



# Anticipation of the discovery potential sensitivity of next-generation neutrinoless double beta decay experiments

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Based on: *Phys. Rev. D* 109, 032001 (2024).



## Introduction

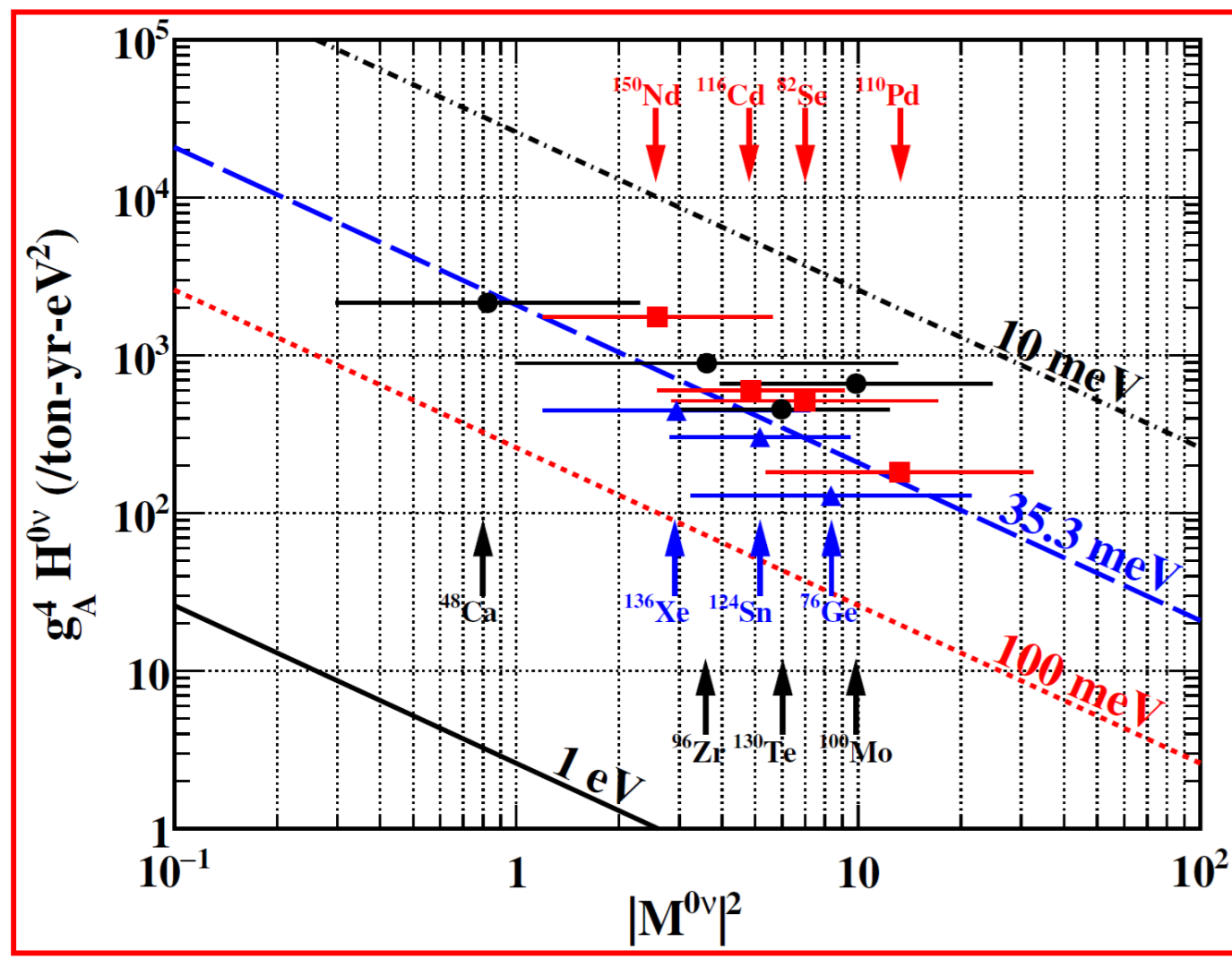
- Neutrinoless double beta decay ( $0\nu\beta\beta$ ) [Furry, 1939]
 
$${}^N_Z A_{\beta\beta} \rightarrow {}^N_{Z+2} A_{\beta\beta} + 2\bar{e}$$
  - Forbidden in Standard Model
  - $\Delta L = 2$
- Observation of  $0\nu\beta\beta$  implies new physics:
  - Neutrinos are Majorana particles ( $\nu = \bar{\nu}$ )
  - Lepton number violations
  - Effective Majorana Neutrino Mass  $\langle m_{\beta\beta} \rangle \neq 0$
- Energetically possible for 35 nuclei
  - A few are experimentally relevant
- Present work: Required Sensitivity: Exposure vs Background

