



# Transverse spin-dependent asymmetries at COMPASS experiment

International Conference on High Energy Physics

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on behalf of COMPASS Collaboration

University of Warsaw, Poland

20 VII 2024, Prague

# Transverse Momentum Dependent Parton Distribution Functions

*"Well begun is half done."*

*Old Proverb*

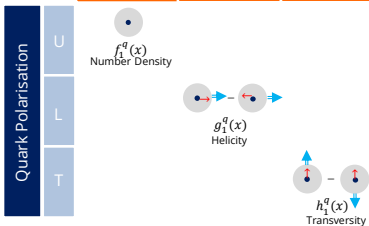


# Nucleon spin structure

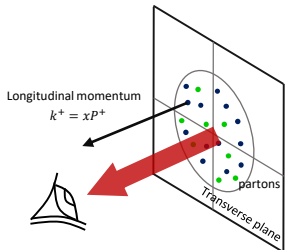
Twist-2 collinear PDFs

Nucleon polarisation

U L T



● Nucleon    ↑ Nucleon spin    ● Quark    ↑ Quark spin    ↗  $k_T$



TMD PDFs accessed through target spin dependent azimuthal asymmetries both in SIDIS and Drell-Yan processes.

$$h_1^{q\perp}(\text{SIDIS}) = -h_1^{q\perp}(\text{DY})$$

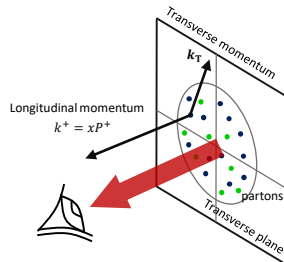
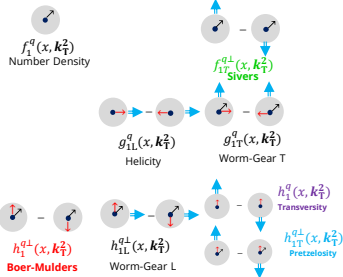
$$f_{1T}^{q\perp}(\text{SIDIS}) = -f_{1T}^{q\perp}(\text{DY})$$

Twist-2 TMDs



Nucleon polarisation

U L T



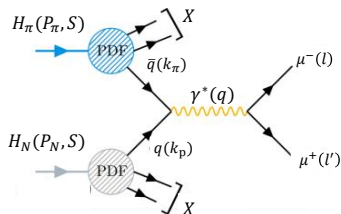


## Single polarised Drell-Yan process

*“Polarisation data has often been the graveyard of fashionable theories. If theorists had their way, they might well ban such measurements altogether out of self-protection.”*

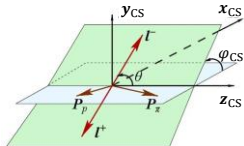
*James Bjorken*

# Single polarised Drell-Yan process

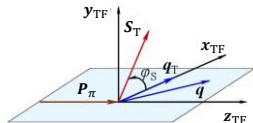


Cross-section, LO TMD approach for transversely polarised target:

$$\frac{d\sigma^{LO}}{dx_p dx_\pi d^2q_T d\varphi_{CS} d(\cos\theta) d\varphi_S} \propto \left\{ \begin{array}{l} 1 + D_{\sin^2\theta} \cos(2\varphi_{CS}) A_U^{\cos(2\varphi_{CS})} \\ + |S_T| \left[ D_{\sin^2\theta} \left( \begin{array}{l} \sin(\varphi_S) A_T^{\sin(\varphi_S)} + \\ \sin(2\varphi_{CS} + \varphi_S) A_T^{\sin(2\varphi_{CS} + \varphi_S)} + \\ \sin(2\varphi_{CS} - \varphi_S) A_T^{\sin(2\varphi_{CS} - \varphi_S)} \end{array} \right) \right] \end{array} \right\}$$



Collin-Soper frame



Target frame

## Boer-Mulders

$$A_U^{\cos(2\varphi_{CS})} \propto h_{1,\pi}^{q\perp} \otimes h_{1,\pi}^{q\perp}$$

## Sivers

$$A_T^{\sin(\varphi_S)} \propto f_{1,\pi}^q \otimes f_{1T,N}^{q\perp}$$

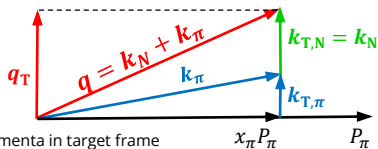
## Pretzelosity

$$A_T^{\sin(2\varphi_{CS} + \varphi_S)} \propto h_{1,\pi}^{q\perp} \otimes h_{1T,N}^{q\perp}$$

## Transversity

$$A_T^{\sin(2\varphi_{CS} - \varphi_S)} \propto h_{1,\pi}^{q\perp} \otimes h_{1,N}^q$$

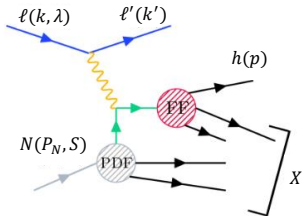
The convolution of TMD PDFs runs over the intrinsic transverse momenta  $k_T$ .



