	Error source	Value	
e j io		Re(A ₀)	$Im(A_0)$
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120/	Wilson coefficients	12%	12%
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21/.

TABLE XXV: Relative systematic errors on the infinite-volume matrix elements of

 $\overline{\text{MS}}$ -renormalized four-quark operators Q'_j .

TABLE XXVI: Relative systematic errors on $Re(A_0)$ and $Im(A_0)$.

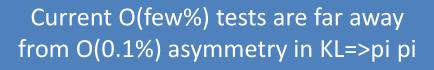
Why EWK cannot be neglected: 3 Reasons

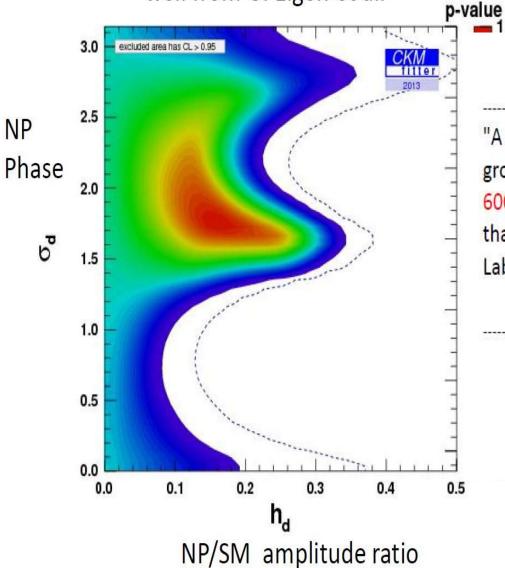
- Despite $\alpha_{QED,EWK}$ << α_{QCD} , EWK contributions are extremely important and CANNOT be neglected:
- EWK are (8,8) and QCD are (8,1), and (8,8) go to constant whereas (8,1) vanish in the chiral limit
- EWK, i.e. those due Z exch have Wilson coeff that go as mt²/mW²

• In E' they enter as

$$\left[\frac{\mathrm{Im}A_2}{\mathrm{Re}A_2} - \frac{\mathrm{Im}A_0}{\mathrm{Re}A_0}\right]$$

Refourda Refa ICHEP2014: Similar results from UTFIT (D. Derkach) as well from G. Eigen et al.





A lesson from history (1)

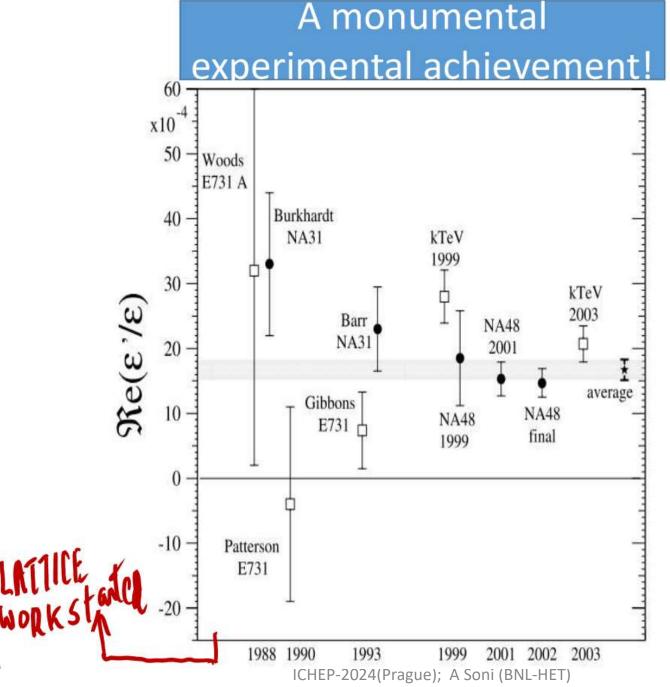
"A special search at Dubna was carried out by E. Okonov and his group. They did not find a single $K_L \rightarrow \pi^+\pi^-$ event among 600 decays into charged particles [12] (Anikira et al., JETP 1962). At that stage the search was terminated by the administration of the Lab. The group was unlucky."

-Lev Okun, "The Vacuum as Seen from Moscow"

1964: BF= 2 x 10⁻³

A failure of imagination ? Lack of patience ?