## Formalism

- Half-life in Mass Mechanism:  $\frac{1}{T_{1/2}^{0\nu}} = G^{0\nu} g_A^4 |M^{0\nu}|^2 \frac{\langle m_{\beta\beta} \rangle^2}{m_e}$
- Effective Mass:  $\langle m_{\beta\beta} \rangle = |U_{e1}^2 m_1 + U_{e2}^2 m_2 e^{i\alpha} + U_{e3}^2 m_3 e^{i\beta}|$
- Experimentally measurable Half-life:
 
$$T_{1/2}^{0\nu} = \ln 2 \cdot N(A_{\beta\beta}) \cdot t_{\text{DAQ}} \left[ \frac{\epsilon_{\text{ROI}}}{N_{\text{Obs}}^{0\nu}} \right] = \ln 2 \cdot \left[ \frac{N_A}{M(A_{\beta\beta})} \right] \cdot \left[ \frac{\epsilon_{\text{ROI}}}{N_{\text{Obs}}^{0\nu}} \right]$$
- Combined Half-life:
 
$$|M^{0\nu}|^2 [g_A^4 H^{0\nu}] = \frac{1}{\langle m_{\beta\beta} \rangle^2} \left[ \frac{1}{\sum \frac{N_{\text{Obs}}^{0\nu}}{\epsilon_{\text{ROI}}}} \right]; H^{0\nu} \equiv \ln 2 \left( \frac{N_A}{M(A_{\beta\beta}) m_e^2} \right) G^{0\nu}$$

## A Model for NME's Uncertainty

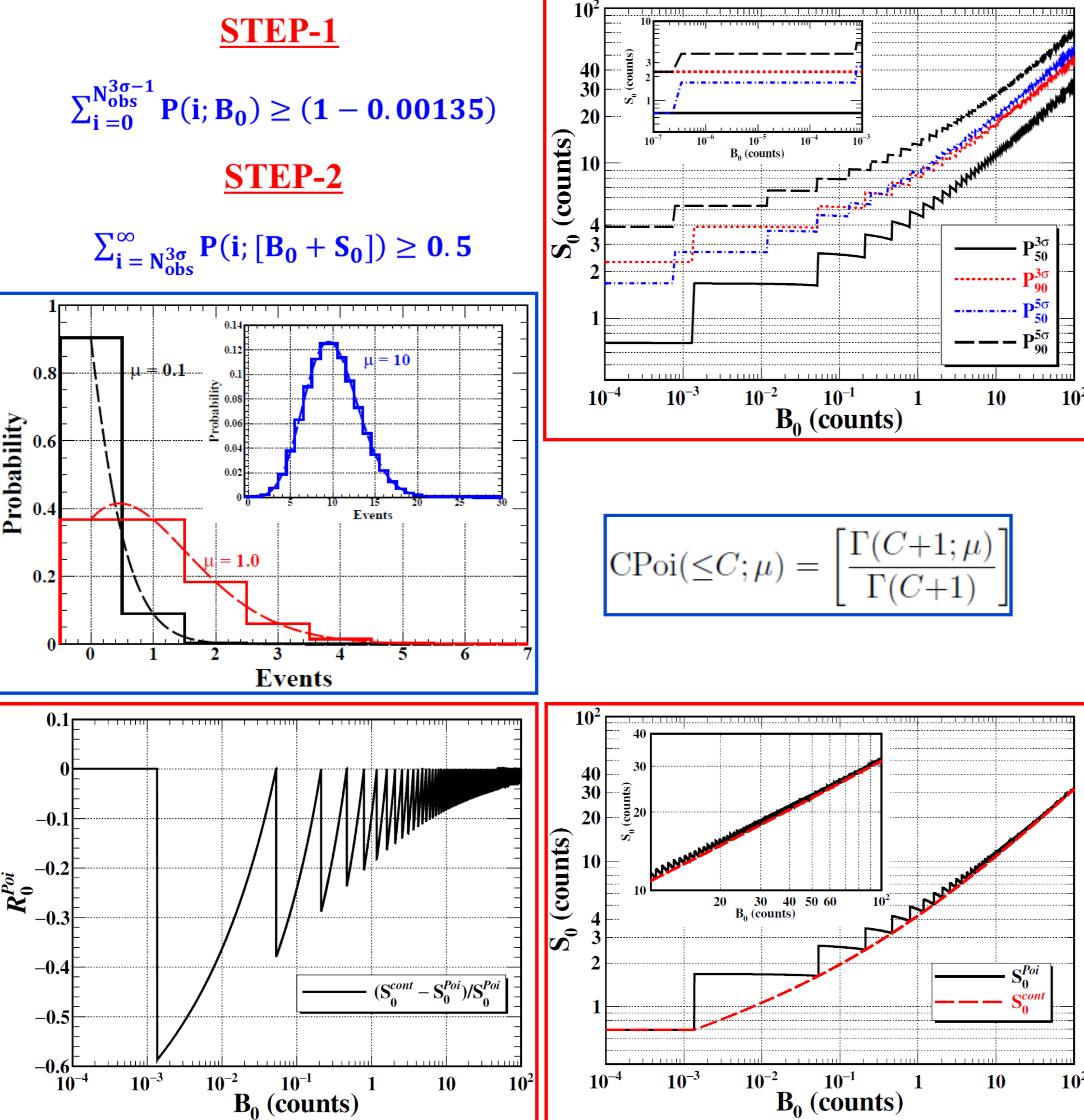
- In Theory - Inverse correlation between  $G^{0\nu}$  and  $|M^{0\nu}|^2$
- Decay rates (1 event/ton-yr with full efficiency) are similar at given  $\langle m_{\beta\beta} \rangle$  and constant  $g_A$