Momenta in target frame

# Semi Inclusive Deep Inelastic Scattering

$$A_{SIDIS} \propto PDF_N \otimes FF$$

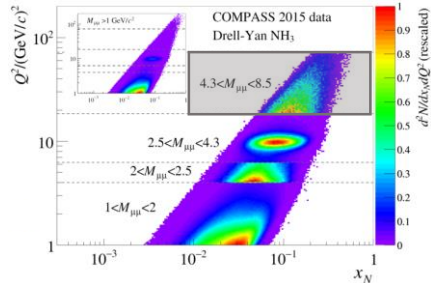
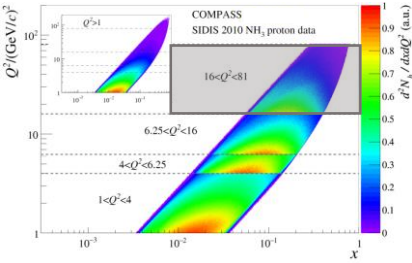
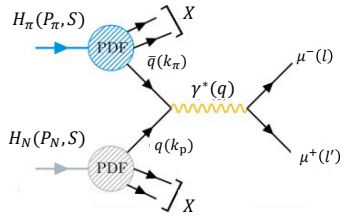


# SIDIS vs. DY

COMPASS achieves comparable  $Q^2 - x$  kinematic coverage  
Minimizing possible  $Q^2$  evolution effects

# Drell-Yan process

$$A_{DY} \propto PDF_N \otimes PDF_{\pi^-}$$



## COMPASS Experiment

*"Knowledge is of no value unless you  
put it into practice."*

*Anton Chekhov*





# COMPASS Collaboration



Common Muon and Proton Apparatus for Structure and Spectroscopy



- 24 institutions from 14 countries (approximately 220 physicists)
- CERN SPS North Area
- Fixed target experiment

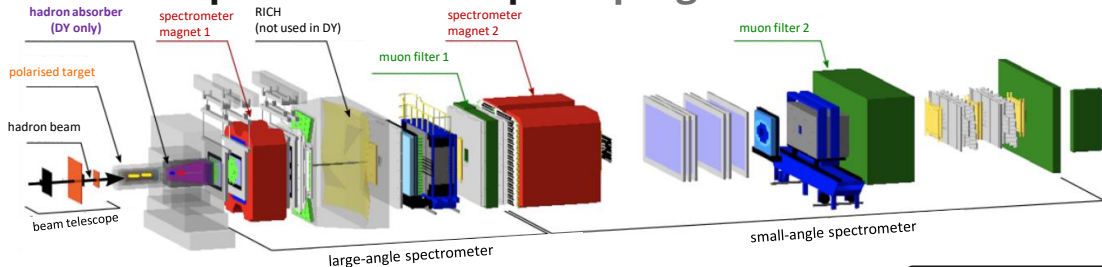
An extensive research programme on the structure of nucleons, including spin and on hadron spectroscopy

Drell Yan data taking  
2015 + 2018

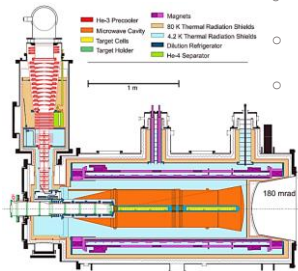




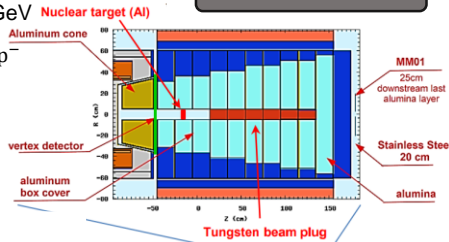
# COMPASS experimental setup: DY programme



Polarised target



Hadron absorber



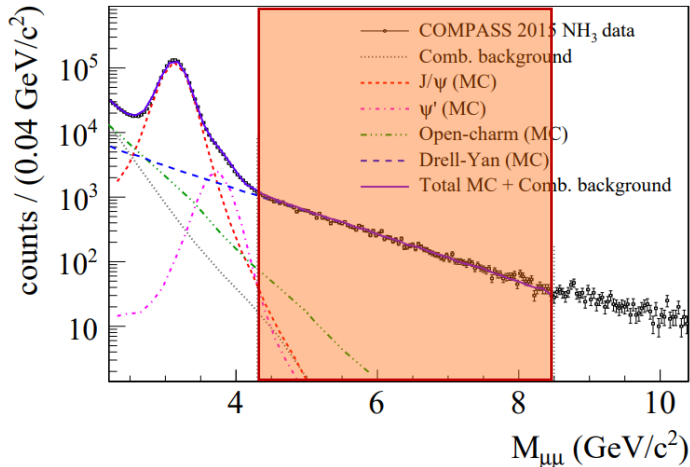
- High energy negative hadron beam: 190 GeV Nuclear target (Al)
- Beam composition: **97%  $\pi^-$** , 2%  $K^-$ , 1%  $p^-$
- Targets:
  - polarised  $NH_3$
  - Al, W
- Hadron absorber
- Muon identification system
- 2 spectrometer stages for a wide phase space coverage

# Drell-Yan measurement at COMPASS

96% pure Drell-Yan in dimuon mass range:  $4.3 < M_{\mu\mu}/(\text{GeV}/c^2) < 8.5$

WTSA

$4.3 < M_{\mu\mu}/(\text{GeV}/c^2) < 8.5$



# Drell-Yan measurement at COMPASS

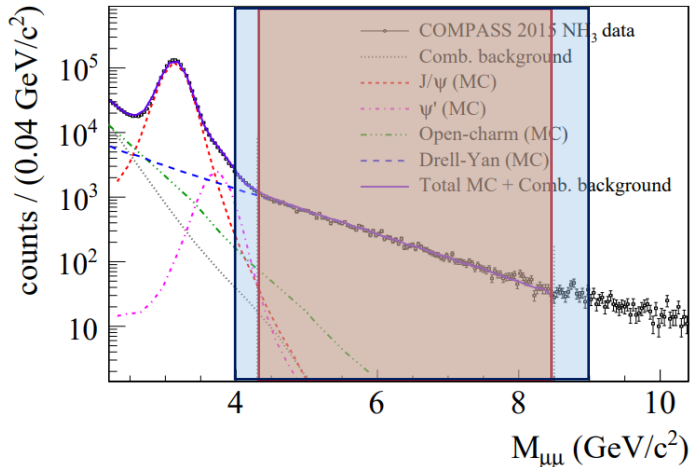
With background correction, achieve mass range:  $4.0 < M_{\mu\mu}/(\text{GeV}/c^2) < 9.0$

