

High-precision QCD physics at FCC-ee

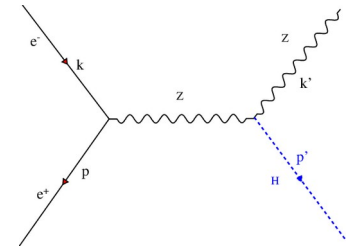
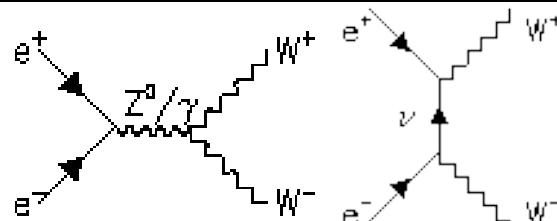
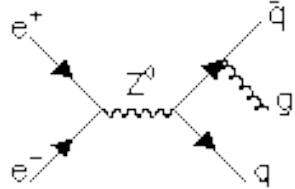
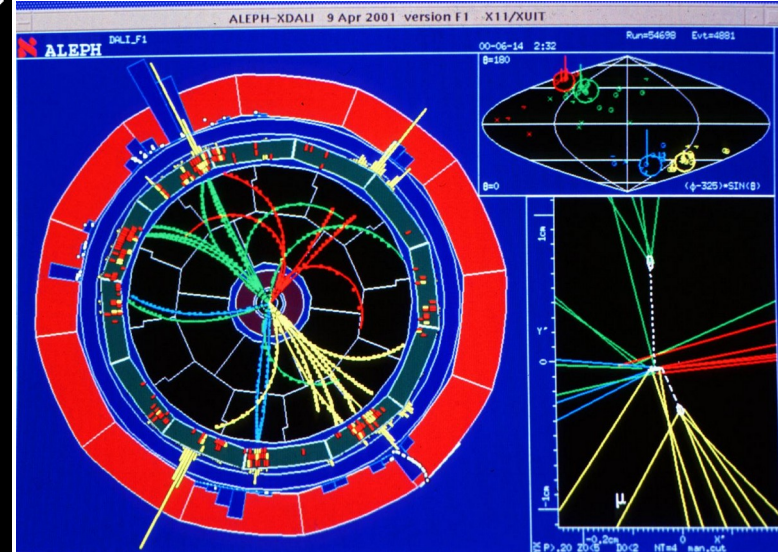
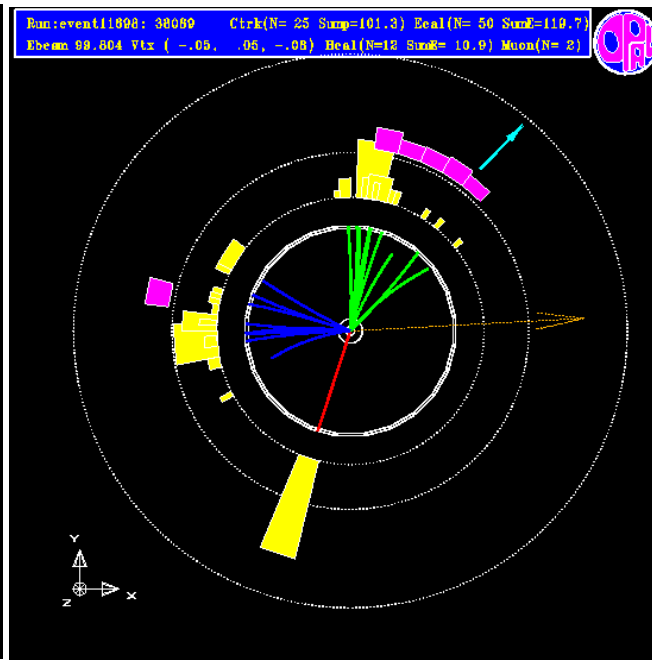
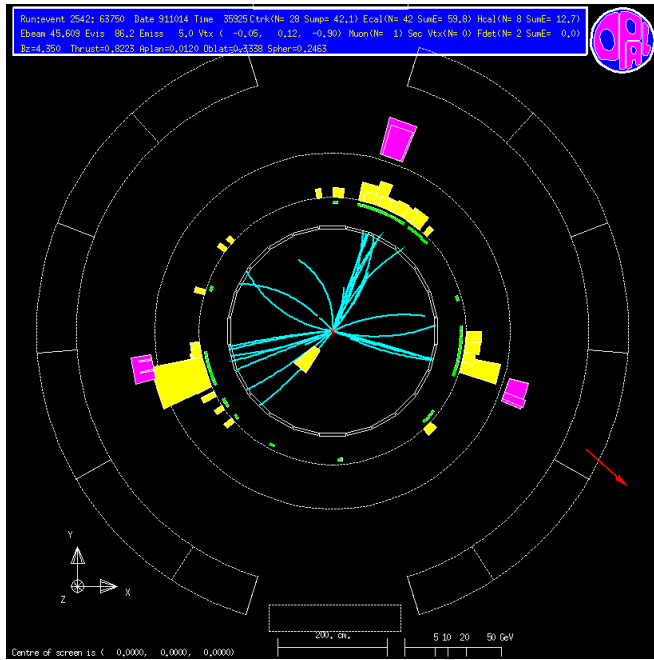
Stefan Kluth
MPI für Physik, Munich
ICHEP 2024 Prague
18.07.2024 16:45, North Hall

High precision QCD in e^+e^-

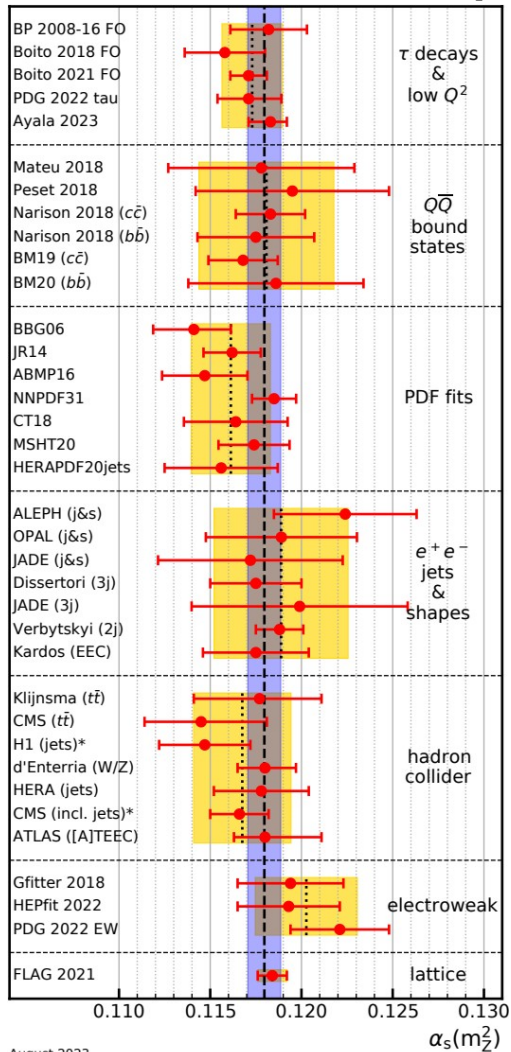
$$e^+e^- \rightarrow q\bar{q}g$$

$$e^+e^- \rightarrow W^+W^- \rightarrow q\bar{q}e\nu_e$$

$$e^+e^- \rightarrow b\bar{b} \text{ (115 GeV) } q\bar{q} \text{ } (\sim m_Z)$$



[Huston, Rabbertz, Zanderighi,
in PDG coll., arXiv: 2312.14015]



