

Hunting for Hypercharge Anapole Dark Matter in All Spin Scenarios

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Dark Matter (DM)

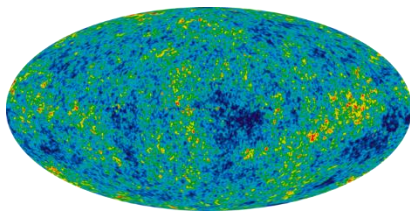
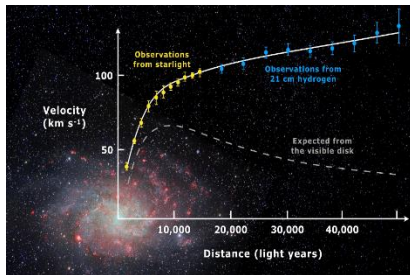
[Wikipedia. PDG]

Empirical Evidences

(several but only **gravitational**)

- Galaxy rotation curves
- Velocity dispersions
- Galaxy clusters
- Gravitational lensing
- Cosmic microwave background
- Structure formation
- Bullet cluster

...



DM Candidates (too many?!)

- QCD axions
- Axion-like particles
- Fuzzy CDM
- SM neutrinos
- Sterile neutrinos
- Supersymmetry
- Extra dimensions
- Little Higgs
- Simplified models
- Effective field theories

- Primordial black holes
- MACHOs
- Macros

- Strangelet
- Superfluid vacuum theory
- Dynamical dark matter

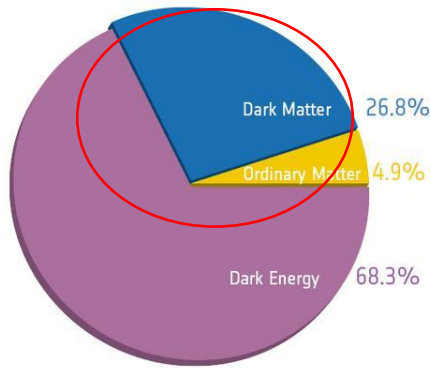
- Modified Newtonian dynamics
- Tensor-vector-scalar gravity
- Entropic gravity

...

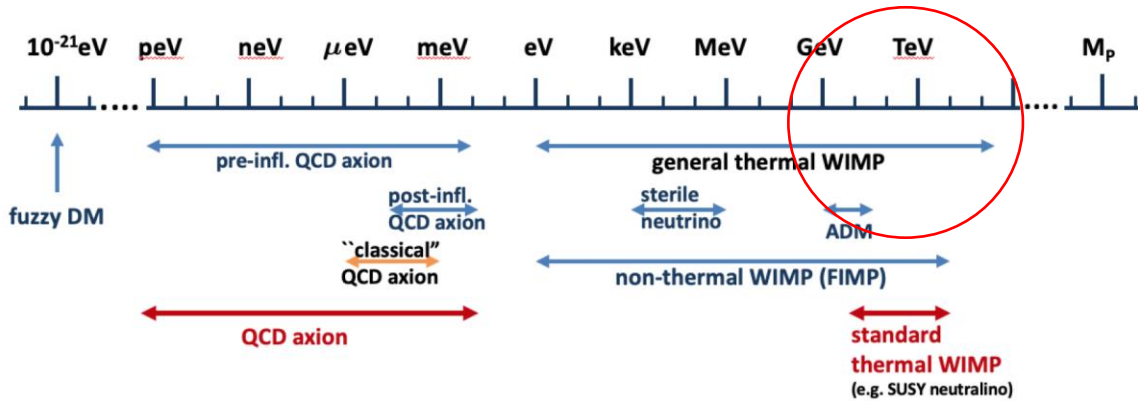
Dark!

conceptually and practically

[NSF]



Our desperate guess and blind betting
A single (elementary or not) Majorana particle



GeV ~ a few TeV mass
Any spin (1/2, 1, 3/2, 2, ...)
Colorless and electrically neutral
Hypercharge U(1) gauge symmetry
Weak due to higher-dim EFT operators

[Bilard ea, 2021]

⊕

Standard Model

(completed with H discovery in 2012)

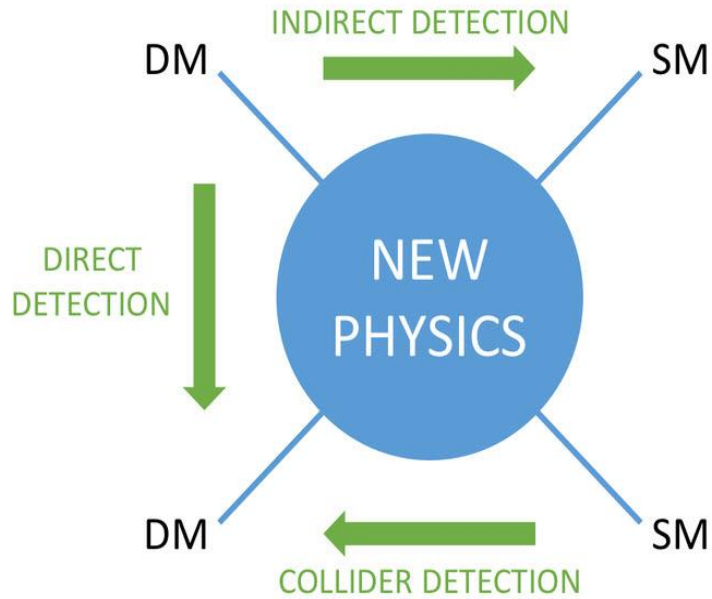
$$SU(3)_C \times SU(2)_L \times U(1)_Y \Rightarrow SU(3)_C \times U(1)_{EM}$$

valid at least up to from zero to several TeV scales!

Anapole
DM Particle

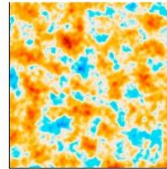
To be, or not to be?
Mass. Spin, couplings?