**WTSA**

$$4.3 < M_{\mu\mu}/(\text{GeV}/c^2) < 8.5$$

**TSA**

$$4.0 < M_{\mu\mu}/(\text{GeV}/c^2) < 9.0$$





## TSA

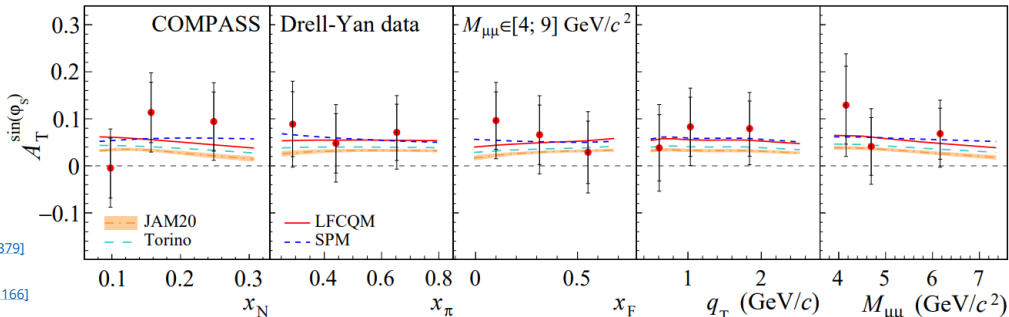
*"Nothing in life is to be feared, it is only to be understood. Now is the time to understand more, so that we may fear less."*

*Maria Skłodowska-Curie*

# TSA Results: Sivers (SIDIS and DY)

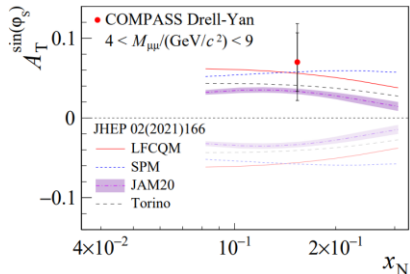
$$A_T^{\sin(\phi_S)} \propto f_{1,\pi}^q \otimes f_{1T,N}^{q\perp}$$

Sivers  
DY TSA



[COMPASS, hep-ex/2312.17379]  
to appear in Phys. Rev. Lett.

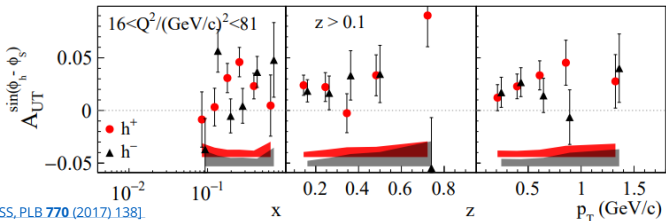
Theo. Pred.: [JHEP 02 (2021) 166]



[COMPASS, PLB 770 (2017) 138]

SIDIS Sivers TSA

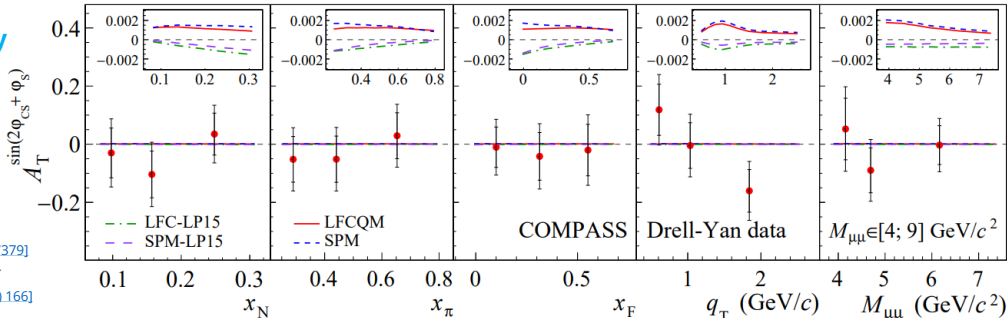
$$A_{UT}^{\sin(\phi_h - \phi_S)} \propto f_{1T,N}^{q\perp} \otimes D_{1q}^h$$



$$A_T^{\sin(2\varphi_{CS}+\varphi_S)} \propto h_{1,\pi}^{q\perp} \otimes h_{1T,N}^{q\perp}$$

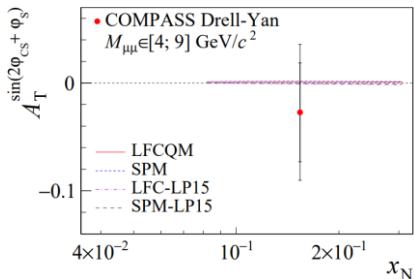
# TSA Results: Pretzelosity (SIDIS and DY)

## Pretzelosity DY TSA



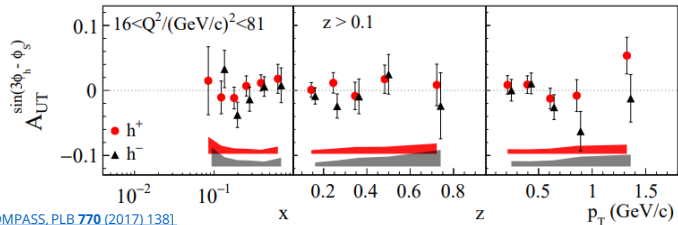
[COMPASS, hep-ex/2312.17379] to appear in Phys. Rev. Lett.