Had KL=>pi pi been abandoned, history of Particle Physics would have been significantly different!



Komad Kleinknecht " "UncabigCPV

16.6(23) X10 4 PDG 2014

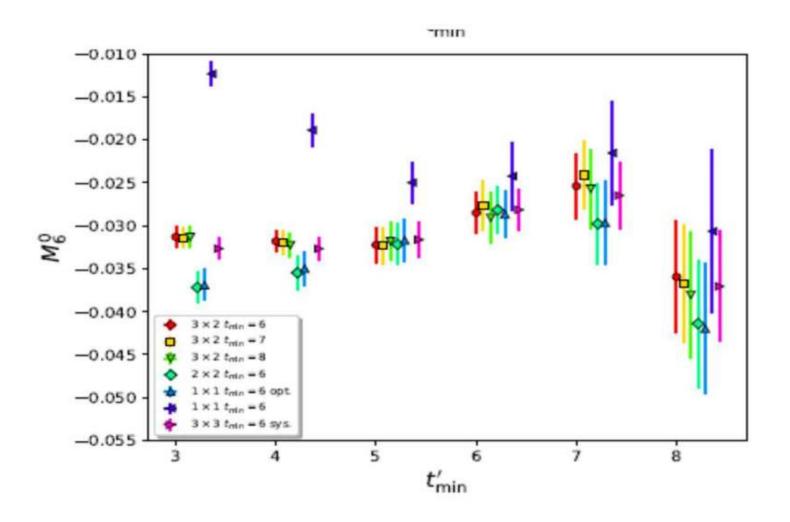
XTRAS

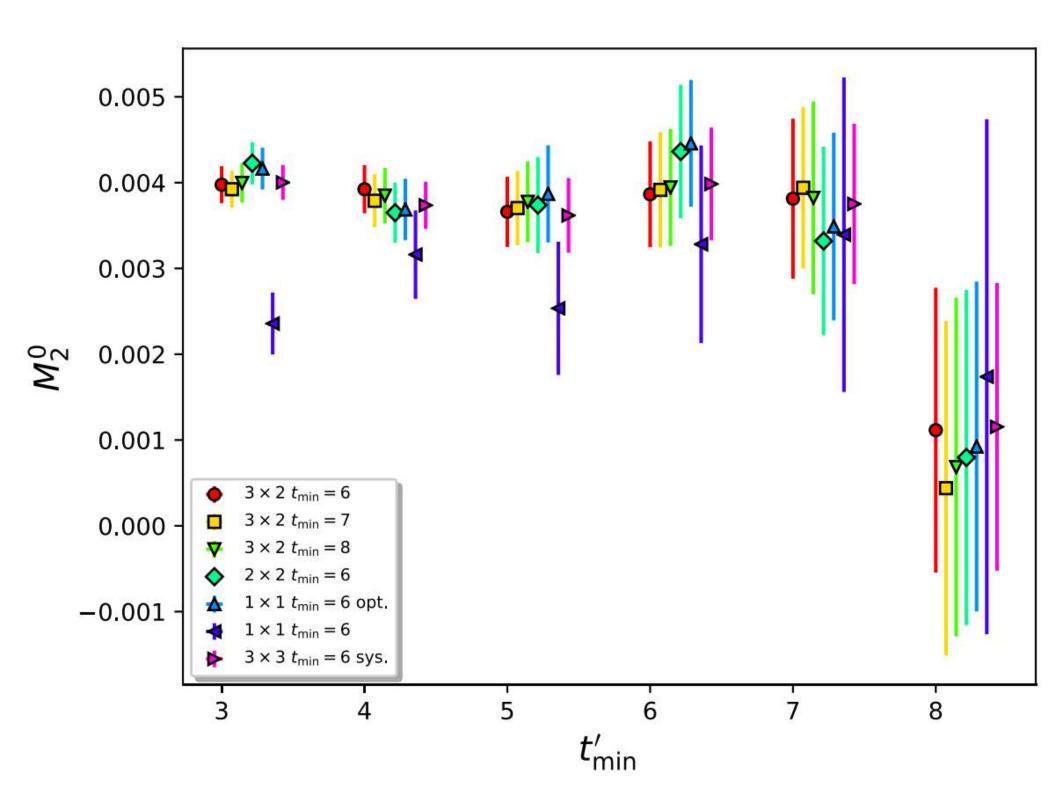
A.S. in Proceedings of Lattice '85 (FSU)..1st Lattice meeting ever attended

