

Study of baryon-strangeness and charge-strangeness correlations in Pb–Pb collisions at 5.02 TeV with ALICE



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(for the ALICE Collaboration)

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Motivation



Correlations between net-conserved quantities such as net-baryon (B), net-charge (Q), and net-strangeness (S) number can **provide valuable insights into the QCD phase structure**:



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- sensitive probes for the equation of state and are directly related to the QCD thermodynamic susceptibilities
- can be studied in the thermal model (HRG) and measurements can constrain the thermal properties of the QCD medium formed at LHC

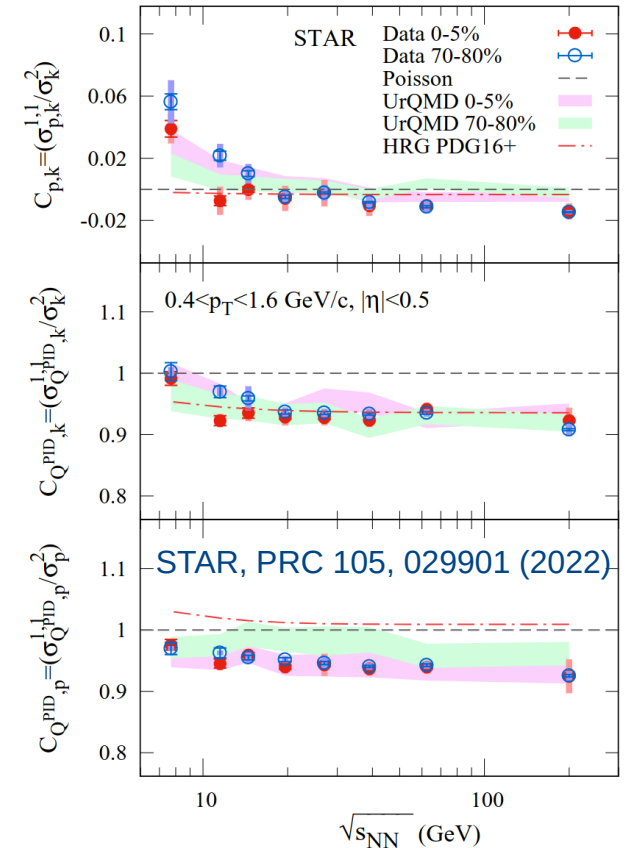
$$\chi_{B,S,Q}^{lmn} = \left[\frac{\partial^{(l+m+n)} (P(\hat{\mu}_B, \hat{\mu}_S, \hat{\mu}_Q)/T^4)}{\partial \hat{\mu}_B^l \partial \hat{\mu}_S^m \partial \hat{\mu}_Q^n} \right]_{\vec{\mu}=0}$$

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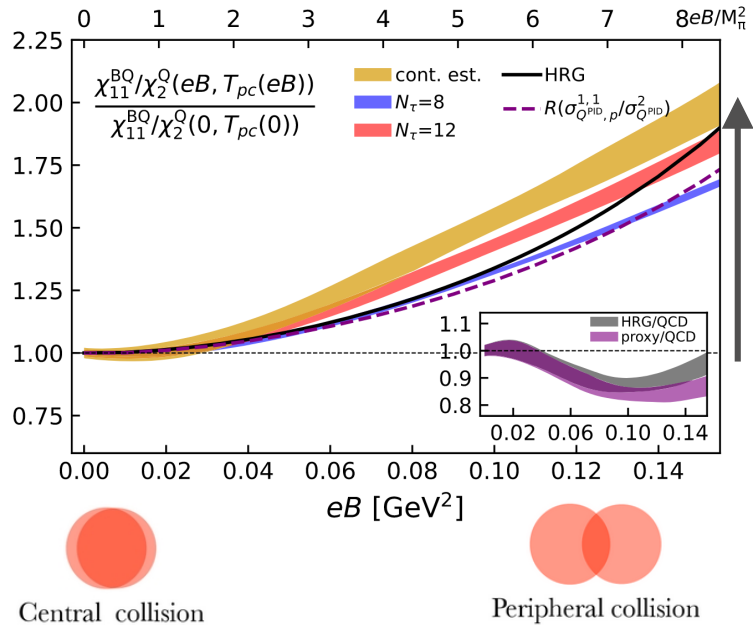
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- Compared to similar measurements at lower energy, STAR experiment at RHIC



LQCD suggests that correlations of B and Q can be a useful probe to detect the imprints of magnetic fields in the final stages of heavy-ion collisions.

H.-T. Ding et al., *Phy.Rev.Lett* 132 (2024) 201903





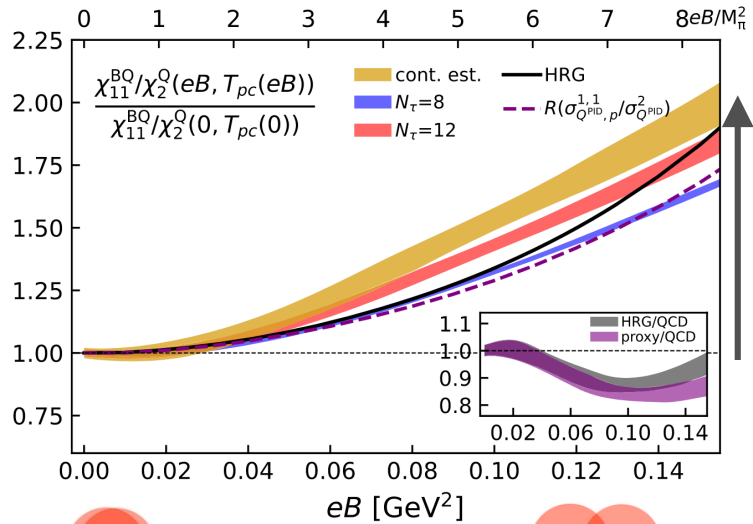
ALICE

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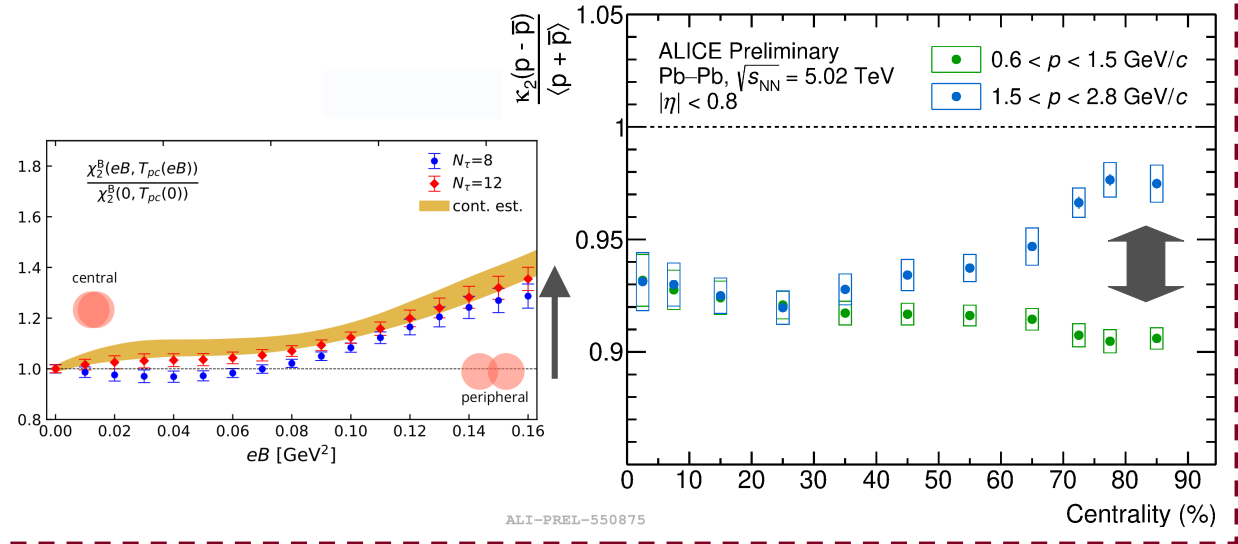


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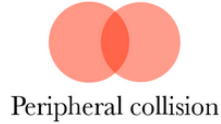
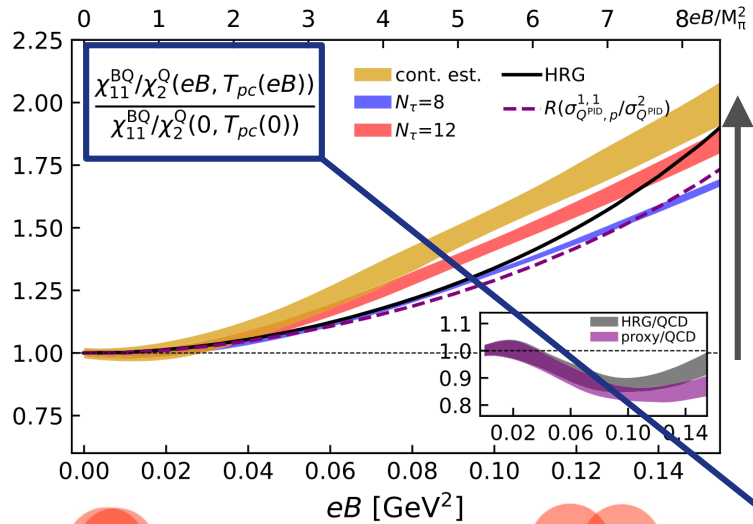
Quark Matter 2023: 2nd order net-proton cumulant



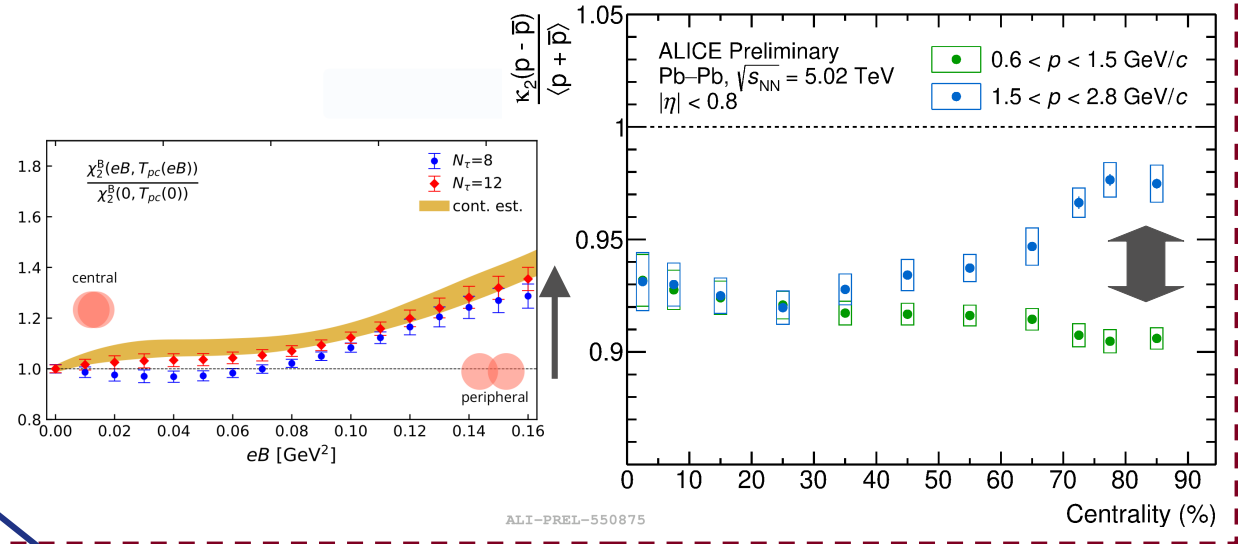
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Quark Matter 2023: 2nd order net-proton cumulant



Can centrality dependence of this quantity reveal a magnetic field in late-stage heavy-ion collisions?