Theo. Pred.: [JHEP 02 (2021) 166]



## Pretzelosity SIDIS TSA

$$A_{UT}^{\sin(3\phi_h - \phi_S)} \propto h_{1T,N}^{q\perp} \otimes H_{1q}^{\perp h}$$

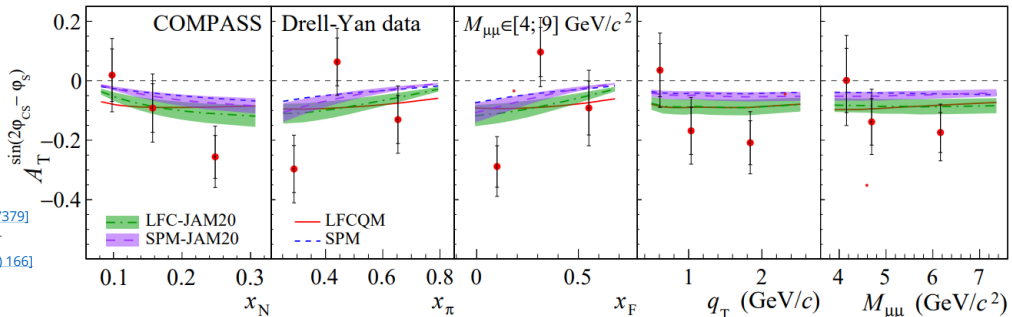


[COMPASS, PLB 770 (2017) 138]

$$A_T^{\sin(2\varphi_{CS}-\varphi_S)} \propto h_{1,\pi}^{q\perp} \otimes h_{1,N}^q$$

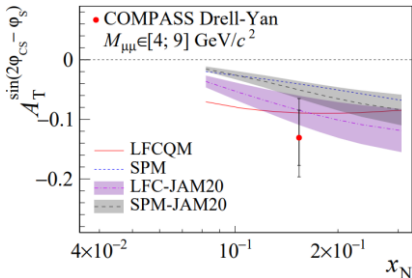
# TSA Results: Transversity (SIDIS and DY)

## Transversity DY TSA



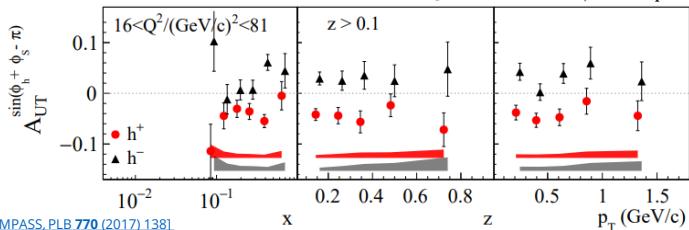
[COMPASS, hep-ex/2312.17379]  
to appear in Phys. Rev. Lett.

Theo. Pred.: [JHEP 02 (2021) 166]



[COMPASS, PLB 770 (2017) 138]

## Transversity SIDIS TSA $A_{UT}^{\sin(\phi_h+\phi_S)} \propto h_{1,N}^q \otimes H_{1q}^{\perp h}$







# Weighted TSAs

*"With four parameters I can fit an elephant,  
and with five I can make him wiggle his  
trunk."*

*John von Neumann*

# Weighted TSAs in Drell-Yan

The convolution cannot be resolved without assumptions about the dependence of the TMD PDF on the intrinsic transverse momentum.

Weighting with powers of the transverse momentum allows to avoid assumptions on  $k_T$ .

TSA		WTSA*
$A_T^{\sin(\varphi_S)} \propto f_{1,\pi}^q \otimes f_{1T,N}^{q\perp}$	← Siviers →	$A_T^{\sin(\varphi_S) \frac{q_T}{M_N}} \propto f_{1,\pi}^q \times f_{1T,N}^{q\perp(1)}$
$A_T^{\sin(2\varphi_{CS}+\varphi_S)} \propto h_{1,\pi}^{q\perp} \otimes h_{1T,N}^{q\perp}$	← Pretzelosity →	$A_T^{\sin(2\varphi_{CS}+\varphi_S) \frac{q_T^3}{2M_N^2 M_\pi}} \propto h_{1,\pi}^{q\perp(1)} \times h_{1T,N}^{q\perp(2)}$
$A_T^{\sin(2\varphi_{CS}-\varphi_S)} \propto h_{1,\pi}^{q\perp} \otimes h_{1,N}^q$	← Transversity →	$A_T^{\sin(2\varphi_{CS}-\varphi_S) \frac{q_T}{M_\pi}} \propto h_{1,\pi}^{q\perp(1)} \times h_{1,N}^q$

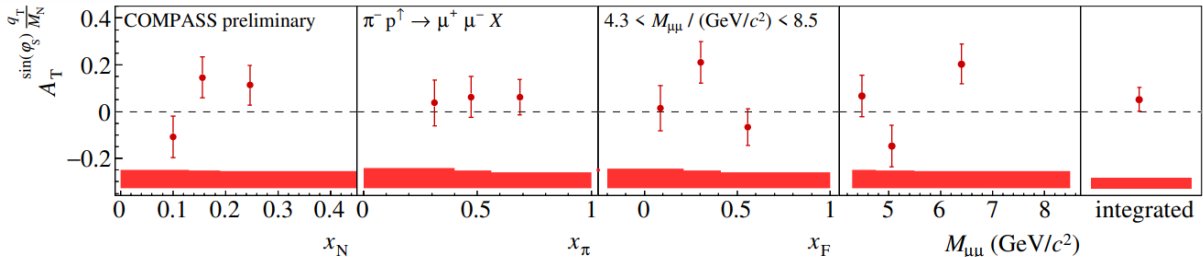
\* The n-th moment of a TMD PDF of a pion or proton:

$$f^{(n)}(x) = \int d^2\mathbf{k}_T \left( \frac{k_T^2}{2M^2} \right)^n f(x, k_T^2)$$

