

Efficient generation of unweighted events with matrix element surrogates

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▶ Problem: unweighted event generation is **resource intensive**

▶ becomes worse at higher partonic multiplicity (→ HL-LHC)



save resources by using **NN matrix element surrogates**



for $ug \rightarrow t\bar{t}gggu$ ($t\bar{t} + 4$ jets) a 4-layer NN is **200.000 times faster** than a full colour-summed calculation!

▶ Problem solved?

→ No! **Results are biased** due to approximation errors!

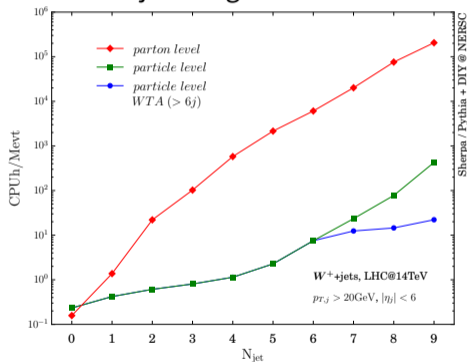
Questions

How to get rid of the bias?

How much can we actually gain?

Motivation

multi-jet merged calculation

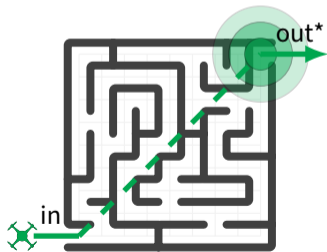
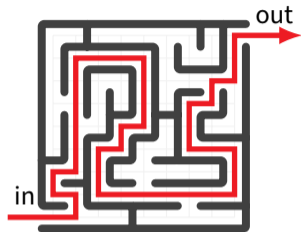


- ▶ computing time for unweighted events scales exponentially with multiplicity
- ▶ two factors contribute:
 - (1) matrix elements become more expensive
 - (2) unweighting efficiency goes down (curse of dimensionality)
- ▶ to deal with (2) need to improve phase space sampler, e.g. using normalizing flows

But what about the ME evaluation time?

- ▶ we have to evaluate the ME for each trial event in unweighting
- ▶ if unw. eff. is small, **ME evaluation time is a bottleneck**

Idea



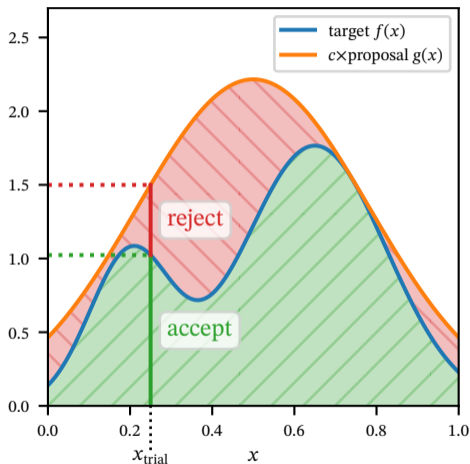
Goal:

increase the number of unweighted events per second

Idea:

- ▶ reduce event generation time by reducing the number of calls to the ME
 - use a **fast & accurate surrogate** (NN)
- ▶ correct all errors from the approximation in a 2nd unweighting step
 - method is **unbiased by design**

Unweighted event generation explained



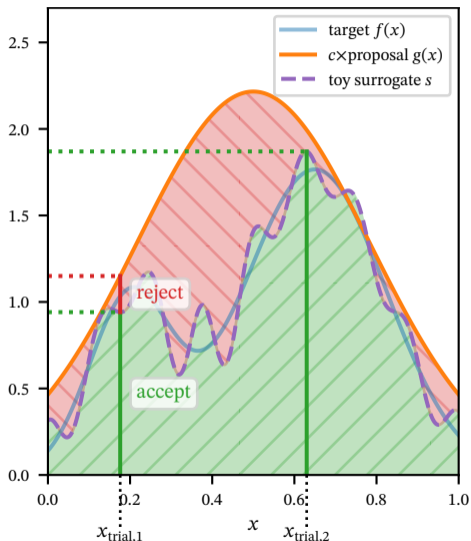
- ▶ Monte Carlo sampled events come with weights w
- ▶ we often want to work with unweighted events
 - produce unit-weight events by **unweighting**
 - deliberately reduce sample size while retaining most of its statistical power
- ▶ accept events with probability $p_{\text{accept}} = \frac{f(x)}{cg(x)}$, where $c \geq w_{\text{max}}$

