

## 1. Introduction

### Femtoscopy

- Study of momentum correlations of identical bosons
- Correlation function:  $C(Q) = \int D(\mathbf{r}) |\psi_Q(\mathbf{r})|^2 d^4r$
- Pair source distribution:
 
$$D(\mathbf{r}, \mathbf{K}) = \int S(\rho + \frac{\mathbf{r}}{2}, \mathbf{K}) S(\rho - \frac{\mathbf{r}}{2}, \mathbf{K}) d^4\rho$$
  - $\psi_Q(\mathbf{r})$ : symmetrized pair wave function
  - $S(\mathbf{x}, \rho)$ : single-particle freeze-out distribution (source)
  - $\mathbf{r}$ : pair separation four-vector
  - $\rho$ : pair center of mass four-vector
  - $\mathbf{K}$ : average momentum of the pair

### Lévy-type of distribution

- Generalization of Gaussian  $\rightarrow$  Lévy distribution:
 
$$\mathcal{L}(\alpha, R; \mathbf{r}) = (2\pi)^{-3} \int d^3q e^{i\mathbf{q}\mathbf{r}} e^{-\frac{1}{2}|qR|^\alpha}$$
- Lévy exponent  $\alpha$ :
  - $\alpha = 2 \rightarrow$  Gaussian shape,  $\alpha < 2 \rightarrow$  Power-law
- Lévy scale  $R$ : Geometry of the source
- Reasons for the appearance of Lévy-type sources [1-4]:
  - Critical behavior, anomalous diffusion, jet fragmentation
- $D(\mathbf{r})$  is autocorrelation of  $S(\mathbf{r})$ :
 
$$S(\mathbf{r}) = \mathcal{L}(\alpha, R; \mathbf{r}) \rightarrow D(\mathbf{r}) = \mathcal{L}(\alpha, 2^{\frac{1}{\alpha}}R; \mathbf{r})$$

### EPOS event generator

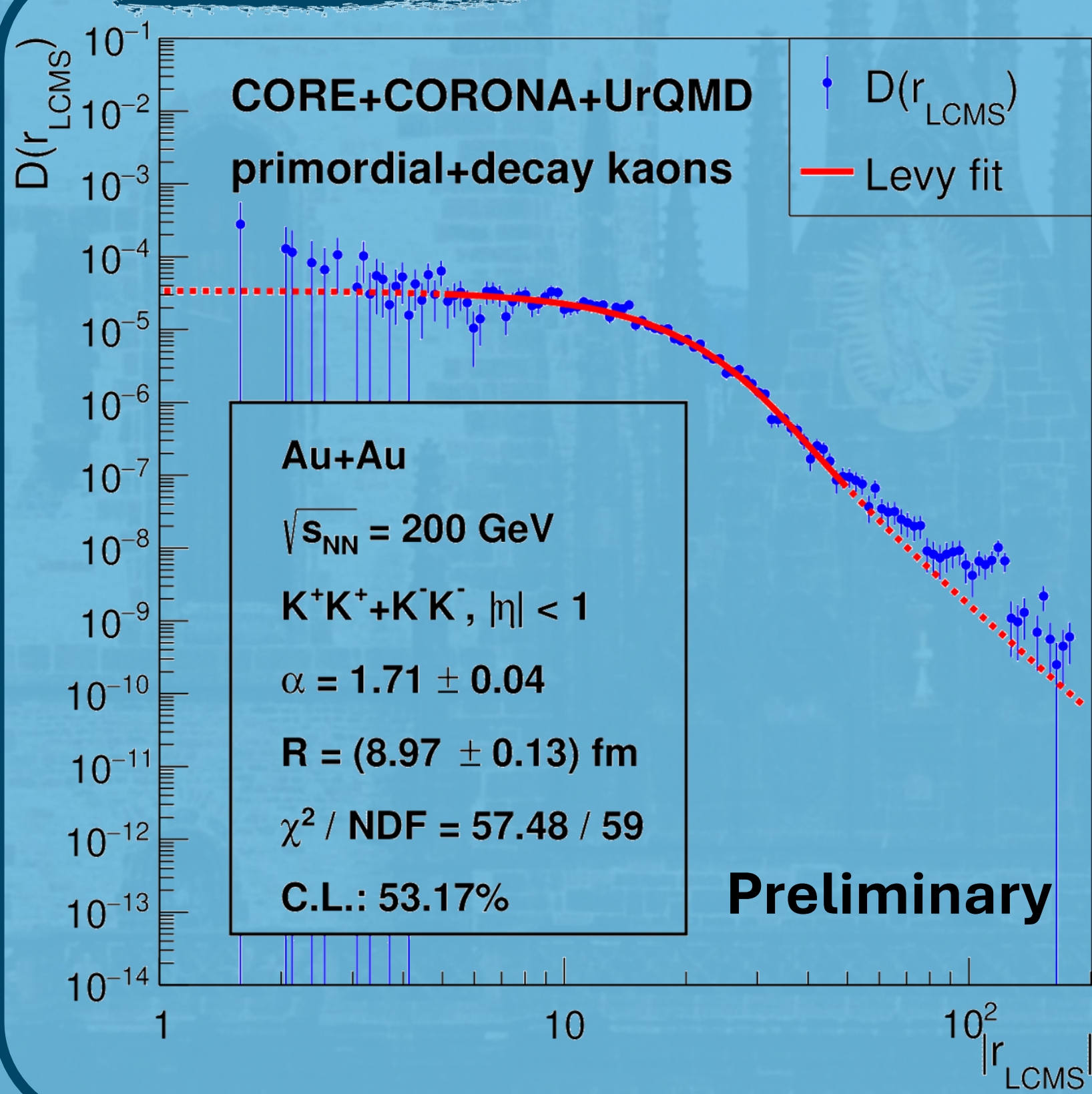
- Phenomenological model using Monte Carlo techniques [5]
- Core-Corona division
- The three stages of evolution:
  - Initial interactions described by Parton-based Gribov-Regge theory
  - Viscous Hydrodynamical evolution
  - Hadronic rescattering, based on UrQMD