Complementary DM Hunting Strategies



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[A lot of ingenious probes]



Planck

$$\Omega_\chi h^2 \simeq 0.12$$

XENONnT
(1.1 t-y and 20 t-y)



**Indirect detection
(relic abundance)**

$$DM + DM \Rightarrow SM + SM$$

Direct detection

$$DM + SM \Rightarrow DM + SM$$

Collider detection

$$SM + SM \Rightarrow DM + DM$$

⊕

Conceptual constraints
unitarity, perturbativity



LHC and HL-LHC
(139 fb⁻¹ and 3 ab⁻¹)

History of Anapole DM Studies

Scenario (Spin)	EM anapole DM		Hypercharge anapole DM			
	1/2	1	1/2	1	3/2	2
Relic abundance	C.M. Ho and R. J. Scherrer, PLB (2013)...	✗	C. Arina, et al. EPJC (2021)...			
LHC search	Y. Gao, C.M. Ho, and R. J. Scherrer (2014)...	✗	This work ✓ ...			
Direct detection	C.M. Ho and R. J. Scherrer, PLB (2013)...	J. Hisano, A. Ibarra, and R. Nagai JCAP (2020)...	↓			

A generic analytic & numerical (phenomenological) analysis for a hypercharge anapole DM particle of any spin (1/2, 1, 3/2, 2, ...)

Hunting Target

A hypercharge anapole DM particle of any spin

Construct general 3-point $\chi\chi B$ vertices by imposing U(1) hypercharge symmetry and identical particle (Majorana) conditions for any spin



Evaluate the relic abundance, production cross sections at the (HL-)LHC and direct detection rate at the XENONnt for spin-1/2, 1, 3/2, 2, ...

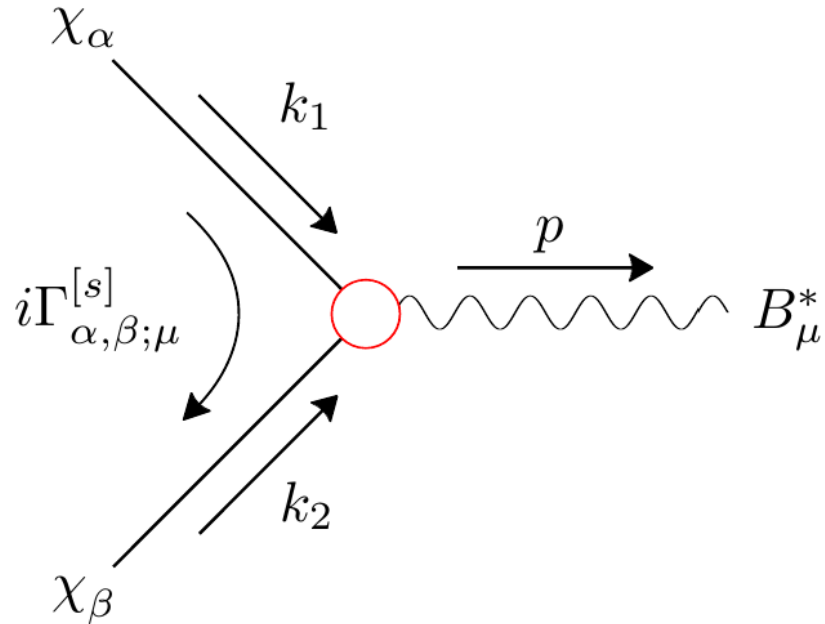


Combining the experimental results with a naïve perturbativity bound (NPD), we draw a unified picture for hunting for the hypercharge anapole DM.



Grasp the implications for higher-spin anapole DM particles.

Constructing Anapole Vertices



$$\begin{aligned}
 p &= k_1 + k_2 & \alpha &\equiv \alpha_1 \cdots \alpha_n & \text{with } n &= \begin{cases} s & \text{for bosons} \\ s - \frac{1}{2} & \text{for fermions} \end{cases} \\
 q &= k_1 - k_2 & \beta &\equiv \beta_1 \cdots \beta_n & &
 \end{aligned}$$

Hypercharge U(1) gauge invariance
 ($B = \gamma \oplus Z$)

$$p^\mu \Gamma_{\alpha,\beta;\mu}^{[s]} = 0$$

Identical-particle (IP) relation

$$C \Gamma_{\beta,\alpha;\mu}^{[s]}(p, -q) C^{-1} = \Gamma_{\alpha,\beta;\mu}^{[s]}(p, q) \quad \text{for fermions}$$

$$\Gamma_{\beta,\alpha;\mu}^{[s]}(p, -q) = \Gamma_{\alpha,\beta;\mu}^{[s]}(p, q) \quad \text{for bosons}$$

$$(C = i\gamma^2\gamma^0)$$

General Algorithm [SY Choi, JH Jeong, PRD (2022)]

$$\hat{p} = p/\sqrt{p^2}$$

$$\hat{q} = q/\sqrt{-q^2}$$



$$g_{\perp\mu\nu} = g_{\mu\nu} - \hat{p}_\mu \hat{p}_\nu + \hat{q}_\mu \hat{q}_\nu$$

$$\gamma_{\perp\mu} = g_{\perp\mu\nu} \gamma^\nu$$

$$\langle \alpha\beta\hat{p}\hat{q} \rangle = \varepsilon_{\alpha\beta\rho\sigma} \hat{p}^\rho \hat{q}^\sigma$$



$$S_{\alpha\beta}^0 = \hat{p}_\alpha \hat{p}_\beta$$

$$S_{\alpha\beta}^\pm = \frac{1}{2} [g_{\perp\alpha\beta} \pm i \langle \alpha\beta\hat{p}\hat{q} \rangle]$$

$$V_{\alpha\beta;\mu}^\pm = \hat{p}_\beta S_{\alpha\mu}^\pm + \hat{p}_\alpha S_{\beta\mu}^\mp$$

$$A_\mu = \gamma_{\perp\mu} \gamma_5$$

$$V_{\alpha\beta;\mu} = \hat{p}_\beta g_{\perp\alpha\mu} + \hat{p}_\alpha g_{\perp\beta\mu}$$