- No favored  $0\nu\beta\beta$  isotope.
- Realistic interpretation lies within a factor of [0.5, 2.0].

## Statistics & Theme

- Discrete/Complete Poisson  $\rightarrow$  (i) Low Background
- Continuous Approximation  $\rightarrow$  (ii) Rare Processes

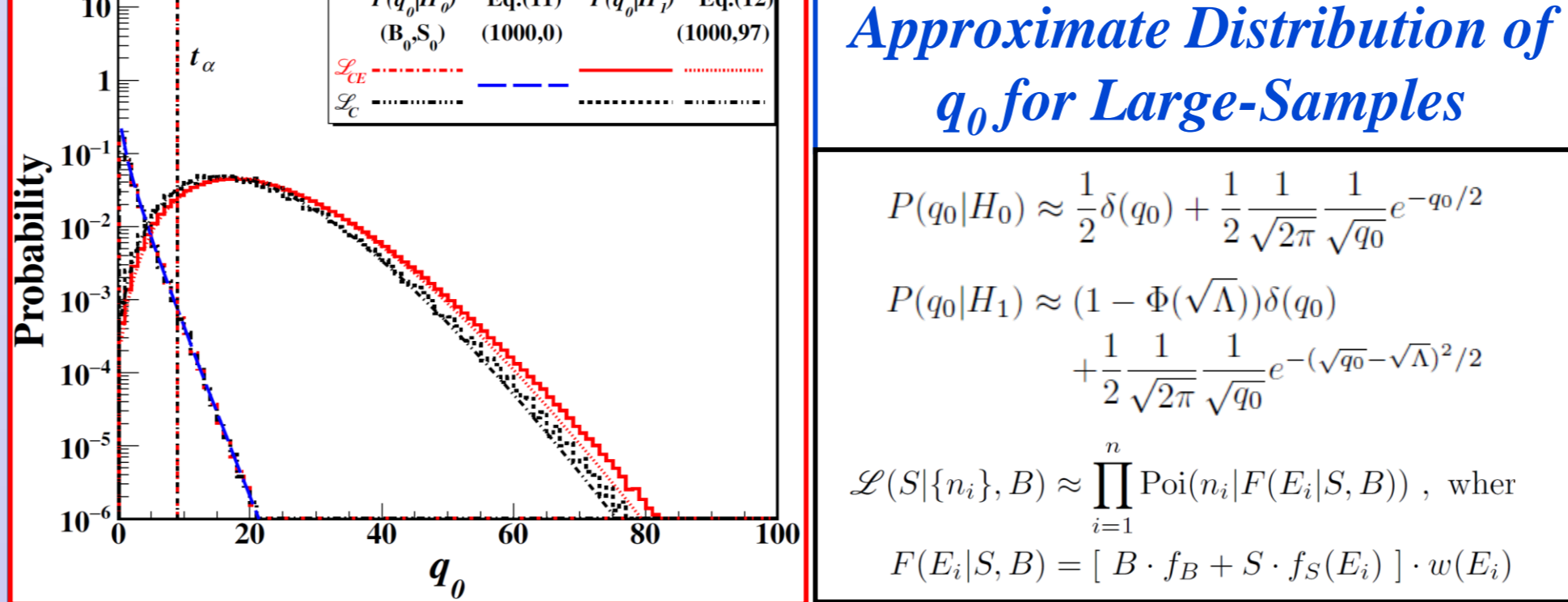


- $S_0$  derived with complete Poisson  $\rightarrow$  Always  $\geq$  Continuous Approximation
- Continuous approximation  $\rightarrow$  Always Underestimate  $S_0$
- Deviation  $\rightarrow$  As much as 60% @ Low Background ( $B_0 \sim 10^{-3}$ )
- Both Consistent  $\rightarrow$  Within 3% @ Large  $B_0 \geq 100$