unweighting efficiency

$$\eta = \frac{\langle w \rangle}{c}$$

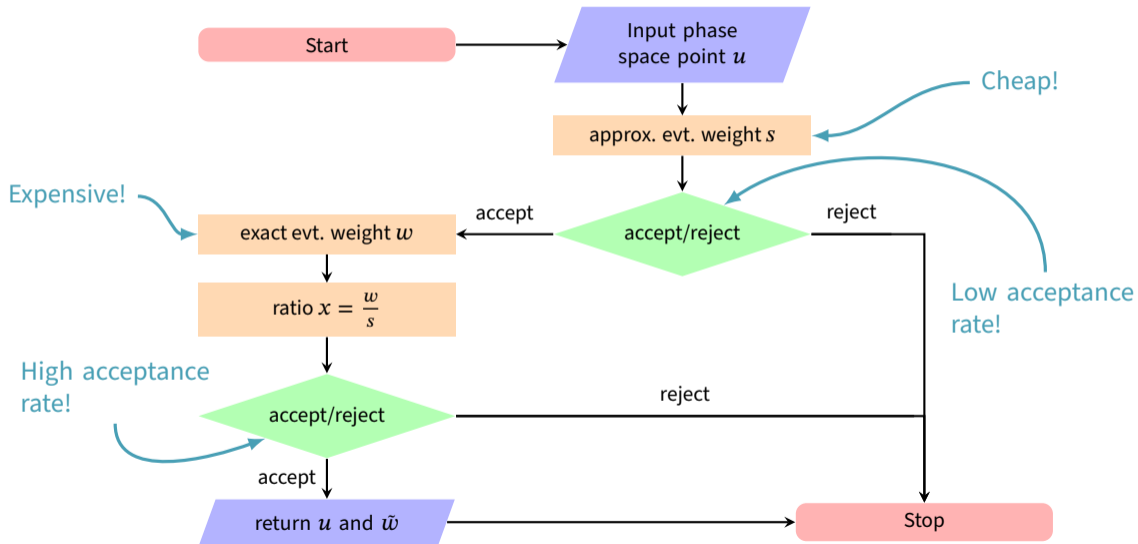
→ ratio between #accepted and #trials

Unweighting against a surrogate function

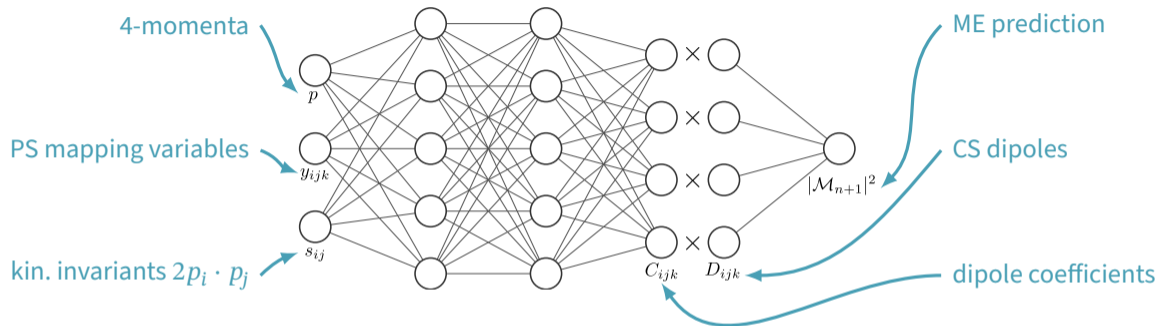


- ▶ replace target $f(x)$ by surrogate $s(x)$
- ▶ accept/reject probabilities are slightly wrong
→ events get correction weights $x = \frac{w}{s} = \frac{f}{gs}$
- ▶ 2nd unweighting step leads to fully unweighted event sample
- ▶ total efficiency: $\eta_1 \cdot \eta_2 = \frac{\langle s \rangle}{s_{\max}} \cdot \frac{\langle x \rangle}{x_{\max}}$
- ▶ trick: eval. true weight only for those events accepted in the 1st step!
- ▶ if $f(x)$ is expensive and $s(x)$ is a good approximation, we can save a lot of time