$[g]^n$	\rightarrow	$g_{\alpha_1\beta_1} \cdots g_{\alpha_n\beta_n}$
$[S^0]^n$	\rightarrow	$S_{\alpha_1\beta_1}^0 \cdots S_{\alpha_n\beta_n}^0$
$[S^\pm]^n$	\rightarrow	$S_{\alpha_1\beta_1}^\pm \cdots S_{\alpha_n\beta_n}^\pm$
$[V^\pm]^n$	\rightarrow	$V_{\alpha_1\beta_1;\mu_1}^\pm \cdots V_{\alpha_n\beta_n;\mu_n}^\pm$
$[A]$	\rightarrow	A_μ
$[V]$	\rightarrow	$V_{\alpha\beta;\mu}$

Half-integer $s = n + 1/2$

$$[\Gamma_F^{[s]}] = \left(\frac{p^2}{\Lambda^2}\right) [A] \sum_{\tau=0}^n \left(\frac{p^2}{\Lambda^2}\right)^\tau f_\tau^- [g]^{n-\tau} [S^0]^\tau + \left(\frac{p^2 \sqrt{p^2}}{\Lambda^3}\right) [V] \sum_{\tau=1}^n \left(\frac{p^2}{\Lambda^2}\right)^{\tau-1} f_\tau^+ [g]^{n-\tau} [S^0]^{\tau-1}$$

Integer $s = n \neq 0$

[Boudjema and Hamzaoui, PRD (1991)]

$$[\Gamma_B^{[s]}] = \sqrt{p^2} \left(\frac{p^2}{\Lambda^2}\right) \sum_{\tau=1}^n \left(\frac{p^2}{\Lambda^2}\right)^{\tau-1} (b_\tau^- [V^-] + b_\tau^+ [V^+]) [g]^{n-\tau} [S^0]^{\tau-1}$$

2s terms \Rightarrow 1 (fermionic) vs 2 (bosonic) leading dim-6 terms

Leading $1/\Lambda^2$ -order Anapole Terms

Half-integer $s = n + 1/2$

$$\Gamma_{\mu}^{[1/2]} = \frac{p^2}{\Lambda^2} a_{1/2} \gamma_{\perp\mu} \gamma_5$$

$$\Gamma_{\alpha,\beta;\mu}^{[3/2]} = \frac{p^2}{\Lambda^2} a_{3/2} \gamma_{\perp\mu} \gamma_5 g_{\alpha\beta}$$

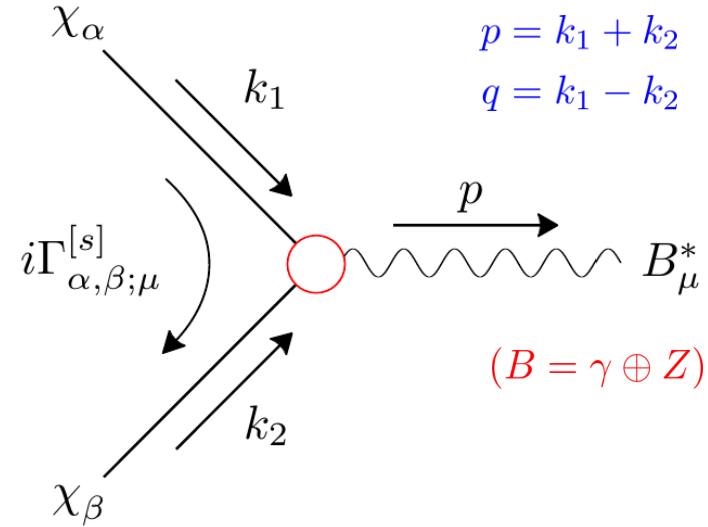
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Integer $s = n \neq 0$

$$\Gamma_{\alpha,\beta;\mu}^{[1]} = \frac{ip^2}{\Lambda^2} [a_1 \langle \alpha\beta\mu q \rangle_{\perp} - b_1 (p_{\alpha} g_{\perp\beta\mu} + p_{\beta} g_{\perp\alpha\mu})]$$

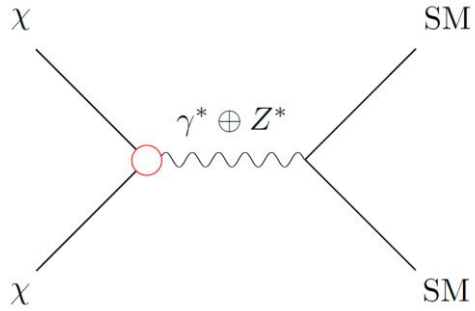
$$\Gamma_{\alpha_1,\alpha_2,\beta_1,\beta_2;\mu}^{[2]} = \frac{ip^2}{\Lambda^2} [a_2 \langle \alpha_1\beta_1\mu q \rangle_{\perp} - b_2 (p_{\alpha_1} g_{\perp\beta_1\mu} + p_{\beta_1} g_{\perp\alpha_1\mu})] g_{\alpha_2\beta_2}$$

...