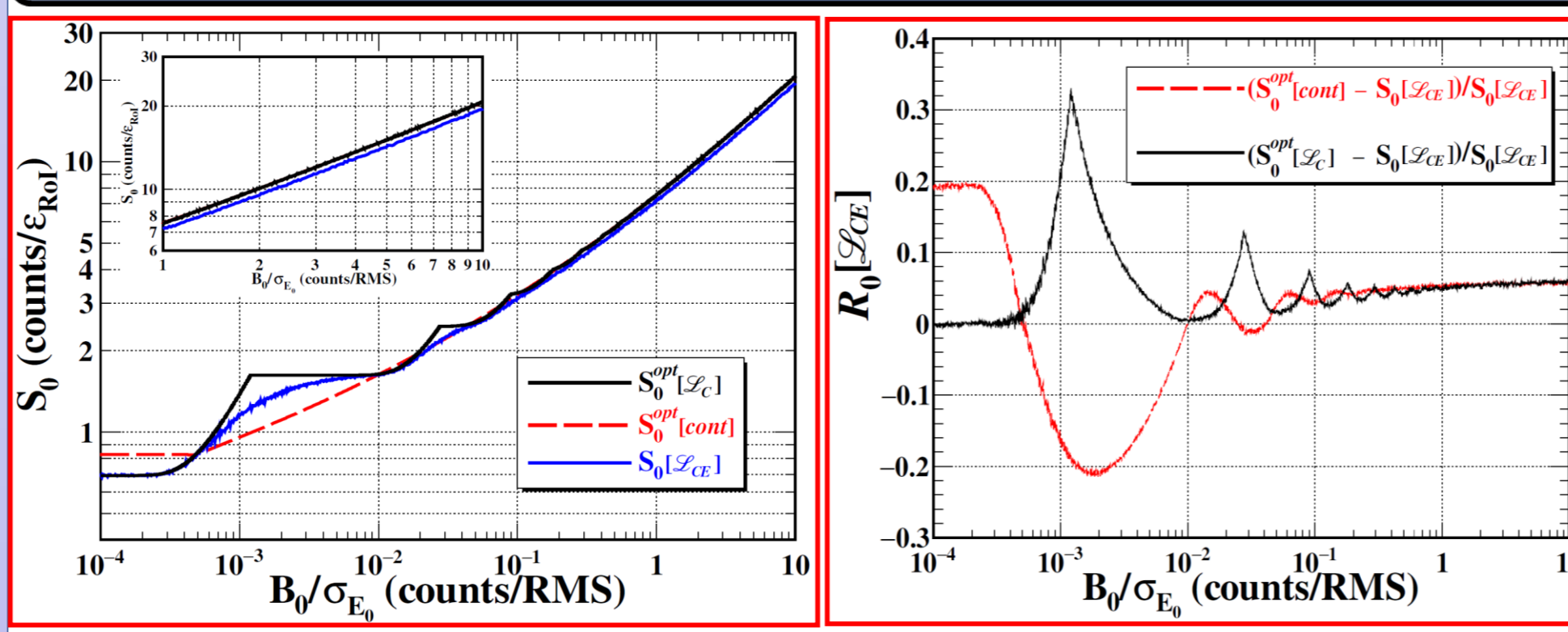
## Likelihood Analysis

$$\mathcal{L}_C \equiv \mathcal{L}(S|N, B) = \frac{e^{-(B+S)} (B+S)^N}{N!} q_0 \equiv t(S=0) = -2 \ln \left[ \frac{\mathcal{L}(S=0)}{\mathcal{L}(\hat{S})} \right]$$

$$\alpha \equiv \int_{t_{\alpha}}^{\infty} P(q_0|H_0) dq_0 \quad \alpha \geq \sum_{q_0 \geq t_{\alpha}} P(q_0|H_0) \quad \beta \equiv \int_0^{t_{\alpha}} P(q_0|H_1) dq_0 \quad \beta = \sum_{q_0 \leq t_{\alpha}} P(q_0|H_1)$$