The susceptibilities of B , S , Q are related to the cumulants (σ) of the event-by-event distribution of the associated conserved charges:

$$\chi_{B,S,Q}^{lmn} = \frac{1}{VT^3} \sigma_{B,S,Q}^{lmn}$$

Definitions: $Q \rightarrow$ net-charge | $B \rightarrow$ net-baryon | $S \rightarrow$ net-strangeness

Observables



ALICE

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Off-diagonal
cumulants

$$\begin{aligned} \sigma_{B,S}^{11} &= \langle BS \rangle - \langle B \rangle \langle S \rangle \\ \sigma_{Q,S}^{11} &= \langle QS \rangle - \langle Q \rangle \langle S \rangle \\ \sigma_{Q,B}^{11} &= \langle QB \rangle - \langle Q \rangle \langle B \rangle \end{aligned}$$

Diagonal
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$$\begin{aligned} \sigma_Q^2 &= \langle Q^2 \rangle - \langle Q \rangle^2 \\ \sigma_B^2 &= \langle B^2 \rangle - \langle B \rangle^2 \\ \sigma_S^2 &= \langle S^2 \rangle - \langle S \rangle^2 \end{aligned}$$



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$$\sigma_\alpha^2 = \langle (\delta N_\alpha)^2 \rangle, \quad \sigma_{\alpha,\beta}^{11} = \langle (\delta N_\alpha)(\delta N_\beta) \rangle$$

$$\delta N_\alpha = (N_{\alpha^+} - N_{\alpha^-}) - \langle (N_{\alpha^+} - N_{\alpha^-}) \rangle \quad \alpha, \beta \rightarrow \mathbf{Q, B, or S}$$

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Experiments:

Proxies:

- $Q \rightarrow$ net-pion+net-kaon+net-proton
- $B \rightarrow$ net-proton (p)
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\rightarrow this is what we measure

ALICE Detector



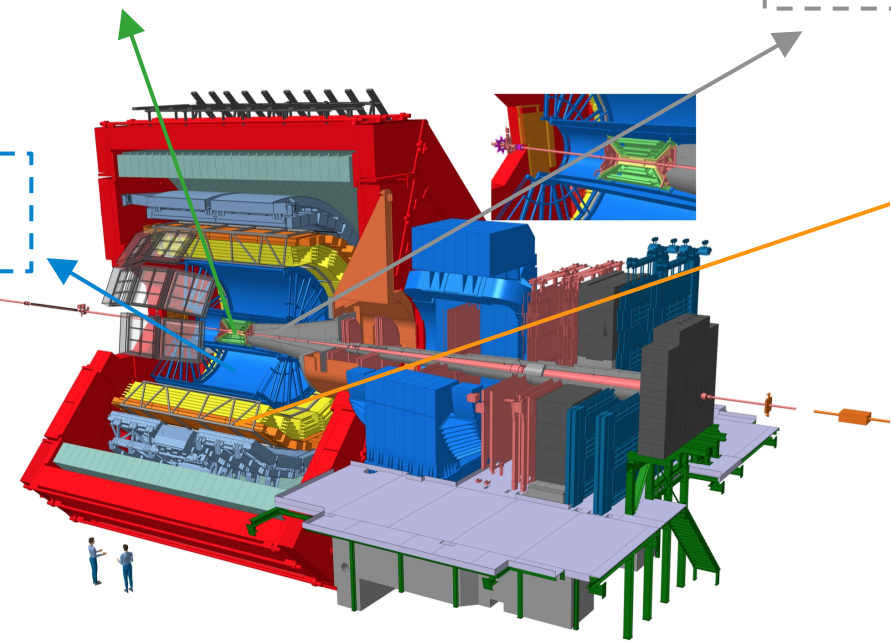
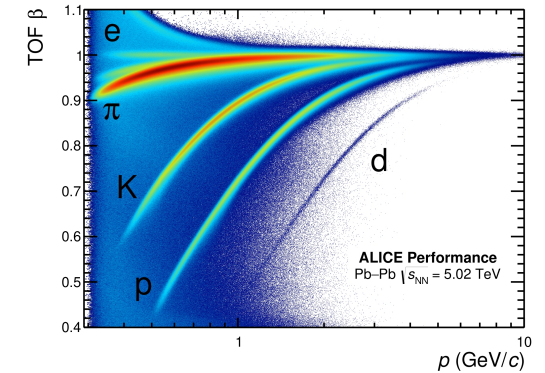
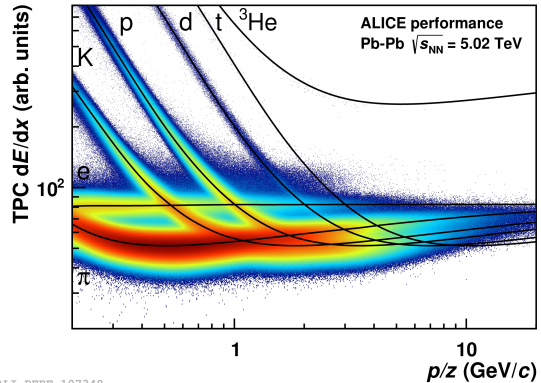
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Inner Tracking System (ITS): tracking, vertexing, trigger

V0: trigger, centrality estimation

Time Projection Chamber (TPC): tracking, PID via dE/dx

Time-Of-Flight (TOF): PID via time of flight



Run 2 data: Pb-Pb $\sqrt{s_{NN}} = 5.02$ TeV

ALICE Detector



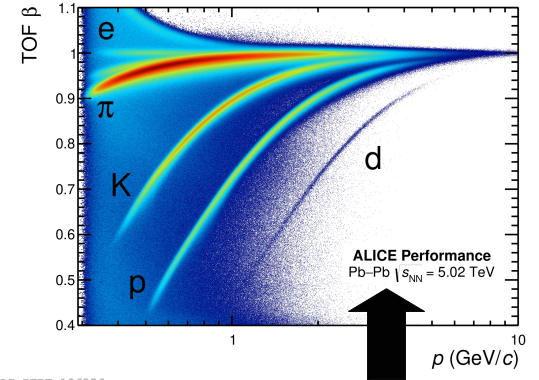
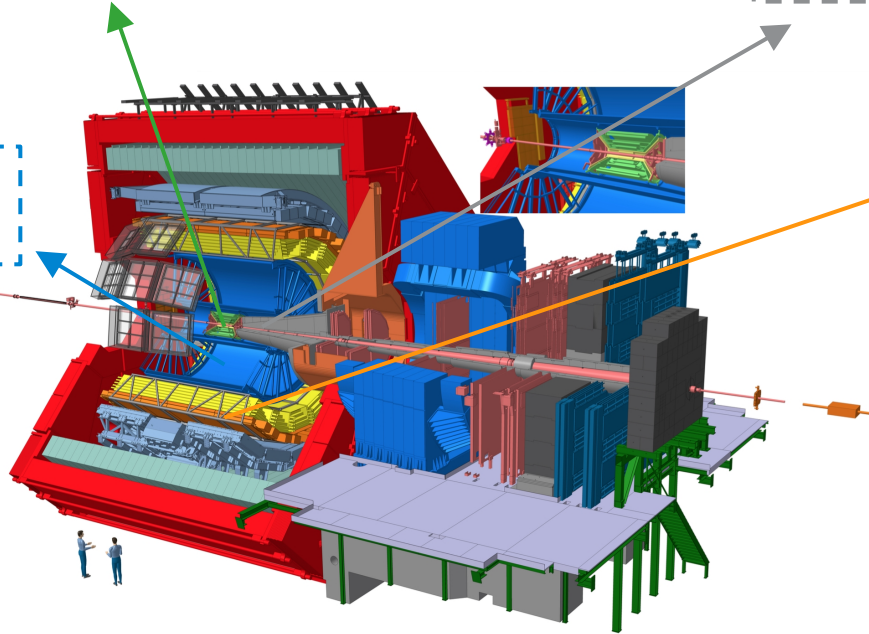
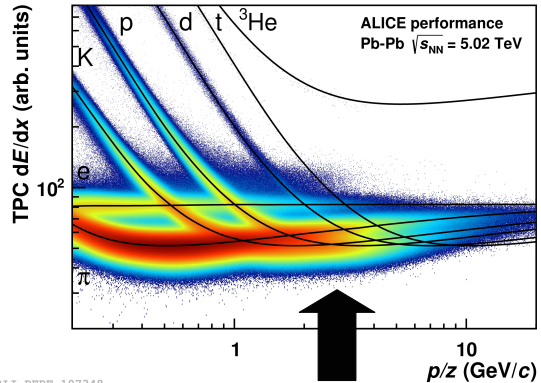
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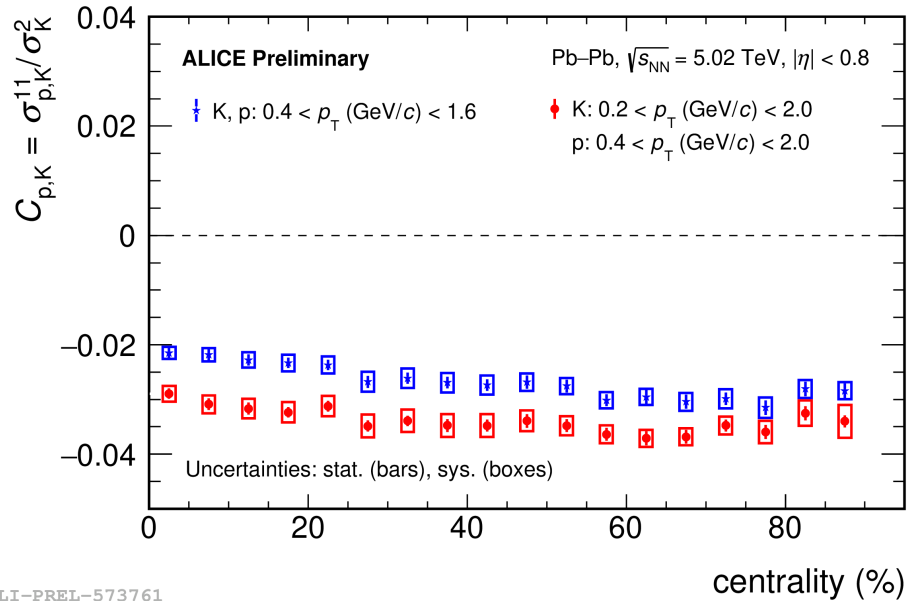


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✓ PID using information from TPC and TOF