The matrix elements of some penguin operators control in the standard model another CP violation parameter, namely ϵ'/ϵ . $^{6,8)}$ Indeed efforts are now underway for an improved measurement of this important parameter. 10) In the absence of a reliable calculation for these parameters, the experimental measurements, often achieved at tremendous effort, cannot be used effectively for constraining the theory. It is therefore clearly important to see how far one can go with MC techniques in alleviating this old but very difficult

With C. Bernard [UCLA]

24(Prague); A Soni (BNL-HET)





Exploring excited-state signals

- ππ energies in PBC
 - $\approx 2m_{\pi}$ for ground st.
 - Need excited-state signals to extract kinematics of K → ππ

Picture in non-interacting 2-pion system with rest frame

	p	$E = 2\sqrt{ \vec{p} ^2 + m_\pi^2}$	
ground st.	(0,0,0)	$2m_{\pi}$	
1st excited st.	2π/L x (1,0,0)	sould bem	
2nd excited st.	2π/L x (1,1,0)	could be ≈ m _K	

- Variational method useful [Lüscher, 1990]
 - Solving GEVP (Generalized Eigenvalue Problem)

$$C(t)v_n(t,t_0) = \lambda_n(t,t_0)C(t_0)v_n(t,t_0) \quad \left\{ \begin{array}{l} C(t): N \ x \ N \ correlator \ matrix \\ C_{ab}(t) = \langle O_a(t)O_b(0)^\dagger \rangle \end{array} \right.$$

- $O'_n = \sum_a v_{n,a}^* O_a$ couples with only n-th, N+1-th & higher states
- $\lambda_{n}(t,t_{0}) = e^{-E_{n}(t-t_{0})}$
- We employ 5 independent ππ operators
 - $\bullet \quad O_a \in \pi_{p=(0,0,0)} \pi_{p=(0,0,0)}, \ \pi_{p=(0,0,1)} \pi_{p=(0,0,-1)}, \ \pi_{p=(0,1,1)} \pi_{p=(0,-1,-1)}, \ \pi_{p=(1,1,1)} \pi_{p=(-1,-1,-1)} \ \& \ \sigma$

$$Q_1 = (\bar{s}_{\alpha}d_{\alpha})_L(\bar{u}_{\beta}u_{\beta})_L,$$

$$Q_2 = (\bar{s}_{\alpha}d_{\beta})_L(\bar{u}_{\beta}u_{\alpha})_L,$$

$$Q_2 = (\bar{s}_{\alpha} d_{\beta})_L (\bar{u}_{\beta} u_{\alpha})_L,$$

$$Q_3 = (\bar{s}_{\alpha} d_{\alpha})_L \sum_{q=u,d,s} (\bar{q}_{\beta} q_{\beta})_L$$

$$Q_{3} = (\bar{s}_{\alpha}d_{\alpha})_{L} \sum_{q=u,d,s} (\bar{q}_{\beta}q_{\beta})_{L},$$

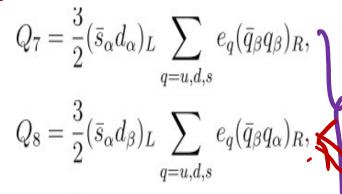
$$Q_{4} = (\bar{s}_{\alpha}d_{\beta})_{L} \sum_{q=u,d,s} (\bar{q}_{\beta}q_{\alpha})_{L},$$

$$Q_{5} = (\bar{s}_{\alpha}d_{\alpha})_{L} \sum_{q=u,d,s} (\bar{q}_{\beta}q_{\beta})_{R},$$

$$Q_{6} = (\bar{s}_{\alpha}d_{\beta})_{L} \sum_{q=u,d,s} (\bar{q}_{\beta}q_{\alpha})_{R},$$

$$Q_5 = (\bar{s}_{\alpha} d_{\alpha})_L \sum_{q=u,d,s} (\bar{q}_{\beta} q_{\beta})_R,$$