Surrogate unweighting algorithm



Factorization-aware matrix element emulation



soft/collinear factorization properties

$$|\mathcal{M}_{n+1}|^2 \rightarrow |\mathcal{M}_n|^2 \otimes \mathbf{V}_{ijk}$$

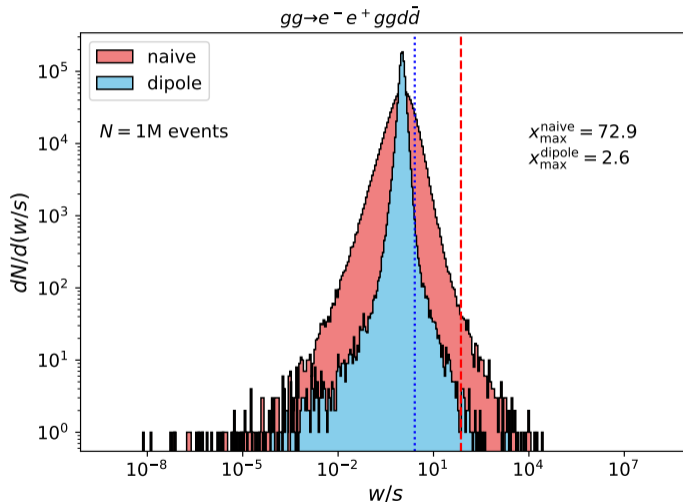
[Catani, Seymour Nucl.Phys. B485 (1997) 291-419]

Ansatz

$$\langle |\mathcal{M}|^2 \rangle \approx \sum_{\{ijk\}} C_{ijk} D_{ijk}$$

Factorisation-aware matrix element emulation

Comparison with naive (non-dipole) model for $Z + 4j$:

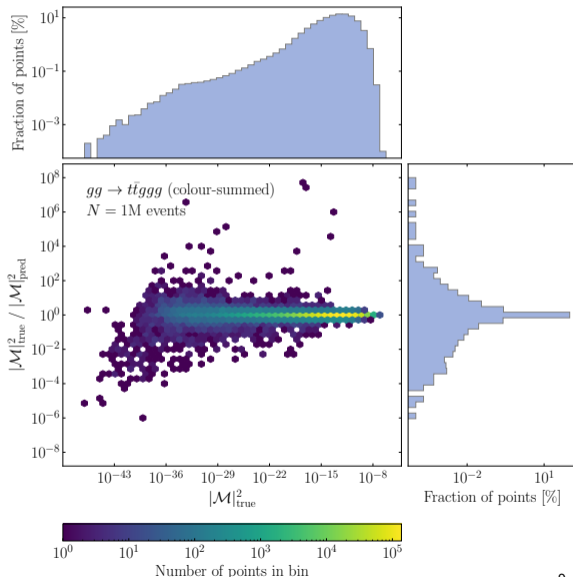


Comparison of
eval time:

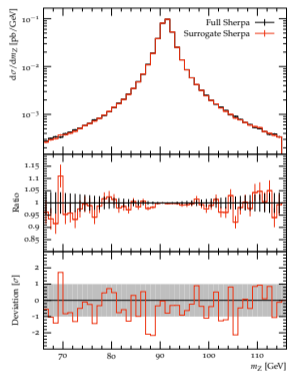
$$\frac{t_{\text{AMEGIC}}}{t_{\text{dipole}}} \approx 388$$

Results: distribution of weights for $t\bar{t} + 3\text{jets}$

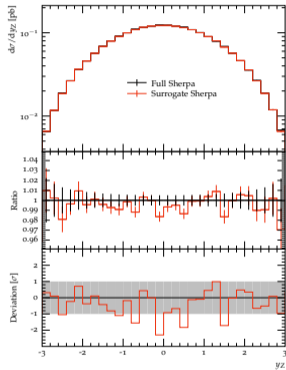
- ▶ MEs reproduced accurately
- ▶ especially in the regions where ME is largest (highest acceptance probabilities)
- ▶ most outliers heavily suppressed in $|\mathcal{M}|^2$
→ deal with them via partial unweighting