Overview

FCC-ee

PDG QCD update 2023, based on

FCC-ee

“ α_s (2022) – Precision measurements of the QCD coupling” at ECT* (Trento)

LHeC

31.01.-04.02.2022

FCC-eh

FCC-ee

FCC-ee impact on most categories

LHeC

Expect $3 \cdot 10^{12}$ hadronic Z decays \Rightarrow

FCC-hh

$6 \cdot 10^{11}$ $Z \rightarrow b\bar{b}$, 10^{11} lepton pairs (e, μ , τ),

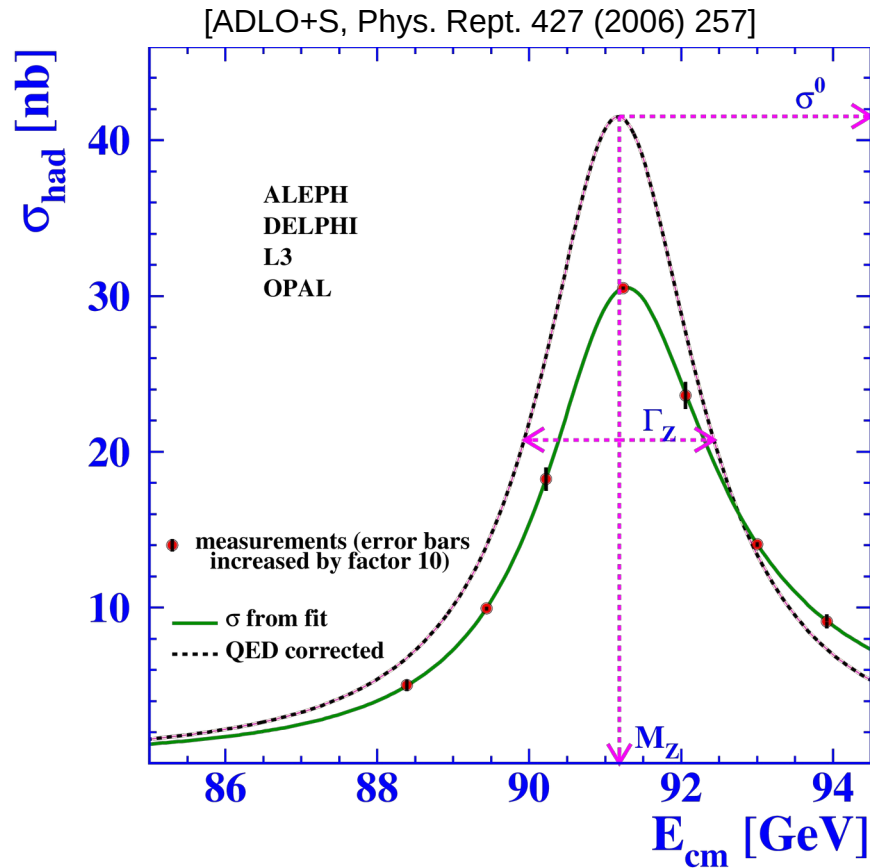
FCC-eh

$5 \cdot 10^8$ W decays, 10^6 $t\bar{t}$ on threshold,

FCC-ee

$O(10^5)$ $H \rightarrow gg$, ...

Z and W decays in e^+e^-



SM prediction: $R_I^{Z,W} = \Gamma_{\text{had}}^{Z,W} / \Gamma_{\text{lep}}^{Z,W} = R_{EW} (1 + \sum a_i (\alpha_s(Q)/\pi)^i + \delta_{EW} + \delta_{\text{mix}} + \delta_{\text{np}})$

N3LO QCD, 2-loop EW corrections

$\Gamma_{\text{had}}, \Gamma_{\text{lep}}, \dots$ (EWPO) mod.ind. fits

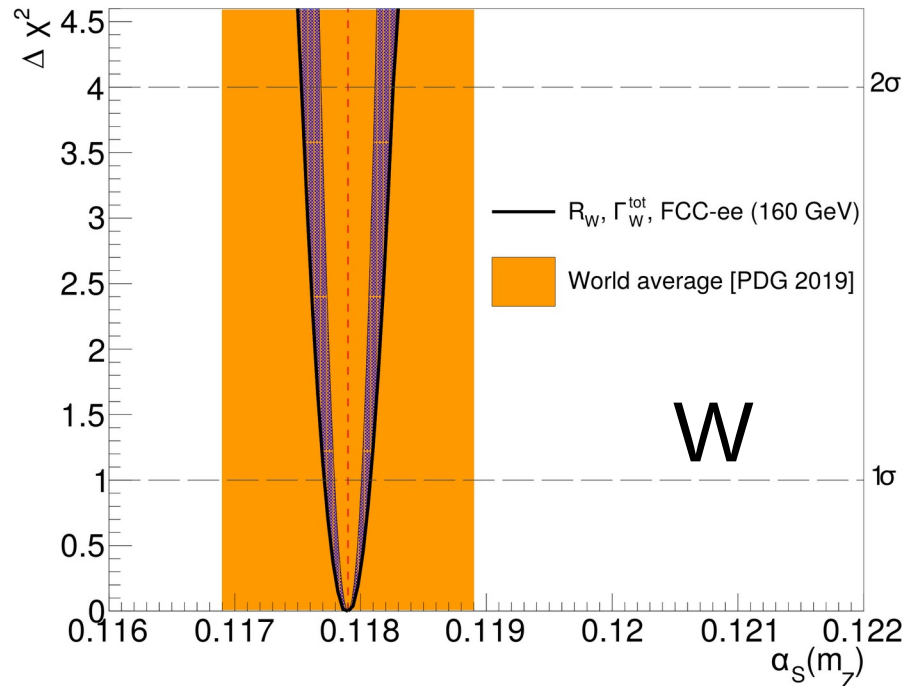
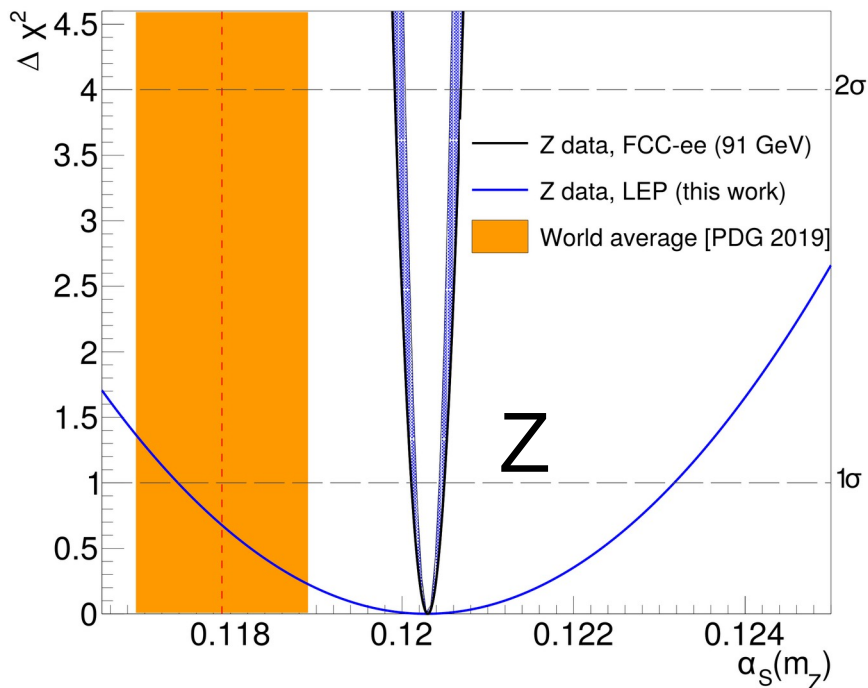
LEP:

Z: $\alpha_s(m_Z) = 0.120 \pm 0.003_{\text{exp}} \pm 0.001_{\text{theo}}$

W: $\alpha_s(m_Z) = 0.107 \pm 0.035_{\text{exp}} \pm 0.002_{\text{theo}}$

[D. d'Enterria, in arxiv: 2203.08271]

Z and W decays in e^+e^-



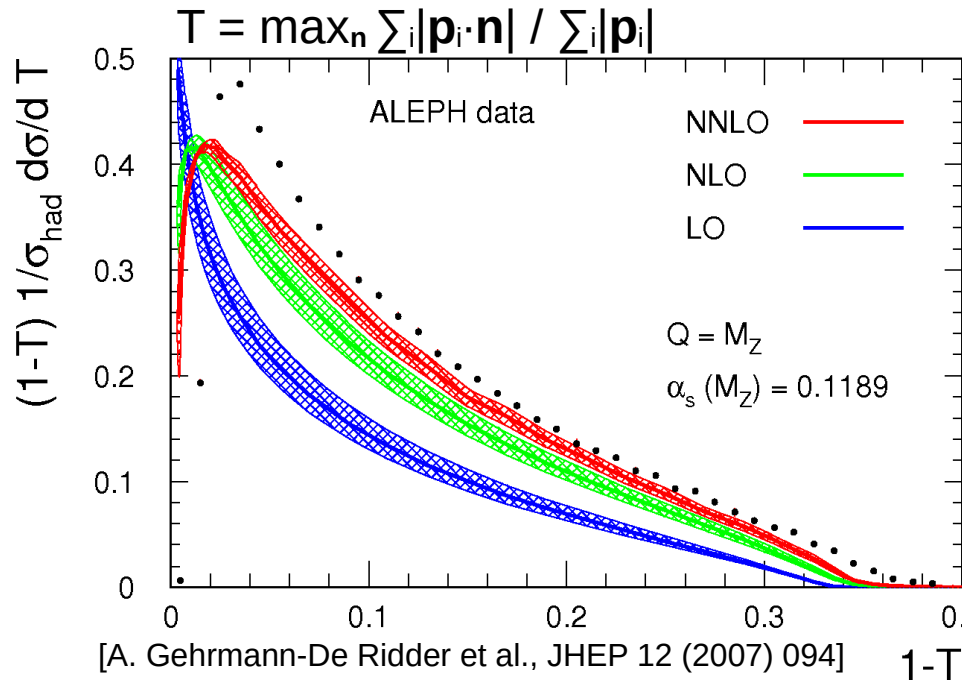
FCC-ee: improved α_{QED} , $|V_{cs}|$, $|V_{cd}|$, m_W ; assume N4LO QCD

Z: $\alpha_s(m_Z) = 0.12020 \pm 0.00013_{\text{exp}} \pm 0.00005_{\text{par}} \pm 0.00022_{\text{theo}}$

W: $\alpha_s(m_Z) = 0.11790 \pm 0.00012_{\text{exp}} \pm 0.00004_{\text{par}} \pm 0.00019_{\text{theo}}$

[D. d'Enterria, in arxiv: 2203.08271]

Jets and event shapes in e^+e^-



$$\begin{aligned}
 1/\sigma d\sigma/dy &= dA/dy \alpha_s(Q) + \\
 & dC/dy \alpha_s(Q)^2 + dC/dy \alpha_s(Q)^3 + \text{h.o.} \\
 & + \text{scale} + \text{“}\sigma_{0 \rightarrow \text{tot}}\text{”}
 \end{aligned}$$

NNLO QCD (+resum.) needs
 np (hadronisation) corr. $\sim 1/Q$

MC-based vs analytic models

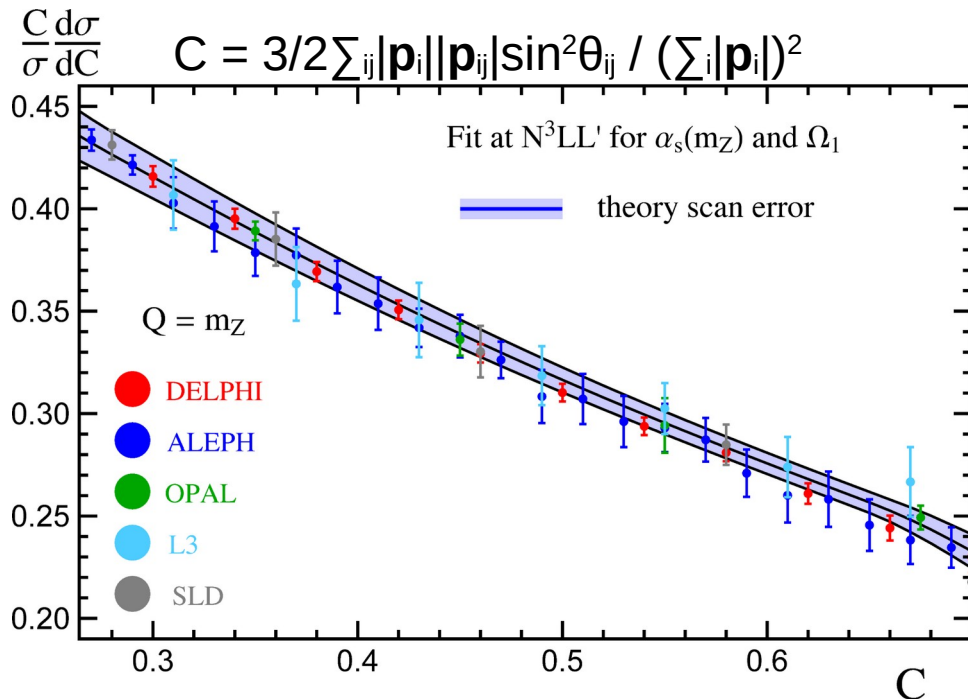
Same structure for other event
 shapes and for jet production
 rates