# WTSA Results: Sivers (SIDIS and DY)

## Sivers DY WTSA

$$A_T^{\sin(\varphi_S) \frac{q_T}{M_N}} \propto f_{1,\pi}^q \times f_{1T,N}^{q\perp(1)}$$

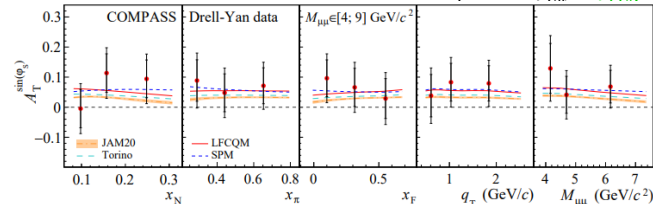


1 $\sigma$  positive Sivers WTSA compatible with Sivers TSA

[COMPASS, hep-ex/2312.17379]  
to appear in Phys. Rev. Lett.

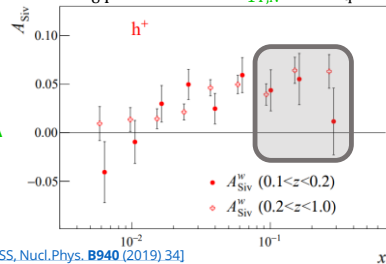
## Sivers DY TSA

$$A_T^{\sin(\varphi_S)} \propto f_{1,\pi}^q \otimes f_{1T,N}^{q\perp}$$



## Sivers SIDIS WTSA

$$A_{UT}^{\sin(\phi_h - \phi_S) \frac{P_T}{z M_N}} \propto f_{1T,N}^{q\perp(1)} \times D_{1q}^h$$



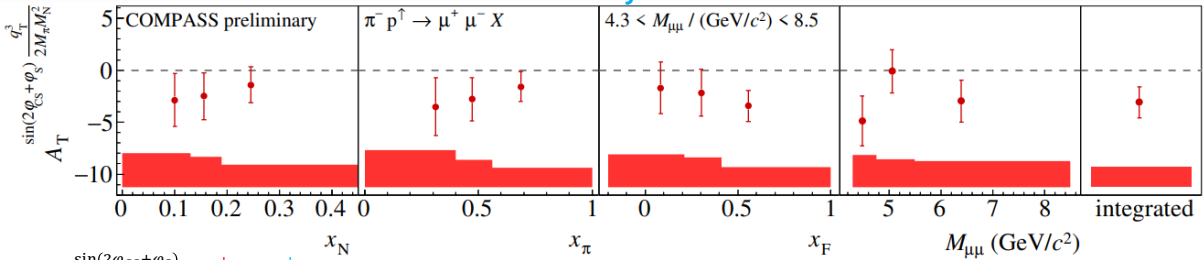
[COMPASS, Nucl.Phys. B940 (2019) 34]

# WTSA Results: Pretzelosity (DY)

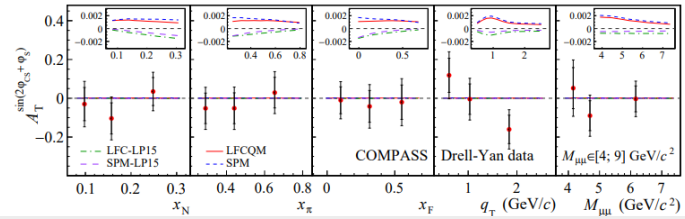
Comparison of WTSA and TSA for Pretzelosity asymmetry

$$A_T^{\sin(2\varphi_{CS}+\varphi_S)} \frac{q_T^3}{2M_N^2 M_\pi} \propto h_{1,\pi}^{q\perp(1)} \times h_{1T,N}^{q\perp(2)}$$

## DY Pretzelosity WTSA



## DY Pretzelosity TSA



**Pretzelosity** is expected to be zero  
 $2\sigma$  negative **Pretzelosity WTSA**

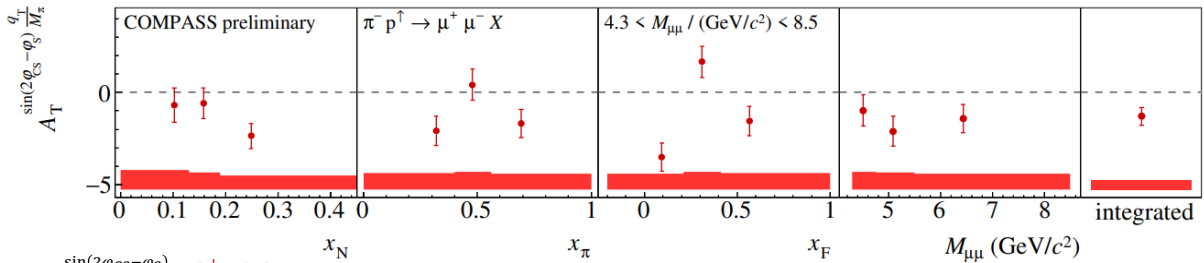
[COMPASS, hep-ex/2312.17379]  
 to appear in Phys. Rev. Lett.