$$Q_6 = (\bar{s}_{\alpha} d_{\beta})_L \sum_{\alpha} (\bar{q}_{\beta} q_{\alpha})_R,$$



$$Q_8 = \frac{3}{2} (\bar{s}_{\alpha} d_{\beta})_L \sum_{q=u,d,s} e_q (\bar{q}_{\beta} q_{\alpha})_R,$$

$$Q_9 = \frac{3}{2} (\bar{s}_{\alpha} d_{\alpha})_L \sum_{q=u,d,s} e_q (\bar{q}_{\beta} q_{\beta})_L,$$

$$Q_{10} = \frac{3}{2} (\bar{s}_{\alpha} d_{\beta})_L \sum_{q=u,d,s} e_q (\bar{q}_{\beta} q_{\alpha})_L,$$

Indirect CP violation in KL=>3 pi

The basic expression for ε is

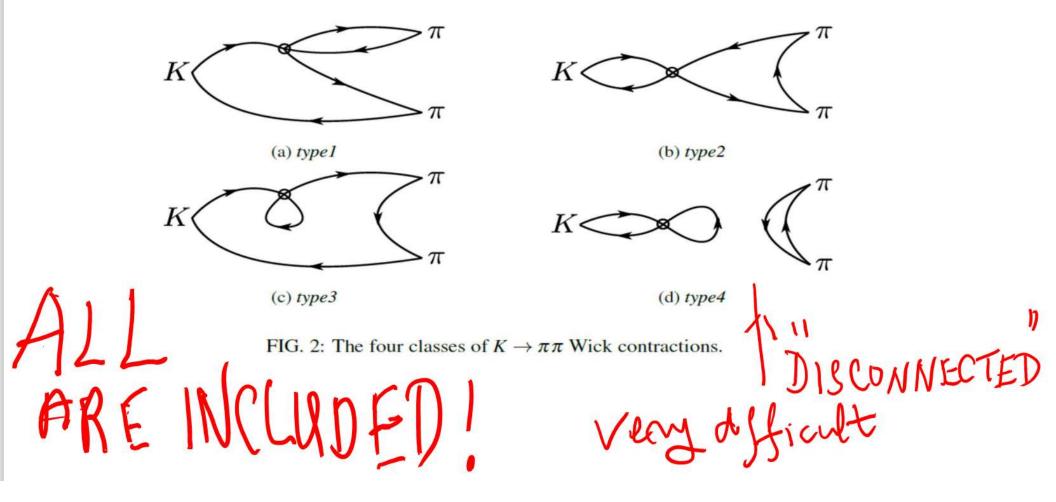
$$\varepsilon = e^{i\phi_{\varepsilon}} \frac{G_F^2 m_W^2 f_K^2 m_K}{12\sqrt{2}\pi^2 \Delta m_K^{\exp}} \hat{B}_K \kappa_{\varepsilon} \text{ Im} \Big[\\ \eta_1 S_0(x_c) \left(V_{cs} V_{cd}^* \right)^2 + \eta_2 S_0(x_t) \left(V_{ts} V_{td}^* \right)^2 \\ + 2\eta_3 S_0(x_c, x_t) V_{cs} V_{cd}^* V_{ts} V_{td}^* \Big],$$
(41)

where the numerical inputs we use are summarized in Table 2. The quantity κ_{ε} summarizes the impact of long distance effects and can be extracted from the knowledge of Im A_0 and from an estimate of the long distance contributions to Δm_K . Following Ref. [76], we have:

$$\kappa_{\varepsilon} = \sqrt{2}\sin(\phi_{\varepsilon}) \left(1 + \frac{\rho}{\sqrt{2} \left| \varepsilon_{\exp} \right|} \frac{\operatorname{Im}(A_0)}{\operatorname{Re}(A_0)} \right) \tag{42}$$

where $\rho = 0.6 \pm 0.3$. Using the most recent RBC determination of $Im(A_0)$ and ϕ_{ε} of Eq. (32), we obtain $\kappa_{\varepsilon} = 0.963 \pm 0.014$ (see also the analysis presented in Ref. [77]).