Typical differences MC vs analytic

$$\Delta \alpha_s(m_Z)_{\text{np-model}} = O(1\%)$$

[e.g. A. Hoang et al., Phys. Rev. D91 (2015) 094018]

Jets and event shapes



Hadronisation unc. within
Fitted SCET based model

Significant deviations from
world average

$$\alpha_s(m_Z) = 0.1179 \pm 0.0009$$

[A. Hoang et al., Phys. Rev. D91 (2015) 094018]

NNLO + N3LL' (SCET), LEP/SLD/PETRA/TRISTAN data:

$$T: \alpha_s(m_Z) = 0.1134 \pm 0.0002_{\text{exp}} \pm 0.0005_{\text{had}} \pm 0.0011_{\text{theo}}$$

$$C: \alpha_s(m_Z) = 0.1123 \pm 0.0002_{\text{exp}} \pm 0.0007_{\text{had}} \pm 0.0014_{\text{theo}}$$

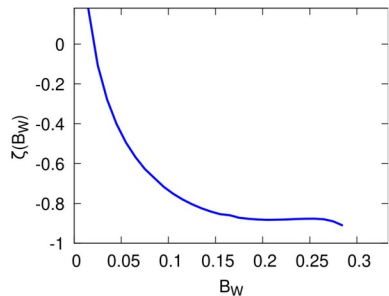
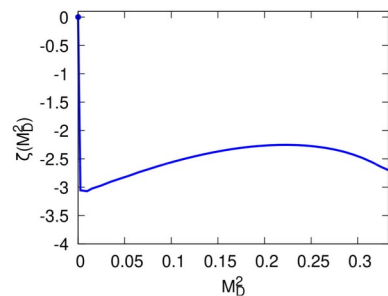
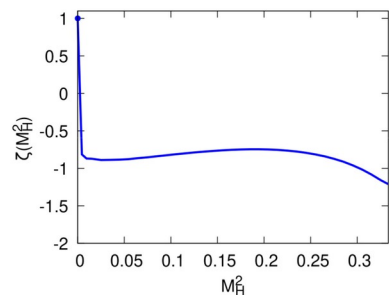
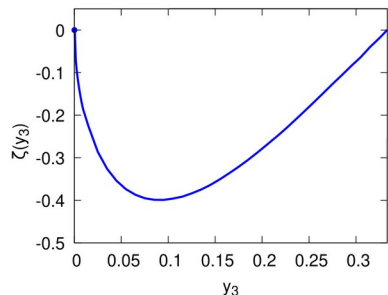
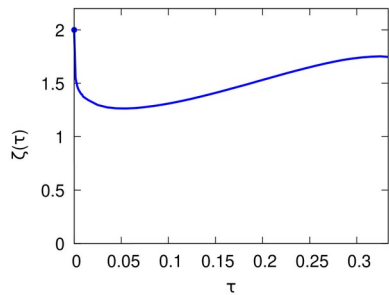
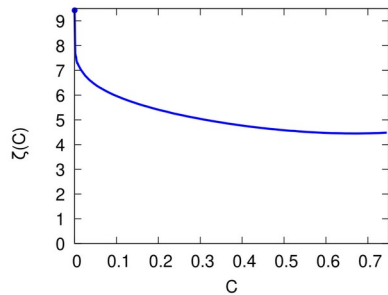
Jets and event shapes

Linear power corrections in large n_f limit
in 3-jet region \Rightarrow constant shift of pert.
prediction replaced by observable
dependent shift $\zeta(\cdot)$

significant $\Delta\alpha_s(m_Z)$ w.r.t. const. shift

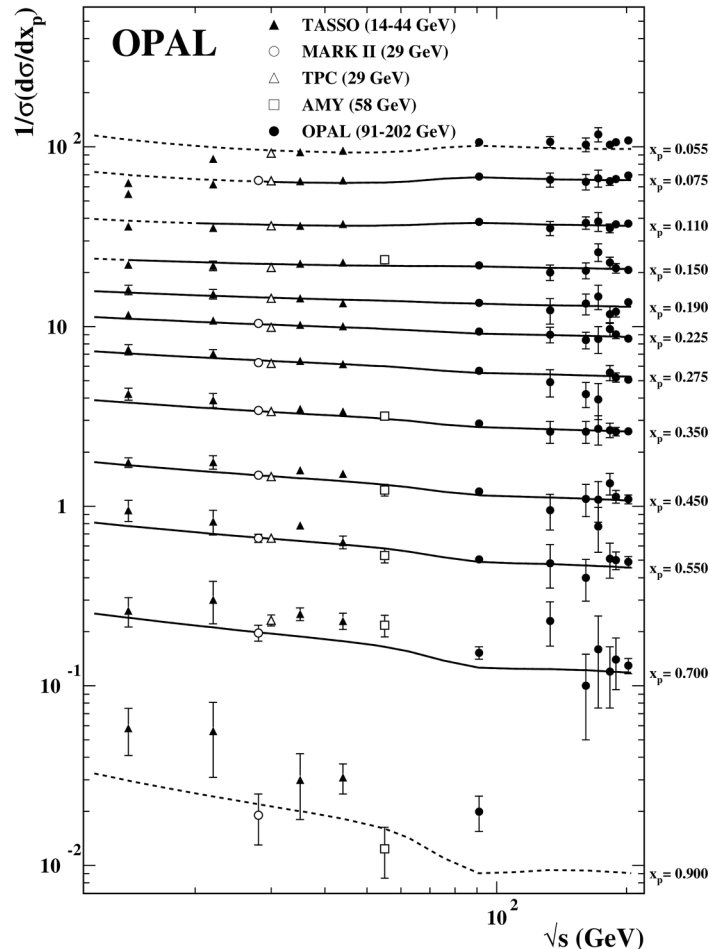
See also: new (groomed) observables,
NLO+NLL-PS MCs [S. Marzani, D. Reichelt, S. Schumann,
G. Soyez, arxiv: 2203.08271]

FCC-ee: $\Delta\alpha_{S,\text{exp}} < 0.1\%$, $\Delta\alpha_{S,\text{had}} < 1\%$?
 $\Delta\alpha_{S,\text{theo}} < 1\%$?, $\Delta\alpha_{S,\text{hadron masses}} \approx 1\%$?