## Counting vs Extended Likelihood

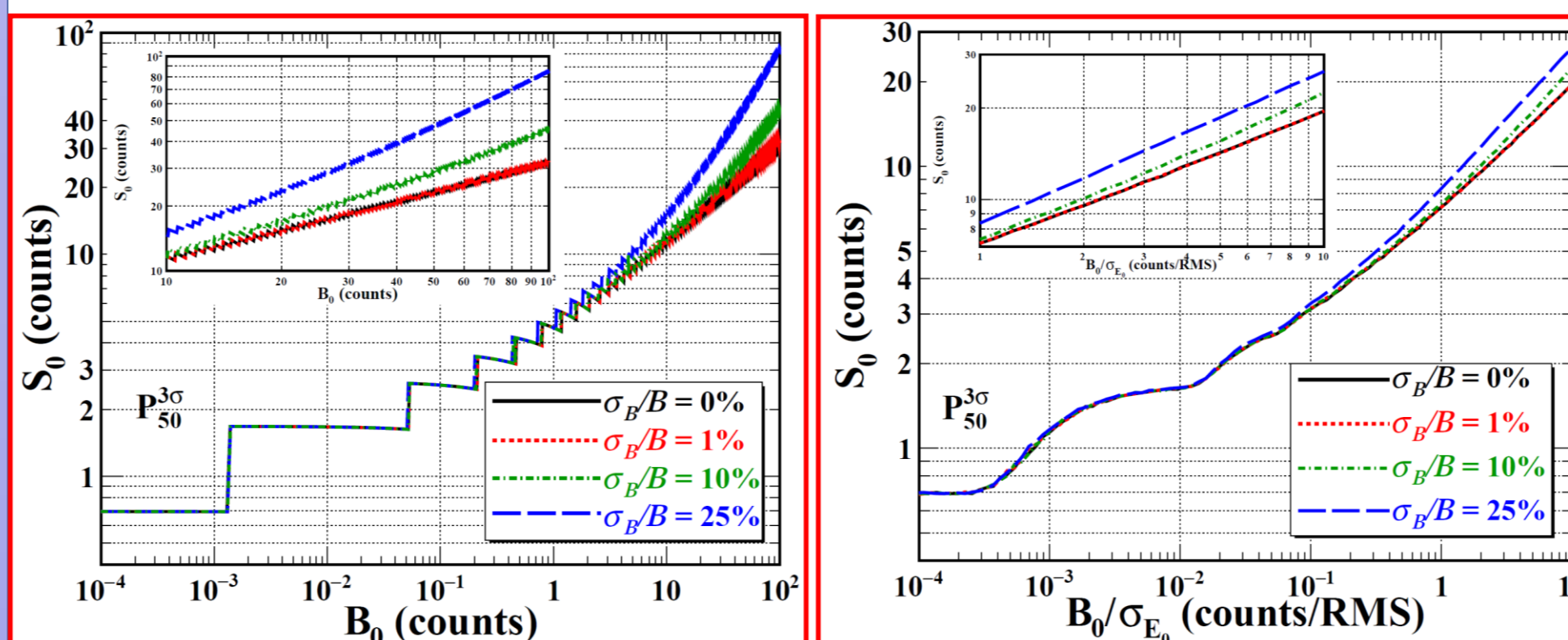


- $S_0[\mathcal{L}_{CE}] \leq S_0^{\text{opt}}[S_0[\mathcal{L}_C]] \rightarrow$  Less Events Required to Establish Positive Signals
- At  $(B_0/\sigma_{E_0}) \leq 0.01 \rightarrow$  Criteria of  $P_{5\sigma}^{\text{cont}}$  Satisfied for all  $B_0$  in  $\mathcal{L}_{CE}$  NOT in  $\mathcal{L}_C$
- At  $(B_0/\sigma_{E_0}) > 1 \rightarrow$  Counting-only Analysis Overestimate  $S_0[\mathcal{L}_{CE}]$  by 6%
- At  $(B_0/\sigma_{E_0}) \sim 10^{-3} \rightarrow$   $S_0^{\text{opt}}[\text{cont}]$  Underestimate Strength of  $S_0[\mathcal{L}_{CE}]$  by 20%
- $S_0^{\text{opt}}[\mathcal{L}_C] \rightarrow$  Overestimated by  $\sim 30\%$  &  $> S_0[\mathcal{L}_{CE}]$  for all  $(B_0/\sigma_{E_0}) > 5 \times 10^{-4}$