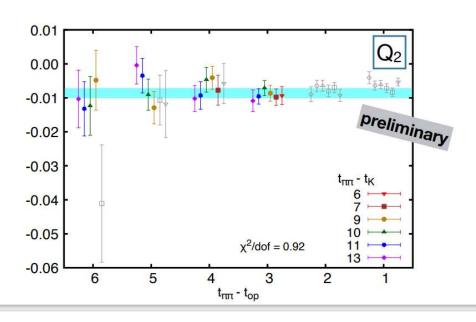
ICHEP-2024(Prague); A Soni (BNL-HET)

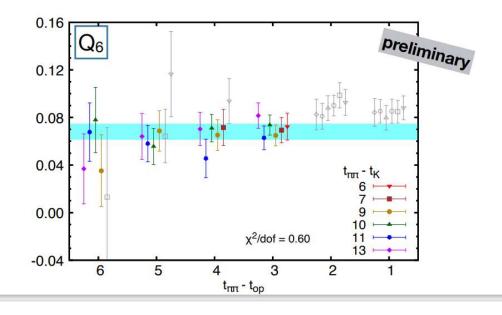


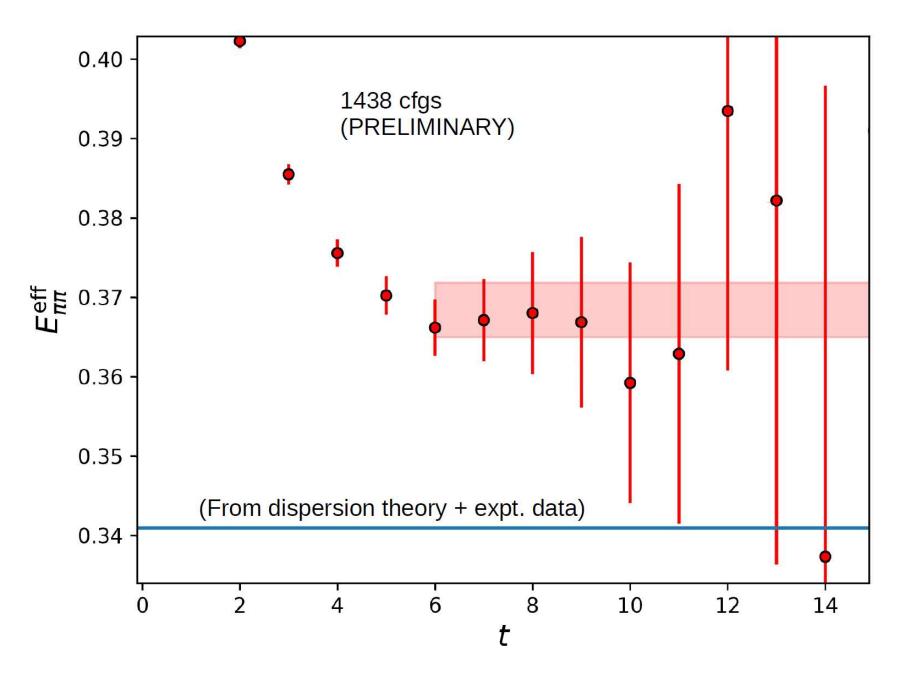
Effective matrix elements ($\Delta I = 1/2$)

- Plateau appears
- : Example of correlated fit result with

 $t_{op}-t_{K} \ge 3 \&\& t_{\pi\pi}-t_{op} \ge 3$ (colored filled data points)







Back to the core story.... Conforting V Symmte little

A chance (crucial) meeting: Yigal Shamir visits me in Haifa ~94 summer

 For K=> pi pi project, way to overcome the fine-tuning problem of Wilson Fermions is to use a new formulation of

fermions on the lattice=> DOMAIN WALL FERMIONS [computationally much harder but are continuum -like possessing chiral symmetry]

- Furman + Shamir: hep-lat/9405004
- See also Yigal Shamir, hep-lat 9303005

Way FORWARD: Adopt DWFfak+111 46'? 95-967.