Relic Abundance Constraints

Self-annihilation



$$\Omega_\chi h^2 \propto \frac{1}{\langle v\sigma_{\chi\chi} \rangle}$$

$$\beta_\chi = \chi \text{ CM speed}$$

$$\sqrt{s} = \text{CM energy}$$

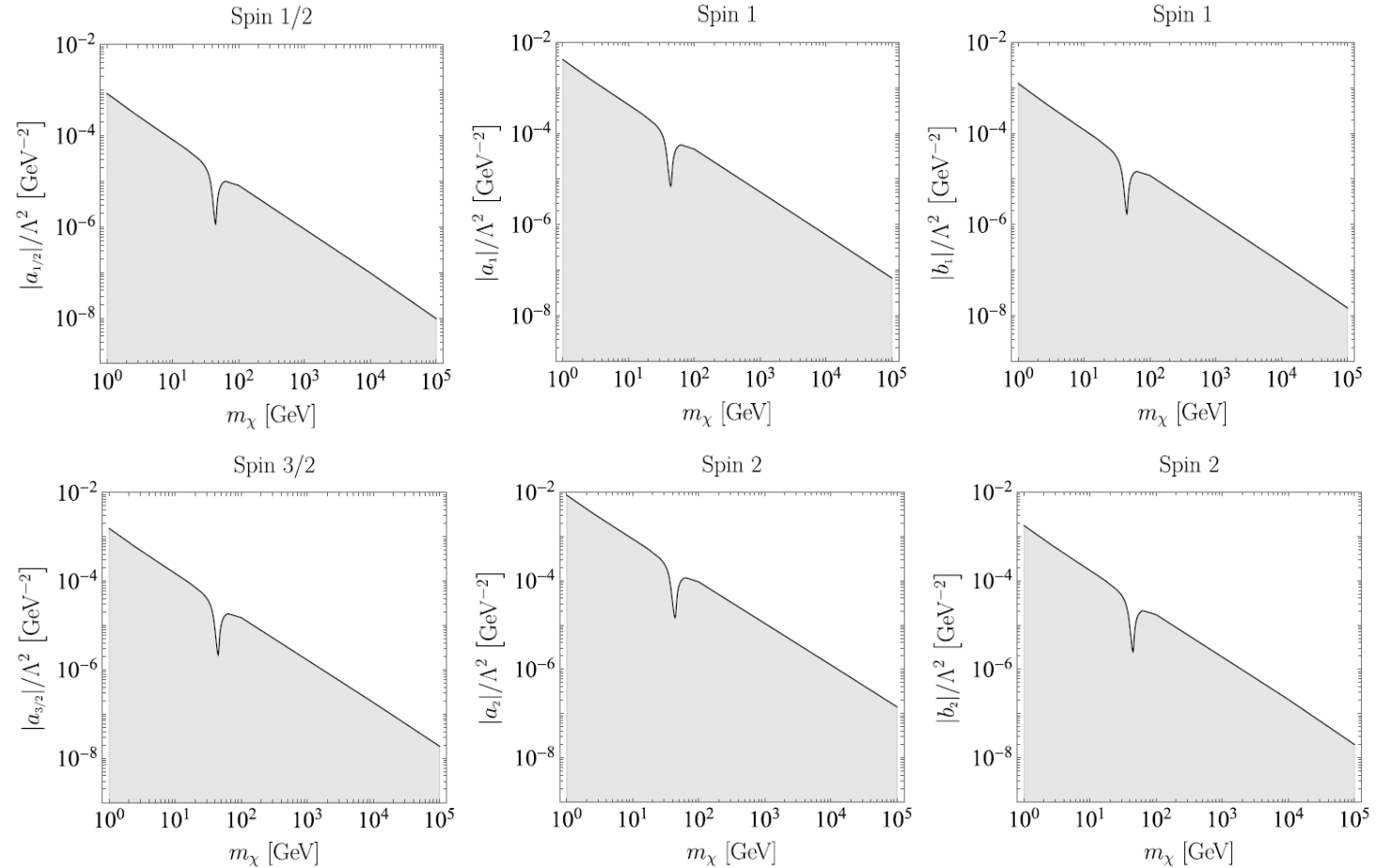
$$\sigma_{1/2}^{[\chi\chi \rightarrow \text{SMSM}]} = \frac{1}{4} \frac{|a_{1/2}|^2}{\Lambda^4} \beta_\chi \Sigma^{\text{SM}}$$

$$\sigma_1^{[\chi\chi \rightarrow \text{SMSM}]} = \frac{1}{9} \left[\frac{|a_1|^2 \beta_\chi^2 + |b_1|^2}{\Lambda^4} \right] \left(\frac{s}{4m_\chi^2} \right) \beta_\chi \Sigma^{\text{SM}}$$

$$\sigma_{3/2}^{[\chi\chi \rightarrow \text{SMSM}]} = \frac{5}{72} \frac{|a_{3/2}|^2}{\Lambda^4} \beta_\chi \Sigma^{\text{SM}}$$

$$\sigma_2^{[\chi\chi \rightarrow \text{SMSM}]} = \frac{1}{300} \left[\frac{7|a_2|^2 \beta_\chi^2 + 15|b_2|^2}{\Lambda^4} \right] \left(\frac{s}{4m_\chi^2} \right) \beta_\chi \Sigma^{\text{SM}}$$

small β_χ
Z-pole enhancement

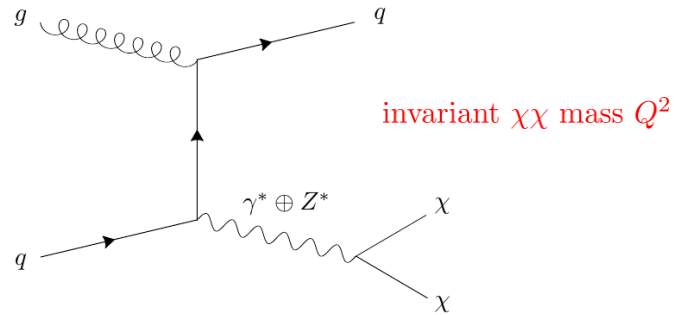


Smaller factors \Rightarrow smaller cross sections
 \Rightarrow Stronger relic-abundance constraints

(HL-)LHC Mono-jet Searches

[Aad et al. [ATLAS], PRD (2021)]