# WTSA Results: Transversity (DY)

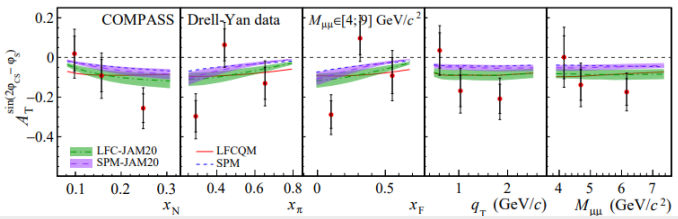
Comparison of WTSA and TSA for **Transversity** asymmetry

## DY Transversity WTSA

$$A_T^{\sin(2\varphi_{CS}-\varphi_S)\frac{q_T}{M_\pi}} \propto h_{1,\pi}^{q\perp(1)} \times h_{1,N}^q$$



## DY Transversity TSA



**2σ negative Transversity**  
Results compatible with **Transversity TSA**

[COMPASS, hep-ex/2312.17379]  
to appear in Phys. Rev. Lett.

# Conclusions

- **COMPASS probes 3-dimensional structure of nucleon**
- COMPASS SIDIS and Drell-Yan TSAs measurements represent a unique experimental input to study the universality of TMD PDFs

## Drell-Yan TSAs

- $1\sigma$  positive **Sivers TSA**
- **Pretzelocity TSA** found to be small and compatible with zero
- $2\sigma$  negative **Transversity TSA**
- Results agree with theoretical predictions and consistent with analogous measurements for SIDIS

$$A_{DY} \propto PDF_N \otimes PDF_{\pi^-}$$

## Transverse momentum weighted Drell-Yan TSA

- A way to overcome the convolution over intrinsic  $k_T$
- A direct access to the  $k_T^2$ -moments of TMD PDFs
- $\sim 1\sigma$  positive **Sivers WTSA** compatible with DY TSA and SIDIS  $P_T$ -weighted TSA
- $\sim 2\sigma$  negative **Pretzelocity WTSA** effect
- $\sim 2\sigma$  negative **Transversity WTSA** consistent with TSAs

$$A_{DY}^W \propto PDF_N \times PDF_{\pi^-}$$

## Prospects

- Analysis of a WTSA ongoing, paper in preparation



**Thank you for attention!**

*"All of physics is either impossible or trivial. It is impossible until you understand it, and then it becomes trivial."*

*Ernest Rutherford*



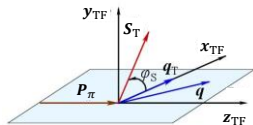


**Backup slides**

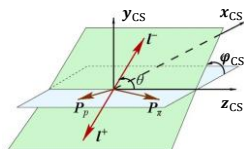
# Single polarised Drell-Yan process

Cross-section, LO TMD approach for transversely polarised target in terms of structure functions:

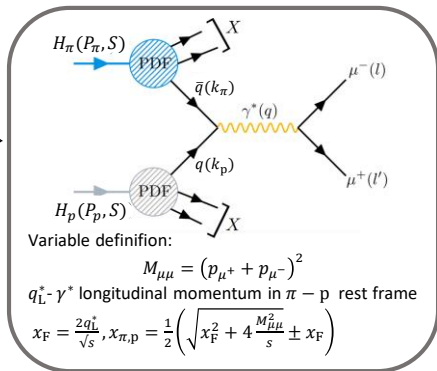
$$\frac{d\sigma^{LO}}{dx_p dx_\pi d^2q_T d\varphi_{CS} d(\cos\theta) d\varphi_S} = C_0 \left\{ \begin{array}{l} (1 + \cos^2 \theta) F_U^1 + \sin^2 \theta \cos 2\varphi F_U^{\cos 2\varphi_{CS}} \\ (1 + \cos^2 \theta) \sin(\varphi_S) F_T^{\sin\varphi_S} + \\ \sin^2 \theta \left( \begin{array}{l} \sin(2\varphi + \varphi_S) F_T^{\sin(2\varphi_{CS} + \varphi_S)} \\ + \\ \sin(2\varphi - \varphi_S) F_T^{\sin(2\varphi_{CS} - \varphi_S)} \end{array} \right) \end{array} \right\}$$



Target frame



Collin-Soper frame



Variable definition:

$$M_{\mu\mu} = (p_{\mu^+} + p_{\mu^-})^2$$

$q_L^*$  -  $\gamma^*$  longitudinal momentum in  $\pi - p$  rest frame

$$x_F = \frac{2q_L^*}{\sqrt{s}}, x_{\pi,p} = \frac{1}{2} \left( \sqrt{x_F^2 + 4 \frac{M_{\mu\mu}^2}{s}} \pm x_F \right)$$

## Boer-Mulders

$$F_U^{\cos 2\varphi_{CS}} \propto h_{1,\pi}^{q\perp} \otimes h_{1,N}^{q\perp}$$

## Sivers

$$F_T^{\sin\varphi_S} \propto f_{1,\pi}^q \otimes f_{1,T,N}^{q\perp}$$

## Pretzelosity

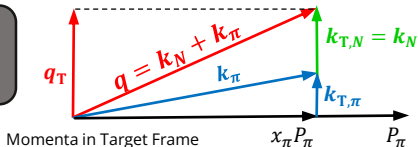
$$F_T^{\sin(2\varphi_{CS} + \varphi_S)} \propto h_{1,\pi}^{q\perp} \otimes h_{1T,N}^{q\perp}$$

## Transversity

$$F_T^{\sin(2\varphi_{CS} - \varphi_S)} \propto h_{1,\pi}^{q\perp} \otimes h_{1,N}^q$$

# Single polarised Drell-Yan process

The convolution of TMD PDFs runs over the intrinsic transverse momenta  $k_T$ .