• As a result, the large accidental cancellations significantly enhances sensitivity of ε' to NP

More demands on the calculation

~ The 1995 discovery of the huge top mass accentuated the cancellation of I=0 and I=2 contributions to ε' significantly, putting additional demands on the calculation but also enhancing the potential for discovery of new physics

$$\frac{\varepsilon'}{\varepsilon} = \frac{i\omega e^{i(\delta_2 - \delta_0)}}{\sqrt{2}\varepsilon} \left[\frac{\operatorname{Im}(A_2)}{\operatorname{Re}(A_2)} - \frac{\operatorname{Im}(A_0)}{\operatorname{Re}(A_0)} \right] \xrightarrow{\text{isospin sym}} \frac{1}{\varepsilon} \frac{1}{\varepsilon} = \frac{i\omega_+ e^{i(\delta_2 - \delta_0)}}{\sqrt{2}\varepsilon} \left[\frac{\operatorname{Im}(A_2^{\text{emp}})}{\operatorname{Re}(A_2^{(0)})} - \frac{\operatorname{Im}(A_0^{(0)})}{\operatorname{Re}(A_0^{(0)})} (1 - \hat{\Omega}_{\text{eff}}) \right] \xrightarrow{\text{isospin sym}} \frac{1}{\varepsilon} \frac{1}{\varepsilon$$

The ultimate theoretical error on γ from $B \to DK$ decays

Secana Miss wholy ministed higher order

CORNECTION Y ISTRIBUTED

In the SM-KM

Concinnati,

CPV

Joachim Brod and Jure Zupan

Department of Physics, University of Cincinnati, Cincinnati, Ohio 45221, U.S.A.

E-mail: brodjm@ucmail.uc.edu, zupanje@ucmail.uc.edu

ABSTRACT: The angle γ of the standard CKM unitarity triangle can be determined from $B \to DK$ decays with a very small irreducible theoretical error, which is only due to second-order electroweak corrections. We study these contributions and estimate that their impact on the γ determination is to introduce a shift $|\delta\gamma| \lesssim \mathcal{O}(10^{-7})$, well below any present or planned future experiment.

A difficulty: strong phases

 The continuum and our lattice determinations of strong phase

diffe

eterminations of strong phase
$$\phi_{\varepsilon'} = \delta_2 - \delta_0 + \frac{\pi}{2} = \begin{cases} (42.3 \pm 1.5)^{\circ} & \text{The polynomial properties of strong phase} \\ (54.6 \pm 5.8)^{\circ} & \text{The polynomial properties of strong phase} \end{cases}$$

Challenges of physical K=>pi pi

with 2 stationary pions in final state dominates. However

$$2m_{\pi} \approx 260 \text{ MeV} \ll m_K \approx 500 \text{ MeV}$$

- Desired state with moving pions is next-to-leading term: require 2exp fits?
 - Avoid 2-exp fits by removing stationary pion state from system through manipulating lattice spatial boundary conditions:
 - > Antiperiodic BCs on down-quark for A₂

$$p_\pi = 0 \to \pi/L$$
 tune L to match E, and E,

Resolving the [I=0] Energy & phase shift in the pi pi channel

• 2015 result has 2σ + discrepancy between our I=0 $\pi\pi$ phase shift (δ_0 =23.8(4.9) $(1.2)^{\circ}$) and dispersion theory prediction (~34°).

> [RBC&UKQCD PRL 115 (2015) 21, 212001] [Colangelo et al, Nucl. Phys. B603 (2001) 125-179]

- Observed discrepancy more significant ($\sim 5\sigma$) with 6.5x stats.
- Most likely explanation is excited-state contamination.
- To address added scalar (σ =ūd) $\pi\pi$ operator to the 2-pt function calculation.
- Combined fits (or GEVP) to $\pi\pi \to \pi\pi$, $\sigma \to \pi\pi$ and $\sigma \to \sigma$ correlators result in considerably lower ground-state energy:

508(5) MeV [1386 cfgs] from $\pi\pi \rightarrow \pi\pi$ alone VS 483(1) MeV [501 cfgs] from sim. fit of all 3 correlators.

• New phase shift $\delta_0 = 30.9(1.5)(3.0)^\circ$ [prelim] compatible with dispersive result.

• Strong evidence for nearby excited finite-volume $\pi\pi$ state. Indeed such a state with $E \sim 770$ MeV is predicted by dispersion theory.