### Method of analysis

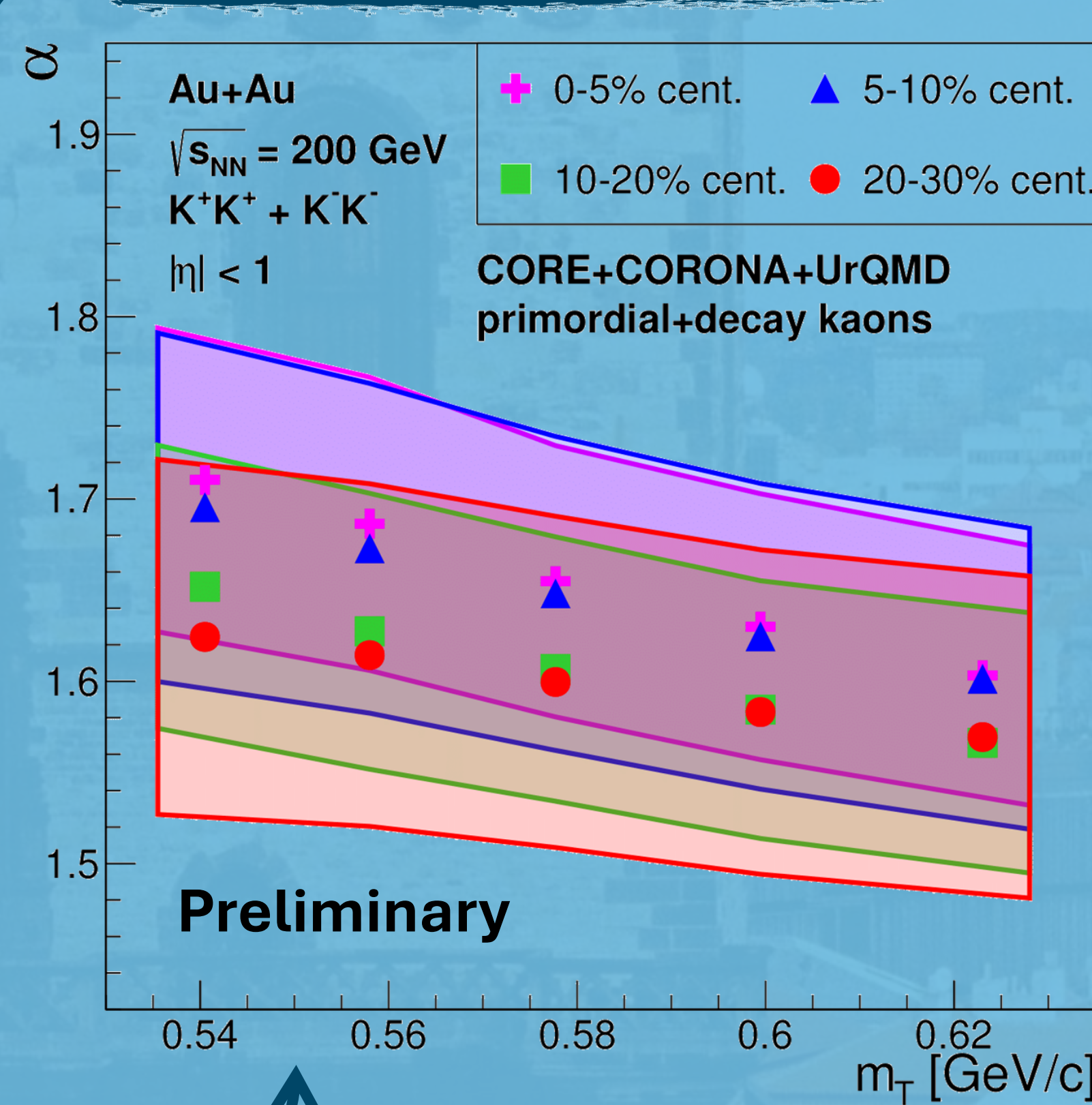
- $\sqrt{s_{NN}} = 200$  GeV Au+Au collisions generated by EPOS359
- Angle-averaged one-dimensional distance distribution:
 
$$D(r_{LCMS}) = \int D(\mathbf{r}_{LCMS}, t) d\Omega_{LCMS} dt$$
 LCMS: Longitudinal co-moving system
- Limited statistics: event-by-event investigation by combining multiple histograms
- The Lévy parameters are calculated from thousands of fits
- Measurements in 4 centrality and 5  $k_T$  classes
- Study of 2 different cases:
  - CORE with primordial kaons
  - CORE+CORONA+UrQMD with primordial + decay kaons