[P. Nason, G. Zanderighi, JHEP 06 (2023) 058]

Scaling violation in hard FFs



Charged hadrons h with scaled momentum $x = 2E_h/\sqrt{s}$ at various $\sqrt{s} = Q$

$$1/\sigma d\sigma/dx = \int_0^1 \sum_f C_f(z, \alpha_s(Q)) D_f(x/z) dz/z$$

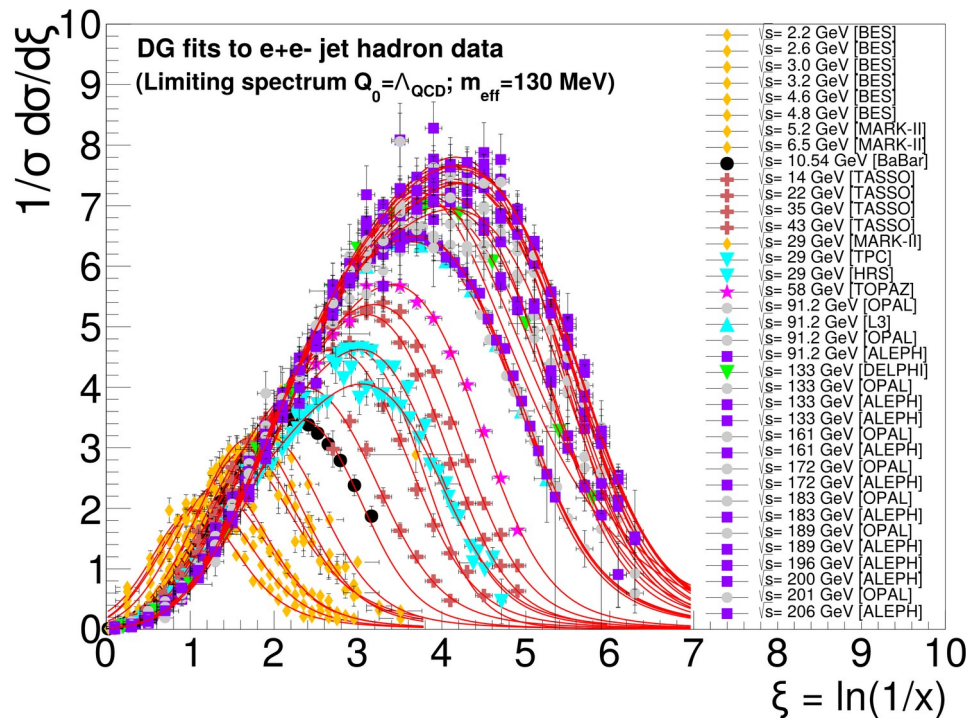
LEP (ADO) NLO DGLAP analyses:

$$\alpha_s(m_Z) = 0.1192 \pm 0.0056_{\text{exp}} \pm 0.0070_{\text{theo}}$$

FCC-ee statistics and systematics \Rightarrow exp. unc. $\Delta\alpha_{S,\text{exp}} < 1\%$ (or better? $\sqrt{s} < m_Z$?)

Today NNLO DGLAP for proton pdfs \Rightarrow theo. unc. $\Delta\alpha_{S,\text{theo}} \approx 0.001?$ (N3LO DGLAP?)

Soft FFs in e^+e^-



Charged hadrons momentum spectra $x = 2E_h/\sqrt{s}$

FF: $D_{a,h}(z, Q)$, $z = p_h/p_a$, $Q = \sqrt{s}$

Distorted Gaussian model:

$D \approx C(\alpha_s(t)) \exp(\int^t \gamma(\alpha_s(t')) dt')$

$t = \ln(Q)$, NNLO*+NNLL evolution of $\gamma(\alpha_s(t'))$

$\alpha_s(m_Z) = 0.121 \pm 0.001_{\text{exp}} \pm 0.002_{\text{theo}}$

FCC-ee: $\Delta\alpha_{S,\text{exp}} < 0.1\%$, full NNLO+NNLL $\Rightarrow \Delta\alpha_{S,\text{theo}} \leq 0.001?$

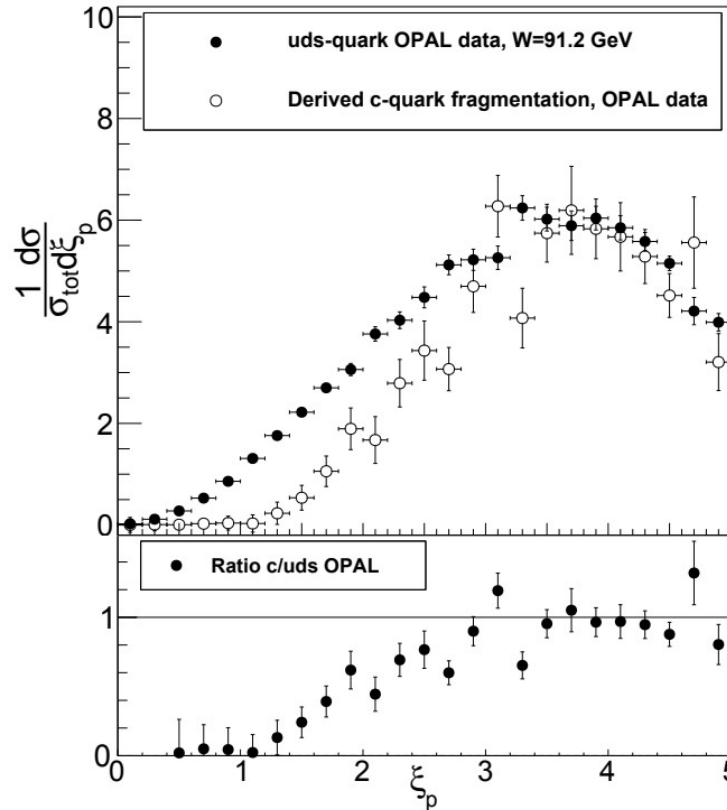
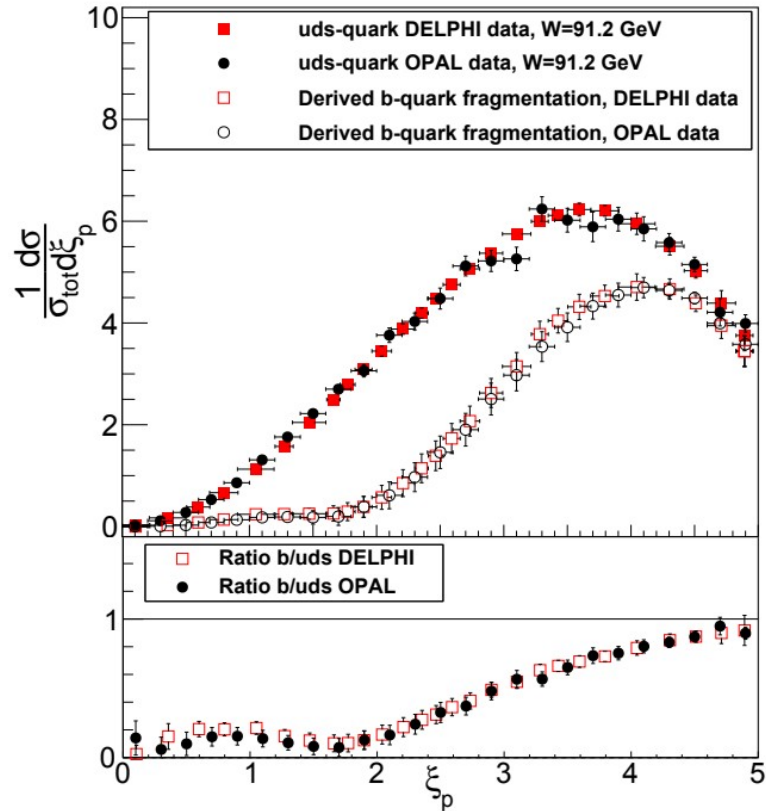
With c, b, (t) tags: study heavy quark fragmentation