Dominant mono-jet processes

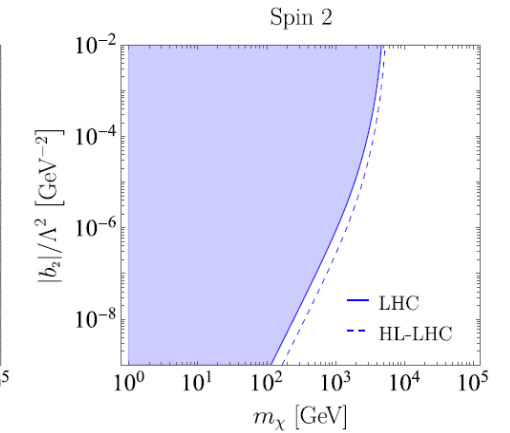
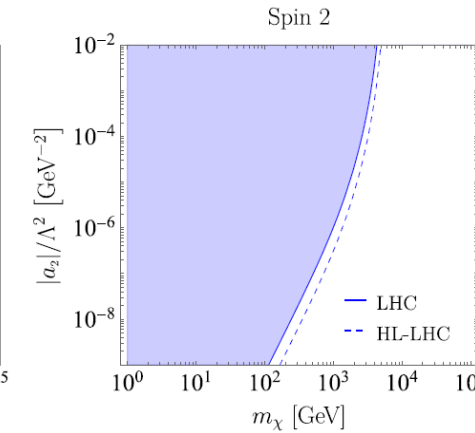
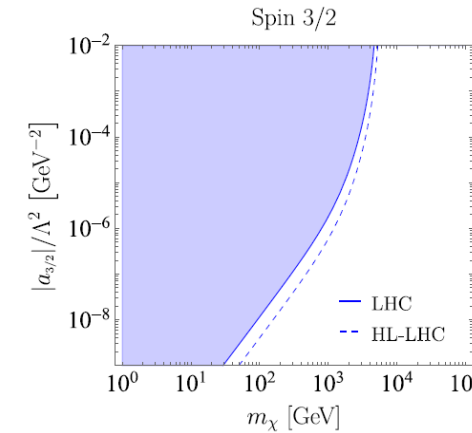
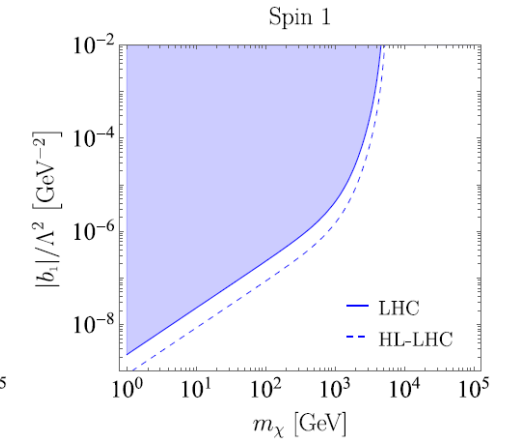
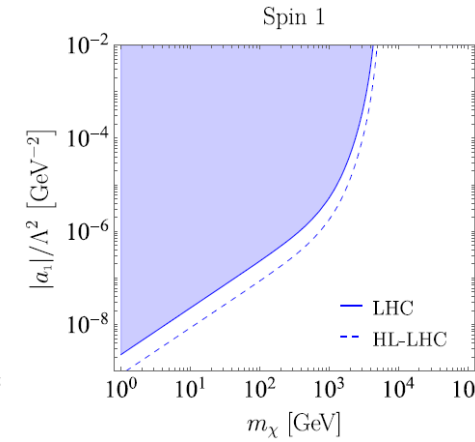
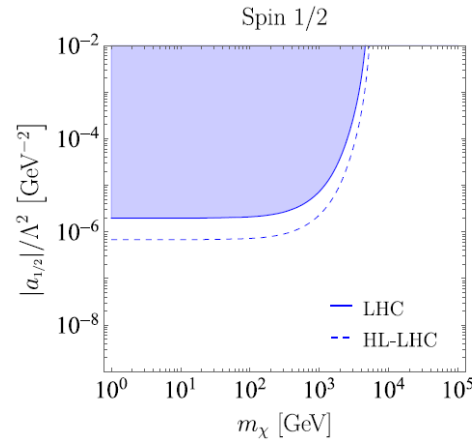


$$\sigma_{1/2}^{[gq \rightarrow q\chi\chi]} \propto \frac{|a_{1/2}|^2}{\Lambda^4}$$

$$\sigma_1^{[gq \rightarrow q\chi\chi]} \propto \left[\frac{|a_1|^2 \beta_\chi^2 + |b_1|^2}{\Lambda^4} \right] \left(\frac{Q^2}{4m_\chi^2} \right)$$

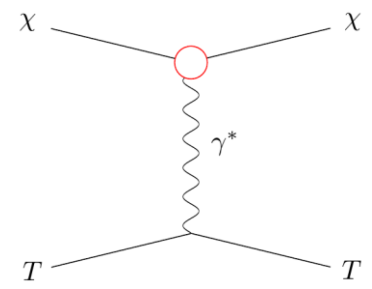
$$\sigma_{3/2}^{[gq \rightarrow q\chi\chi]} \propto \frac{16|a_{3/2}|^2}{9\Lambda^4} \left(\frac{Q^2}{4m_\chi^2} \right)^2$$

$$\sigma_2^{[gq \rightarrow q\chi\chi]} \propto \left[\frac{8|a_2|^2 \beta_\chi^2 + 7|b_2|^2}{6\Lambda^4} \right] \left(\frac{Q^2}{4m_\chi^2} \right)^3$$



More longitudinal (L) modes \Rightarrow Stronger (HL-)LHC constraints

NR scattering
(negligible Z-exchange)



DM Direct Detection XENONnT

[Hisano, Ibarra, Nagai, JCAP (2020)]