TMD PDFs are accessed through measurement of target spin dependent azimuthal asymmetries TSA.

**Sivers Asymmetries**

$$A_T^{\sin(\varphi_S)} = \frac{F_T^{\sin(\varphi_S)}}{F_U^1}$$

**Sivers** for nucleon, number density for  $\pi^-$

**Pretzelosity Asymmetries**

$$A_T^{\sin(2\varphi_{CS} + \varphi_S)} = \frac{F_T^{\sin(2\varphi_{CS} + \varphi_S)}}{2F_U^1}$$

**Pretzelosity** for nucleon, **Boer-Mulders** for  $\pi^-$

**Transversity Asymmetries**

$$A_T^{\sin(2\varphi_{CS} - \varphi_S)} = \frac{F_T^{\sin(2\varphi_{CS} - \varphi_S)}}{2F_U^1}$$

**Transversity** for nucleon, **Boer-Mulders** for  $\pi^-$

# Backup: Single Polarised Drell-Yan Process

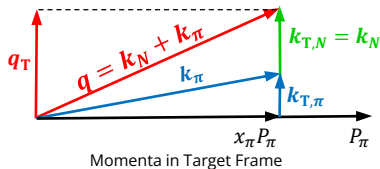
Each structure function can be written as a TMD PDF convolution over the intrinsic transverse momenta.

$$F_T^{\sin(\varphi_S)} = \mathcal{C} \left[ \frac{\mathbf{q}_T \mathbf{k}_{T,N}}{q_T M_N} f_{1,\pi} f_{1T,p}^\perp \right] \quad \text{Sivers for proton, number density for } \pi^-$$

$$F_T^{\sin(2\varphi_{CS} + \varphi_S)} = -\mathcal{C} \left[ \frac{2(\mathbf{q}_T \mathbf{k}_{T,N}) [2(\mathbf{q}_T \mathbf{k}_{T,N})(\mathbf{q}_T \mathbf{k}_{T,\pi}) - q_T^2 (\mathbf{k}_{T,N} \mathbf{k}_{T,\pi})] - q_T^2 k_{T,N}^2 (\mathbf{q}_T \mathbf{k}_{T,\pi})}{2q_T^3 M_N^2 M_\pi} h_{1,\pi}^\perp h_{1T,N}^\perp \right] \quad \begin{array}{l} \text{Pretzelosity for proton,} \\ \text{Boer-Mulders for } \pi^- \end{array}$$

$$F_T^{\sin(2\varphi_{CS} - \varphi_S)} = -\mathcal{C} \left[ \frac{\mathbf{q}_T \mathbf{k}_{T,\pi}}{q_T M_\pi} h_{1,\pi}^\perp h_{1,N}^\perp \right] \quad \text{Transversity for proton, Boer-Mulders for } \pi^-$$

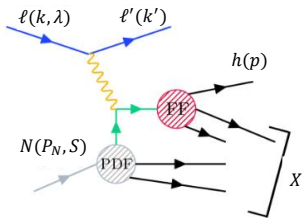
$$\mathcal{C}[w(\mathbf{k}_{T,\pi}; \mathbf{k}_{T,N}; \mathbf{q}_T) f_\pi f_N] = \frac{1}{N_c} \sum_q \left\{ \begin{array}{l} e_q^2 \int d^2 \mathbf{k}_{T,\pi} d^2 \mathbf{k}_{T,N} \delta^{(2)}(\mathbf{q}_T - \mathbf{k}_{T,\pi} - \mathbf{k}_{T,N}) \\ \times w(\mathbf{k}_{T,\pi}; \mathbf{k}_{T,N}; \mathbf{q}_T) \left[ \begin{array}{l} f_\pi^{\bar{q}}(x_\pi, k_{T,\pi}^2) f_N^q(x_N, k_{T,N}^2) \\ + \\ f_\pi^q(x_\pi, k_{T,\pi}^2) f_N^{\bar{q}}(x_N, k_{T,N}^2) \end{array} \right] \end{array} \right\}$$



TMD PDFs can be accessed through measurement of target spin (in)dependent azimuthal asymmetries

$$A_U^{\cos(\varphi_{CS})} = \frac{F_U^{\cos(\varphi_{CS})}}{F_U^1} \quad A_T^{\sin(\varphi_S)} = \frac{F_T^{\sin(\varphi_S)}}{F_U^1} \quad A_T^{\sin(2\varphi_{CS} + \varphi_S)} = \frac{F_T^{\sin(2\varphi_{CS} + \varphi_S)}}{2F_U^1} \quad A_T^{\sin(2\varphi_{CS} - \varphi_S)} = \frac{F_T^{\sin(2\varphi_{CS} - \varphi_S)}}{2F_U^1}$$