Correlation of net-proton and net-kaon

→ a proxy of $B - S$ correlation

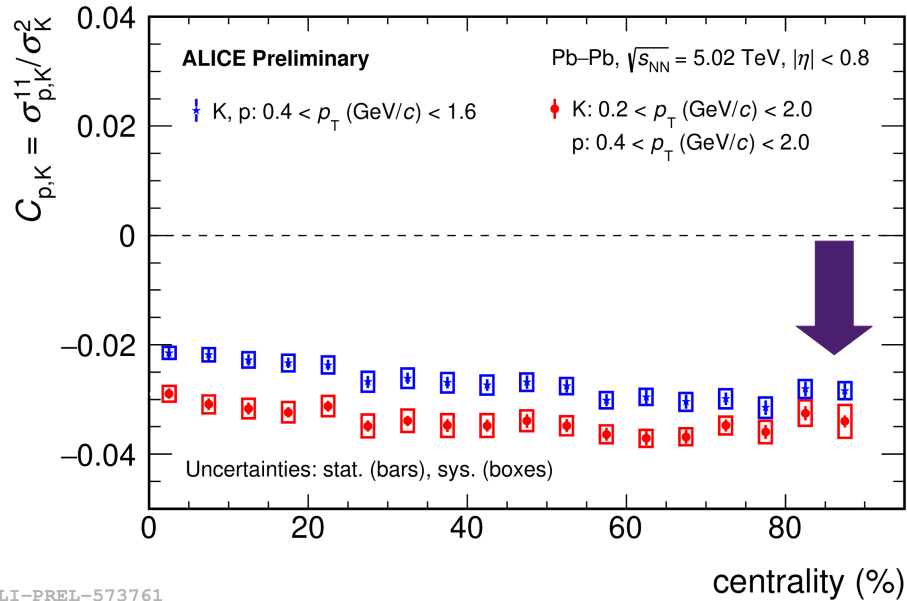


ALI-PREL-573761

- **Anti-correlation** between fluctuations in B and S
- Momentum range dependence

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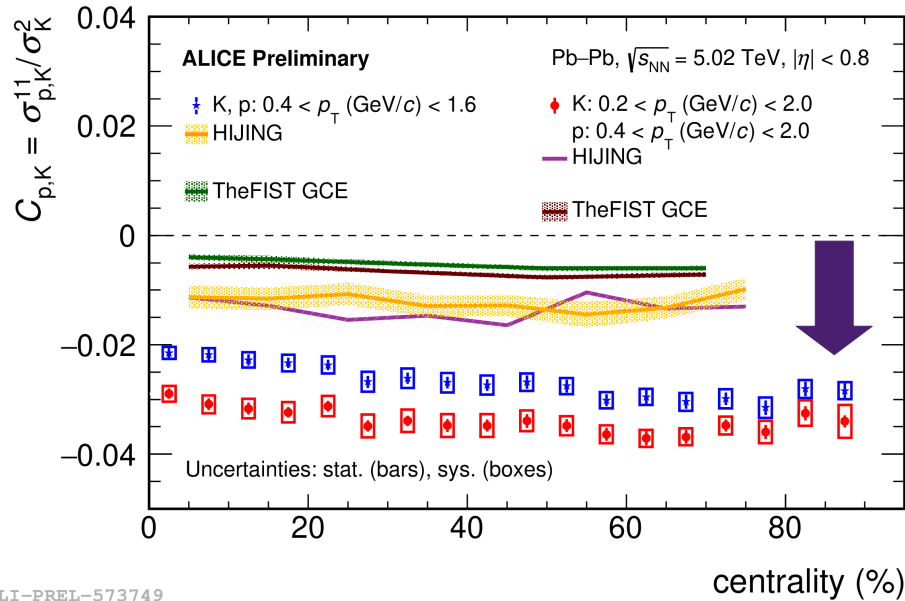


ALI-PREL-573761

- **Anti-correlation** between fluctuations in B and S
- Momentum range dependence
- **Larger correlations** compared to the Poisson baseline

Correlation of net-proton and net-kaon

→ a proxy of **B – S** correlation



ALI-PREL-573749

- **Anti-correlation** between fluctuations in **B** and **S**
- Momentum range dependence
- **Larger correlations** compared to the Poisson baseline, **HIJING** model, and **GCE** limit in thermal model

ThermalFIST (Statistical Hadronization Model) - Parameters from published fit

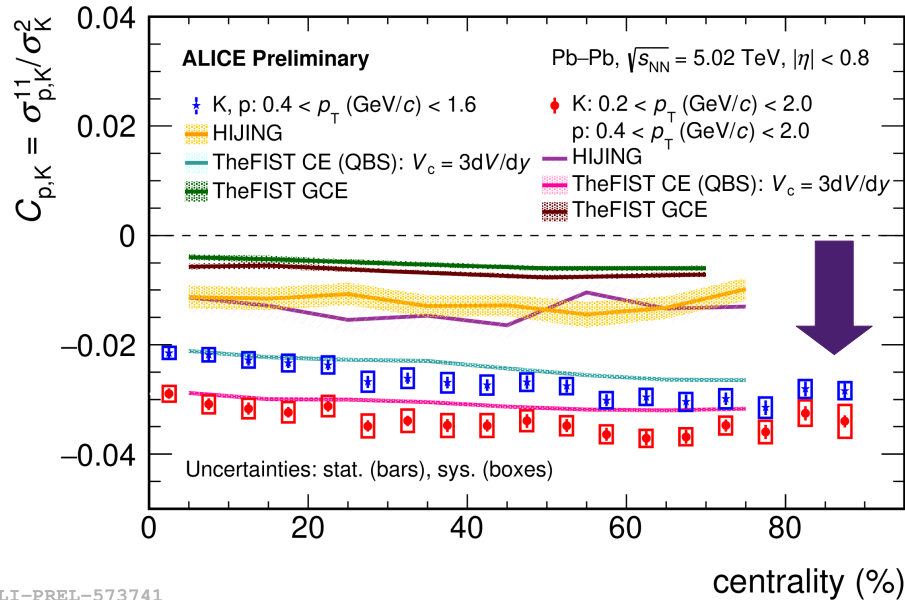
- Grand Canonical Ensemble (**GCE**) → quantum numbers conserved on average

V. Vovchenko et al., Phys.Rev.C 100 (2019) 5, 054906

Swati Saha, NISER, India

Correlation of net-proton and net-kaon

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ALI-PREL-573741

- **Anti-correlation** between fluctuations in **B** and **S**
- Momentum range dependence
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- Correlation volume of $V_c = 3dV/dy$ with **Q, B, S** conservation in **CE favours data**

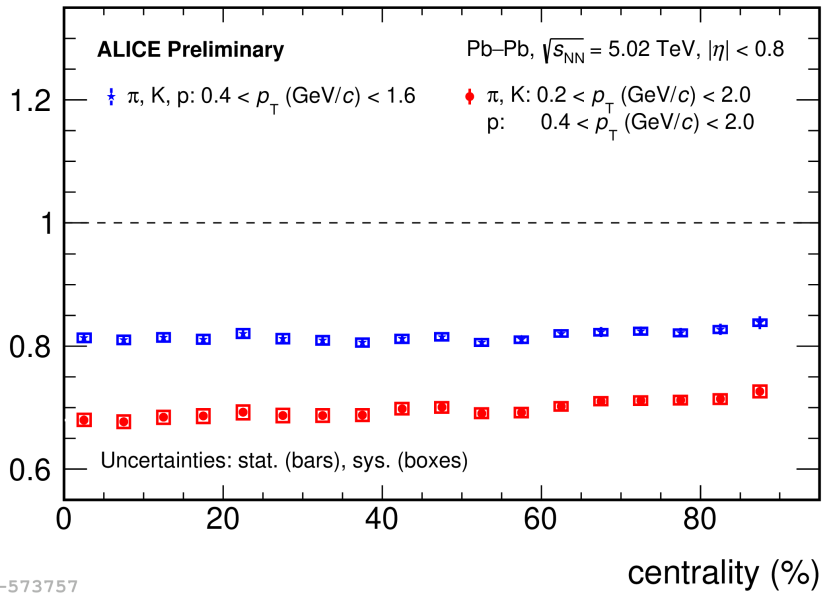
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V. Vovchenko et al., Phys.Rev.C 100 (2019) 5, 054906

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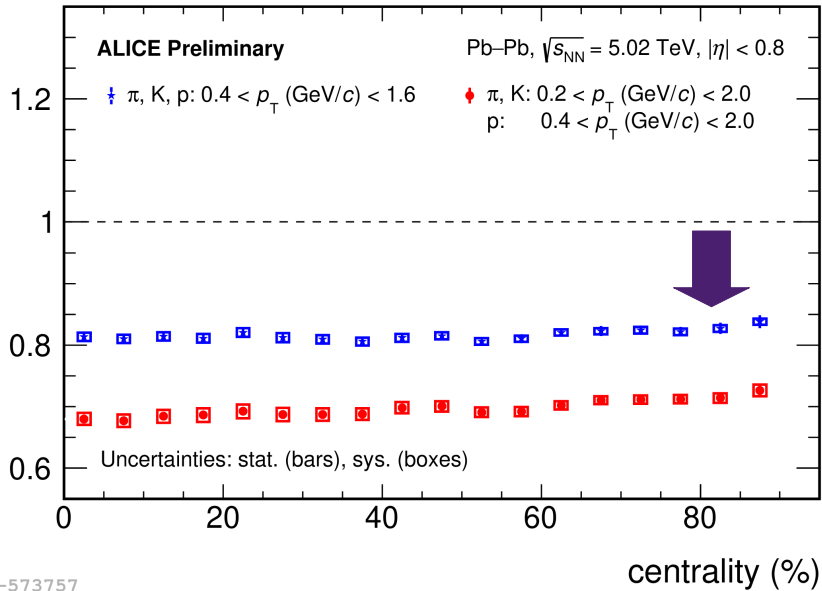
→ a proxy of $Q - S$ correlation

- Momentum range dependence

ALI-PREL-573757

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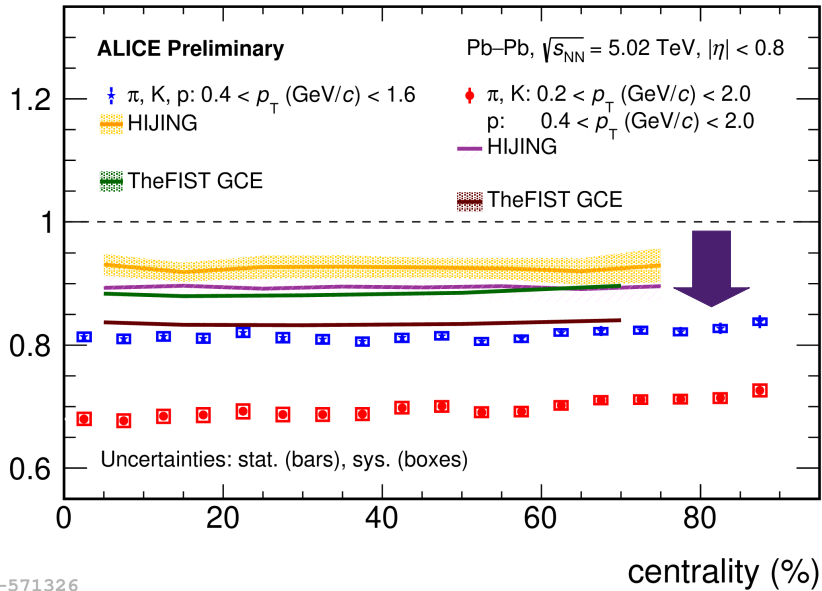
ALI-PREL-573757