[R. Perez-Ramos, D. d'Enterria, arxiv: 2203.08271]

Soft FFs in e^+e^- : dead cone effect

Study heavy quark Q scaled momentum dist'n

[SK, Ochs, Perez Ramos, Phys. Rev. D107 (2023) 094039]



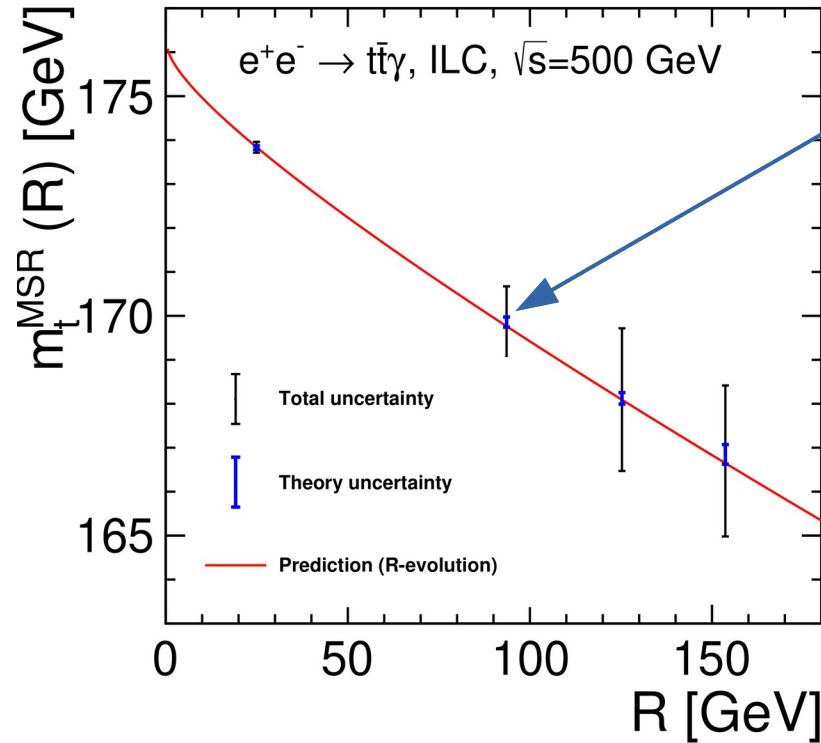
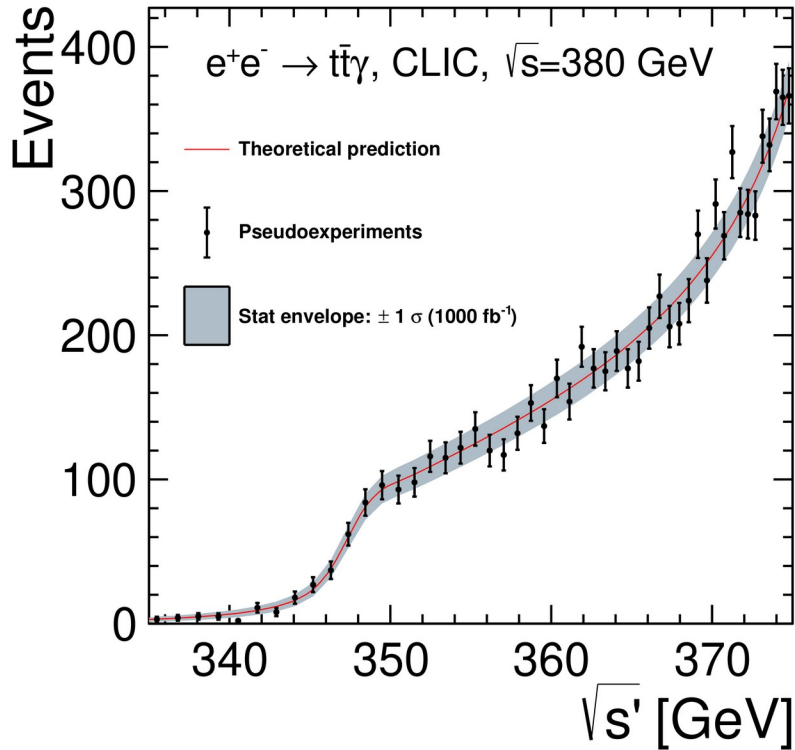
Frag'n of Q with $v_Q/c < 1$ different from light q

Q jet modelling
 Q tagging
 m_Q ?

Future e^+e^- :
 Reduced stat.
 and exp. errors
 \sqrt{s} dependence

Quark mass running: top

$e^+e^- \rightarrow t\bar{t}\gamma$ to access $m_t(s')$ at production: $s' = s(1-2E_\gamma/\sqrt{s})$

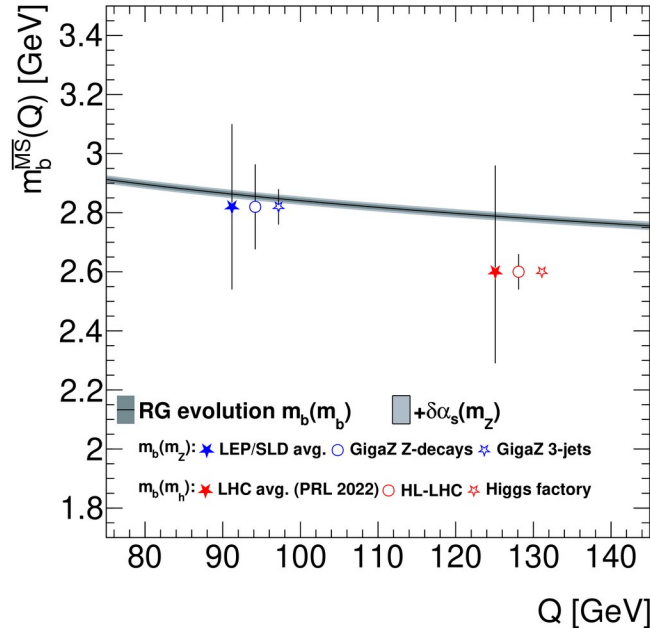
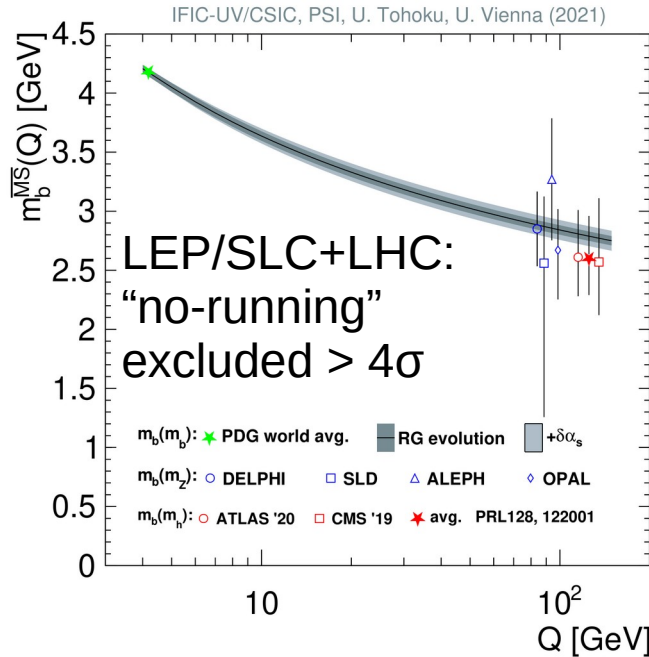