# SIDIS



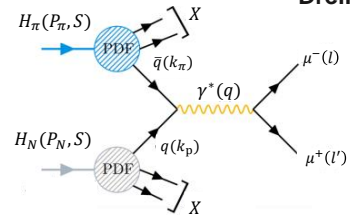
$$A_{SIDIS} \propto PDF_N \otimes FF$$

$$\frac{d\sigma_{SIDIS}^{LO}}{dx dy dz^2 p_T d\phi_h d\phi_S} \propto \left\{ +|S_T| \left[ \begin{array}{l} 1 + \cos(2\phi_h) \varepsilon A_{UU}^{\cos(2\phi_h)} \\ \sin(\phi_h - \phi_S) A_{UT}^{\sin(\phi_h - \phi_S)} + \\ \sin(\phi_h + \phi_S) \varepsilon A_{UT}^{\sin(\phi_h + \phi_S)} + \\ \sin(3\phi_h - \phi_S) \varepsilon A_{UT}^{\sin(3\phi_h - \phi_S)} + \end{array} \right] \right\}$$

$$\begin{aligned} A_{UU}^{\cos(2\phi_h)} &\propto h_{1,N}^{q\perp} \otimes H_{1q}^{\perp h} \\ A_{UT}^{\sin(\phi_h - \phi_S)} &\propto f_{1T,N}^{q\perp} \otimes D_{1q}^h \\ A_{UT}^{\sin(3\phi_h - \phi_S)} &\propto h_{1T,N}^{q\perp} \otimes H_{1q}^{\perp h} \\ A_{UT}^{\sin(\phi_h + \phi_S)} &\propto h_{1T,N}^q \otimes H_{1q}^{\perp h} \end{aligned}$$

# SIDIS vs. DY

# Drell-Yan



$$A_{DY} \propto PDF_N \otimes PDF_{\pi^-}$$

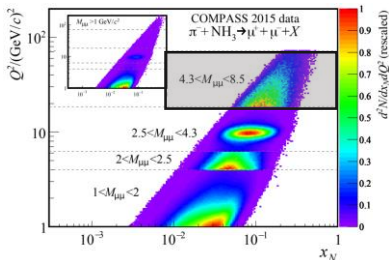
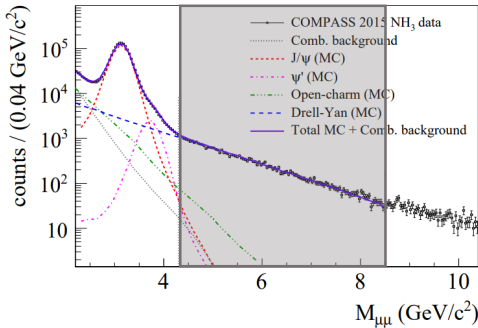
$$\frac{d\sigma_{DY}^{LO}}{d\Omega d^4q} \propto \left\{ +|S_T| \left[ \begin{array}{l} 1 + D_{\sin^2 \theta} \cos(2\varphi_{CS}) A_U^{\cos(2\varphi_{CS})} \\ \sin(\varphi_S) A_T^{\sin(\varphi_S)} + \\ \sin(2\varphi_{CS} + \varphi_S) A_T^{\sin(2\varphi_{CS} + \varphi_S)} + \\ \sin(2\varphi_{CS} - \varphi_S) A_T^{\sin(2\varphi_{CS} - \varphi_S)} \end{array} \right] \right\}$$



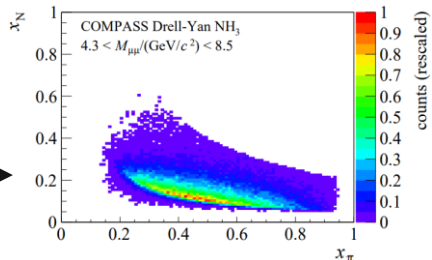
# Drell-Yan measurement at COMPASS

The dimuon mass range  $4.3 < M_{\mu\mu}/(\text{GeV}/c^2) < 8.5$  is 96% pure Drell-Yan.

- Low background
- Valence region



Valence region of  $x_N$  and  $x_\pi$  in a given  $Q^2 - x$  kinematic coverage



# Weighted TSAs in Drell-Yan

The convolution cannot be resolved without assumptions about the dependence of the TMD PDF on the intrinsic transverse momentum.

Weighting with powers of the transverse momentum allows to avoid assumptions on  $k_T$ .

Asymmetries in terms of structure functions:

$$A_T^{\sin\Phi W_\Phi} = \frac{\int d^2\mathbf{q}_T W_\Phi F_T^{\sin\Phi}}{\int d^2\mathbf{q}_T F_U^1},$$

where  $W_\Phi$  is weight for  $\Phi = \varphi_S, 2\varphi_{CS} + \varphi_S, 2\varphi_{CS} - \varphi_S$ .

TSA

$$A_T^{\sin(\varphi_S)} \propto f_{1,\pi}^q \otimes f_{1T,N}^{q\perp}$$

$$A_T^{\sin(2\varphi_{CS}+\varphi_S)} \propto h_{1,\pi}^{q\perp} \otimes h_{1T,N}^{q\perp}$$

$$A_T^{\sin(2\varphi_{CS}-\varphi_S)} \propto h_{1,\pi}^{q\perp} \otimes h_{1,N}^q$$

Sivers

Pretzelosity

Transversity

WTSA

The n-th moment of a TMD PDF of a pion or proton:

$$f^{(n)}(x) = \int d^2\mathbf{k}_T \left( \frac{k_T^2}{2M^2} \right)^n f(x, k_T^2).$$

$$A_T^{\sin(\varphi_S) \frac{q_T}{M_N}} \propto f_{1,\pi}^q \times f_{1T,N}^{q\perp(1)}$$

$$A_T^{\sin(2\varphi_{CS}+\varphi_S) \frac{q_T^3}{2M_N^2 M_\pi}} \propto h_{1,\pi}^{q\perp(1)} \times h_{1T,N}^{q\perp(2)}$$

$$A_T^{\sin(2\varphi_{CS}-\varphi_S) \frac{q_T}{M_\pi}} \propto h_{1,\pi}^{q\perp(1)} \times h_{1,N}^q$$