→ a proxy of $Q - S$ correlation

- Momentum range dependence
- **Suppressed correlations** compared to the Poisson baseline

Correlation of net-charge and net-kaon

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ALI-REL-571326

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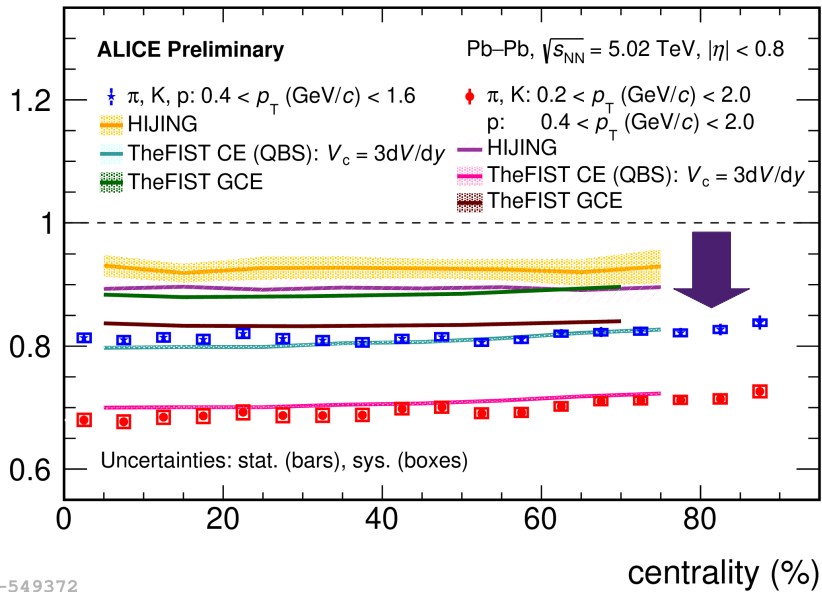
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Correlation of net-charge and net-kaon



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ALI-PREL-549372

→ a proxy of $Q - S$ correlation

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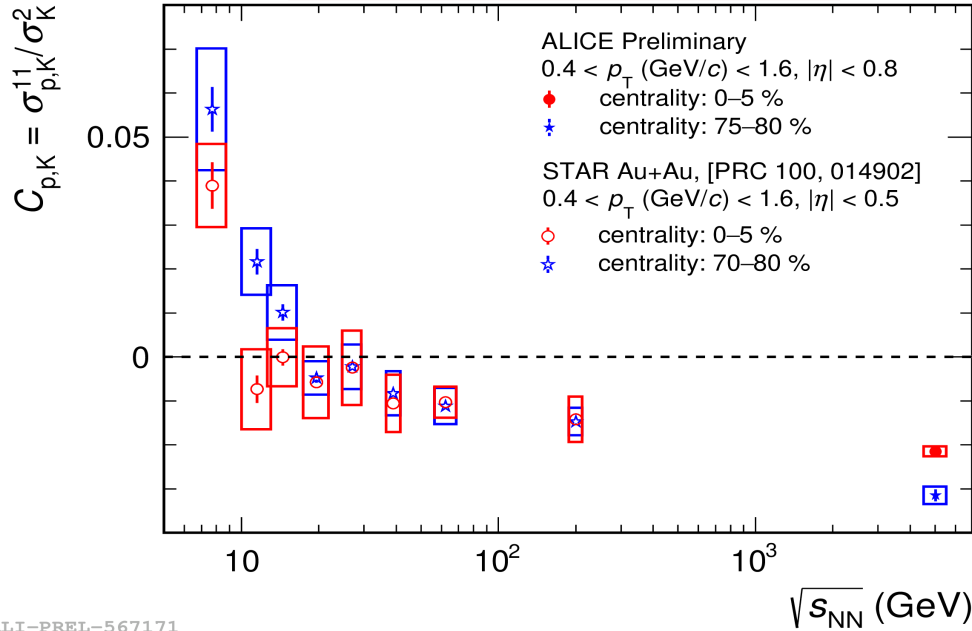
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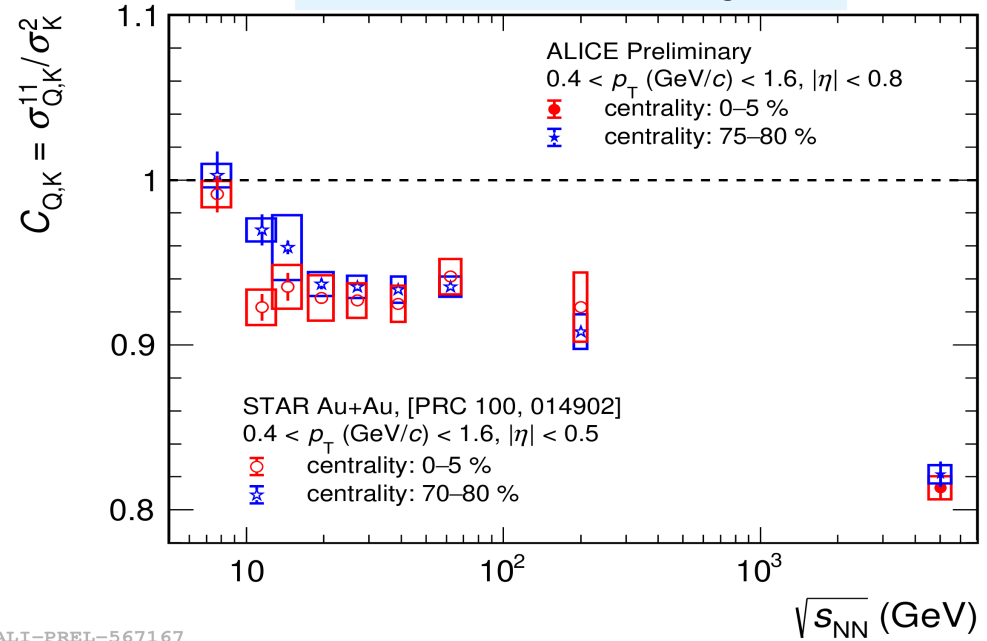
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Energy dependence

Correlation between p - K



Correlation between Q - K



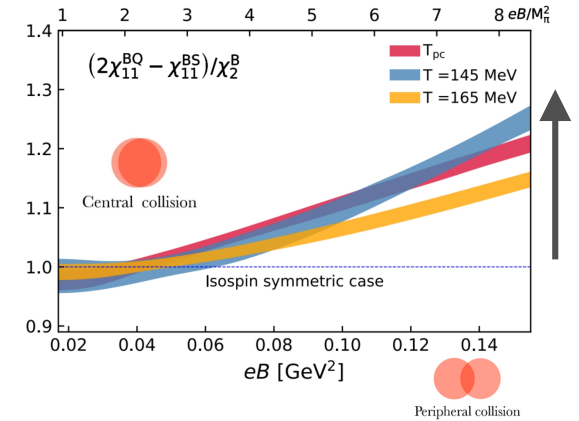
- Decreasing trend of the correlations with increasing energy from RHIC to LHC

Magnetic field effect?

Magnetic field: **Absent**
Isospin symmetry of u and d quarks

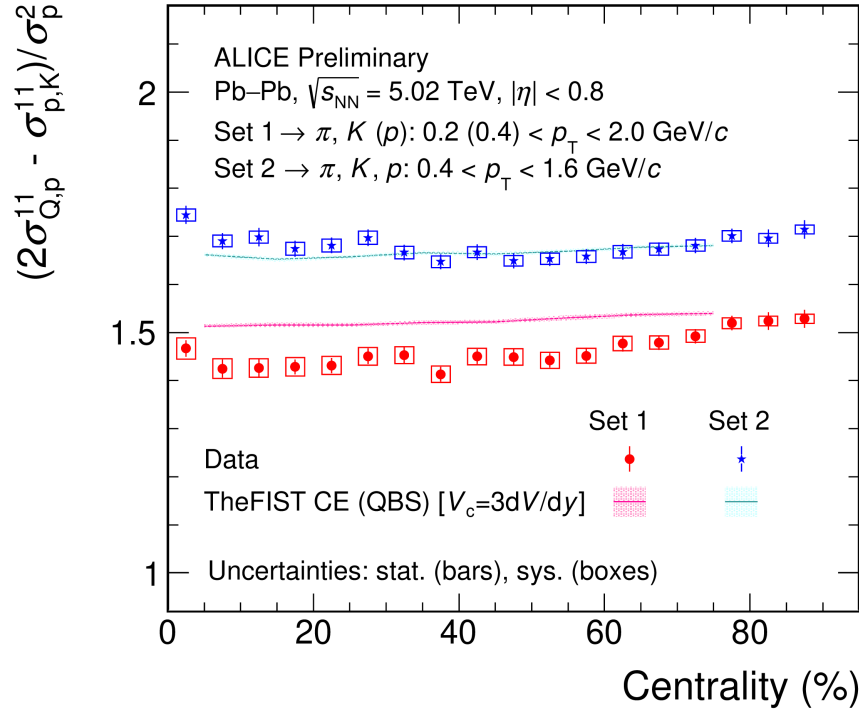


Magnetic field: **Present**
Isospin symmetry breaks



H.-T. Ding et al., EPJ. A (2021) 57:202, CPOD-2024

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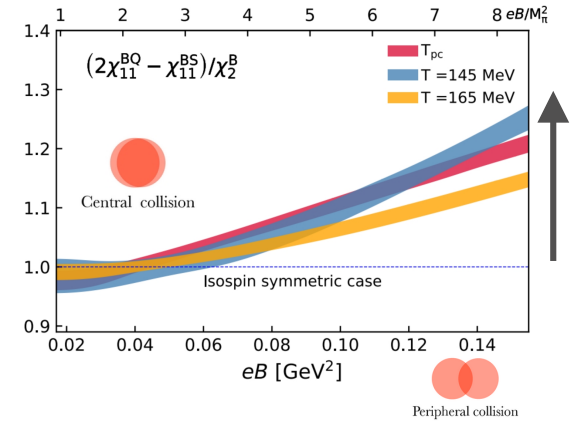