Note: 5 = -11.6 + 25 + 12 0 4 [+11 (5=2)= 573.0 + 2.9 MeV ICHEP-2024(Prague); A Soni (BNL-HET) See PRL 2015 61

anxiv: 2004, 09440



Parameter	Value	
	2-state fit	3-state fit
Fit range	6-15	4-15
$A^0_{\pi\pi(111)}$	0.3682(31)	0.3718(22)
$A^0_{\pi\pi(311)}$	0.00380(32)	0.00333(27)
A_{σ}^{0}	-0.0004309(41)	-0.0004318(42)
E_0	0.3479(11)	0.35030(70)
$A^1_{\pi\pi(111)}$	0.1712(91)	0.1748(67)
$A^1_{\pi\pi(311)}$	-0.0513(27)	-0.0528(30)
A_{σ}^{1}	0.000314(17)	0.000358(13)
E_1	0.568(13)	0.5879(65)
$A^2_{\pi\pi(111)}$	_	0.116(29)
$A^2_{\pi\pi(311)}$	_	0.063(10)
A_{σ}^{2}	_	0.000377(94)
E_2	_	0.94(10)
p-value	0.314	0.092

RBC-UKBCP 2020

TABLE III: Fit parameters in lattice units and the p-values for multi-operator fits to the I=0 $\pi\pi$ two-point functions. Here E_i are the energies of the states and A^i_{α} represents the matrix element of the operator α between the state i and the vacuum, given in units of $\sqrt{1\times10^{13}}$. The second column gives the parameters for our primary fit which uses two-states and three operators. The third column shows a fit with the same three operators and one additional state that is used to probe the systematic effects of this third state on the $K \to \pi\pi$ matrix element fits.

PHYSICAL REVIEW D 102, 054509 (2020)

Editors' Suggestion

Featured in Physics

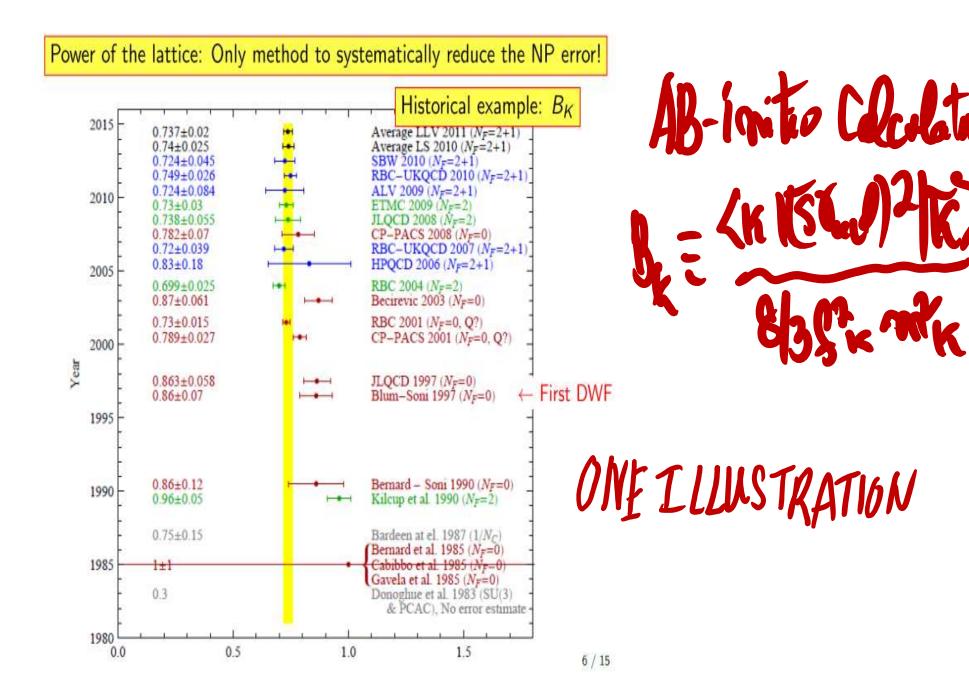
Direct *CP* violation and the $\Delta I = 1/2$ rule in $K \to \pi\pi$ decay from the standard model

R. Abbott, T. Blum, P. A. Boyle, M. Bruno, N. H. Christ, D. Hoying, C. Jung, C. Kelly, C. Lehner, R. D. Mawhinney, D. J. Murphy, C. T. Sachrajda, A. Soni, M. Tomii, and T. Wang