## Background Uncertainties

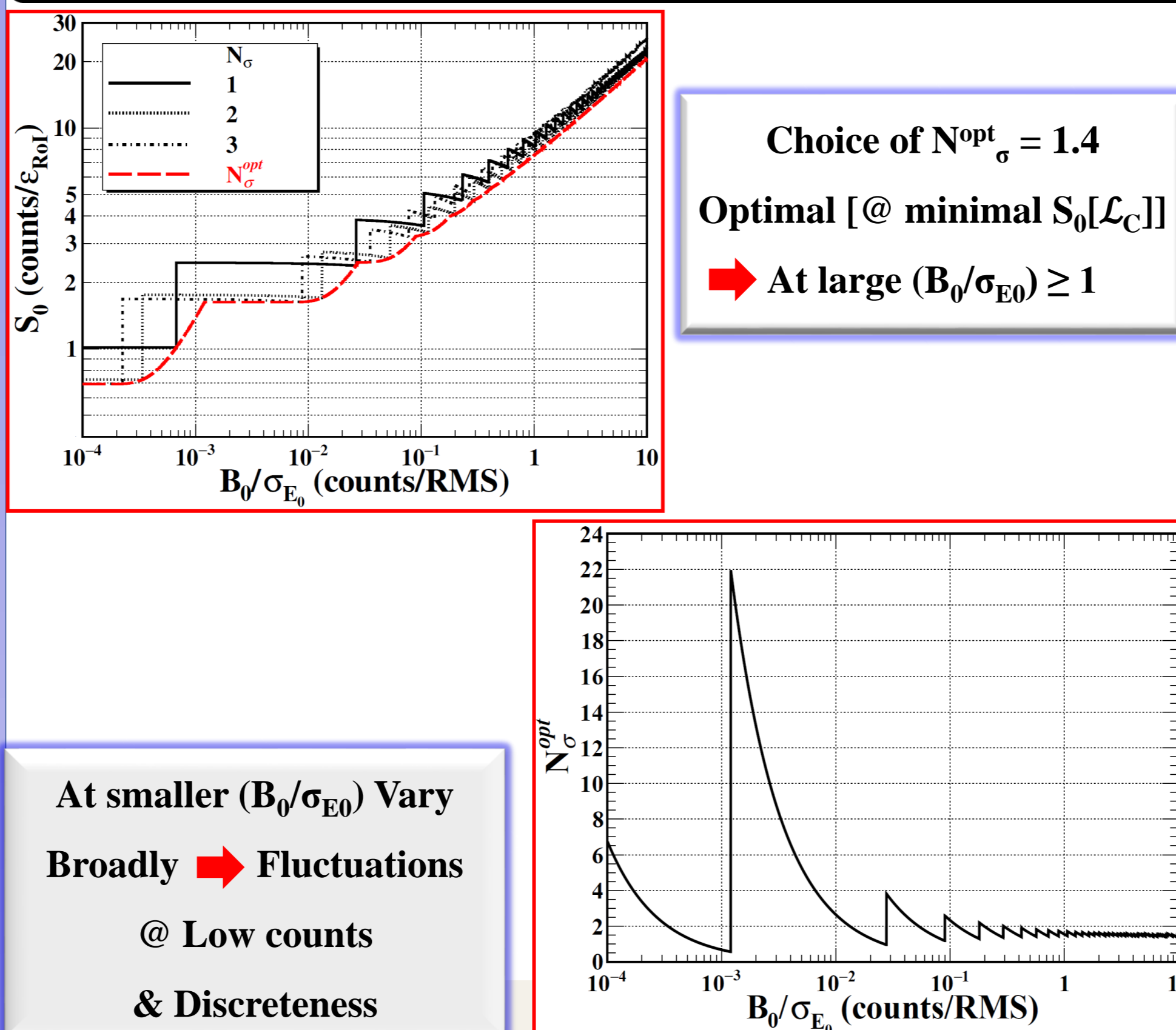
$$\mathcal{L}_{CEB} \equiv \mathcal{L}(S, B|E) = \frac{e^{-(B+S)} (B+S)^N}{N!} e^{-\tau B} (\tau B)^{n_0} q_0 \equiv t(S=0) = -2 \ln \left[ \frac{\mathcal{L}_{CEB}(S=0, \hat{B})}{\mathcal{L}_{CEB}(\hat{S}, \hat{B})} \right]$$

$$\mathcal{L}(S|\{n_i\}, B) \approx \left[ \prod_{i=1}^n \text{Poi}(n_i|F(E_i|S, B)) \right] \cdot \text{Poi}(n_0|\tau B)$$



- Realistic Experiments  $\rightarrow$  Background  $B_0$  can have Uncertainty  $\sigma_B$
- At low-statistics ( $B_0 < 1$ )  $\rightarrow$  Negligible Effects of  $\sigma_B$  [Larger in  $\mathcal{L}_C$  than  $\mathcal{L}_{CE}$ ]
- Statistical Fluctuations  $\rightarrow$  Dominate Over Uncertainty in  $B_0$