Poisson baseline $\rightarrow 2$

Magnetic field: **Absent**
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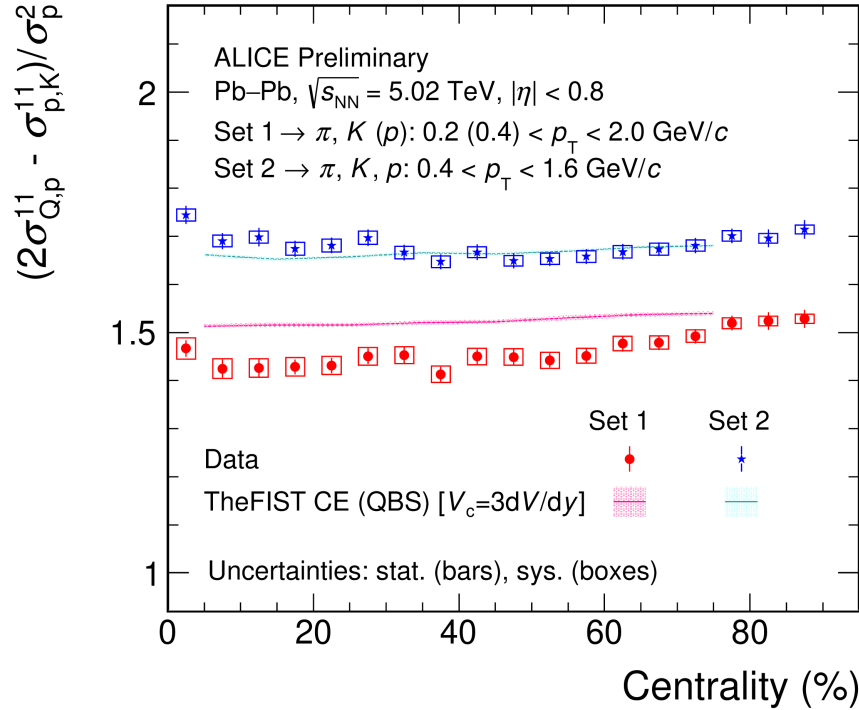
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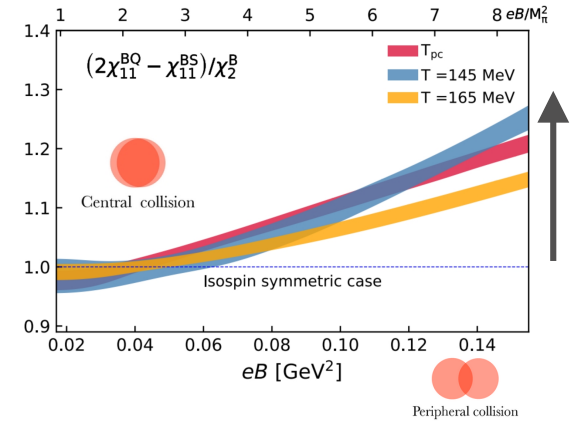


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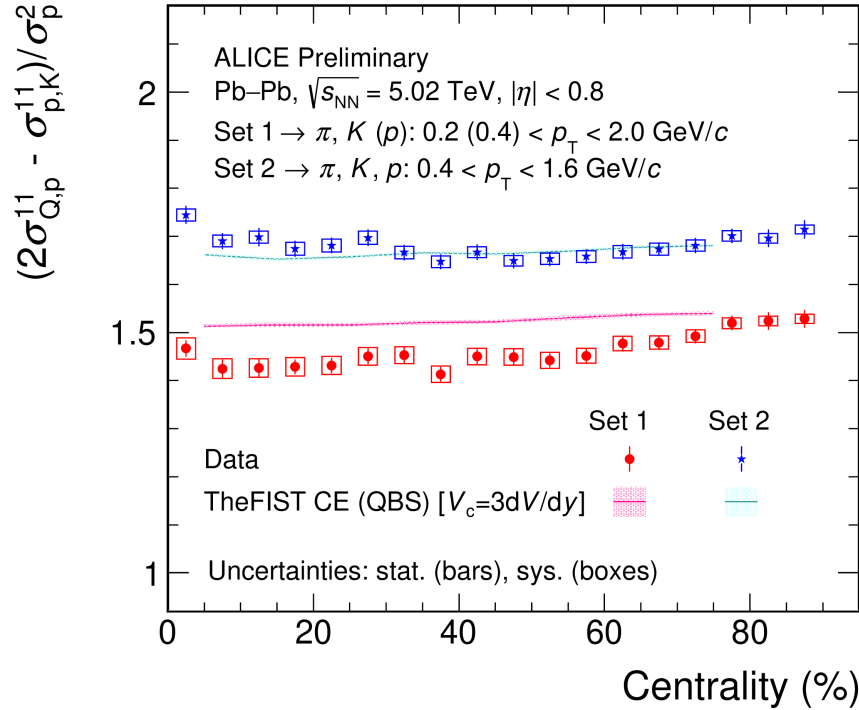
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H.-T. Ding et al., EPJ. A (2021) 57:202, CPOD-2024

- Momentum range dependence
- Deviation from Poisson baseline
- Subtle increasing trend from semicentral to peripheral collisions: $\sim 4-5\%$
 - \rightarrow Resonance decays!
 - \rightarrow Correlation volume effect!
 - \rightarrow Effect of magnetic field??

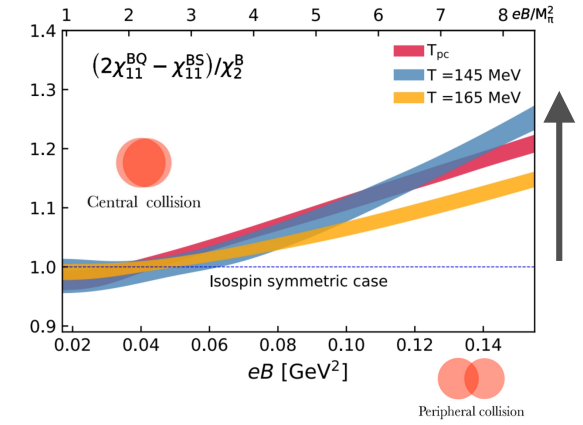
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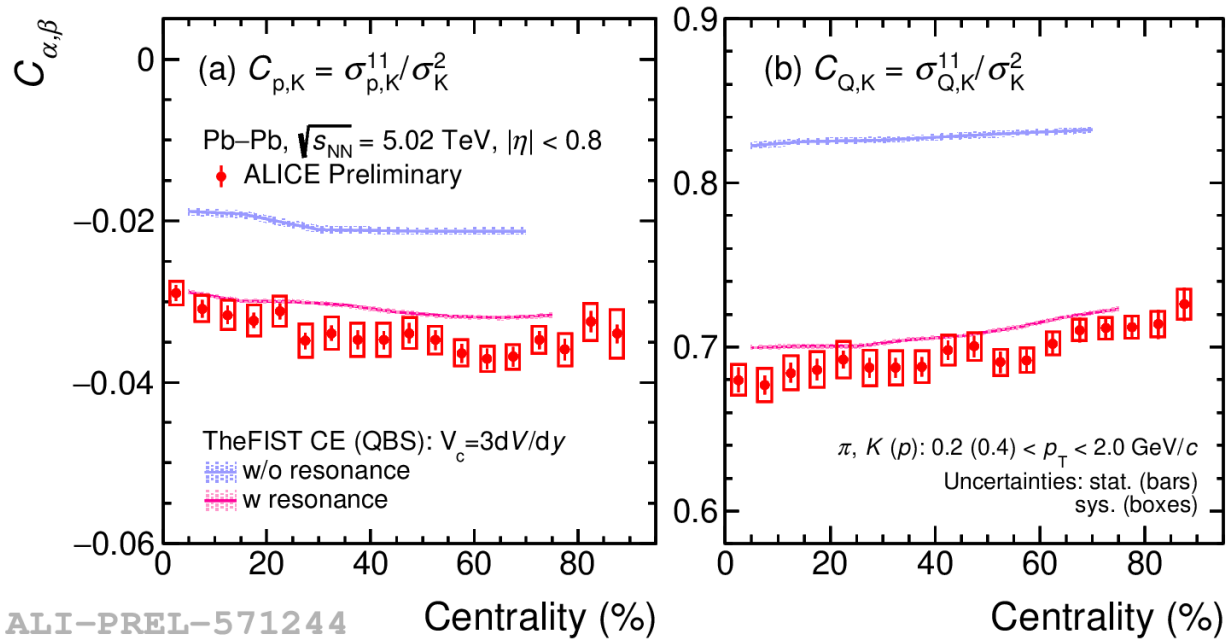
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ALI-PREL-574188



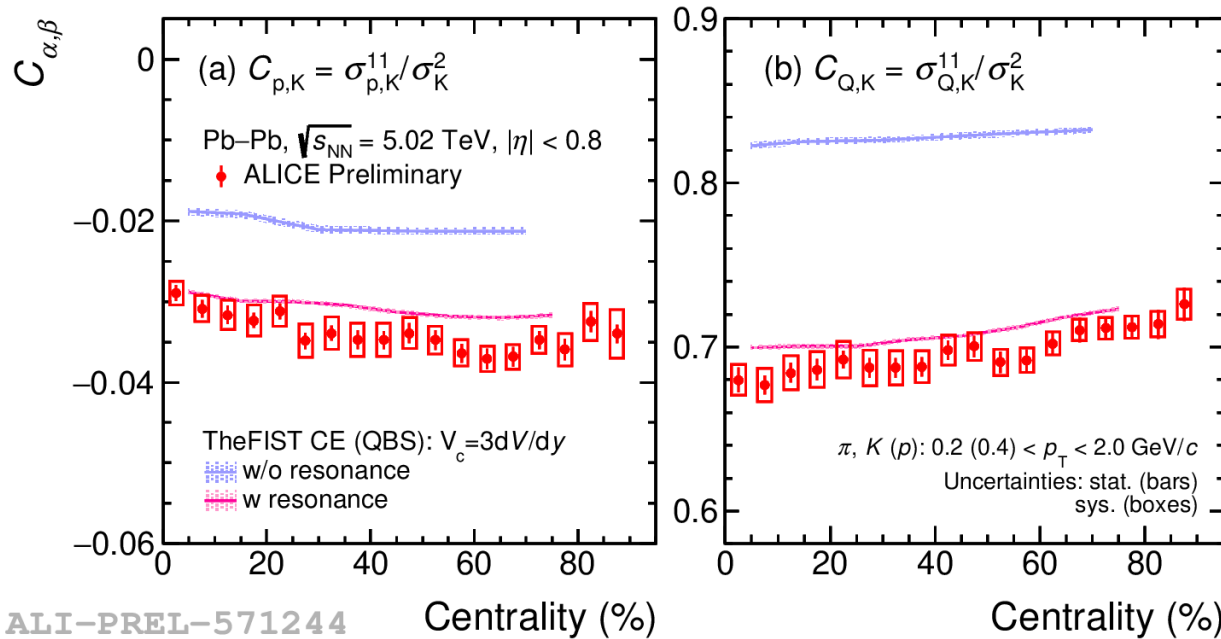
ThermalFIST Model: Parameters from published fit V. Vovchenko et al., Phys.Rev.C 100 (2019) 5, 054906



Canonical ensemble (CE) → exact conservation of Q, B, S in $V_c = 3 \text{ dV/dy}$

- **Significant impact of resonances**

ThermalFIST Model: Parameters from published fit V. Vovchenko et al., Phys.Rev.C 100 (2019) 5, 054906