Target nucleus $T = \text{Xe}$

Recoil energy E_R
($E_R \ll m_\chi$)

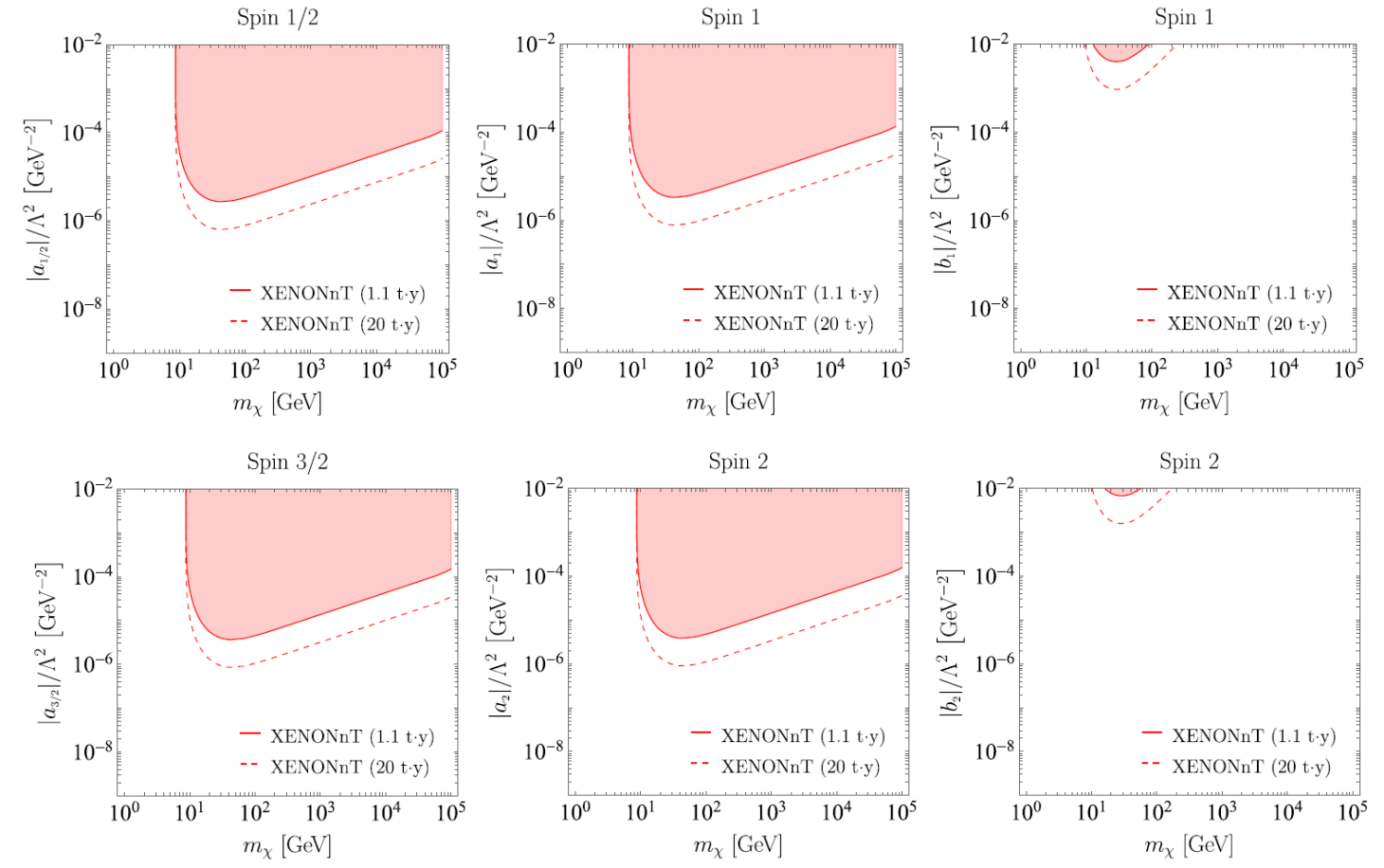
$3.3 \text{ keV} \leq E_R \leq 60.5 \text{ keV}$

$$\frac{d\sigma_{1/2}^{[\chi T \rightarrow \chi T]}}{dE_R} \propto \frac{1}{2} \frac{|a_{1/2}|^2}{\Lambda^4}$$

$$\frac{d\sigma_1^{[\chi T \rightarrow \chi T]}}{dE_R} \propto \frac{1}{3} \left[|a_1|^2 \left(1 + \frac{m_T E_R}{2m_\chi^2} \right) + |b_1|^2 \frac{m_T E_R}{2m_\chi^2} \right]$$

$$\frac{d\sigma_{3/2}^{[\chi T \rightarrow \chi T]}}{dE_R} \propto \frac{5}{18} \frac{|a_{3/2}|^2}{\Lambda^4}$$

$$\frac{d\sigma_2^{[\chi T \rightarrow \chi T]}}{dE_R} \propto \frac{1}{60} \left[15|a_2|^2 \left(1 + \frac{13m_T E_R}{10m_\chi^2} \right) + 7|b_2|^2 \frac{m_T E_R}{2m_\chi^2} \right]$$