## Optimal Region of Interest

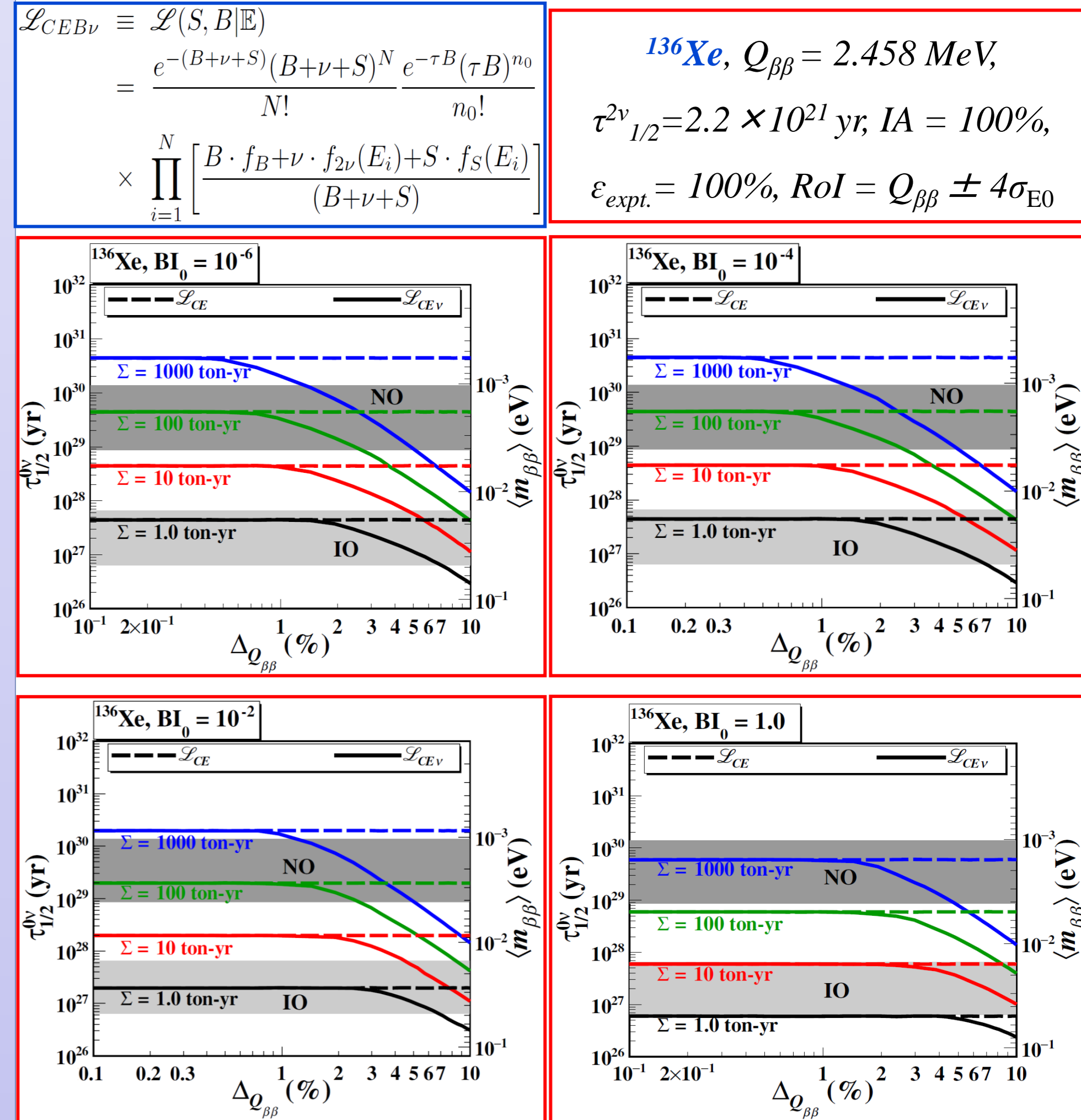


- At smaller  $(B_0/\sigma_{E_0})$  Vary Broadly  $\rightarrow$  Fluctuations @ Low counts & Discreteness