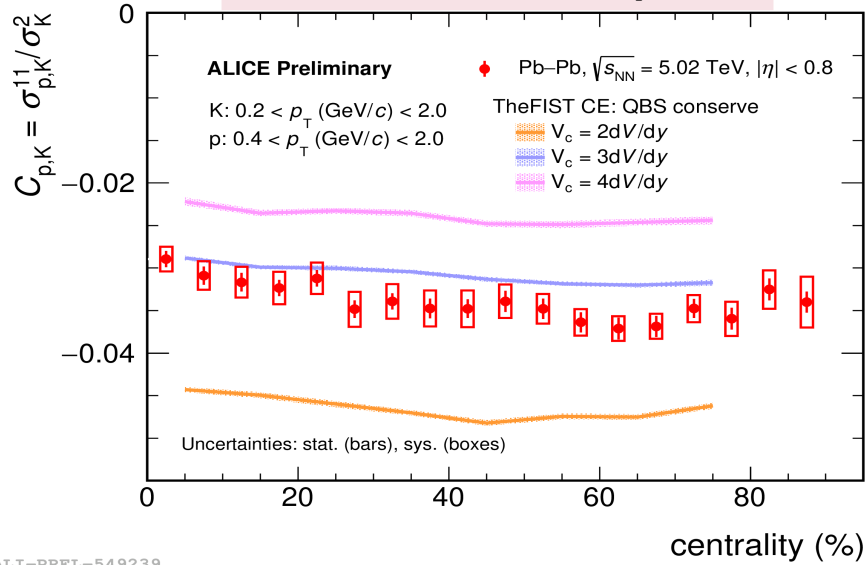
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- **Significant impact of resonances**
- **ThermalFIST is comparatively better** in capturing the resonance contributions

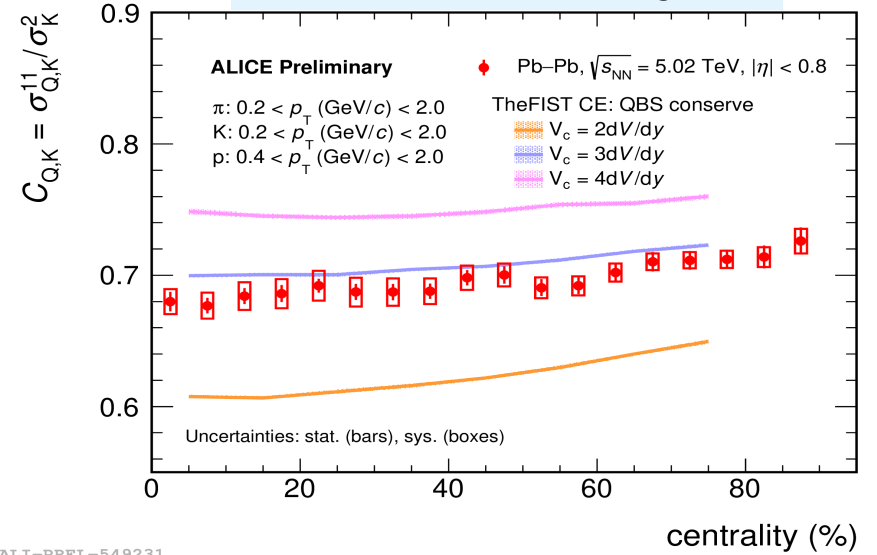
Effect of correlation volume



Correlation between p – K



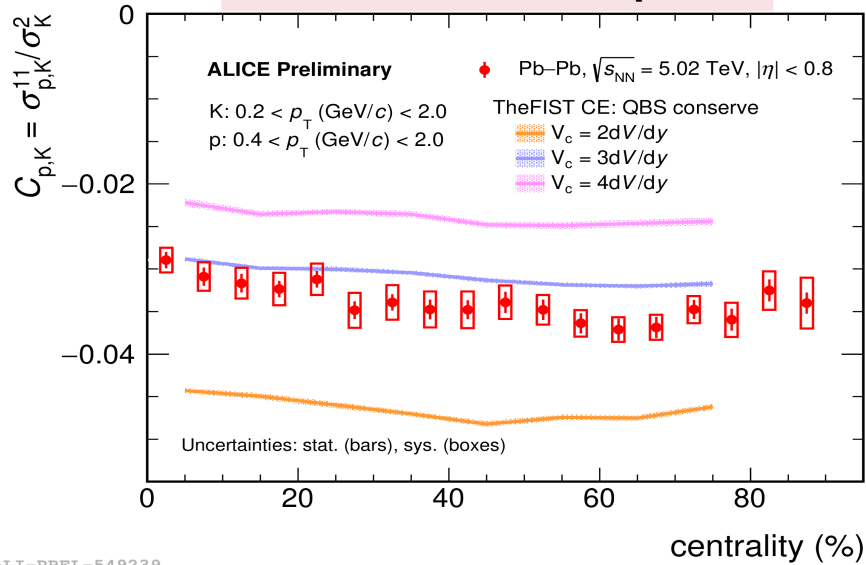
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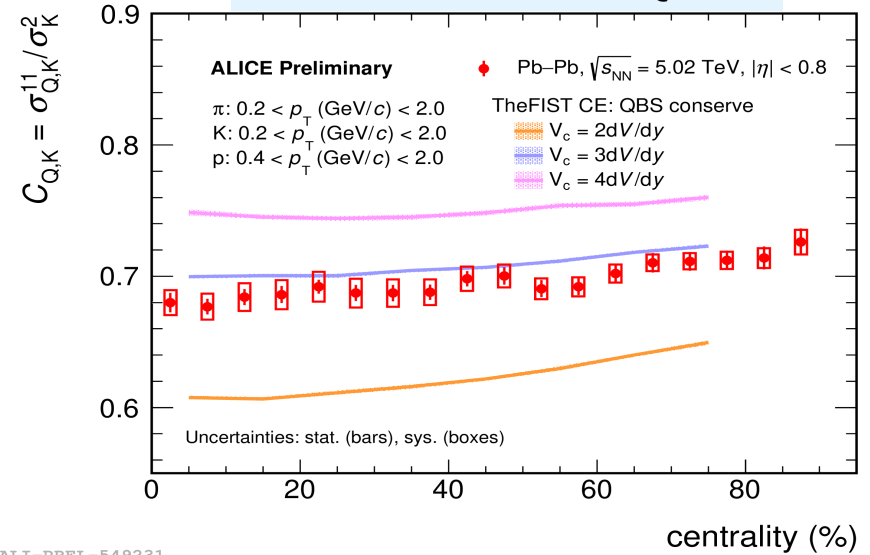
Effect of correlation volume

Correlation between p – K



ALI-PREL-549239

Correlation between Q – K

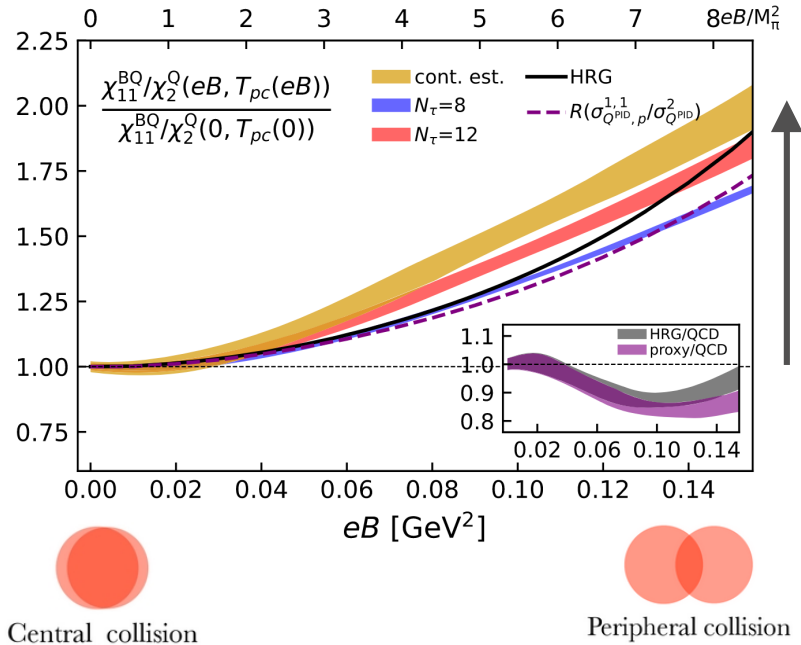


ALI-PREL-549231

- Sensitive to the correlation volume (V_c) in thermal model
- A combined χ^2 -minimization of three correlations (p – K, Q – K and Q – p) gives $V_c \sim 2.6dV/dy$ for Q, B, and S conservation
 - slightly lower than that of net-proton fluctuations, net- Λ fluctuations, and net- Ξ –net-K correlations ($V_c \sim 3dV/dy$)

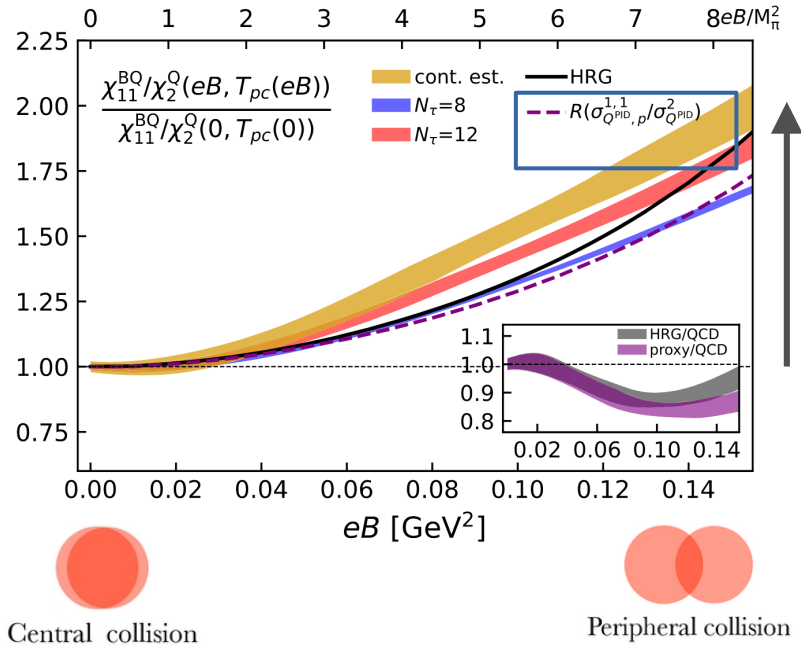
Magnetic field effect?

H.-T. Ding et al., *Phys.Rev.Lett* 132 (2024) 201903



Magnetic field effect?