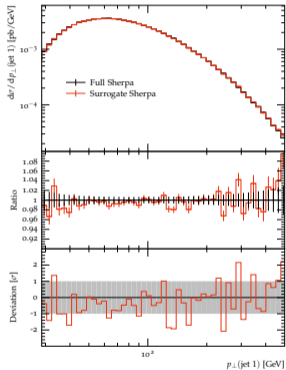
Results: validation plots



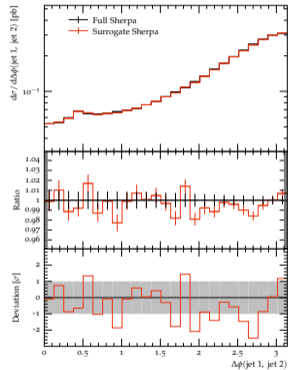
Z mass



Z rapidity



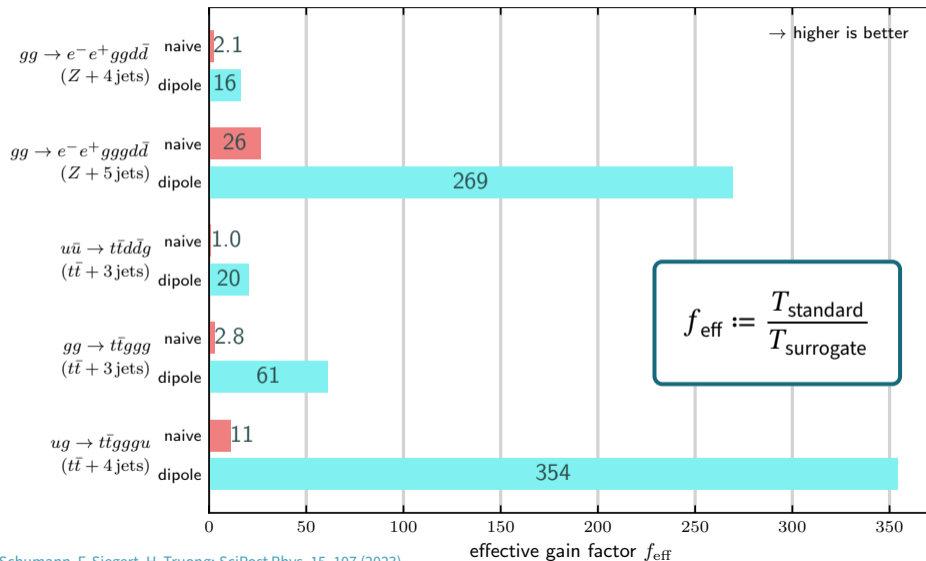
leading jet p_{\perp}



$\Delta\phi(\text{jet 1, jet 2})$

Results: effective gain factors for LHC multi-jet processes

Using 1M training events:



Outlook

- ▶ extend to more realistic settings:
 - deal with hadronic processes (groups of partonic channels)
 - multijet merged
- ▶ new baseline: COMIX colour-summed mode
- ▶ tune NN architecture (hyperparameter optimization)
- ▶ Is it also worthwhile at NLO?

Summary

This talk ...

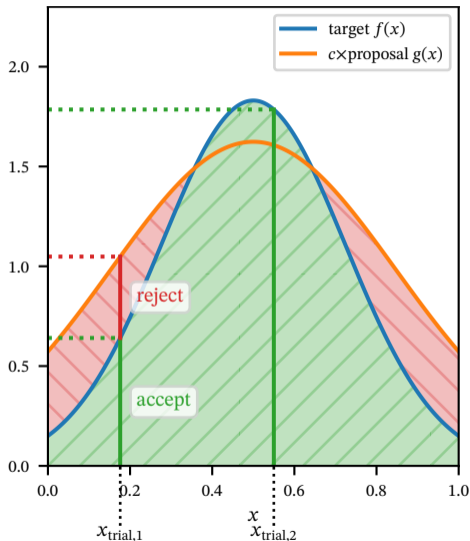
- ▶ introduced a **generic & unbiased method** to speed up unweighted event generation **using fast & accurate surrogates**
- ▶ showed that the **factorisation-aware ME emulation model is very accurate** for colour-summed MEs (incl. hadronic initial states & massive quarks)
- ▶ demonstrated that **large gain factors** can be achieved for unweighting of colour-summed MEs in relevant LHC processes

Conclusion

More physics using the same resources!

Backup Slides

Unweighting in two steps / partial unweighting



- ▶ let's allow $c < w_{\max}$ so that $p_{\text{accept}} \geq 1$ in some regions
- ▶ if accepted, events with $p_{\text{accept}} < 1$ get unit weights
- ▶ events with $p_{\text{accept}} \geq 1$ are always accepted
→ these events get overweights $x = \frac{w}{s}$
- ▶ There is no bias as long as we take the overweights into account!
- ▶ can still produce fully unweighted sample by unweighting against overweights x , respecting their maximum x_{\max}

Implementation details

- ▶ for NN evaluation use **ONNX Runtime** with all possible optimisations
- ▶ two step unweighting implemented in **SHERPA 2** [[Bothmann et al. SciPost Phys. 7, 034 \(2019\)](#)] and **SHERPA 3**
- ▶ **CPU single threaded**
 - use in existing workflows without changes
 - apply to vectorised workflows for even better performance
- ▶ ME generator: AMEGIC [[Krauss et al. JHEP 02 \(2002\) 044](#)]
- ▶ we evaluate the performance for processes that are very important for the LHC: **V +jets** & **$t\bar{t}$ +jets**

Going to NLO

- ▶ at NLO the weight function can become negative
- ▶ unweighting produces events with weight ± 1
- ▶ NN will happily output negative predictions but unweighting needs to be adapted
- ▶ use single maximal weight: $w_{\max} = |w|_{\max} > 0$
- ▶ surrogate may predict wrong sign \rightarrow signed overweights