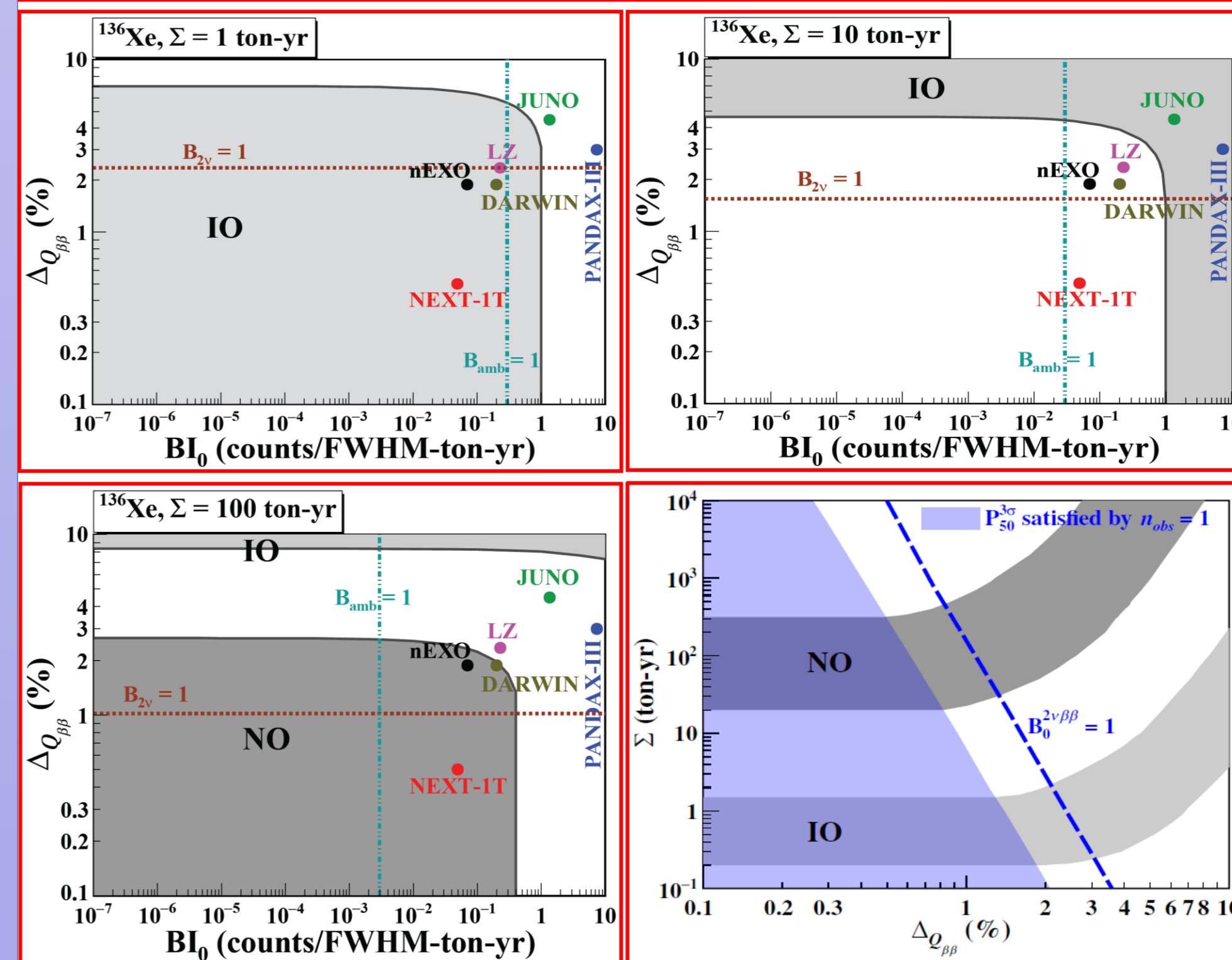
## Sensitivity Projection

Standard-Model-allowed irreducible background

$N A_{\beta\beta} \rightarrow N_{Z+2} A_{\beta\beta} + 2\bar{e} + 2\bar{\nu}$  [Goeppert-Mayer, 1935]  
Worse resolution ( $\Delta$ )  $\leftrightarrow$  Larger RoI  $\leftrightarrow$  Larger  $2\nu\beta\beta$  Background



- Divergence: Solid & Dotted lines  $\rightarrow 2\nu\beta\beta$  Start to Dominate the Sensivities
- At  $BI_0=10^{-6}$  (counts/FWHM-ton-yr)  $\rightarrow (\Delta_{Q_{\beta\beta}}, \Sigma) \approx (<1\%, >1.5 \text{ ton-yr})$  & ( $<0.4\%$ ,  $>310 \text{ ton-yr}$ ) to cover IO & NO
- At  $BI_0 = 1$  (Best Achieved)  $\rightarrow$  Overlap of Solid & Dotted lines  $2\nu\beta\beta$  is insignificant



- $\Sigma$  of 10 ton-yr (with  $\Delta_{Q_{\beta\beta}} < 1.4\%$ ) & 100 ton-yr (with  $\Delta_{Q_{\beta\beta}} \sim 8\%$ ) Required to Cover IO
- Probing Entire NO  $\rightarrow$  Not Possible even with 1000 ton-yr @ Best Achieved Resolution = 0.12% of  ${}^{76}\text{Ge}$
- Coming Generation of Projects  $\rightarrow$  Could Cover IO at  $\Sigma > 10$  ton-yr
- Covering NO entirely  $\rightarrow$  Require  $\Sigma \sim 1000$  ton-yr at  $\Delta_{Q_{\beta\beta}} \leq 1\%$  Together with  $BI_0$  at  $\leq 10^{-1}$  counts/FWHM-ton-yr
- Required  $\Sigma$  in Realistic Experiments:  $\Sigma' = \Sigma / [IA \cdot \epsilon_{\text{exp}}]$

## Summary & Prospects

- Two Expected Features  $\rightarrow$  Required Signal Strength
  - In counting-only experiments:
  - Strength can be derived correctly with complete Poisson analysis
  - Continuous Approximation would underestimate the values
- Incorporating continuous variables as additional constraints:
  - Reduced Signal Strength relative to Counting-only analysis

## Acknowledgment

This work is supported by the Academia Sinica Principal Investigator Award AS-IA-106-M02, contracts 106-2923-M-001-006-MY5, 107-2119-M-001-028-MY3 and 110-2112-M-001-029-MY3, from the Ministry of Science and Technology, Taiwan, and 2021/TG2.1 from the National Center of Theoretical Sciences, Taiwan.