(RBC and UKQCD Collaborations)

¹Physics Department, Columbia University, New York, New York 10027, USA
²Physics Department, University of Connecticut, Storrs, Connecticut 06269-3046, USA
³RIKEN-BNL Research Center, Brookhaven National Laboratory, Upton, New York 11973, USA
⁴Brookhaven National Laboratory, Upton, New York 11973, USA
⁵SUPA, School of Physics, The University of Edinburgh, Edinburgh EH9 3JZ, United Kingdom
⁶Theoretical Physics Department, CERN, 1211 Geneve 23, Switzerland
⁷Universität Regensburg, Fakultät für Physik, 93040 Regensburg, Germany
⁸Center for Theoretical Physics, Massachusetts Institute of Technology,
Boston, Massachusetts 02139, USA
⁹School of Physics and Astronomy, University of Southampton, Southampton SO17 1BJ, United Kingdom

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The RBC & UKQCD collaborations

UC Berkeley/LBNL

Aaron Meyer

BNL and BNL/RBRC

Yasumichi Aoki (KEK)

Peter Boyle (Edinburgh)

Taku Izubuchi

Chulwoo Jung

Christopher Kelly

Meifeng Lin

Nobuyuki Matsumoto

Shigemi Ohta (KEK)

Amarjit Soni

Tianle Wang

CERN

Andreas Jüttner (Southampton)

Tobias Tsang

Columbia University

Norman Christ

Yikai Huo

Yong-Chull Jang

Joseph Karpie

Bob Mawhinney

Bigeng Wang (Kentucky)

Yidi Zhao

University of Connecticut

Tom Blum

Luchang Jin (RBRC)

Douglas Stewart

Joshua Swaim

Masaaki Tomii

Edinburgh University

Matteo Di Carlo

Luigi Del Debbio

Felix Erben

Vera Gülpers

Tim Harris

Ryan Hill

Raoul Hodgson

Nelson Lachini

Michael Marshall

Fionn Ó hÓgáin

Antonin Portelli

James Richings

Azusa Yamaguchi

Andrew Z.N. Yong

Liverpool Hope/Uni. of Liverpool

Nicolas Garron

Michigan State University

Dan Hoying

University of Milano Bicocca

Mattia Bruno

Nara Women's University

Hiroshi Ohki

Peking University

Xu Feng

University of Regensburg

Davide Giusti

Christoph Lehner (BNL)

University of Siegen

Matthew Black Oliver Witzel

University of Southampton

Alessandro Barone

Jonathan Flynn

Nikolai Husung

Rajnandini Mukherjee

Callum Radley-Scott

Chris Sachrajda

Stony Brook University

Jun-Sik Yoo

Sergey Syritsyn (RBRC)

Relating lattice ME to physical amplitudes

$$A_{2/0} = F \frac{G_F}{\sqrt{2}} V_{ud} V_{us} \sum_{i=1}^{10} \sum_{j=1}^{7} \left[\left(z_i(\mu) + \tau y_i(\mu) \right) Z_{ij}^{\text{lat} \to \overline{\text{MS}}} M_j^{\frac{3}{2}/\frac{1}{2}, \text{lat}} \right]$$

F is the Lellouch-Luscher factor which relates finite volume ME to the infinite volume

$$A = \frac{1}{\pi q} \sqrt{\frac{\partial \phi}{\partial q} + \frac{\partial \delta}{\partial q}} \sqrt{m_K} E_{\pi\pi} L^{2/3} M$$

$$\phi \text{ is a somewhat complicated function of q and boundary Conditions [See Daiqian Zhang thesis]}$$

Main: (Old) and new points

- In naturalness we trust
- Early history: The crucial role of BK
- Current tensions in B-UT
- A moral (for the lattice) from epsilon'
- Importance of K-UT
- eps': Periodic Boundary Condition appear promising
- [with RBC-UKQCD]
- Improving LD contribution to K+ => pi+ nu nu [with Enrico Lunghi]
- K0=> pi0 l+ l-: should help significantly in constraining the extremely challenging gold plated mode: KL => pi0 nu nu. [with Stefan Schacht]
- Summary