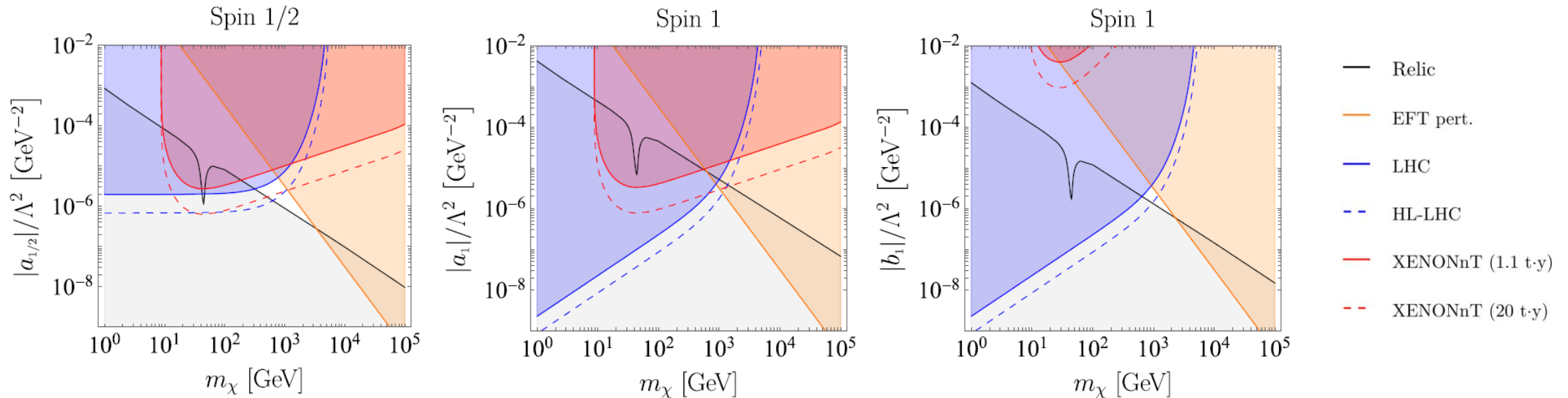
extremely small $m_T E_R / 2m_\chi^2 < 4 \times 10^{-3} \Rightarrow$ very weak constraints on $|b_{1,2}|$

Combined Constraints \oplus Naive Perturbativity Bound

$$\frac{C}{\Lambda^2} s \leq 4\pi \Rightarrow \frac{C}{\Lambda^2} m_\chi^2 \leq \pi \text{ with } C = |a_{1/2,3/2}| \text{ or } \sqrt{|a_{1,2}|^2 + |b_{1,2}|^2}$$

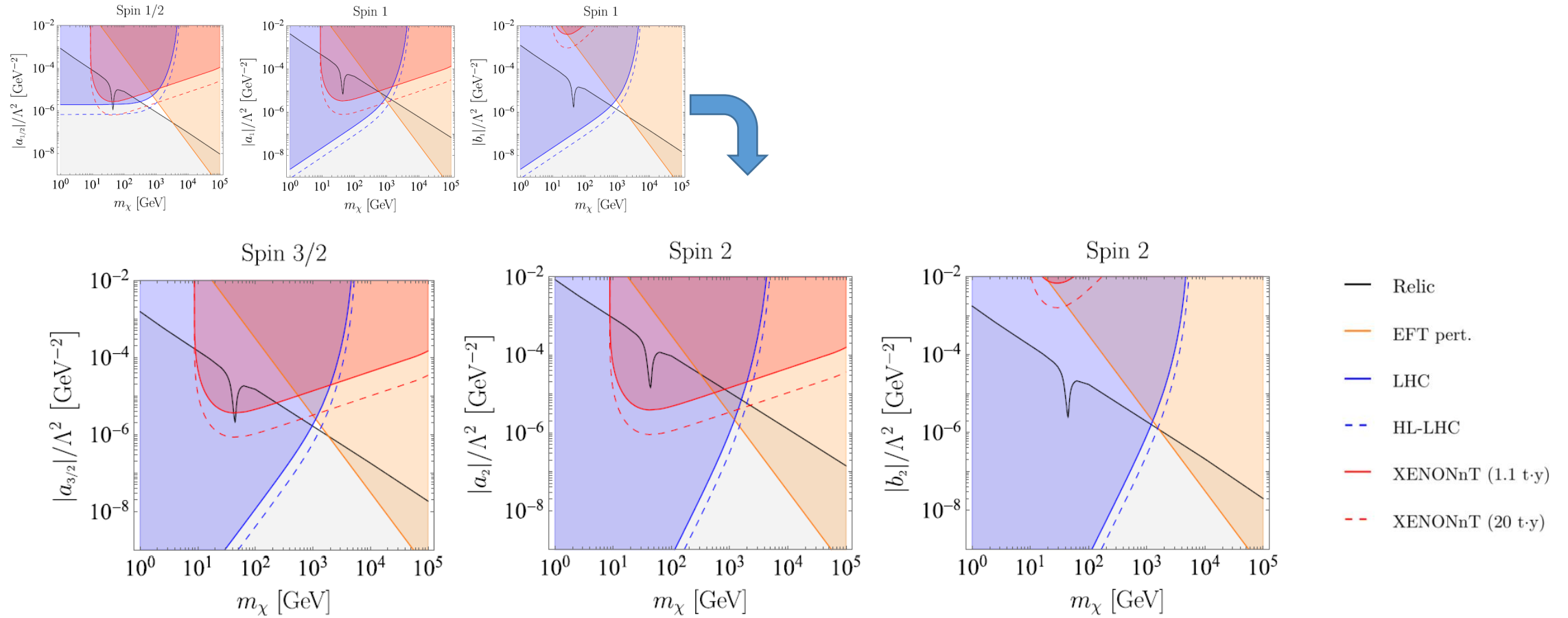
[Bruning, Zerlauth, JCoW (2023), TUYG1]
[Aalbersetal ea, J.Phys (2023)]

(yellow exclusion regions)



Stronger constraints for the spin-1 case than the spin-1/2 case
 The spin-1 case with $|a_1|$ (middle) is already completely excluded
 Promising XENONnt (20 t-y) and HL-LHC especially for the spin-1/2 case

Combined constraints



Stronger constraints for the higher-spin 3/2 and 2 cases
 Nearly full exclusion or discovery is expected in the near future!