## 2. Analysis

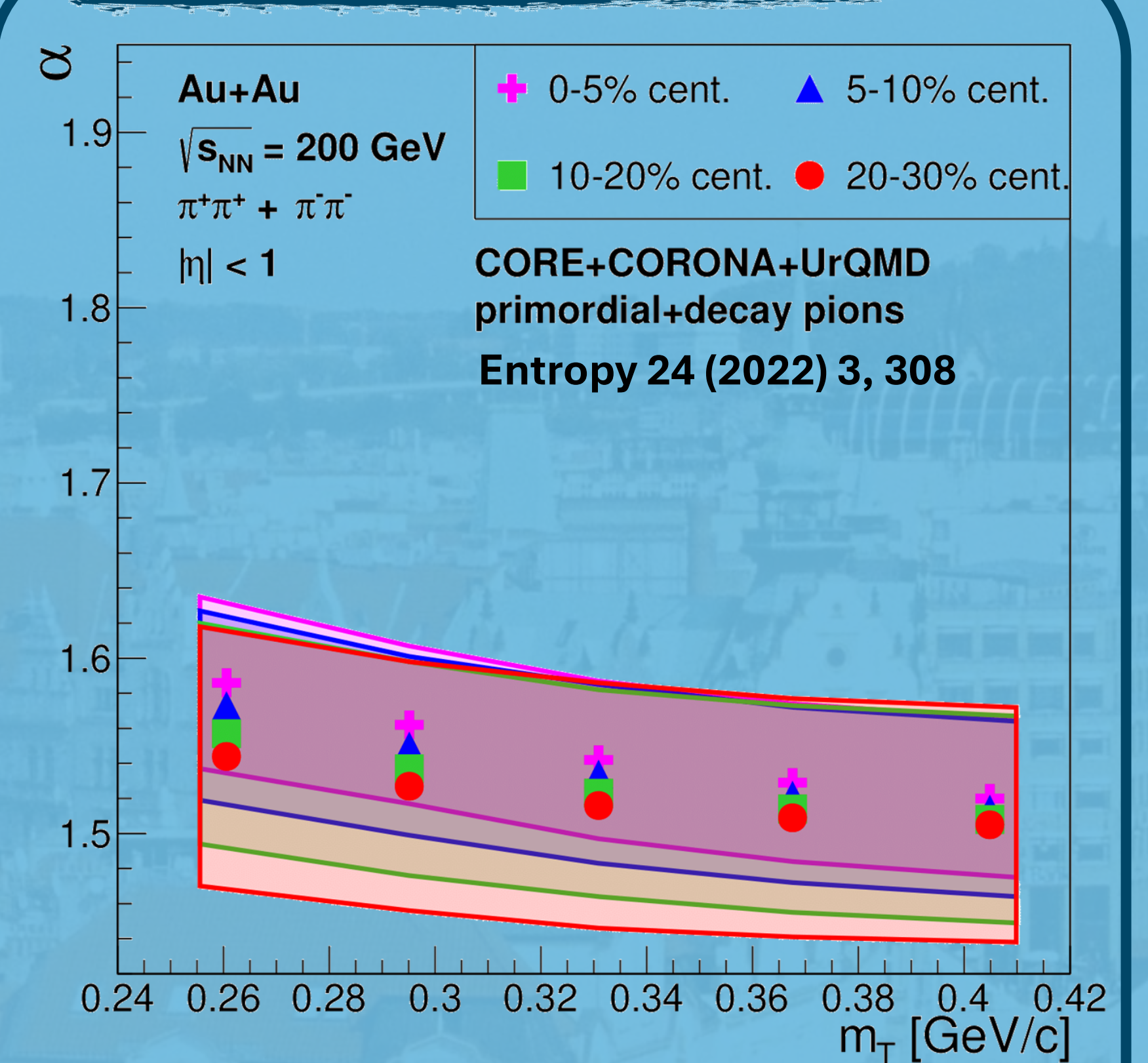
### Example fit



### Lévy parameters - Kaons



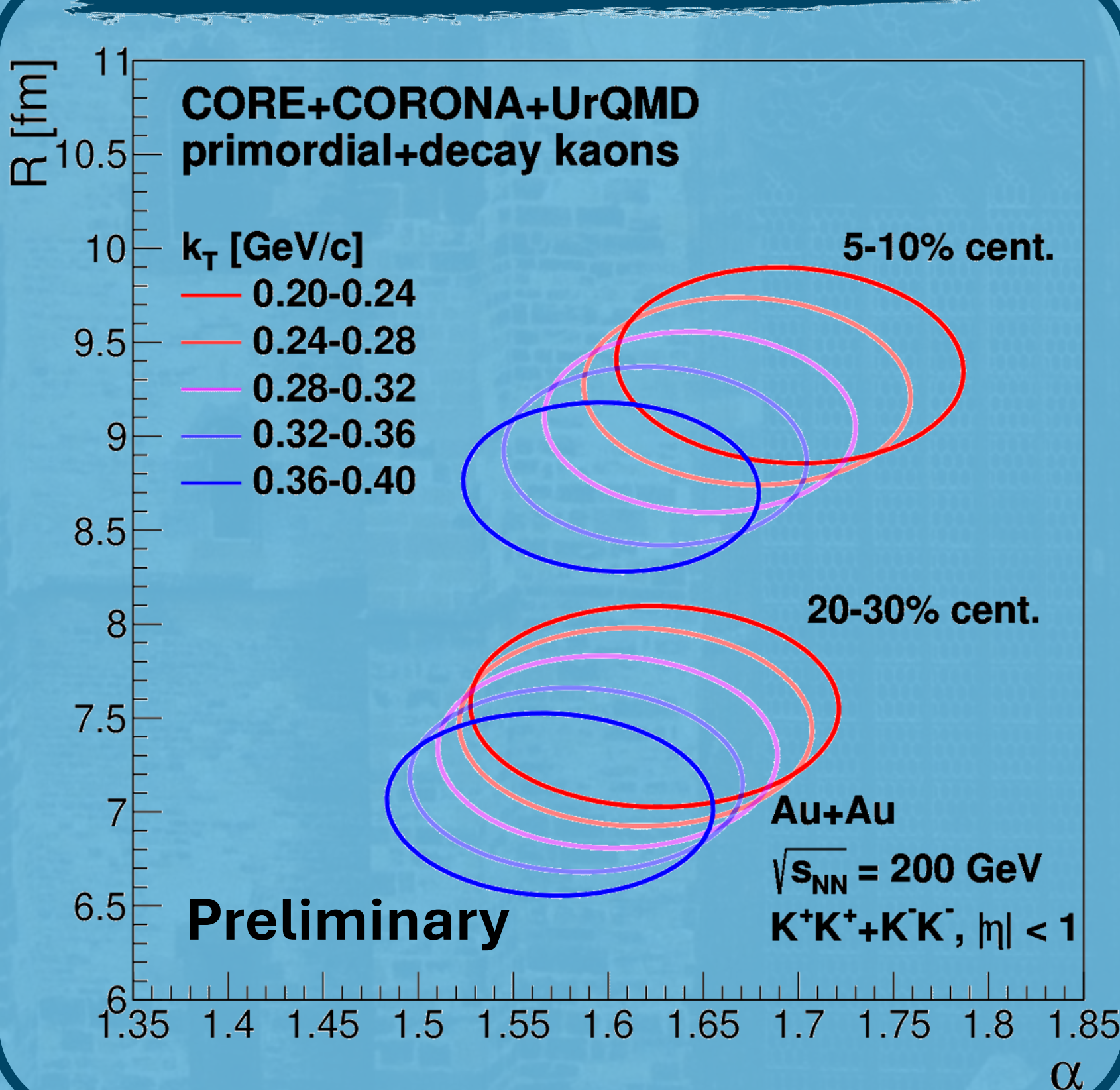
### Lévy parameters - Pions [6]