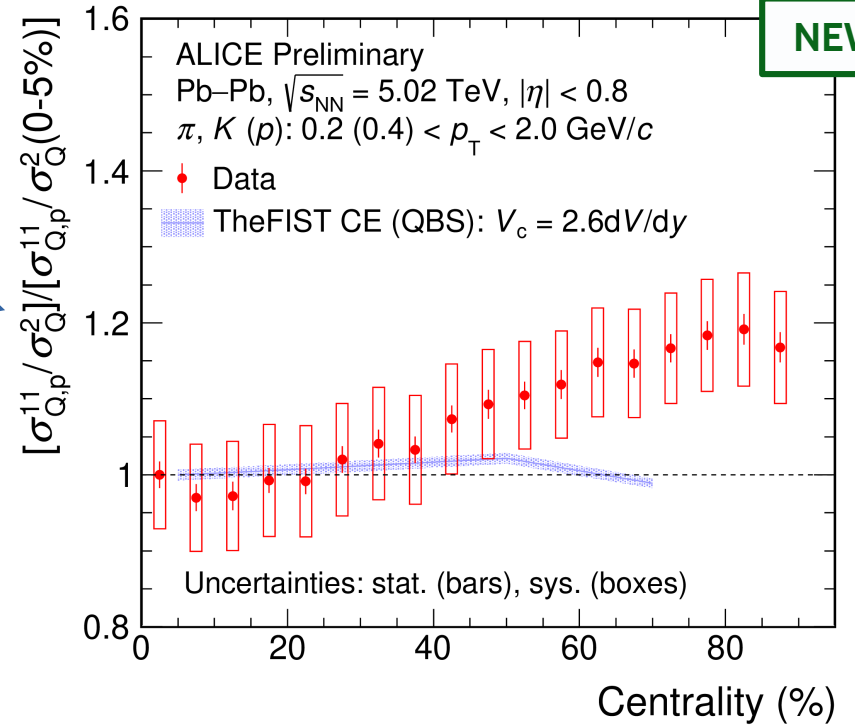
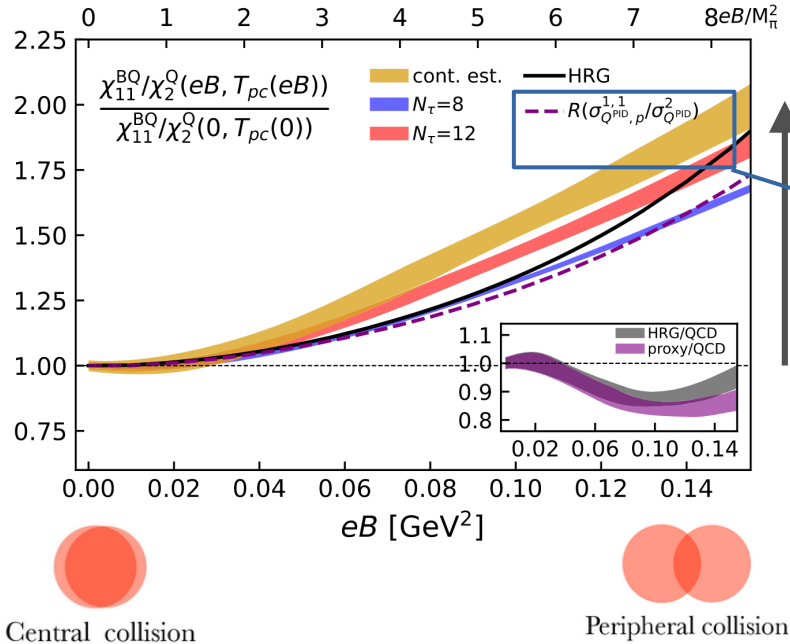
H.-T. Ding et al., *Phys.Rev.Lett* 132 (2024) 201903



Magnetic field effect?



H.-T. Ding et al., *Phy.Rev.Lett* 132 (2024) 201903

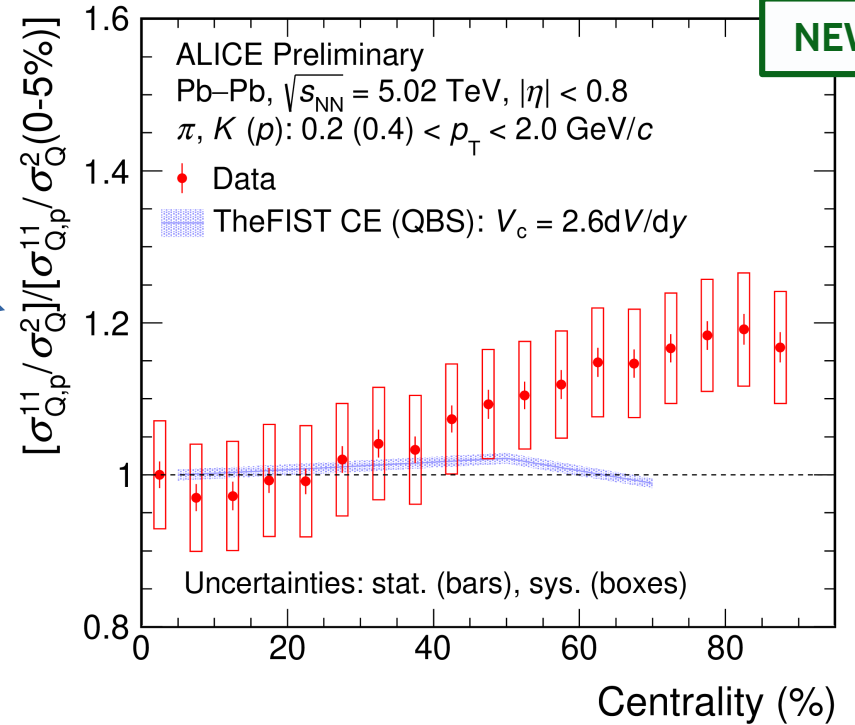
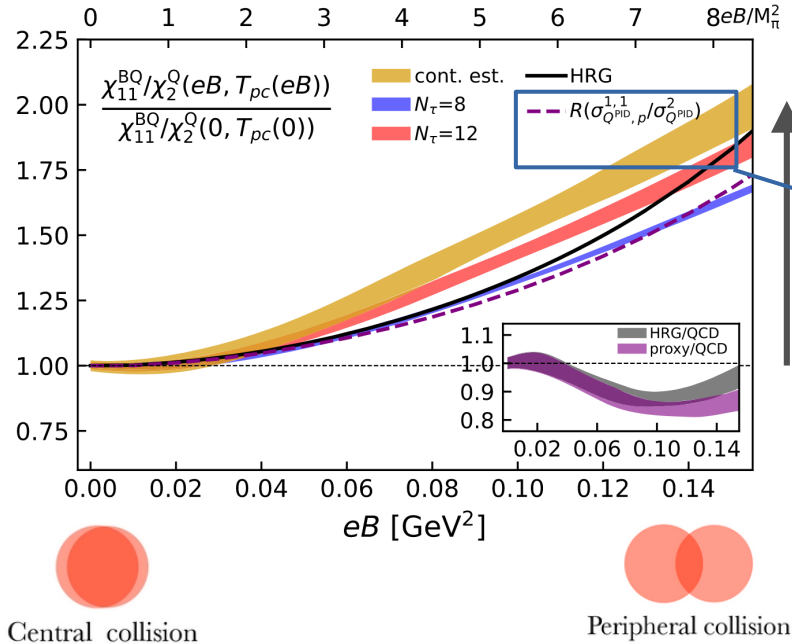


ALI-PREL-573205

Magnetic field effect?



H.-T. Ding et al., *Phy.Rev.Lett* 132 (2024) 201903



NEW

ALI-PREL-573205

- Observed **an increase of ~20% from central to peripheral collisions**
 – Hint of magnetic field effect?

- Centrality dependence of correlations among net-charge, net-baryon, and net-strangeness are presented for Pb–Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV.
- **Resonance decay** leads to deviation from Poisson baseline for all three measured correlations.
- Thermal-FIST model within CE framework and Q , B and S conservation suggests a correlation volume, $V_c \sim 2.6 dV/dy$ for explanation of all three correlations simultaneously.
- **Hint of magnetic field** effect in correlation of net-charge and net-proton.

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Stay tuned for more results on event-by-event fluctuations with Run 3 data.

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Stay tuned for more results on event-by-event fluctuations with Run 3 data.