Conclusions

General 3-point anapole vertices for any spin were constructed in a compact form for systematic analytic analyses and other projects

Detailed analytic and phenomenological analyses were performed for the spin-1/2, 1, 3/2 and 2 hypercharge anapole DM particles



Nearly half of the allowed region for the spin-1/2 case is excluded by the future XENONnT experiments in 5 years

Nearly half of the allowed region for the spin-1 case is excluded by the full running of the HL-LHC

Constraints are stronger from relic abundance and (HL-)LHC but weaker from XENONnT for the higher-spin cases, leading to complete exclusion or discovery of the anapole DM?!!



Finding UV scenarios of the hypercharge anapole DM

Back-up Slides

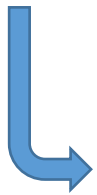
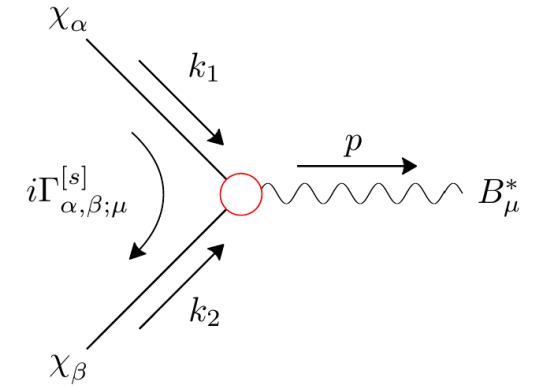
(Leading-order) Effective Lagrangian

$$\mathcal{L}_{1/2} = \frac{a_{1/2}}{2\Lambda^2} \bar{\chi}_{\frac{1}{2}} \gamma^\mu \gamma_5 \chi_{\frac{1}{2}} \partial_\nu B^{\mu\nu}$$

$$\mathcal{L}_1 = \left[\frac{a_1}{2\Lambda^2} \epsilon_{\alpha\beta\mu\rho} [\chi_1^\alpha (\partial^\rho \chi_1^\beta) - (\partial^\rho \chi_1^\alpha) \chi_1^\beta] + \frac{b_1}{2\Lambda^2} \partial^\rho (\chi_{1\rho} \chi_{1\mu} + \chi_{1\mu} \chi_{1\rho}) \right] \partial_\nu B^{\mu\nu}$$

$$\mathcal{L}_{3/2} = \frac{a_{3/2}}{2\Lambda^2} \bar{\chi}_{\frac{3}{2}\rho} \gamma^\mu \gamma_5 \chi_{\frac{3}{2}}^\rho \partial_\nu B^{\mu\nu},$$

$$\mathcal{L}_2 = \left[\frac{a_2}{2\Lambda^2} \epsilon_{\alpha\beta\mu\rho} [\chi_2^{\alpha\sigma} (\partial^\rho \chi_{2\sigma}^\beta) - (\partial^\rho \chi_2^{\alpha\sigma}) \chi_{2\sigma}^\beta] + \frac{b_2}{2\Lambda^2} \partial^\rho (\chi_{2\rho}^\sigma \chi_{2\mu\sigma} + \chi_{2\mu}^\sigma \chi_{2\rho\sigma}) \right] \partial_\nu B^{\mu\nu}$$



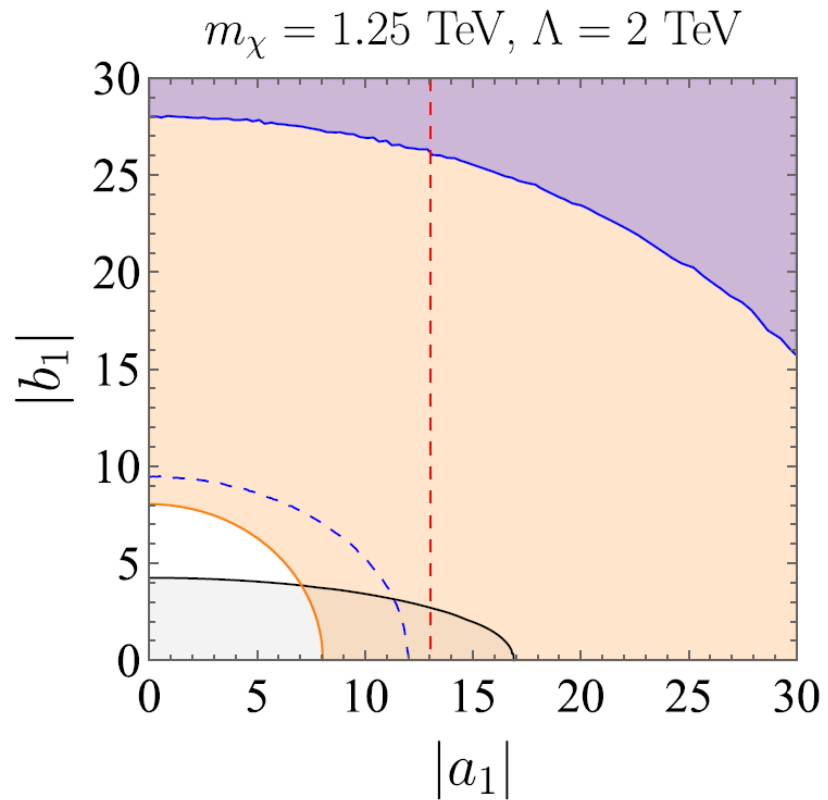
$$a_i \rightarrow H \propto -\frac{\vec{\mathbf{S}}}{S} \cdot \vec{j}_{\text{ext}} \quad (\text{odd-parity dipole})$$

$$b_i \rightarrow H \propto \frac{3}{2S(2S-1)} \left[\mathbf{S}^l \mathbf{S}^m + \mathbf{S}^l \mathbf{S}^m - \frac{2}{3} \delta^{ij} S(S+1) \right] \nabla^l j_{\text{ext}}^m \quad (\text{even-parity quadrupole})$$

Non-relativistic limit

Elliptically-correlated $a_{1,2}$ & $b_{1,2}$ Constraints

Spin 1



Spin 2