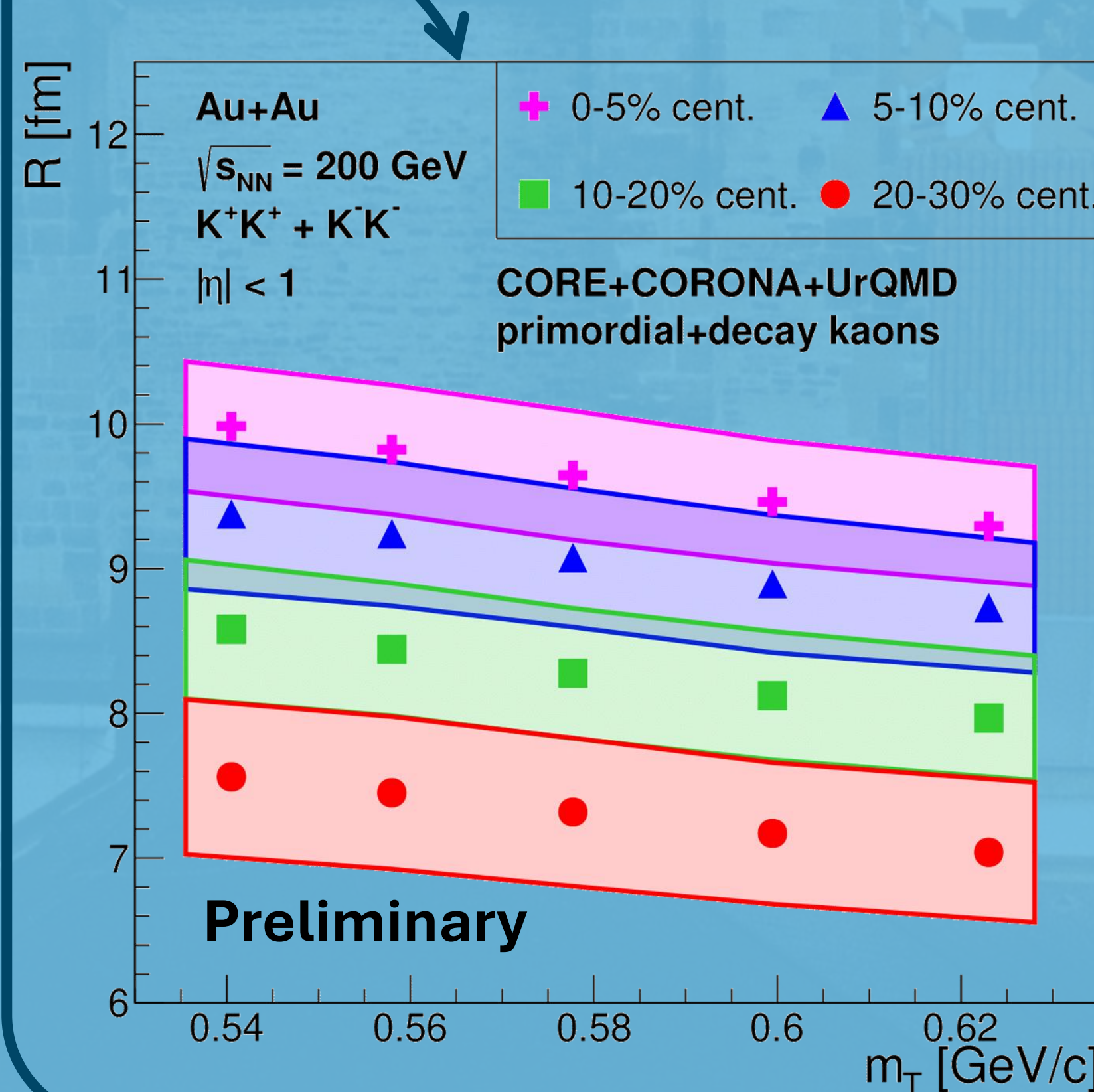
## 3. Results

Fit results loaded into a 2D histogram

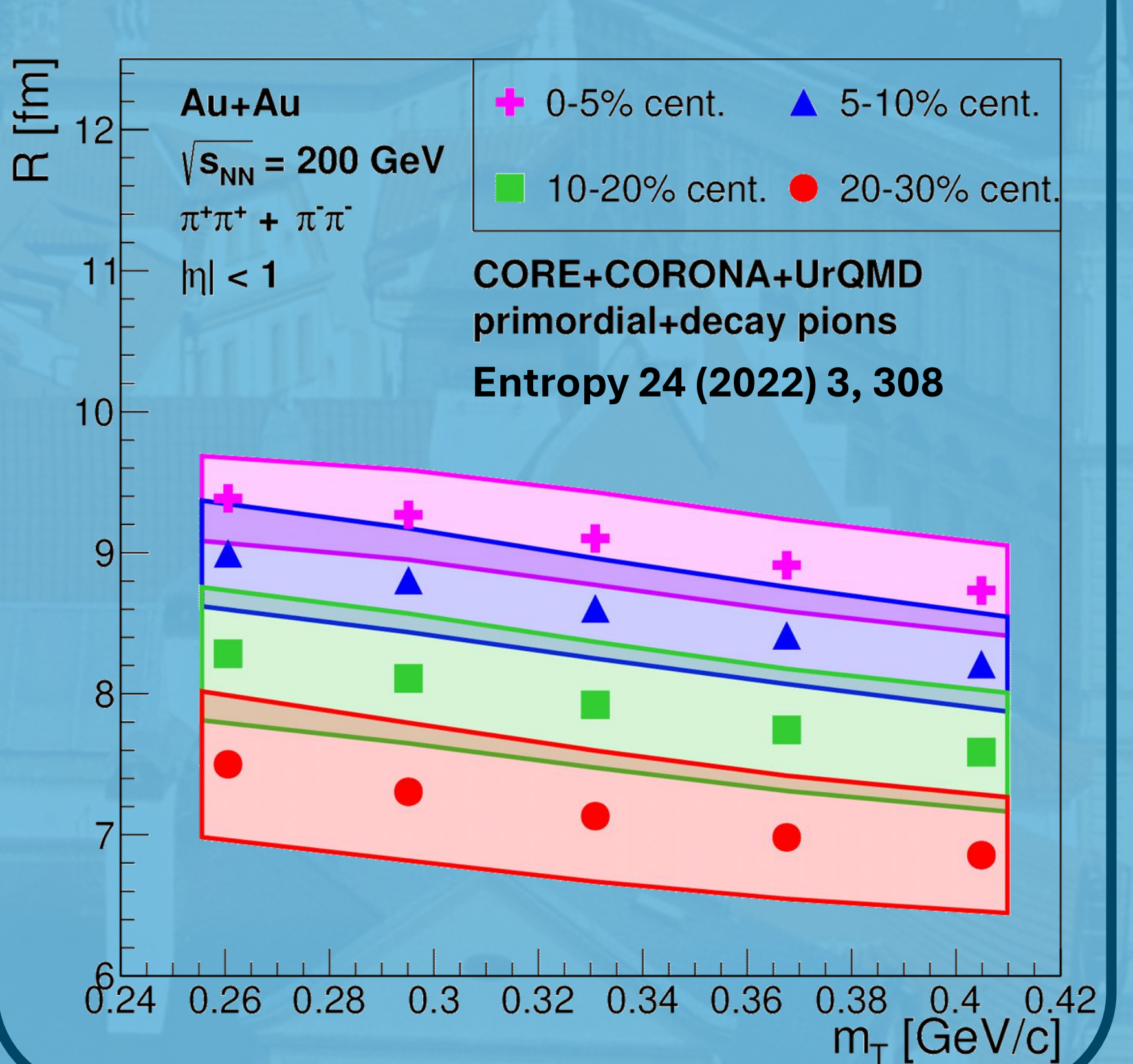
### 1 $\sigma$ contours of $R$ vs. $\alpha$ dist.



Extracted mean and variance values of the parameters



- $\alpha(K^\pm) \geq \alpha(\pi^\pm)$ , contrary to expectations [7]
- $R(K^\pm) \geq R(\pi^\pm)$  despite larger  $m_T$



## 4. Endnote

### Summary

- Kaon-kaon and pion-pion pair sources fitted with Lévy function
- **CORE with primordial particles: Gaussian source for both kaons and pions**
- **CORE+CORONA+UrQMD with primordial + decay particles:**
  - $\alpha(K^\pm) > \alpha(\pi^\pm)$ , anomalous diffusion suggests opposite [7]
  - $R(K^\pm) \geq R(\pi^\pm)$  despite larger  $m_T$ ,  $R$  decreases with  $m_T$  and cent.
- Lévy sources observed from SPS through RHIC to LHC [8]
- EPOS analysis conducted for kaons, pions, and protons at  $\sqrt{s_{NN}} = 2.76$  TeV [9]
- No agreement with PHENIX kaon preliminary results [10]

### References

- [1] Csörgő, Hegyi, Zajc, Eur.Phys.J. C36;
- [2] Csörgő, Hegyi, Novák, Zajc, AIP Conf.Proc. 828;
- [3] Metzler, Klafter, Physics Reports 339 (2000) 1-77
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- [5] Werner, K. et al., Phys. Rev.C82, 044904 (2010)
- [6] D. Kincses, M. Stefaniak and M. Csanád, Entropy 24 (2022) 3, 308
- [7] M. Csanád, T. Csörgő, M. Nagy, Braz.J.Phys. 37 (2007) 1002
- [8] M. Csanád, D. Kincses, Universe 10 (2024) 2, 54
- [9] B. Kórodi, D. Kincses, M. Csanád, Phys.Lett.B 847 (2023), 138295
- [10] L. Kovács for the PHENIX Collaboration, Universe 9 (2023) 7, 336