Thank you



Additional slides



Swati Saha, NISER, India

Theory predictions

Magnetic field **✗**
 Isospin symmetry of u and d quarks

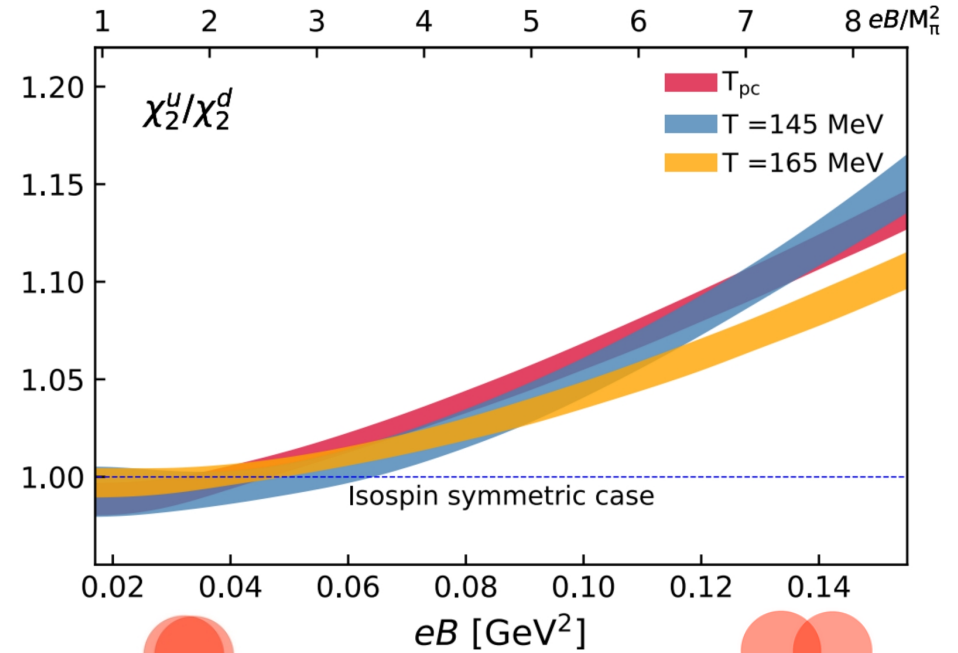


Magnetic field **✓**
 Isospin symmetry breaks

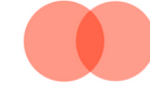
$$\text{At } eB = 0, \chi_u = \chi_d$$

$$2\chi_{11}^{QS} - \chi_{11}^{BS} = \chi_2^S$$

$$2\chi_{11}^{BQ} - \chi_{11}^{BS} = \chi_2^B$$



Central collision

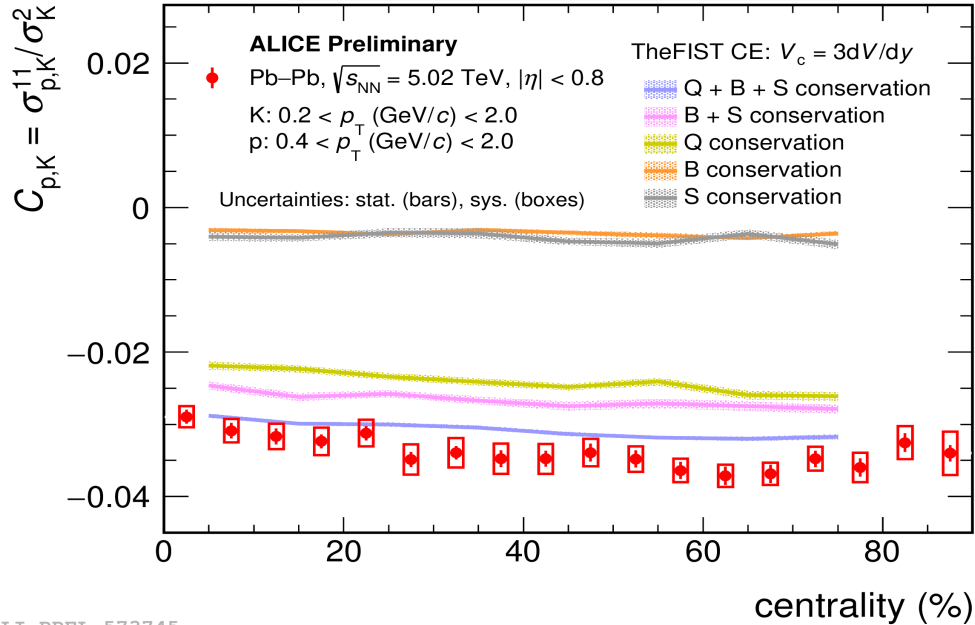


Peripheral collision

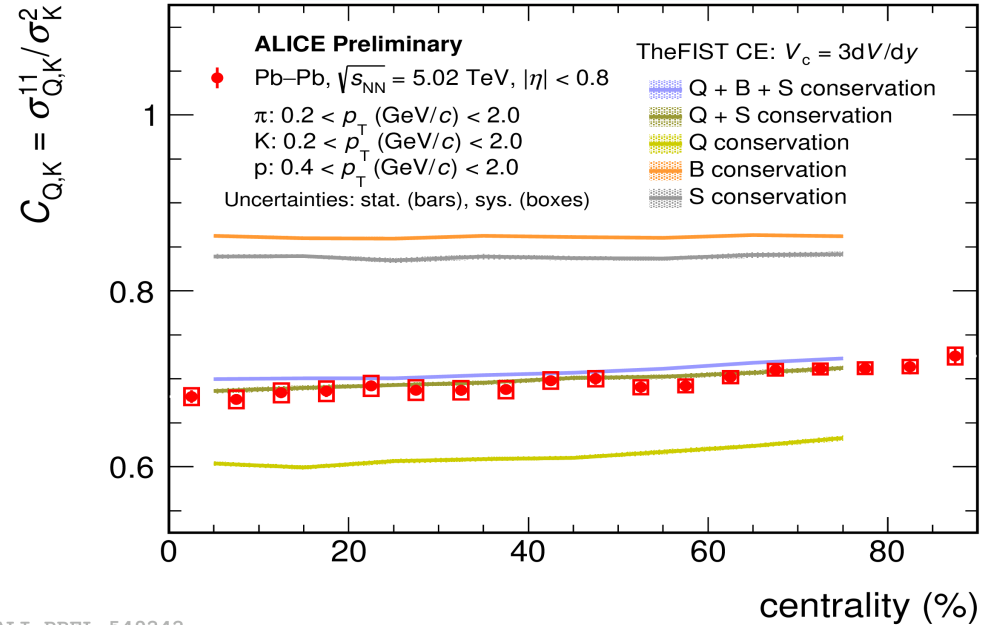
H.-T. Ding et al., EPJ. A (2021) 57:202, CPOD-2024

Effect of charge conservations

Correlation between p - K



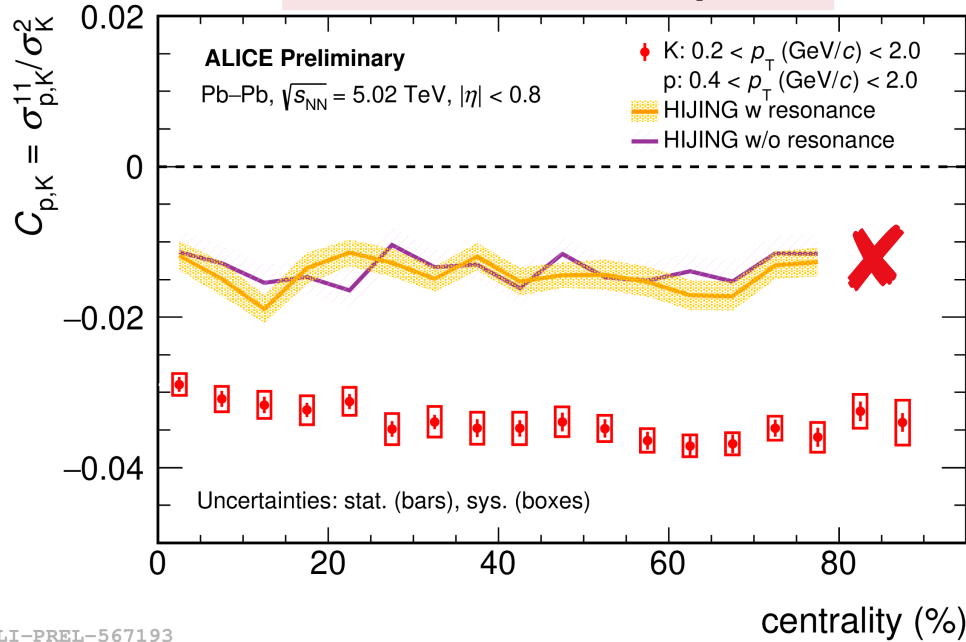
Correlation between Q - K



- Contribution to the net-particle correlations from Q, B, and S conservation are shown

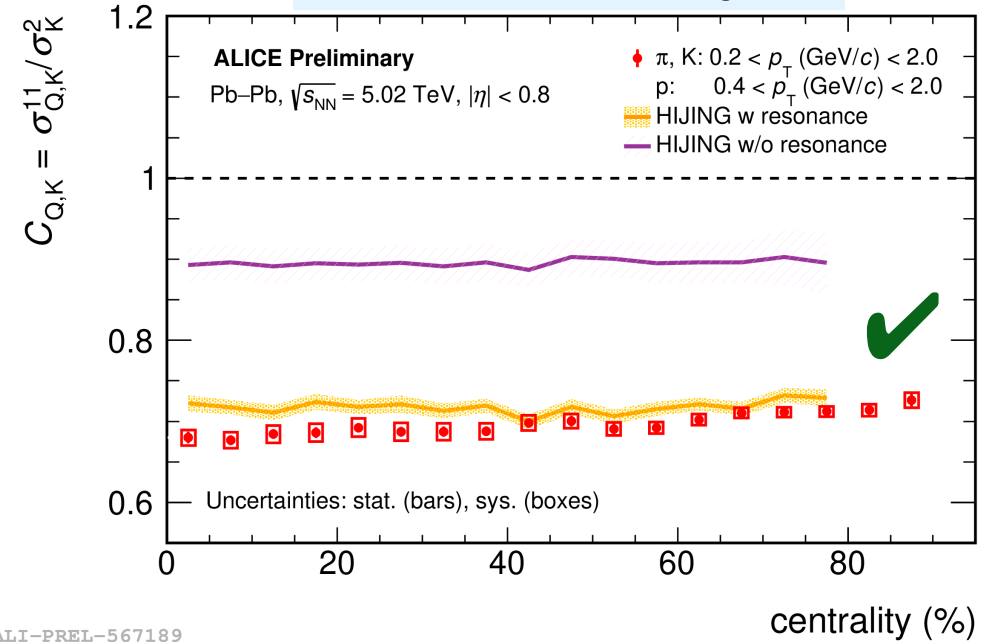
Effect of resonances

Correlation between p - K



ALI-PREL-567193

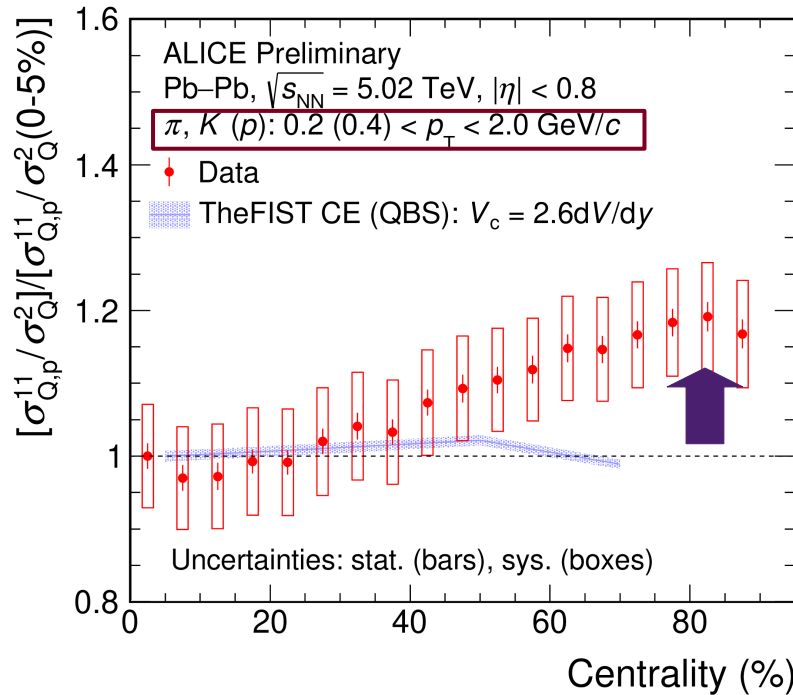
Correlation between Q - K



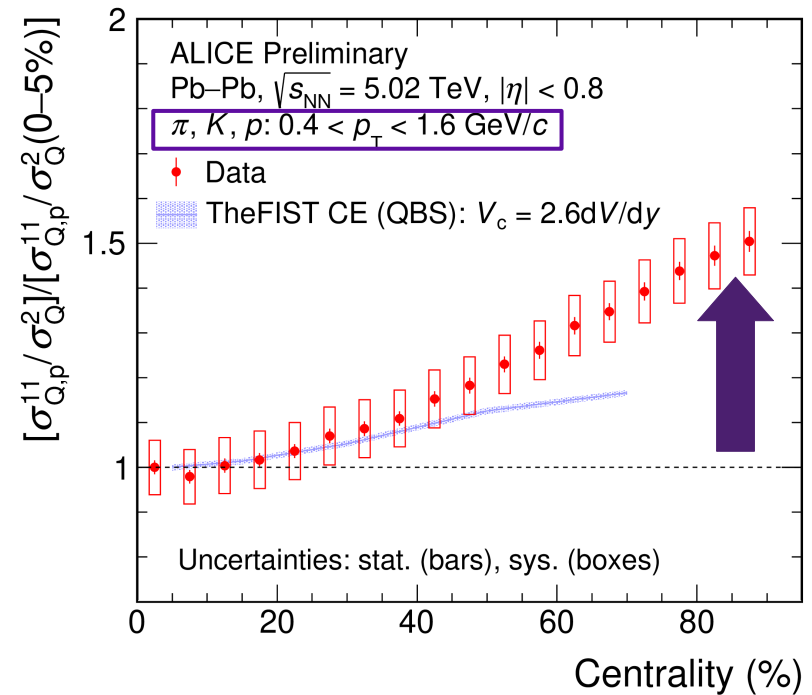
ALI-PREL-567189

- HIJING is not good in capturing the resonances for $C_{p,K}$, but good for $C_{Q,K}$

Magnetic Field?



ALI-PREL-573205



ALI-PREL-573623

- Larger deviation with change in the momentum range
→ low p_T pions diminishing the effect of magnetic field on Q – K correlations?