[M. Boronat et al, Phys. Lett. B804 (2020) 135353]

Quark mass running: b

$$e^+e^- \rightarrow Z \rightarrow b\bar{b}(+\text{jet}): R_{0,b} = \Gamma_{Z \rightarrow b\bar{b}}/\Gamma_{Z \rightarrow \text{had}} \sim (m_b/m_Z)^2,$$

$$R_3^{(b)}/R_3^{(\text{light})} \sim (m_b/m_Z)^2/y_{\text{cut}}; pp \rightarrow H(H \rightarrow b\bar{b}, ZZ) + X, \Gamma_{H \rightarrow b\bar{b}}/\Gamma_{H \rightarrow ZZ} \sim m_b^2$$



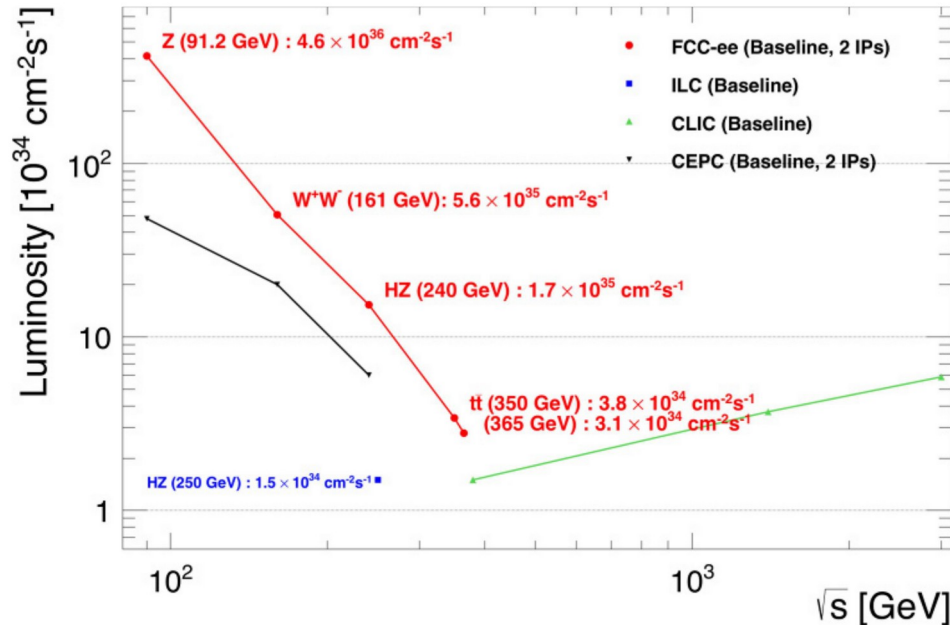
[J. Aparisi et al, arxiv: 2203.16994 and refs]

SM Yukawa $y_b = m_b/(\sqrt{2}v_{\text{ev}_H}) \Rightarrow y_b$ or m_b from $H \rightarrow b\bar{b}$

Extrapolation of “GigaZ 3-jets” needs NNLO for $e^+e^- \rightarrow b\bar{b}+\text{jet}$

FCC-ee with $\sqrt{s} < m_Z$

Collect 10^9 events with FCC-ee
at $\sqrt{s} = 20, 30, 40, \dots$ GeV



Or consider ISR events on Z peak

Benefactors:

MC tuning and soft QCD

FFs: scaling violation, long., transv.,
asym., soft FFs $\xi = \ln(1/x)$, ...

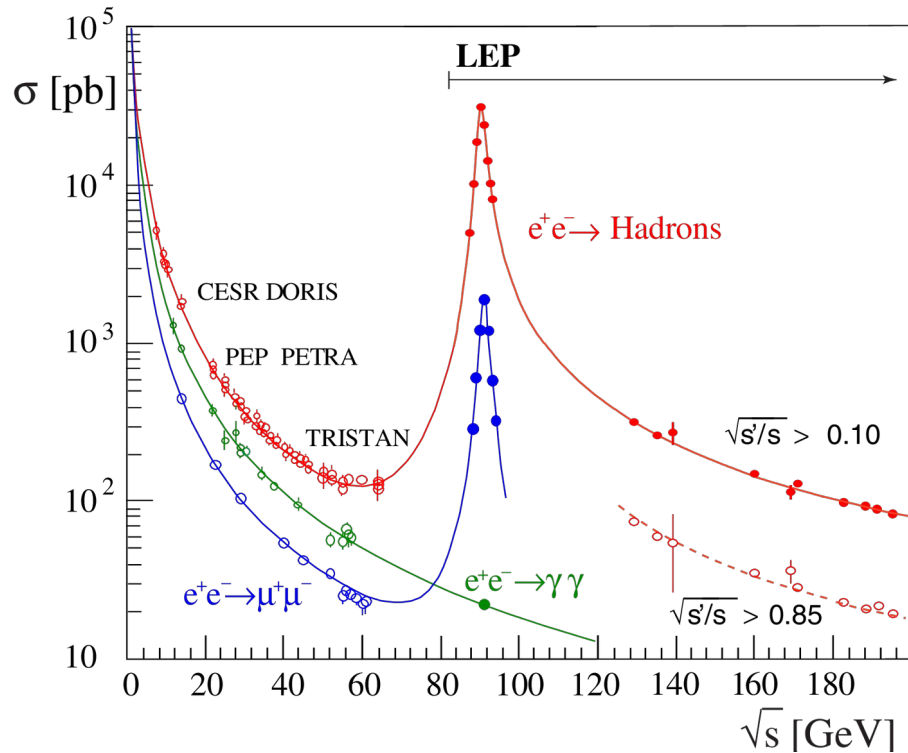
R_1^y and $\alpha_s(m_Z)$ at high precision?

$\sin^2\theta_W(\sqrt{s})$ from $A_{FB}^{(l,q)}(\sqrt{s})$?

$m_{b(c)}(\sqrt{s})$?

In-situ calibrations?, EW, etc pp

R_1^γ at $\sqrt{s} < m_Z$ with FCC-ee



$$R_{1\text{ exp}}^\gamma = \sigma(e^+e^- \rightarrow \text{hadrons}) / \sigma(e^+e^- \rightarrow \mu^+\mu^-)$$

$$R_{1\text{ theo}}^\gamma = 3 \sum_i q_i^2 (1 + \alpha_s/\pi + 1.441(\alpha_s/\pi)^2 + \dots)$$

[A.V. Nesterenko, in arxiv: 2203.08271]

$$\Delta R_1^\gamma / R_1^\gamma \approx \Delta \alpha_s \Rightarrow \Delta \alpha_{s,\text{stat}} \approx 0.0001 \text{ with}$$

$$\Delta R_1^\gamma / R_1^\gamma \approx 10^{-4} \Rightarrow O(10^8) \text{ events}$$

[FCC coll., Eur. Phys. J. C79 (2019) 474]

$$\Delta R_1^Z / R_1^Z \approx 5 \cdot 10^{-5} \text{ FCC-ee, dominated}$$

by lepton acceptance \Rightarrow similar for R_1^γ

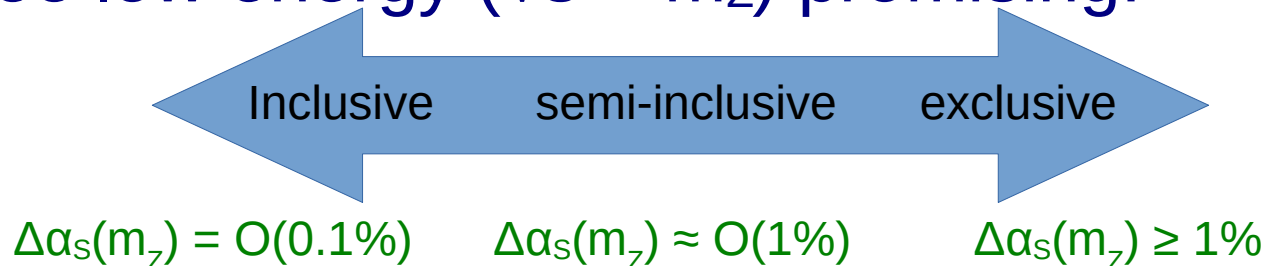
$$\Rightarrow \Delta \alpha_{s,\text{exp}} \approx 0.0001$$

$$\Delta \alpha_{s,\text{theo}} \approx 0.0002 \text{ as for } R_1^{Z,W} \text{ (pg3)}$$

Pure γ couplings, low scale
 \Rightarrow less BSM “pollution”

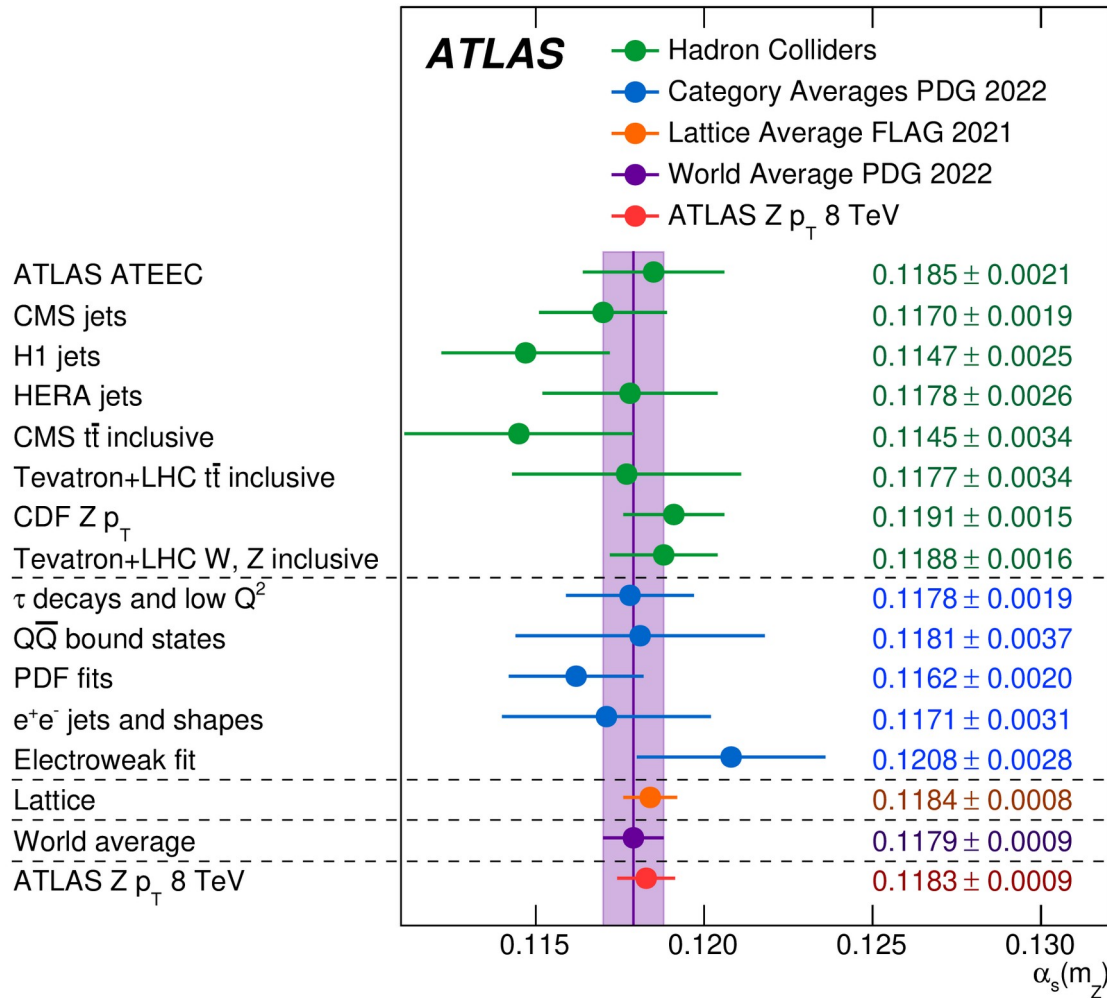
Summary / Outlook

- FCC-ee et al great potential for QCD
 - Running strong coupling and quark masses
 - q and g properties (FFs, subjects, ML training)
 - Non-pert. QCD: power corr., colour recon., MC models, ...
- FCC-ee, ep colliders (FCC-eh, LHeC) and Lattice QCD for $\Delta\alpha_s(m_Z) \approx 0.1\%$
- FCC-ee low energy ($\sqrt{s} < m_Z$) promising!



Summary

Future $\Delta\alpha_s(m_Z)$ estimates



[ATLAS-STDM-2023-01, arXiv: 2309.1298]

- 1.5% (theory,pdfs)
- <1% (theory, spectral functions)
- 1.5% (theory)
- 0.2% (future ep pdfs)
- 1% (theory)
- 0.1% (future ee)
- 0.1% (theory)
- <1% (theory,pdfs)

[D. d'Enterria, S. Kluth, G. Zanderighi (eds.), arxiv: 2203.08271]